

```
In [1]: 1 import numpy as np
2 import pandas as pd
3 import statsmodels.api as sm
4 from statsmodels.tsa.api import VAR
5 from statsmodels.tsa.statespace.sarimax import SARIMAX
6 import matplotlib.pyplot as plt
7 from statsmodels.tsa.stattools import adfuller
8 from statsmodels.tsa.base.datetools import dates_from_str
9 from sklearn.metrics import mean_squared_error
10
11 def diff(data, interval=1):
12     diff = list()
13     for i in range(interval, len(data)):
14         value = data[i] - data[i - interval]
15         diff.append(value)
16     return diff
17
18 def plot_graph(title, data, color, name):
19     fig, ax = plt.subplots(figsize=(12, 6))
20     ax.plot(data, color=color)
21
22     ax.grid(True, 'major', linewidth=0.34)
23     spines = [ax.spines['bottom'], ax.spines['top'], ax.spines['right'], ax.spines['left']]
24     for spine in spines:
25         spine.set_visible(False)
26
27     plt.title(title, fontweight=500, fontsize=22)
28     plt.savefig(name)
```

```
In [2]: 1 df_zillow = pd.read_csv('data/zillow-california.csv', index_col='Date')
2 df_zillow = df_zillow[df_zillow['MedianSoldPrice_AllHomes.California'].isnull()]
3 df_zillow.index = dates_from_str(df_zillow.index)
```

```
In [3]: 1 df_zillow.shape
Out[3]: (95, 3)
```

```
In [4]: 1 df_zillow.columns
Out[4]: Index(['MedianSoldPrice_AllHomes.California', 'MedianMortgageRate',
              'UnemploymentRate'],
              dtype='object')
```

```
In [5]: 1 df_zillow.tail()
Out[5]:
```

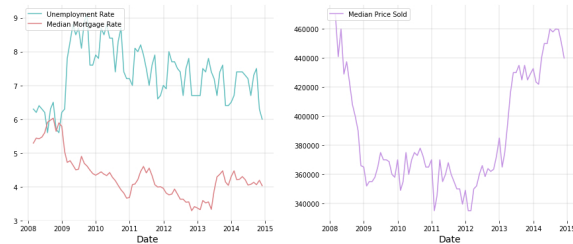
	MedianSoldPrice_AllHomes.California	MedianMortgageRate	UnemploymentRate
2015-08-31	475000.0	3.95	5.2
2015-09-30	470000.0	3.87	5.1
2015-10-31	470000.0	3.80	5.0
2015-11-30	485790.0	3.69	5.0
2015-12-31	485000.0	3.89	5.1

```
In [6]: 1 X = df_zillow[['MedianMortgageRate', 'UnemploymentRate']]
2 y = df_zillow[['MedianSoldPrice_AllHomes.California']]
```

```
In [7]: 1 X_train = X.loc['11-30-2014']
2 y_train = y.loc['11-30-2014']
3 X_valid = X.loc['12-01-2014':'11-30-2015']
4 y_valid = y.loc['12-01-2014':'11-30-2015']
```

```
In [8]: 1 fig, axes = plt.subplots(1, 2, figsize=(15, 6))
2
3 axes[0].plot(X_train['UnemploymentRate'], label='Unemployment Rate', color='#61c0bf')
4 axes[0].plot(X_train['MedianMortgageRate'], label='Median Mortgage Rate', color='#DC8185')
5 axes[1].plot(y_train, label='Median Price Sold', color='#C493E3')
6
7 for ax in axes:
8     ax.grid(True, 'major', linewidth=0.34)
9     ax.legend(loc='upper left')
10
11 ax.set_xlabel('Date', fontweight=530, fontsize=14)
12 #ax.set_ylabel('Beer Drunk (Liters)', fontweight=530, fontsize=13)
13 spines = [ax.spines['bottom'], ax.spines['top'], ax.spines['right'], ax.spines['left']]
14 for spine in spines:
15     spine.set_visible(False)
16
17 plt.title('Zillow Housing Training Data', fontweight=500, fontsize=22, x=-0.1, y=1.05)
18
19 plt.savefig('results/Zillow Housing EDA')
```

Zillow Housing Training Data

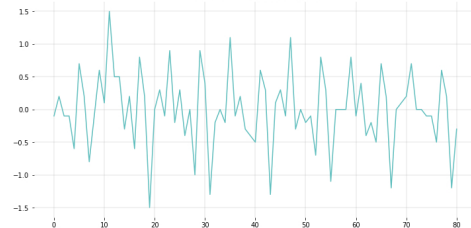


## Unemployment Rate:

- Somewhat quadratic? Difference twice to detrend and see what happens
- Seasonality: 1 year cycles (m=12)

```
In [9]: 1 UnempDiff1 = diff(X_train['UnemploymentRate'], 1)
In [10]: 1 plot_graph("Once-Differenced", UnempDiff1, '#61c0bf', 'results/Unemployment-1D.png')
```

Once-Differenced

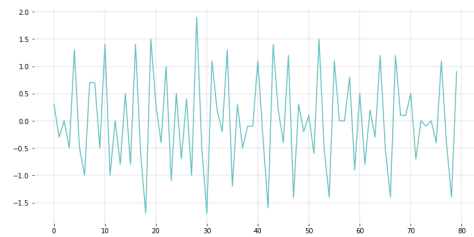


```
In [11]: 1 dfTest = adfuller(UnempDiff1, autolag='BIC')
2 UnemploymentTest = pd.Series(dfTest[0:2], index=['Test Statistic', 'p-value'])
3 UnemploymentTest
```

```
Out[11]: Test Statistic -1.566814
p-value 0.500239
dtype: float64
```

```
In [12]: 1 UnempDiff2 = diff(UnempDiff1, 1)
In [13]: 1 plot_graph("Twice-Differenced", UnempDiff2, '#61c0bf', 'results/Unemployment-2D.png')
```

Twice-Differenced



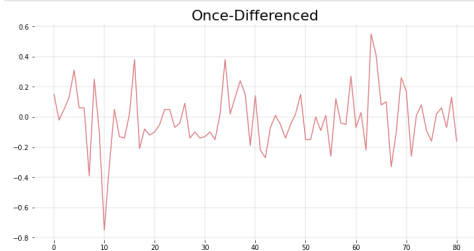
```
In [14]: 1 dfctest = adfuller(UnempDiff1, autolag='BIC')
2 UnemploymentTest = pd.Series(dfctest[0:2], index=['Test Statistic', 'p-value'])
3 UnemploymentTest
```

```
Out[14]: Test Statistic    -1.436825e+01
p-value                9.590671e-27
dtype: float64
```

## Median Mortgage Rate

- Linear, difference once
- Around a two year seasonality:  $m=24$

```
In [17]: 1 MortRateDiff1 = diff(X_train['MedianMortgageRate'], 1)
2 plot_graph('Once-Differenced', MortRateDiff1, '#DC8185', 'results/Median-Mortgage-1D.png')
```



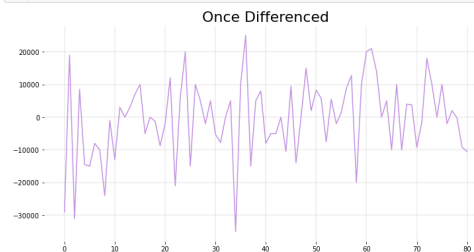
```
In [18]: 1 dfctest = adfuller(MortRateDiff1, autolag='BIC')
2 MortRateTest = pd.Series(dfctest[0:2], index=['Test Statistic', 'p-value'])
3 MortRateTest
```

```
Out[18]: Test Statistic    -7.895040e+00
p-value                4.333583e-12
dtype: float64
```

## Median Price Sold

- Also shows quadratic nature: difference twice

```
In [21]: 1 MedPriceDiff1 = diff(y_train['MedianSoldPrice_AllHomes.California'], 1)
2 plot_graph('Once Differenced', MedPriceDiff1, '#C493E3', 'results/Median-Price-1D.png')
```



```
In [22]: 1 dfctest = adfuller(MedPriceDiff1, autolag='BIC')
2 MedPriceTest = pd.Series(dfctest[0:2], index=['Test Statistic', 'p-value'])
3 MedPriceTest
```

```
Out[22]: Test Statistic    -1.080568e+01
p-value                1.966155e-19
dtype: float64
```

## EDA Conclusion:

-since Unemployment Rate needs to be twice differenced to become stationary, all other columns will follow suit

```
In [23]: 1 # MedPrice_Col2 = diff(MedPrice_Col, 1)
2 # MortRate_Col2 = diff(MortRate_Col, 1)
3 # zillow_diff = pd.DataFrame({'UnemploymentRate': Unemployment_Col,
4 #                               'MedianMortgageRate': MortRate_Col2,
5 #                               'MedianPriceSold': MedPrice_Col2
6 #                               })
7 # zillow_diff
8
9 zillow_diff = df_zillow.diff().dropna()
10 zillow_diff = zillow_diff.diff().dropna()
11 zillow_diff_train = zillow_diff.loc['11-30-2014':]
12 zillow_diff_test = zillow_diff.loc['12-1-2014':]
```

```
In [24]: 1 fig, axes = plt.subplots(1, 3, figsize=(20, 6))
2
3 axes[0].plot(zillow_diff_train['UnemploymentRate'], label='Unemployment Rate', color='#61c0bf')
4 axes[1].plot(zillow_diff_train['MedianMortgageRate'], label='Median Mortgage Rate', color='#DC8185')
5 axes[2].plot(zillow_diff_train['MedianSoldPrice_AllHomes.California'], label='Median Price Sold', color='#C493E3')
6
7 for ax in axes:
8     ax.grid(True, 'major', linewidth=0.34)
9     ax.legend(loc='upper left')
10
11 ax.set_xlabel('Date', fontweight=530, fontsize=14)
12 #ax.set_ylabel('Beer Drunk (Liters)', fontweight=530, fontsize=13)
13 spines = [ax.spines['bottom'], ax.spines['top'], ax.spines['right'], ax.spines['left']]
14
15 for spine in spines:
16     spine.set_visible(False)
17
18 plt.title("Twice Differenced Training Data", fontweight=500, fontsize=22, x=-.75, y=1.05)
19
20 plt.savefig('results/Zillow-Bousing-2D-EDA.png')
```



- Everything is now stationary
- Let's normalize so that all columns are between 0 and 1

• Using so because we are using a regression function which is sensitive to scale

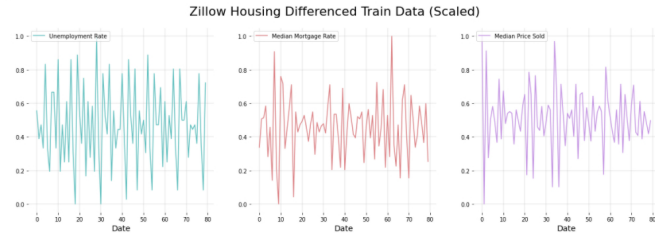
```
In [25]: 1 from sklearn.preprocessing import MinMaxScaler
2 scaler = MinMaxScaler(feature_range=(0, 1))
3 scaled_input = scaler.fit_transform(zillow_diff_train)
4 zillow_diff_scaled = pd.DataFrame(scaled_input)
5 cols = zillow_diff_train.columns
6 zillow_diff_scaled.rename(columns = {0:cols[0], 1:cols[1], 2:cols[2]}, inplace=True)
7 zillow_diff_scaled.head()
```

```
Out[25]:
```

	MedianSoldPrice_AllHomes.California	MedianMortgageRate	UnemploymentRate
0	1.000000	0.338028	0.555556
1	0.000000	0.507042	0.388889
2	0.913285	0.514085	0.472222
3	0.275510	0.584507	0.333333
4	0.505102	0.281690	0.833333

```
In [26]: 1 df_zillow = df_zillow.rename(columns={"MedianSoldPrice_AllHomes.California":"MedianPriceSold",
2                                         "MedianMortgageRate":"MedianMortgageRate",
3                                         })
4 zillow_diff_scaled = zillow_diff_scaled.rename(columns={"MedianSoldPrice_AllHomes.California":"MedianPriceSold",
5                                                         "MedianMortgageRate":"MedianMortgageRate",
6                                                         })
```

```
In [27]: 1 fig, axes = plt.subplots(1, 3, figsize=(20, 6))
2
3 axes[0].plot(zillow_diff_scaled['UnemploymentRate'], label='Unemployment Rate', color='#41c0bf')
4 axes[1].plot(zillow_diff_scaled['MedianMortgageRate'], label='Median Mortgage Rate', color='#DC185')
5 axes[2].plot(zillow_diff_scaled['MedianPriceSold'], label='Median Price Sold', color='#C493E3')
6
7 for ax in axes:
8     ax.grid(True, 'major', linewidth=0.34)
9     ax.legend(loc='upper left')
10
11 ax.set_xlabel("Date", fontweight=530, fontsize=14)
12 ax.set_ylabel("Beer Drunk (Liters)", fontweight=530, fontsize=13)
13 spines = [ax.spines['bottom'], ax.spines['top'], ax.spines['right'], ax.spines['left']]
14
15 for spine in spines:
16     spine.set_visible(False)
17
18 plt.title("Zillow Housing Differenced Train Data (Scaled)", fontweight=500, fontsize=22, x=-.75, y=1.05)
19
20 plt.show()
```



```
In [28]: 1 model = VAR(zillow_diff_scaled)
2 results = model.fit(maxlags=15, ic='bic')
3 results.summary()
```

```
Out[28]:
```

Summary of Regression Results

Model: VAR  
Method: OLS  
Date: Mon, 08, Nov, 2021  
Time: 19:11:02

No. of Equations: 3.00000 BIC: -10.46017  
Nobs: 75.0000 HQIC: -11.4927  
Log likelihood: 181.922 FPE: 5.75806e-06  
AIC: -12.0849 Det(Omega\_mle): 3.22356e-06

Results for equation MedianPriceSold

	coefficient	std. error	t-stat	prob
const	0.808931	0.266405	3.036	0.002
L1.MedianPriceSold	-0.807157	0.135795	-5.944	0.000
L1.MedianMortgageRate	0.038633	0.064047	0.585	0.559
L1.UnemploymentRate	0.131373	0.058569	2.322	0.020
L2.MedianPriceSold	-0.521436	0.151130	-3.450	0.001
L2.MedianMortgageRate	0.077491	0.078102	0.992	0.321
L2.UnemploymentRate	0.134453	0.076314	1.762	0.078
L3.MedianPriceSold	-0.214626	0.140026	-1.533	0.125
L3.MedianMortgageRate	0.132654	0.085020	1.560	0.119
L3.UnemploymentRate	0.403773	0.082506	4.894	0.000
L4.MedianPriceSold	-0.024349	0.120712	-0.202	0.840
L4.MedianMortgageRate	-0.062845	0.078180	-0.804	0.421
L4.UnemploymentRate	0.298898	0.097189	3.086	0.002
L5.MedianPriceSold	-0.070050	0.092012	-0.854	0.393
L5.MedianMortgageRate	0.063569	0.067940	0.936	0.349
L5.UnemploymentRate	-0.070137	0.079234	-0.885	0.376

Results for equation MedianMortgageRate

	coefficient	std. error	t-stat	prob
const	0.360321	0.494555	0.729	0.466
L1.MedianPriceSold	-0.163778	0.252091	-0.650	0.516
L1.MedianMortgageRate	-0.700044	0.122609	-5.710	0.000
L1.UnemploymentRate	0.081409	0.105014	0.775	0.438
L2.MedianPriceSold	0.204519	0.200558	0.729	0.466
L2.MedianMortgageRate	-0.636471	0.144989	-4.390	0.000
L2.UnemploymentRate	-0.002091	0.141670	-0.015	0.988
L3.MedianPriceSold	0.302594	0.259945	1.164	0.244
L3.MedianMortgageRate	-0.356814	0.157831	-2.261	0.024
L3.UnemploymentRate	0.140902	0.153165	0.920	0.358
L4.MedianPriceSold	0.507503	0.224089	2.265	0.024
L4.MedianMortgageRate	-0.017846	0.145114	-0.130	0.741
L4.UnemploymentRate	0.228997	0.180422	1.274	0.203
L5.MedianPriceSold	0.383198	0.152247	2.517	0.012
L5.MedianMortgageRate	-0.034017	0.126125	-0.745	0.456
L5.UnemploymentRate	0.189584	0.147091	1.289	0.197

Results for equation UnemploymentRate

	coefficient	std. error	t-stat	prob
const	2.789087	0.542785	5.138	0.000
L1.MedianPriceSold	0.322277	0.276676	1.165	0.244
L1.MedianMortgageRate	0.077964	0.134567	0.579	0.562
L1.UnemploymentRate	-0.956789	0.115255	-8.301	0.000
L2.MedianPriceSold	0.306579	0.307919	0.996	0.319
L2.MedianMortgageRate	0.179395	0.159129	1.127	0.260
L2.UnemploymentRate	-0.914701	0.154446	-6.269	0.000
L3.MedianPriceSold	-0.244309	0.285296	-0.856	0.392
L3.MedianMortgageRate	-0.137769	0.173223	-0.795	0.426
L3.UnemploymentRate	-0.763859	0.148102	-5.144	0.000
L4.MedianPriceSold	-0.540047	0.245943	-2.196	0.028
L4.MedianMortgageRate	-0.219592	0.159288	-1.379	0.168
L4.UnemploymentRate	-0.800094	0.198017	-4.041	0.000
L5.MedianPriceSold	-0.509329	0.167095	-3.048	0.002
L5.MedianMortgageRate	-0.037279	0.138425	-0.269	0.788
L5.UnemploymentRate	-0.563706	0.161436	-3.492	0.000

Correlation matrix of residuals

	MedianPriceSold	MedianMortgageRate	UnemploymentRate
MedianPriceSold	1.000000	-0.072780	0.289204
MedianMortgageRate	-0.072780	1.000000	0.250494
UnemploymentRate	0.289204	0.250494	1.000000

## Forecast Analysis

- Now that we have our forecast, we will:
  1. Unscale all columns
  2. Undifference all columns

```
In [30]: 1 test = pd.read_csv('data/test.csv', index_col='Month')
2 test.index = dates_from_str(test.index)
```

```
In [31]: 1 X_valid
```

```
Out[31]:
```

	MedianMortgageRate	UnemploymentRate
--	--------------------	------------------

2014-12-31	3.90	6.2
2015-01-31	3.85	6.2
2015-02-28	3.89	5.7
2015-03-31	3.91	5.5
2015-04-30	3.79	5.4
2015-05-31	3.73	5.4
2015-06-30	3.85	5.6
2015-07-31	3.87	5.3
2015-08-31	3.95	5.2
2015-09-30	3.87	5.1
2015-10-31	3.80	5.0
2015-11-30	3.69	5.0