

**Tutorial 5**

10/09/2024

1. Solve all the exercises of pages 105-107, 111 and 115-116 of the book by Hoffman and Kunze.
2. Let  $A$  and  $B$  be  $n \times n$  matrices over  $F$  such that  $A^2 = A$  and  $B^2 = B$ . Assume that the matrix  $I - (A + B)$  is invertible, where  $I$  is a  $n \times n$  identity matrix. Prove that  $\text{rank } A = \text{rank } B$ .