

**Tutorial 1**

06/08/2024

1. Prove that if two homogeneous systems in two unknowns have the same solutions, then they are equivalent.

2. Find the solution of

$$2x_1 - 3x_2 - 7x_3 + 5x_4 + 2x_5 = -2$$

$$x_1 - 2x_2 - 4x_3 + 3x_4 + x_5 = -2$$

$$2x_1 - 4x_3 + 2x_4 + x_5 = 3$$

$$x_1 - 5x_2 - 7x_3 = 6x_4 + 2x_5 = -7.$$

3. Show that the system of linear equations

$$x_1 - 2x_2 + x_3 + 2x_4 = 1$$

$$x_1 + x_2 - x_3 + x_4 = 2$$

$$x_1 + 7x_2 - 5x_3 - x_4 = 3$$

has no solution.

4. Determine the row reduced form of the following matrix:

$$M = \begin{bmatrix} 1 & 2 & 1 & 0 \\ -1 & 0 & 3 & 5 \\ 1 & -2 & 1 & 1 \end{bmatrix}$$

. Also find the invertible  $3 \times 3$  matrix such that  $P$  such that  $R = PM$ .

5. Suppose  $A$  is  $2 \times 1$  matrix and  $B$  is  $1 \times 2$  matrix. Prove that the matrix  $AB$  matrix is not invertible matrix. Generalise this result.