Geometric and negative binomial

Sunday, June 9, 2024 12:

能, 注意不同的 parametrizetan, 这假事, 否则 疏充强推导. (SI appendix 中并和于应...)

②从下切一中选出工了起心。

(1) X: # foilures

Geomtp)
$$P(X=x|p) = p(1-p)^{X}$$
 $x=0,1,2...$

NB(p;r) $P(Y=y|r,p) = p \cdot {r+y-1 \choose y}$ $(1-p)^{y}p^{r-1}$

$$= {r+y-1 \choose y} (1-p)^{y}p^{r} \qquad y=0,1,2...$$
Sidenote:
$$0 \ \text{$\not= \text{$f$-$roil}$}$$
 \$\frac{1}{8} \tau_{1} \frac{1}{8} \tau_{1} \tau_{1}

((r+x-1, 2) r+21/201,

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$$E(e^{t\times}) = \sum_{x=0}^{\infty} e^{t\times} \cdot p(1-p)^{x}$$

$$= p \sum_{x=0}^{\infty} \left[e^{t(1-p)} \right]^{x}$$

$$= e^{t(1-p)} \quad \text{common ratio or } |x| = e^{t(1-p)} < |x|$$

$$= \frac{p}{1-(1-p)e^{t}}$$

$$Soc = \frac{1}{1-r} \quad e^{t} < (1-p)^{-1}$$

$$= \frac{t}{1-r} < -\log(1-p)$$

$$= \frac{1}{1-r}$$

$$E(etY) = \int_{y=0}^{\infty} e^{\pm y} {r+y-1 \choose y} - (1-p)y p^{r}$$

$$= p^{r} \int_{y=0}^{\infty} {r+y-1 \choose y} (1-p) \cdot e^{\pm y} y$$

$$= p^{r} (-(1-p)e^{\pm +1})^{r} \qquad (x+e)^{-n} = \int_{k=0}^{\infty} {r+y-1 \choose k} x^{r} e^{-n-k}$$

$$= p^{r} (-(1-p)e^{\pm +1})^{r} \qquad (x-e)^{-n} e^{\pm x} e^{-n-k}$$

$$= e^{-n-k} e^{-n-k}$$

$$= e^{-$$

2 X = # of trails

Geom
$$P(X=x|p) = p(I-p)^{x-1} x:1,2,3...$$
 $P(Y=y|r,p) = {y-1 \choose r-1} P^{x}(1-p)^{y-r} y:1,2,3...$

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$$Ele^{tx}) = \sum_{xy}^{\infty} e^{tx} p(1-p)^{x-1}$$

$$= \frac{p}{1-p} \sum_{xy}^{\infty} [e^{t}(1-p)]^{x}$$

$$= \frac{1}{1-p} (\sum_{xy}^{\infty} [e^{t}(1-p)]^{x} - 1)$$

$$= \frac{1}{1-p} (\frac{1}{1-1-p})e^{t} - 1)$$

$$= \frac{p}{1-p} \cdot \frac{1-(1-1-p)e^{t}}{1-(1-p)e^{t}}$$

$$= \frac{pe^{t}}{1-(1-p)e^{t}}$$

$$= \frac{pe^{t}}{1-(1-p)e^{t}}$$

$$E(e^{t\gamma}) = \sum_{j=1}^{\infty} e^{ty} \cdot {y-1 \choose r-1} p^{r} (1-p)^{y-r}$$

$$= \frac{p}{p} \sum_{j=1}^{\infty} {y-1 \choose r-1} (1-p)e^{t} y^{j}$$

$$= \frac{p}{p} \sum_{k=0}^{\infty} {r+k-1 \choose r-1} (1-p)e^{t} r+k$$

$$= \frac{p}{1-p} \sum_{k=0}^{\infty} {r+k-1 \choose r-1} r+k$$