Monday, May 27, 2024

τ**Θ** ⁄2......

理例 Order statistics

思路: order stats defn 中有 初如 有一些联系

⇒转化为Bom | Bin

Continuous case;

random sampling XI, X2...XK...Xn n R.U.S.

Is For
$$X_k$$
, x_k , x_k a fixed value x_k .

$$I\{X_k \in X\} = \begin{cases} 1 & P(X_k \in X) = F_{X_k}(X_k) \\ 0 & 1 - F_{X_k}(X_k) \end{cases}$$

us For all R.V.S. count # of trials where Xxxx Ci.e., # of successes)

$$P(x=y)=\binom{n}{y}\left(F_{x}(x)\right)^{y}\left(I-F_{x}(a)\right)^{n-y}$$

成 order stat. 前 CDF可转化为Bin.

e.g.
$$F_{x,y}(x) = P(x,y) \in X$$
 I the jth largest X is smaller regards to X]
$$= P(Y,y,y)$$

$$= \text{at least } j \times \mathbb{R} \cup \mathbb{R} \cup$$

order stat pot is then:

$$f_{x_{jj}}(x) = \frac{d}{dx} \int_{E_{ij}}^{n} \binom{n}{k} \frac{f_{x(x)}^{k}}{f_{x(x)}^{k}} \frac{(1-f_{x(x)})^{n-k}}{g}$$

$$= \int_{E_{ij}}^{n} \binom{n}{k} \left[k \left(f_{x(x)} \right)^{k-1} f_{(x)} \cdot \left((1-f_{x(x)})^{n-k} \right)^{n-k} \right]$$

$$- \int_{E_{ij}}^{n} \binom{n}{k} \frac{f_{(x)}^{k}}{(n-k)} \frac{f_{(x)}^{k}}{(1-f_{x(x)})^{n-k-1}} f_{(x)} \int_{E_{ij}}^{n-k} \frac{f_{(x)}^{k}}{f_{(x)}^{k}} \frac{f_{(x)}^{k}}{f_{(x)}^{k$$

Discrete cese:

P(X===)=Pi

IR生有一个Random sample X1, X2...Xn.

For
$$X_k$$
. $X_k = x_i (Tixed x)$

$$I f X_k = x_i f = \begin{cases} 0 & P(X_k \in x_i) = P_1 + P_2 + \cdots P_i & P_i \\ 0 & 1 - (P_1 + P_1 + \cdots P_i) \end{cases} = P_i$$

$$P(X_{j}) = \lambda() = P(Y_{j}) = \sum_{k \neq j}^{n} {n \choose k} P_{i}^{k} (1-P_{i})^{n-k}$$

$$P(X_{j}) = x_{i}) = P(X_{j}) = x_{i}) - P(X_{ij}) \in X_{i-1}$$

$$= \sum_{k=1}^{n} {n \choose k} \left[P_{i}^{k} \left(1 - P_{i} \right)^{n-k} - P_{i}^{k} \left(1 - P_{i-1} \right)^{n+k} \right]$$