

MISC

```
3
data Tree2 a = Nil | B a (Tree2
  a) (Tree2 a)
data Gtree a = Nil | Gtree a [
  Gtree a] deriving (Show)
data Name a = Name {getterX,
  getterY :: a}
-- constructor takes 2 arg of
  different type a and also
  expose the getters
let var1 = value1
  var2 = value2
in body
$ -- evaluate before right
  expression
show -- print
v@(T x' l' c' r') -- pickup
  data on the right inside v
if condition then body else body
f (x, y) = x -- couple as arg
```

LISTS

```
[a] -- list of variable type
list !! 0 -- take element at
  index 0
[1, 3 .. 10] -- [1, 3, 6, 9]
1:[] -- cons operator: single:
  list not contrary
++ -- list concat
take 3 list -- return first 3
  elems
drop 3 list -- remove first 3
  elems and return new list
head list -- return first
  element
tail list -- return list without
  first element
last 1 -- return last elem from
  list
init 1 -- returns all elem of 1
  except last
reverse list -- reverse list
lst [ x * 2 | x <- [0, 1 ..]] --
  even numbers
zip lst1 lst2 -- couples from
  each lst
```

```
null v -- returns true if v
  empty
length l -- returns the length
  of the list
```

FUNCTIONS

```
fname arg = body
map (f1 . f2) lst -- first map
  f2 then f1
concatMap f lst -- for every
  elem f creates a list,
  concatMap concats all the
  lists into a single list
(\ x -> x * 2) -- lambda
fname arg@(cur:next:rest) = body
  -- arg is list decomposed
fname num
  | f1 < 2 = "small"
  | f1 > 2 = "big"
  | otherwise = "normal"
where
  f1 = fbody
id -- identity function
4 `div` 2 -- integer division
filter f v -- f boolean
  function, returns a list of
  the elements of v for which f
  returned true
maximum v--returns v max element
```

CLASSES

```
class Equal a where -- pseudo
  class
    (==) :: a -> a -> bool
    x /= y = not (x == y)
instance (Equal a) => Equal (
  Tree2 a) where
  Nil == s = s == Nil
  s == Nil = s == Nil
  (B v l r) == (B v2 l2 r2) =
    v == v2 && l == l2 && r == r2
  _ == _ = False
-- instantiating Equal pseudo
  class with a Tree as arg
```

FOLDABLE

```
instance Foldable Slist where
  foldr f acc (Slist list len) =
```

```
  foldr f acc list
instance Foldable Tree where
  foldr :: (a -> b -> b) -> b
  -> Tree a -> b
  foldr f acc Nil = acc
  foldr f acc (Leaf x) = f acc
    x
  foldr f acc (B l r) = foldr
    f (foldr f acc r) l
```

FUNCTORS

```
instance Functor Slist where
  fmap :: (a -> b) -> Slist a ->
    Slist b
  fmap f (Slist list len) =
    Slist (fmap f list) len
instance Functor Tree where
  fmap :: (a -> b) -> Tree a ->
    Tree b
  fmap f Nil = Nil
  fmap f (Leaf a) = Leaf (f a)
  fmap f (B l r) = B (fmap f l)
    (fmap f r)
```

APPLICATIVES

```
--[(+1), (*2), (^3)] <*> [1,2,3]
--[2, 3, 4, 2, 4, 6, 1, 8, 27]
-- partial f applied to list and
  concat
instance Applicative Slist where
  pure :: a -> Slist a
  pure a = Slist [a] 1
  (<*>) :: Slist (a -> b) ->
    Slist a -> Slist b
  (Slist flist _) <*> (Slist a
    alen) = Slist (flist <*> a)
    alen
instance Applicative Tree where
  pure x = Leaf x
  Nil <*> _ = Nil
  _ <*> Nil = Nil
  (Leaf f) <*> (Leaf x) = Leaf (
    f x)
  (Leaf f) <*> (B left right) =
    B (Leaf f <*> left) (Leaf f
    <*> right)
  (B leftF rightF) <*> tree = B
    (leftF <*> tree) (rightF <*>
```

```
  tree)
instance Applicative Tree where
  pure :: a -> Tree a
  pure = Leaf
  (<*>) :: Tree (a -> b) -> Tree
    a -> Tree b
  Nil <*> _ = Nil
  _ <*> Nil = Nil
  (Leaf f) <*> t = fmap f t
  (B t1 t2) <*> t = B (t1 <*> t)
    (t2 <*> t)
ltconcat :: BTT (BTT a) -> BTT a
ltconcat t = foldr (<+>) Nil t
ltconcmmap :: ((a->b) -> BTT b)
  -> BTT (a -> b) -> BTT b
ltconcmmap f t = ltconcat (fmap f
  t)
instance Applicative BTT where
  pure :: a -> BTT a
  pure x = B2 x Nil Nil
  (<*>) :: BTT (a -> b) -> BTT a
    -> BTT b
  x <*> y = ltconcmmap (\f ->
    fmap f y) x
(<+>) :: Gtree a -> Gtree a ->
  Gtree a
Nil +++ s = s
s +++ Nil = s
(Gtree a l) +++ g = Gtree a (g:l
  )
instance Applicative Gtree where
  pure a = Gtree a []
  x <*> y = foldr (<+>) Nil (
    fmap (\f -> fmap f y) x)
```

MONADS

```
instance Monad Result where
  Ok x >>= f = f x
  Err >>= _ = Err
instance Monad Slist where
  (>>=) :: Slist a -> (a ->
    Slist b) -> Slist b
  (Slist list len) >>= f = let
    finalL = (list >>= (\x -> let
      Slist xs _ = f x in xs)) in
    Slist finalL $ length finalL
instance Monad Tree where
  (>>=) :: Tree a -> (a -> Tree
```

```
    b) -> Tree b
Nil >>= f = Nil
(Leaf a) >>= f = f a
(B t1 t2) >>= f = B (t1 >>= f)
               (t2 >>= f)
```

STATE MONADS

```
import Control.Monad.State
type Stack = [Int]
popM :: State Stack Int
popM = state $ \(x : xs) -> (x,
                             xs)
pushM :: Int -> State Stack ()
pushM a = state $ \(xs -> ((), a :
                             xs)
stackManipM :: State Stack Int
stackManipM = do
    pushM 3
    a <- popM
    popM
state0 = [1,2,3,4,5]
result = runState stackManipM
         state0
```

Examples

```
data Btree a = Leaf a | Branch (
    Btree a)(Btree a) deriving (
    Show, Eq)
instance Functor Btree where
    fmap f (Leaf x) = Leaf (f x)
    fmap f (Branch x y) = Branch
        (fmap f x) (fmap f y)
addLevel :: Btree a -> Btree a
addLevel t = Branch t t
btrees :: a -> [(Btree a)]
btrees x = (Leaf x) : [addLevel
    t | t <- btrees x]
incBtrees :: [Btree Integer]
incBtrees = (Leaf 1) : [
    addLevel (fmap (+1) t) | t <-
        incBtrees]
counts :: [Integer]
counts = map (\x -> 2^x - 1)
         [1..]
```
