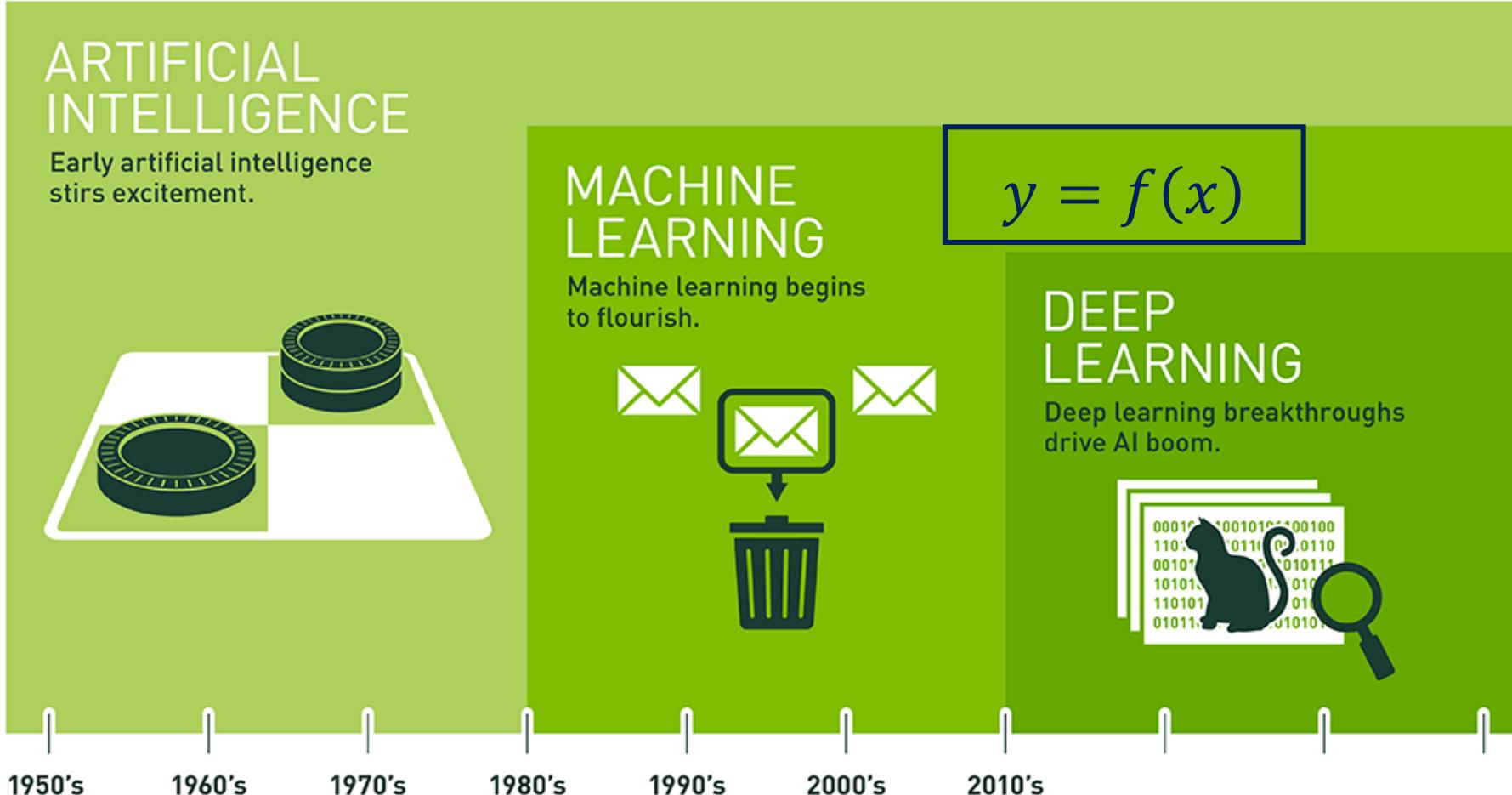


# Regression vs Classification

y learned is continuous → Regression  
y learned is categorical → Classification



# Notations

 $x_i$ 

No	age	t1	t2	t3	t4	t5	t6	time	Step frequency	n1	n2	n3	n4	n5	n6	px	py	pz	Steps	Gender	TUG	y1	BBS	y2
1	70	1.76	2.64	6.24	7.02	10	12.8	11	2.285	80	120	282	317	453	575	11.67	1.809	-1.99	13	F	11	0	26	0
2	86	1.64	2.6	5.82	7.27	10.4	12.6	11	1.934	75	118	263	328	470	570	11.14	2.302	-4.651	12	F	11	0	24	0
3	76	1.76	2.93	6.27	7.04	10.3	12.8	11	2.109	80	133	283	318	465	575	11.53	2.169	-3.253	14	F	11	0	22	1
4	70	2.38	3.29	5.58	6.47	9.02	10.4	8	2.461	108	149	252	292	407	468	11.6	1.838	-3.138	12	F	8	0	24	0
5	66	3.09	4.07	6.6	7.4	10.2	12.1	9	2.461	140	184	298	334	462	545	11.55	2.531	-2.742	12	F	9	0	26	0
6	79	1.76	2.91	5.87	6.6	10.2	12.8	11	2.109	80	132	265	298	462	575	1.788	-1.349	13	F	11	0	26	0	
7	85	1.2	2.33	5.42	8.31	12.1	17.2	16	2.988	55	106	245	375	545	775	$x_i^n$	2.203	-4.89	17	M	16	1	18	1
8	81	1.64	2.93	5.98	7.47	10.9	13.6	12	1.758	75	133	270	337	493	615	11.1	2.667	4.594	10	F	12	0	24	0
9	82	0.64	1.47	4.76	5.76	9.36	11.6	11	2.109	30	67	215	260	422	525	11.26	4.1	-2.693	14	M	11	0	24	0
10	69	1.64	2.49	5.02	5.98	9.82	12.6	11	2.637	75	113	227	270	443	570	11.27	3.292	-3.522	13	F	11	0	20	1
11	84	0.64	1.4	5.67	7.29	11.5	14.6	14	1.934	30	64	256	329	520	660	11.53	2.335	-2.999	15	M	14	1	26	0
12	69	1.09	1.98	5	5.62	8.38	10.1	9	2.109	50	90	226	254	378	455	11.15	1.919	-4.608	11	M	9	0	26	0
13	73	1.09	2.13	6.78	8.38	12.4	17.1	16	3.691	50	97	306	378	558	770	11.46	2.264	-3.333	16	F	16	1	14	1
14	81	0.64	1.87	9.24	11.2	19	22.6	22	1.934	30	85	417	507	857	1020	11.58	2.511	-2.157	27	M	22	1	24	0
15	80	0.76	1.71	3.98	5	7.58	9.76	9	2.109	35	78	180	226	342	440	11.33	2.821	-3.595	10	M	9	0	26	0
16	88	0.98	2.13	6.31	7.44	11.5	14	13	1.934	45	97	285	336	518	630	11.38	2.498	-3.702	16	M	14	1	26	0
17	81	1.09	2.09	4.18	5.16	7.76	10.1	9	2.285	50	95	189	233	350	455	11.21	2.241	-4.337	10	M	9	0	28	0
18	76	1.76	2.64	5.87	6.98	9.98	12.8	11	1.406	80	120	265	315	450	575	11.33	2.679	-3.736	10	M	11	0	26	0
19	69	0.36	3.76	13.3	16.7	24.2	29.4	29	3.691	17	170	598	753	1090	1322	11.31	1.361	-4.171	28	F	29	1	10	1
20	75	1.98	2.93	5.98	7.91	12.2	15	13	1.934	90	133	270	357	551	675	11.5	2.202	-1.495	14	M	13	0	28	0
21	87	1.53	3.2	10.9	13.8	21.3	26.5	25	2.9	70	145	492	624	960	1195	11.6	2.199	-2.54	19	F	25	1	16	1
22	72	0.2	1.02	3.36	4.11	7.42	10.2	10	1.758	10	47	152	186	335	460	11.52	2.658	-2.081	9	M	10	0	28	0
23	109	0.64	1.93	5.04	5.71	9.13	10.6	10	2.285	30	88	228	258	412	480	11.51	2.056	-3.158	15	F	10	0	28	0

# Mechanism for computer to learn from data

- Define a function to be learned:  $y^n = f(x^n)$
- Define a loss function  $\mathcal{L}(f)$  to describe the error between  $y^n$  and  $\hat{y}^n$
- Find the optimal parameters that minimize  $\mathcal{L}(f)$

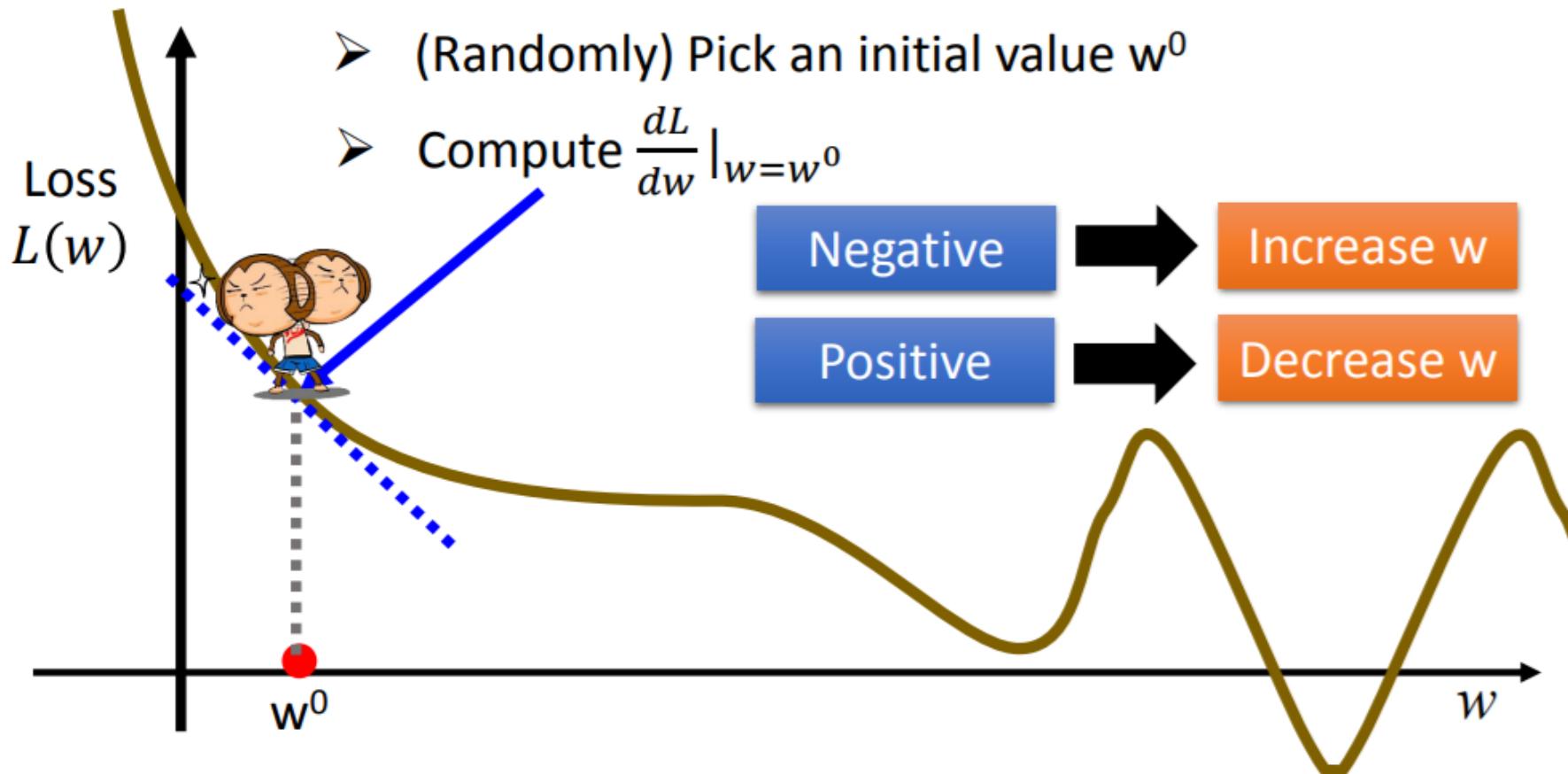
# ML model (1) – Linear regression

- Linear model:  $y^n = \sum_i (w_i x_i^n) + b$
- Loss function:  $L(w, b) = \sum_{n=1}^N (\hat{y}^n - y^n)^2 = \sum_{n=1}^N (\hat{y}^n - (\sum_i (w_i x_i^n) + b))^2$
- Find the optimal parameters that minimize loss:  $\arg \min_{w, b} L(w, b)$

# Use gradient decent to find optimal parameters

$$w^* = \arg \min_w L(w)$$

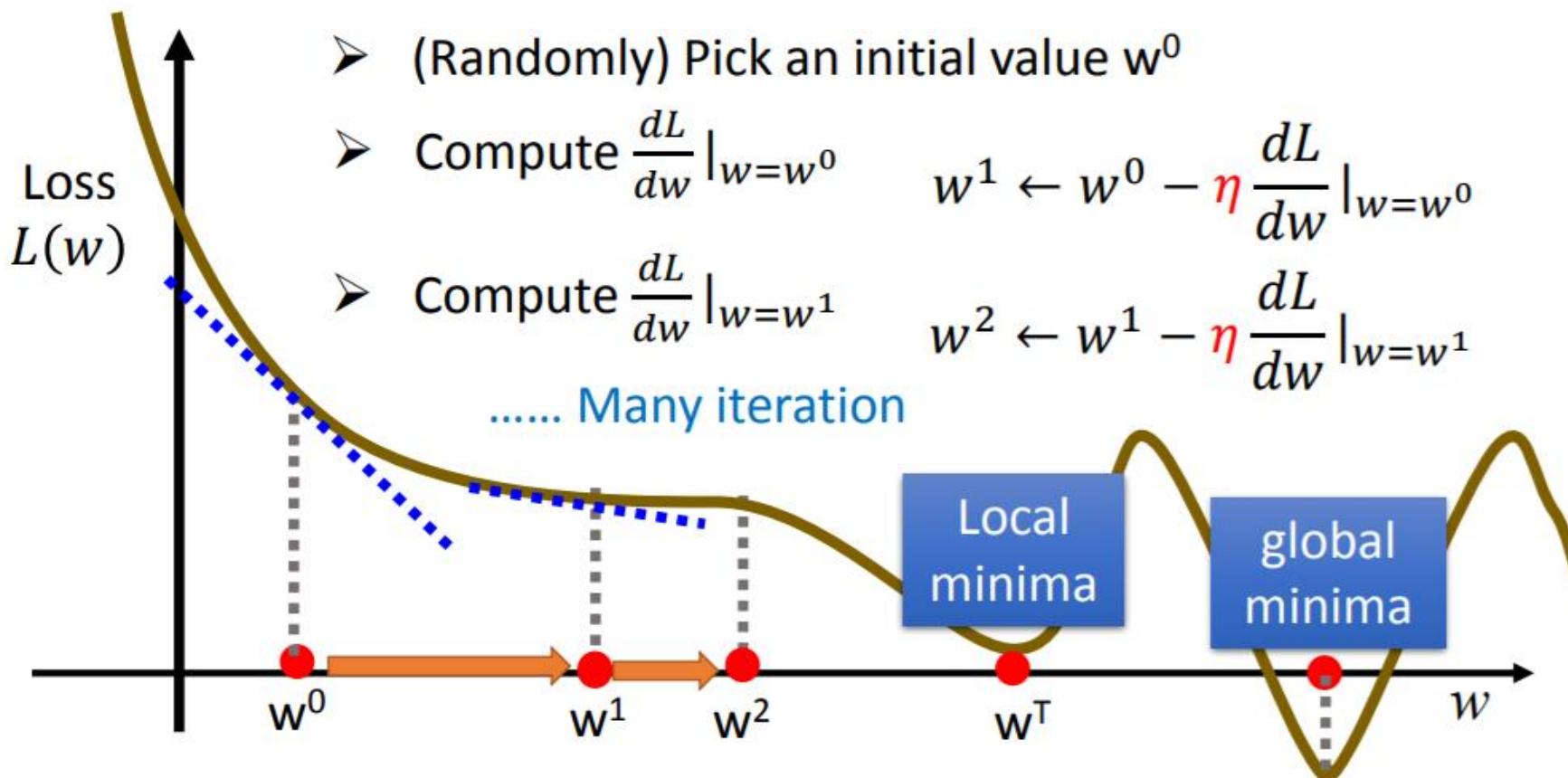
- Consider loss function  $L(w)$  with one parameter  $w$ :



# Gradient decent

$$w^* = \arg \min_w L(w)$$

- Consider loss function  $L(w)$  with one parameter  $w$ :



# Gradient decent to find two parameters $w^*$ and $b^*$

- How about two parameters?  $w^*, b^* = \arg \min_{w,b} L(w, b)$

- (Randomly) Pick an initial value  $w^0, b^0$
- Compute  $\frac{\partial L}{\partial w} |_{w=w^0, b=b^0}, \frac{\partial L}{\partial b} |_{w=w^0, b=b^0}$

$$\left[ \begin{array}{c} \frac{\partial L}{\partial w} \\ \frac{\partial L}{\partial b} \end{array} \right] \text{gradient}$$

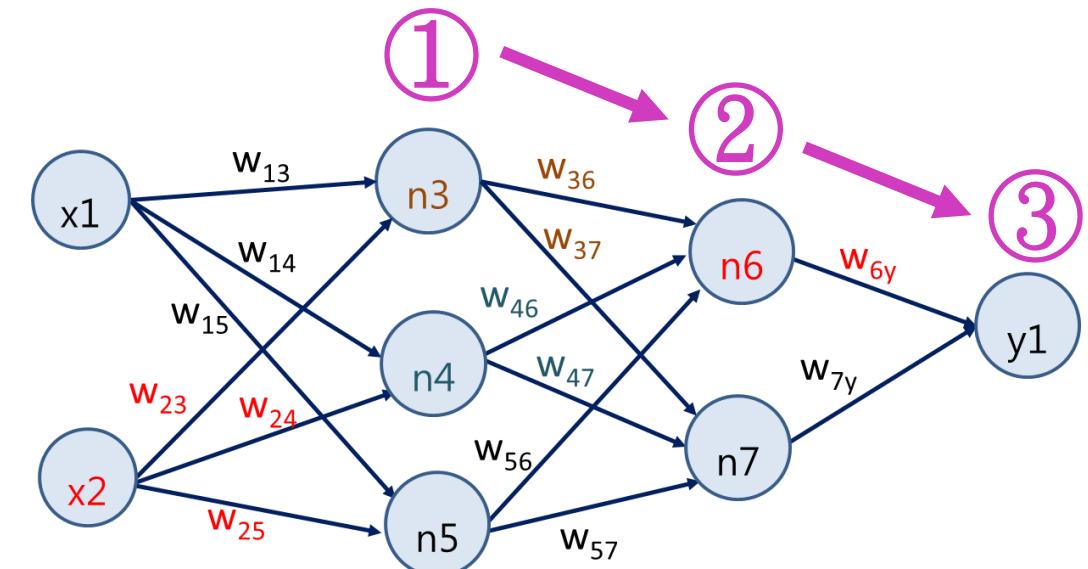
$$w^1 \leftarrow w^0 - \eta \frac{\partial L}{\partial w} |_{w=w^0, b=b^0} \quad b^1 \leftarrow b^0 - \eta \frac{\partial L}{\partial b} |_{w=w^0, b=b^0}$$

- Compute  $\frac{\partial L}{\partial w} |_{w=w^1, b=b^1}, \frac{\partial L}{\partial b} |_{w=w^1, b=b^1}$

$$w^2 \leftarrow w^1 - \eta \frac{\partial L}{\partial w} |_{w=w^1, b=b^1} \quad b^2 \leftarrow b^1 - \eta \frac{\partial L}{\partial b} |_{w=w^1, b=b^1}$$

# Machine learning model (2) – Deep learning

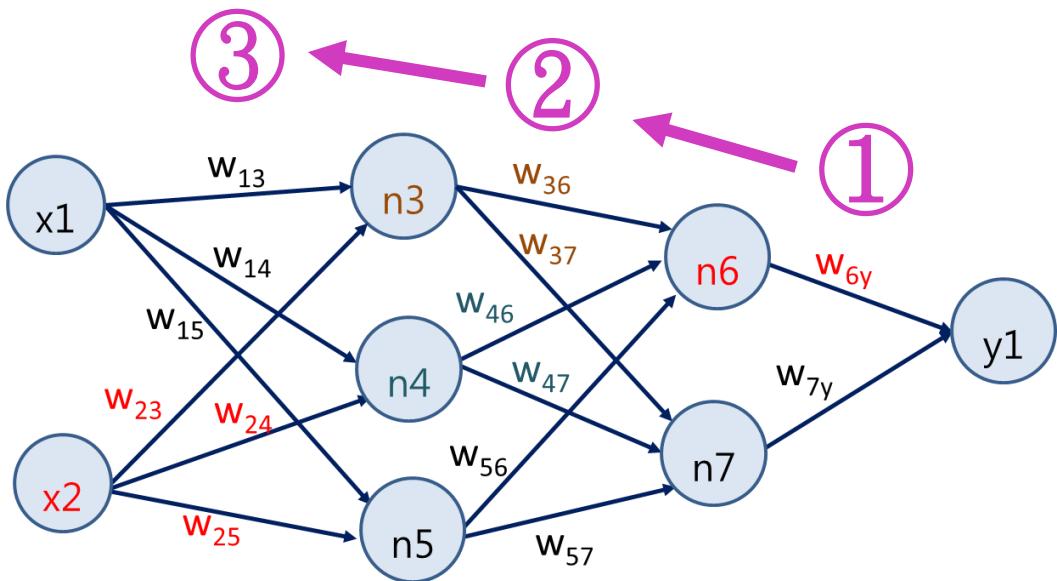
Define a function to be learned:  $y^n = f(x^n)$



- ①  $n_3 = \sigma(x_1 * w_{13} + x_2 * w_{23} + b_3)$
- ①  $n_4 = \sigma(x_1 * w_{14} + x_2 * w_{24} + b_4)$
- ①  $n_5 = \sigma(x_1 * w_{15} + x_2 * w_{25} + b_5)$
- ②  $n_6 = \sigma(n_3 * w_{36} + n_4 * w_{46} + n_5 * w_{56} + b_6)$
- ②  $n_7 = \sigma(n_3 * w_{37} + n_4 * w_{47} + n_5 * w_{57} + b_7)$
- ③  $y_1 = \sigma(n_6 * w_{6y} + n_7 * w_{7y} + b_y)$

# Machine learning model (2) – Deep learning

Use gradient decent to find optimal parameters



$$w_i \leftarrow w_i - \eta \frac{\partial e}{\partial w_i}$$

$$L = g(y - \hat{y}) \quad y = \sigma(n_6 * w_{6y} + n_7 * w_{7y} + b_y)$$

①  $w_{6y} \leftarrow w_{6y} - \eta \frac{\partial L}{\partial w_{6y}} \quad \frac{\partial L}{\partial w_{6y}} = \frac{\partial L}{\partial y} \frac{\partial y}{\partial w_{6y}}$

②  $w_{7y} \leftarrow w_{7y} - \eta \frac{\partial L}{\partial w_{7y}} \quad \frac{\partial L}{\partial w_{7y}} = \frac{\partial L}{\partial y} \frac{\partial y}{\partial w_{7y}}$

③  $w_{57} \leftarrow w_{57} - \eta \frac{\partial L}{\partial w_{57}} \quad \frac{\partial L}{\partial w_{57}} = \frac{\partial L}{\partial y} \frac{\partial y}{\partial n_7} \frac{\partial n_7}{\partial w_{57}}$

$$n_7 = f(n_3 * w_{37} + n_4 * w_{47} + n_5 * w_{57} + b_7)$$

# Jeffery Hinton



Geoffrey Hinton spent 30 years hammering away at an idea most other scientists dismissed as nonsense. Then, one day in 2012, he was proven right. Canada's most influential thinker in the field of artificial intelligence is far too classy to say I told you so

<https://torontolife.com/tech/ai-superstars-google-facebook-apple-studied-guy/>

For more than 30 years, Geoffrey Hinton hovered at the edges of artificial intelligence research, an outsider clinging to a simple proposition: that computers could think like humans do—using intuition rather than rules.

Geoffrey Hinton 多年來堅持着一個簡單的觀點：電腦可以像人類一樣思考-用直覺而不是規則。Hinton 一直好奇的是，電腦能不能像人類大腦一樣的工作：信息通過一個巨大的，由神經元圖譜連接起來的細胞網絡傳播，在多達十億條的路徑上發射、連接和傳輸。

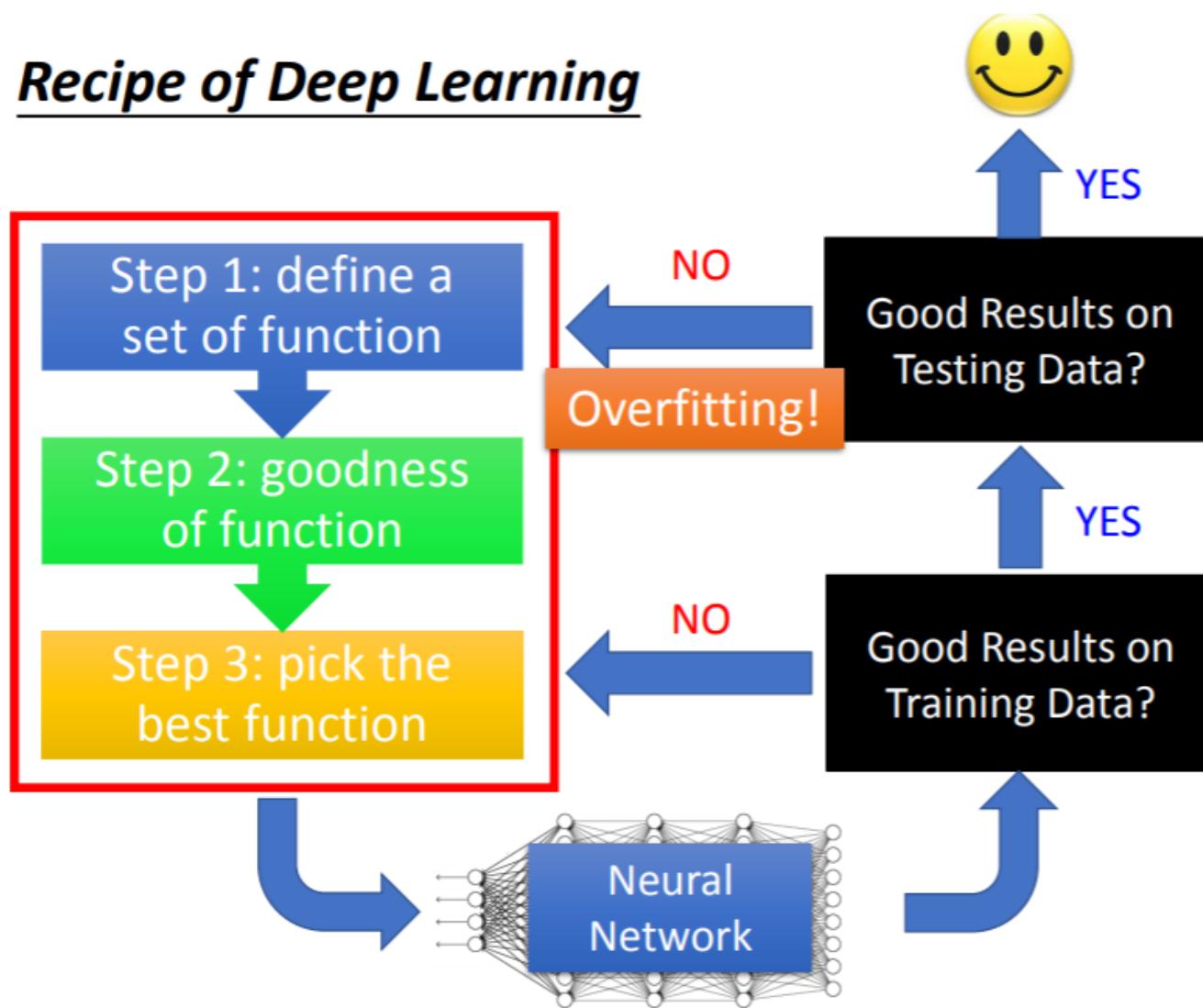
# Practice – MLP regression

The screenshot shows a Google Colaboratory interface with a modal dialog for GitHub integration. The dialog has a yellow header bar with tabs for '範例' (Examples), '最近' (Recent), 'Google 雲端硬碟' (Google Cloud Storage), 'GitHub' (selected), and '上傳' (Upload). A red circle highlights the 'GitHub' tab. Below the tabs is a search bar labeled '輸入 GitHub 網址或依機構或使用者搜尋' (Enter GitHub URL or search by organization or user) with a placeholder 'TienLungSun'. To the right of the search bar is a checkbox for '包括私人存放區' (Include private repositories) and a search icon. A red circle highlights the search bar and its placeholder. Below the search bar are fields for '存放區:' (Repository) with a dropdown set to 'TienLungSun/2020-PyTorch-Colab' and '分支版本:' (Branch) with a dropdown set to 'main'. A red circle highlights these fields. The main content area displays a list of Jupyter notebooks:

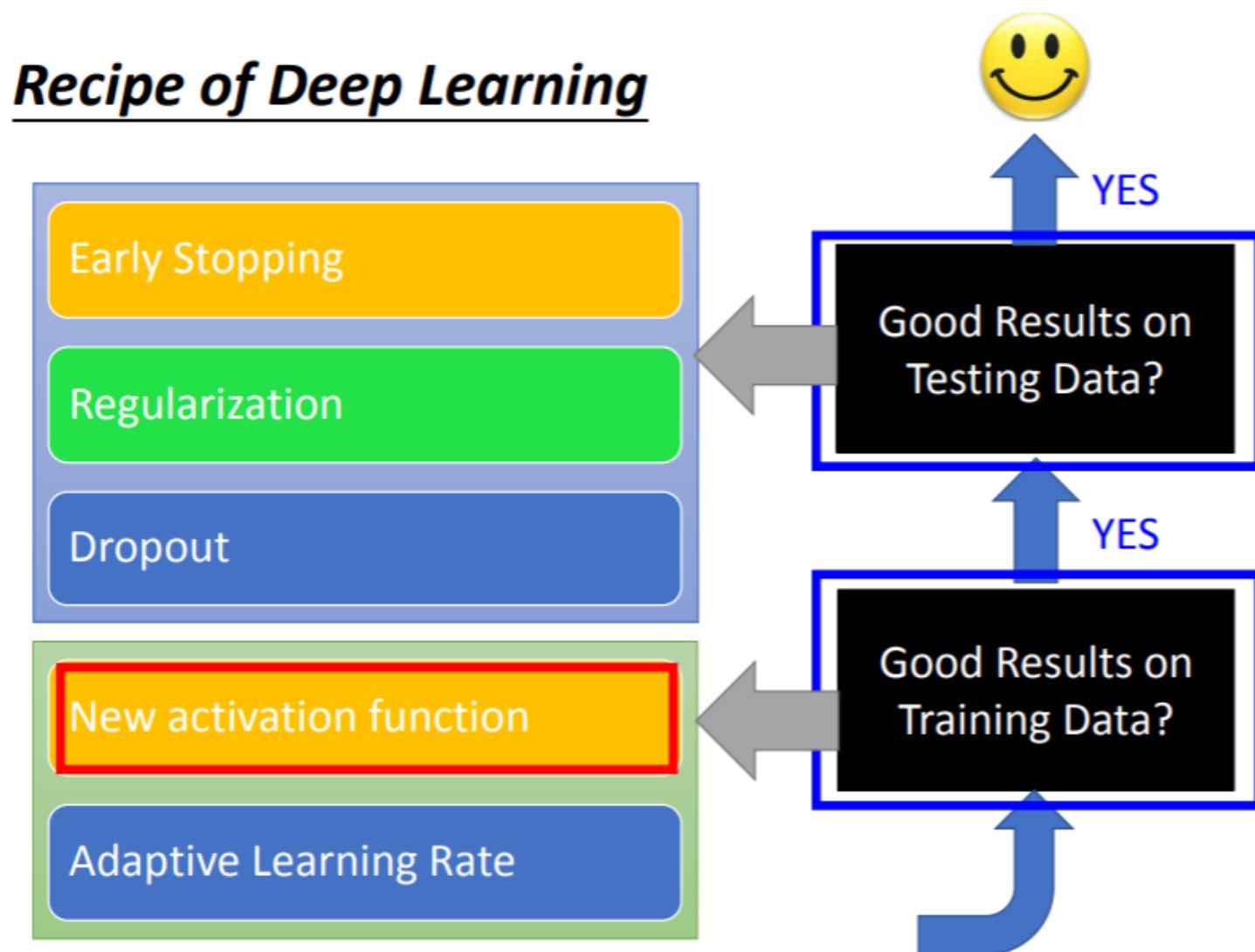
- 1. 1. Understand MLP.ipynb
- 1. 2. MLP regression.ipynb (highlighted with a red circle)
- 1. 3. MLP Classification.ipynb
- 2. 1. Understand CNN.ipynb

At the bottom right of the dialog is a '取消' (Cancel) button. The background shows the standard Colaboratory dashboard with various tabs like 'Machine Learning (Hung-yi)', 'Hung-yi Lee', and '歡迎使用 Colaboratory - Colab'.

# Recipe of deep learning



# When training result is not good

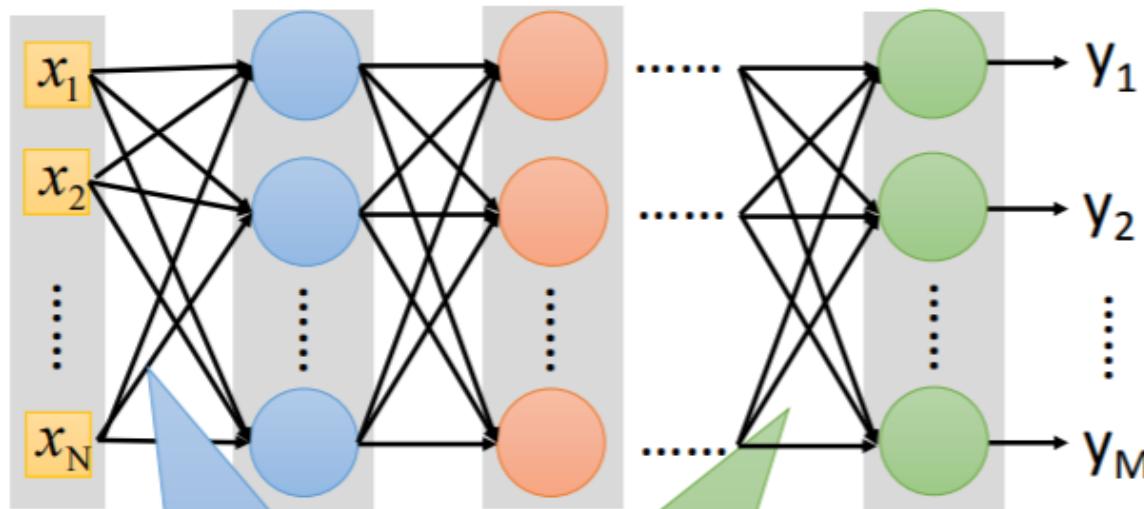


# Practice – Activation function

- Run "1.2 MLP regression.ipynb", change the activation function from ReLU to Sigmoid and explain why the results become worse?



# Vanishing gradient problem



Smaller gradients

Learn very slow

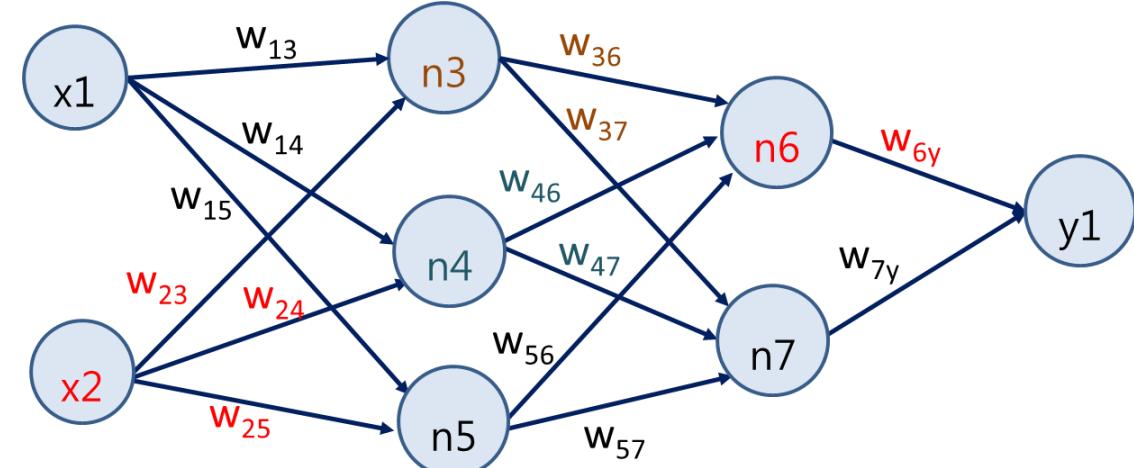
Almost random

Larger gradients

Learn very fast

Already converge

based on random!?

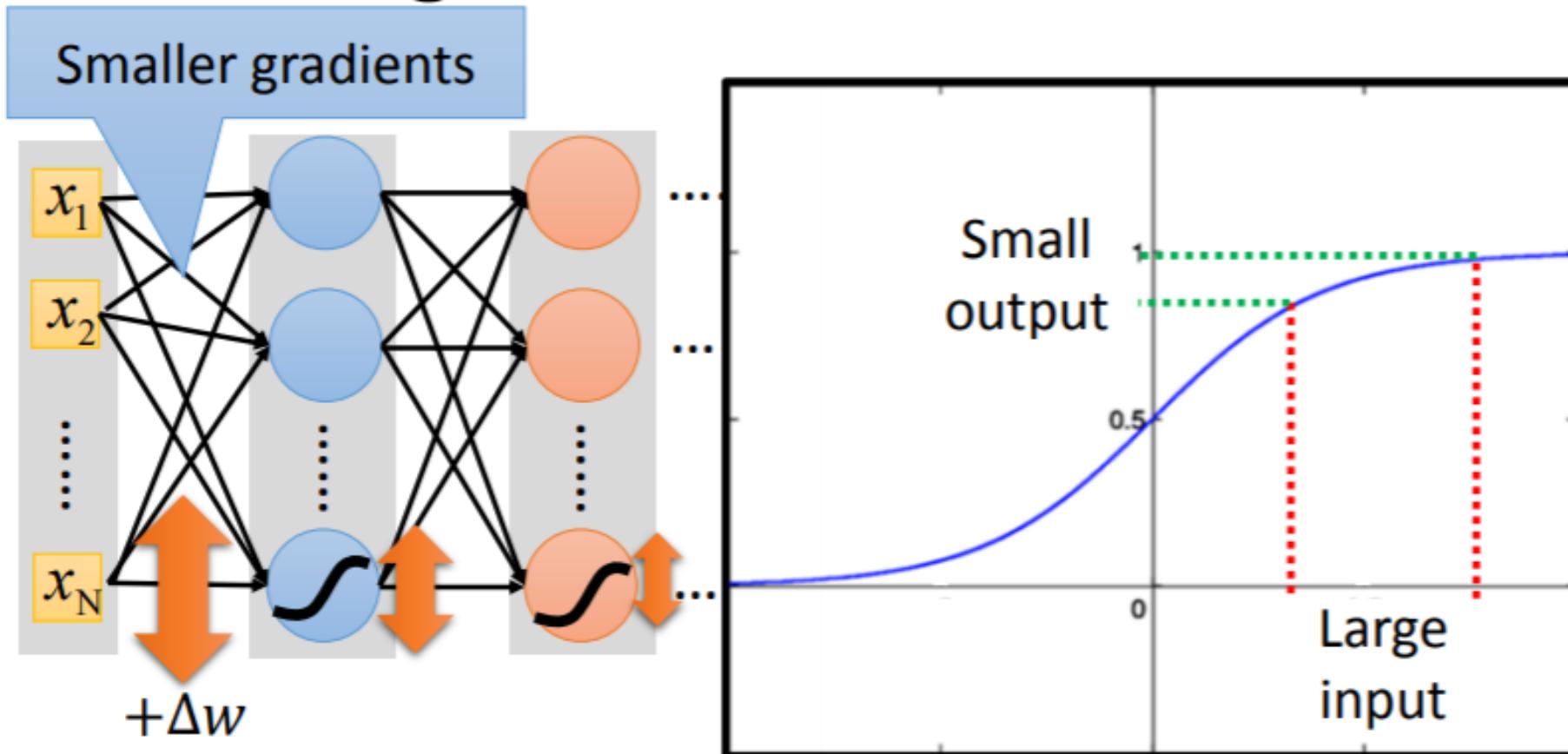


$$\frac{\partial L}{\partial w_{6y}} = \frac{\partial L}{\partial y_1} \frac{\partial y_1}{\partial w_{6y}}$$

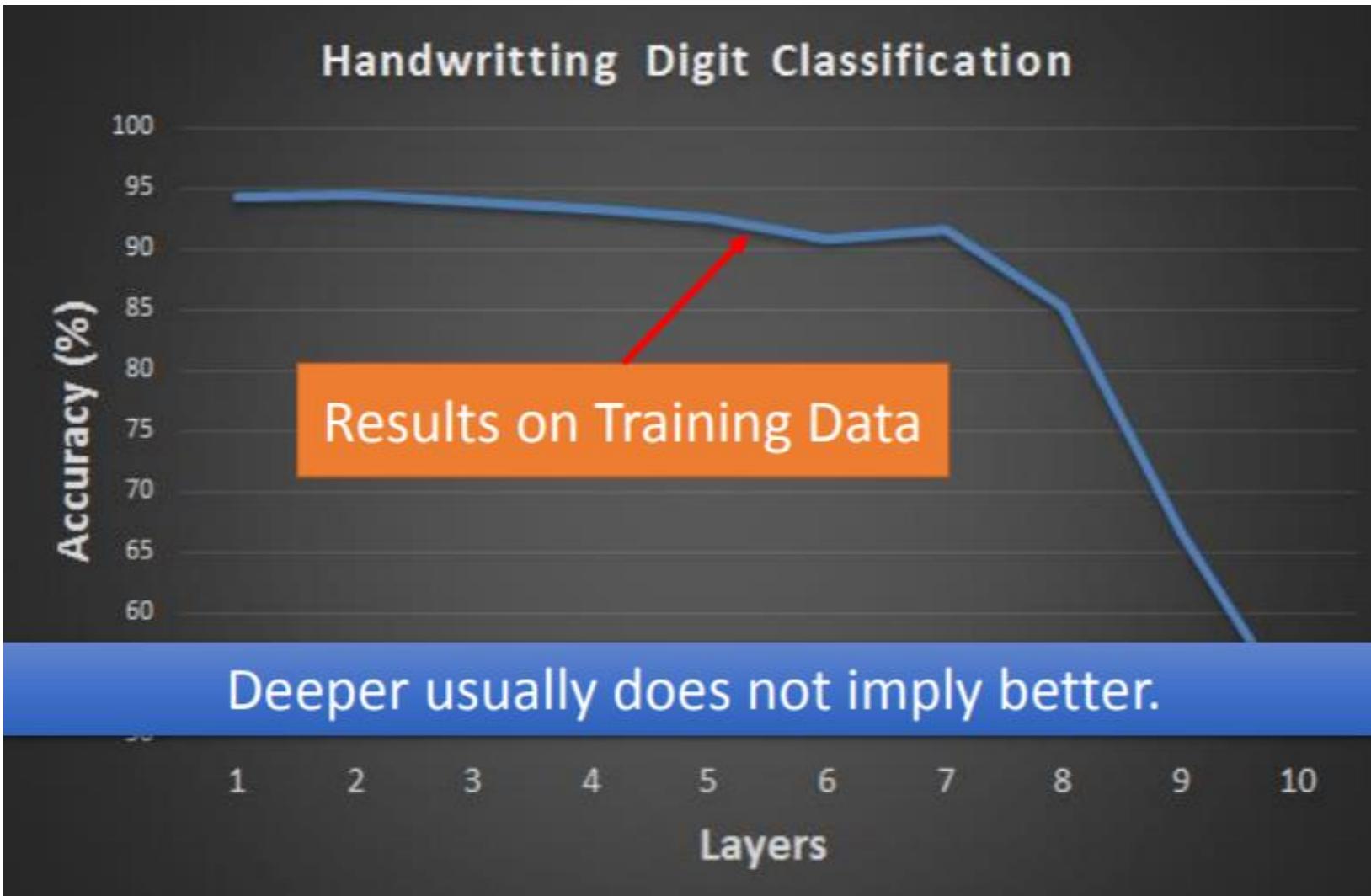
$$\frac{\partial L}{\partial w_{57}} = \frac{\partial L}{\partial y_1} \frac{\partial y_1}{\partial n_7} \frac{\partial n_7}{\partial w_{57}}$$

# Vanishing gradient problem

$$n_7 = \sigma(n_3 * w_{37} + n_4 * w_{47} + n_5 * w_{57} + b_7)$$

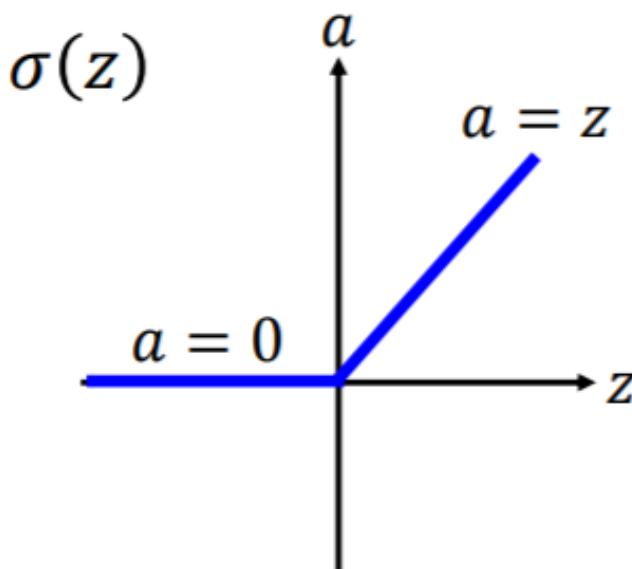


# Sigmoid is hard to get the power of deep



# ReLU

- Rectified Linear Unit (ReLU)



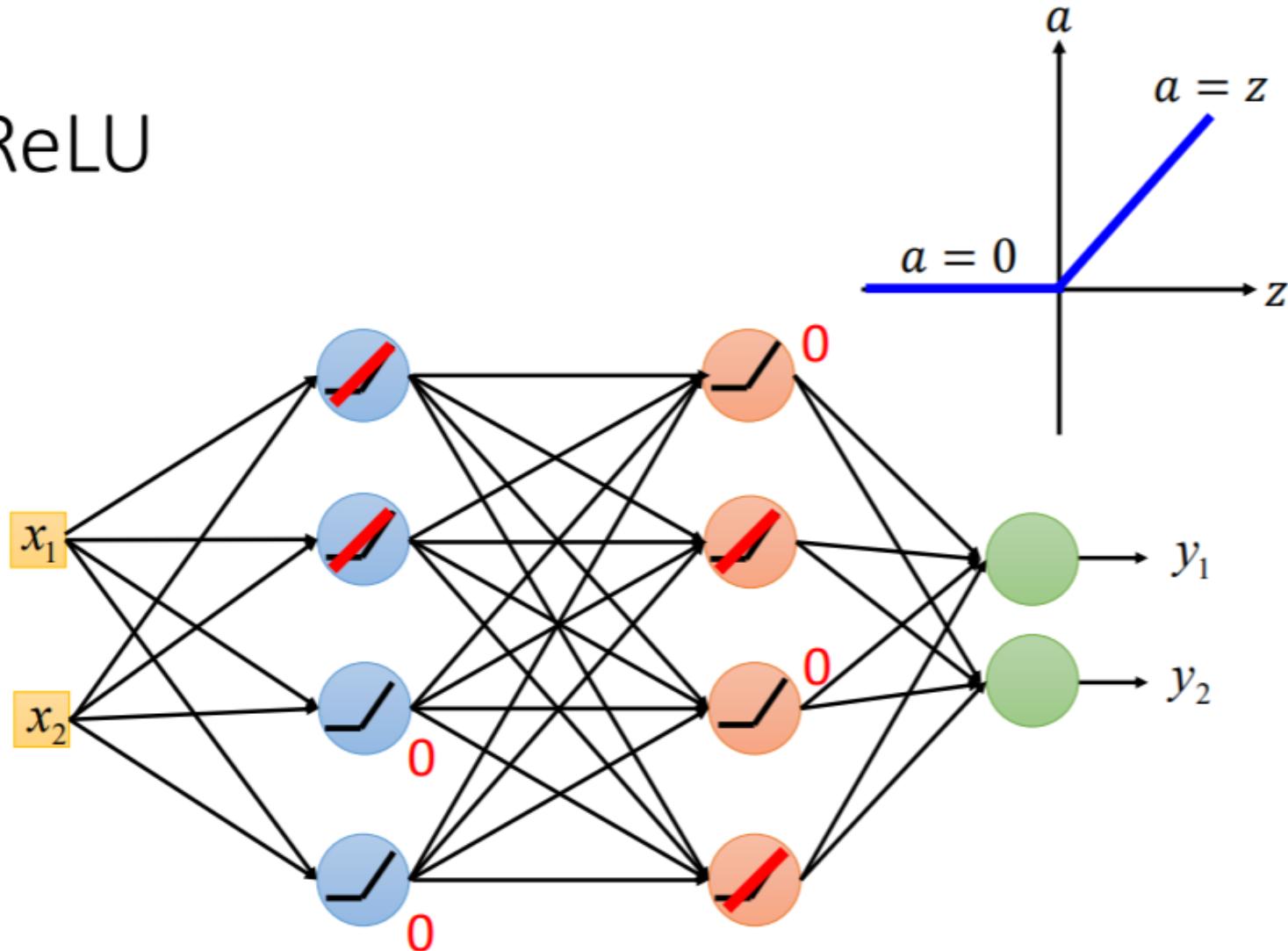
[Xavier Glorot, AISTATS'11]  
[Andrew L. Maas, ICML'13]  
[Kaiming He, arXiv'15]

**Reason:**

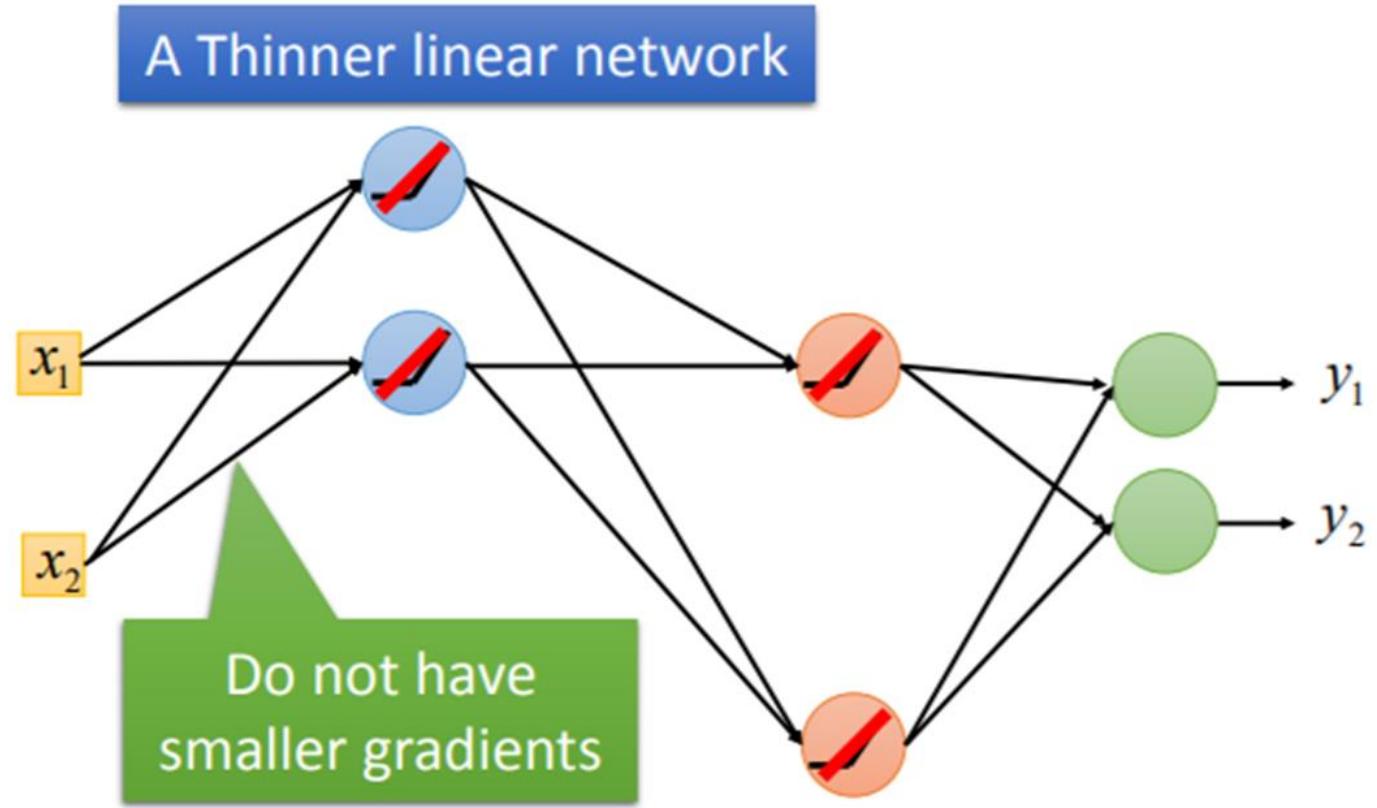
1. Fast to compute
2. Biological reason
3. Infinite sigmoid with different biases
4. Vanishing gradient problem

# ReLU

ReLU



# ReLU



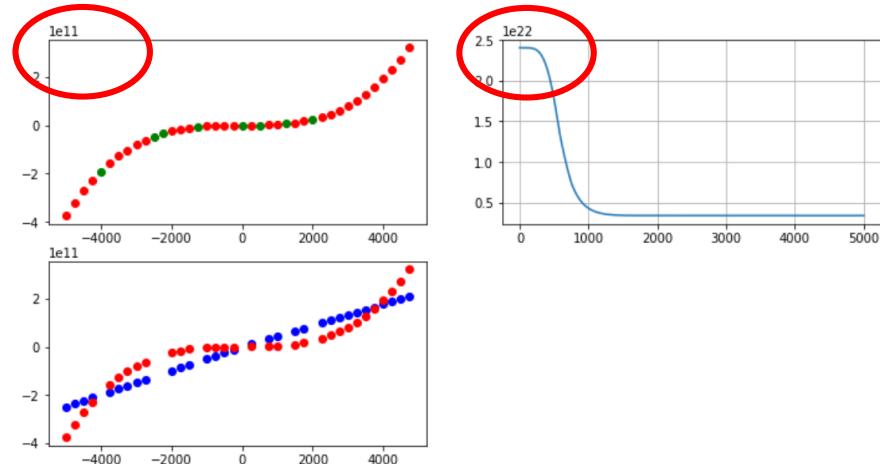
# Practice

- Run "1. 2.1 MLP regression practice.ipynb"

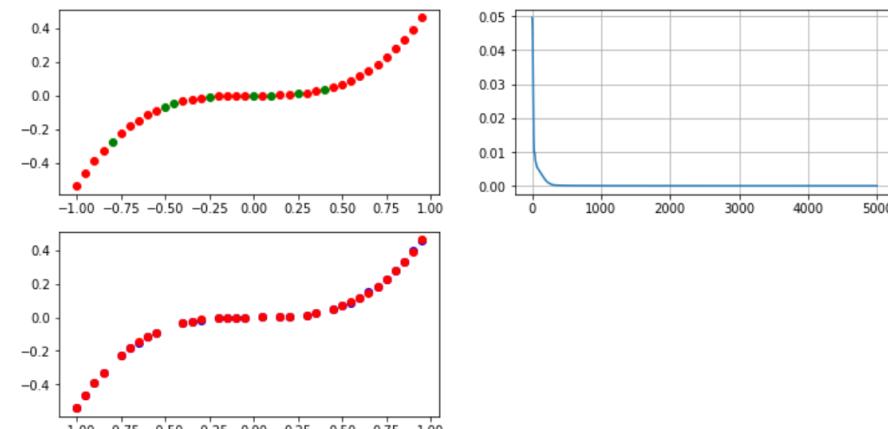


# 3-Lyaer NN

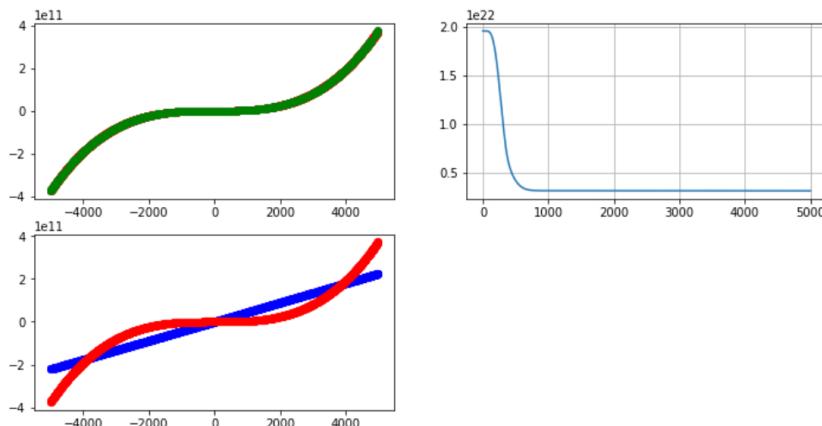
Without normalization, the 3-layer NN is not able to learn from 32 data sampled from -5000 to 5000.



With both  $x$  and  $y$  normalized to  $[-1, 1]$ , the 3-layer NN is able to learn from 32 data sampled from  $[-5000, 5000]$  that full describe the characteristics of the cubic function.

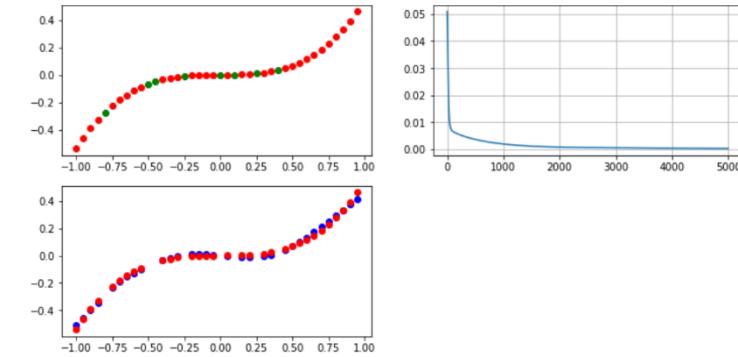


Increase the number of data from 32 to 1600. Without normalization, the 3-layer NN is not able to learn.

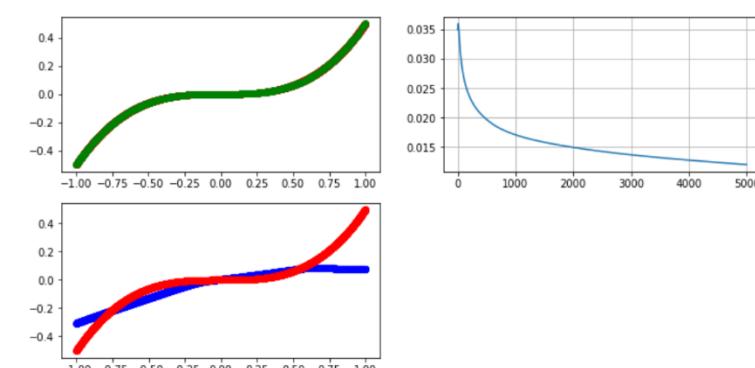


# 2-Lyaer NN

The 2-layer NN can also learn from 32 data. As long as  $x$  and  $y$  are normalized and the data full describe the characteristics of the cubic function.



Even  $x$  and  $y$  are normalized to  $[-1, 1]$ , the 2-layer NN is not able to learn from 1600 data.



# HW3 (1)

- Design your training data and  $y = f(x)$ . Experiment with different NN designs.

		Training
No of parameters =	Deep and thing	
	Shallow and fat	
	In-between version	
No of parameters =	Deep and thing	
	Shallow and fat	
	In-between version	



Overfitting problem – NN performs well on training  
data but not good on test data

	<b>Underfitting</b>	<b>Just right</b>	<b>Overfitting</b>
<b>Symptoms</b>	<ul style="list-style-type: none"> <li>• High training error</li> <li>• Training error close to test error</li> <li>• High bias</li> </ul>	<ul style="list-style-type: none"> <li>• Training error slightly lower than test error</li> </ul>	<ul style="list-style-type: none"> <li>• Very low training error</li> <li>• Training error much lower than test error</li> <li>• High variance</li> </ul>
<b>Regression illustration</b>			
<b>Classification illustration</b>			
<b>Deep learning illustration</b>			
<b>Possible remedies</b>	<ul style="list-style-type: none"> <li>• Complexify model</li> <li>• Add more features</li> <li>• Train longer</li> </ul>		<ul style="list-style-type: none"> <li>• Perform regularization</li> <li>• Get more data</li> </ul>

# Practice – Overfitting

- Run "1. 2.2. Overfitting.ipynb", observe the overfitting problem.



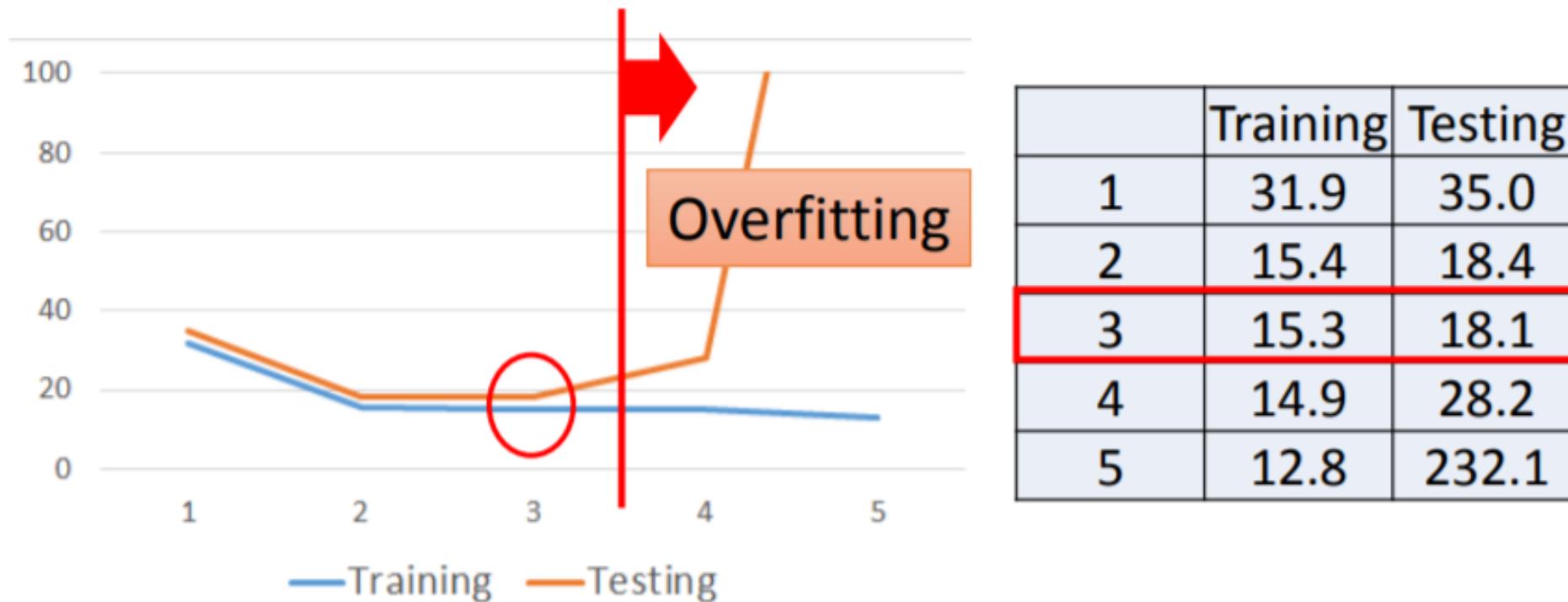
## HW3 (2)

- Extend HW3(1) to report overfitting problem.

		Training	Testing
No of parameters =	Deep and thing		
	Shallow and fat		
	In-between version		
No of parameters =	Deep and thing		
	Shallow and fat		
	In-between version		



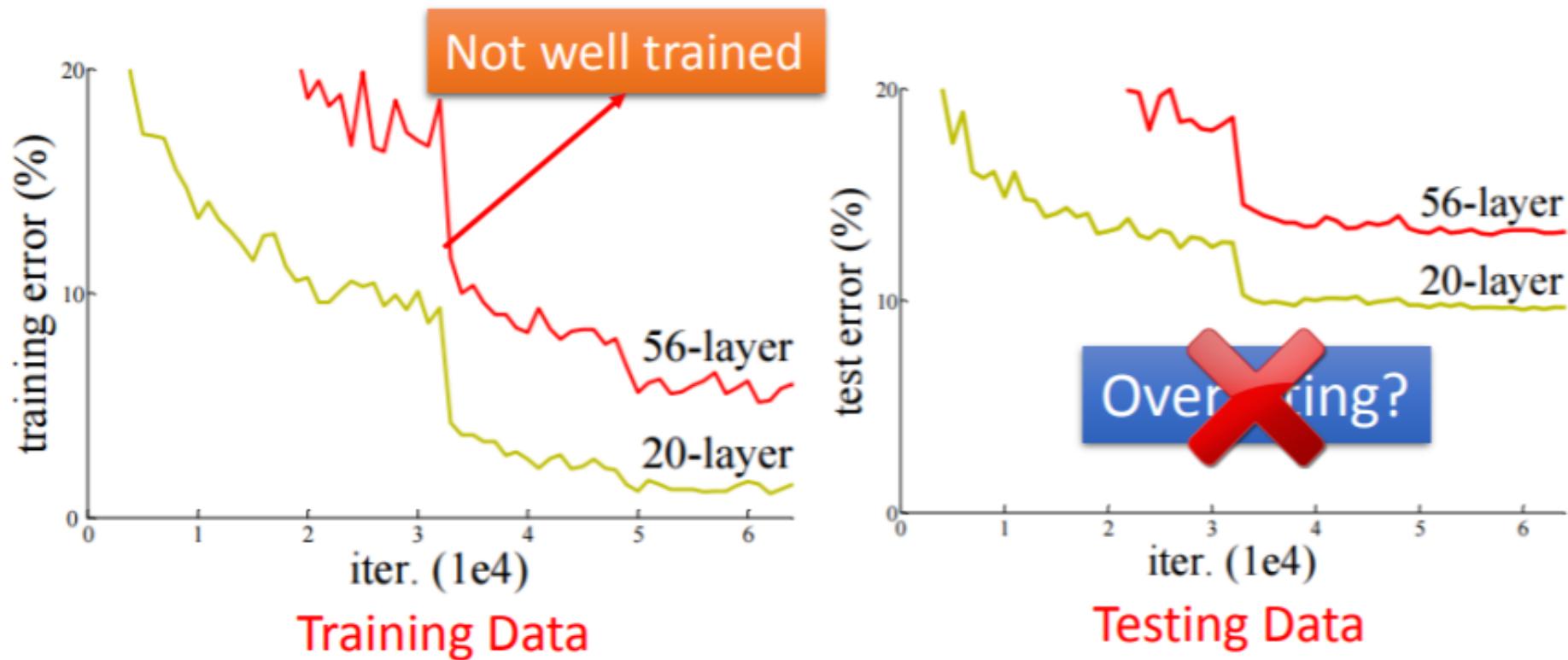
# Overfitting problem



A more complex model does not always lead to better performance on testing data.

This is **Overfitting**. ➔ Select suitable model

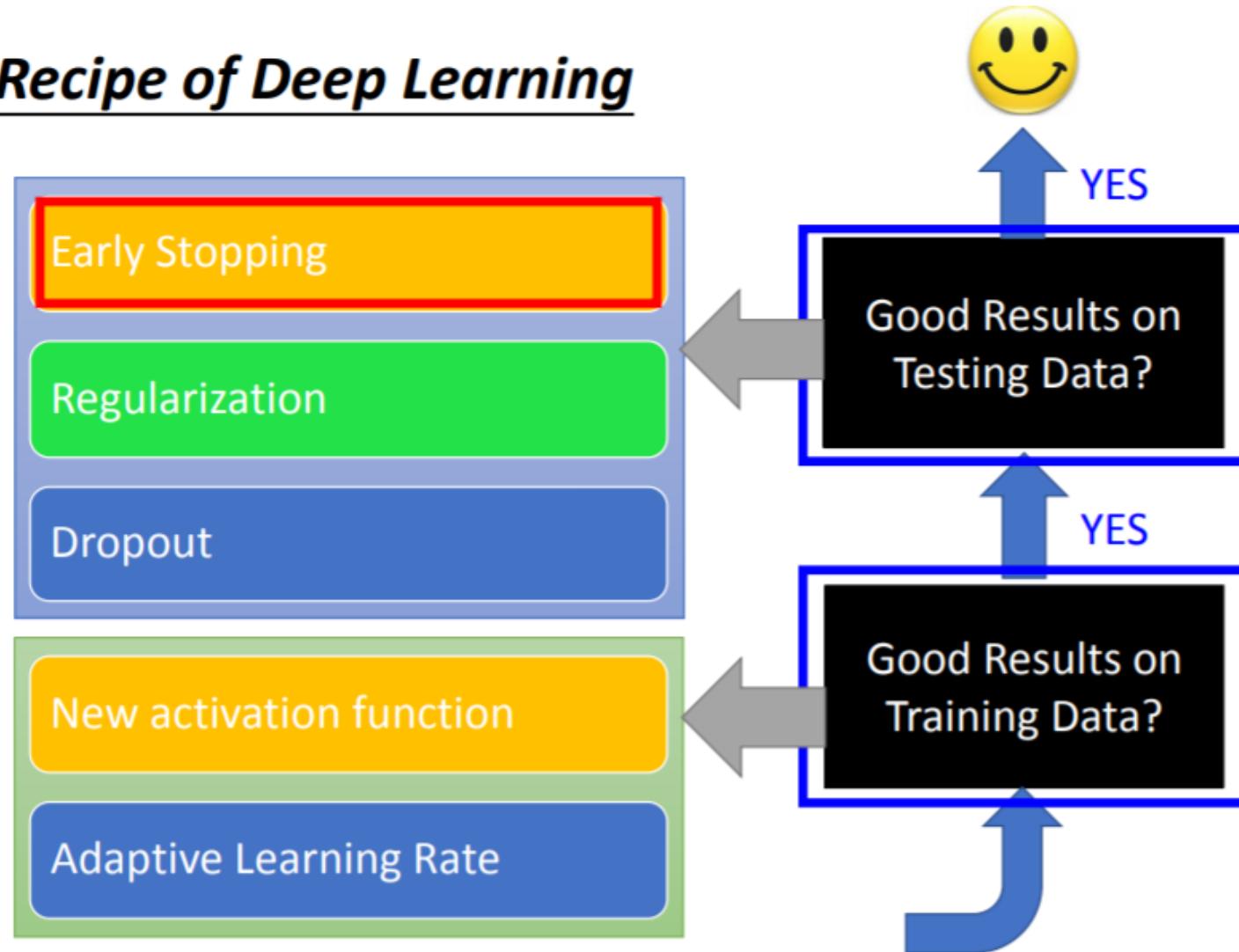
# Do not always blame overfitting



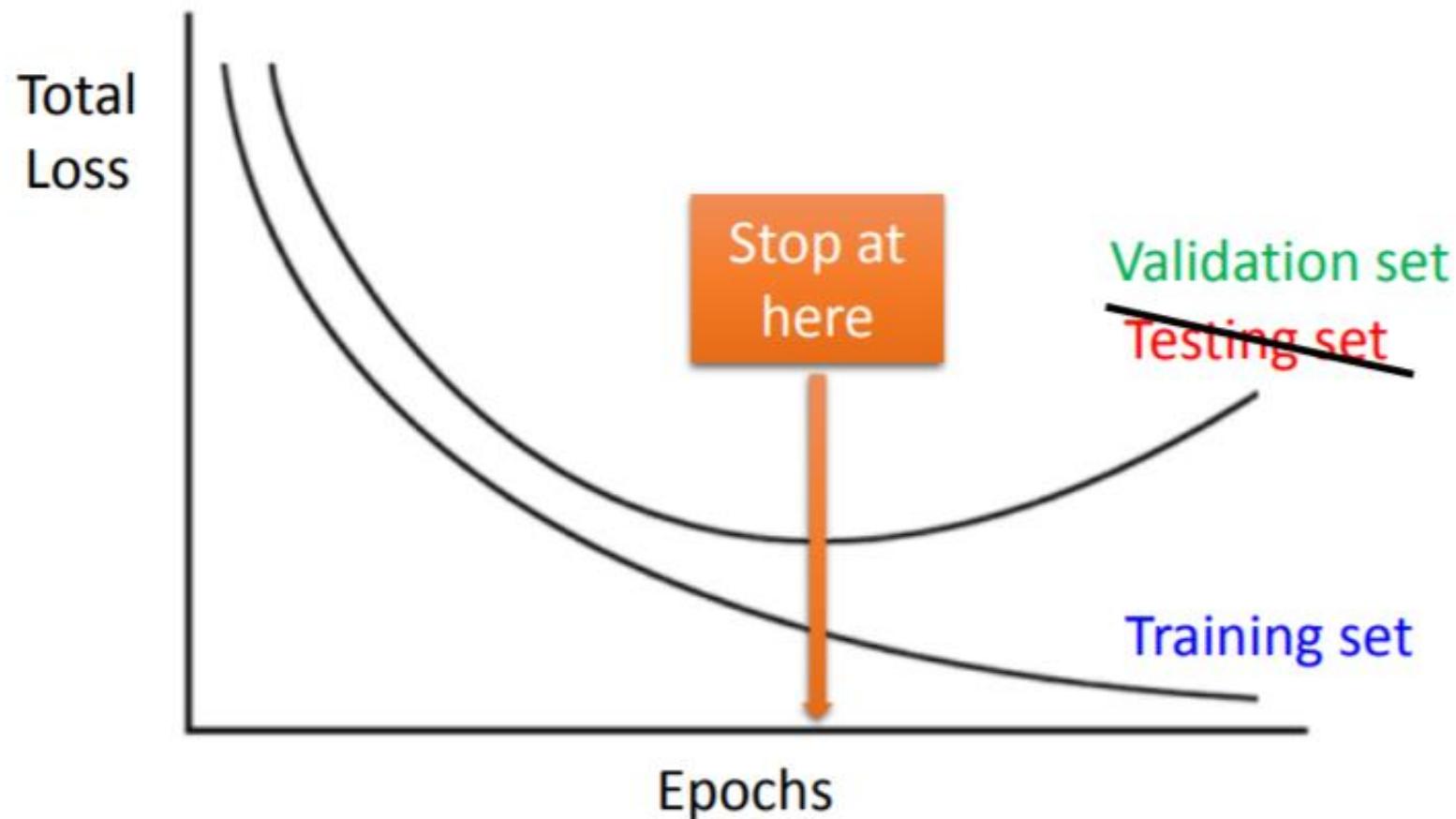
Deep Residual Learning for Image Recognition  
<http://arxiv.org/abs/1512.03385>

# What to do if overfitting?

## Recipe of Deep Learning



# Early stopping



Keras: [http://keras.io/getting-started/faq/#how-can-i-interrupt-training-when-the-validation-loss-isn't-decreasing-anymore](http://keras.io/getting-started/faq/#how-can-i-interrupt-training-when-the-validation-loss-isn-t-decreasing-anymore)

## HW3 (3)

- Based on HW3(2), experiment the effect of early stop on resolving overfitting.

		Training with early stop	Testing
No of parameters =	Deep and thing		
	Shallow and fat		
	In-between version		
No of parameters =	Deep and thing		
	Shallow and fat		
	In-between version		



# Regularization – L2

- Find a set of weight not only minimizing original cost but also close to zero

$$L'(\theta) = \underline{L(\theta)} + \lambda \frac{1}{2} \|\theta\|_2 \rightarrow \text{Regularization term}$$

Original loss

$$L(\theta) = \sum_{n=1}^N (\hat{y}^n - y^n)^2$$

$$\theta = \{w_1, w_2, \dots\}$$

L2 regularization:

$$\|\theta\|_2 = (w_1)^2 + (w_2)^2 + \dots$$

(usually not consider biases)

# L2 regularization

$$L'(\theta) = L(\theta) + \lambda \frac{1}{2} \|\theta\|_2 \quad \text{Gradient: } \frac{\partial L'}{\partial w} = \frac{\partial L}{\partial w} + \lambda w$$

Update:  $w^{t+1} \rightarrow w^t - \eta \frac{\partial L'}{\partial w} = w^t - \eta \left( \frac{\partial L}{\partial w} + \lambda w^t \right)$

$$= \underbrace{(1 - \eta \lambda)w^t}_{\downarrow} - \eta \underbrace{\frac{\partial L}{\partial w}}_{\text{Weight Decay}}$$

Closer to zero

Vanilla gradient decent update  $w^{t+1} \rightarrow w^t - \eta \frac{\partial L}{\partial w}$

## HW3 (4)

- Based on HW3(2), experiment the effect of L2 regularization on resolving overfitting.

		Train with L2 regularization	Testing
No of parameters =	Deep and thing		
	Shallow and fat		
	In-between version		
No of parameters =	Deep and thing		
	Shallow and fat		
	In-between version		



# L1 regularization

L1 regularization:

$$\|\theta\|_1 = |w_1| + |w_2| + \dots$$

$$L'(\theta) = L(\theta) + \lambda \frac{1}{2} \|\theta\|_1 \quad \frac{\partial L'}{\partial w} = \frac{\partial L}{\partial w} + \lambda \operatorname{sgn}(w)$$

Update:

$$\begin{aligned} w^{t+1} &\rightarrow w^t - \eta \frac{\partial L'}{\partial w} = w^t - \eta \left( \frac{\partial L}{\partial w} + \lambda \operatorname{sgn}(w^t) \right) \\ &= w^t - \eta \frac{\partial L}{\partial w} - \underline{\eta \lambda \operatorname{sgn}(w^t)} \quad \text{Always delete} \\ &= (1 - \eta \lambda) w^t - \eta \frac{\partial L}{\partial w} \quad \dots \dots \text{L2} \end{aligned}$$

## HW3 (5)

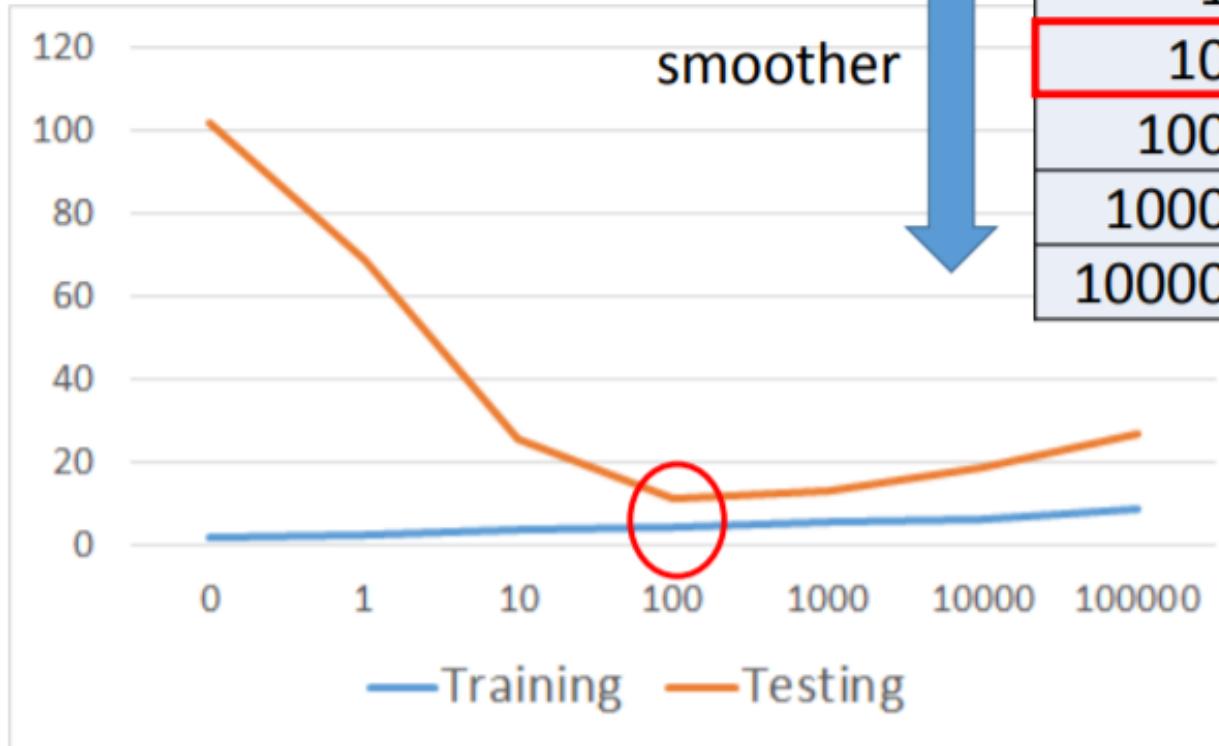
- Based on HW3(2), experiment the effect of L1 regularization on resolving overfitting.

		Train with L1 regularization	Testing
No of parameters =	Deep and thing		
	Shallow and fat		
	In-between version		
No of parameters =	Deep and thing		
	Shallow and fat		
	In-between version		



# Regularization

## Regularization

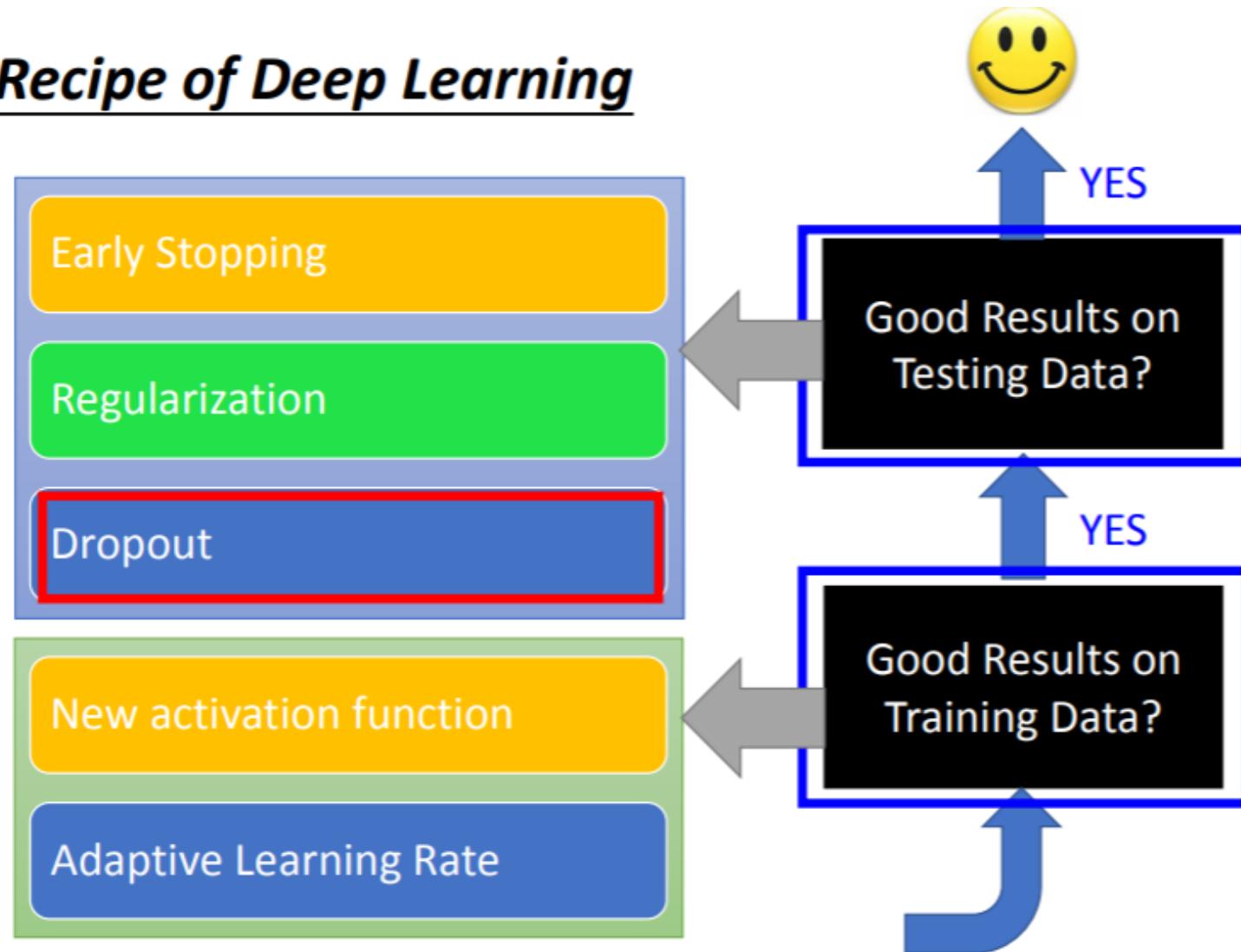


$\lambda$	Training	Testing
0	1.9	102.3
1	2.3	68.7
10	3.5	25.7
100	4.1	11.1
1000	5.6	12.8
10000	6.3	18.7
100000	8.5	26.8

How smooth?  
Select  $\lambda$  obtaining  
the best model

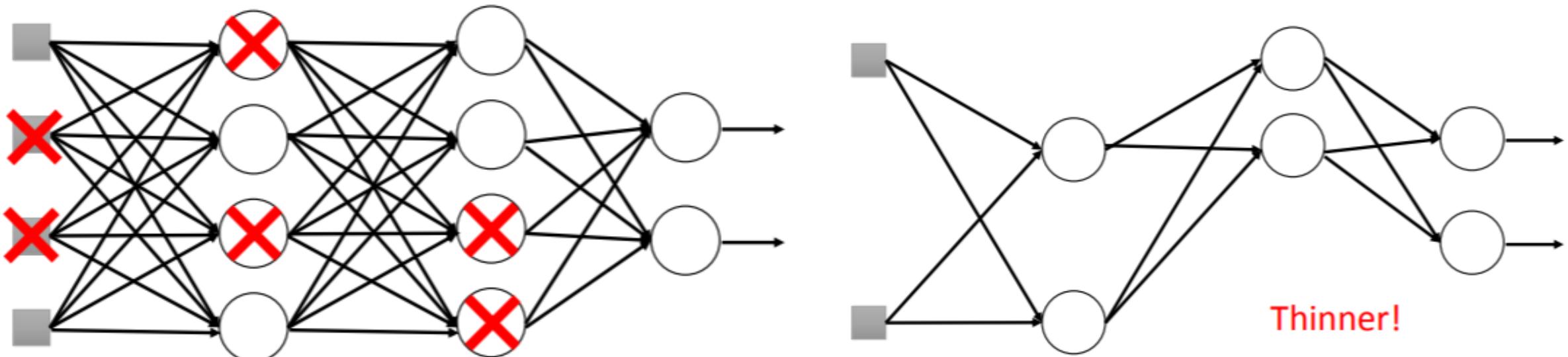
# Drop out

## Recipe of Deep Learning



# Drop out

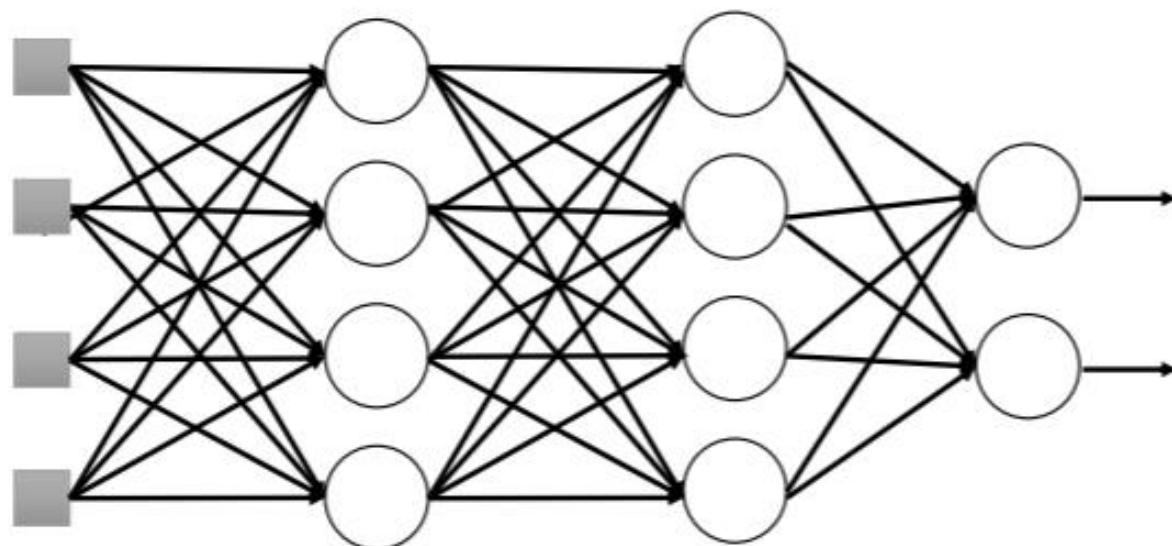
Each time before updating  $\theta$ , each neuron has  $p\%$  to dropout. So the  $NN$  structure is changed (become thinner). That is, for each mini-batch, we resample the dropout neurons.



# Drop out

No neuron drop out at test stage. All weights time  $1 - p\%$

## Testing:



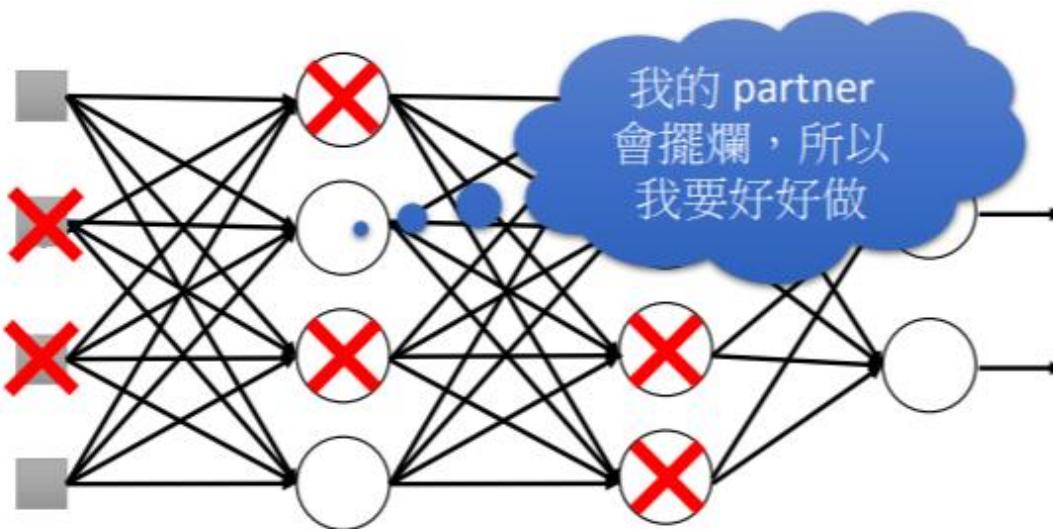
## HW3 (6)

- Based on HW3(2), experiment the effect of drop out on resolving overfitting.

		Train using drop out	Testing
No of parameters =	Deep and thin		
	Shallow and fat		
	In-between version		
No of parameters =	Deep and thin		
	Shallow and fat		
	In-between version		



# Why drop out makes NN perform better?



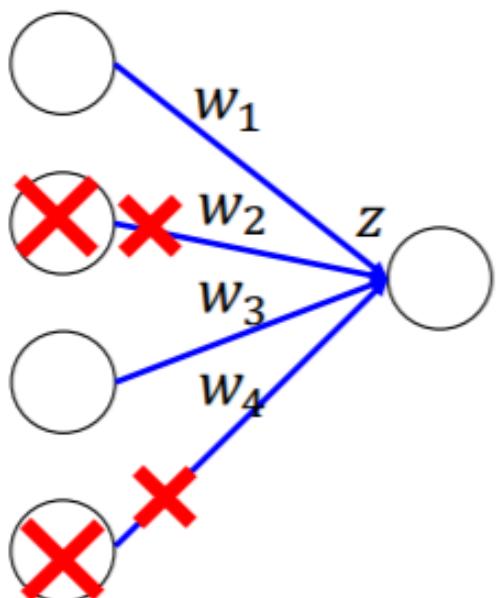
- When teams up, if everyone expect the partner will do the work, nothing will be done finally.
- However, if you know your partner will dropout, you will do better.
- When testing, no one dropout actually, so obtaining good results eventually.

# Why multiply weights by $(1-p)\%$ during testing?

- Why the weights should multiply  $(1-p)\%$  (dropout rate) when testing?

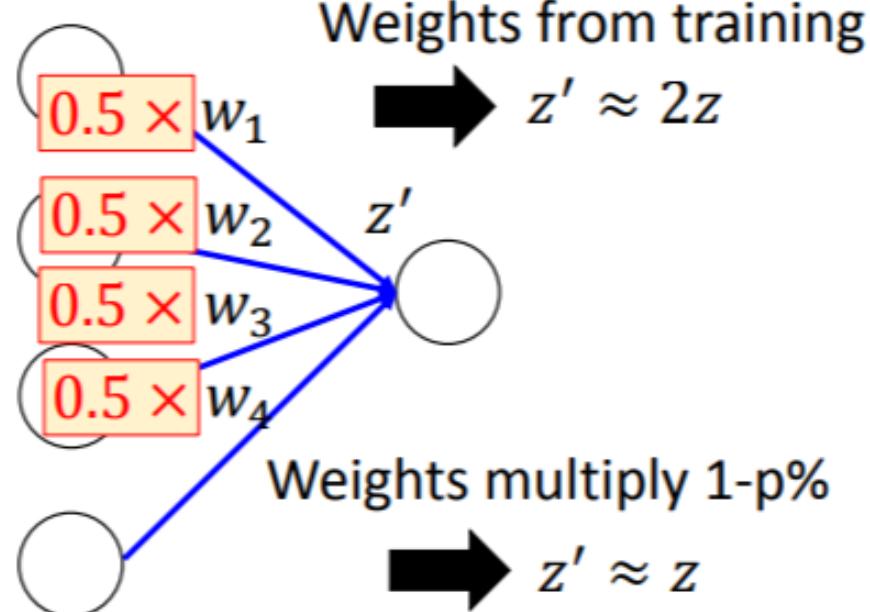
## Training of Dropout

Assume dropout rate is 50%



## Testing of Dropout

No dropout

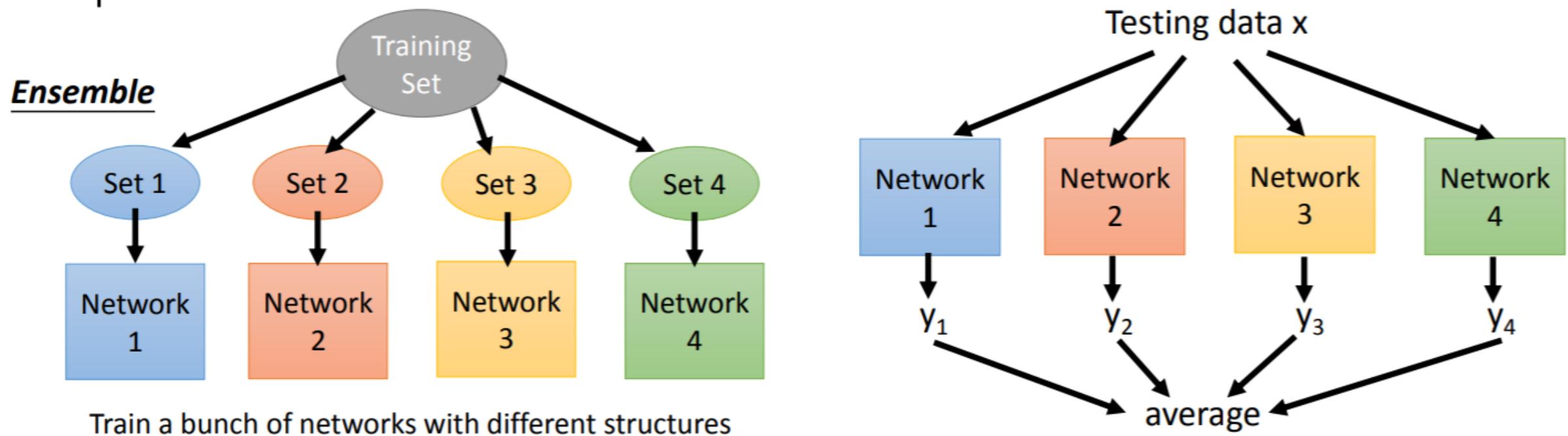


Weights multiply  $1-p\%$

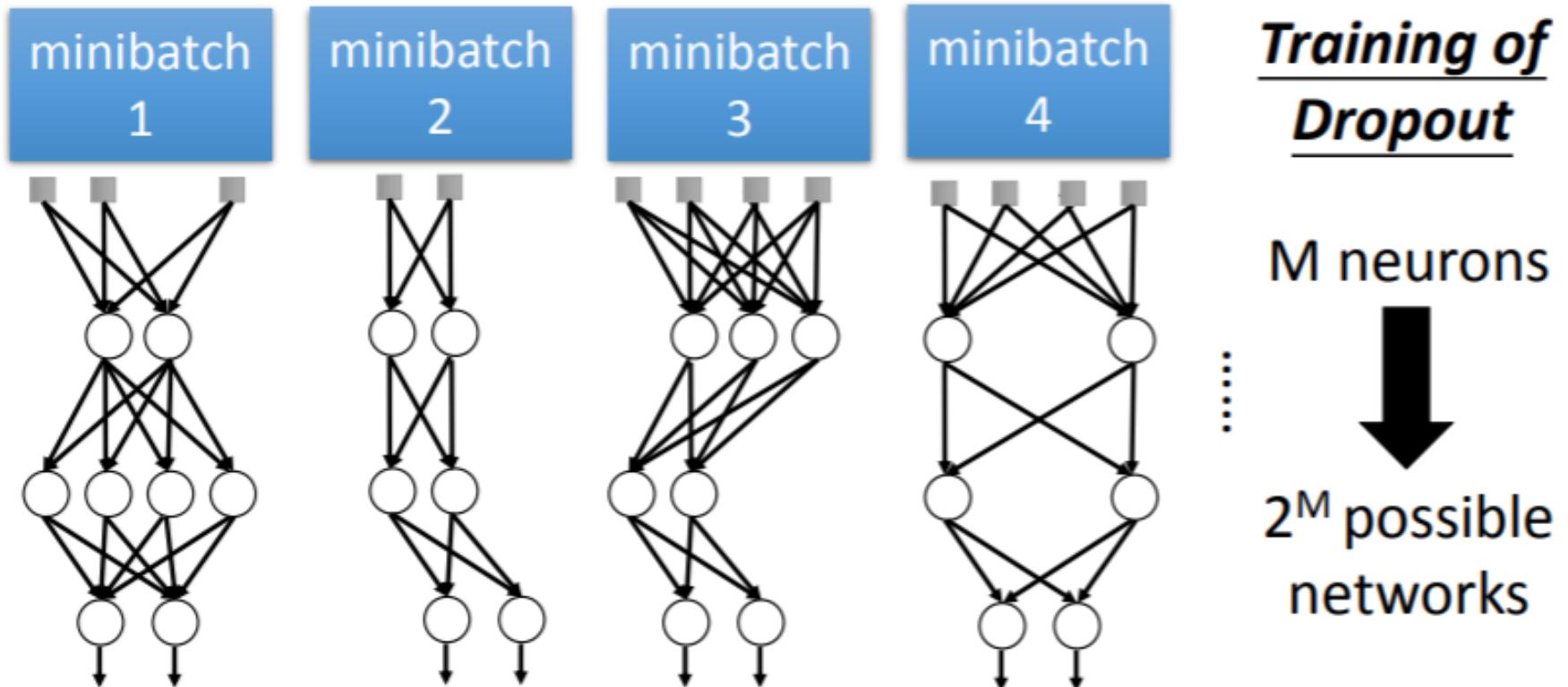
$$\rightarrow z' \approx z$$

# Why drop out makes NN performs better?

Drop out can be seen as an ensemble method.

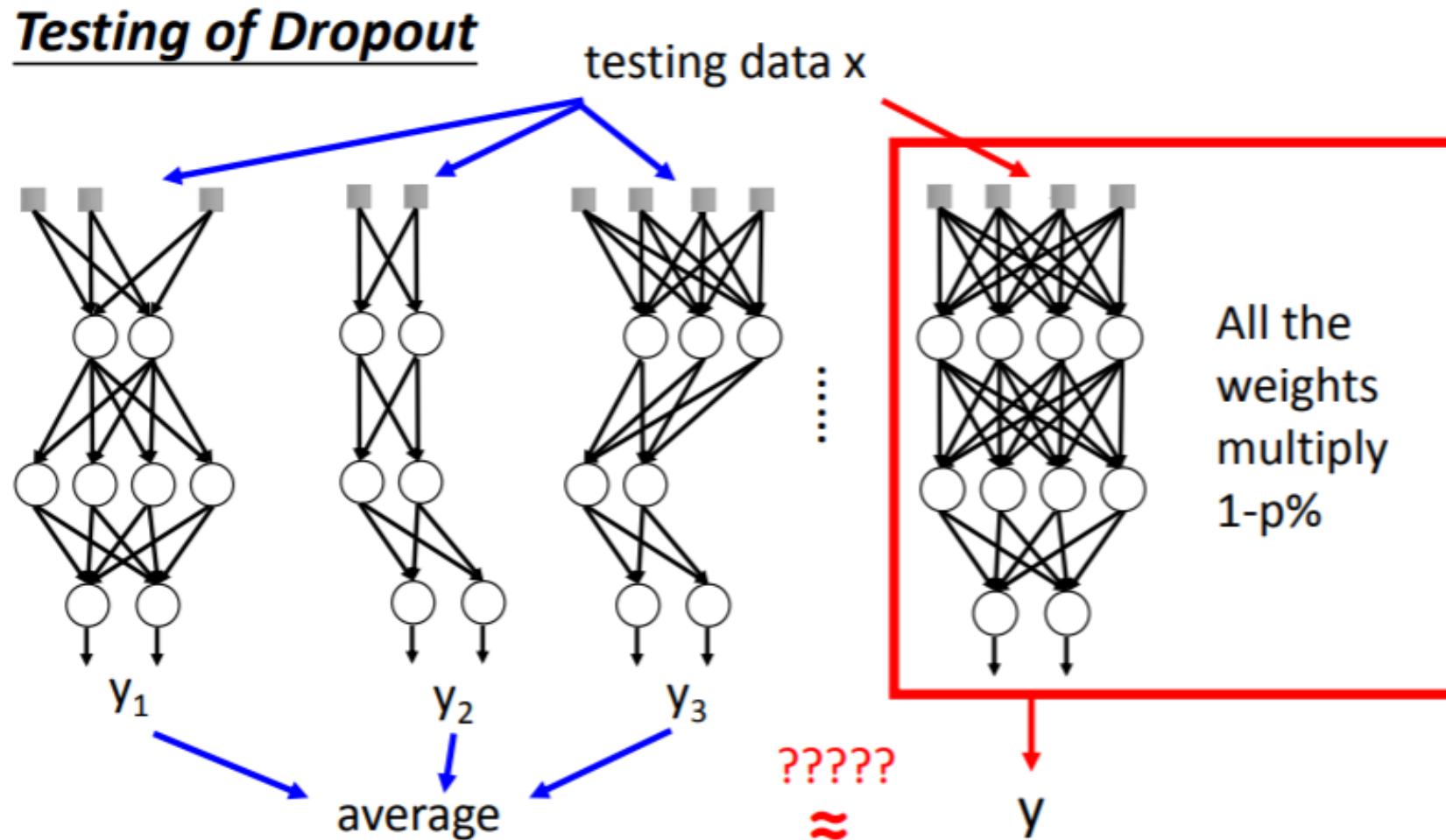


# Why drop out makes NN performs better?



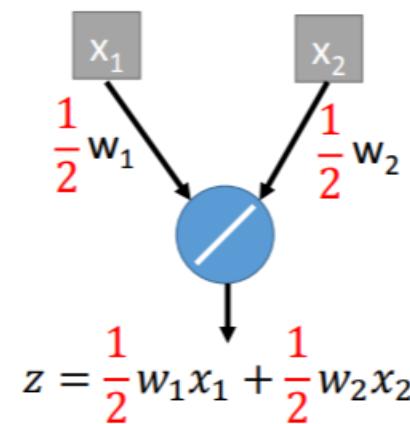
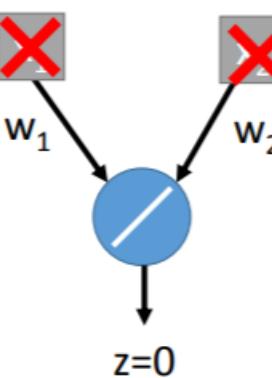
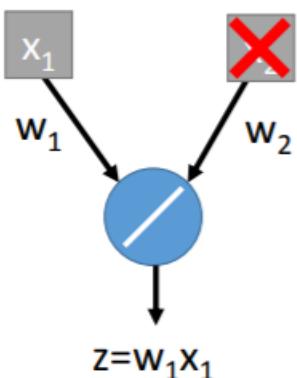
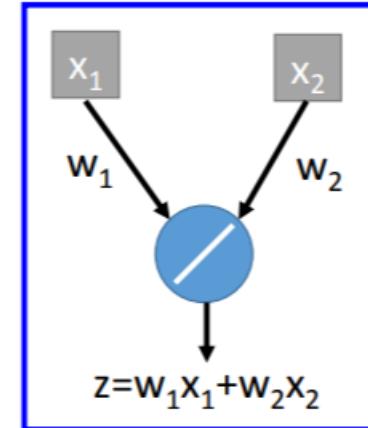
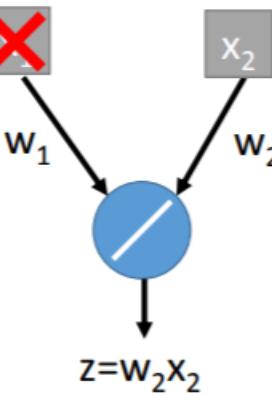
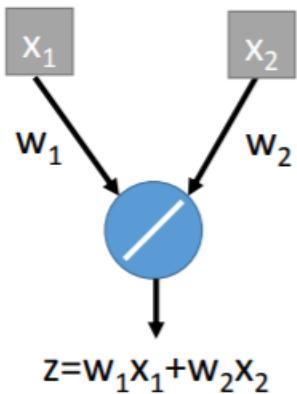
- Using one mini-batch to train one network
- Some parameters in the network are shared

# Why multiply weights by $(1-p)\%$ during testing?



# Why multiply weights by (1-p)% during testing?

## Testing of Dropout

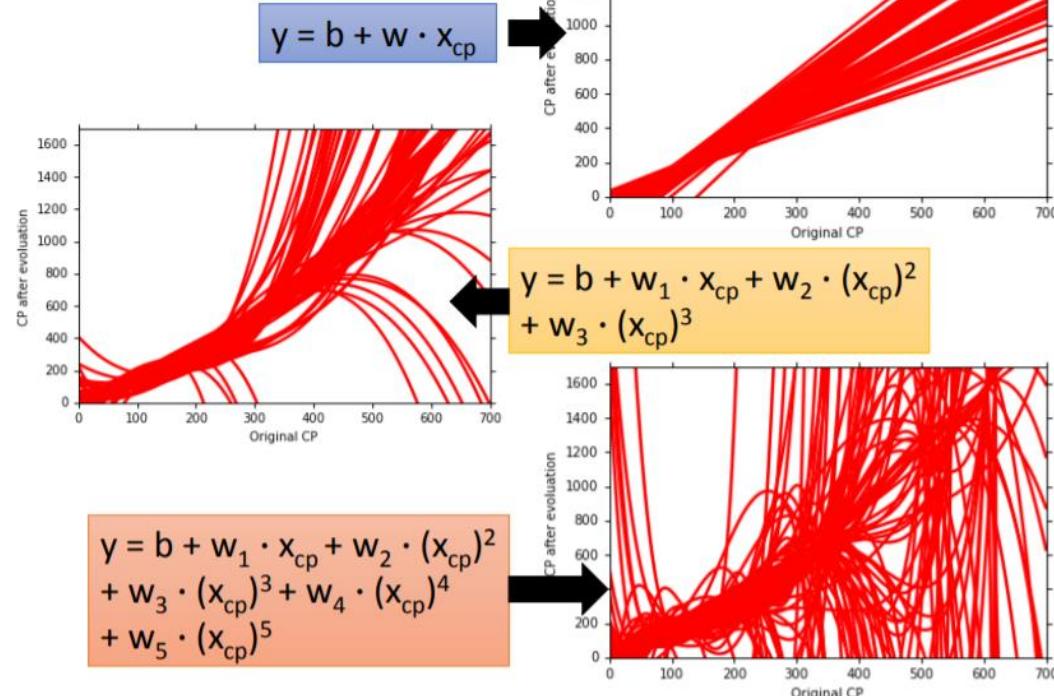


Report model's performance using bias and variance

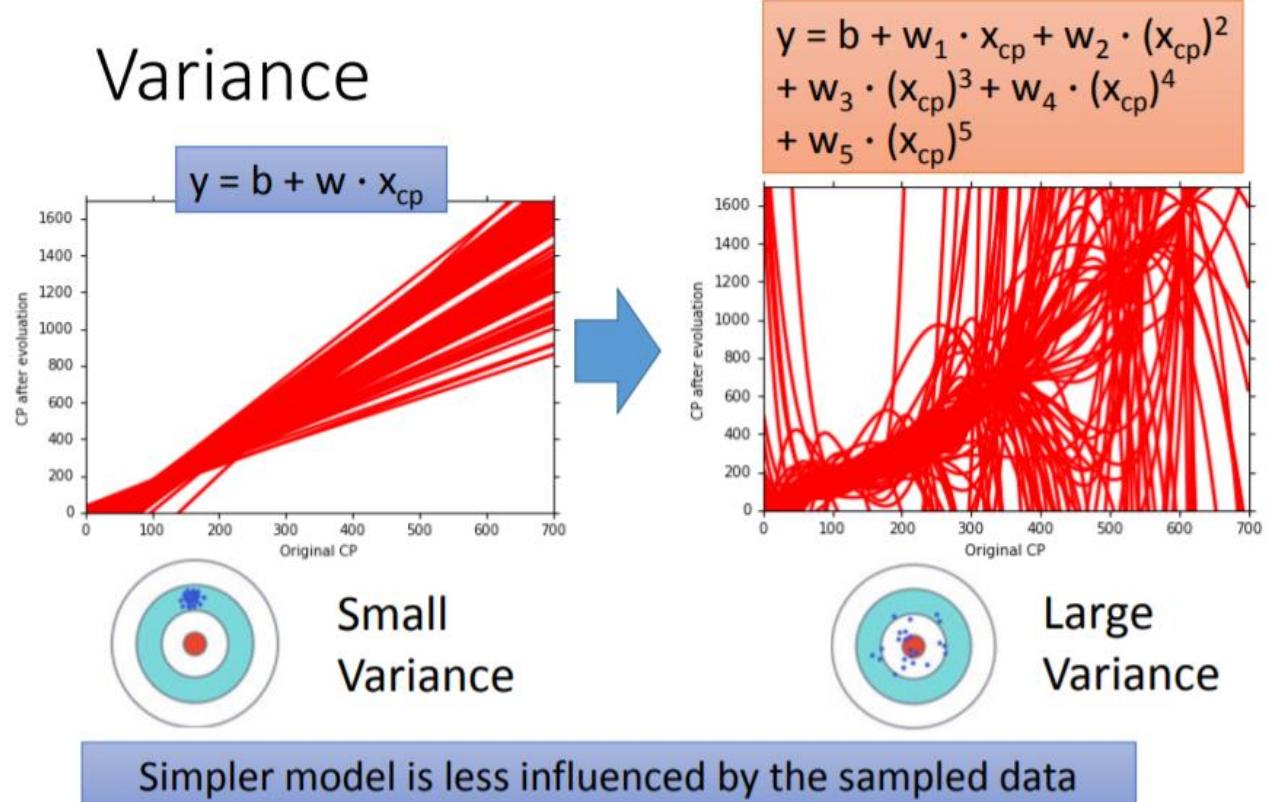
# Model's variance

Simpler model is less influenced by the sampled data and has smaller variance.

Each model is learned from 100 sampled data.



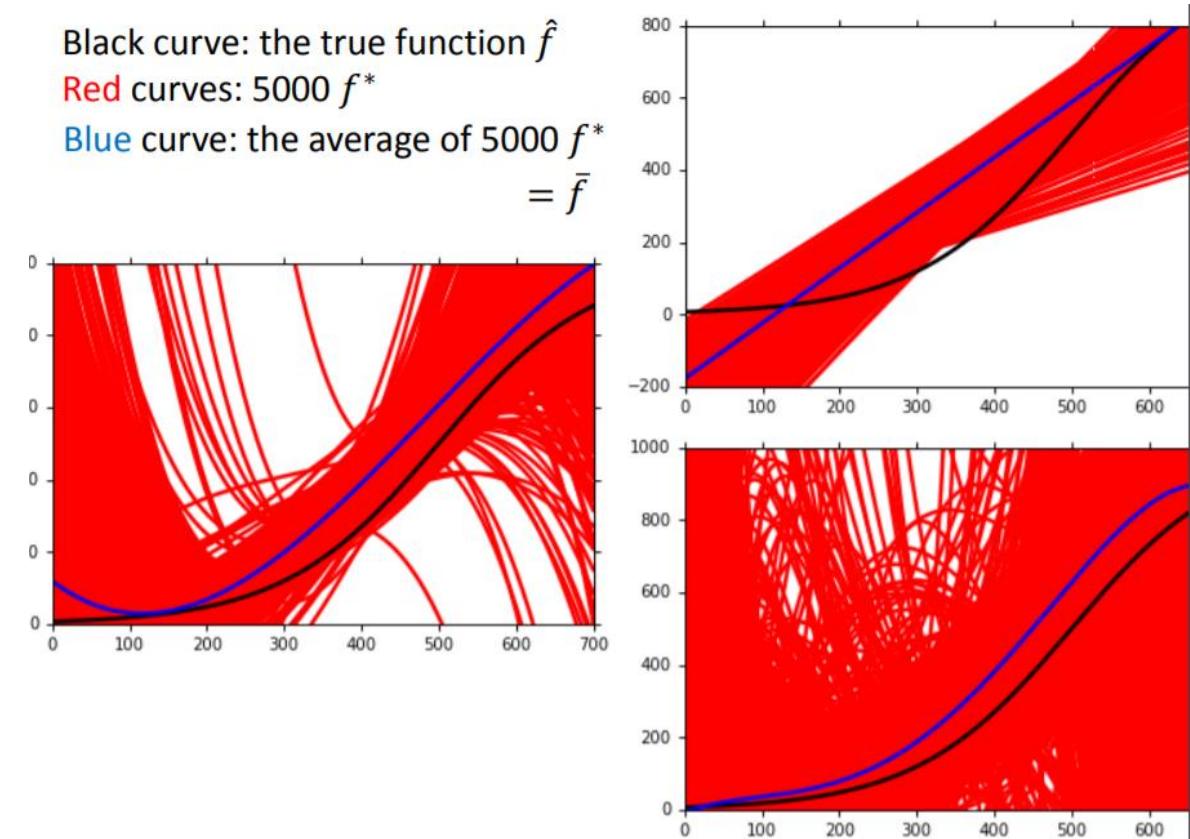
## Variance



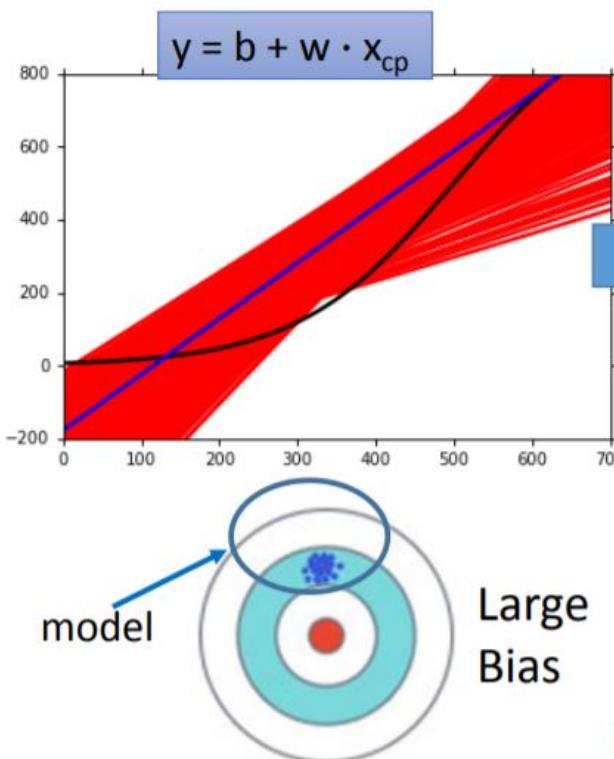
# Bias and variance of ML models

Simpler model has larger bias.

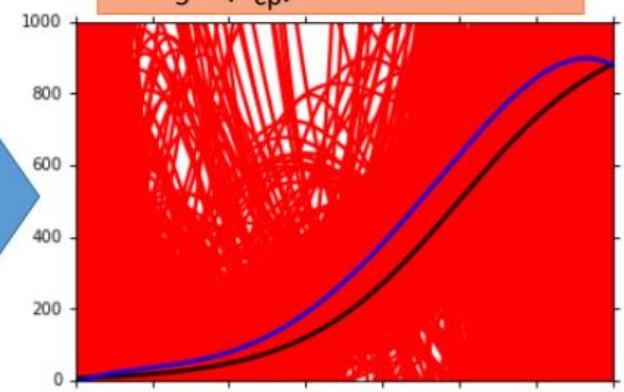
Black curve: the true function  $\hat{f}$   
Red curves: 5000  $f^*$   
Blue curve: the average of 5000  $f^*$   
 $= \bar{f}$



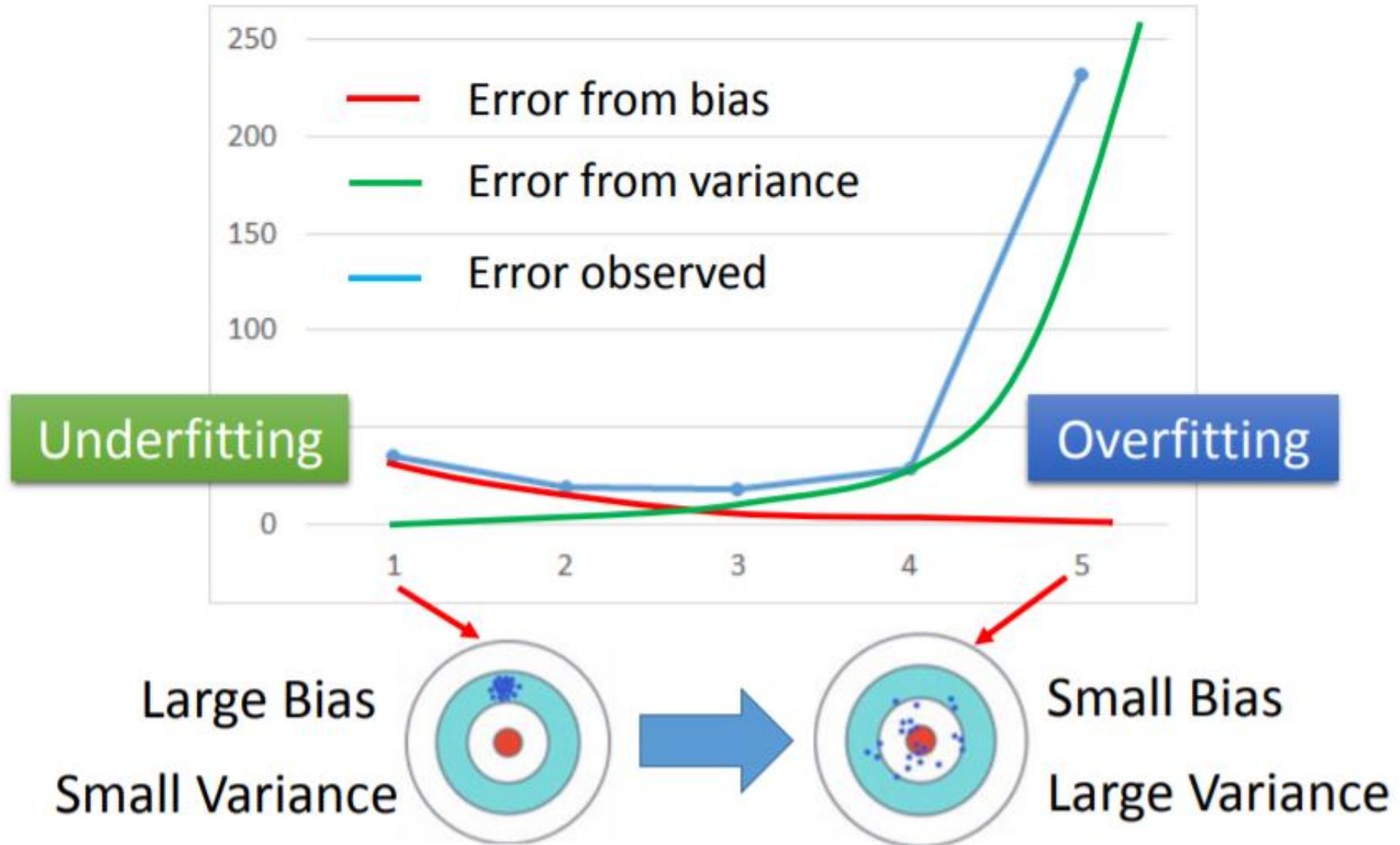
Bias



$$y = b + w_1 \cdot x_{cp} + w_2 \cdot (x_{cp})^2 + w_3 \cdot (x_{cp})^3 + w_4 \cdot (x_{cp})^4 + w_5 \cdot (x_{cp})^5$$



# Errors of ML model



# Practice – Variance of model prediction errors

- Run “1. 2.4. Variance of predicting error.ipynb” .



## HW3 (7)

- Based on HW3(2), show the box plot and discuss the bias and variance of the NN models.

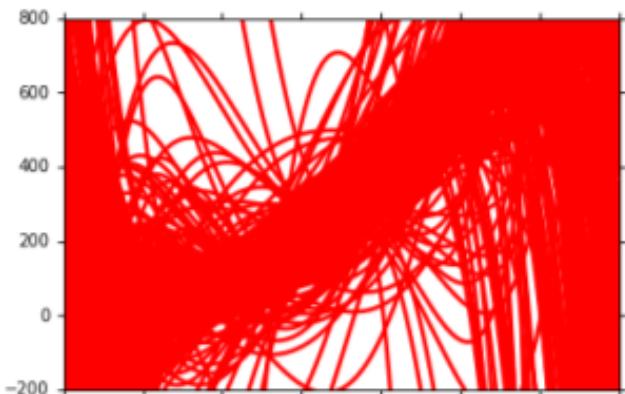
		Box plot
No of parameters =	Deep and thing	
	Shallow and fat	
	In-between version	
No of parameters =	Deep and thing	
	Shallow and fat	
	In-between version	



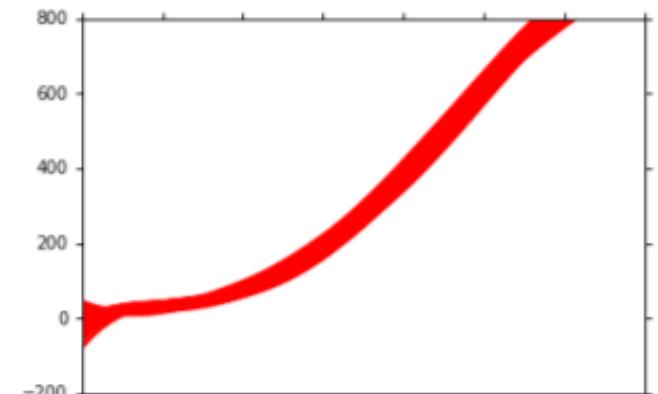
# How to reduce model's variances?

## ① More data

Very effective,  
but not always  
practical

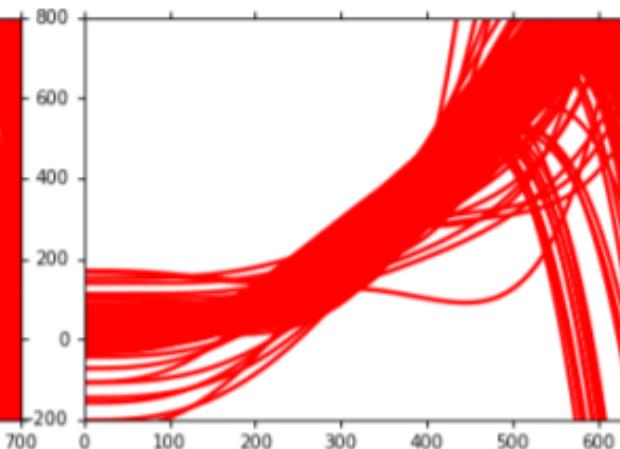
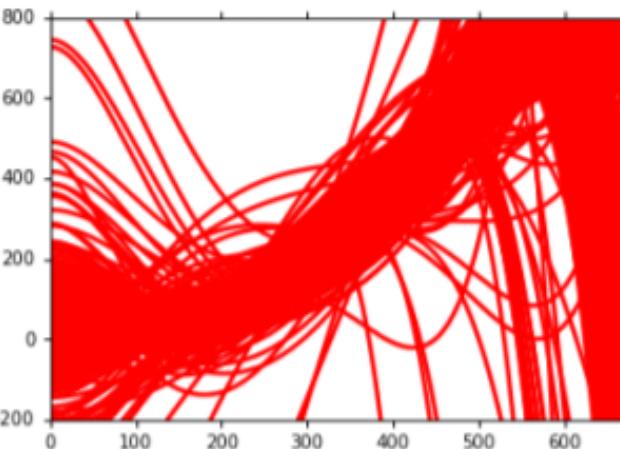
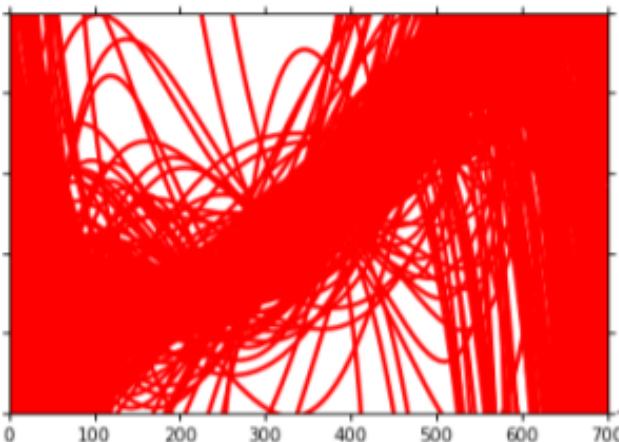


10 examples

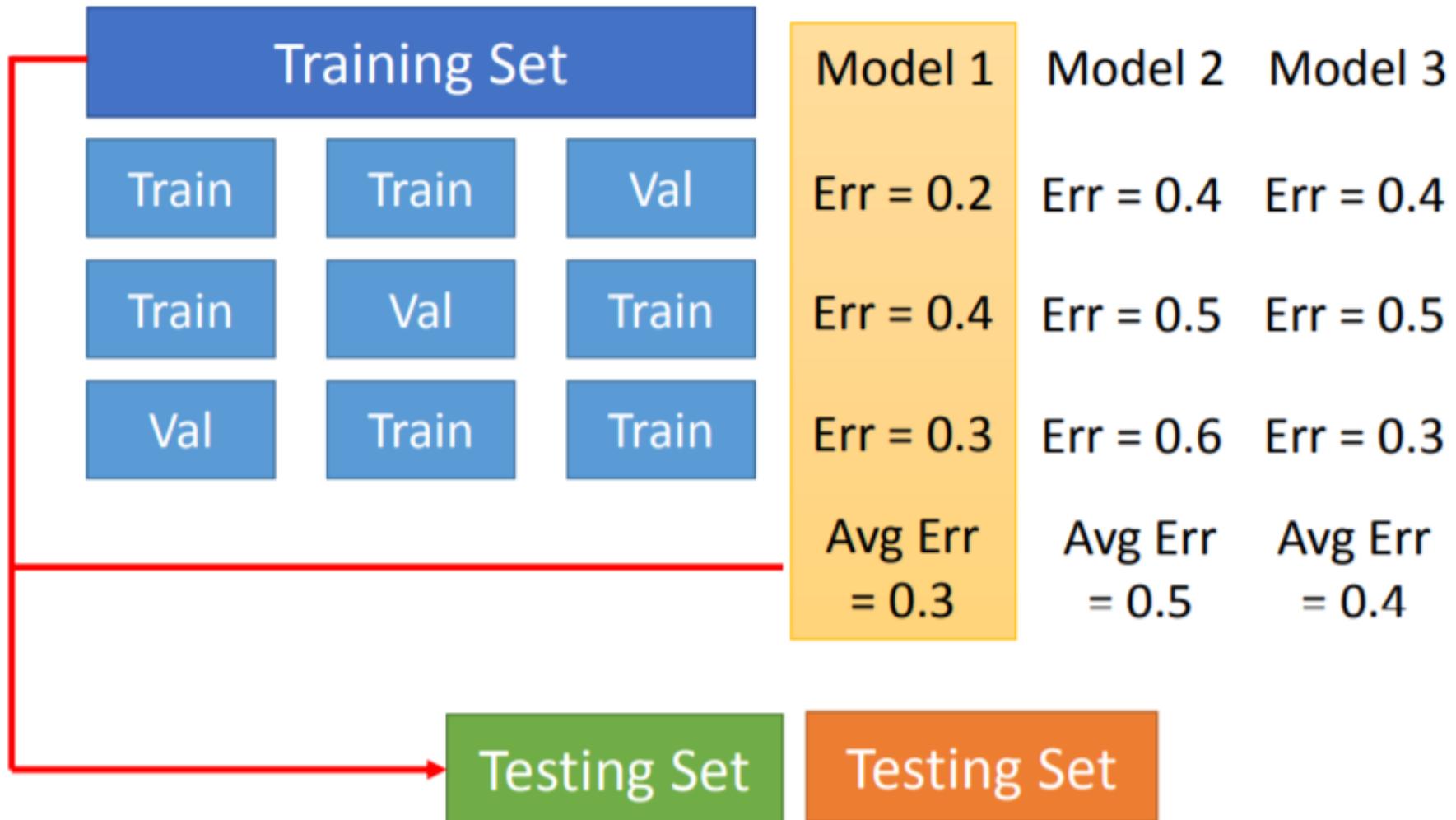


100 examples

## ② Regularization



# Training with cross validation



# Student HW Results

# Overfitting occurs when function to be learned $y=f(x)$ is random

$N=40, x=-5000 \sim 5000$  step 250,  $y=\text{randarange}(-500, 500, 5)$

No of para.		Training	Test
1000	In-between (1-30-30-1)	0.05	0.18
	Shallow and fat (1-60-15-1)	0.05	0.08
	Deep and thin (1-40-20-10-1)	0.07	0.10
11000	In-between (1-105-105-1)	0.01	0.21
	Shallow and fat (1-150-75-1)	0.05	0.06
	Deep and thin (1-100-80-40-1)	0.01	0.17
500000	In-between (?)	0.00	0.11
	Shallow and fat (?)	0.00	0.21
	Deep and thin (?)	0.00	0.22

## L2 Regularization

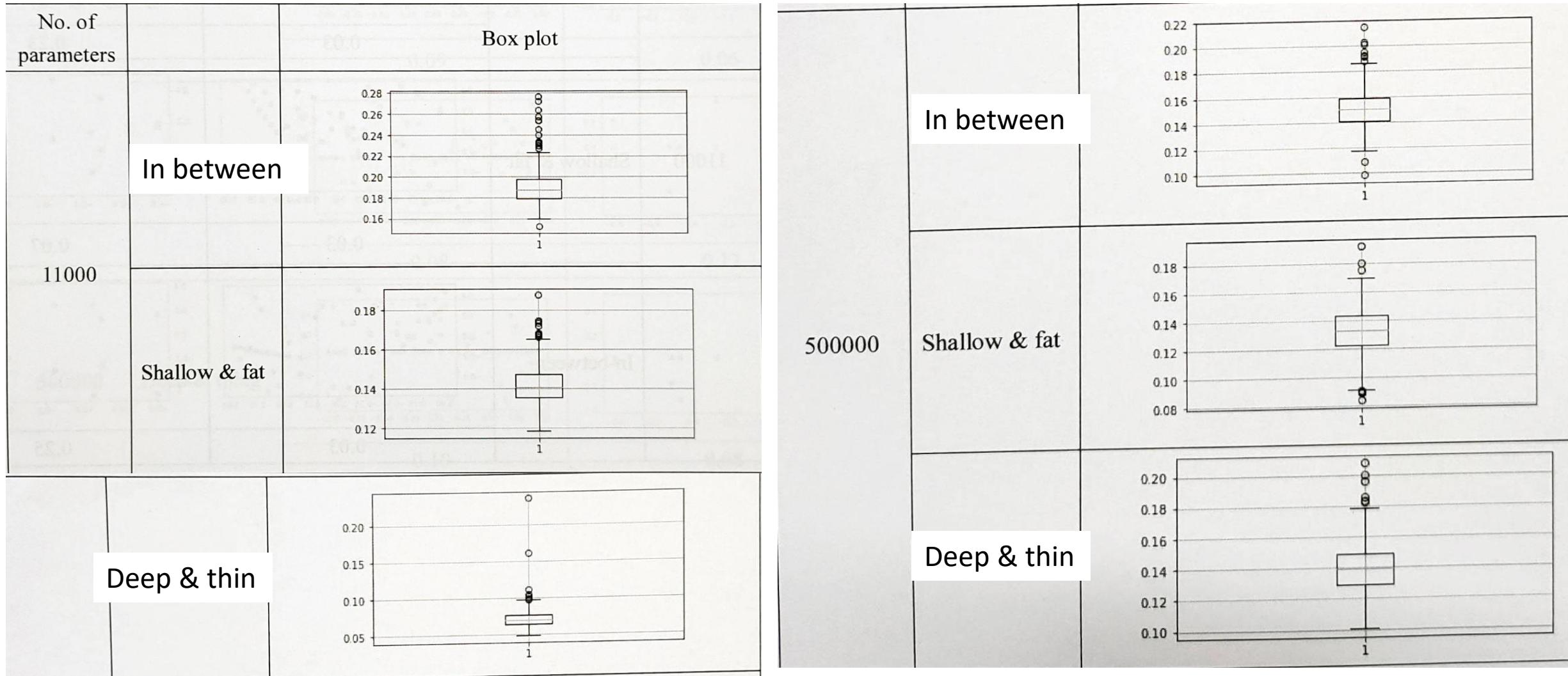
No of para.		Training	Test
11000	In-between	0.04	0.16
	Shallow and fat	0.07	0.14
	Deep and thin	0.05	0.16
500000	In-between	0.04	0.07
	Shallow and fat	0.03	0.09
	Deep and thin	0.02	0.09

## Dropout

No of para.		Training	Test
11000	In-between	0.03	0.23
	Shallow and fat	0.03	0.07
	Deep and thin	0.03	0.25
500000	In-between	0.00	0.13
	Shallow and fat	0.00	0.13
	Deep and thin	0.00	0.12

# Unstable model prediction performance due to overfitting

Predict ? times on randomly shuffled test data



# Overfitting occurs when function to be learned is dominated by the random item

$N=40, x=-100 \sim 100 \text{ step } 5, y=3x+\text{random}(0,1)*200$

1071347 劉恩  
Dropout

No of para.		Training	Test
750000	Deep and thin (1-10-15-20-30-40-45-50-55-65-50-40-30-20-10-1, 20367)	0.00147	0.0187
	Shallow and fat (1-1500-500-1, 745001)	0.00249	0.0051
	In-between (1-150-450-750-350-250-1, 757351)	0.00031	0.0102
20000	Deep and thin	0.00103	0.02017
	Shallow and fat	0.00221	0.01417
	In-between	0.00163	0.01661

L1, lamda=0.00001

L1, lamda=10

L2

No of para.		Training	Test
750000	Deep and thin	0.00231	0.00412
	Shallow and fat	0.00193	0.12884
	In-between	0.00078	0.00823
20000	Deep and thin	0.00284	0.00506
	Shallow and fat	0.00466	0.00455
	In-between		

No of para.		Training	Test
750000	Deep and thin	0.0045	0.02372
	Shallow and fat	0.0049	0.00845
	In-between	0.0043	0.00569
20000	Deep and thin	0.0825	0.02105
	Shallow and fat	0.0048	0.00987
	In-between	0.4846	0.07374

No of para.		Training	Test
750000	Deep and thin	0.07109	0.03726
	Shallow and fat	0.07854	0.04556
	In-between	0.08414	0.05698
20000	Deep and thin	0.08611	0.06453
	Shallow and fat	0.08656	0.04857
	In-between	0.00544	0.00542

No of para.		Training	Test
750000	Deep and thin	0.00240	0.01382
	Shallow and fat	0.00376	0.00461
	In-between	0.00318	0.01142
20000	Deep and thin	0.00454	0.01220
	Shallow and fat	0.00309	0.00608
	In-between	0.00259	0.00821

# Overfitting occurs when the function to be learned is regular but the NN design is exaggerated

N=40, x=-5000~5000 step 200

$$y = 3x^3 + 2x^2 + 5x - \text{random.uniform}(0,1)*500$$

x, y normalized to [0, 1]

No of para.		Training (10-3)	Test (10-3)
20000	Deep and thin (1-80-65-65-65-65-80-1, 23656)	0.083	2.89
	Shallow and fat (1-200-150-1, 30701)	0.032	2.20
	In-between (1-100-100-10-1, 21421)	0.004	1.80
3000	Deep and thin (1-30-20-20-20-20-30-1, 2601)	0.333	2.221
	Shallow and fat (1-65-50-1, 3418)	0.267	1.010
	In-between (1-30-40-30-40-1, 3811)	0.019	2.77

## L2 Regularization

No of para.		Training (10-3)	Test (10-3)
20000	Deep and thin	0.795	4.047
	Shallow and fat	1.077	1.914
	In-between	1.788	1.748
3000	Deep and thin	1.377	1.271
	Shallow and fat	1.338	2.113
	In-between	0.733	2.326

## Dropout

No of para.		Training (10-3)	Test (10-3)
20000	Deep and thin	1.691	1.805
	Shallow and fat	2.74	3.382
	In-between	4.28	3.965
3000	Deep and thin	1.899	2.484
	Shallow and fat	14.412	11.139
	In-between	2.749	3.780

The function to be learned  $y=f(x)$  is regular and NN design is normal

### L2 Regularization

Why overfitting still occurs in this case? Is the result correct?

$N=40$ ,  $x=-5000 \sim 5000$  step 250,  $y=$  cubic function of  $x$

No of para.		Training	Test
7500	Deep and thin (1-150-50-1, 7501)	0.05	1637
	Shallow and fat (1-2500-1, 7501)	0.05	733
	In-between(1-90-60-30-1, 7901)	0.0001	1087
250000	In-between (1-770-365-1, 251501)	0.00	979
	Shallow and fat ( 1-87000-1, 261001)	0.01	739
	In-between (1-250-500-250-1, 283321)	0.00	1302

No of para.		Trainin g	Test
7500	Deep and thin	664.26	1010.68
	Shallow and fat	603.38	1043.32
	In-between	821.11	902.72
250000	Deep and thin	779.09	1817.40
	Shallow and fat	656.99	1218.57
	In-between	681.43	652.29

### Dropout

No of para.		Training	Test
7500	Deep and thin	2097.54	2021.28
	Shallow and fat	795.88	1461.11
	In-between	945.70	1847.20
250000	Deep and thin	913.75	1118.50
	Shallow and fat	3155.72	1467.53
	In-between	911.19	402.58

# Unstable model prediction performance when $N\bar{N}$ is large because of overfitting

1071340 吳沛鋒

