

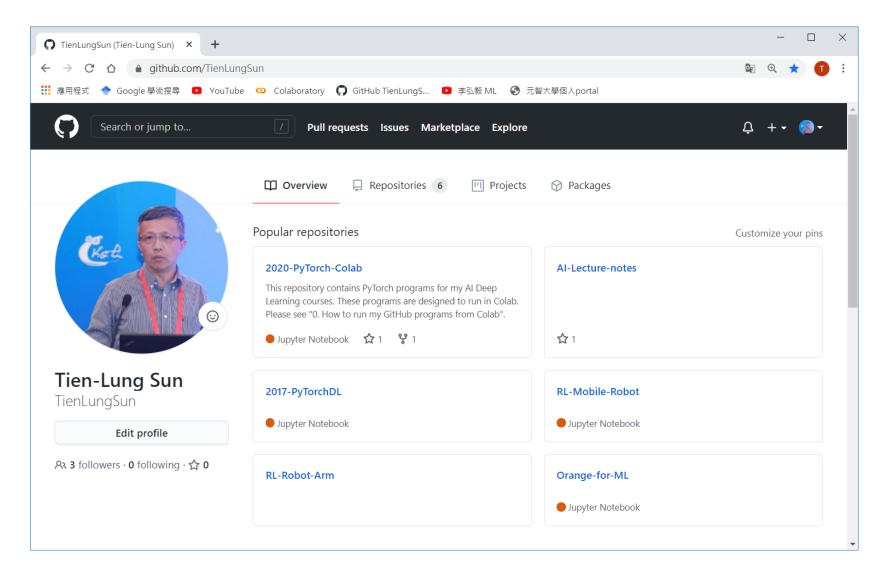
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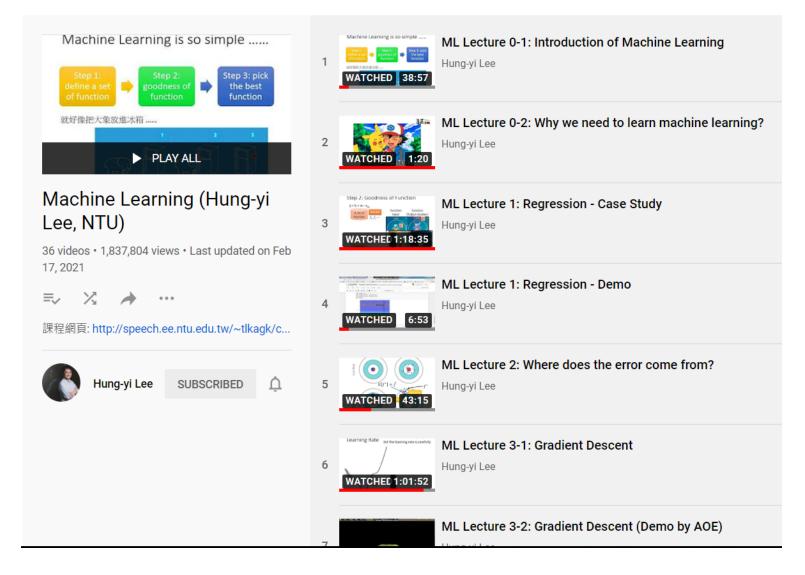
Deep Learning – Concepts and PyTorch Development

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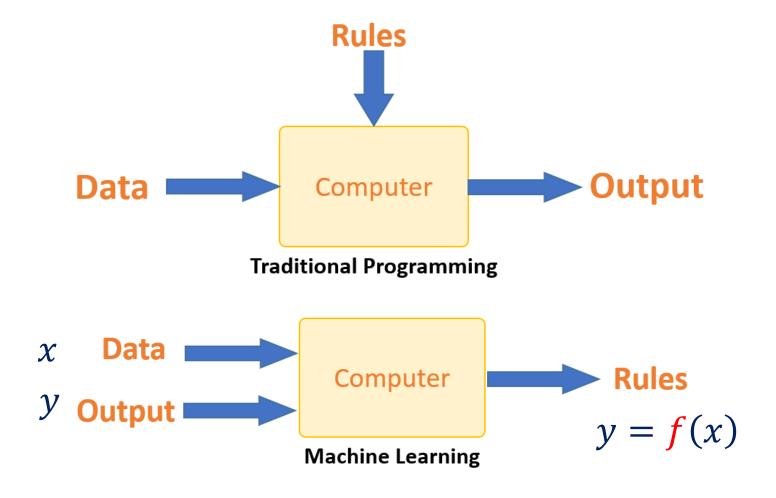
My GitHub



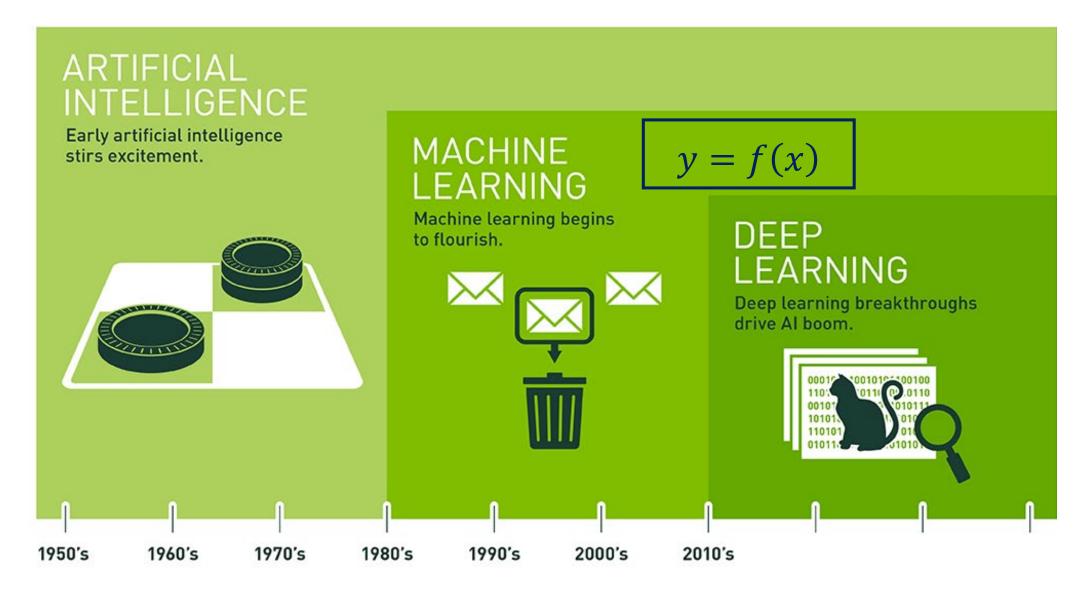
Acknowledgement



ML vs programming approach to let computer have intelligence



AI, ML and DL



Machine learning mechanism

- 1. Define a function to be learned: y = f(x)
- 2. Define a loss function \mathcal{L} to describe the error between y = f(x) and \hat{y}
- 3. Find the optimal parameters of f that minimize \mathcal{L}

Deep Learning - Machine learns a connected network



Geoffrey Hinton spent 30 years hammering away at an idea most other scientists dismissed as nonsense. Then, one day in 2012, he was proven right. Canada's most influential thinker in the field of artificial intelligence is far too classy to say I told you so

https://torontolife.com/tech/ai-superstars-google-facebook-apple-studied-guy/

For more than 30 years , Geoffrey Hinton hovered at the edges of artificial intelligence research , an outsider clinging to a simple proposition: that computers could think like humans do—using intuition rather than rules.

Geoffrey Hinton 多年來堅持着一個簡單的觀點:電腦可以像人類一樣思考-用直覺而不是規則。 Hinton 一直好奇的是,電腦能不能像人類大腦一樣的工作:信息通過一個巨大的,由神經元圖譜連接 起來的細胞網絡傳播,在多達十億條的路徑上發射、連接和傳輸。

Notations

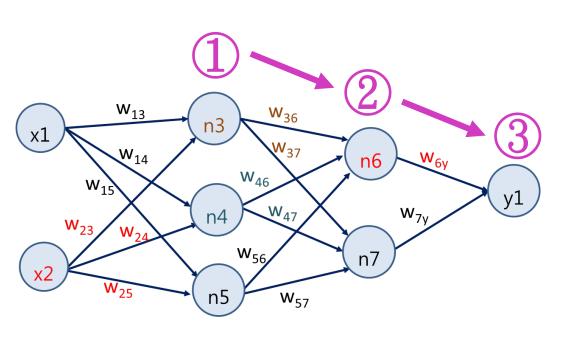
 x_i

No	age t	t1	t2	t3	t4	t5	t6	time	Step frequency 1	n1	n2	n3	n4	n5	пб	рх	ру	pz	Steps Ge	ender T	TUG y	1 E	ВВЅ у	2
1	70	1.76	2.64	6.24	7.02	10	12.8	11	2.285	80	120	282	317	453	575	11.67	1.809	-1.99	13 F		11	0	26	0
2	86	1.64	2.6	5.82	7.27	10.4	12.6	11	1.934	75	118	263	328	470	570	11.14	2.302	-4.651	12 F		11	0	24	0
3	76	1.76	2.93	6.27	7.04	10.3	12.8	11	2.109	80	133	283	318	465	575	11.53	2.169	-3.253	14 F		11	0	22	1
4	70	2.38	3.29	5.58	6.47	9.02	10.4	8	2.461	108	149	252	292	407	468	11.6	1.838	-3.138	12 F		8	0	24	0
5	66	3.09	4.07	6.6	7.4	10.2	12.1	9	2.461	140	184	298	334	462	545	11.55	2.531	-2.742	12 F		9	0	26	0
6	79	1.76	2.91	5.87	6.6	10.2	12.8	11	2.109	80	132	265	298		575		1.788	-1.349	13 F		11	0	26	0
7	85	1.2	2.33	5.42	8.31	12.1	17.2	16	2.988	55	106	245	375	545	775	λi	2.203	-4.89	17 M		16	1	18	1
8	81	1.64	2.93	5.98	7.47	10.9	13.6	12	1.758	75	133	270	337	493	£15	11.1	2.667	-4.594	10 F		12	0	24	0
9	82	0.64	1.47	4.76	5.76	9.36	11.6	11	2.109	30	67	215	260	422	525	11.26	4.1	-2.693	14 M		11	0	24	0
10	69	1.64	2.49	5.02	5.98	9.82	12.6	11	2.637	75	113	227	270	443	570	11.27	3.292	-3.522	13 F		11	0	20	1
11	84	0.64	1.4	5.67	7.29	11.5	14.6	14	1.934	30	64	256	329	520	660	11.53	2.335	-2.999	15 M		14	1	26	0
12	69	1.09	1.98	5	5.62	8.38	10.1	9	2.109	50	90	226	254	378	455	11.15	1.919	-4.608	11 M		9	0	26	0
13	73	1.09	2.13	6.78	8.38	12.4	17.1	16	3.691	50	97	306	378	558	770	11.46	2.264	-3.333	16 F		16	1	14	1
14	81	0.64	1.87	9.24	11.2	19	22.6	22	1.934	30	85	417	507	857	1020	11.58	2.511	-2.157	27 M		22	1	24	0
15	80	0.76	1.71	3.98	5	7.58	9.76	9	2.109	35	78	180	226	342	440	11.33	2.821	-3.595	10 M		9	0	26	0
16	88	0.98	2.13	6.31	7.44	11.5	14	13	1.934	45	97	285	336	518	630	11.38	2.498	-3.702	16 M		14	1	26	0
17	81	1.09	2.09	4.18	5.16	7.76	10.1	9	2.285	50	95	189	233	350	455	11.21	2.241	-4.337	10 M		9	0	28	0
18	76	1.76	2.64	5.87	6.98	9.98	12.8	11	1.406	80	120	265	315	450	575	11.33	2.679	-3.736	10 M		11	0	26	0
19	69	0.36	3.76	13.3	16.7	24.2	29.4	29	3.691	17	170	598	753	1090	1322	11.31	1.361	-4.171	28 F		29	1	10	1
20	75	1.98	2.93	5.98	7.91	12.2	15	13	1.934	90	133	270	357	551	675	11.5	2.202	-1.495	14 M		13	0	28	0
21	87	1.53	3.2	10.9	13.8	21.3	26.5	25	2.9	70	145	492	624	960	1195	11.6	2.199	-2.54	19 F		25	1	16	1
22	72	0.2	1.02	3.36	4.11	7.42	10.2	10	1.758	10	47	152	186	335	460	11.52	2.658	-2.081	9 M		10	0	28	0
23	109	0.64	1.93	5.04	5.71	9.13	10.6	10	2.285	30	88	228	258	412	480	11.51	2.056	-3.158	15 F		10	0	28	0

 x^n

Multiple-layer perception (MLP)

1. Define a function to be learned: $y^n = f(x^n)$



$$n_3 = \sigma(x_1 * w_{13} + x_2 * w_{23} + b_3)$$

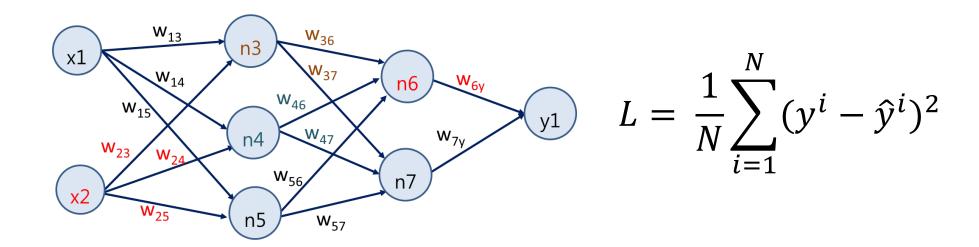
$$1 n_4 = \sigma(x_1 * w_{14} + x_2 * w_{24} + b_4)$$

$$n_5 = \sigma(x_1 * w_{15} + x_2 * w_{25} + b_5)$$

3
$$y_1 = \sigma (n_6 * w_{6y} + n_7 * w_{7y} + b_y)$$

Calculate error

2. Define a loss function $\mathcal{L}(f)$ to describe the error between y^i and \hat{y}^i

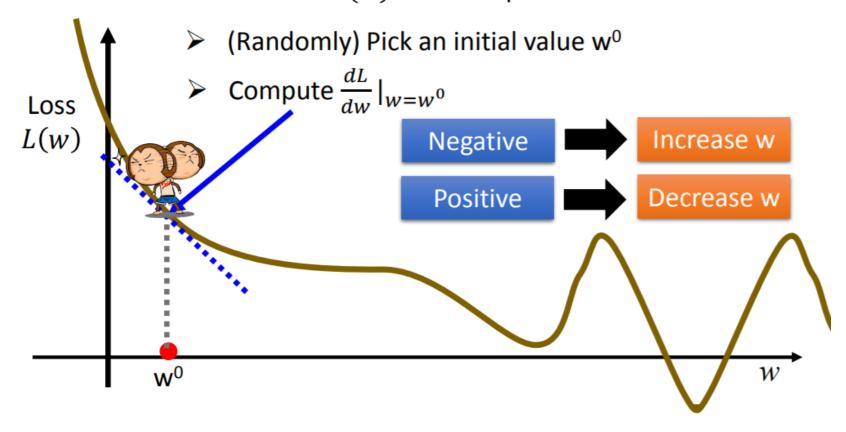


Use gradient decent to find optimal parameters

3. Find the optimal parameters that minimize $\mathcal{L}(f)$

$$w^* = \arg\min_{w} L(w)$$

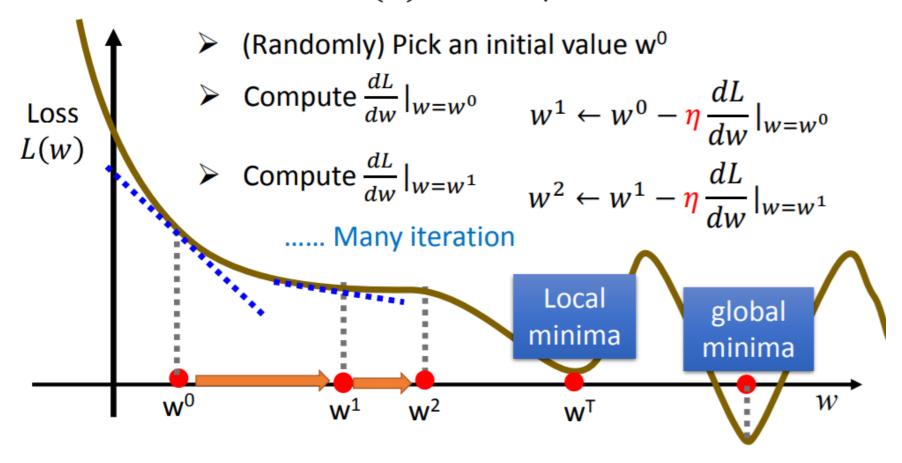
• Consider loss function L(w) with one parameter w:



Use gradient decent to find optimal parameters

$$w^* = \arg\min_{w} L(w)$$

• Consider loss function L(w) with one parameter w:



Gradient decent to find two parameters w^* and b^*

- How about two parameters? $w^*, b^* = arg \min_{w,b} L(w,b)$
 - (Randomly) Pick an initial value w⁰, b⁰
 - ightharpoonup Compute $\frac{\partial L}{\partial w}|_{w=w^0,b=b^0}$, $\frac{\partial L}{\partial b}|_{w=w^0,b=b^0}$

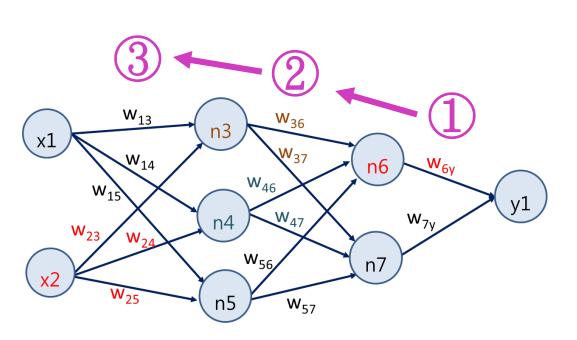
$$w^{1} \leftarrow w^{0} - \frac{\partial L}{\partial w}|_{w=w^{0},b=b^{0}} \qquad b^{1} \leftarrow b^{0} - \frac{\partial L}{\partial b}|_{w=w^{0},b=b^{0}}$$

$$ightharpoonup$$
 Compute $\frac{\partial L}{\partial w}|_{w=w^1,b=b^1}$, $\frac{\partial L}{\partial b}|_{w=w^1,b=b^1}$

$$w^2 \leftarrow w^1 - \eta \frac{\partial L}{\partial w}|_{w=w^1,b=b^1} \qquad b^2 \leftarrow b^1 - \eta \frac{\partial L}{\partial b}|_{w=w^1,b=b^1}$$

Use gradient decent to find optimal NN weights

3. Find the optimal parameters that minimize $\mathcal{L}(f)$



$$L = g(y - \hat{y})$$
 $y = \sigma(n_6 * w_{6y} + n_7 * w_{7y} + b_y)$

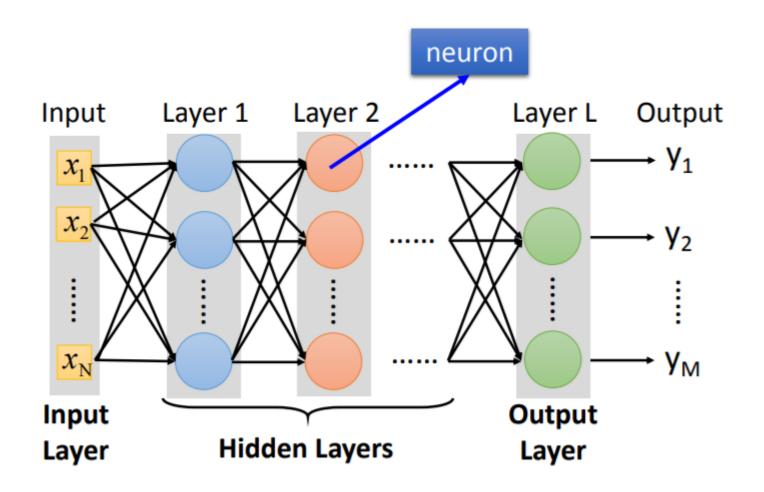
$$\mathbf{w}_{6y} \leftarrow \mathbf{w}_{6y} - \eta \frac{\partial L}{\partial \mathbf{w}_{6y}} \qquad \frac{\partial L}{\partial \mathbf{w}_{6y}} = \frac{\partial L}{\partial y} \frac{\partial y}{\partial \mathbf{w}_{6y}}$$

$$w_{7y} \leftarrow w_{7y} - \eta \frac{\partial L}{\partial w_{7y}} \frac{\partial L}{\partial w_{7y}} = \frac{\partial L}{\partial y} \frac{\partial y}{\partial w_{7y}}$$

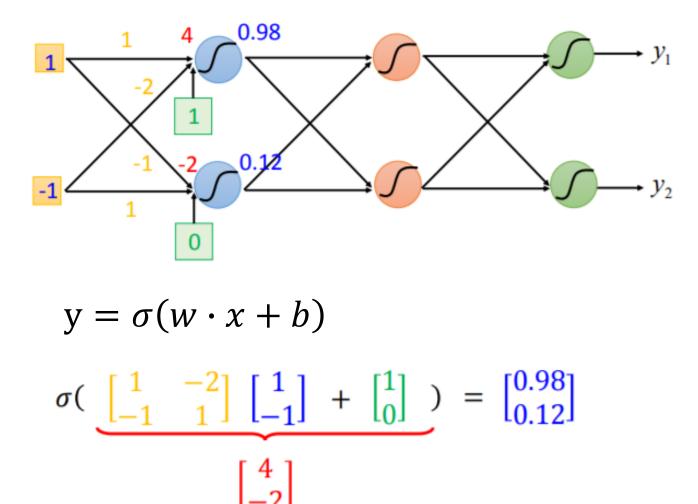
$$\mathbf{w_i} \leftarrow \mathbf{w_i} - \eta \frac{\partial e}{\partial \mathbf{w_i}}$$

2
$$w_{57} \leftarrow w_{57} - \eta \frac{\partial L}{\partial w_{57}}$$
 $\frac{\partial L}{\partial w_{57}} = \frac{\partial L}{\partial y} \frac{\partial y}{\partial n_7} \frac{\partial n_7}{\partial w_{57}}$
 $n_7 = f(n_3 * w_{37} + n_4 * w_{47} + n_5 * w_{57} + b_7)$

MLP is a fully connected feedforward network



Fully connected feed forward network is implemented as matrix operation



Reference: 李弘毅 ML Lecture 6 https://youtu.be/Dr-WRIEFefw

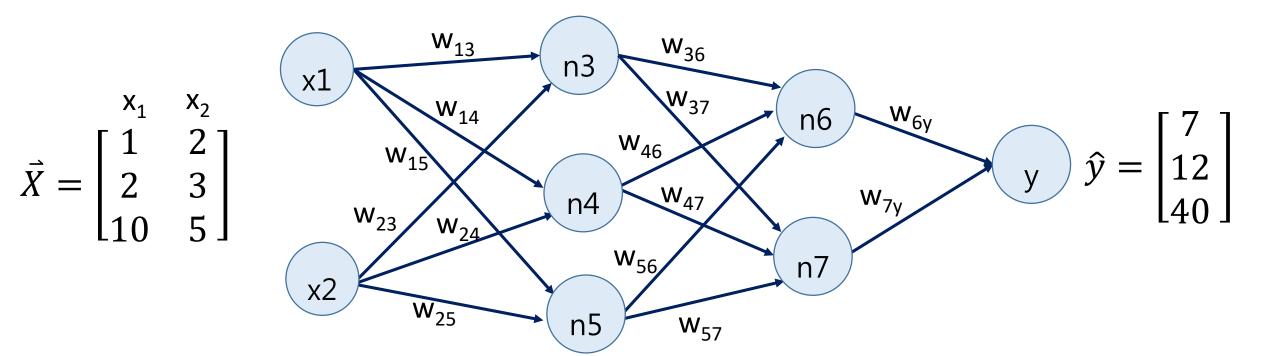
Practice

Run "1.1 Matrix operation.ipynb"



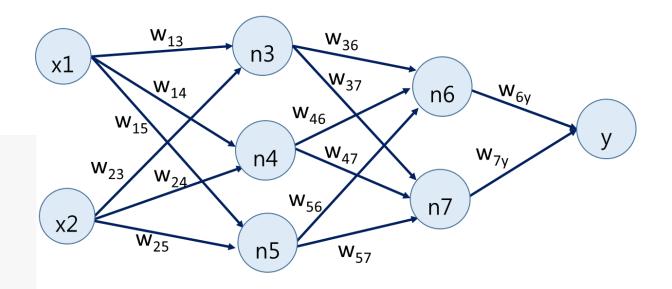
Matrix operation

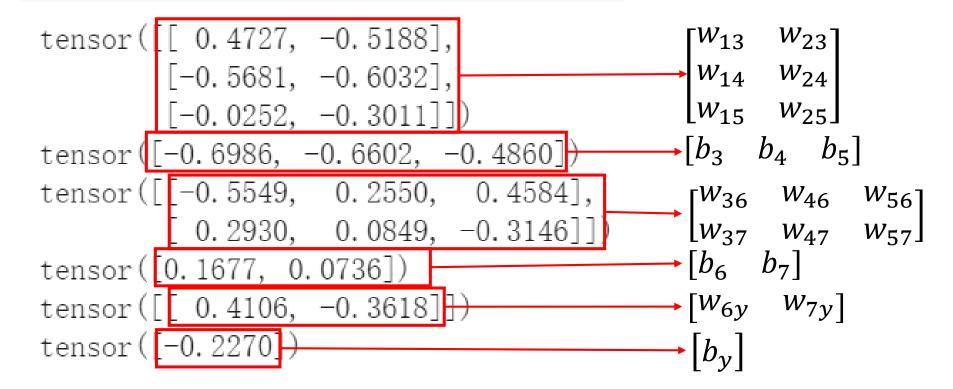
```
MyNet = nn. Sequential(
    nn. Linear(2, 3),
    nn. Linear(3, 2),
    nn. Linear(2, 1)
)
```



Matrix operation

```
for param in MyNet.parameters():
    if param.requires_grad:
        print(param.data)
```





$$\vec{X} = \begin{bmatrix} x_1 & x_2 \\ 1 & 2 \\ 2 & 3 \\ 10 & 5 \end{bmatrix} \qquad \begin{array}{c} w_{13} \\ w_{14} \\ w_{23} \\ w_{24} \end{array}$$

$$\begin{bmatrix} 1 & 2 \\ 2 & 3 \\ 10 & 5 \end{bmatrix} \begin{bmatrix} w_{13} & w_{14} & w_{15} \\ w_{23} & w_{24} & w_{25} \end{bmatrix} + [b_3 \quad b_4 \quad b_5]$$

$$\begin{bmatrix} k_3^1 & k_4^1 & k_5^1 \\ k_3^2 & k_4^2 & k_5^2 \\ k_3^3 & k_4^3 & k_5^3 \end{bmatrix} + \begin{bmatrix} b_3 & b_4 & b_5 \\ b_3 & b_4 & b_5 \\ b_3 & b_4 & b_5 \end{bmatrix}$$

$$\begin{bmatrix} n_3^1 & n_4^1 & n_5^1 \\ n_3^2 & n_4^2 & n_5^2 \\ n_3^3 & n_4^3 & n_5^3 \end{bmatrix}$$

Use Excel to verify

n3

n4

n5

```
#Calculate n3, n4, n5
HiddenLayer1 = MyNet[0](tensorX)
print(HiddenLayer1)
```

```
tensor([[-1.2635, -2.4348, -1.1135], [-1.3097, -3.6061, -1.4398], [ 1.4340, -9.3577, -2.2441]],
```

```
#Calculate n3, n4, n5 using Pytorch matrix operation

HiddenLayer1 = tensorX.mm(torch.transpose(W1, 1, 0)) + b1

print(HiddenLayer1)
```

```
tensor ([[-1.2635, -2.4348, -1.1135],

[-1.3097, -3.6061, -1.4398],

[ 1.4340, -9.3577, -2.2441]], grad_fn=<AddBackward0>)
```

```
#Calculate n6, n7 using PyTorch matrix operation
W2 = MyNet[1].weight
b2 = MyNet[1].bias
HiddenLayer2 = HiddenLayer1. mm(torch. transpose(W2, 1, 0)) +b2
print(HiddenLayer2)
tensor([[-0.2625, -0.1530],
        [-0.6852, -0.1632],
        [-4.0429, 0.4054]], grad_fn=<AddBackward0>)
                                        W_{36}
                               n3
                                        W<sub>37</sub>
                                                    n6
                                    W_{46}
```

n4

n5

W₄₇

W₅₇

W₅₆

$$\begin{bmatrix} n_3^1 & n_4^1 & n_5^1 \\ n_3^2 & n_4^2 & n_5^2 \\ n_3^3 & n_4^3 & n_5^3 \end{bmatrix}$$

$$\begin{bmatrix} -1.2635 & -2.4348 & -1.1135 \\ -1.3097 & -3.6061 & -1.4398 \\ 1.4340 & -9.3577 & -2.2441 \end{bmatrix} \begin{bmatrix} w_{36} & w_{37} \\ w_{46} & w_{47} \\ w_{56} & w_{57} \end{bmatrix} + \begin{bmatrix} b_6 & b_7 \end{bmatrix}$$

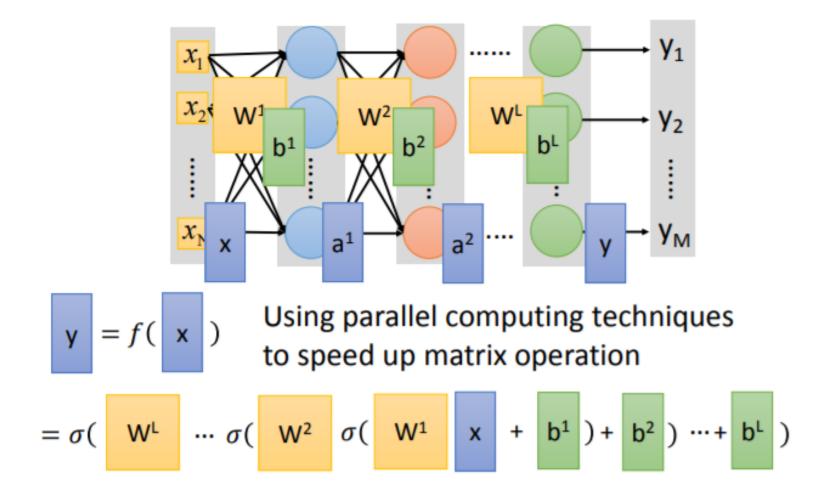
$$\begin{bmatrix} k_6^1 & k_7^1 \\ k_6^2 & k_7^2 \\ k_6^3 & k_7^3 \end{bmatrix}$$

$$+ \begin{bmatrix} b_6 & b_7 \\ b_6 & b_7 \\ b_6 & b_7 \end{bmatrix}$$

$$\begin{bmatrix} n_6^1 & n_7^1 \\ n_6^2 & n_7^2 \\ n_6^3 & n_7^3 \end{bmatrix} \quad \begin{array}{c} \text{Use Excel to} \\ \text{verify} \end{array}$$

n7

Use parallel computing to speed up matrix operation



Use parallel computing to speed up matrix operation

```
In [2]: if(torch.cuda.is_available()):
    device = torch.device("cuda")
    print(device, torch.cuda.get_device_name(0))
else:
    device= torch.device("cpu")
    print(device)
```

```
tensorX = torch.FloatTensor(trainX).to(device)
tensorY_hat = torch.FloatTensor(trainY_hat).to(device)
print(tensorX.shape, tensorY_hat.shape)
```

```
torch.Size([128, 2]) torch.Size([128, 1])
```

```
conv1_out = conv1(imageTensor.to(device))
conv1_out.shape
#output image (feature map) has 64 channels
torch.Size([1, 64, 55, 55])
```

Learning strategies

	Supervised Learning	Self-supervised Learning	Reinforcement Learning				
1. Function to be	MLP, CNN families	AE/VAE, GAN	Actor				
learned	y = f(x)	$\hat{x} = f(x)$	a = f(s)				
2. Loss function $\mathcal{L}(f)$	MSE, CE	MSE, CE, KLD, JSD	MSE, KLD				
3. Minimize $\mathcal{L}(f)$	Gradient decent, Maximum Likelihood						

Challenges in learning a=f(s)

- Define a function to be learned: a = f(s)
- Define a loss function $\mathcal{L}(f)$ to describe the error between y^n and

Time-delayed answer – If at time t we perform action a_t under state s_t , we only know the immediate reward r_t and there is a time delay to know the total accumulated reward \hat{y} .

Adversial interaction – After preforming a_t at state s_t , there are infinite number of possibilities for following state- actions s_{t+1} , a_{t+1} , s_{t+2} , a_{t+2} , \cdots s_{t+T} , a_{t+T} . It is difficult to estimate the true answer y (the true final reward).

• Find the optimal parameters that minimize $\mathcal{L}(f)$

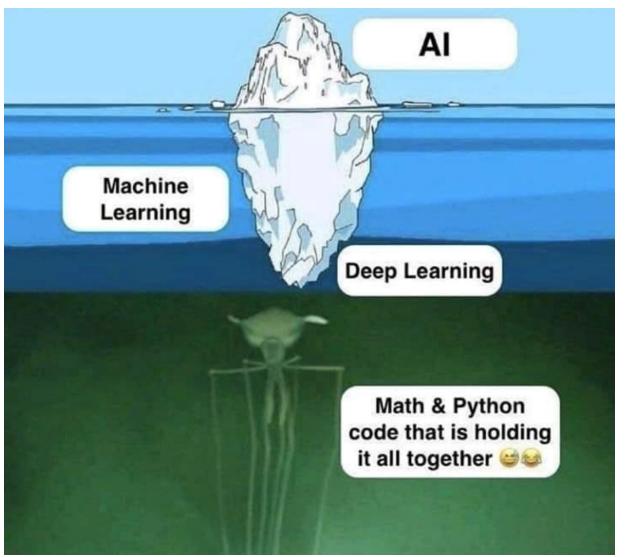
Intelligent skills learned by SL, SSL and RL

	Supervised Learning	Self-supervised Learning	Reinforcement Learning			
Function	MLP, CNN families	AE/VAE, GAN	Actor			
learned	y = f(x)	$\hat{x} = f(x)$	a = f(s)			
Intelligence	Recognitio	n	Interact with dynamic, adversial environment			
Skills learned	 Regression Classification CV tasks (Object detection, tracking) 	Feature extractionImage generationAnomaly detection	 Play chess Play video game Robot (arm) that can play with people 			

More...

- Labelling cost in SL
- SSL is particularly suitable in domains that have
 - Large-amount of data, e.g., FB, Youtube, ...
 - Unbalanced data, e.g., manufacturing, health-care
- RL has to consider
 - Prepare training environment, e.g., Unity and ML Agent
 - Reward engineering
 - Other training settings
 - Timed delay and adversial interaction
- Integrate pre-trained models with application software, e.g., flask, app
- Deployed to edge computing devices (Jetson Nano, Xavier)

Math and coding



- Probability and statistics
- Non-linear optimization
- Linear algebra

Python









Run my PyTorch code in GitHub from Colab

