

Feature-based Time Series Forecasting

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Joint work with



Rob J Hyndman



George Athanasopoulos



Pablo Montero-Manso

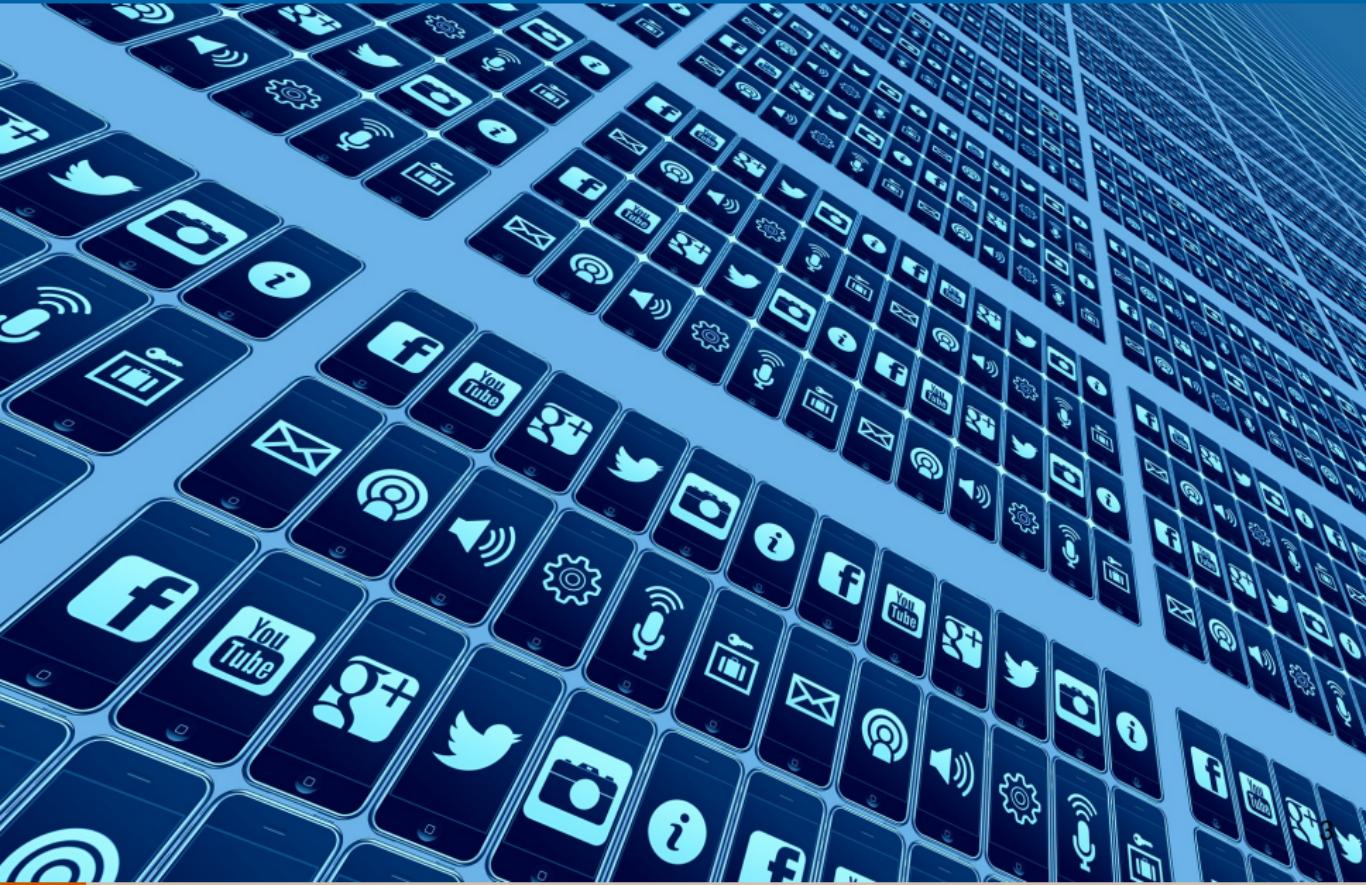


Feng Li



Yanfei Kang

Introduction



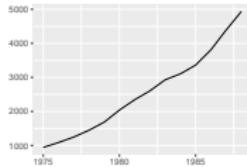
Time series features

- Transform a given time series $y = \{y_1, y_2, \dots, y_n\}$ to a feature vector $F = (f_1(y), f_2(y), \dots, f_p(y))'$.

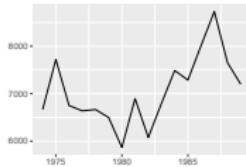
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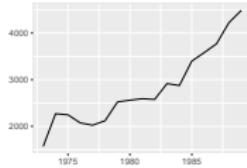
N0001



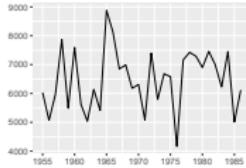
N0633



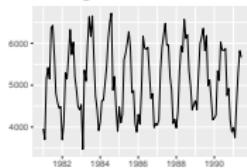
N0625



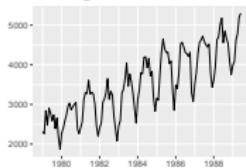
N0645



N1912



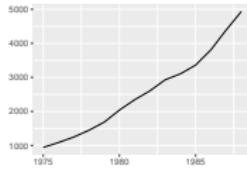
N2012



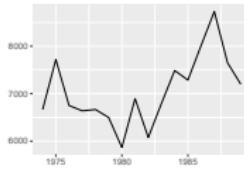
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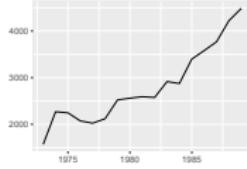
N0001



N0633



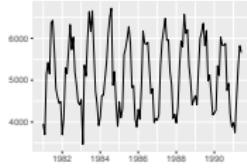
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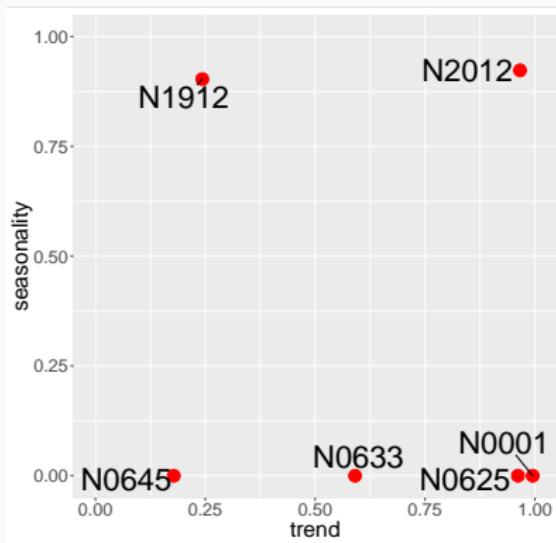
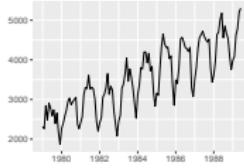
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N1912



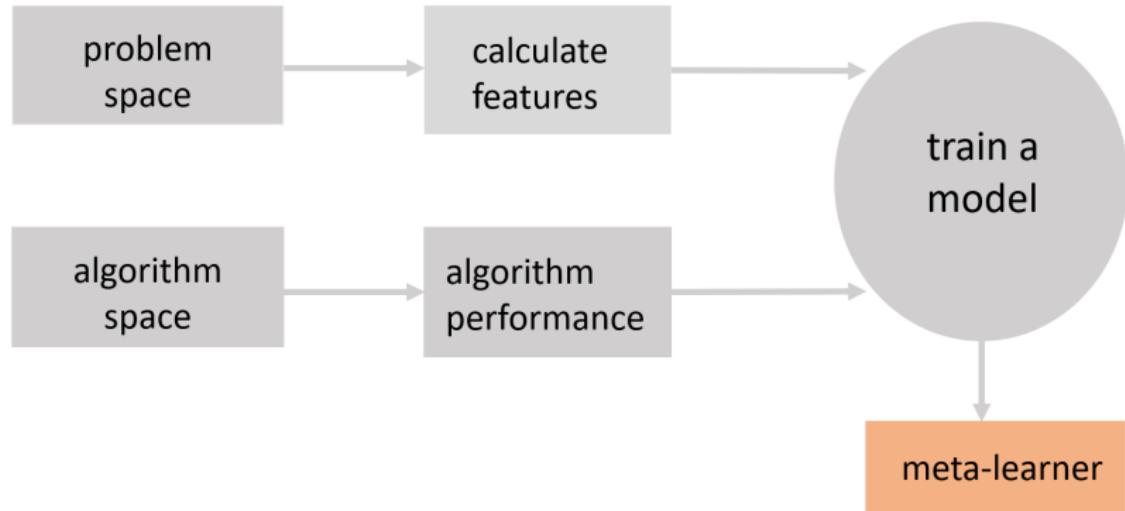
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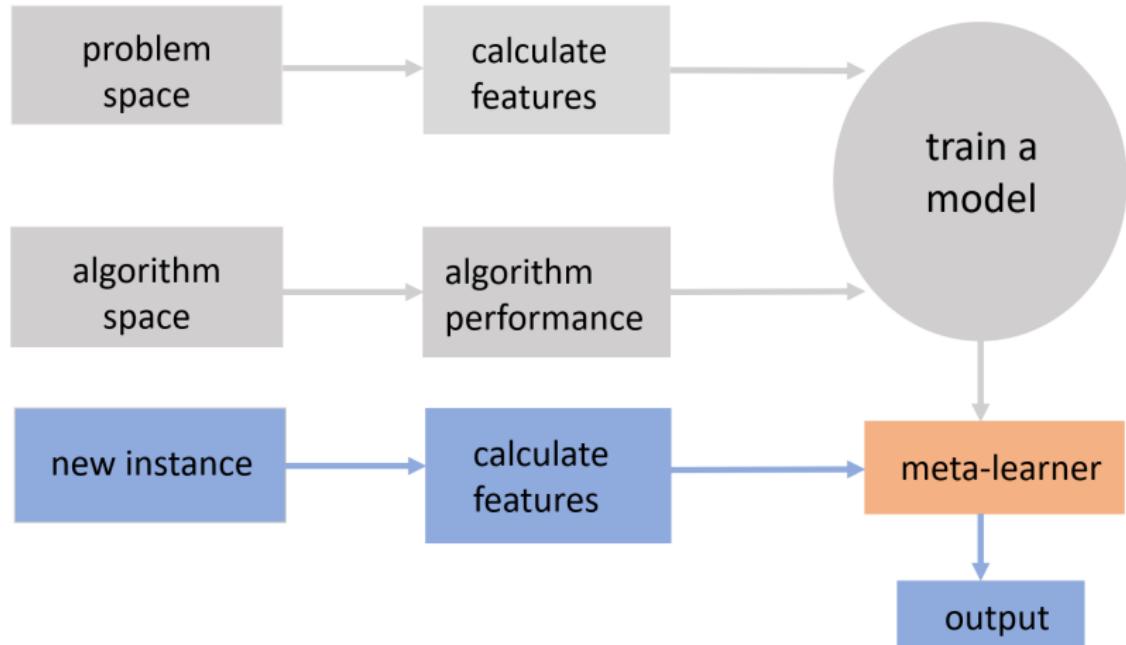
Features used to select a forecasting model

- length
- strength of seasonality
- strength of trend
- linearity
- curvature
- spikiness
- stability
- lumpiness
- parameter estimates of Holt's linear trend method
- spectral entropy
- Hurst exponent
- nonlinearity
- parameter estimates of Holt-Winters' additive method
- unit root test statistics
- crossing points, flat spots
- peaks, troughs
- ACF and PACF based features - calculated on raw, differenced, and remainder series.
- ARCH/GARCH statistics and ACF of squared series and residuals.

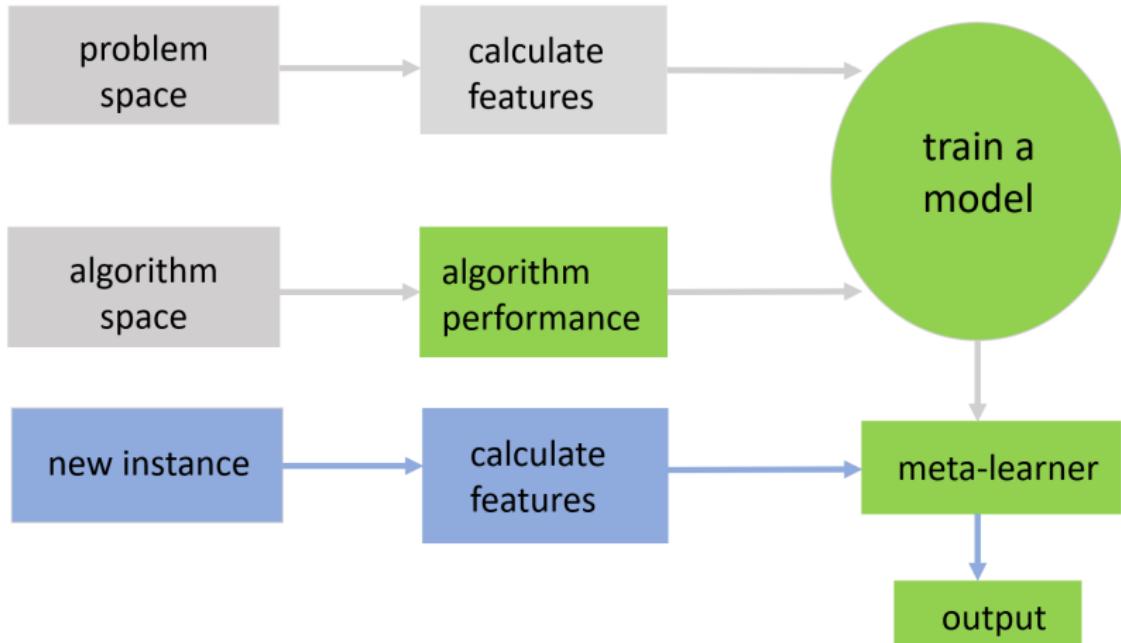
Meta-learning



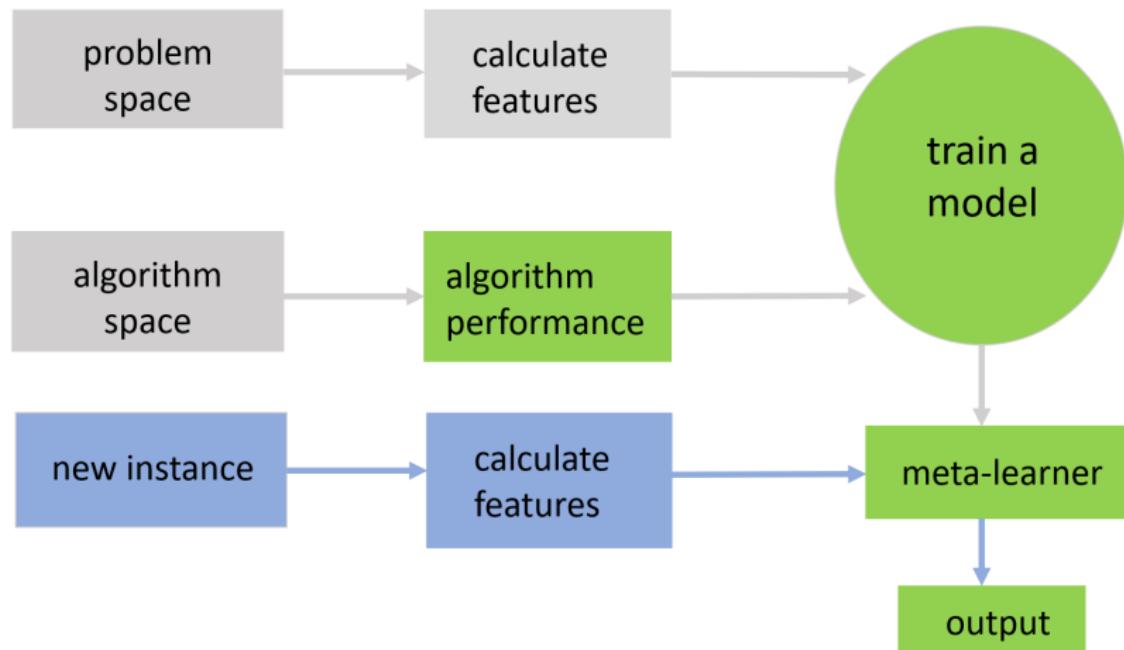
Meta-learning



Feature-based forecasting algorithms



Feature-based forecasting algorithms

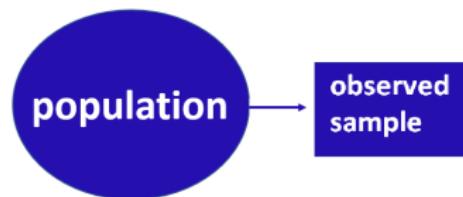


- three algorithms: **FFORMS**, **FFORMA**, **FFORMPP**

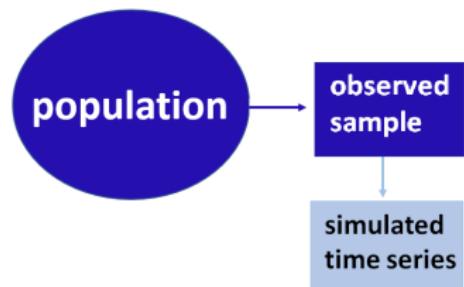
FFORMS: Feature-based FOrecast Model Selection



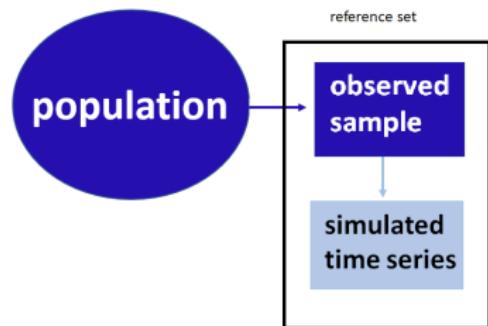
FFORMS: observed sample



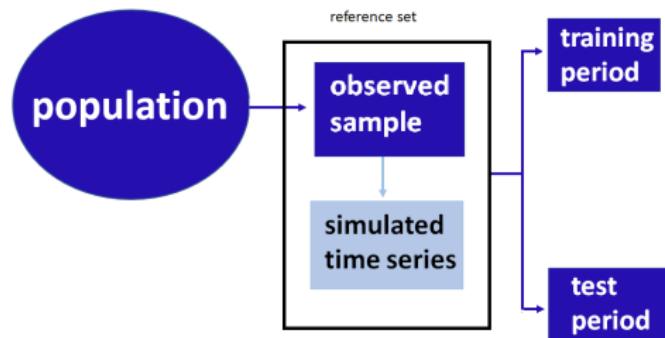
FFORMS: simulated time series



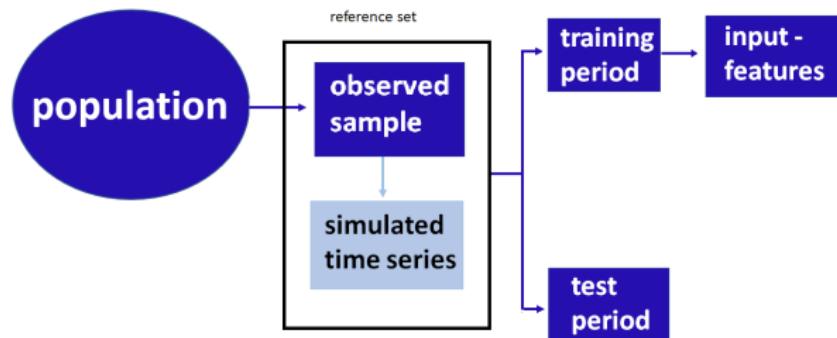
FFORMS: reference set



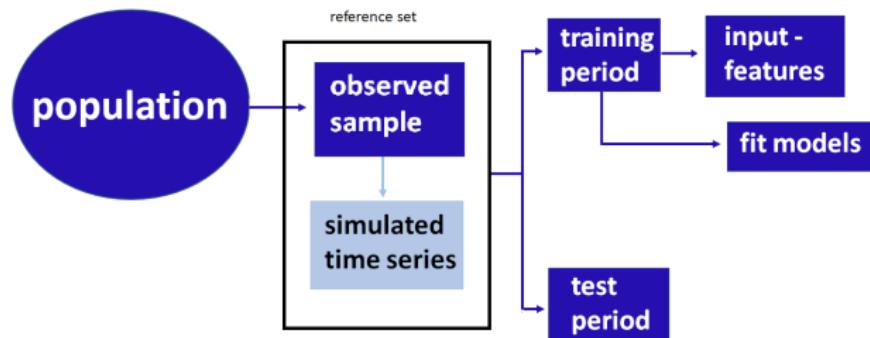
FFORMS: Meta-data



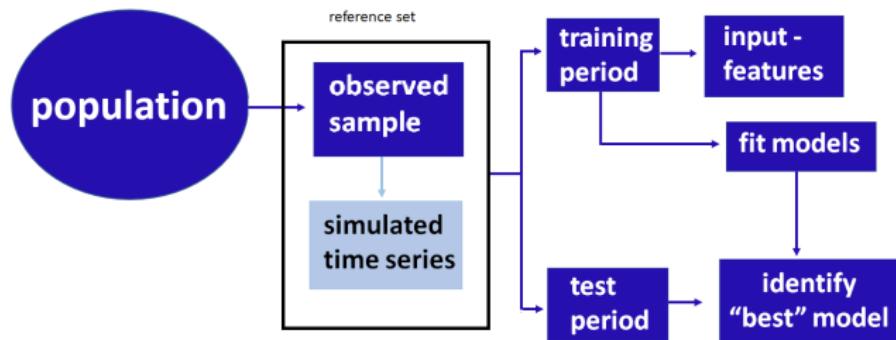
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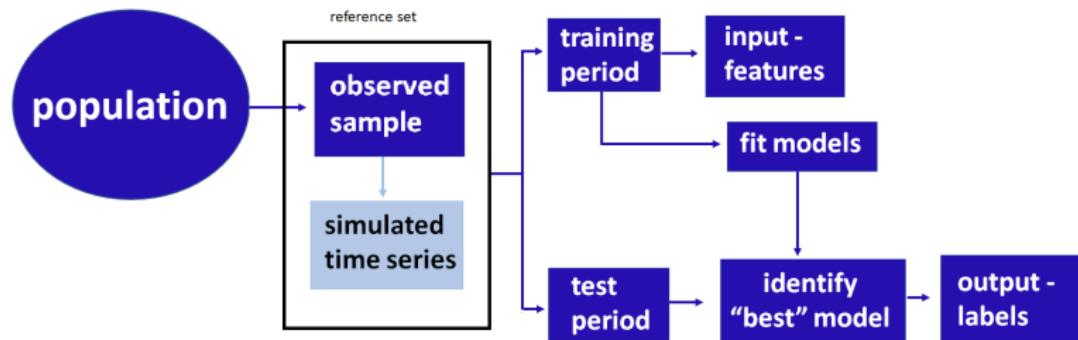
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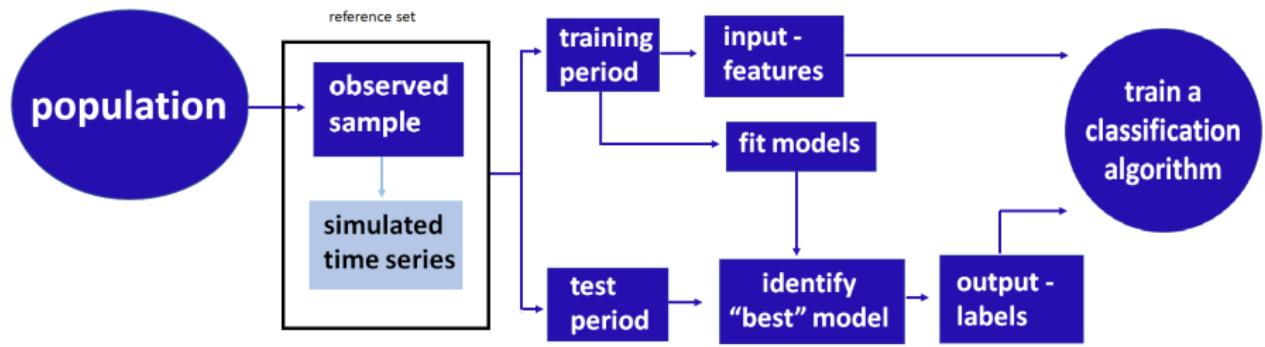
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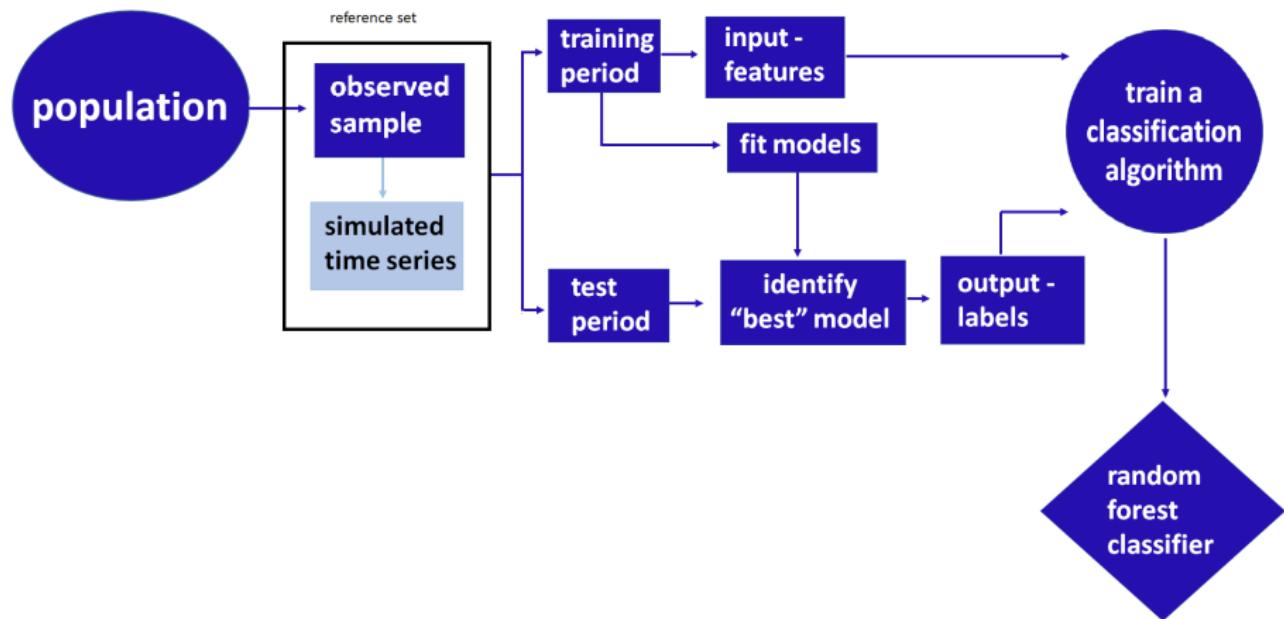
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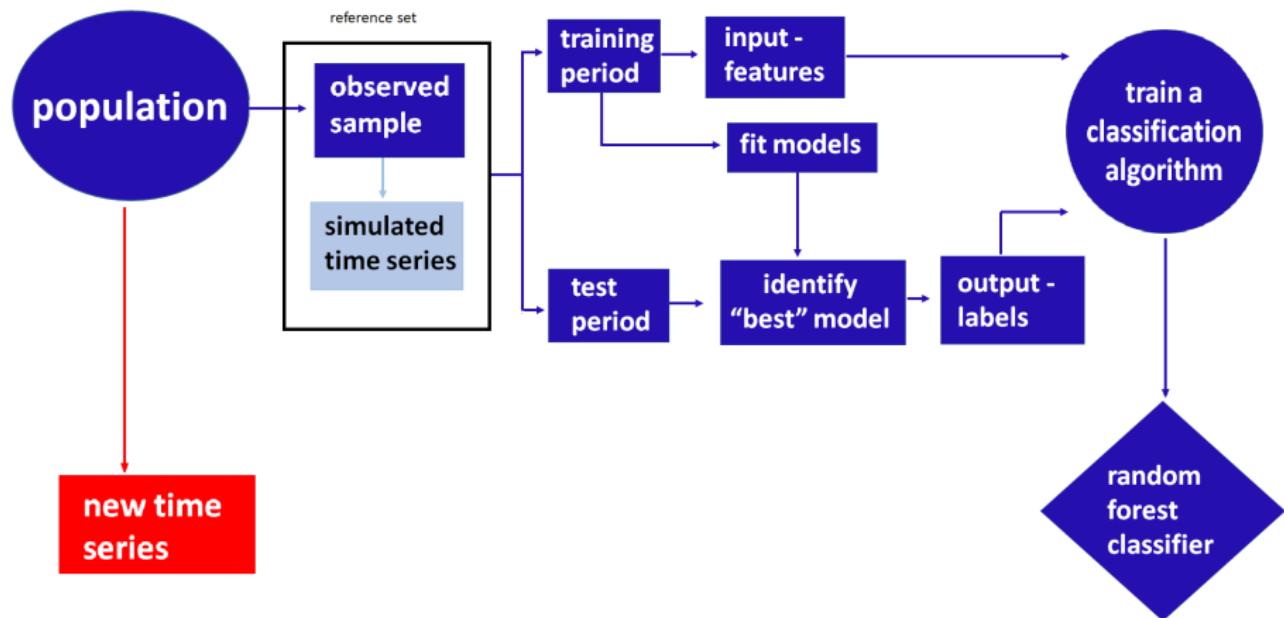
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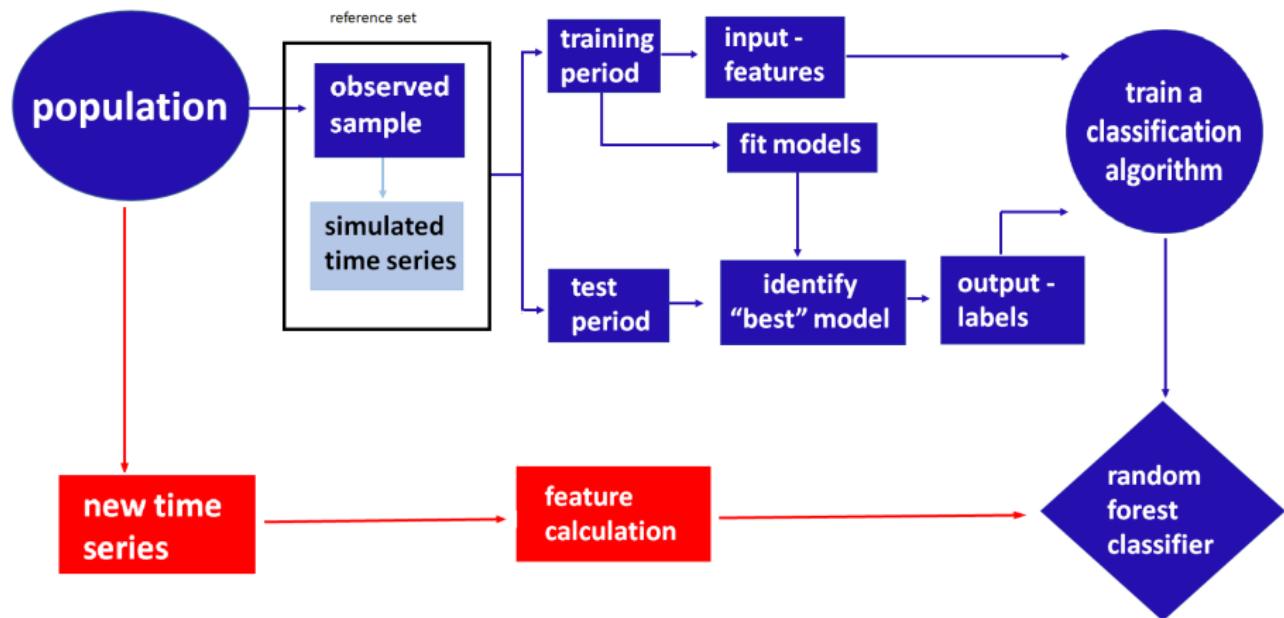
FFORMS: Random-forest classifier



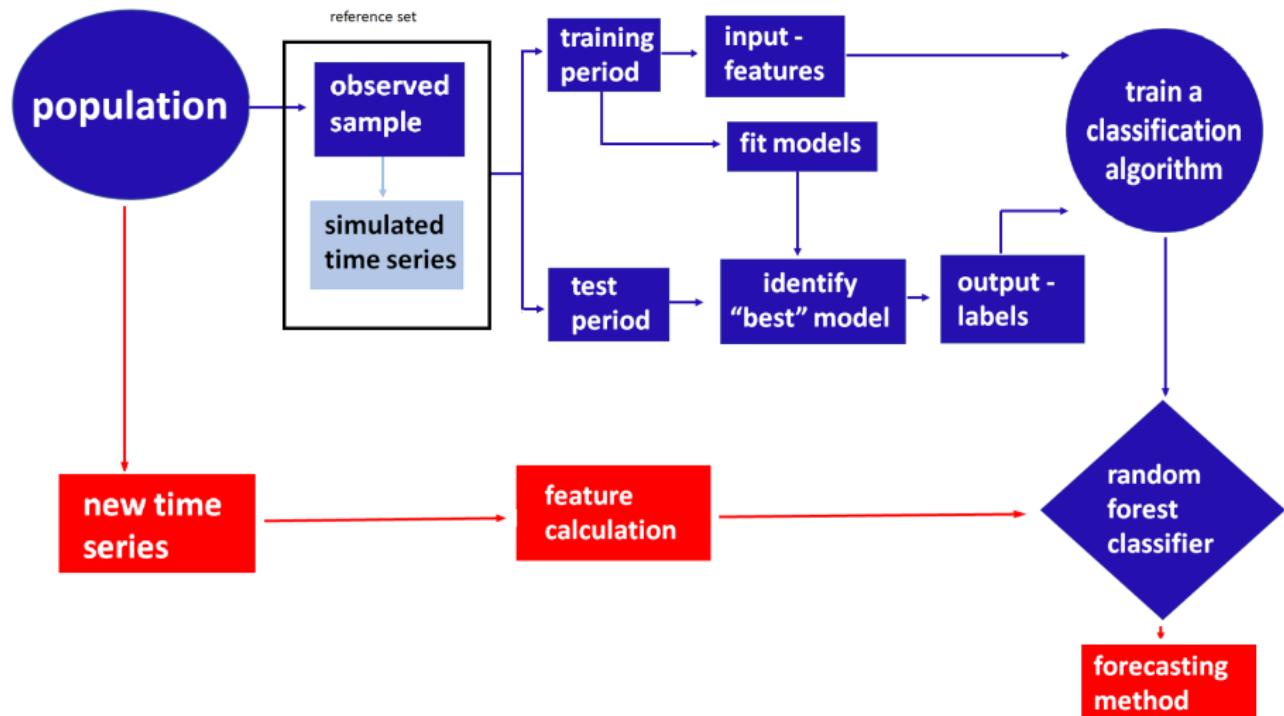
FFORMS: “online” part of the algorithm



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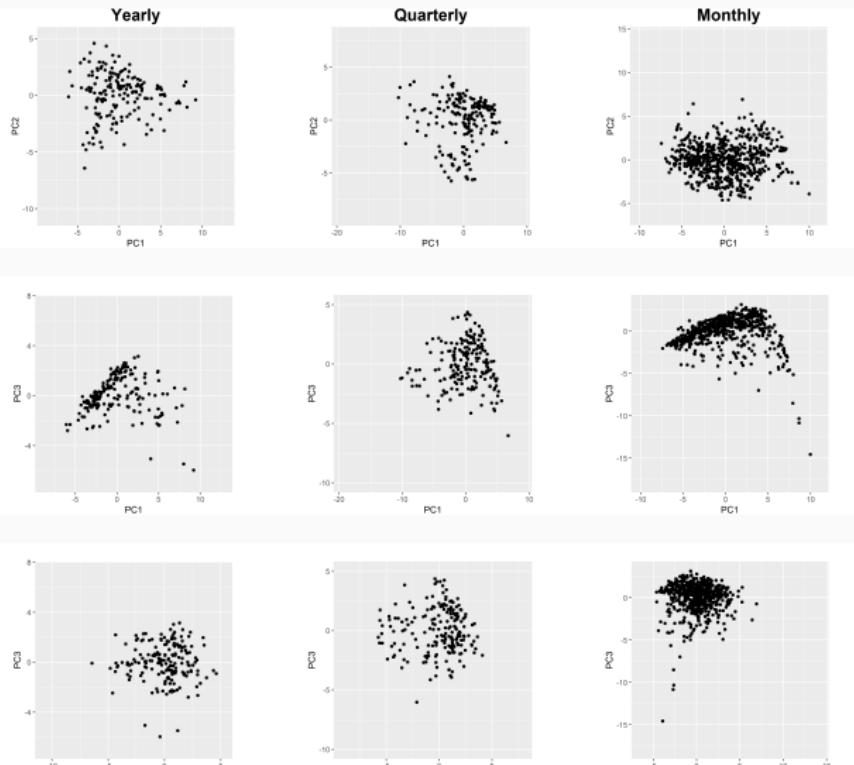
Application to M competition data

- Proposed algorithm is applied to yearly, quarterly and monthly series separately.
- We run two experiments for each case.

	Source	Experiment 1			Source	Experiment 2		
		Y	Q	M		Y	Q	M
Observed series	M1	181	203	617	M3	645	756	1428
Simulated series		362000	406000	123400		1290000	1512000	285600
New series	M3	645	756	1428	M1	181	203	617

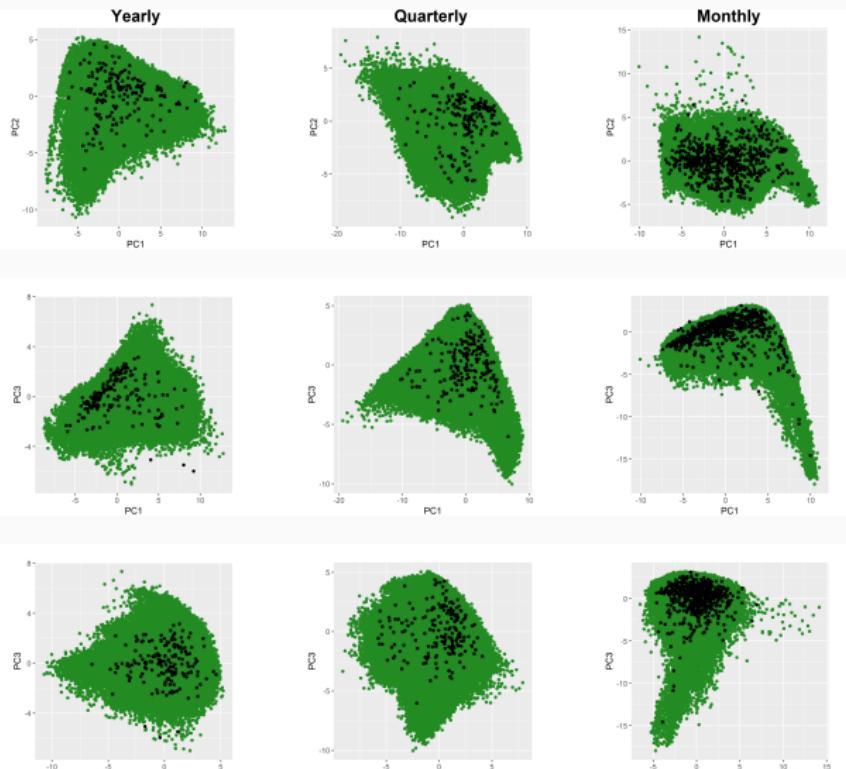
Experiment 1: Distribution of time series in the PCA space

observed - M1



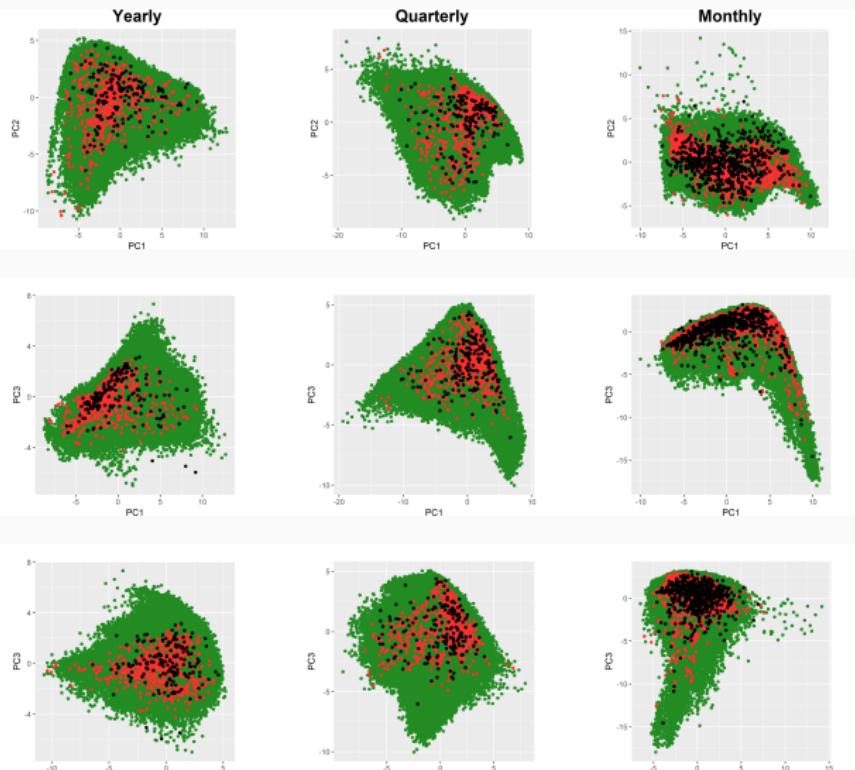
Experiment 1: Distribution of time series in the PCA space

observed - M1 simulated



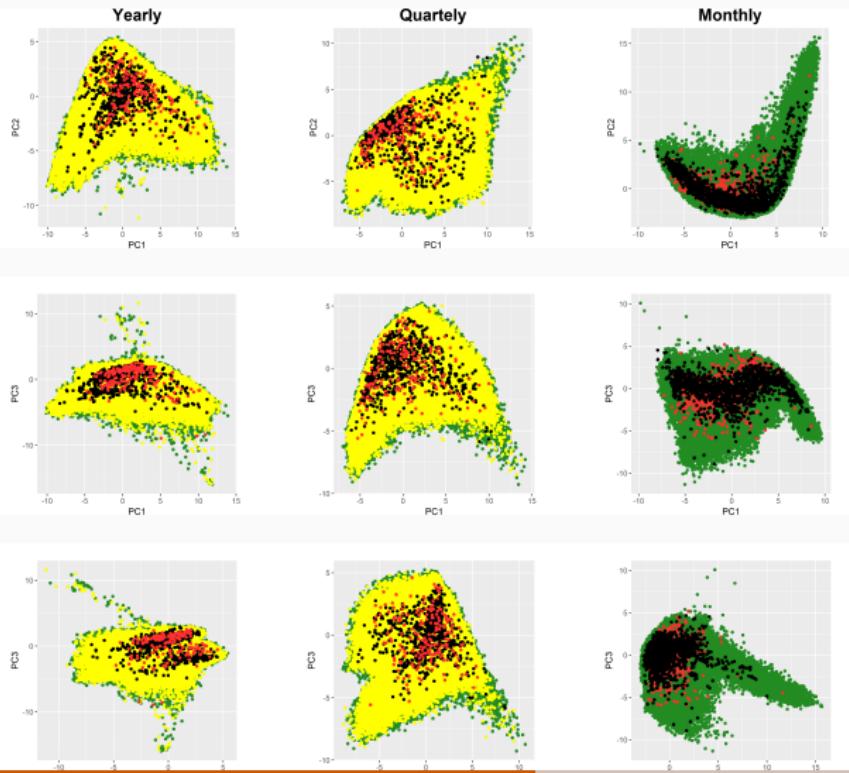
Experiment 1: Distribution of time series in the PCA space

observed - M1 simulated new - M3

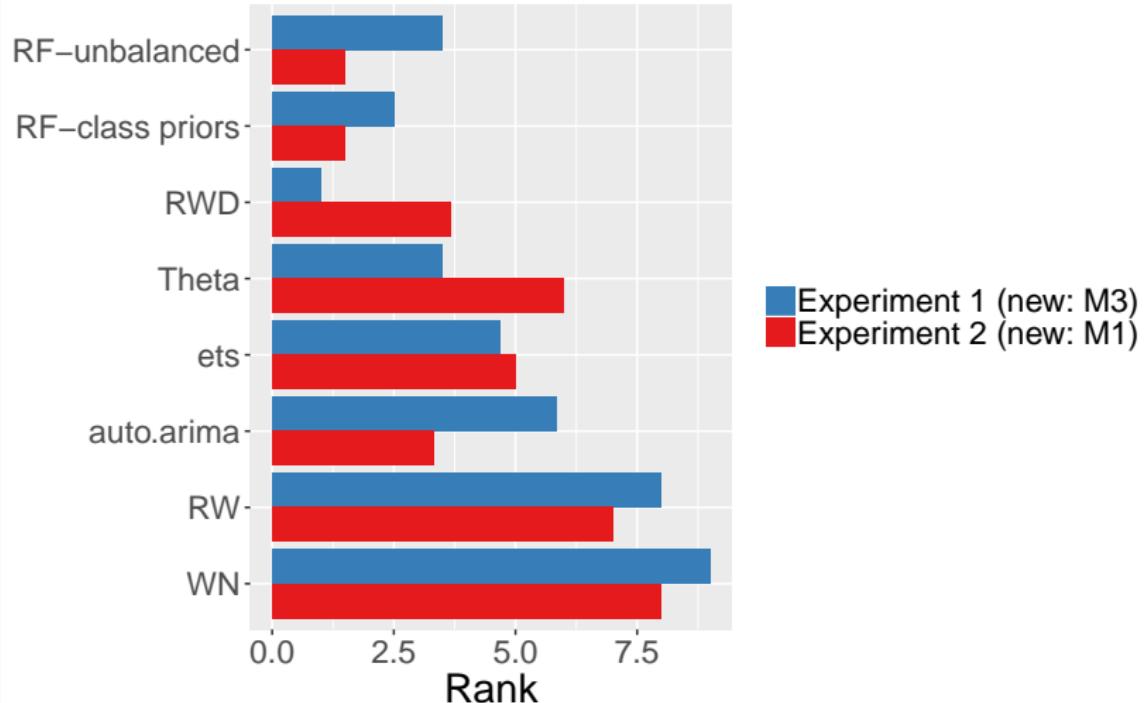


Experiment 2: Distribution of time series in the PCA space

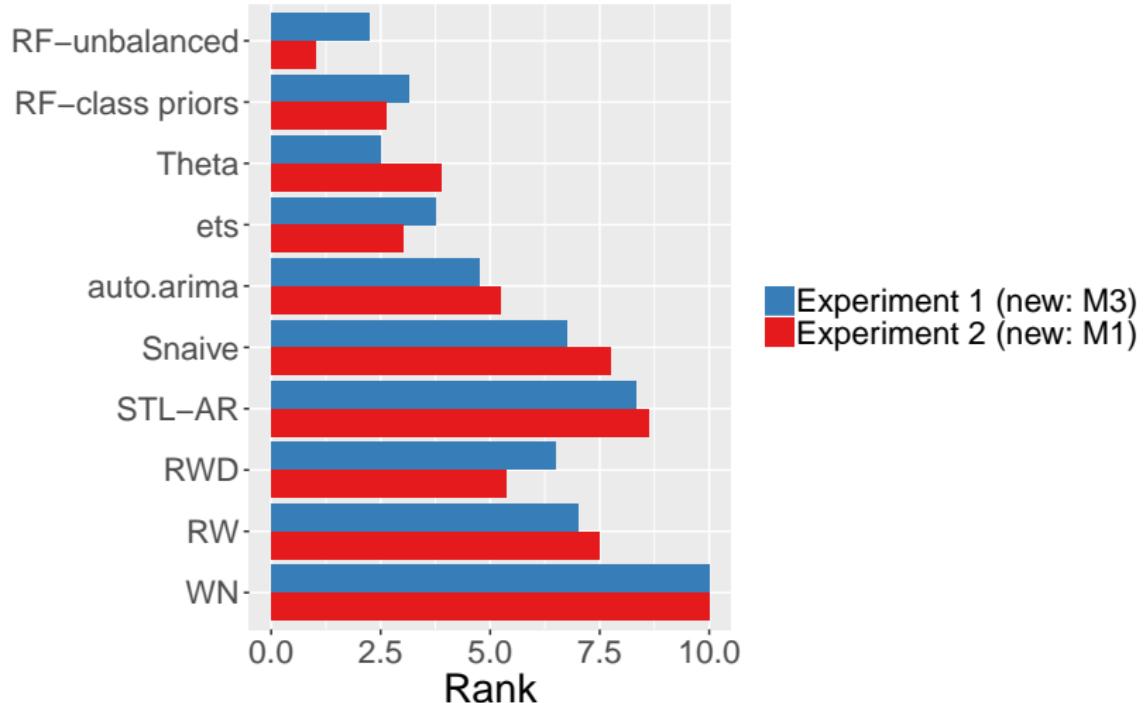
observed - M3 simulated subset new - M1



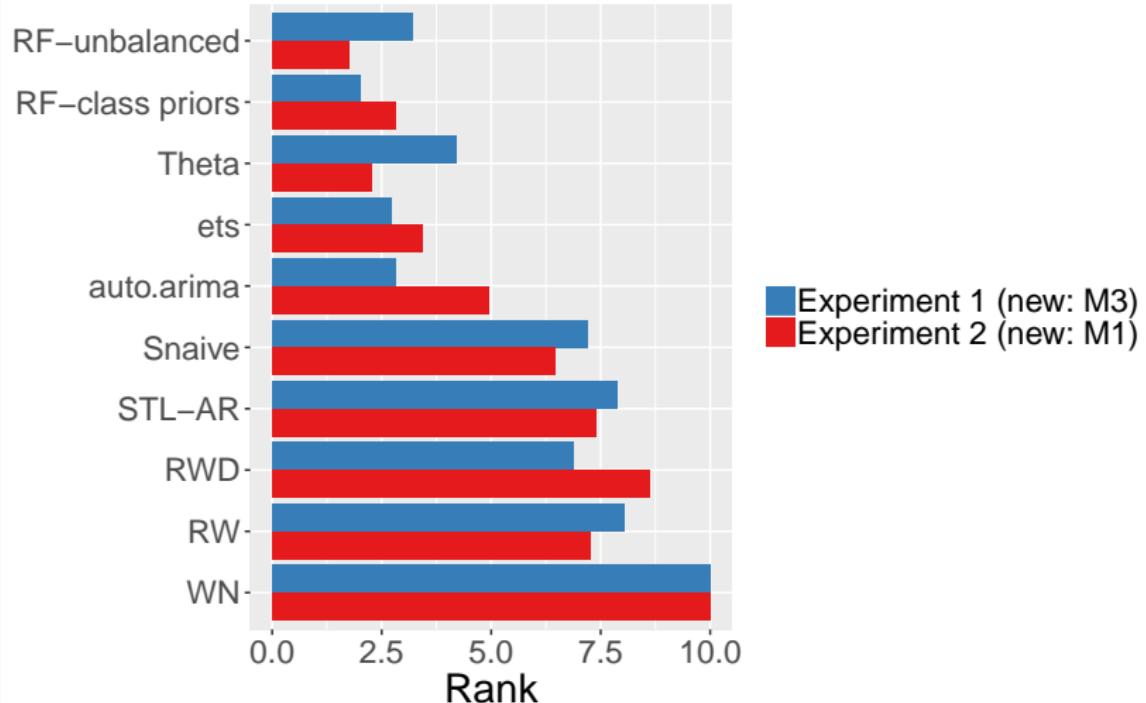
Results: Yearly



Results: Quarterly



Results: Monthly



M4 Competition: 2018

M4COMPETITION Forecast. Compete. Excel.

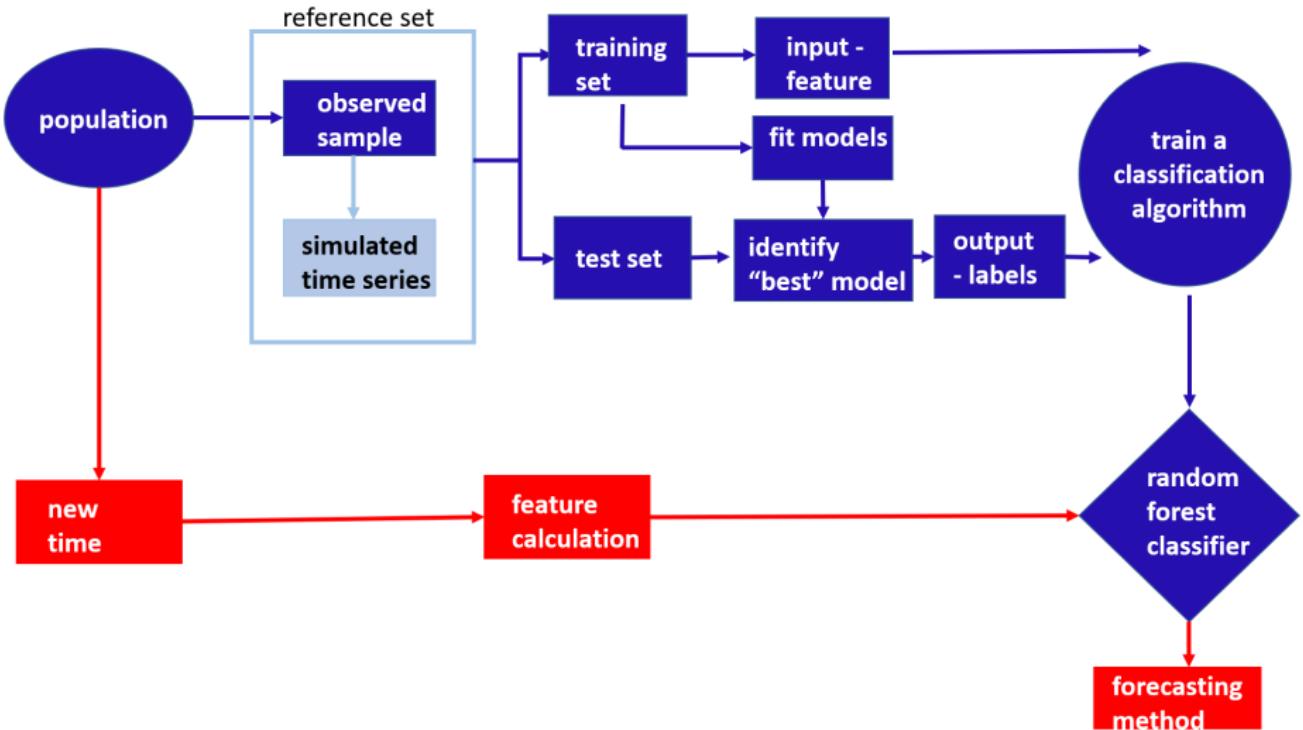


The M4 logo is centered on a grid background. The letters 'M' and '4' are large, with 'M' being white and '4' being black. Behind the logo, there are several faint, overlapping time series plots showing various trends and seasonal patterns.

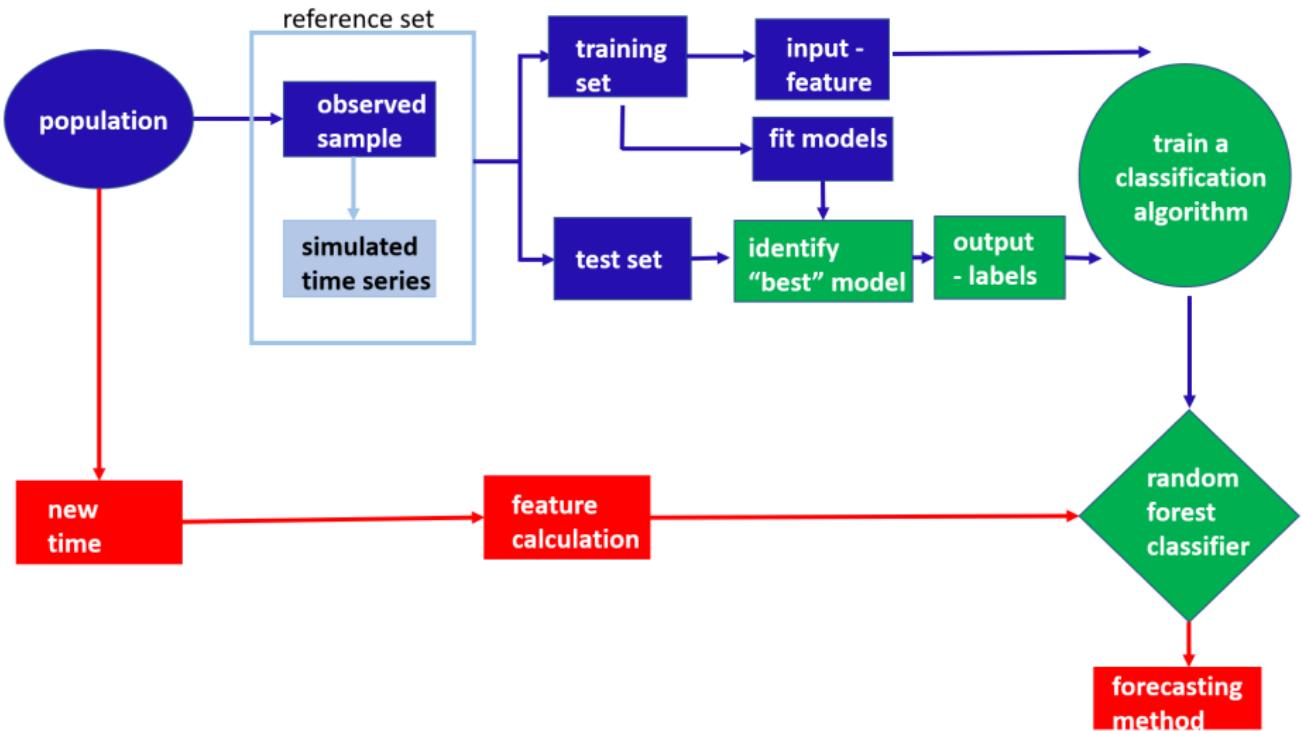
M4

- 100,000 time series: yearly, quarterly, monthly, weekly, daily, hourly

FFORMS: Feature-based FORecast Model Selection

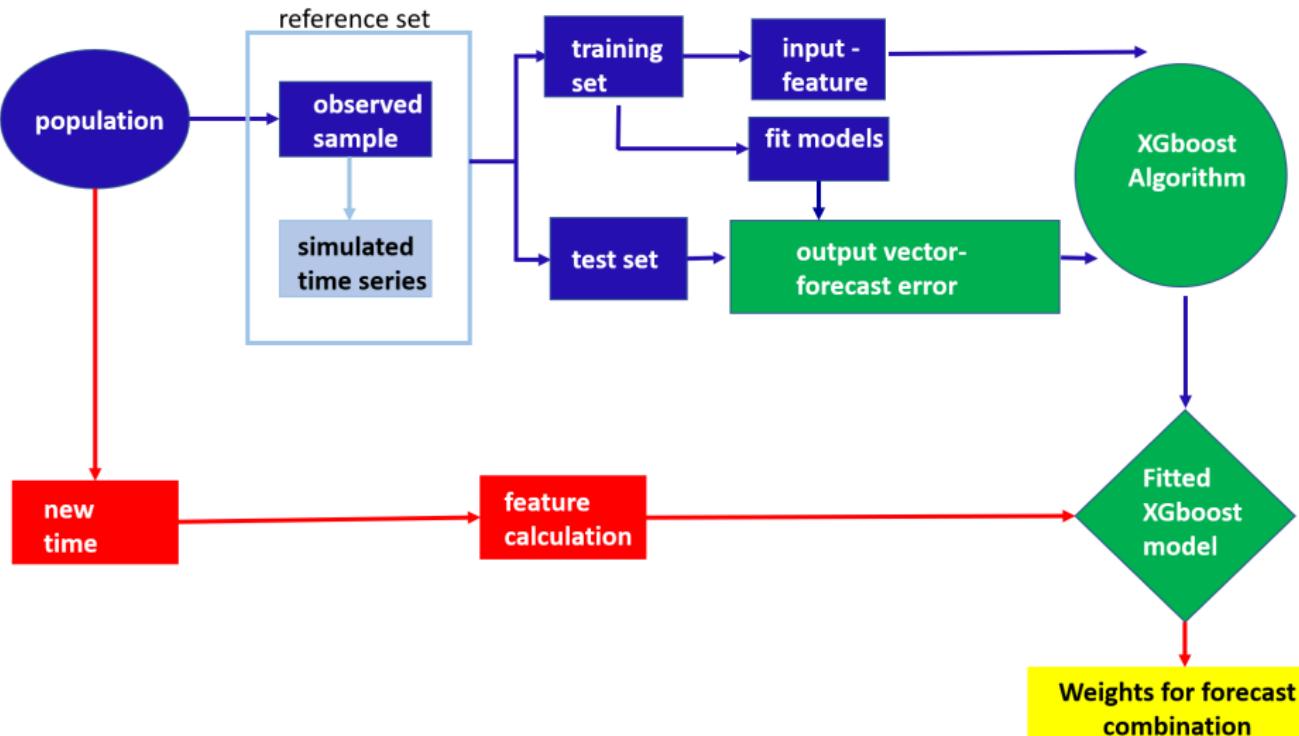


FFORMS: Feature-based FORecast Model Selection



■ optimization criterion: classification accuracy

FFORMA: Feature-based FORecast Model Averaging



■ optimization criterion: forecast accuracy

FFORMA: Models included

- naive
- random walk with drift
- seasonal naive
- theta method
- automated ARIMA algorithm
- automated exponential smoothing algorithm
- TBATS model
- STLM-AR Seasonal and Trend decomposition
using Loess with AR modeling of the seasonally
adjusted series
- neural network time series forecasts

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- A combination forecast is produced using these weights.

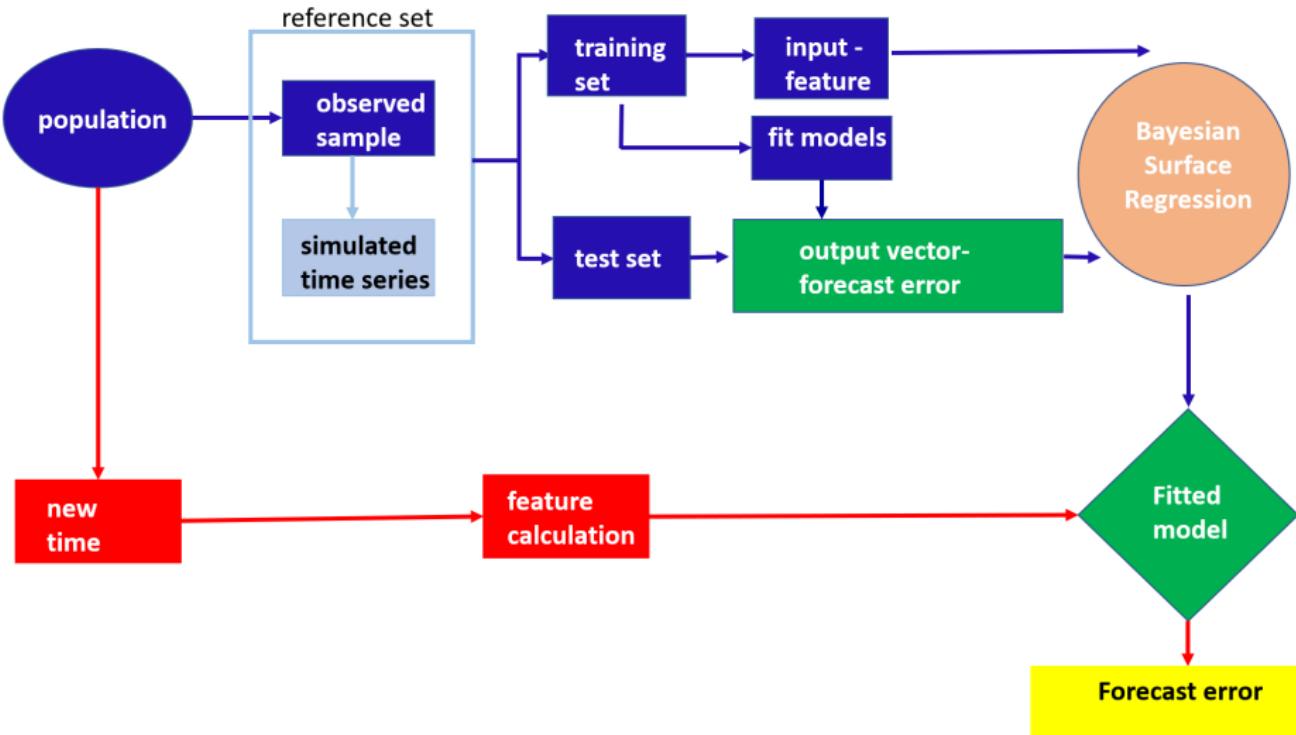
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- 248 registrations, 50 submissions

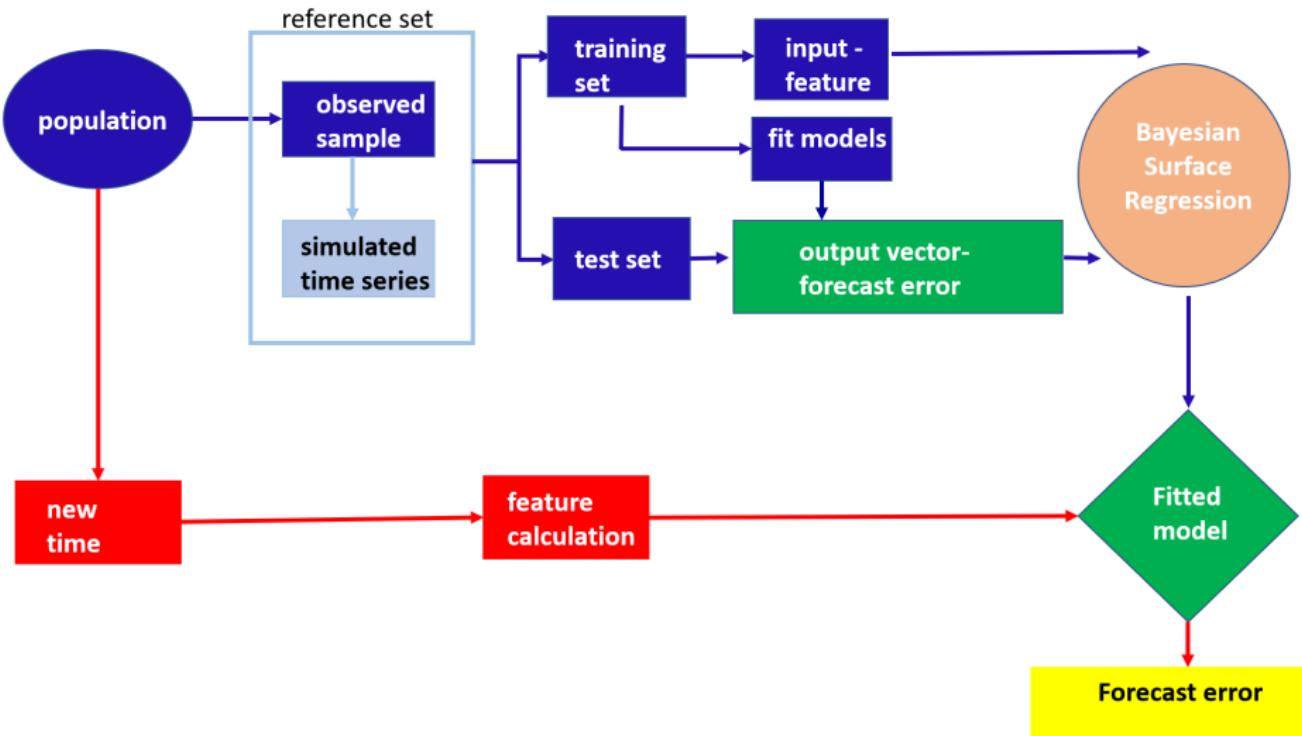
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- Came second in the M4 competition

FFORMPP: Feature-based FOrecast Model Performance Prediction



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- use the minimum predicted MASE to select forecast method(s)

- We use Efficient Bayesian Multivariate Surface Regression

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- Y: forecast error of each method, we take the correlation structure between the errors into account.

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- Why Efficient Bayesian Multivariate Surface Regression?
 - ▶ handles interactions and nonlinear relationships between features
 - ▶ allows the knot locations to move freely in the feature space, thus a less number of knots are usually used

Application to M4 Competition

- Composition of the time series in the reference set and collection of new time series

Frequency	Reference set			New series M4
	M1	M3	Simulated	
Yearly	181	645	10000	23000
Quarterly	203	756	10000	24000
Monthly	617	1428	10000	48000
Weekly	-	-	10000	359
Daily	-	-	10000	4227
Hourly	-	-	10000	414

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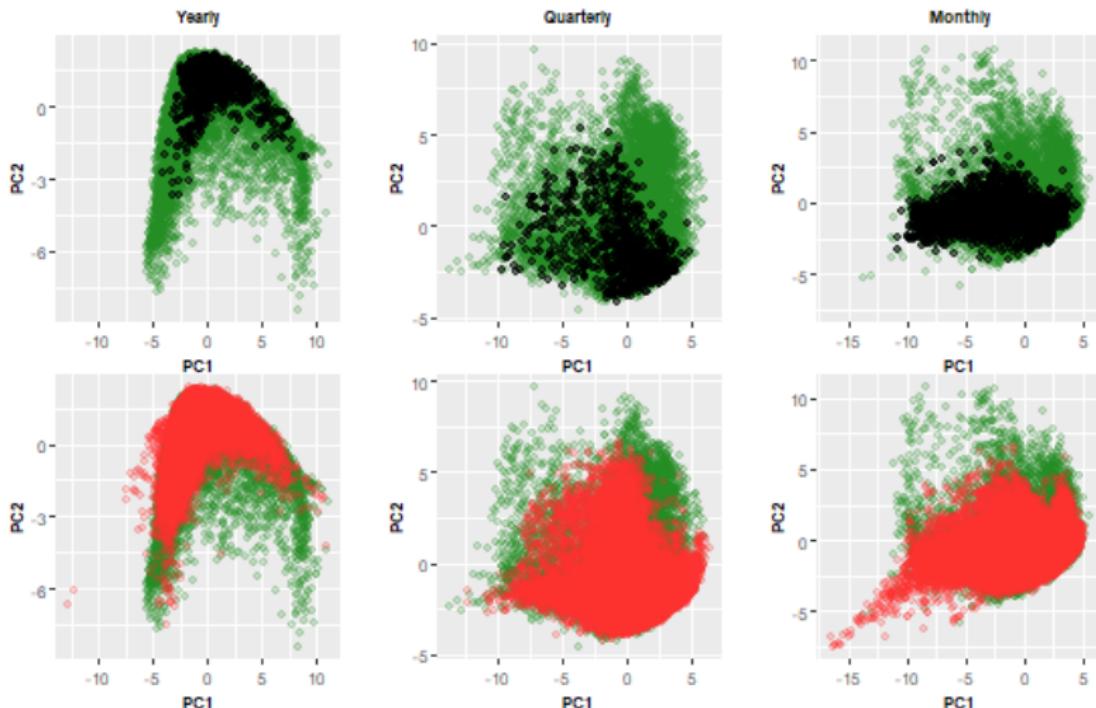
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Simulated data

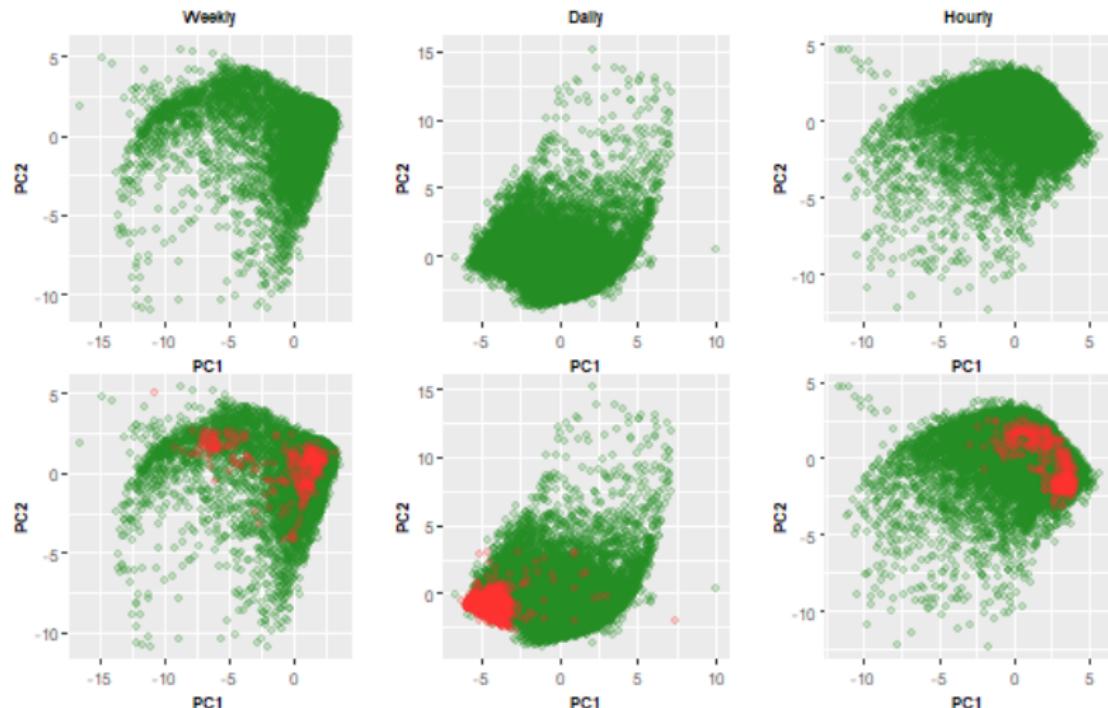
- Augmenting the observed sample with simulated time series from mixture autoregressive(MAR) models
- Proposed by Kang, Hyndman and Li (2018), Efficient generation of time series with diverse and controllable characteristics
- R package:
<https://github.com/ykang/tsgeneration>

Distribution of time series in the PCA space



■ black: observed, green-simulated, orange-M4

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Results: forecast accuracy based on MASE

	Yearly	Quarterly	Monthly	Weekly	Daily	Hourly
FFORMPP-combination*	3.07	1.13	0.89	2.46		0.96
FFORMPP-individual	3.37	1.17	1.05	2.53		1.06
auto.arima	3.40	1.17	0.93	2.55	-	-
ets	3.44	1.16	0.95	-	-	-
theta	3.37	1.24	0.97	2.64		1.59
rwd	3.07	1.33	1.18	2.68		11.45
rw	3.97	1.48	1.21	2.78		11.60
stlar	-	2.02	1.33	3.15		1.49
snaive	-	1.66	1.26	2.78		2.86
tbats	-	1.19	1.05	2.49		1.30
wn	13.42	6.50	4.11	49.91		11.68
mstlarima	-	-	-	-		1.12
mstlets	-	-	-	-		1.23
combination (median)	3.29	1.22	0.95	2.57		1.33
combination (mean)	4.09	1.58	1.16	6.96		3.93

FFORMPP-combination*: based on median forecasts of the four algorithms with minimum predicted MASE

Results: FFORMS, FFORMA, FFORMPP

R packages

References