

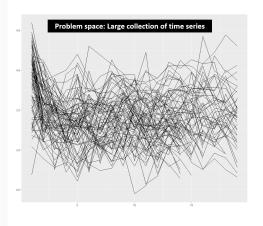


Feature-based Time Series Forecasting

Thiyanga Talagala, Rob J Hyndman, George Athanasopoulos Feng Li, Yanfei Kang

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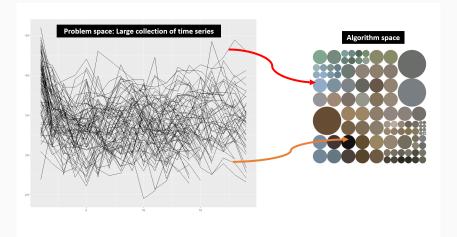
Big picture





■ What algorithm is likely to perform best?

Big picture



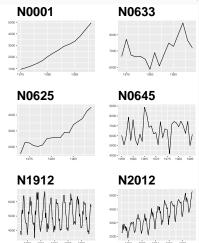
- What algorithm is likely to perform best?
- Algorithm selection problem, John Rice (1976)

Time series features

■ Transform a given time series $y = \{y_1, y_2, \dots, y_n\}$ to a feature vector $F = (f_1(y), f_2(y), \dots, f_p(y))'\}$.

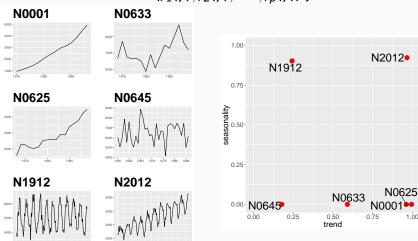
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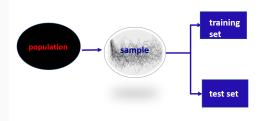
More features

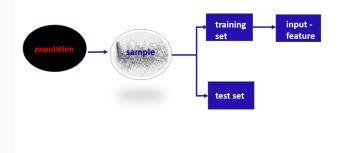
- length
- strength of seasonality
- strength of trend
- linearity
- curvature
- spikiness
- stability
- lumpiness
- spectral entropy
- Hurst exponent
- nonlinearity

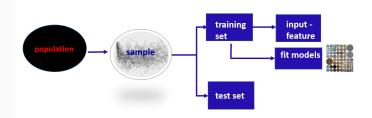
- unit root test statistics
- parameter estimates of Holt's linear trend method
- parameter estimates of Holt-Winters' additive method
- ACF and PACF based features calculated on raw, differenced, seasonally-differenced series and remainder series.

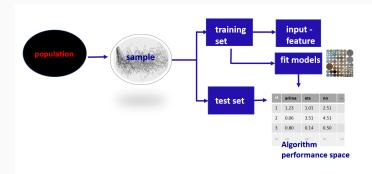


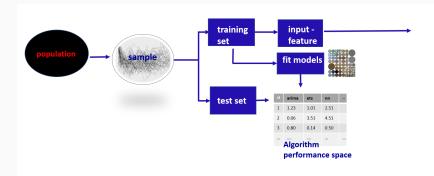


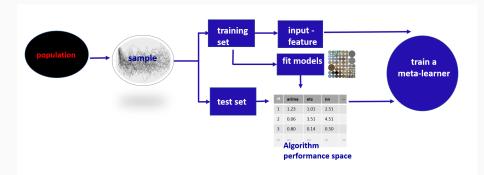


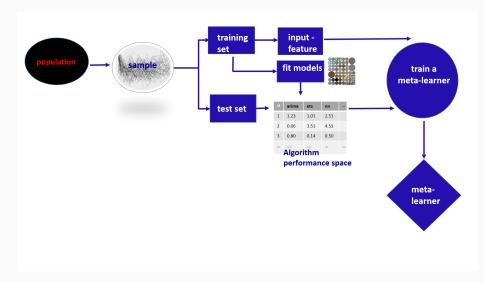


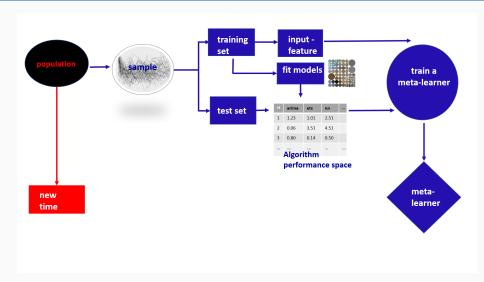


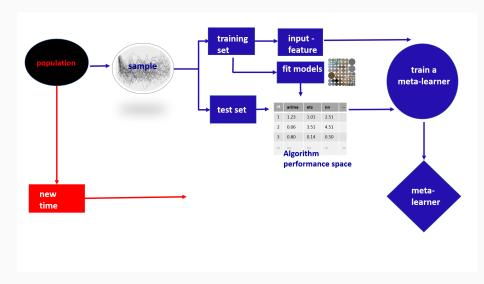


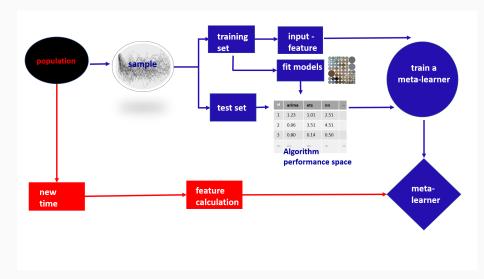


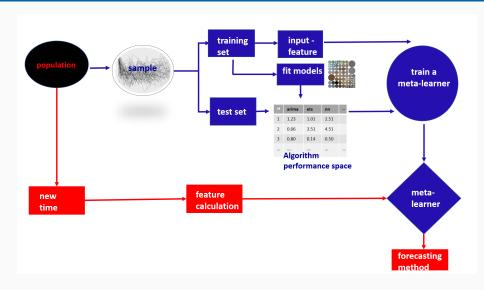


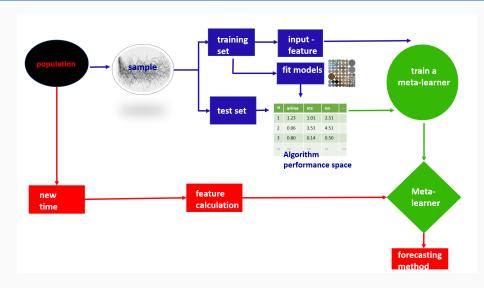




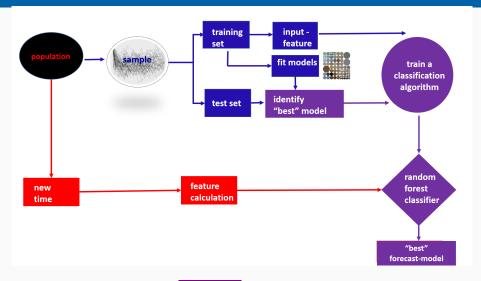






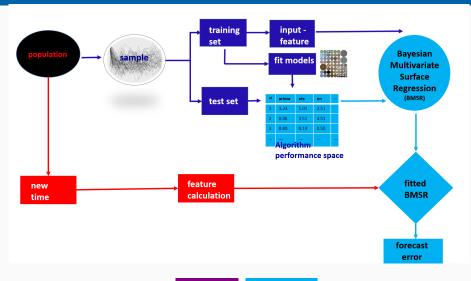


FFORMS: Feature-based FORecast Model Selection



■ three algorithms: FFORMS, FFORMPP

FFORMPP: Feature-based FORecast Model Performance Prediction



■ three algorithms: FFORMS, FFORMPP

seer R package

Installation

```
devtools::install_github("thiyangt/seer")
library(seer)
```



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Example datasets

observed time series - M1 yearly series (181)

```
library(Mcomp)
yearlym1 <- subset(M1, "yearly")</pre>
```

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Example datasets

observed time series - M1 yearly series (181)

```
library(Mcomp)
yearlym1 <- subset(M1, "yearly")</pre>
```

Input: features

```
cal_features(yearlym1[1:3], database="M1",
h=6, highfreq=FALSE)
```

```
# A tibble: 2 x 25
 entropy lumpiness stability hurst trend spikiness linearity curvature
             <dbl>
                      <dbl> <dbl> <dbl>
   <dbl>
                                          <dbl>
                                                    <dbl>
                                                             <dbl>
   0.683 0.0400 0.977 0.985 0.985 1.32e-6 4.46
                                                             0.705
   0.711 0.0790 0.894 0.988 0.989 1.54e-6 4.47
                                                             0.613
# ... with 17 more variables: e acf1 <dbl>, y acf1 <dbl>,
#
   diff1y_acf1 <dbl>, diff2y_acf1 <dbl>, y_pacf5 <dbl>,
#
   diff1y pacf5 <dbl>, diff2y pacf5 <dbl>, nonlinearity <dbl>,
#
   lmres acf1 <dbl>, ur pp <dbl>, ur kpss <dbl>, N <int>, y acf5 <dbl>,
#
   diff1v acf5 <dbl>, diff2v acf5 <dbl>, alpha <dbl>, beta <dbl>
```

Input: features

[1,] 579581.0 390955.9 [2.] 605761.9 407325.1

[3,] 631942.9 423694.4

```
seer::fcast_accuracy(tslist=yearlym1[1:2],
              models= c("arima", "ets", "rw", "rwd", "theta", "nn"),
              database ="M1", cal_MASE, h=6,
              length out = 1,
              fcast save = TRUE)
$accuracy
        arima
                                      rwd theta
                    ets
                              rw
                                                           nn
YAF2 10.527612 10.319029 13.52428 10.527612 12.088375 11.779322
YAF3 5.713867 7.704409 7.78949 5.225965 6.225463 6.700763
$ARIMA
                    YAF2
                                              YAF3
"ARIMA(0,1,0) with drift" "ARIMA(0,1,1) with drift"
$ETS
       YAF2
                    YAF3
"ETS(A,A,N)" "ETS(M,A,N)"
$forecasts
$forecasts$arima
        YAF2
                 YAF3
```

Training set

```
prepare_trainingset(accuracy_set = accuracy_m1,
feature_set = features_m1)$trainingset
```

```
# A tibble: 2 x 26
 entropy lumpiness stability hurst trend spikiness linearity curvature
   <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
                                                   <dbl>
                                                             dbl>
   0.683 0.0400 0.977 0.985 0.985 1.32e-6 4.46
                                                            0.705
1
   0.711 0.0790 0.894 0.988 0.989 1.54e-6 4.47
                                                            0.613
# ... with 18 more variables: e_acf1 <dbl>, y_acf1 <dbl>,
#
   diff1y acf1 <dbl>, diff2y acf1 <dbl>, y pacf5 <dbl>,
   diff1y_pacf5 <dbl>, diff2y_pacf5 <dbl>, nonlinearity <dbl>,
#
#
   lmres_acf1 <dbl>, ur_pp <dbl>, ur_kpss <dbl>, N <int>, y_acf5 <dbl>,
#
   diff1y acf5 <dbl>, diff2y acf5 <dbl>, alpha <dbl>, beta <dbl>,
#
   classlabels <chr>
```

FFORMS classifer