

Ta có: $\left. \begin{array}{l} BQ \parallel MC \\ BQ = MC \end{array} \right\} \rightarrow BQCM \text{ là h.b.h}$

b) $\diamond ABQM$ là hình cn cm cần a.

c) $S_{AQC} = \frac{1}{2} QM \cdot AC$

$$= \frac{1}{2} \cdot BA \cdot \frac{1}{2} \cdot BA = \frac{1}{4} \cdot 5 = \frac{5}{4} \text{ cm}$$

d)

a) Xét $\triangle MCN$ và $\triangle QBN$:

$$\widehat{MN} = \widehat{QN} \text{ (đối đỉnh)}$$

$$\widehat{CMN} = \widehat{QNB} \text{ (đối đỉnh)}$$

$$\widehat{MCN} = \widehat{QNB} \text{ (đối đỉnh)}$$

$$NC = NB \text{ (đề bài)}$$

$$\left. \begin{array}{l} \widehat{MN} = \widehat{QN} \\ \widehat{CMN} = \widehat{QNB} \\ \widehat{MCN} = \widehat{QNB} \end{array} \right\} \Rightarrow \triangle MCN = \triangle QBN \text{ (c.g.c)}$$

$$\Rightarrow MC = BQ$$

$$\widehat{CMN} = \widehat{QBN} = 90^\circ$$

$$\Rightarrow MC \parallel BQ$$

Vì $MC \parallel BQ$ nên $\diamond BQCM$ là h.b.h

$$MC = BQ$$

b) Ta có: $MN = \frac{1}{2} AB \left\{ \begin{array}{l} \rightarrow AB = 2MN \text{ (1)} \\ MN = \frac{1}{2} MQ \end{array} \right.$

$$MA = MC = BQ \text{ (2)}$$

Mặt khác $\left. \begin{array}{l} AC = 2AB \\ AC = 2AM \end{array} \right\} \Rightarrow AM = AB \text{ (3)}$

$$(1)(2)(3) \Rightarrow AM = MQ = QB = AB \left\{ \begin{array}{l} \rightarrow \triangle AMB \text{ là} \\ \widehat{MAB} = 90^\circ \end{array} \right. \text{ hình vuông}$$

$\triangle BEO$ đồng dạng với $\triangle BOF$:

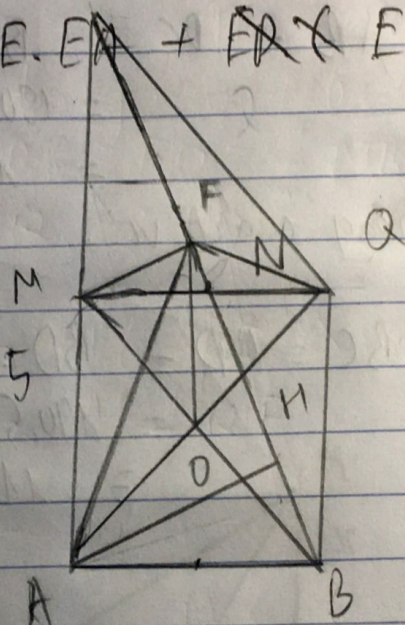
$$\frac{BE}{BO} = \frac{BO}{BF}$$

$$\Rightarrow BE \cdot BF = BO^2$$

$$BE(BE + EF) = BO^2$$

$$\Rightarrow BE^2 + BE \cdot EF = BO^2$$

$$\Rightarrow OE \cdot EN + ED \cdot EF = R^2$$



a) Theo đề bài: $\left. \begin{array}{l} MA = MC \\ NB = NC \end{array} \right\} \Rightarrow MN \text{ là đg trung bình}$
 $\triangle ABC$

$\rightarrow MN \parallel AB \rightarrow MQ \parallel AB$

$$MN = \frac{1}{2} AB$$

Mặt khác $MN = \frac{1}{2} MQ \rightarrow MQ = AB$

Tại: $\left. \begin{array}{l} MQ = BA \\ \widehat{BAM} = \widehat{AMQ} = 90^\circ \\ MQ \parallel BA \end{array} \right\} \Rightarrow \text{Thứ giác } AMQB \text{ là hcn}$

$\rightarrow BQ \parallel AC$

$$BQ = AM$$

$$\Rightarrow BQ = AM = MC$$