

(1)

$$495 \times 70 = 34650$$

(2)

abc, acb, bac, bca, cab, cba

(3)

$$P(A) = P(D) \times P(D|D-1)$$

$$P(A) = (4/12) \times (3/11) = 1/11$$

$$P(B) = P(N) \times P(N|N-1)$$

$$P(B) = (8/12) \times (7/11) = 14/33$$

$$P(\text{at least one item is defective}) = 1 - P(\text{both items are non-defective})$$

$$P(\text{both items are non-defective}) = P(B) = 14/33$$

Therefore,

$$P(\text{at least one item is defective}) = 1 - 14/33 = 19/33$$

(4)

$${}_n C_r = n! / (r! \times (n-r)!)$$

$${}_{10} C_3 = 10! / (3! \times (10-3)!) = 120$$

$${}_{15} C_3 = 15! / (3! \times (15-3)!) = 455$$

$$P(\text{none defective}) = 120 / 455 = 24 / 91$$

$${}_5 C_1 = 5$$

$${}_{10} C_2 = 45$$

$$5 \times 45 = 225$$

$$P(\text{exactly one defective}) = 225 / 455 = 45 / 91$$

$$P(\text{at least one defective}) = 1 - P(\text{none defective})$$

We have already calculated $P(\text{none defective})$ in part (i).

Therefore,

$$P(\text{at least one defective}) = 1 - 24/91 = 67/91$$

(5)

$$P(B) = 10 / 30 = 1/3$$

$$P(M) = 15 / 30 = 1/2$$

Mansoura University is $5/2 = 2.5$, which is not possible. Therefore, $P(B \text{ and } M) = 0$.

$$P(B \text{ or } M) = P(B) + P(M) - P(B \text{ and } M)$$

$$= 1/3 + 1/2 - 0$$

$$= 5/6$$

-
- (6)
- (i) $P(A^c) = 5/8$
 - (ii) $P(B^c) = 1/2$
 - (iii) $P(A \cap B) = 5/8$
 - (iv) $P(A \cup B) = 1/2$
 - (v) $P(A \cap B)$ is not possible ($-1/8$)
 - (vi) $P(B \cap A^c) = 0$
-

(7)

$$1 - 6/36 = 5/6$$

$$(5/6)^3 = 125/216$$

$$1 - 125/216 = 91/216$$

(8)

Since we are given that $\sum P(x) = k^2 - 8$, we can start by using the fact that the sum of probabilities for all possible outcomes in a probability distribution is equal to 1:

$$\sum P(x) = 1$$

Substituting $\sum P(x) = k^2 - 8$, we get:

$$k^2 - 8 = 1$$

Adding 8 to both sides, we get:

$$k^2 = 9$$

Taking the square root of both sides, we get:

$$k = \pm 3$$

Since k must be a non-negative number in this context, we can take $k = 3$. Therefore, the value of k is 3.

(9)

$$P(A \cap B) = P(A) + P(B) - P(A \cup B)$$

$$P(A \cup B) = P(A) + P(B)$$

Substituting the given values, we get:

$$P(A \cup B) = 0.35 + 0.45 = 0.8$$

So, the probability of neither A nor B occurring is:

$$\begin{aligned} P(A' \cap B') &= 1 - P(A \cup B) \\ &= 1 - 0.8 = 0.2 \end{aligned}$$

