

# **DEVELOPMENT OF A MONOCULAR THREE-DIMENSIONAL SELF-CALIBRATING RECONSTRUCTION ALGORITHM BASED ON DIGITAL PHOTOGRAMMETRY**

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by

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