

Compression Models are getting larger

Alexnet 2012 → 8 layers 1.4 GFlop
~16% Error.

2015 → 152 22.6 GFlop
3.5% Error

] 16X

The increase in size → increased accuracy
→ need for acceleration

- run a network faster (performance, runtime, inf/sec)
→ run a network more efficiently (energy, monetary, cost)

Objectives of acceleration inf/J inf/#

For inference (previous lecture) → cascades
→ replication
(just focus on the
fast forward passes forward pass)

Training : → fast back-prop. (gradients)
→ update.

Today's lecture: How do we reduce cost for all three operations?

I) Using reduced precision arithmetic
→ increase the amount of data we can fit into a given processing unit and hence optimize util.

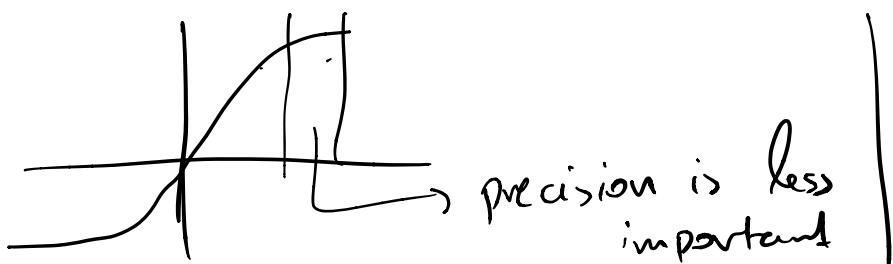
2) Compression \rightarrow pruning. (reduce the ops we are performing)

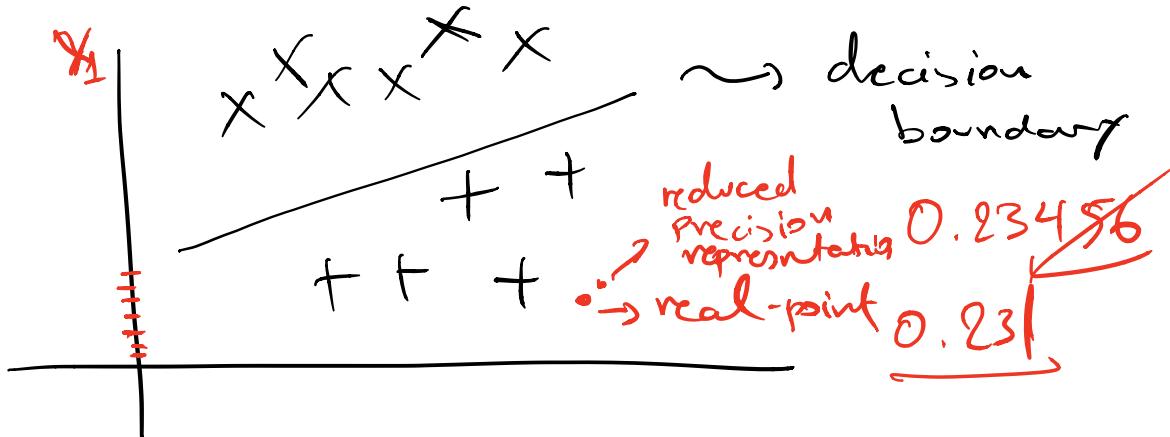
3) Better algorithm. (fastest alg possible)
Low-rank approx. of fundamental ops in DNNs.

Reduced Precision

- We get reduced storage
- We get reduced energy (because we need less complex hardware "fewer transistors" when we use reduced precision.)
- Improved performance (speed)
- Sometimes: has little effect on the accuracy.

Examples $\max(0, x)$, $x \leq 0$





DNN: \rightarrow relu, or other non-lin.

$$b_i = f \left(\sum_j w_{ij} a_i \right)$$

↑ ↑ ↑
output. Params. input variables.

$$b = \begin{matrix} \text{weight} \\ \text{matrix} \end{matrix} \cdot \begin{matrix} \text{input} \\ \text{vector} \end{matrix}$$

b a

\rightarrow Multiplication
+ Addition.

$b = f(Wa)$ forward.

↓ ↓
Matrix vector

$W_{ij} = W_{ij} + \lambda a_i q_j$ updates

↓ ↴
learning rate Multiplication
 Addition

Add, Mult units	Range
FP32 (full precision)	$10^{-38} \dots 10^{30}$ $\sim 6 \times 10^{15}$
FP16	$6 \times 10^{-5} \dots 6 \times 10^4$ $\sim 0.05\%$
INT32	$2 \times 10^{-9} \quad 0.5$
INT16	$6 \times 10^{-4} \quad 0.5$
INT8	$0 \dots 127 \quad 0.5$

Goal of low-prec arithmetic

Optimize the tradeoff between
prediction accuracy of the network and

$$\text{cost} = f(\text{energy}, \text{runtime}, \text{accuracy})$$

Add in FP32 $\rightarrow 0.9 \text{ pJ}$ $4k^2 \mu\text{m}^2$

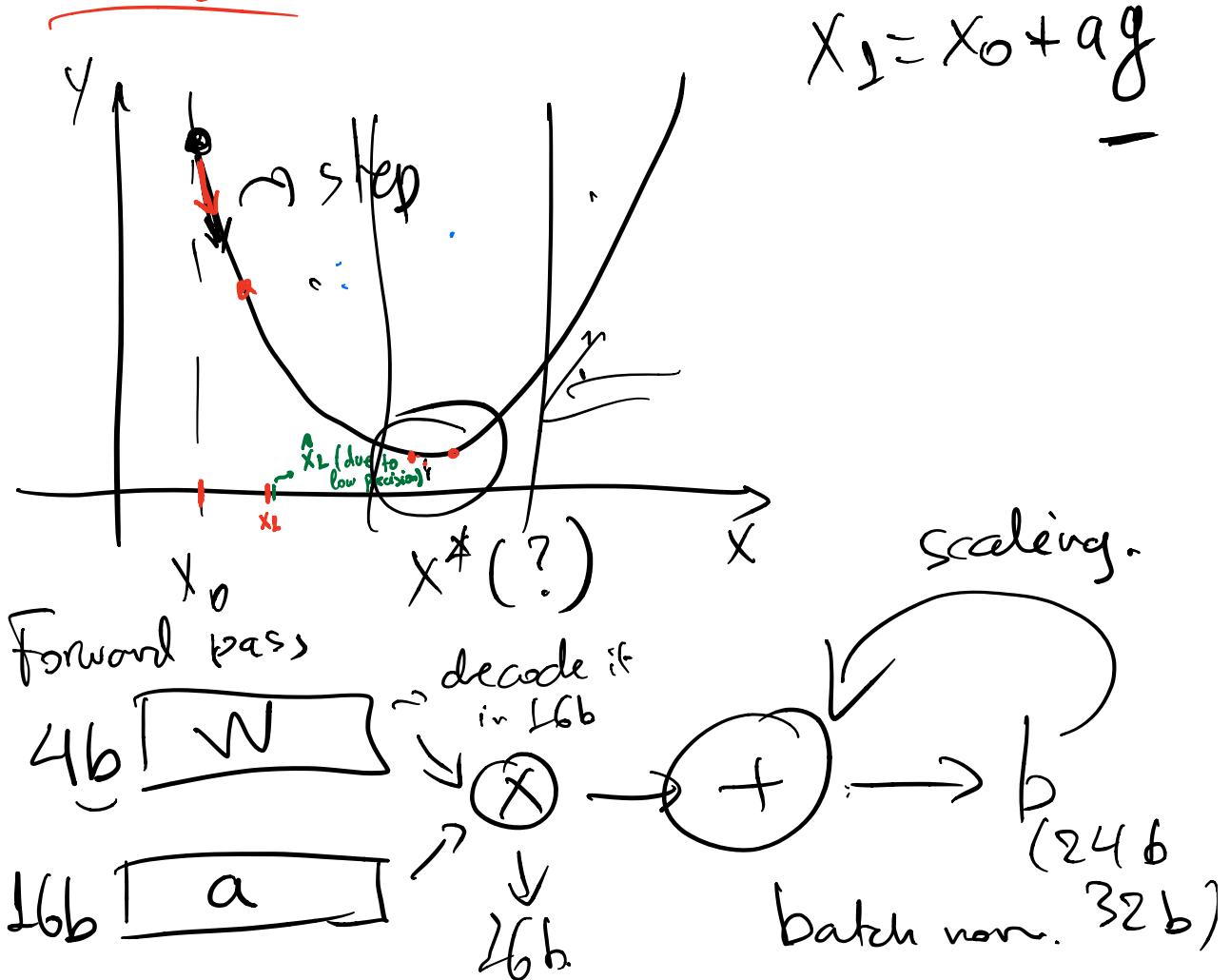
Add in FPL6 $\rightarrow \underline{0.4 \text{ pJ}}$ $1k^2 \mu\text{m}^2$

Mult, Add \rightarrow operations

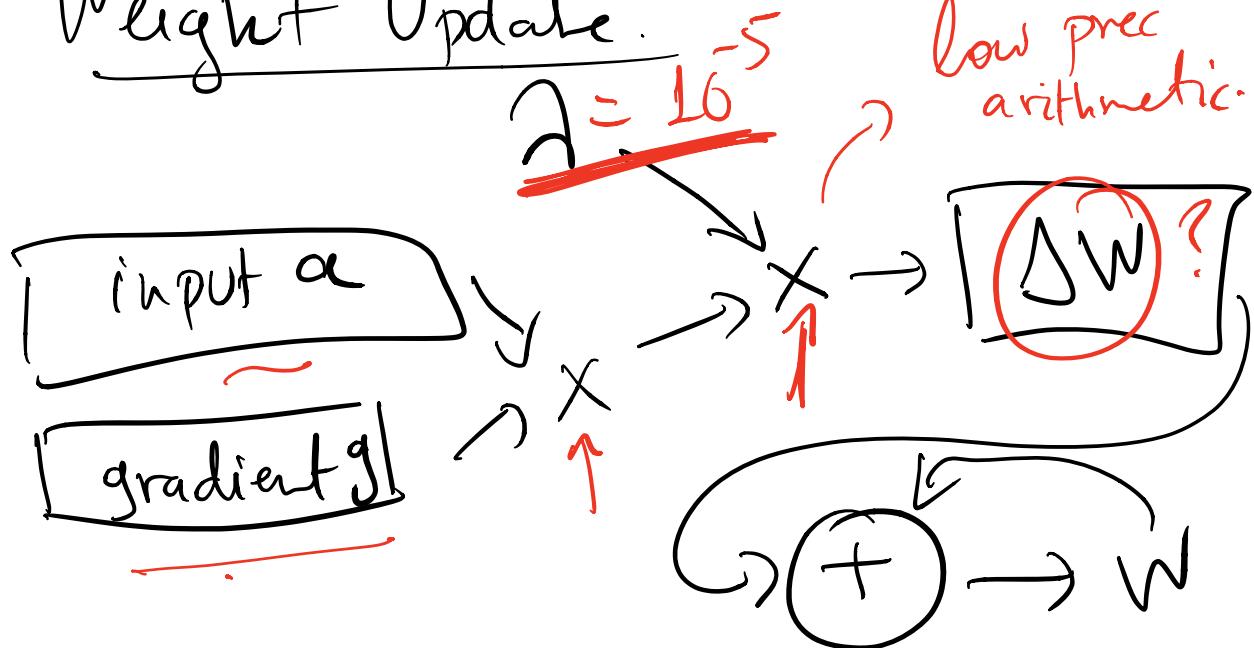
Parameters : { weights, inputs/outputs
either use
1) the same precision
2) mixed precision }
raw data to the intermediate results
gradient, learning rate.

design.

Mixed precision says:
use different arithmetic for
ya inputs / outputs / gradients
weight et.



Weight Update

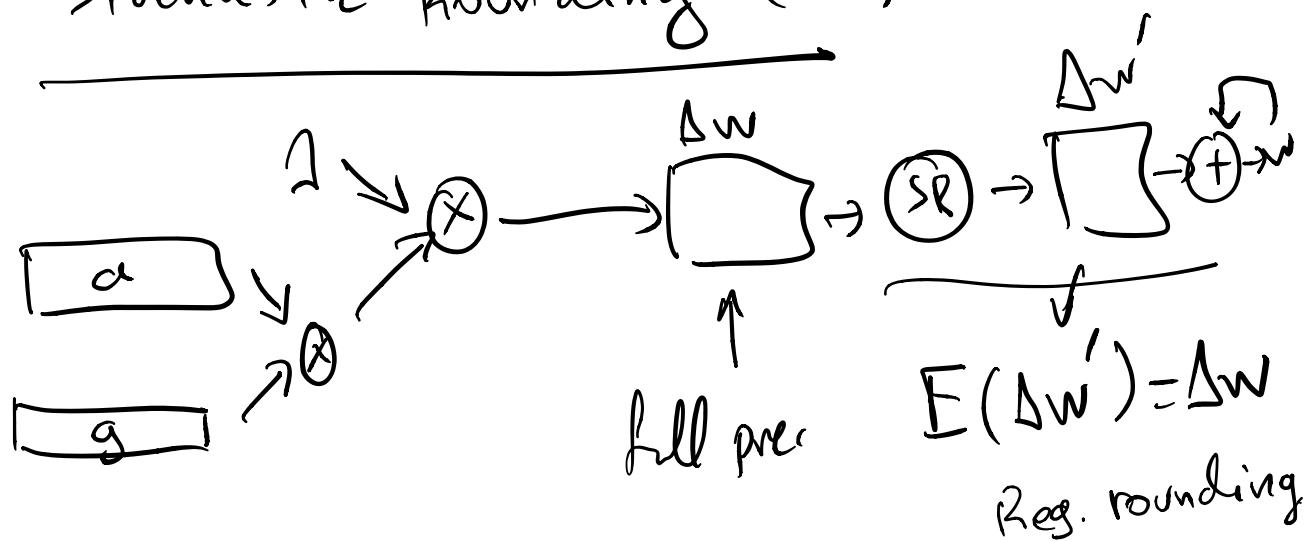


What is the effect of
low precision here (assuming
(quantization / rounding))

10^{-5} ← very low
learning rate.

To avoid $\Delta W = 0$ due to low-prec.

Stochastic Rounding (SR)



I want to add. 0.3 to 0
100 times.

$$0.3 \rightarrow 0$$

$$\underline{0} \neq 30$$

$$\text{Round}(x) = \begin{cases} \lfloor x \rfloor, & \text{w. prob. } 1 - (x - \lfloor x \rfloor) \\ \lfloor x \rfloor + 1, & \text{w. } x - \lfloor x \rfloor \end{cases}$$

$$\text{Round}(0.3) = \begin{cases} 0, & 70\% \\ 1, & 30\% \end{cases} \quad E[\text{Sum}] = 30$$

Chris De Sa ISCA '1f discusses
efficient stochastic rounding schemes

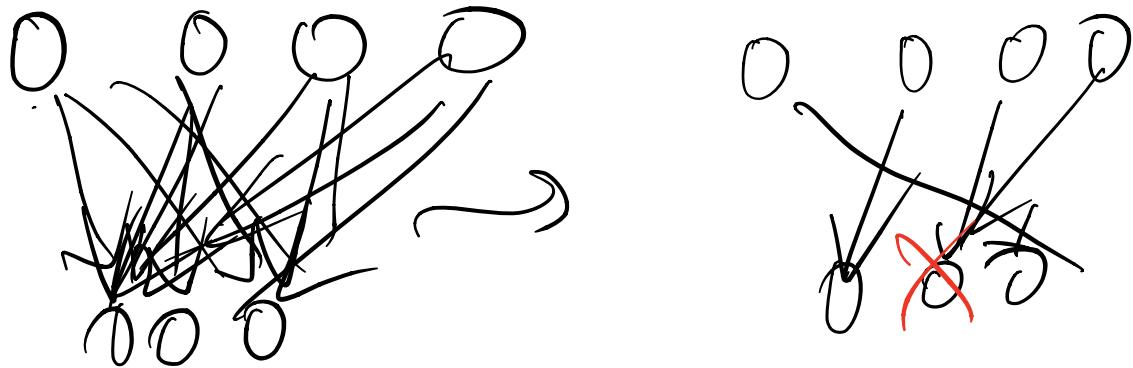
Summary

Reduced prec. → save memory space
bandwidth
→ Important points

High prec → Batch norm → cert.

Stochastic Rounding during upc.

2. Pruning



after training.

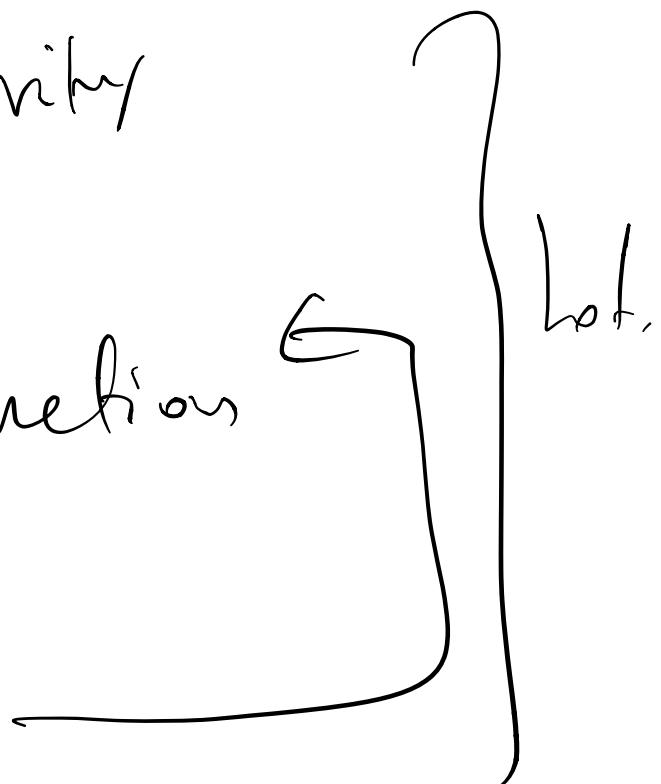
Train w. full
Connectivity



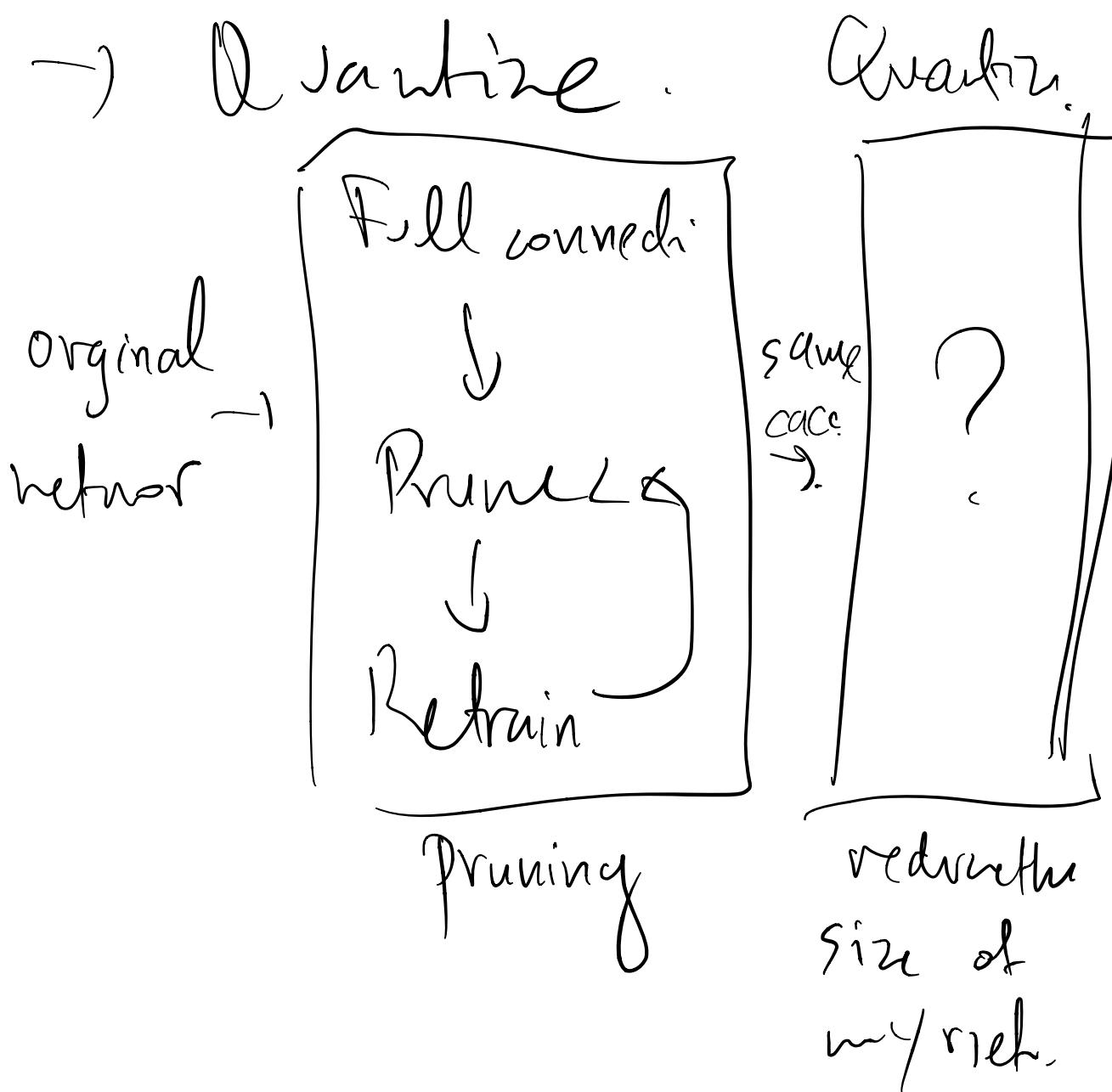
Prune Connections



Retrain



After pruning (whatever params
are left)



Want to group weight n.
similar values into One
weight.

$$\underline{2.09}, \underline{2.12}; \underline{1.92}$$

$$\underline{1.95}$$

assigns these params into
a cluster k + 2.00



avg

$\overline{\overline{\quad}}$

↳ FPL6

4xFP16 vs. 4xint8 + FP16

This requires changing how one performs updates and learning.

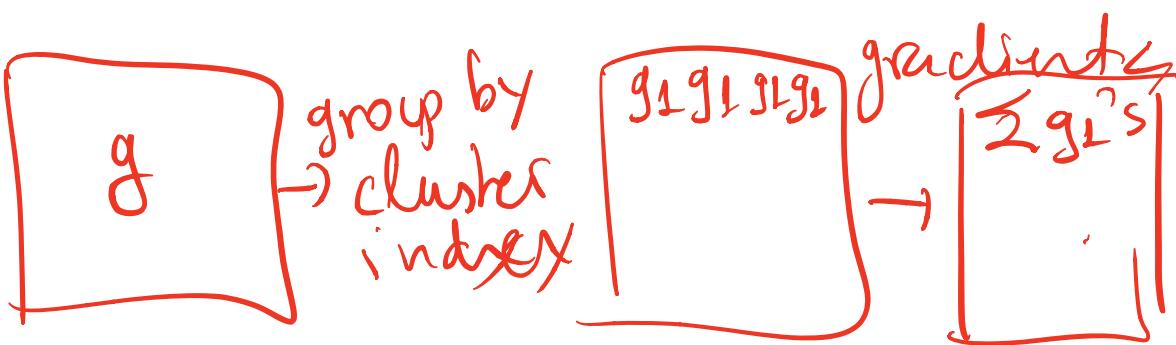
$$\boxed{\text{W Matrix}} = \boxed{\text{W Matrix}} + \lambda \begin{bmatrix} a \\ g \end{bmatrix}$$

$$\boxed{\text{W Matrix}} = \boxed{\frac{\text{int8}}{INT}} \rightarrow k \underbrace{\text{FP16}}$$

cluster index a
 centroids.

Now I only update the cluster.
centroids and the indexes

they don't care about



Some W's are changing frequently

What does it mean that W is changing frequently?

from an opt perspective. (we have not converged)

Freq. weights \rightarrow less bits

infreq. weights \rightarrow increased bits

(Huffman Coding)

