

Parallel Programming

Recitation Session 4

Thomas Weibel <weibelt@ethz.ch>

Laboratory for Software Technology,
Swiss Federal Institute of Technology Zürich

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Executive Summary

- Write parallel MergeSort together
- Parallel MergeSort performance
- Classroom exercise: Parallel Matrix multiplication

Outline

- 1 Parallel MergeSort**
- 2 Performance Measurement
- 3 Parallel Matrix Multiplication

Parallel MergeSort

```
void mergesort (int start, int end) {  
    if (end - start >= 1) {  
        int middle = (start + end) / 2;  
        mergesort(start, middle);  
        mergesort(middle+1, end);  
        merge(start, middle, middle+1, end);  
    }  
}
```

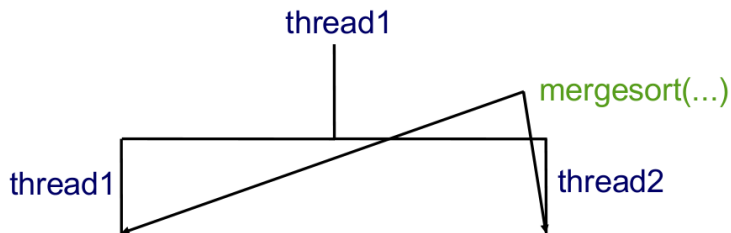
Recursive Thread Creation

```
void mergesort (int start, int end) {  
    if (end - start >= 1) {  
        int middle = (start + end) / 2;  
  
        // thread 1 executes the first mergesort  
        mergesort(start, middle);  
  
        // thread 2 executes the second mergesort  
        mergesort(middle+1, end);  
  
        // join, remaining thread executes merge  
        merge(start, middle, middle+1, end);  
    }  
}
```

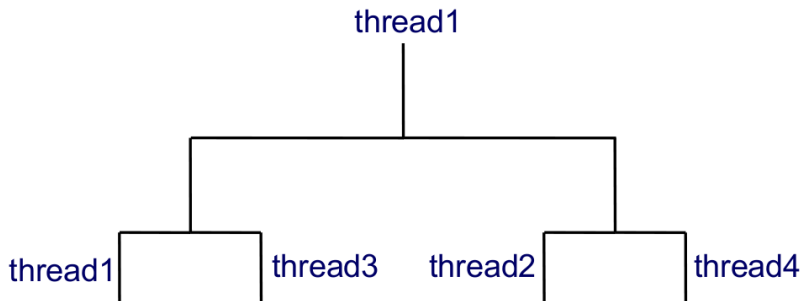
Example: Graph with 4 Threads



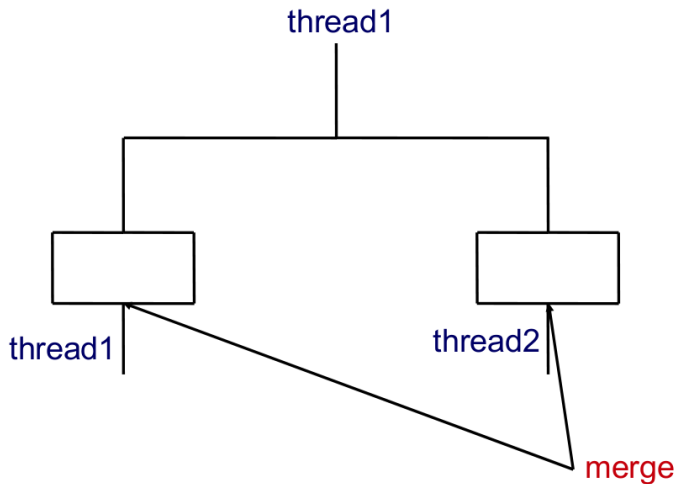
Example: Graph with 4 Threads



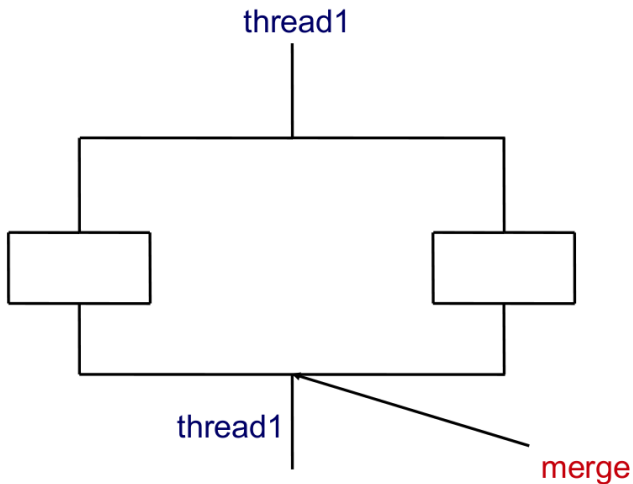
Example: Graph with 4 Threads



Example: Graph with 4 Threads

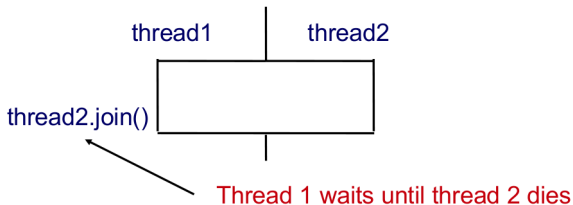


Example: Graph with 4 Threads



Synchronization: Join

- `join()` waits for this thread to die
- Exception: If another thread has interrupted the current thread



Solution

Let's solve it together!

Outline

1 Parallel MergeSort

2 Performance Measurement

3 Parallel Matrix Multiplication

Measurements

```
int_to_sort = createRandIntArray(no_elements);
MTMergeSort m = new MTMergeSort(int_to_sort,
                                no_threads);

// start timing
long start = System.currentTimeMillis();
m.sort();
// stop timing
long stop = System.currentTimeMillis();
long time = stop - start;
```

Extra keys for Java VM:

- -Xms<size>: set initial Java heap size (eg. to 1024M)
- -Xmx<size>: set maximum Java heap size (eg. to 2048M)

Questions

- Is the parallel version faster?
- How many threads give the best performance?
- What is the influence of the CPU model/CPU frequency?



Intel Pentium M @ 1 GHz / 512 MB / XP

Threads	1	2	4	8	16	32	64
100 000	70	70	60	70	70	80	80
10 000 000	9947	10728	10241	10128	10124	-	-

Intel Core2 Duo CPU E8500 @ 3.16GHz / 4 GB / Ubuntu 8.10 x64

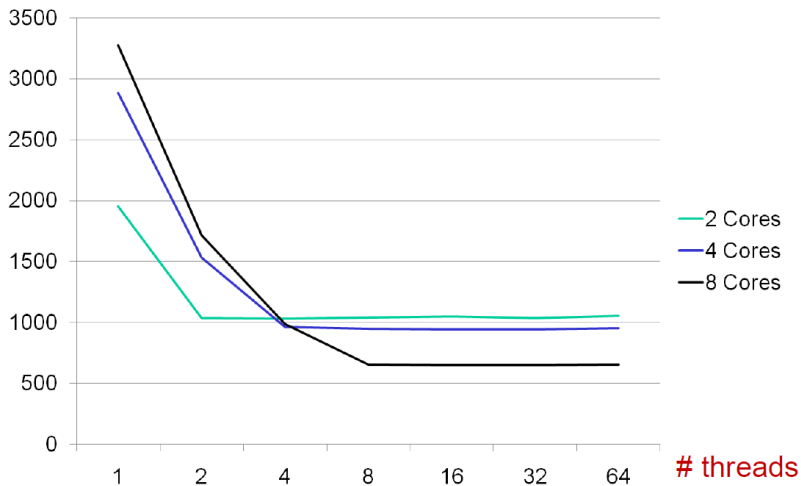
Threads	1	2	4	8	16	32	64
100 000	13	7	7	7	8	10	12
10 000 000	1951	1034	1029	1040	1050	1036	1054

Intel Core2 Quad CPU Q9400 @ 2.66GHz / 4 Gb / 64 bit Vista

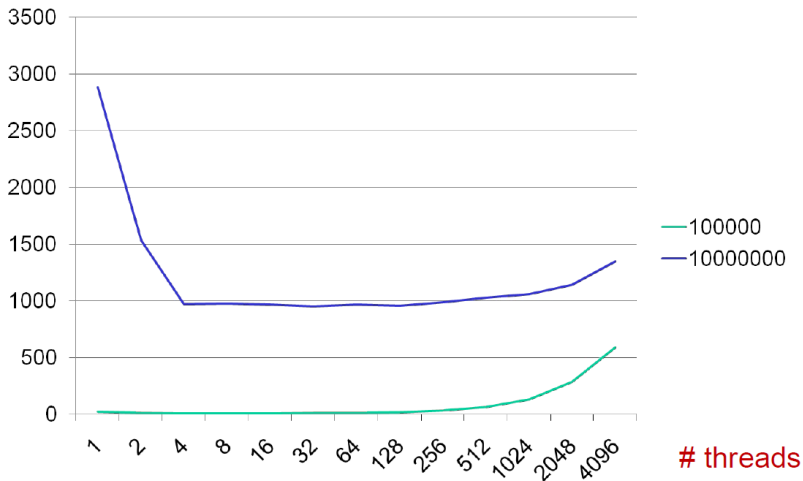
Threads	1	2	4	8	16	32	64
100 000	21	11	7	7	8	9	12
10 000 000	2883	1530	958	946	941	943	950

Intel Xeon 8 Core E5345 @2.33 / 2.47 Gb visible due to 32 bit XP

Threads	1	2	4	8	16	32	64
100 000	15	0	0	0	0	0	0
10 000 000	3276	1718	989	656	650	650	656



Intel Core2 Quad CPU Q9400 @ 2.66GHz / 4 Gb / 64 bit Vista



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- 1 Parallel MergeSort
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- 3 Parallel Matrix Multiplication**

Matrix Multiplication

- Problem: Given two matrices **A**, **B** of size $N \times N$.
- Compute the matrix product **C** = **AB** with

$$C_{ij} = \sum_{k=0}^{N-1} A_{ik} \cdot B_{kj}$$

- **A**, **B** elements are double-precision floating point numbers (`double`)

Dense Matrices

- Assume that **A** and **B** are dense matrices
- Sparse matrices have many zero elements
 - Only the non-zero elements are stored
- Dense matrices have mostly non-zero elements
- Each matrix requires N^2 storage cells

Parallel Matrix Multiplication

Which operations can be done in parallel?



Programming Matrix Multiplication

Java code for the loop nest is easy:

```
double [][] a = new double[N][N];
double [][] b = new double[N][N];
double [][] c = new double[N][N];

for (i=0; i<N; i++) {
    for (j=0; j<N; j++) {
        a[i][j] = rand.nextDouble();
        b[i][j] = rand.nextDouble();
        c[i][j] = 0.0;
    }
}

for (i=0; i<N; i++) {
    for (j=0; j<N; j++) {
        for (k=0; k<N; k++) {
            c[i][j] += a[i][k] * b[k][j];
        }
    }
}
```

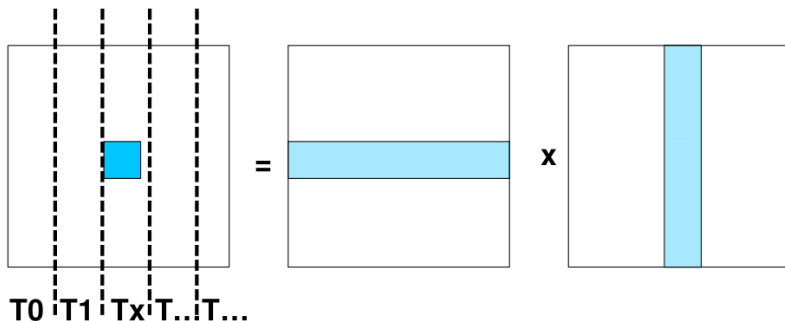
Parallel Matrix Multiplication

- Data partitioning based on
 - Input matrix **A**
 - Input matrix **B**
 - Output matrix **C**
- We assume that all threads can read inputs **A** and **B**
 - Start with partitioning of output matrix **C**
 - No need to use [synchronized](#)!

Parallel Matrix Multiplication

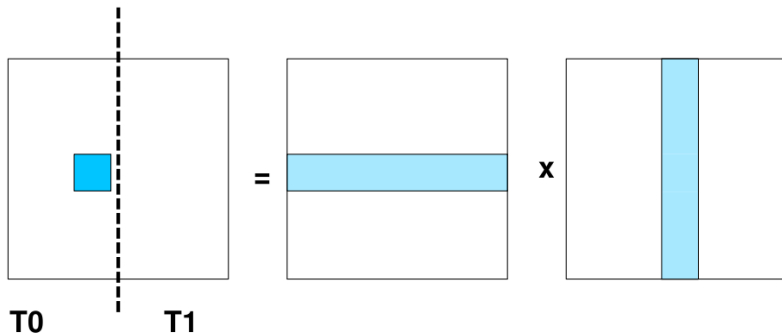
Each thread computes its share of the output **C**

Partition **C** by columns



Two Threads

One thread computes columns $0 \dots \frac{N}{2}$, the other columns $\frac{N}{2} + 1 \dots N - 1$



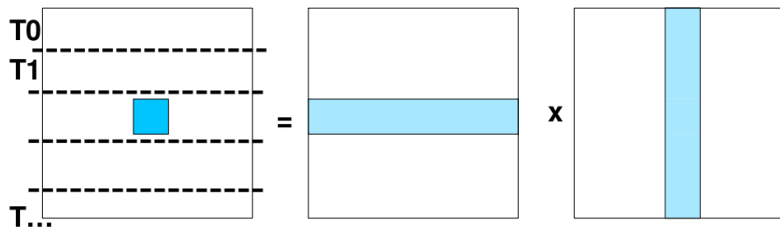
Two Threads

```
// Thread 0
for (i=0; i<N; i++) {
    for (j=0; j<N; j++) {
        for (k=0; k<N/2; k++) {
            c[i][j] += a[i][k] * b[k][j];
        }
    }
}

// Thread 1
for (i=0; i<N; i++) {
    for (j=0; j<N; j++) {
        for (k=N/2; k<N; k++) {
            c[i][j] += a[i][k] * b[k][j];
        }
    }
}
```

Other Aspects

Partition **C** by columns or by rows?



Other Aspects

What should be the order of the loops?

```
for (i=0; i<N; i++) {  
    for (j=0; j<N; j++) {  
        for (k=0; k<N; k++) {  
            c[i][j] += a[i][k] * b[k][j];  
        }  
    }  
}
```

```
for (k=0; k<N; k++) {  
    for (i=0; i<N; i++) {  
        for (j=0; j<N; j++) {  
            c[i][j] += a[i][k] * b[k][j];  
        }  
    }  
}
```

Performance Measurement

Matrix size	Number of threads								
	1	2	4	8	16	32	64	...	1024
100									
200									
...									
10'000									

One Thread per Matrix Element

Classroom exercise

Don't try this at home!



- Threads Require resources
 - Memory for stacks
 - Setup, teardown
- Scheduler overhead
- Worse for short-lived threads

Summary

- Parallel MergeSort
- Performance issues
- Parallel Matrix multiplication



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