Parallel Programming

Recitation Session 6

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Introduction

Executive Summary

- Formalize understanding of mutual exclusion
- Closer look at volatile
- Proof mutual exclusion

Outline

- 1 Volatile
- **2** Mutual Exclusion Proofs

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Parallel Programming
Volatile

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Original Version

```
static int foo;

void bar () {
   foo = 0;
   while (foo != 255)
   ;
}
```

Optimized Version

Compiler will "optimize" the previous version:

```
static int foo;
void bar () {
  foo = 0;
  while (true)
  ;
}
```

⇒ Infinite loop

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Volatile

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Volatile

With volatile the loop condition will not be optimized away:

```
volatile static int foo;
void bar () {
  foo = 0;
  while (foo != 255)
  ;
}
```

The variable is re-read from memory each time it is accessed

Java Language Specification

Volatile

A field may be declared volatile, in which case a thread must reconcile its working copy of the field with the master copy every time it accesses the variable. Moreover, operations on the master copies of one or more volatile variables on behalf of a thread are performed by the main memory in exactly the order that the thread requested.

Source: http://java.sun.com/docs/books/jls/second_edition/html/classes.doc.html#36930

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Mutual Exclusion Proofs

Outline

- 1 Volatile
- **2** Mutual Exclusion Proofs

Classroom Exercise 1

Program for thread A (myid == 0)

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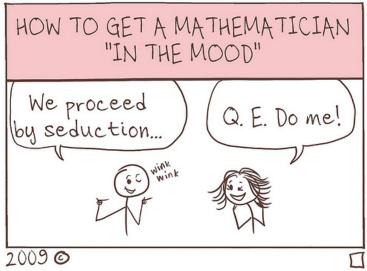
Mutual Exclusion Proofs

Classroom Exercise: PingPong

Program for thread B (myid == 1)

Your Task (Now!)

- Show that these threads will never be both in their critical section at the same time.
- You should prove this property in a manner that's similar to the proof given in class.



Source: http://brownsharpie.courtneygibbons.org/?p=1146

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Mutual Exclusion Proofs

Some thoughts on how to proceed

- We introduced already labels for statements and produced two distinct versions for thread A and thread B.
- Now you should formulate the invariant.

Invariants

- 1 at(A3) \rightarrow turn == 0
- 2 at(B3) \rightarrow turn == 1
- 3 not [at(A3) AND at(B3)]

We use the notation "at(S)" to indicate that execution is "at statement (location) S" \Rightarrow all previous statements have executed while S has not yet started to execute

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Mutual Exclusion Proofs

Proof strategy

- Proof by induction on the execution sequence.
- Base case: does (1) hold at the start of the execution of the program (threads at A1 and B1)?
- Induction step: Assume that (1) holds. Will execution of an additional step invalidate (1)?

Proof (1)

- \blacksquare at(A1): condition (1) is false \Rightarrow do not care about signal
- at(A2): condition (1) is false \Rightarrow do not care about signal
- at(A3): condition (1) is true ⇒ turn == 0, follows from
 the fact that turn was 0 at(A2) and the transition from A2
 → A3 did not change value of turn
- \blacksquare at(A4): condition (1) is false \Rightarrow do not care about turn

Now, we consider:

- at(B1): no change to turn
- at(B2): no change to turn
- at(B3): no change to turn
- at(B4): changes turn to 0
- \Rightarrow Invariant (1) is true

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Mutual Exclusion Proofs

Proof (2)

Same way. Please do it if you had trouble with proof of (1).

Proof (3): Proof by induction

Induction start trivial

Proof of induction step by contradiction:

- Assume thread A entered CS (A3) at time t1
- Assume thread B entered CS (B3) at time t2, where $t2 = t1 + \delta$
- \rightarrow Contradiction: since we are in A3 signal must be 0 (cannot be 0 and 1 at the same time)
 - Assume thread B entered CS (B3) at time t1
 - Assume thread A entered CS (A3) at time t2, where $t2 = t1 + \delta$
- \rightarrow Contradiction: since we are in B3 signal must be 1 (cannot be 0 and 1 at the same time)

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Mutual Exclusion Proofs

Classroom Exercise 2: Based on 3rd Variation

```
class Turn {
    // 0 : wants to enter exclusive section
    // 1 : does not want to enter...
    private volatile int flag = 1;

    void request() {
        flag = 0;
    }

    void free() {
        flag = 1;
    }

    int read() {
        return flag;
    }
}
```

Worker

```
class Worker implements Runnable {
    private int myid;
    private Turn mysignal;
    private Turn othersignal;
    Worker(int id, Turn t0, Turn t1) {
        myid = id;
        mysignal = t0;
        othersignal = t1;
    public void run() {
        while (true) {
            mysignal.request();
            while (true) {
                if (othersignal.read() == 1) break;
            // critical section
            mysignal.free();
        }
    }
}
```

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Mutual Exclusion Proofs

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Worker 0

```
public void run() {
    while (true) {
A1:
A2:
        s0.request();
        while (true) {
A3:
            if (s1.read() == 1)
                break;
        }
        // critical section
A4:
       s0.free();
A5:
    }
}
```

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Mutual Exclusion Proofs

Worker 1

```
public void run() {
    while (true) {
B1:
        s1.request();
B2:
        while (true) {
B3:
             if (s0.read() == 1)
                 break;
        }
        // critical section
B4:
        s1.free();
B5:
    }
}
```

Mutual exclusion

Show that this solution provides mutual exclusion.

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Mutual Exclusion Proofs

Invariants

```
1 s0.flag == 0 equivalent to
  (at(A3) \( \text{ at(A4)} \( \text{ v at(A5)} \)
```

3 not $(at(A4) \land at(B4))$

Induction

Show with induction that (1), (2), and (3) hold.

At the start, s0.flag == 1 and at(A1) \Rightarrow OK

Induction step: assume (1) is true. Consider all possible moves

- \blacksquare A1 \rightarrow A2
- \blacksquare A2 \rightarrow A3
- \blacksquare A3 \rightarrow A3
- \blacksquare A3 \rightarrow A4
- \blacksquare A4 \rightarrow A5
- \blacksquare A5 \rightarrow A1

Let's look at them one by one:

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Mutual Exclusion Proofs

Induction Step

- A1 \rightarrow A2: no effect on (1) \Rightarrow OK
- A2 \rightarrow A3: (1) holds (s0.flag == 0 and at(A3)) \Rightarrow OK
- A3 \rightarrow A3: (1) holds, no change to s0.flag, at(A3) \Rightarrow OK
- A3 \rightarrow A4: (1) holds, no change to s0.flag, at(A4) \Rightarrow OK
- A4 \rightarrow A5: (1) holds, no change to s0.flag, at(A5) \Rightarrow OK
- A5 \rightarrow A1: (1) holds, s0.flag == 1 and at(A1) \Rightarrow OK

Note that the " \Rightarrow OK" is based on the observation that no action by Thread Worker 1 will have any effect on s0.flag

 \Rightarrow So (1) holds.

Your turn

Show that (2) holds as well.

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Mutual Exclusion Proofs

Proving (3)

Proof by induction

At the start, at(A1) and at(B1), so (3) holds.

Induction step: assume (3) holds and consider possible transitions.

Assume at (A4) and consider B3 \rightarrow B4 (while Worker0 remains at A4!) \Rightarrow no other transition is relevant or possible

But since s0.flag==0 (because of (1)), a transition B3 \rightarrow B4 is not possible, so (3) remains true.

Proving (3)

Same argument applies if we start with the assumption at (B4).

So no transition will violate (3).

Of course this proof sketch depends on the fact that

- no action of WorkerO will modify any of the states of Worker1, and
- no action of Worker1 will modify any of the states of Worker0

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Parallel Programming Outro

Summary

- Mutual exclusion
- Volatile in Java
- Proofs for mutual exclusion
 - Try to solve assignment 6 there will be at least one proof at the exam



