Parallel Programming

Recitation Session 4

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Introduction

Executive Summary

- Write parallel MergeSort together
- Parallel MergeSort performance
- Classroom exercise: Parallel Matrix multiplication

Outline

- 1 Parallel MergeSort
- **2** Performance Measurement
- 3 Parallel Matrix Multiplication

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Parallel Programming

Parallel MergeSort

Parallel MergeSort

```
void mergesort (int start, int end) {
  if (end - start >= 1) {
    int middle = (start + end) / 2;
    mergesort(start, middle);
    mergesort(middle+1, end);
    merge(start, middle, middle+1, end);
}
```

,

Recursive Thread Creation

```
void mergesort (int start, int end) {
  if (end - start >= 1) {
    int middle = (start + end) / 2;

    // thread 1 executes the first mergesort
    mergesort(start, middle);

    // thread 2 executes the second mergesort
    mergesort(middle+1, end);

    // join, remaining thread executes merge
    merge(start, middle, middle+1, end);
}
```

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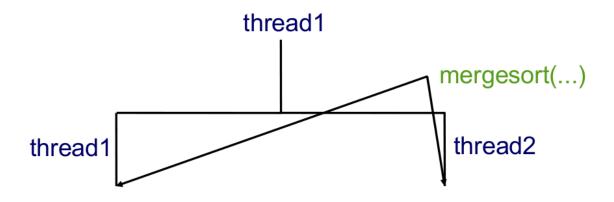
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Parallel MergeSort

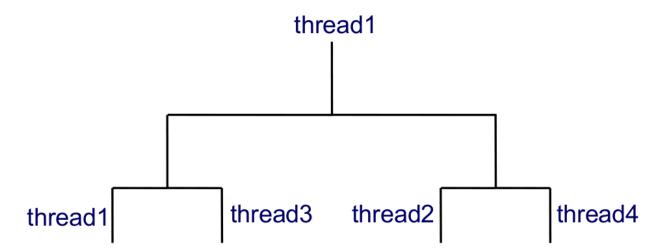
Example: Graph with 4 Threads



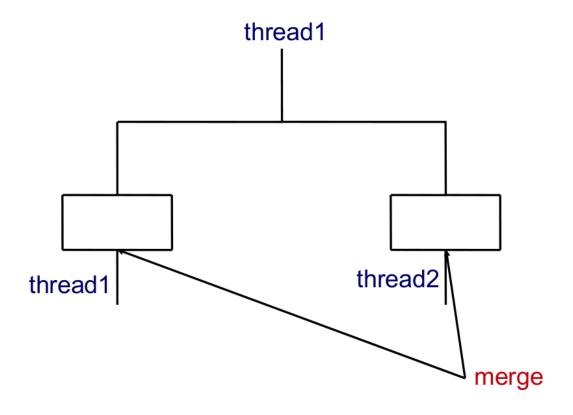
Example: Graph with 4 Threads



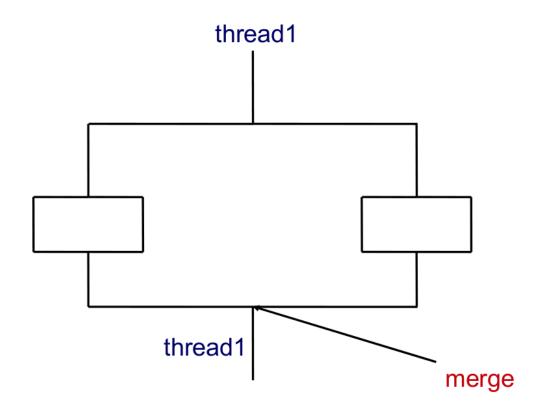




Example: Graph with 4 Threads

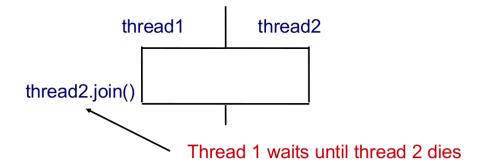






Synchronization: Join

- join() waits for this thread to die
- Exception: If another thread has interrupted the current thread



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Solution

Let's solve it together!

Outline

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Performance Measurement

Measurements

Extra keys for Java VM:

- -Xms<size>: set initial Java heap size (eg. to 1024M)
- -Xmx<size>: set maximum Java heap size (eg. to 2048M)

Questions

- Is the parallel version faster?
- How many threads give the best performance?
- What is the influence of the CPU model/CPU frequency?



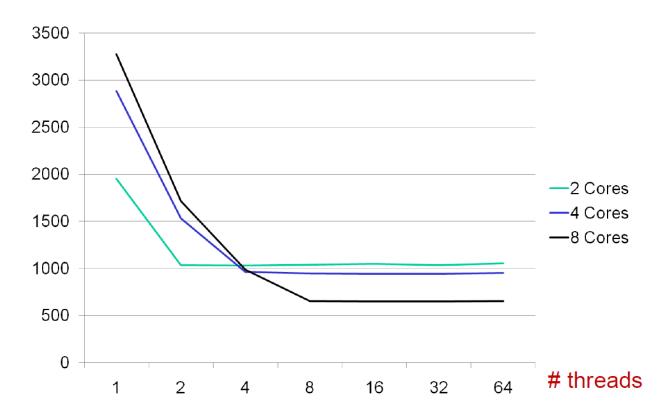
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Performance Measurement Results

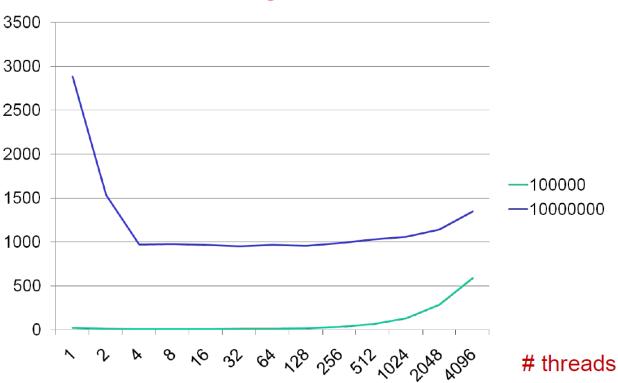
Intel Pentium M @ 1 GHz / 512 MB / XP

	$\overline{}$										
Threads	1	2	4	8	16	32	64				
100 000	70	70	60	70	70	80	80				
10 000 000	9947	10728	10241	10128	10124	-	-				
Intel Core2 Duo CPU E8500 @ 3.16GHz / 4 GB / Ubuntu 8.10 x64											
Threads	1	2	4	8	16	32	64				
100 000	13	7	7	7	8	10	12				
10 000 000	1951	1034	1029	1040	1050	1036	1054				
Intel Core2 Quad CPU Q9400 @ 2.66GHz / 4 Gb / 64 bit Vista											
Threads	1	2	4	8	16	32	64				
100 000	21	11	7	7	8	9	12				
10 000 000	2883	1530	958	946	941	943	950				
Intel Xeon 8 Core E5345 @2.33 / 2.47 Gb visible due to 32 bit XP											
Threads	1	2	4	8	16	32	64				
100 000	15	0	0	0	0	0	0				
10 000 000	3276	1718	989	656	650	650	656				



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Performance Measurement More Threads

Intel Core2 Quad CPU Q9400 @ 2.66GHz / 4 Gb / 64 bit Vista



Outline

- 1 Parallel MergeSort
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Parallel Matrix Multiplication

Matrix Multiplication

- Problem: Given two matrices **A**, **B** of size $N \times N$.
- Compute the matrix product C = AB with

$$\mathbf{C}_{ij} = \sum_{k=0}^{N-1} \mathbf{A}_{ik} \cdot \mathbf{B}_{kj}$$

■ A, B elements are double-precision floating point numbers (double)

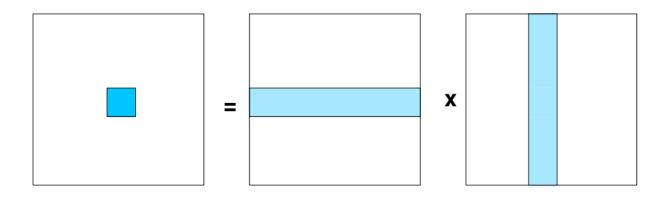
Dense Matrices

- Assume that A and B are dense matrices
- Sparse matrices have many zero elements
 - Only the non-zero elements are stored
- Dense matrices have mostly non-zero elements
- Each matrix requires N^2 storage cells

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Parallel Matrix Multiplication

Parallel Matrix Multiplication

Which operations can be done in parallel?



Programming Matrix Multiplication

Java code for the loop nest is easy:

```
double[][] a = new double[N][N];
double[][] b = new double[N][N];
double[][] c = new double[N][N];
for (i=0; i<N; i++) {</pre>
  for (j=0; j<N; j++) {</pre>
    a[i][j] = rand.nextDouble();
    b[i][j] = rand.nextDouble();
    c[i][j] = 0.0;
  }
}
for (i=0; i<N; i++) {</pre>
  for (j=0; j<N; j++) {</pre>
    for (k=0; k<N; k++) {</pre>
      c[i][j] += a[i][k] * b[k][j];
  }
}
```

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Parallel Matrix Multiplication

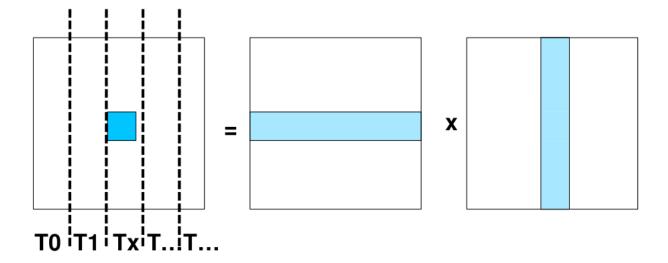
Parallel Matrix Multiplication

- Data partitioning based on
 - Input matrix A
 - Input matrix B
 - Output matrix C
- We assume that all threads can read inputs **A** and **B**
 - Start with partitioning of output matrix **C**
 - No need to use synchronized!

Parallel Matrix Multiplication

Each thread computes its share of the output C

Partition **C** by columns



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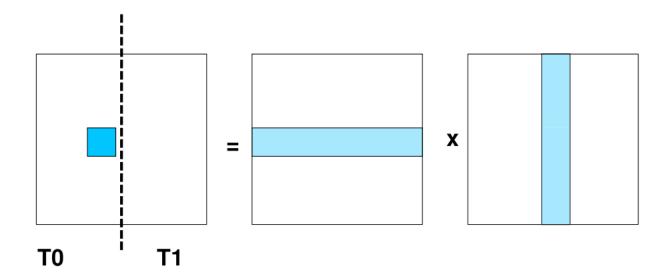
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Parallel Matrix Multiplication

Two Threads

One thread computes columns $0\dots\frac{N}{2},$ the other columns $\frac{N}{2}+1\dots N-1$



Two Threads

```
// Thread 0
for (i=0; i<N; i++) {
   for (j=0; j<N; j++) {
      for (k=0; k<N/2; k++) {
        c[i][j] += a[i][k] * b[k][j];
      }
   }
}

// Thread 1
for (i=0; i<N; i++) {
   for (j=0; j<N; j++) {
      for (k=N/2; k<N; k++) {
        c[i][j] += a[i][k] * b[k][j];
      }
   }
}</pre>
```

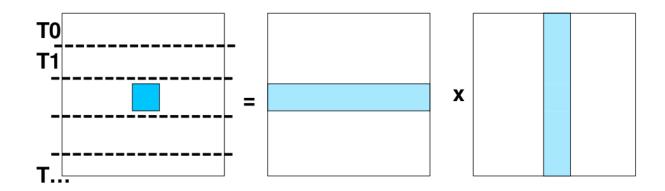
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Parallel Matrix Multiplication

Other Aspects

Partition **C** by columns or by rows?



2-

Other Aspects

What should be the order of the loops?

```
for (i=0; i<N; i++) {
   for (j=0; j<N; j++) {
     for (k=0; k<N; k++) {
      c[i][j] += a[i][k] * b[k][j];
     }
}

for (k=0; i<N; i++) {
   for (i=0; j<N; j++) {
     for (j=0; k<N; k++) {
      c[i][j] += a[i][k] * b[k][j];
     }
}</pre>
```

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Parallel Matrix Multiplication

Performance Measurement

	Number of threads									
Matrix size	1	2	4	8	16	32	64		1024	
100										
200										
10'000										

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One Thread per Matrix Element

Classroom exercise

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Parallel Matrix Multiplication

Don't try this at home!



- Threads Require resources
 - Memory for stacks
 - Setup, teardown
- Scheduler overhead
- Worse for short-lived threads

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Summary

- Parallel MergeSort
- Performance issues
- Parallel Matrix multiplication



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