Executive Summary

Parallel Programming

Recitation Session 6

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Volatile

- Formalize understanding of mutual exclusion
- Closer look at volatile
- Proof mutual exclusion

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Volatile

Outline

Original Version

```
1 Volatile
```

2 Mutual Exclusion Proofs

```
static int foo;

void bar () {
   foo = 0;
   while (foo != 255)
   ;
}
```

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Volatile Volatile

Optimized Version

Volatile

Compiler will "optimize" the previous version:

```
static int foo;
void bar () {
  foo = 0;
  while (true)
  ;
}
```

 \Rightarrow Infinite loop

With volatile the loop condition will not be optimized away:

```
volatile static int foo;

void bar () {
  foo = 0;
  while (foo != 255)
  ;
}
```

The variable is re-read from memory each time it is accessed

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Mutual Exclusion Proofs

Java Language Specification

Outline

Volatile

A field may be declared volatile, in which case a thread must reconcile its working copy of the field with the master copy every time it accesses the variable. Moreover, operations on the master copies of one or more volatile variables on behalf of a thread are performed by the main memory in exactly the order that the thread requested.

Source: http://java.sun.com/docs/books/jls/second_edition/html/classes.doc.html#36930

1 Volatile

2 Mutual Exclusion Proofs

Mutual Exclusion Proofs Mutual Exclusion Proofs

Classroom Exercise 1

Program for thread A (myid == 0)

Classroom Exercise: PingPong

// Thread A public void run() { while (true) { A1: non_critical section while (!(signal.turn == 0)) {} A2: // critical_section A3: signal.turn = 1; A4: }

```
Program for thread B (myid == 1)
// Thread B
public void run() {
    while (true) {
B1:
        non_critical section
        while (!(signal.turn == 1)) {}
B2:
        // critical_section
B3:
        signal.turn = 0;
B4:
}
```

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Parallel Programming Mutual Exclusion Proofs

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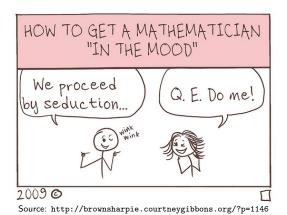
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Mutual Exclusion Proofs

Your Task (Now!)

■ Show that these threads will never be both in their critical section at the same time.

■ You should prove this property in a manner that's similar to the proof given in class.



Some thoughts on how to proceed

- We introduced already labels for statements and produced two distinct versions for thread A and thread B.
- Now you should formulate the invariant.

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Invariants

Proof strategy

- 11 at(A3) \rightarrow turn == 0
- 2 at(B3) \rightarrow turn == 1
- 3 not [at(A3) AND at(B3)]

Mutual Exclusion Proofs

We use the notation "at(S)" to indicate that execution is "at statement (location) S" \Rightarrow all previous statements have executed while S has not yet started to execute

- Proof by induction on the execution sequence.
- Base case: does (1) hold at the start of the execution of the program (threads at A1 and B1)?
- Induction step: Assume that (1) holds. Will execution of an additional step invalidate (1)?

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Proof (1)			Proof (2)			

- at(A1): condition (1) is false \Rightarrow do not care about signal
- at(A2): condition (1) is false \Rightarrow do not care about signal
- at(A3): condition (1) is true ⇒ turn == 0, follows from the fact that turn was 0 at(A2) and the transition from A2 → A3 did not change value of turn
- at(A4): condition (1) is false \Rightarrow do not care about turn

Now, we consider:

- at(B1): no change to turn
- at(B2): no change to turn
- at(B3): no change to turn
- at(B4): changes turn to 0
- \Rightarrow Invariant (1) is true

Same way. Please do it if you had trouble with proof of (1).

Mutual Exclusion Proofs Mutual Exclusion Proofs

Proof (3): Proof by induction

Induction start trivial

Proof of induction step by contradiction:

- Assume thread A entered CS (A3) at time t1
- Assume thread B entered CS (B3) at time t2, where $t2 = t1 + \delta$
- \rightarrow Contradiction: since we are in A3 signal must be 0 (cannot be 0 and 1 at the same time)
 - Assume thread B entered CS (B3) at time t1
 - Assume thread A entered CS (A3) at time t2, where $t2 = t1 + \delta$
- \rightarrow Contradiction: since we are in B3 signal must be 1 (cannot be 0 and 1 at the same time)

```
Classroom Exercise 2: Based on 3rd Variation
```

```
class Turn {
    // 0 : wants to enter exclusive section
    // 1 : does not want to enter...
    private volatile int flag = 1;

    void request() {
        flag = 0;
    }

    void free() {
        flag = 1;
    }

    int read() {
        return flag;
    }
}
```

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Mutual Exclusion Proofs

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Mutual Exclusion Proofs

Worker

Master

```
class Worker implements Runnable {
    private int myid;
    private Turn mysignal;
    private Turn othersignal;
    Worker(int id, Turn t0, Turn t1) {
        mvid = id;
        mysignal = t0;
        othersignal = t1;
    public void run() {
        while (true) {
            mysignal.request();
            while (true) {
                if (othersignal.read() == 1) break;
            // critical section
            mysignal.free();
        }
}
```

Mutual Exclusion Proofs

Worker 0

Worker 1

```
public void run() {
    while (true) {
A1:
A2:
        s0.request();
A3:
        while (true) {
            if (s1.read() == 1)
                 break;
        }
        // critical section
A4:
A5:
        s0.free();
}
```

Mutual Exclusion Proofs

```
public void run() {
    while (true) {
B1:
B2:
        s1.request();
B3:
        while (true) {
            if (s0.read() == 1)
                break;
        // critical section
B4:
        s1.free();
B5:
}
```

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Parallel Programming Mutual Exclusion Proofs

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Mutual Exclusion Proofs

Mutual exclusion

Invariants

Show that this solution provides mutual exclusion.

```
1 s0.flag == 0 equivalent to
   (at(A3) \lor at(A4) \lor at(A5))
2 s1.flag == 0 equivalent to
   (at(B3) \lor at(B4) \lor at(B5))
\blacksquare not (at(A4) \land at(B4))
```

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Induction

Induction Step

Show with induction that (1), (2), and (3) hold.

Mutual Exclusion Proofs

At the start, s0.flag == 1 and at(A1) \Rightarrow OK

Induction step: assume (1) is true. Consider all possible moves

- \blacksquare A1 \rightarrow A2
- \blacksquare A2 \rightarrow A3
- \blacksquare A3 \rightarrow A3
- \blacksquare A3 \rightarrow A4
- \blacksquare A4 \rightarrow A5
- \blacksquare A5 \rightarrow A1

Let's look at them one by one:

■ A1	\rightarrow	A2:	no	effect	on	$(1) \Rightarrow OK$
------	---------------	-----	----	--------	----	----------------------

- A2 \rightarrow A3: (1) holds (s0.flag == 0 and at(A3)) \Rightarrow OK
- A3 \rightarrow A3: (1) holds, no change to s0.flag, at(A3) \Rightarrow OK
- A3 \rightarrow A4: (1) holds, no change to s0.flag, at(A4) \Rightarrow OK
- A4 \rightarrow A5: (1) holds, no change to s0.flag, at (A5) \Rightarrow OK
- A5 \rightarrow A1: (1) holds, s0.flag == 1 and at(A1) \Rightarrow OK

Note that the " \Rightarrow OK" is based on the observation that no action by Thread Worker 1 will have any effect on s0.flag

 \Rightarrow So (1) holds.

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Mutual Exclusion Proofs			Mutual Exclusion Proofs			
Your turn			Proving (3)			

Show that (2) holds as well.

Proof by induction

At the start, at (A1) and at (B1), so (3) holds.

Induction step: assume (3) holds and consider possible transitions.

Assume at (A4) and consider B3 \rightarrow B4 (while Worker0 remains at A4!)

 \Rightarrow no other transition is relevant or possible

But since s0.flag==0 (because of (1)), a transition B3 \rightarrow B4 is not possible, so (3) remains true.

Mutual Exclusion Proofs Outro

Proving (3)

Same argument applies if we start with the assumption at (B4).

So no transition will violate (3).

Of course this proof sketch depends on the fact that

- no action of WorkerO will modify any of the states of Worker1, and
- no action of Worker1 will modify any of the states of Worker0

Summary

- Mutual exclusion
- Volatile in Java
- Proofs for mutual exclusion
 - Try to solve assignment 6 there will be at least one proof at the exam



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20