

Subregular Syntax

The What, How, and Why

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the slides here
under “News”

A Mathematical Distinctness Theorem

- ▶ From a computational perspective, there is a split between “P-side” and “S-side”.

regular < context-free < mildly context-sensitive < ...

Phonology

Morphology

Syntax

- ▶ Matches linguistic practice (despite attempts at unification, e.g. DM)
- ▶ Why is syntax the outlier?

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Karttunen et al. (1992)

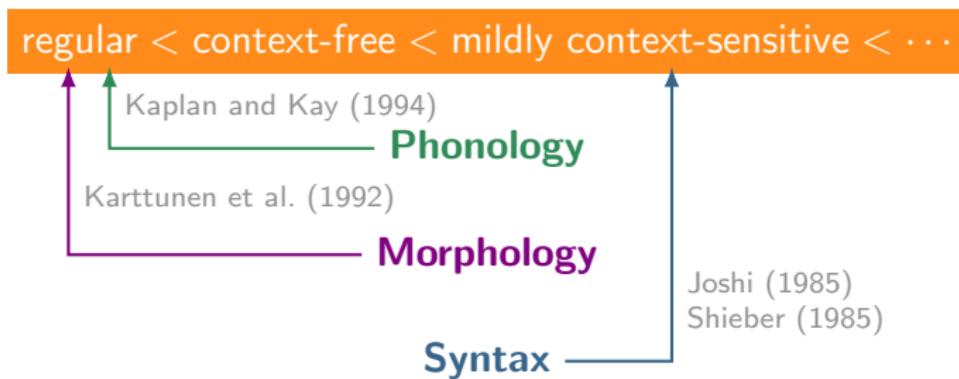
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An Alternative: Simple Syntax

- ▶ The postulated split is misleading.
- ▶ If we probe deeper, we find that
 - ▶ syntax is just as simple,
 - ▶ phonology, morphology, and syntax are weaker than regular ⇒ **subregular**
 - ▶ relativized locality plays a major role,
 - ▶ and is approximated by the formal class **TSL**.
- ▶ This has repercussions for
 - ▶ cognitive architecture of language,
 - ▶ learning,
 - ▶ processing.

Outline

1 Locality and Tiers in Phonology

- Tier-Based Strictly Local (TSL)
- The Cognitive Picture

2 c-Command Constraints in Syntax

- c-Strings
- The Cognitive Picture

3 Syntax

- Minimalist Grammars
- Merge is TSL
- Move is TSL

The Subregular Program

- ▶ **Received view:** class of regular (= finite-state) string languages maximally complex
- ▶ **Subregular hierarchy:** even weaker/simpler subclasses
- ▶ The **tier-based strictly local (TSL)** languages have emerged as particularly important.



**Jeff
Heinz**



**Jane
Chandlee**



**Adam
Jardine**



**Kevin
McMullin**

Example: Word-Final Devoicing

- ▶ Captured by forbidding voiced segments at the end of a word
 - ▶ **German:** Don't have **z\$** or **v\$** or **d\$** (where **\$** = word edge).

* \$ r a d \$

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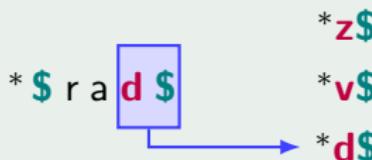
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 - ▶ $[-\text{voice}] = \{\text{s}, \text{f}\}$
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A Problem: Samala Sibilant Harmony

- ▶ If multiple sibilants occur in the same word, they must all be +anterior (**s,z**) or –anterior (**ʃ,ʒ**).
- ▶ In other words: Don't mix **purple** and **teal**.

***sʃ** ***sʒ** ***zʃ** ***zʒ**
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- ▶ **But:** Sibilants can be arbitrarily far away from each other!

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Making Long-Distance Dependencies Local

- ▶ Let's take a clue from phonology:
create locality with **tiers**.
(Goldsmith 1985; Heinz et al. 2011)
- ▶ Enforce constraints on tier,
rather than string



Jeff Heinz

Example: Samala Revisited

- 1 Project sibilant tier
- 2 $*\text{s}\text{ʃ}$, $*\text{s}\text{ʒ}$, $*\text{z}\text{ʃ}$, $*\text{z}\text{ʒ}$, $*\text{ʃ}\text{s}$, $*\text{ʒ}\text{s}$, $*\text{ʃ}\text{z}$, $*\text{ʒ}\text{z}$

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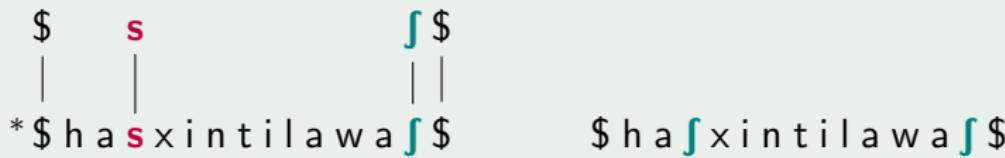


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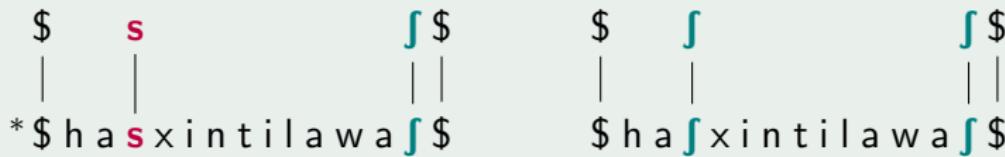


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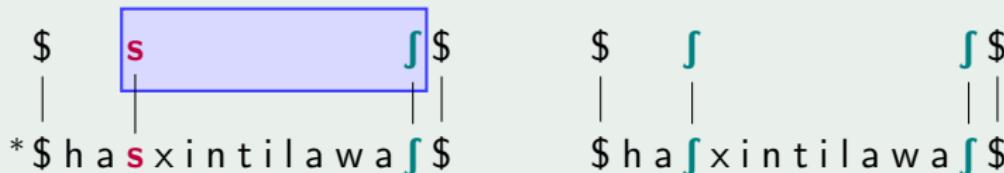


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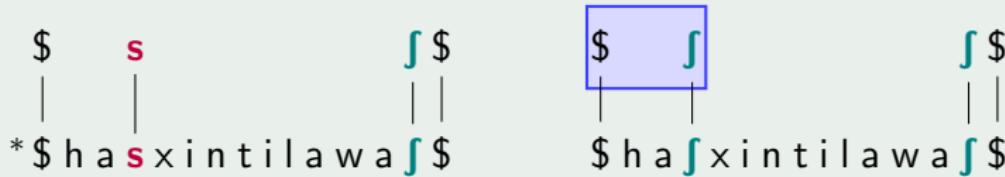


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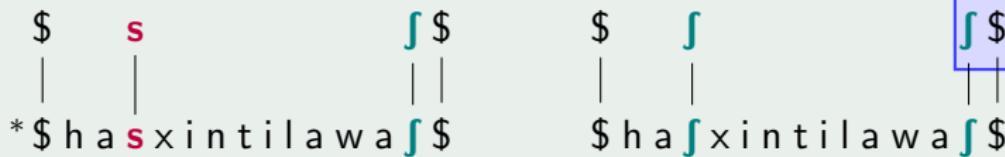


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Tier projection controlled by

- 1 label of segment
- 2 local context
- 3 symbols already on tier

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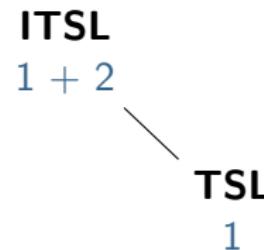
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TSL
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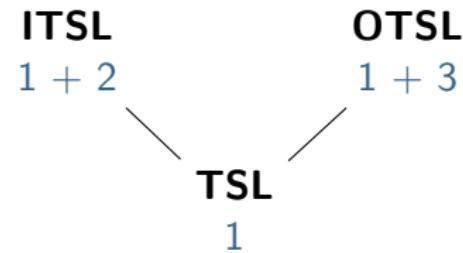
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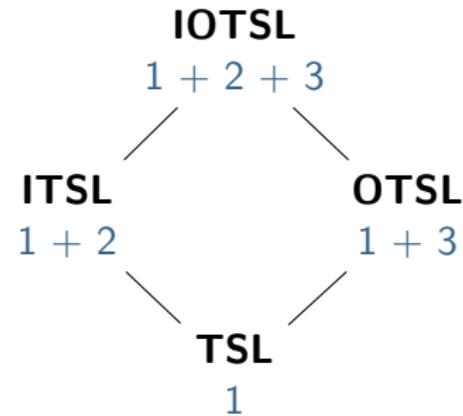
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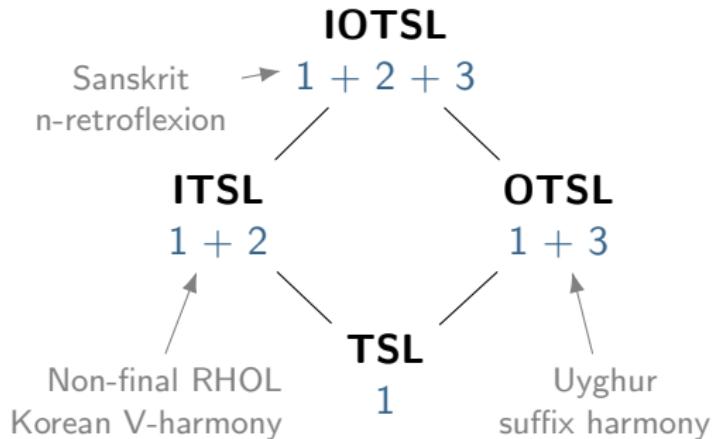
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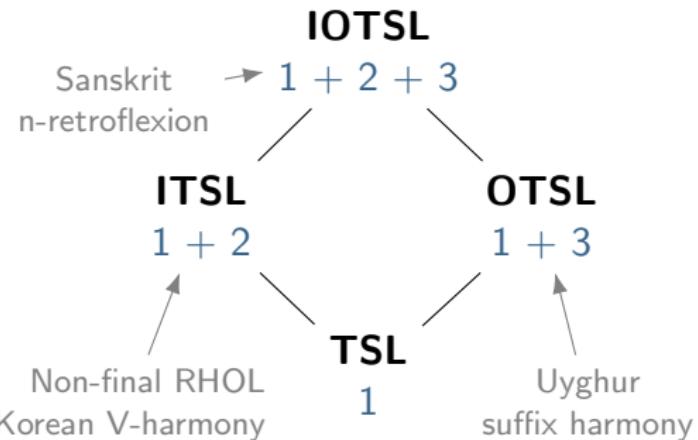
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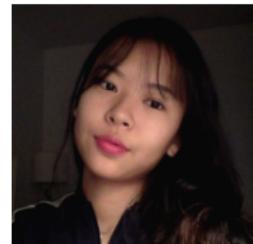
Hyunah
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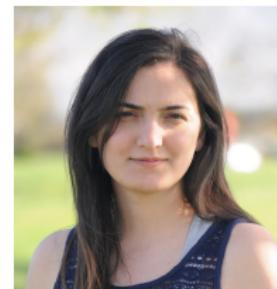
Suji
Yang

TSL Across Language Modules

- ▶ Phonological dependencies fall within the TSL region.
- ▶ Morphological dependencies do, too.
(Aksënova et al. 2016; Aksënova and De Santo 2017;
Chandlee 2017)
- ▶ Phonology and morphology are **computationally similar**.



Alëna
Aksënova

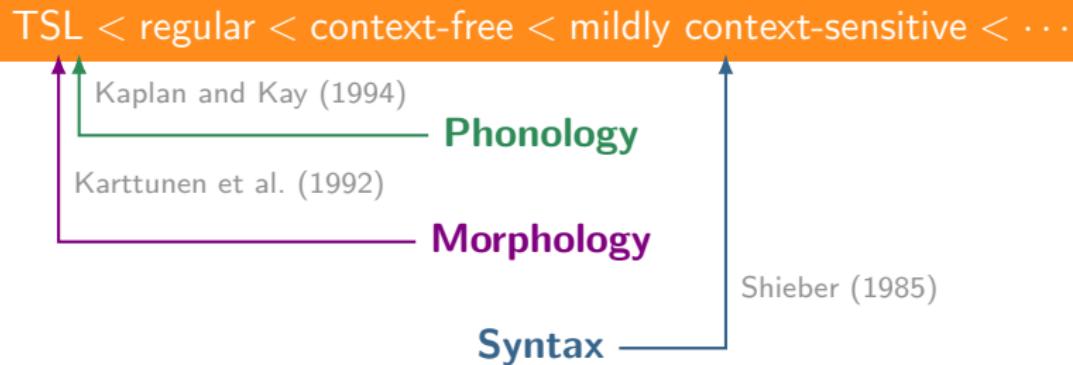


Sophie
Moradi

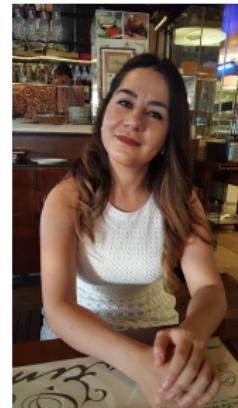
Why is TSL Relevant?

- ▶ Linguistically natural
- ▶ Captures wide range of phonotactic dependencies
- ▶ Correct and efficient learning algorithms
(I/O-TSL work in progress)
(Jardine and McMullin 2017)
- ▶ Low resource demand
 - ▶ remember the last n symbols of a specific type
 - ▶ requires little working memory
 - ▶ no complex memory architecture
- ▶ Rules out unattested patterns
 - ▶ center embedding
 - ▶ harmony only if separated by even number of segments

Could Syntax Also be Subregular?



- ▶ Syntax seems even more like an outlier...
- ▶ Don't look at strings!
What about **syntactic dependencies**?



Nazila Shafiei

c-Strings

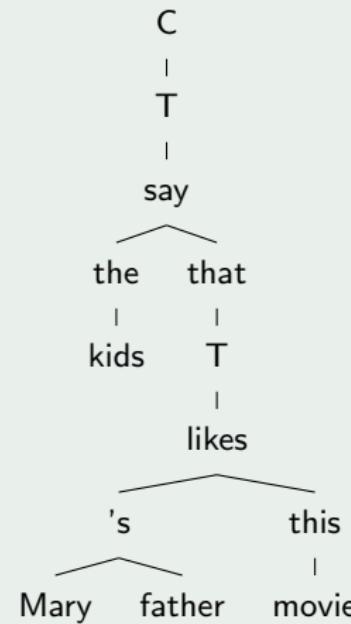
Command-Strings

The **c[ommand]-string** of a node n contains

- ▶ n and
- ▶ every node that commands n .

- ▶ easily computed from dependency trees
- ▶ c-command constraints seem to be largely **IOTSL over c-strings**

Example



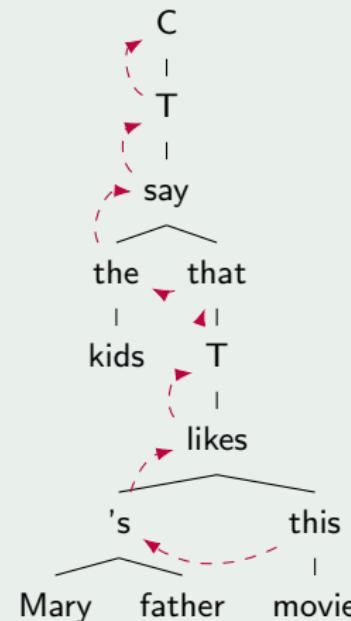
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Example



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Principle A (as a distributional constraint)

Every reflexive must be c-commanded by a DP in the same TP.

Equivalent c-String Constraint

If the c-string starts with a reflexive,
then at least one D must occur before the first T.

TSL Strategy for Principle A

- 1 Always project first symbol (ITSL)
- 2 Project D/T if previous symbol is Refl (OTSL)
- 3 Constraint: ***Refl T** (bigram)

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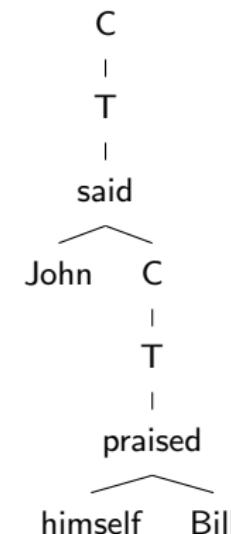
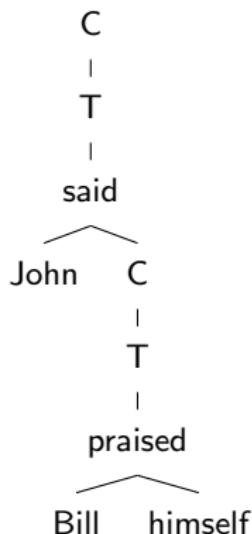
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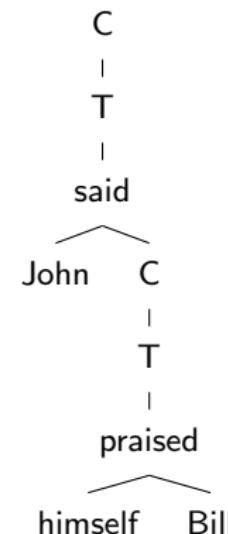
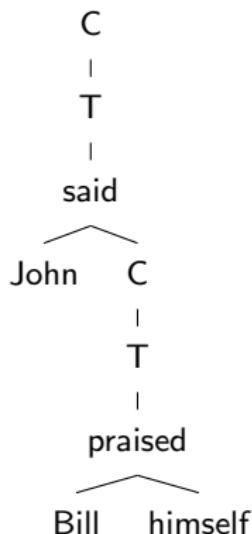
Example of Principle A as a TSL Constraint



\$ **himself** Bill
 | |
himself Bill praised T C ...

\$ **himself** **T** \$
 | |
himself praised **T** C ...

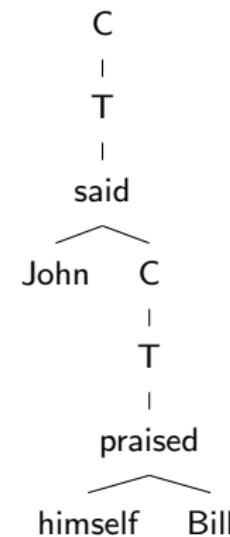
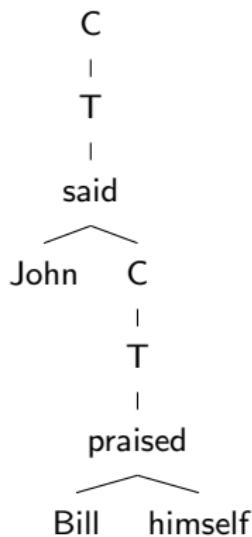
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Another Example: Swedish *sig*

- ▶ Swedish *sig* must be non-locally bound.

- (1) a. John said Bill praised sig.
 b. * Bill praised sig.

TSL Strategy for *sig*

- 1 Always project first symbol (ITSL)
- 2 Project T if previous symbol is sig (OTSL)
- 3 Project D if previous symbol is T (OTSL)
- 4 Constraint: *sig T \$ (trigram)



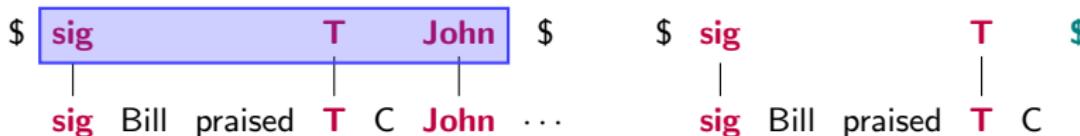
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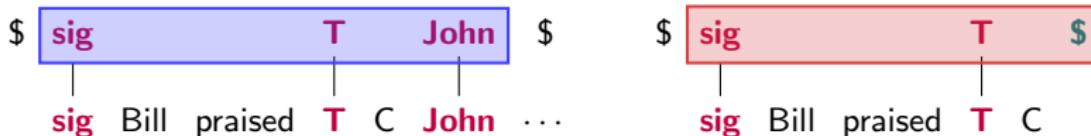
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Comparison to Phonology and Morphology

Similarities

- ▶ mostly bigram and trigram constraints
- ▶ simple structural contexts
- ▶ dependencies in phonology are also c-command-like
(Graf 2018a)

Differences

- ▶ OTSL seems more common in syntax

A Typological Prediction

Formal typology of syntactic constraints
should mirror phonology and morphology.

Connection to Parsing

- ▶ A tree is well-formed only if each node has a well-formed c-string.
- ▶ verifiable by deterministic top-down tree automaton with finite look-ahead
⇒ **efficient incremental parsing**

An Intriguing Hypothesis

- ▶ Why c-command (rather than, say, precedence)?
- ▶ Because it allows for more efficient processing!
- ▶ But syntax isn't just c-command.
There's also displacement/movement...

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Minimalist Grammars

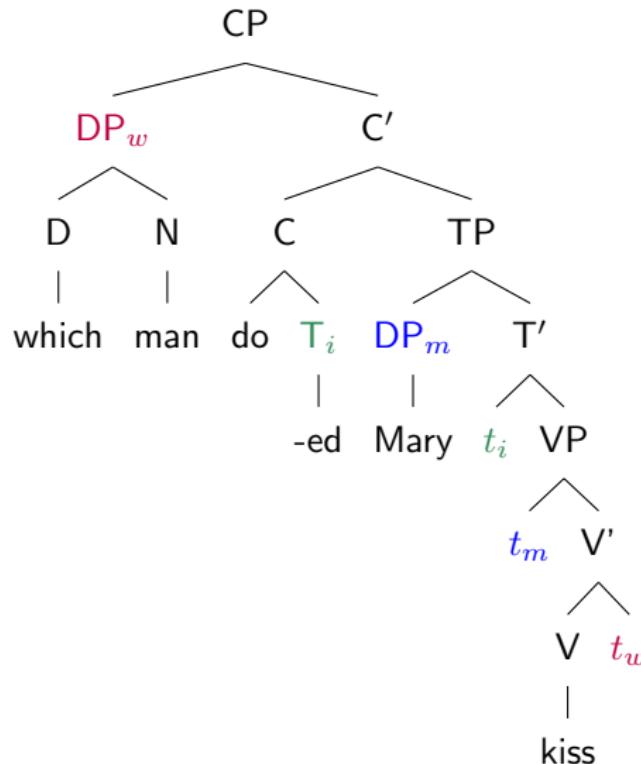


Ed Stabler

- ▶ Minimalist grammars (MGs) are a formalization of Minimalist syntax.
(Stabler 1997, 2011)
- ▶ Operations: **Merge** and **Move**
- ▶ Adopt Chomsky-Borer hypothesis:
Grammar is just a finite list of feature-annotated lexical items

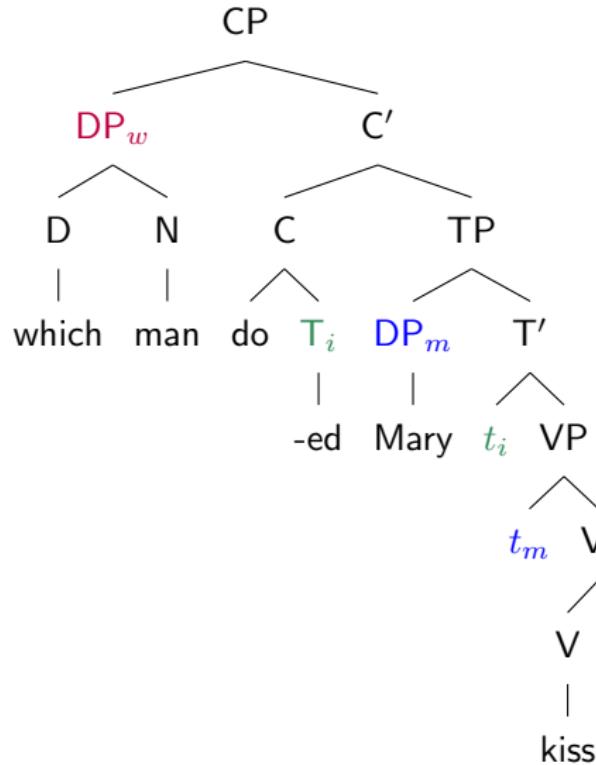
Chemistry	Syntax
atoms	words
electrons	features
molecules	sentences

MG Syntax in Action

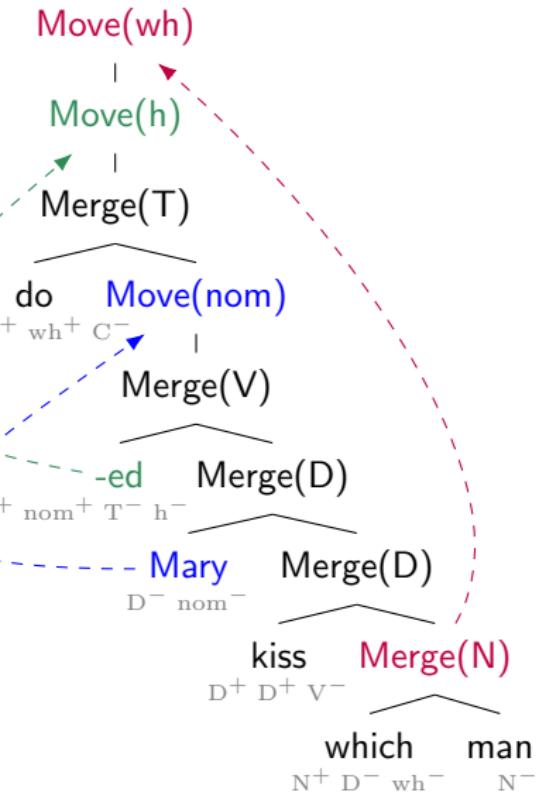


Phrase Structure Tree

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Phrase Structure Tree

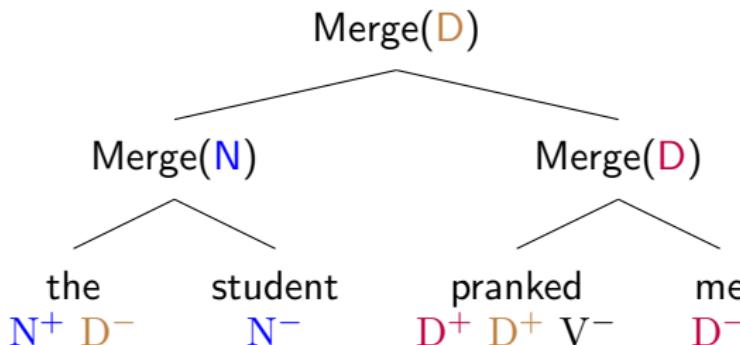


Derivation Tree

The Central Role of Derivation Trees

- ▶ Derivation trees are rarely considered in generative syntax.
(but see Epstein et al. 1998)
- ▶ Satisfy Chomsky's structural desiderata:
 - ▶ no linear order
 - ▶ label-free
 - ▶ extension condition
 - ▶ inclusiveness condition
- ▶ Contain all information to produce phrase structure trees
⇒ **central data structure** of Minimalist syntax

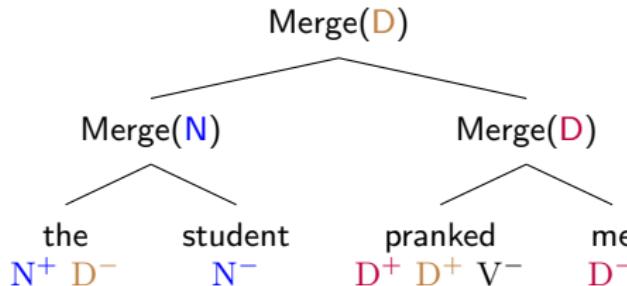
Merge is TSL



- ▶ The selector features of the head have to match the category features of the arguments.
- ▶ 1-to-1 match between selector features and category features.
- ▶ This is naturally expressed as **TSL over trees**.

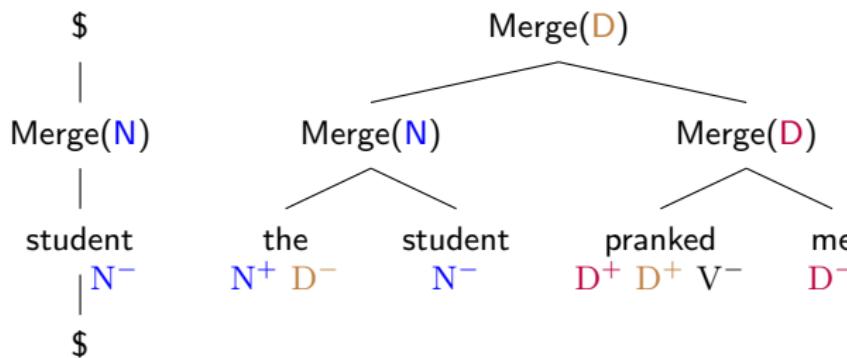
Category Tiers for Merge

- ▶ Project tree tier for each category X .
- ▶ Every X^- has a Merge node as its mother.
- ▶ Every Merge node has exactly one X^- among its daughters.



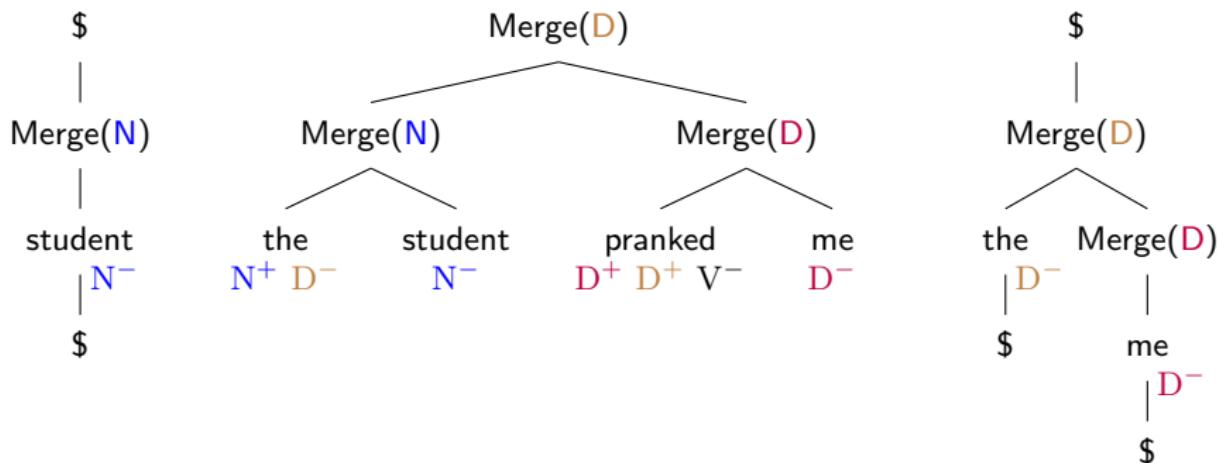
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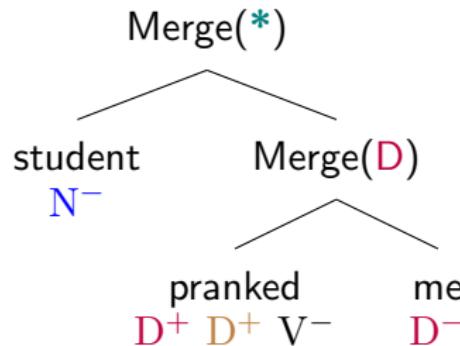


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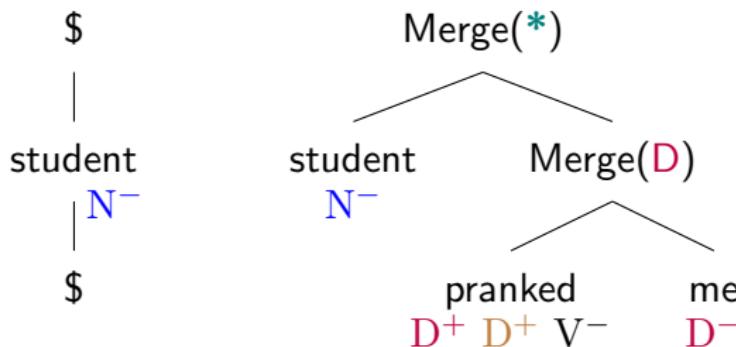


Illicit Merge Yields Ill-Formed Tiers



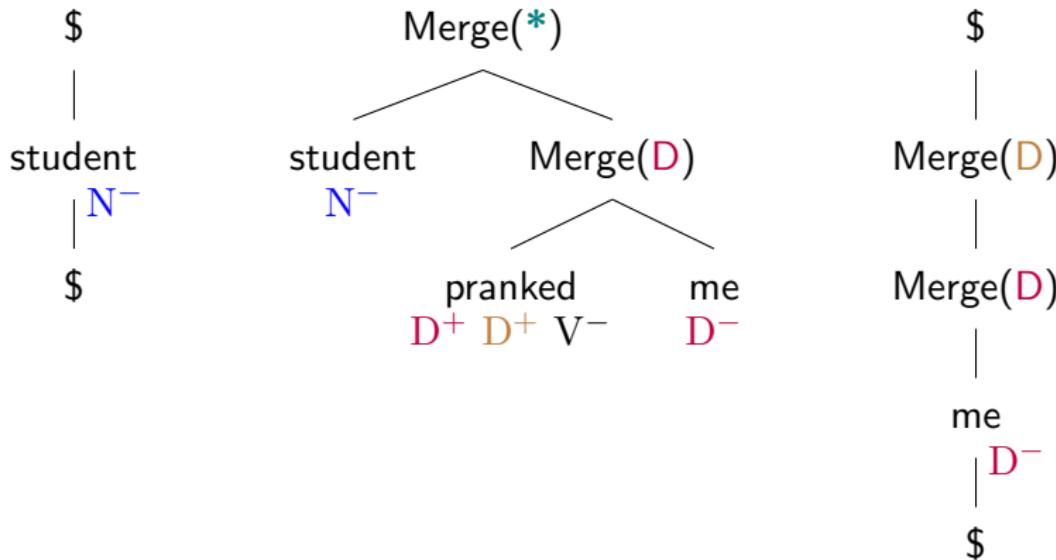
- ▶ This handles Merge.
- ▶ Moving on to Move...

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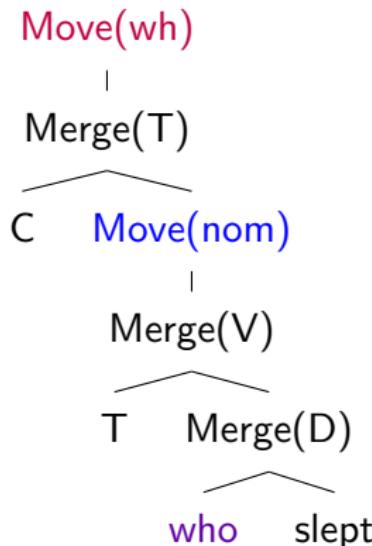
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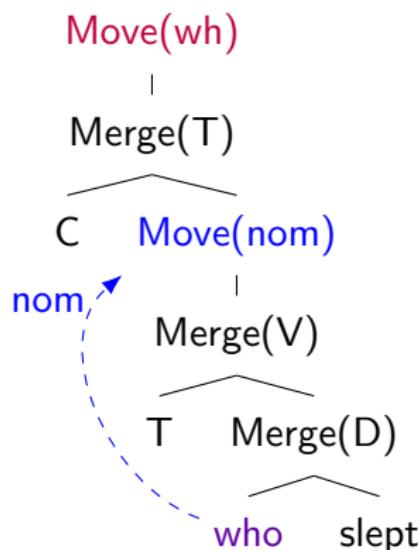
Move: Single Movement Normal Form

- ▶ **Assumption:** every phrase at most one movement feature
- ▶ Intermediate landing sites not feature-triggered
(Graf et al. 2016)



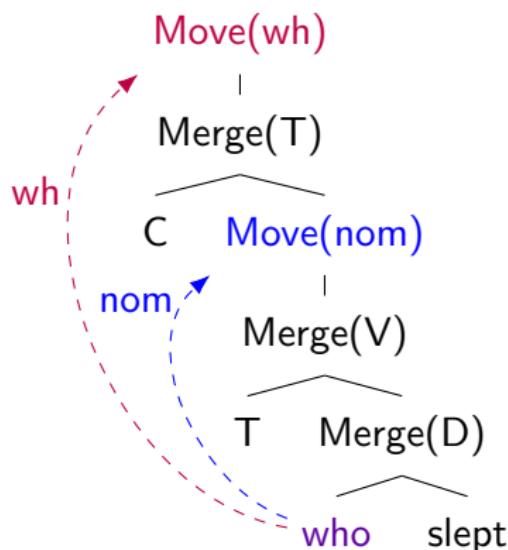
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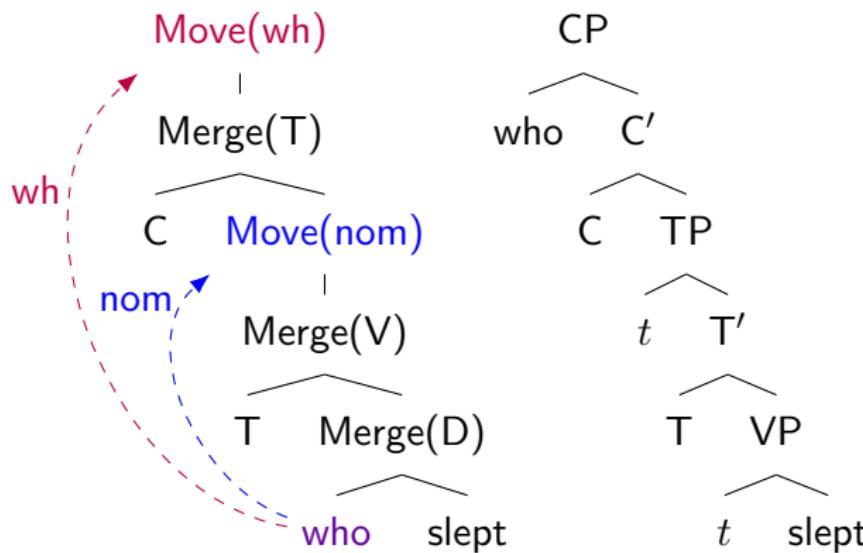
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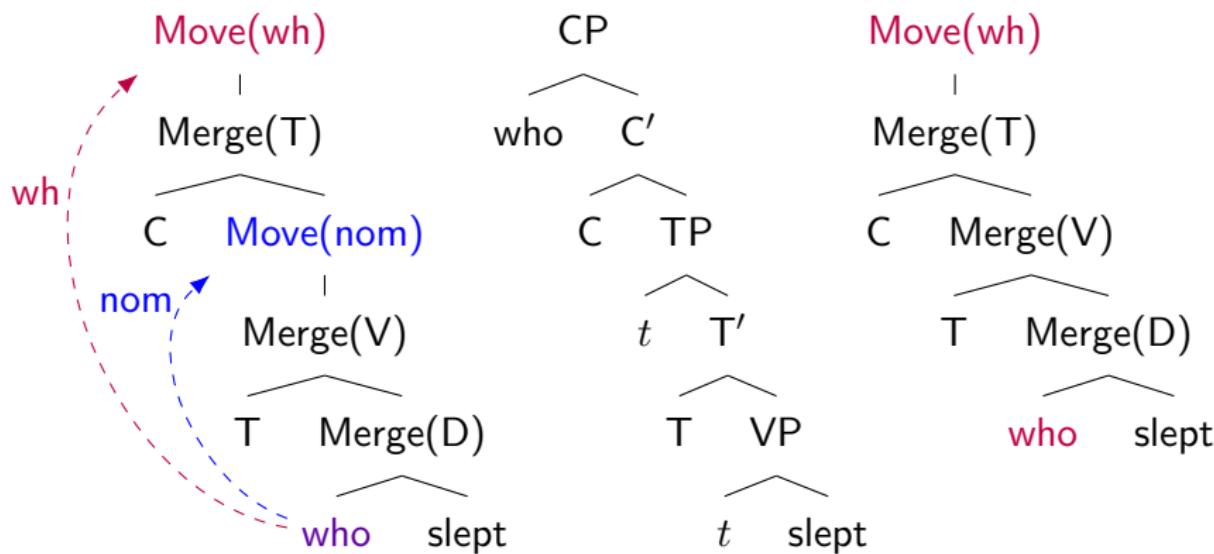
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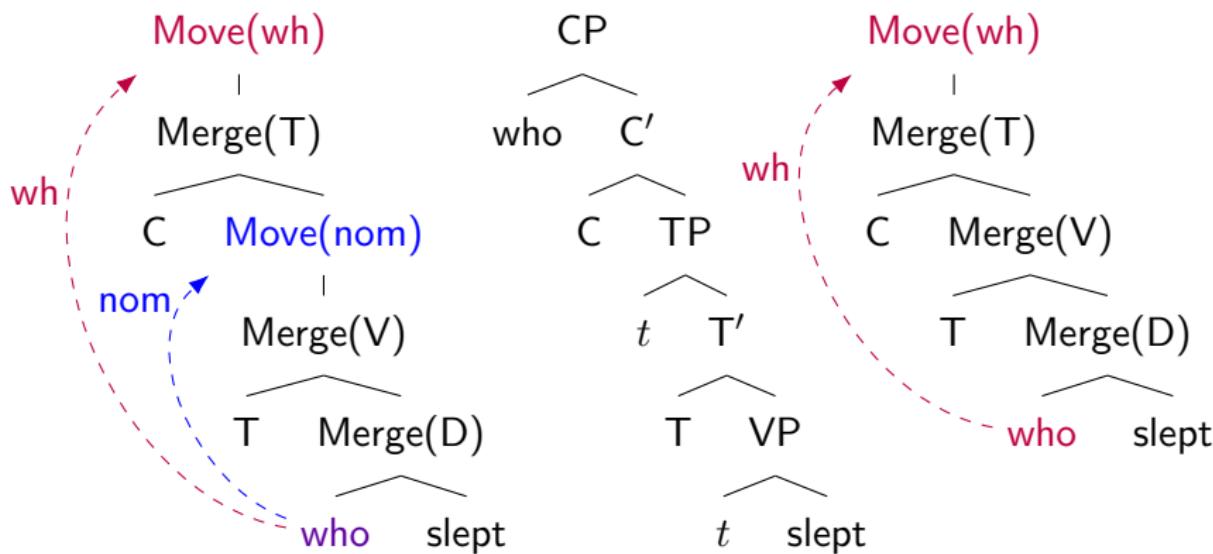
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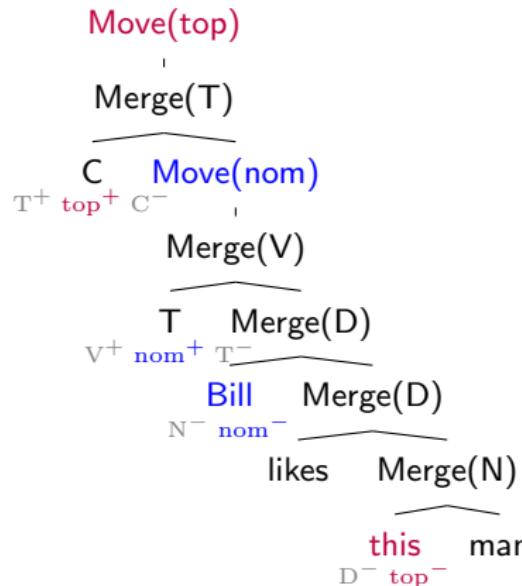
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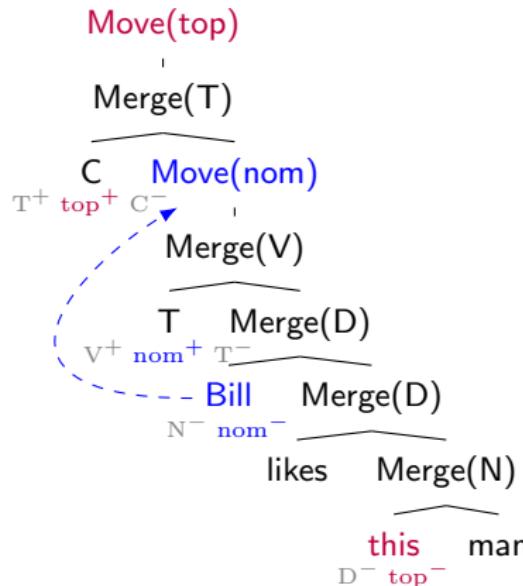
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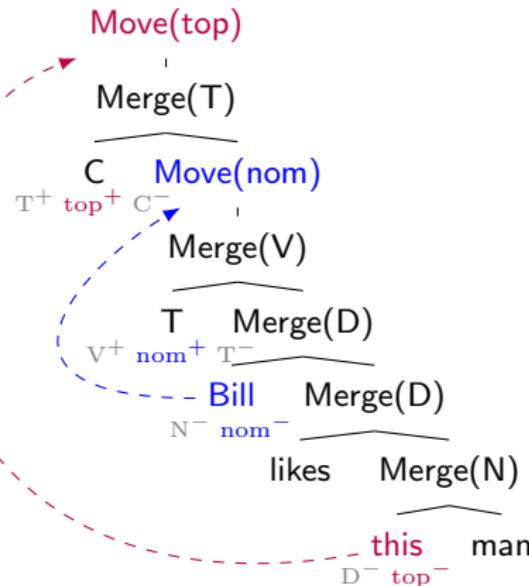
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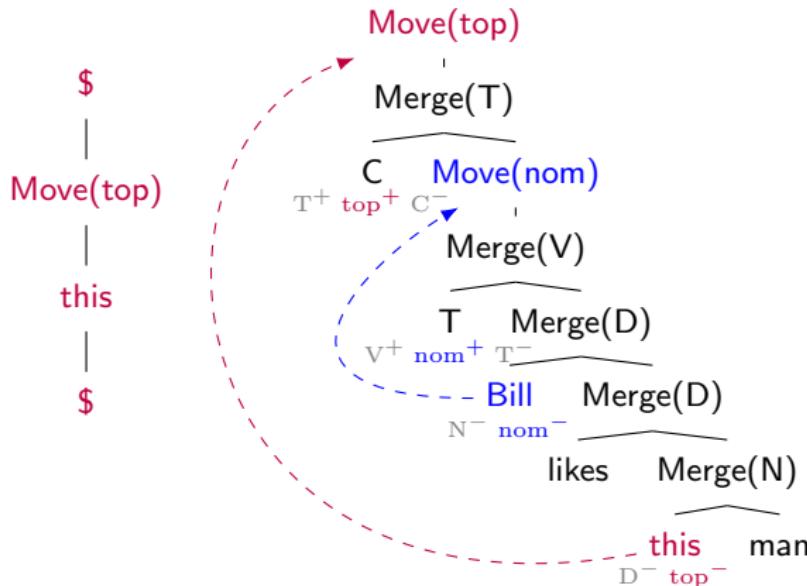
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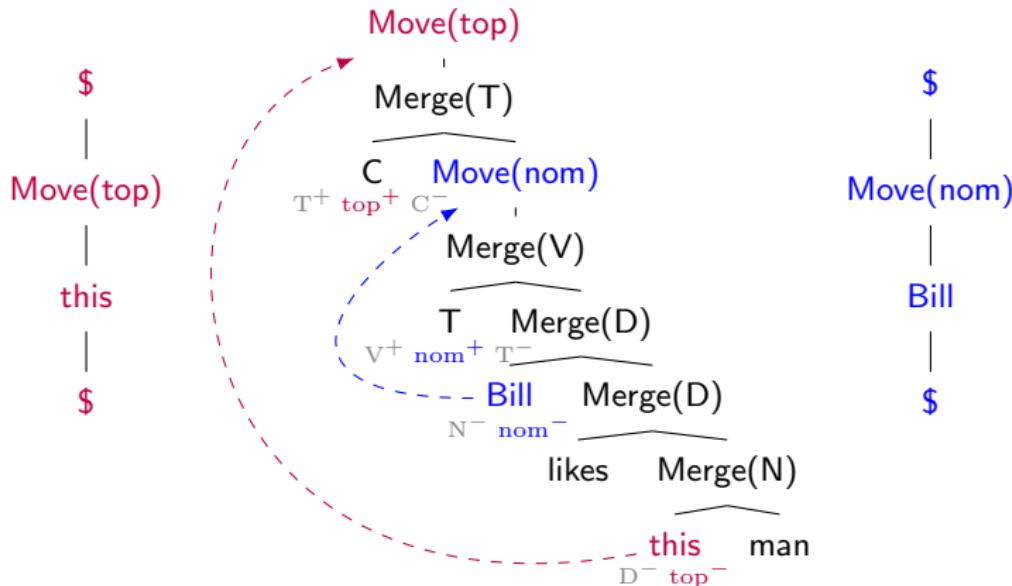
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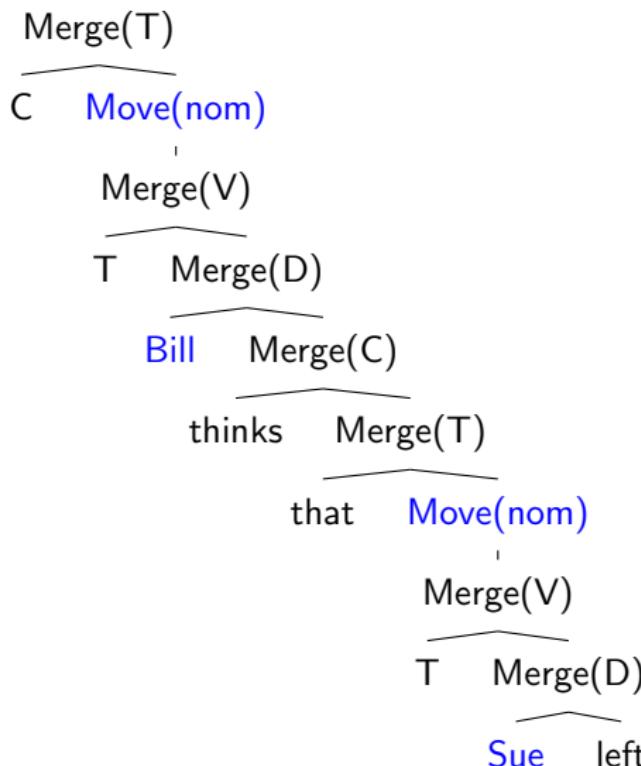


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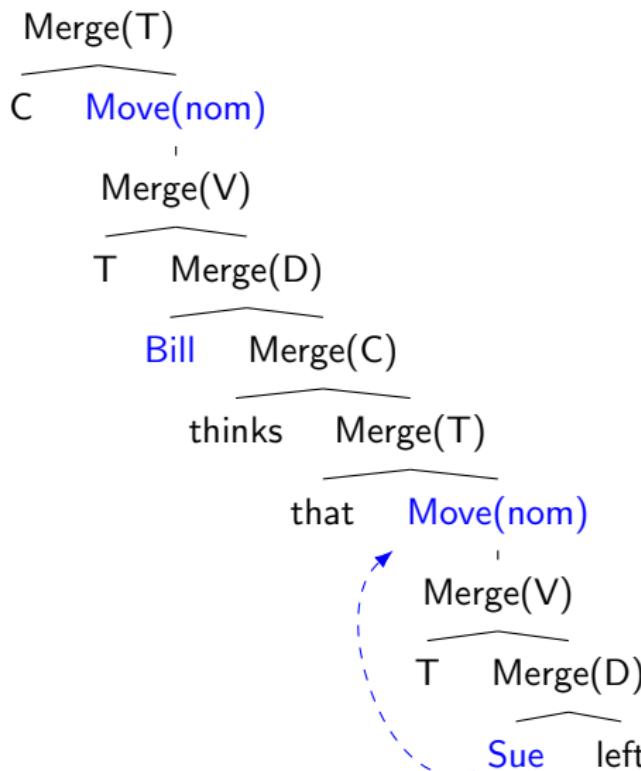
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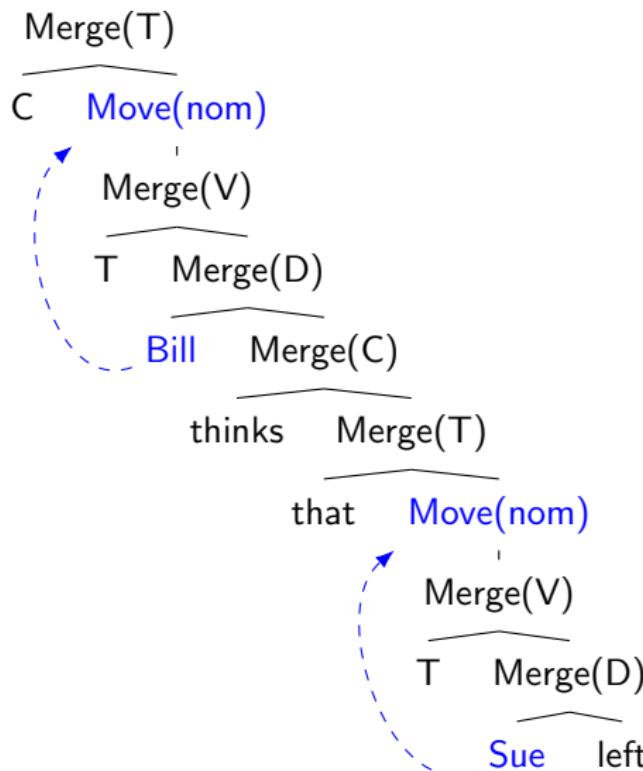
A Tier With Multiple Movers



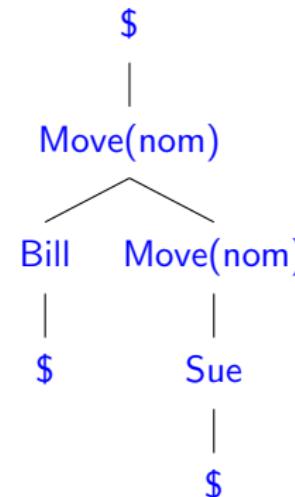
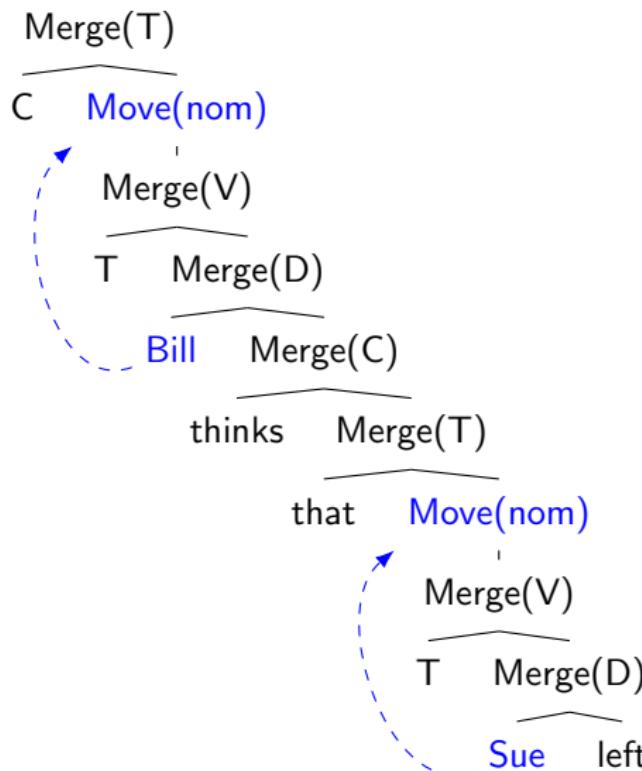
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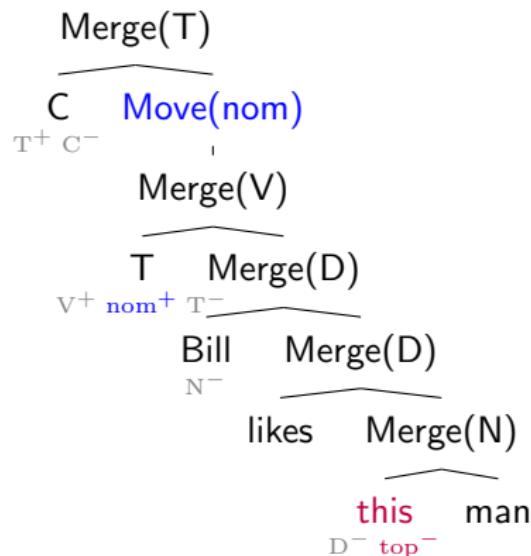
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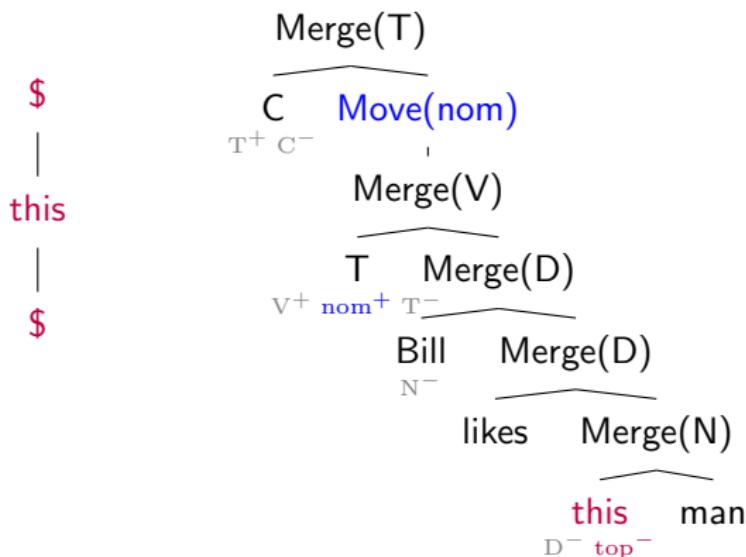
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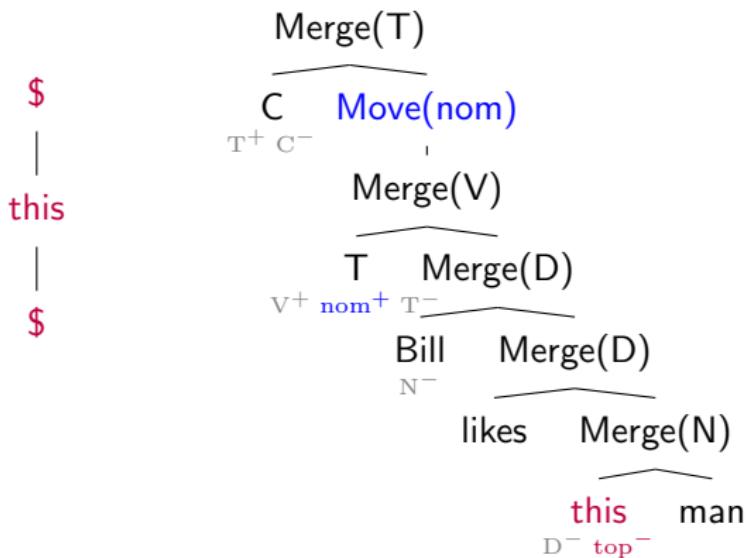
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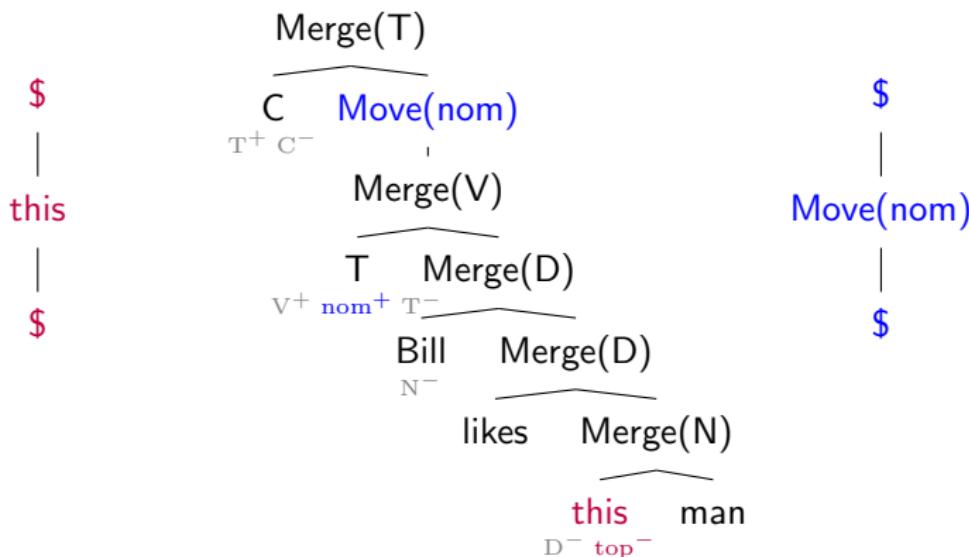
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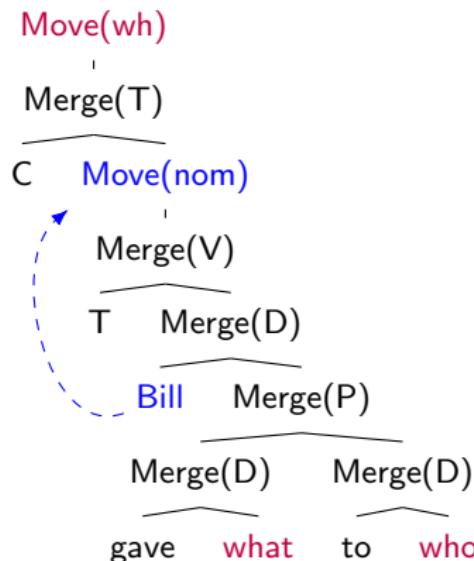
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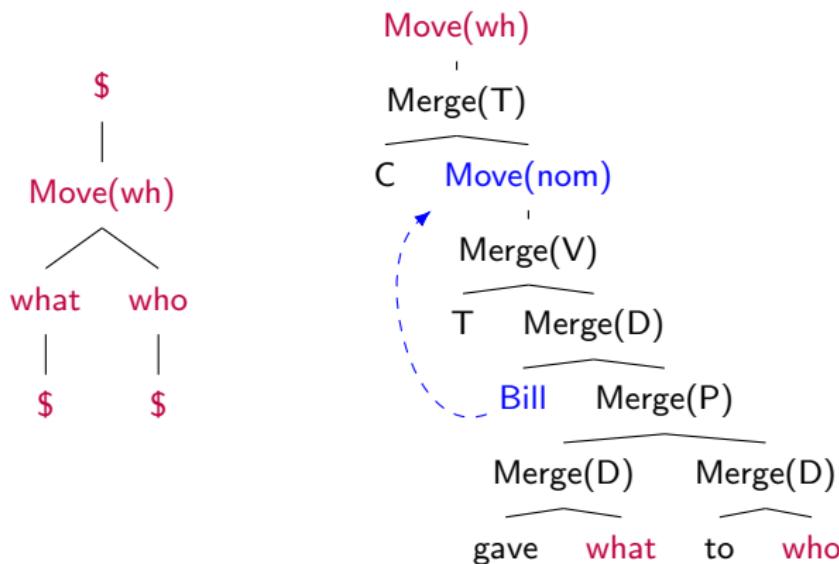
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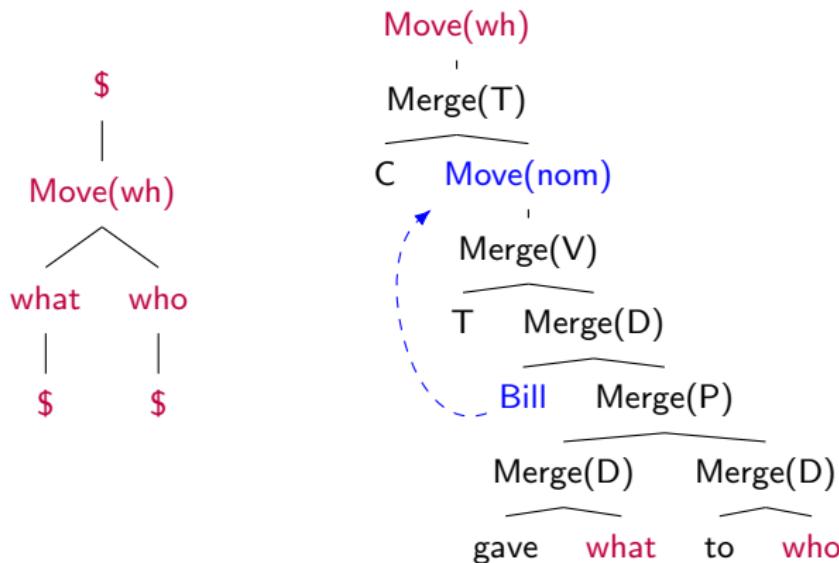
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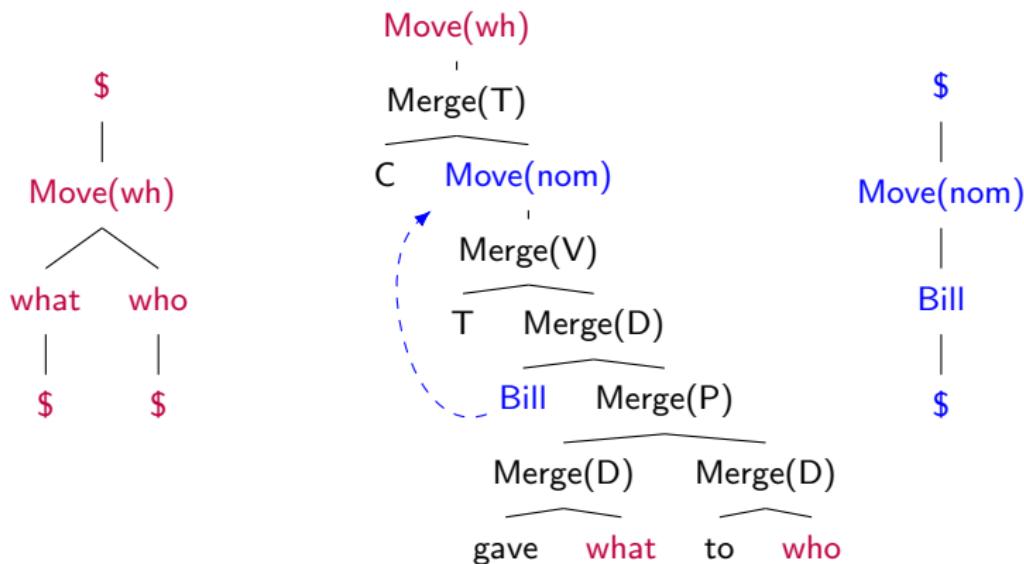
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Blocking Many-to-One Movement



The Common Core of Merge and Move

TSL Strategy for Merge

- ▶ Project tree tier for each **category** X .
- ▶ Every X^- has a **Merge** node as its mother.
- ▶ Every **Merge** node has exactly one X^- among its daughters.

TSL Strategy for Move

- ▶ Project tree tier for each **movement type** x .
- ▶ Every x^- has a **Move** node as its mother.
- ▶ Every **Move** node has exactly one x^- among its daughters.

Note: constraints again **highly local**

Summary

- ▶ Syntax looks like a complex outlier.
- ▶ But not if we choose appropriate representations:
 - ▶ c-command dependencies are TSL over c-strings
 - ▶ Merge and Move are TSL over derivation trees
- ▶ **Computational parallelism:**
 - ▶ phonology is TSL
 - ▶ morphology is TSL
 - ▶ syntax is TSL

Work In Progress

▶ Movement

- ▶ Interaction of movement and c-command
- ▶ Complexity without
Single Movement Normal Form

▶ Empirical work

- ▶ limits of c-string constraints
- ▶ unified treatment of island constraints
- ▶ modeling specific phenomena
(e.g. case assignment)

▶ Processing & Learning

- ▶ compiling c-string constraints
into MG parser
- ▶ learning via semantic bootstrapping



Sabine Laszakovits



Mai Ha Vu

Open Issues

- ▶ experimental evidence for computational parallelism
- ▶ even tighter subclasses of TSL
- ▶ full predicted typology
- ▶ model concrete aspects of acquisition

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Join the program!

Resources and Readings

- 1 Survey papers:** Pullum and Rogers (2006); Heinz (2011a,b, 2018); Rogers and Pullum (2011); Chandlee and Heinz (2016)
- 2 TSL and its extensions:** Heinz et al. (2011); McMullin (2016); Baek (2017); De Santo (2017); De Santo and Graf (2017); Graf (2017c); Graf and Mayer (2018); Mayer and Major (2018); Yang (2018)
- 3 TSL morphology:** Aksënova et al. (2016); Graf (2017b)
- 4 TSL morpho-semantics:** Graf (2017d)
- 5 TSL syntax:** Graf (2012a, 2018b); Graf and Shafiei (2019); Vu (2018); Vu et al. (2019)
- 6 Mappings:** Courcelle and Engelfriet (2012); Chandlee (2014, 2017); Jardine (2016)
- 7 Learnability:** Heinz (2010); Kasprzik and Kötzting (2010); Heinz et al. (2012); Jardine et al. (2014); Lai (2015); Jardine and Heinz (2016); Jardine and McMullin (2017)

Appendix

Psychological Reality of Derivation Trees

Central role of derivation trees backed up by **processing data**:

- ▶ Derivation trees can be parsed top-down (Stabler 2013)
- ▶ Parsing models update Derivational Theory of Complexity, make correct processing predictions for
 - ▶ right < center embedding (Kobele et al. 2013)
 - ▶ crossing < nested dependencies (Kobele et al. 2013)
 - ▶ SC-RC < RC-SC (Graf et al. 2017)
 - ▶ SRC < ORC in English (Graf et al. 2017)
 - ▶ SRC < ORC in East-Asian (Graf et al. 2017)
 - ▶ quantifier scope preferences (Pasternak 2016)
 - ▶ stacked relative clauses (Zhang 2017)
 - ▶ Korean attachment ambiguities

Technical Fertility of Derivation Trees

Derivation trees made it easy for MGs to accommodate the full syntactic toolbox:

- ▶ sideways movement (Stabler 2006; Graf 2013)
- ▶ affix hopping (Graf 2012b, 2013)
- ▶ clustering movement (Gärtner and Michaelis 2010)
- ▶ tucking in (Graf 2013)
- ▶ ATB movement (Kobele 2008)
- ▶ copy movement (Kobele 2006)
- ▶ extraposition (Hunter and Frank 2014)
- ▶ Late Merge (Kobele 2010; Graf 2014a)
- ▶ Agree (Kobele 2011; Graf 2012a)
- ▶ adjunction (Fowlie 2013; Graf 2014b; Hunter 2015)
- ▶ TAG-style adjunction (Graf 2012c)

Even More MG Extensions

- ▶ local and global constraints (Kobele 2011; Graf 2012a, 2017a)
- ▶ transderivational constraints (Graf 2010, 2013)
- ▶ Principle A and B (Graf and Abner 2012)
- ▶ GPSG-style feature percolation (Kobele 2008)
- ▶ idioms (Kobele 2012)
- ▶ grafts (multi-rooted multi-dominance trees) (Graf in progress)

Long Story Short

Derivation trees are a more useful and fertile data structure than phrase structure trees.

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