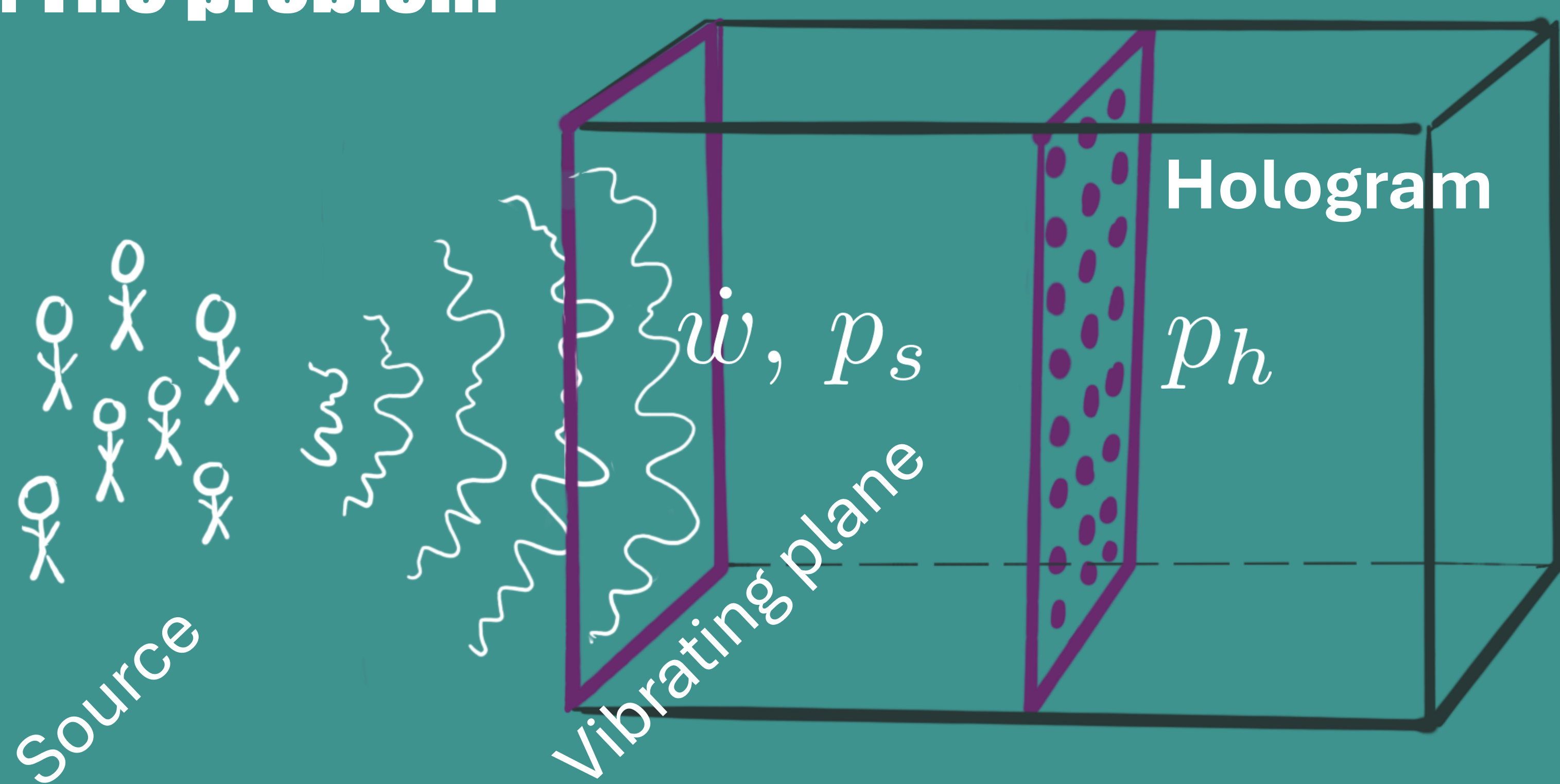


# Sound-Based Imaging:

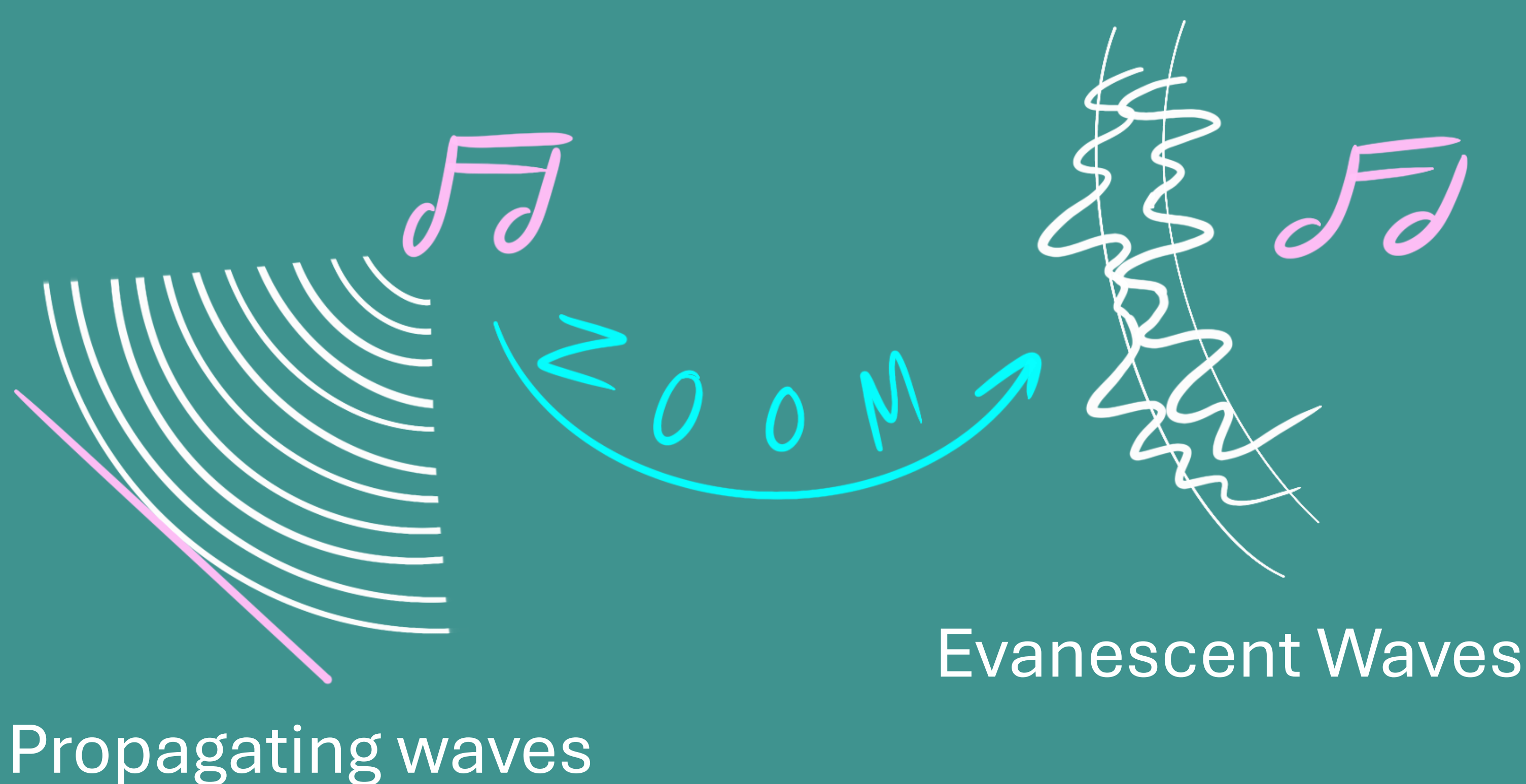
## Regularization Approaches in Near-field Acoustic Holography (NAH)

### 1. The problem



Near-field acoustic holography (NAH) is a method for solving the **inverse problem**: Based on the hologram measurements, how does the plane source look? i.e. **Where are the sources?**

It is important the measurements are close to the source (so that we don't miss anything).



### 2. Why to use regularization?

The NAH problem is an ill-posed problem, in the Hadamard sense. Small changes in the measurements yield big changes in the source field.

Regularization  $\implies$  well-posedness

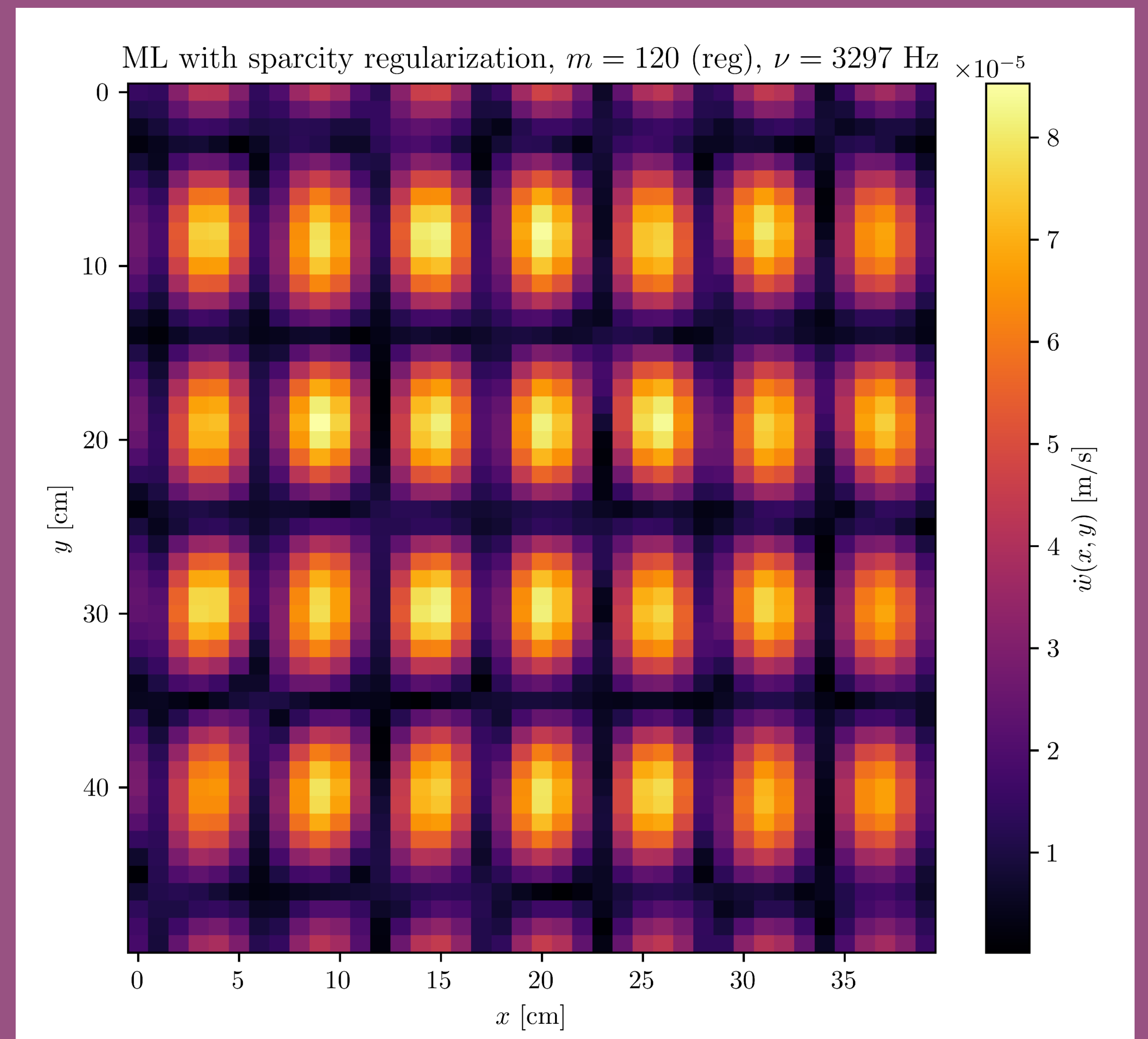


### 6. What you should take home

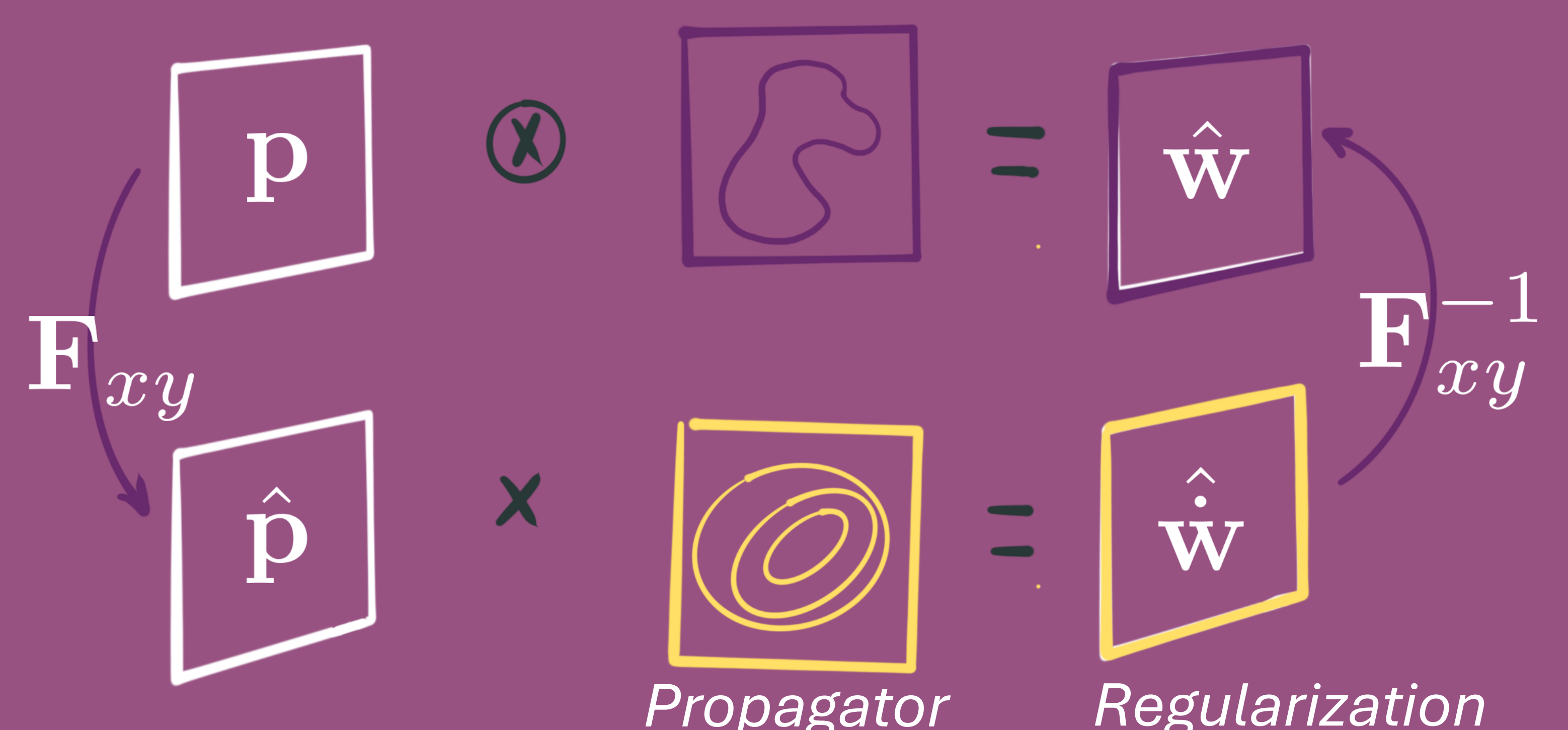
Not only can we see with our eyes, we can also **see** sound. NAH is an **inverse, ill-posed** problem that requires **regularization** which tries to find sound sources based on forward measurements.

Also, you just saw some really cool pixelated figures.

### 5. The results



### 4. The algorithm



### 3. The Regularization Methods

Tikhonov:  $\hat{\mathbf{w}} = \min_{\mathbf{w}} \|\mathbf{p} - \mathbf{H}\mathbf{w}\|_2^2 + \lambda \|\mathbf{L}\mathbf{w}\|_2^2$

Sparsity:  $\mathbf{x} = \sum_{j \in J} \alpha_j \mathbf{d}_j, \quad |J| \ll M$

ML: Finding  $\lambda$  for maximizing contrast

Green's Functions:  $\delta E = 0$