Begin with a set $S_0 \subset \mathbb{X}$ of one or multiple randomly sampled solutions