
SciComp Homework 3

Table of Contents

Problem 2	1
Problem 3	3
Problem 4	3
PART 1	3
PART 2	6
PART 3	7
Problem 5	8

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Problem 2

I create a 0-1 matrix with 50 columns, turn it into a vandermonde matrix where all the values previously in the columns 1-50 now are in column 2, rows 1-50, with the rest of the columns formatted according to the vandermonde matrix.

```
m = 50;
n = 5;

t = linspace(0,1,m)'; % Creating t, the 0-1 vector with m spaces.
A = fliplr(vander(t)); % Creating a vandermonde matrix
                        % (the right way around with fliplr)

A = A(:,1:n); % Removing the entries after the fifth row
b = cos(4*t); % The "real" cos(4*t)

figure(1);
hold on

COS = plot(t,b,'r-.'); % What does cos(4t) look like?
set(COS,'LineWidth',15);

xx(:,1) = A\b; % Solving by Matlab's backslash command
BACKS = plot(t,A*xx(:,1),'b');
set(BACKS,'LineWidth',9);

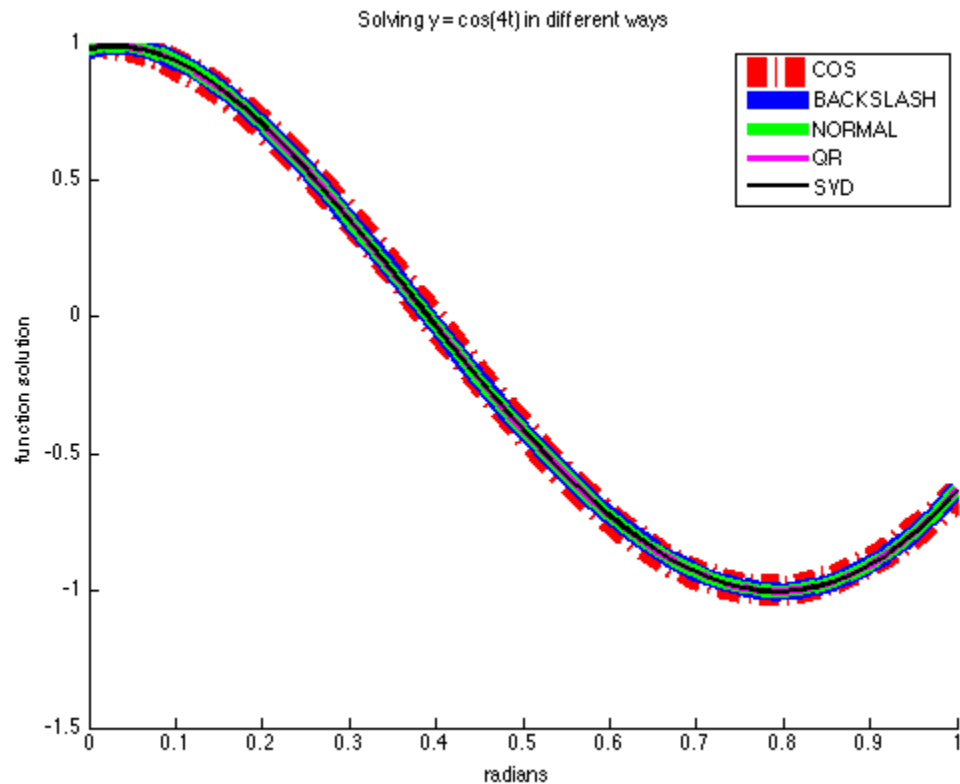
xx(:,2) = (A'*A)\(A'*b); % Finding the normal equations by
                        % multiplying with the transpose of A
NORMAL = plot(t,A*xx(:,2),'g');
set(NORMAL,'LineWidth',6);

[Q,R] = qr(A); % Finding the solution by QR factorisation:
xx(:,3) = R\Q'*b;
QR = plot(t,A*xx(:,3),'m');
set(QR,'LineWidth',3)
```

```
[U,S,V] = svd(A,0); % Finding the solution by svd:
G = U * S * V';
xx(:,4) = (G'*G)\(G'*b);

SVD = plot(t,A*xx(:,4),'black');
set(SVD,'LineWidth',2)

legend('COS','BACKSLASH','NORMAL','QR','SVD')
title('Solving y = cos(4t) in different ways')
xlabel('radians');
ylabel('function solution')
hold off
```



Norms:

```
for c = 1:4
    N(c) = norm(A*xx(:,c)-b,2);
end
```

Table of solutions of x and 2-norms:

```
normtable(xx,N)
```

```
=====
Backslash      Normal equation      QR
=====
x      +0.977651051050956  +0.787296437030590  -13.726690028111138  +14.
```

```

-3.665759654743957 +0.977651051050360 +0.787296437042173 -13.72
+14.993014653670262 -3.665759654779711 +0.977651051050948 +0.78
-13.726690028111079 +14.993014653596113 -3.665759654743917 +0.9
+0.787296437030878 -13.726690028111268 +14.993014653595205 -3.6
-----
2-norm +0.061356756239887 +0.061356756239888 +0.061356756239887 +0.061
=====

```

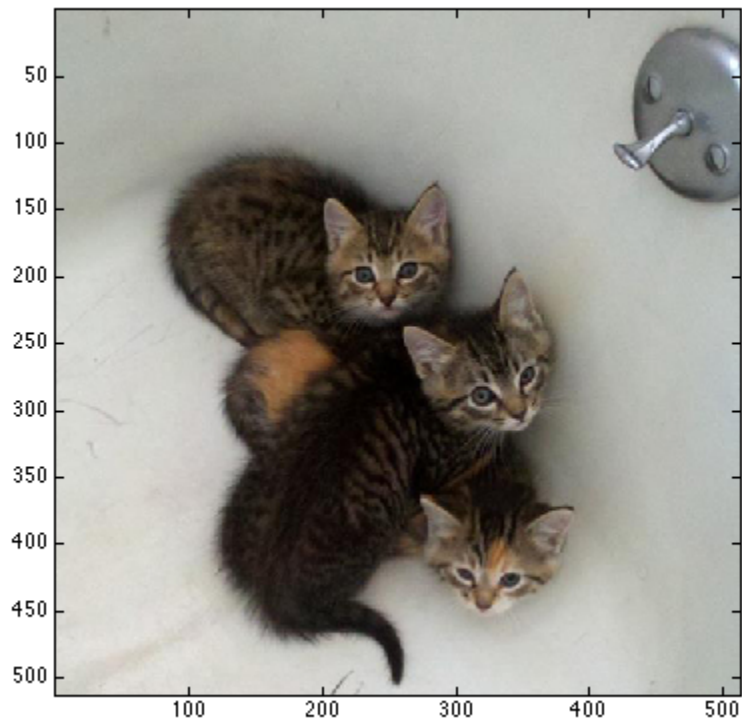
Problem 3

I have literally no idea how to do this. Have one of the top rated pictures of all time on reddit.com/r/cats instead:

```

cats = imread('cats.jpg');
figure(2); imagesc(cats);
axis equal, axis tight

```



Problem 4

PART 1

Starting with the unsharp mask

```

clear all

```

```
type('reading.m')
u = reading('testpat_blur2.png');

type('unsharpen.m')

unsharp = unsharpen(u,10); % Apply image unsharp mask

figure(3); clf; % Clears figure for new images (in case it contains cats)

subplot(1,2,1), imagesc(u);
type('greying.m')
greying();

subplot(1,2,2), imagesc(unsharp);
greying();

%% -----
%% reading()
% Code reads a square greyscale image, passes it to u

function [u] = reading(imgstring)
u = imread(imgstring);
u = double(u) / 255;

[n,n2] = size(u);
if (n ~= n2)
    error('by default, this only supports square images')
end
end
%% -----

%% -----
%% unsharpen() function
% Code creates a blurry mask, subtracts it from image u to find the
% difference, then adds the difference to the image in order to sharpen it

function [unsharp] = unsharpen(u,iterations)

[n,n2] = size(u);

e = ones(n,1);
L1 = spdiags([e -2*e e], [-1 0 1], n, n);

L1(1,1) = -1;
L1(end,end) = -1;

I = speye(n,n);
L = kron(L1, I) + kron(I, L1);

v = reshape(u, n*n, 1);

for i=1:iterations
    v = v + 0.1*(L*v);
```

```

end

ubblur = reshape(v, n, n);
%%
% This changes a blurring function to a unsharp mask.
edgemap = u - ubblur;
unsharp = u + edgemap;

end
%% -----

%% -----
%% greying() function
% Code formats images with a colour axis from 0 to 1 (grey) and equal axis

function [] = greying()
caxis([0 1])
colormap(gray)
axis equal, axis tight
end
%% -----

```

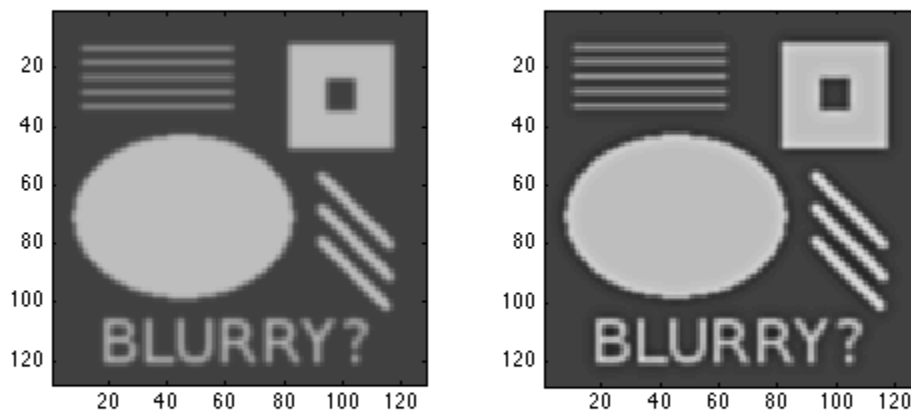


Image becomes sharpened!

PART 2

What happens if we unsharpen a non-blurry image?

```
[u] = reading('testpat_noblur.png'); % Read image from file

unsharp = unsharpen(u,10); % Apply image unsharp mask

figure(4); clf; % Clears figure for new images

% Plots full size and zoomed versions of original image, 10 step blurring
% and 100 step blurring.
subplot(3,2,1), imagesc(u);
greyimg();
title('Original "testpat noblur.png"')

subplot(3,2,2), imagesc(u);
greyimg();
axis([30 60 30 60])
title('Zoomed original')

subplot(3,2,3), imagesc(unsharp);
greyimg();
title('Unsharpened image')

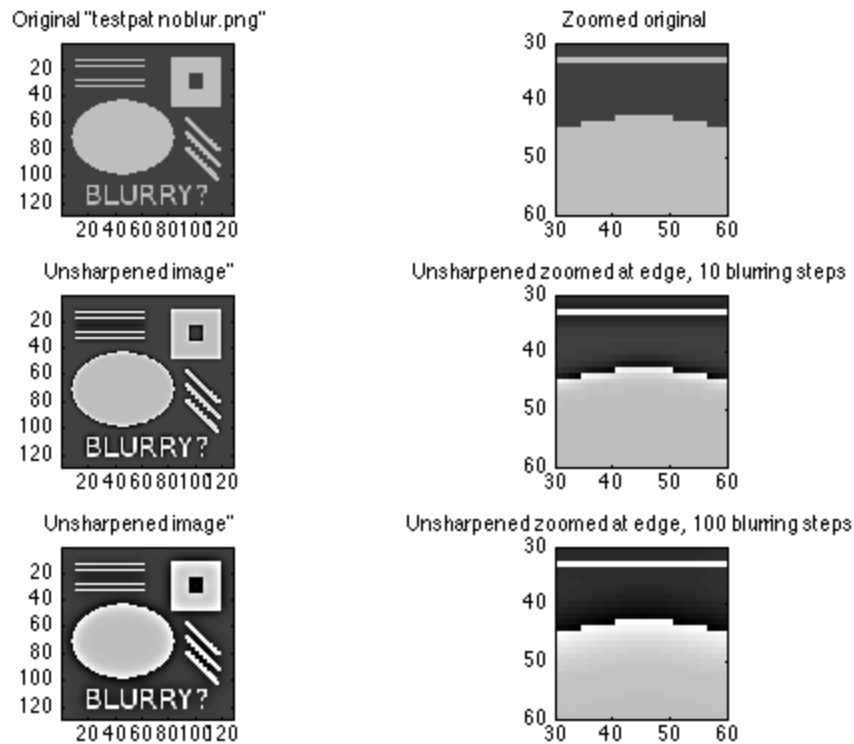
subplot(3,2,4), imagesc(unsharp);
greyimg();
axis([30 60 30 60])
title('Unsharpened zoomed at edge, 10 blurring steps')

unsharp100 = unsharpen(u,100);

subplot(3,2,5), imagesc(unsharp100);
greyimg();
title('Unsharpened image')

subplot(3,2,6), imagesc(unsharp100);
greyimg();
axis([30 60 30 60])
title('Unsharpened zoomed at edge, 100 blurring steps')

hold off
```



The sharpening of the image enhances the contrast between points that are already contrasting. For a unblurred image, this ramps up the "whiteness" of the image to the point of making it "grainy", as can be seen on the zoomed plot of the 100 stepped blurring image.

PART 3

```
u = reading('eye.png'); % Read image from file

unsharp1 = unsharpendeg(u,10,0.1); % Apply image unsharp mask
unsharp5 = unsharpendeg(u,10,0.5); % Apply image unsharp mask

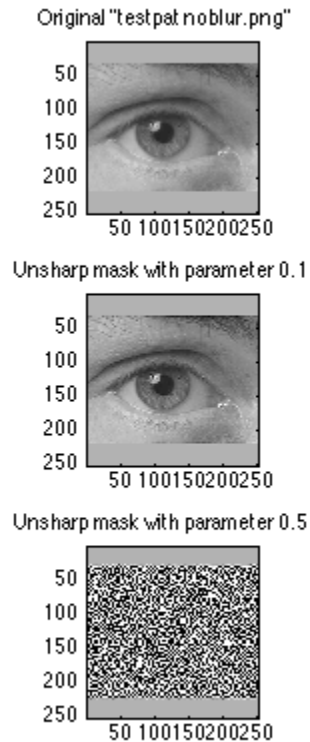
figure(5); clf; % Clears figure for new images

% Plots full size and zoomed versions of original image, 10 step blurring
% and 100 step blurring.
subplot(3,1,1), imagesc(u);
greyimg();
title('Original "testpat noblur.png"')

subplot(3,1,2), imagesc(unsharp1);
greyimg();
title('Unsharp mask with parameter 0.1')

subplot(3,1,3), imagesc(unsharp5);
greyimg();
```

```
title('Unsharp mask with parameter 0.5')
```



With the parameter set to 0.5, the image becomes a contrasty mess with no identifiable image.

Problem 5

What is the data we want to fit against?

```
xx = [3,1,0,-1,-2,0,-2,2]'  
yy = [3,-2,3,2,-2,-4,0,0]'  
% Having a look:  
figure(6);  
scatter(xx,yy,100,'r','filled')  
axis([-6,6,-6,6])  
hold on  
  
type('ellipse.m')  
  
[b,c,d] = ellipse(xx,yy);  
  
grid on  
  
[b,c,d] = ellipse(xx,yy);  
  
type('ellipseplot.m')  
ellipseplot(b,c,d);
```


xx =

3
1
0
-1
-2
0
-2
2

yy =

3
-2
3
2
-2
-4
0
0

%% -----
%% ellipse() function
% Takes a set of X and Y points and computes the b, c and d value for a
% ellipse of equation $bx^2+cxy+dy^2 = 1$!

function [b,c,d] = ellipse(x,y)

format long

A(:,1) = x.^2;
A(:,2) = x.*y;
A(:,3) = y.^2;

B = ones(length(x),1);

X = A\B
b = X(1)
c = X(2)
d = X(3)

end

%% -----

X =

0.257358001450461
-0.200536979030043
0.075581341521749

$b =$

0.257358001450461

$c =$

-0.200536979030043

$d =$

0.075581341521749

$X =$

0.257358001450461
-0.200536979030043
0.075581341521749

$b =$

0.257358001450461

$c =$

-0.200536979030043

$d =$

0.075581341521749

```
%% -----
%% ellipseplot() function
% Takes the b, c and d values for an ellipsis of equation  $bx^2+cxy+dy^2 =$ 
% 1, and plots it!

function [] = ellipseplot (b,c,d)

ang = (1/2)*atan(c/(d-b));
e = sqrt((1-tan(ang)^2)/(b-d*(tan(ang)^2)));
f = sqrt((tan(ang)^2-1)/(b*(tan(ang)^2-d)));

t = linspace(0,2*pi,200);
u = e*cos(t);
v = f*sin(t);

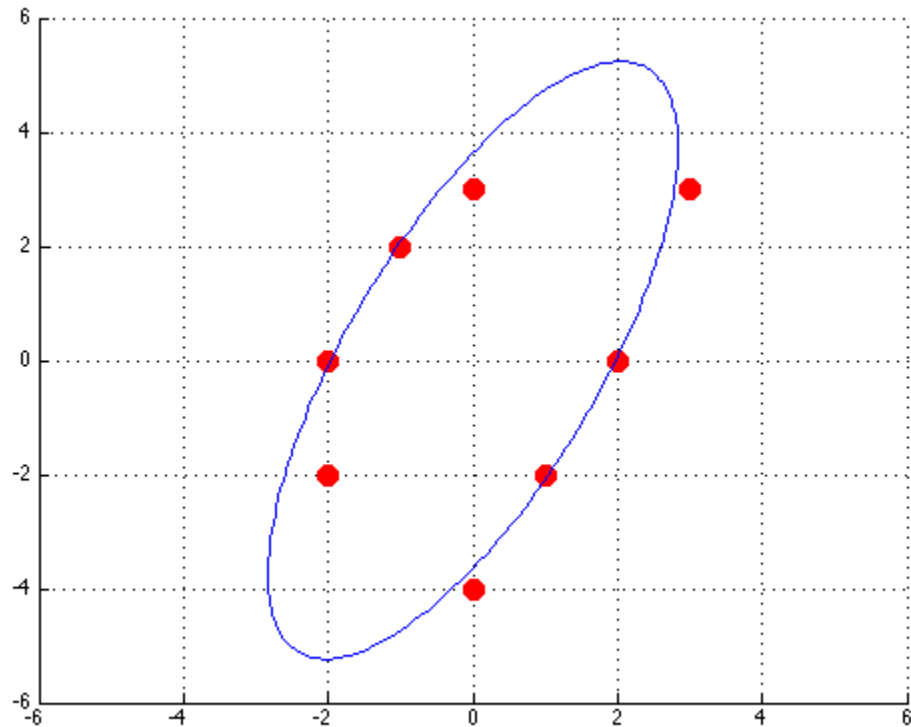
X = u*cos(-ang) - v*sin(-ang);
```

```
Y = u*sin(-ang) + v*cos(-ang);
```

```
plot(X,Y)
```

```
end
```

```
%% -----
```



Now we create the points, and the program finds the best fitting ellipse!

```
figure(7);
```

```
axis([-3 3 -3 3]), axis manual, hold on, grid on
```

```
x = []; y = []; button = 1;
```

```
disp('input points with mouse, button >= 2 for final point')
```

```
while button == 1
```

```
    [xx,yy,button] = ginput(1);
```

```
    x = [x; xx]; y = [y; yy]; plot(xx,yy, '.', 'color', 'red', 'MarkerSize', 32)
```

```
end
```

```
[b,c,d] = ellipse(x,y)
```

```
ellipseplot(b,c,d);
```

```
clear
```

```
input points with mouse, button >= 2 for final point
```

```
X =
```

2.533888761742440
-0.807308182329279
0.848465541956224

$b =$

2.533888761742440

$c =$

-0.807308182329279

$d =$

0.848465541956224

$b =$

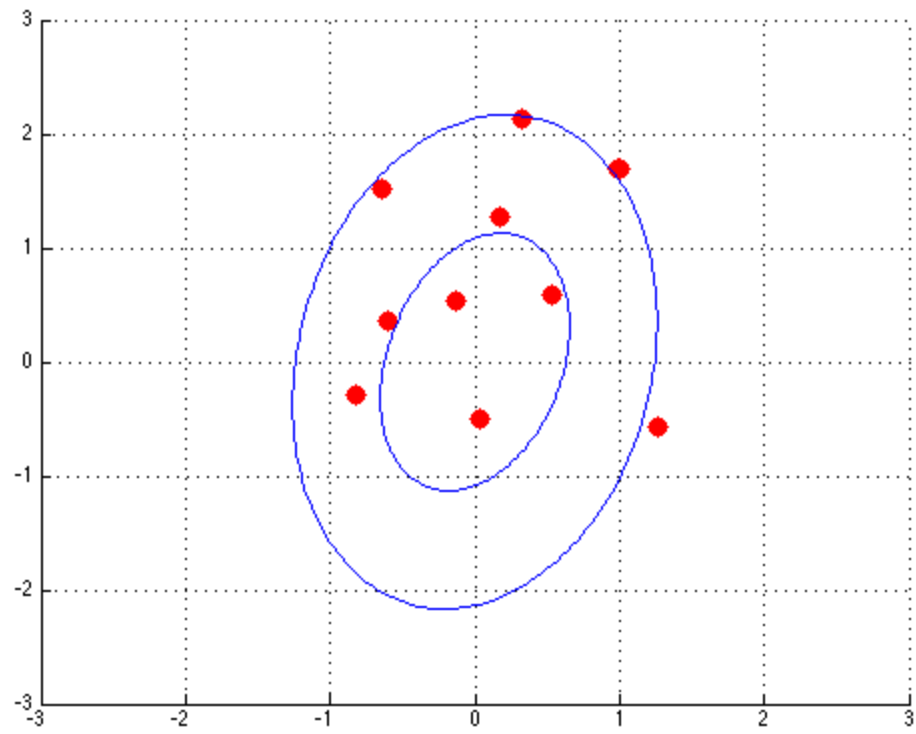
2.533888761742440

$c =$

-0.807308182329279

$d =$

0.848465541956224



Published with MATLAB® 8.0