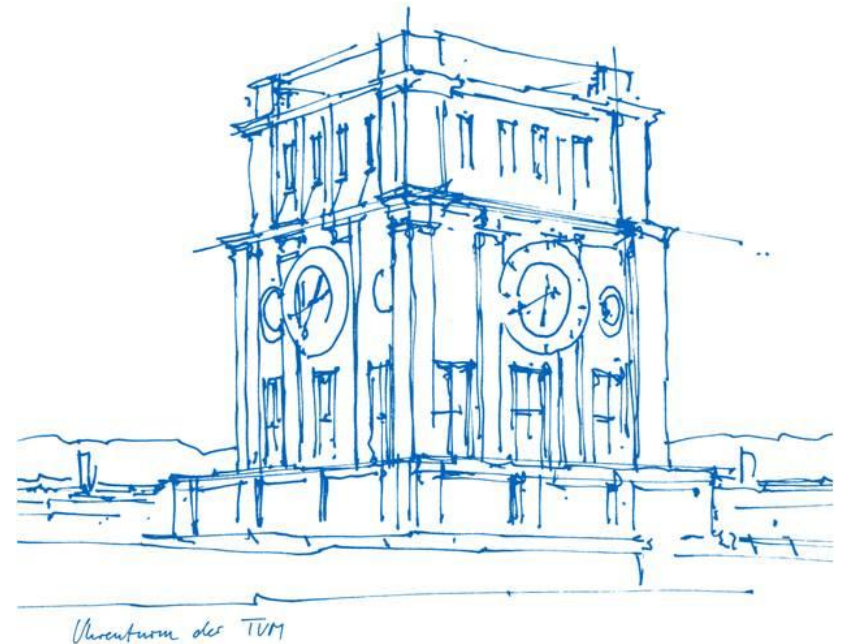


# Invertible Neural Networks for Inverse Kinematics

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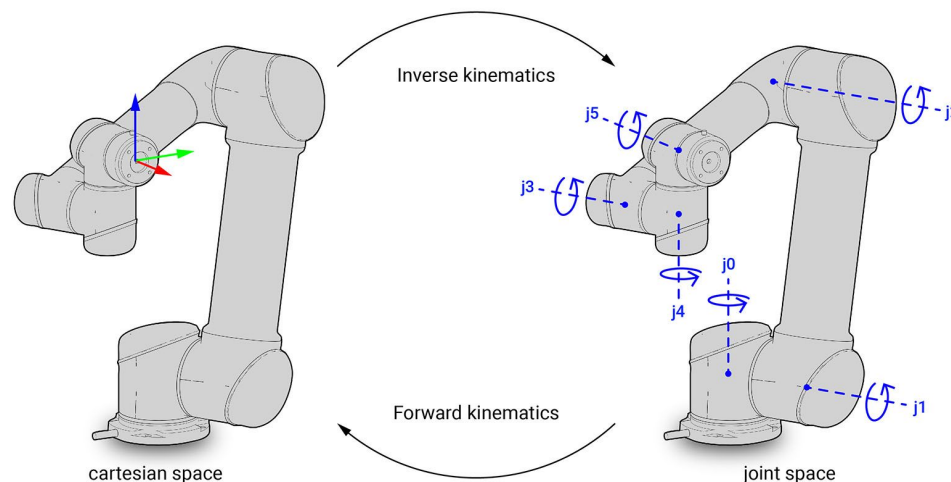


# Motivation - Inverse Kinematics

Determining the joint variables corresponding to an end-effector position and orientation

Complex problem: nonlinear, closed-form solution only for few cases

Problem can be ill-posed: single, multiple, infinite or no solutions



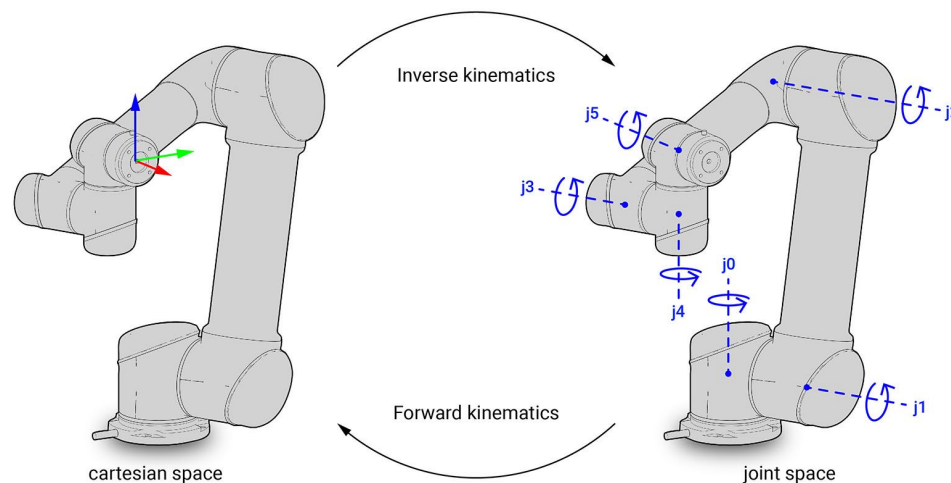
# Motivation - Inverse Kinematics

Classical approaches:

analytical solution  $\rightarrow$  not always possible

numerical solution  $\rightarrow$  expensive, limited to few solutions

Can we use neural networks to learn inverse kinematics?

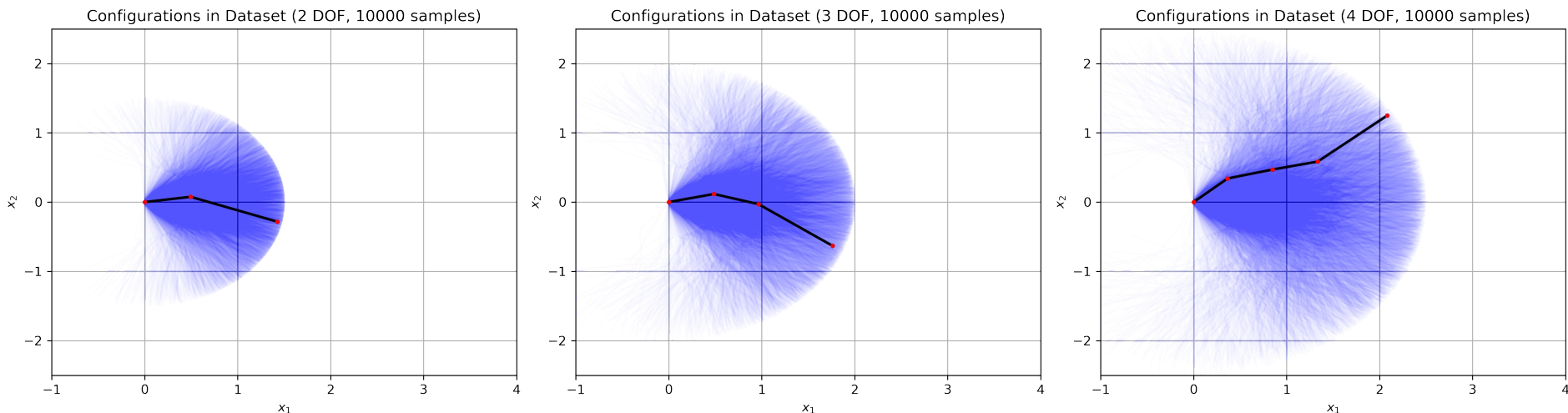


# Methods - Dataset

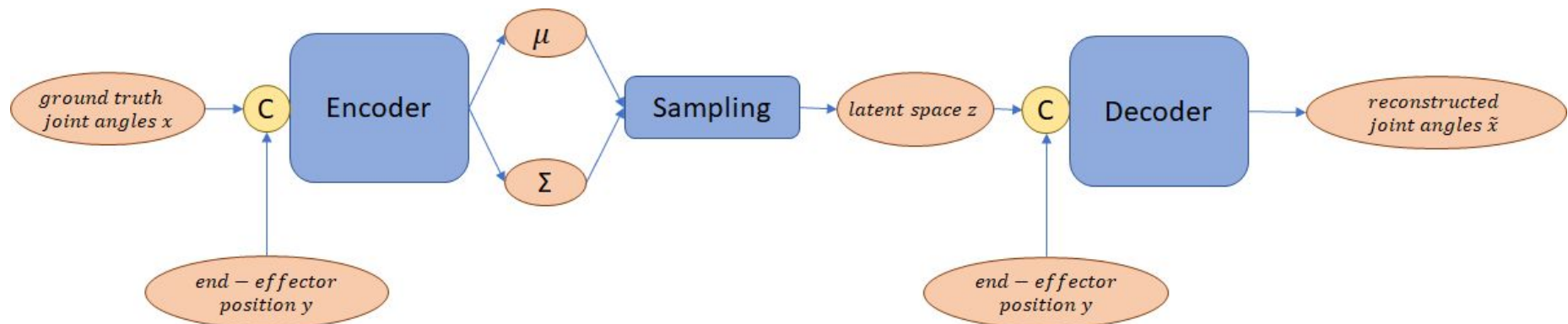
Simulation of different planar robots: 2 DoF, 3 DoF and 4 DoF

Joint orientations from a normal distribution:  $\theta_i = \mathcal{N}(\mu = 0, \sigma^2 = 0.25)$

One million samples of robot configurations

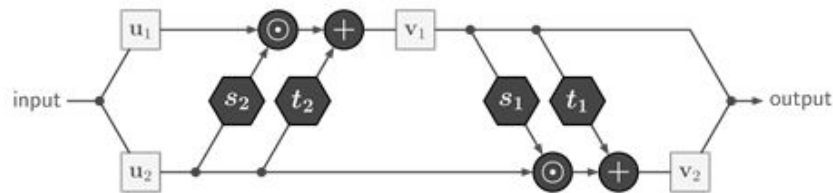


# Methods - Conditional Variational Autoencoder (cVAE)

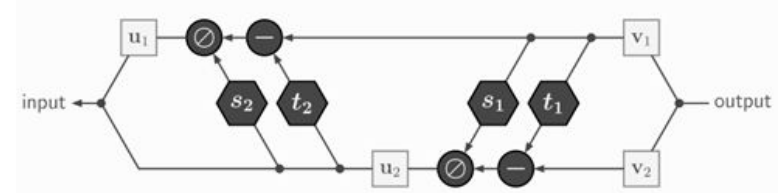


# Methods - Invertible Neural Network (INN)

## Affine Coupling Layer



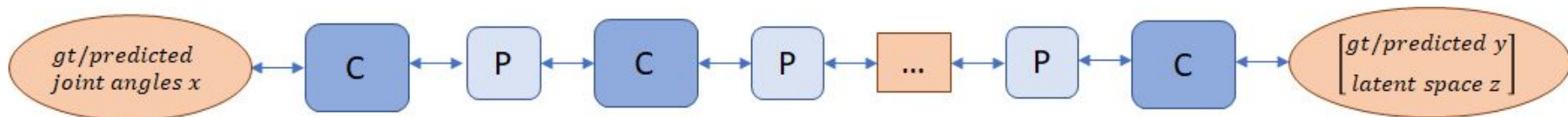
$$\begin{aligned} \mathbf{v}_1 &= \mathbf{u}_1 \odot \exp(s_2(\mathbf{u}_2)) + t_2(\mathbf{u}_2) \\ \mathbf{v}_2 &= \mathbf{u}_2 \odot \exp(s_1(\mathbf{v}_1)) + t_1(\mathbf{v}_1), \end{aligned}$$



$$\begin{aligned} \mathbf{u}_2 &= (\mathbf{v}_2 - t_1(\mathbf{v}_1)) \odot \exp(-s_1(\mathbf{v}_1)) \\ \mathbf{u}_1 &= (\mathbf{v}_1 - t_2(\mathbf{u}_2)) \odot \exp(-s_2(\mathbf{u}_2)). \end{aligned}$$

C: coupling layer

P: fixed but random permutation block



# Results

1. Average mismatch between true posterior and predicted posterior

$$e_{posterior} = MMD(\tilde{p}(x|y_{gt}), p_{gt}(x|y_{gt}))$$

2. Average re-simulation error

$$e_{resim} = E_{x \sim \tilde{p}(x|y_{gt})}(\|f(x) - y_{gt}\|_2^2)$$

DoF	$e_{posterior}$	$e_{resim}$	Trainable Parameters	Model
2	0.077	<b>0.003</b>	164,808	cVAE
3	<b>0.045</b>	0.045	370,214	
4	0.063	<b>0.006</b>	373,220	
2	<b>0.061</b>	0.012	169,632	INN
3	0.066	<b>0.036</b>	369,660	
4	<b>0.044</b>	0.075	374,960	

# Results

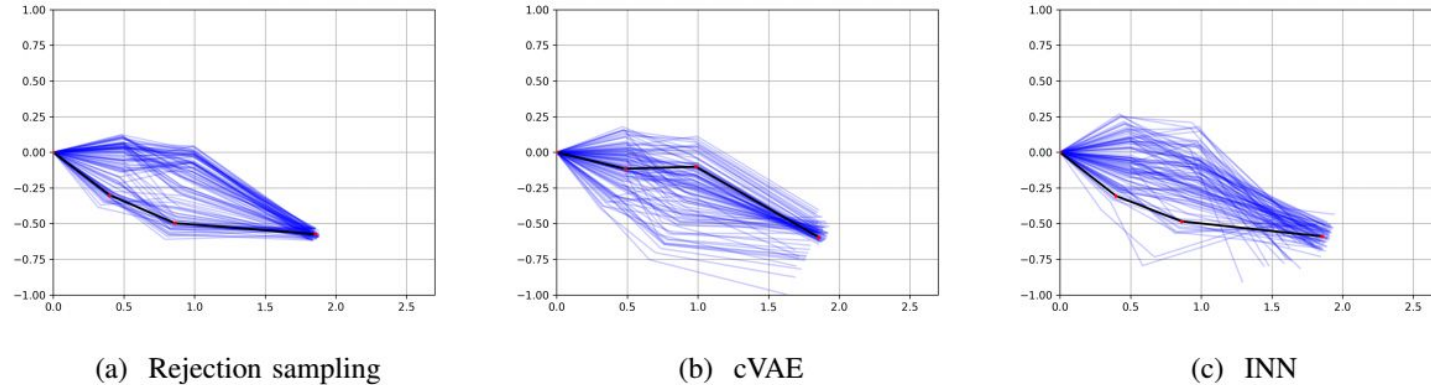


Fig. 1: Arm configuration of a planar manipulator with 3 revolute joints and end-effector position at  $(x, y) = [1.83, -0.57]$ . 100 samples are drawn from each model's predicted posterior  $\tilde{p}(x|y_{gt})$ , one random sample configuration is highlighted.

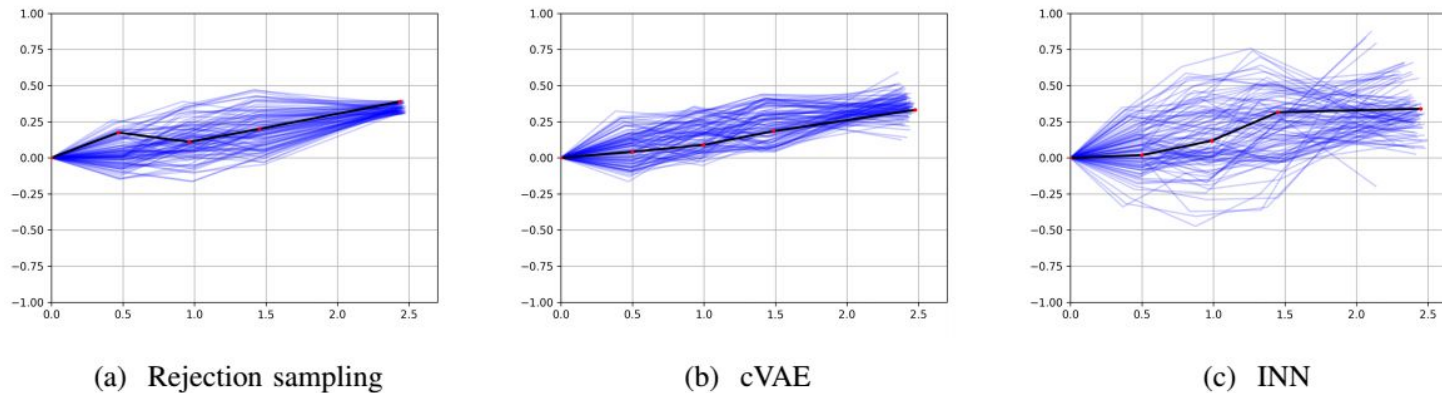


Fig. 2: Arm configuration of a planar manipulator with 4 revolute joints and end-effector position at  $(x, y) = [2.44, 0.35]$ . 100 samples are drawn from each model's predicted posterior  $\tilde{p}(x|y_{gt})$ , one random sample configuration is highlighted.



# Next Steps

1. Increase DoFs of 2D robots and see where models break
2. Extend to 3D robots
3. Hyperparameter optimization (Random Search)

# References

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# Questions