

### Data Structures and Algorithms



*Michael Thielscher*

Web Site: [webcms3.cse.unsw.edu.au/COMP9024/18s2/](http://webcms3.cse.unsw.edu.au/COMP9024/18s2/)

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## Course Convenor

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- Research: Artificial Intelligence, Robotics, General Problem-Solving Systems
- Pastimes: Fiction, Films, Food, ~~Football~~
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## ... Course Convenor

- Tutors:* Shanush Prema Thasarathan, [shanushp@cse.unsw.edu.au](mailto:shanushp@cse.unsw.edu.au)
- Friday, 1-3pm CSE Clavier Lab (LG20 in **K14**)
- Michael Manansala, [m.manansala@unsw.edu.au](mailto:m.manansala@unsw.edu.au)
- Course admin:* Michael Schofield, [mschofield@cse.unsw.edu.au](mailto:mschofield@cse.unsw.edu.au)
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## Course Goals

COMP9021 ...

- gets you thinking like a *programmer*
- solving problems by developing programs
- expressing your ideas in the language Python

COMP9024 ...

- gets you thinking like a *computer scientist*
- knowing fundamental data structures/algorithms
- able to reason about their applicability/effectiveness
- able to analyse the efficiency of programs
- able to code in C

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## ... Course Goals

5/85

COMP9021 ...

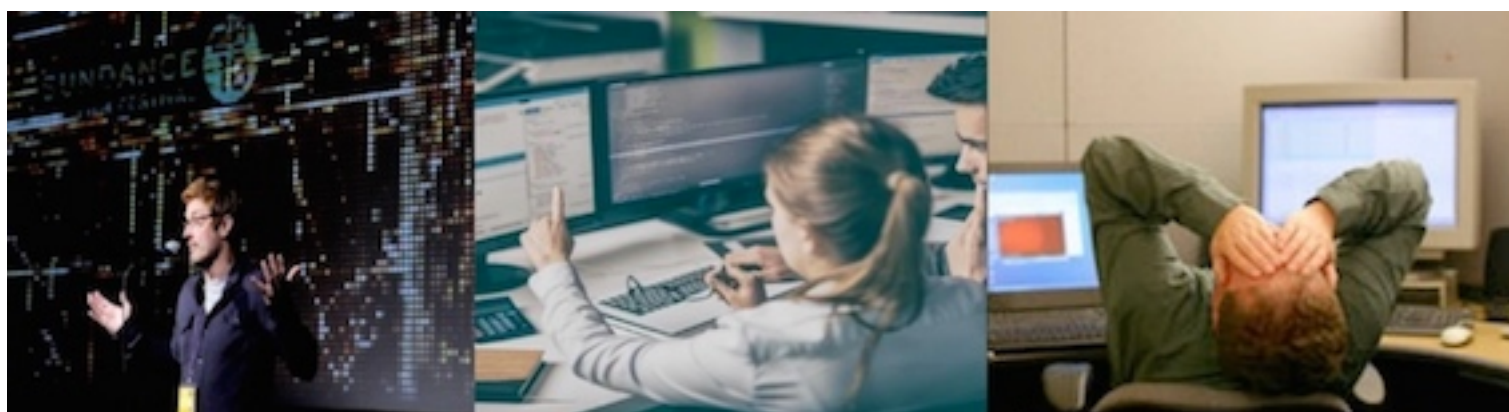


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## ... Course Goals

6/85

COMP9024 ...



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## Pre-conditions

7/85

At the *start* of this course you should be able to:

- produce correct programs from a specification
- understand the state-based model of computation

- (variables, assignment, function parameters)
  - use fundamental data structures  
(characters, numbers, strings, arrays, linked lists, binary trees)
  - use fundamental control structures (if, while, for)
  - fix simple bugs in incorrect programs
- 

## Post-conditions

8/85

At the *end* of this course you should be able to:

- choose/develop effective data structures (DS)
  - analyse performance characteristics of algorithms
  - choose/develop algorithms (A) on these DS
  - package a set of DS+A as an abstract data type
  - develop and maintain C programs
- 

## COMP9024 Themes

9/85

*Data structures*

- how to store data inside a computer for efficient use

*Algorithms*

- step-by-step process for solving a problem (within finite amount of space and time)

Major themes ...

1. Data structures, e.g. for graphs, trees
2. A variety of algorithms, e.g. on graphs, trees, strings
3. Analysis of algorithms

For data types: alternative data structures and implementation of operations

For algorithms: complexity analysis

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## Access to Course Material

10/85

All course information is placed on the main course website:

- [webcms3.cse.unsw.edu.au/COMP9024/18s2/](http://webcms3.cse.unsw.edu.au/COMP9024/18s2/)

Need to login to access material, submit assignments, post on the forum, view your marks

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## Schedule

11/85

Week	Lectures	Ch	Notes
02	Introduction, C language	M2-4,7-8	first help lab

03	Abstract data types (ADTs)	S4	
04	Dynamic data structures	M10	<a href="#">Assignment 1</a>
05	Analysis of algorithms	S2	
06	Graph data structures	S17	<a href="#">due</a>
07	Graph algorithms: graph search	S18	
08	<b>Mid-term test (Mon 12noon—Tue 12noon)</b>		
08	Graph algorithms: spanning trees, shortest paths	S20-21	<a href="#">Assignment 2</a>
09	Tree algorithms: balanced trees	S12-13	
—	<i>Mid-semester break</i>		
10	Tree algorithms: splay-, AVL-, red-black trees	S13	
11	Text processing algorithms: pattern matching	S15	<a href="#">due</a>
12	Text processing algorithms: tries, compression	S15	last help lab
13	Randomised algorithms	—	

Credits for Material

12/85

Always give credit when you use someone else's work.

Ideas for the COMP9024 material are drawn from

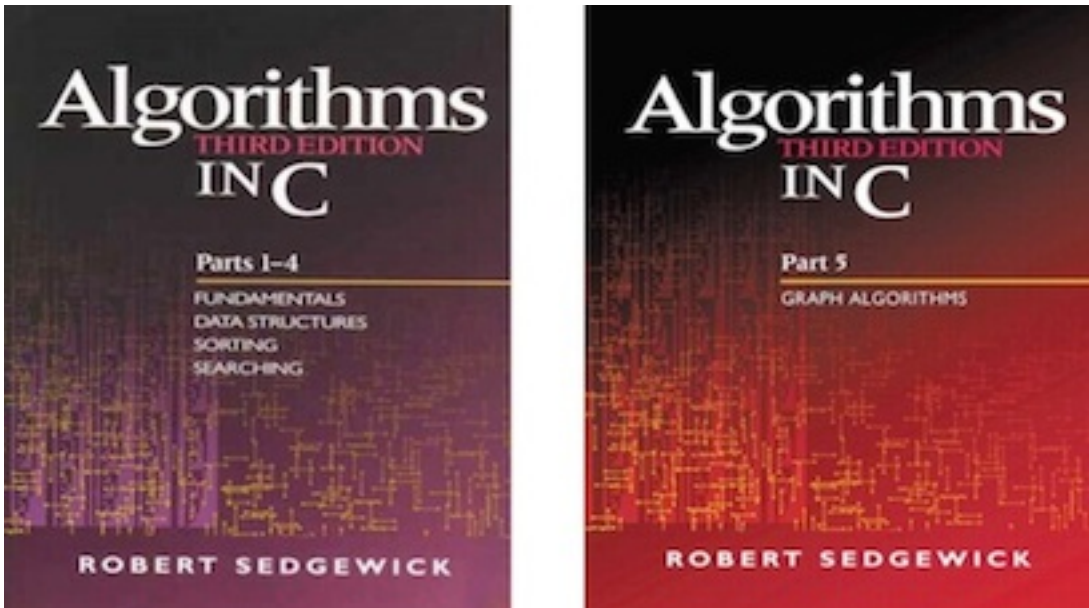
- slides by John Shepherd (COMP1927 16s2), Hui Wu (COMP9024 16s2) and Alan Blair (COMP1917 14s2)
- Robert Sedgewick's and Alistair Moffat's books, Goodrich and Tamassia's Java book, Skiena and Revilla's programming challenges book

Resources

13/85

Textbook is a "double-header"

- Algorithms in C, Parts 1-4, Robert Sedgewick
- Algorithms in C, Part 5, Robert Sedgewick



Good books, useful beyond COMP9024 (but coding style ...)

Supplementary textbook:

- Alistair Moffat  
*Programming, Problem Solving, and Abstraction with C*  
Pearson Educational, Australia, Revised edition 2013, ISBN 978-1-48-601097-4



Also, numerous online C resources are available.

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## Lectures

15/85

Lectures will:

- present theory
- demonstrate problem-solving methods
- give practical demonstrations

Lectures provide an alternative view to textbook

Lecture slides will be made available before lecture

Feel free to ask questions, but **No Idle Chatting**

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## Problem Sets

16/85

The weekly homework aims to:

- clarify any problems with lecture material
- work through exercises related to lecture topics
- give practice with algorithm design skills (think before coding)

Problem sets available on web at the time of the lecture

Sample solutions will be posted in the following week

**Do them yourself!** and **Don't fall behind!**

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# Assignments

The assignments give you experience applying tools/techniques (but to a larger programming problem than the homework)

The assignments will be carried out individually.

Both assignments will have a *Monday 11:59pm* deadline.

**15% penalty** will be applied to the maximum mark for every 24 hours late after the deadline.

- 1 day late: mark is capped to 85% of the maximum possible mark
- 2 days late: mark is capped to 70% of the maximum possible mark
- 3 days late: mark is capped to 55% of the maximum possible mark
- ...

The two assignments contribute 10% + 15% to overall mark.

## ... Assignments

Advice on doing the assignments:

They always take longer than you expect.

Don't leave them to the last minute.

Organising your time → no late penalty.

If you do leave them to the last minute:

- take the late penalty rather than copying

## Plagiarism



Just Don't Do it

We get **very annoyed** by people who plagiarise.

## ... Plagiarism

Examples of [Plagiarism](http://student.unsw.edu.au/plagiarism) (student.unsw.edu.au/plagiarism):

### 1. Copying

Using same or similar idea *without acknowledging the source*  
This includes copying ideas from a website, internet

### 2. Collusion

Presenting work as independent when produced in collusion with others  
This includes *students providing their work to another student*

Plagiarism will be checked for and **punished** (e.g. reduced mark for assignment, 0 marks for assignment, 0 marks for course)

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## Help Lab

21/85

The *help lab*:

- aims to help you if you have difficulties with the weekly programming exercises
- ... and the assignments
- non-programming exercises from problem sets may also be discussed

Fridays (Week 2-12) from 1-3pm in *CSE Clavier Lab (LG20, Bldg K14)* (walk past Keith Burrows (J14) towards Old Main)

Attendance is entirely voluntary

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## Mid-term Test

22/85

1-hour online test in week 8 (*at your own time between Mon, 10 Sep, 12noon — Tue, 11 Sep, 12noon*).

Format:

- some multiple-choice questions
- some descriptive/analytical questions with open answers

The mid-term test contributes 15% to overall mark.

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## Final Exam

23/85

2-hour ~~torture~~ written exam during the exam period.

Format:

- some multiple-choice questions
  - some descriptive/analytical questions
-

How to pass the mid-term test and the Final Exam:

- do the Homework *yourself*
  - do the Homework *every week*
  - do the Assignments *yourself*
  - practise programming outside classes
  - read the lecture notes
  - read the corresponding chapters in the textbooks
- 

## Assessment Summary

25/85

```
assn1 = mark for assignment 1    (out of 10)
assn2 = mark for assignment 2    (out of 15)
mid    = mark for mid-term test  (out of 15)
exam   = mark for final exam     (out of 60)
```

```
if (exam >= 25)
    total = assn1 + assn2 + mid + exam
else
    total = exam * (100/60)
```

To pass the course, you must achieve:

- at least **25/60** for exam
  - at least **50/100** for total
- 

## Summary

26/85

The goal is for you to become a better Computer Scientist

- more confident in your own ability to choose data structures
  - more confident in your own ability to develop algorithms
  - able to analyse and justify your choices
  - producing a better end-product
  - ultimately, enjoying the program design process
- 

## C Programming Language

### Why C?

28/85

- good example of an imperative language
  - gives the programmer great control
  - produces fast code
  - many libraries and resources
  - widely used in industry (and science)
-



# Brief History of C

- C and UNIX operating system share a complex history
  - C was originally designed for and implemented on UNIX
  - **Dennis Ritchie** was the author of C (around 1971)
  - In 1973, UNIX was rewritten in C
  - B (author: **Ken Thompson**, 1970) was the predecessor to C, but there was no A
- 

## ... Brief History of C

- B was a typeless language
  - C is a typed language
  - In 1983, American National Standards Institute (ANSI) established a committee to clean up and standardise the language
  - ANSI C standard published in 1988
    - this greatly improved source code portability
  - Current standard: C11 (published in 2011)
  - C is the main language for writing operating systems and compilers; and is commonly used for a variety of applications
- 

## Basic Structure of a C Program

<code>// include files</code>	•
<code>// global definitions</code>	•
	•
<code>// function definitions</code>	•
<code>function_type f(arguments) {</code>	•
<code>// local variables</code>	
<code>// body of function</code>	
<code>return ...;</code>	
<code>}</code>	
•	
•	

	<code>// main function</code>
	<code>int main(arguments) {</code>
	<code>// local variables</code>
	<code>// body of main function</code>
	<code>return 0;</code>
	<code>}</code>

---

## Exercise #1: What does this program compute?

```
#include <stdio.h>
```

```
int f(int m, int n) {
```

```
    while (m != n) {
        if (m > n) {
            m = m-n;
        } else {
            n = n-m;
        }
    }
```

```

    }
}
return m;
}

int main(void) {

    printf("%d\n", f(30,18));
    return 0;
}

```

## Example: Insertion Sort in C

33/85

Reminder — Insertion Sort algorithm:

```

insertionSort(A):
|   Input array A[0..n-1] of n elements
|
|   for all i=1..n-1 do
|   |   element=A[i], j=i-1
|   |   while j≥0 and A[j]>element do
|   |   |   A[j+1]=A[j]
|   |   |   j=j-1
|   |   end while
|   |   A[j+1]=element
|   end for

```

## ... Example: Insertion Sort in C

34/85

```

#include <stdio.h> // include standard I/O library defs and functions

#define SIZE 6     // define a symbolic constant

void insertionSort(int array[], int n) { // function headers must provide types
    int i; // each variable must have a type
    for (i = 1; i < n; i++) { // for-loop syntax
        int element = array[i];
        int j = i-1;
        while (j >= 0 && array[j] > element) { // logical AND
            array[j+1] = array[j];
            j--; // abbreviated assignment j=j-1
        }
        array[j+1] = element; // statements terminated by ;
    } // code blocks enclosed in { }
}

int main(void) { // main: program starts here
    int numbers[SIZE] = { 3, 6, 5, 2, 4, 1 }; // array declaration
                                              // and initialisation */

    int i;
    insertionSort(numbers, SIZE);
    for (i = 0; i < SIZE; i++)
        printf("%d\n", numbers[i]); // printf defined in <stdio>

    return 0; // return program status (here: no error) to environment
}

```

## Compiling with gcc

35/85

C source code: `prog.c`



`a.out` (executable program)

To compile a program `prog.c`, you type the following:

```
prompt$ gcc prog.c
```

To run the program, type:

```
prompt$ ./a.out
```

---

## ... Compiling with gcc

36/85

Command line options:

- The default with `gcc` is not to give you any warnings about potential problems
- Good practice is to be tough on yourself:

```
prompt$ gcc -Wall prog.c
```

which reports all warnings to anything it finds that is potentially wrong or non ANSI compliant

- The `-o` option tells `gcc` to place the compiled object in the named file rather than `a.out`

```
prompt$ gcc -o prog prog.c
```

---

## Algorithms in C

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## Basic Elements

38/85

Algorithms are built using

- assignments
- conditionals
- loops
- function calls/return statements

---

## Assignments

39/85

- In C, each statement is terminated by a semicolon `;`
- Curly brackets `{ }` used to enclose statements in a block
- Usual arithmetic operators: `+`, `-`, `*`, `/`, `%`

- Usual assignment operators: `=`, `+=`, `-=`, `*=`, `/=`, `%=`
- The operators `++` and `--` can be used to increment a variable (add 1) or decrement a variable (subtract 1)
  - It is recommended to put the increment or decrement operator after the variable:

```
// suppose k=6 initially
k++;    // increment k by 1; afterwards, k=7
n = k--; // first assign k to n, then decrement k by 1
        // afterwards, k=6 but n=7
```

- It is also possible (but NOT recommended) to put the operator before the variable:

```
// again, suppose k=6 initially
++k;    // increment k by 1; afterwards, k=7
n = --k; // first decrement k by 1, then assign k to n
        // afterwards, k=6 and n=6
```

---

## ... Assignments

40/85

C assignment statements are really expressions

- they return a result: the value being assigned
- the return value is generally ignored

Frequently, assignment is used in loop continuation tests

- to combine the test with collecting the next value
- to make the expression of such loops more concise

Example: The pattern

```
v = getNextItem();
while (v != 0) {
    process(v);
    v = getNextItem();
}
```

is often written as

```
while ((v = getNextItem()) != 0) {
    process(v);
}
```

---

## Exercise #2: What are the final values of a and b?

41/85

1.

```
a = 1; b = 5;
while (a < b) {
    a++;
    b--;
}
```

2.

```
a = 1; b = 5;
```

```
while ((a += 2) < b) {  
    b--;  
}
```

1. `a == 3, b == 3`
2. `a == 5, b == 4`

---

## Conditionals

43/85

```
if (expression) {  
    some statements;  
}
```

```
if (expression) {  
    some statements1;  
} else {  
    some statements2;  
}
```

- *some statements* executed if, and only if, the evaluation of *expression* is non-zero
- *some statements*<sub>1</sub> executed when the evaluation of *expression* is non-zero
- *some statements*<sub>2</sub> executed when the evaluation of *expression* is zero
- Statements can be single instructions or blocks enclosed in { }

---

## ... Conditionals

44/85

*Indentation* is very important in promoting the readability of the code

Each logical block of code is indented:

```
// Style 1  
if (x)  
{  
    statements;  
}
```

```
// Style 2 (preferred)  
if (x) {  
    statements;  
}
```

```
// Preferred else-if style  
if (expression1) {  
    statements1;  
} else if (exp2) {  
    statements2;  
} else if (exp3) {  
    statements3;  
} else {  
    statements4;  
}
```

---

## ... Conditionals

45/85

Relational and logical operators

`a > b`      a greater than b

a >= b      a greater than or equal b

a < b      a less than b

a <= b      a less than or equal b

a == b      a equal to b

a != b      a not equal to b

a && b      a logical **and** b

a || b      a logical **or** b

! a      logical **not** a

A relational or logical expression evaluates to **1** if true, and to **0** if false

---

### Exercise #3: Conditionals

46/85

1. What is the output of the following program?

```
if ((x > y) && !(y-x <= 0)) {  
    printf("Aye\n");  
} else {  
    printf("Nay\n");  
}
```

2. What is the resulting value of x after the following assignment?

```
x = (x >= 0) + (x < 0);
```

---

1. The condition is unsatisfiable, hence the output will always be

**Nay**

2. No matter what the value of x, one of the conditions will be true (==1) and the other false (==0)  
Hence the resulting value will be **x == 1**

---

### Sidetrack: Printing Variable Values with printf()

48/85

Formatted output written to standard output (e.g. screen)

```
printf(format-string, expr1, expr2, ...);
```

*format-string* can use the following placeholders:

%d	decimal	%f	fixed-point
%c	character	%s	string
\n	new line	\"	quotation mark



Examples:

```
num = 3;
printf("The cube of %d is %d.\n", num, num*num*num);
```

The cube of 3 is 27.

```
id  = 'z';
num = 1234567;
printf("Your \"login ID\" will be in the form of %c%d.\n", id, num);
```

Your "login ID" will be in the form of z1234567.

- Can also use width and precision:

```
printf("%8.3f\n", 3.14159);

3.142
```

---

## Loops

49/85

C has two different "while loop" constructs

<pre>// while loop while (expression) {     some statements; }</pre>	<pre>// do .. while loop do {     some statements; } while (expression);</pre>
----------------------------------------------------------------------	--------------------------------------------------------------------------------

The `do .. while` loop ensures the statements will be executed at least once

---

## ... Loops

50/85

The "for loop" in C

```
for (expr1; expr2; expr3) {
    some statements;
}
```

- `expr1` is evaluated before the loop starts
- `expr2` is evaluated at the beginning of each loop
  - if it is non-zero, the loop is repeated
- `expr3` is evaluated at the end of each loop

Example:

```
for (i = 1; i < 10; i++) {
    printf("%d %d\n", i, i * i);
}
```

---

## Exercise #4: What is the output of this program?

51/85

```

int i, j;
for (i = 8; i > 1; i /= 2) {
    for (j = i; j >= 1; j--) {
        printf("%d%d\n", i, j);
    }
    putchar( '\n' );
}

```

---

88  
87  
..  
81  
  
44  
..  
41  
  
22  
21

---

## Functions

53/85

Functions have the form

```

return-type function-name(parameters) {

    declarations

    statements

    return ...;
}

```

- if *return\_type* is **void** then the function does not return a value
  - if *parameters* is **void** then the function has no arguments
- 

## ... Functions

54/85

When a function is called:

1. memory is allocated for its parameters and local variables
  2. the parameter expressions in the calling function are evaluated
  3. C uses "call-by-value" parameter passing ...
    - the function works only on its own local copies of the parameters, not the ones in the calling function
  4. local variables need to be assigned before they are used (otherwise they will have "garbage" values)
  5. function code is executed, until the first **return** statement is reached
- 

## ... Functions

55/85

When a **return** statement is executed, the function terminates:

`return expression;`

1. the returned *expression* will be evaluated
2. all local variables and parameters will be thrown away when the function terminates
3. the calling function is free to use the returned value, or to ignore it

Example:

```
int euclid_gcd(int m, int n) {
    if (n == 0) {
        return m;
    } else {
        return euclid_gcd(n, m % n);
    }
}
```

The return statement can also be used to terminate a function of return-type `void`:

`return;`

---

# Data Structures in C

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## Basic Data Types

57/85

- In C each variable must have a type
- C has the following generic data types:

<b>char</b>	character	'A', 'e', '#', ...
<b>int</b>	integer	2, 17, -5, ...
<b>float</b>	floating-point number	3.14159, ...
<b>double</b>	double precision floating-point	3.14159265358979, ...

There are other types, which are variations on these

- Variable declaration must specify a data type and a name; they can be initialised when they are declared:

```
float x;
char ch = 'A';
int j = i;
```

---

# Basic Aggregate Data Types

---

## Aggregate Data Types

59/85

Families of aggregate data types:

- homogenous ... all elements have same base type
    - arrays (e.g. `char s[50]`, `int v[100]`)
  - heterogeneous ... elements may combine different base types
    - structures
- 

## Arrays

60/85

An *array* is

- a collection of same-type variables
- arranged as a linear sequence
- accessed using an integer subscript
- for an array of size  $N$ , valid subscripts are  $0..N-1$

Examples:

```
int  a[20];    // array of 20 integer values/variables
char b[10];    // array of 10 character values/variables
```

---

## ... Arrays

61/85

Larger example:

```
#define MAX 20

int i;          // integer value used as index
int fact[MAX];  // array of 20 integer values

fact[0] = 1;
for (i = 1; i < MAX; i++) {
    fact[i] = i * fact[i-1];
}
```

---

## Sidetrack: C Style

62/85

We can define a [symbolic constant](#) at the top of the file

```
#define SPEED_OF_LIGHT 299792458.0
#define ERROR_MESSAGE "Out of memory.\n"
```

Symbolic constants make the code easier to understand and maintain

```
#define NAME replacement_text
```

- The compiler's pre-processor will replace all occurrences of `name` with `replacement_text`
  - it will **not** make the replacement if `name` is inside quotes ("...") or part of another name
- 

## ... Sidetrack: C Style

63/85

Not strictly mandatory for COMP9024, but very useful guideline

- use proper layout, including indentation
- keep functions short and break into sub-functions as required
- use meaningful names (for variables, functions etc)

Style considerations that *do* matter for your COMP9024 assignments:

- use symbolic constants to avoid burying "magic numbers" in the code
- use indentation consistently (3 or 4 spaces, do *not* use TABs)
- comment your code

... Sidetrack: C Style

64/85

C has a reputation for allowing obscure code, leading to ...

The International Obfuscated C Code Contest

- Run each year since 1984
- Goal is to produce
  - a working C program
  - whose appearance is obscure
  - whose functionality unfathomable
- Web site: [www.ioccc.org](http://www.ioccc.org)
- 100's of examples of bizarre C code  
(understand these → you are a C master)

... Sidetrack: C Style

65/85

Most artistic code (Eric Marshall, 1986)

```
extern int
errno
;char
grrr
r,
,
P( );
choo choo\n"
) ;
| cc[ ! j ]
i ){* argv[i++ +!-i]
: i )++
0;; i++
);
/ cc[1*argc]|-1<4 ] ) ;printf("%d",P(""));}}
P ( a ) char a ; { a ; while( a > " B "
/* - by E ricM arsh all- */); }
```

... Sidetrack: C Style

66/85

```
#define o define
#o __o write
#o ooo (unsigned)
#o o_o_ 1
#o _o_ char
#o _oo goto
#o _oo_ read
#o o_o for
#o o_ main
#o o__ if
#o oo_ 0
#o _o(_,_ ,__)(void)___o(_ ,__ ,ooo(__))
#o __o (o_o_<<((o_o_<<(o_o_<<o_o_))+ (o_o_<<o_o_))+ (o_o_<<(o_o_<<(o_o_<<o_o_)))
o_(){_o_ _=oo_ ,__ ,__ ,__[__o];_oo _____;_____:_=__o-o_o_ ; _____:
_o(o_o_ ,____ ,__=(_-o_o_<__?_-o_o_:_)) ;o_o( ;__ ;_o(o_o_ ,"\b",o_o_ ) ,__--);
_o(o_o_ , " " ,o_o_ ) ;o__(--__)_oo _____ ;_o(o_o_ ,"\n",o_o_ ) ;_____ :o__( _=oo_(
oo_ ,____ ,__o))_oo _____ ;}
```

# Strings

"String" is a special word for an array of characters

- end-of-string is denoted by '**\0**' (of type char and always implemented as 0)

Example:

If a character array `s[11]` contains the string "hello", this is how it would look in memory:

0	1	2	3	4	5	6	7	8	9	10
h	e	l	l	o	\0					

# Array Initialisation

Arrays can be initialised by code, or you can specify an initial set of values in declaration.

Examples:

```
char s[6] = {'h', 'e', 'l', 'l', 'o', '\0'};

char t[6] = "hello";

int fib[20] = {1, 1};

int vec[] = {5, 4, 3, 2, 1};
```

In the third case, `fib[0] == fib[1] == 1` while the initial values `fib[2] .. fib[19]` are undefined.

In the last case, C infers the array length (as if we declared `vec[5]`).



```
1  #include <stdio.h>
2
3  int main(void) {
4      int arr[3] = {10,10,10};
5      char str[] = "Art";
6      int i;
7
8      for (i = 1; i < 3; i++) {
9          arr[i] = arr[i-1] + arr[i] + 1;
10         str[i] = str[i+1];
11     }
12     printf("Array[2] = %d\n", arr[2]);
13     printf("String = \"%s\"\n", str);
14     return 0;
15 }
```

---

Array[2] = 32  
String = "At"

---

## Arrays and Functions

71/85

When an array is passed as a parameter to a function

- the address of the start of the array is actually passed

Example:

```
int total, vec[20];
...
total = sum(vec);
```

Within the function ...

- the types of elements in the array are known
  - the size of the array is unknown
- 

### ... Arrays and Functions

72/85

Since functions do not know how large an array is:

- pass in the size of the array as an extra parameter, or
- include a "termination value" to mark the end of the array

So, the previous example would be more likely done as:

```
int total, vec[20];
```

```
...
total = sum(vec,20);
```

Also, since the function doesn't know the array size, it can't check whether we've written an invalid subscript (e.g. in the above example 100 or 20).

Exercise #6: Arrays and Functions73/85

Implement a function that sums up all elements in an array.

Use the *prototype*

```
int sum(int[], int)
```

```
int sum(int vec[], int dim) {
    int i, total = 0;

    for (i = 0; i < dim; i++) {
        total += vec[i];
    }
    return total;
}
```

Multi-dimensional Arrays75/85

Examples:

```
float q[2][2];
```

$$\begin{bmatrix} 0.5 & 2.7 \\ 3.1 & 0.1 \end{bmatrix}$$

```
int r[3][4];
```

$$\begin{bmatrix} 5 & 10 & -2 & 4 \\ 0 & 2 & 4 & 8 \\ 21 & 2 & 1 & 42 \end{bmatrix}$$

Note: `q[0][1]==2.7`   `r[1][3]==8`   `q[1]=={3.1,0.1}`

Multi-dimensional arrays can also be initialised:

```
float q[][] = {
    { 0.5, 2.7 },
    { 3.1, 0.1 }
};
```

... Multi-dimensional Arrays76/85

Iteration can be done row-by-row or column-by-column:

```

int m[NROWS][NCOLS];
int row, col;

//row-by-row
for (row = 0; row < NROWS; row++) {
    for (col = 0; col < NCOLS; col++) {
        ... m[row][col] ...
    }
}
// column-by-column
for (col = 0; col < NCOLS; col++) {
    for (row = 0; row < NROWS; row++) {
        ... m[row][col] ...
    }
}

```

Row-by-row is the most common style of iteration.

---

## Sidetrack: Defining New Data Types

77/85

C allows us to define new data type (names) via typedef:

```
typedef ExistingDataType NewTypeName;
```

Examples:

```

typedef float Temperature;

typedef int Matrix[20][20];

```

---

## ... Sidetrack: Defining New Data Types

78/85

Reasons to use typedef:

- give meaningful names to value types (documentation)
  - is a given number Temperature, Dollars, Volts, ...?
- allow for easy changes to underlying type

```

typedef float Real;
Real complex_calculation(Real a, Real b) {
    Real c = log(a+b); ... return c;
}

```

- "package up" complex type definitions for easy re-use
  - many examples to follow; Matrix is a simple example

---

## Structures

79/85

*A structure*

- is a collection of variables, perhaps of different types, grouped together under a single name
- helps to organise complicated data into manageable entities
- exposes the connection between data within an entity
- is defined using the `struct` keyword

Example:

```
typedef struct {
    int day;
    int month;
    int year;
} DateT;
```

## ... Structures

80/85

One structure can be *nested* inside another:

```
typedef struct {
    int day, month, year;
} DateT;
```

```
typedef struct {
    int hour, minute;
} TimeT;
```

```
typedef struct {
    char    plate[7];    // e.g. "DSA42X"
    double  speed;
    DateT   d;
    TimeT    t;
} TicketT;
```

## ... Structures

81/85

Possible memory layout produced for TicketT object:

D   S   A   4   2   X   \0	7 bytes + 1 padding
68.4	8 bytes
27   7   2017	12 bytes
20   45	8 bytes

Note: padding is needed to ensure that `plate` lies on a 4-byte boundary.

Don't normally care about internal layout, since fields are accessed by name.

Defining a structure itself does not allocate any memory

We need to declare a variable in order to allocate memory

```
DateT christmas;
```

The components of the structure can be accessed using the "dot" operator

```
christmas.day    =    25;
christmas.month  =    12;
christmas.year   = 2018;
```

---

With the above TicketT type, we declare and use variables as ...

```
#define NUM_TICKETS 1500

typedef struct {...} TicketT;

TicketT tickets[NUM_TICKETS]; // array of structs

// Print all speeding tickets in a readable format
for (i = 0; i < NUM_TICKETS; i++) {
    printf("%s %6.3f %d-%d-%d at %d:%d\n", tickets[i].plate,
                                                tickets[i].speed,
                                                tickets[i].d.day,
                                                tickets[i].d.month,
                                                tickets[i].d.year,
                                                tickets[i].t.hour,
                                                tickets[i].t.minute);
}
```

---

A structure can be passed as a parameter to a function:

```
void print_date(DateT d) {

    printf("%d-%d-%d\n", d.day, d.month, d.year);
}

int is_leap_year(DateT d) {

    return ( ((d.year%4 == 0) && (d.year%100 != 0))
              || (d.year%400 == 0) );
}
```

---

- Introduction to Algorithms and Data Structures
  - C programming language, compiling with `gcc`
    - Basic data types (`char`, `int`, `float`)
    - Basic programming constructs (`if ... else` conditionals, `while` loops, `for` loops)
    - Basic data structures (atomic data types, arrays, structures)
  
  - Suggested reading (Moffat):
    - introduction to C ... Ch.1; Ch.2.1-2.3, 2.5-2.6;
    - conditionals and loops ... Ch.3.1-3.3; Ch.4.1-4.4
    - arrays ... Ch.7.1,7.5-7.6
    - structures ... Ch.8.1
-