

$N(\mu, \sigma^2)$	$f(x) = \frac{1}{\sqrt{2\pi}\sigma} e^{\frac{-(x-\mu)^2}{2\sigma^2}} \quad \forall x \in \mathbb{R}$	$Z = \frac{X - \mu}{\sigma}$	$\Phi(z) = P(X \leq x) = P(\frac{X - \mu}{\sigma} \leq \frac{x - \mu}{\sigma}) = P(Z \leq z)$
Distribution	Formula	$E(X), V(X)$	Special Notes
Exponential	$f(x) = \lambda e^{-\lambda x}, \quad x \in (0, \infty)$	$\mu = \frac{1}{\lambda}, \quad \sigma^2 = \frac{1}{\lambda^2}$	λ is <i>Scale Parameter</i> that controls shape and location.
Gamma	$f(x) = \frac{\lambda^r x^{r-1} e^{-\lambda x}}{\Gamma(r)}, \quad \Gamma(r) = (r - 1)!$	$\mu = \frac{r}{\lambda}, \quad \sigma^2 = \frac{r}{\lambda^2}$	r (skew \rightarrow sym), λ (scale), Γ (Gamma fun.) model fail rate; $r \rightarrow 1$ tends to exp. dist.
Weibull	$f(x) = \frac{\beta}{\delta} \left[\frac{x}{\delta}\right]^{\beta-1} e^{-\left[\frac{x}{\delta}\right]^\beta}, \quad x \in (0, \infty)$ $F(x) = 1 - \exp\left[-\left(\frac{x}{\delta}\right)^\beta\right] \quad \forall x \in \mathbb{R}^+$	$\mu = \delta \Gamma(1 + \frac{1}{\beta})$ $\sigma^2 = \delta^2 \Gamma\left(1 + \frac{2}{\beta}\right) - \delta^2 \left[\Gamma\left(1 + \frac{1}{\beta}\right)\right]^2$	β (shape: skew to sym), δ (scale: narrow to wide); models time dependent fail rate
Lognormal	$F(x) = \Phi\left(\frac{\ln(x) - \theta}{\omega}\right)$ $f(x) = \frac{1}{\sqrt{2\pi}\omega x} \exp\left[-\frac{(\ln(x) - \theta)^2}{2\omega^2}\right]$	$\mu = e^{\theta + \omega^2/2}$ $\sigma^2 = e^{2\theta + \omega^2} (e^{\omega^2} - 1)$	Let W be normal rv. with mean θ and variance ω^2 , let $X = e^W$. $F(x) = P(X \leq x) = P(W \leq \ln(x))$ $= P(Z \leq (\ln(x) - \theta)/\omega)$
Binomial	$f(x) = \binom{n}{x} \cdot p^x \cdot (1 - p)^{n-x}, \quad \binom{n}{r} = \frac{n!}{r! (n - r)!}$	$\mu = np$ $\sigma^2 = np(1 - p)$	n is # trials, x is # success, p is the probability of a success on each trial
Poisson	$f(x) = \frac{\lambda^x e^{-\lambda}}{x!}$	$\mu = \lambda$ $\sigma^2 = \lambda$	Poisson dist. is Bernoulli Trial at infinitesimal segment ($p_{seg} = \lambda \Delta t / T, n = T / \Delta t$)
	$E(X)$	$V(x)$	
Sample	$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$	$s^2 = \frac{1}{n - 1} \sum_{i=1}^n (x_i - \bar{x})^2 = \frac{1}{n - 1} \left[\sum_{i=1}^n x_i^2 - \frac{1}{n} \left(\sum_{i=1}^n x_i \right)^2 \right]$	
Population	$\mu = \frac{1}{N} \sum_{i=1}^N x_i$	$\sigma^2 = \frac{1}{N} \sum_{i=1}^N (x_i - \mu)^2$	
Continuous RV	$\mu = \int_{-\infty}^{\infty} x \cdot f(x) dx$	$\sigma^2 = \int_{-\infty}^{\infty} (x - \mu)^2 f(x) dx$	
Discrete RV	$\mu = \sum_{i=1}^n x_i \cdot f(x_i)$	$\sigma^2 = \sum_{i=1}^n (x_i - \mu)^2 \cdot f(x_i) = \left[\sum_{i=1}^n x_i^2 \cdot f(x_i) \right] - \mu^2$	
Central Limit Theorem		Student t	
Let X_1, \dots, X_n be a random sample of size n taken from a population with mean μ and variance σ^2 . \bar{X} is sample mean:		$t = \frac{\bar{x} - \mu}{s/\sqrt{n}}$	μ is population mean, \bar{x} is sample mean, s is sample st. deviation, and n is sample size.
$Z = \frac{\bar{X} - \mu}{\sigma/\sqrt{n}}$	μ and σ should be given. If σ unknown, $n > 30 \Rightarrow \sigma \approx s$.	Like st. norm. dist., except shape of curve changes depends on the degree of freedom $k = n - 1$	
$n \geq 4$ works for normally distributed data $n \geq 30$ works for all distributions		$t_{\alpha,k}$: α is given and is the probability in range $(t_{\alpha,k} + \infty)$, k again is degree of freedom.	
Confidence Interval is the percentage $(1 - \alpha)\%$, where heads and tail both share $\alpha/2$ probability.			
	Normal Approximation	Explanation	Continuity Correction
Binomial	$Z = \frac{X - np}{\sqrt{np(1 - p)}}$	when $np > 5 \wedge n(1 - p) > 5$ the norm. approx. is good enough	A correction factor to improve approx. accuracy: Let X be a discrete rv., Y be a continuous rv.: $P(X = x_i) = P(x_i - 0.5 < Y < x_i + 0.5)$ $P(X \leq x_i) = P(Y < x_i + 0.5)$
Poisson	$Z = \frac{X - \lambda}{\sqrt{\lambda}}$	when $\lambda > 5$, the norm. approx. is good enough	
Quartiles: q_1 interpolate to $(n + 1)/4$ pos. Percentiles: interpolate to $k(n + 1)$ pos, k is a percentage. Inter-Quartile Range (IQR): $IQR = q_3 - q_1$ Whiskers: smallest/biggest within 1.5 IQR from q_1/q_3 Outliers: points beyond whiskers within 3 IQR from q_1/q_3 . Extreme Outlier: a point more than 3 IQR from q_1/q_3 . Box Plot: boxes bound by q_1, q_2, q_3 ; line extends to whiskers; outliers plotted as dots.		Probability Plotting: Plot data points for $n \leq 20$, sort data in ascending order, for each point calculate cumulative freq. $\frac{j - 0.5}{n} = P(Z \leq z_j) = \Phi(z_j)$ where j is # pt. after sorting, n is sample size. Plot cumulative freq. histogram for $n \geq 20$, choose bin size, add prev. bin height to current, divide by $n \rightarrow$ relative freq. Fit data from the center of the graph, NOT at the limits. Big variation at small, large end means sample not normal.	