

$$\begin{aligned} &Type(?cp, ConstraintProperty) \longleftrightarrow \\ &(Type(?cp, ConstraintResource) \wedge Type(?cp, Property)) \end{aligned}$$

domain and range are constraint properties:

$$\begin{aligned} &Type(domain, ConstraintProperty) \\ &Type(range, ConstraintProperty) \end{aligned}$$

domain and range define, respectively, the domain and range of a property. Recall that the domain of a property P is the set of all objects to which P applies. If the domain of P is D , then for every $P(x, y)$, $x \in D$.

$$\begin{aligned} &PropVal(domain, ?p, ?d) \longrightarrow \\ &\forall ?x \forall ?y (PropVal(?p, ?x, ?y) \longrightarrow Type(?x, ?d)) \end{aligned}$$

The range of a property P is the set of all values P can take. If the range of P is R , then for every $P(x, y)$, $y \in R$.

$$\begin{aligned} &PropVal(range, ?p, ?r) \longrightarrow \\ &\forall ?x \forall ?y (PropVal(?p, ?x, ?y) \longrightarrow Type(?y, ?r)) \end{aligned}$$

Formulas that can be inferred from the preceding ones:

$$\begin{aligned} &PropVal(domain, range, Property) \\ &PropVal(range, range, Class) \\ &PropVal(domain, domain, Property) \\ &PropVal(range, domain, Class) \end{aligned}$$

Thus we have formalized the semantics of RDF and RDFS. Software equipped with this knowledge is able to draw interesting conclusions. For example, given that the range of *rents* is *ResidentialUnit*, that *ResidentialUnit* is a subclass of *Unit*, and that *rents*(*JeffMeyer*, *BaronWayApartment*), the agent can automatically deduce *Unit*(*BaronWayApartment*) using the predicate logic semantics or one of the predicate logic proof systems.