# Bandits Meet Mechanism Design to Combat Clickbait in Online Recommendation

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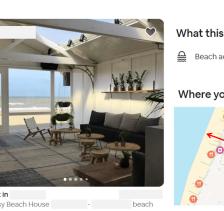
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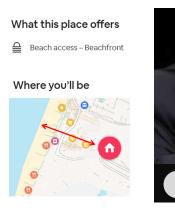
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#### Motivation

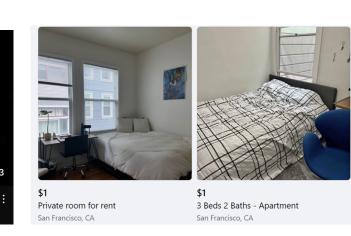
- Recommendation platforms serve as intermediates between **vendors** and **users** so as to recommend **items** from the former to the latter.
- Vendor chosen **item descriptions** are an essential aspect of the problem that is often ignored. These invite vendors to strategically exaggerate their true value in the description to increase their **click-rate**.











We combine **bandit learning** with **mechanism design** to incentivize desirable vendor strategies under uncertainty while minimizing regret.

# The Strategic Click-Bandit Problem

Every (strategic) arm  $i \in [K]$  is associated with

- 1) a **reward distribution** with mean  $\mu_i$ , and
- 2) a **click-rate**  $s_i$  which is **strategically** chosen by arm i.

#### Interaction Protocol.

- Learner commits to an algorithm M, which is shared with all arms
- <sup>2</sup> Arms choose strategies  $(s_1, \ldots, s_K) \in [0, 1]^K$ , unknown to the learner
- $_{\mathbf{3}}$  for  $t=1,\ldots,T$  do
- Algorithm M selects arm  $i_t \in [K]$
- Arm  $i_t$  is clicked with probability  $s_{i_t}$ , i.e.,  $c_{t,i_t} \sim \mathrm{Bern}(s_{i_t})$
- Arm  $i_t$  receives utility 1 from the click
  - M observes noisy post-click reward  $r_{t,i_t} \in [0,1]$  with mean  $\mu_i$ .

We must learn both the strategically chosen click-rates  $s_1, \ldots, s_K$  and the post-click rewards  $\mu_1, \ldots, \mu_K$  through repeated interaction.

**Learner's Utility.** The learner's utility of selecting an arm i with click-rate  $s_i$  and post-click value  $\mu_i$  is denoted by  $u(s_i, \mu_i)$ . As an example, consider

$$u(s,\mu) = s\mu - \lambda(s-\mu)^2.$$

However, we derive our results for a **broad class of utility functions**  $u:[0,1]\times[0,1]\to\mathbb{R}$  satisfying basic regularity assumptions (Lipschitzness ...).

**Arms' Utility.** Each arm i aims to maximize its **total number of clicks** given algorithm M and strategies  $(s_i, s_{-i})$ :

$$v_i(M,s_i,s_{-i}) := \mathbb{E}_M \left[ \sum_{t=1}^T \mathbb{I}\{i_t=i\} \ c_{t,i} \right].$$

We can also express this as  $v_i(M, s_i, s_{-i}) = \mathbb{E}_M[n_T(i)] \cdot s_i$  where  $n_T(i)$  is the number of times i has been selected by the algorithm.

# Nash Equilibrium and Strategic Regret

We study the situation where the arms respond to the learner's algorithm by playing a (possibly mixed) **Nash Equilibrium** of the general-sum game induced by the utilities  $v_1, \ldots, v_K$ .

Note that the arms' strategy space is given by [0,1]. Let  $\sigma \in \Sigma^K$  denote a mixed strategy profile, i.e., a distribution over pure strategies  $s \in [0,1]^K$ . Let

$$NE(M) := {\boldsymbol{\sigma} \in \Sigma^K : \boldsymbol{\sigma} \text{ is NE under } M}$$

denote the set of all Nash equilibria for the K arms under algorithm M.

The Strategic Regret of M under a pure-strategy NE  $s \in NE(M)$  is:

$$R_T(M, \mathbf{s}) := \mathbb{E}\left[\sum_{t=1}^T u(s^*, \mu^*) - u(s_{i_t}, \mu_{i_t})\right].$$

Accordingly, for a **mixed-strategy NE**  $\sigma \in NE(M)$ :

$$R_T(M, \boldsymbol{\sigma}) := \mathbb{E}_{\boldsymbol{s} \sim \boldsymbol{\sigma}}[R_T(M, \boldsymbol{s})].$$

Strong Strategic Regret is defined under the worst-case NE in NE(M):

$$R_T^+(M) := \max_{\boldsymbol{\sigma} \in NE(M)} R_T(M, \boldsymbol{\sigma}).$$

Weak Strategic Regret is defined under the best-case NE in NE(M):

$$R_T^-(M) := \min_{\boldsymbol{\sigma} \in \operatorname{NE}(M)} R_T(M, \boldsymbol{\sigma}).$$

Naturally,  $R_T^-(M) \leq R_T^+(M)$ .

# **Limitations of Incentive-Unaware Learning**

**Proposition** (simplified). The algorithm with **oracle knowledge** of both the post-click rewards  $\mu_1, \ldots, \mu_K$  and arm strategies  $s_1, \ldots, s_K$ , and every round  $t \in [T]$  plays the utility maximizing arm

$$i_t = \operatorname*{argmax} u(s_i, \mu_i)$$

suffers linear regret  $\Omega(T)$  in every Nash equilibrium of the arms.

The above suggests that any **incentive-unaware** algorithm that is oblivious to the strategic nature of the arms will fail to achieve low regret.

#### **No-Regret Incentive-Aware Learning**

From past observations, we construct **lower** and **upper confidences** on the arms' **strategies** (i.e., click-rates) and the **mean post-click rewards** denoted  $\underline{s}_i^t$  and  $\overline{s}_i^t$  and  $\underline{\mu}_i^t$ , respectively

While playing optimistically w.r.t.  $\mu_1, \ldots, \mu_K$ , we **threaten arms with elimination** if we **detect** them deviating from the desired strategies, i.e., the strategies maximizing the learner's utility.

If we can show that the threat of elimination is **credible** and **justified** it will incentivize arms to play approximately the desired strategies.

#### Mechanism 0: UCB with Screening (UCB-S)

# Characterizing the Nash Equilibria under UCB-S

Let  $\Delta_i := \mu^* - \mu_i$  with  $\mu^* := \max_{j \in [K]} \mu_j$ . Let  $s^*(\mu) := \operatorname{argmax}_{s \in [0,1]} u(s,\mu)$  denote the strategy maximizing the learner's utility u given post-click reward  $\mu$ . Hence,  $s^*(\mu_i)$  is the **desired strategy** for arm i.

**Theorem** (simplified): For every pure-strategy profile in the support of a Nash equilibrium, i.e.,  $s \in \operatorname{supp}(\sigma)$  with  $\sigma \in \operatorname{NE}(\operatorname{UCB-S})$ , we find that

$$s_i = s^*(\mu_i) + O\left(\sqrt{\frac{K\log(T)}{T}} \vee \Delta_i\right).$$

Due to our **uncertainty** about the arms' **strategies** and **rewards**, we can only **approximately** incentivize the desired strategies  $s^*(\mu_1), \ldots, s^*(\mu_K)$ .

In particular, under the UCB-S Mechanism every arm i's strategy is  $\tilde{O}(\sqrt{K/T} \vee \Delta_i)$  close to the desired strategy.

# **Strong Strategic Regret of UCB-S**

**Theorem** (simplified): The strong strategic regret of UCB-S is bounded as

$$R_T(\text{UCB-S}) = O\left(\sqrt{KT\log(T)}\right)$$

That is, the **upper bound** holds for **every** equilibrium  $\sigma \in NE(UCB-S)$ .

A more detailed bound (see paper) can be derived consisting of a first term due to the arms exploiting UCB-S' uncertainty about their strategies, and a second term due to the standard MAB regret.

#### Lower Bound on Weak Strategic Regret

**Theorem** (simplified): For any algorithm M there exists a problem instance such that the algorithm M suffers weak strategic regret  $R_T^-(M) = \Omega(\sqrt{KT})$ .

That is, any algorithm M suffers at least regret  $R_T(M, \sigma) = \Omega(\sqrt{KT})$  in **every** of its incentivized equilibria  $\sigma \in NE(M)$ .