Convolutional neural networks

In this notebook, we'll put together our convolutional layers to implement a 3-layer CNN. Then, we'll ask you to implement a CNN that can achieve > 65% validation error on CIFAR-10.

If you have not completed the Spatial BatchNorm Notebook, please see the following description from that notebook:

Please copy and paste your prior implemented code from HW #4 to start this assignment. If you did not correctly implement the layers in HW #4, you may collaborate with a classmate to use their layer implementations from HW #4. You may also visit TA or Prof OH to correct your implementation.

You'll want to copy and paste from HW #4:

```
    - layers.py for your FC network layers, as well as batchnorm and
    dropout.
    - layer_utils.py for your combined FC network layers.
    - optim.py for your optimizers.
```

Be sure to place these in the `nndl/` directory so they're imported correctly. Note, as announced in class, we will not be releasing our solutions.

In [ ]:

```
# As usual, a bit of setup

import numpy as np
import matplotlib.pyplot as plt
from nndl.cnn import *
from utils.data_utils import get_CIFAR10_data
from utils.gradient_check import eval_numerical_gradient_array, eval_numerical_gradie
from nndl.layers import *
from nndl.conv_layers import *
from utils.fast_layers import *
from utils.solver import Solver

%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'

# for auto-reloading external modules
# see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
%load_ext autoreload
%autoreload 2

def rel_error(x, y):
  """ returns relative error """
  return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

```
The autoreload extension is already loaded. To reload it, use:
  %reload_ext autoreload
```

In [ ]:

```
# Load the (preprocessed) CIFAR10 data.

data = get_CIFAR10_data()
for k in data.keys():
  print('{}: {} '.format(k, data[k].shape))
```

```
X_train: (49000, 3, 32, 32)
y_train: (49000,)
X_val: (1000, 3, 32, 32)
y_val: (1000,)
X_test: (1000, 3, 32, 32)
y_test: (1000,)
```

Three layer CNN

In this notebook, you will implement a three layer CNN. The `ThreeLayerConvNet` class is in `nndl/cnn.py`. You'll need to modify that code for this section, including the initialization, as well as the calculation of the loss and gradients. You should be able to use the building blocks you have either earlier coded or that we have provided. Be sure to use the fast layers.

The architecture of this CNN will be:

conv - relu - 2x2 max pool - affine - relu - affine - softmax

We won't use batchnorm yet. You've also done enough of these to know how to debug; use the cells below.

Note: As we are implementing several layers CNN networks. The gradient error can be expected for the `eval_numerical_gradient()` function. If your `W1 max relative error` and `W2 max relative error` are around or below 0.01, they should be acceptable. Other errors should be less than 1e-5.

In [ ]:

```
num_inputs = 2
input_dim = (3, 16, 16)
reg = 0.0
num_classes = 10
X = np.random.randn(num_inputs, *input_dim)
y = np.random.randint(num_classes, size=num_inputs)

model = ThreeLayerConvNet(num_filters=3, filter_size=3,
                          input_dim=input_dim, hidden_dim=7,
                          dtype=np.float64)
loss, grads = model.loss(X, y)
for param_name in sorted(grads):
    f = lambda _: model.loss(X, y)[0]
    param_grad_num = eval_numerical_gradient(f, model.params[param_name], verbose=Fal
    e = rel_error(param_grad_num, grads[param_name])
    print('{} max relative error: {}'.format(param_name, rel_error(param_grad_num, gr
```

```
W1 max relative error: 0.0002488501764834004
W2 max relative error: 0.003948945800855896
W3 max relative error: 0.00021886323984299767
b1 max relative error: 8.85599468158084e-06
b2 max relative error: 1.5716398688532598e-07
b3 max relative error: 1.7369077067956374e-09
```

Overfit small dataset

To check your CNN implementation, let's overfit a small dataset.

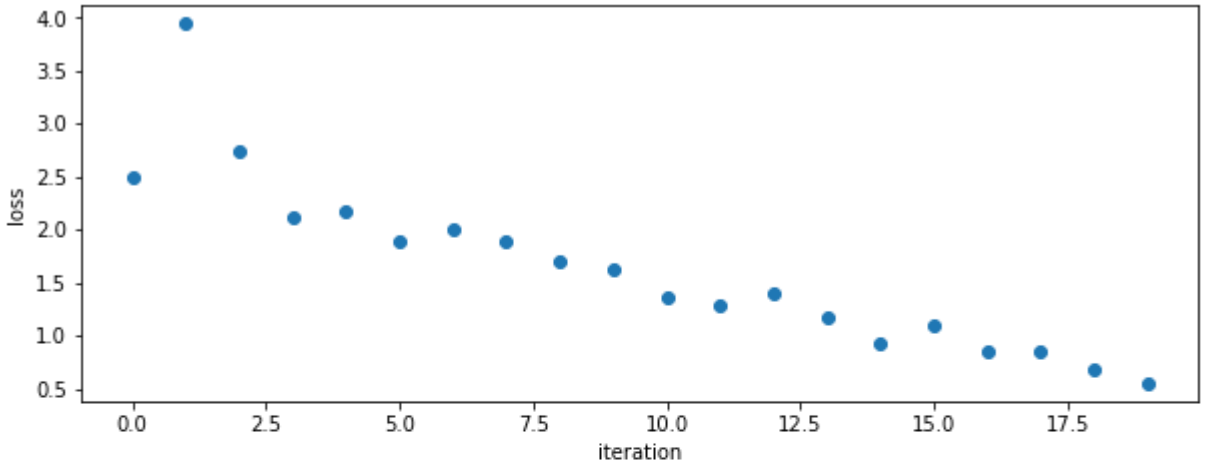
In [ ]:

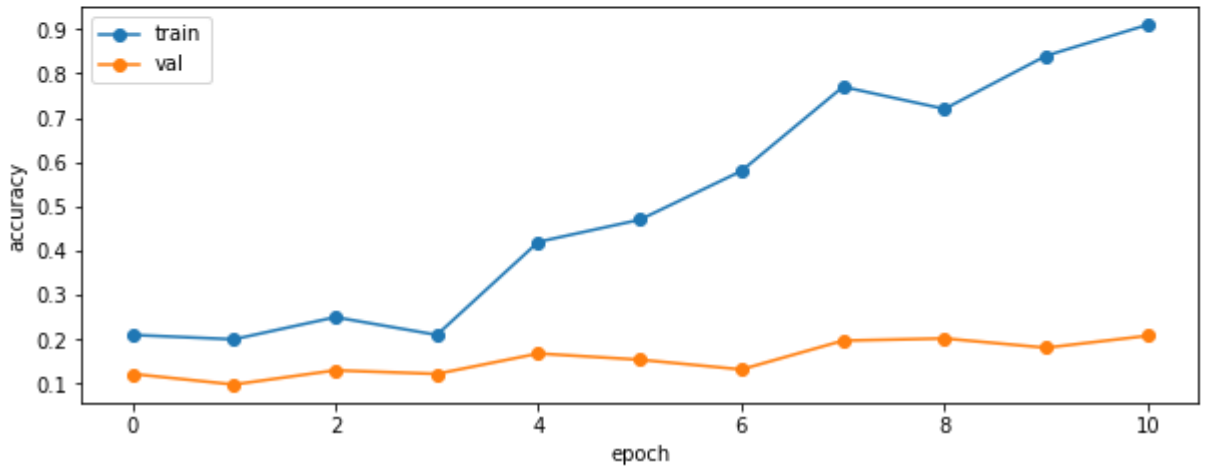
```
num_train = 100
small_data = {
  'X_train': data['X_train'][:num_train],
  'y_train': data['y_train'][:num_train],
  'X_val': data['X_val'],
  'y_val': data['y_val'],
}

model = ThreeLayerConvNet(weight_scale=1e-2)

solver = Solver(model, small_data,
                num_epochs=10, batch_size=50,
                update_rule='adam',
                optim_config={
                  'learning_rate': 1e-3,
                },
                verbose=True, print_every=1)
solver.train()
```

```
(Iteration 1 / 20) loss: 2.494793
(Epoch 0 / 10) train acc: 0.210000; val_acc: 0.122000
(Iteration 2 / 20) loss: 3.949324
(Epoch 1 / 10) train acc: 0.200000; val_acc: 0.098000
(Iteration 3 / 20) loss: 2.747618
(Iteration 4 / 20) loss: 2.114993
(Epoch 2 / 10) train acc: 0.250000; val_acc: 0.130000
(Iteration 5 / 20) loss: 2.181091
(Iteration 6 / 20) loss: 1.882443
(Epoch 3 / 10) train acc: 0.210000; val_acc: 0.122000
(Iteration 7 / 20) loss: 1.997152
(Iteration 8 / 20) loss: 1.891769
(Epoch 4 / 10) train acc: 0.420000; val_acc: 0.168000
(Iteration 9 / 20) loss: 1.692051
(Iteration 10 / 20) loss: 1.630298
(Epoch 5 / 10) train acc: 0.470000; val_acc: 0.154000
(Iteration 11 / 20) loss: 1.355024
(Iteration 12 / 20) loss: 1.279636
(Epoch 6 / 10) train acc: 0.580000; val_acc: 0.132000
(Iteration 13 / 20) loss: 1.390850
(Iteration 14 / 20) loss: 1.177008
(Epoch 7 / 10) train acc: 0.770000; val_acc: 0.197000
(Iteration 15 / 20) loss: 0.931049
(Iteration 16 / 20) loss: 1.095090
(Epoch 8 / 10) train acc: 0.720000; val_acc: 0.202000
(Iteration 17 / 20) loss: 0.847036
(Iteration 18 / 20) loss: 0.851923
(Epoch 9 / 10) train acc: 0.840000; val_acc: 0.181000
(Iteration 19 / 20) loss: 0.672591
(Iteration 20 / 20) loss: 0.556128
(Epoch 10 / 10) train acc: 0.910000; val_acc: 0.208000
```

In [ ]:

```
plt.subplot(2, 1, 1)
plt.plot(solver.loss_history, 'o')
plt.xlabel('iteration')
plt.ylabel('loss')

plt.subplot(2, 1, 2)
plt.plot(solver.train_acc_history, '-o')
plt.plot(solver.val_acc_history, '-o')
plt.legend(['train', 'val'], loc='upper left')
plt.xlabel('epoch')
plt.ylabel('accuracy')
plt.show()
```





Train the network

Now we train the 3 layer CNN on CIFAR-10 and assess its accuracy.

In [ ]:

```
model = ThreeLayerConvNet(weight_scale=0.001, hidden_dim=500, reg=0.001)

solver = Solver(model, data,
                num_epochs=1, batch_size=50,
                update_rule='adam',
                optim_config={
                  'learning_rate': 1e-3,
                },
                verbose=True, print_every=20)
solver.train()
```

```
(Iteration 1 / 980) loss: 2.304764
(Epoch 0 / 1) train acc: 0.103000; val_acc: 0.107000
(Iteration 21 / 980) loss: 2.425069
(Iteration 41 / 980) loss: 2.092212
(Iteration 61 / 980) loss: 1.993756
(Iteration 81 / 980) loss: 1.884502
(Iteration 101 / 980) loss: 1.939821
(Iteration 121 / 980) loss: 1.874147
(Iteration 141 / 980) loss: 1.604520
(Iteration 161 / 980) loss: 1.665388
(Iteration 181 / 980) loss: 1.597035
(Iteration 201 / 980) loss: 1.944901
(Iteration 221 / 980) loss: 1.748709
(Iteration 241 / 980) loss: 1.802607
(Iteration 261 / 980) loss: 1.551756
(Iteration 281 / 980) loss: 1.732312
(Iteration 301 / 980) loss: 1.787897
(Iteration 321 / 980) loss: 1.776285
(Iteration 341 / 980) loss: 1.794188
(Iteration 361 / 980) loss: 1.215740
(Iteration 381 / 980) loss: 1.932686
(Iteration 401 / 980) loss: 1.743341
(Iteration 421 / 980) loss: 1.942593
(Iteration 441 / 980) loss: 1.971735
(Iteration 461 / 980) loss: 1.554475
(Iteration 481 / 980) loss: 1.663659
(Iteration 501 / 980) loss: 1.699227
(Iteration 521 / 980) loss: 1.630995
(Iteration 541 / 980) loss: 1.751090
(Iteration 561 / 980) loss: 1.676828
(Iteration 581 / 980) loss: 1.541406
(Iteration 601 / 980) loss: 1.754407
(Iteration 621 / 980) loss: 1.378506
(Iteration 641 / 980) loss: 1.744322
(Iteration 661 / 980) loss: 1.509168
(Iteration 681 / 980) loss: 1.520740
(Iteration 701 / 980) loss: 1.366820
(Iteration 721 / 980) loss: 1.715713
(Iteration 741 / 980) loss: 1.916641
(Iteration 761 / 980) loss: 1.691096
(Iteration 781 / 980) loss: 1.618696
(Iteration 801 / 980) loss: 1.405078
(Iteration 821 / 980) loss: 1.464352
(Iteration 841 / 980) loss: 1.449771
(Iteration 861 / 980) loss: 1.480750
(Iteration 881 / 980) loss: 1.653143
(Iteration 901 / 980) loss: 1.332100
(Iteration 921 / 980) loss: 1.723188
(Iteration 941 / 980) loss: 1.579345
(Iteration 961 / 980) loss: 1.933270
(Epoch 1 / 1) train acc: 0.491000; val_acc: 0.499000
```

Get > 65% validation accuracy on CIFAR-10.

In the last part of the assignment, we'll now ask you to train a CNN to get better than 65% validation accuracy on CIFAR-10.

Things you should try:

- Filter size: Above we used 7x7; but VGGNet and onwards showed stacks of 3x3 filters are good.
- Number of filters: Above we used 32 filters. Do more or fewer do better?
- Batch normalization: Try adding spatial batch normalization after convolution layers and vanilla batch normalization aafter affine layers. Do your networks train faster?
- Network architecture: Can a deeper CNN do better? Consider these architectures:
  - [conv-relu-pool]xN - conv - relu - [affine]xM - [softmax or SVM]
  - [conv-relu-pool]XN - [affine]XM - [softmax or SVM]
  - [conv-relu-conv-relu-pool]xN - [affine]xM - [softmax or SVM]

Tips for training

For each network architecture that you try, you should tune the learning rate and regularization strength. When doing this there are a couple important things to keep in mind:

- If the parameters are working well, you should see improvement within a few hundred iterations
- Remember the coarse-to-fine approach for hyperparameter tuning: start by testing a large range of hyperparameters for just a few training iterations to find the combinations of parameters that are working at all.
- Once you have found some sets of parameters that seem to work, search more finely around these parameters. You may need to train for more epochs.

In [ ]:

```
# ================================================================ #
# YOUR CODE HERE:
#   Implement a CNN to achieve greater than 65% validation accuracy
#   on CIFAR-10.
# ================================================================ #

model = CNN(weight_scale=0.001, hidden_dim=[500,500],
            reg=0.001,filter_size=[3, 3, 3], num_filters =[16, 16, 16],
            use_batchnorm=True)
solver = Solver(model, data,
                num_epochs=15, batch_size=100,
                update_rule='adam',
                optim_config={
                  'learning_rate': 1e-3
                },
                lr_decay = 0.9,
                verbose=True, print_every=40)
solver.train()
print('Best Validation Accuracy: {}'.format(solver.best_val_acc))# ==================
# END YOUR CODE HERE
# ================================================================ #
```

```
(Iteration 1 / 7350) loss: 2.302655
(Epoch 0 / 15) train acc: 0.110000; val_acc: 0.113000
(Iteration 41 / 7350) loss: 1.803508
(Iteration 81 / 7350) loss: 1.734403
(Iteration 121 / 7350) loss: 1.606335
(Iteration 161 / 7350) loss: 1.465869
(Iteration 201 / 7350) loss: 1.577258
(Iteration 241 / 7350) loss: 1.283124
(Iteration 281 / 7350) loss: 1.473341
(Iteration 321 / 7350) loss: 1.562898
(Iteration 361 / 7350) loss: 1.390258
(Iteration 401 / 7350) loss: 1.359348
(Iteration 441 / 7350) loss: 1.194664
(Iteration 481 / 7350) loss: 1.313071
(Epoch 1 / 15) train acc: 0.487000; val_acc: 0.481000
(Iteration 521 / 7350) loss: 1.181209
(Iteration 561 / 7350) loss: 1.270262
(Iteration 601 / 7350) loss: 1.374345
(Iteration 641 / 7350) loss: 1.233254
(Iteration 681 / 7350) loss: 1.303247
(Iteration 721 / 7350) loss: 1.195112
(Iteration 761 / 7350) loss: 1.311840
(Iteration 801 / 7350) loss: 1.184776
(Iteration 841 / 7350) loss: 1.386791
(Iteration 881 / 7350) loss: 1.143339
(Iteration 921 / 7350) loss: 1.087335
(Iteration 961 / 7350) loss: 1.165306
(Epoch 2 / 15) train acc: 0.579000; val_acc: 0.586000
(Iteration 1001 / 7350) loss: 1.213739
(Iteration 1041 / 7350) loss: 1.130376
(Iteration 1081 / 7350) loss: 1.173637
(Iteration 1121 / 7350) loss: 1.057551
(Iteration 1161 / 7350) loss: 0.956618
(Iteration 1201 / 7350) loss: 1.149916
(Iteration 1241 / 7350) loss: 1.048252
(Iteration 1281 / 7350) loss: 1.183427
(Iteration 1321 / 7350) loss: 1.020264
(Iteration 1361 / 7350) loss: 1.081342
(Iteration 1401 / 7350) loss: 1.041560
(Iteration 1441 / 7350) loss: 0.923697
(Epoch 3 / 15) train acc: 0.673000; val_acc: 0.625000
(Iteration 1481 / 7350) loss: 1.119976
(Iteration 1521 / 7350) loss: 1.146043
(Iteration 1561 / 7350) loss: 0.914440
(Iteration 1601 / 7350) loss: 1.020548
(Iteration 1641 / 7350) loss: 1.106134
(Iteration 1681 / 7350) loss: 0.910226
(Iteration 1721 / 7350) loss: 0.982581
(Iteration 1761 / 7350) loss: 0.996144
(Iteration 1801 / 7350) loss: 1.125041
(Iteration 1841 / 7350) loss: 0.989074
(Iteration 1881 / 7350) loss: 1.045669
(Iteration 1921 / 7350) loss: 1.015760
(Epoch 4 / 15) train acc: 0.676000; val_acc: 0.659000
(Iteration 1961 / 7350) loss: 1.058606
(Iteration 2001 / 7350) loss: 0.969773
(Iteration 2041 / 7350) loss: 0.928150
(Iteration 2081 / 7350) loss: 0.900460
(Iteration 2121 / 7350) loss: 0.822955
(Iteration 2161 / 7350) loss: 1.010296
```

```
(Iteration 2201 / 7350) loss: 0.908979
(Iteration 2241 / 7350) loss: 1.105357
(Iteration 2281 / 7350) loss: 0.765039
(Iteration 2321 / 7350) loss: 0.909188
(Iteration 2361 / 7350) loss: 0.760542
(Iteration 2401 / 7350) loss: 0.976452
(Iteration 2441 / 7350) loss: 0.661224
(Epoch 5 / 15) train acc: 0.692000; val_acc: 0.648000
(Iteration 2481 / 7350) loss: 0.864581
(Iteration 2521 / 7350) loss: 0.834735
(Iteration 2561 / 7350) loss: 1.022388
(Iteration 2601 / 7350) loss: 0.883391
(Iteration 2641 / 7350) loss: 0.707082
(Iteration 2681 / 7350) loss: 0.977329
(Iteration 2721 / 7350) loss: 0.974723
(Iteration 2761 / 7350) loss: 0.927258
(Iteration 2801 / 7350) loss: 1.018892
(Iteration 2841 / 7350) loss: 0.904486
(Iteration 2881 / 7350) loss: 0.802790
(Iteration 2921 / 7350) loss: 0.858995
(Epoch 6 / 15) train acc: 0.728000; val_acc: 0.658000
(Iteration 2961 / 7350) loss: 0.971352
(Iteration 3001 / 7350) loss: 0.880387
(Iteration 3041 / 7350) loss: 0.809605
(Iteration 3081 / 7350) loss: 0.651819
(Iteration 3121 / 7350) loss: 0.662147
(Iteration 3161 / 7350) loss: 0.984978
(Iteration 3201 / 7350) loss: 0.761012
(Iteration 3241 / 7350) loss: 0.801878
(Iteration 3281 / 7350) loss: 0.844731
(Iteration 3321 / 7350) loss: 0.933035
(Iteration 3361 / 7350) loss: 0.876903
(Iteration 3401 / 7350) loss: 0.717079
(Epoch 7 / 15) train acc: 0.757000; val_acc: 0.655000
(Iteration 3441 / 7350) loss: 0.826276
(Iteration 3481 / 7350) loss: 0.699664
(Iteration 3521 / 7350) loss: 0.780981
(Iteration 3561 / 7350) loss: 0.763232
(Iteration 3601 / 7350) loss: 0.861797
(Iteration 3641 / 7350) loss: 0.786876
(Iteration 3681 / 7350) loss: 0.770379
(Iteration 3721 / 7350) loss: 0.809672
(Iteration 3761 / 7350) loss: 0.633032
(Iteration 3801 / 7350) loss: 0.843253
(Iteration 3841 / 7350) loss: 0.897674
(Iteration 3881 / 7350) loss: 0.872241
(Epoch 8 / 15) train acc: 0.764000; val_acc: 0.686000
(Iteration 3921 / 7350) loss: 0.779082
(Iteration 3961 / 7350) loss: 0.846202
(Iteration 4001 / 7350) loss: 0.647722
(Iteration 4041 / 7350) loss: 0.675294
(Iteration 4081 / 7350) loss: 0.866707
(Iteration 4121 / 7350) loss: 0.747921
(Iteration 4161 / 7350) loss: 0.622123
(Iteration 4201 / 7350) loss: 0.706008
(Iteration 4241 / 7350) loss: 0.679787
(Iteration 4281 / 7350) loss: 0.801655
(Iteration 4321 / 7350) loss: 0.833604
(Iteration 4361 / 7350) loss: 0.704306
(Iteration 4401 / 7350) loss: 0.710069
```

```
(Epoch 9 / 15) train acc: 0.790000; val_acc: 0.668000
(Iteration 4441 / 7350) loss: 0.616289
(Iteration 4481 / 7350) loss: 0.649706
(Iteration 4521 / 7350) loss: 0.566045
(Iteration 4561 / 7350) loss: 0.713105
(Iteration 4601 / 7350) loss: 0.709793
(Iteration 4641 / 7350) loss: 0.738260
(Iteration 4681 / 7350) loss: 0.776508
(Iteration 4721 / 7350) loss: 0.770573
(Iteration 4761 / 7350) loss: 0.710020
(Iteration 4801 / 7350) loss: 0.797737
(Iteration 4841 / 7350) loss: 0.694705
(Iteration 4881 / 7350) loss: 0.524104
(Epoch 10 / 15) train acc: 0.785000; val_acc: 0.679000
(Iteration 4921 / 7350) loss: 0.729449
(Iteration 4961 / 7350) loss: 0.807470
(Iteration 5001 / 7350) loss: 0.655969
(Iteration 5041 / 7350) loss: 0.633908
(Iteration 5081 / 7350) loss: 0.657515
(Iteration 5121 / 7350) loss: 0.710987
(Iteration 5161 / 7350) loss: 0.687206
(Iteration 5201 / 7350) loss: 0.555943
(Iteration 5241 / 7350) loss: 0.649028
(Iteration 5281 / 7350) loss: 0.745905
(Iteration 5321 / 7350) loss: 0.846878
(Iteration 5361 / 7350) loss: 0.696988
(Epoch 11 / 15) train acc: 0.807000; val_acc: 0.687000
(Iteration 5401 / 7350) loss: 0.579288
(Iteration 5441 / 7350) loss: 0.670022
(Iteration 5481 / 7350) loss: 0.561476
(Iteration 5521 / 7350) loss: 0.691800
(Iteration 5561 / 7350) loss: 0.656277
(Iteration 5601 / 7350) loss: 0.718212
(Iteration 5641 / 7350) loss: 0.640236
(Iteration 5681 / 7350) loss: 0.571131
(Iteration 5721 / 7350) loss: 0.578667
(Iteration 5761 / 7350) loss: 0.591127
(Iteration 5801 / 7350) loss: 0.692456
(Iteration 5841 / 7350) loss: 0.561948
(Epoch 12 / 15) train acc: 0.809000; val_acc: 0.662000
(Iteration 5881 / 7350) loss: 0.630199
(Iteration 5921 / 7350) loss: 0.595757
(Iteration 5961 / 7350) loss: 0.512781
(Iteration 6001 / 7350) loss: 0.669341
(Iteration 6041 / 7350) loss: 0.549278
(Iteration 6081 / 7350) loss: 0.698475
(Iteration 6121 / 7350) loss: 0.625605
(Iteration 6161 / 7350) loss: 0.686786
(Iteration 6201 / 7350) loss: 0.674485
(Iteration 6241 / 7350) loss: 0.629728
(Iteration 6281 / 7350) loss: 0.592154
(Iteration 6321 / 7350) loss: 0.555192
(Iteration 6361 / 7350) loss: 0.543404
(Epoch 13 / 15) train acc: 0.832000; val_acc: 0.693000
(Iteration 6401 / 7350) loss: 0.621833
(Iteration 6441 / 7350) loss: 0.595530
(Iteration 6481 / 7350) loss: 0.614688
(Iteration 6521 / 7350) loss: 0.585853
(Iteration 6561 / 7350) loss: 0.557021
(Iteration 6601 / 7350) loss: 0.654462
```

```
(Iteration 6641 / 7350) loss: 0.577992
(Iteration 6681 / 7350) loss: 0.657395
(Iteration 6721 / 7350) loss: 0.584414
(Iteration 6761 / 7350) loss: 0.533019
(Iteration 6801 / 7350) loss: 0.599832
(Iteration 6841 / 7350) loss: 0.472208
(Epoch 14 / 15) train acc: 0.845000; val_acc: 0.679000
(Iteration 6881 / 7350) loss: 0.569957
(Iteration 6921 / 7350) loss: 0.492671
(Iteration 6961 / 7350) loss: 0.515164
(Iteration 7001 / 7350) loss: 0.517872
(Iteration 7041 / 7350) loss: 0.692366
(Iteration 7081 / 7350) loss: 0.575629
(Iteration 7121 / 7350) loss: 0.541320
(Iteration 7161 / 7350) loss: 0.549571
(Iteration 7201 / 7350) loss: 0.579445
(Iteration 7241 / 7350) loss: 0.540459
(Iteration 7281 / 7350) loss: 0.465794
(Iteration 7321 / 7350) loss: 0.643577
(Epoch 15 / 15) train acc: 0.862000; val_acc: 0.687000
Best Validation Accuracy: 0.693
```