

The compositionality of neural networks: integrating symbolism and connectionism

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The appropriateness of neural models

Testing
compositionality

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- ▶ “Modern approaches [...] do not explicitly formulate and execute compositional paths” (Johnson et al., 2017)

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The appropriateness of neural models

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- ▶ “Neural network models lack the ability to extract systematic rules” (Lake and Baroni, 2018)

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- ▶ “[...] neural networks are essentially very large correlation engines that hone in on any statistical, potentially spurious pattern” (Hudson and Manning, 2018)

The appropriateness of neural models

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- ▶ “They do not learn in a compositional way” (Liška et al., 2018)
- ▶ “[...] neural networks are essentially very large correlation engines that hone in on any statistical, potentially spurious pattern” (Hudson and Manning, 2018)
- ▶ Neural networks are data-hungry because they don't develop re-usable representations (almost everyone)



Mathijs Mul



Verna Dankers



Elia Bruni

What is compositionality

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The principle of compositionality

The meaning of a complex expression is determined by the meanings of its constituents and by its structure

Szabó (2000)

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The principle of compositionality

The meaning of a complex expression is determined by the meanings of its constituents and by its structure

Szabó (2000)

The meaning of a whole is a function of the meanings of the parts and of the way they are syntactically combined.

Partee (1995)

What is compositionality

What does it mean that neural networks are not compositional?

- ▶ They find different parts than we expect
- ▶ They find different rules than we expect
- ▶ They find other aspects of the data more salient
- ▶ They cannot represent hierarchy

What is compositionality

What does it mean that neural networks are not compositional?

- ▶ They find different parts than we expect
- ▶ They find different rules than we expect
- ▶ They find other aspects of the data more salient

- ▶ They favour modelling exceptions over learning rules
- ▶ They are not getting the right signal from the data
- ▶ The 'test' data is distributionally too different from the training data
- ▶ ...

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Our approach: “dissect” compositionality:

- ▶ Does a model find the right parts and rules?

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Our approach: “dissect” compositionality:

- ▶ Does a model find the right parts and rules?
- ▶ Does a model use the parts and rules it finds *systematically*

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Our approach: “dissect” compositionality:

- ▶ Does a model find the right parts and rules?
- ▶ Does a model use the parts and rules it finds *systematically*
- ▶ Does a model use the parts and rules it finds *productively*

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- ▶ Does a model find the right parts and rules?
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Data

PCFG SET

Testing
compositionality

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Unary functions: reverse, swap, copy, ...

Binary functions: prepend, append, remove_first, ...

Characters: A, B, C, ...

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reverse A B C

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reverse A B C \Rightarrow C B A

Data

PCFG SET

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reverse A B C \Rightarrow C B A

copy D E

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Data PCFG SET

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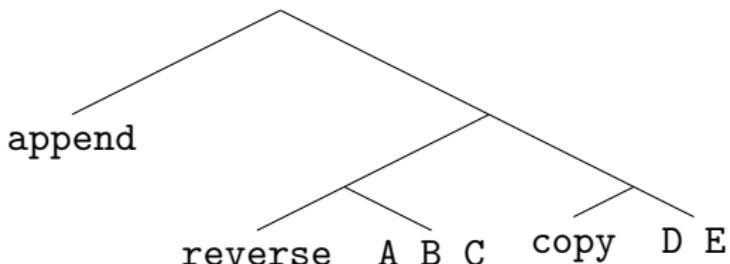
References

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append reverse A B C , copy D E \Rightarrow C B A D E



PCFG SET

Data Naturalisation

Testing
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Compositionality

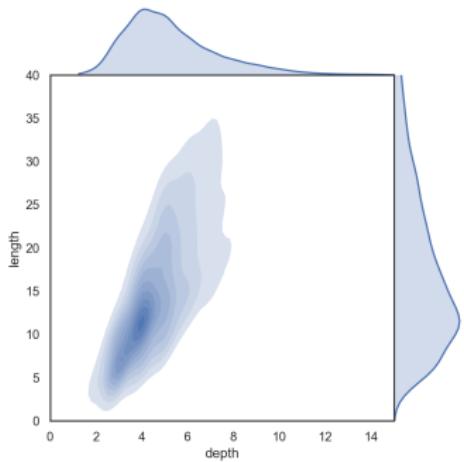
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Models

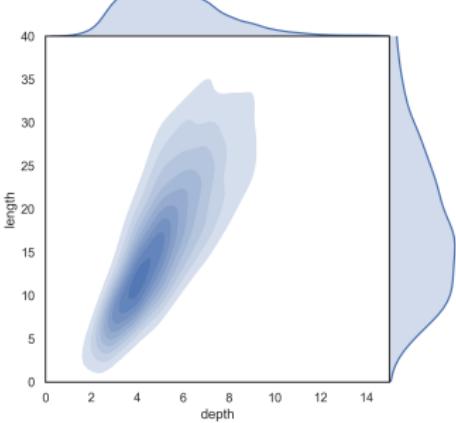
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(a) PCFG SET



(b) WMT 2017

Figure: Distribution of sentence depth and length in the PCFG SET and WMT2017 data.

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1. **LSTMS2S** Recurrent encoder-decoder model with attention
2. **ConvS2S** Convolutional encoder and decoder with multistep attention
3. **Transformer** Fully attention based model

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Experiment	LSTMS2S	ConvS2S	Transformer
PCFG SET*	0.77 ± 0.01	0.84 ± 0.01	0.93 ± 0.01

Systematicity

Testing
compositionality

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Compositionality

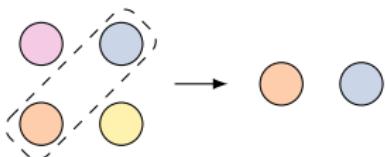
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Can models systematically recombine unseen pairs of functions?

Results

Systematicity

Testing
compositionality

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Compositionality

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References

Experiment	LSTMS2S	ConvS2S	Transformer
PCFG SET*	0.77 ± 0.01	0.84 ± 0.01	0.93 ± 0.01
Systematicity*	0.51 ± 0.03	0.55 ± 0.01	0.70 ± 0.01

Productivity

Testing
compositionality

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Compositionality

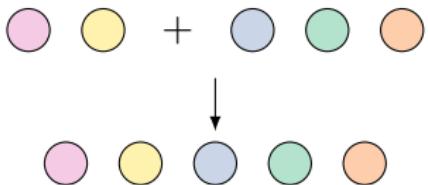
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Can models productively combine functions to generate longer sequences?

- ▶ Newly formed sequences (generalisation)
- ▶ Combinations of known sequences (concatenation)

Results

Productivity

Testing
compositionality

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Experiment	LSTMS2S	ConvS2S	Transformer
PCFG SET*	0.77 ± 0.01	0.84 ± 0.01	0.93 ± 0.01
Systematicity*	0.51 ± 0.03	0.55 ± 0.01	0.70 ± 0.01
Productivity, <i>generalisation</i> * <i>concatenation</i> †	0.29 ± 0.01 0.20 ± 0.01	0.32 ± 0.00 0.30 ± 0.03	0.56 ± 0.02 0.54 ± 0.01

Compositionality

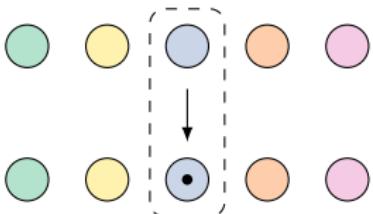
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Do models support substitution of synonyms?

- ▶ Equal distributions in training data
- ▶ Only in ‘primitive’ condition in training data

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Substitutivity

Testing
compositionality

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Compositionality

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Experiment	LSTMS2S	ConvS2S	Transformer
PCFG SET*	0.77 ± 0.01	0.84 ± 0.01	0.93 ± 0.01
Systematicity*	0.51 ± 0.03	0.55 ± 0.01	0.70 ± 0.01
Productivity, <i>generalisation</i> * <i>concatenation</i> †	0.293 ± 0.01 0.20 ± 0.01	0.32 ± 0.00 0.30 ± 0.03	0.56 ± 0.02 0.54 ± 0.01
Substitutivity, <i>eq. distributed</i> † <i>primitive</i> †	0.76 ± 0.01 0.61 ± 0.04	0.96 ± 0.01 0.61 ± 0.03	0.98 ± 0.00 0.88 ± 0.04

Substitutivity

Cosine distances

	LSTMS2S	ConvS2S	Transformer
<i>Equally distributed</i>	0.389	0.142	0.079
<i>Primitive</i>	0.408	0.461	0.373
<i>Other</i>	0.960	0.862	0.772

Compositionality

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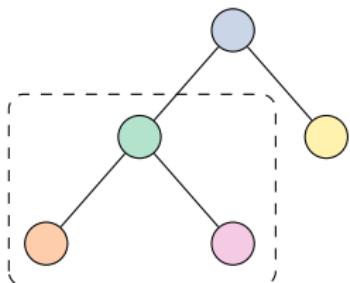


Figure: Localism

Do models build representations incrementally?

append reverse A B C , copy D E

≡

append C B A , D E

?

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Localism

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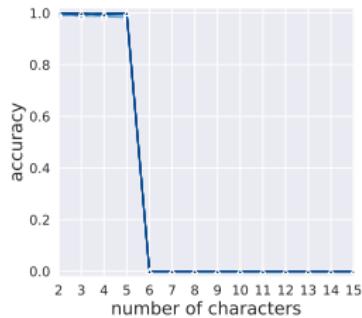
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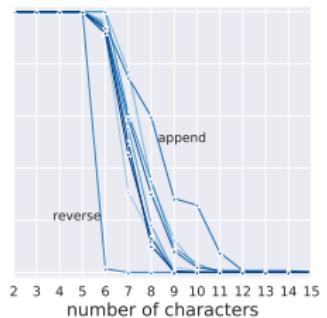
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Localism†	0.45 ± 0.01	0.57 ± 0.04	0.56 ± 0.03

Results

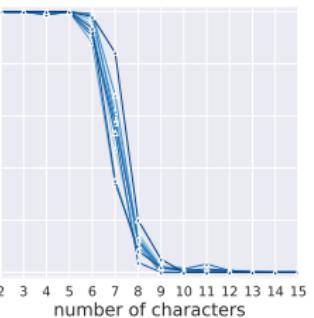
Generality of representations



(a) LSTM2S



(b) Conv2S



(c) Transformer

Compositionality

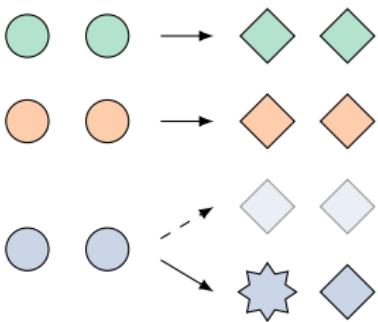
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Do models overgeneralise during training?

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Overgeneralisation

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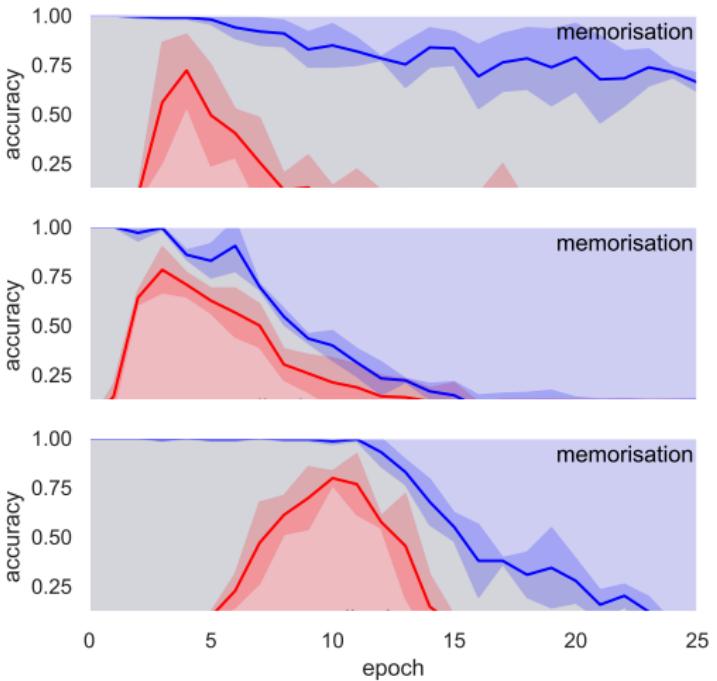
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PCFG SET*	0.77 ± 0.01	0.84 ± 0.01	0.93 ± 0.01
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Localism†	0.45 ± 0.01	0.57 ± 0.04	0.56 ± 0.03
Overgeneralisation*	0.73 ± 0.18	0.78 ± 0.12	0.84 ± 0.02

Overgeneralisation profile

LSTM2S



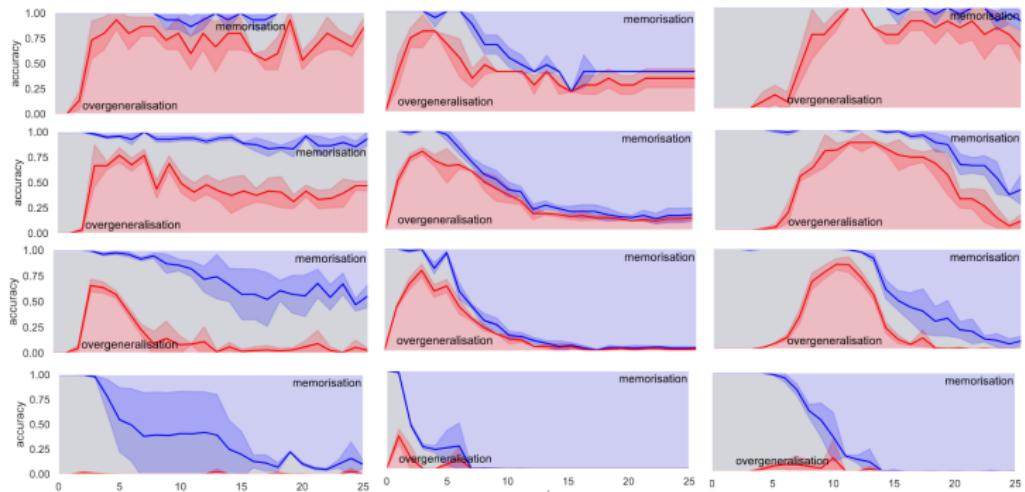
ConvS2S

Transformer

Overgeneralisation

Different exception rates

Overgeneralisation profiles for exceptions occurring 0.01%,
0.05%, 0.1% and 0.5%



(a) LSTM2S

(b) Conv2S

(c) Transformer

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- ▶ Does a model find the right parts and rules?

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Conclusion

The rest of the team



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Verna Dankers



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