

## Constraints of the 2M3G APIM

The 2M3G APIM, as described by Equations 4 and 5, requires the following 48 parameter

constraints:

Structural coefficients:  $b_{101} = b_{202}$ ,  $b_{102} = b_{201}$ ,  $b_{103} = b_{204}$ ,  $b_{104} = b_{203}$ ,  $b_{105} = b_{209}$ ,  $b_{106} = b_{208}$ ,

$b_{107} = b_{207}$ ,  $b_{108} = b_{206}$ ,  $b_{109} = b_{205}$ ,  $b_{110} = b_{211}$ ,  $b_{111} = b_{210}$ .

Variances:  $s_{X_1}^2 = s_{X_2}^2$ ,  $s_{G_1}^2 = s_{G_2}^2$ ,  $s_{X_1G_1}^2 = s_{X_2G_2}^2$ ,  $s_{X_1G_2}^2 = s_{X_2G_1}^2$ ,  $s_{X_1G_1G_2}^2 = s_{X_2G_1G_2}^2$ ,  $s_{e_1}^2 = s_{e_2}^2$ .

Covariances:  $\text{Cov}(X_1, G_1) = \text{Cov}(X_2, G_2)$ ,  $\text{Cov}(X_1, G_2) = \text{Cov}(X_2, G_1)$ ,  $\text{Cov}(X_1, G_1G_2) = \text{Cov}(X_2, G_1G_2)$ ,

$\text{Cov}(X_1, X_1G_1) = \text{Cov}(X_2, X_2G_2)$ ,  $\text{Cov}(X_1, X_1G_2) = \text{Cov}(X_2, X_2G_1)$ ,  $\text{Cov}(X_1, X_2G_1) =$

$\text{Cov}(X_2, X_1G_2)$ ,  $\text{Cov}(X_1, X_2G_2) = \text{Cov}(X_2, X_1G_1)$ ,  $\text{Cov}(X_1, X_1G_1G_2) = \text{Cov}(X_2, X_2G_1G_2)$ ,

$\text{Cov}(X_1, X_2G_1G_2) = \text{Cov}(X_2, X_1G_1G_2)$ ,  $\text{Cov}(G_1, G_1G_2) = \text{Cov}(G_2, G_1G_2)$ ,  $\text{Cov}(G_1, X_1G_1) =$

$\text{Cov}(G_2, X_2G_2)$ ,  $\text{Cov}(G_1, X_1G_2) = \text{Cov}(G_2, X_2G_1)$ ,  $\text{Cov}(G_1, X_2G_1) = \text{Cov}(G_2, X_1G_2)$ ,

$\text{Cov}(G_1, X_2G_2) = \text{Cov}(G_2, X_1G_1)$ ,  $\text{Cov}(G_1, X_1G_1G_2) = \text{Cov}(G_2, X_2G_1G_2)$ ,  $\text{Cov}(G_1, X_2G_1G_2) =$

$\text{Cov}(G_2, X_1G_1G_2)$ ,  $\text{Cov}(X_1G_1, X_1G_2) = \text{Cov}(X_2G_2, X_2G_1)$ ,  $\text{Cov}(X_1G_1, X_2G_1) = \text{Cov}(X_2G_2, X_1G_2)$ ,

$\text{Cov}(X_1G_1, G_1G_2) = \text{Cov}(X_2G_2, G_1G_2)$ ,  $\text{Cov}(X_1G_1, X_1G_1G_2) = \text{Cov}(X_2G_2, X_2G_1G_2)$ ,

$\text{Cov}(X_1G_1, X_2G_1G_2) = \text{Cov}(X_2G_2, X_1G_1G_2)$ ,  $\text{Cov}(X_1G_2, G_1G_2) = \text{Cov}(X_2G_1, G_1G_2)$ ,

$\text{Cov}(X_1G_2, X_1G_1G_2) = \text{Cov}(X_2G_1, X_2G_1G_2)$ ,  $\text{Cov}(X_1G_2, X_2G_1G_2) = \text{Cov}(X_2G_1, X_1G_1G_2)$ ,

$\text{Cov}(G_1G_2, X_1G_1G_2) = \text{Cov}(G_1G_2, X_2G_1G_2)$ .

Means:  $M_{X_1} = M_{X_2}$ ,  $M_{G_1} = M_{G_2}$ ,  $M_{X_1G_1} = M_{X_2G_2}$ ,  $M_{X_1G_2} = M_{X_2G_1}$ ,  $M_{X_1G_1G_2} = M_{X_2G_1G_2}$ .

Intercepts:  $b_{100} = b_{200}$ .