

# **Workshop**

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## **Power Analysis using G\*Power**

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In designing a study, we commonly want to know what sample size is required to detect a specific effect or in the case the data collection is completed what is the power for a specific effect.

# Overview

1. Power
2. Effect Size
3. Effect Size Measures
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5. Power Analysis
6. G\*Power
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9. Non-Centrality Parameter

# Power

Power ( $1 - \beta$ ) is

- the probability of correctly assuming there is an effect (i.e., correctly rejecting the null hypothesis).
- inversely related to the probability of making a Type II Error (concluding there is no effect when there is one).

	In the population	
	$H_0$ is true	$H_0$ is false ( $H_1$ is true)
Decision (Empiry)		
Do not reject $H_0$	Correct ( $1 - \alpha$ )	<b>Type II Error (<math>\beta</math>)</b>
Reject $H_0$	Type I Error ( $\alpha$ )	<b>Correct (<math>1 - \beta</math>)</b>

If power is high, the probability of making a **Type II Error** (i.e., **false negative**) is low.

# Power



## How much power is enough?

A power of .80 is probably the most reasonable compromise between the chance of detecting a substantial effect without involving more recourses in raising the power any higher and the risk of committing a Type I error (i.e., incorrectly concluding there is an effect).

- Studies with low power are statistically underpowered and have a high risk for false negative conclusions (Type II error).
- Studies with high power have a high risk for false positive conclusions (Type I error).

⇒ Each study should be adequately powered.

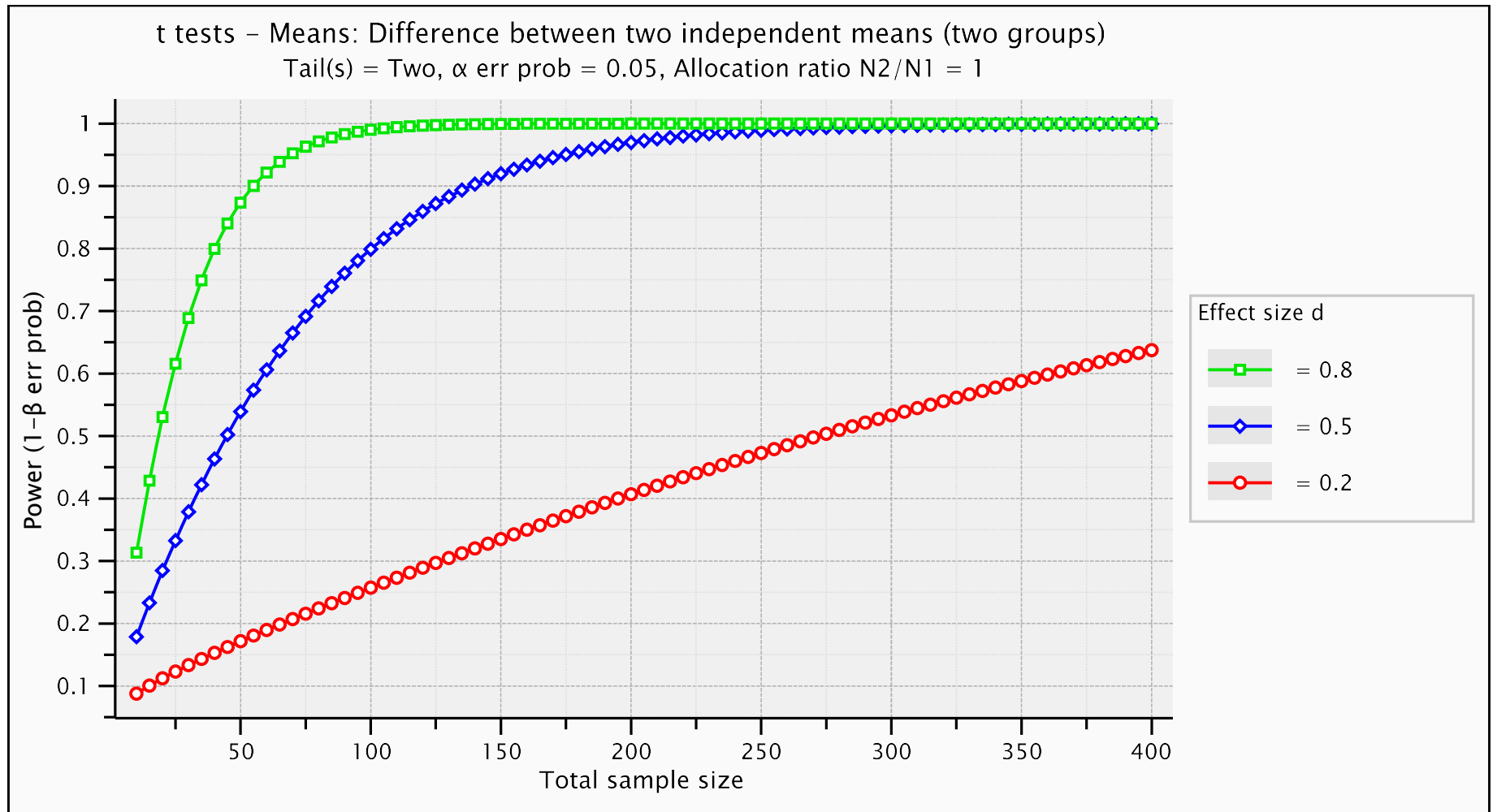
# Power

## **Statistical Power depends on:**

- the Type of Statistical Test (statistical model)
- the Size of the Effect ( $\uparrow$ )
- the Sample Size  $N$  ( $\uparrow$ )
- the Significance Level  $\alpha$  ( $\uparrow$ )

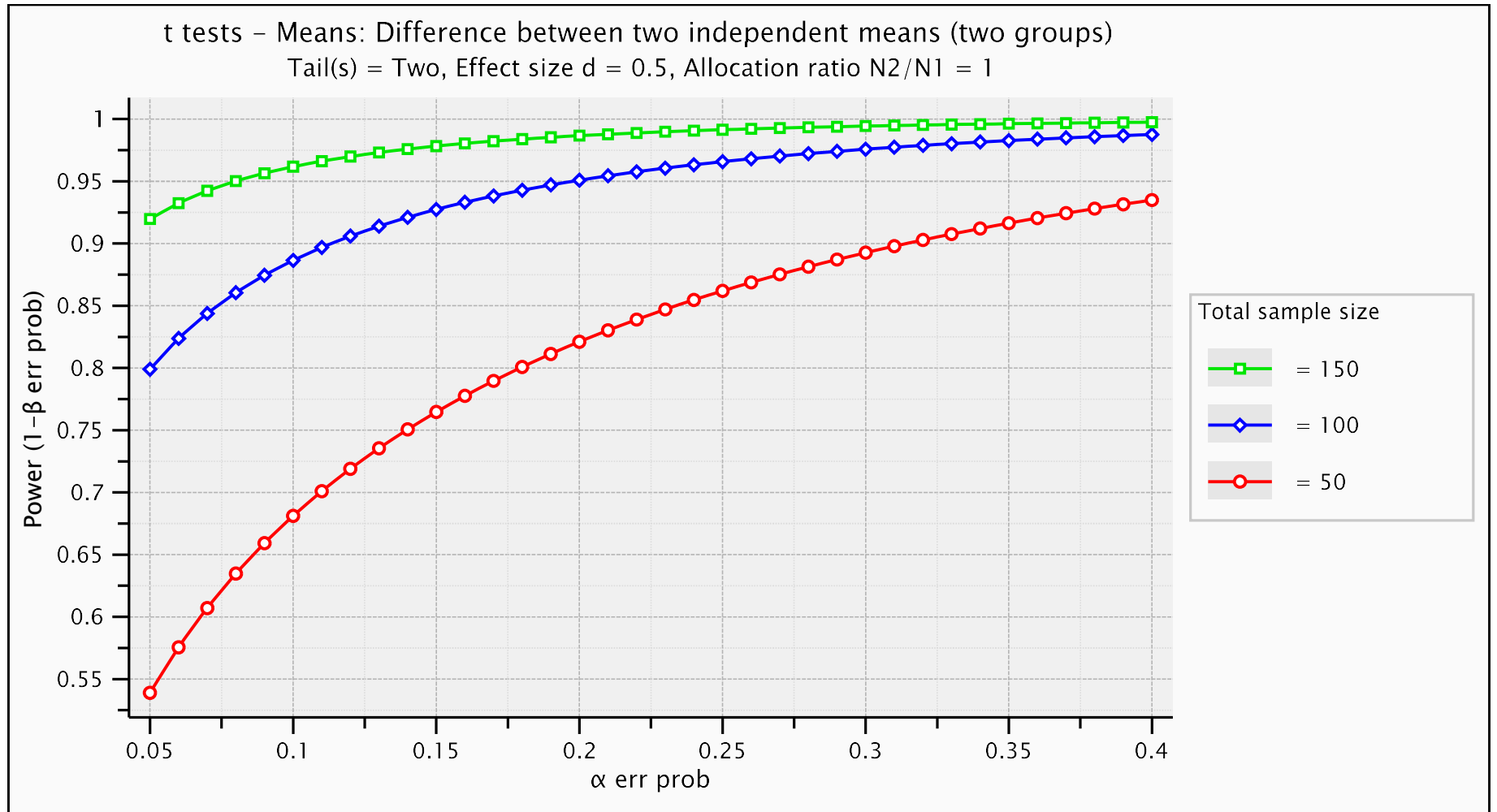
# Power

## Power as a function of $N$ and Effect Size (Cohen's $d$ )



# Power

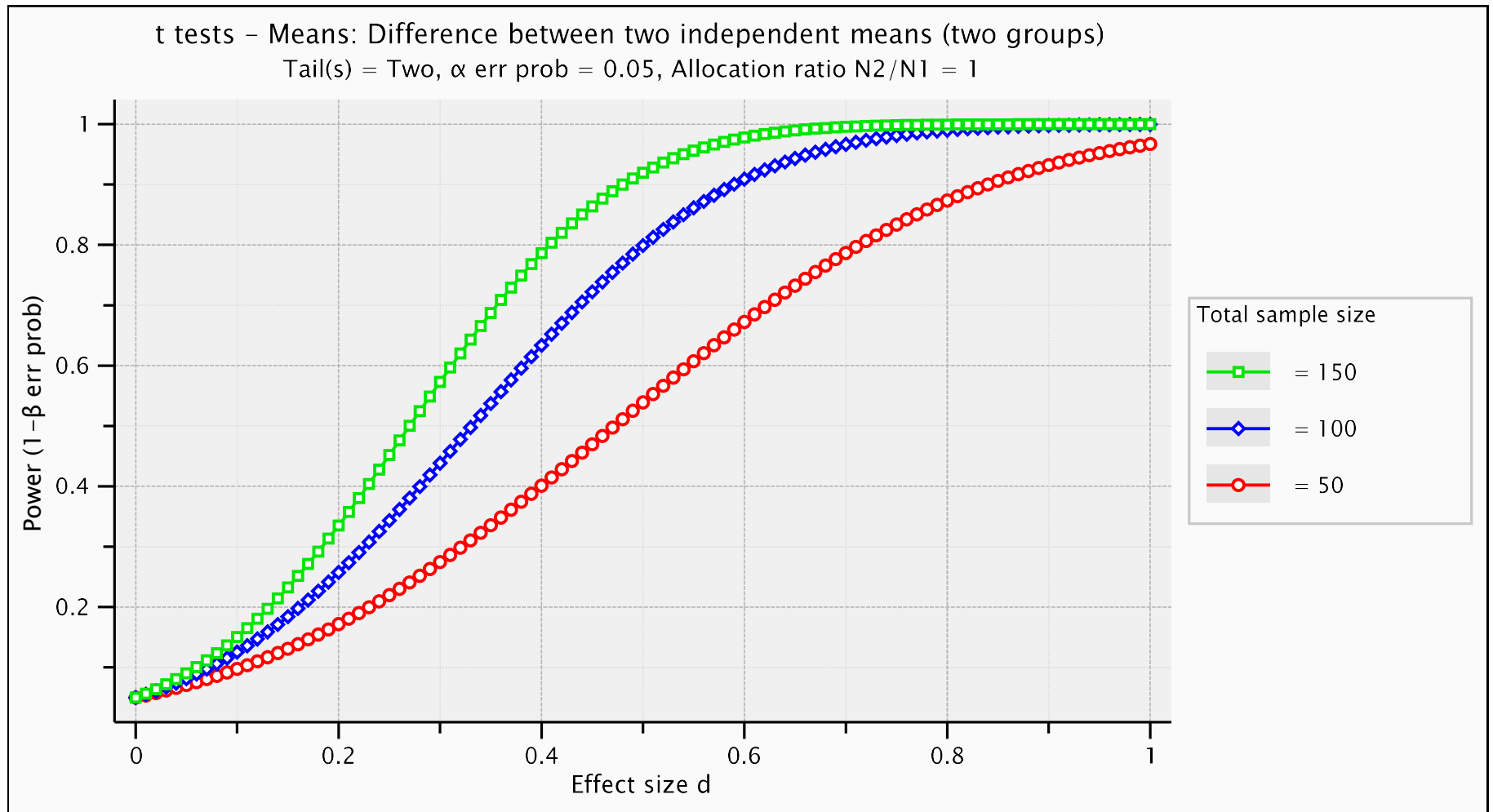
## Power as a function of $\alpha$ and $N$





# Power

## Power as a function of Effect Size (Cohen's $d$ ) and $N$



# Power

## Ways to Increase Power

- Increase the sample size.
- Chose a higher alpha level.
- Use a one-tailed test instead of a two-tailed test (not always possible and against consensus).
- Increase the effect size.

In comparing groups, the effect size can be increased by:

- increasing the variability between the groups (bigger difference).
- reducing the variability within groups.

## Effect Size

Effect size (ES) is a name given to a family of indices that measure the magnitude of an effect (e.g., the difference between groups or relationships between variables) in a standardized way.

Unlike significance tests, effect sizes are independent of the sample size.

# Effect Size

Effect sizes are used

- to judge the practical importance.
- to determine the sample size needed for detecting a specific effect and estimate power in cases where raw data are not available.
- to compare results across studies (and methods).  
⇒ meta-analysis studies

## Effect Size Measures

Effect Size	Statistical Analysis
$r$	Correlation Analysis
$R^2$	Regression Analysis
$\eta^2$	ANOVA family
Cohen's $f$	Regression Analysis and ANOVA
Odds Ratio	Logistic Regression Analysis
Cohen's $d$	Difference between 2 means
$\Delta$	Hotelling $T^2$ test
$w$	Contingency table ( $\chi^2$ -test)

Effect size converters:

<https://www.escal.site/#>

[https://www.psychometrica.de/effect\\_size.html](https://www.psychometrica.de/effect_size.html)

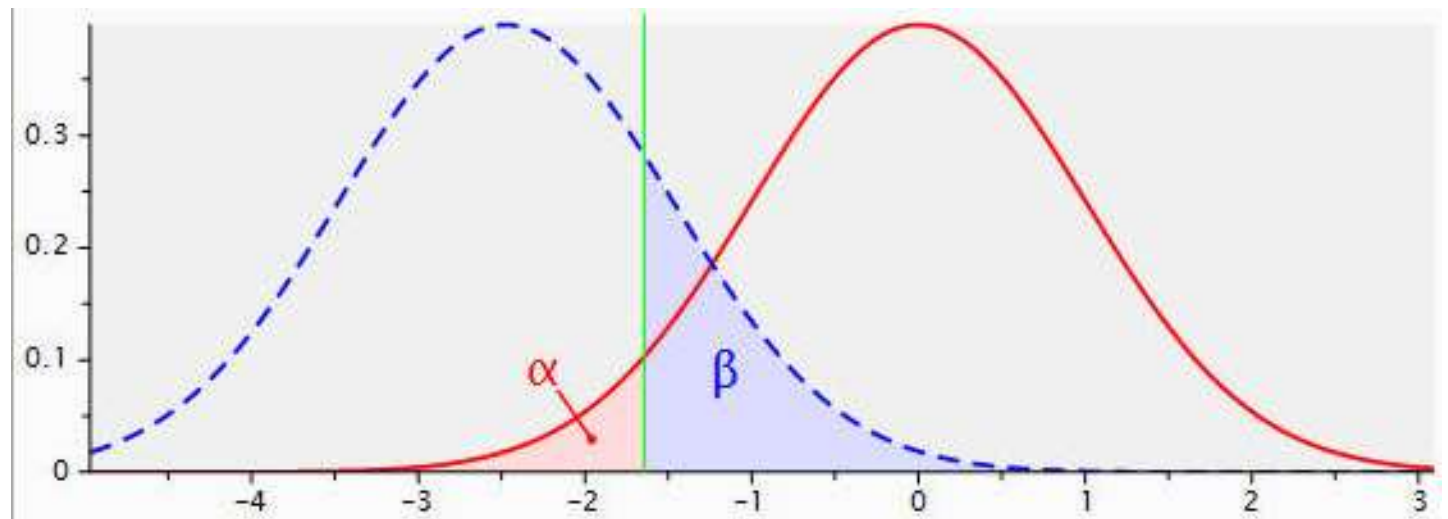
# Classification of Effect Sizes

Jacob Cohen (1988) suggested benchmarks for many effect sizes to classify effects as

- small in size
- medium in size
- large in size

# Power Analysis

Power analysis refers to statistical methods used to determine the sample size required to detect a specific effect or to estimate power for a specific effect.



# Power Analysis

## Important types of power analyses

- **A Priori Power Analyses**  
compute  $N$  as a function of power,  $\alpha$ , and the (assumed) population ES.
- **Post Hoc Power Analyses**  
compute power (also known as estimated power) as a function of  $\alpha$ ,  $N$ , and ES.
- **Sensitivity Analyses**  
compute the critical population ES as a function of  $\alpha$ , power, and  $N$ .



# Power Analysis

## Other types of power analyses offered by G\*Power

- **Criterion Analyses**

compute  $\alpha$  as a function of power, the population ES, and  $N$ .

- **Compromise Power Analyses**

compute both  $\alpha$  and power as a function of  $N$ , the population ES, and the error probability ratio  $q$ , which is  $\beta/\alpha$ .

# G\*Power



G\*Power was developed by Faul et al. (2009) and is a free-to-use stand-alone power analysis software program.

G\*Power can be used for the following

- statistical tests:  $F$  test,  $t$  test,  $\chi^2$  test, and  $z$  test.
- statistical methods:
  - correlation and regression analysis
  - analysis of means
  - analysis of proportions
  - analysis of variance

# Example 1

## Research Design

Three-wave longitudinal study with two groups.

## Question

What sample size is required to detect a medium-sized time-by-group interaction effect with power of .80?

## Assumptions

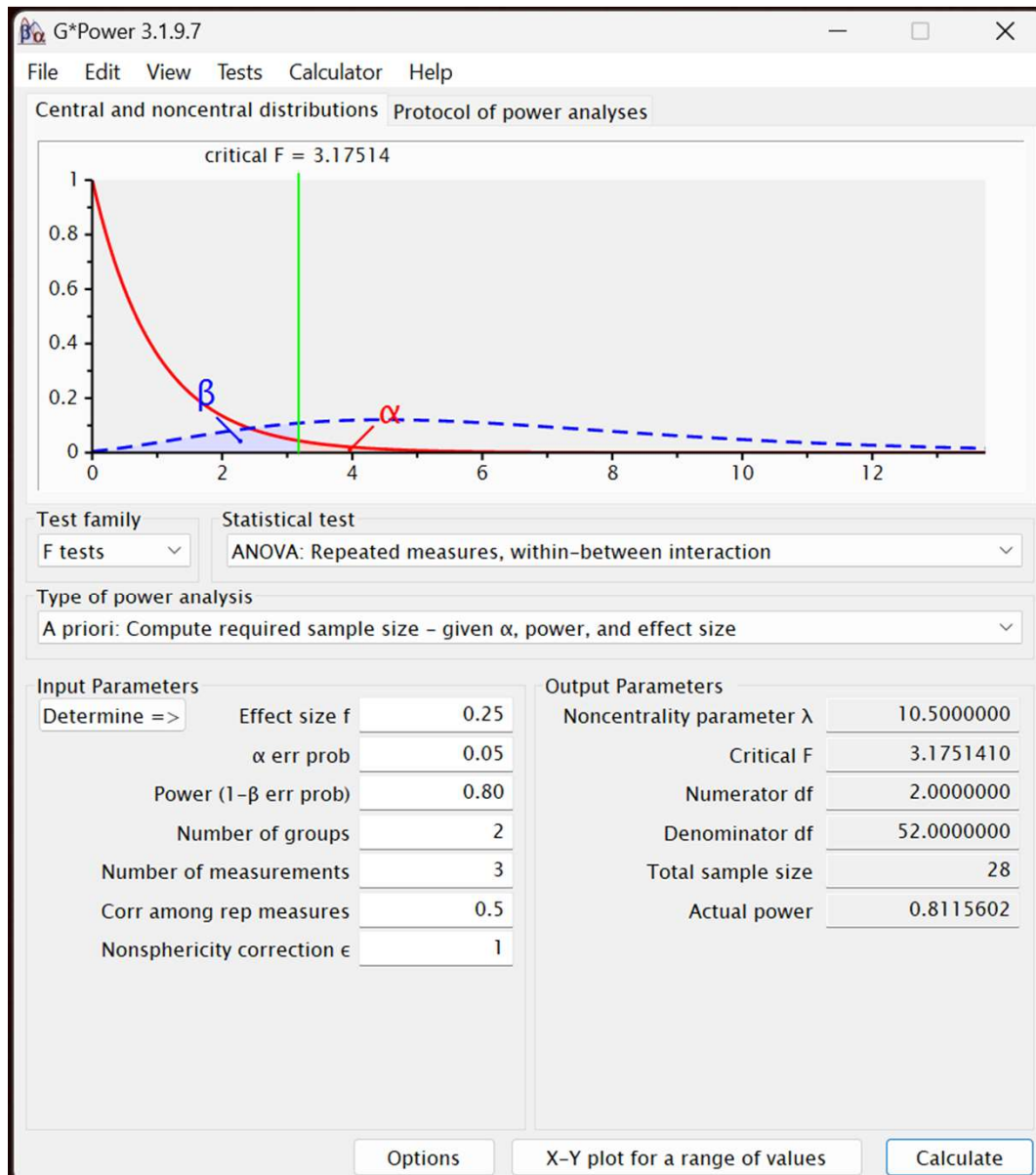
15% missing data

Significance level  $\alpha = .05$

Autocorrelation  $\rho = .50$

Non-sphericity correction  $\epsilon = 1$

# Example 1



**Required sample size:**

28 complete cases (14 in each group)

**Plus 15% missings (28/.85):**

32.9 cases total (17 in each group)

The same number of cases would be required for the within-subject (time) effect.

For the between-subject (group) effect, 86 cases would be needed.

## Example 2

### Research Design

Regression model with 3 covariates and 3 predictor variables.

$$Y = b_0 + b_1C_1 + b_2C_2 + b_3C_3 + b_4X_1 + b_5X_2 + b_6X_3 + e$$

### Question

What sample size is needed to detect a medium-sized incremental effect ( $R^2$  increase) for the 3 predictor variables?

### Assumption

Significance level  $\alpha = .05$

## Example 2

The screenshot shows the G\*Power 3.1.9.7 window with the 'Protocol of power analyses' tab selected. The 'Tests' section is set to 'Linear multiple regression: Fixed model, R<sup>2</sup> increase'. The 'Analysis' is 'A priori: Compute required sample size'. The 'Input' parameters are: Effect size f<sup>2</sup> = 0.15, α err prob = 0.05, Power (1-β err prob) = 0.80, Number of tested predictors = 3, and Total number of predictors = 6. The 'Output' parameters are: Noncentrality parameter λ = 11.5500000, Critical F = 2.7355415, Numerator df = 3, Denominator df = 70, Total sample size = 77, and Actual power = 0.8007605. The 'Test family' is 'F tests' and the 'Statistical test' is 'Linear multiple regression: Fixed model, R<sup>2</sup> increase'. The 'Type of power analysis' is 'A priori: Compute required sample size - given α, power, and effect size'. The 'Input Parameters' section shows a 'Determine =>' button and the same input values. The 'Output Parameters' section shows the same output values. At the bottom, there are buttons for 'X-Y plot for a range of values' and 'Calculate'.

Input Parameters		Output Parameters		
Determine =>	Effect size f <sup>2</sup>	0.15	Noncentrality parameter λ	11.5500000
	α err prob	0.05	Critical F	2.7355415
	Power (1-β err prob)	0.80	Numerator df	3
	Number of tested predictors	3	Denominator df	70
	Total number of predictors	6	Total sample size	77
			Actual power	0.8007605

**Required sample size:**

77 complete cases

**Small effect:**

550 cases

**Large effect:**

36 cases

## Possible Scenarios

There are two rare but possible scenarios:

- Power is high and the  $p$  value of an effect is high (not statistically significant).
- The  $p$  value of an effect is low (statistically significant) although power is low.

In either case, further investigation of the data is warrant.

## Noncentrality Parameter

- Many statistical tests involve a test statistic with a normal,  $t$ ,  $F$ , or chi-square distribution.
- When  $H_0$  is true, then these test statistics have a central distribution (e.g., central  $t$  distribution).
- When  $H_0$  is false, the test statistics have a non-central distribution, which depends on the size of the effect.



# Noncentrality Parameter

The noncentral distributions

- show how the test statistics are distributed when there is an effect (i.e.,  $H_0$  is false).
- have an additional parameter, the noncentrality parameter  $\delta$  (delta).

A central distribution is a special case of a noncentral distribution where the  $\delta$  is zero.

## Noncentrality Parameter

The noncentrality parameter  $\delta$  represents the degree to which the mean of the sampling distribution of the test statistic departs from its mean when the null is true.

For the two-sample  $t$  test, the noncentrality parameter is

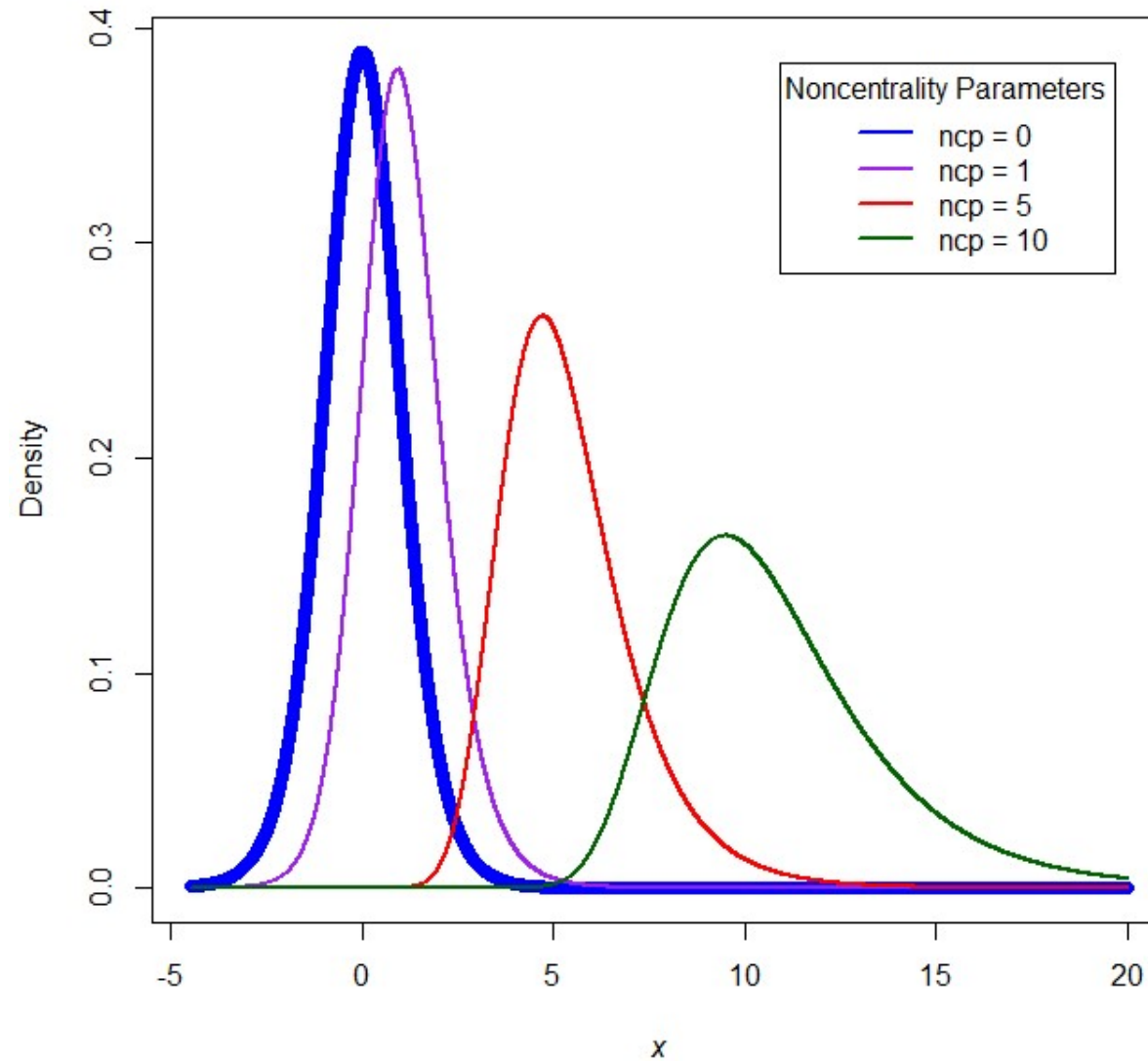
$$\delta = \text{Cohen's } d \sqrt{\frac{n_1 n_2}{n_1 + n_2}}$$

When the two samples are equal in size, then

$$\delta = \text{Cohen's } d \sqrt{\frac{n}{2}}$$

# Noncentrality Parameter

$t$  Distributions with different Noncentrality Parameters and  $df = 10$



## References and Readings

Cohen, J. (1992). A power primer. *Psychological Bulletin*, 112 (1), 155-159. <https://doi.org/10.1037/0033-2909.112.1.155>

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Kang H. (2021). Sample size determination and power analysis using the G\*Power software. *Journal of Educational Evaluation for Health Professions*, 18, 17. <https://doi.org/10.3352/jeehp.2021.18.17>

Lan, L., & Lian, Z. (2010). Application of statistical power analysis—How to determine the right sample size in human health, comfort and productivity research. *Building and Environment*, 45(5), 1202-1213. <https://doi.org/10.1016/j.buildenv.2009.11.002>

# Thank you!

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GitHub: <https://github.com/thomasledermann/powerAPIM>