

Restart the Maple server to clear old definitions, etc.

```
> restart;
```

Load the special Maple tools packages needed for operations within the *MCMC\_ISO* procedure.

```
> with(plots): with(plottools): with(stats): with(statplots): with  
  (StringTools):
```

Warning, the name changecoords has been redefined

Warning, the assigned name arrow now has a global binding

Warning, the previous binding of the name transform has been  
removed and it now has an assigned value

Warning, the assigned name Group now has a global binding

\*\*\*\*\*

Initialize the procedure

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The *MCMC\_ISO* procedure takes the following arguments:

*Path*: the file path where the ISO data files (\*.spi) are stored.

*File*: the filename of the raster you wish to work with.

*Position*: the position in the raster whose spectrum you wish to fit. The positions count consecutively up from 1, in the order in which they were observed in the raster.

*BadBins*: a list (enclosed in square brackets and separated by commas) of bins to be removed from the spectrum before the fit is attempted. ISO bins are numbered 1-?? from right to left. If no bins are to be removed, an empty list must be entered: [ ].

*CParam*: a list of the maximum, minimum, step size, and initial value to use when fitting the Gaussian centroid.

*FParam*: a list of the maximum, minimum, step size, and initial value to use when fitting the Gaussian FWHM.

*OParam*: a list of the maximum, minimum, step size, and initial value to use when fitting the baseline offset. In this program, I have defined the baseline as  $y=m(x-\text{average}(x[i]))+b$ , such that the offset,  $b$ , is the offset at the center of the spectrum, not at the  $y$ -axis (i.e., not at  $x=0$ ).

*SParam*: a list of the maximum, minimum, step size, and initial value to use when fitting the baseline slope.

*HParam*: a list of the maximum, minimum, step size, and initial value to use when fitting the Gaussian height.

*N*: total number of steps to attempt in your Markov Chain random walk.

*BadN*: number of steps to throw out from the beginning of the Markov Chain (start-up iterations). This is only necessary if you choose an initial point far from the  $\chi^2$  minimum.

*sigma*: a parameter that controls the size of proposed steps in the Markov Chain. More precisely, *sigma* is the standard deviation of the random normal distribution which is used to determine the Markov step size.

*r2*: a parameter that controls the acceptance rate of proposed steps in the Markov Chain. (In principle this is best done by changing *sigma*. While *r2* lowers the standard on what points are accepted, *sigma* raises the actual number of points with good fits to the data!).

*Nvar*: Number of unconstrained variables. (Degrees of Freedom (d.o.f.) = *NumBins* - *Nvar*).

*RandSeed*: the seed to use when generating random numbers. It can be set to either an integer or to 'random'.

*AdditionalError*: sometimes the  $\chi^2$  value of a fit is so large that the significance,  $\alpha$ , is so small that it cannot be computed to the digits of precision in the program (currently Digits=50). This means that we have grossly underestimated the real error of the data, and must add some additional systematic error. This parameter allows the user to add some error (in units of  $W \text{ m}^{-2} \text{ um}^{-1}$ ), which will add in quadrature to the previously calculated error of the data.

```
> MCMC_ISO:=proc(Path,File,Position,BadBins,CParam,FParam,SParam,  
  OParam,HParam,N,BadN,sigma,r2,Nvar,RandSeed,AdditionalError)
```

Define the local variables. These variables will only retain their definitions within the *MCMC\_ISO* procedure.

```
> local
```

```
  i, j, k,
```

```
  CMin, CMax, dC, C0, Cmean, Csigma, Cgrid, Cfit,
```

```
  FMin, FMax, dF, F0, Fmean, Fsigma, Fgrid, Ffit,
```

```
  SMin, SMax, dS, S0, Smean, Ssigma, Sgrid, Sfit,
```

```
  OMin, OMax, dO, O0, Omean, Osigma, Ogrid, Ofit,
```

```
  HMin, HMax, dH, H0, Hmean, Hsigma, Hgrid, Hfit,
```

```
ErrorArray, Flatfield, Gain, Efficiency, VelocityShift,
HOFPIOffset, HOFPIslope,
XBadBins, YBadBins,
Mins, Maxs, ds,
Mnew, Seed, Rand1, Rand2, r1, r, Naccept, AcceptRate, Nbestfit,
M, G1, G2, chi1, chi2, chif, a, a1, a2, af, amax,
Baseline, SysErrorSqd, Signal, Noise, SNR, Intensity, Isigma:
```

Define the global variables. These are variables that retain their definitions outside of the *MCMC\_ISO* procedure (including its sub-procedures).

```
> global
X, Y, XBins, YBins, XScaled, YScaled, XFinal, YFinal, Gf, TotError,

graph1a, graph1b, graph2a, graph2b, graph3a, graph3b, graph3c,
title1, title2, title3,
AvgError, AvgErrorScaled, Transmission, NumBins, BinLength,
BinLengthScaled, Histogram,
Cpdf, Fpdf, Spdf, Opdf, Hpdf:
```

Rename and reorganize the fitting parameters:

```
> CMin:=CParam[1]: CMax:=CParam[2]: dC:=CParam[3]: C0:=CParam[4]:
> FMin:=FParam[1]: FMax:=FParam[2]: dF:=FParam[3]: F0:=FParam[4]:
> SMin:=SParam[1]: SMax:=SParam[2]: dS:=SParam[3]: S0:=SParam[4]:
> OMin:=OParam[1]: OMax:=OParam[2]: dO:=OParam[3]: O0:=OParam[4]:
> HMin:=HParam[1]: HMax:=HParam[2]: dH:=HParam[3]: H0:=HParam[4]:
> Mins:=[CMin,FMin,SMin,OMin,HMin]: Maxs:=[CMax,FMax,SMax,OMax,
HMax]: ds:=[dC,dF,dS,dO,dH]:
```

Specify the number of decimal places to carry through calculations, and the properties of the output display:

```
> Digits:=50:
> interface(prettyprint=0): interface(displayprecision=20):
```

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Read and display raw data

\*\*\*\*\*

Call and execute a sub-procedure, named *readSPIFIdata\_andX*, that reads ISO data from the \*.spi file specified by the *Path*, *Filename*, and *Position* variables:

```
> read("C://Documents and Settings/Tom Oberst/Desktop/SPIFI &
ZEUS/SPIFI observing plan/Maple Worksheets/SPIFI/read SPIFI
data +X v2.mpl"):
> readSPIFIdata_andX(Path, File, Position): X:=convert(X,list): X:=
ListTools[Reverse](X): Y:=convert(Y,list): Y:=ListTools[Reverse]
(Y):
```

Call and execute a sub-procedure, named *readSPIFIerrors\_andX*, that reads ISO errors from the "error" version of the \*.spi data file. The result is the global variable *AvgError*, which is a single value representing the average error (in flux units) of the requested *Position*'s spectrum. It is the average (across all bins in the spectrum) of the individual errors in each bin:

```
> read("C://Documents and Settings/Tom Oberst/Desktop/SPIFI &
ZEUS/SPIFI observing plan/Maple Worksheets/SPIFI/read
SPIFI errors +X v2.mpl"):

```

```
> readSPIFIerrors_andX(Path, File, Position):

```

Define the transmission. ISO was in space, therefore transmission is 100%:

```
> Transmission:=100:

```

Call a sub-procedure, named *HistDiscont*, that creates histogram-style displays of data. The suffix "Discont" refers to the fact that it can create histograms of discontinuous data sets (i.e. where bins have been removed).

```
> read("C://Documents and Settings/Tom Oberst/Desktop/SPIFI &
ZEUS/SPIFI observing plan/Maple Worksheets/SPIFI/SPIFI
histogram discontinuous v4.mpl"):

```

Create a graph of raw data:

```
> graph1a:=pointplot({seq([X[k],Y[k]], k=1..nops(X))}):
> HistDiscont(X,Y): graph1b:=Histogram:
> title1:=cat(File," position ",Position," raw ISO data"):

```

```
*****

```

Scale data and display scaled data

```
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```

Y-scaling factors (flatfielding, gain, efficiency, and transmission) & X-scaling factors (velocity shift, HOFPI offset, HOFPI slope):

Since our ISO data has already been processed, we set all of these values to zero or unity; the exception is the Gain, which I use to convert the ISO fluxes from  $W \text{ cm}^{-2} \text{ um}^{-1}$  to  $W \text{ m}^{-2} \text{ um}^{-1}$ :

```
> Flatfield:=1:
> Gain:=100^2:
> Efficiency:=1:
> VelocityShift:=0:
> HOFPIOffset:=0:
> HOFPIslope:=1:

```

Remove bins:

```
> NumBins:=nops(X)-nops(BadBins): BinLength:=(X[1]-X[nops(X)])/
(nops(X)-1):
> for i from 1 to nops(BadBins) do XBadBins[BadBins[i]]:=DEL:
YBadBins[BadBins[i]]:=DEL: end do:
> j:=1:
> for i from 1 to nops(X) do
> if XBadBins[i]<>DEL then XBins[j]:=X[i]: YBins[j]:=Y[i]: j:=j+1:
end if:
> end do:

```

Scale Data (since the ISO data I am using is supposed to be already processed, scaling is not necessary):

```
> for i from 1 to NumBins do
> YScaled[i]:=Gain*YBins[i]:
> XScaled[i]:=XBins[i]:

```

```
> end do:
> AvgErrorScaled:=sqrt(AdditionalError^2+AvgError^2):
> BinLengthScaled:=BinLength:
```

Create a graph of the scaled data:

```
> graph2a:=pointplot({seq([XScaled[k],YScaled[k]], k=1..NumBins)}):
> HistDiscont(convert(XScaled,list),convert(YScaled,list)):
graph2b:=Histogram:
> title2:=cat(File,"", position ",",Position,"", scaled ISO data):
```

```
*****
```

Output "header"

```
*****
```

File  
Position  
Bins Removed; "BadBins"  
HOFPI offset (counts)  
HOFPI slope (km/s per count)  
Velocity offset (counts)  
Gain  
Flatfielding  
Efficiency (fraction)  
Transmission (%)  
Centroid Min (um)  
Centroid Max (um)  
Centroid s (um)  
Centroid0 (um)  
FWHM Min (um)  
FWHM Max (um)  
FWHM s (um)  
FWHM0 (um)  
Height Min ( $W \text{ m}^{-2} \text{ um}^{-1}$ )  
Height Max ( $W \text{ m}^{-2} \text{ um}^{-1}$ )  
Height s ( $W \text{ m}^{-2} \text{ um}^{-1}$ )  
Height0 ( $W \text{ m}^{-2} \text{ um}^{-1}$ )  
Slope Min ( $W \text{ m}^{-2} \text{ um}^{-2}$ )  
Slope Max ( $W \text{ m}^{-2} \text{ um}^{-2}$ )  
Slope s ( $W \text{ m}^{-2} \text{ um}^{-2}$ )  
Slope0 ( $W \text{ m}^{-2} \text{ um}^{-2}$ )  
Offset Min ( $W \text{ m}^{-2} \text{ um}^{-1}$ )  
Offset Max ( $W \text{ m}^{-2} \text{ um}^{-1}$ )  
Offset s ( $W \text{ m}^{-2} \text{ um}^{-1}$ )  
Offset0 ( $W \text{ m}^{-2} \text{ um}^{-1}$ )  
MCMC steps; "N"  
MCMC initial steps to throw out; "BadN"  
s of MCMC random gaussian  
acceptance aggression; "r2"  
unconstrained variables; "Nvar"  
additional error; "AdditionalError" ( $W \text{ m}^{-1} \text{ um}^{-1}$ )

```
print(File):
print(Position):
print(BadBins):
print(HOFPIOffset):
```

```

print(HOFPISlope):
print(VelocityShift):
print(Gain):
print(Flatfield):
print(Efficiency):
print(Transmission):
print(evalf(CMin)):
print(evalf(CMax)):
print(evalf(dC)):
print(evalf(C0)):
print(evalf(FMin)):
print(evalf(FMax)):
print(evalf(dF)):
print(evalf(F0)):
print(evalf(HMin)):
print(evalf(HMax)):
print(evalf(dH)):
print(evalf(H0)):
print(evalf(SMin)):
print(evalf(SMax)):
print(evalf(dS)):
print(evalf(S0)):
print(evalf(OMin)):
print(evalf(OMax)):
print(evalf(dO)):
print(evalf(O0)):
print(N):
print(BadN):
print(sigma):
print(r2):
print(Nvar):
print(evalf(AdditionalError)):

```

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Markov Chain Monte Carlo

\*\*\*\*\*

Calculate the figures of merit for the first point in the Markov Chain,  $M_0$ :

```
> M[0]:=[C0,F0,S0,O0,H0]:
```

Gaussian (the baseline has a funny form so that the offset is defined at the emission line center, not at  $x=0$ ):

```
> G1:=unapply(H0*exp(-(x-C0)^2/(F0/sqrt(4*ln(2)))^2)+(S0*(x-sum
(XScaled[k],k=1..NumBins)/NumBins)+O0), x):
```

Chi squared:

```
> chi1:=sum((G1(XScaled[k])-YScaled[k])^2, k=1..NumBins)/
```

**(AvgErrorScaled^2):**

Alpha ("confidence" or "significance level"):

```
> a1:=1-statevalf[cdf,chisquare[NumBins-Nvar]](chi1):
```

The following variables need initialized before starting the Markov Chain. Naccept is a tally of the number of times a proposed point Mnew is accepted, a is an array of the confidences of each point visited in the Markov Chain, Nbestfit is the position (i.e. iteration number) of the maximum value in a, Mnew is the first proposed step in the MCMC, and Seed is used to generate random numbers based on a user-supplied integer or your computer's clock:

```
> Naccept:=0: a[0]:=a1: Nbestfit:=0: Mnew:=[C0,F0,S0,O0,H0]:
```

```
> if type(RandSeed, integer)=true then Seed:=randomize(RandSeed):  
  else Seed:=randomize(): end if:
```

Do the Markov Chain loop:

```
> for i from 1 to N do
```

Generate a new proposed point, Mnew:

```
> Rand1:=[random[normald[0,sigma]](5)]:
```

```
> for j from 1 to 5 do Mnew[j]:=M[i-1][j]+ds[j]*Rand1[j]:
```

```
> if Mnew[j]>Maxs[j] then Mnew[j]:=Maxs[j]:
```

```
> elif Mnew[j]<Mins[j] then Mnew[j]:=Mins[j]:
```

```
> end if: end do:
```

Calculate the figures of merit for the proposed point, Mnew:

```
> G2:=unapply(Mnew[5]*exp(-(x-Mnew[1])^2/(Mnew[2]/sqrt(4*ln(2)))^2)  
  +(Mnew[3]*(x-sum(XScaled[k],k=1..NumBins)/NumBins)+Mnew[4]), x):
```

```
> chi2:=sum((G2(XScaled[k])-YScaled[k])^2, k=1..NumBins)/  
  (AvgErrorScaled^2):
```

```
> a2:=1-statevalf[cdf,chisquare[NumBins-Nvar]](chi2):
```

Compare Mnew with the last point in the Markov Chain, M[i-1], and decide whether to accept or reject it:

```
> r1:=a2/a1: r:=r1*r2: print(chi2, a2, a1, r):
```

```
> Rand2:=evalf(rand(0..1000)/1000):
```

```
> if Rand2 <= r then
```

```
> M[i]:=Mnew:
```

```
> a[i]:=a2: print(chi2/(NumBins-Nvar)):
```

```
> if a[i]>max(seq(a[k],k=0..i-1)) then Nbestfit:=i end if:
```

```
> a1:=a2:
```

```
> Naccept:=Naccept+1:
```

```
> else M[i]:=M[i-1]:
```

```
> a[i]:=a1:
```

```
> end if:
```

```
> end do:
```

Calculate the acceptance rate of your MCMC. This can be adjusted using sigma and r2 (in that order) . Empirical data suggests aiming for *AcceptRate* ~ 25% for data with >2 d.o.f. (Gregory 2005) .

```
> AcceptRate:=100*evalf(Naccept/N):
```

Calculate parameter pdfs, means, and sigmas:

```
> Cpdf:=histogram([seq(M[i][1], i=BadN..N)], area=N):
```

```
> Cmean:=describe[mean]([seq(M[i][1], i=BadN..N)]):
```

```

> Csigma:=describe[standarddeviation]([seq(M[i][1], i=BadN..N)]):

> Fpdf:=histogram([seq(M[i][2], i=BadN..N)], area=N):
> Fmean:=evalf(describe[mean]([seq(M[i][2], i=BadN..N)])):
> Fsigma:=describe[standarddeviation]([seq(M[i][2], i=BadN..N)]):

> Spdf:=histogram([seq(M[i][3], i=BadN..N)], area=N):
> Smean:=describe[mean]([seq(M[i][3], i=BadN..N)]):
> Ssigma:=describe[standarddeviation]([seq(M[i][3], i=BadN..N)]):

> Opdf:=histogram([seq(M[i][4], i=BadN..N)], area=N):
> Omean:=describe[mean]([seq(M[i][4], i=BadN..N)]):
> Osigma:=describe[standarddeviation]([seq(M[i][4], i=BadN..N)]):

> Hpdf:=histogram([seq(M[i][5], i=BadN..N)], area=N):
> Hmean:=describe[mean]([seq(M[i][5], i=BadN..N)]):
> Hsigma:=describe[standarddeviation]([seq(M[i][5], i=BadN..N)]):

```

\*\*\*\*\*

Use the point in the MCMC with maximum alpha (*Nbestfit*) to do final fit

\*\*\*\*\*

Compute the baseline and subtract it from the data points. Note that the baseline is defined in such a way that the offset is the offset at the center of the spectrum, not at the y-axis (not at  $x=0$ ):

```

> Baseline:=unapply(M[Nbestfit][3]*(x-sum(XScaled[k],k=1..NumBins)
  /NumBins)+M[Nbestfit][4], x):
> for i from 1 to NumBins do YFinal[i]:=YScaled[i]-Baseline(XScaled
  [i]): XFinal[i]:=XScaled[i]: end do:

```

Compute the Gaussian (without the baseline):

```

> Gf:=unapply(M[Nbestfit][5]*exp(-(x-M[Nbestfit][1])^2/(M[Nbestfit]
  [2]/sqrt(4*ln(2)))^2), x):
> chif:=sum((Gf(XFinal[k])-YFinal[k])^2, k=1..NumBins)/
  (AvgErrorScaled^2):
> af:=1-statevalf[cdf,chisquare[NumBins-Nvar]](chif):

```

If  $\chi^2$  is not equal to 1, then there is some systematic error that has been underestimated or overestimated. The total error (TotError) is the sum of the calculated error (AvgErrorScaled) and the systematic error (SysError):

```

> SysErrorSqd:=fsolve(sum((Gf(XFinal[k])-YFinal[k])^2, k=1..
  NumBins)/(AvgErrorScaled^2+x)/(NumBins-Nvar)=1,x):
> TotError:=sqrt(AvgErrorScaled^2+SysErrorSqd):

> Signal:=evalf(sqrt(Pi/(4*ln(2)))*M[Nbestfit][5]*M[Nbestfit][2]
  /BinLengthScaled):
> Noise:=evalf(sqrt((TotError^2)*(sqrt(Pi/(4*ln(2)))*(M[Nbestfit]
  [2]/BinLengthScaled)))):
> SNR:=Signal/Noise:
> Intensity:=Signal*BinLengthScaled:

```

```

> Isigma:=Noise*BinLengthScaled:

> graph3a:=pointplot({seq([XFinal[k],YFinal[k]], k=1..NumBins)}):
> HistDiscont(convert(XFinal,list),convert(YFinal,list)): graph3b:=
  Histogram:
> graph3c:=plot(Gf(x), x=XFinal[NumBins]-BinLengthScaled/2..XFinal
  [1]+BinLengthScaled/2):
> title3:=cat(File," ", position ",Position,`\n`","MCMC chi^2 fit to
  Gaussian"):

```

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Print outputs

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```

fitting method
random number generator seed; "Seed"
MCMC acceptance rate (%)
reduced chi^2
confidence; "alpha" (%)
Known Error "AvgErrorScaled" ( $W m^{-2} \mu m^{-1}$ )
Unknown Error Squared "SysErrorSqd" ( $(W m^{-2} \mu m^{-1})^2$ )
Total Error "TotError" ( $W m^{-2} \mu m^{-1}$ )
Signal  $((W m^{-2} \mu m^{-1}) * Nbins)$ 
Noise  $((W m^{-2} \mu m^{-1}) * \text{sqrt}(Nbins))$ 
SNR
Intensity ( $W m^{-2}$ )
Intensity s ( $W m^{-2}$ )
Centroid ( $\mu m$ )
Centroid s ( $\mu m$ )
FWHM ( $\mu m$ )
FWHM s ( $\mu m$ )
Height ( $W m^{-2} \mu m^{-1}$ )
Height s ( $W m^{-2} \mu m^{-1}$ )
Slope ( $W m^{-2} \mu m^{-2}$ )
Slope s ( $W m^{-2} \mu m^{-2}$ )
Offset ( $W m^{-2} \mu m^{-1}$ )
Offset s ( $W m^{-2} \mu m^{-1}$ )
Final list of X values ( $\mu m$ )
Final list of Y values ( $W m^{-2} \mu m^{-1}$ )

```

```

> print(`MCMC min fit`):
> print(Seed):
> print(AcceptRate):
> print(chif/(NumBins-Nvar)):
> print(100*af):
> print(AvgErrorScaled):
> print(SysErrorSqd):
> print(TotError):
> print(Signal):
> print(Noise):
> print(SNR):

```



```

> print(Intensity):
> print(Isigma):
> print(M[Nbestfit][1]):
> print(Csigma):
> print(M[Nbestfit][2]):
> print(Fsigma):
> print(M[Nbestfit][5]):
> print(AvgErrorScaled*sqrt(chif/(NumBins-Nvar))):
> print(M[Nbestfit][3]):
> print(Ssigma):
> print(M[Nbestfit][4]):
> print(Osigma):
> for i from 1 to nops(X) do print(XFinal[i]) od:
> for i from 1 to nops(X) do print(YFinal[i]) od:

*****

*****

>end proc:
> MCMC_ISO("C://Documents and Settings/Tom Oberst/Desktop/SPIFI &
ZEUS/SPIFI observing plan/ISO Carina data/",
  "ISO145_Car2.spi",14,[],[145,146,.292,145.525],[.584,.85,.292,
.8],[-20*10^(-15),20*10^(-15),2*10^(-15),2*10^(-15)],
[-10*10^(-14),150*10^(-14),0.5*10^(-15),4.4*10^(-14)],[0.1*10^
(-15),20*10^(-15),0.1*10^(-15),1.75*10^(-15)],10000,0,1,1,4,
random,2*10^(-15)):

"ISO145_Car2.spi"
14
[]
0
1
0
10000
1
1
100

```

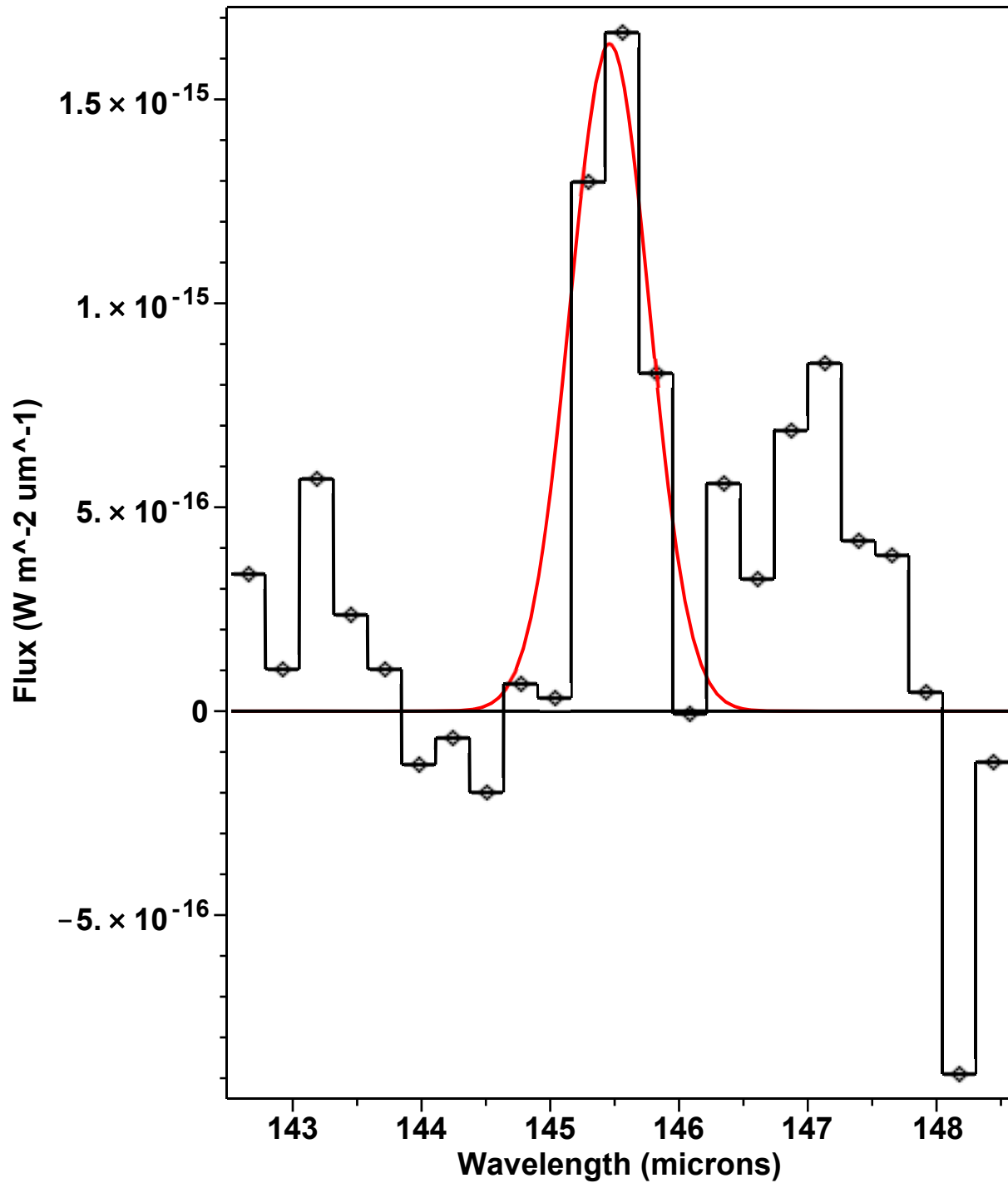
145.  
146.  
.292  
145.525  
.584  
.85  
.292  
.8  
0.1000000000e-15  
0.2000e-13  
0.1000000000e-15  
0.1750000000e-14  
-0.200e-13  
0.200e-13  
0.200e-14  
0.200e-14  
-0.100e-12  
0.15000e-11  
0.5000000000e-15  
0.4400000000e-13  
10000  
0  
1  
1  
4  
0.2000e-14  
  
`MCMC min fit`  
1218126566  
28.78000  
0.48925132841340296362200655037471186761325636377531e-1  
99.999999959976086382303668994191441246779055721897  
0.20000000004467341717837555381348774936276826177337e-14  
-0.38042994703341493870788813918118114184504089900612e-29  
0.44238052788610316528527188250132752548128330027994e-15  
0.48084378389664798231326545523033525400801648065579e-14  
0.75828818701928623898633381069096556797583515439922e-15  
6.3411746632473682635955147554477538525127336995498  
0.12639488991265035295281782109625956516365647153340e-14  
0.19932409470633076525429326988154826642261034123952e-15  
145.46110724012391057404964878799898441802846498455  
.35583915947154002086687189054926907697598024204328

.72555422509578073969255566505866134030425389104101  
.11737243819795930910354954779762911785838165537722  
0.16365430358483175864891852842350618639082388762678e-14  
0.44238052788610316528527188250132752548128330027992e-15  
-0.62938106948896663594192603763500379209200627927346e-15  
0.51501892166450371686851147425320028923322948786637e-15  
0.41139467450241511799801236419953061144251561212787e-13  
0.84899739047132937777015005871941036453635918333789e-15  
148.4362792  
148.1751625  
147.9139609  
147.6526292  
147.3912083  
147.1296583  
146.8679792  
146.6061625  
146.3441792  
146.0819913  
145.819675  
145.5571542  
145.2944333  
145.0314792  
144.7683208  
144.5049  
144.2412417  
143.9773167  
143.7131083  
143.4486208  
143.18385  
142.9187957  
142.6533458  
-0.124579559998289417971064056243399899238410184352e-15  
-0.888921467905719072358321174834727893916960960375e-15  
0.46683189734051659987030237053348899582539652269e-16  
0.382205964896681877773045604363929379088689094896e-15  
0.417672599267913679735134951871952816256583930563e-15  
0.853057980543074456104524196728517574434919688219e-15  
0.688362108722164206881213338933623653623696367864e-15  
0.323579634066092275848796872115951156290681187445e-15  
0.558692304523843482974832480420408667325903478780e-15  
-0.6323796385222752472845629342433943414736254369e-17  
0.828579290176388628763421317591491111357719398875e-15

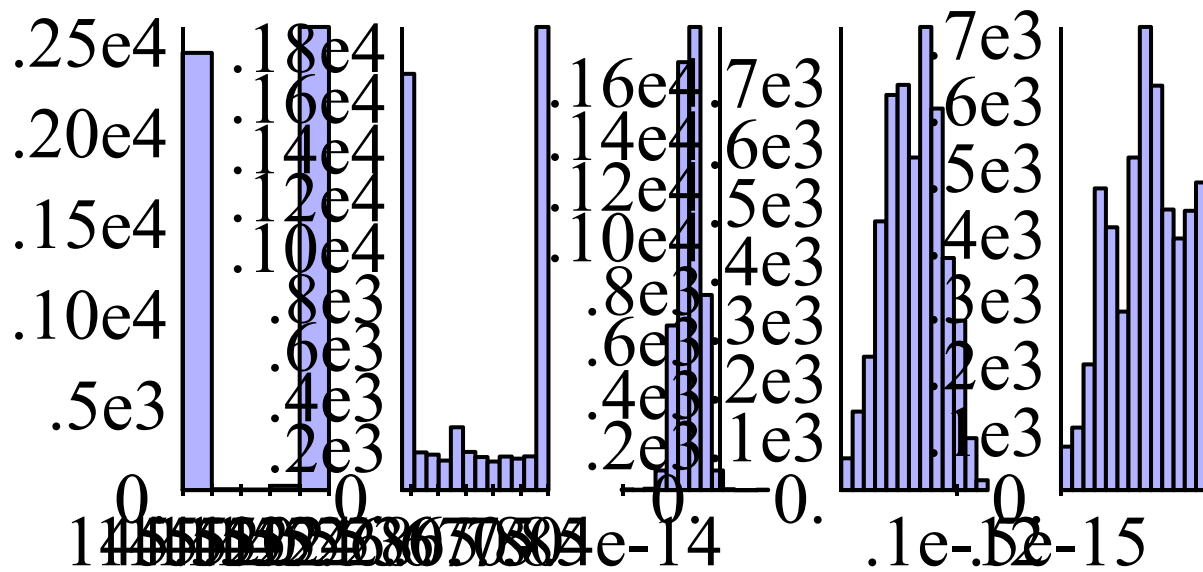
```
0.1663353668309289516322638140650719807854692236835e-14
0.1298002107290185661658002984309817740092867464339e-14
0.32503774605676979973866170816939189446726835978e-16
0.66876859368671702406006421834571807525861810735e-16
-0.198915205460967480007124488540070999390048156957e-15
-0.64856748294610291996291606348652119706579976139e-16
-0.130966147059485811387264435831470495534462733396e-15
0.102746087580545496077136792846645368562975634767e-15
0.236282661964082432953446629967657303102041123977e-15
0.569640932690633145581794119442207241066806947809e-15
0.102820773883983736168852072885087655456514687861e-15
0.335751631926244491554731400387479662346070830228e-15
```

```
> display(graph3a,{op(graph3b),graph3c,plot(0, x=XFinal[1]+
  BinLengthScaled/2..XFinal[NumBins]-BinLengthScaled/2,color=black)}, axes=
  boxed, title=title3, titlefont=[Times,14,bold],
  labels=["Wavelength (microns)","Flux (W m^-2 um^-1)"], labelfont=[Arial,11,
  bold], font=[Arial,11,bold], labeldirections=[horizontal,vertical]);
```

ISO145\_Car2.spi, position 14  
MCMC  $\chi^2$  fit to Gaussian

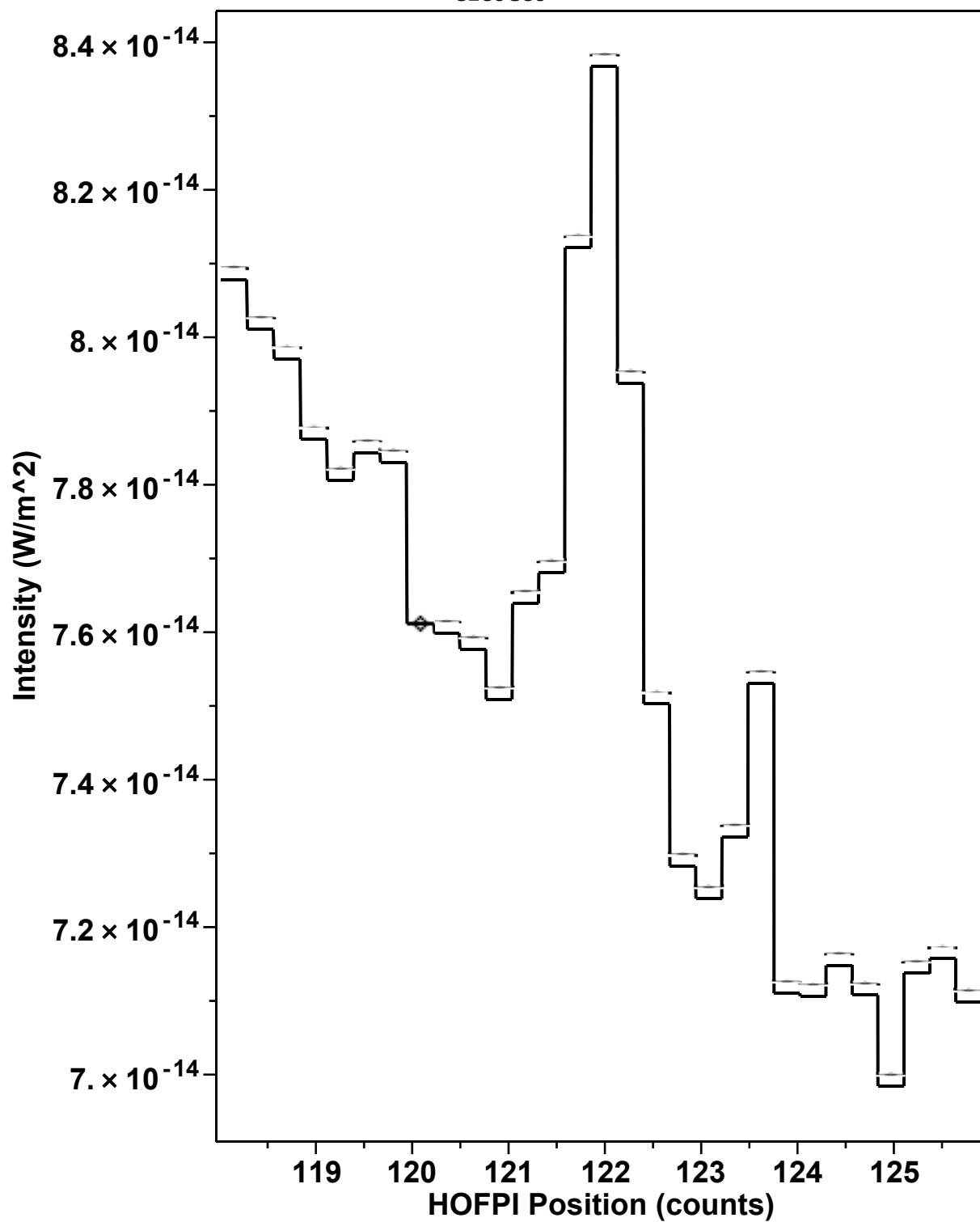


```
> display(array([Cpdf,Fpdf,Spdf,Opdf,Hpdf]));
```



```
> display({graph2a,op(graph2b)},view=[XScaled[NumBins]
-BinLengthScaled/2..XScaled[1]+BinLengthScaled/2,(min(op(convert
(YScaled,list)))-0.05*(max(op(convert(YScaled,list)))-min(op
(convert(YScaled,list))))..(max(op(convert(YScaled,list)))+0.05*
(max(op(convert(YScaled,list)))-min(op(convert(YScaled,list))))
],axes=boxed,title=title2, titlefont=[Times,16,bold], labels=["HOFPI
Position (counts)","Intensity (W/m^2)", labelfont=[Arial,11,bold], font=
[Arial,11,bold], labeldirections=[horizontal,vertical]]);
```

# ISO122\_Car2.spi, position 20, scaled ISO data



```
> display({graph1a,op(graph1b)},view=[X[NumBins]-BinLength/2..X[1]+  
BinLength/2,(min(op(convert(Y,list)))-0.05*(max(op(convert(Y,  
list)))-min(op(convert(Y,list)))))..(max(op(convert(Y,list)))+  
0.05*(max(op(convert(Y,list)))-min(op(convert(Y,list))))],axes=  
boxed,title=title1, titlefont=[Times,16,bold], labels=["HOFPI Position  
(counts)","Signal (mV)"], labelfont=[Arial,11,bold], font=[Arial,11,bold],  
labeldirections=[horizontal,vertical]);
```



# ISO122\_Car2.spi, position 20, raw ISO data

