

## HW2 – Report

1. Precision at rank 10 is a measure of the proportion of relevant documents within the top ten documents returned by your search engine. Average precision can be considered to be the area under the interpolated curve when you plot the precision (y) and recall (x) on a cartesian plot. Therefore, average precision is recall sensitive.

One would want to use precision at rank 10 instead of average precision in a situation where recall is less important than precision. This could be, for example, searching up the definition of a word on google. When doing this, you want to ideally only consult one website to fulfil your information need. It is important for the top results to be exactly what you are looking for. It is much less important for all the web pages that define your word (hundreds of online dictionaries), to be returned. In this situation, you can find exactly what you want with terrible recall, meaning a very low average precision.

This average precision would be lower than one that you would want when searching for a washing machine on an e-commerce website, where you would want to see most likely everything they have on offer and would feel cheated if you were not shown all the washing machines. In the second case, you would prefer average precision over precision at rank 10.

2. NDCG is normalized, discounted, cumulative, gain. As defined in question 1, precision at rank 10 is the proportion of relevant documents within the top ten documents returned by the search engine.

The notion of a proportion of a “relevant” or “non-relevant” document used by precision at rank ten implies that gain must be binary. This is the first advantage of nDCG at rank 10; it takes into account graded relevance. This is a more realistic way to model search results as a document can be somewhat relevant to a user.

The second advantage of nDCG at rank 10 is that it has a measure of discount. Users do not all reach the same rank and will not receive any gain from results past where they stop reading. Precision at rank 10 unrealistically assumes that users will look at all the first ten results and will count gain from results that would not be visited. NDCG is therefore a more accurate model of user behavior.

3.
  - a. Randomization and Bootstrapping tests are appropriate to determine the statistical significance of the two medians because they can be used with any statistic (mean, median, mode) and are distribution free. A student’s T test only applies to means and thus cannot be applied to determine the statistical significance of the difference between two medians. The sign test can incorrectly predict significance and should not be used in IR research (Smucker, Alan, & Carterette, 2007).
  - b. You should use a non-paired test of statistical significance because these are two independent groups doing the evaluations of the two systems. If it was the same group doing both evaluations then a paired test would be appropriate.

- c. As mentioned in B, the same group would need to complete both evaluations for a paired T test to be appropriate. Meaning that one group of 50 users would evaluate both system A and system B. In this situation, to account for the effect of users having seen the evaluation questions already when evaluating their second search engine, the order in which they evaluate them would need to be different for two halves of the group, split randomly.
  - d. In a situation where we calculate a p-value of 0.8, we say that we “fail to reject the null hypothesis”. A p-value of 0.8 means that according to our statistical test (which can be flawed), there is an 80% chance that the difference in our results could have occurred randomly under the null hypothesis. This does not mean that you have proven the null hypothesis. The statement “we are forced to accept the null hypothesis” would only be appropriate if you had statistically significant data showing that the null hypothesis is true. In this case we only fail to have statistically significant data showing that it is untrue. Thus, we “fail to reject the null hypothesis”.
- 4.
- a. The null hypothesis of the randomization test is that both systems are in fact the same and any variation in performance is caused by randomness. To evaluate this, the randomization test assigns random signs, to the difference between the nDCG of the two systems in question for each of the 50 topics and calculates the mean difference in nDCG. If 1000 samples are used, this is done 1000 different times with 1000 randomizations of the differences in nDCG for the 50 topics. Thus, the randomization test found that the absolute value of the mean difference in nDCG for systems A and B is greater than  $|0.21-0.39|$  6% of the time (60 out of 1000 times). The second test found that the absolute value of the mean difference in nDCG for systems A and C is greater than  $|0.21-0.22|$  0.2% of the time (2 out of 1000 times).
  - b. In this situation, C is clearly statistically significant, beyond much doubt. However, it offers only a very small improvement in normalized discounted cumulated gain compared to A. This means that C is probably consistently offering a very small improvement. B on the other hand, offers a larger average improvement but is not quite statistically significant. This indicates a lot of variance in the differences in nDCG between A and B.  
In this situation, I would recommend further testing. One measure of search engine quality used with one set of topics and one statistical test is hardly definitive. I would recommend using other measures such as MAP and perhaps different topic sets as well if they are available. This would give a clearer picture of what should be implemented.

5.

- a. Table from hw3-5a-WatIAMUserID.csv (also contains bolding and italicization from “b”):

| Run Name    | Mean Average Precision | Mean P@10    | Mean NDCG@10 | Mean NDCG@1000 | Mean TBG     |
|-------------|------------------------|--------------|--------------|----------------|--------------|
| msmuckerAND | 0.098                  | 0.133        | 0.17         | 0.202          | 0.818        |
| student1    | <b>0.25</b>            | <i>0.282</i> | <b>0.371</b> | <b>0.485</b>   | <b>2.03</b>  |
| student2    | 0.141                  | 0.193        | 0.251        | 0.344          | 1.25         |
| student3    | 0.099                  | 0.158        | 0.181        | 0.312          | 1.252        |
| student4    | 0.202                  | 0.244        | 0.328        | 0.427          | 1.753        |
| student5    | <i>0.224</i>           | 0.256        | 0.32         | <i>0.464</i>   | <i>1.976</i> |
| student6    | bad format             | bad format   | bad format   | bad format     | bad format   |
| student7    | 0.107                  | 0.153        | 0.189        | 0.284          | 1.209        |
| student8    | 0.213                  | 0.26         | <i>0.346</i> | 0.438          | 1.864        |
| student9    | 0.139                  | 0.204        | 0.241        | 0.327          | 1.586        |
| student10   | bad format             | bad format   | bad format   | bad format     | bad format   |
| student11   | 0.137                  | 0.167        | 0.21         | 0.299          | 1.125        |
| student12   | bad format             | bad format   | bad format   | bad format     | bad format   |
| student13   | 0.073                  | <b>0.747</b> | 0.115        | 0.199          | 0.767        |
| student14   | 0.2                    | 0.251        | 0.323        | 0.414          | 1.753        |


- b. See bolding and italics in table above.  
c. See Table in D  
d. See Table Below.

| Effectiveness Measure | Best run score | Second best run score | Relative Percent Improvement | Student's t-test, two-side, paired, p-value |
|-----------------------|----------------|-----------------------|------------------------------|---|
| Mean AP               | 0.25           | 0.224                 | 11.46%                       | 0.171                                       |
| Mean P@10             | 0.747          | 0.282                 | 164.57%                      | 0.001*                                      |
| Mean NDCG@10          | 0.371          | 0.346                 | 7.44%                        | 0.248                                       |
| Mean NDCG@1000        | 0.485          | 0.464                 | 4.67%                        | 0.193                                       |
| MEAN TBG              | 2.03           | 1.976                 | 2.722                        | 0.569                                       |

- e. The run for student 2 is below

```
PS C:\Users\thoma\Documents\3Bterm\MSCI541\hw3-thomaspenns> python Evaluate.py LA-only.trec8-401.450.minus416-423-437-444-447.txt s
tudent2.results
PS C:\Users\thoma\Documents\3Bterm\MSCI541\hw3-thomaspenns>
```


This produces two output files, one CSV file for computing purposes and one human readable TXT file.

 student2-measures

2022-11-04 9:42 PM

Microsoft Excel Com...

4 KB

 student2-measures

2022-11-04 9:42 PM

Text Document

8 KB

The human readable text file output is similar to the sample output provided for the assignment. Abbreviations are used for each metric: AP for average precision, P@10 for precision at rank 10, nDCG@10 and nDCG@1000 for normalised discounted cumulated gain at ranks 10 and 1000 respectively, and TBG for time biased gain. The full contents of the file can be found in Appendix A.

The run for student 12 is below:

```
PS C:\Users\thoma\Documents\3Bterm\MSCI541\hw3-thomaspaenns> python Evaluate.py LA-only.trec8-401.450.minus416-423-437-444-447.txt s
tudent12.results
Use correctly formatted results file please
PS C:\Users\thoma\Documents\3Bterm\MSCI541\hw3-thomaspaenns>
```

For this run, the results file is incorrectly formatted so the program simply prompts the user to use a correctly formatted results file.

6. This answer is written assuming that the instructions meant we should compare the best overall student run with the msmuckerAND run, not the individual best for each metric. The best student run was by far the run for Student 1. It had the top metric in 4 of the five categories and in the one where it was not the top, it was the second best. The metric chose was the student's two side, paired T-test. This is appropriate as the metrics being compared are means. The metrics for the student1 run and the msmuckerAND run are compared in the table below.

| Effectiveness Measure | student1 Score | smuckerAND score | Relative Percent Improvement | Student's t-test, two-side, paired, p-value |
|-----------------------|----------------|------------------|------------------------------|---|
| Mean AP               | 0.25           | 0.098            | 155.42                       | 0   |
| Mean P@10             | 0.282          | 0.133            | 111.667                      | 0   |
| Mean NDCG@10          | 0.371          | 0.17             | 117.871                      | 0   |
| Mean NDCG@1000        | 0.485          | 0.202            | 140.396                      | 0   |
| MEAN TBG              | 2.03           | 0.818            | 148.017                      | 0   |

Note that the values in the above table are rounded to three decimal places. As such, the P-values are all shown to be zero. Running my script without rounding showed that all the P values are around  $E^{-6}$  order, meaning that there are non-zero values beginning at 6 decimal places. This means that the results are most definitely statistically significant. The large relative percentages of improvement indicate that the conventional search engine far surpasses a BooleanAnd search in terms of all these metrics. Overall, the BooleanAnd search had far too many searches with no results or no relevant results to measure up against the conventional algorithm.

There are very few topics where BooleanAnd performs better than or equal to Student1. In some cases they are equal for some metrics. In the table below, you can see the delta between a metric for student1 and booleanAnd. In the green cells, it is above or equal to zero:

|     | MAP      | P@10 | Ndcg@10  | NDCG@1000   | TBG      |
|-----|----------|------|----------|-------------|----------|
| 401 | -0.09339 | -0.2 | -0.16141 | -0.39337194 | -1.23495 |
| 402 | -0.17095 | -0.2 | -0.20098 | -0.48183076 | -1.695   |
| 403 | -0.02393 | -0.2 | -0.06753 | 0.03490317  | -0.24765 |
| 404 | -0.0104  | 0    | 0        | -0.171972   | -0.01044 |
| 405 | -0.01215 | 0    | 0.021424 | -0.08161878 | -0.71378 |
| 406 | -0.29029 | -0.1 | -0.28551 | -0.29156091 | -1.04361 |
| 407 | -0.1322  | -0.3 | -0.28351 | -0.40892291 | -2.00739 |
| 408 | -0.12036 | -0.3 | -0.35971 | -0.37214776 | -2.96821 |
| 409 | -0.1     | -0.1 | -0.28906 | -0.28906483 | -0.35688 |
| 410 | 0        | 0    | 0        | 0           | -0.01411 |
| 411 | -0.17542 | -0.3 | -0.4441  | -0.47233631 | -1.97519 |
| 412 | -0.36476 | -0.6 | -0.55275 | -0.30135434 | -5.11812 |
| 413 | -0.08333 | 0    | 0        | -0.27023815 | -0.31937 |
| 414 | -0.10539 | -0.1 | -0.20211 | -0.34365427 | -0.55178 |
| 415 | -0.21429 | 0    | -0.26025 | -0.26025337 | -0.26797 |
| 417 | -0.28272 | -0.6 | -0.70077 | -0.29626608 | -2.83295 |
| 418 | -0.26042 | -0.6 | -0.72733 | -0.61805722 | -4.72893 |
| 419 | -0.325   | -0.2 | -0.35915 | -0.35914753 | -0.66207 |
| 420 | -0.25076 | -0.3 | -0.22784 | -0.28173609 | -1.34795 |
| 421 | -0.0168  | 0    | 0        | -0.24663103 | -0.25443 |
| 422 | -0.34997 | -0.5 | -0.38785 | -0.62950483 | -7.15262 |
| 424 | -0.14128 | -0.1 | -0.06362 | -0.494983   | -2.07012 |
| 425 | -0.18883 | 0    | -0.16592 | -0.35314712 | -1.29274 |
| 426 | -0.00069 | 0.3  | 0.249843 | -0.04705346 | -0.22524 |
| 427 | -0.05267 | -0.1 | -0.08514 | -0.25152072 | -1.14797 |
| 428 | -0.06501 | 0    | -0.05613 | -0.19246116 | -0.22102 |
| 429 | -0.54861 | -0.3 | -0.53195 | -0.53194603 | -1.22056 |
| 430 | -0.47359 | -0.2 | -0.36005 | -0.44913488 | -1.11408 |
| 431 | -0.23476 | -0.2 | -0.21821 | -0.45789924 | -1.65665 |
| 432 | -0.00167 | 0    | 0        | -0.06787393 | -0.05126 |
| 433 | -0.00484 | 0    | 0        | -0.10910973 | -0.01684 |
| 434 | -0.5157  | -0.1 | -0.61315 | -0.60253691 | -0.44725 |
| 435 | -0.03831 | 0    | 0        | -0.27550377 | -0.55348 |
| 436 | -0.05905 | -0.4 | -0.35546 | -0.20662764 | -2.25209 |
| 438 | -0.08859 | -0.1 | -0.0784  | -0.25990853 | -1.18161 |
| 439 | -0.0146  | 0    | 0        | -0.1679477  | -0.33279 |
| 440 | -0.51778 | -0.5 | -0.62741 | -0.47082615 | -2.60215 |
| 441 | -0.15884 | -0.3 | -0.22961 | -0.00044724 | -0.42876 |
| 442 | -0.00871 | 0.2  | 0.189379 | -0.126234   | -0.32027 |
| 443 | -0.05858 | -0.1 | -0.08852 | -0.23714757 | -0.6496  |
| 445 | -0.21944 | -0.2 | -0.41618 | -0.23787745 | -0.6947  |
| 446 | -0.02142 | 0    | 0        | -0.19127231 | -0.16258 |

|            |          |   |          |             |          |
|------------|----------|---|----------|-------------|----------|
| <b>448</b> | -0.00925 | 0 | 0        | -0.19489335 | -0.02431 |
| <b>449</b> | -0.00698 | 0 | 0        | -0.0898461  | -0.22572 |
| <b>450</b> | -0.02717 | 0 | -0.09985 | -0.20690536 | -0.11221 |

From this table, we can see that topic 410 is the only place where the algorithms seem to be on an equal footing. In some other topics, BooleanAnd is equal or better only for the metrics at rank 10, most likely because it may return far fewer documents. Overall however, the Student1 run is far better by all metrics considered and this is statistically significant with p-values less than 0.001.

## Appendix A – Full Output for Student 2

|      |     |                       |         |     |                     |
|------|-----|-----------------------|---------|-----|---------------------|
| AP   | 401 | 0.0403377583185201    | P@10    | 418 | 0.4                 |
| AP   | 402 | 0.155595467805563     | P@10    | 419 | 0.1                 |
| AP   | 403 | 0.5181658314928408    | P@10    | 420 | 0.6                 |
| AP   | 404 | 0.026792114695340503  | P@10    | 421 | 0.0                 |
| AP   | 405 | 0.023218294051627383  | P@10    | 422 | 0.2                 |
| AP   | 406 | 0.5396358524344804    | P@10    | 424 | 0.3                 |
| AP   | 407 | 0.12691027321387646   | P@10    | 425 | 0.3                 |
| AP   | 408 | 0.17613258578682506   | P@10    | 426 | 0.2                 |
| AP   | 409 | 0.07142857142857142   | P@10    | 427 | 0.1                 |
| AP   | 410 | 0.7028846153846153    | P@10    | 428 | 0.0                 |
| AP   | 411 | 0.2835203570626717    | P@10    | 429 | 0.1                 |
| AP   | 412 | 0.0969455240957383    | P@10    | 430 | 0.3                 |
| AP   | 413 | 0.005405405405405406  | P@10    | 431 | 0.6                 |
| AP   | 414 | 0.10833333333333334   | P@10    | 432 | 0.0                 |
| AP   | 415 | 0.125                 | P@10    | 433 | 0.0                 |
| AP   | 417 | 0.05884848769805482   | P@10    | 434 | 0.0                 |
| AP   | 418 | 0.07067448933608388   | P@10    | 435 | 0.1                 |
| AP   | 419 | 0.28407014979905004   | P@10    | 436 | 0.4                 |
| AP   | 420 | 0.48257872961484244   | P@10    | 438 | 0.1                 |
| AP   | 421 | 0.005804936852296678  | P@10    | 439 | 0.1                 |
| AP   | 422 | 0.03867659574599077   | P@10    | 440 | 0.1                 |
| AP   | 424 | 0.05506923888302862   | P@10    | 441 | 0.5                 |
| AP   | 425 | 0.2720934005508434    | P@10    | 442 | 0.2                 |
| AP   | 426 | 0.018594560268947468  | P@10    | 443 | 0.2                 |
| AP   | 427 | 0.05366500273711303   | P@10    | 445 | 0.0                 |
| AP   | 428 | 0.01111111111111111   | P@10    | 446 | 0.1                 |
| AP   | 429 | 0.25                  | P@10    | 448 | 0.0                 |
| AP   | 430 | 0.3990972950304047    | P@10    | 449 | 0.1                 |
| AP   | 431 | 0.1421563816876285    | P@10    | 450 | 0.0                 |
| AP   | 432 | 0.0026239052263011143 | nDCG@10 | 401 | 0.06943122193677727 |
| AP   | 433 | 0.010852451641925326  | nDCG@10 | 402 | 0.3499667779514209  |
| AP   | 434 | 0.002551020408163265  | nDCG@10 | 403 | 0.5766882048947064  |
| AP   | 435 | 0.02262963461382038   | nDCG@10 | 404 | 0.0                 |
| AP   | 436 | 0.028251423059134598  | nDCG@10 | 405 | 0.06943122193677727 |
| AP   | 438 | 0.01677592827690599   | nDCG@10 | 406 | 0.5682963021961281  |
| AP   | 439 | 0.04701077174424722   | nDCG@10 | 407 | 0.39375843764607193 |
| AP   | 440 | 0.17038995950286273   | nDCG@10 | 408 | 0.5384313152574521  |
| AP   | 441 | 0.6486111111111111    | nDCG@10 | 409 | 0.0                 |
| AP   | 442 | 0.010270990970239717  | nDCG@10 | 410 | 0.8048099750039491  |
| AP   | 443 | 0.12274342016822896   | nDCG@10 | 411 | 0.6870165078530993  |
| AP   | 445 | 0.0                   | nDCG@10 | 412 | 0.1681522864689108  |
| AP   | 446 | 0.02130996448778139   | nDCG@10 | 413 | 0.0                 |
| AP   | 448 | 0.0                   | nDCG@10 | 414 | 0.2836929289153804  |
| AP   | 449 | 0.041666666666666664  | nDCG@10 | 415 | 0.24630238874073    |
| AP   | 450 | 0.049333767966270765  | nDCG@10 | 417 | 0.13886244387355454 |
| P@10 | 401 | 0.1                   | nDCG@10 | 418 | 0.34445239307233994 |
| P@10 | 402 | 0.3                   | nDCG@10 | 419 | 0.3903800499921017  |
| P@10 | 403 | 0.5                   | nDCG@10 | 420 | 0.6339753813071974  |
| P@10 | 404 | 0.0                   | nDCG@10 | 421 | 0.0                 |
| P@10 | 405 | 0.1                   | nDCG@10 | 422 | 0.20248323207250624 |
| P@10 | 406 | 0.4                   | nDCG@10 | 424 | 0.3222722491219547  |
| P@10 | 407 | 0.3                   | nDCG@10 | 425 | 0.3963918729015093  |
| P@10 | 408 | 0.4                   | nDCG@10 | 426 | 0.14465249243306436 |
| P@10 | 409 | 0.0                   | nDCG@10 | 427 | 0.22009176629808017 |
| P@10 | 410 | 0.3                   | nDCG@10 | 428 | 0.0                 |
| P@10 | 411 | 0.6                   | nDCG@10 | 429 | 0.3903800499921017  |
| P@10 | 412 | 0.2                   | nDCG@10 | 430 | 0.5773584151532217  |
| P@10 | 413 | 0.0                   | nDCG@10 | 431 | 0.4362115423097744  |
| P@10 | 414 | 0.2                   | nDCG@10 | 432 | 0.0                 |
| P@10 | 415 | 0.1                   | nDCG@10 | 433 | 0.0                 |
| P@10 | 417 | 0.1                   | nDCG@10 | 434 | 0.0                 |

|           |     |                     |     |     |                        |
|-----------|-----|---------------------|-----|-----|------------------------|
| nDCG@10   | 435 | 0.07336392209936005 | TBG | 406 | 2.5237021311587293     |
| nDCG@10   | 436 | 0.38589303732090635 | TBG | 407 | 2.0596840601130197     |
| nDCG@10   | 438 | 0.06943122193677727 | TBG | 408 | 4.369457841344936      |
| nDCG@10   | 439 | 0.13886244387355454 | TBG | 409 | 0.29989928021294365    |
| nDCG@10   | 440 | 0.22009176629808017 | TBG | 410 | 1.3729268048807286     |
| nDCG@10   | 441 | 0.81383546042969    | TBG | 411 | 2.7014945041411504     |
| nDCG@10   | 442 | 0.16421958630632802 | TBG | 412 | 1.6378641018146731     |
| nDCG@10   | 443 | 0.2863459897524692  | TBG | 413 | 0.0002543214186581846  |
| nDCG@10   | 445 | 0.0                 | TBG | 414 | 0.6950101585229458     |
| nDCG@10   | 446 | 0.06625422345438903 | TBG | 415 | 0.45466224320881293    |
| nDCG@10   | 448 | 0.0                 | TBG | 417 | 1.1062188700376006     |
| nDCG@10   | 449 | 0.12647135138382856 | TBG | 418 | 2.387557960279907      |
| nDCG@10   | 450 | 0.0                 | TBG | 419 | 0.6699494300991664     |
| nDCG@1000 | 401 | 0.34531796226771455 | TBG | 420 | 4.4873838268175215     |
| nDCG@1000 | 402 | 0.5644811891434851  | TBG | 421 | 0.005358914219573441   |
| nDCG@1000 | 403 | 0.8043327944774391  | TBG | 422 | 1.828279653416333      |
| nDCG@1000 | 404 | 0.20677703780378764 | TBG | 424 | 2.158547129926396      |
| nDCG@1000 | 405 | 0.12192609118967468 | TBG | 425 | 3.530478129416083      |
| nDCG@1000 | 406 | 0.8213458149293233  | TBG | 426 | 1.48108953398607       |
| nDCG@1000 | 407 | 0.46983966017884593 | TBG | 427 | 0.821667316336073      |
| nDCG@1000 | 408 | 0.5043200013417638  | TBG | 428 | 0.11010817761988546    |
| nDCG@1000 | 409 | 0.2559580248098155  | TBG | 429 | 0.4764708553148599     |
| nDCG@1000 | 410 | 0.8693954474736921  | TBG | 430 | 1.341096092688127      |
| nDCG@1000 | 411 | 0.5706678667406713  | TBG | 431 | 2.4882102758727025     |
| nDCG@1000 | 412 | 0.47003365567540917 | TBG | 432 | 0.04830877756307518    |
| nDCG@1000 | 413 | 0.13264079256781566 | TBG | 433 | 0.09517058908482569    |
| nDCG@1000 | 414 | 0.2836929289153804  | TBG | 434 | 0.00013608540466778765 |
| nDCG@1000 | 415 | 0.24630238874073    | TBG | 435 | 0.47363943347187254    |
| nDCG@1000 | 417 | 0.3120255562188371  | TBG | 436 | 2.1169648163008623     |
| nDCG@1000 | 418 | 0.31634725600759656 | TBG | 438 | 0.5871862856087394     |
| nDCG@1000 | 419 | 0.5371844324883698  | TBG | 439 | 0.4487811030201035     |
| nDCG@1000 | 420 | 0.8025593814675845  | TBG | 440 | 1.1587069633647902     |
| nDCG@1000 | 421 | 0.14138056597469106 | TBG | 441 | 2.042086314516553      |
| nDCG@1000 | 422 | 0.24340190493419323 | TBG | 442 | 0.8783985932395991     |
| nDCG@1000 | 424 | 0.28963303303702886 | TBG | 443 | 0.887183199253599      |
| nDCG@1000 | 425 | 0.6273705715199219  | TBG | 445 | 0.0                    |
| nDCG@1000 | 426 | 0.16958503154759783 | TBG | 446 | 0.5274382597487242     |
| nDCG@1000 | 427 | 0.22931594445056047 | TBG | 448 | 0.0                    |
| nDCG@1000 | 428 | 0.1313686820619115  | TBG | 449 | 0.4445312234168459     |
| nDCG@1000 | 429 | 0.3903800499921017  | TBG | 450 | 0.5613802038434605     |
| nDCG@1000 | 430 | 0.6936246003813059  |     |     |                        |
| nDCG@1000 | 431 | 0.45056320819115575 |     |     |                        |
| nDCG@1000 | 432 | 0.08685168454816747 |     |     |                        |
| nDCG@1000 | 433 | 0.13057954254544643 |     |     |                        |
| nDCG@1000 | 434 | 0.08044384993556623 |     |     |                        |
| nDCG@1000 | 435 | 0.20648883759119663 |     |     |                        |
| nDCG@1000 | 436 | 0.1652333830278222  |     |     |                        |
| nDCG@1000 | 438 | 0.1476227415757353  |     |     |                        |
| nDCG@1000 | 439 | 0.18164658358740723 |     |     |                        |
| nDCG@1000 | 440 | 0.4494986628189501  |     |     |                        |
| nDCG@1000 | 441 | 0.81383546042969    |     |     |                        |
| nDCG@1000 | 442 | 0.11173460213428242 |     |     |                        |
| nDCG@1000 | 443 | 0.38526582769247436 |     |     |                        |
| nDCG@1000 | 445 | 0.0                 |     |     |                        |
| nDCG@1000 | 446 | 0.19294029313468744 |     |     |                        |
| nDCG@1000 | 448 | 0.0                 |     |     |                        |
| nDCG@1000 | 449 | 0.12647135138382856 |     |     |                        |
| nDCG@1000 | 450 | 0.3780722023346104  |     |     |                        |
| TBG       | 401 | 0.5944531751747446  |     |     |                        |
| TBG       | 402 | 1.8403250255332442  |     |     |                        |
| TBG       | 403 | 3.42822190225812    |     |     |                        |
| TBG       | 404 | 0.2312341235930742  |     |     |                        |
| TBG       | 405 | 0.8577155983523271  |     |     |                        |