

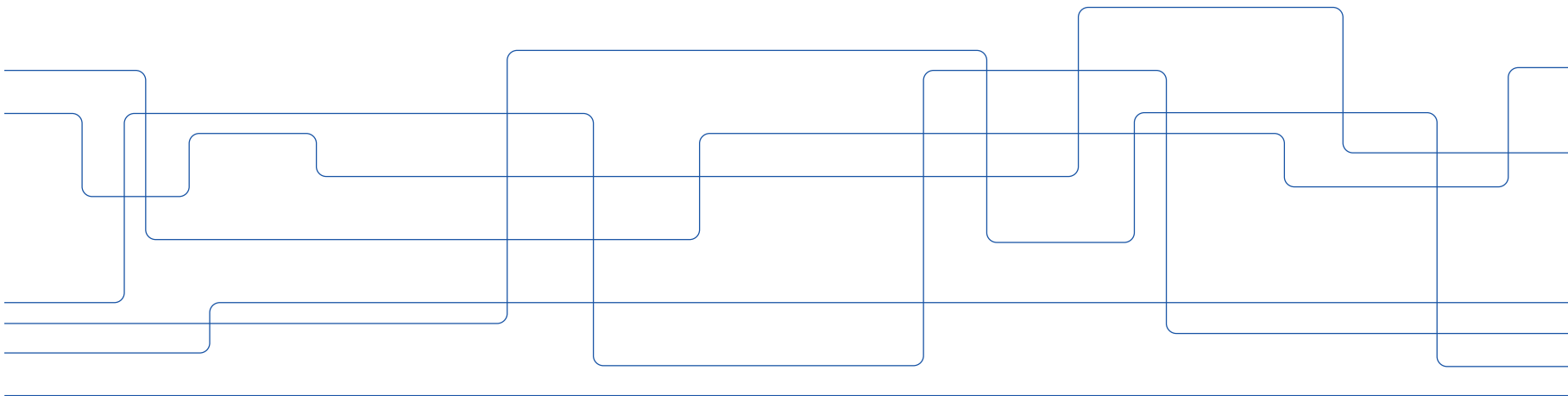


# Applied Vehicle Dynamics Control SD2231

## Lab 3

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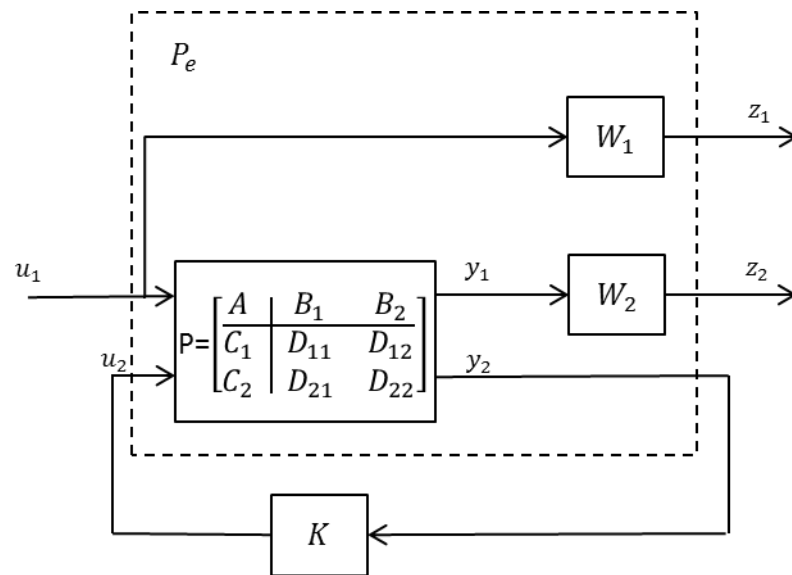
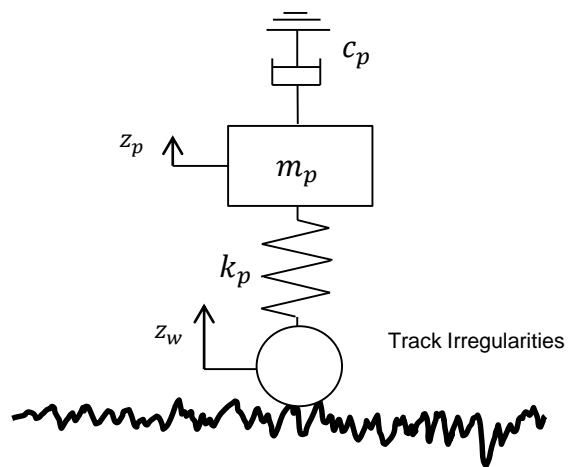


# Introduction

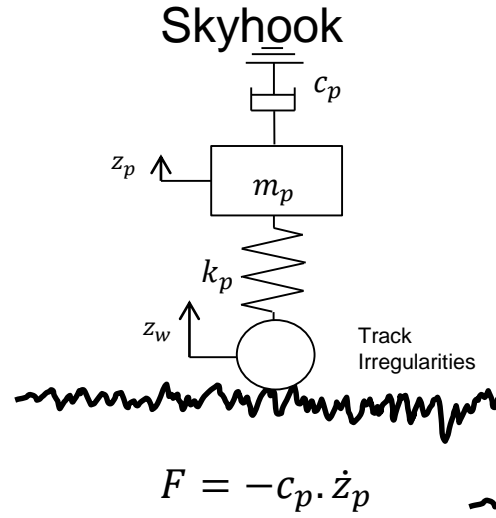
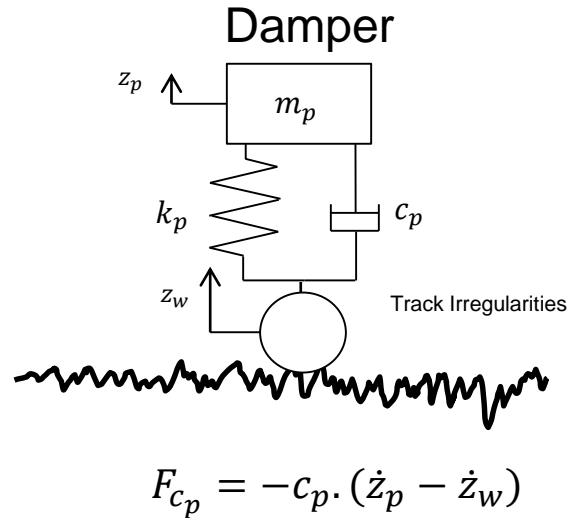
- laboratory aim: control vehicle vibration to improve passenger comfort
- To achieve acceptable vibration level, suspension system is used.
- Passive suspension: springs and dampers
- Active suspension
- Controllers you will use: PD, PID, skyhook and  $H_\infty$

# Theory

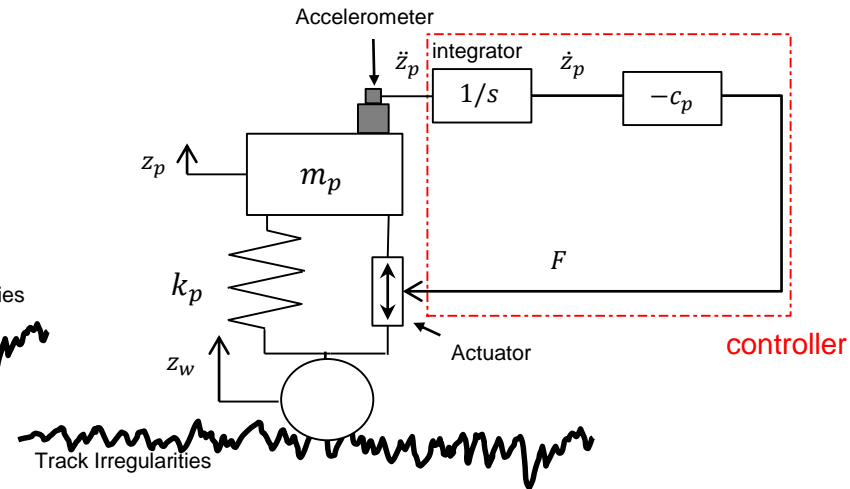
- Skyhook controller
- $H_\infty$  controller



# Skyhook



## Implementation:



- Vibration isolation by decoupling the body from track or road irregularities.

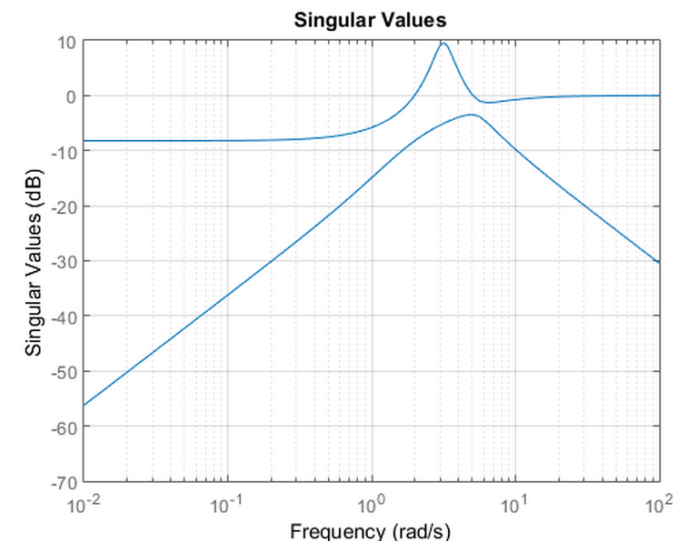
## $H_\infty$ norm:

Infinity norm of a SISO system with transfer function  $P(s)$  is:

$$\|P(s)\|_\infty = \sup_w |P(iw)|$$

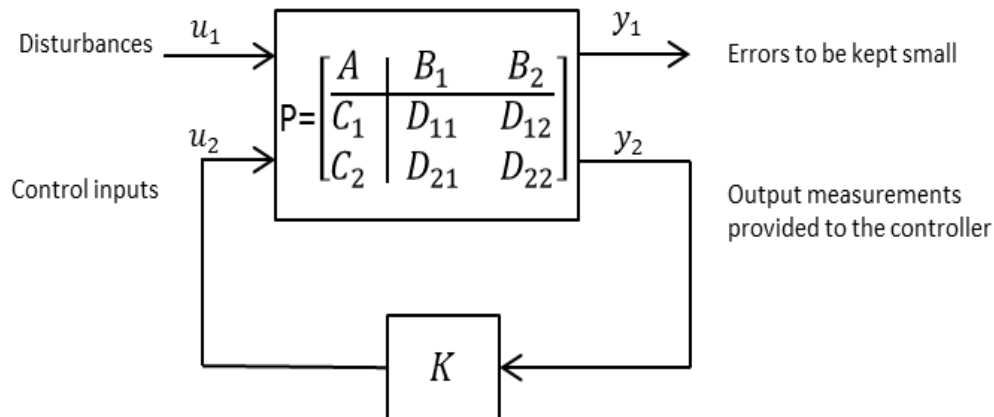
For a MIMO system:

$$\|P(s)\|_\infty = \sup_w |\bar{\sigma}(P(iw))|$$



# $H_\infty$ controller principle:

Consider plant  $P$



The aim is to design a controller so that the infinity norm of the closed-loop system ( $CL$ ) is minimum.

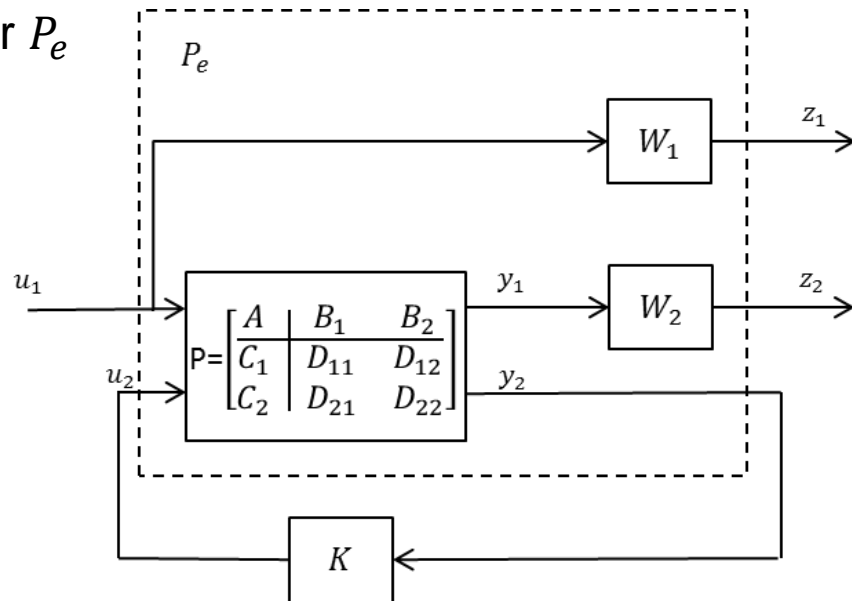
$$\gamma = \|CL\|_\infty$$

$$\min(\gamma)$$

# Extending the model $P$ with weighting functions

One can extend the model  $P$  with weighting functions.

Design controller  $K$  for  $P_e$

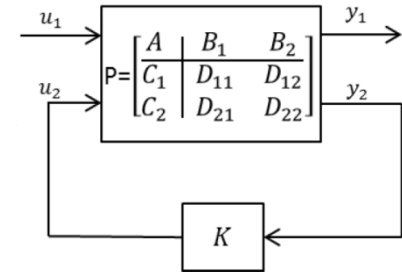


Why? to penalize the desired signals at the desired frequencies.

# Contd.

Having the weighting functions, controller  $K$  can be designed by MATLAB.

**Test:** to check the performance of the derived controller  $K$ , it should be implemented in the control loop of the main model.



**Unsatisfactory response:** Change the weighing functions and look for a new controller.



# $H_\infty$ concept

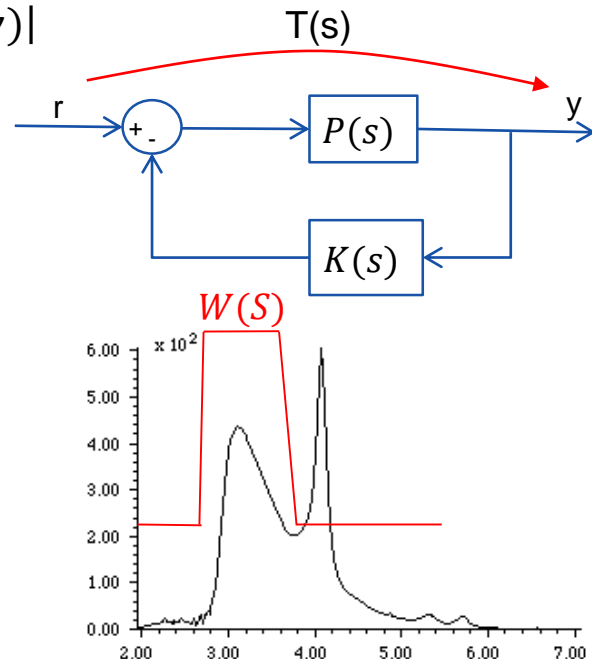
## $H_\infty$ norm:

of a transfer function is its maximum magnitude over the whole frequency range.

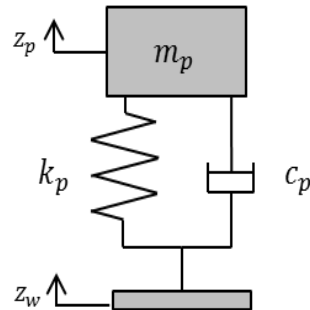
$$\|T(i\omega)\|_\infty = \sup_{\omega} |T(i\omega)|$$

$H_\infty$  control tries to design the controller  $K$  such that the infinity norm of the closed loop transfer function  $T(s)$  is minimized.

We can focus this minimization process on specific frequency ranges by proper weighting functions  $W(s)$  (penalizing)

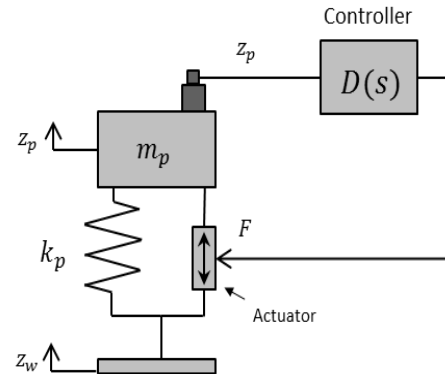


# Control of a single degree of freedom (SDOF) system



Passive

- Damped
- Undamped



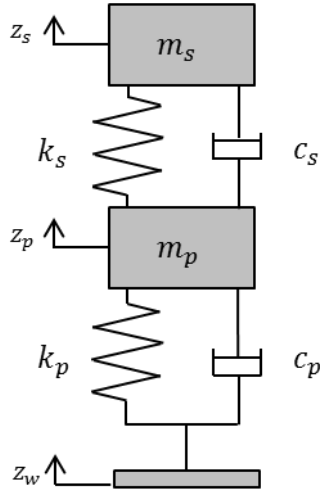
Active

- PD
- PID
- Skyhook

Excitation:

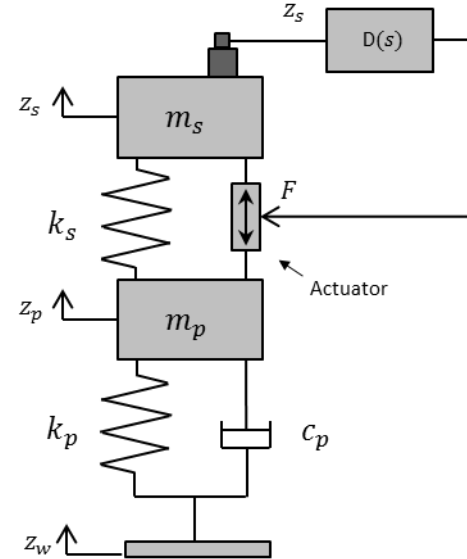
- Sinusoidal excitation
- Impulse response
- Response to track excitation (PSD)

# Control of a 2 degrees of freedom system



Passive

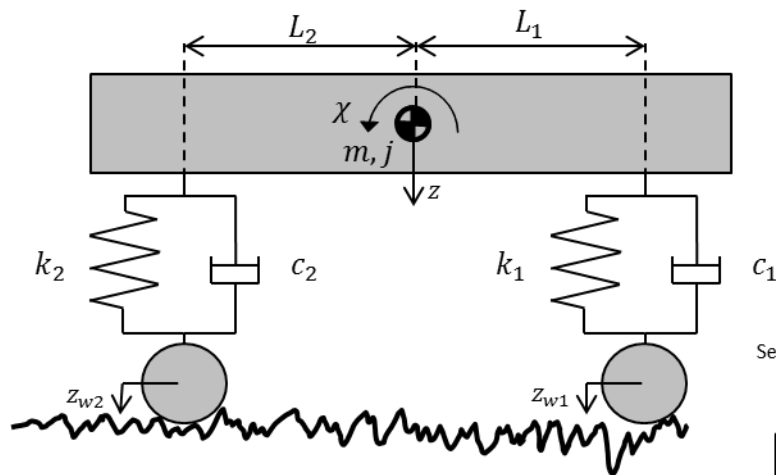
- Damped



Active

- Skyhook

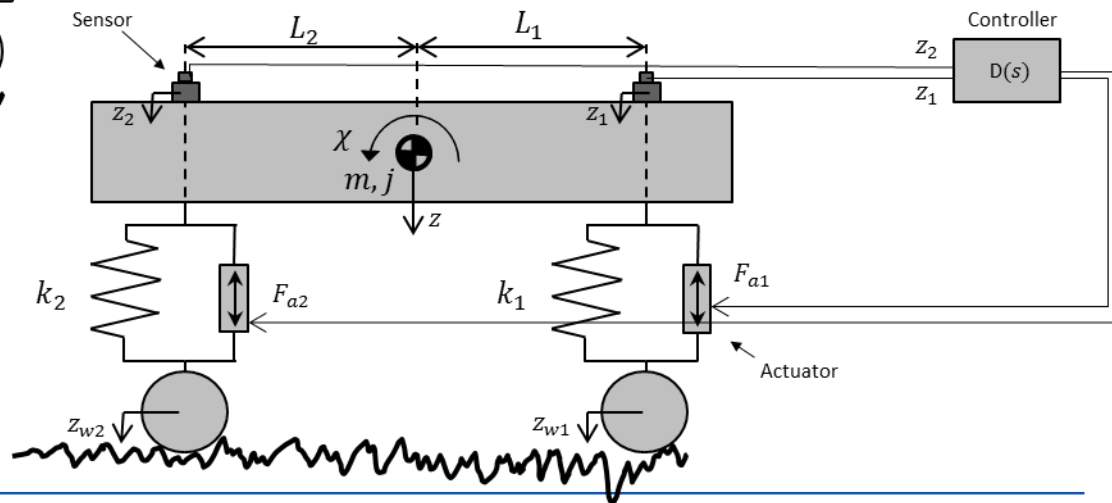
# Control of bounce and pitch using Skyhook and $H_\infty$



Passive system

Active system

- Skyhook
- $H_\infty$





# Report writing

- Read each chapter to the end before answering questions.
- Tasks marked as 'midway step' should be answered but you do not need to reflect them in the report.
- You should use the template on Canvas for your final report.
- **Report grading:** See grading criteria!



# Other notes

## Teachers supporting this Lab:

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Alireza Qazizadeh, [alirezaq@kth.se](mailto:alirezaq@kth.se)

## Lab material:

- You find all necessary documents in Canvas under 'files>Lab 3'
- Almost same presentation was recorded in 2020 and you can find it under 'files>Lab 3>Presentation'

## Supplementary material:

If you have problem with deriving Equations of motion and transfer functions, read chapter 5 of the 'Rail Vehicle Dynamics' book. This can be found on Canvas under 'files>Lab 3>Supplementary material' and the file is named 'Rail vehicle dynamics-chap5'. Sections 5.1 and 5.3 can be very helpful.