

From Collisions to Chosen-Prefix Collisions

Application to Full SHA-1

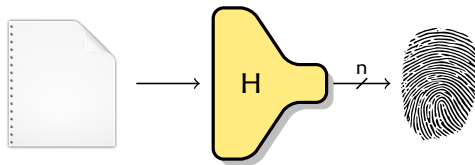
Gaëtan Leurent Thomas Peyrin

Inria, France

NTU, Singapour

Eurocrypt 2019

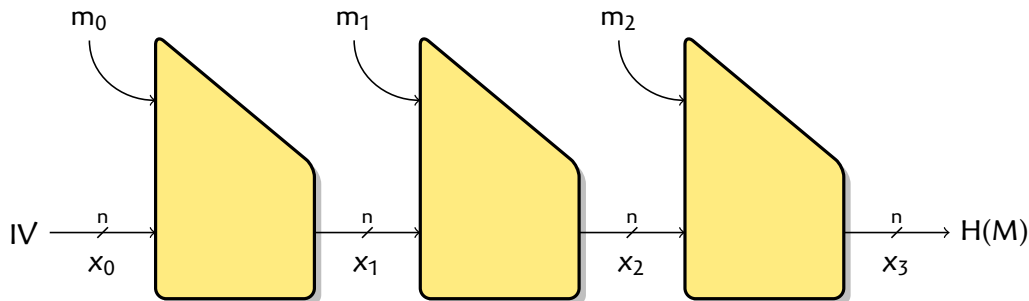
Hash functions



- ▶ Hash function: **public function** $\{0, 1\}^* \rightarrow \{0, 1\}^n$
 - ▶ Maps arbitrary-length message to fixed-length hash
- ▶ Hash function should behave **like a random function**
 - ▶ Hard to find collisions, preimages
 - ▶ Hash can be used as fingerprint, identifier
- ▶ Used in many **different contexts**
 - ▶ Signature: hash-and-sign
 - ▶ MAC: hash-and-PRF
 - ▶ Blockchain: Proof-of-work, ...

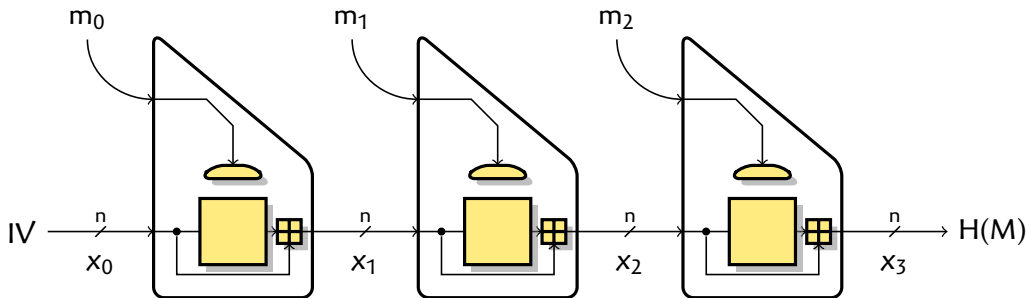
SHA-1

- ▶ Designed by NSA: SHA-0 [1993], then SHA-1 [1995]
- ▶ Standardized by NIST, ISO, IETF, ... Widely used until quite recently
- ▶ State size: $n = 160$
 - ▶ Expected collision security 2^{80}
- ▶ Iterative structure: Merkle-Damgård construction
- ▶ Block cipher-based compression function: Davies-Meyer



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SHA-1 Cryptanalysis

- 2005-02 **Theoretical** collision with 2^{69} operations [Wang & al., Crypto'05]
... Several unpublished collision attacks in the range $2^{51} - 2^{63}$
- 2010-11 **Theoretical** collision with 2^{61} operations [Stevens, EC'13]
- 2015-10 Practical freestart collision (on GPU) [Stevens, Karpman & Peyrin, Crypto'15]
- 2017-02 **Practical** collision with $2^{64.7}$ operations (on GPU) [Stevens & al., Crypto'17]

SHAttered attack: Colliding PDFs

SHAttered

The first concrete collision attack against SHA-1
<https://shattered.io>

CWI

Marc Stevens
Pierre Karpman

Google

Elie Bursztein
Ange Albertini
Yarik Markov

SHA-1 =

38762cf7f55934b34d17

9ae6a4c80cadccbb7f0a

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SHA-1 today

- ▶ Modern web browsers **reject SHA-1 certificates** since 2017
- ▶ SHA-1 certificates **still exists**
 - ▶ CAs still sell legacy SHA-1 certificates



SHA-1 SSL certificate using
Symantec's Private CA technology...

\$995 /yearly

BUY/RENEW NOW

- ▶ SHA-1 certificates **still accepted** by modern non-browser TLS clients
 - ▶ Until a few week ago, a mailserver in TU Darmstadt used a SHA-1 certificate
 - ▶ Windows 10 "Mail" app connects without error

```
$ sslscan mail.sim.informatik.tu-darmstadt.de:993  
[...]
```

SSL Certificate:

Signature Algorithm: **sha1WithRSAEncryption**

- ▶ SHA-1 also used in Git, TLS 1.2 handshake, ...

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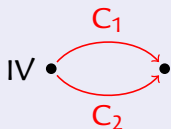
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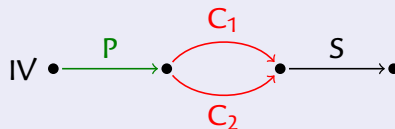
Exploiting collisions

Collision attack



- ▶ Start from IV
- ▶ C_1 and C_2 collide

Adding prefix and suffix



- ▶ Add **identical prefix** and suffix using iterative structure
- ▶ Usually same difficulty (just a different IV)

- ▶ Issue: C_1 and C_2 **look random** (not controlled)
 - ▶ Solution: hide in some ignored sections of the file (e.g. comment)
- ▶ Issue: collision is **not meaningful**
 - ▶ Solution: many file formats (e.g. PDF) allow conditional branches

$M_1 = \text{"if } (C_1 == C_1) \{ \text{good} \} \text{ else } \{ \text{evil} \} \text{"}$

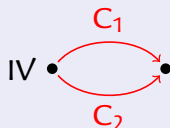
$M_2 = \text{"if } (C_2 == C_1) \{ \text{good} \} \text{ else } \{ \text{evil} \} \text{"}$

prefix

suffix

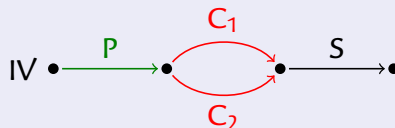
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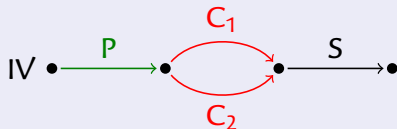
$\underbrace{\hspace{10cm}}$
suffix

Chosen-Prefix Collisions *[Stevens, Lenstra & de Weger, EC'07]*

- ▶ Even with a prefix and suffix, many protocols seem unaffected by collision attacks

Identical-prefix collision

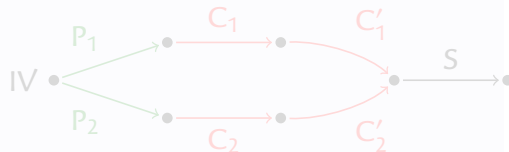
- ▶ Given IV, find $M_1 \neq M_2$ s. t.
 $H(M_1) = H(M_2)$



- ▶ Arbitrary common prefix/suffix, random collision blocks
- ▶ Breaks integrity verification
- ▶ Breaks signatures (in theory)

Chosen-prefix collision

- ▶ Given P_1, P_2 , find $M_1 \neq M_2$ s. t.
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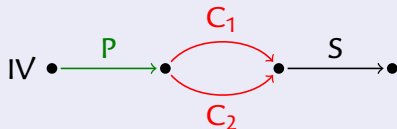
- ▶ Breaks certificates
[Stevens & al, Crypto'09]
- ▶ Breaks TLS, IKE, SSH
[Bhargavan & L, NDSS'16]

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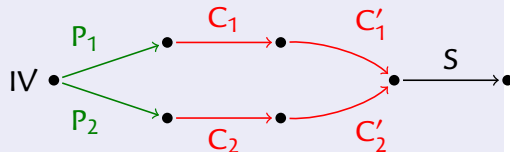
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Attacking key certification

[Stevens, Lenstra & de Weger, EC'07]



PKI Infrastructure

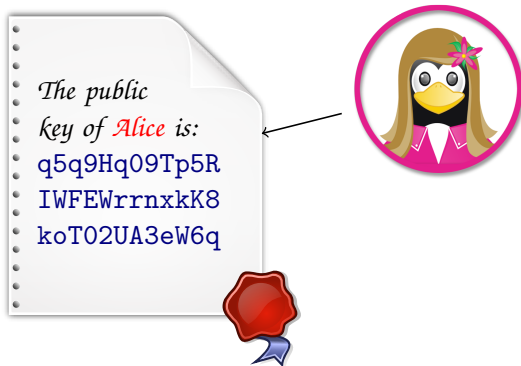
- ▶ Alice generates key
- ▶ Ask PKI to sign
- ▶ Certificate proves ID

Impersonation attack

- Bob creates keys s.t. $H(\text{Alice}||k_A) = H(\text{Bob}||k_B)$
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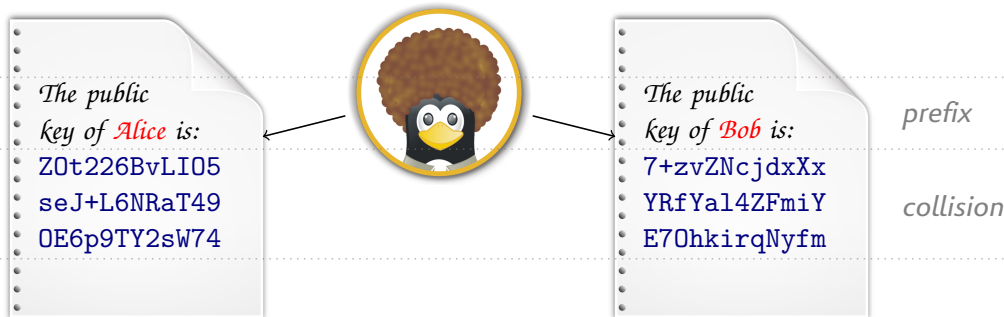
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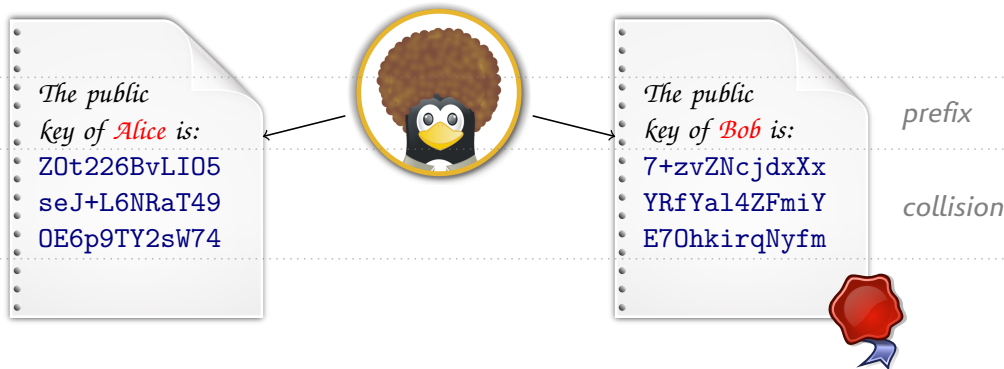
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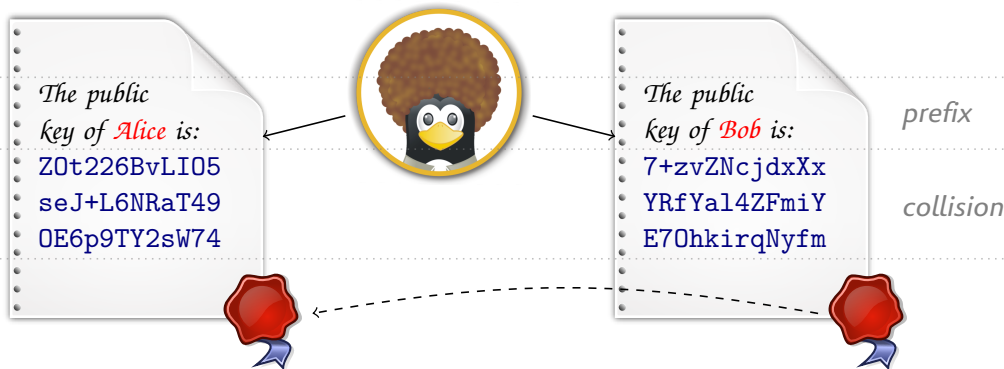
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Outline

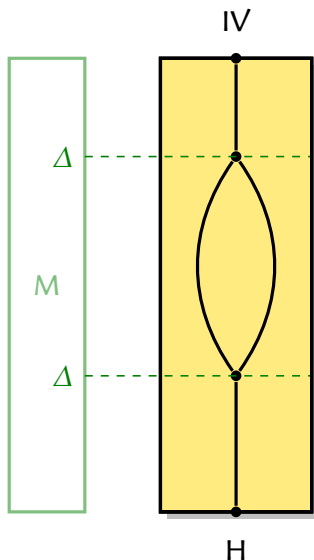
- ▶ Chosen-prefix collisions are **more dangerous** than identical-prefix collisions
 - ▶ Creation of a **rogue CA** with MD5 CPC [SSALMO, Crypto'09]
 - ▶ Abused in the wild: **Flame malware** (MD5 CPC)
- ▶ Generic attacks require $2^{n/2}$ operations in both cases
- ▶ Cryptanalytic attack harder for chosen-prefix collisions

	Identical-Prefix Collisions		Chosen-Prefix Collisions	
MD5	2^{16}	[SSALMO C'09]	$2^{39.1}$	[SSALMO C'09]
SHA-1	$2^{64.7}$	[Stevens EC'13, SBKAM C'17]	$2^{77.1}$	[Stevens EC'13]

Goal of this work

- ▶ Improve SHA-1 chosen-prefix collision attacks
- ▶ Reduce the gap between Identical-Prefix and Chosen-Prefix Collisions

Differential collision attacks



1 Differential cryptanalysis

- ▶ Find a high probability trail $0 \rightarrow 0$
- ▶ Find a conforming message

2 Linearized trails [Chabaud & Joux, C'98]

- ▶ Linear combinations of local collisions
- ▶ High probability, but non-zero input / output diff.

3 Message modification [BC04, WYY05]

- ▶ Satisfy first rounds without paying probability

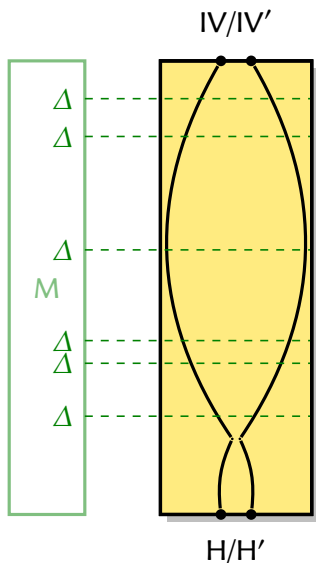
4 Non-linear trails [Wang & al., C'05]

- ▶ Modify trail in first rounds using non-linearity
- ▶ Can start from arbitrary difference
⇒ near-collision

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- ▶ Two trails with same linear core: $0 \rightarrow \delta$ and $\delta \rightarrow \delta$
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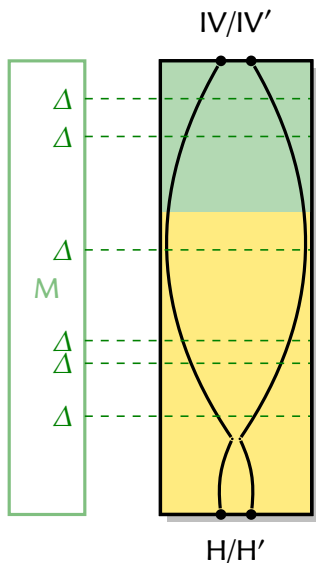
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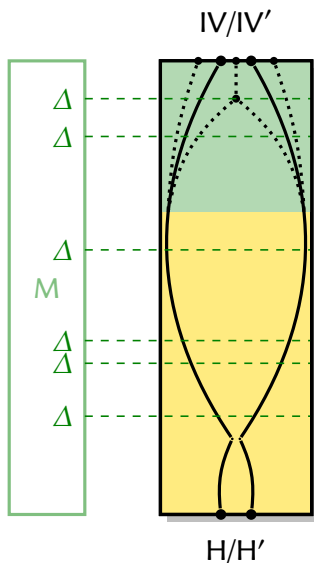
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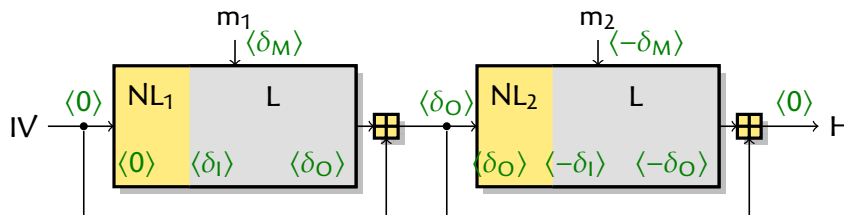
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MD5/SHA-1 collision attack

[Wang & al.]

Multi-block technique

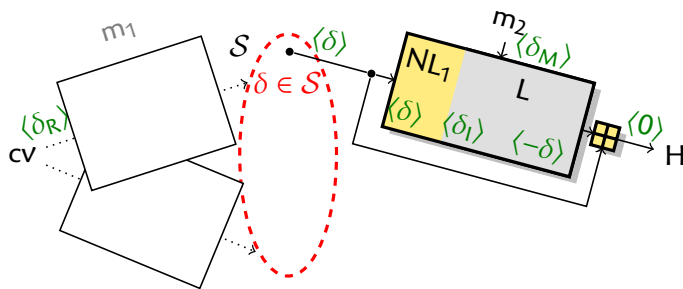
- ▶ Start from a good core linear trail $\delta_I \rightarrow \delta_O$
- ▶ Build two non-linear trails $0 \rightarrow \delta_I, \delta_O \rightarrow -\delta_I$
- ▶ Differences cancel due to feed-forward



Chosen-prefix collision attack [Stevens, Lenstra & de Weger, EC'07]

Main idea

Find a set of “nice” chaining value differences \mathcal{S}



1 Birthday phase

- Find m_1, m'_1 such that $H(P_1 \parallel m_1) - H(P_2 \parallel m'_1) \in \mathcal{S}$
- Complexity about $\sqrt{2^n/|\mathcal{S}|}$

2 Near-collision phase

- Adjust non-linear trail
- Erase the state difference, using near-collision blocks

How to build \mathcal{S} : previous works

MD5

[SLW07]

- ▶ Family of core trails, output on different bits
- ▶ Several near-collision blocks, erase differences bit by bit
- ▶ Very structured set \mathcal{S}

SHA-1

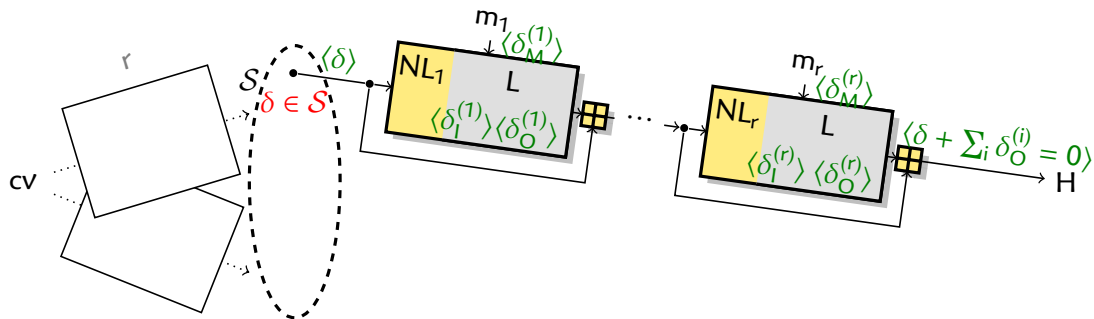
[S13]

- ▶ Single core trail, vary the last rounds
- ▶ Single near-collision block
- ▶ Small set \mathcal{S} , no structure

Our work

- ▶ The **bottleneck** of the SHA-1 attack is the birthday phase
 - ▶ Complexity around $\sqrt{2^n/|\mathcal{S}|}$
 - ▶ We need a larger set \mathcal{S}
- ▶ Can we **combine** those ideas and **improve** them?

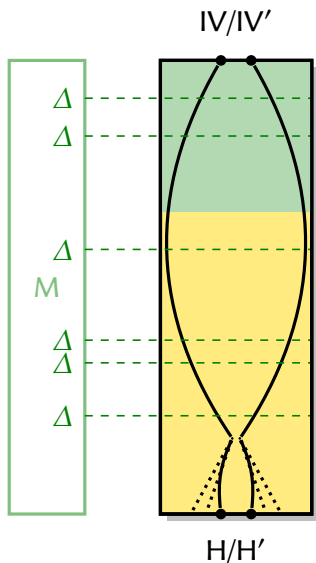
New techniques



- 1 **Larger set** of output differences for the compression function
- 2 **Multi-block** technique using a single core trail
- 3 **Dynamic selection** of near-collision targets (clustering)

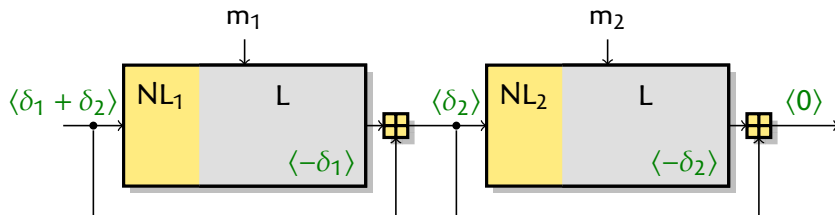
(192 \rightarrow 8768)
 $|\mathcal{S}| \approx 2^{30}$

Relaxing the final rounds



- ▶ Start from a core linear trail
- ▶ Modify last rounds to reach new difference
- ▶ Previous work: [Stevens, EC'13]
192 differences with optimal probability
- ▶ Our work:
8768 differences with non-optimal probability
- ▶ Reduce the complexity from $2^{77.1}$ to $2^{74.3}$

Multi-block technique with unstructured set



- ▶ Assume we reach a set of output differences \mathcal{D} with one block
- ▶ With two blocks, we can reach a set of output differences:
 $\mathcal{S} := \{\delta_1 + \delta_2 \mid \delta_1, \delta_2 \in \mathcal{D}\}$
- ▶ With n blocks:
 $\mathcal{S} := \{\delta_1 + \delta_2 + \dots + \delta_n \mid \delta_1, \delta_2, \dots, \delta_n \in \mathcal{D}\}$
- ▶ Reduce the complexity from $2^{74.3}$ to $2^{68.6}$

Clustering

Observation

A value in \mathcal{S} can be reached in many different ways

$$\delta_1 + \delta_2 + \delta_3 = \delta_1 + \delta_3 + \delta_2 = \delta_2 + \delta_1 + \delta_3 = \dots$$

▶ Near-collision block search:

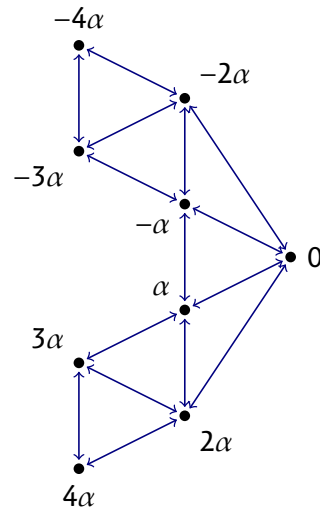
- 1 Choice of δ gives message conditions
- 2 Search for message reaching δ

▶ Target δ values with same conditions **simultaneously!**

- ▶ Eg. half work with two δ with similar cost

▶ With weights: $w_N = \min \left\{ \left(1 + \sum (w_j / c_j^\beta) \right) / \sum (1 / c_j^\beta) \right\}$

▶ Reduce the complexity from $2^{68.6}$ to $2^{66.9}$



Graph \mathcal{G} : transitions in \mathcal{S}
Ex: $\mathcal{D} := \{-2\alpha, -\alpha, \alpha, 2\alpha\}$

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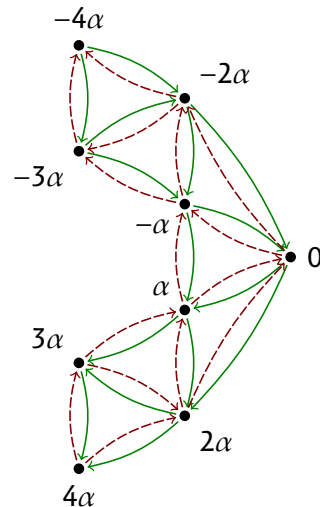
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Clustering

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A value in S can be reached in many different ways

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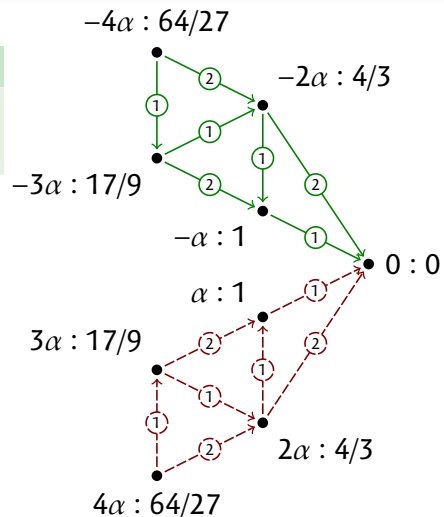
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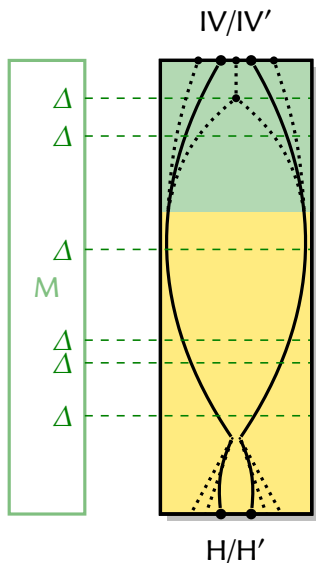
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Application to SHA-1: low-level details



- ▶ Start from the SHattered collision attack
 - ▶ Proven to work
 - ▶ Complexity $2^{64.7}$ on GPU
- ▶ Relax the last rounds
 - ▶ 8768 possible output differences
- ▶ Assume that we can build trails in the first rounds
 - ▶ More constrained than IPC attack
 - ▶ C_{block} between $2^{64.7}$ (optimistic) and $2^{67.7}$ (conservative), depending on degrees of freedom
- ▶ Build set \mathcal{S} and graph \mathcal{G}
 - ▶ Large **computational effort**
 - ▶ $|\mathcal{S}| = 2^{33.7}$, iterations for clustering

Attack parameters

Set \mathcal{S}		Birthday parameters					Attack cost
Max cost	Size	Mask	Proba	# coll.	Ch. len.	# chain	
$2.0 \cdot C_{\text{block}}$	$2^{24.66}$	106 bits	0.71	$2^{30.83}$	2^{34}	$2^{34.74}$	$2^{68.74} + 2^{65.83} + 2.0 \cdot C_{\text{block}}$
$2.5 \cdot C_{\text{block}}$	$2^{28.59}$	102 bits	0.65	$2^{31.03}$	2^{32}	$2^{34.84}$	$2^{66.84} + 2^{64.03} + 2.5 \cdot C_{\text{block}}$
$3.0 \cdot C_{\text{block}}$	$2^{30.95}$	98 bits	0.76	$2^{32.44}$	2^{31}	$2^{34.55}$	$2^{65.55} + 2^{64.44} + 3.0 \cdot C_{\text{block}}$
$3.5 \cdot C_{\text{block}}$	$2^{32.70}$	98 bits	0.76	$2^{30.70}$	2^{30}	$2^{34.68}$	$2^{64.68} + 2^{61.70} + 3.5 \cdot C_{\text{block}}$
$4.0 \cdot C_{\text{block}}$	$2^{33.48}$	98 bits	0.74	$2^{29.95}$	2^{30}	$2^{34.30}$	$2^{64.30} + 2^{60.95} + 4.0 \cdot C_{\text{block}}$
$4.5 \cdot C_{\text{block}}$	$2^{33.66}$	98 bits	0.74	$2^{29.77}$	2^{30}	$2^{34.21}$	$2^{64.21} + 2^{60.77} + 4.5 \cdot C_{\text{block}}$

Optimal parameters

- ▶ Optimistic estimate: $2^{66.9}$ ($C_{\text{block}} = 2^{64.7}$, max cost of $3.5 \cdot C_{\text{block}}$)
- ▶ Conservative estimate: $2^{69.4}$ ($C_{\text{block}} = 2^{67.7}$, max cost of $2.5 \cdot C_{\text{block}}$)

Results

► Generic framework to turn collision attacks into chosen-prefix collision attacks

Function	Collision type	Complexity (GPU)	Ref.
SHA-1	collision	2^{69}	[Wang & al., C'05]
		$2^{64.7}$	[Stevens, EC'13], [Stevens & al., C'17]*
	chosen-prefix collision	$2^{77.1}$	[Stevens, EC'13]
		$2^{66.9} - 2^{69.4}$	New
MD5	collision	2^{40}	[Wang & al., EC'05]
		2^{16}	[Stevens & al., C'09]
	chosen-prefix collision (9 blocks)	$2^{39.1}$	[Stevens & al., C'09]
		(3 blocks) 2^{49}	[Stevens & al., C'09]
		(1 block) $2^{53.2}$	[Stevens & al., C'09]
		(2 blocks) $2^{46.3}$	New

- **Small gap** between SHA-1 Identical-Prefix and Chosen-Prefix collisions ($\times 4.6 - \times 26$)
- Improvement for MD5 CPC limited to two blocks

*The attack has a complexity of 2^{61} on CPU, and $2^{64.7}$ on GPU

Attack cost and future work

- ▶ We are now looking more closely at the low-level details
 - ▶ We believe we can keep two boomerangs
 - ▶ This gives $C_{\text{block}} = 2^{65.1}$, and the total cost is around $2^{67.2}$
- ▶ **Cost estimation** by renting GPUs:
 - ▶ About **2.6M\$** on Amazon's AWS (using spot p3.16xlarge instances @7.5\$/hr)
 - ▶ Around **540 000\$** renting GPU (former mining farms?)
 - ▶ Affordable for state-level adversaries
- ▶ Security advice: retire SHA-1 **NOW!**

On-going work

- ▶ **New ideas** for small improvements of various parts of attacks
- ▶ Get the cost below **100 000\$**
- ▶ We hope to build a **practical** chosen-prefix collision in 2019...

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