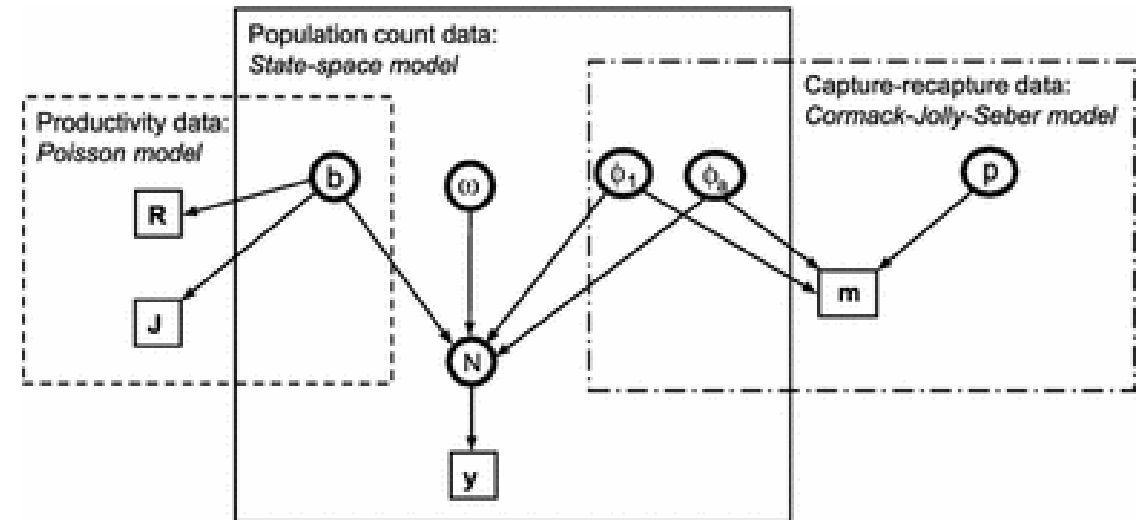
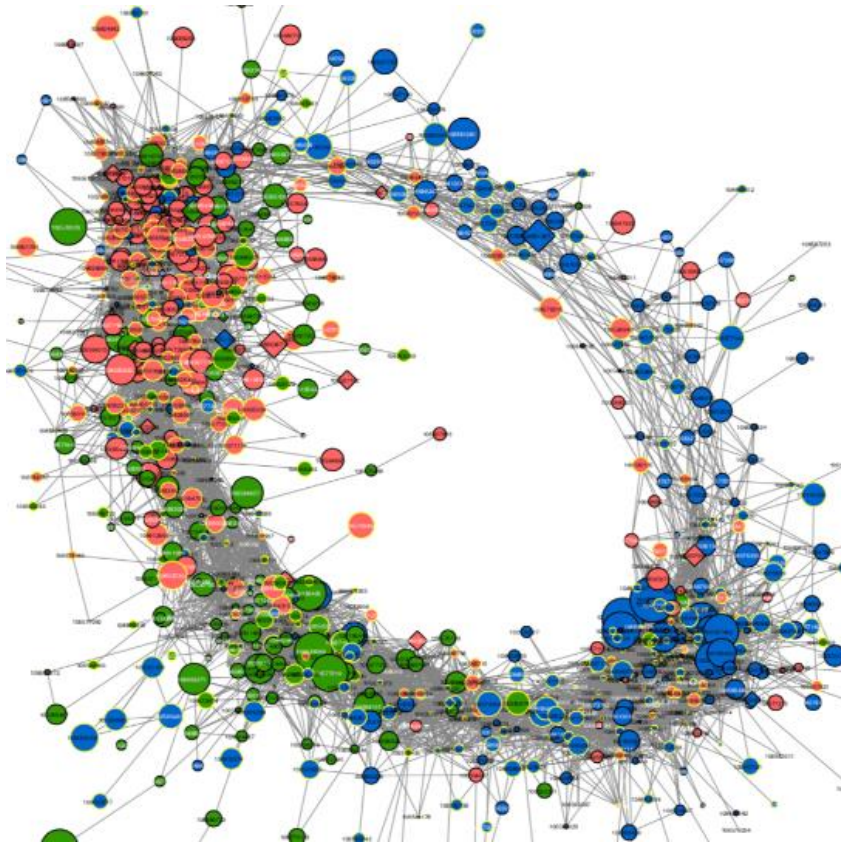


Cross-lags or dynamic SEMs, Bayesian inference & conclusions

TV Riecke



Cross-lags or dynamic SEMs

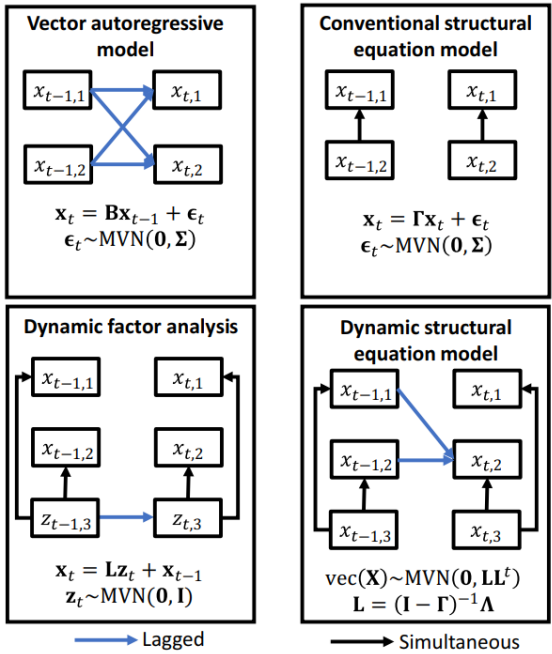
Received: 31 July 2023 | Accepted: 3 January 2024
DOI: 10.1111/2041-210X.14289

RESEARCH ARTICLE

Methods in Ecology and Evolution

Dynamic structural equation models synthesize ecosystem dynamics constrained by ecological mechanisms

James T. Thorson¹ | Alexander G. Andrews III² | Timothy E. Essington³ | Scott I. Large⁴



Thorson et al. (2024) *MEE*

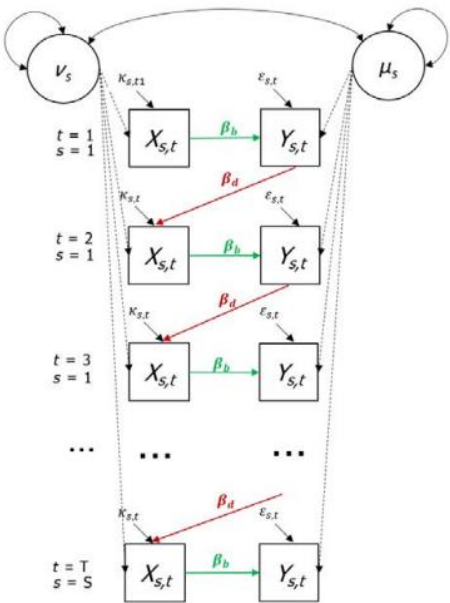
Received: 6 October 2020 | Accepted: 21 July 2021
DOI: 10.1111/1365-2656.13572

RESEARCH METHODS GUIDE

Journal of Animal Ecology

Cross-lags and the unbiased estimation of life-history and demographic parameters

Martijn van de Pol¹ | Lyanne Brouwer^{2,3}

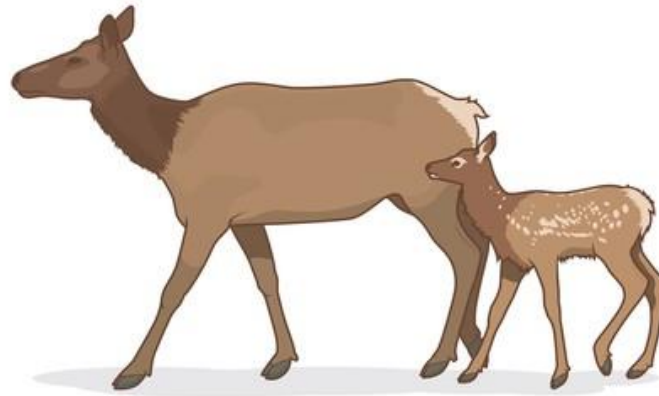
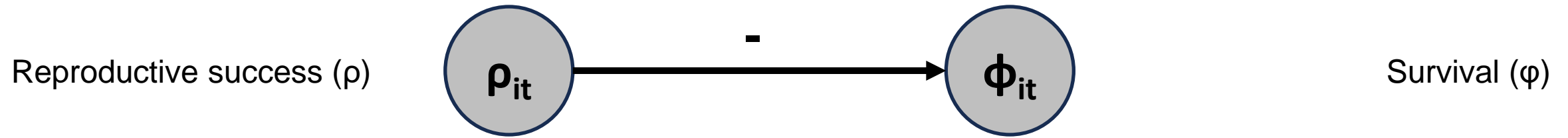


Van de Pol & Brouwer (2021) *JAnE*

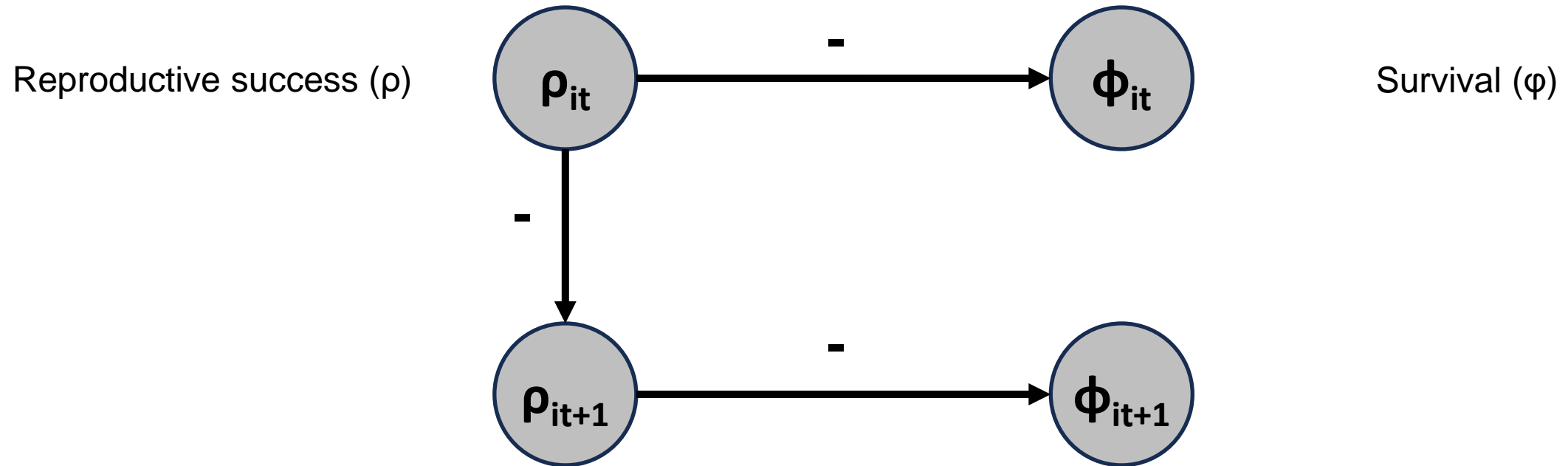
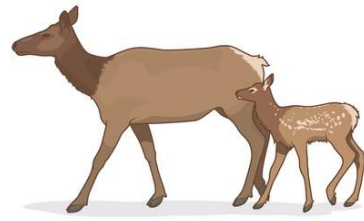
Two examples

1. Life-history trade-offs
 - Based on an *in revision* manuscript
2. Density-dependence and environmental heterogeneity
 - Based on our work with ducks

Life-history trade-off example

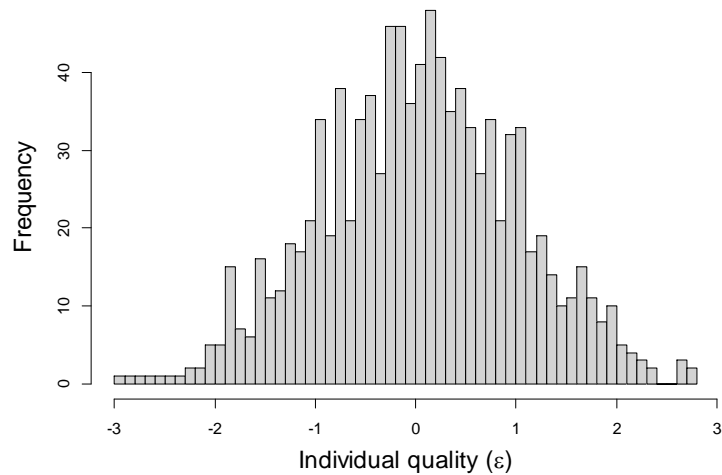
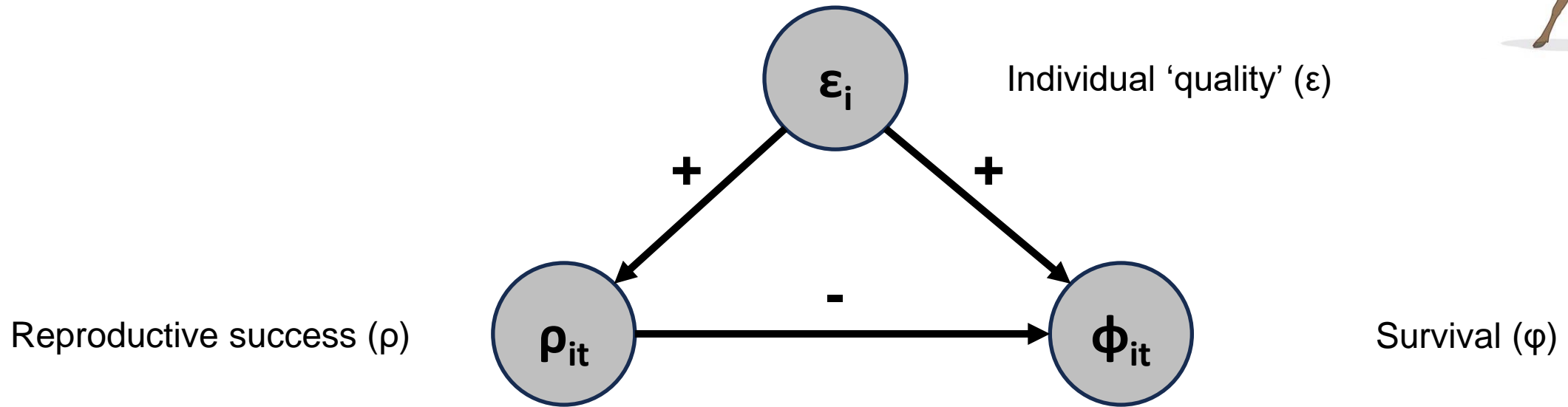
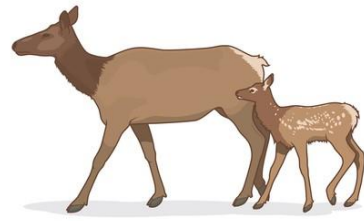


Life-history trade-off example

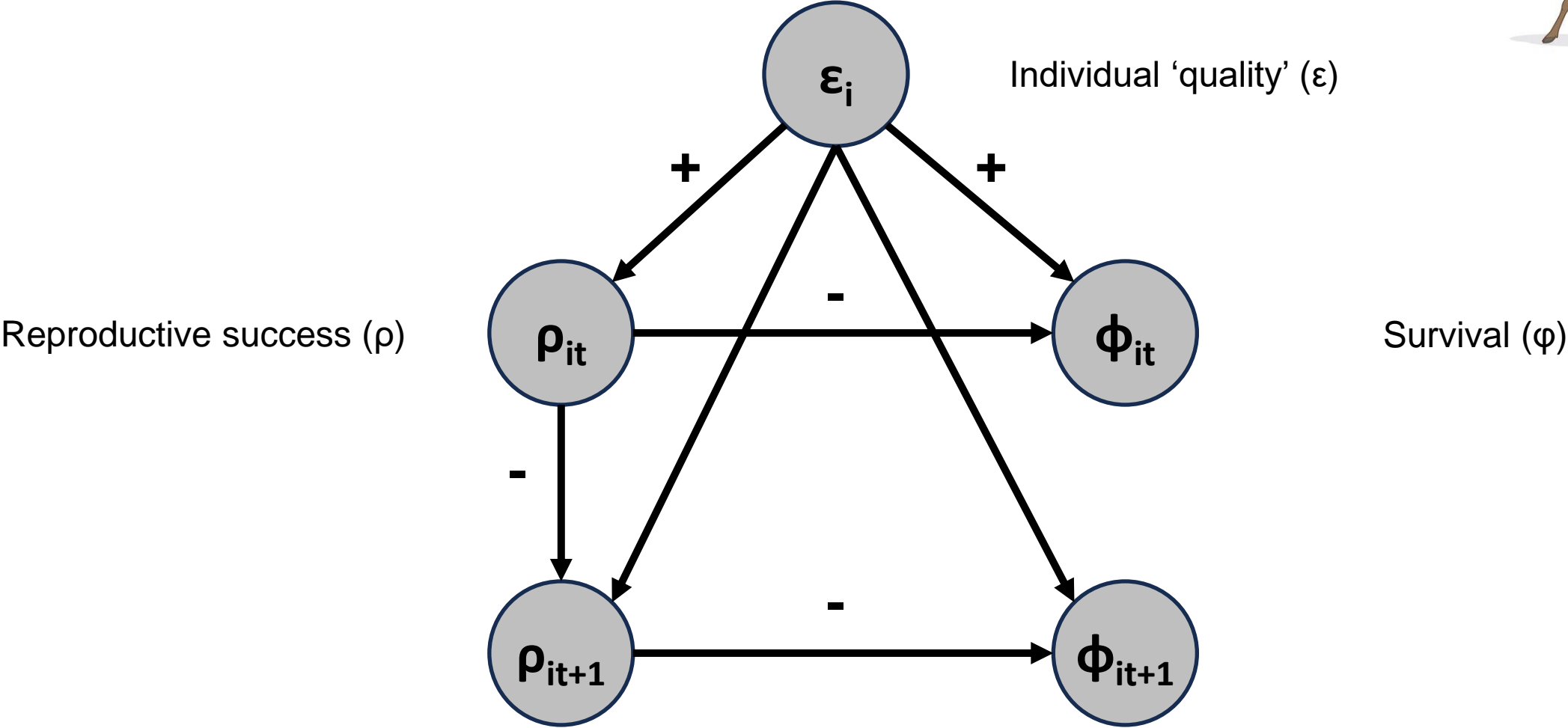
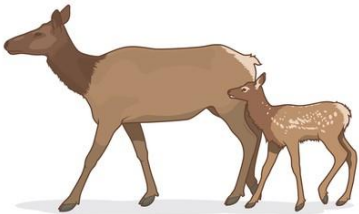


Negative effect of increased reproductive investment in $t+1$

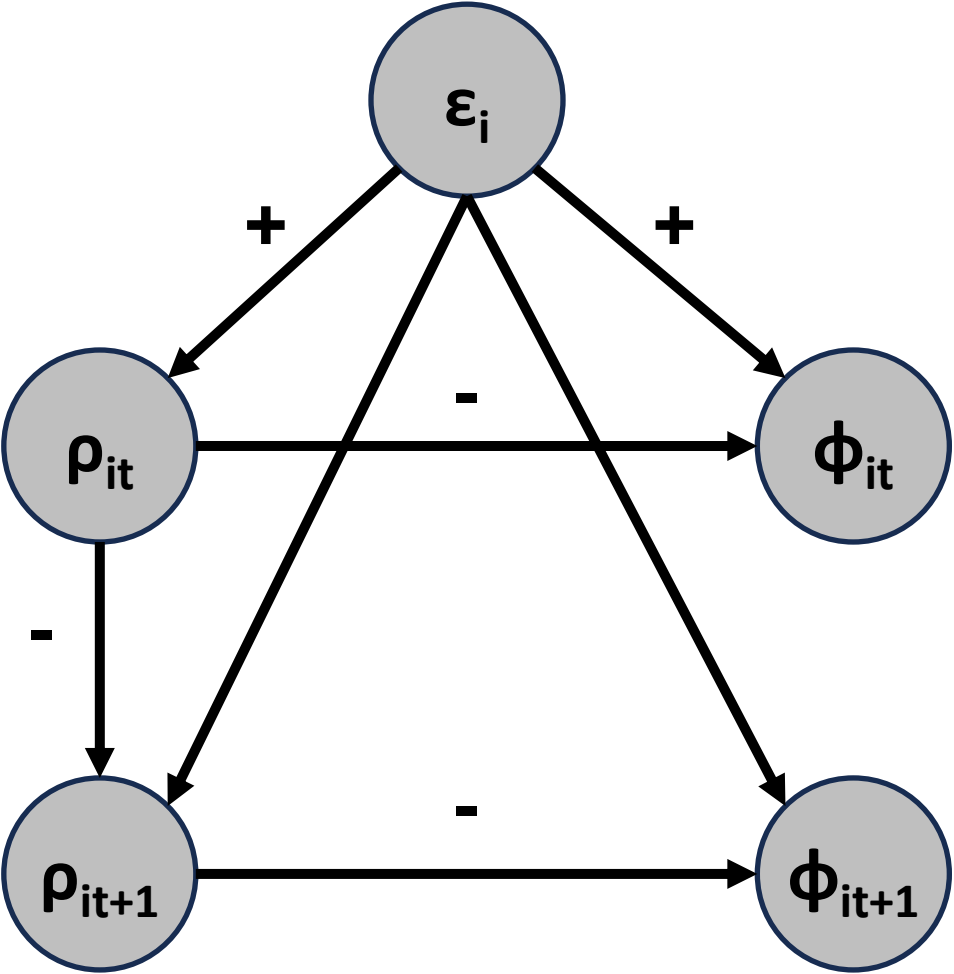
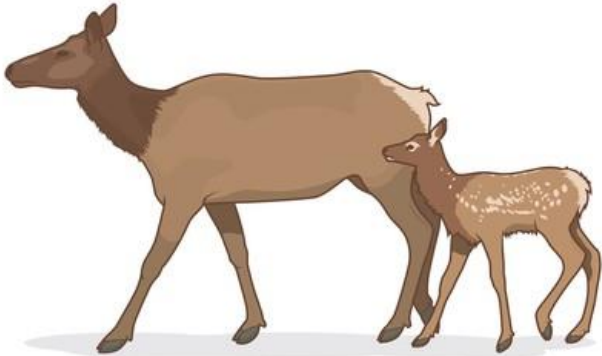
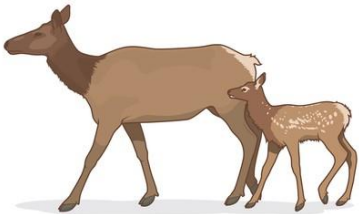
There's a twist... individuals are... different!



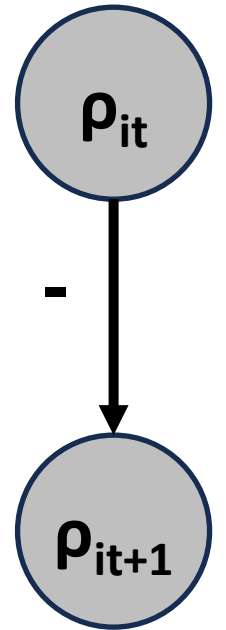
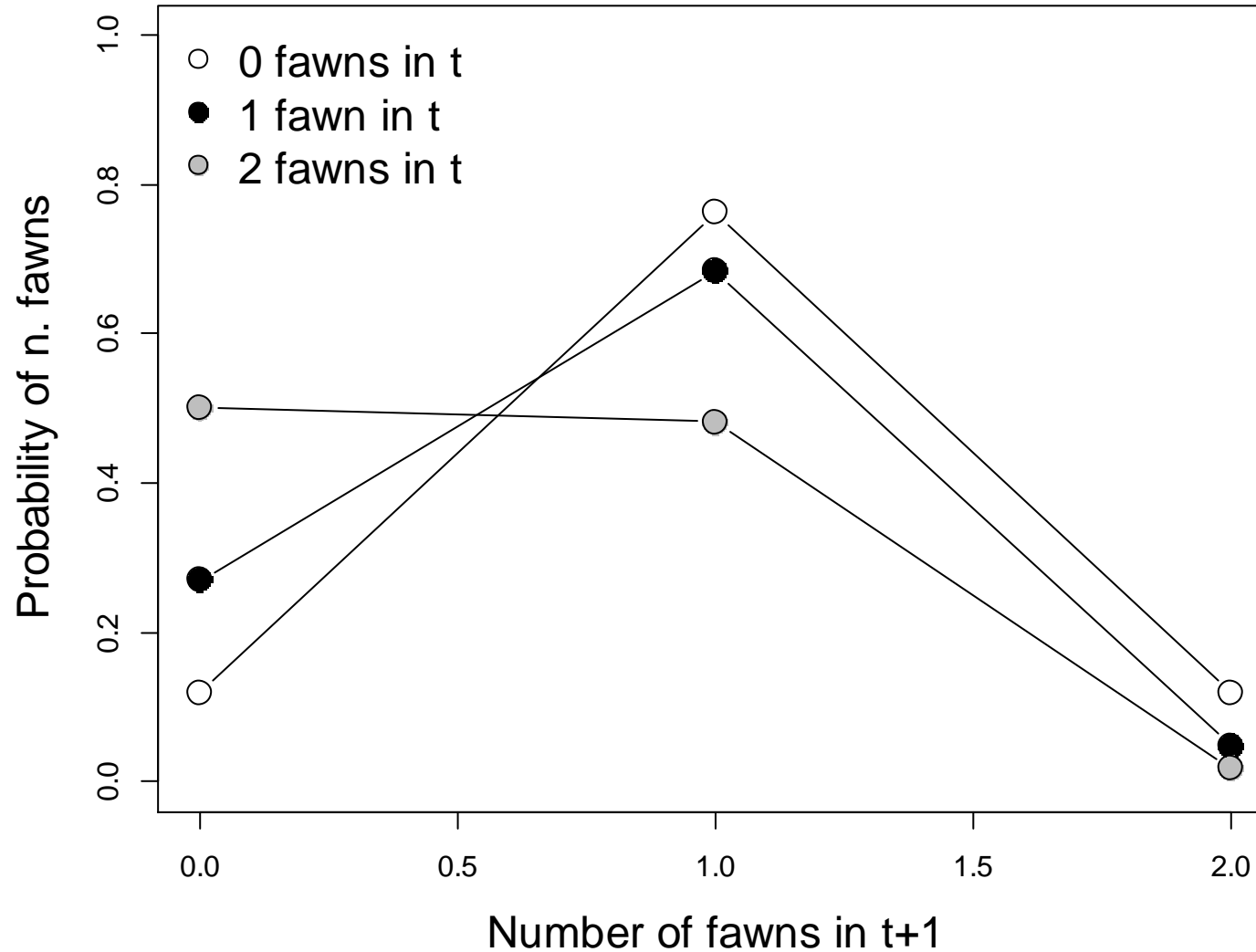
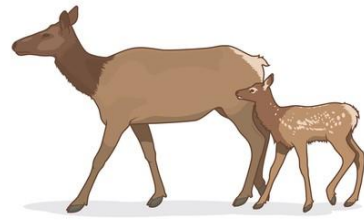
The full model



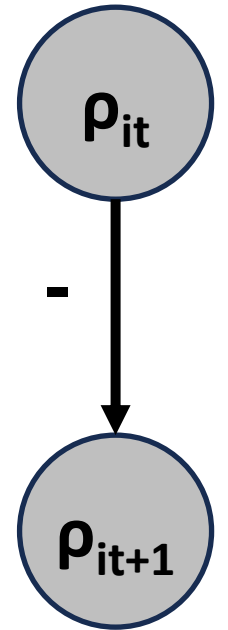
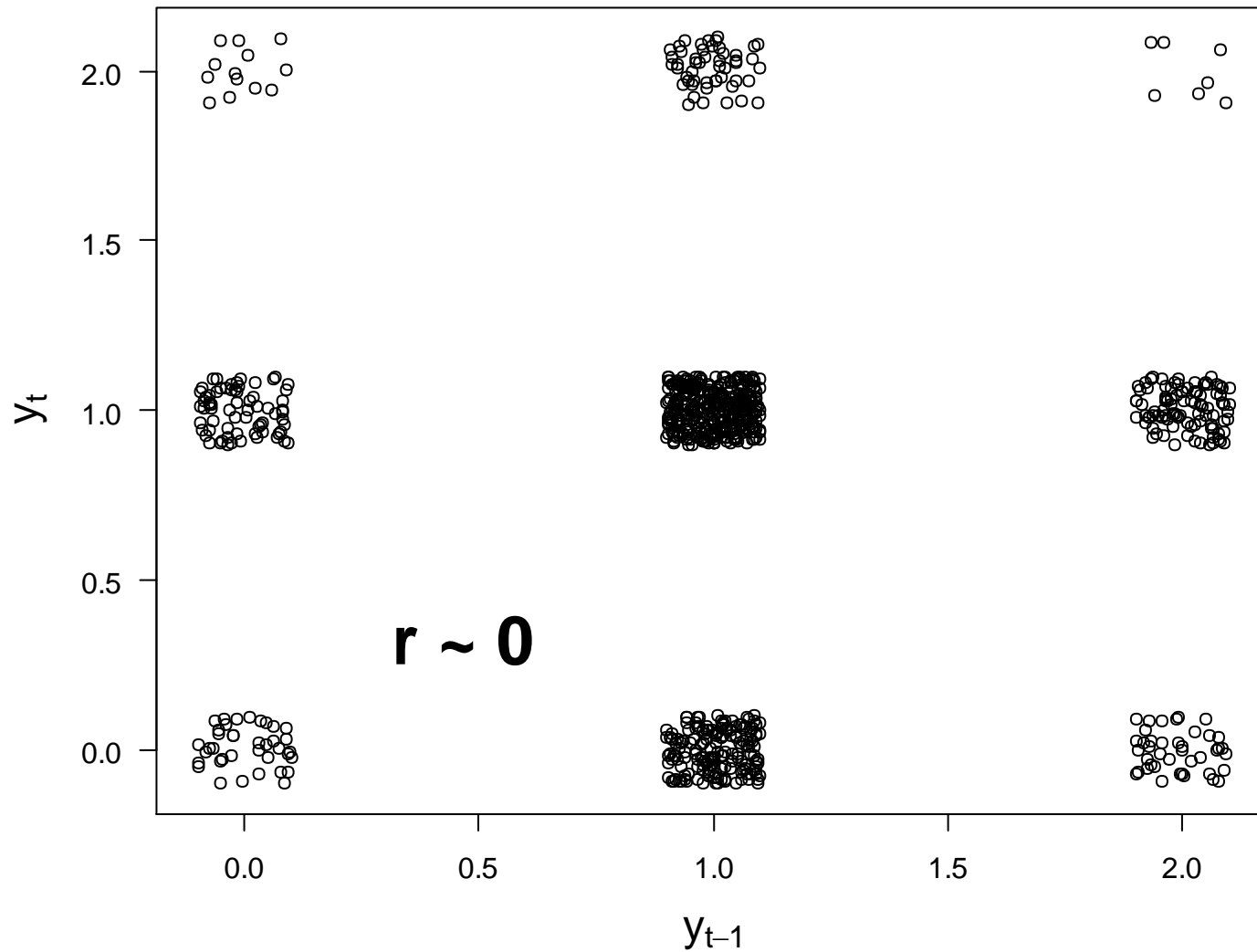
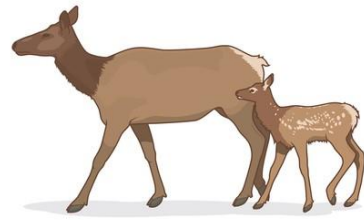
The full model



What is our true carry-over effect of reproduction?

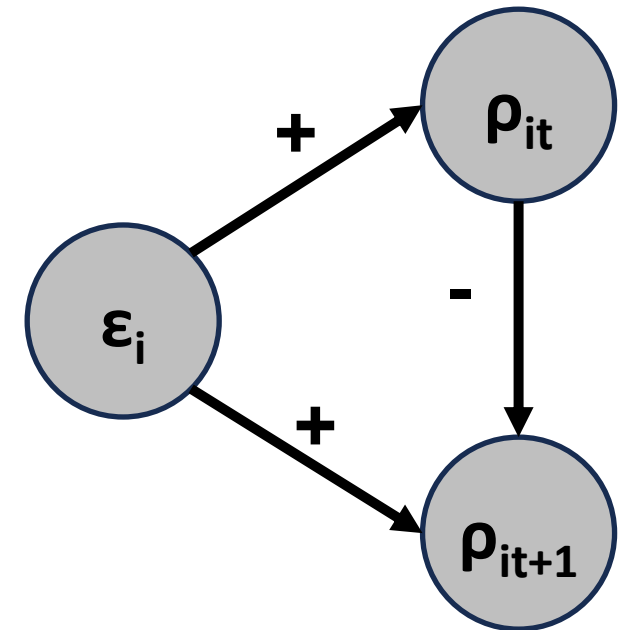
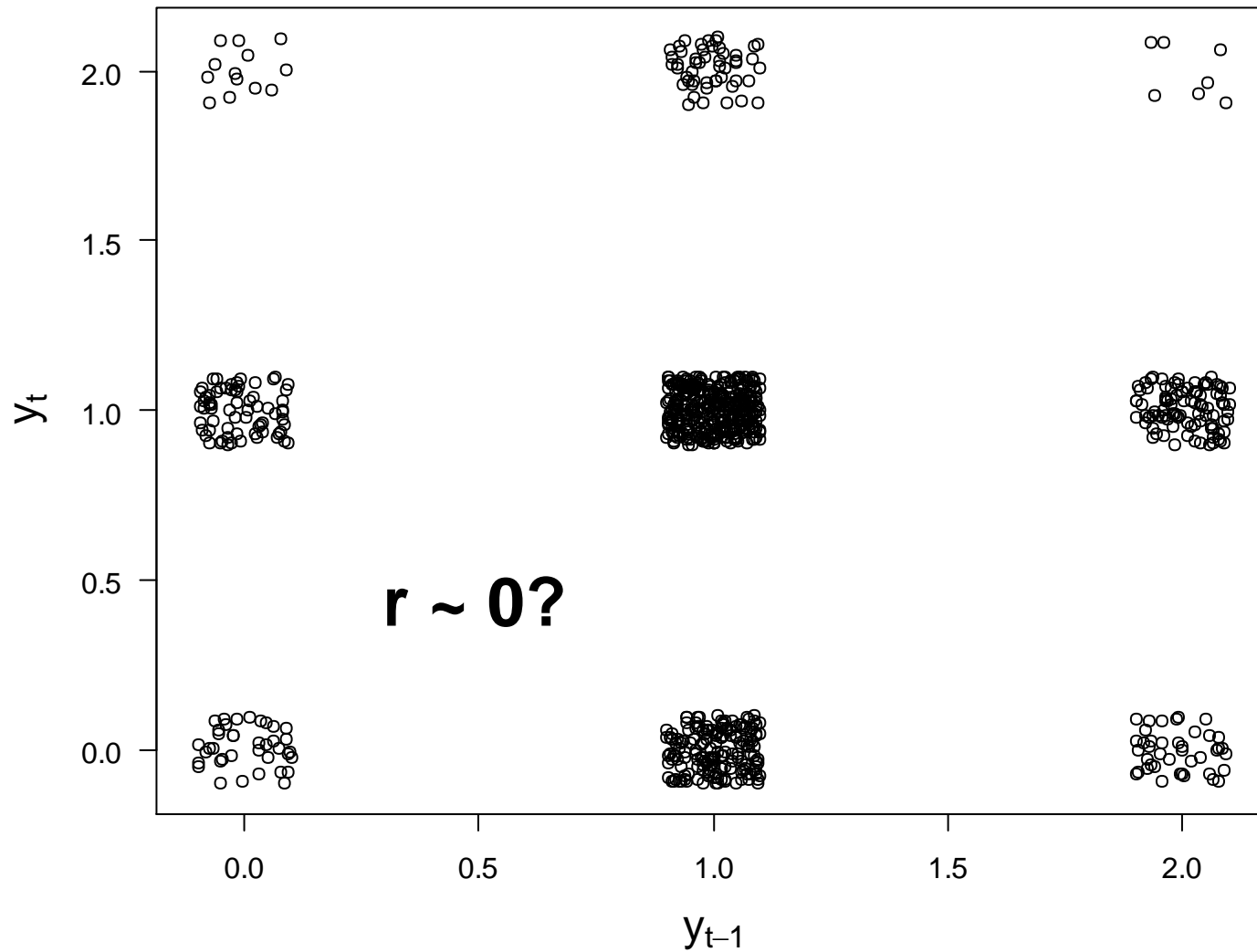
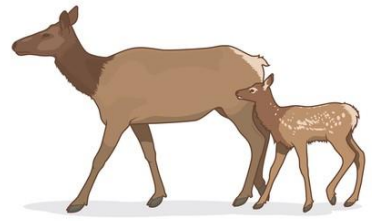


What is our observed carry-over effect of reproduction?



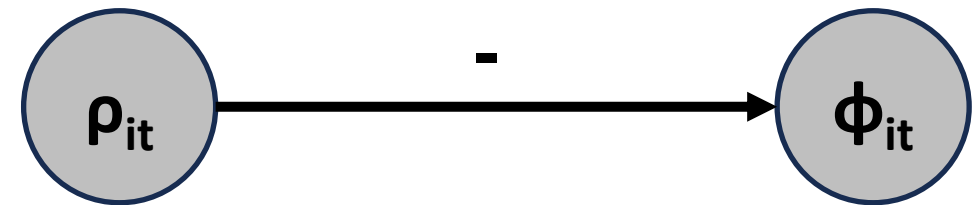
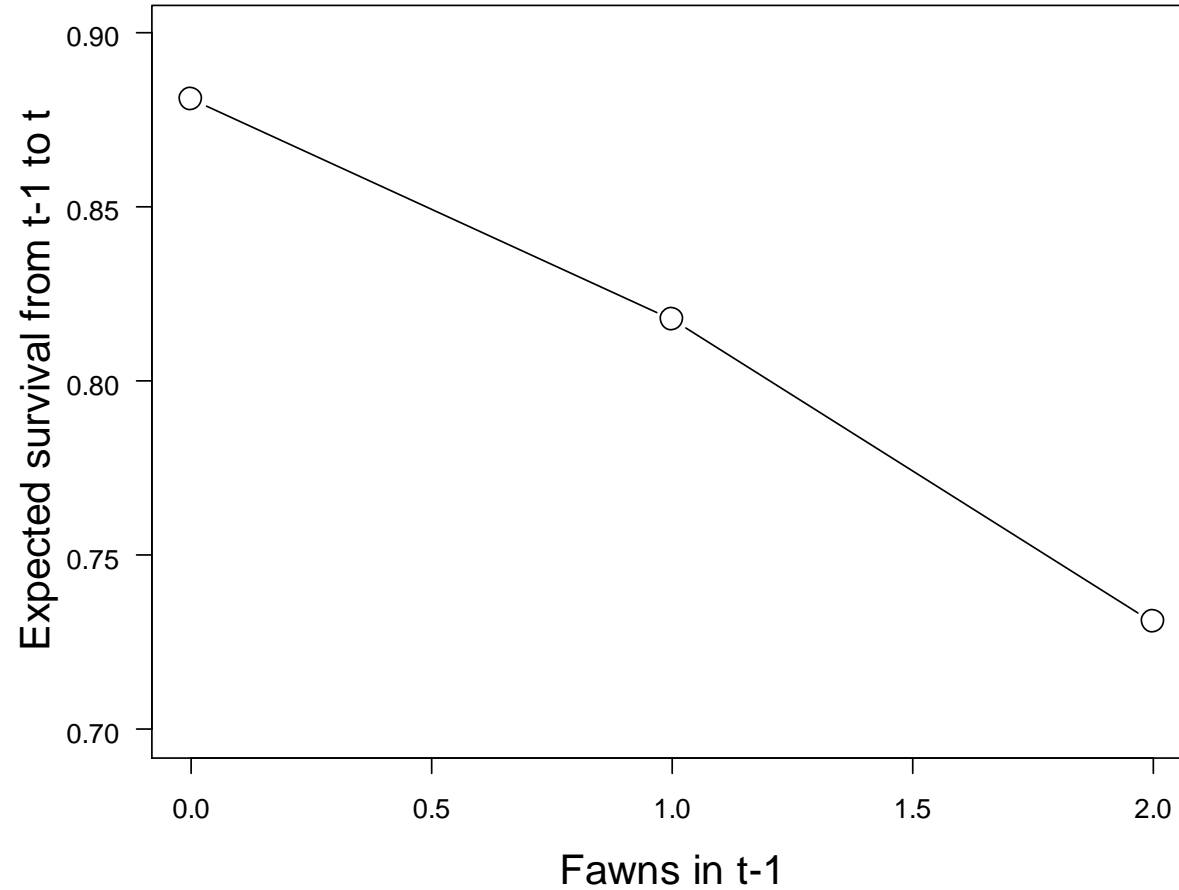
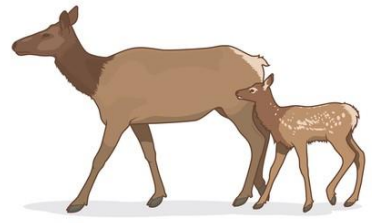
What's happening?

High-quality females have more offspring, more often

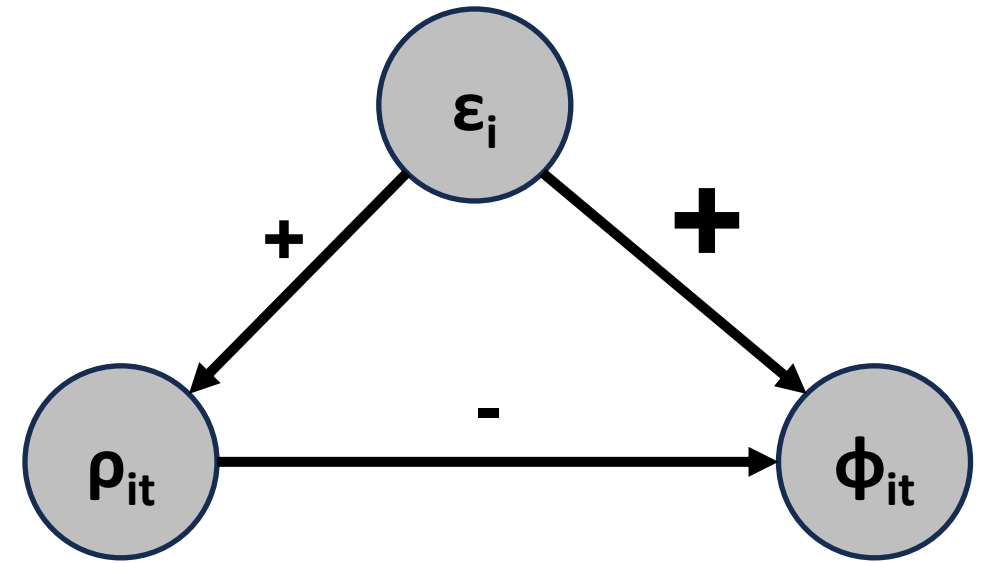
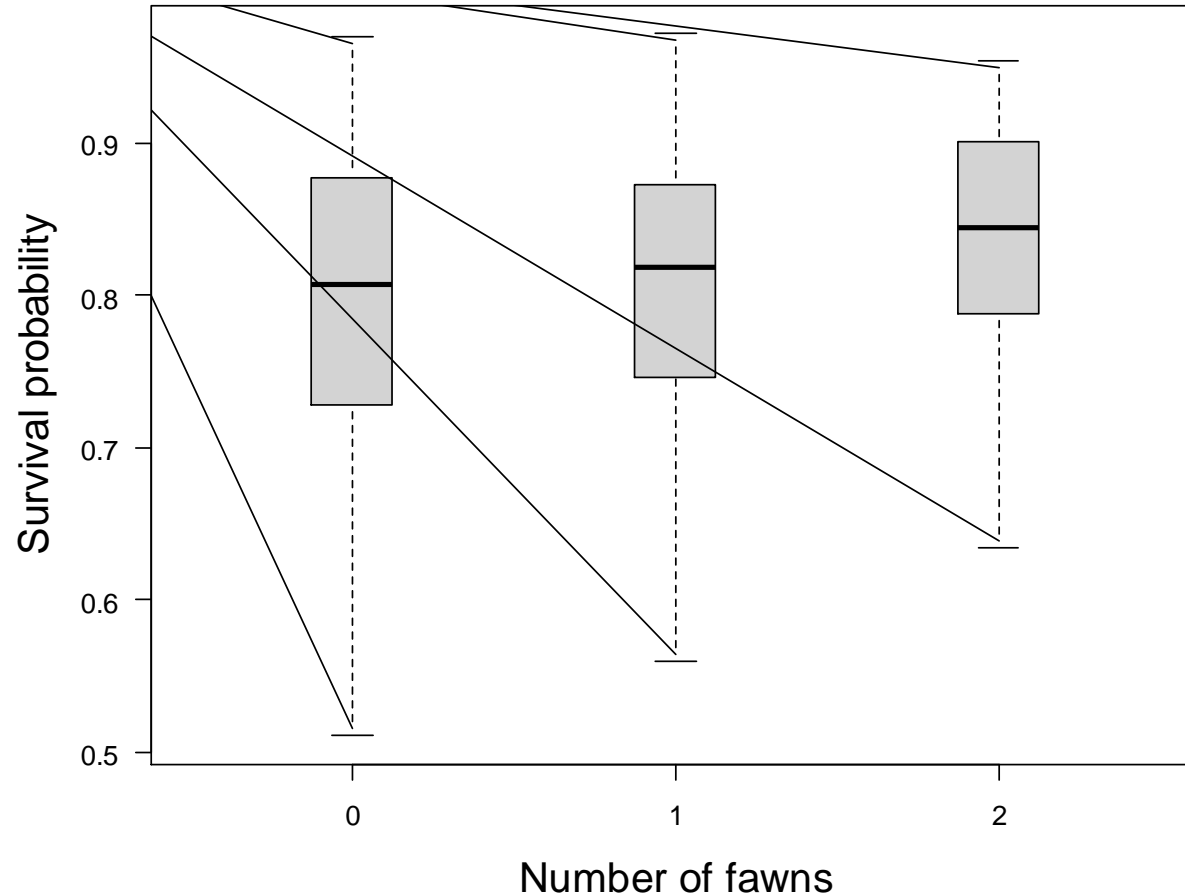
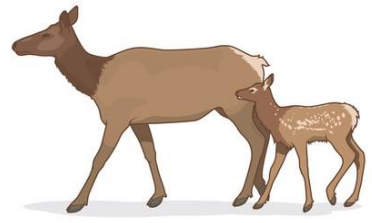


This 'disguises' trade-offs

What is our true effect of reproduction on survival?

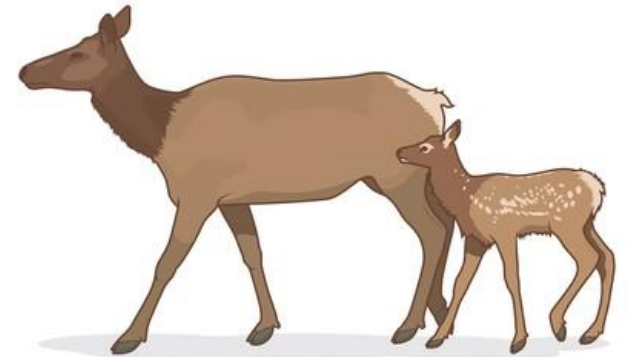
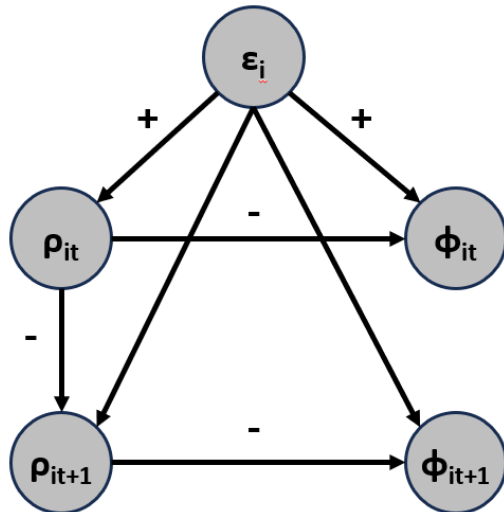


What is our observed effect of reproduction on survival?

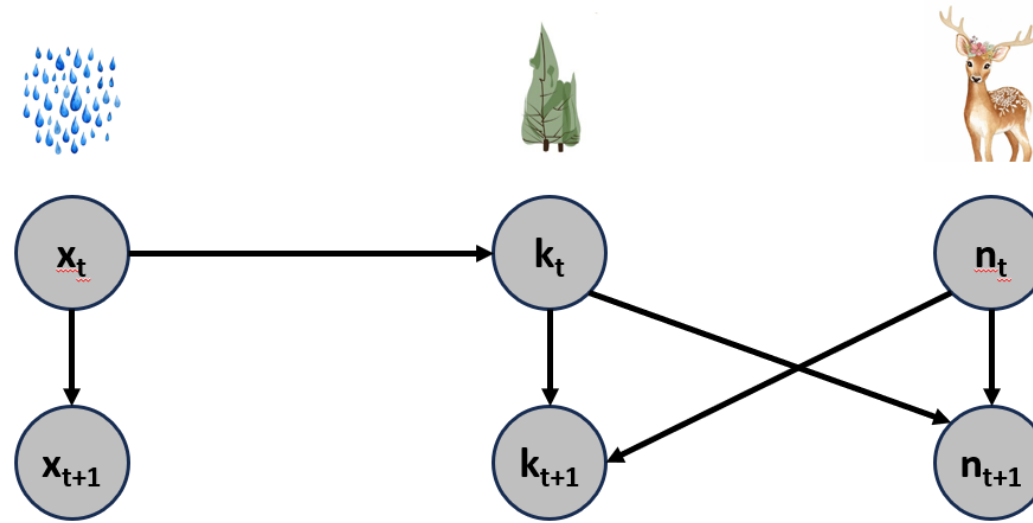


Hi-quality females have more fawns
They also survive at higher rates

Failing to account for cross-lags or dynamic processes increases error (i.e., false negatives and false positives)

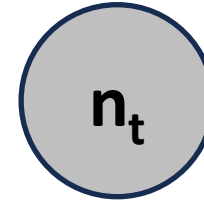
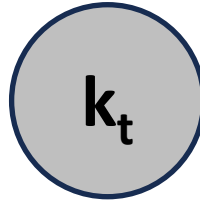
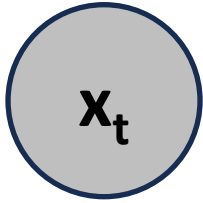


Density-dependence example

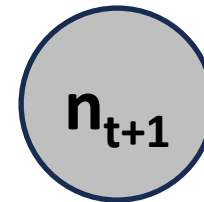
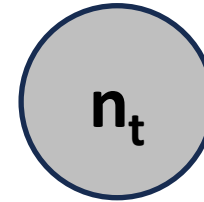
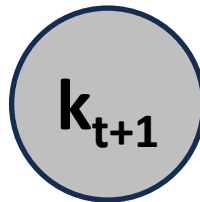
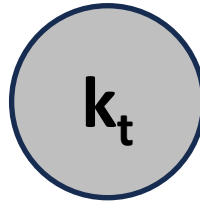
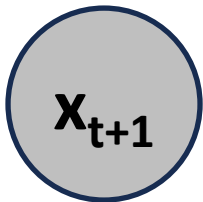
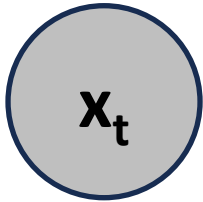


Leopold (1933); Ricker (1954)

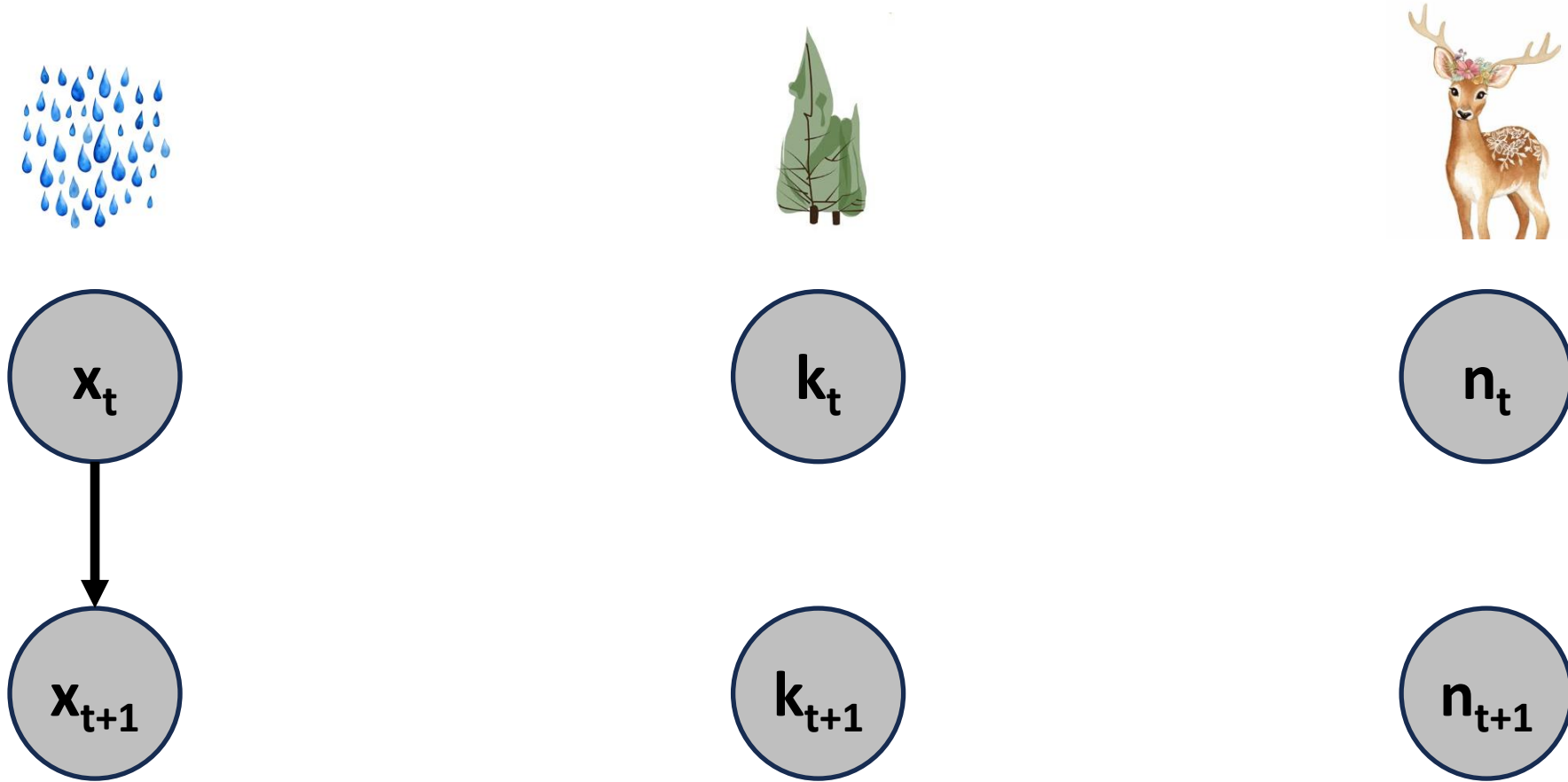
Environmental variation (x), vegetation (k), and an herbivore (n)



Environmental variation (x), vegetation (k), and an herbivore (n)

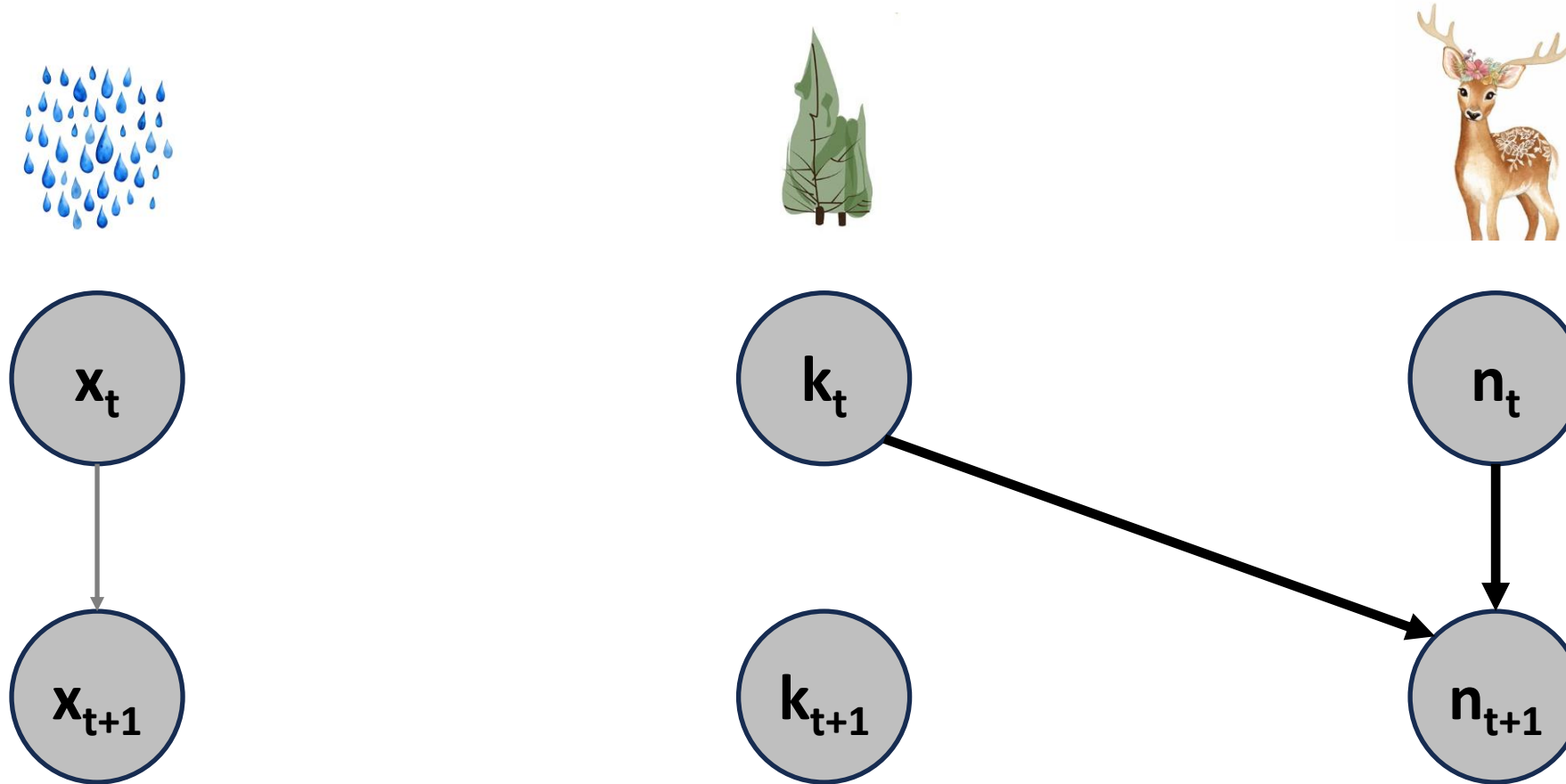


Environmental variation (x) is auto-regressive (AR1)



$$x_{t+1} \sim \text{normal}(\rho \times x_t, \sigma^2)$$

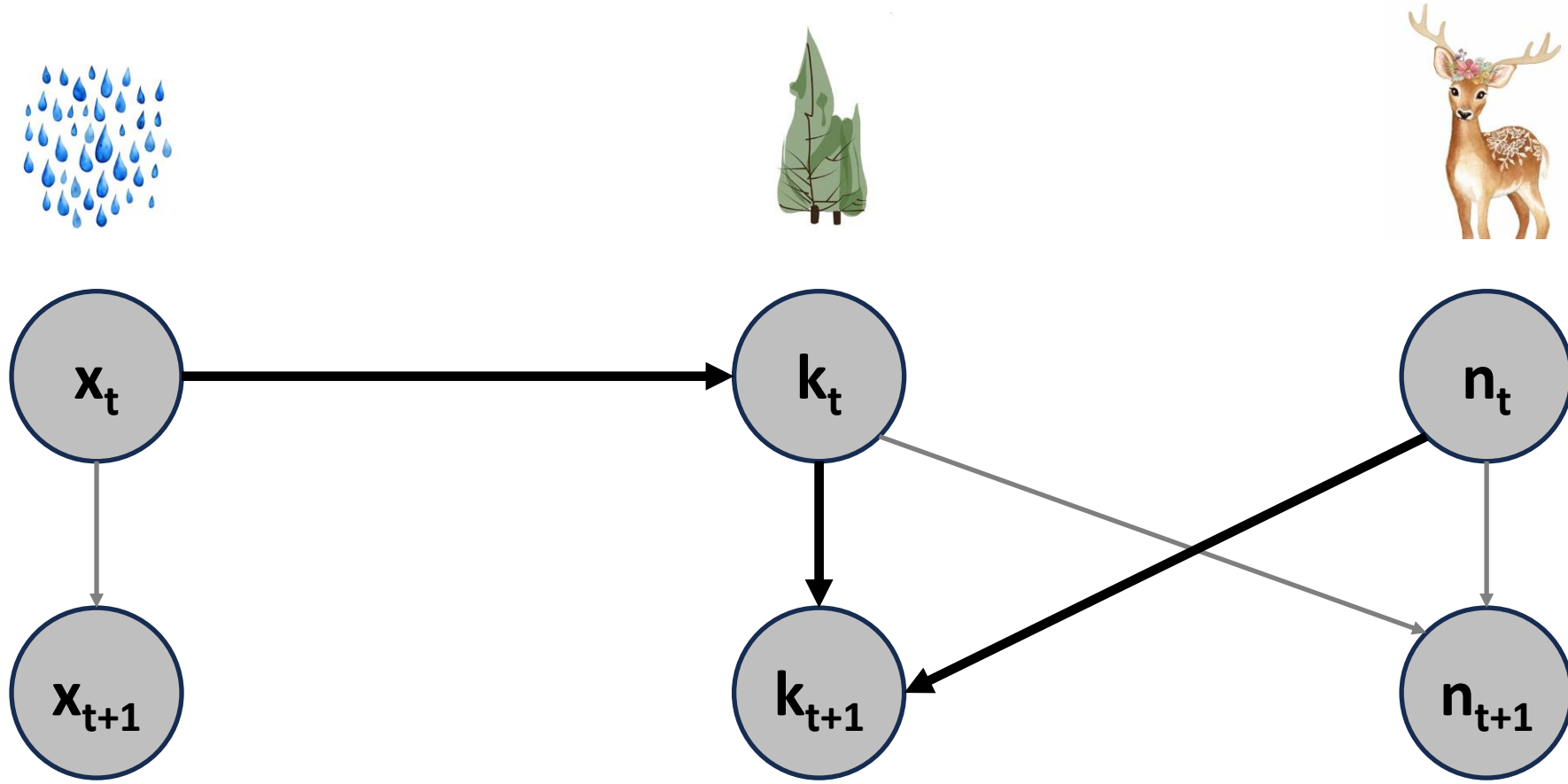
Herbivore (n) population growth is density-dependent



$$n_{t+1} \sim \text{Poisson} \left(n_t \times e^{r \left(1 - \frac{n_t}{k_t} \right)} \right)$$

Ricker (1954)

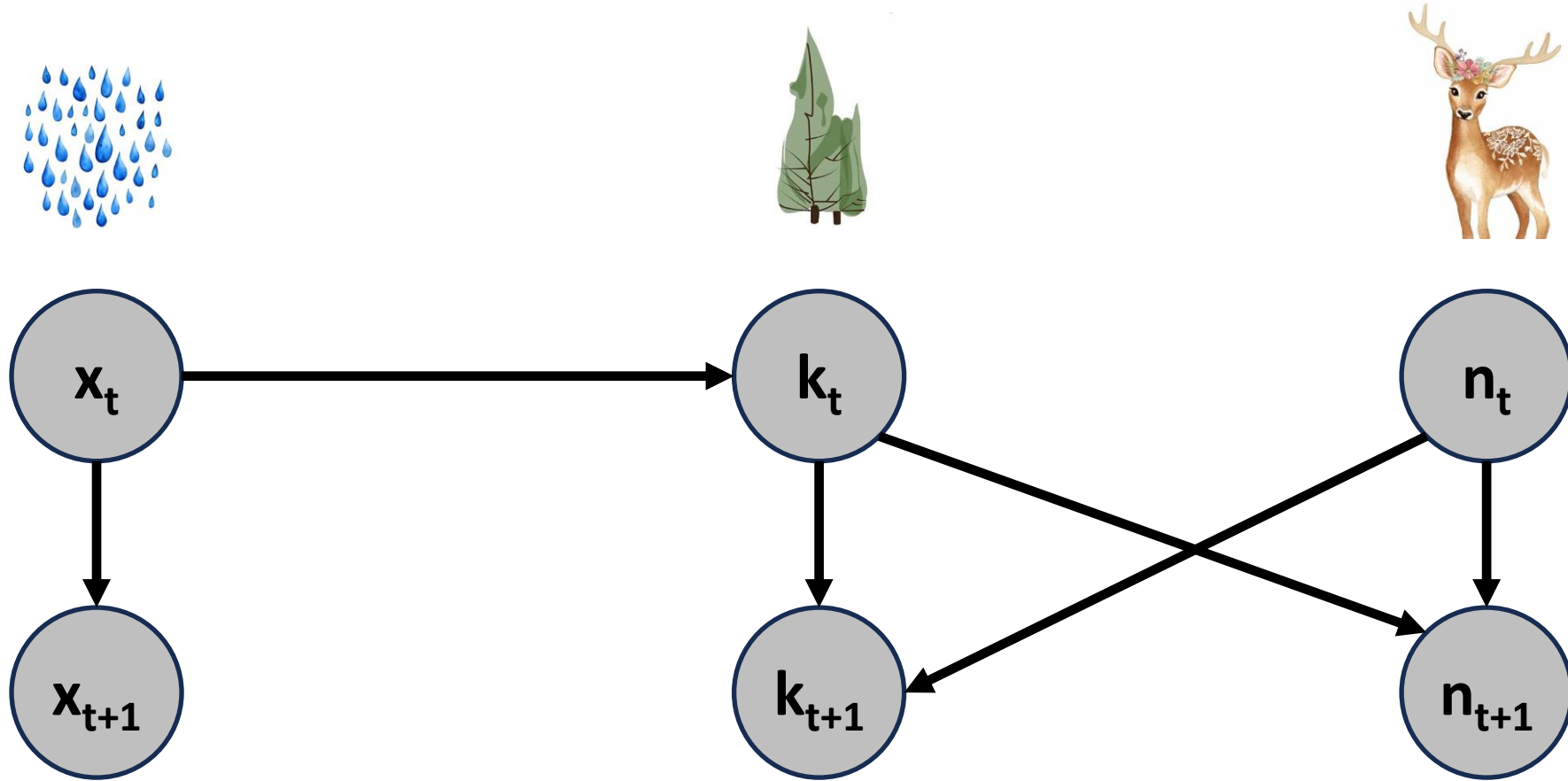
Carrying capacity changes due to x and ungulate density (n/k)



$$k_{t+1} \sim \text{Poisson} \left(k_t \times e^{\delta_1 \left(1 - \frac{n_t}{k_t} \right) + \delta_2 x_t} \right)$$

Leopold (1933)

This is complicated, but not really (?)

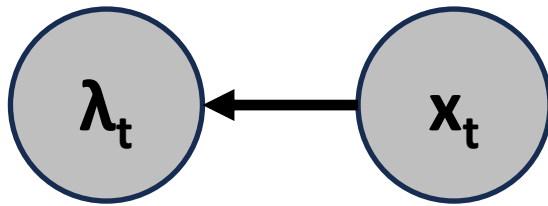


Leopold (1933); Ricker (1954)

Let's simulate some data and run a naïve model

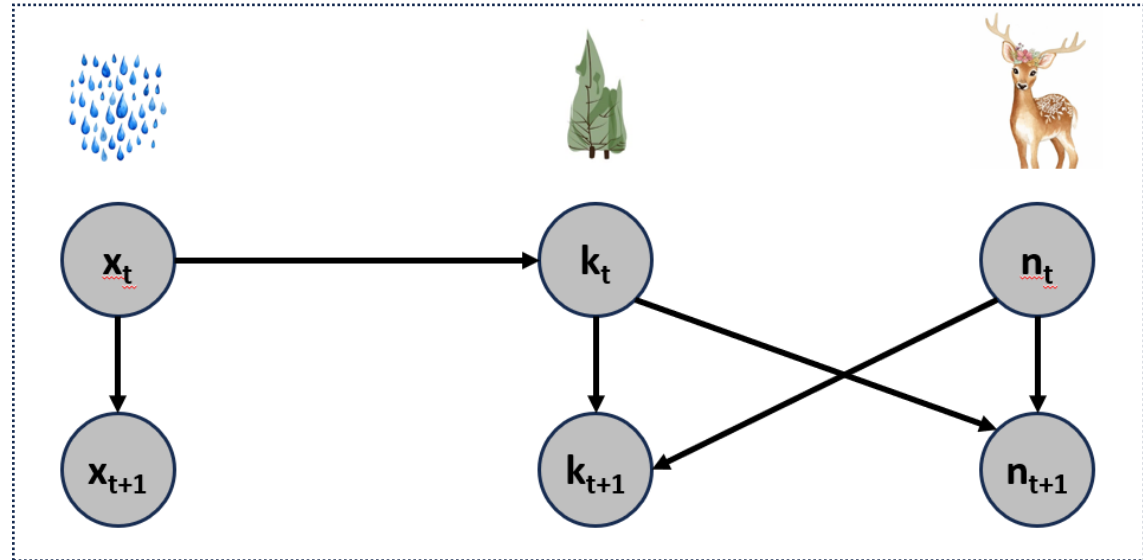
Analysis

$$\lambda_t = \frac{n_{t+1}}{n_t}$$



$$\lambda_t \sim \text{normal}(\beta x_t, \sigma^2)$$

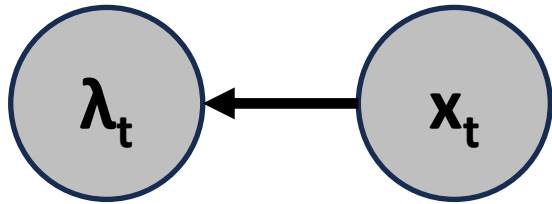
Simulation



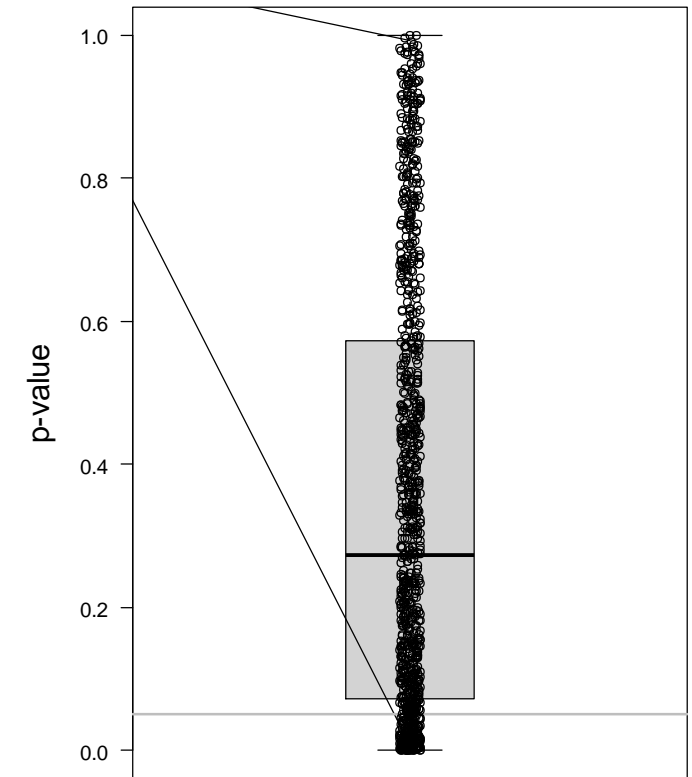
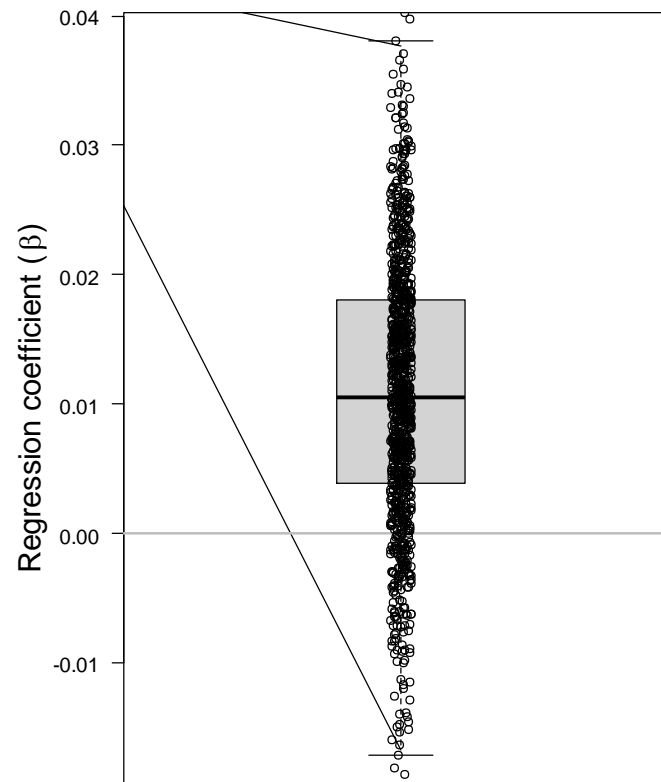
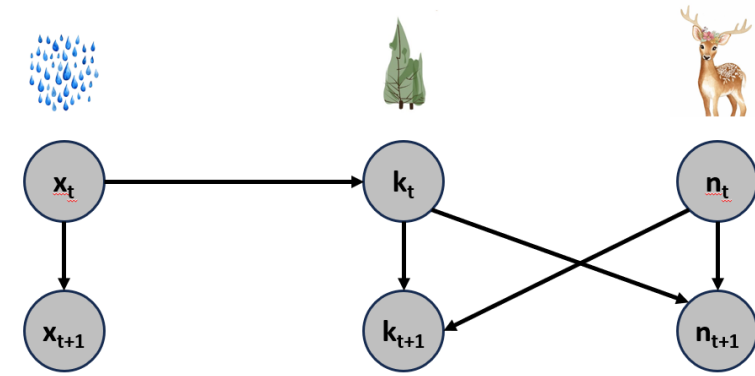
What does $\lambda_t \sim x_t$ look like across 1k simulations?

Results are not encouraging

$$\lambda_t = \frac{n_{t+1}}{n_t}$$



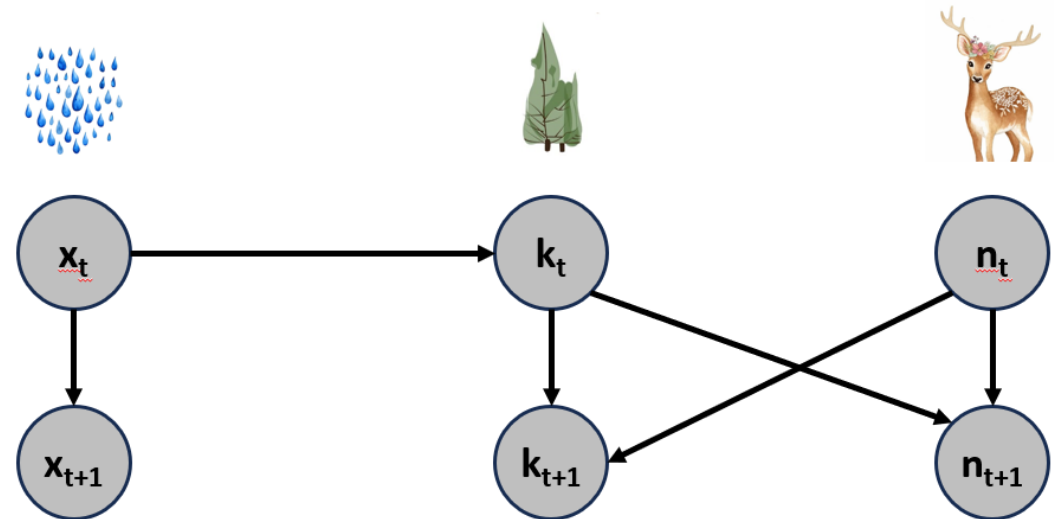
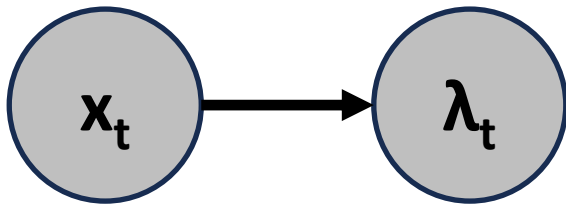
$$\lambda_t \sim \text{normal}(\beta x_t, \sigma^2)$$



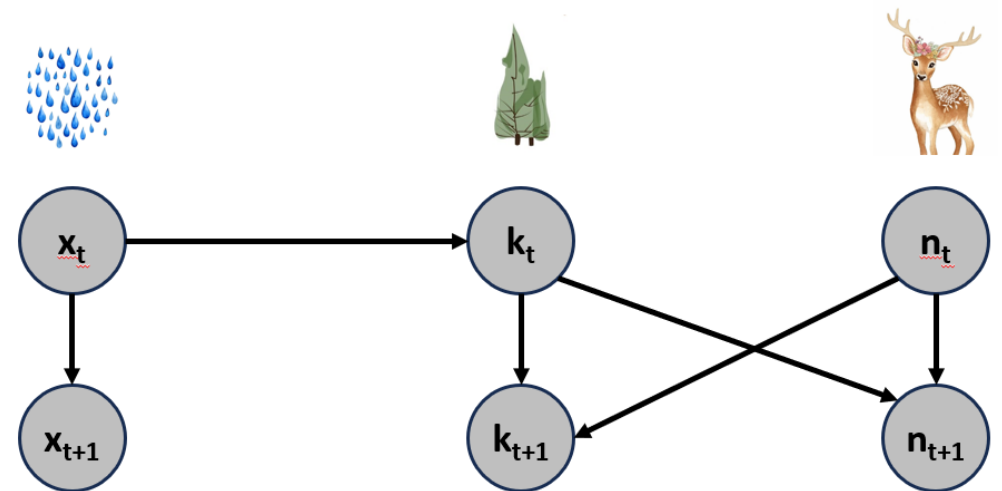
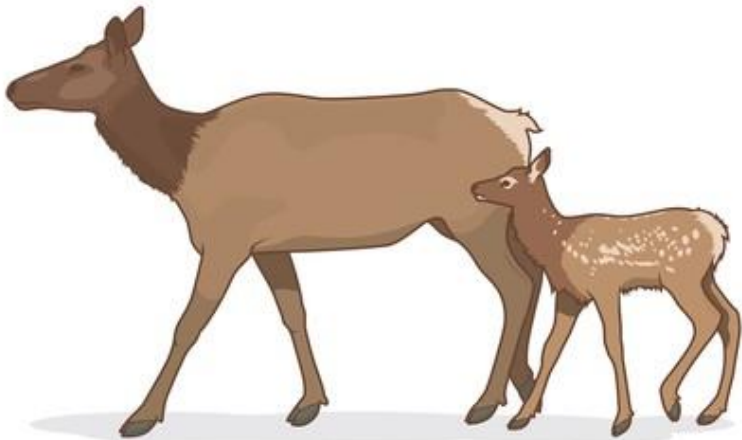
85% of betas are positive, 80% are 'not statistically significant'

Failing to account for cross-lags or dynamic processes increases type II error (i.e., false negatives)

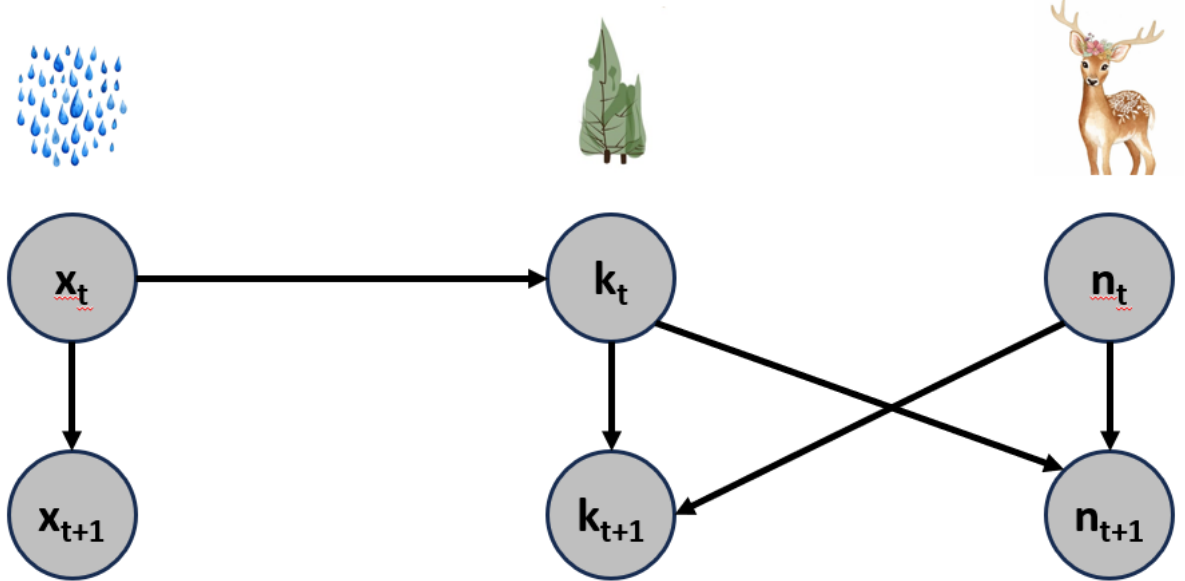
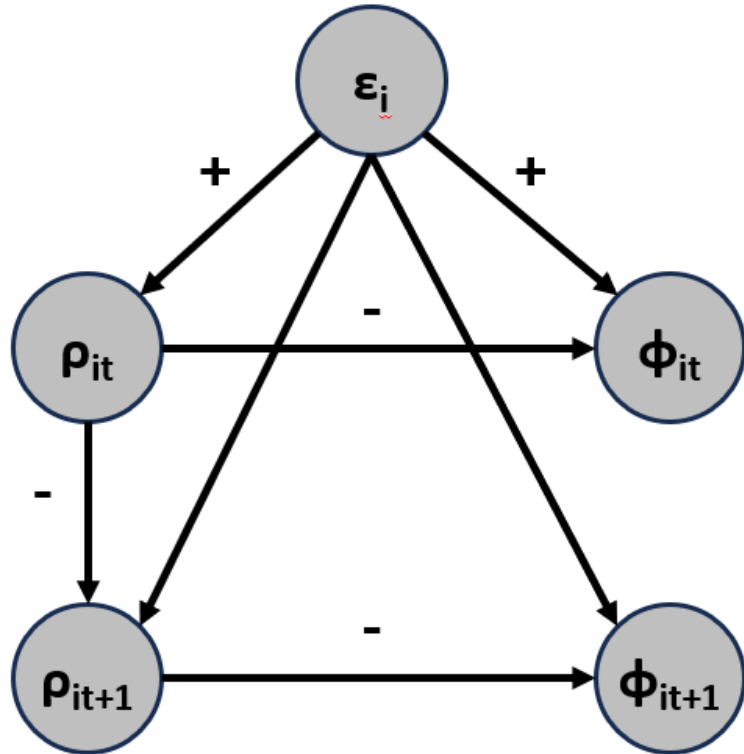
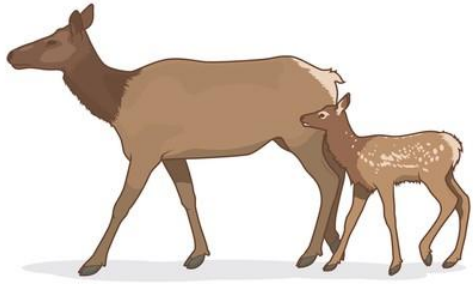
$$\lambda_t = \frac{n_{t+1}}{n_t}$$



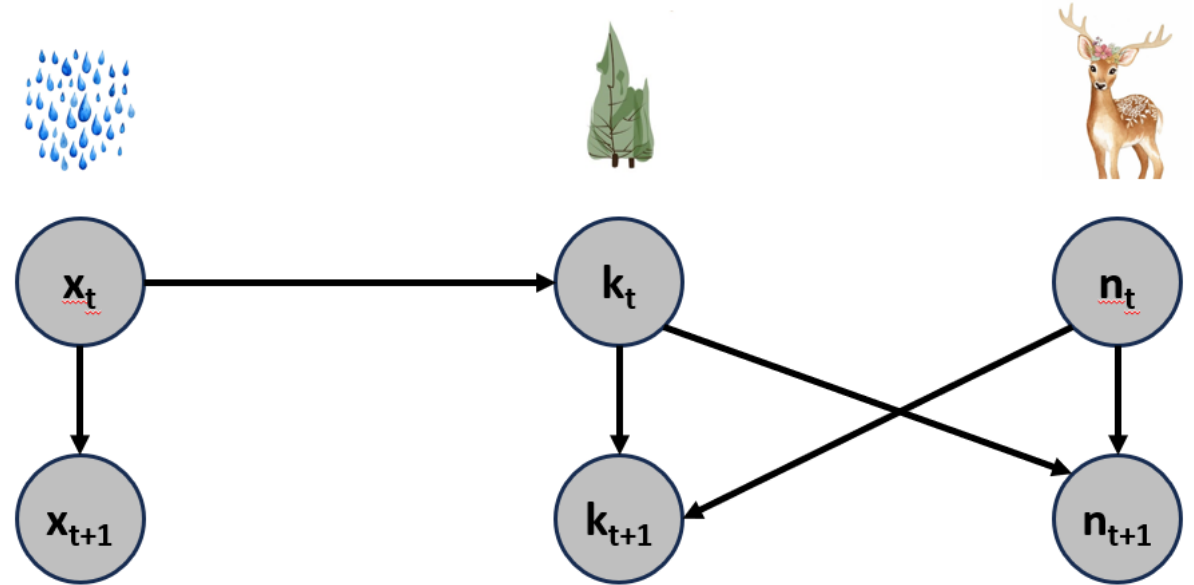
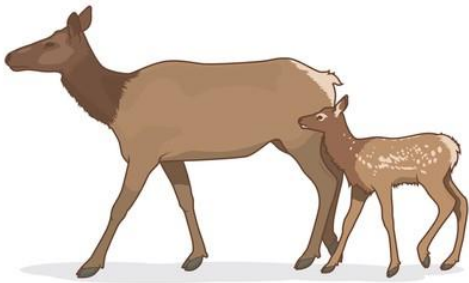
Failing to account for cross-lags or dynamic processes increases type I and type II error



These are 'simple' models! [or at least simple ideas]



JAGS code is provided for both analyses on GitHub



SEM_workshop/R_scripts/Lecture6_scripts/Lecture6a_life_history_trade_off.R

SEM_workshop/R_scripts/Lecture6_scripts/Lecture6b_dynamic_SEM_herbivore_carrying_capacity.R

Bayesian inference and flexibility moving forward

There is a Bayesian SEM package with the exact same syntax as 'lavaan'...

It's called 'blavaan'

Bayesian inference and flexibility moving forward

Instead of using 'sem()' it uses 'bsem()'

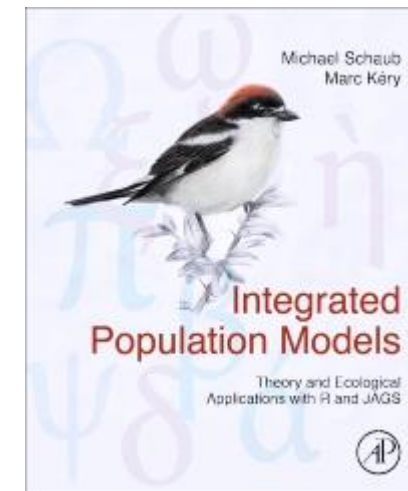
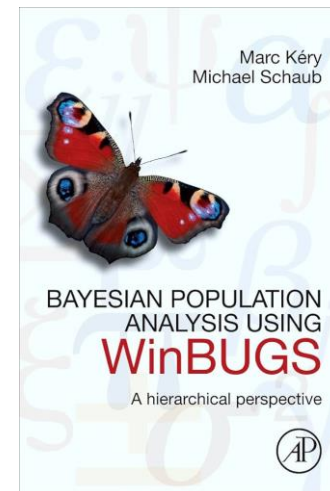
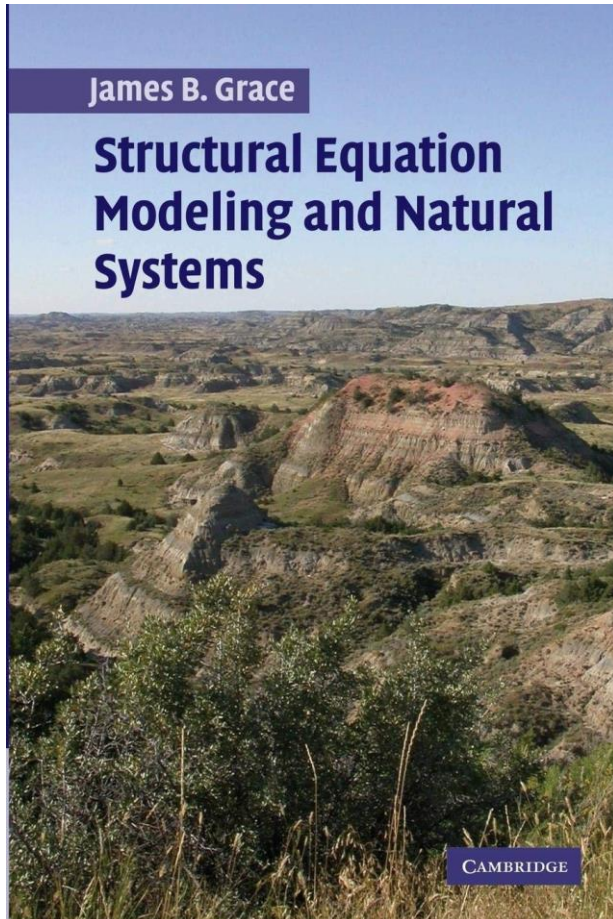
You can literally change two letters and run the same analysis in JAGS or Stan

This package will also output functioning JAGS or Stan code for you
*(the Stan code will be quite complicated)

```
230 d <- data.frame(c = canopy, s = subcan, y = warblers)
231 sem1 <- bsem('m =~ c + s
232           y ~ m
233           c ~ 1
234           s ~ 1',
235           data = d,
236           target = 'jags',
237           mcmcfile = T)
238 summary(sem1)
239 # ~~~~~
240 # look in your working directory
241 # there will be a perfectly functioning JAGS model file
242 # that was used to generate the parameter estimates in a lavExport folder
243 # you may have to change some parameter names & priors, but that's it!
244 # ~~~~~
```

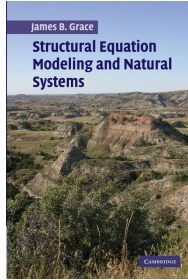
R_scripts > Lecture6_scripts > lavExport				
	Name	Date modified	Type	Size
	sem	3/2/2025 10:58 AM	JAG File	2 KB
	semjags	3/2/2025 10:58 AM	RDA File	5 KB

Imagine you are interested in a SEM underlying an IPM...

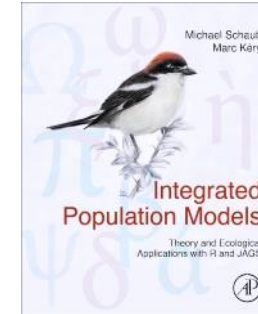
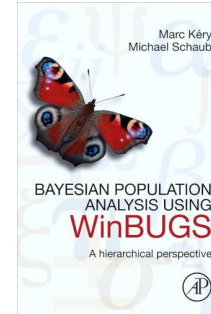
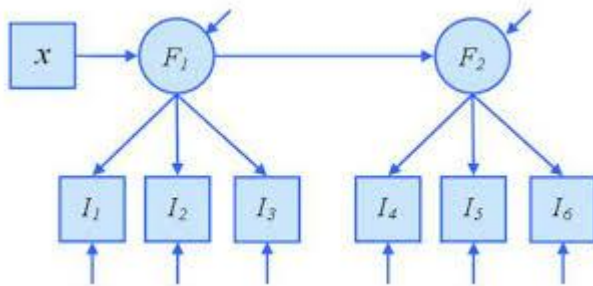


Or an occupancy model, or a complex RSF or SSF, etc.

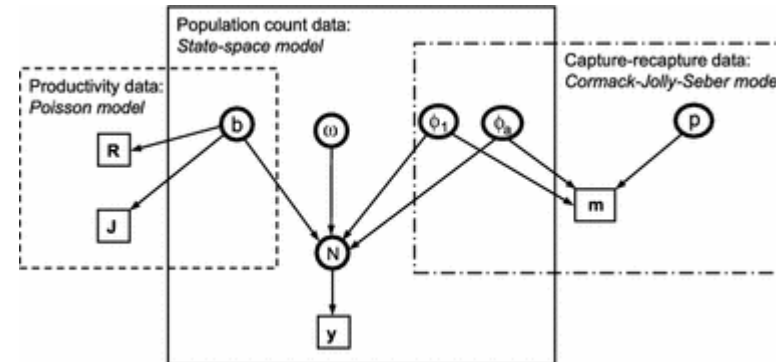
Imagine you are interested in a SEM underlying an IPM



An ecological system model



An integrated population model



There is no R package for this (there shouldn't be either)

Imagine you are interested in a SEM underlying an IPM

Riecke et al. · Tengmalm's owl IPM

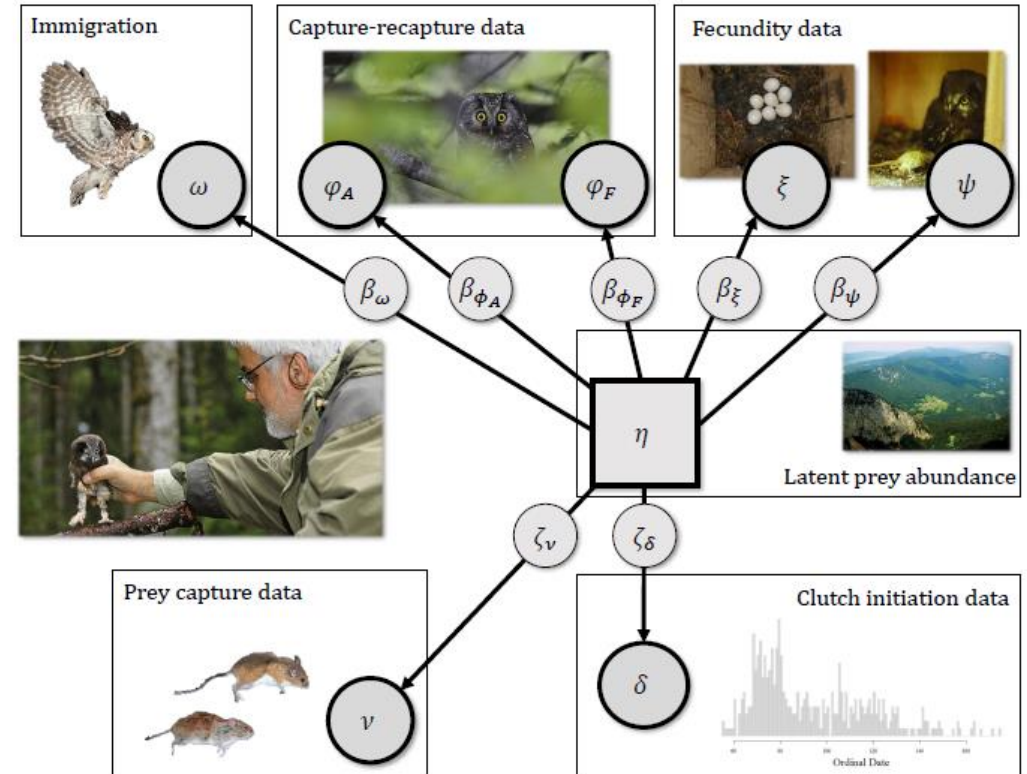
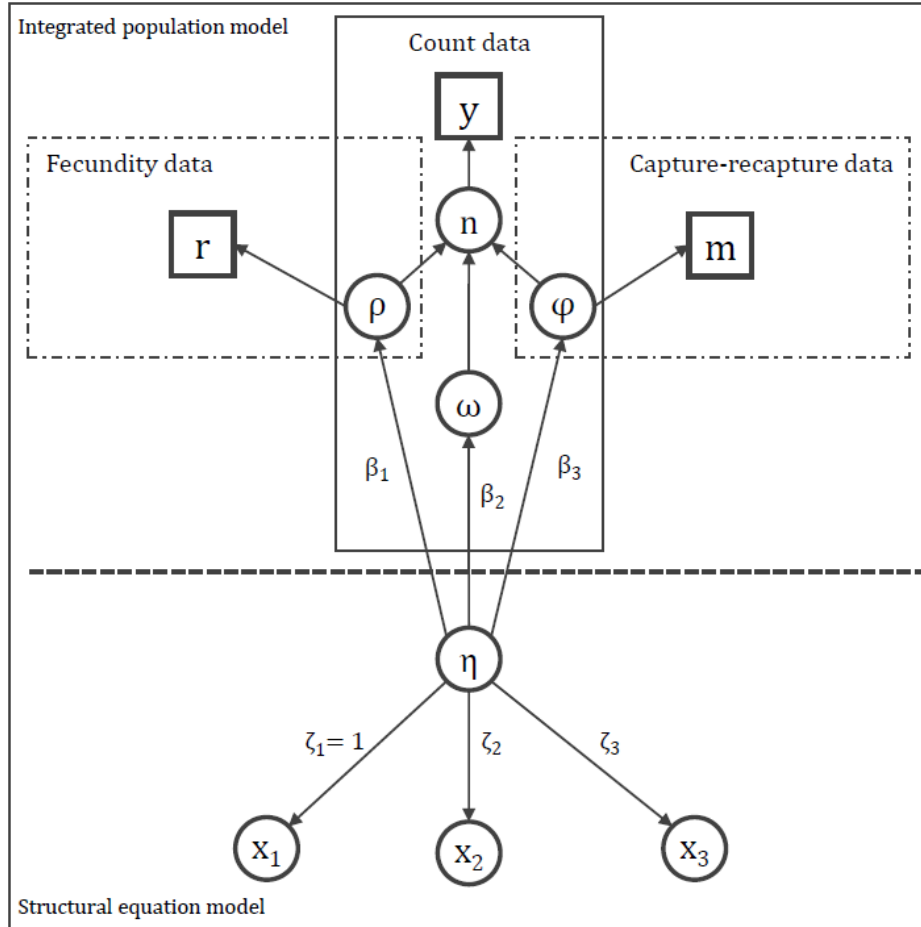
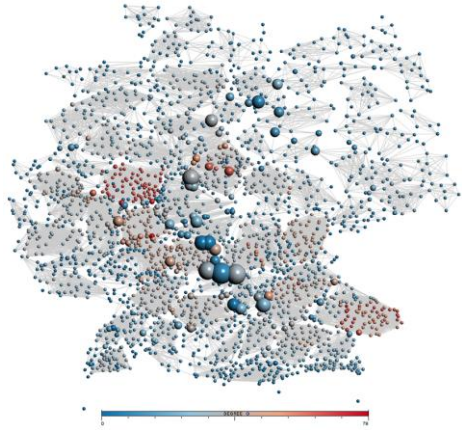


Figure 2. A conceptual figure demonstrating the modelled relationships between the mean number of *Apodemus* mouse and vole (Arvicolinae) remains discovered in nest boxes following breeding (ν), mean laying date (δ), latent breeding conditions (η ; i.e., rodent abundance), and the demographic parameters clutch size (ξ), the probability that each egg fledges (ψ), adult survival (ϕ_A), fledgling survival to adulthood (ϕ_F), and the expected number of immigrants (ω) for Tengmalm's owls breeding in the Jura Mountains in northwestern Switzerland and eastern France (1990-2020).

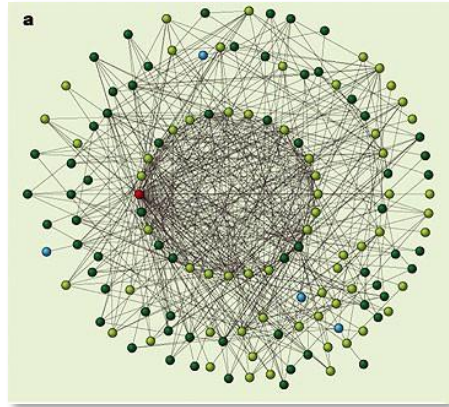
Conclusion

Ecological systems are unbelievably complex and beautiful!



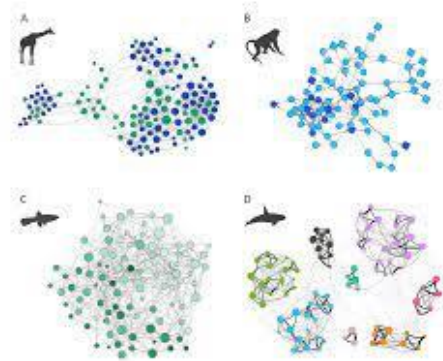
Climate network

Abiotic systems



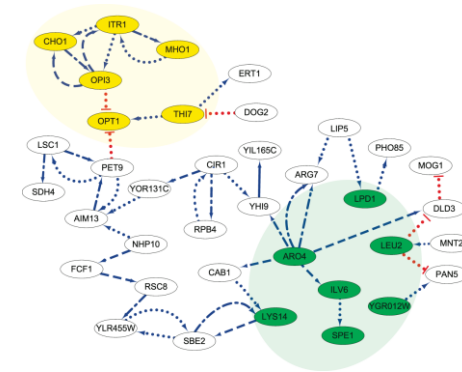
Food Network

Within communities



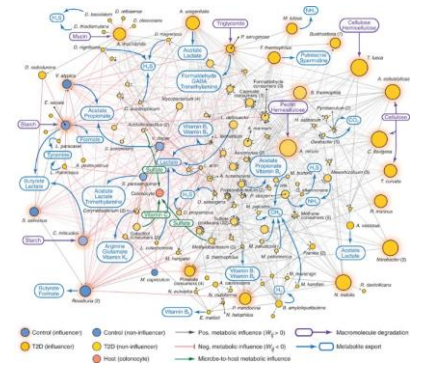
Social Network

Within populations



Gene Network

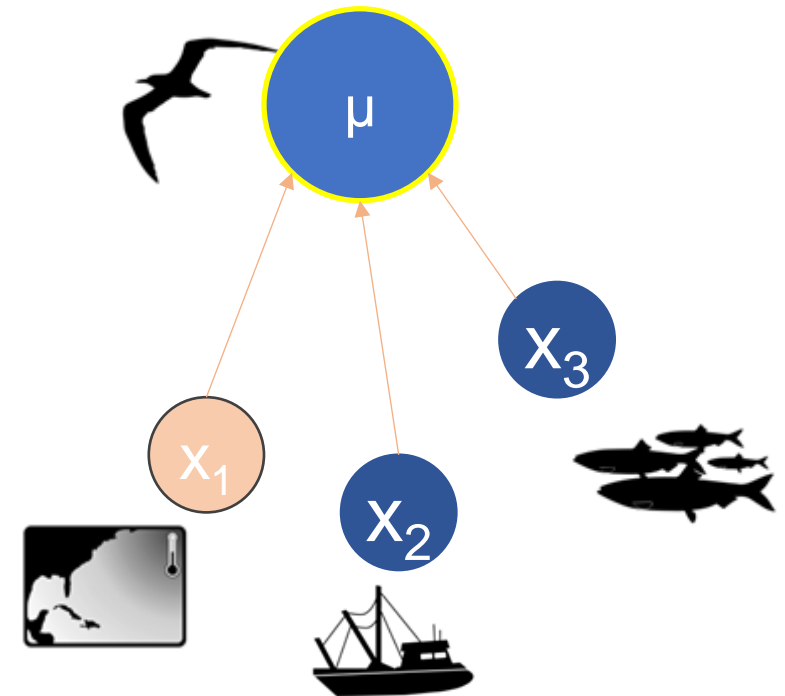
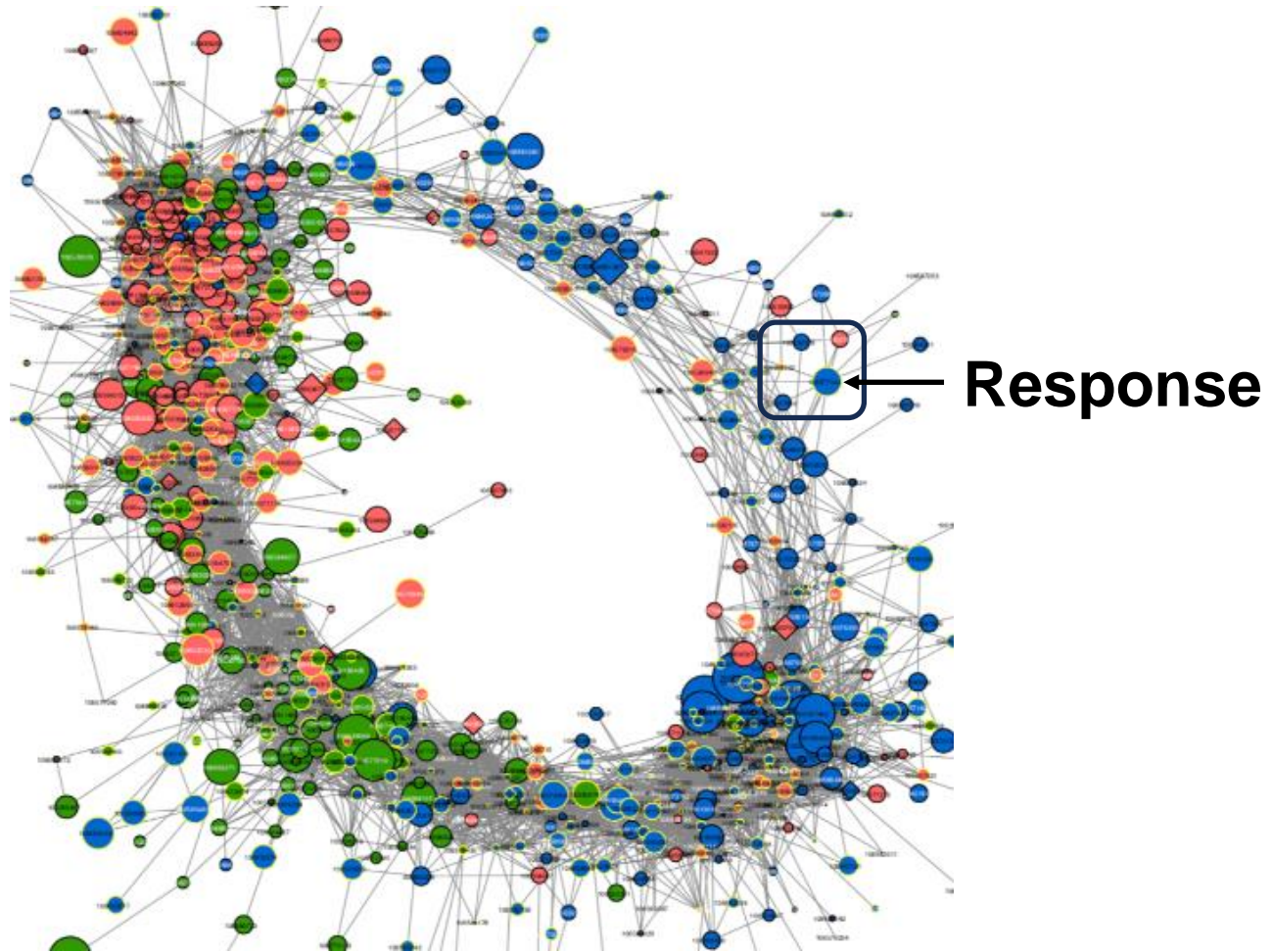
Within individuals



Microbial Network

Within individuals

GLMs are not bad, SEMs don't 'replace' them!



SEMs are just more than one GLM

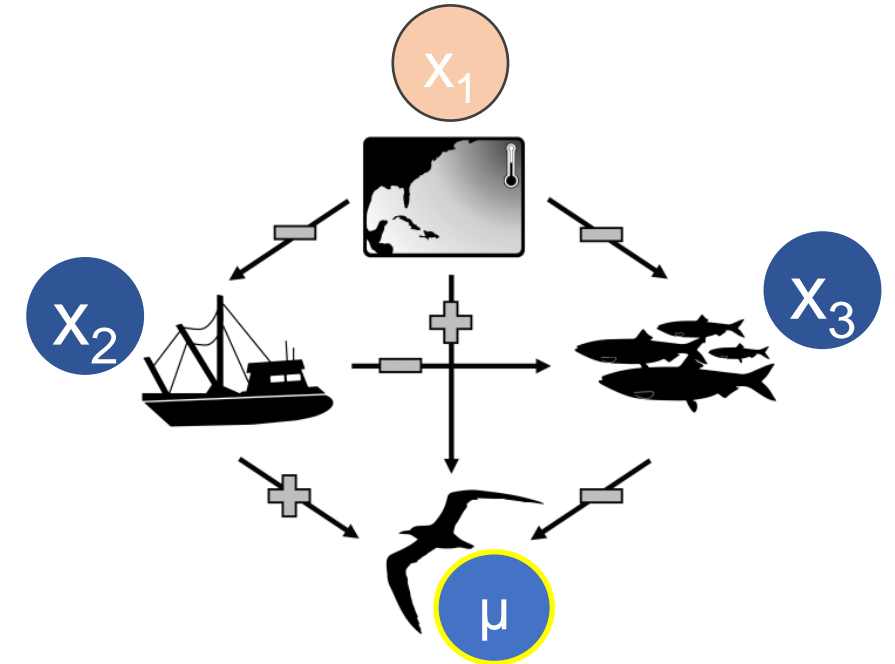
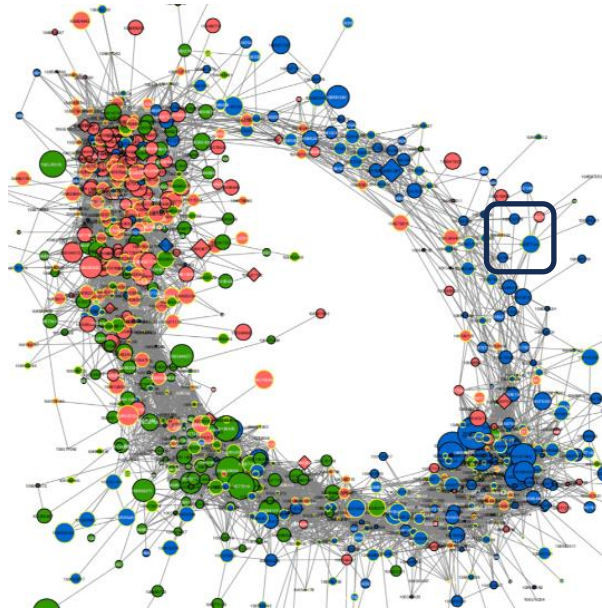
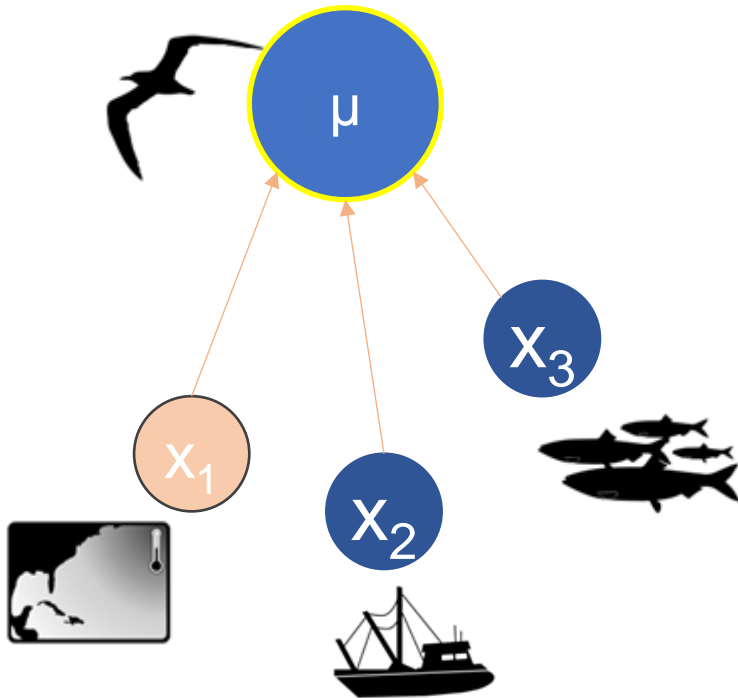
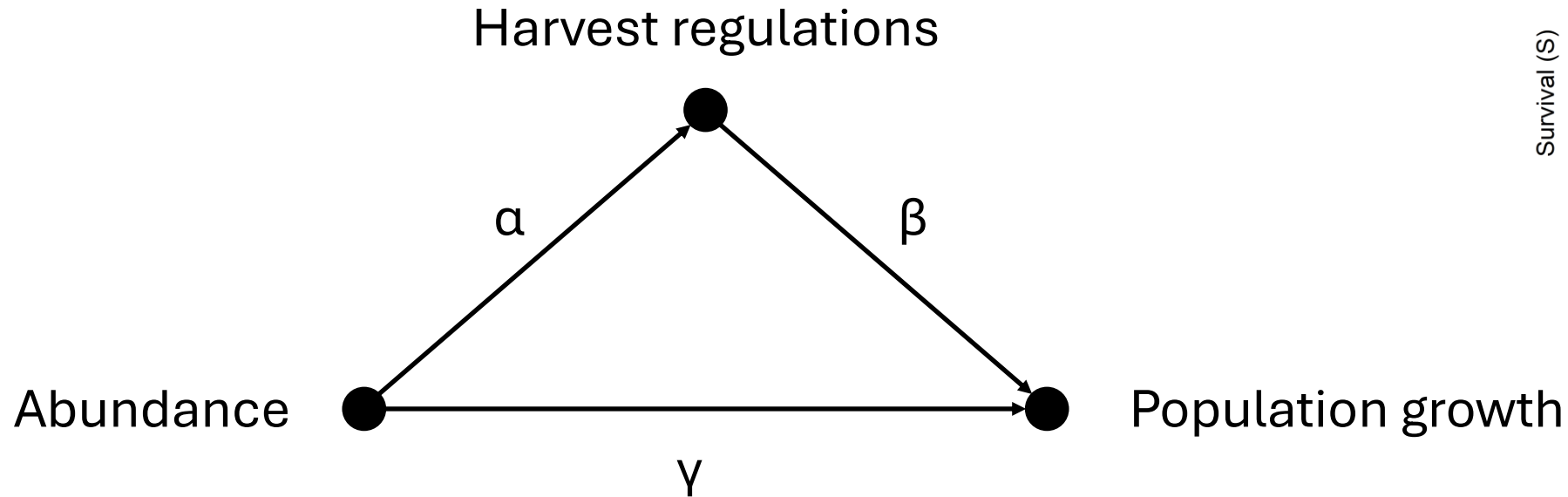
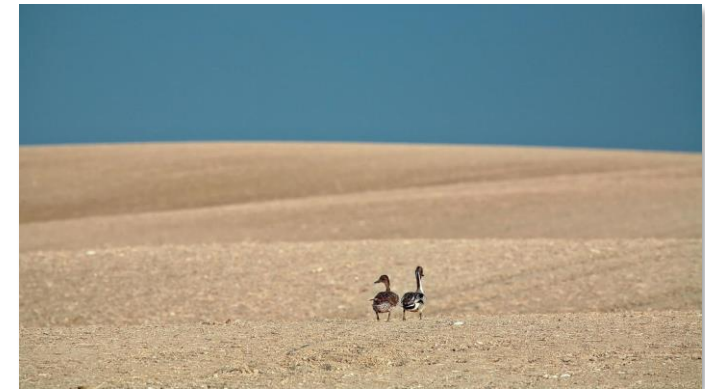
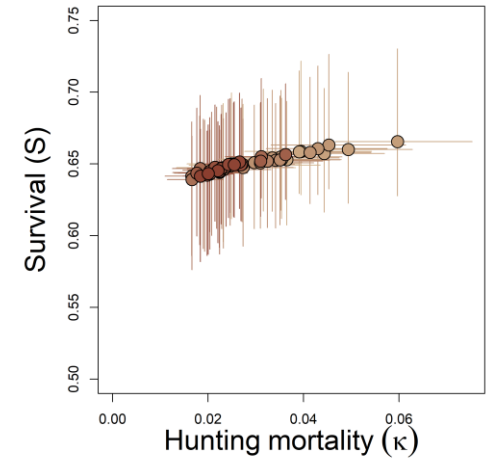


FIGURE 1 Simplified path diagram describing the hypothesized directionality (plus: Positive, bar: Negative association) regarding how environmental variables (i.e., sea-surface temperatures in the North Atlantic, fishery pressure, and fish production) influenced one another, as well as the indirect and direct pathways in which these sources of environmental variability influenced Royal tern mortality.

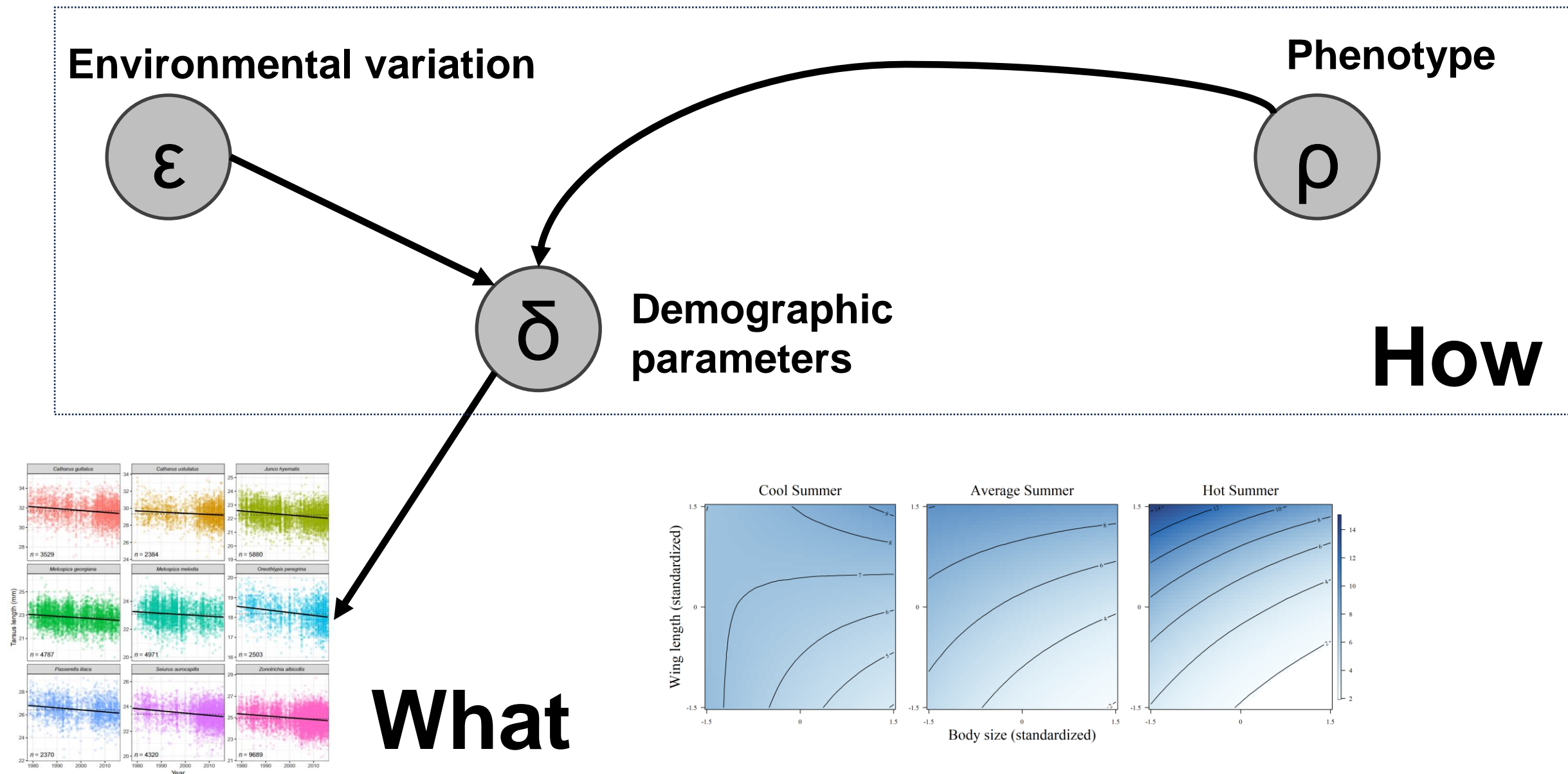
SEMs allow us to think simply about complex processes



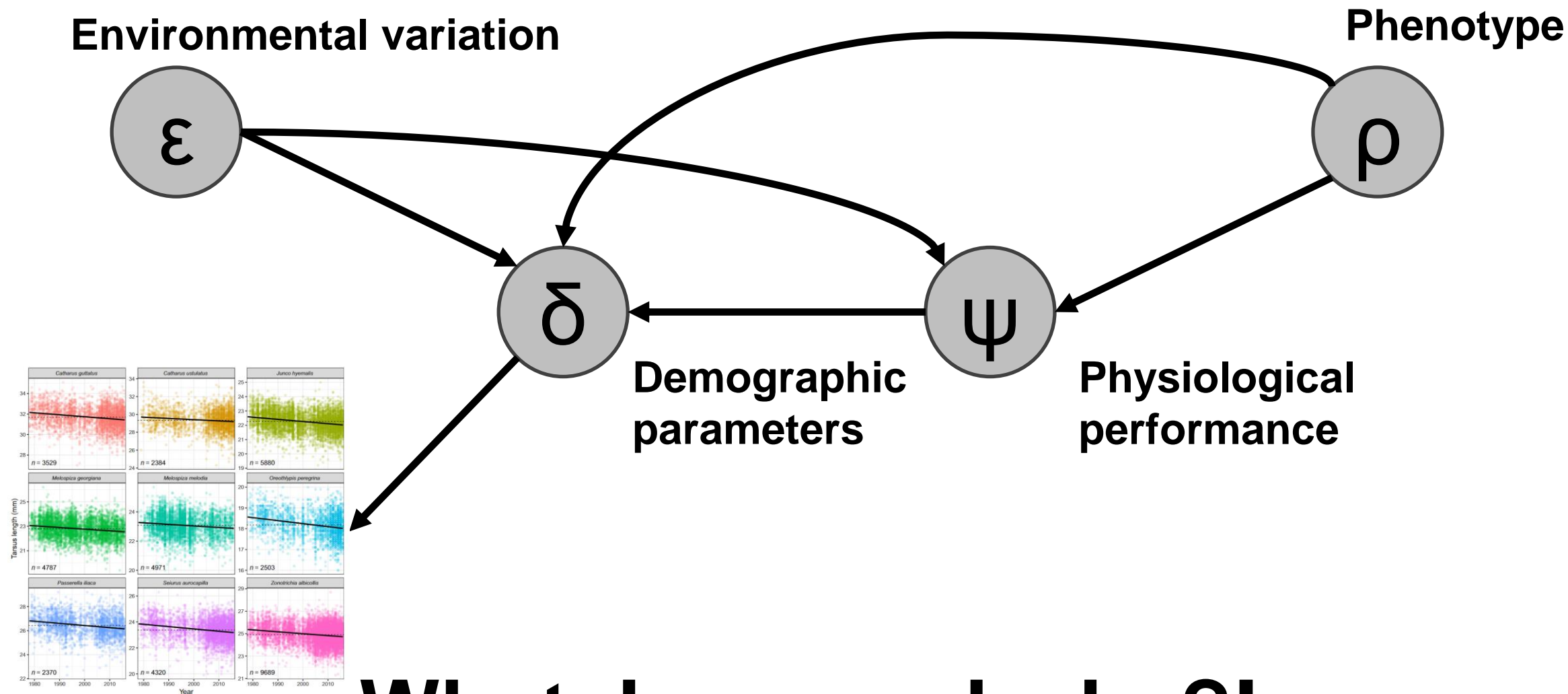
α : harvest management strategies
 β : effects of harvest
 γ : density-dependence



SEMs facilitate 'inter-disciplinary' models!

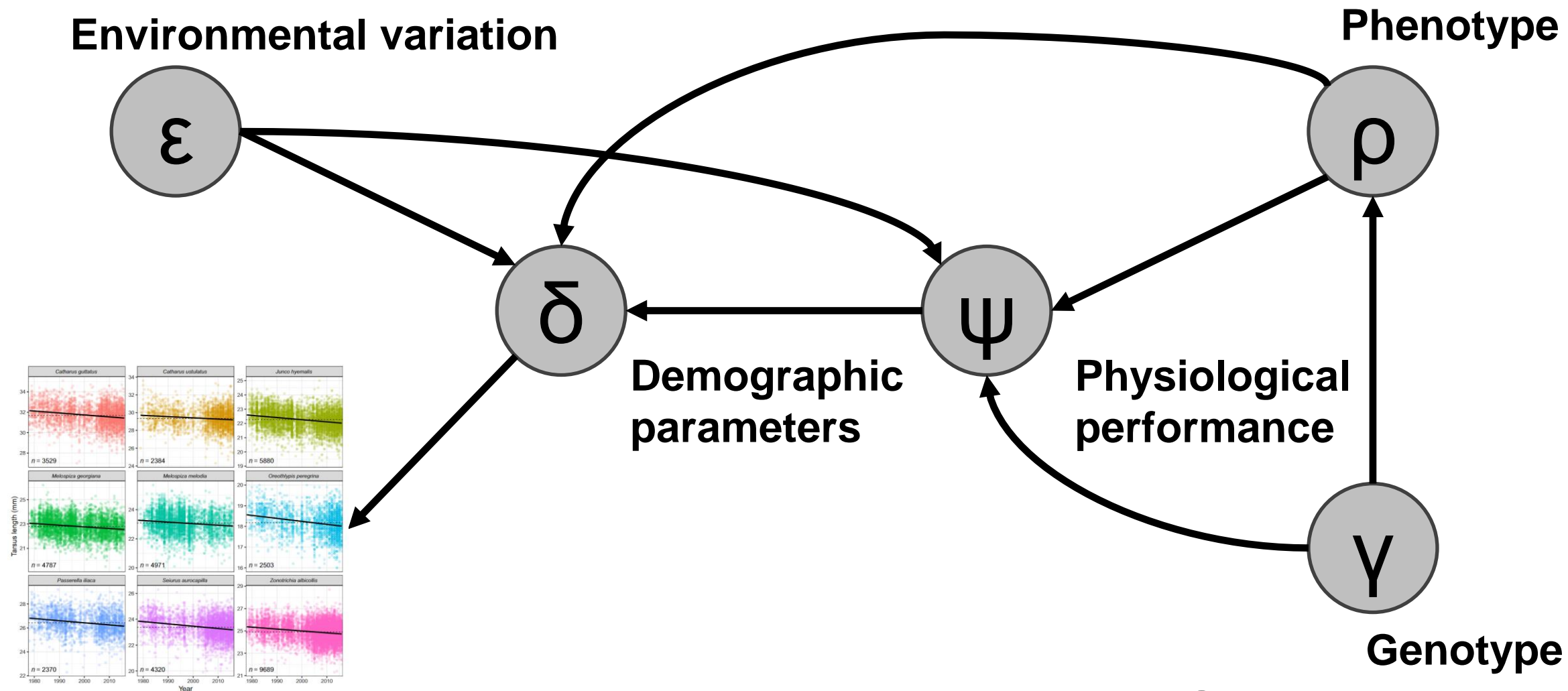


SEMs facilitate 'inter-disciplinary' models!



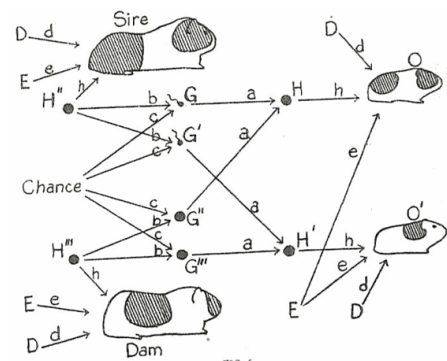
What, how, and why?!

SEMs facilitate 'inter-disciplinary' models!



What, how, and why?!

These aren't new concepts

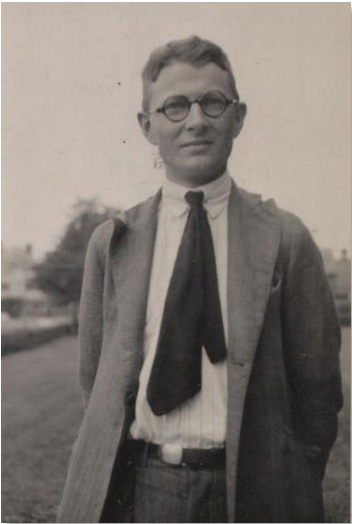


THE METHOD OF PATH COEFFICIENTS

By

SEWALL WRIGHT

Department of Zoology, The University of Chicago.



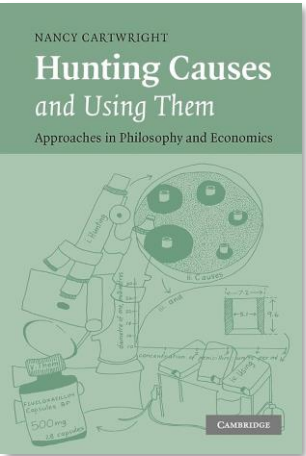
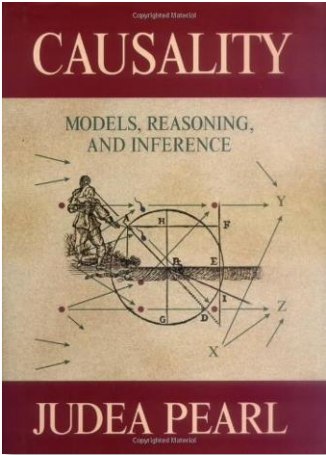
ON THE INADEQUACY OF THE PARTIAL AND MULTIPLE CORRELATION TECHNIQUE

BARBARA STODDARD BURKS

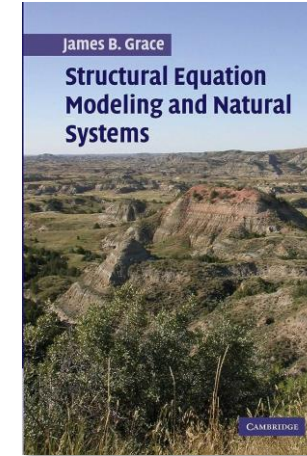
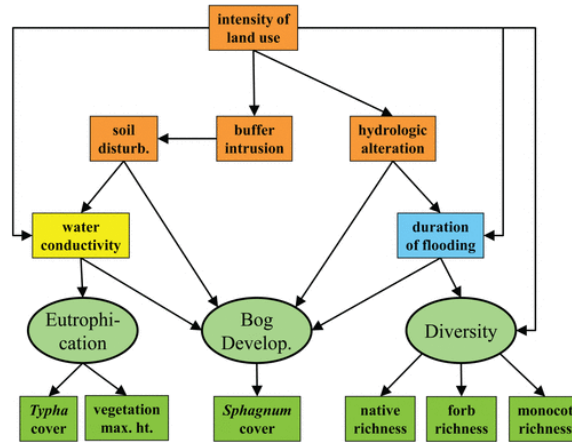
Stanford University

PART I. IN THE STUDY OF CAUSATION

Logical considerations lead to the conclusion that the techniques of partial and multiple correlation are fraught with dangers that seriously restrict their applicability. In fact their attempted use in (a) isolating the causes which operate upon observed effects, and (b) defining the extent to which two measures involve common factors unique to themselves, often result in interpretations that are misleading and even untrue excepting in a few special types of situation. Only issues arising in the first field (i.e., causation) will be discussed at this time. Consideration of the second field will be left for a subsequent paper (Part II).



These aren't new concepts

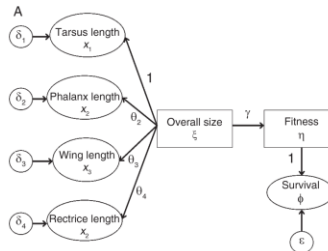


Ecology, 93(2), 2012, pp. 248–255
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Testing hypotheses in evolutionary ecology with imperfect detection: capture–recapture structural equation modeling

SARAH CUBAYNES,^{1,2,4} CLAIRE DOUTRELANT,¹ ARNAUD GRÉGOIRE,¹ PHILIPPE PERRET,¹ BRUNO FAIVRE,³
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¹Centre d'Ecologie Evolutive et Fonctionnelle UMR 5175, 1919 Route de Mende, 34293 Montpellier, Cedex 5, France
²Institut de Mathématiques et Modélisation de Montpellier, UNR 5149, Place Eugène Bataillon, 34095 Montpellier, Cedex 5, France
³Biogéosciences, Université de Bourgogne UMR 5561, 6 Boulevard Gabriel, 21000 Dijon, France



Journal of Animal Ecology

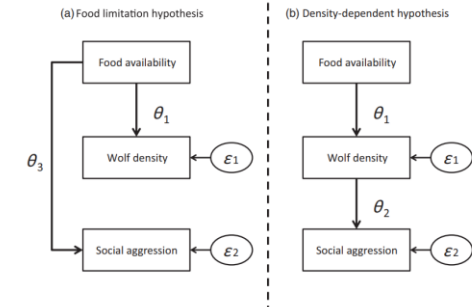
Journal of Animal Ecology 2014, 83, 1344–1356

doi: 10.1111/1365-2656.12238

Density-dependent intraspecific aggression regulates survival in northern Yellowstone wolves (*Canis lupus*)

Sarah Cubaynes^{1*}, Daniel R. MacNulty², Daniel R. Stahler³, Kira A. Quimby³, Douglas W. Smith³ and Tim Coulson¹

¹Department of Zoology, University of Oxford, South Parks Road, Oxford, OX1 3PS, UK; ²Department of Wildland Resources, Utah State University, Logan, UT 84322, USA; and ³Yellowstone Wolf Project, Yellowstone Center for Resources, Yellowstone National Park, Mammoth, WY 82190, USA



Cubaynes et al. **(2012)** *Ecology*; Cubaynes et al. **(2014)** *Journal of Animal Ecology*

SEMs feel overwhelming?!

- SEMs are just more than one GLM
- SEMs allow us to model in the same way that we think...
- Dig into the code, and use `blavaan` to help 'check' yourself
- Feel free to reach out with questions (or goofy bug fixes!)



Journal of Animal Ecology

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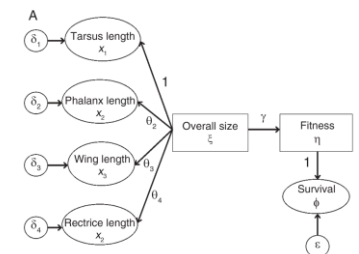
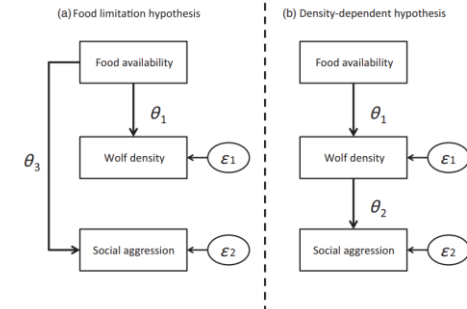
Testing hypotheses in evolutionary ecology with imperfect detection: capture–recapture structural equation modeling

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³Biogéosciences, Université de Bourgogne UMR 5561, 6 Boulevard Gabriel, 21000 Dijon, France



Facilitators!



Colton Padilla



Kaitlyn Vega



Sunny Domschot



Liv Lundin

Questions?

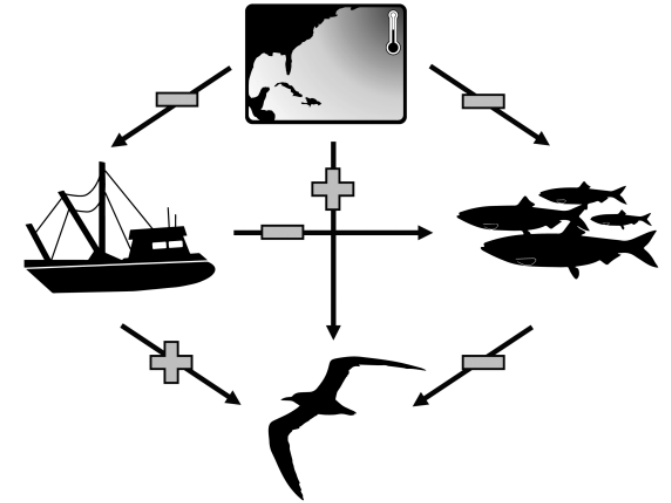


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