

# Path analysis & SEMs in ecology (WILD 595)

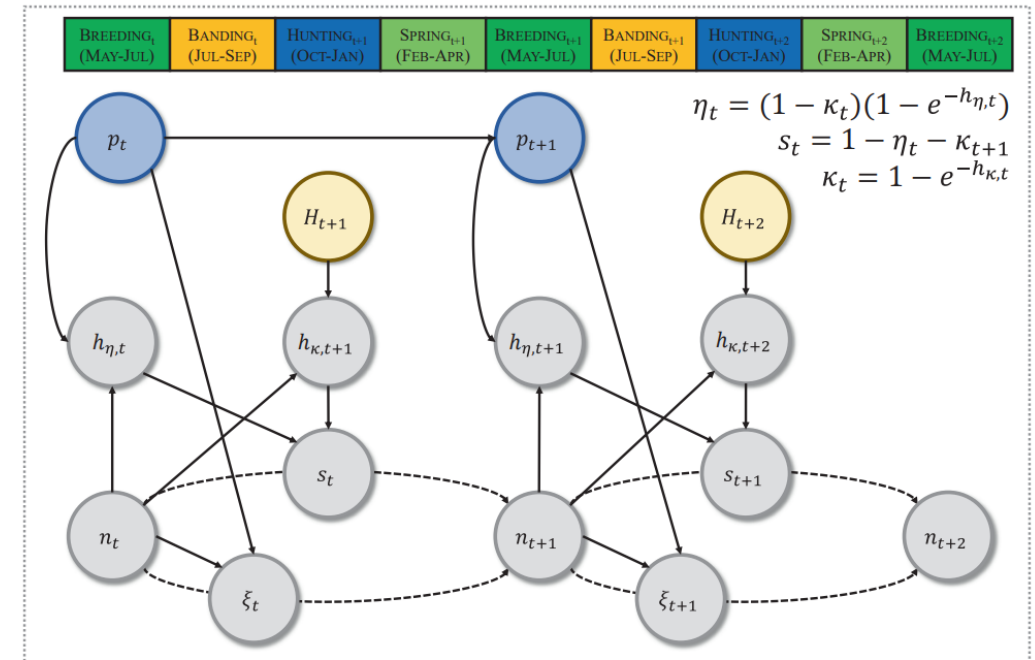
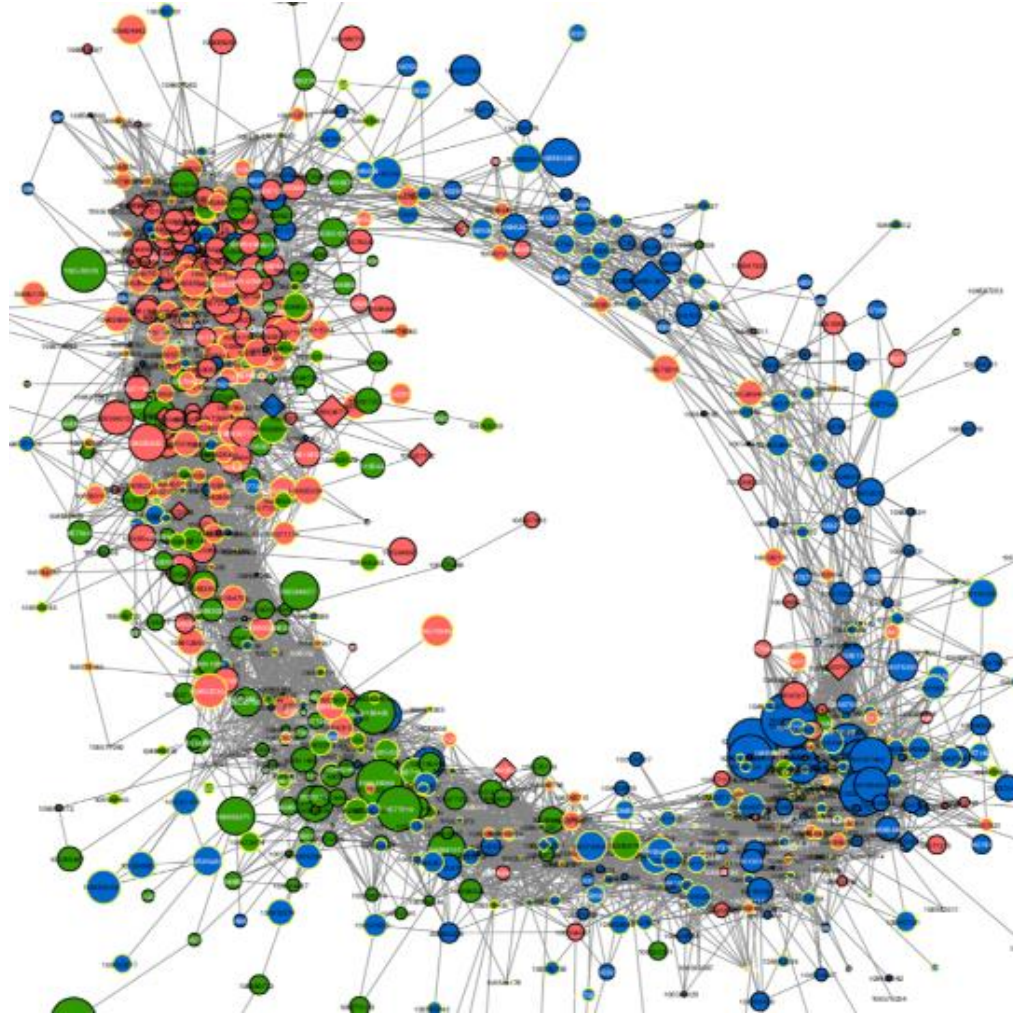


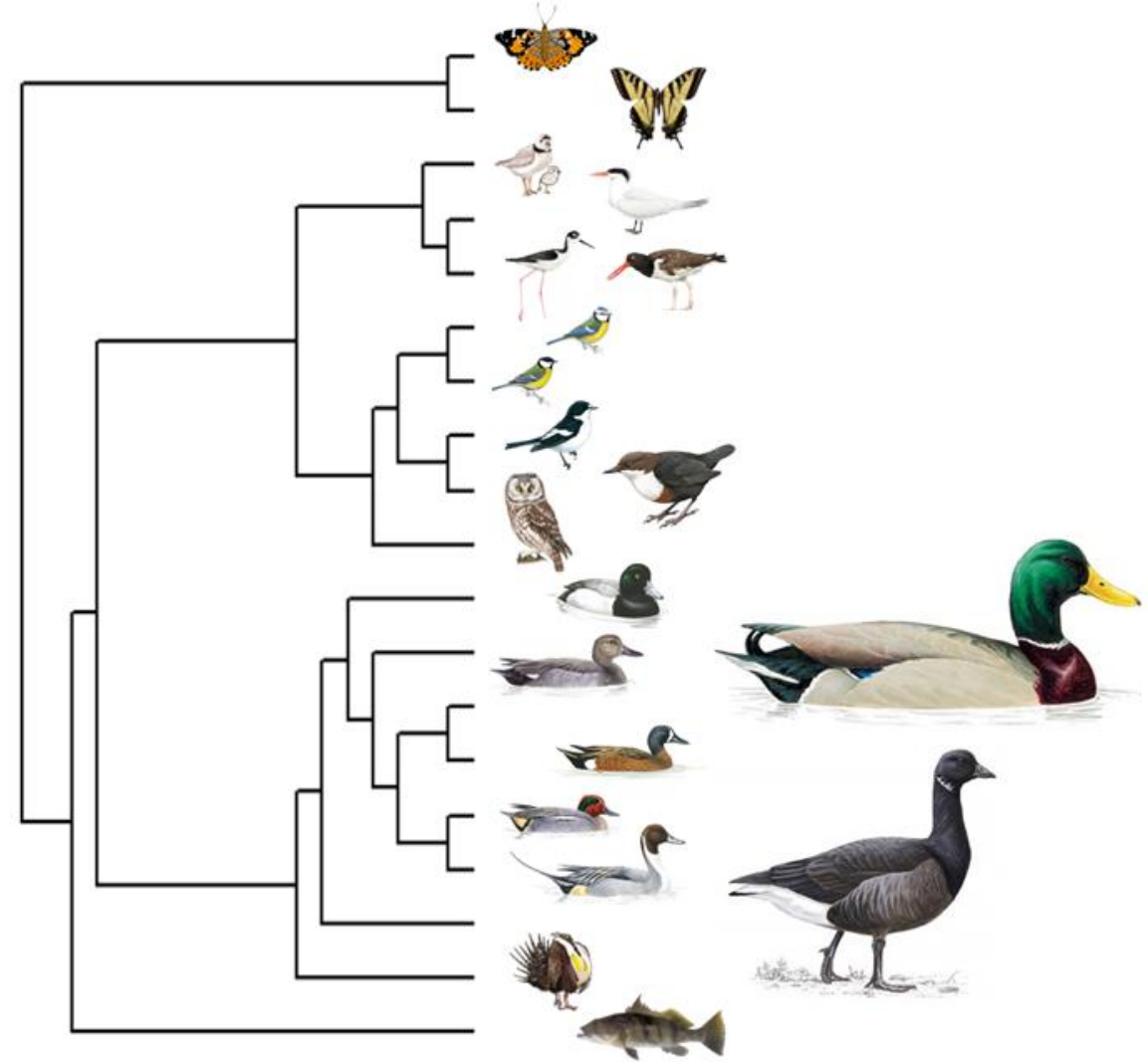
FIGURE 2 A directed acyclic graph demonstrating the relationships among abundance ( $n$ ), ponds ( $p$ ; blue), fecundity ( $\xi$ ), hunting mortality hazard rate ( $h_{\eta}$ ), natural mortality hazard rate ( $h_{\kappa}$ ), survival ( $s$ ) and the number of duck hunters ( $H$ ; brown) for blue-winged teal breeding in the North American Prairie Pothole Region across the annual cycle (1973–2016). Solid arrows represent estimated directional relationships, and dashed arrows represent processes leading to changes in population abundance.

# Hi!

# Thomas Riecke

## Assistant Professor

## James K. Ringelman Chair in Waterfowl Conservation



**thomas.riecke@umontana.edu**

**Who are you?**

## Accommodations

- **Let me know** (*as much as you need to/feel comfortable with*)

## Other professional obligations

- **Let me know** (*as much as you need to/feel comfortable with*)

## Anything else?

- **Let me know** (*as much as you need to/feel comfortable with*)

# Grades

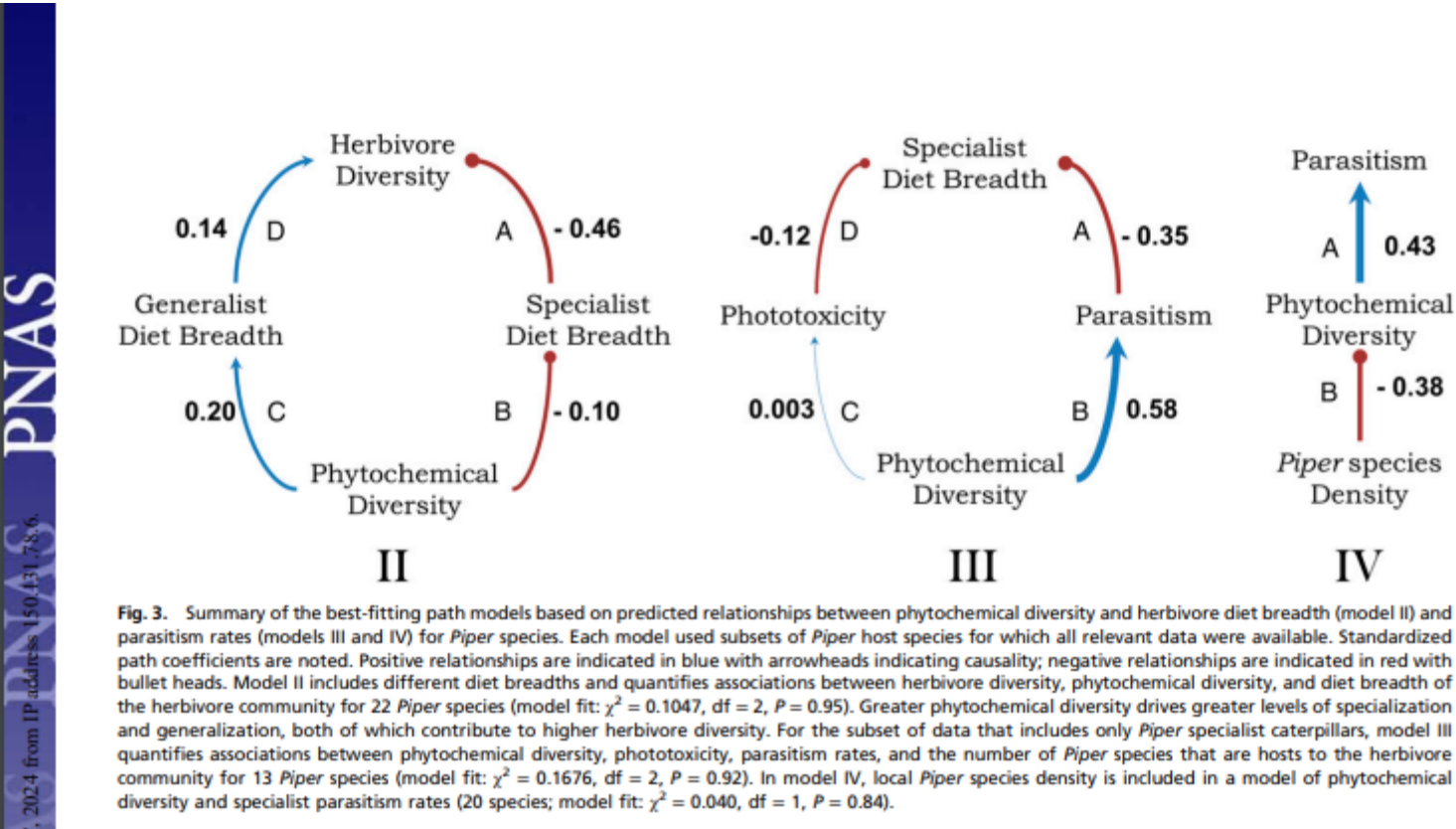
- You'll almost certainly receive an excellent grade unless:
  - *You don't do a project*
  - ~~*You disrupt the teaching/learning process*~~
  - ~~*You don't come to class*~~

# Project

- Perform and write up an analysis.
  - i.e., **‘finish or at least draft a methods and results section for a thesis or dissertation chapter.’**
- **If you’re early in the program or don’t have any data yet,** I can help with simulating data that will be similar to future data, we can use an existing dataset that’s similar, or you can simply work on writing an excellent methods section for a proposal?

**So why are we doing this?**

# Structural equation models are the best tool ever! – Lee Dyer





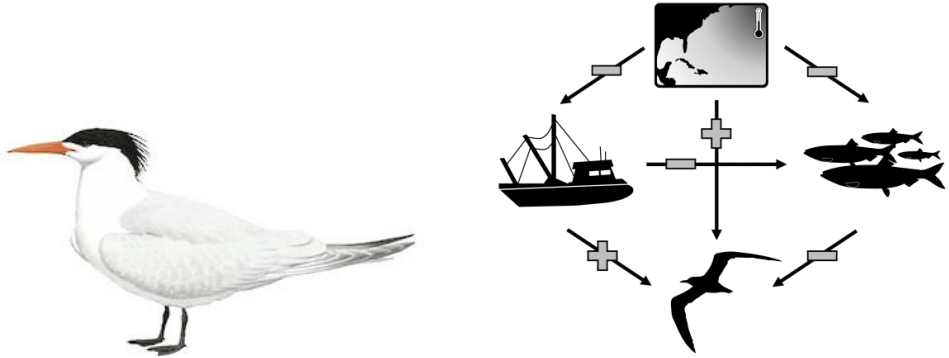


***Structural equation models are the best tool ever! – Lee Dyer***

**I was moderately skeptical**

**I began to use these approaches in my own research**

## Example(s): population dynamics (CMR, IPMs)



**FIGURE 1** Simplified path diagram describing the hypothesized directionality (plus: Positive, bar: Negative association) regarding how environmental variables (i.e., sea-surface temperatures in the North Atlantic, fishery pressure, and fish production) influenced one another, as well as the indirect and direct pathways in which these sources of environmental variability influenced Royal tern mortality.

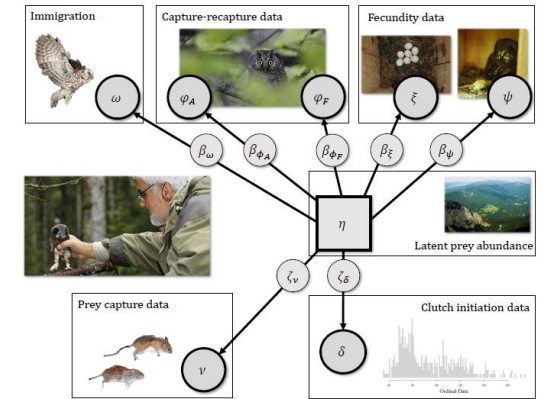


Figure 2. Directed acyclic graph demonstrating the modelled relationships between the mean number of *Apodemus* mouse and vole (Arvicolinae) remains discovered in nest boxes following breeding ( $\nu$ ), mean laying date ( $\delta$ ), latent breeding conditions ( $\eta$ ; i.e., rodent abundance), and the demographic parameters clutch size ( $\zeta$ ), the probability that each egg fledges ( $\phi_e$ ), breeding probability ( $\gamma$ ), adult survival ( $\phi_a$ ), fledging survival to adulthood ( $\phi_{fa}$ ), and the expected number of immigrants ( $\omega$ ) for Tengmalm's owls breeding in the Jura Mountains in northwestern Switzerland and eastern France (1990–2020).

A hierarchical population model for the estimation of latent prey

abundance and demographic rates of a nomadic predator

Thomas V. Riecke<sup>1,2,\*</sup>, Pierre-Alain Ravussin<sup>3</sup>, Ludovic Longchamp<sup>4</sup>, Daniel Trolliet<sup>5</sup>, DanGibson<sup>6</sup> and Michael Schaub<sup>1</sup>

Received: 28 June 2022 | Revised: 26 September 2022 | Accepted: 5 October 2022

DOI: 10.1111/gcb.16482

RESEARCH ARTICLE

Global Change Biology WILEY

# Climate change and commercial fishing practices codetermine survival of a long-lived seabird

Daniel Gibson<sup>1,2</sup> | Thomas V. Riecke<sup>3</sup> | Daniel H. Catlin<sup>2</sup> | Kelsi L. Hunt<sup>2</sup> |  
Chelsea E. Weithman<sup>2</sup> | David N. Koons<sup>1</sup> | Sarah M. Karpanty<sup>2</sup> | James D. Fraser<sup>2</sup>

Gibson, Riecke, et al. (2023) *Global Change Biology*

Riecke et al. (in revision) *Ecological Modelling*



# Example(s): understanding harvest effects

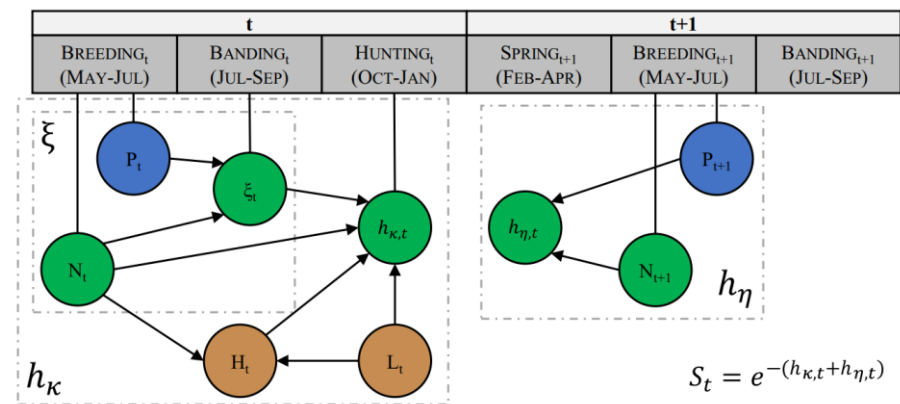


FIGURE 2 Directed acyclic graph demonstrating the hypothesized relationships among mallard breeding pair abundance ( $N$ ), the number of ponds ( $P$ ), harvest limits ( $L$ ), the abundance of duck hunters ( $H$ ), fecundity ( $z$ ), harvest mortality hazard rate ( $h_\eta$ ), natural mortality hazard rate ( $h_\kappa$ ) and survival ( $S$ ) for mallards marked and released in the Prairie Pothole Region of the United States and Canada, 1974–2016. Arrows represent covariate effects, grey dashed lines enclose separate generalized linear models and vertical solid lines denote the time period or interval when parameters were estimated, where survival ( $S$ ) and natural mortality in year  $t$  are estimated from banding in year  $t$  to banding in year  $t+1$ . We estimated age-specific band recovery probabilities ( $f$ ) as a function of age-specific harvest probability ( $\kappa$ ), reporting rate ( $r$ ) and crippling rate ( $c$ ),  $f = \kappa(1 - c)r$ . We note that we hypothesized the same relationships among demographic components for both juvenile and adult females.

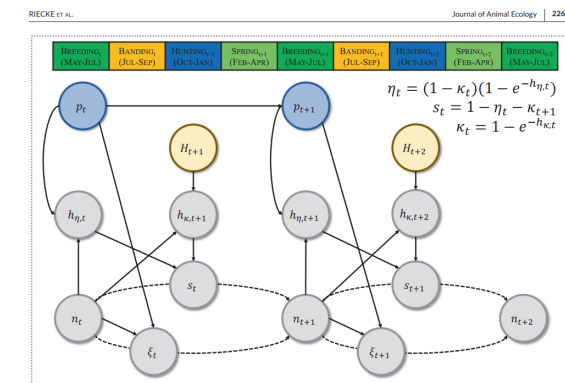


FIGURE 2 A directed acyclic graph demonstrating the relationships among abundance ( $N$ ), ponds ( $P$ ), fecundity ( $z$ ), hunting mortality hazard rate ( $h_\eta$ ), natural mortality hazard rate ( $h_\kappa$ ), survival ( $S$ ) and the number of duck hunters ( $H$ , brown) for blue-winged teal breeding in the North American Prairie Pothole Region across the annual cycle (1973–2016). Solid arrows represent estimated directional relationships, and dashed arrows represent processes leading to changes in population abundance.

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DOI: 10.1111/1365-2656.13747

## RESEARCH ARTICLE

### A hierarchical model for jointly assessing ecological and anthropogenic impacts on animal demography

Thomas V. Riecke<sup>1,2,3</sup> | Benjamin S. Sedinger<sup>4</sup> | Todd W. Arnold<sup>5</sup> | Dan Gibson<sup>6</sup> | David N. Koons<sup>5</sup> | Madeleine G. Lohman<sup>1,2</sup> | Michael Schaub<sup>3</sup> | Perry J. Williams<sup>2</sup> | James S. Sedinger<sup>2</sup>

<sup>1</sup>Program in Ecology, Evolution, and Conservation Biology, University of Nevada, Reno, NV, USA; <sup>2</sup>Department of Natural Resources and Environmental Science, University of Nevada, Reno, NV, USA; <sup>3</sup>Swiss Ornithological Institute, Sempach, Switzerland; <sup>4</sup>College of Natural Resources, University of Wisconsin-Stevens Point, Stevens Point, WI, USA; <sup>5</sup>Department of Fisheries, Wildlife, and Conservation Biology, University of Minnesota, St. Paul, MN, USA and <sup>6</sup>Department of Fish, Wildlife, and Conservation Biology, Colorado State University, CO, USA

Received: 2 November 2021 | Accepted: 10 August 2022  
DOI: 10.1111/1365-2656.13807

## RESEARCH ARTICLE

### Density-dependence produces spurious relationships among demographic parameters in a harvested species

Thomas V. Riecke<sup>1,2,3</sup> | Madeleine G. Lohman<sup>1,2</sup> | Benjamin S. Sedinger<sup>1,2,4</sup> | Todd W. Arnold<sup>5</sup> | Cliff L. Feldheim<sup>6</sup> | David N. Koons<sup>7</sup> | Frank C. Rohwer<sup>8</sup> | Michael Schaub<sup>3</sup> | Perry J. Williams<sup>2</sup> | James S. Sedinger<sup>2</sup>

<sup>1</sup>Graduate Program in Ecology, Evolution, and Conservation Biology, University of Nevada, Reno, Nevada, USA; <sup>2</sup>Department of Natural Resources and Environmental Science, University of Nevada, Reno, Nevada, USA; <sup>3</sup>Swiss Ornithological Institute, Sempach, Switzerland; <sup>4</sup>University of Wisconsin-Stevens Point, Stevens Point, Wisconsin, USA; <sup>5</sup>Department of Fisheries, Wildlife, and Conservation Biology, University of Minnesota, St. Paul, Minnesota, USA; <sup>6</sup>California Trout, San Francisco, California, USA; <sup>7</sup>Fish, Wildlife, and Conservation Biology & Graduate Degree Program in Ecology, Colorado State University, Ft. Collins, Colorado, USA and <sup>8</sup>Delta Waterfowl Foundation, Bismarck, North Dakota, USA



# Example(s): sequential fitness components

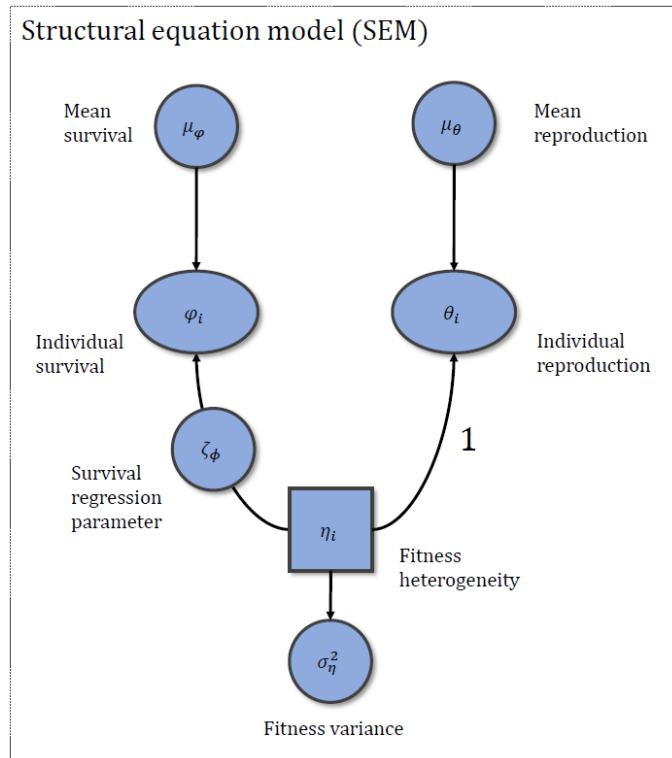
- 1 Individual quality and environmental factors interact to shape
- 2 reproduction and survival in a resident bird of prey
- 3 Roman Bühler<sup>1,2</sup>, Thomas V. Riecke<sup>1,3</sup>, Kim Schalcher<sup>2</sup>, Alexandre Roulin<sup>2</sup> and Bettina
- 4 Almasi<sup>1</sup>



**Figure 4:** A directed acyclic graph demonstrating the relationships of intrinsic (red) and extrinsic (green) covariates on female reproductive success (blue) and survival (yellow). Estimates and f-values (in brackets) are derived from the models shown in supplementary material S9 and are based on 556 individuals over 5 years. Bold arrows indicating f values >0.975, solid lines f values between 0.9 and 0.974 and dashed lines f values <0.9.

## Example: latent individual heterogeneity & life-history trade-offs

## Estimating latent fitness heterogeneity

Thomas V. Riecke<sup>1,2,3</sup>, Dan Gibson<sup>4</sup>, Rémi Fay<sup>5</sup>, Sarah Cubaynes<sup>6</sup>, Madeleine G. Lohman<sup>7,8</sup> andMichael Schaub<sup>1</sup>

# Estimating latent heterogeneity in individual fitness using structural equation models

Thomas V. Riecke<sup>1,2,3</sup>, Rémi Fay<sup>4</sup>, Johann Hegelbach<sup>5</sup>, Pierre-Alain Ravussin<sup>6</sup>, Daniel Arrigo<sup>7</sup> and Michael Schaub<sup>1</sup>

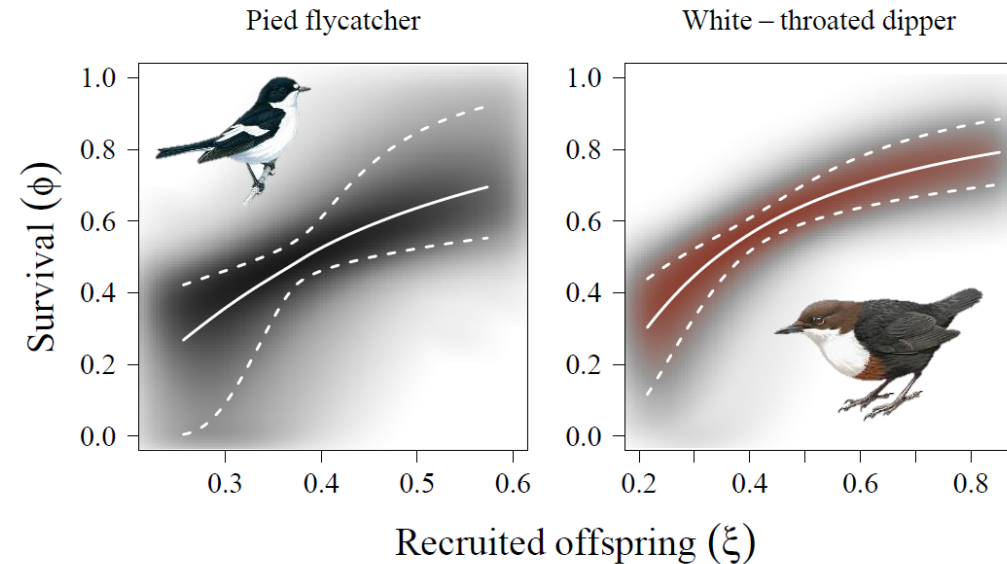


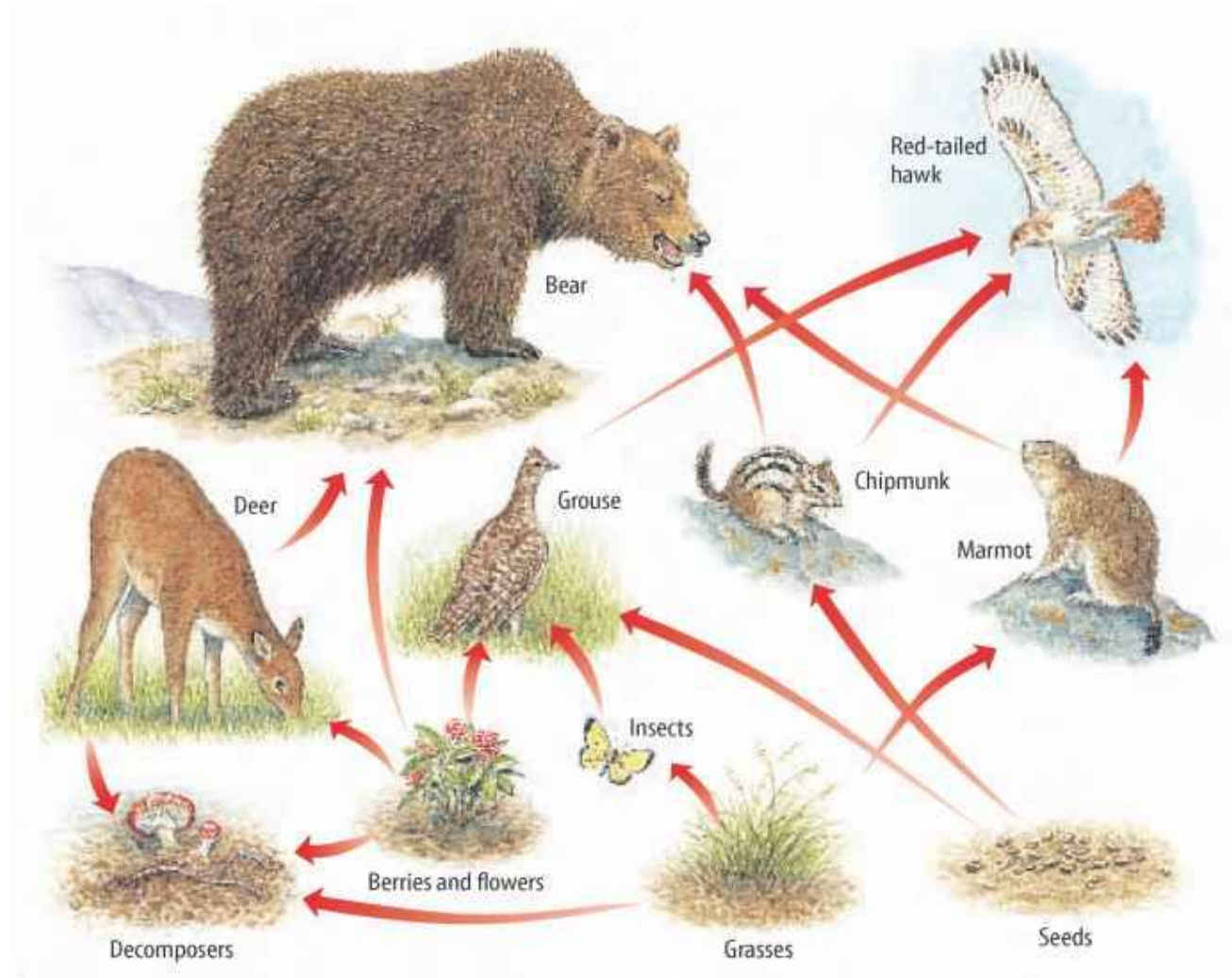
Figure 1. Medians (solid lines) and 95% confidence intervals (dashed lines) for joint estimates of survival ( $\phi$ ) and mean recruits per breeding season ( $\xi$ ) of one-year-old European pied flycatcher (left; *Ficedula hypoleuca*) and white-throated dipper (right; *Cinclus cinclus*) females breeding in Switzerland. The density of the shading corresponds to the density of the posterior distribution.

**These tools have transformed how I do research.**

**I still have a tremendous amount to learn (it's been 3 years)!**

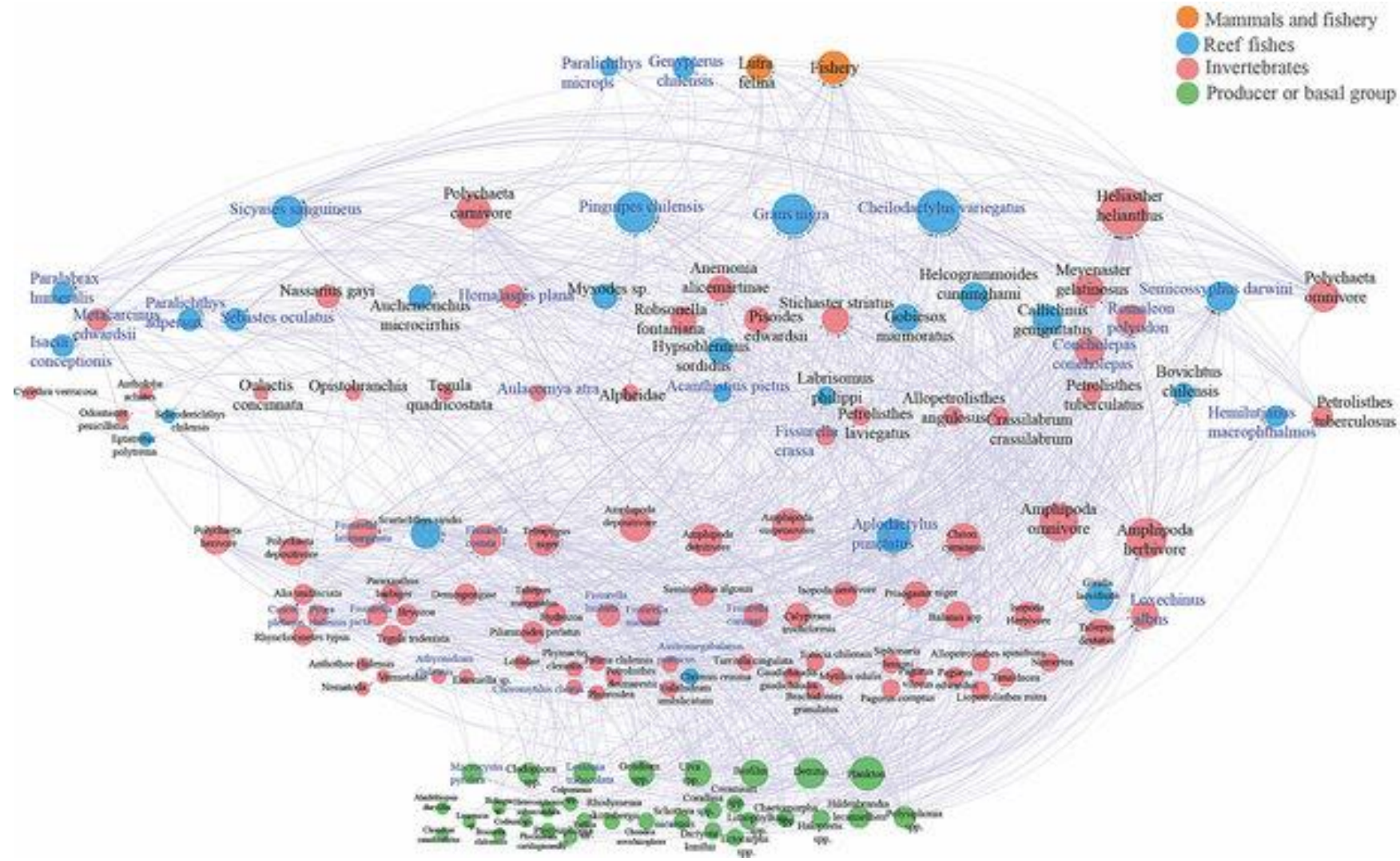


# Ecological systems are complex networks (e.g., food webs)



Your elementary school biology textbook (probably)

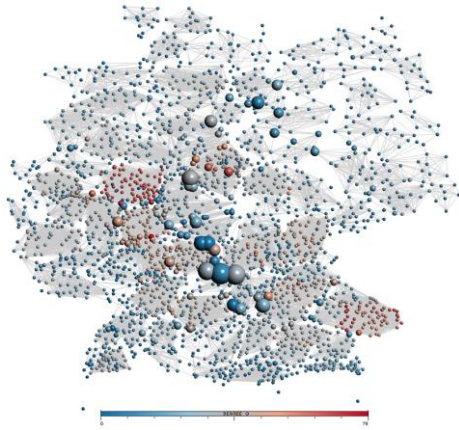
# Ecological systems are complex networks (e.g., food webs)



**Perez-Matus et al. (2017) Marine Ecology Progress Series**



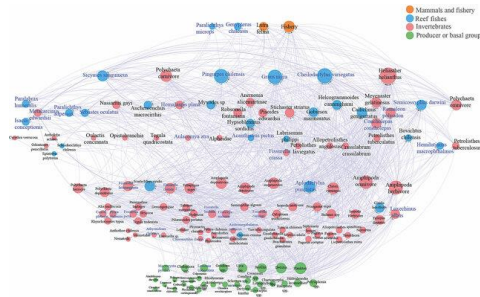
# Ecological systems are unbelievably complex networks...



# Climate network

## Abiotic systems

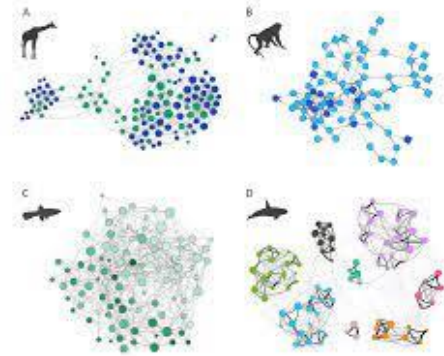
**Tominski et al. (2017)**  
*Information Visualization IV*



# Food Network

## Among populations

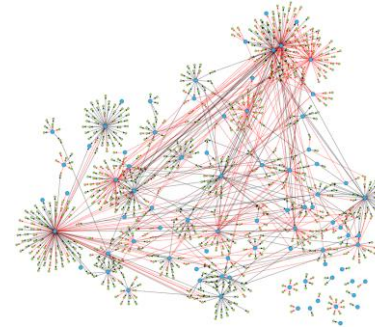
**Perez-Matus et al. (2017)**  
*Marine Ecology Progress Series*



# Social Network

## Within populations

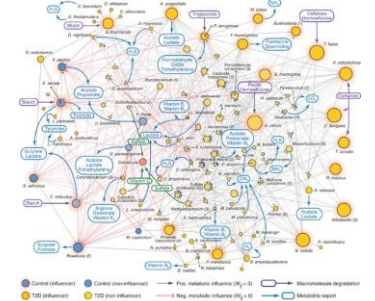
**Brask et al. (2005)**  
*arXiv*



# Gene Network

## Within individuals

**Ma et al. (201)**  
*PLOS ONE*

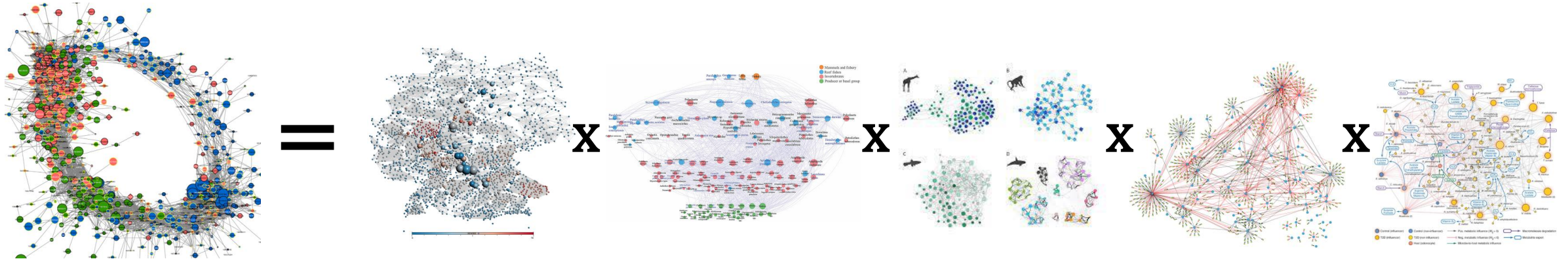


# Microbial Network

### Within individuals

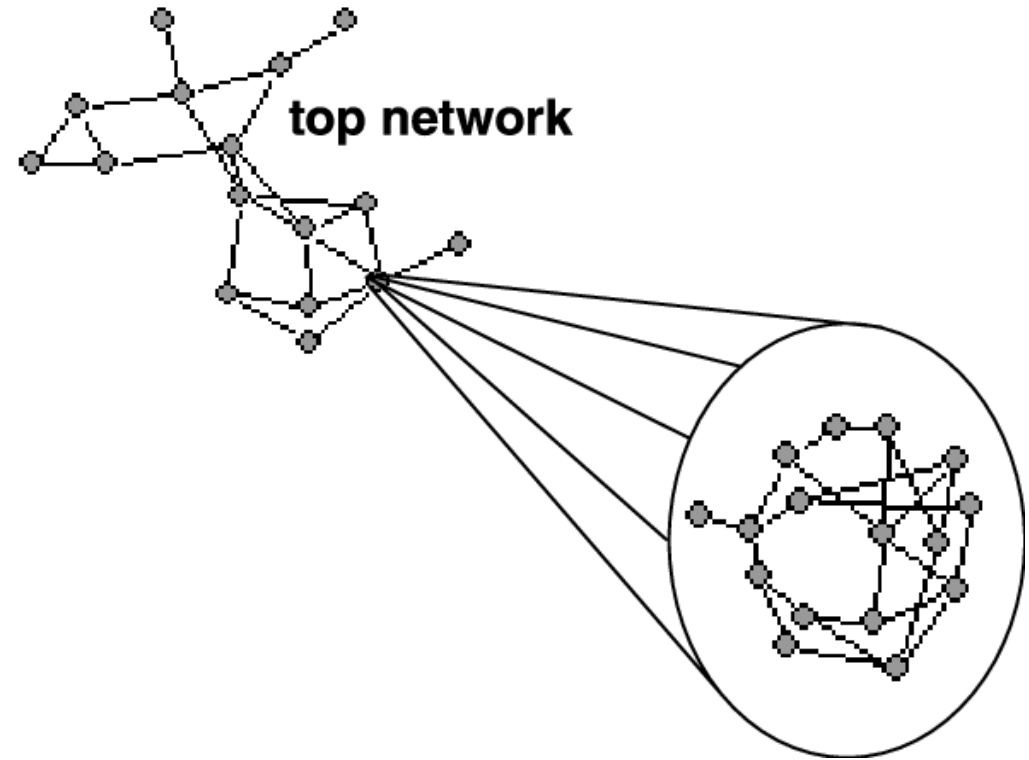
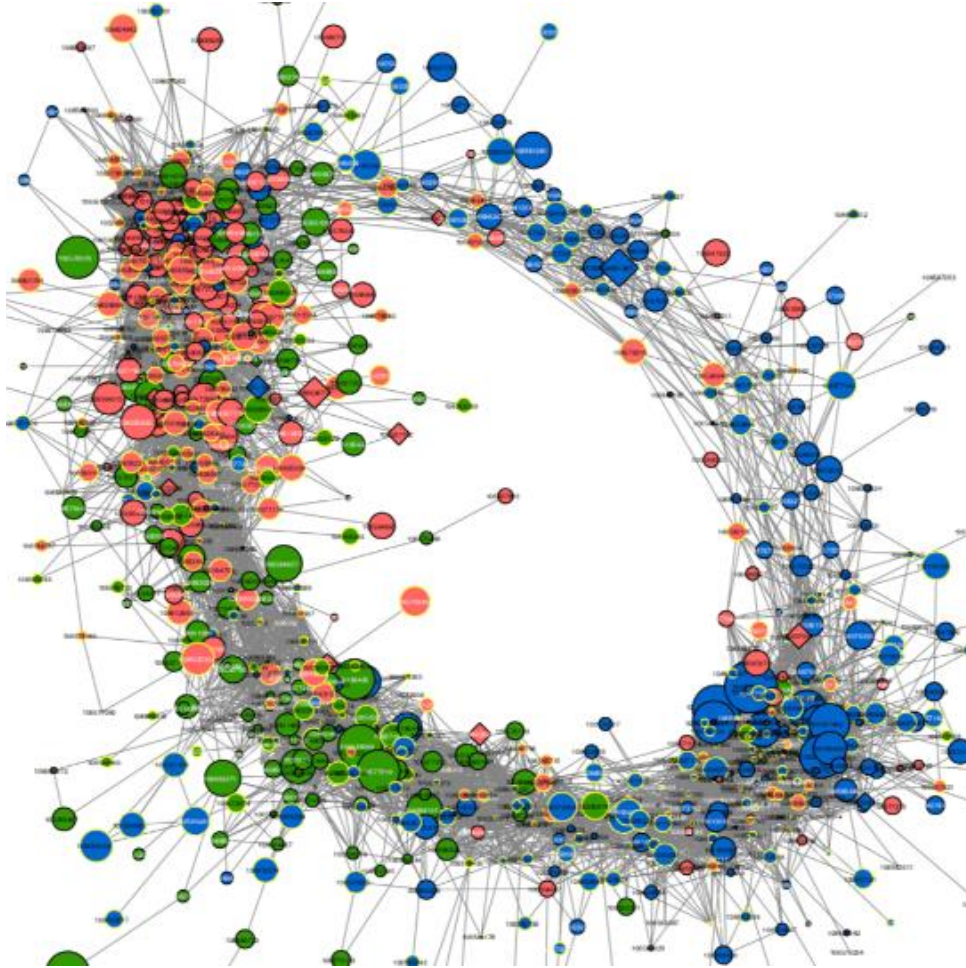
**Sung et al. (2017)**  
*Nature Communications*

# Ecological 'reality' is a complex product of abiotic conditions, community & social dynamics, genetics, & microbial communities



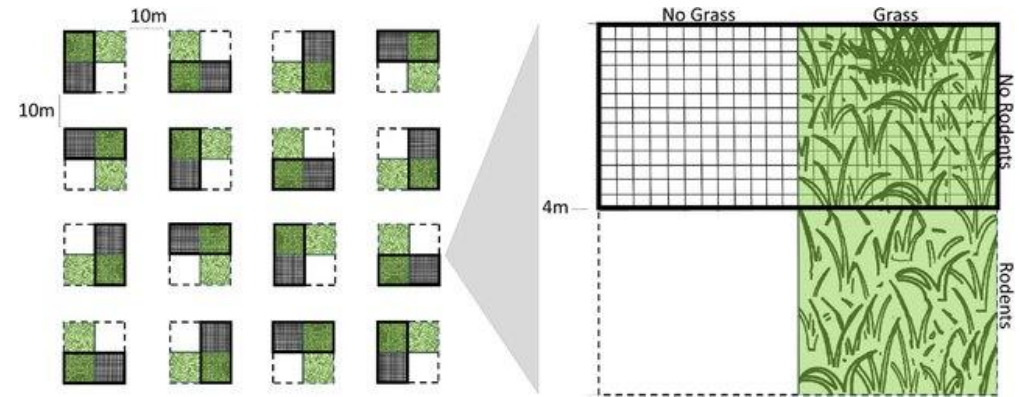
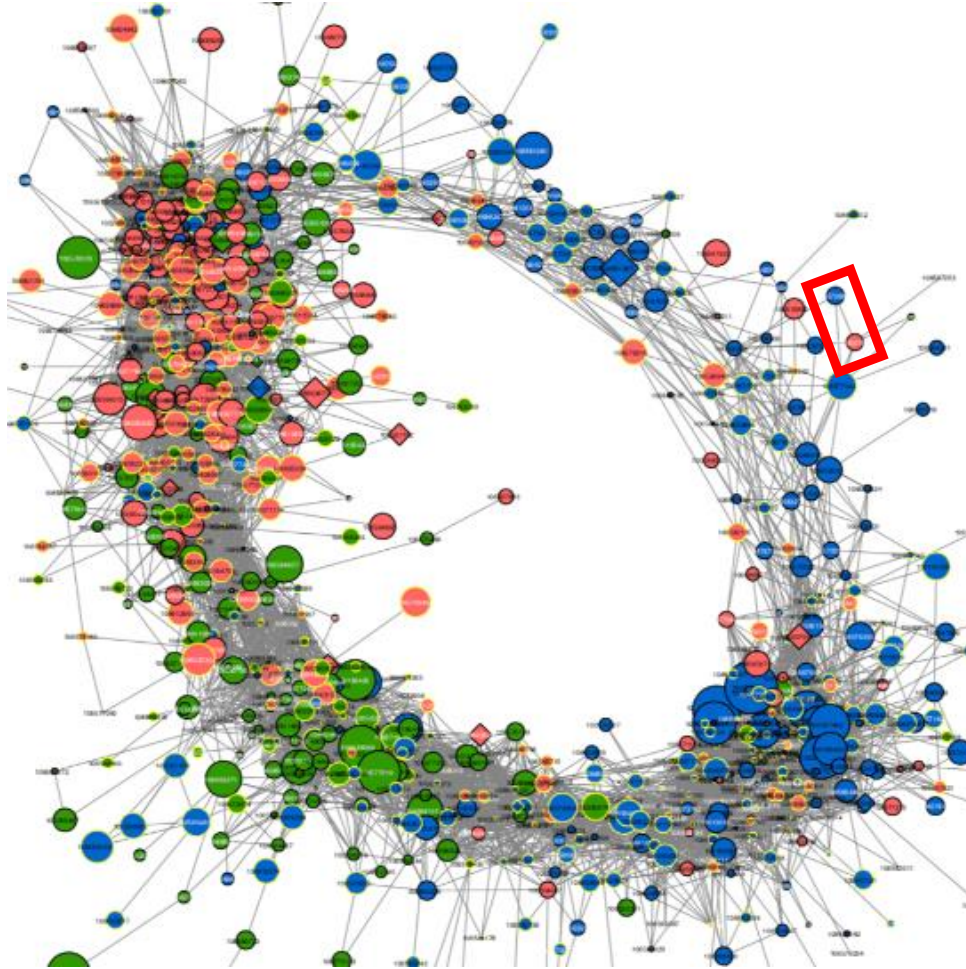
**'Reality'**

# Ecological reality is beyond our comprehension





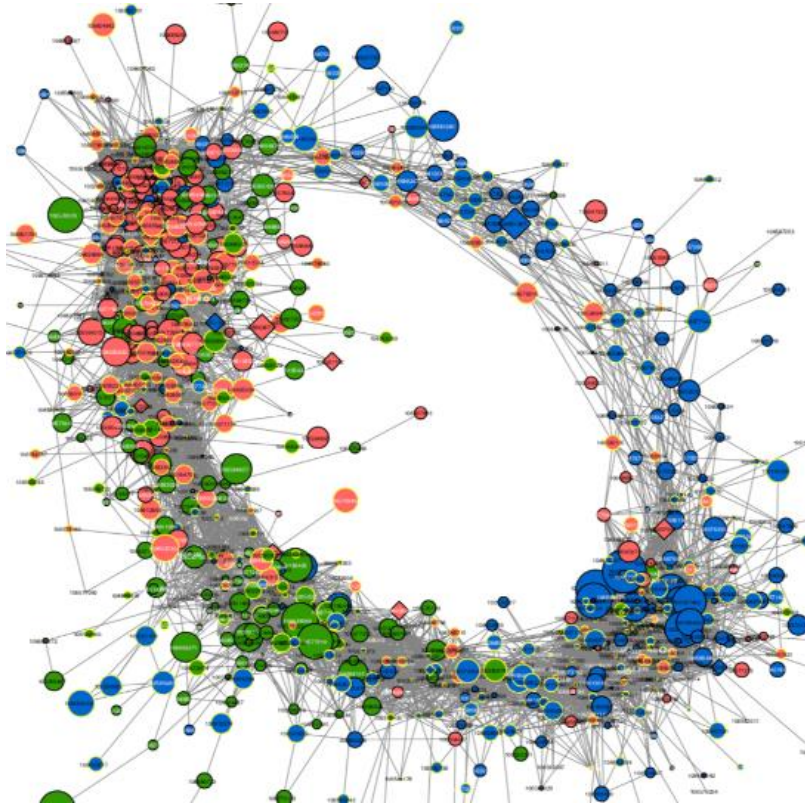
# Science responds to this complexity with experiments



Experiments are beautiful!



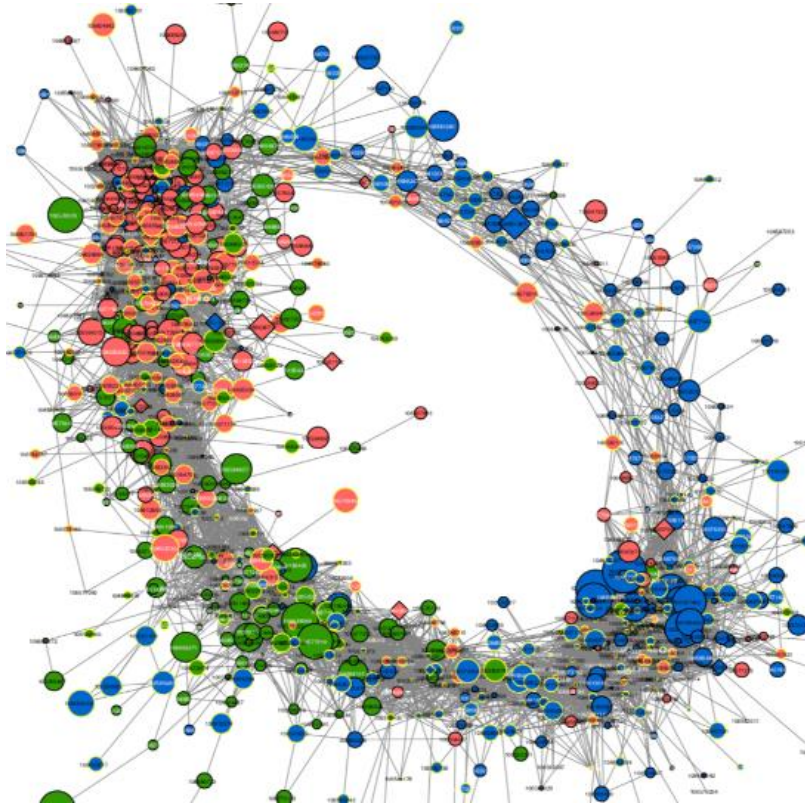
# We can't always do experiments (for myriad reasons)



**Similar problems in other fields (e.g., epidemiology, social sciences)**



# We can never do experiments in the past!

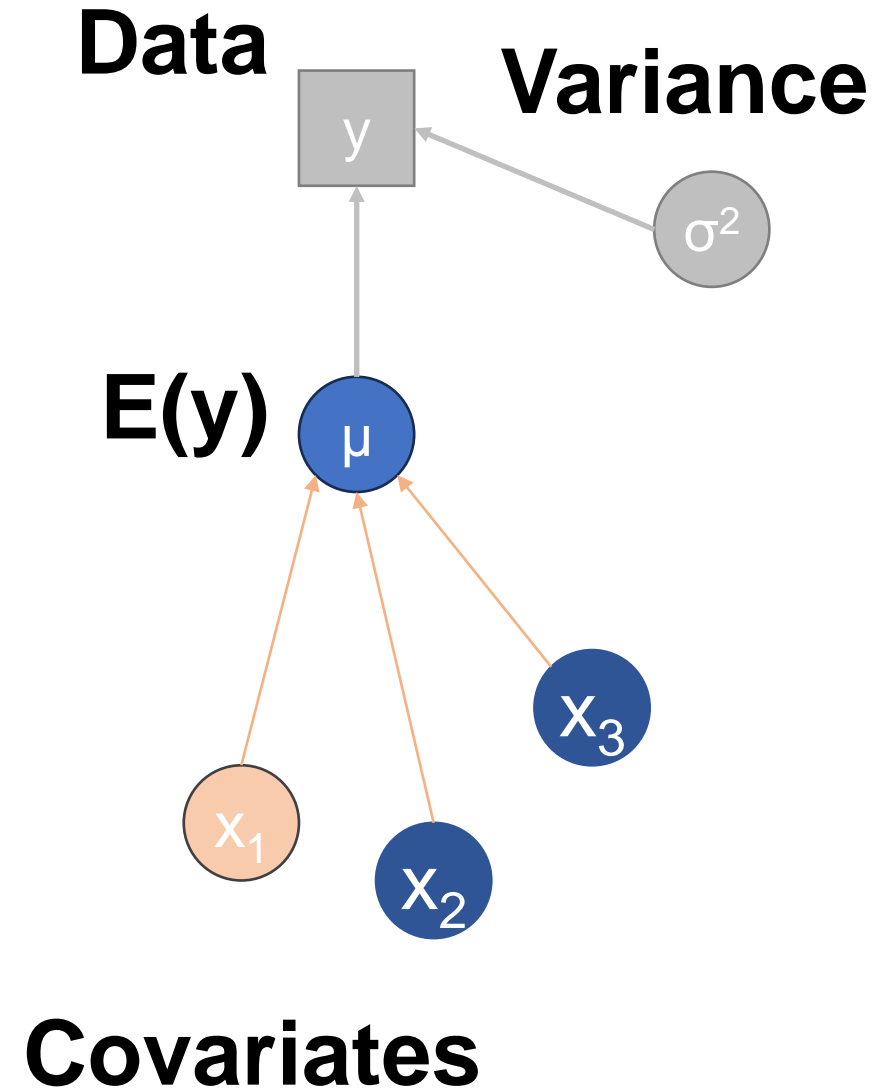
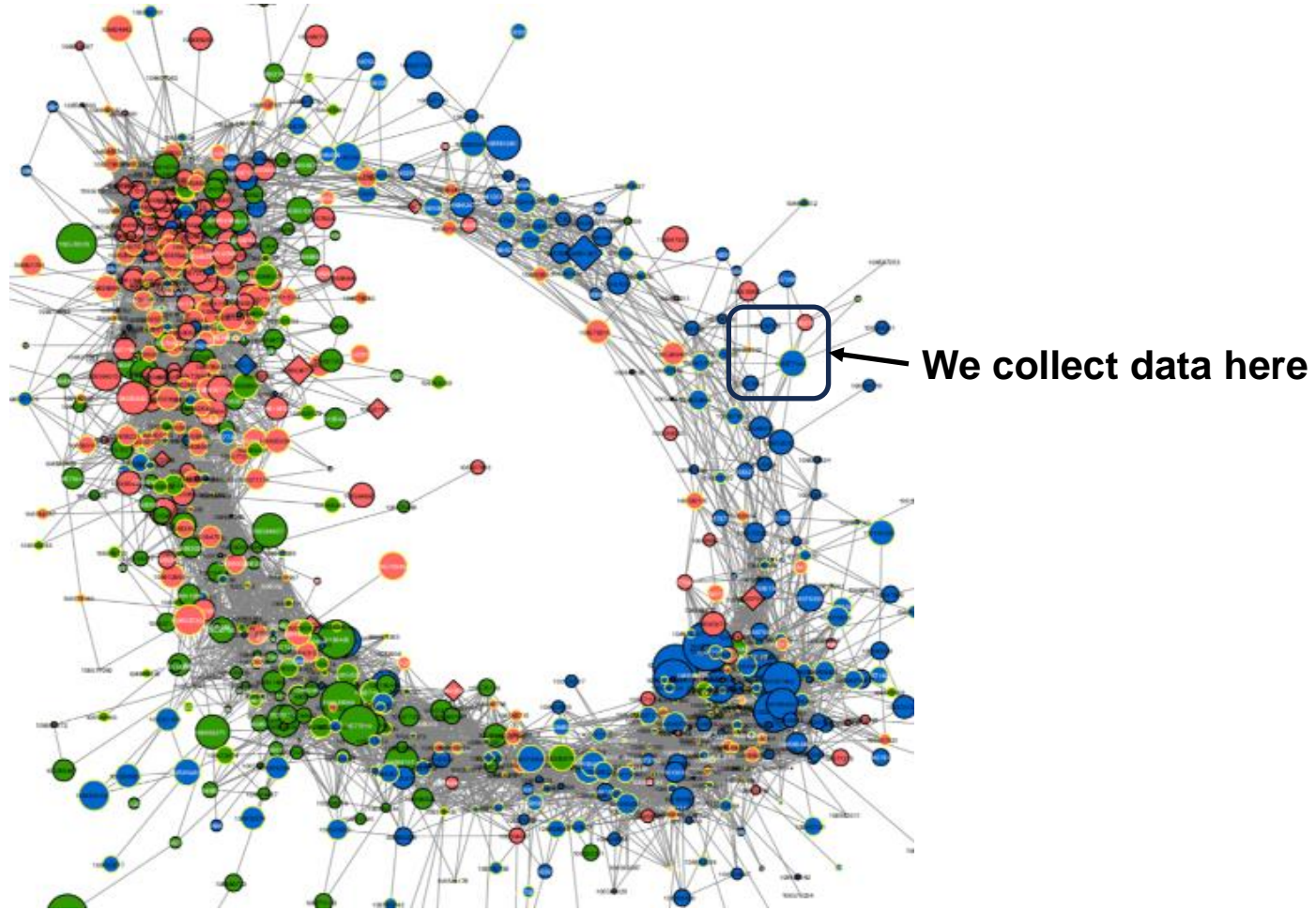


Similar problems in other fields (e.g., epidemiology, social sciences)

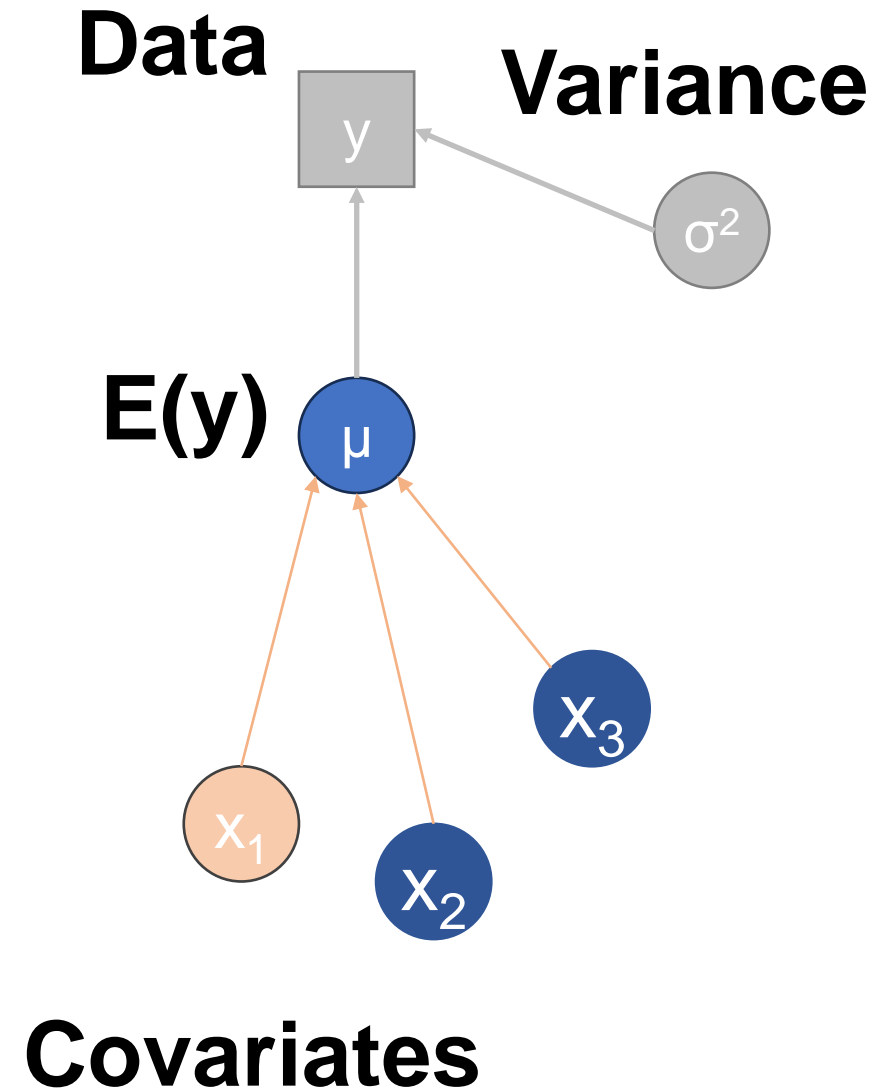
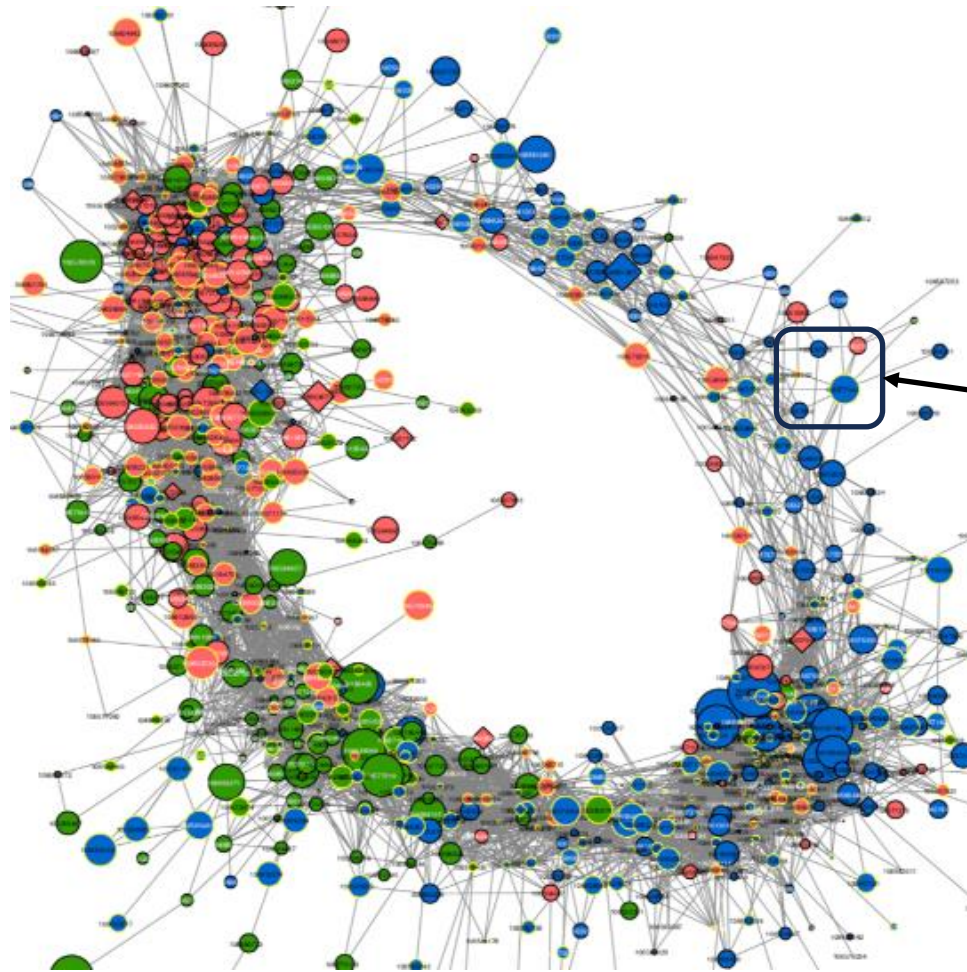


**So what do we do?!**

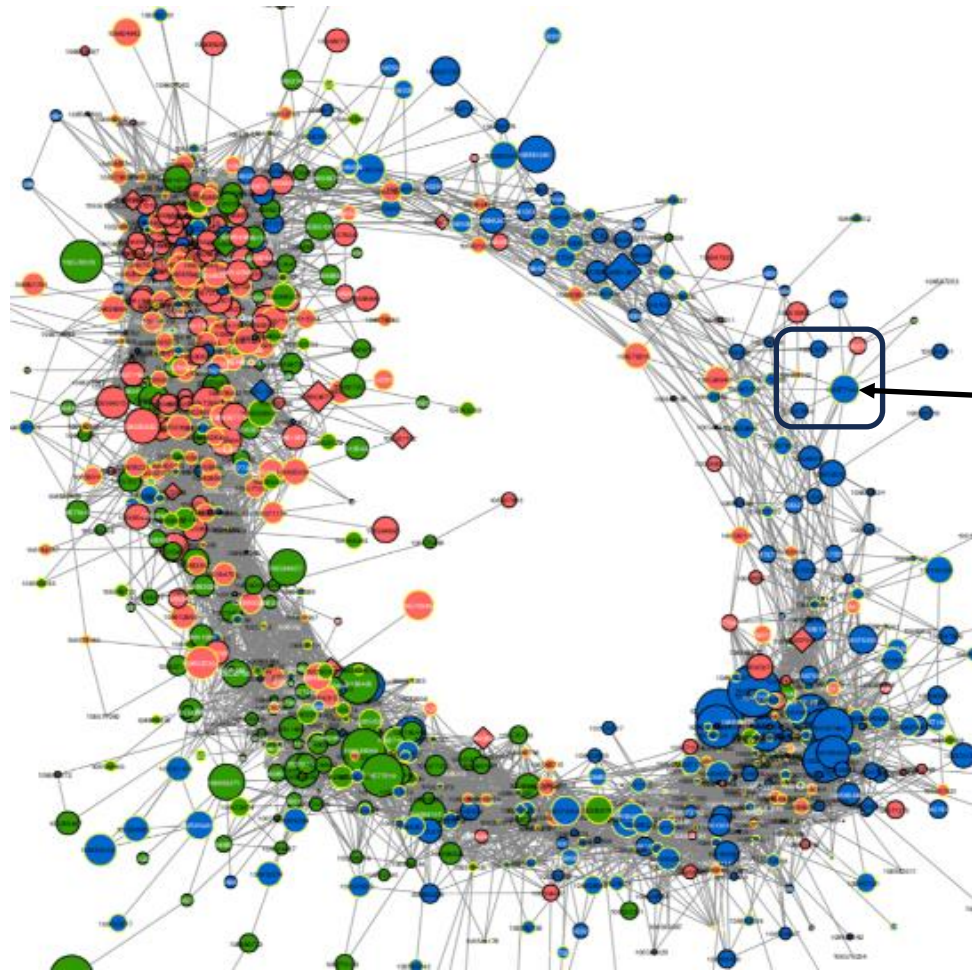
# GLMs dominate observational ecological analyses



# GLMs focus on a single response as a function of covariates



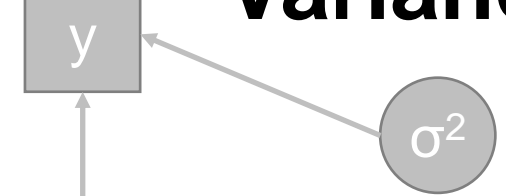
**GLMs focus on a single response (i.e., dependent variable)...**



**Dependent variable**

**Data**

**Variance**



$\mu$

$x_1$

$x_2$

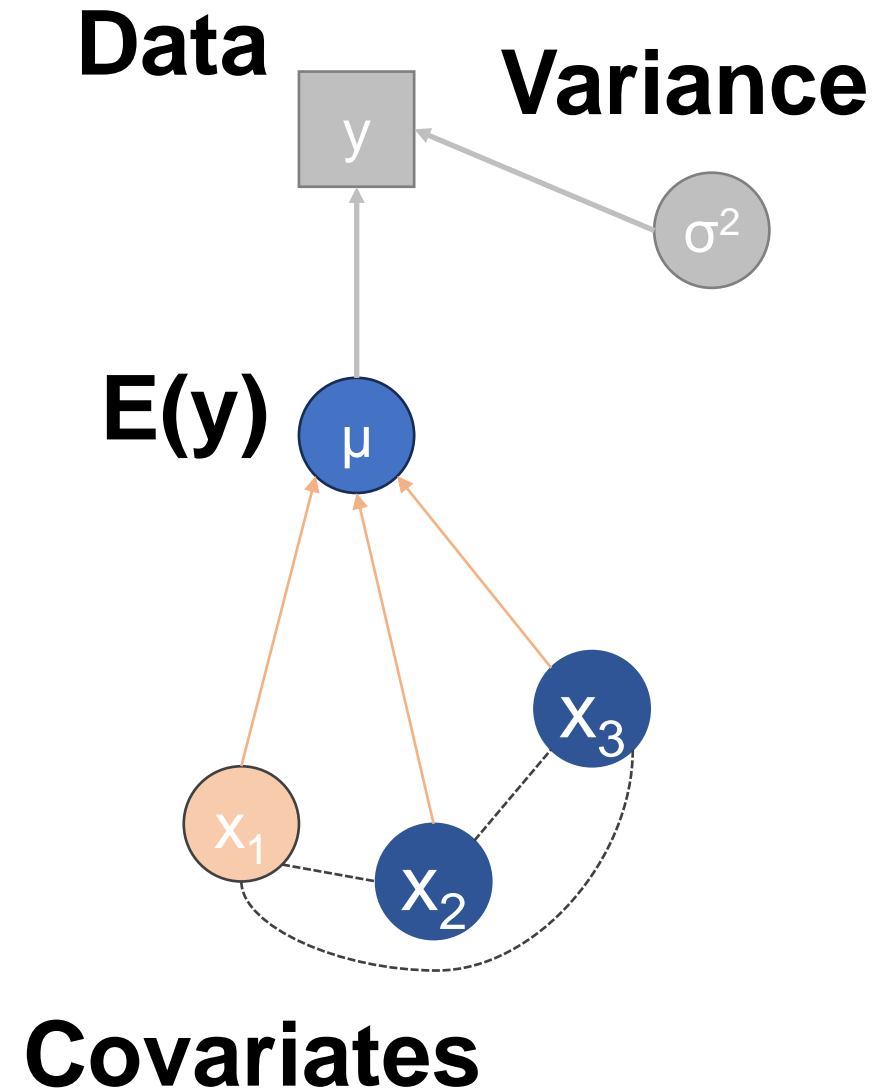
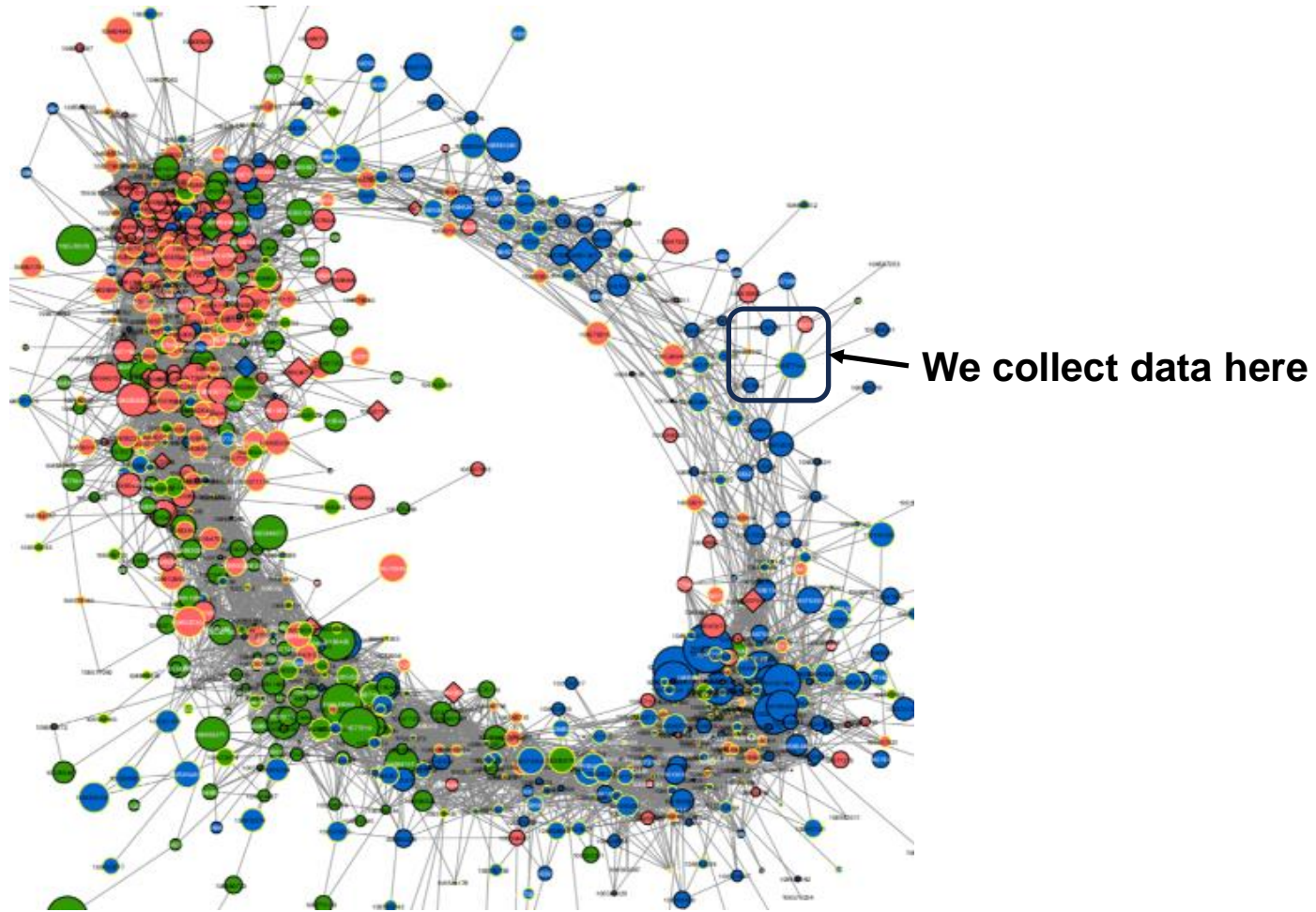
$x_3$

**Independent variables**

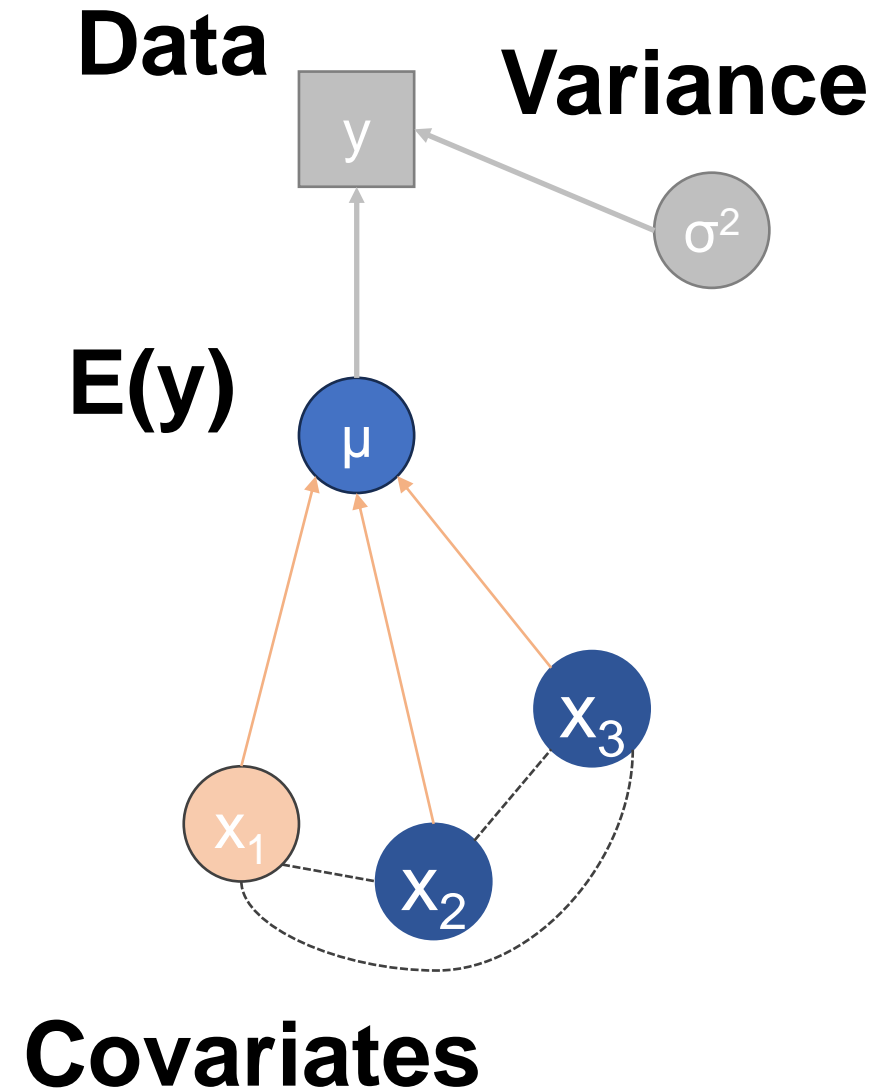
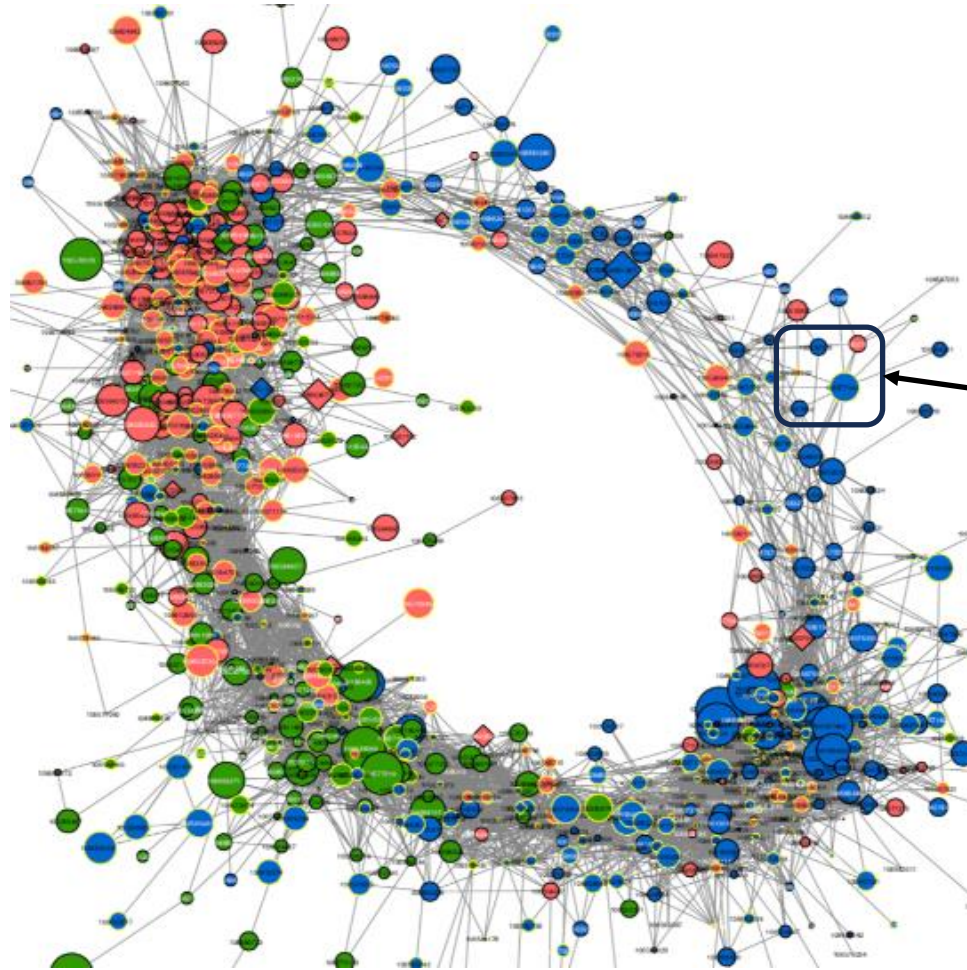
**as a function of covariates (i.e., independent variables)**



Covariates are often connected, or collinear (NOT 'independent')

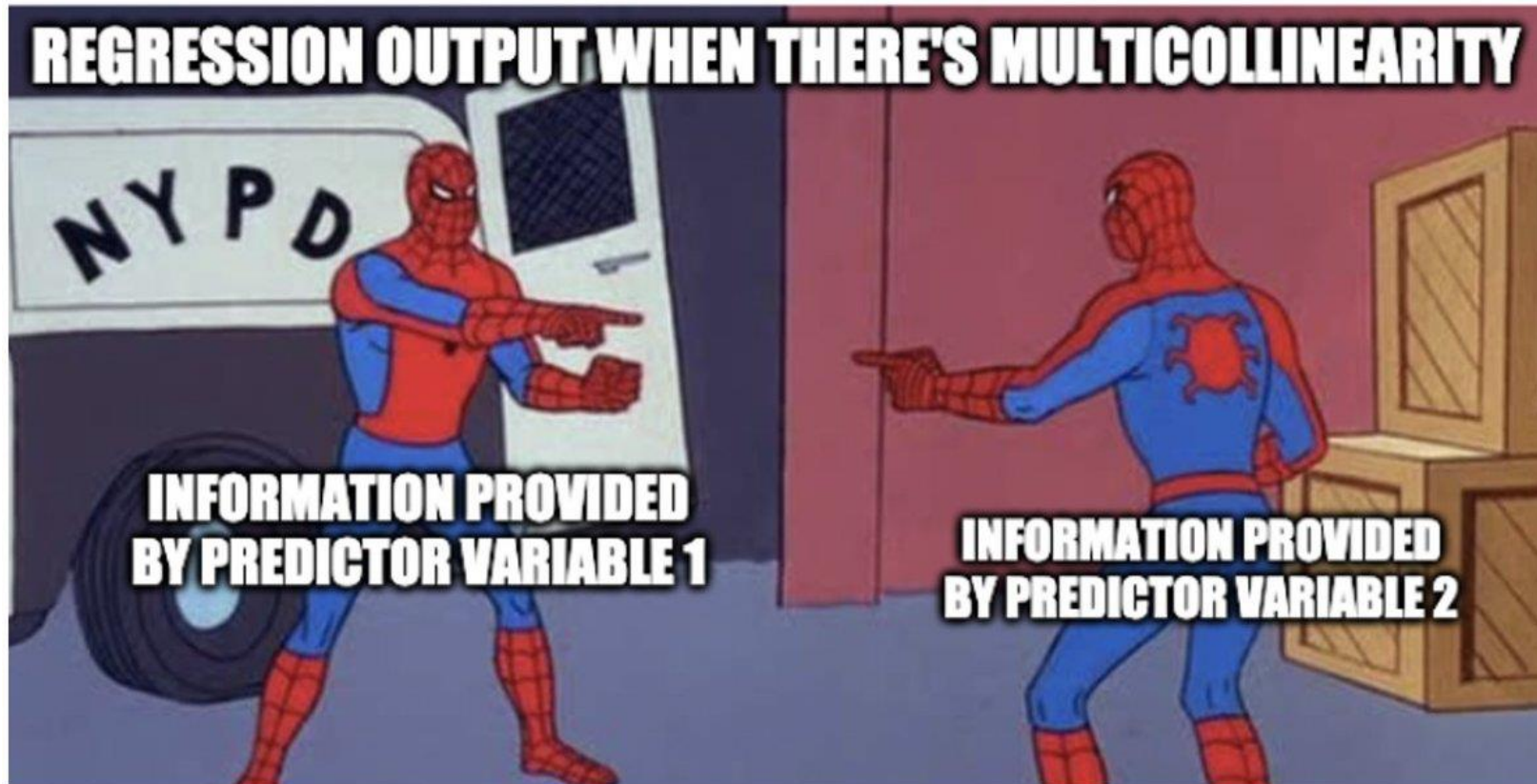


# Multicollinearity is a major 'problem' in ecological analysis



**How many of you have had to exclude collinear ( $r > 0.7$ ) covariates?**

Why did you do that?



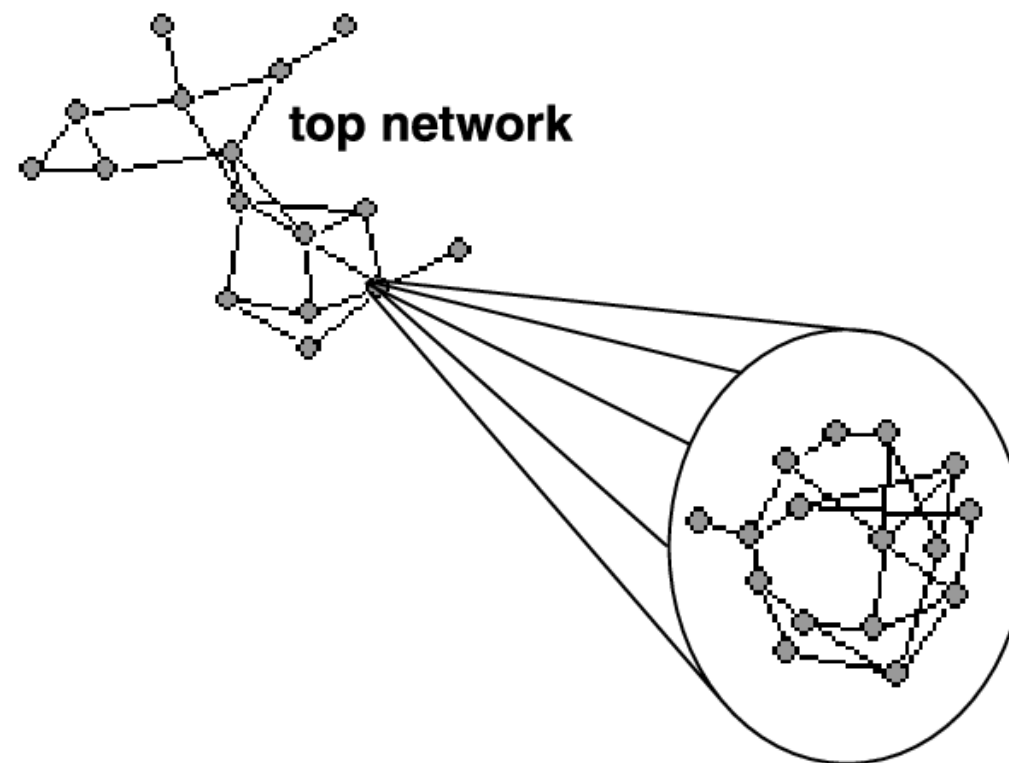
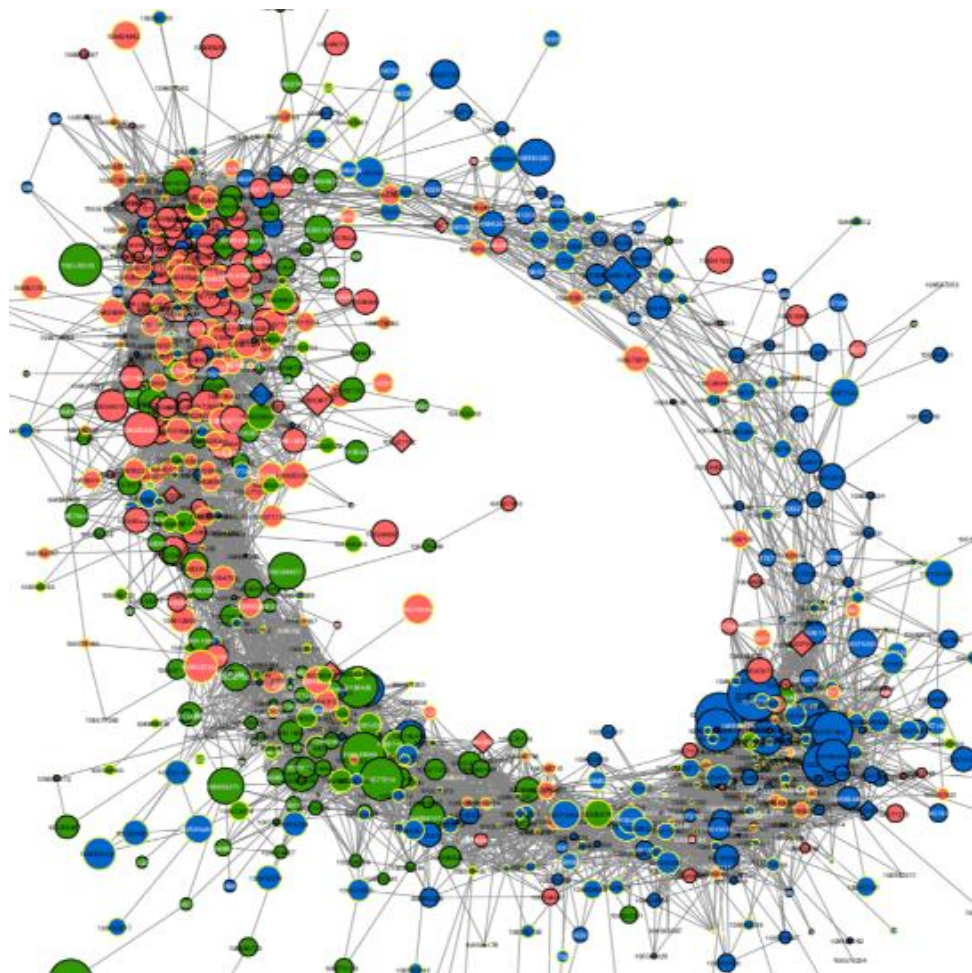


## How did you exclude covariates?

- *a priori*
- test which fit 'best' (i.e., 'iterative' model selection?)
- haphazardly?
- $r = 0.694...$  it's fine!

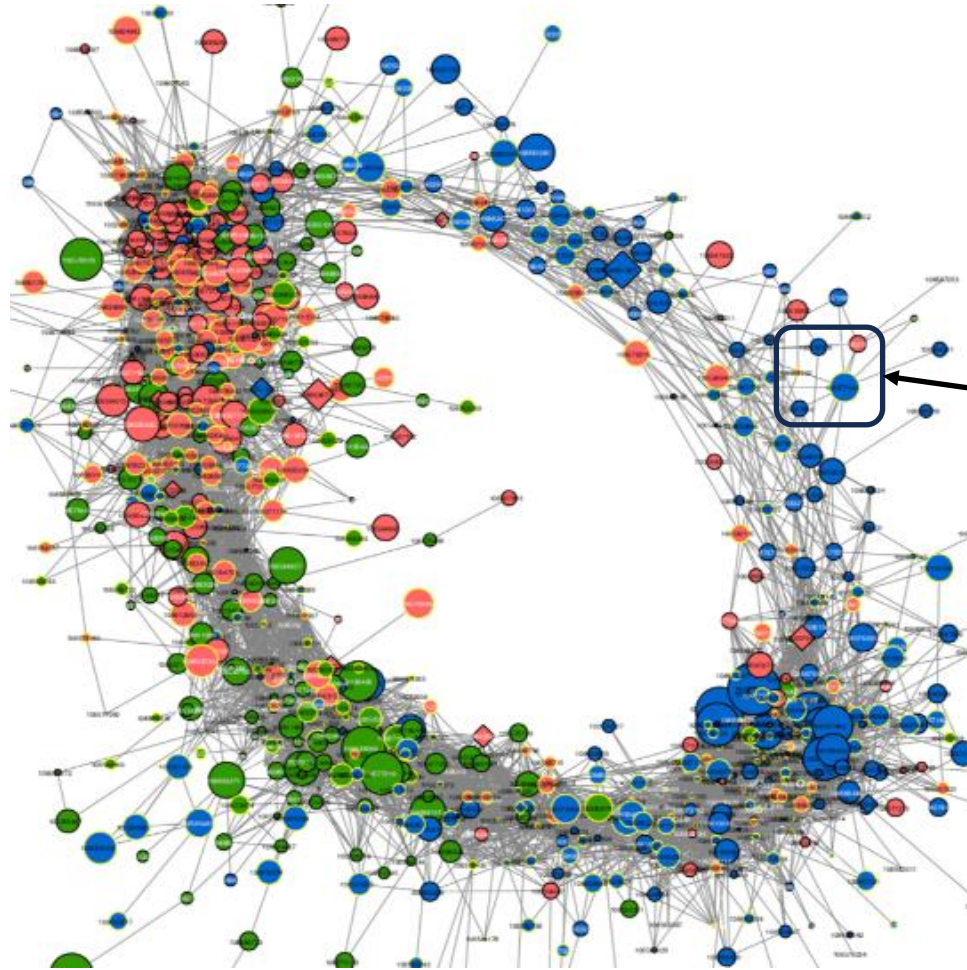
**How many of you felt 'good' about throwing away data?**

# So what do we do?

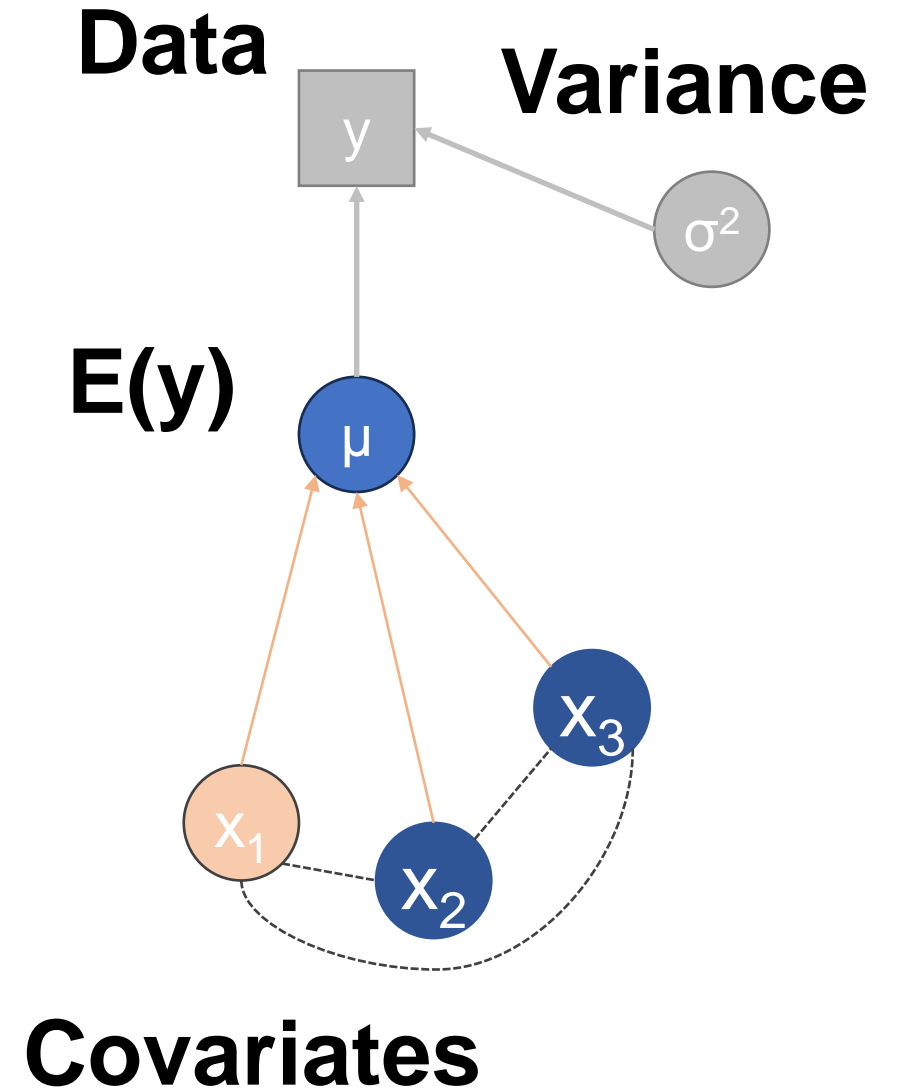


**Why were they collinear?**

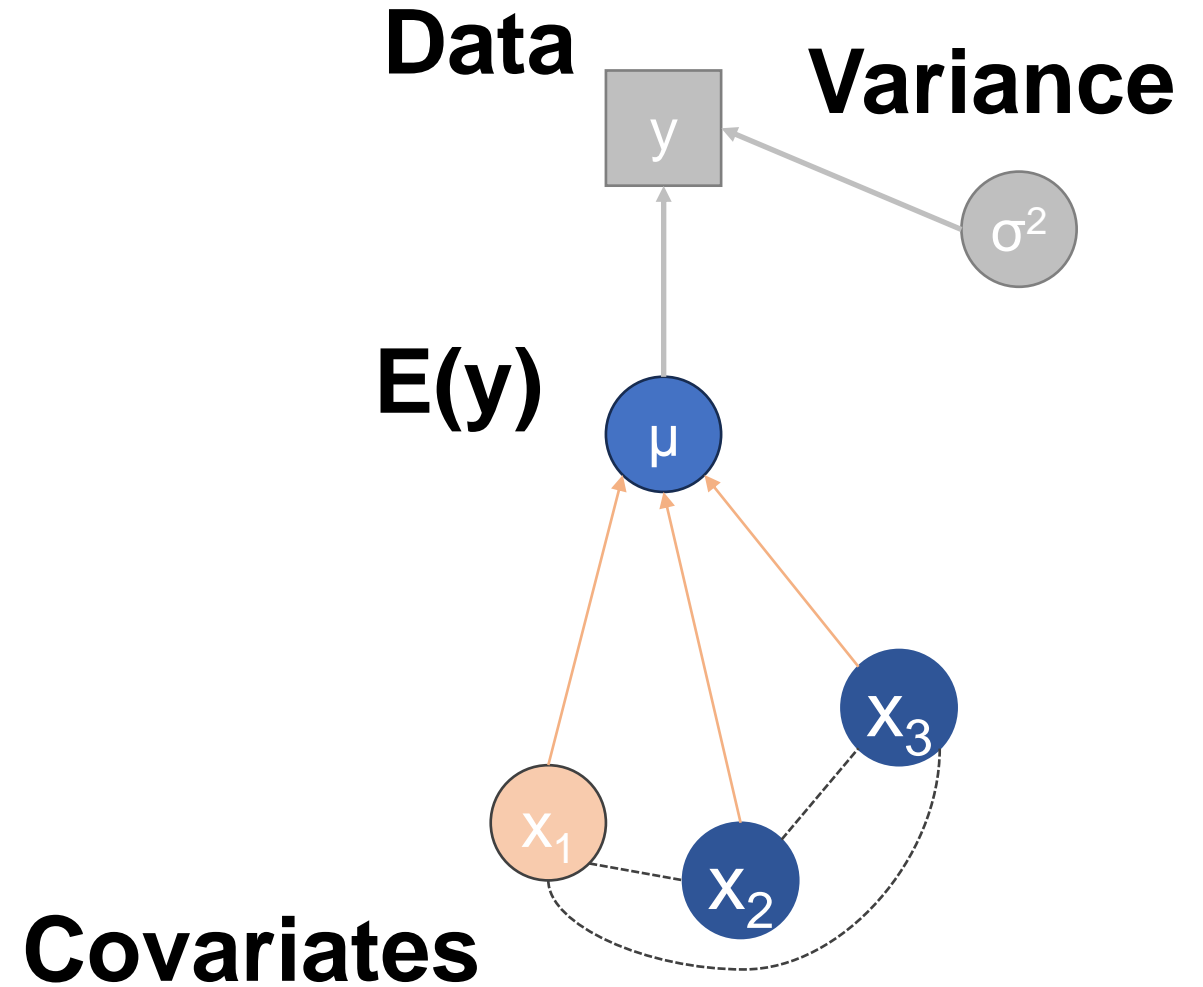
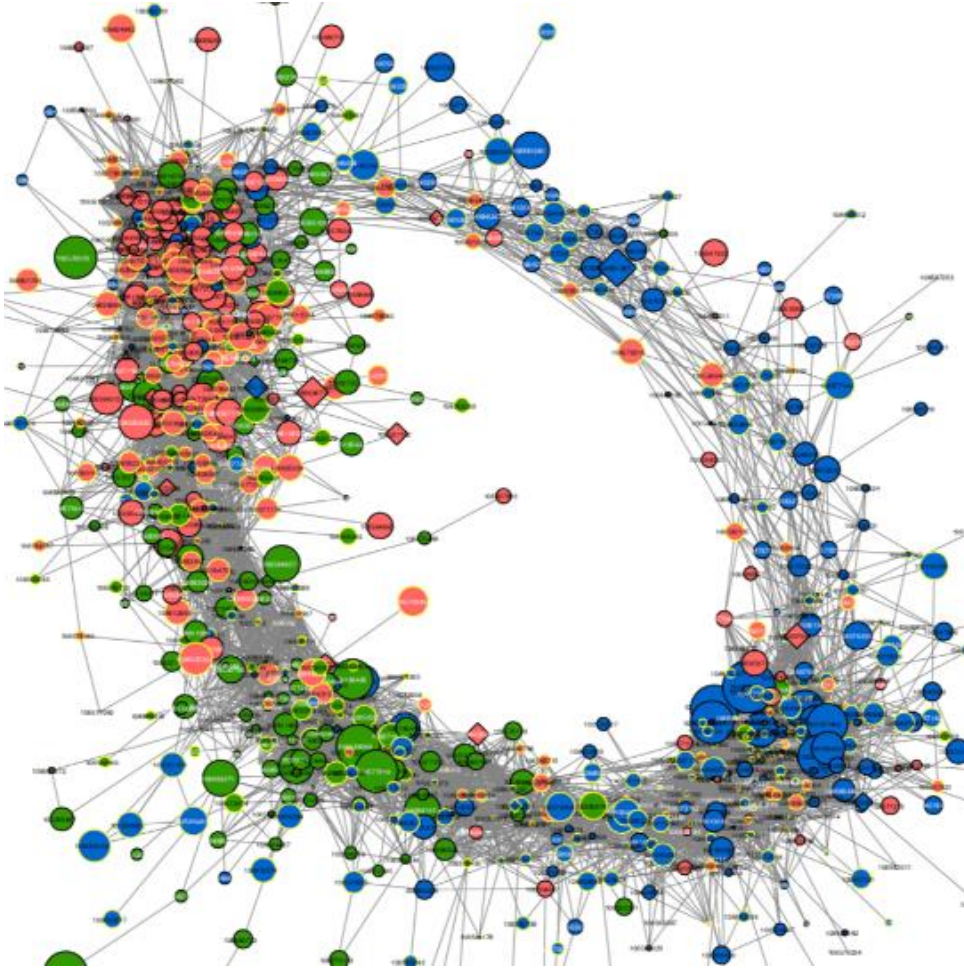
# Why were they collinear? The motivating problem!



We collect data here



***All models are wrong, but some are useful – GC Box***



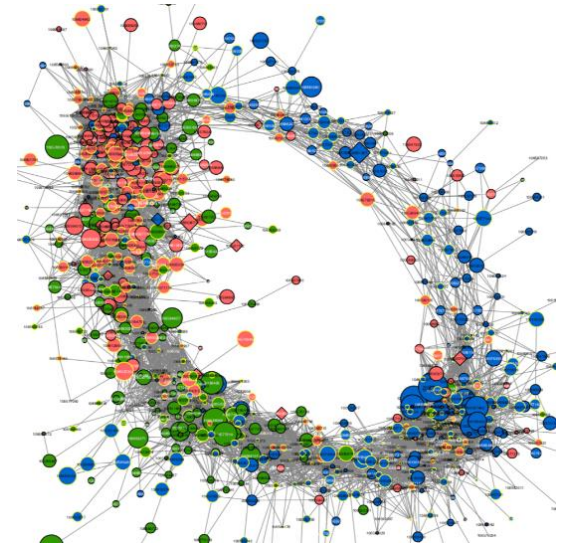
***No models are right, and most are useless – TW Arnold***

# Why were they collinear?

- 1) One affects the other
- 2) They're both a result of an underlying latent process
- 3) ~~'random'?~~



The key idea for this class...



Can we model that\* instead of pleading ‘multicollinearity’?

*\*No. Not in it's entirety, reality is far too complicated for us to begin to comprehend*

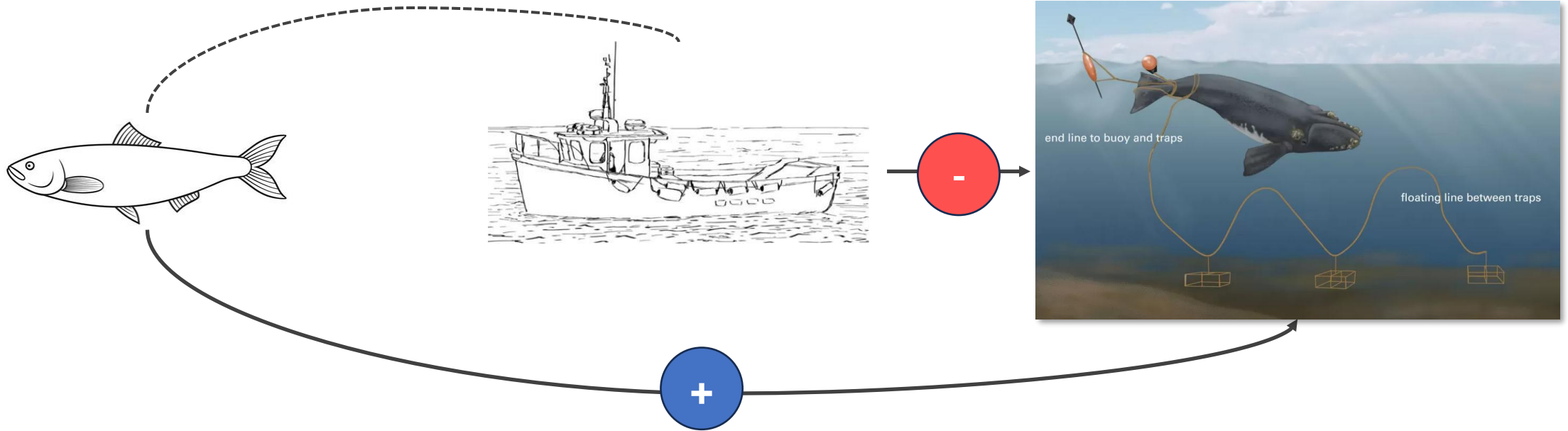


**We can do better...**

**The 'intellectual leap' is to be able to think about more than one response variable at a time**

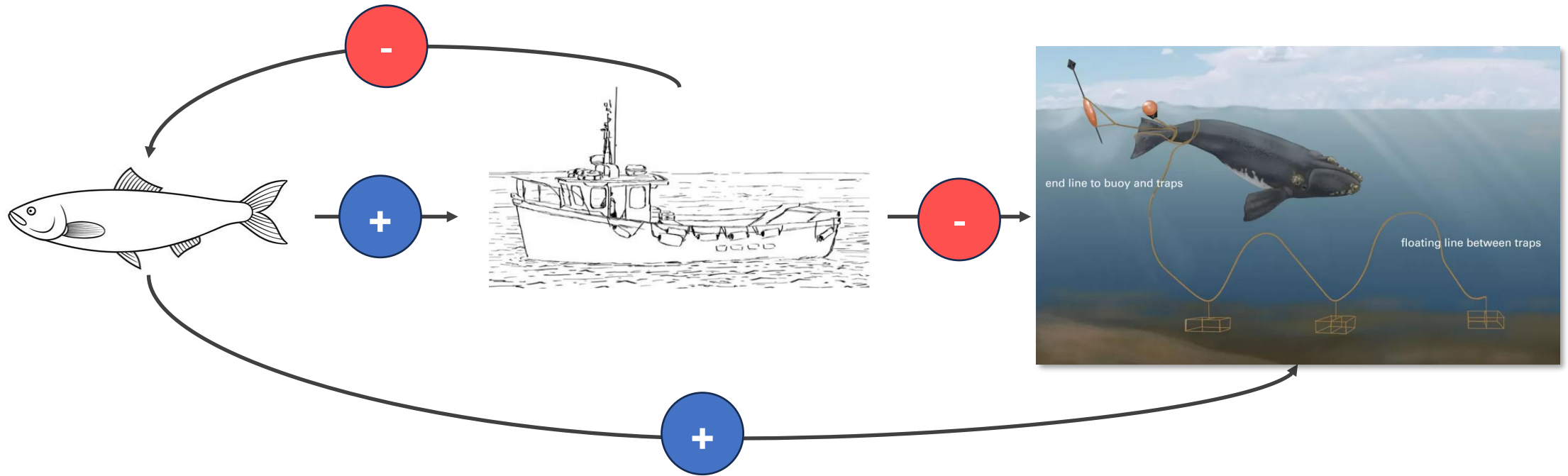
**i.e., more than one variable will 'depend' on other variables...**

# GLM problem



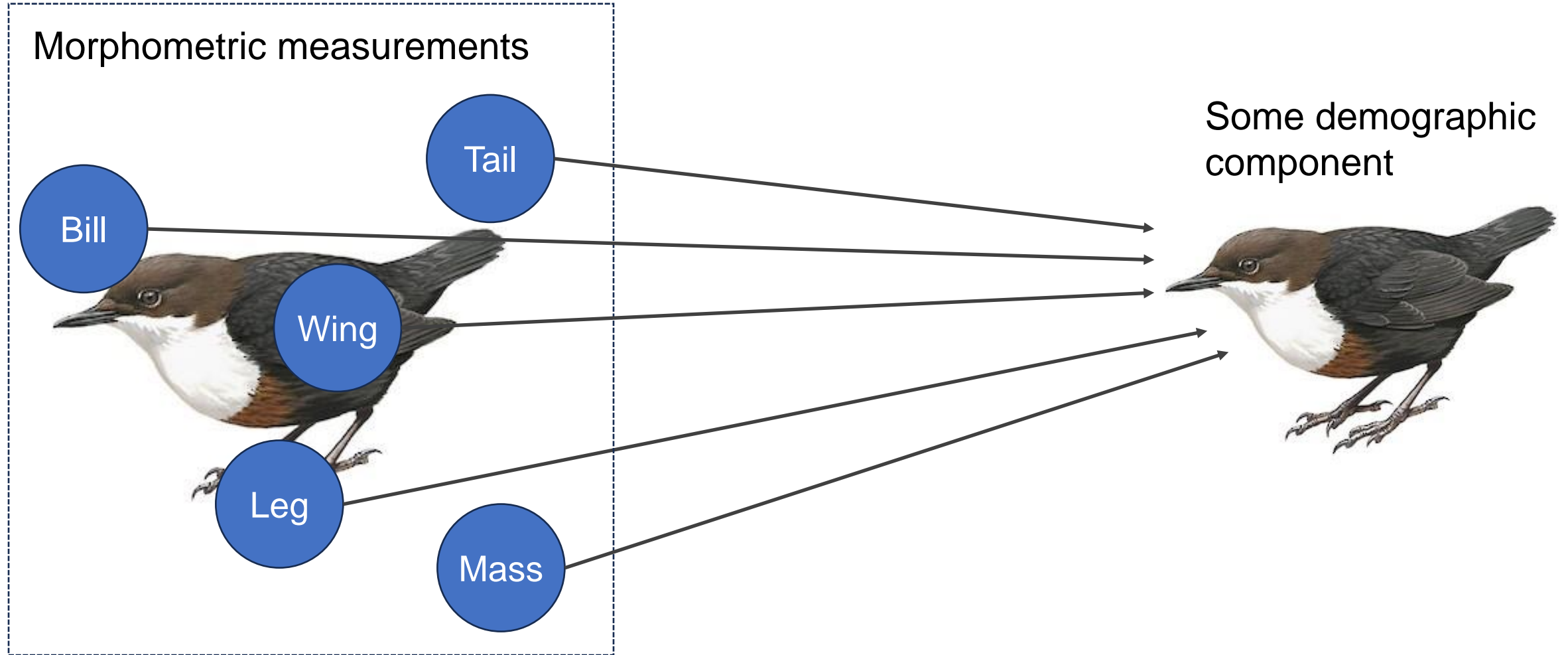
**Fish and fishing are collinear because they affect each other**

# ‘Path analysis’ solution



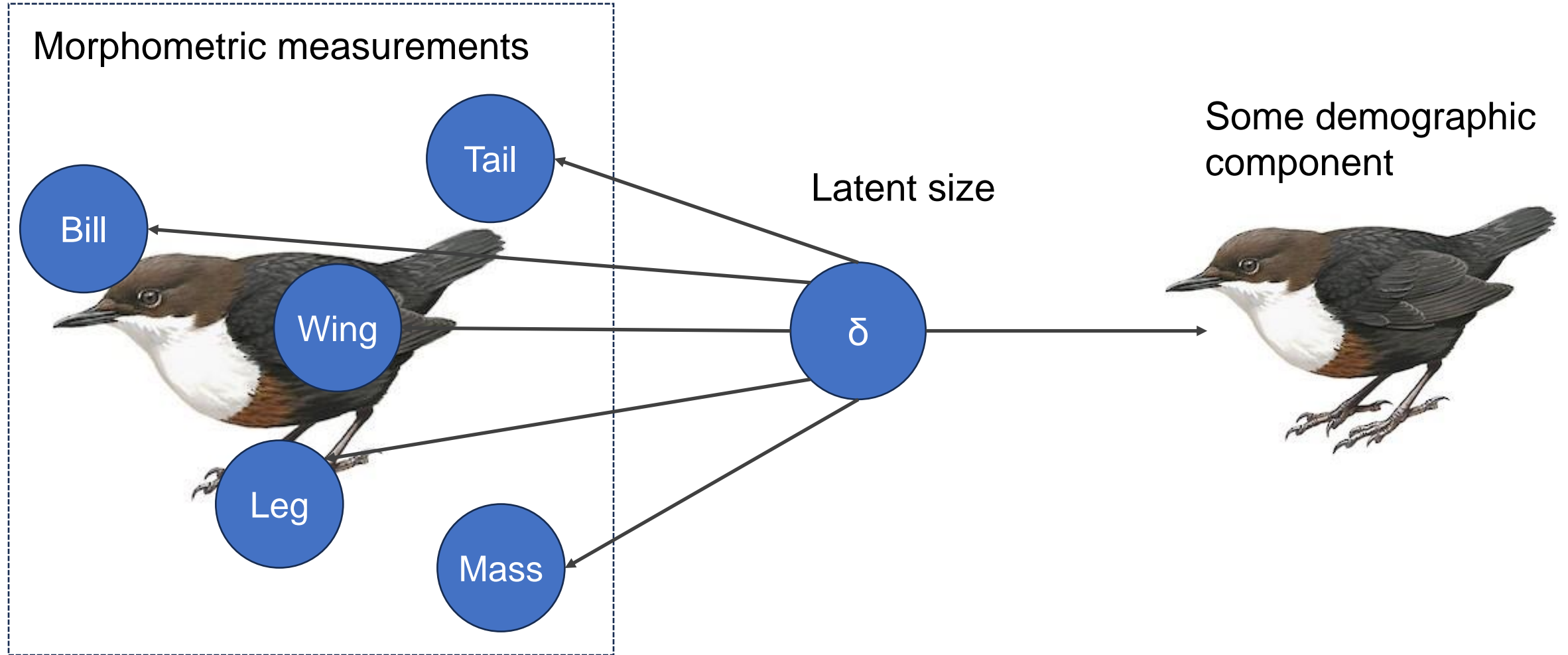
**We can explicitly model those relationships**

# Structural equation model (when covariates arise from a latent process)



**These are all measurement of different aspects of 'size'**

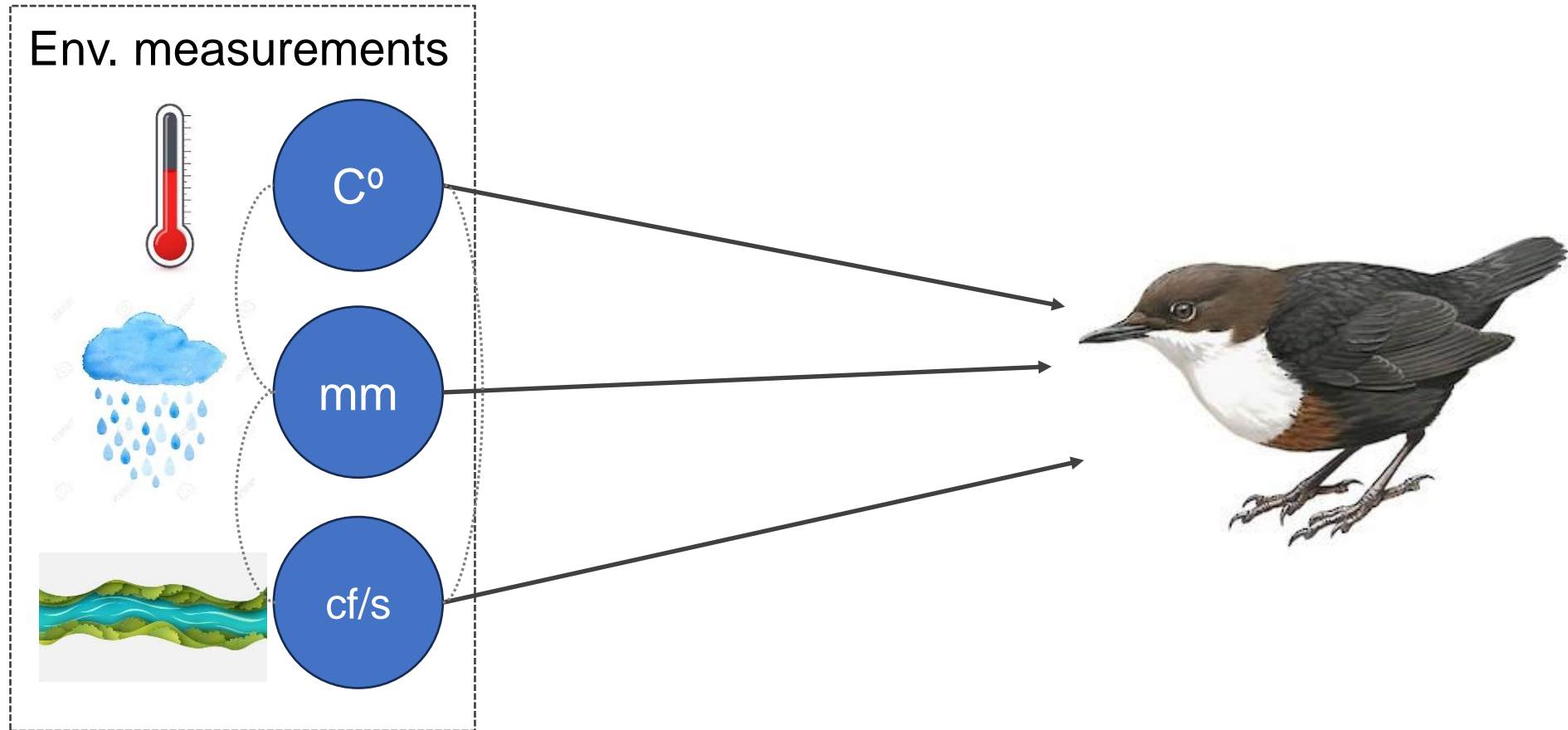
# Structural equation model (when covariates arise from a latent process)



**These are all measurement of different aspects of 'size'**

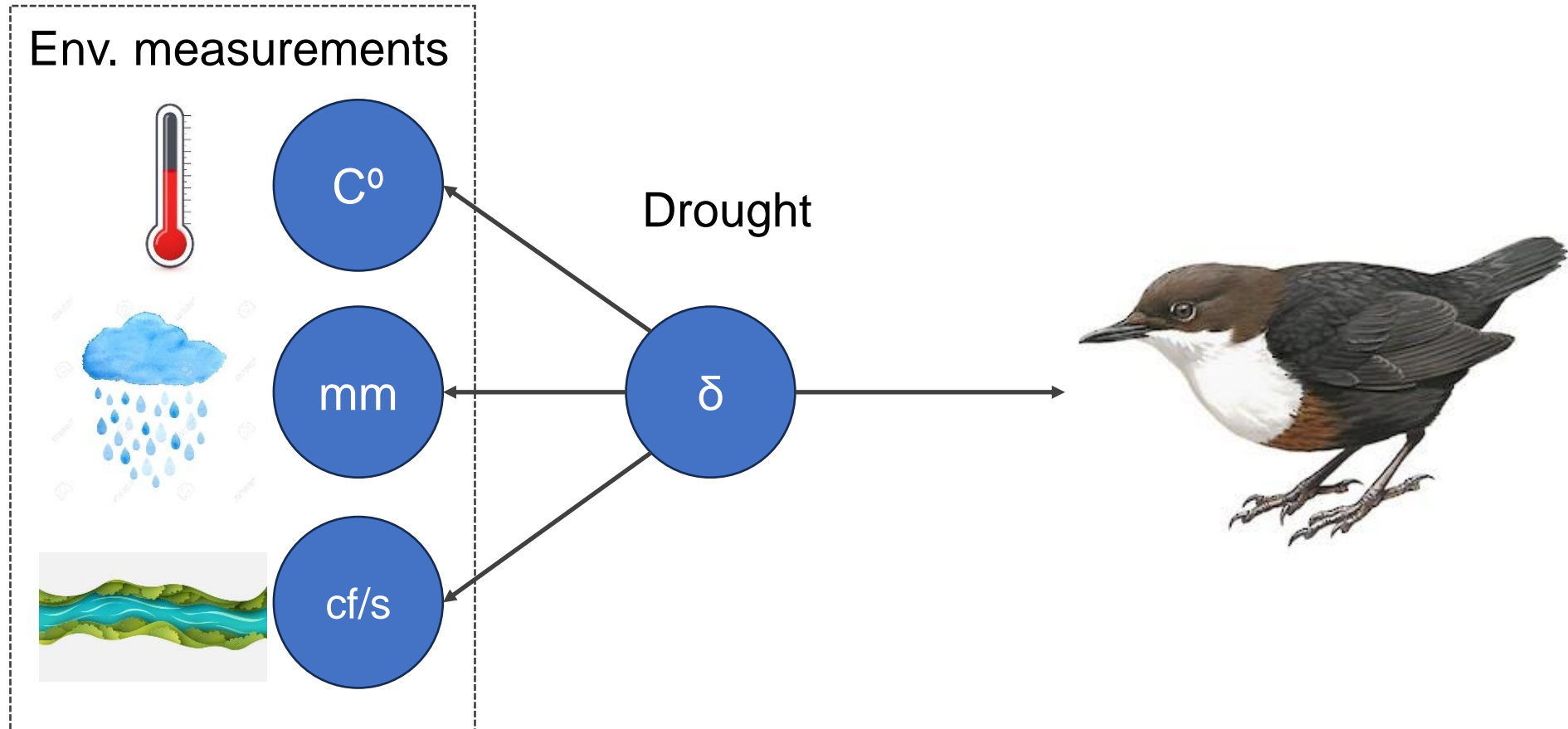


# Structural equation model (when covariates arise from a latent process)



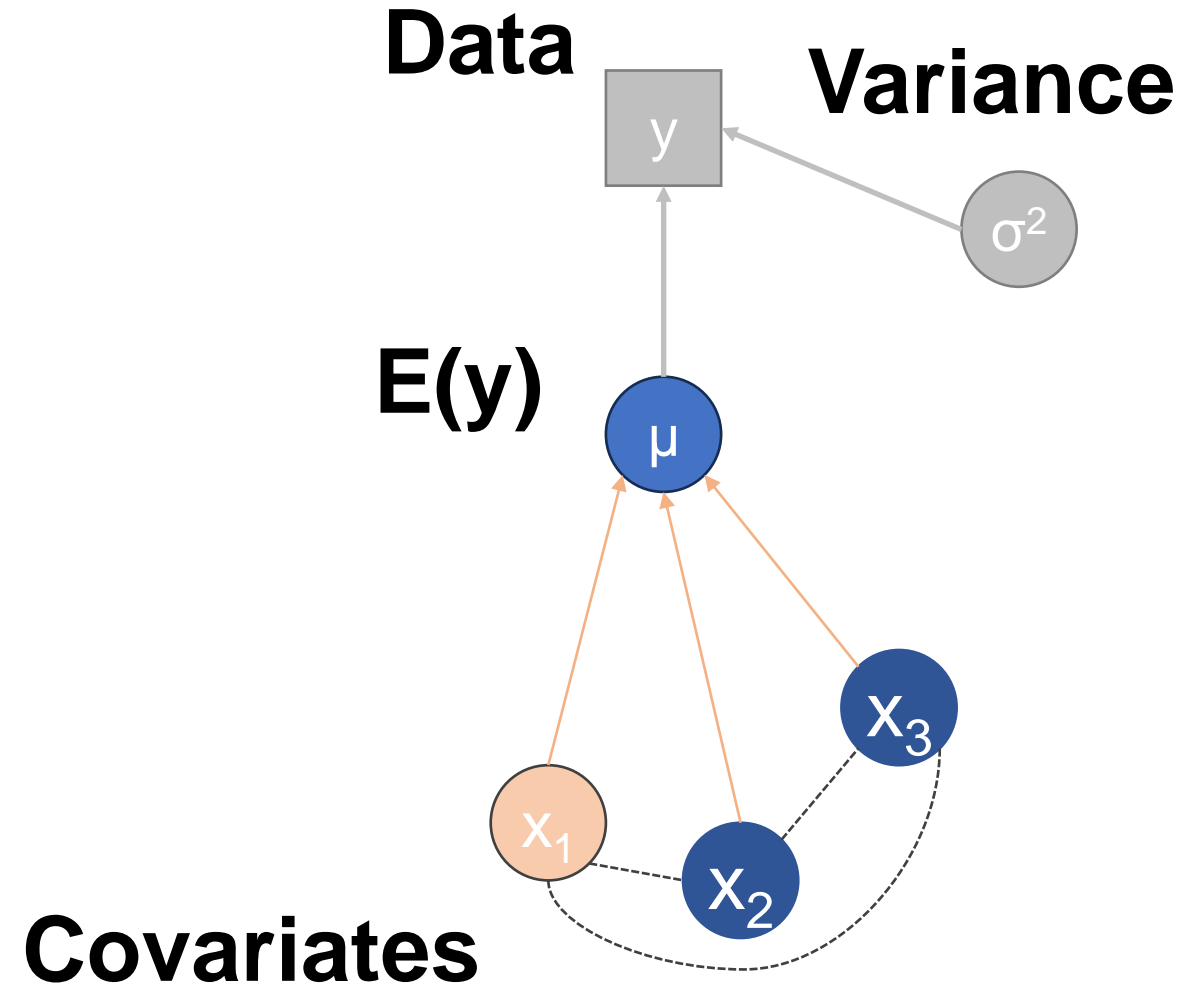
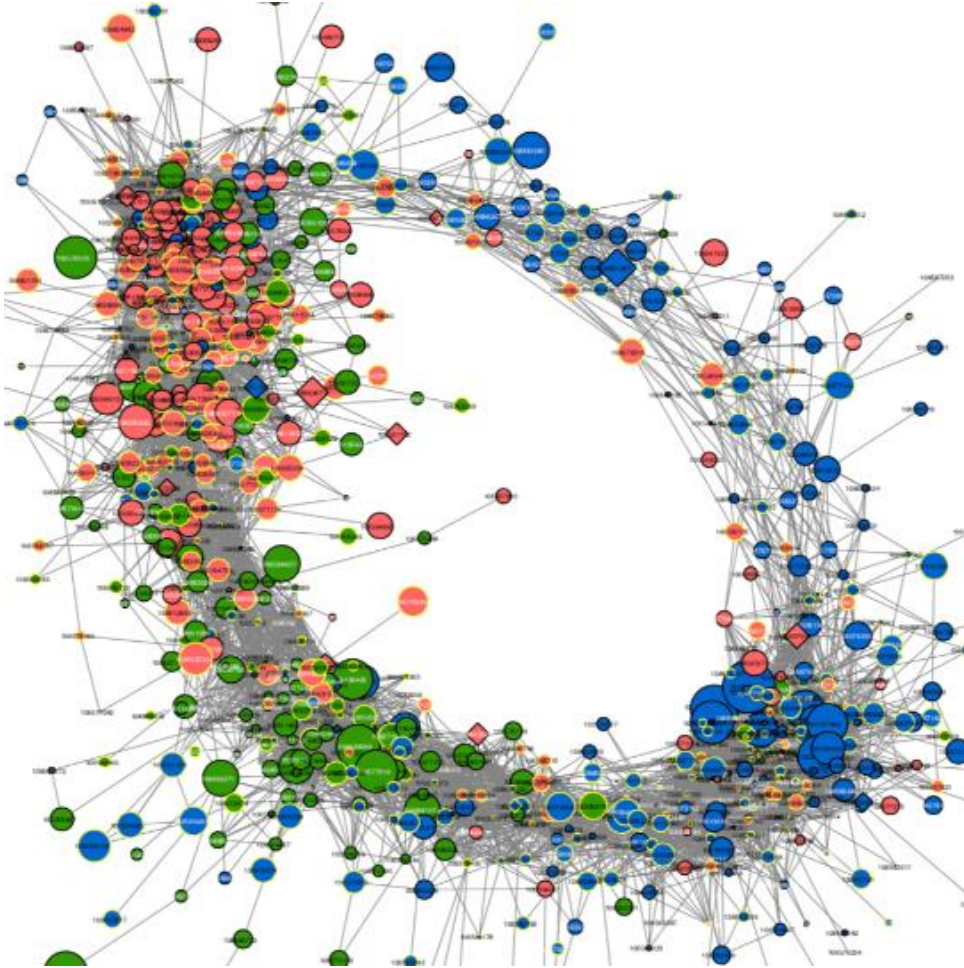
Flow rate, precipitation, and temperature as measurements of hot/dry v. cool/wet

# Structural equation model (when covariates arise from a latent process)



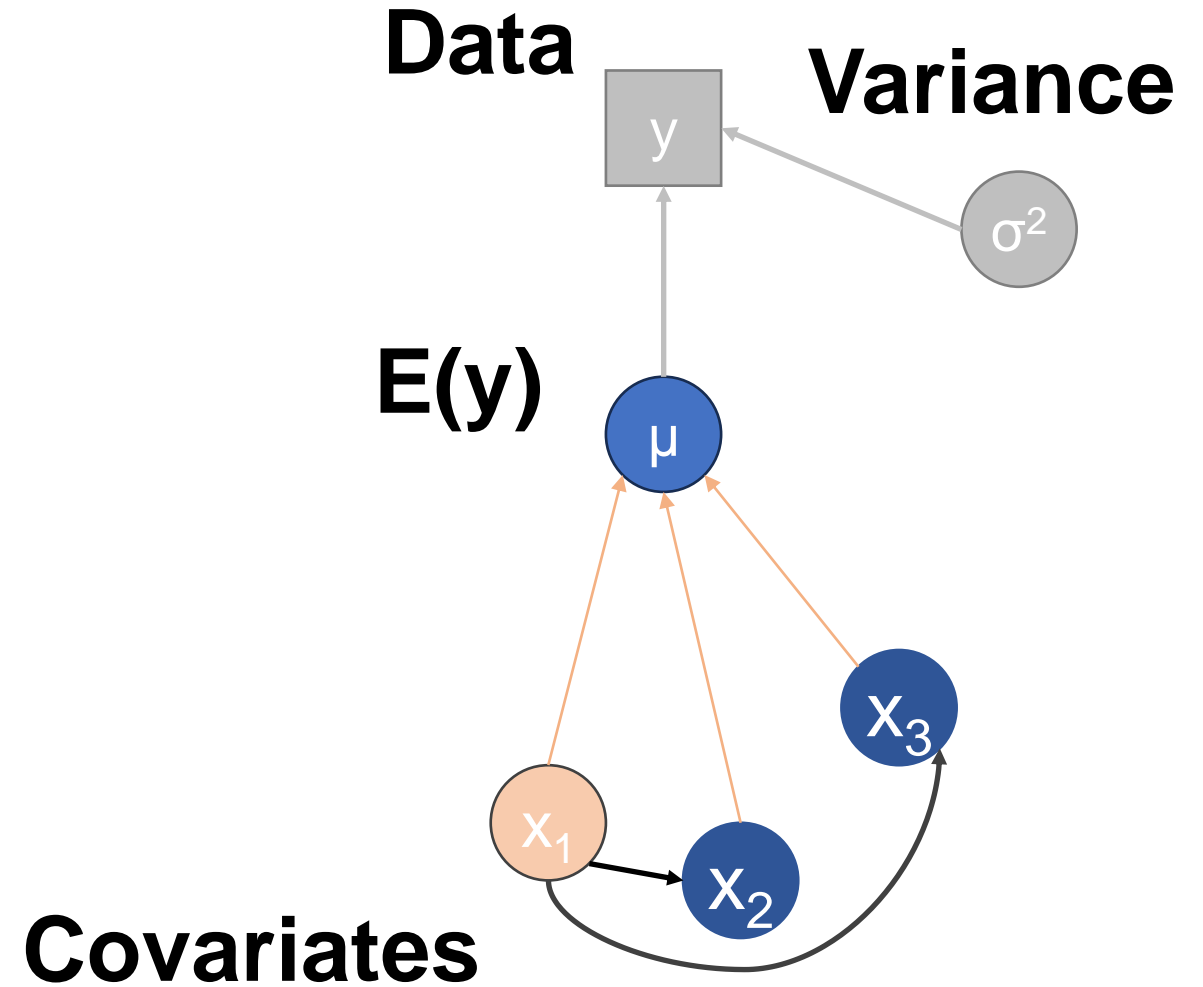
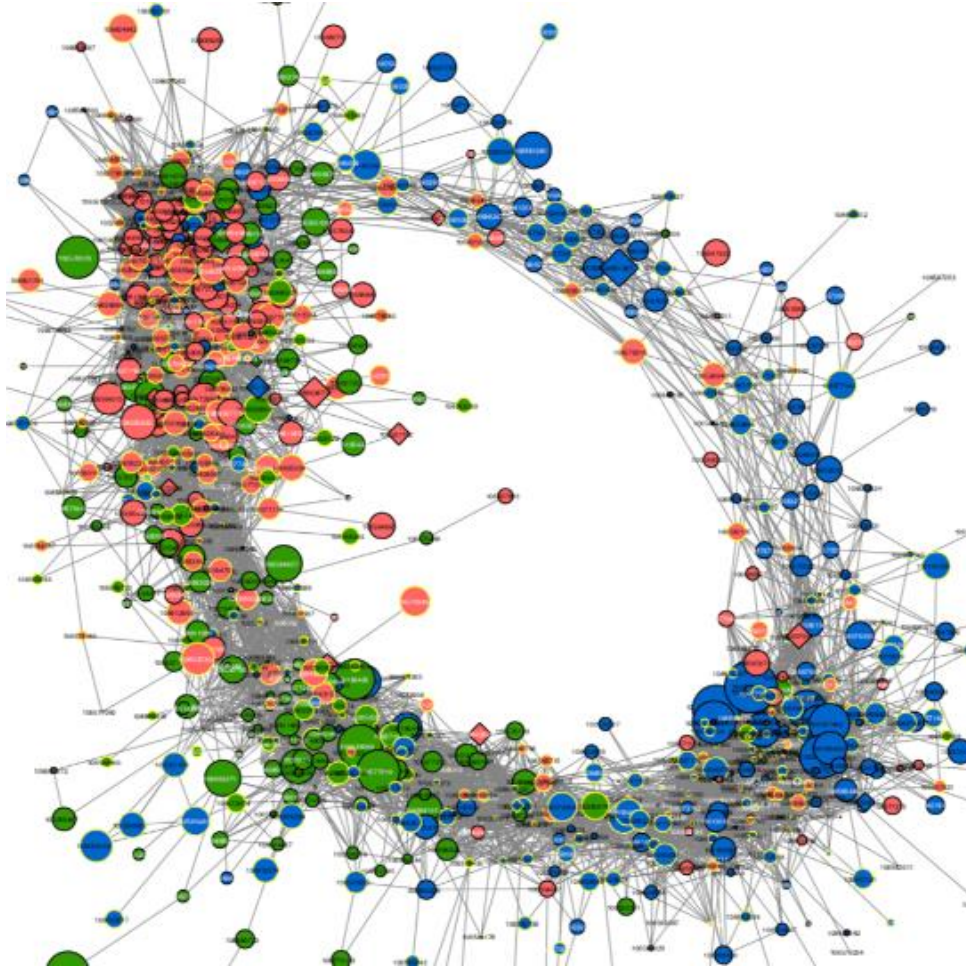
**Flow rate, precipitation, and temperature as measurements of hot/dry v. cool/wet**

***All models are wrong, but some are useful – GC Box***



***No models are right, and most are useless – TW Arnold***

***All models are wrong, but some are useful – GC Box***



***No models are right, and most are useless – TW Arnold***



# These can get pretty complicated pretty quickly...

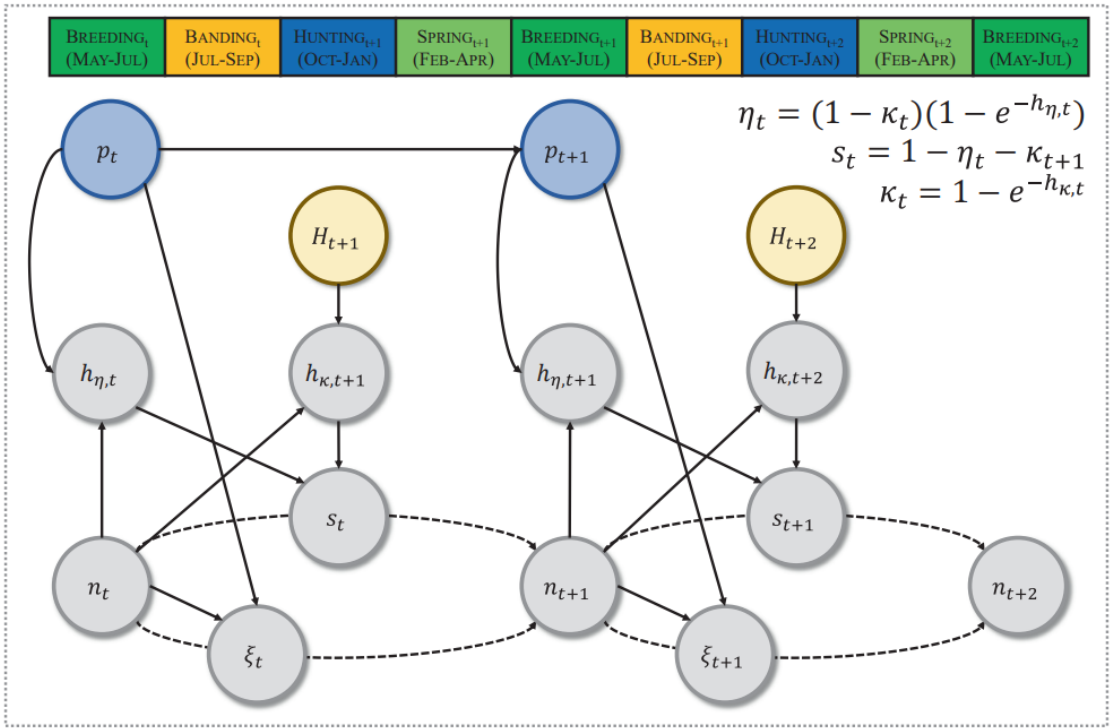


FIGURE 2 A directed acyclic graph demonstrating the relationships among abundance ( $n$ ), ponds ( $p$ ; blue), fecundity ( $\xi$ ), hunting mortality hazard rate ( $h_{\kappa}$ ), natural mortality hazard rate ( $h_{\eta}$ ), survival ( $s$ ) and the number of duck hunters ( $H$ ; brown) for blue-winged teal breeding in the North American Prairie Pothole Region across the annual cycle (1973–2016). Solid arrows represent estimated directional relationships, and dashed arrows represent processes leading to changes in population abundance.



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DOI: 10.1111/1365-2656.13807

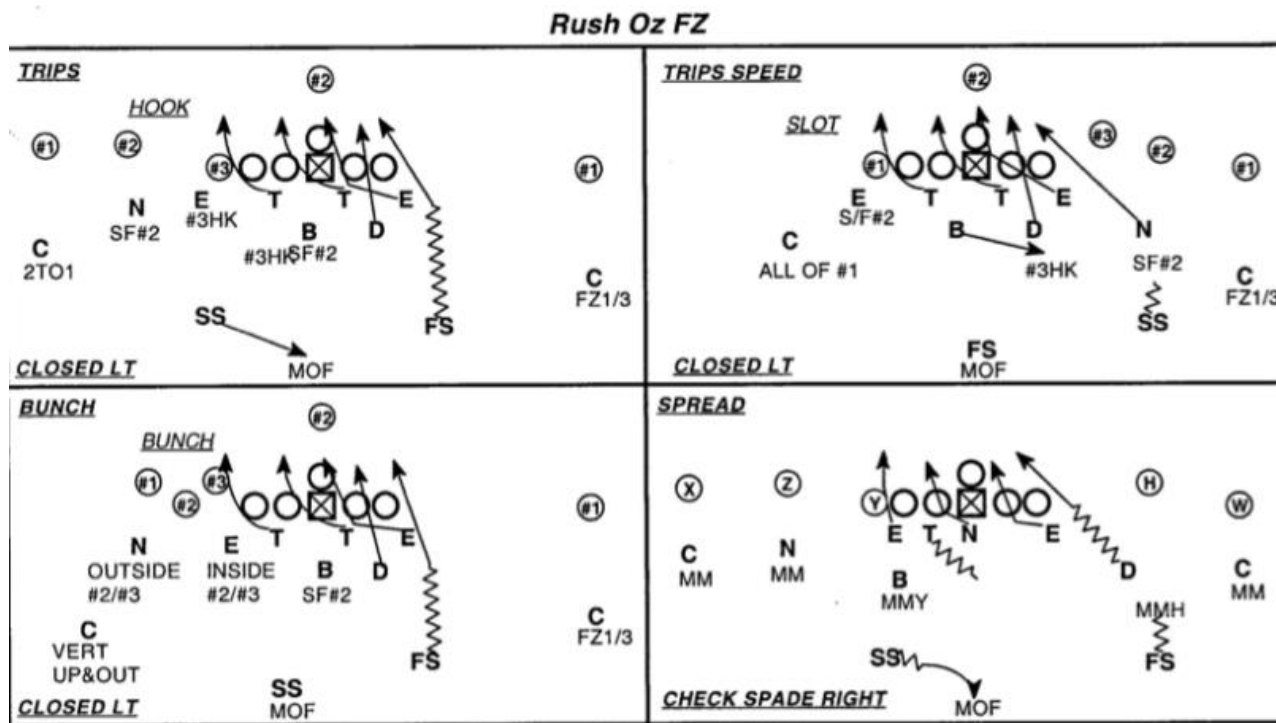
RESEARCH ARTICLE Journal of Animal Ecology

## Density-dependence produces spurious relationships among demographic parameters in a harvested species

Thomas V. Riecke<sup>1,2,3</sup> | Madeleine G. Lohman<sup>1,2</sup> | Benjamin S. Sedinger<sup>1,2,4</sup> |  
Todd W. Arnold<sup>5</sup> | Cliff L. Feldheim<sup>6</sup> | David N. Koons<sup>7</sup> | Frank C. Rohwer<sup>8</sup> |  
Michael Schaub<sup>3</sup> | Perry J. Williams<sup>2</sup> | James S. Sedinger<sup>2</sup>

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# These can get pretty complicated pretty quickly...



RIECKE ET AL.

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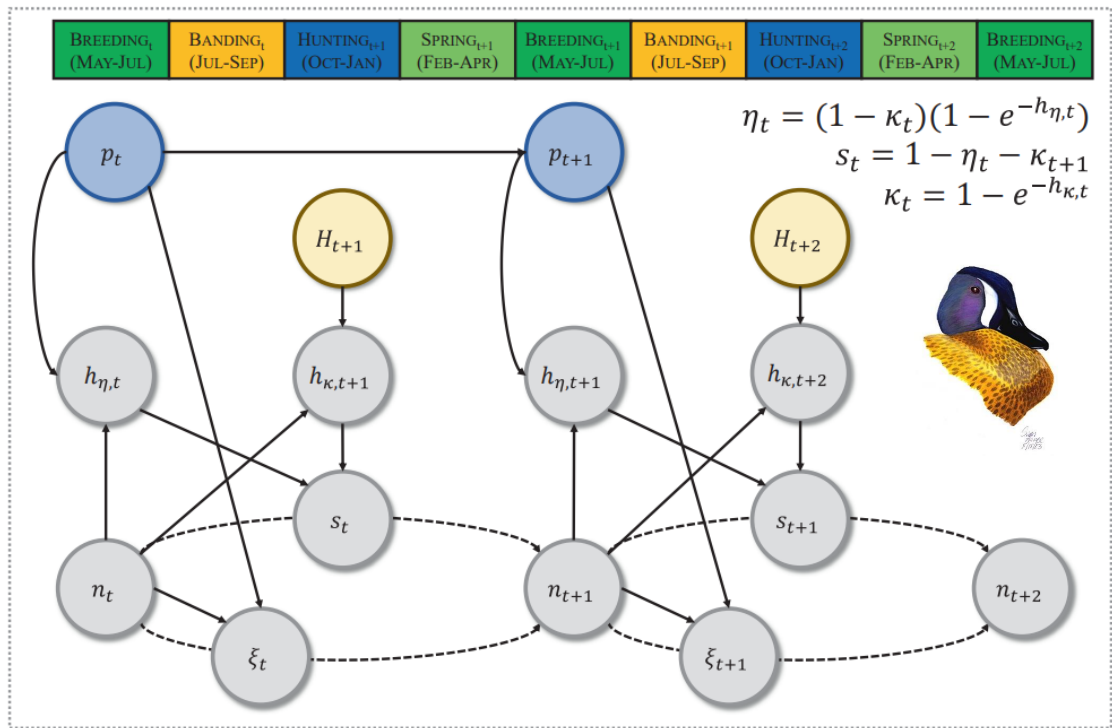


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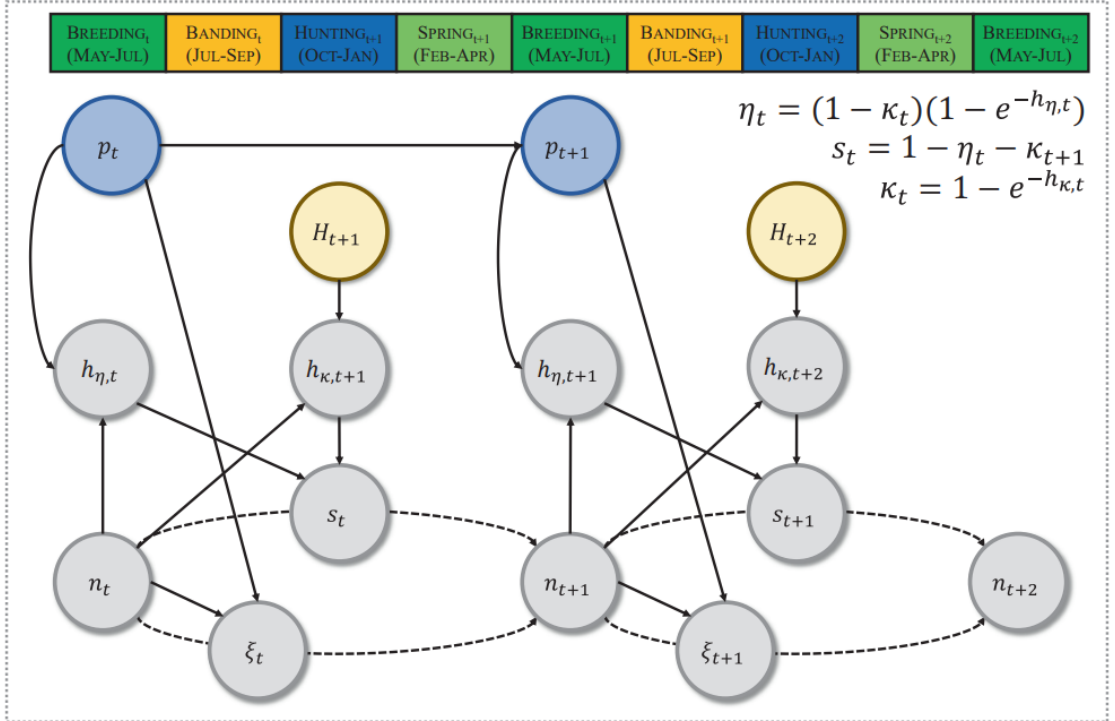
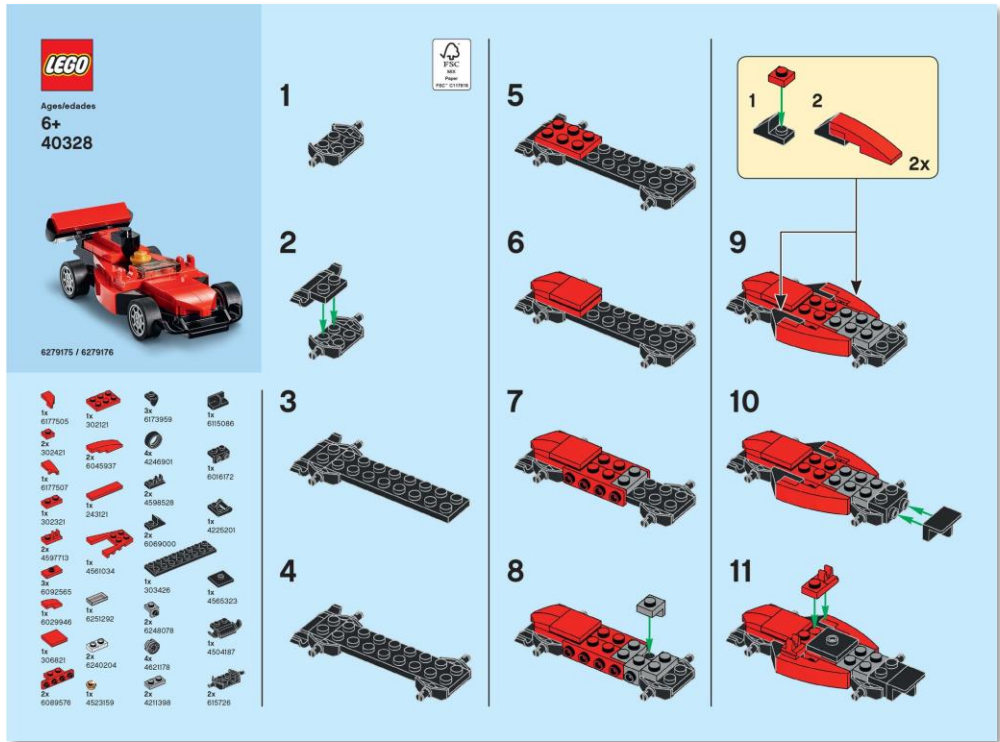
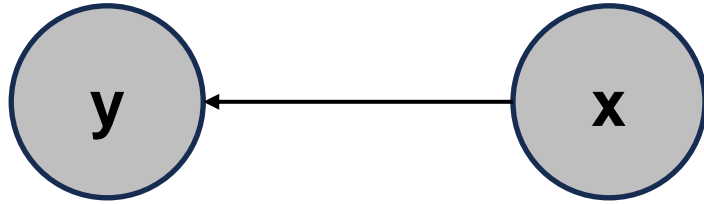


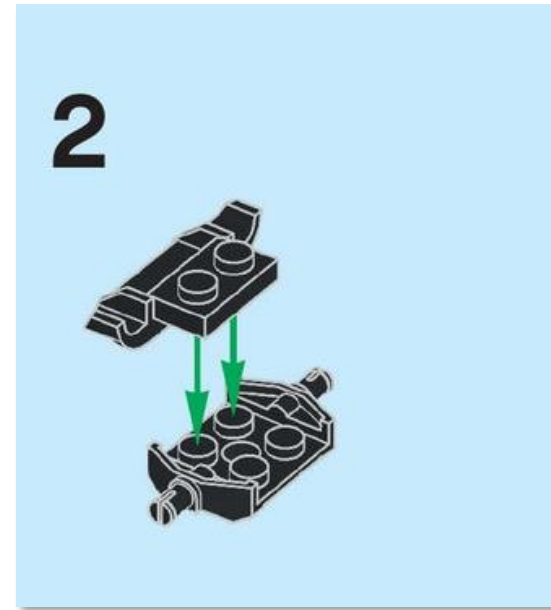
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# We can overcome this complexity

1. Develop a fundamental understanding of linear models

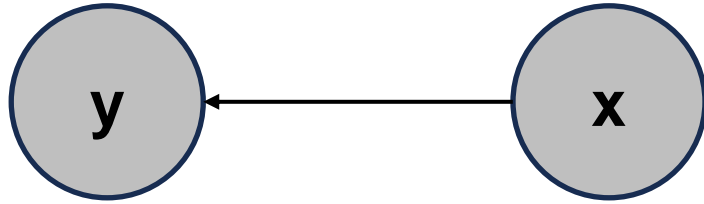


$$y_i \sim \text{normal}(\beta_0 + \beta_1 x_i, \sigma^2)$$

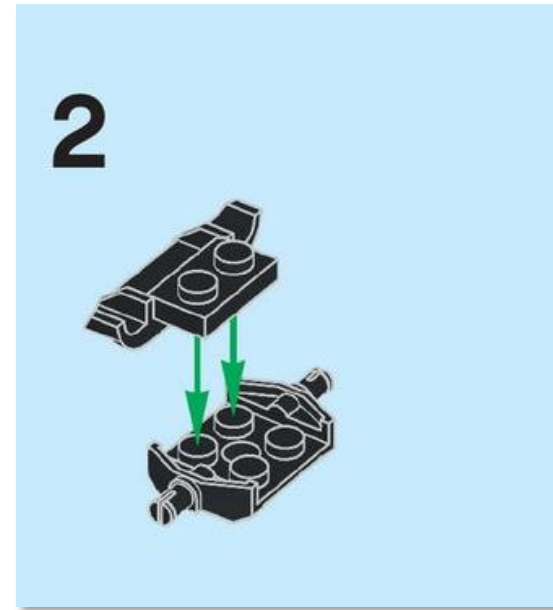


# We can overcome this complexity

1. Develop a fundamental understanding of (generalized) linear models

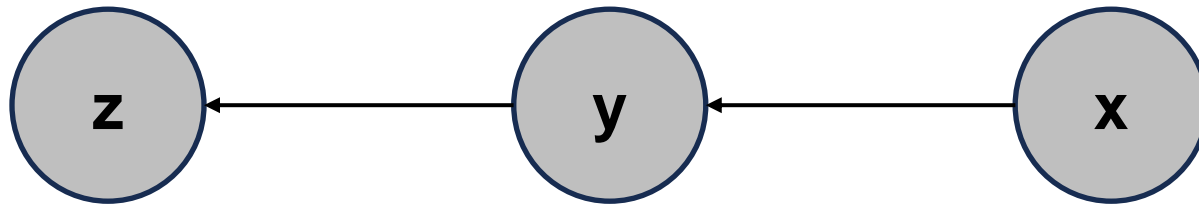


$$y_i \sim \text{lognormal}(\beta_0 + \beta_1 x_i, \sigma^2)$$

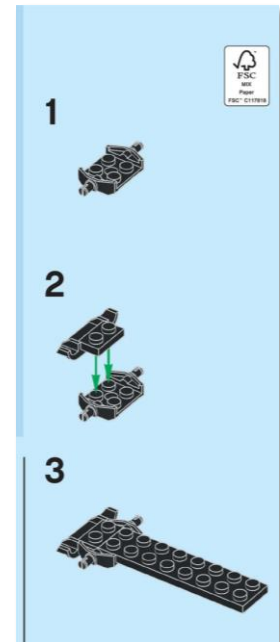


# We can overcome this complexity

1. Develop a fundamental understanding of (generalized) linear models
2. Understand that linear models can be applied in 'layers' or hierarchies with multiple response variables and multiple measurements of response variables



$$y_i \sim \text{normal}(\beta_0 + \beta_1 x_i, \sigma_y^2)$$
$$z_i \sim \text{normal}(\alpha_0 + \alpha_1 y_i, \sigma_z^2)$$



# We can overcome this complexity

1. Develop a fundamental understanding of linear models
2. Understand that linear models can be applied in 'layers' or hierarchies with multiple response variables and multiple measurements of response variables
3. Understand that's what structural equation models and path analyses are...

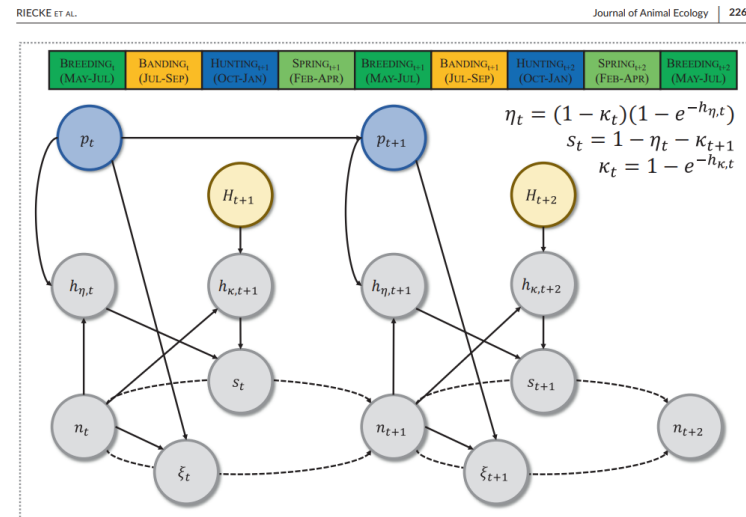
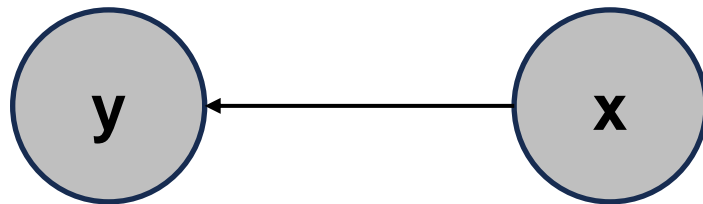


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# Goals of this class

1. Develop a fundamental understanding of linear models
2. Understand that linear models can be applied in 'layers' or hierarchies with multiple response variables and multiple measurements of response variables
3. Understand that's what structural equation models and path analyses are, and apply these concepts to your own data (if you want?)



**How are we going to get there?**

- **PART I. Introduction and linear models**
  - **Week 1:** *Why SEM? Why Bayesian?*
  - **Week 3:** *Linear models*
  - **Week 4:** *Generalized linear models*

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- **PART II. Structural equation models**
  - **Week 5:** *Direct and indirect effects*
  - **Week 6:** *Latent variables*
  - **Week 7:** *Composite covariates and cross-lags*

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  - **Week 6:** *Latent variables*
  - **Week 7:** *Composite covariates and cross-lags*
- **PART III. Case studies to reinforce concepts**
  - **Week 8:** *Resource selection and reproductive success*
  - **Week 9:** *Occupancy and body condition*
  - **Week 10:** *Cross-lags: life-history trade-offs*
  - **Week 11:** *Cross-lags: density-dependence and harvest*

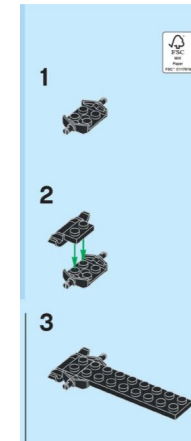
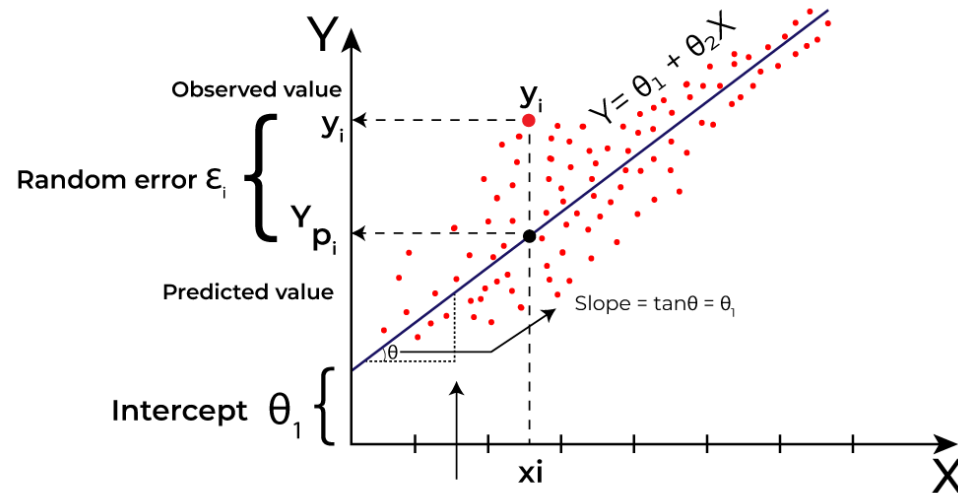


## Things you need to do by next week

- **Install programs**
  - *JAGS*
  - *The latest version of R*
  - *The latest version of RStudio*
- **Install packages**
  - *jagsUI*
  - *rstan*
  - *rtools*
  - *vioplot*
- **Run test scripts from course GitHub**

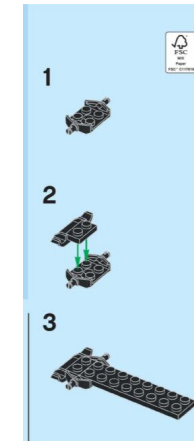
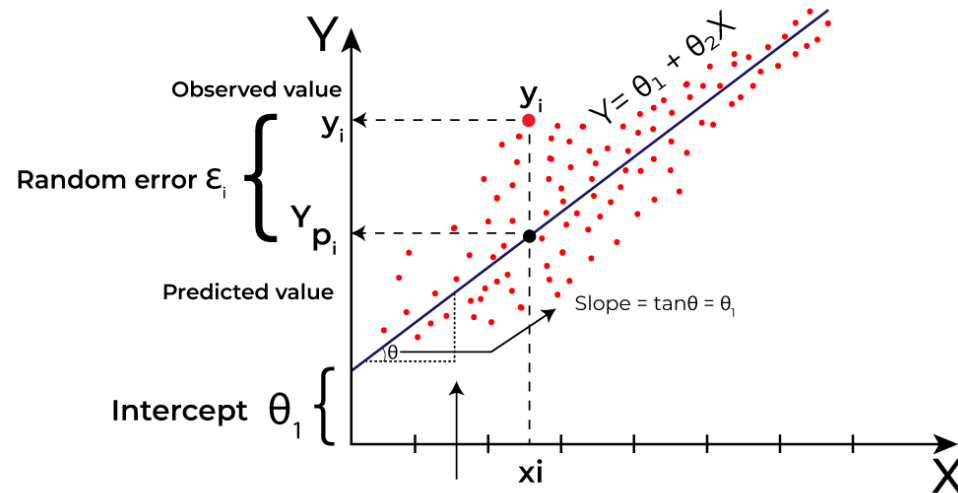
# A note on 'attitude'

- Parts of this class are going to be extremely complicated. That's a good thing.

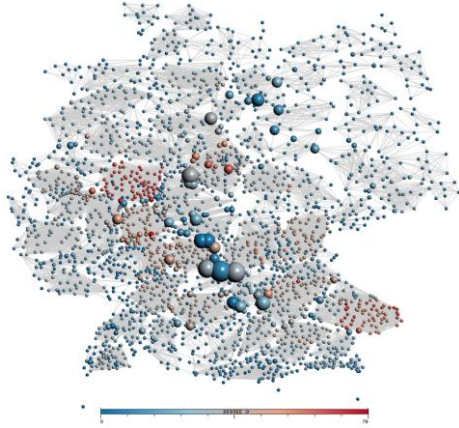


# A note on 'attitude'

- Parts of this class are going to be extremely complicated. That's a good thing.
- **Three goals for learning**
  1. Don't give up. These are all 'expanded' or more complicated linear models.
  2. Set realistic goals, and celebrate small achievements/progress!
  3. Ask questions.

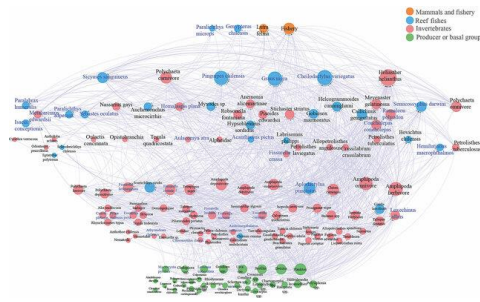


# We're never going to model reality



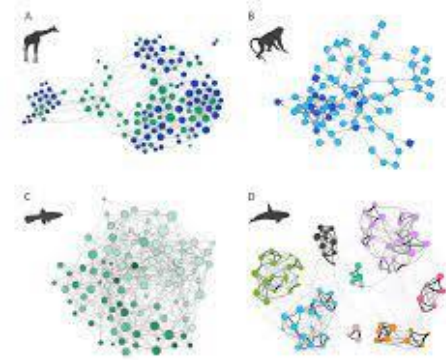
## Climate network

Abiotic systems



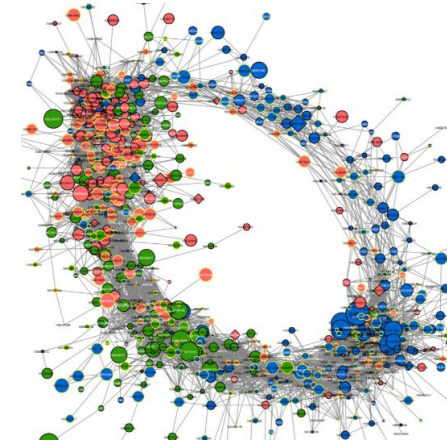
## Food Network

Among populations



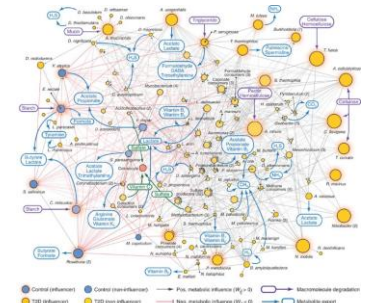
## Social Network

Within populations



## Gene Network

Within individuals

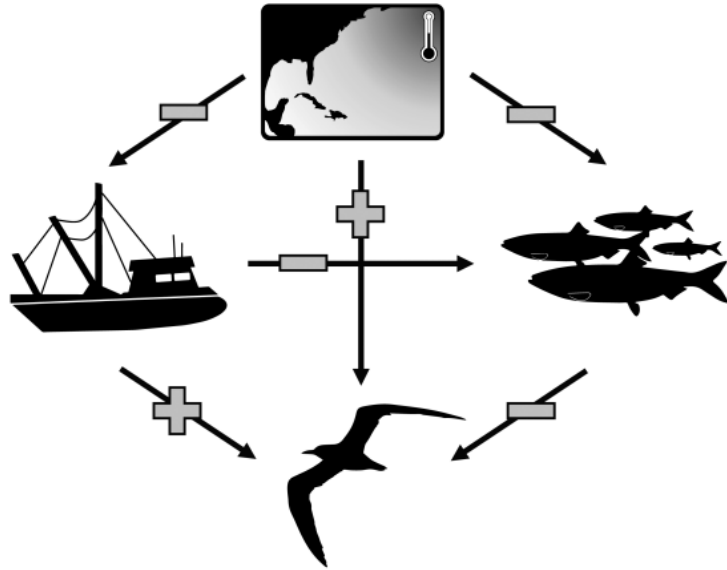


## Microbial Network

Within individuals

***No models are right, and most are useless – TW Arnold***

# SEMs let us get closer (maybe a little more useful?)

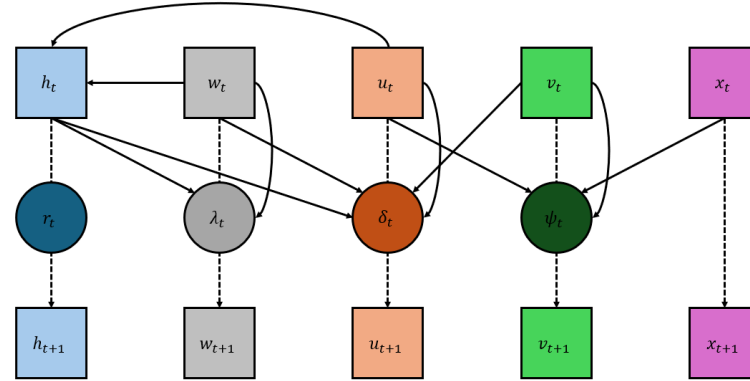


**FIGURE 1** Simplified path diagram describing the hypothesized directionality (plus: Positive, bar: Negative association) regarding how environmental variables (i.e., sea-surface temperatures in the North Atlantic, fishery pressure, and fish production) influenced one another, as well as the indirect and direct pathways in which these sources of environmental variability influenced Royal tern mortality.



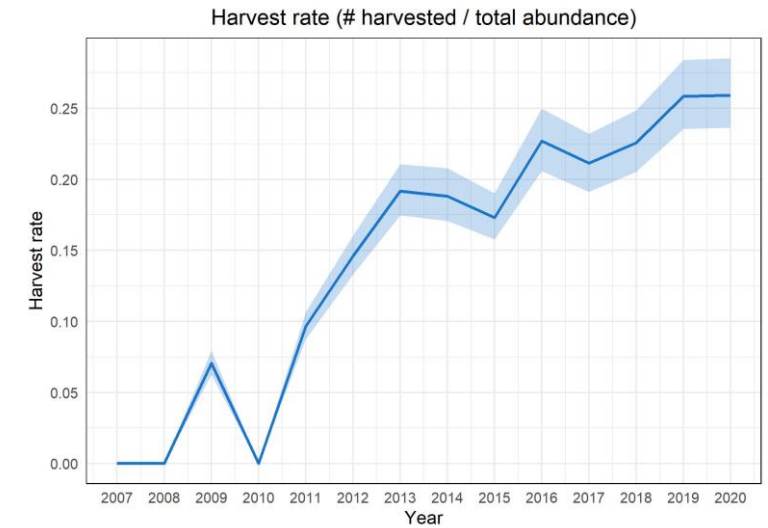
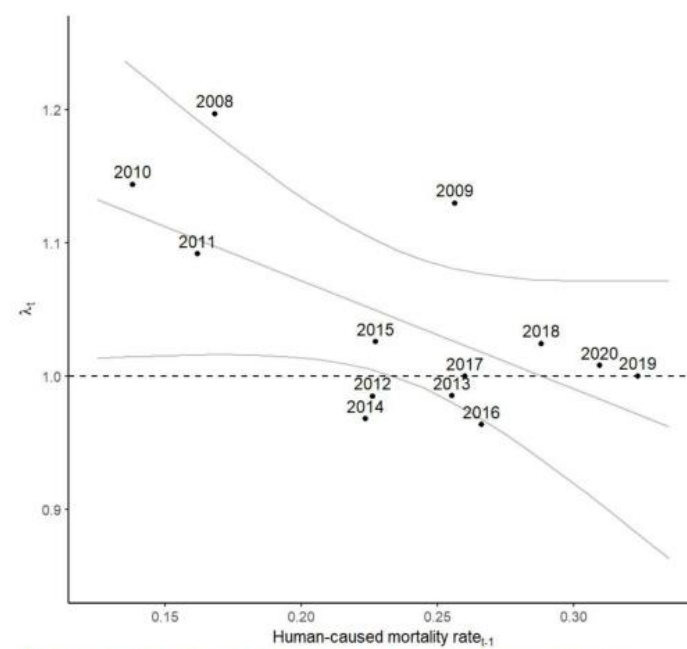
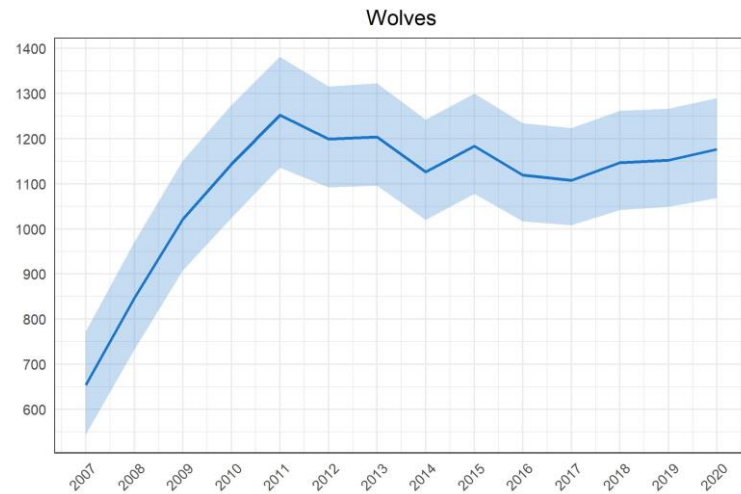


# Cross-lags and wildlife harvest: better models for critical decisions



**Let's start controversially and close to home!**

# MT wolf population recovery and harvest (2008 – present)



# Population is stable at $m = 0.29$ ?

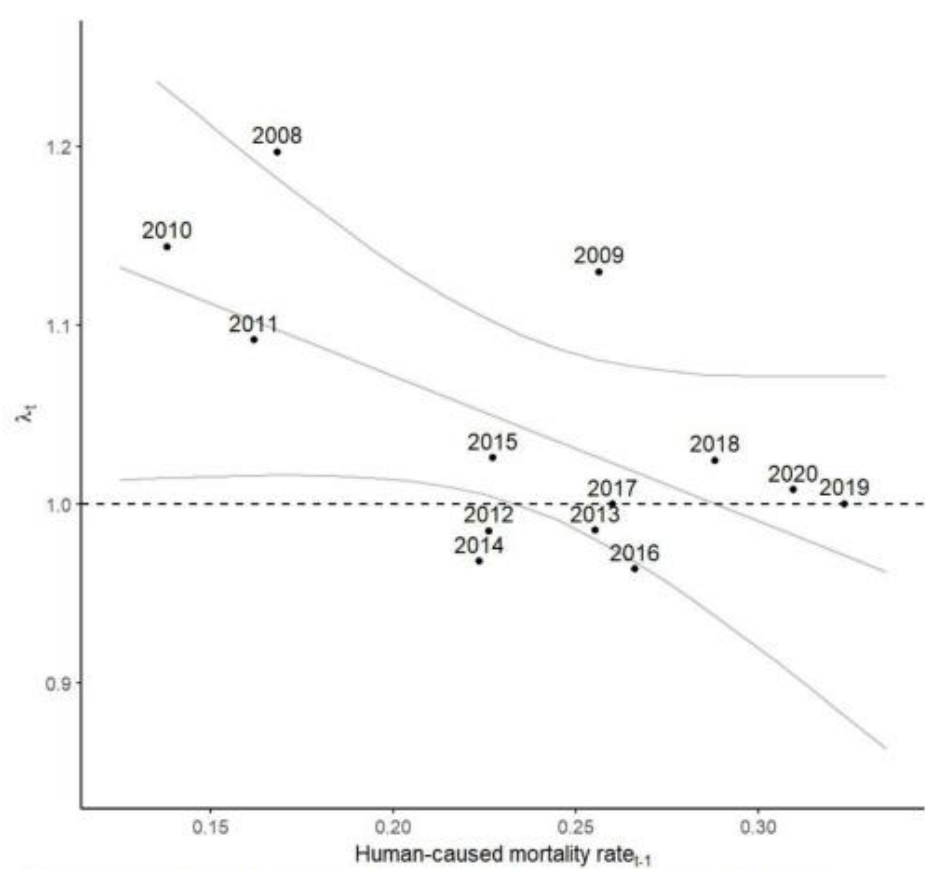
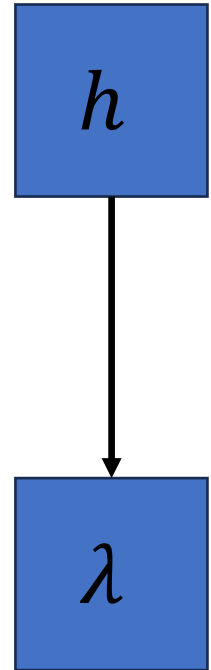
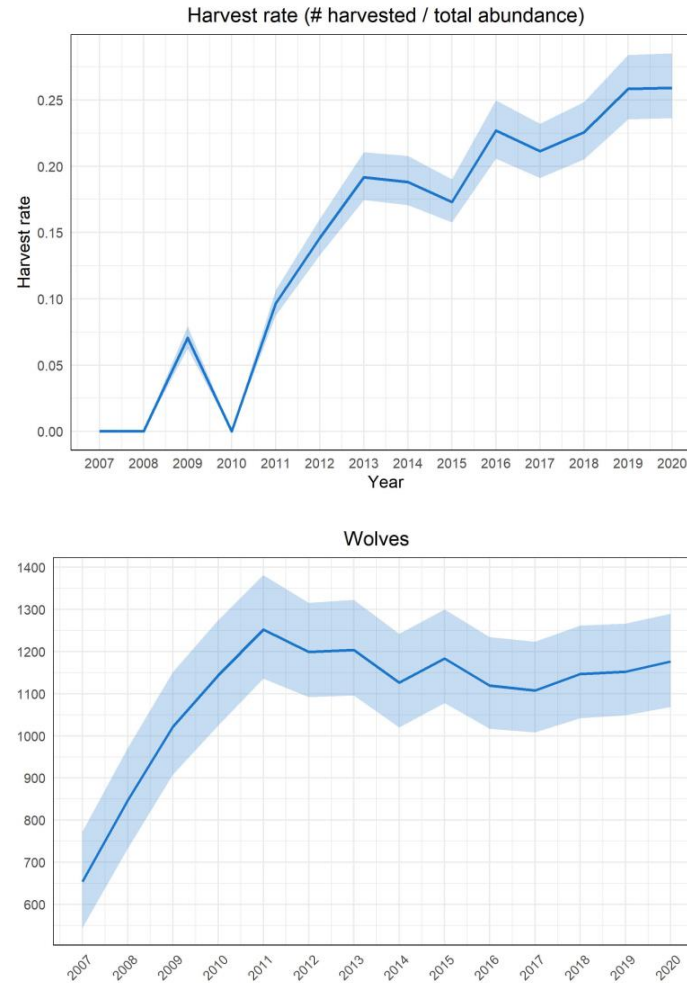


Figure 2. Estimated linear relationship and 90% credible intervals (grey lines) between annual population growth rate ( $\lambda_t$ ) and human-caused mortality rate (human-caused mortalities<sub>t</sub> / iPOM wolves<sub>t-1</sub>). The human-caused mortality rate resulting in an expected stable population ( $\lambda = 1$ ) is approximately 29%.



# Ok, what about $m = 0$ [counter-factual]?

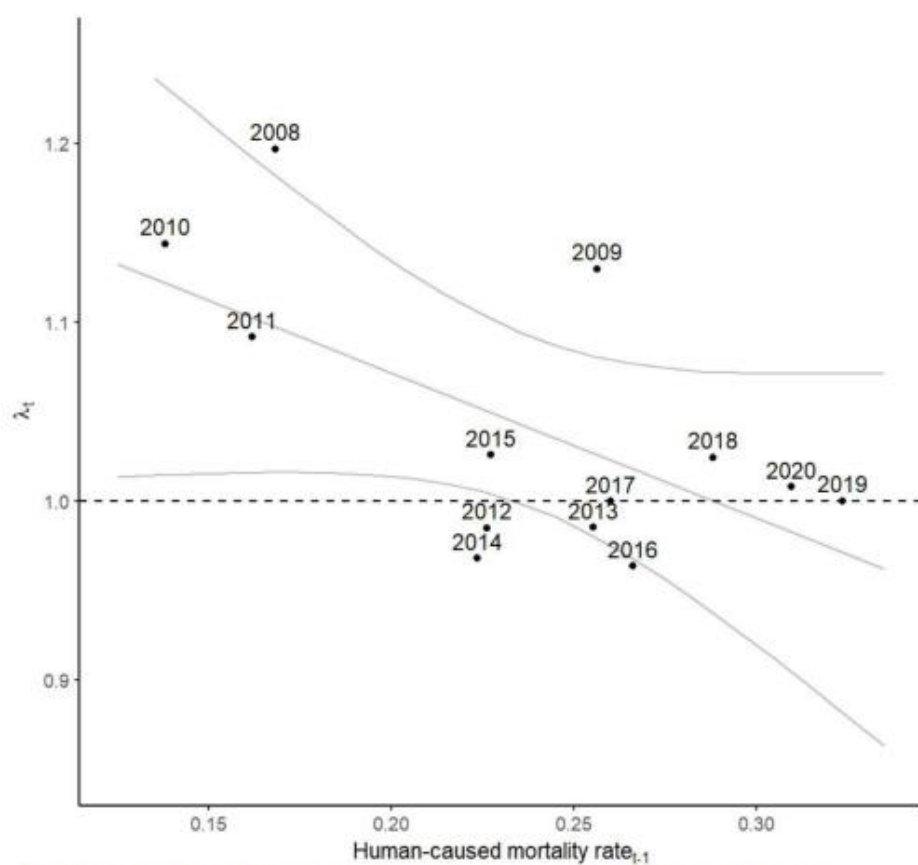
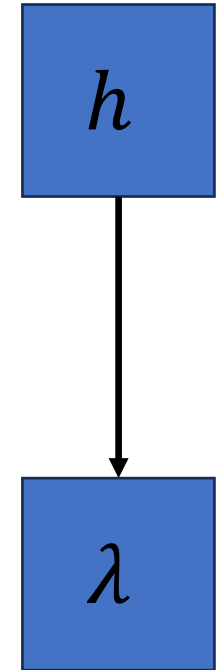
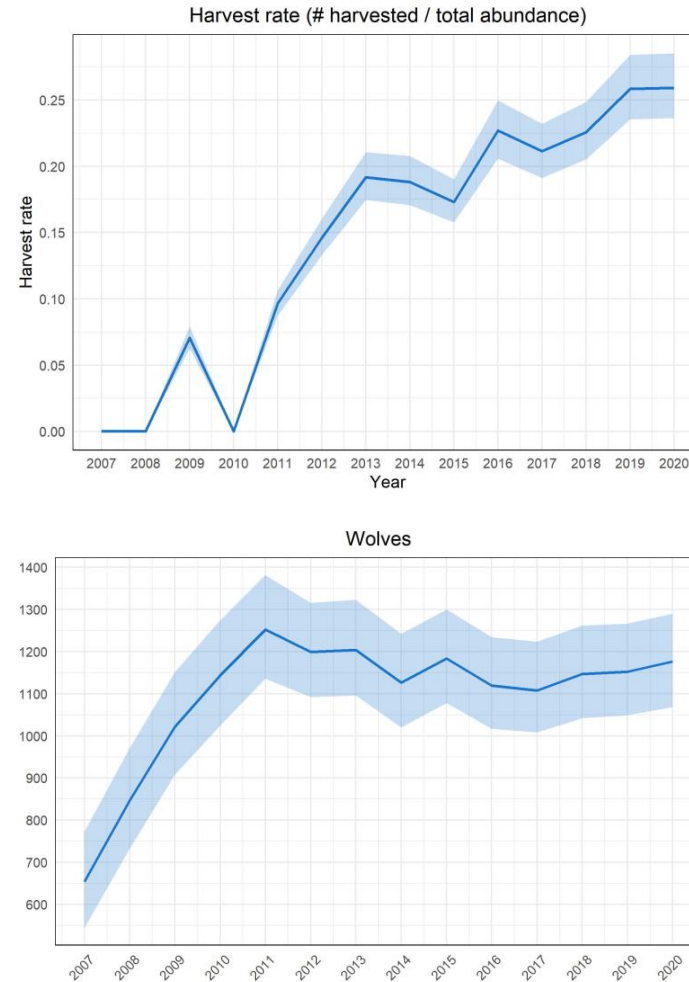


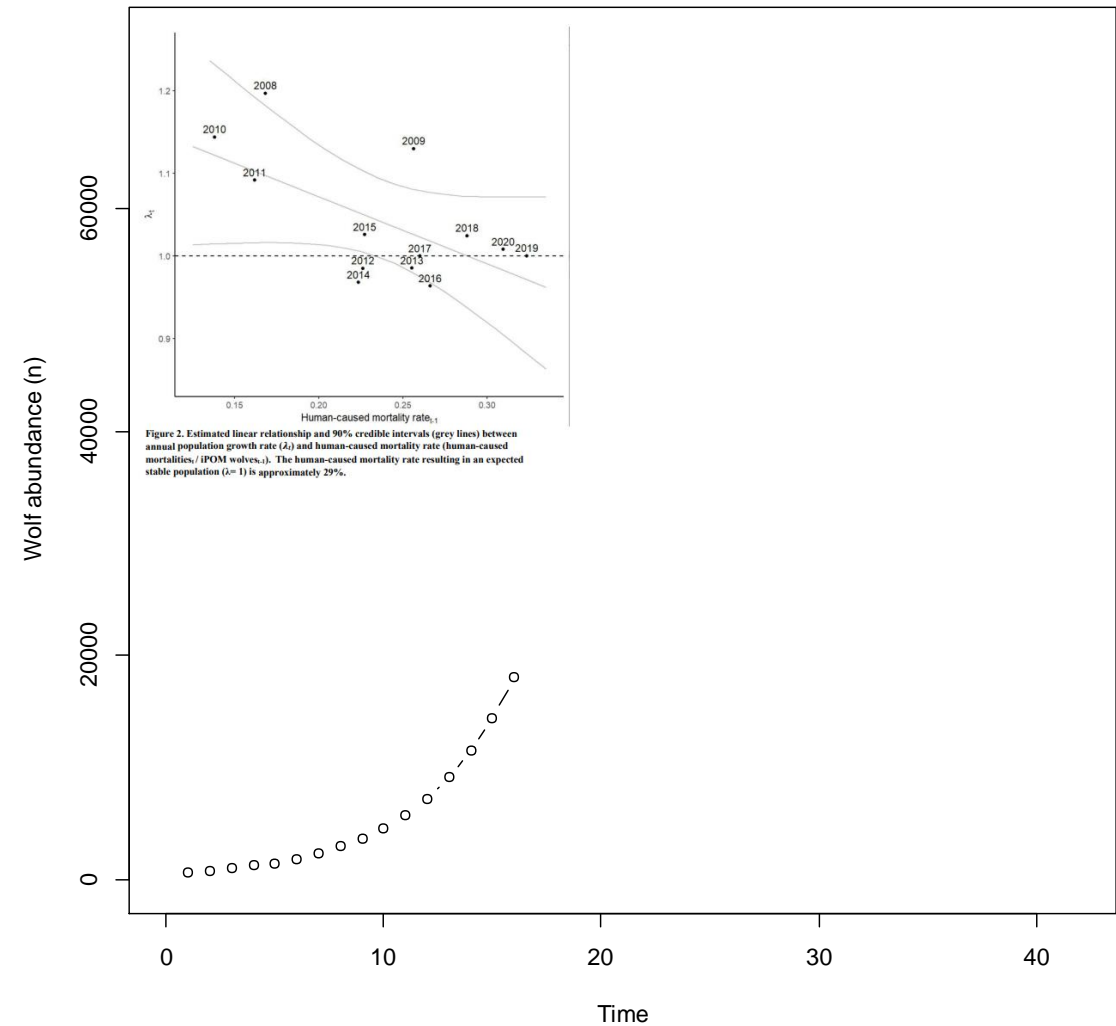
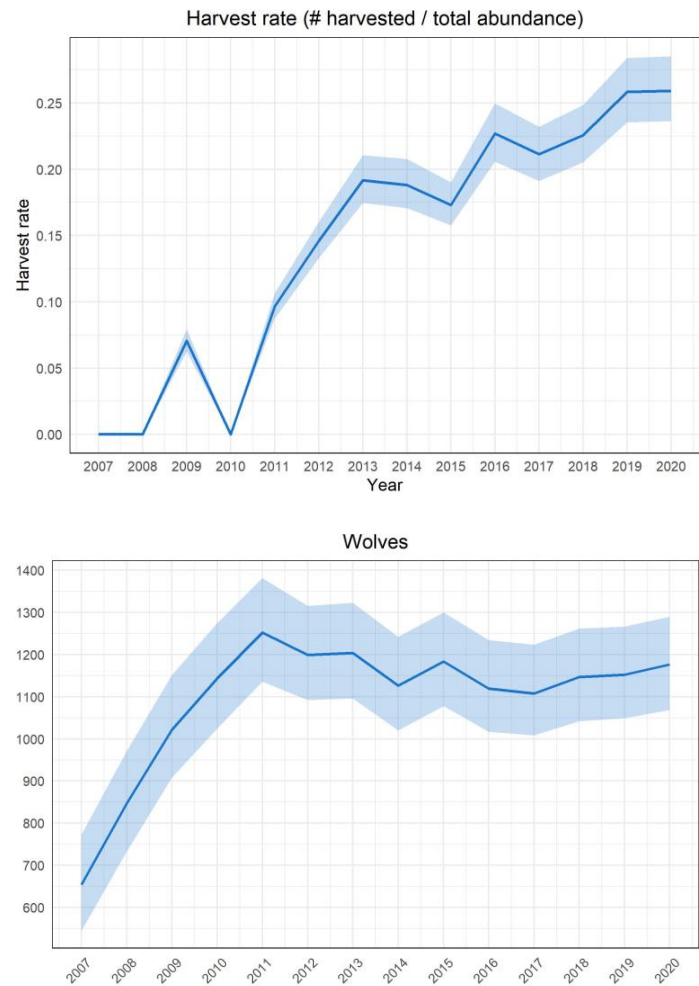
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## Population growth ( $\lambda$ ) at $m = 0$ is approximately 1.25

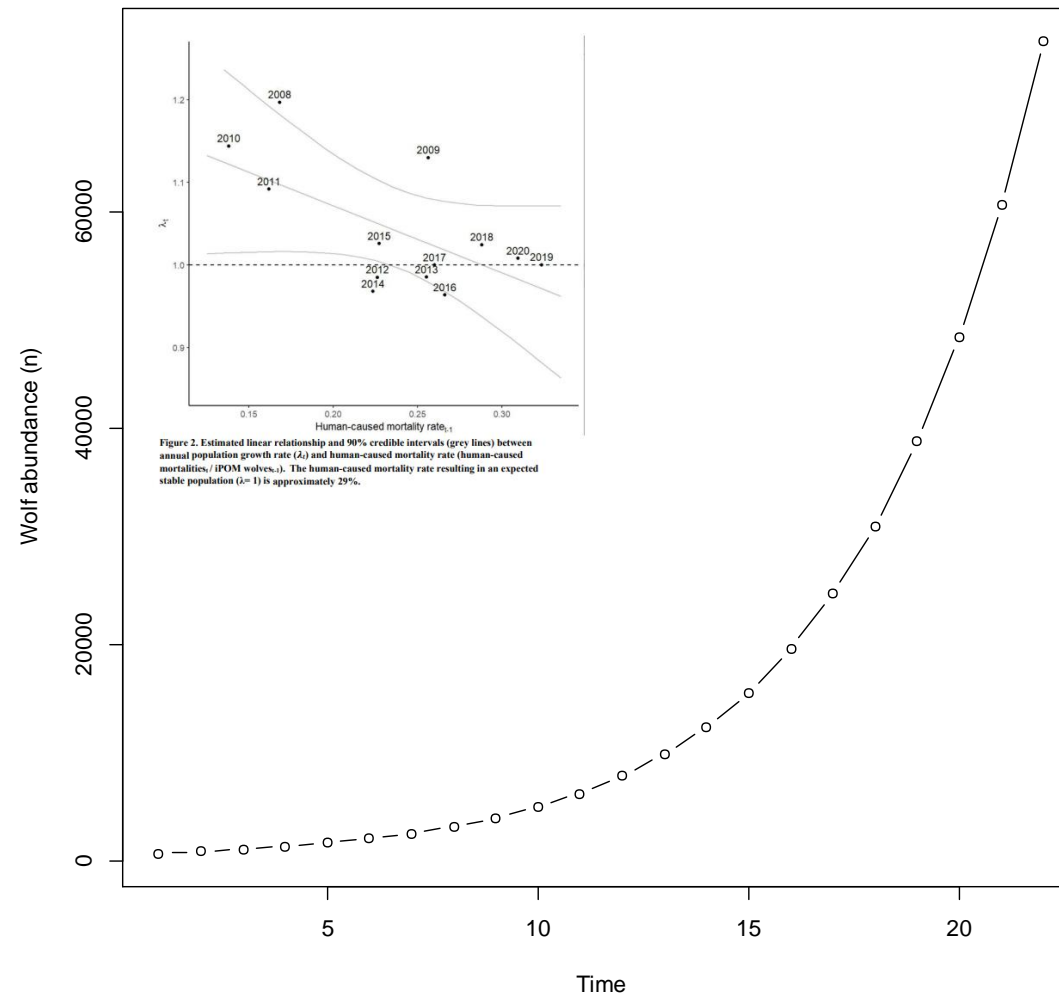
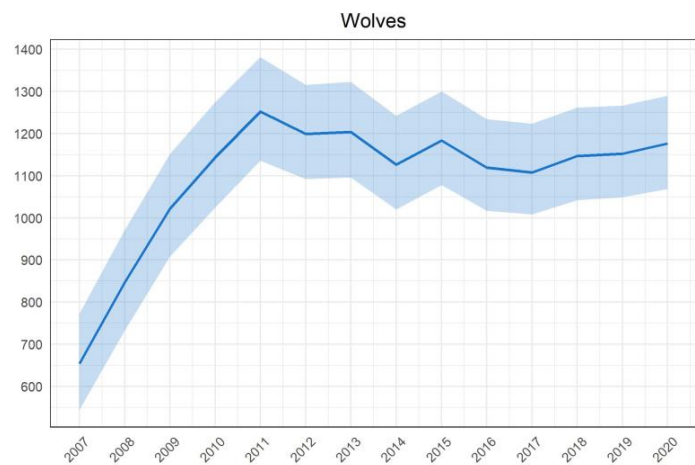
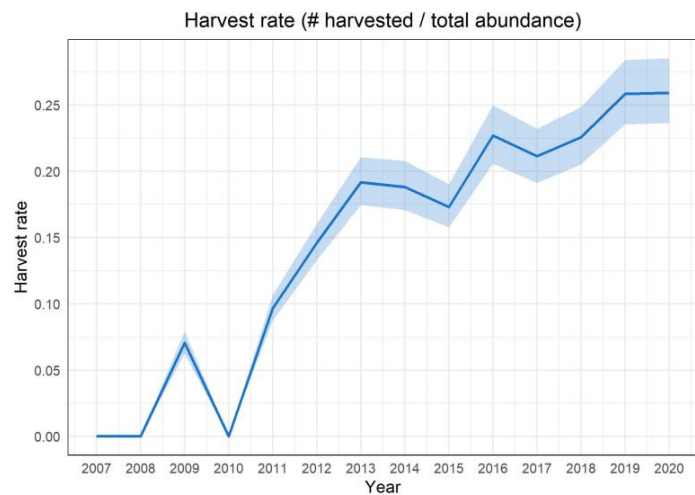


# Projected increase w/o harvest (16 years or 2024; 17k)

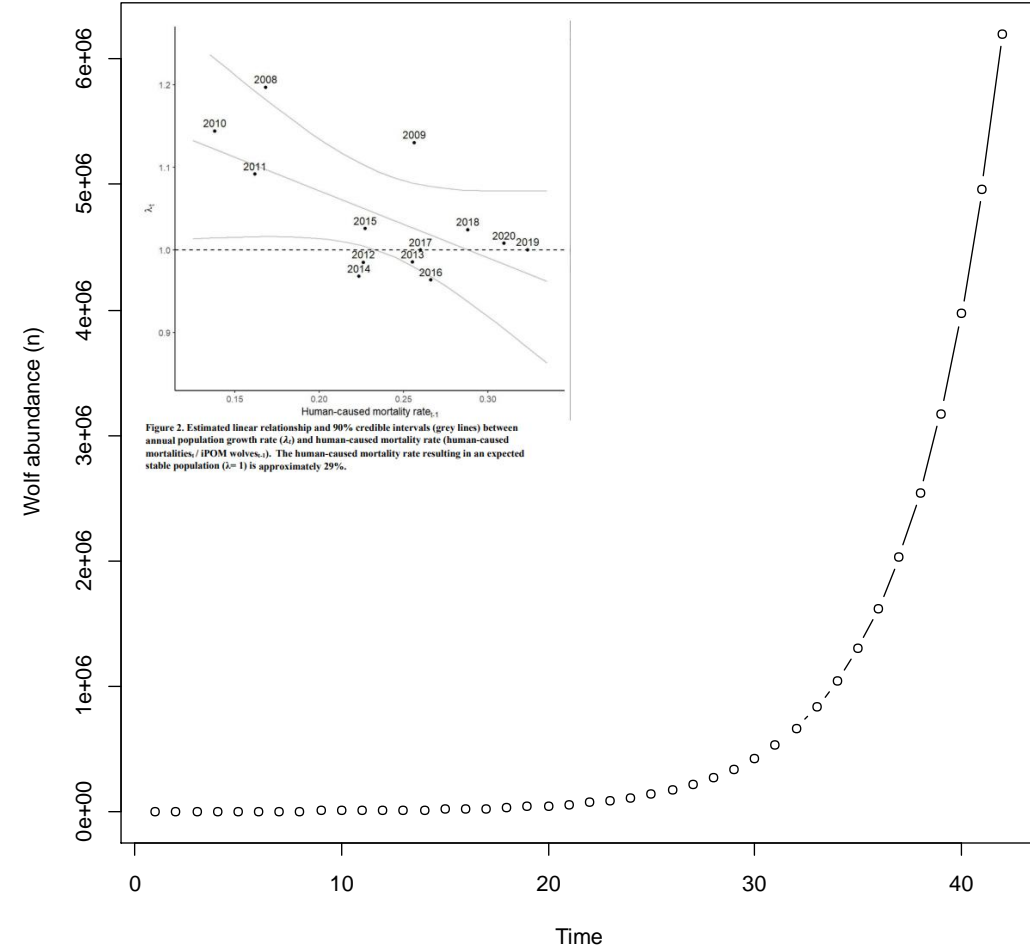
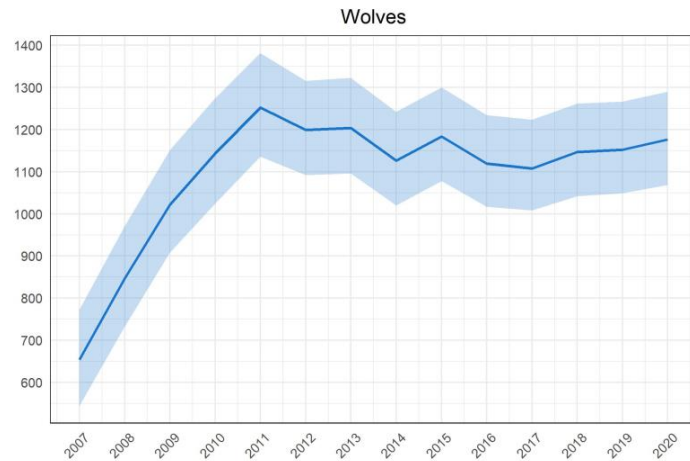
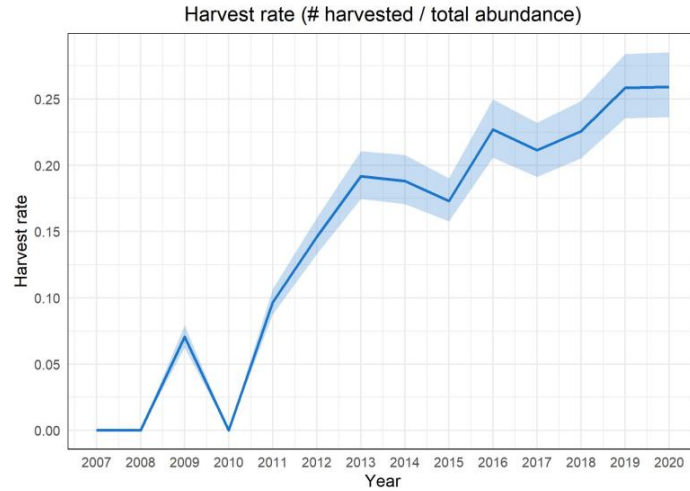


Population growth at  $m = 0$  is approximately 1.25

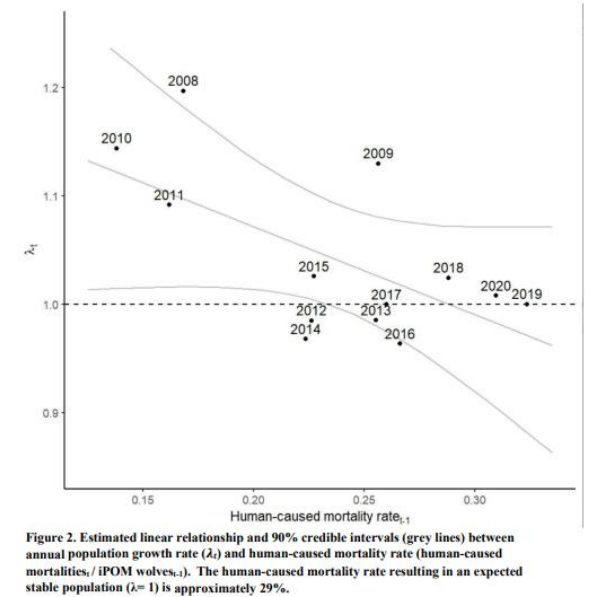
# Projected increase w/o harvest (22 years or 2030; 75k)



# Projected increase w/o harvest (42 years or 2050; 600k)



**It has been stable at  $h = 0.29$ ...**



**I don't think it will increase at 25% forever at  $h = 0$   
(absurd counterfactual!)**

**What's happening?**

# It's stable at $h = 0.29$ & $N \sim 1100$

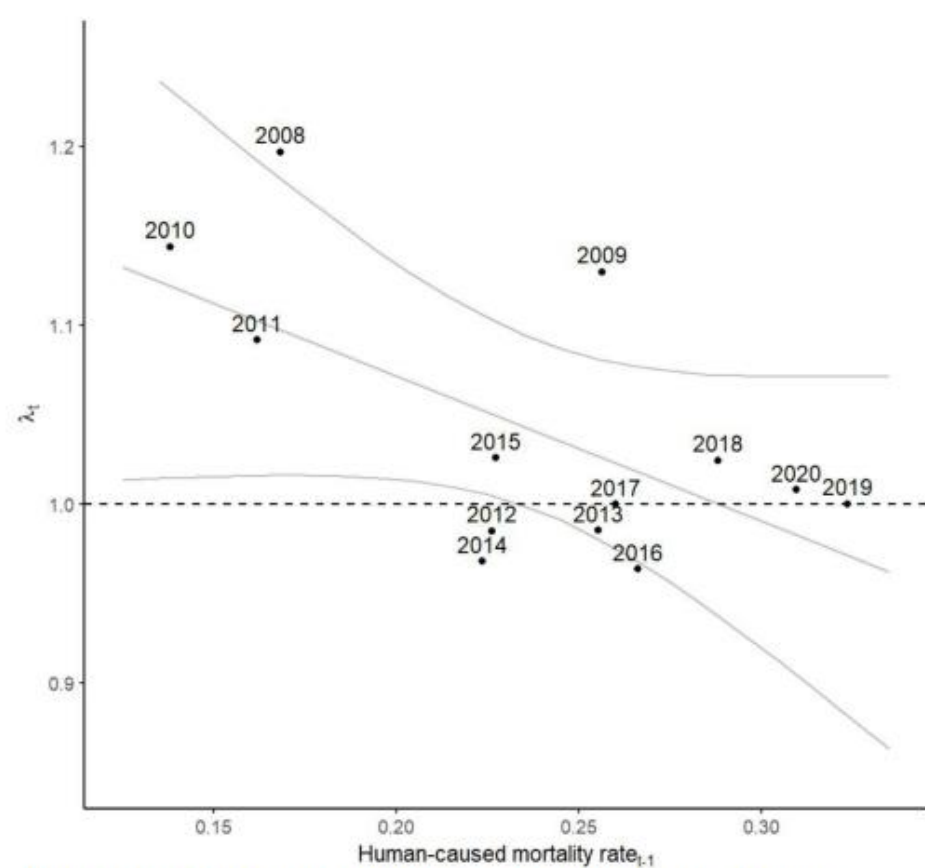
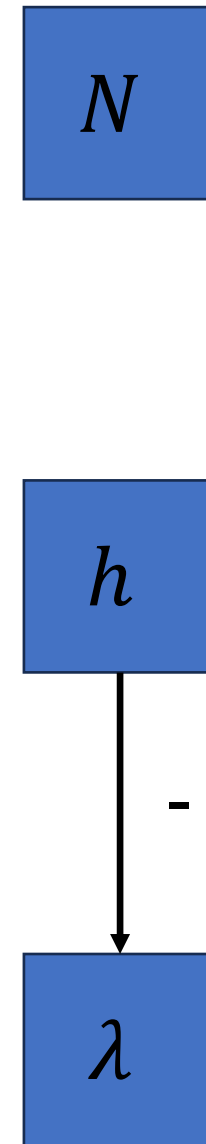
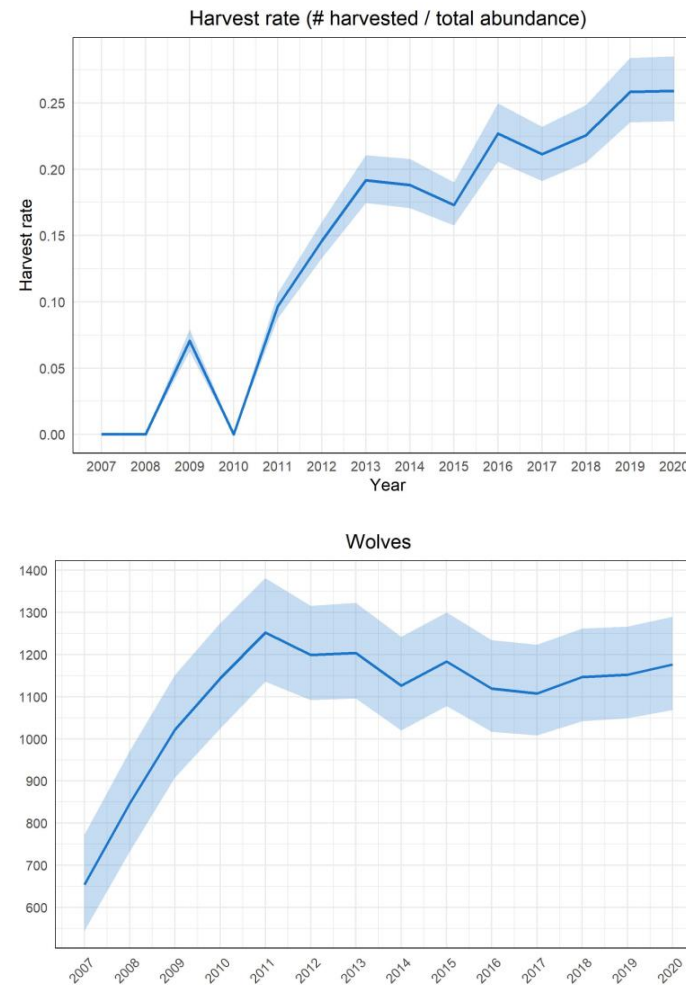


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# Abundance affects harvest rates

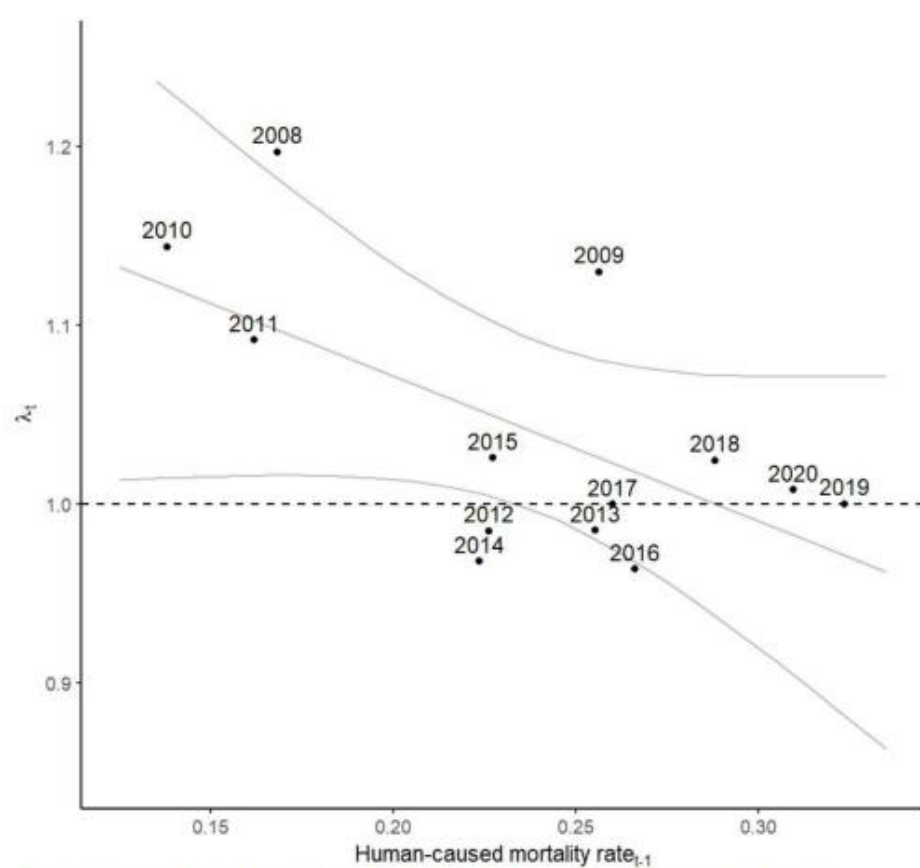
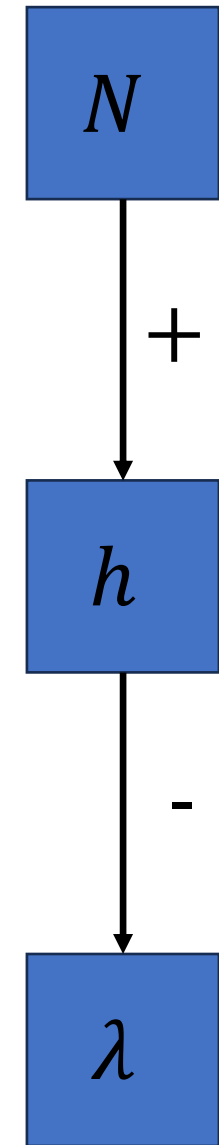
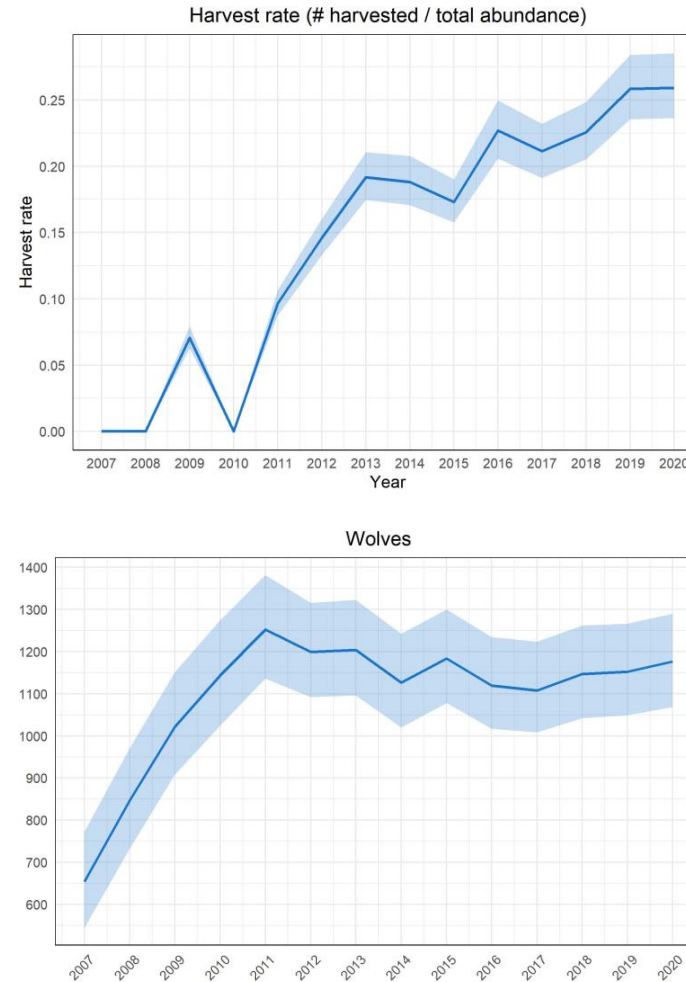


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**B/C federal laws (clear legal cause and effect) & ‘people’**

# Abundance affects population growth?

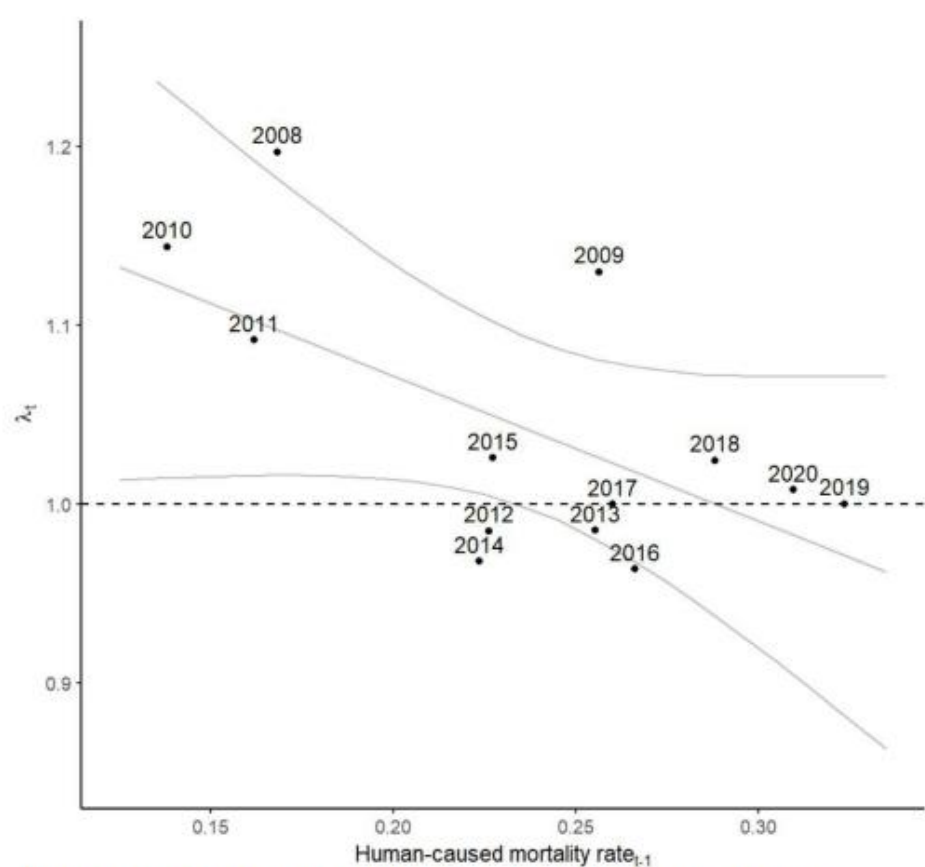
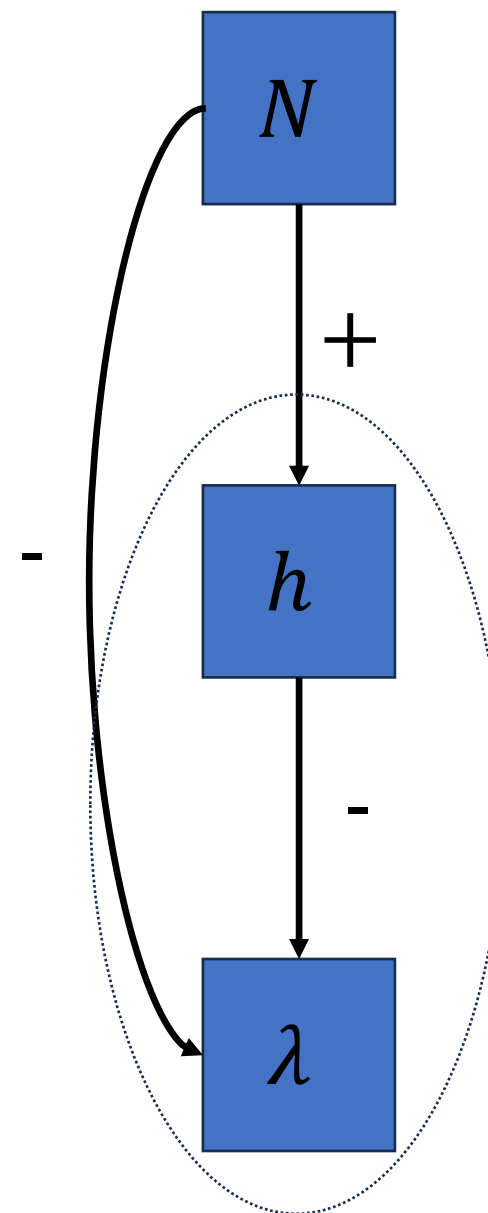


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## Density-dependence ('Ecological law')

?

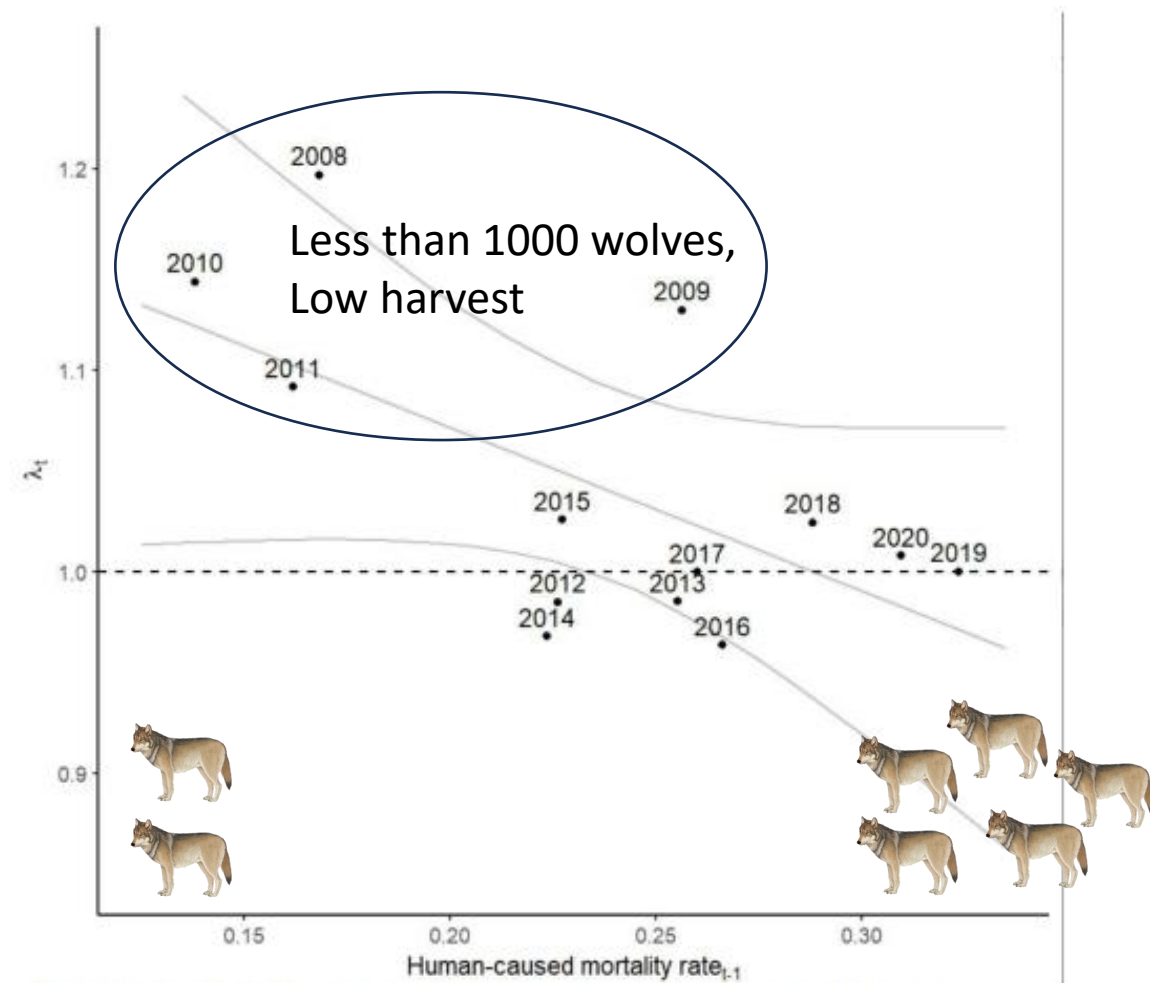
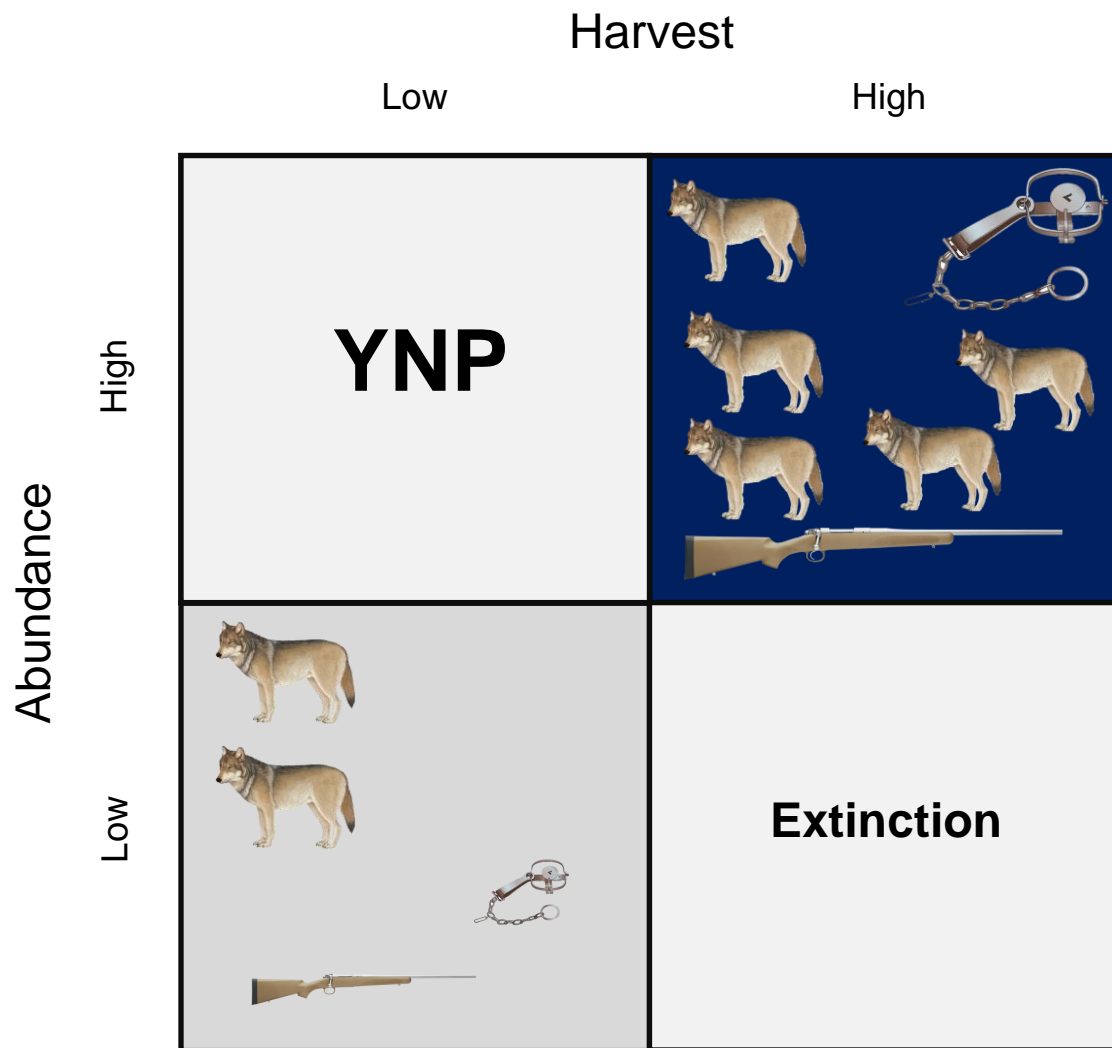
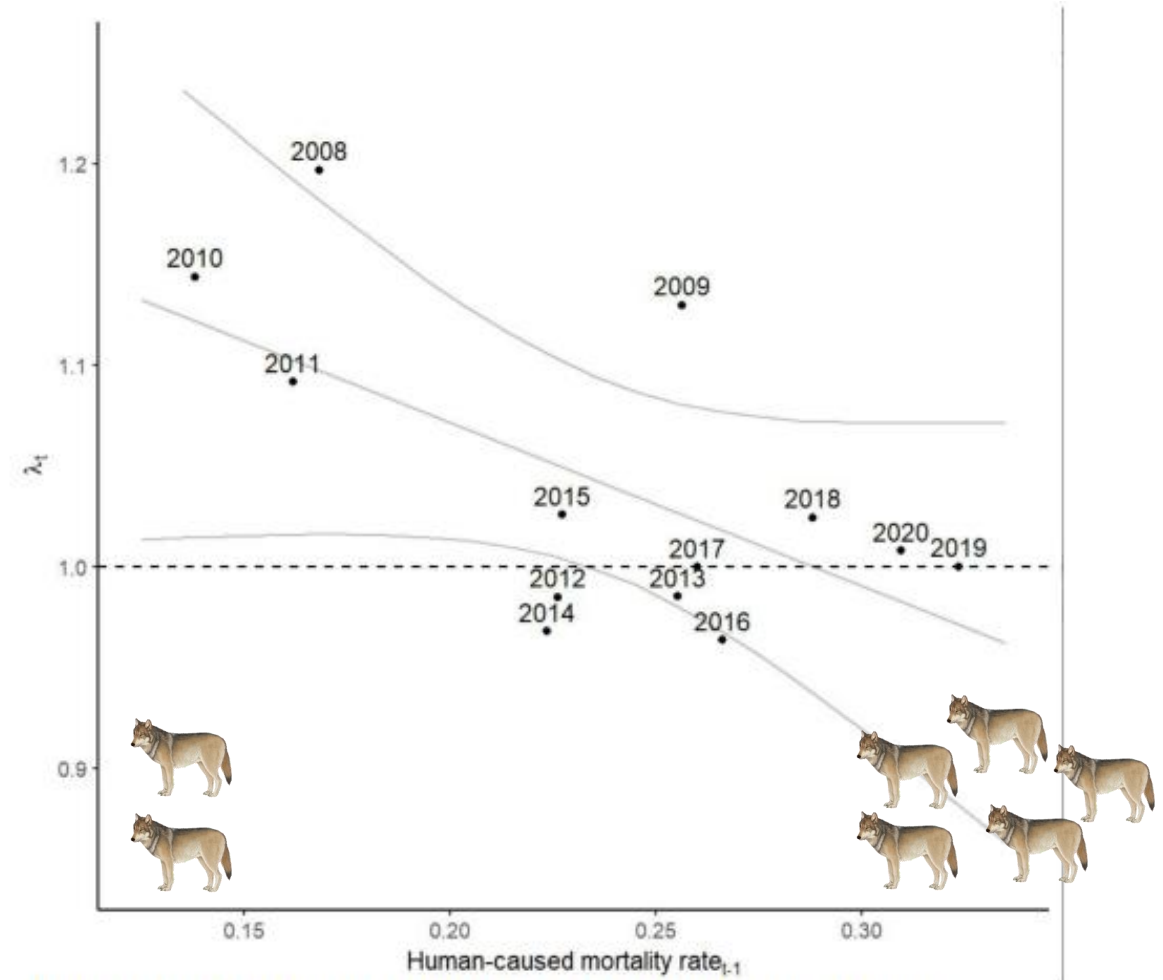
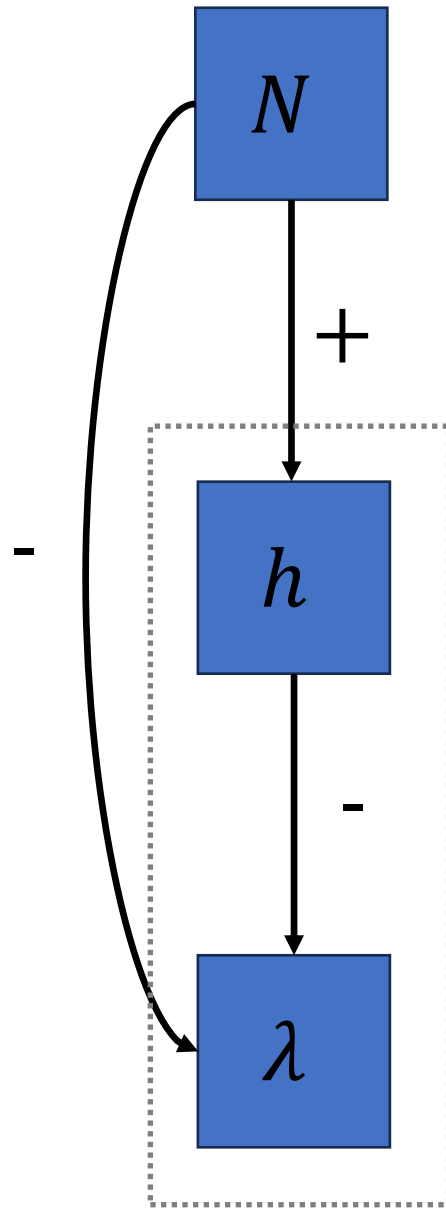
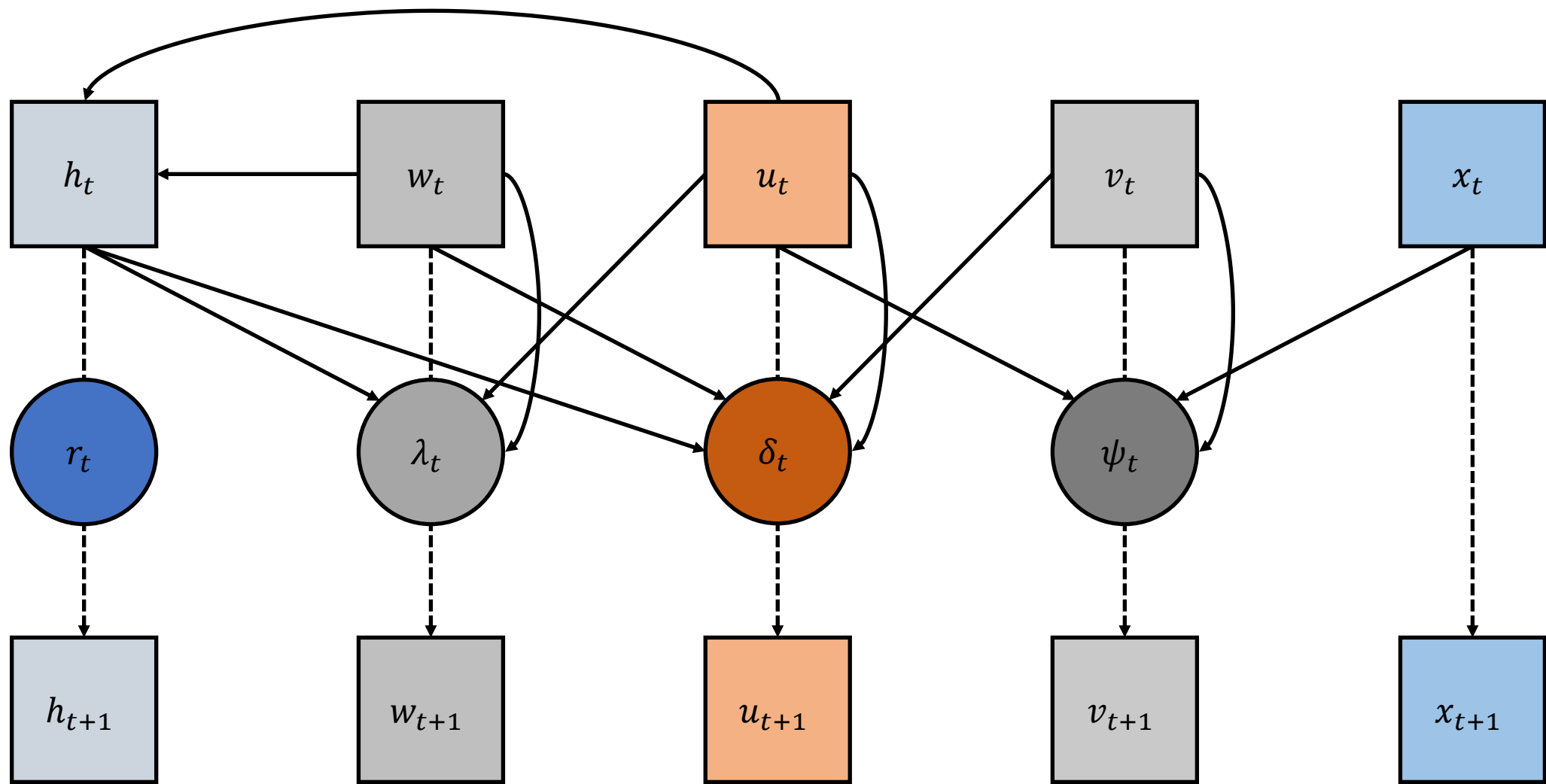


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Humans

Wolves

Ungulates

Veg.

Weather



## **Questions to think about:**

- **How does my system work?**
- **Are my covariates truly 'independent'?**
- **What type of data do I have? What can I acquire?**