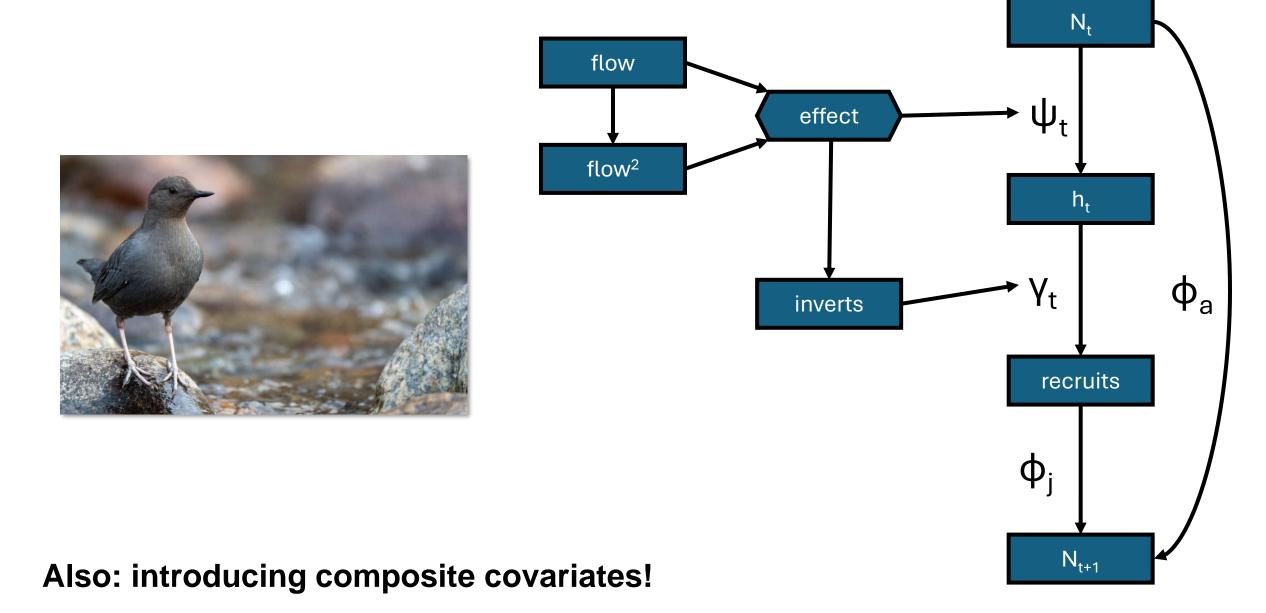
# Case study: modeling reproductive success via path analysis



Today we're going to use composite covariates

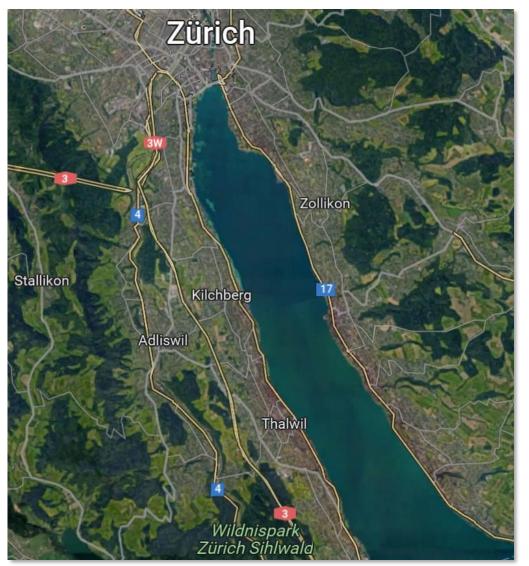
\*Do not use 'blavaan' in JAGS to develop code for composite covariates (bug alert!) See blavaan\_issue.R



# Simulated data (\*based on a true story)



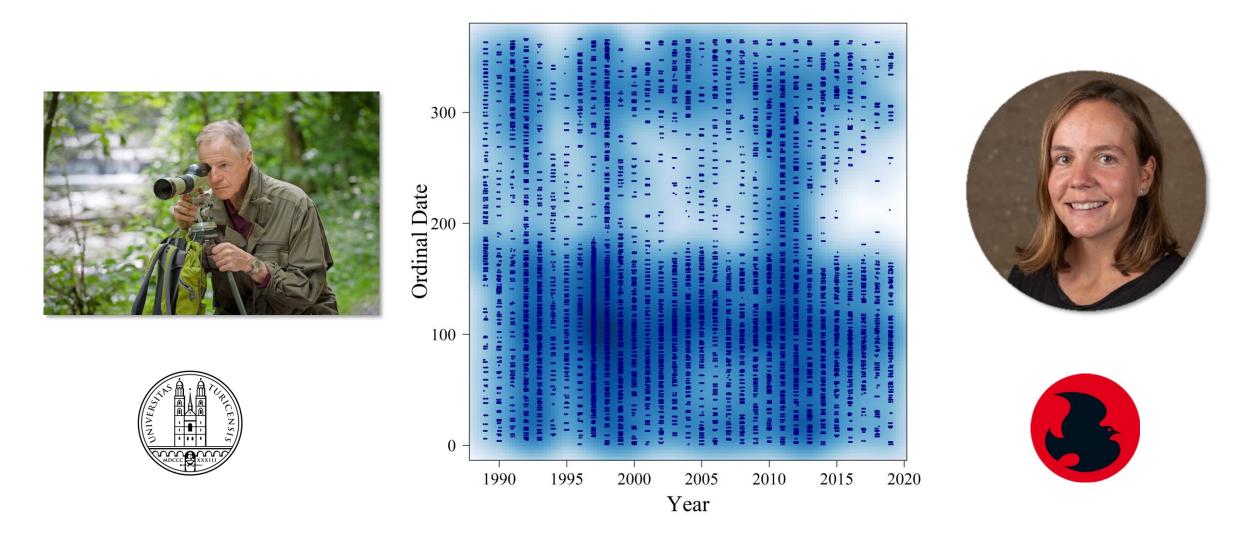






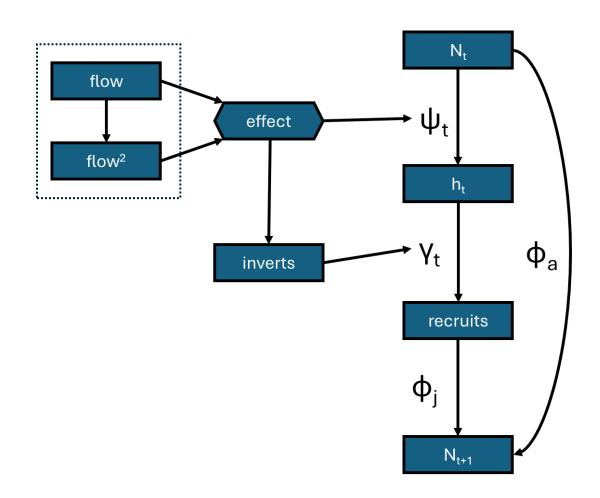


## Simulated data (\*based on a true story)

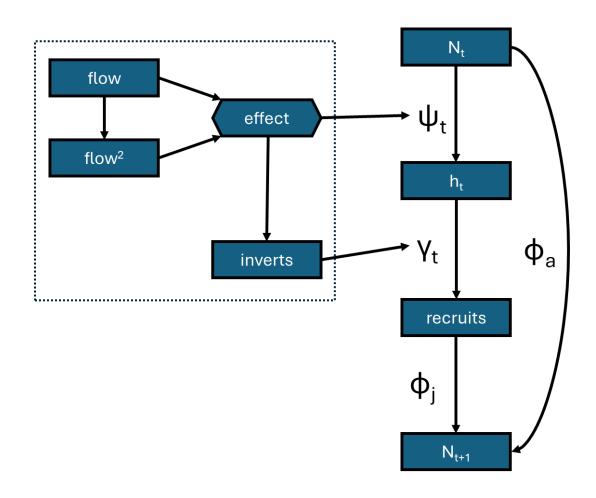


8.5k rings, 3k recaps, 40k resights

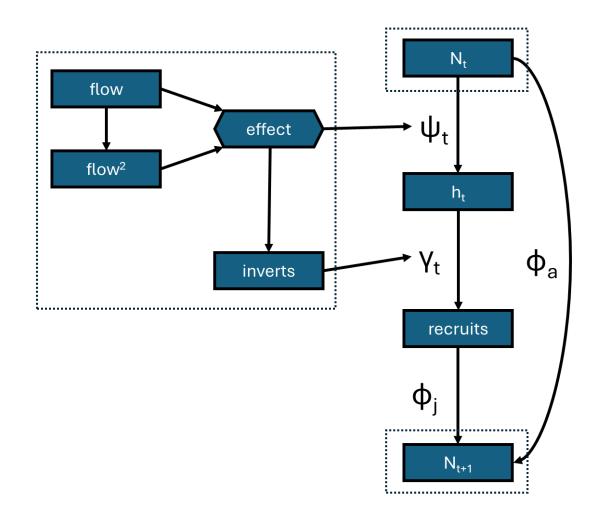
1. Flow rate of our study stream (f)



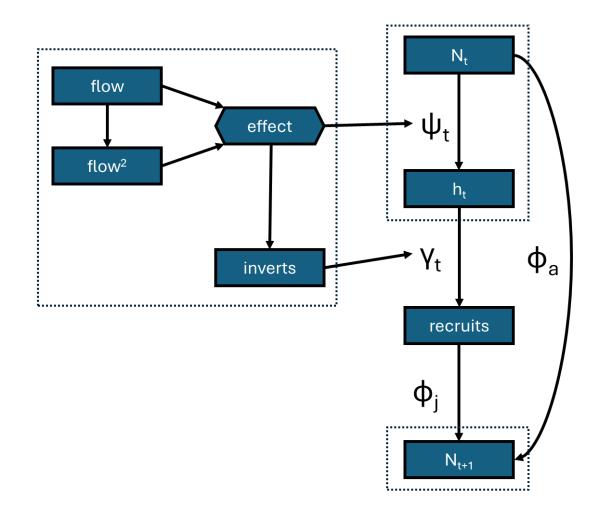
- 1. Flow rate of our study stream (f)
- 2. Invertebrate abundance (i)



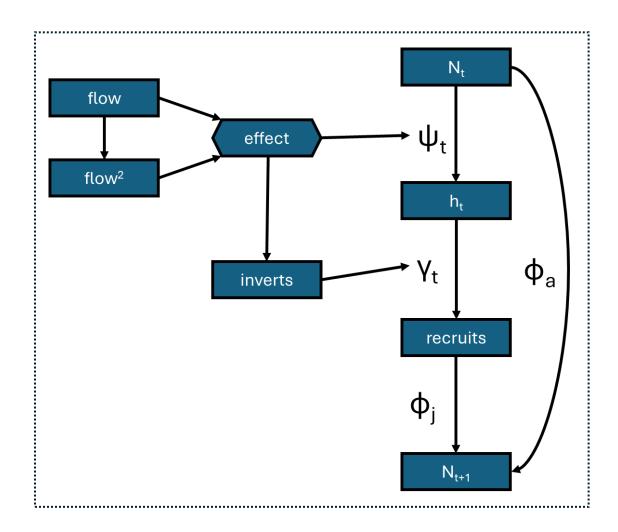
- 1. Flow rate of our study stream (f)
- 2. Invertebrate abundance (i)
- 3. A census (y) of breeding pairs



- 1. Flow rate of our study stream (f)
- 2. Invertebrate abundance (i)
- 3. A census (y) of breeding pairs
- 4. The number of Hatched nests (h)

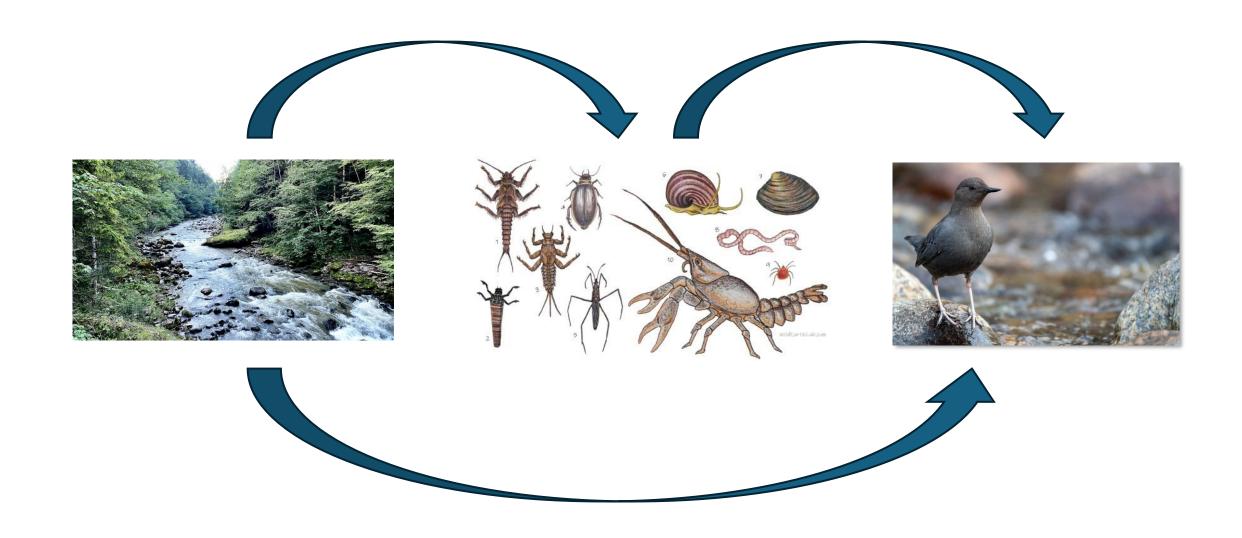


- 1. Flow rate of our study stream (f)
- 2. Invertebrate abundance (i)
- 3. A census (y) of breeding pairs
- 4. The number of Hatched nests (h)
- 5. The number of potential Recruits (r)



We could build an IPM + SEM with these data!

# This ain't that wild conceptually

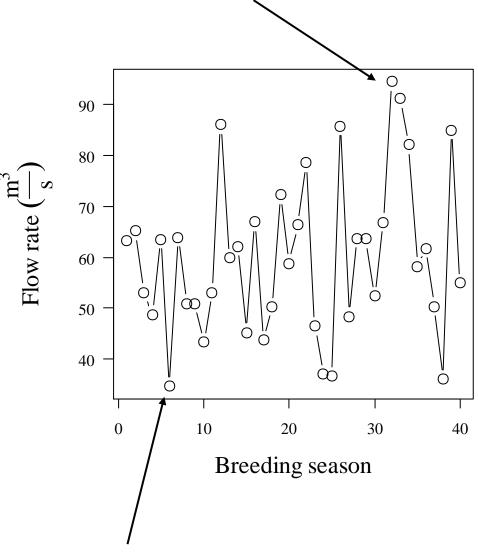


## 1. Flow rate of our study stream (f)

$$f \sim \text{lognormal}(\mu_f = 4, \sigma_f^2 = 0.0625)$$



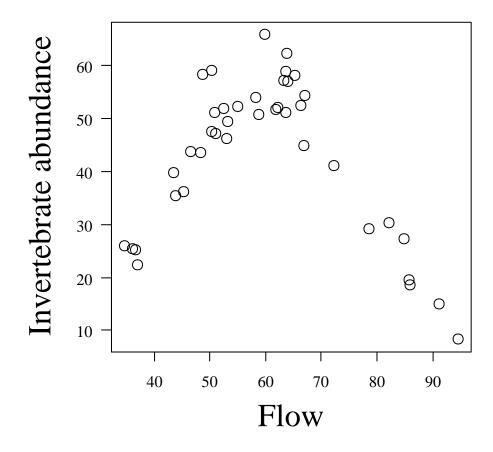
#### **Extreme flooding**

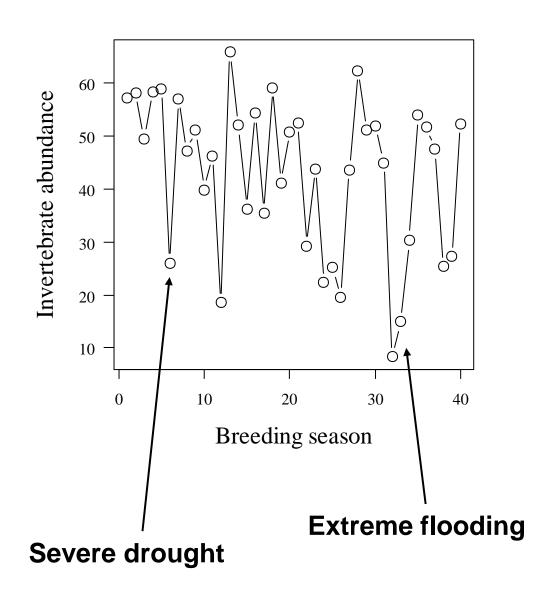


**Severe drought** 

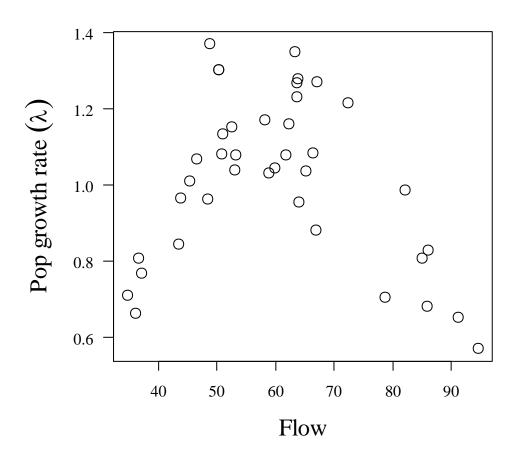
#### 2. Invertebrate abundance (i)

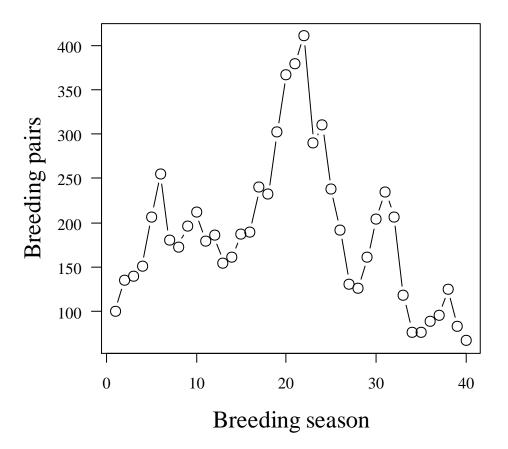
$$i \sim \text{lognormal}(\alpha_1 + \beta_1 f + \beta_2 f^2, \sigma_i^2)$$





# 3. The number of breeding adults (y)

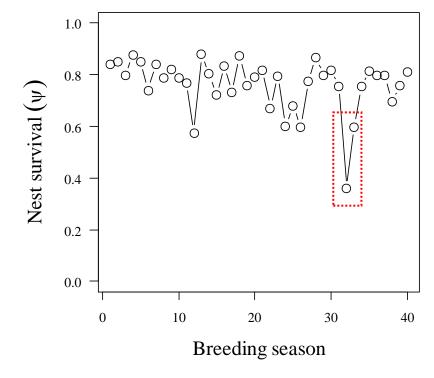


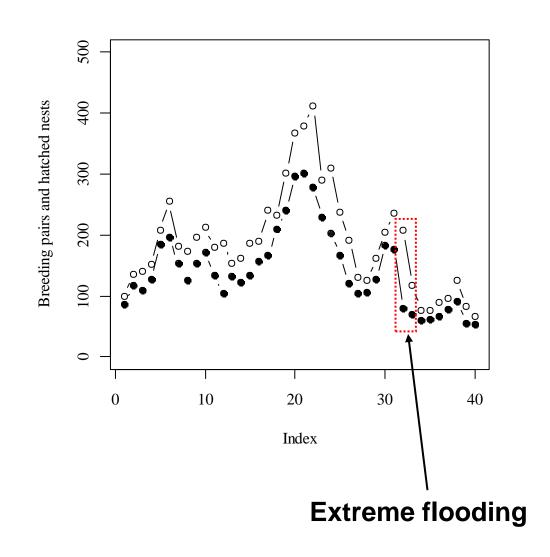


#### 4. The number of hatched nests (h)

 $h\sim$ binomial $(y, \psi)$ 

$$logit(\boldsymbol{\psi}) = \alpha_2 + \beta_3 \boldsymbol{f} + \beta_4 \boldsymbol{f}^2$$



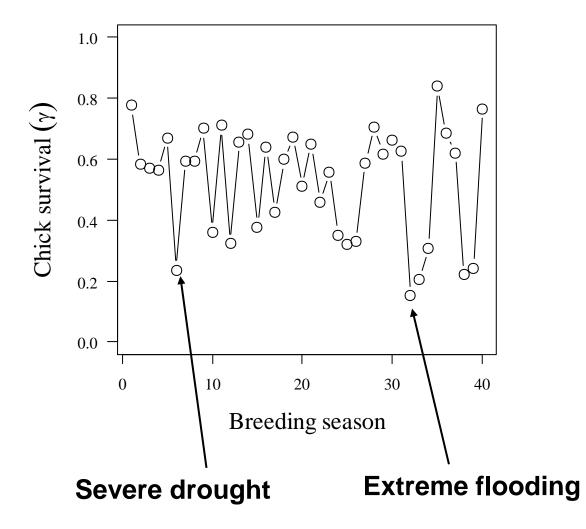


## 5. The number of surviving potential Recruits (r)

$$r\sim Poisson(h \times \zeta \times \gamma)$$

$$\zeta = 4$$

$$logit(\boldsymbol{\gamma}) = \alpha_3 + \beta_5 \boldsymbol{i}$$



 $\zeta$  is clutch size;  $\gamma$  is probability of becoming an independent 'juvenile'

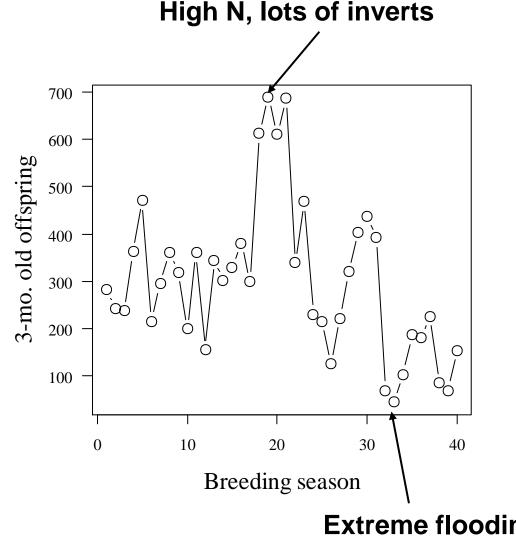
## 5. The number of surviving potential Recruits (r)

$$r\sim Poisson(h \times \zeta \times \gamma)$$

$$\zeta = 4$$



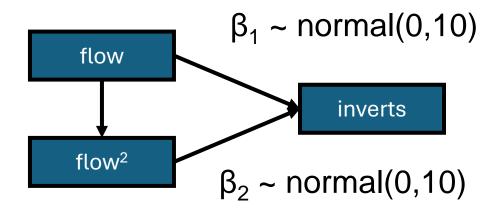
$$logit(\boldsymbol{\gamma}) = \alpha_3 + \beta_5 \boldsymbol{i}$$



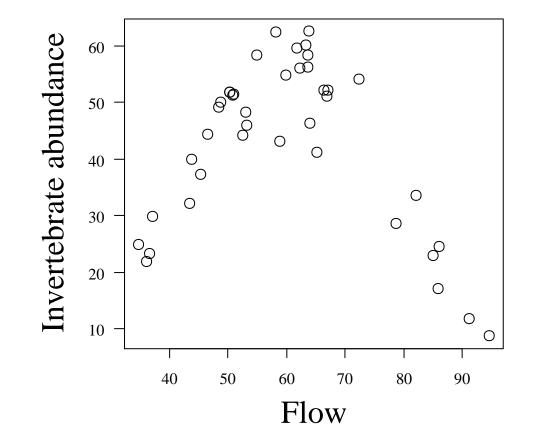
**Extreme flooding** 

 $\zeta$  is clutch size;  $\gamma$  is probability of becoming an independent 'juvenile'

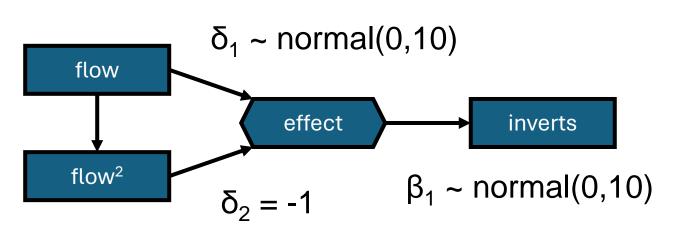
## Ok, so what is a composite covariate?!



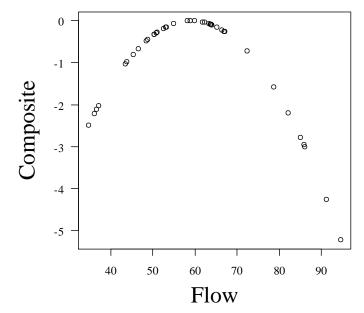
$$i \sim \text{lognormal}(\beta_0 + \beta_1 f + \beta_2 f^2, \sigma_i^2)$$

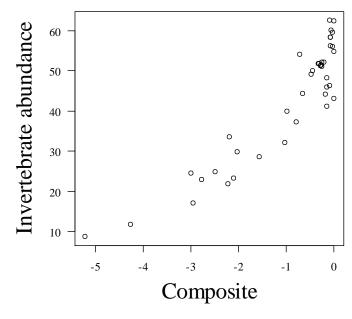


#### Ok, so what is a composite covariate?!



$$\mathbf{c} = \delta_1 \mathbf{f} + \delta_2 \mathbf{f}^2$$
  
 $\mathbf{i} \sim \text{lognormal}(\beta_0 + \beta_1 \mathbf{c}, \sigma_i^2)$ 

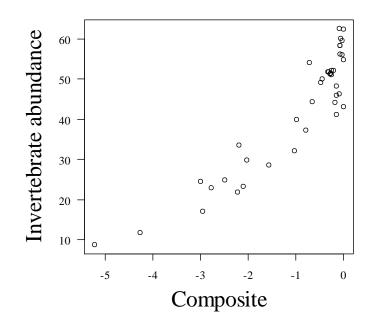


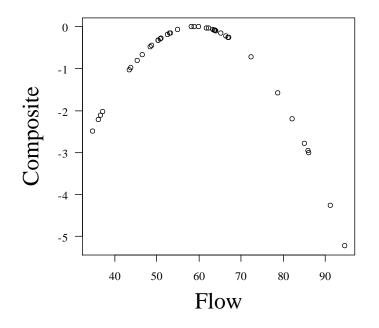


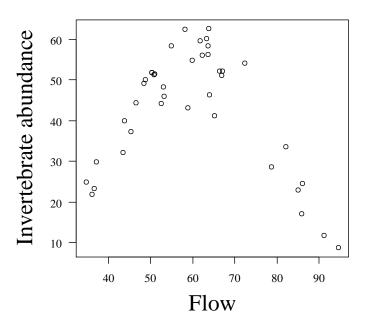
#### 1. What's the difference? 2. Why would we do that?

$$i \sim \text{lognormal}(\beta_0 + \beta_1 f + \beta_2 f^2, \sigma_i^2)$$

$$\mathbf{c} = \delta_1 \mathbf{f} + \delta_2 \mathbf{f}^2$$
  
 $\mathbf{i} \sim \text{lognormal}(\beta_0 + \beta_1 \mathbf{c}, \sigma_i^2)$ 



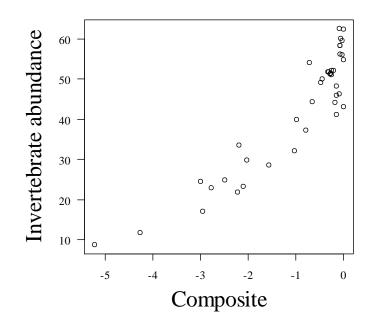


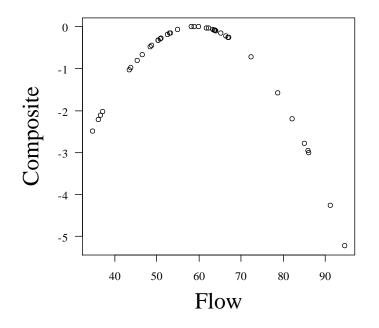


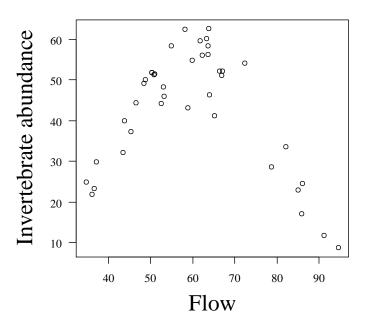
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$$\mathbf{c} = \delta_1 \mathbf{f} + \delta_2 \mathbf{f}^2$$
  
 $\mathbf{i} \sim \text{lognormal}(\beta_0 + \beta_1 \mathbf{c}, \sigma_i^2)$ 







#### Go to the 'in\_class\_question.R' script

#### **Data simulation**

 $\mathbf{x_1} \sim \text{normal}(0,1)$ 

 $x_2 = x_1 + normal(0,1)$ 

 $x_3 = x_1 + normal(0,1)$ 

 $\beta = [1, 0.5, 2]$ 

 $y \sim \text{normal}(\beta X, \sigma^2)$ 

#### Linear model

 $\beta \sim \text{normal}(0,1)$ 

 $y \sim \text{normal}(\beta X, \sigma^2)$ 

#### Composite covariate

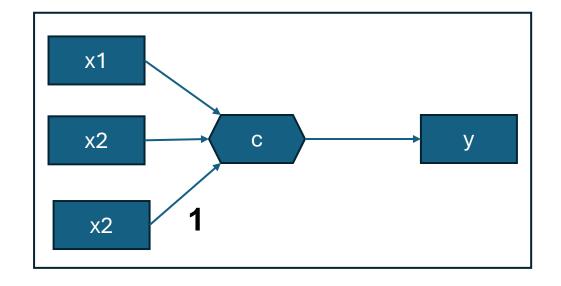
 $\beta \sim \text{normal}(0,1)$ 

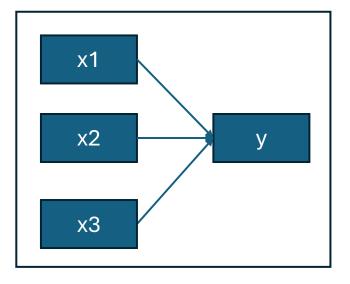
 $c = \beta X$ 

 $\mathbf{y} \sim \text{normal}(\mathbf{c}, \sigma^2)$ 

1. What's the difference? 2. Why would we do that?

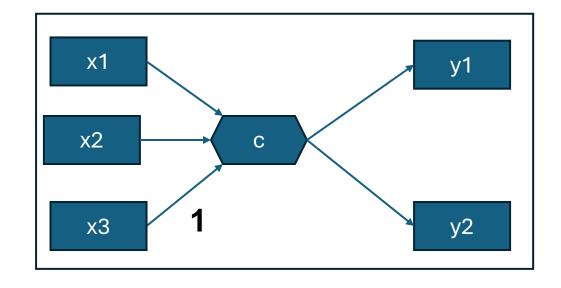
#### 1. What's the difference?

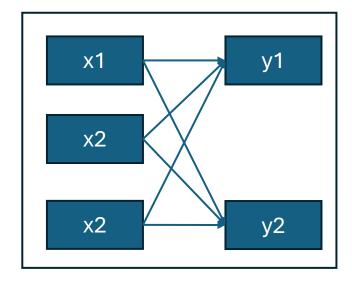




These models are equivalent?!

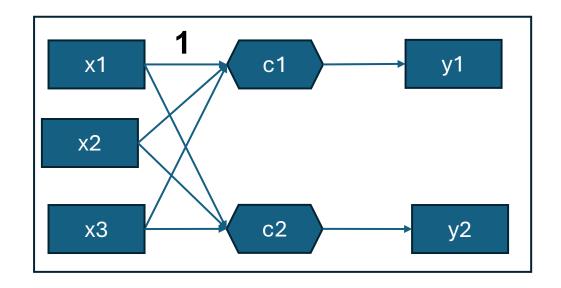
# 2. Why would we do that?

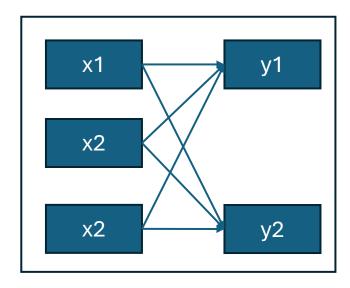




These models don't have to be

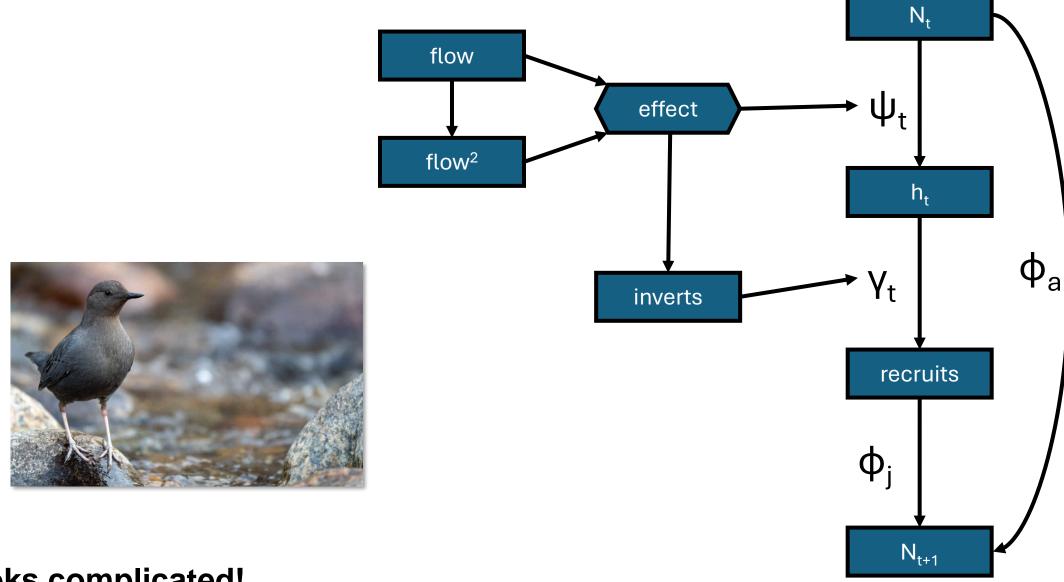
# 2. Why would we do that?





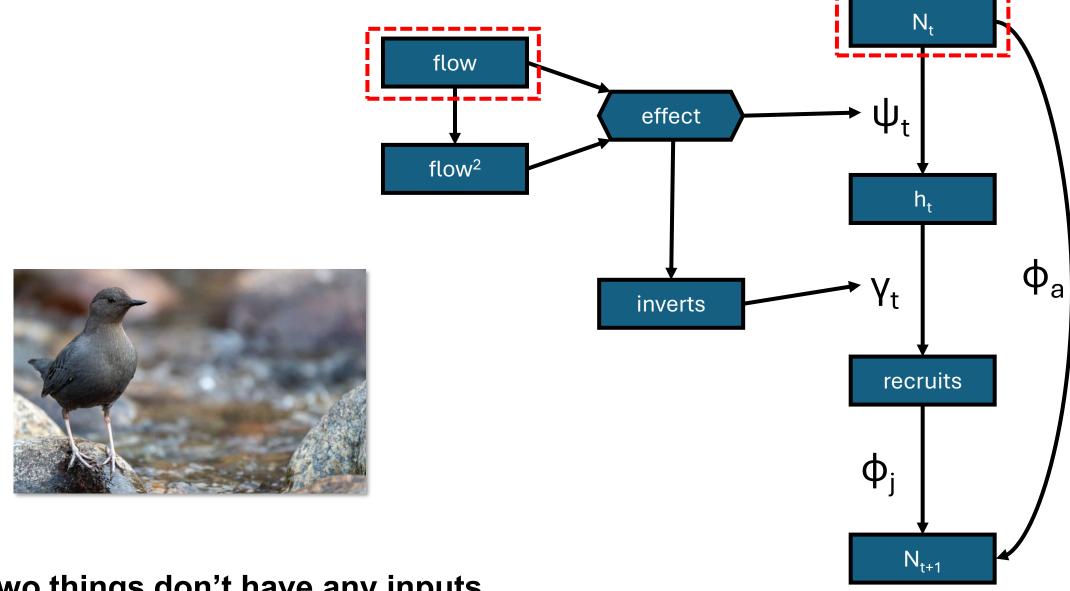
## These models are equivalent

## Let's simulate this population



This looks complicated!

## Let's simulate this population



These two things don't have any inputs...

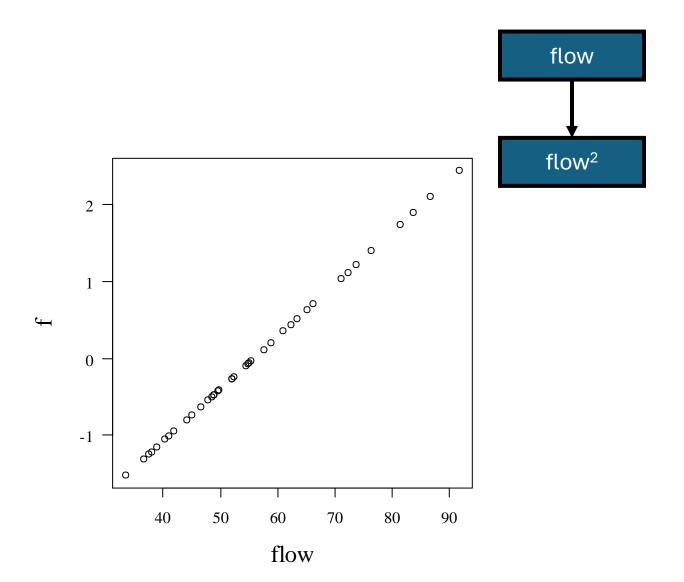
We'll start with some number of breeding pairs ( $N_1 = 100$ )...

 $N_{t}$ 

flow

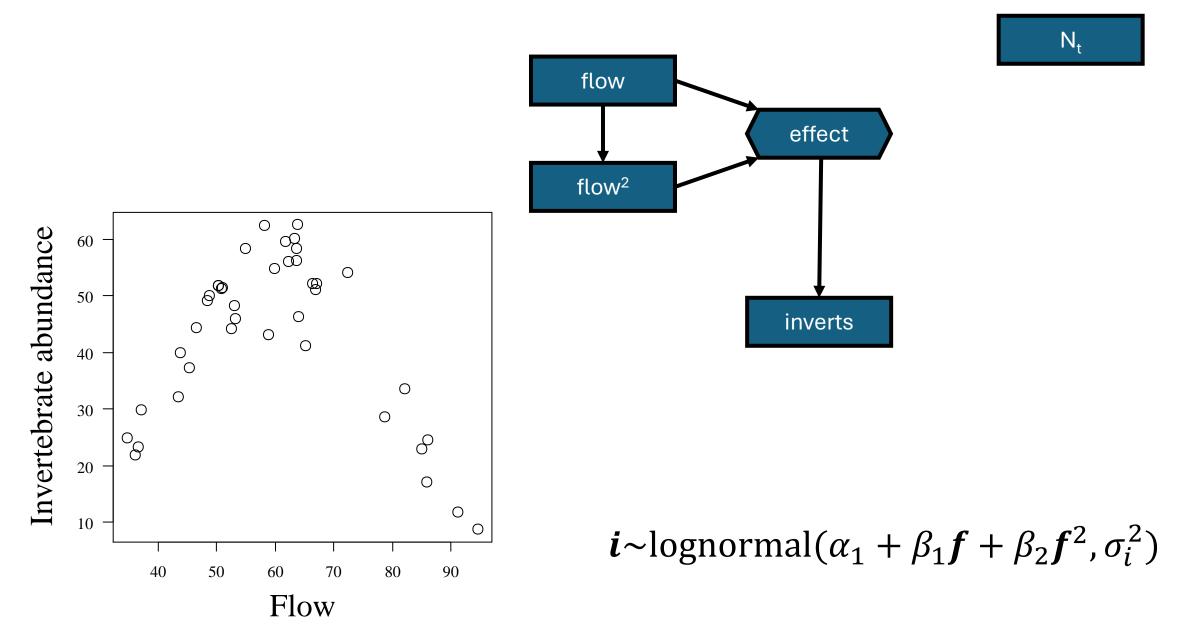
And a flow rate ( $f_1 = 63.2 \text{ m}^3/\text{s}$ ; about half the size of the Clark Fork in spring)

# From there we can z-standardize flow (f), and square it (f<sup>2</sup>)

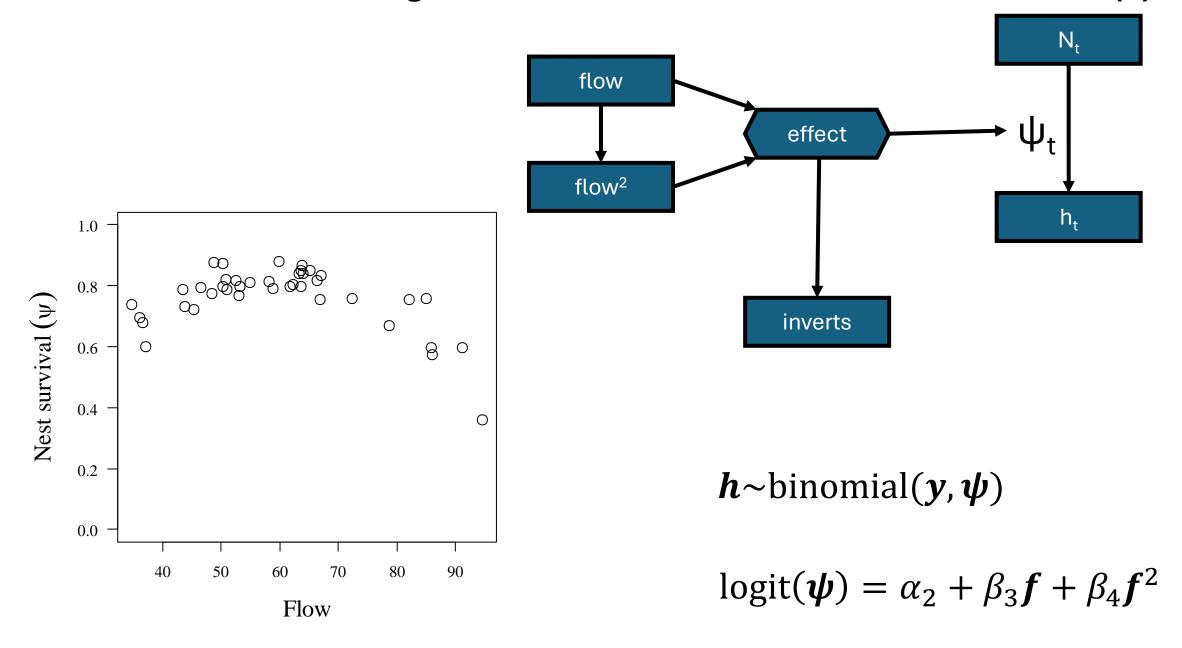


 $N_{t}$ 

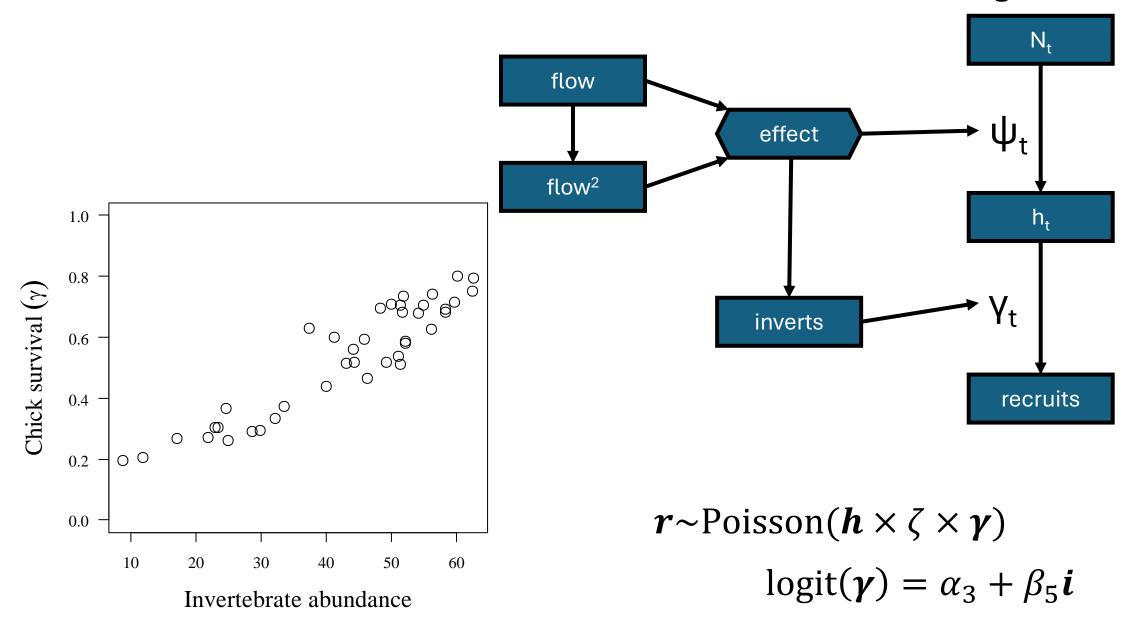
#### Now, we can simulate invertebrates as a function of flow



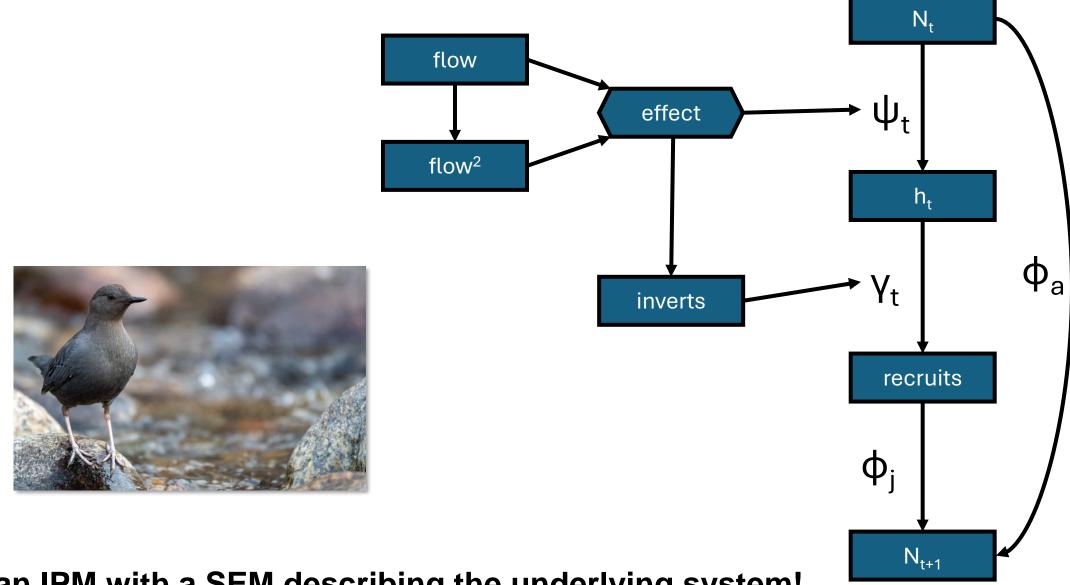
#### We can do the same thing with nest survival to simulate hatched nests (h)



# Then we simulate chick survival as a function of invertebrates to get recruits

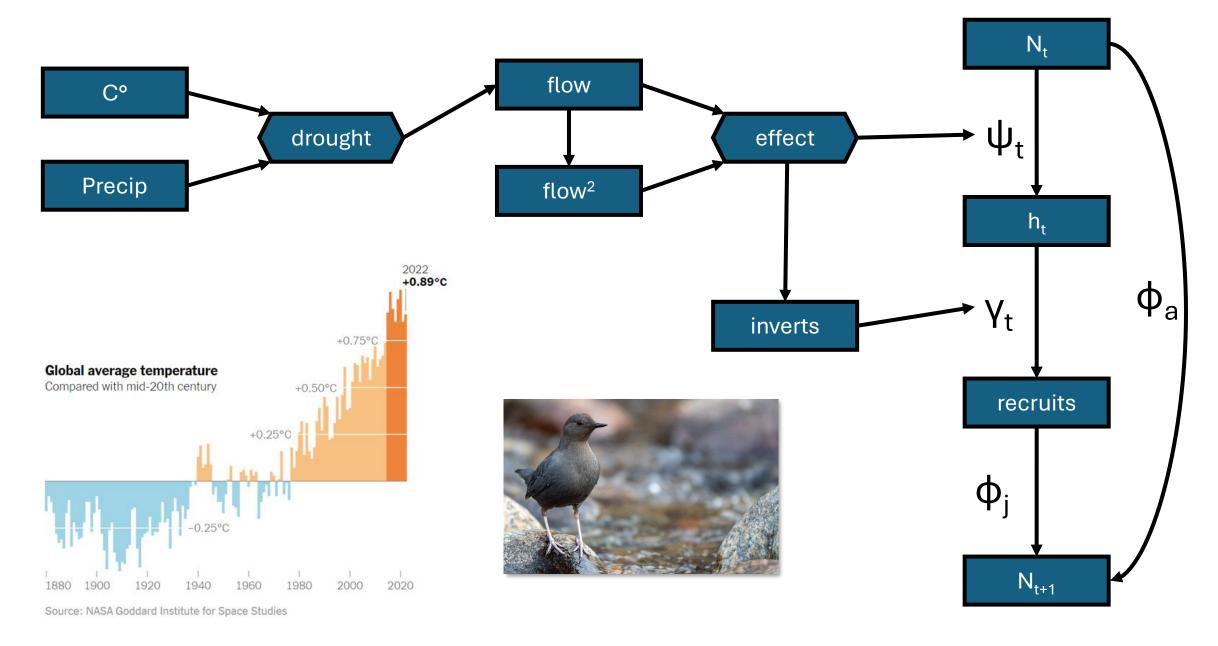


#### And allow adults and potential recruits to survive into the next year

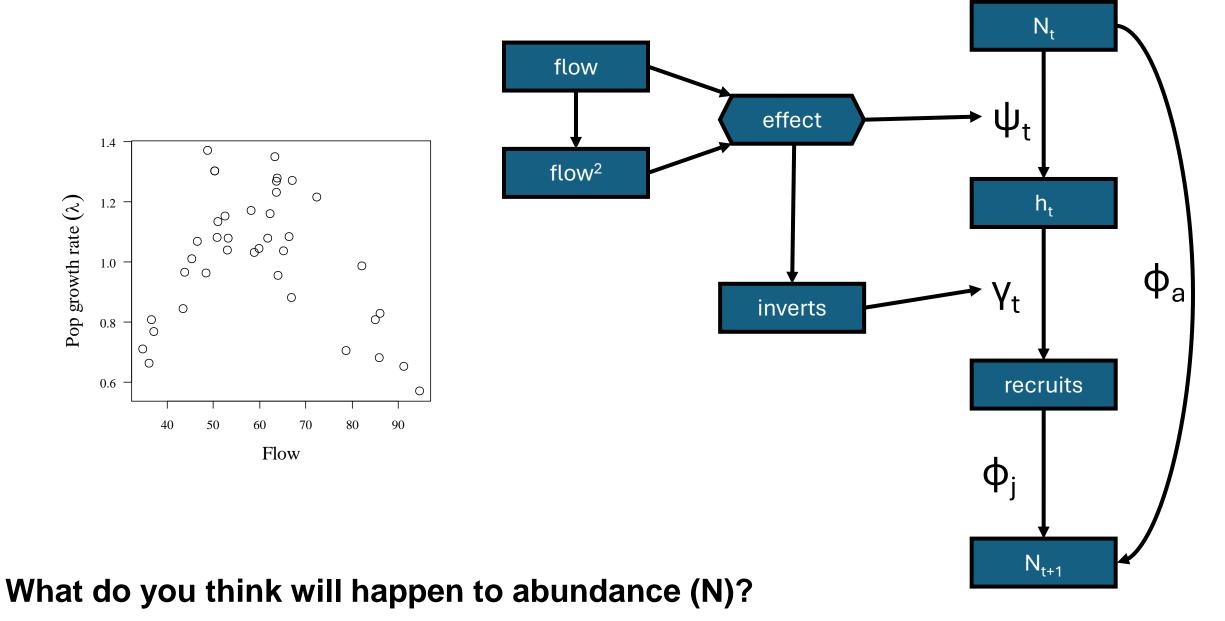


This is an IPM with a SEM describing the underlying system!

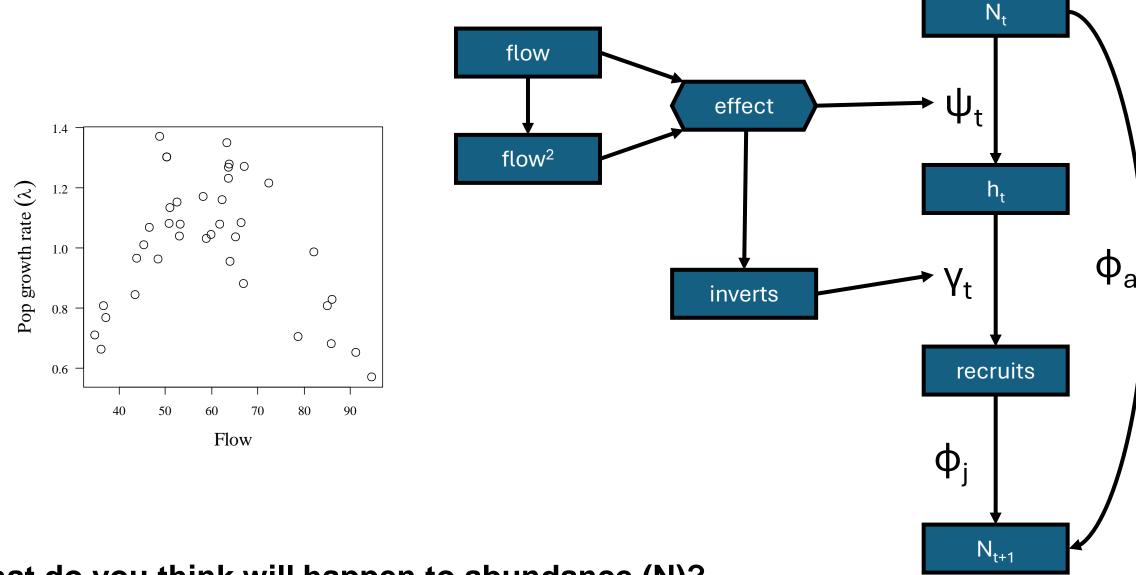
#### Think about how useful this is!



#### Imagine that the mean of flow declines...



#### Now imagine that the variance of flow increases (flood or dry)...



What do you think will happen to abundance (N)?