A network enrichment account of cognitive aging

Thomas T. Hills¹

¹ University of Warwick

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- Correspondence concerning this article should be addressed to Thomas T. Hills,
- 8 Gibbet Hill Road, Coventry, CV4 7AL, UK. E-mail: t.t.hills@warwick.ac.uk

Abstract

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Late-life cognitive development is associated with a decline in fluid intelligence which occurs alongside a corresponding increase in crystallized intelligence. Theory often treats 11 these accounts independently, seeing the former as a consequence of biological aging and 12 the latter as a consequence of learning. What has not been fully explored is that lifelong 13 learning may explain both accounts. This article describes a formal enrichment account that shows how a lifetime of experience encodes a cognitive representation that, when used 15 to guide behavior, produces numerous quantitative effects commonly described for cognitive aging: with age, similarity judgments between concepts fall, free associations become less 17 predictable (higher entropy), and free association networks produced by aggregating output 18 across associates show patterns of declining connectivity. The enrichment account demonstrates how these behavioral outcomes arise when a general prediction error model (Rescorla-Wagner) is used to train a cognitive representation through repeated experience 21 with a structured environment and the cognitive representation is then sampled from to 22 produce behavior. The resulting diffusion of activity and its associated consequences is a 23 general property of network enrichment which also speaks directly to cognitive aging. Moreover, as measures of co-activation, rising entropy and falling similarity judgments 25 provide mechanisms for cognitive slowing, explaining declining fluid intelligence. These results help better inform mechanisms of aging and its associated pathologies by better 27 calibrating our predictions for accounts based on atrophy and enrichment. 28

Keywords: cognitive aging, Rescorla Wagner, spreading activation, network science, free associations, fluid intelligence, crystallized intelligence, cognitive slowing

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Cognitive aging across the adult lifespan is characterized by two distinct and 32 well-documented patterns. As individuals age, measures of working memory, processing 33 speed, and long-term memory show performance decrements from approximately age 20, while at the same time, measures of vocabulary and other kinds of general knowledge 35 increase (Brysbaert, Stevens, Mandera, & Keuleers, 2016; Park & Reuter-Lorenz, 2009; Salthouse, 2004). This distinction between the ability to solve novel problems in a fast and 37 accurate way, called *fluid intelligence*, and the quantity of one's prior knowledge, called crystallized intelligence, is a classic division of intelligence (Cattell, 1987). This division also characteristically distinguishes the old from the young. What explains these age-related changes? Might they be explained by a single process? The evidence I provide below suggests that the answer is yes: the outcome of enriching one's cognitive representation through a lifetime of experiencing associations in the world produces an average decline in activation between any two concepts chosen at random. Before demonstrating how this effect arises, it is first useful to highlight the focal alternative accounts of aging this work addresses and to describe the behavioral effects we hope to explain.

Degradation or enrichment

Cognitive aging is a rich process with evidence supporting a wide range of
phenomenology and theoretical explanations (Cao et al., 2014; Grady, Springer,
Hongwanishkul, McIntosh, & Winocur, 2006; Koen & Rugg, 2019; Mata, Schooler, &
Rieskamp, 2007; e.g., Reuter-Lorenz & Cappell, 2008; Spreng & Turner, 2021; Troyer,
Moscovitch, & Winocur, 1997). Much of this work is often interpreted as supporting either
degradation-based accounts (e.g., involving declining frontal lobe or executive function and
neural atrophy) or enrichment-based accounts (e.g., involving adaptive consequences of

lifelong learning), and sometimes both. This dichotomy between things falling apart or things coming together is well characterized by the distinction between fluid and crystallized intelligence.

Declines in fluid intelligence are often seen as independent of rising crystallized 59 intelligence. One prominant explanation for declines in fluid intelligence is the common 60 cause theory of age-related cognitive decline, which argues that biological aging in the 61 brain is the source of processing speed deficits (Deary et al., 2009). The supposition is that aging is a general process of degradation, in which factors like oxidative stress and telomere 63 shortening damage the physiological mechanisms underpinning cognitive performance. Salthouse (1992) describes some potential mechanisms as follows: "a slower speed of transmission along single (e.g., loss of myelination) or multiple (e.g., loss of functional cells dictating circuitous linkages) pathways, or. . . delayed propagation at the connections between neural units (e.g., impairment in functioning of neurotransmitters, reduced synchronization of activation patterns)" (p. 116). Consistent with this, percent volume of grey and white-matter declines in late life (Ge et al., 2002; Giorgio et al., 2010). Cortical 70 thickness also declines alongside increases in cerebrospinal fluid space (Lemaitre et al., 71 2012). These findings are often associated with atrophy and fit with common intuitions for biological aging—as biological things fall apart, so do the cognitive counterparts which they underpin. Moreover, neuropathology—associated with posthumously verified evidence of Alzheimer's and other neurodegenerative and cerebrovascular disease—accounts for up to 40% of the variation in late-life cognitive decline (Boyle et al., 2021). Though this leaves substantial variance in cognitive-decline unexplained, it nonetheless identifies an important correspondence between biology and cognition, especially in unhealthy aging. 78

Alternatively, and far more rarely, some accounts of cognitive aging have proposed an causal interdependence between the positive consequences of learning associated with crystallized intelligence and the resulting negative consequences for fluid intelligence. For example, Buchler and Reder (2007) showed using simulations that if they assumed that the

number of relations between concepts increased over the lifespan this would lead to more
diffuse activation between concepts, analogous to a contextual fan effect. This reproduced
age-related changes in recognition and familiarity. Using a different approach, Ramscar,
Hendrix, Shaoul, Milin, and Baayen (2014) demonstrated how associations would change
through repeated learning. They based their work on Desrosiers and Ivison (1986) study of
paired-associate learning in older adults, which found that older adults perform most poorly
on stimuli that are least consistent with their prior experience. Ramscar, Sun, Hendrix,
and Baayen (2017) showed that the difficulty of learning unrelated word pairs is entirely
predictable from the co-occurrence frequency of those pairs in past experience. Training a
Rescorla-Wagner model on typical patterns of word co-occurrences, unrelated word pairs
become negatively associated over time, impairing the future learning of their association.

Still more recent work has argued for a much broader influence of age-related mental 'clutter', which may arise from representational changes across the lifespan as well as changes in cognitive control at the time of encoding or retrieval (Amer, Wynn, & Hasher, 2022). According to this account, processing deficits and the inability to filter out past experience can lead older adults to attend to too much information. This in turn creates processing difficulties when that information turns out to be irrelevant. For example, Li and Siew (2022) showed older individuals were more likely to show processing difficulties for words that changed their meaning during their lifetime. Though there is no existing formal model of clutter development, the enrichment account provided below offers one.

The different accounts describe above can be broadly categorized as degradation versus enrichment accounts, and the evidence for both is compelling. However, to what extent we subscribe to one explanation over another should largely depend on how they work and what they explain. To my knowledge, the degradation accounts have not provided formal computational mechanisms for how degradation might lead to the observed age-related changes in healthy individuals. Presumably such mechanisms could be developed and would offer useful predictions. For example, Borge-Holthoefer, Moreno, and

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Arenas (2011) have developed a compelling model of degradation for hyper-priming in
Alzheimer's patients, but similar models for healthy aging are still needed. A key challenge
for formal degradation models is that they would need to explain how degradation alters
fluid intelligence but not crystallized intelligence.

On the other hand, enrichment explanations either assume more connectivity (e.g., 114 Buchler & Reder, 2007) or evaluate how differential experience impairs or enhances 115 pair-wise associations (e.g., Ramscar et al., 2014). As called for elsewhere (Wulff, De 116 Deyne, Jones, & Mata, 2019), what is lacking in both cases is a full model of representational development and behavior across the adult lifespan that takes into 118 account our understanding of the aging lexicon. This would represent a computational prediction for what we should expect from lifelong enrichment and what remains to be 120 explained by degradation. This is what we hope to achieve here. To benchmark such a 121 model, we can use a number of empirical observations made over the last decade. 122

The aging lexicon, entropy, and similarity

Several efforts to chart the mental lexicon across the lifespan have identified 124 reproducible trends. Dubossarsky, De Devne, and Hills (2017) asked over 8000 people, 125 ranging in age from roughly 10 to 70, to provide three free associates to each of 420 words. 126 With approximately 1000 people in each age group, data was aggregated within age-groups 127 to produce networks among the 420 words with edges representing a weighted function of 128 common associates. After removing edges below a threshold, older networks were found to 129 have a lower average degree (number of associations per word) higher average shortest path length (greater distance between associates), and lower average clustering coefficient (the 131 proportion of a concept's neighbors that are themselves connected). Evidence also identified a rising entropy for associations, with associates becoming less predictable across 133 the lifespan. Both Zortea, Menegola, Villavicencio, and Salles (2014) and Wulff, De Deyne, 134 Aeschbach, and Mata (2022) found similar patterns with varying numbers of participants 135

and cues and with some variations based on network construction methods.

Analyses of memory search in older and younger adults also find consistent patterns 137 of change in the aging mental lexicon. Using a semantic fluency task ("name all the 138 animals you can think of"), Wulff, Hills, and Mata (2022) constructed lexical networks by 139 connecting words that appeared nearby in the lists that older and younger adults 140 produced. Older adults' produced less well-connected networks, similar to the patterns for 141 free associations described above. Hills, Mata, Wilke, and Samanez-Larkin (2013) modeled 142 semantic fluency data from adults across the lifespan and found that, compared with 143 younger adults, older adults produced strings of animal names that were less predictable, 144 one from the next. Finally, Cosgrove, Kenett, Beaty, and Diaz (2021) used percolation 145 analysis to investigate the resilience of older adults' mental lexicons by artificially removing 146 connections between words and found that older adults' lexicons were less resilient to 147 decay. These findings are all suggestive of more sparse connectivity in the outputs retrieved 148 from the mental lexicon.

Slower judgments of similarity between words are consistent with the above patterns.

Wulff, Hills, et al. (2022) asked younger and older adults to judge the similarity of 77

different animals over a period of several weeks using a tablet participants took to their

homes. Rating the similarity of pairs of animals on a scale from 1 to 20, they found that

older adults rated animals as less similar to one another than did young adults. Again, this

indicates a sparsening of the connectivity between concepts in the mental lexicon.

The above results indicate that older adults produce less predictable associations
(higher entropy), lower similarity judgments, and show evidence of sparsening free
association networks. These results are intuitively consistent with representational
degradation: one may imagine that a sparseness in output reflects a sparseness in the
underlying representation, which is in turn caused by degradation in the neural
architecture that underpins it. However, without understanding what we might expect

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from lifelong learning, efforts to explain cognitive aging as the result of degradation may attempt to bridge an explanatory gap that does not exist. Moreover, degradation accounts 163 may even get the causation backwards. Which is to say, if life experience gives rise to some 164 of the primary markers of age-related cognitive decline, then so-called atrophy in 165 physiological structure may not be the cause of age-related cognitive decline. Rather, it 166 may be the consequence of life-long experience. As demonstrated below, by extending 167 standard learning and retrieval models across the lifespan, we can predict all of the above 168 effects—rising entropy, falling similarity, and sparsening free association networks—as a 169 consequence of enrichment, without the need for assuming any additional processes 170 associated with biological aging or degradation. 171

The enrichment account

The enrichment account envisions behavior as the outcome of learning relationships from the environment to develop a cognitive representation, and then using this representation to generate behavior. This follows calls from previous researchers to model not only the representation but the processes that access that representation to generate behavior (Castro & Siew, 2020; Estes, 1975; Hills & Kenett, 2022; Johns, Jamieson, & Jones, 2023; Jones, Hills, & Todd, 2015). Formally, the enrichment account involves modeling three separate components:

- 1. Environment: The environment presents the set of all possible associations that could be learned.
- 2. Representation: Learning associations from the environment generates a cognitive representation. This continues to develop across the lifespan.
- 3. Behavior: Behavior is recovery of information from the cognitive representation appropriate to the environmental context. This generates free-associations, memory search, similarity judgments, and so on.

These stages are presented in Figure 1 and each are explained in detail below. The R code to reproduce the environments, the learning of cognitive representations, the behavior, and all analyses and figures in this manuscript are available at https://github.com/thomasthills/enrichment.

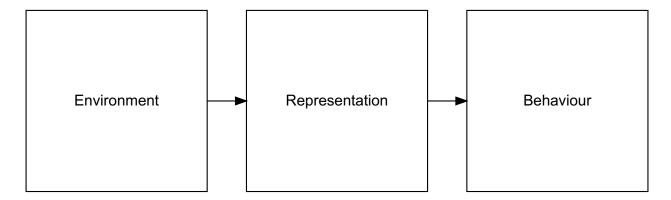


Figure 1. The process of translating experience with the environment into behaviour. Arrows represent processes that translate one domain into another. Learning translates experience with the environment into a cognitive representation. Additional cognitive processes then act on the representation to generate behavior.

191 Environment

The environment is represented here as network of concepts (e.g., words), with the 192 edges (links) between concepts indicating associations that can be learned. This follows the 193 basic idea that things in the world predict one another, and learning is here taken to 194 address one association at a time. The qualitative pattern of behavioral results described 195 below are not dependent on the specific network structure. To demonstrate this, I use a general framework for network construction. This is a variation of a fitness-based network 197 model (Menczer, Fortunato, & Davis, 2020) in which all nodes are present at the start and 198 edges are formed using rank-based sampling. Each concept is assigned a rank, r, from 1 to 199 n. Then pairs of concepts are chosen from the lexicon each with probability $p \propto r^{-a}$ and an 200 edge is created between them. When a=1, this process produces a scale-free network, 201

which is characterized by a long-tail in which most concepts have very few associations and a few have very many. This structure is consistent with the ubiquity of scaling laws in the cognitive sciences and the natural world (Johns & Jones, 2010; Kello et al., 2010). Providing a useful point of comparision, when a = 0 the resulting network approximates a weighted Erdös-Renyi random graph, in which all nodes are connected with equal probability.

The estimate of the number of concepts people know in late life varies widely. A 208 factor of 10 estimate is generally around 100,000, though this increases across the lifespan 209 (Brysbaert et al., 2016). The number of relationships between concepts is limited only by 210 the network size and the human capacity to relate them. In practice, humans report only a 211 subset of all potential associations (De Deyne, Navarro, Perfors, Brysbaert, & Storms, 212 2019; Nelson, McEvoy, & Schreiber, 2004). For example, the number of associations people 213 reported between the approximately 12,000 cues provided in De Deyne et al. (2019) 0.15%214 of the approximately 72 million possible associations. These are unlikely to represent all 215 possible associations in the environment or in their cognitive representation. For example, 216 people rarely provide "eyes" as an associate of "horse", though most people probably see 217 horses with eyes about as often as they see horses. This makes predicting the number of 218 associations in the environment problematic. For the purposes of demonstration, a small 219 vocabulary is used of n = 500 concepts. From these concepts, 2000 pairs are sampled (with 220 replacement) and weighted edges are formed between them, with the weight corresponding 221 to the number of times the pair is chosen. The edges are weighted and undirected. Figure 2 222 presents two example networks and their weighted degree (strength) distributions for the different values of a. The Supplementary Material demonstrates that the qualitative pattern of results presented here is not altered by substantially increasing or decreasing the 225 number of sampled pairs.

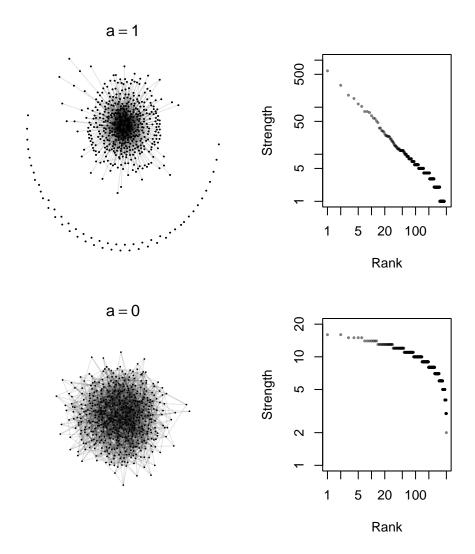


Figure 2. The structure of the environment for two network types: A scale-free network (a=1) and a weighted Erdös-Renyi random graph (a=0). Each network has 500 concepts (or nodes) and the weighted edges between them are the result of repeatedly sampling 2000 pairs of nodes and adding 1 to the edge weight between the pairs. The strength distributions (sum of the edge weights) are shown to help communicate the difference in the underlying structure.

27 Representation

Cognitive representations are built from experience with the environment. I use the 228 prediction error framework set out in the Rescorla-Wagner model (Rescorla & Wagner, 229 1972) to encode properties of the environment into a cognitive representation. The choice 230 of the Rescorla-Wagner model follows the strong evidence for learning as a process of 231 minimizing prediction error, which is a fundamental assumption among models of 232 reinforcement learning (Dayan & Abbott, 2005; Hoppe, Hendriks, Ramscar, & Rij, 2022; 233 McClelland & Rumelhart, 1981; Sutton & Barto, 2018). The Rescorla-Wagner model 234 captures this phenomenology—including associative learning, blocking, inhibition, and 235 extinction—and it is a model on which many subsequent models have been based (e.g., Sutton & Barto, 1981). Though it is not without limitations (Miller, Barnet, & Grahame, 237 1995; e.g., Yau & McNally, 2023), these are largely irrelevant here and the Supplementary Material shows that removing a key assumption (the context cue) does not alter the 239 results. I therefore use the model to capture the generic prediction-error process inherent 240 in the Rescorla-Wagner design and in recognition of its extreme predictive utility (Miller et 241 al., 1995; Roesch, Esber, Li, Daw, & Schoenbaum, 2012; e.g., Soto, Vogel, 242 Uribe-Bahamonde, & Perez, 2023; Trimmer, McNamara, Houston, & Marshall, 2012). 243 Formally, the Rescorla-Wagner model minimizes the prediction error between the 244 values of an observed outcome, j, and a cue predictive of that outcome, i. The value 245 associated with the outcome is λ_j and the value for that outcome as predicted by the cue is $V_{i\to j}$. The prediction error is the difference between them, $(\lambda_j - V_i)$, and it is minimized following each learning event according to the following rule:

$$\Delta V_{i \to j} = \alpha_i \beta_j (\lambda_j - V_{i \to j})$$

The parameter α_i corresponds to the salience (some cues are easier to learn about than others) and β_j to the learning rate (some outcomes are learned about faster than

others). Both α and β values are confined to values between 0 and 1. After learning at time t, the updated cue value is

$$V_{i \to j, t+1} = V_{i \to j, t} + \Delta V_{i \to j, t}$$

Thus, with repeated experience, $V_{i\to j}$ will approach the observed value λ_j . This follows exactly the formalization set out in prior work (Ramscar et al., 2017; Rescorla & Wagner, 1972).

The cognitive representation is formed by applying the Rescorda-Wagner model to the 256 environment in the following way. Each learning event randomly samples a relationship 257 (i.e., edge) from the environment in proportion to its weight (the number of times it is 258 represented in the environment). Of the two concepts associated with the relationship, one is randomly assigned as the cue and the other as the outcome. The representation is then updated according to the Rescorla-Wagner model. Here, we let all outcomes be equivalent 261 and associated with $\alpha = 1$ and $\lambda = 1$. To demonstrate that the qualitative results are not 262 dependent on the precise learning values, β is varied from .01 to .1 in the manuscript, and 263 from .1 to .5 in the Supplemental material, covering the range of values common to this 264 model in the literature cited above. 265

To simulate development, learning occurs in 4 epochs each with 200 learning trials.

The precise number of learning trials per epoch is unrelated to the qualitative pattern of results, and is explored further in the Supplemental Material. Figure 3 provides examples of two learning representations over the four epochs for the different network types (a = 0 and a = 1) and varying values of β .

Results: Behavior

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The stylized facts associated with cognitive aging are rising entropy, a reduction in pairwise similarity judgments, and changes in the structure of the free association network.

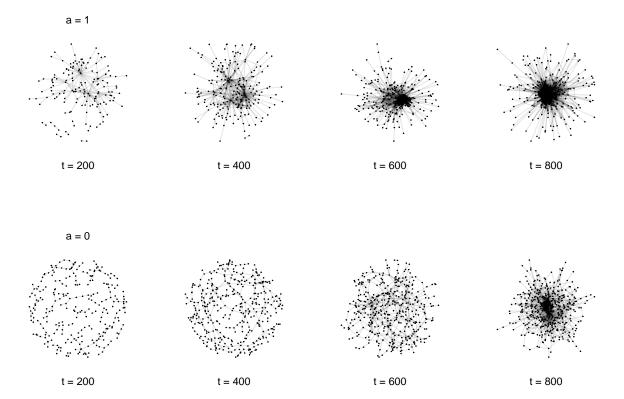


Figure 3. Examples of the growing mental lexicon resulting from training a Rescorla-Wagner model on the network types shown in Figure 2. Training occurs in 200 event epochs, with edges from the environment sampled in proportion to their weight. Nodes represent individual concepts and edges represent learned associations.

Each of these is recovered from the representation as described below. In each case,
environments are constructed independently 1000 times and then learning occurs over 4
epochs of 200 trials each.

Rising entropy. Rising entropy refers to the reduction in the predictability of free association targets as individuals age (Dubossarsky et al., 2017). We can measure this using Shannon's information entropy. This measures the surprisingness of associates given the cue. If a cue has only a few strong associations, any given associate will be less surprising than if it has many equally weighted associations. Because the output of Rescorla-Wagner learning is a weighted edge, we can compute this for every cue in the network representation as follows:

$$H = -\sum_{i=1}^{k} p_i log(p_i)$$

Here, p_i is the proportion of the weight along edge i for all k edges for that cue. That is, $p_i = \frac{w_i}{\sum_k w_k}$. The entropy for the network reported below is the mean across all cues.

This is taken here to represent the long-term entropy of persons producing repeated associations for each cue.

The result of this computation is shown in Figure 4. For various network constructions and learning rates, the results consistently show that entropy rises with increased learning, following that observed in Dubossarsky et al. (2017). In addition, entropy is higher in the scale-free network than in the weighted Erdös-Renyi random graph.

Falling similarity. To simulate similarity judgments, we can create a measure of co-activation between cues. To do this, we allow spreading activation to leave one node and measure activation at the other node, $A_{j\to k}$. This allows us to measure the extent to which one word co-activates the other. Doing this for both cues, we take similarity as the summed co-activation.

$$S = A_{j \to k} + A_{j \to k}$$

We measure this similarity for a random selection of 20 concept pairs in the representation, all of which are learned during the first epoch of learning. This ensures that individuals at each age (epoch) have experience with the concepts.

The result of this computation is shown in Figure 4. For various network
constructions and learning rates, the results consistently show that similarity judgments
fall with increased learning, following that found in Wulff et al. (2019). In addition,
similarity is smaller for the scale-free network than the Erdös-Renyi random graph.

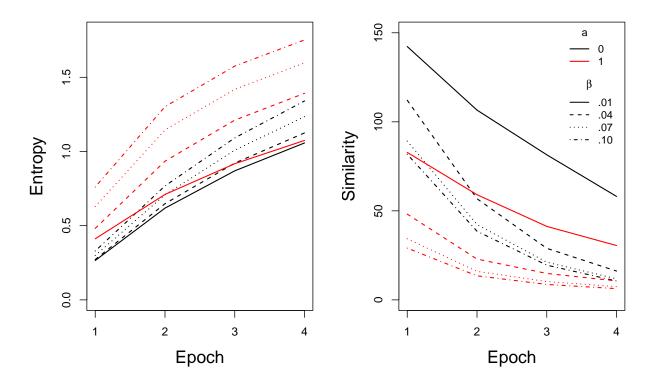


Figure 4. Entropy and similarity measures computed from the cognitive representation at different epochs of development.

Sparsening free association networks. As noted above, Dubossarsky et al. 304 (2017) and others found that free association networks collected across the adult lifespan 305 showed patterns of decreasing network degree, increasing average shortest path length, and 306 decreasing clustering coefficient. We simulate this on the cognitive representations across 307 the four epochs as follows. For each cognitive representation, we simulate 10 participants 308 who retrieve 3 associates from each of 30 cues. The three associates are sampled without replacement for each participant and each cue is sampled in proportion to the associative 310 strength encoded in the cognitive representation, i.e., the output from the Rescorla-Wagner 311 training epochs. Negative association strengths are set to 0. This produces a cue by 312 associate matrix, with each cell indicating the number of times each associate was 313 produced in response to each cue. From this matrix, cue-by-cue similarities are computed 314

using cosine similarity of their corresponding associate vectors. To transform these into 315 unweighted and undirected networks, the median cue-by-cue similarity is computed across 316 all epochs and, for each age, cue similarities below this median value are set to 0, and all 317 other values are set to 1. This matrix is then transformed into a network on which degree 318 (the number of connections), average shortest path length (the shortest number of edges 319 between cues), and clustering coefficient (the proportion of a node's neighbors that are 320 themselves connected) are computed. This entire process is repeated for 1000 different 321 initial starting environments. The results are shown in Figure 5. The results follow the 322 pattern found by Dubossarsky et al. (2017) and others. 323

324 Discussion

Aging is marked by complex and multi-faceted phenomenology. The enrichment
account provided here demonstrates that a subset of this phenomenology is predicted by
cognitive enrichment. Specifically, the enrichment account demonstrates how learning
enriches the cognitive representation and then, using various processes, gives rise to
behavior commonly associated with cognitive aging. In particular, enrichment reproduces
rising entropy, falling similarity judgments, and a sparsening of the free association network
across the lifespan.

The enrichment account is not meant to be a complete explanation of cognitive aging. 332 Rather, like any model, it puts guardrails on our ignorance. It does this by showing how 333 many of the behaviors that might be intuitively interpreted as evidence of cognitive and 334 neural degradation are straightforward outcomes of learning. Whereas we might have 335 suspected degradation, enrichment may be the more likely candidate, especially given that 336 we know enrichment is already occurring in association with crystallized intelligence. 337 Moreover, degradation can produce the opposite effect. Borge-Holthoefer et al. (2011) used 338 degradation not to demonstrate diffusion of activation and greater slowing, but rather to 339 demonstrate an increasing of activation between associates, producing hyper-priming, a

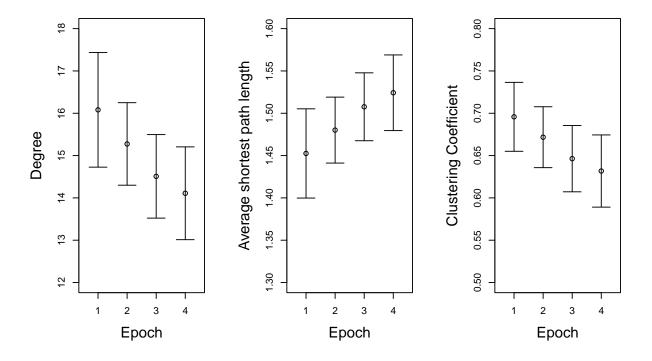


Figure 5. The degree, average shortest path length, and clustering coefficient for networks of associations across the lifespan. Simulations were repeated for learning cognitive representations in 1000 different environments (a=1) with four training epochs each of 200 learning events $\operatorname{each}(beta=.1)$. Representations were then each sampled from by 10 simulated participants who each retrieved 3 associates for each of 30 cues with probability proportional to the associative strengths output from the Rescorla-Wagner training epochs. The cosine similarity of cues was then computed from the cue by association matrix to produce associative networks for each epoch. These networks were then thresholded separately for each learning environment by the median similarity value across all ages. Error bars indicate one standard deviation. Results are consistent with Dubossarsky et al., 2017.

well-documented behavior in patients with Alzheimer's Disease. Nonetheless, the patterns
of biological and neural change outlined in the introduction are themselves data, and any
full account of cognitive aging must take this evidence into account. Ideally, we want
understand how these changes in neural architecture interact with enrichment to produce
the behavioral variation that we see. With respect to parsimony, enrichment may be
sufficient to explain how fluid intelligence might change as a result of changes in crystallized
intelligence (as opposed to treating each independently), but our theories must also be
parsimonious with respect to observed changes in the underlying neural architecture.

The enrichment account is incomplete for several other reasons as well. One key 349 extension is that lifelong experience with language follows Herdan-Heap's law (Brysbaert et 350 al., 2016). Herdan-Heaps' law is the observation that the number of new word types is an 351 increasing function of the number of word tokens, and this appears to be true for human 352 experience with language as well. This is easily added to the enrichment account by 353 allowing the environment to grow over time. Future work should investigate various 354 implications of this addition. A further limitation is that the enrichment account is not 355 meant to characterize child development, which has special developmental features of its 356 own. For example, early vocabulary acquisition is driven by a variety of processes including semantics, phonology, social pragmatics, and perceptual features (Ciaglia, Stella, & Kennington, 2023; Engelthaler & Hills, 2017; Fourtassi, Bian, & Frank, 2020; Jiménez & Hills, 2022; Yu, Suanda, & Smith, 2019). This different pattern of acquisition may extend into young adulthood, possibly as a result of standardized formal education (Dubossarsky 361 et al., 2017). Extending our understanding of the development of the cognitive representation from early childhood to late life remains for future work. 363

Despite these limitations, the fundamental mechanism of the enrichment account is supported empirically. For example, the fan effect demonstrates that learning many relationships with a target concept reduces the speed of accessing any one of those relationships (Anderson & Reder, 1999). This diffusion of activation is a general and

well-understood outcome of spreading activation or random walker models (Abbott,
Austerweil, & Griffiths, 2015; Siew, 2019). Activation follows pathways and the more
pathways there are the less targeted the activation. In addition, one can see this effect in
natural experiments: Ramscar et al. (2017) showed that individuals with more language
experience (native speakers) were more impaired in paired-associative learning in that
language than age-matched individuals with less experience (second language learners).
This suggests the effect is not about age, but about enrichment.

We also know that external clutter influences processing speed in older adults more 375 strongly than young adults (Amer et al., 2022; McCarley, Yamani, Kramer, & Mounts, 376 2012). This is consistent with higher conceptual entropy creating a more level-playing field 377 for competition. If there is greater associative competition in older adults, because the 378 associative entropy is higher, then older adults will suffer more from clutter in internal and 379 external processing. This may explain the enhanced variability in resting-state brain 380 synchronization among older adults (Jauny, Eustache, & Hinault, 2022). However, because 381 external cues gain their relevance via their encoded associations in memory (Easdale, Le 382 Pelley, & Beesley, 2019), this may also explain the impact of external clutter. The 383 attentional contribution to clutter on aging memory, as elegantly described by Amer et al. (2022), could therefore be a consequence of enrichment: the activation strengths associated with extraneous and potentially irrelevant information have a greater relative competitive advantage in individuals with more enriched representations, making older individuals 387 more susceptible to internal and external distractions. 388

One challenge to the enrichment account is that individuals with higher education and occupational attainment are less likely to experience late-life cognitive decline (Lövdén, Fratiglioni, Glymour, Lindenberger, & Tucker-Drob, 2020; Stern et al., 1994).

This is known to be partially a consequence of compensation accorded by skills or strategic repertoires, what is called cognitive reserve (Scarmeas & Stern, 2003). Additionally, however, there is ample evidence that differences in cognitive skills emerge early in life,

prior to education, and therefore lay the foundation for educational attainment later in life 395 (Deary, Whiteman, Starr, Whalley, & Fox, 2004; Lövdén et al., 2020). If differences in 396 processing speed at an early age influence educational attainment at a later age, then 397 slowing later as a consequence of education will be confounded by early differences in 398 processing. Early processing advantages may not be a result of experience at all. Brain 390 volume is correlated with IQ (Pietschnig, Gerdesmann, Zeiler, & Voracek, 2022) and is 400 strongly heritable (Peper, Brouwer, Boomsma, Kahn, & Hulshoff Pol. 2007). Furthermore, 401 measures of 'brain age' in late life are well-predicted by indicators present in early life 402 (Vidal-Pineiro et al., 2021). Nonetheless, if we believe that formal education (or 403 occupational attainment) is an indicator of increased associative density (not just in 404 quality, but quantity), then an ideal test might be to investigate twins who differ in 405 educational enrichment and are then evaluated on age-related cognitive decline. The Ramscar et al. (2017) study on age-matched bilinguals and monolinguals is another 407 approach. What kinds of education matter for enrichment is an open question. Is 408 rewatching the 11 seasons of the 1970s TV series M*A*S*H (approximately 125 hours 409 runtime) different from reading the complete works of Gabriel Garcia Marquez for the first 410 time? If enrichment is about the variety of associations, and not the quality of associations 411 (if such quality could be objectively measured), then the difference may not matter. 412

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