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T R 5:40 – 7:20

Homework # 2

3.2a Write EBNF descriptions for the following: A Java class definition header statement

```
<head> -> {<modifier>} class <id> [extends name]
               [implements <interface_name>, {<interface_name>}]
<modifier> -> public | abstract | final
```

3.2c Write EBNF descriptions for the following: A C switch statement

```
<switch_stmt> -> switch (<expr>) {case <literal> : <stmt_list>
                                         {case <literal> : <stmt_list>} [default : <stmt_list>] }
```

3.3 Rewrite the BNF of Example 3.4 to give + precedence over * and force + to be right associative

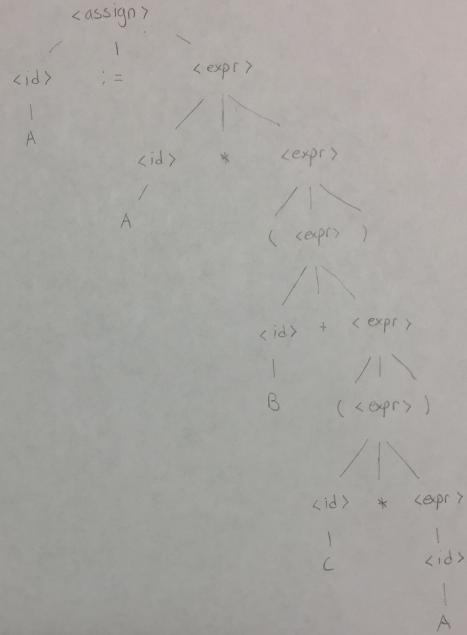
```
<assign> -> <id> = <expr>
<id> -> A | B | C
<expr> -> <expr> * <term>
             | <term>
<term> -> <term> + <factor>
             | <factor>
<factor> -> ( <expr> )
             | <id>
```

3.6 Using the grammar in Example 3.2, show a parse tree and a leftmost derivation for each of the following statements:

A = A * (B + (C * A))

```
<assign> => <id> = <expr>
=> A = <expr>
=> A = <id> * <expr>
=> A = A * <expr>
=> A = A * (<expr>)
=> A = A * (<id> + <expr>)
=> A = A * (B + <expr>)
=> A = A * (B + (<expr>))
=> A = A * (B + (<id> * <expr>))
=> A = A * (B + (C * <id>))
=> A = A * (B + (C * A))
```

(3.6a) $A = A * (B + (C * A))$



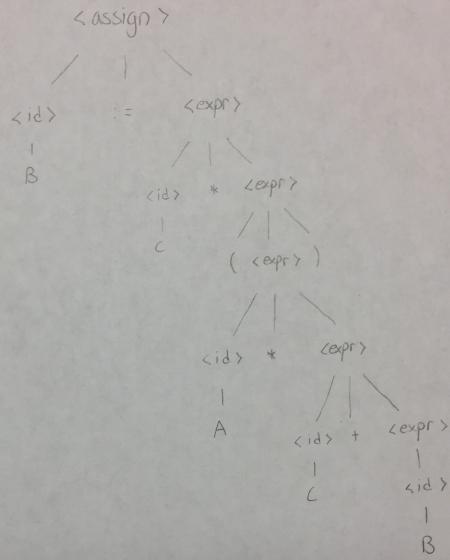
$$B = C * (A * C + B)$$

<assign> => <id> = <expr>

=> B = <expr>
=> B = <id> * <expr>
=> B = <id> * (<expr>)
=> B = C * (<id> * <expr>)
=> B = C * (A * <expr>)
=> B = C * (A * <id> + <expr>)
=> B = C * (A * C + <id>))
=> B = C * (A * C + B)

(3.6b)

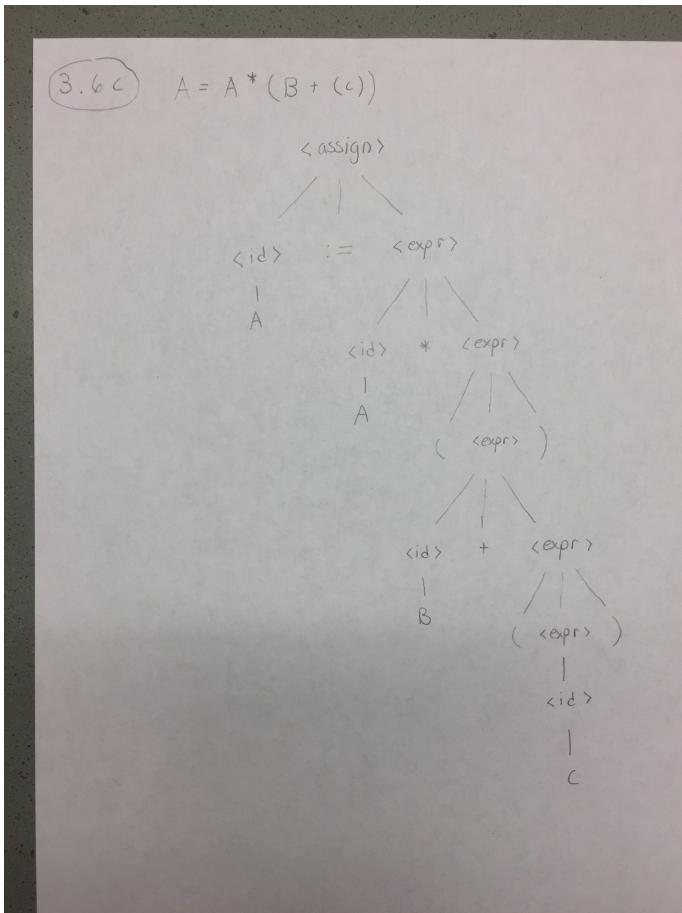
$$\beta = C^* (A^* C + \beta)$$



$$A = A * (B + (C))$$

$$<\text{assign}> \Rightarrow <\text{id}> = <\text{expr}>$$

$$\begin{aligned} &\Rightarrow A = <\text{expr}> \\ &\Rightarrow A = <\text{id}> * <\text{expr}> \\ &\Rightarrow A = A * <\text{expr}> \\ &\Rightarrow A = A * (<\text{expr}>) \\ &\Rightarrow A = A * (<\text{id}> + <\text{expr}>) \\ &\Rightarrow A = A * (B + <\text{expr}>) \\ &\Rightarrow A = A * (B + (<\text{expr}>)) \\ &\Rightarrow A = A * (B + (<\text{id}>)) \\ &\Rightarrow A = A * (B + (C)) \end{aligned}$$

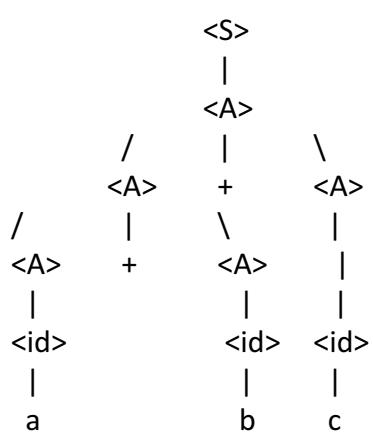


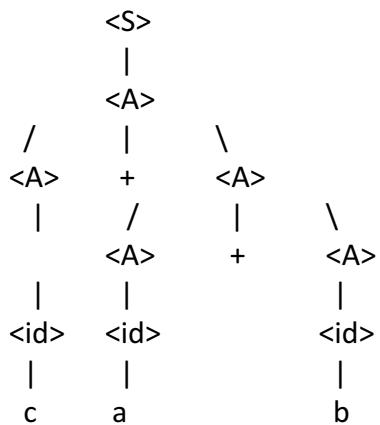
3.8 Prove that the following grammar is ambiguous:

$<S> \rightarrow <A>$

$<A> \rightarrow <A> + <A> \mid <id>$

$<id> \rightarrow a \mid b \mid c$





3.12 Consider the following grammar:

```

<S> -> a <S> c <B> | <A> | b
<A> -> c <A> | c
<B> -> d | <A>
  
```

Which of the following sentences are in the language generated by this grammar

The following two sentences can be generated using the grammar above

- A. abcd
- E. accc

3.16 Convert the BNF of Example 3.3 to EBNF

```

<assign> -> <id> = <expr>
<id> -> A | B | C
<expr> -> <expr> (+ | *) <expr>
          | (<expr>
          | <id>
  
```

3.21b Use the virtual machine instructions given in Section 3.5.1.1, give an operational semantic definition of the following: Ada for

i = first

loop: if i < last goto out

```

...
i = i + 1;
  
```

goto loop
out: ...

3.21c Use the virtual machine instructions given in Section 3.5.1.1, give an operational semantic definition of the following: C++ if-then-else

i = expr1
loop: if expr2 == 0 goto out
...
expr3
goto loop
out: ...

3.22a Write a denotational semantics mapping function for the following statements: Ada for

$M_{\text{for}}(\text{for var } i \text{ in init_expr .. final_expr loop } L \text{ end loop}, s)$
if $\text{VARMAP}(i, s) = \text{undef}$ for var
 then error
 else if $M_e(\text{init_expr}, s) < M_e(\text{final_expr}, s)$
 then s
 else $M_l(\text{while init_expr} - 1 \leq \text{final_expr do } L)$

3.22b Write a denotational semantics mapping function for the following statements: Java do-while

$M_{\text{do}}(L, s)$
 $M_{\text{while}}(\text{repeat } L \text{ until } B)$
 if $M_b(B, s) = \text{undef}$
 then error
 else $M_{\text{while}}(\text{repeat } L \text{ until } B)$

3.24 Compute the weakest precondition for each of the following sequences of assignment statements and their post conditions:

- A. $a < 3 \ \& \ b < 1$
- B. $a > 3 \ \& \ b > (1 - a)/2$

3.25 Compute the weakest precondition for each of the following selection constructs and their post conditions:

- A. $a > 0$
- B. $x < 0$
- C. $x > 2$