Problem A2 Increasing Matrix (Hard Version)

Time limit: 2 seconds

Memory limit: 2048 megabytes

Problem Description

Given two **increasing** arrays, a_1, a_2, \ldots, a_n and b_1, b_2, \ldots, b_m , we create an "increasing matrix" A with dimensions $n \times m$, where the j-th element of the i-th row can be determined as $A_{i,j} = a_i^2 + a_i b_j + b_j^2$. The term "increasing matrix" is used because the elements in each row are arranged in ascending order.

Your task is to find the k smallest elements in the matrix A. To avoid large amount of output, you have to output the bitwise XOR of the k smallest elements.

Input Format

The first line of the input contains three integers n, m and k. The second line of the input contains n space-separated integers a_1, a_2, \ldots, a_n . The third line of the input contains m space-separated integers b_1, b_2, \ldots, b_m .

Output Format

Output the bitwise XOR of the k smallest elements in one line.

Technical Specification

- $1 \le n, m \le 10^5$
- $1 \le k \le 10^6$
- $1 \le a_i \le 10^9 \text{ for } i = 1, 2, \dots, n$
- $1 \le b_i \le 10^9 \text{ for } i = 1, 2, \dots, m$

Sample Input 1

- 2 3 6
- 1 2
- 3 4 5

Sample Output 1

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Sample Input 2

```
10 10 15
3 4 5 6 7 9 10 19 19 29880
1 8 12 20 30 49 64 87 94 100000
```

Sample Output 2

56

Sample Input 3

Sample Output 3

3000000000000000000

Hint

One problem from the handwritten assignments may help in this problem.