## Statistics 641, Fall 2012 Homework #1 Answers

- 1. Suppose in a randomized trial, subjects' responses are measured at three times: baseline (randomization), month 1, month 2. The data file "data1.csv" (in csv format, comma delimited) contains columns
  - x0: baseline value of response variable
  - x1: value of response variable at month 1
  - x2: value of response variable at month 2
  - z: treatment variable (0,1).

Note: this file can be read into R using the command

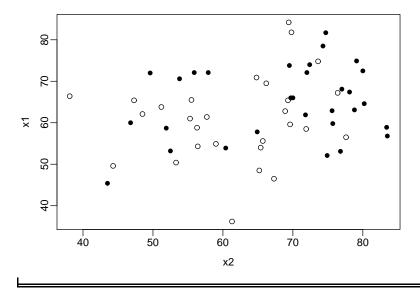
```
> data = read.csv(data1.csv)
```

Assume that the responses are normally distributed.

(a) For the response at month 1 (x1), compute the mean and standard deviation for each treatment group (z = 0, 1)

(b) Plot the month 1 response against the month 2 response, using a different plotting symbol for each treatment group.

```
> plot(x1~x2, data=data, pch=c(1,16)[z+1])
```



(c) Perform a two-sample t-test comparing the month 1 response between treatment groups (you may assume equal variances).

```
> summary(lm(x1~z, data=data))
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
              60.914
(Intercept)
                           1.809
                                  33.677
                                            <2e-16 ***
               3.886
                           2.515
                                   1.545
                                             0.128
z
                0 '*** 0.001 '** 0.01 '* 0.05 '. ' 0.1 ' ' 1
Signif. codes:
The t-statistic is 1.545.
```

(d) Fit a linear model comparing the month 1 response by treatment adjusted for the base-line value, **x0**.

```
> summary(lm(x1~z+x0, data=data))
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept)
             13.7465
                         3.6149
                                  3.803 0.000361 ***
              3.6458
                         1.2252
                                  2.976 0.004337 **
z
x0
              0.7709
                         0.0573 13.454 < 2e-16 ***
Signif. codes:
               0 '*** 0.001 '** 0.01 '* 0.05 '. ' 0.1 ' ' 1
Residual standard error: 4.662 on 55 degrees of freedom
F-statistic: 95.54 on 2 and 55 DF, p-value: < 2.2e-16
```

(e) Why does (d) yield a different answer than (c)? Is x0 a confounder?

The t-statistic is much larger in (d) than in (c). In (c), the mean difference is 3.886, and in (d) it is 3.646, whereas in (c) the standard error of the difference is 2.515 versus 1.225 in (d). Accounting for the association between baseline and month 1 increases the precision of the estimate of difference.

Regardless of this result, x0 cannot be confounder because the study is randomized.

(f) Perform a two-sample t-test comparing the month 2 response between treatment groups.

(g) Fit a linear model comparing the month 2 response by treatment adjusted for the month 1 value, x1.

```
> summary(lm(x2~z+x1, data=data))
Coefficients:
           Estimate Std. Error t value
                                         Pr(>|t|)
(Intercept) 47.6754
                        9.4015
                                 5.071 0.00000481 ***
             5.9828
                        2.8954
                                 2.066
                                           0.0435 *
z
             0.2289
                        0.1507
                                 1.519
                                           0.1344
x1
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Residual standard error: 10.79 on 55 degrees of freedom
```

(h) Why does (g) yield a different answer than (f)? Is x1 a confounder?

The t-statistic is larger in (g) than in (f) because x1 accounts for some (small amount) of the effect of treatment on x2. However, because the study is randomized x1 cannot be a confounder. In fact, x1 is observed after treatment start, so the causal pathway is from z to x1, rather than x1 to z, which is required for confounding.