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**Algorithm 1** Computation of the first and the next distance columns

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1: function firstEDtabcolumn( $E, u$ )
2:    $E(0) \leftarrow 0$ 
3:   for  $i \leftarrow 1$  upto  $|u|$  do  $E(i) \leftarrow E(i-1) + \delta(u[i] \rightarrow \varepsilon)$ 
4:   end for
5: end function
6: function nextEDtabcolumn( $E, E', u, b$ )
7:    $E(0) \leftarrow E'(0) + \delta(\varepsilon \rightarrow b)$ 
8:   for  $i \leftarrow 1$  upto  $|u|$  do  $E(i) \leftarrow \min \begin{Bmatrix} E(i-1) + \delta(u[i] \rightarrow \varepsilon) \\ E'(i) + \delta(\varepsilon \rightarrow b) \\ E'(i-1) + \delta(u[i] \rightarrow b) \end{Bmatrix}$ 
9:   end for
10: end function
11: function evaluateallEDtabcolumns( $E, u, v$ )
12:   allocate vector  $E'$  of length  $|u| + 1$ 
13:   firstEDtabcolumn( $E, u$ )
14:   for  $j \leftarrow 1$  upto  $|v|$  do  $E' \leftarrow E$ ; nextEDtabcolumn( $E, E', u, v[j]$ )
15:   end for
16: end function
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**Algorithm 2** The recurrence for table  $R_{j_0}$ . The values depend on column  $E_{\text{col}}^{j-1}$  and  $E_{\text{col}}^j$ . Line 3 handles the case where the insertion edge is minimizing. Line 4 handles the case where the replacement edge is minimizing. Line 5 handles the case where the deletion edge is minimizing. If  $j > j_0$ , then at least one of the three cases applies, so the *else if* in line 5 could be replaced by *otherwise*. As usual, with a distance value  $E_{\text{col}}^j(i)$  we can store which of the incoming edges is minimizing, as to remove the dependency on other entries in  $E_{\text{col}}^{j-1}$  and  $E_{\text{col}}^j$ .

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$$R_{j_0}(i, j) = \begin{cases} \text{undefined} & \text{if } 0 \leq j \leq j_0 - 1 \\ i & \text{else if } j = j_0 \\ R_{j_0}(i, j-1) & \text{else if } E_{\text{col}}^j(i) = E_{\text{col}}^{j-1}(i) + \delta(\varepsilon \rightarrow v[j]) \\ R_{j_0}(i-1, j-1) & \text{else if } E_{\text{col}}^j(i) = E_{\text{col}}^{j-1}(i-1) + \delta(u[i] \rightarrow v[j]) \\ R_{j_0}(i-1, j) & \text{else if } E_{\text{col}}^j(i) = E_{\text{col}}^j(i-1) + \delta(u[i] \rightarrow \varepsilon) \end{cases}$$


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**Algorithm 3** A recursive function to compute crosspoints.

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**Input:**  $i, j, p, q$  with  $1 \leq i \leq m, 1 \leq j \leq n, 0 \leq p \leq m-i+1, 0 \leq q \leq n-j+1$ , and uninitialized  $(m+1)$ -element vectors  $E$  and  $R$  to store distance and row index columns

**Output:** table  $C$  of crosspoints

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1: function evaluatecrosspoints( $C, i, j, p, q$ )
2:   if  $q \geq 2$  then
3:      $j_0 \leftarrow \lfloor q/2 \rfloor$ 
4:     evaluateallcolumns( $E, R, j_0, u[i \dots i+p-1], v[j \dots j+q-1]$ )
5:      $i_0 \leftarrow R[p]$  ▷ last value of last  $R_{j_0}$ -column
6:      $C(j-1+j_0) \leftarrow i-1+i_0$  ▷  $i/j$  refer to strings  $\Rightarrow$  subtract 1
7:     evaluatecrosspoints( $C, i, j, i_0, j_0$ ) ▷ eval. upper/left part
8:     evaluatecrosspoints( $C, i+i_0, j+j_0, p-i_0, q-j_0$ ) ▷ low./right
9:   end if
10: end function
11: create table  $C$  of  $n+1$  entries and set  $C(0) \leftarrow 0$  and  $C(n) \leftarrow m$ 
12: evaluatecrosspoints( $C, 1, 1, m, n$ )

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