

# COMP 182: Algorithmic Thinking

## 11 February 2014

An algorithm that explores graphs in a different fashion than **BFS** is the *depth-first search*, or **DFS**, algorithm. To explore a graph  $g$  with **DFS**, the algorithm is called as **DFS**( $g, p$ ) with  $p_i$  initialized to *null* for every node  $i \in V$ . The algorithm modifies the  $p$  values for every node in the graph.

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**Algorithm 1: DFS**

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**Input:** Graph  $g = (V, E)$ ,  $V = \{0, 1, \dots, n-1\}$ , and  $p_i, \forall i \in V$ .

**Output:** None.

**Modifies:**  $p$ .

```
foreach  $i \in V$  do
    if  $p_i = \text{null}$  then
         $p_i \leftarrow -1$ ;           // We designate the parent of the initial node to be '-1'
        Visit( $g, i, p$ );
```

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**Algorithm 2: Visit**

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**Input:** Graph  $g = (V, E)$ , node  $i \in V$ , and  $p_j, \forall j \in V$ .

**Output:** None.

**Modifies:**  $p$ .

```
foreach neighbor  $h$  of  $i$  do
    if  $p_h = \text{null}$  then
         $p_h \leftarrow i$ ;
        Visit( $g, h, p$ );
```

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1. Consider graph  $g = (V, E)$ ,  $V = \{0, 1, 2, 3, 4, 5\}$  and  $E = \{(0, 1), (0, 3), (1, 4), (2, 4), (2, 5), (3, 1), (4, 3)\}$ . Run **DFS** on  $g$  and report the  $p$  values for all nodes.
2. For a graph  $g = (V, E)$  given by its adjacency list, what is worst-case running time of **DFS**, as a function of  $m = |E|$  and  $n = |V|$ ?
3. A directed, acyclic graph (DAG) is a directed graph that has no cycles. A *topological sort* of a DAG  $g = (V, E)$  is a linear ordering of all its nodes such that if  $g$  contains an edge  $(u, v)$ , then  $u$  appears before  $v$  in the ordering. Give the pseudo-code of an  $O(m + n)$  algorithm for topologically sorting a DAG.