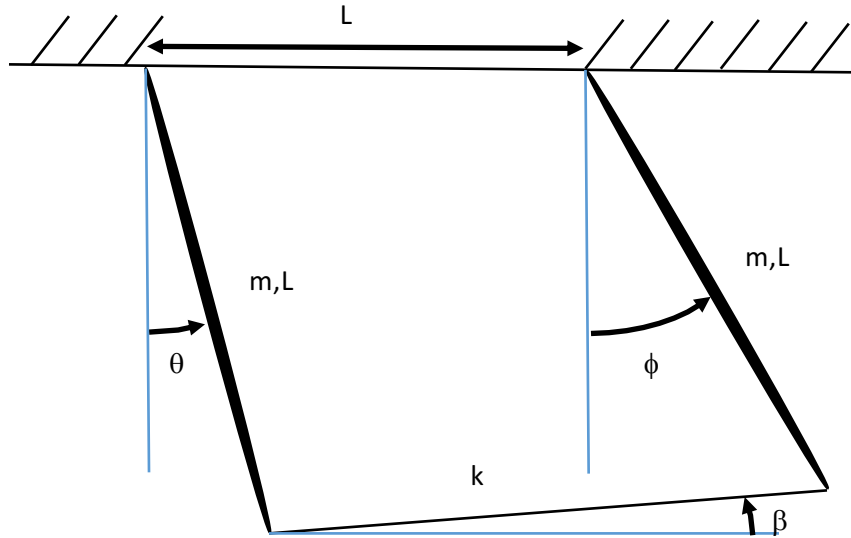


There is a rigid-body pendulum system with each having equal mass,  $m = 0.25$  kg, and length,  $L = 0.5$  m. A linear spring, with spring coefficient  $k = 25$  N/m and unstretched length  $L$ , is attached at the ends of the two bars as shown.



- Determine the 6 equation / 6 unknown system to solve for the system EOMs.
- Integrate the EOMs for the system using various initial conditions to show the different styles of motion that the system exhibits. All systems start at rest
  - Initial positions:  $\theta_o = \frac{\pi}{12} \text{ rad}$ ,  $\phi_o = \frac{\pi}{12} \text{ rad}$   
Plot the response for 10 seconds.
  - Initial positions:  $\theta_o = -\frac{\pi}{12} \text{ rad}$ ,  $\phi_o = \frac{\pi}{12} \text{ rad}$   
Plot the response for 10 seconds.
  - Initial positions:  $\theta_o = \frac{\pi}{36} \text{ rad}$ ,  $\phi_o = \frac{\pi}{12} \text{ rad}$   
Plot the response for 10 seconds.
- Linearize the EOMs by assuming small angular positions and velocities, i.e.,  $\sin(x) = x$ ,  $\cos(x) = 1$ , and any angular position or velocity times any other angular position or velocity is negligible.

$$\begin{bmatrix} \ddot{\theta} \\ \ddot{\phi} \end{bmatrix} = [A] \begin{bmatrix} \theta \\ \phi \end{bmatrix}$$

What is the  $[A]$  matrix?

- By calculating the eigenvalues and eigenvectors of  $[A]$ , what are the 2 natural frequencies for this system and their associated eigenvectors?

5. Using the previous information, solve for the analytical solution to the linearized EOMs and plot these analytical solutions for the 3 sets of initial conditions with the numerical solutions from Part 2.