

New CA Classifiers (random colours)

Wolfram Classes of ECAs

```
In[1]:= CAClasses = {1, 2, 2, 2, 2, 2, 2, 2, 1, 2, 2, 2, 2, 2, 2, 2, 2, 2, 3, 2, 2, 2, 3, 2, 2, 2, 2, 2,  
    2, 2, 3, 2, 1, 2, 2, 2, 2, 2, 2, 2, 1, 3, 2, 2, 2, 3, 2, 2, 2, 2, 2, 2, 2, 2, 4, 2, 2,  
    2, 2, 2, 3, 2, 2, 2, 1, 2, 2, 2, 2, 2, 2, 2, 2, 2, 3, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2,  
    3, 2, 2, 3, 3, 2, 2, 2, 2, 2, 1, 3, 2, 2, 2, 3, 3, 2, 2, 3, 3, 3, 2, 2, 4, 2, 2, 2, 2, 2,  
    2, 2, 2, 2, 2, 3, 3, 3, 2, 4, 2, 3, 2, 1, 3, 2, 2, 2, 2, 2, 3, 1, 4, 2, 2, 2, 2, 2, 2, 2,  
    2, 2, 3, 4, 2, 3, 3, 3, 2, 3, 2, 2, 2, 2, 2, 2, 1, 3, 2, 2, 2, 3, 2, 2, 1, 3, 2, 2,  
    2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 3, 3, 2, 2, 2, 2, 2, 2, 2, 1, 4, 2, 3, 2, 2, 2, 2,  
    2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 3, 2, 2,  
    2, 2, 2, 2, 2, 2, 1, 1, 2, 2, 1, 1, 2, 2, 2, 2, 2, 2, 2, 2, 1, 1, 1, 1, 1, 1, 1};
```

Functions for creating net and random datasets (ECAs, all 4 classes)

```

In[2]:= RandomRuleC[n_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[n, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[],
      3 -> RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[],
      6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
netC[W_Integer, H_Integer] := NetInitialize@NetChain[
  {ConvolutionLayer[16, {2, 3}], Ramp, PoolingLayer[{H, W} - {1, 2}], FlattenLayer[],
    LinearLayer[256], SoftmaxLayer[]], "Input" -> NetEncoder[{"Image", {W, H}}],
  "Output" -> NetDecoder[{"Class", Range[0, 255]}]]
netTwoCC[W_Integer, H_Integer] := NetInitialize@
  NetChain[<|"conv1" -> ConvolutionLayer[16, {2, 3}], "ramp1" -> Ramp,
    "conv3" -> ConvolutionLayer[16, {2, 3}], "ramp2" -> Ramp,
    "pooling" -> PoolingLayer[{H, W} - {2, 4}], "flatten" -> FlattenLayer[],
    "linear" -> 512, "linear2" -> 4, "softmax" -> SoftmaxLayer[]>,
  "Input" -> NetEncoder[{"Image", {W, H}}], "Output" -> NetDecoder[{"Class", Range[1, 4]}]]
dataC[W_Integer, H_Integer, n_Integer] :=
  Table[RandomRuleC[i, W, H] -> CAClasses[[i + 1]], {i, RandomChoice[Range[0, 255], n]}]

```

```

In[6]:= netThreeCC[W_Integer, H_Integer] :=
  NetInitialize@NetChain[<|"conv1" → ConvolutionLayer[16, {2, 3}],
    "ramp1" → Ramp, "conv2" → ConvolutionLayer[16, {2, 3}],
    "ramp2" → Ramp, "conv3" → ConvolutionLayer[16, {2, 3}], "ramp3" → Ramp,
    "pooling" → PoolingLayer[{H, W} - {4, 8}], "flatten" → FlattenLayer[],
    "linear" → 512, "linear2" → 4, "softmax" → SoftmaxLayer[]|>,
    "Input" → NetEncoder[{"Image", {W, H}}, "Output" → NetDecoder[{"Class", Range[1, 4]}]]

```

```

In[7]:= netThreeCC1024[W_Integer, H_Integer] :=
  NetInitialize@NetChain[<|"conv1" → ConvolutionLayer[16, {2, 3}],
    "ramp1" → Ramp, "conv2" → ConvolutionLayer[16, {2, 3}],
    "ramp2" → Ramp, "conv3" → ConvolutionLayer[16, {2, 3}], "ramp3" → Ramp,
    "pooling" → PoolingLayer[{H, W} - {4, 8}], "flatten" → FlattenLayer[],
    "linear" → 1024, "linear2" → 4, "softmax" → SoftmaxLayer[]|>,
    "Input" → NetEncoder[{"Image", {W, H}}, "Output" → NetDecoder[{"Class", Range[1, 4]}]]

```

```

In[8]:= netFourCC512[W_Integer, H_Integer] :=
  NetInitialize@NetChain[<|"conv1" → ConvolutionLayer[32, {2, 3}],
    "ramp1" → Ramp, "conv3" → ConvolutionLayer[32, {2, 3}], "ramp2" → Ramp,
    "pooling" → PoolingLayer[{H, W} - {2, 4}], "flatten" → FlattenLayer[],
    "linear" → 512, "linear2" → 4, "softmax" → SoftmaxLayer[]|>,
    "Input" → NetEncoder[{"Image", {W, H}}, "Output" → NetDecoder[{"Class", Range[1, 4]}]]

```

```

In[9]:= netFiveCC512[W_Integer, H_Integer] := NetInitialize@
  NetChain[<|"conv1" → ConvolutionLayer[32, {2, 3}], "bat1" → BatchNormalizationLayer[],
    "ramp1" → Ramp, "conv3" → ConvolutionLayer[32, {2, 3}],
    "bat2" → BatchNormalizationLayer[], "ramp2" → Ramp,
    "pooling" → PoolingLayer[{H, W} - {2, 4}], "flatten" → FlattenLayer[],
    "linear" → 512, "linear2" → 4, "softmax" → SoftmaxLayer[]|>,
    "Input" → NetEncoder[{"Image", {W, H}}, "Output" → NetDecoder[{"Class", Range[1, 4]}]]

```

```

In[10]:= netSixCC512drop[W_Integer, H_Integer] := NetInitialize@
  NetChain[<|"drop1" → DropoutLayer[0.2], "conv1" → ConvolutionLayer[32, {3, 3}],
    "bat1" → BatchNormalizationLayer[], "ramp1" → Ramp,
    "conv3" → ConvolutionLayer[32, {3, 3}], "bat2" → BatchNormalizationLayer[],
    "ramp2" → Ramp, "pooling" → PoolingLayer[{H, W} - {4, 8}],
    "flatten" → FlattenLayer[], "linear" → 512, "drop2" → DropoutLayer[0.2],
    "linear2" → 4, "softmax" → SoftmaxLayer[]|>,
    "Input" → NetEncoder[{"Image", {W, H}}, "Output" → NetDecoder[{"Class", Range[1, 4]}]]

```

```
In[11]:= netSevenCC512drop[W_Integer, H_Integer] :=
  NetInitialize@NetChain[<|"conv1" → ConvolutionLayer[24, {3, 3}],
    "bat1" → BatchNormalizationLayer[], "ramp1" → Ramp,
    "conv3" → ConvolutionLayer[24, {3, 3}], "bat2" → BatchNormalizationLayer[],
    "ramp2" → Ramp, "pooling" → PoolingLayer[{H, W} - {4, 8}],
    "flatten" → FlattenLayer[], "linear" → 512, "drop2" → DropoutLayer[0.2],
    "linear2" → 4, "softmax" → SoftmaxLayer[]|>,
    "Input" → NetEncoder[{"Image", {W, H}}, "Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

```
In[12]:= netEightCC512drop[W_Integer, H_Integer] :=
  NetInitialize@NetChain[<|"conv1" → ConvolutionLayer[24, {3, 3}],
    "bat1" → BatchNormalizationLayer[], "ramp1" → Ramp,
    "conv2" → ConvolutionLayer[16, {2, 3}], "bat2" → BatchNormalizationLayer[],
    "ramp2" → Ramp, "conv3" → ConvolutionLayer[24, {3, 3}],
    "bat3" → BatchNormalizationLayer[], "ramp3" → Ramp, "pooling" →
    PoolingLayer[{H, W} - {8, 16}], "flatten" → FlattenLayer[], "linear" → 1024,
    "drop2" → DropoutLayer[0.2], "linear2" → 4, "softmax" → SoftmaxLayer[]|>,
    "Input" → NetEncoder[{"Image", {W, H}}, "Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

```
In[13]:= netNineCC512drop[W_Integer, H_Integer] :=
  NetInitialize@NetChain[<|"conv1" → ConvolutionLayer[24, {3, 3}],
    "bat1" → BatchNormalizationLayer[], "ramp1" → Ramp,
    "conv2" → ConvolutionLayer[24, {3, 3}], "bat2" → BatchNormalizationLayer[],
    "ramp2" → Ramp, "conv3" → ConvolutionLayer[24, {3, 3}],
    "bat3" → BatchNormalizationLayer[], "ramp3" → Ramp, "pooling" →
    PoolingLayer[{H, W} - {12, 12}], "flatten" → FlattenLayer[], "linear" → 512,
    "drop2" → DropoutLayer[0.2], "linear2" → 4, "softmax" → SoftmaxLayer[]|>,
    "Input" → NetEncoder[{"Image", {W, H}}, "Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

```
In[180]:= netTenCC1024drop[W_Integer, H_Integer] :=
  NetInitialize@NetChain[<|"conv1" → ConvolutionLayer[24, {3, 3}],
    "bat1" → BatchNormalizationLayer[], "ramp1" → Ramp,
    "conv2" → ConvolutionLayer[24, {3, 3}], "bat2" → BatchNormalizationLayer[],
    "ramp2" → Ramp, "conv3" → ConvolutionLayer[24, {3, 3}],
    "bat3" → BatchNormalizationLayer[], "ramp3" → Ramp,
    "conv4" → ConvolutionLayer[24, {3, 3}], "bat4" → BatchNormalizationLayer[],
    "ramp4" → Ramp, "pooling" → PoolingLayer[{H, W} - {12, 12}],
    "flatten" → FlattenLayer[], "linear" → 1024,
    "drop2" → DropoutLayer[0.3], "linear2" → 4, "softmax" → SoftmaxLayer[]|>,
    "Input" → NetEncoder[{"Image", {W, H}}, "Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

Functions for creating datasets (1D totalistic CAs)

k=3, r=1 totalistic (class 4 only)

```
In[14]:= gen3TC[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {3, 1}}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules ->
      {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 -> RandomColor[],
        5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data3T2C[W_Integer, H_Integer, n_Integer] := Table[gen3TC[i, W, H] -> 4,
  {i, RandomChoice[{1635, 1815, 2007, 2043, 2049, 1388, 1041}, n]}]
```

k=4, r=1 totalistic (class 4 only, 1 example)

```
In[16]:= gen4TC[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {4, 1}}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules ->
      {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 -> RandomColor[],
        5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data4TC[W_Integer, H_Integer, n_Integer] := Table[gen4TC[1004600, W, H] -> 4, n]
```

k=2, r=2 totalistic (all 4 classes)

```
In[18]:= gen2r2C[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {2, 1}, 2}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules ->
      {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 -> RandomColor[],
        5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data2r2c4C[W_Integer, H_Integer, n_Integer] :=
  Table[gen2r2C[i, W, H] -> 4, {i, RandomChoice[{20, 52}, n]}]
data2r2c3C[W_Integer, H_Integer, n_Integer] := Table[gen2r2C[i, W, H] -> 3,
  {i, RandomChoice[{2, 6, 10, 12, 14, 18, 22, 26, 28, 30, 34, 38, 42, 44, 46, 50}, n]}]
data2r2c2C[W_Integer, H_Integer, n_Integer] :=
  Table[gen2r2C[i, W, H] -> 2, {i, RandomChoice[{8, 24, 56}, n]}]
data2r2c1C[W_Integer, H_Integer, n_Integer] := Table[gen2r2C[i, W, H] -> 1,
  {i, RandomChoice[{0, 4, 16, 32, 36, 40, 48, 54, 58, 60, 62}, n]}]
genData2r2C[W_Integer, H_Integer, n_Integer] :=
  Join[data2r2c4C[W, H, n], data2r2c3C[W, H, n], data2r2c2C[W, H, n], data2r2c1C[W, H, n]]
```

k=5, r=1 totalistic (class 4 only)

In[24]:=

```
gen5T4C[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {5, 1}}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules ->
      {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 -> RandomColor[],
        5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data5T4C[n_Integer, W_Integer, H_Integer] := Table[gen5T4C[i, W, H] -> 4,
  {i, RandomChoice[{781 130 654, 772 514 435, 1 151 319 452, 309 095 787, 880 862 046,
    973 835 714, 779 446 817, 345 466 505, 535 500 975, 793 363 571, 1 052 373 865,
    455 984 785, 339 227 109, 1 050 973 846, 513 368 817, 91 315 820, 113 925 357}, n]}]
```

k=5, r=1 totalistic (classes 2/3/4)

In[26]:=

```
gen5TC[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {5, 1}, 1}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules ->
      {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 -> RandomColor[],
        5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data5T4CC[W_Integer, H_Integer, n_Integer] := Table[gen5TC[i, W, H] -> 4,
  {i, RandomChoice[{644 218 533, 491 739 943, 6 889 640, 986 144 962, 1 099 816 682,
    988 971 204, 300 829 994, 272 622 024, 304 100 638, 626 595 633}, n]}]
data5T3CC[W_Integer, H_Integer, n_Integer] := Table[gen5TC[i, W, H] -> 3,
  {i, RandomChoice[{889 082 395, 541 068 260, 807 907 479, 816 180 062, 650 485 139,
    643 827 745, 753 940 864, 871 525 323, 351 440 311, 83 501 460}, n]}]
data5T2CC[W_Integer, H_Integer, n_Integer] := Table[gen5TC[i, W, H] -> 2,
  {i, RandomChoice[{525 735 659, 1 022 330 944, 1 007 796 739, 495 633 437, 1 036 827 943}, n]}]
genData5TCC[W_Integer, H_Integer, n_Integer] :=
  Join[data5T4CC[W, H, n], data5T3CC[W, H, n], data5T2CC[W, H, n]]
```

Generate test datasets

k=2, r=2 non-totalistic

```
In[31]:= genk2r2C[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, 2, 2}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules ->
      {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 -> RandomColor[],
        5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
datak2r2C[W_Integer, H_Integer, n_Integer] := Table[genk2r2C[i, W, H] -> i,
  {i, RandomChoice[Range[0, 4 294 967 295], n]}]
```

k=2, r=3 non-totalistic

```
In[33]:= genk2r3NT[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, 2, 3}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules ->
      {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 -> RandomColor[],
        5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
datak2r3NT[W_Integer, H_Integer, n_Integer] :=
  Table[genk2r3NT[i, W, H] -> i, {i, RandomInteger[2^2^7 - 1, n]}]
```

k=3, r=1 non-totalistic

```
In[35]:= genk3r1NT[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, 3}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[],
      3 -> RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[],
      6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
datak3r1NT[W_Integer, H_Integer, n_Integer] :=
  Table[genk3r1NT[i, W, H] -> i, {i, RandomInteger[3^3^3 - 1, n]}]
```

k=3, r=2 totalistic

```
In[37]:= genk3r2C[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {3, 1}, 2}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules ->
      {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 -> RandomColor[],
        5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
datak3r2C[W_Integer, H_Integer, n_Integer] := Table[genk3r2C[i, W, H] -> i,
  {i, RandomChoice[Range[0, 177 146], n]}]
```

k=3, r=3 totalistic

```
In[39]:= genk3r3C[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {3, 1}, 3}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules ->
      {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 -> RandomColor[],
        5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
datak3r3C[W_Integer, H_Integer, n_Integer] := Table[genk3r3C[i, W, H] -> i,
  {i, RandomChoice[Range[0, 14 348 906], n]}]
```

k=4, r=1 non-totalistic

```
In[41]:= genk4r1NT[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, 4}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[],
      3 -> RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[],
      6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
datak4r1NT[W_Integer, H_Integer, n_Integer] :=
  Table[genk4r1NT[i, W, H] -> i, {i, RandomInteger[4^4^3 - 1, n]}]
```

k=4, r=1 totalistic

```
In[43]:= genk4r1C[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {4, 1}}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules ->
      {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 -> RandomColor[],
        5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
datak4r1C[W_Integer, H_Integer, n_Integer] := Table[genk4r1C[i, W, H] -> i,
  {i, RandomChoice[Range[0, 1 048 575], n]}]
```

k=4, r=2 totalistic

```
In[45]:= genk4r2C[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {4, 1}, 2}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules ->
      {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 -> RandomColor[],
        5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
datak4r2C[W_Integer, H_Integer, n_Integer] := Table[genk4r2C[i, W, H] -> i,
  {i, RandomChoice[Range[0, 4 294 967 295], n]}]
```

k=5, r=1 totalistic

```
In[47]:= gen5T2C[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {5, 1}, 1}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules ->
      {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 -> RandomColor[],
        5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data5T2C[n_Integer, W_Integer, H_Integer] := Table[gen5T2C[i, W, H] -> i,
  {i, RandomChoice[Range[0, 1 220 703 125], n]}]
```

k=6, r=1 totalistic

```
In[49]:= gen6TC[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {6, 1}, 1}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules ->
      {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 -> RandomColor[],
        5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data6TC[n_Integer, W_Integer, H_Integer] := Table[gen6TC[i, W, H] -> i,
  {i, RandomInteger[2 821 109 907 455, n]}]
```

k=6, r=2 totalistic

```
In[51]:= gen6T2C[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {6, 1}, 2}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules ->
      {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 -> RandomColor[],
        5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data6T2C[n_Integer, W_Integer, H_Integer] := Table[gen6T2C[i, W, H] -> i,
  {i, RandomInteger[170 581 728 179 578 208 255, n]}]
```


k=7, r=1 totalistic

```
In[53]:= gen7TC[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {7, 1}, 1}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules ->
      {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 -> RandomColor[],
        5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data7TC[n_Integer, W_Integer, H_Integer] := Table[gen7TC[i, W, H] -> i,
  {i, RandomInteger[11 398 895 185 373 142, n]}]
```

k=8, r=1 totalistic

```
In[55]:= gen8TC[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {8, 1}, 1}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules ->
      {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 -> RandomColor[],
        5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data8TC[n_Integer, W_Integer, H_Integer] := Table[gen8TC[i, W, H] -> i,
  {i, RandomInteger[73 786 976 294 838 206 463, n]}]
```

Network XIII - Two convolutions, dropout on linear only, BatchNorm

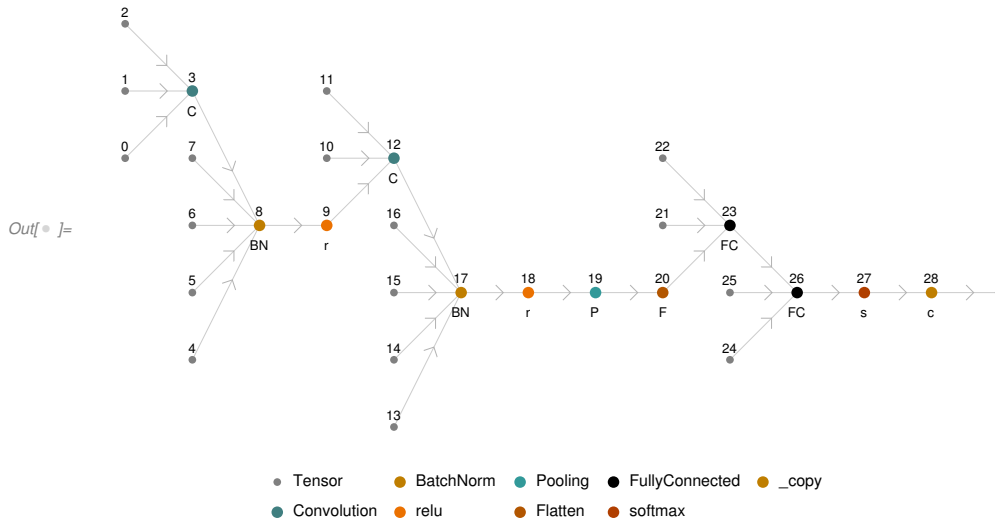
```
In[ ]:= netECA13 = netSevenCC512drop[128, 128]
```

```
Out[ ]:= NetChain[
```

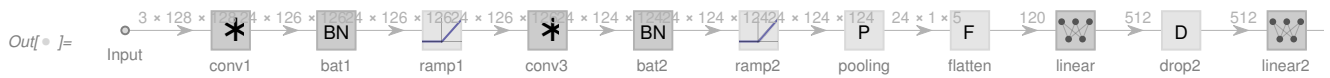


```
]
```

```
In[ ]:= NetInformation[netECA13, "MXNetNodeGraphPlot"]
```



```
In[ ]:= NetInformation[netECA13, "SummaryGraphic"]
```



```
In[ ]:= dataECA13 = dataC[128, 128, 8192];
```

```
In[ ]:= dataTotalistic2BigC13 = genData2r2C[128, 128, 1024];
```

```
In[ ]:= dataTotalistic3BigC13 = data3T2C[128, 128, 1024];
```

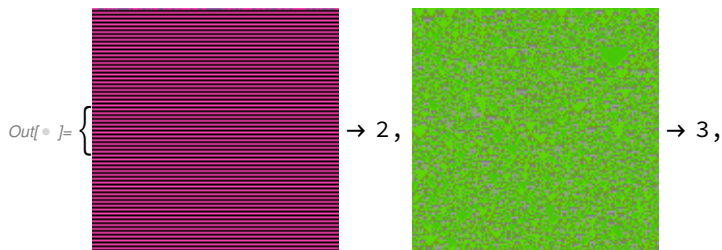
```
In[ ]:= dataTotalistic4BigC13 = data4TC[128, 128, 1024];
```

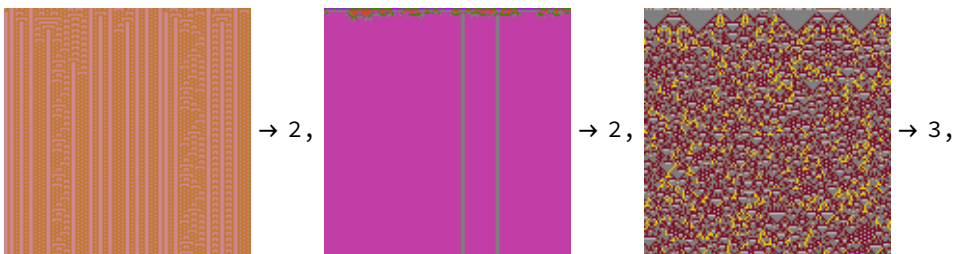
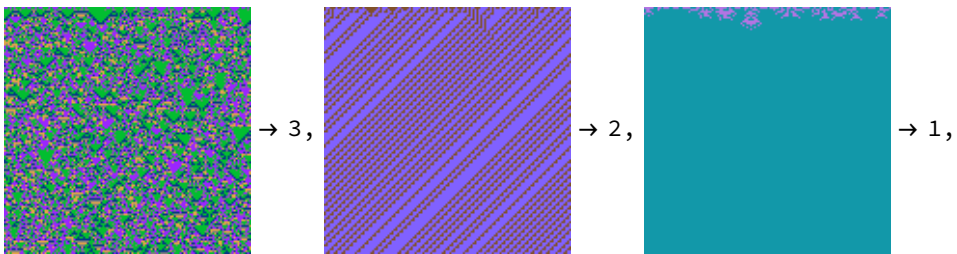
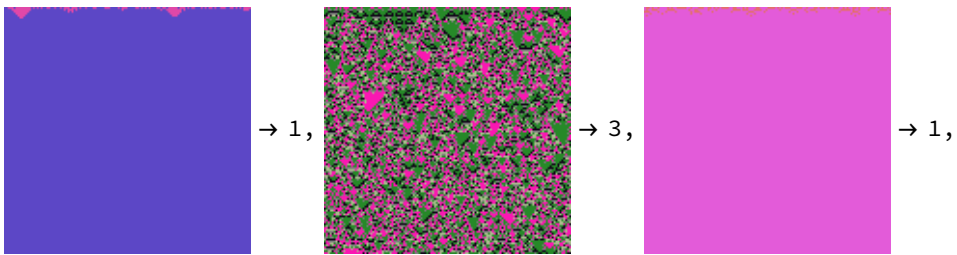
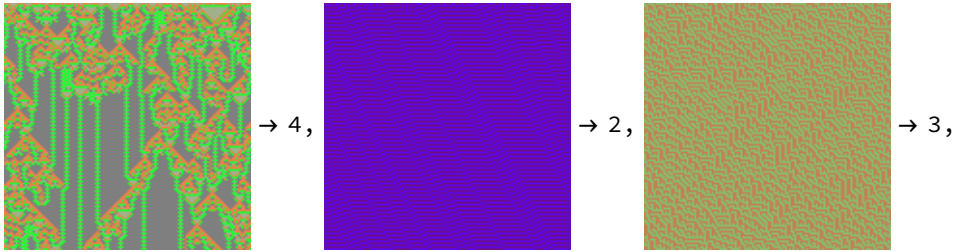
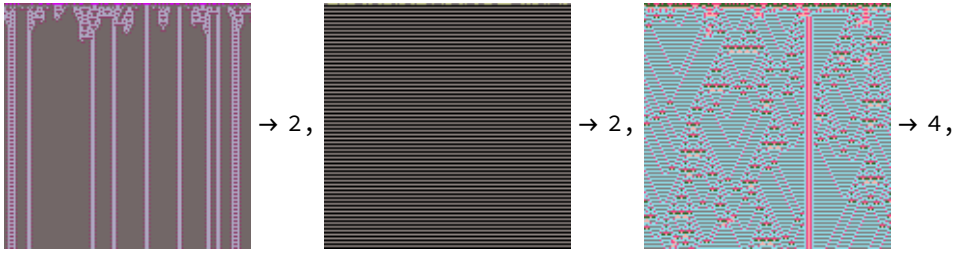
```
In[ ]:= dataTotalistic5BigC13 = genData5TCC[128, 128, 4096];
```

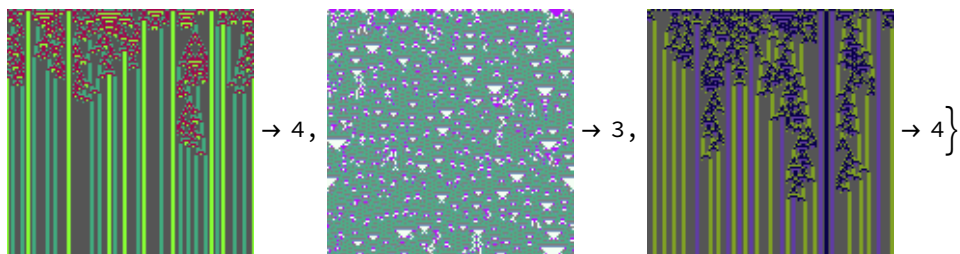
```
In[ ]:= fullTrainingBigC13 = Join[dataECA13, dataTotalistic2BigC13,
    dataTotalistic3BigC13, dataTotalistic4BigC13, dataTotalistic5BigC13];
Length[fullTrainingBigC13]
```

Out[]:= 26 624

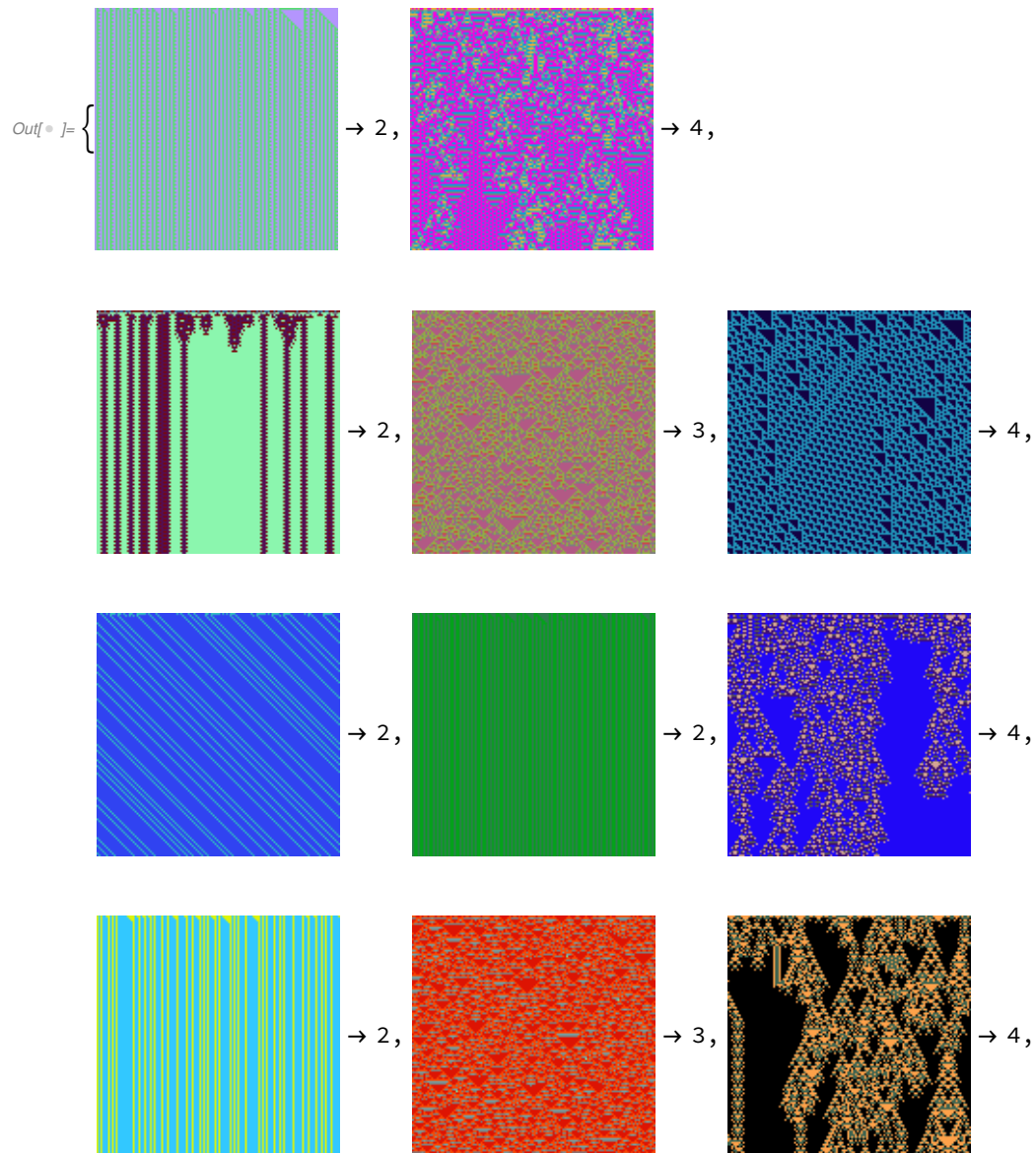
```
In[ ]:= RandomSample[fullTrainingBigC13, 20]
```

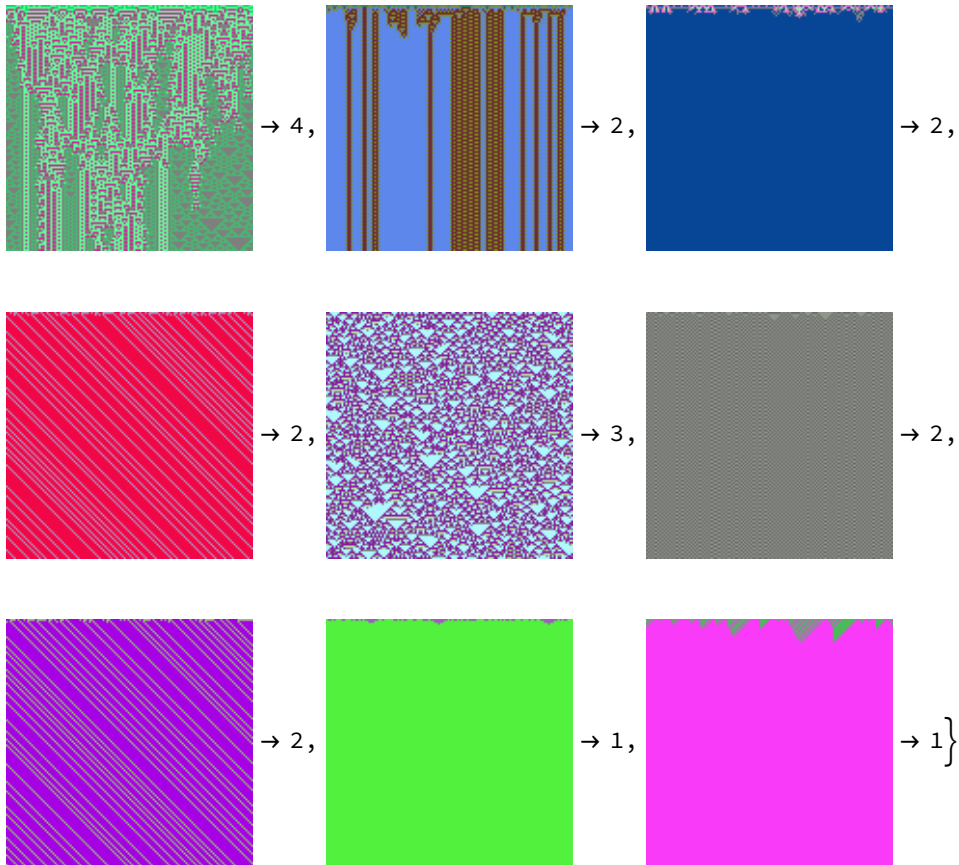






`In[]:= RandomSample[fullTrainingBigC13, 20]`





```
In[ ]:= dir = SetDirectory[NotebookDirectory[]]
```

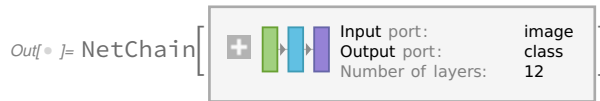
```
Out[ ]:= /Users/thorsilver/Downloads/Wolfram notebooks
```

```
In[ ]:= netECA12 = Import["netECA12-r12.wlnet"]
```

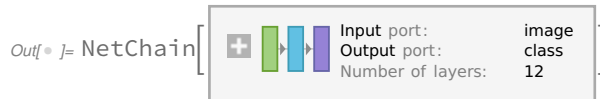
```
Out[ ]:= NetChain[
```

	conv1	Input	image
	bat1	ConvolutionLayer	array (size: 3 × 120 × 200)
	ramp1	BatchNormalizationLayer	array (size: 24 × 118 × 198)
	conv3	Ramp	array (size: 24 × 118 × 198)
	bat2	ConvolutionLayer	array (size: 24 × 116 × 196)
	ramp2	BatchNormalizationLayer	array (size: 24 × 116 × 196)
	pooling	Ramp	array (size: 24 × 116 × 196)
	flatten	PoolingLayer	array (size: 24 × 1 × 5)
	linear	FlattenLayer	vector (size: 120)
	drop2	LinearLayer	vector (size: 512)
	linear2	DropoutLayer	vector (size: 512)
	softmax	LinearLayer	vector (size: 4)
		SoftmaxLayer	vector (size: 4)
		Output	class

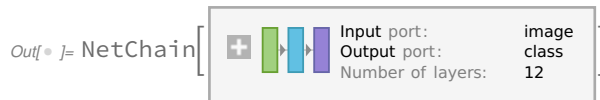
```
In[ ]:= netECA13 =
  NetTrain[netECA13, fullTrainingBigC13, MaxTrainingRounds → 20, BatchSize → 256 * 4,
    TargetDevice → "CPU", TrainingProgressCheckpointing → {"Directory", dir}]
```



```
In[ ]:= netECA13 = Import["netECA13-r20.wlnet"]
```



```
In[ ]:= netECA13 =
  NetTrain[netECA13, fullTrainingBigC13, MaxTrainingRounds → 20, BatchSize → 256 * 4,
    TargetDevice → "CPU", TrainingProgressCheckpointing → {"Directory", dir}]
```



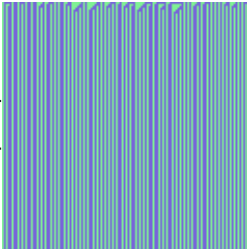
Generate test data for Network XIII

```
In[ ]:= testDataECABigC = dataC[128, 128, 1024];
testData2TBigC = genData2r2C[128, 128, 1024];
testData3TBigC = data3T2C[128, 128, 1024];
testData4TBigC = data4TC[128, 128, 1024];
testData5TBigC = genData5TCC[128, 128, 1024];
fullTestSetBigC = Join[testDataECABigC,
  testData2TBigC, testData3TBigC, testData4TBigC, testData5TBigC];
Length[fullTestSetBigC]
```

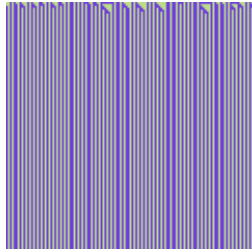
Out[]:= 10 240


```
In[ ]:= RandomSample[fullTestSetBigC, 10]
```

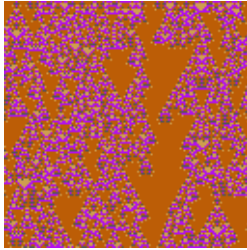
Out[]:= {



→ 2,



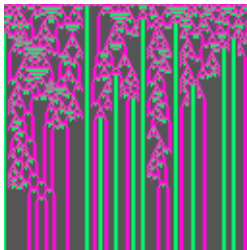
→ 2,



→ 4,



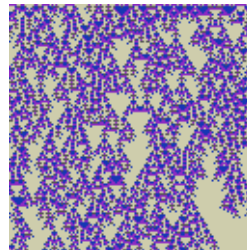
→ 3,



→ 4,



→ 4,



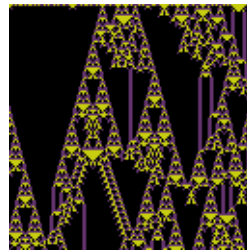
→ 4,



→ 4,



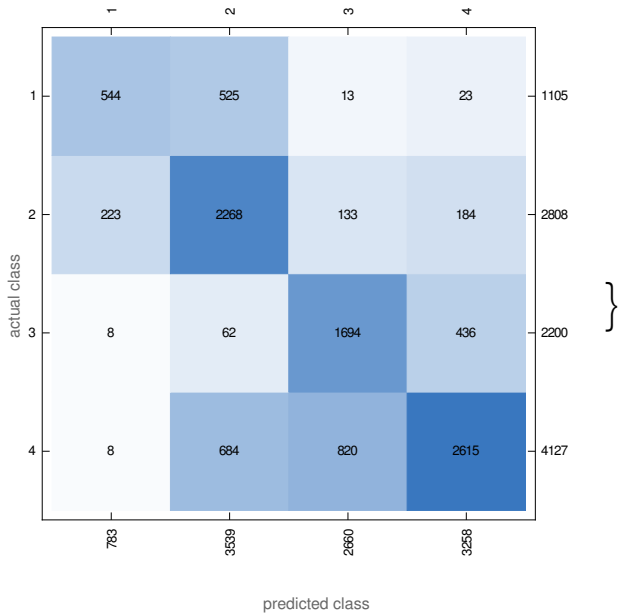
→ 4,



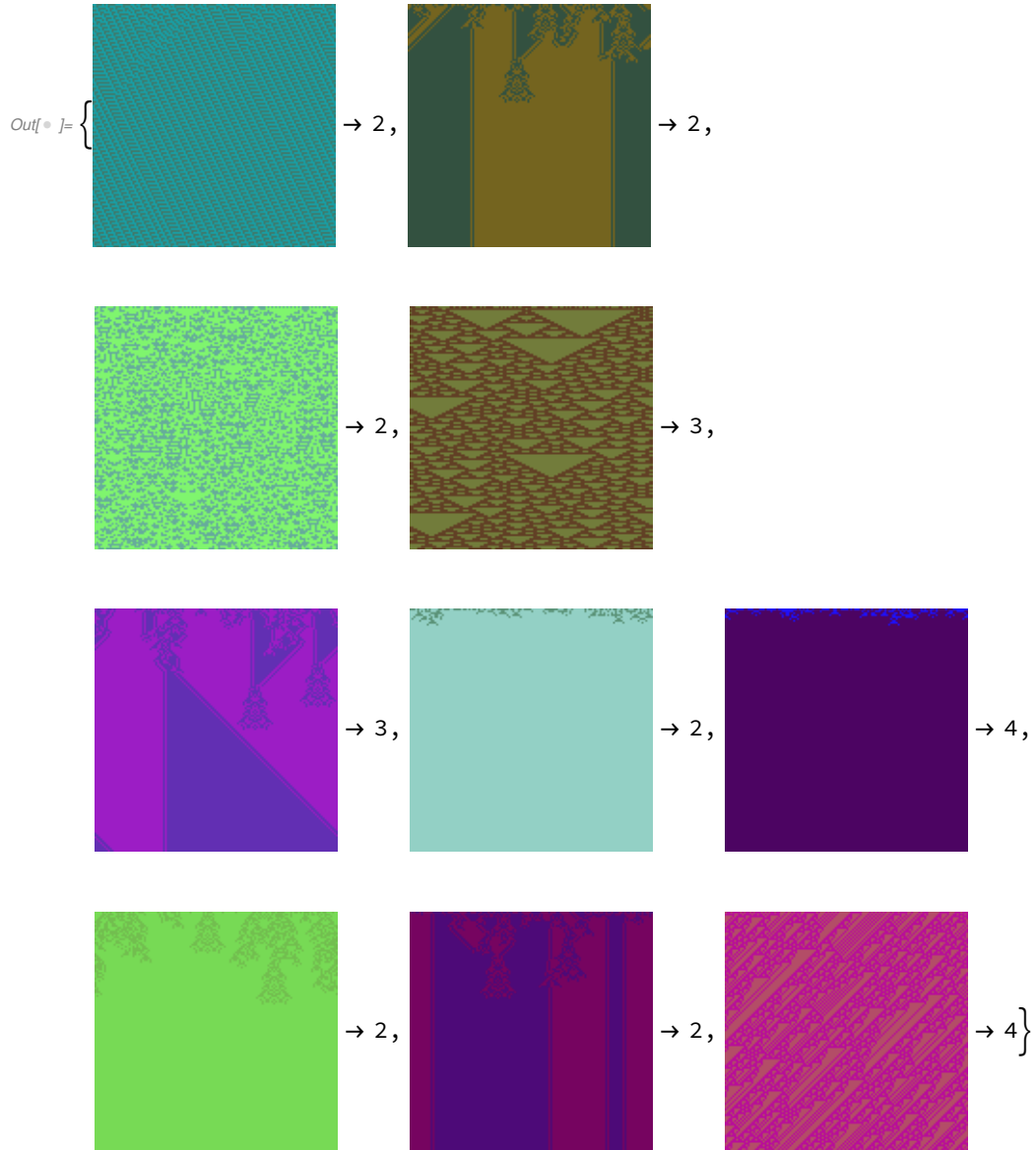
→ 4}

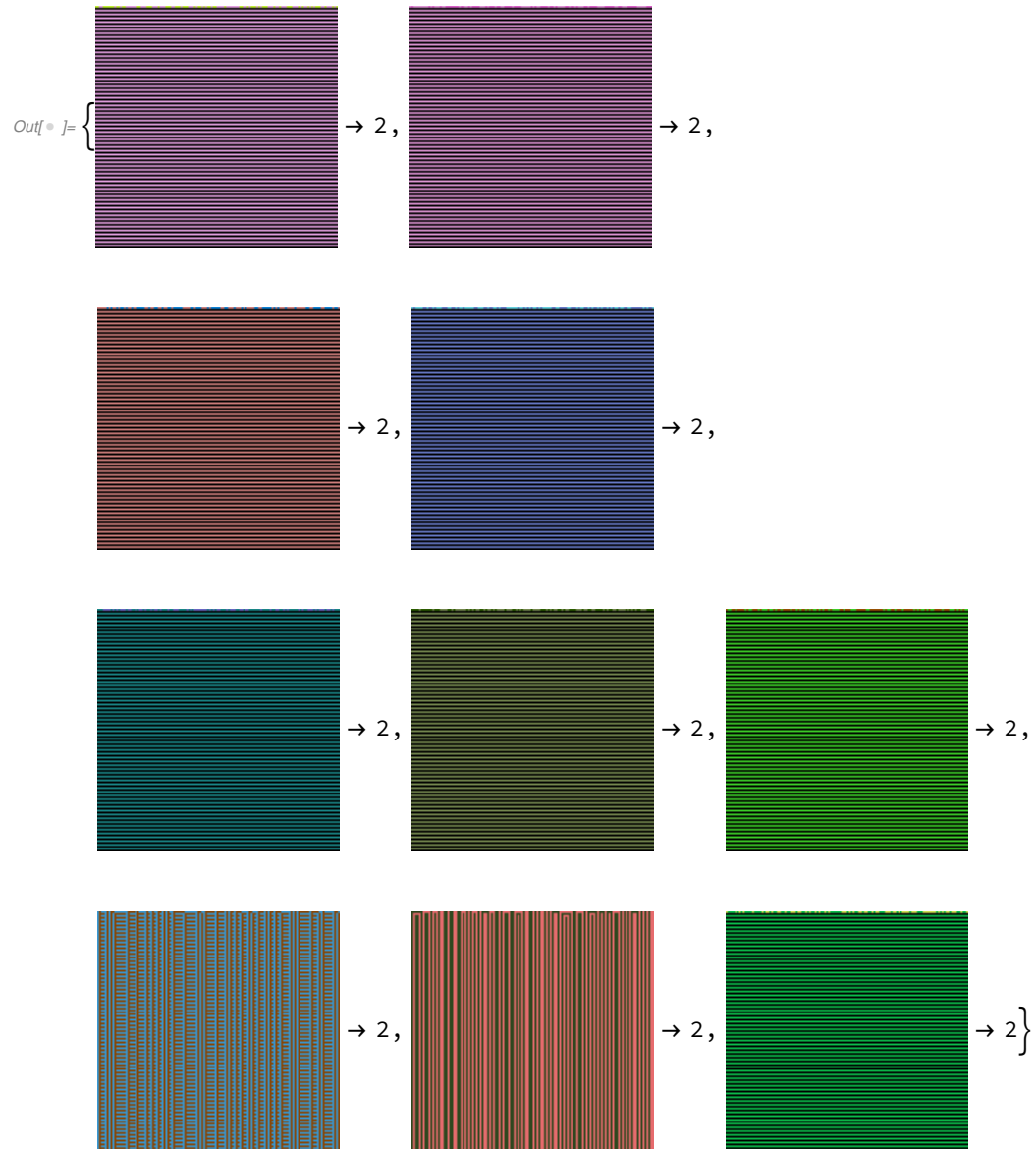
```
In[ ]:= NetMeasurements[netECA13, fullTestSetBigC,
  {"Accuracy", "Precision", "ConfusionMatrixPlot"}]
```

```
Out[ ]:= {0.69541, <| 1 → 0.694764, 2 → 0.640859, 3 → 0.636842, 4 → 0.80264 |>,
```



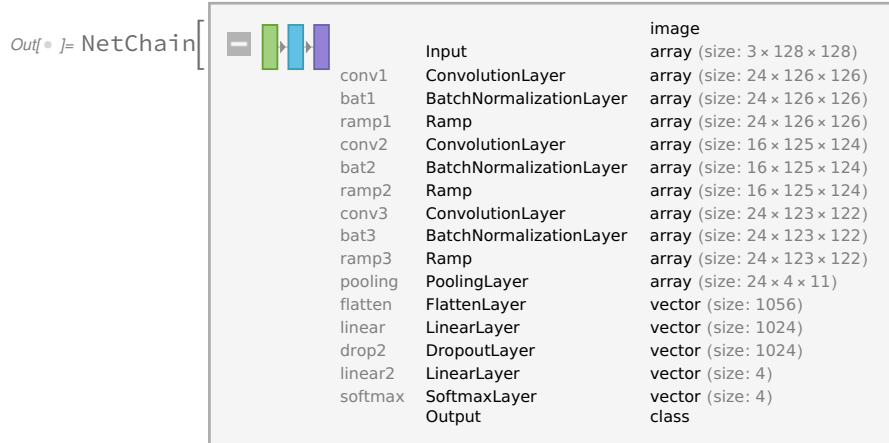
```
In[ ]:= entropyImagesBigC = RandomSample[Keys[fullTestSetBigC], 500];
  entropiesBigC = netECA13[entropyImagesBigC, "Entropy"];
  highEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, -10]]];
  lowEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, 10]]];
  Thread[highEntBigC → netECA13[highEntBigC]]
  Thread[lowEntBigC → netECA13[lowEntBigC]]
```



Network XIV - BatchNorm, 1024 linear, dropout

```
In[ ]:= netECA14 = netEightCC512drop[128, 128]
```



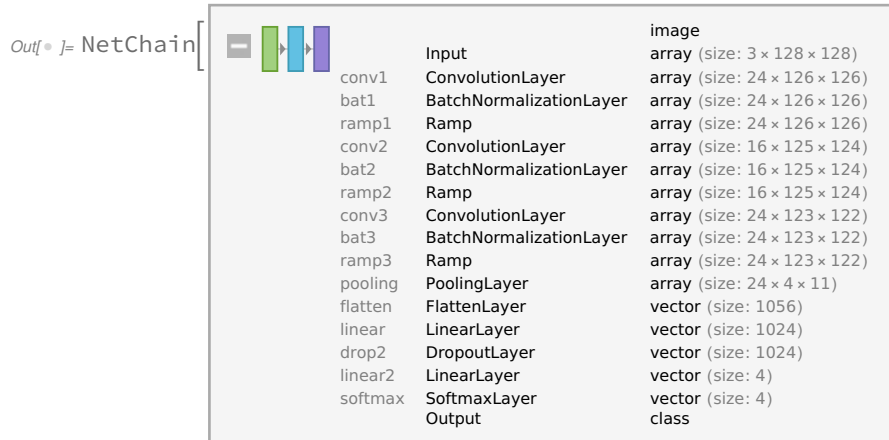
```
netECA14 =
```

```
NetTrain[netECA14, fullTrainingBigC13, MaxTrainingRounds → 20, BatchSize → 256 * 4,  
TargetDevice → "CPU", TrainingProgressCheckpointing → {"Directory", dir}]
```

```
In[ ]:= dir = SetDirectory[NotebookDirectory[]]
```

```
Out[ ]:= /Users/thorsilver/Downloads/Wolfram notebooks
```

```
In[ ]:= netECA14 = Import["netECA14-r20.wlnet"]
```

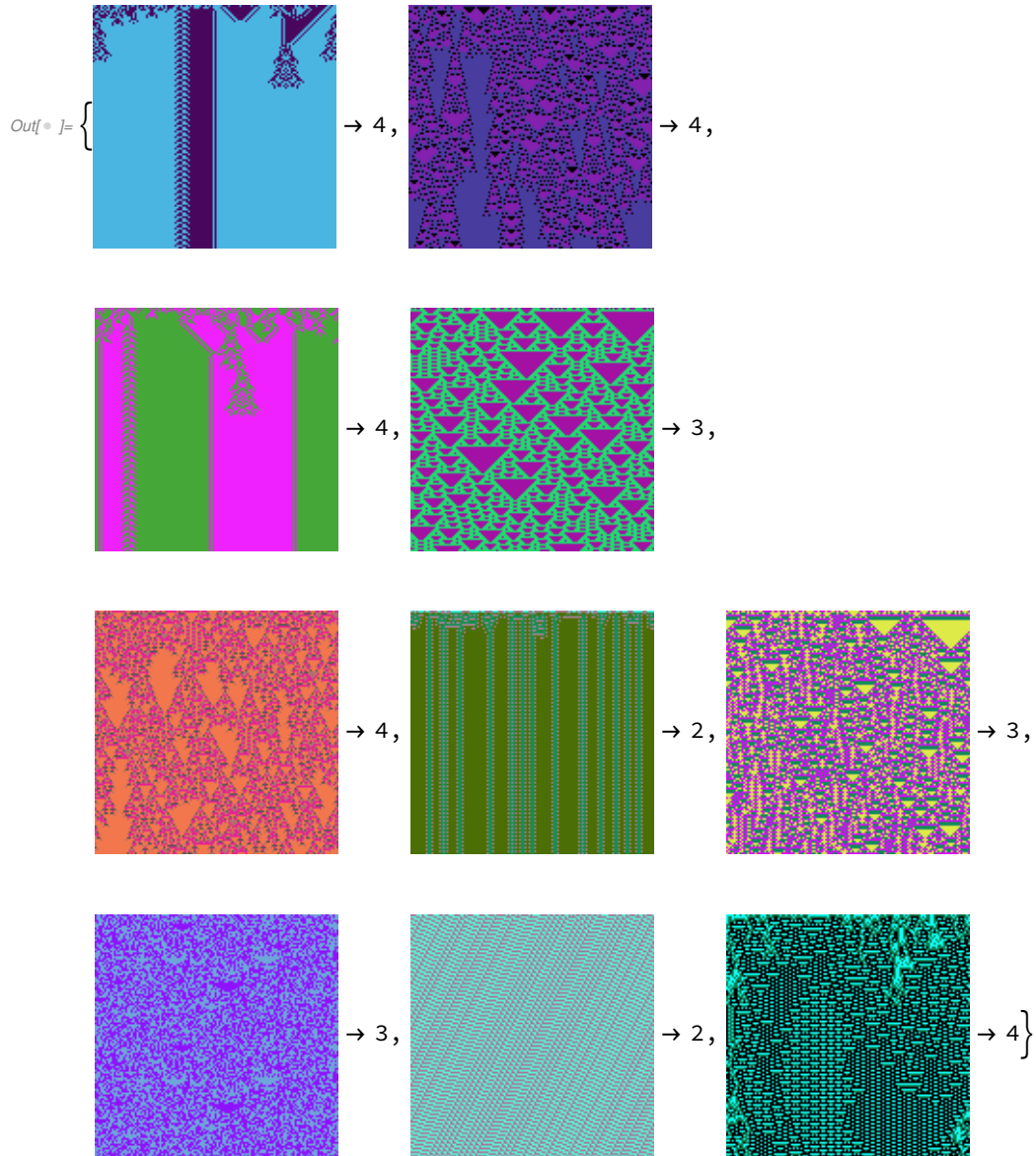


Generating test data for Network XIV

```
In[ ]:= testDataECABigC = dataC[128, 128, 1024];  
testData2TBigC = genData2r2C[128, 128, 1024];  
testData3TBigC = data3T2C[128, 128, 1024];  
testData4TBigC = data4TC[128, 128, 1024];  
testData5TBigC = genData5TCC[128, 128, 1024];  
fullTestSetBigC = Join[testDataECABigC,  
  testData2TBigC, testData3TBigC, testData4TBigC, testData5TBigC];  
Length[fullTestSetBigC]
```

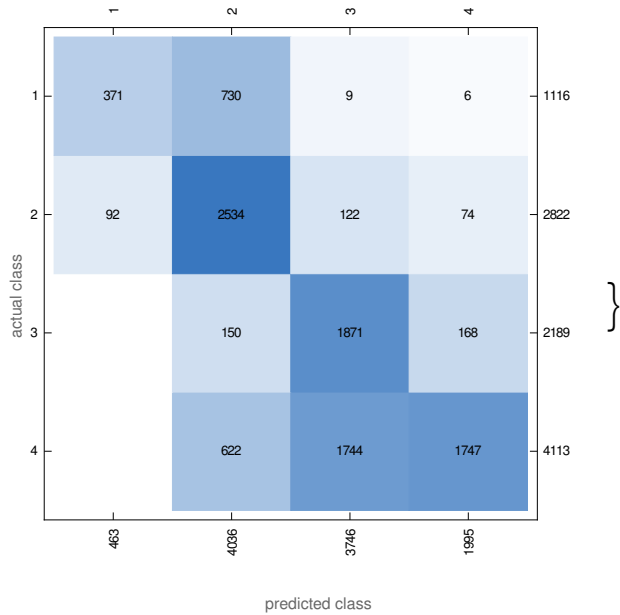
```
Out[ ]:= 10 240
```

```
In[ ]:= RandomSample[fullTestSetBigC, 10]
```

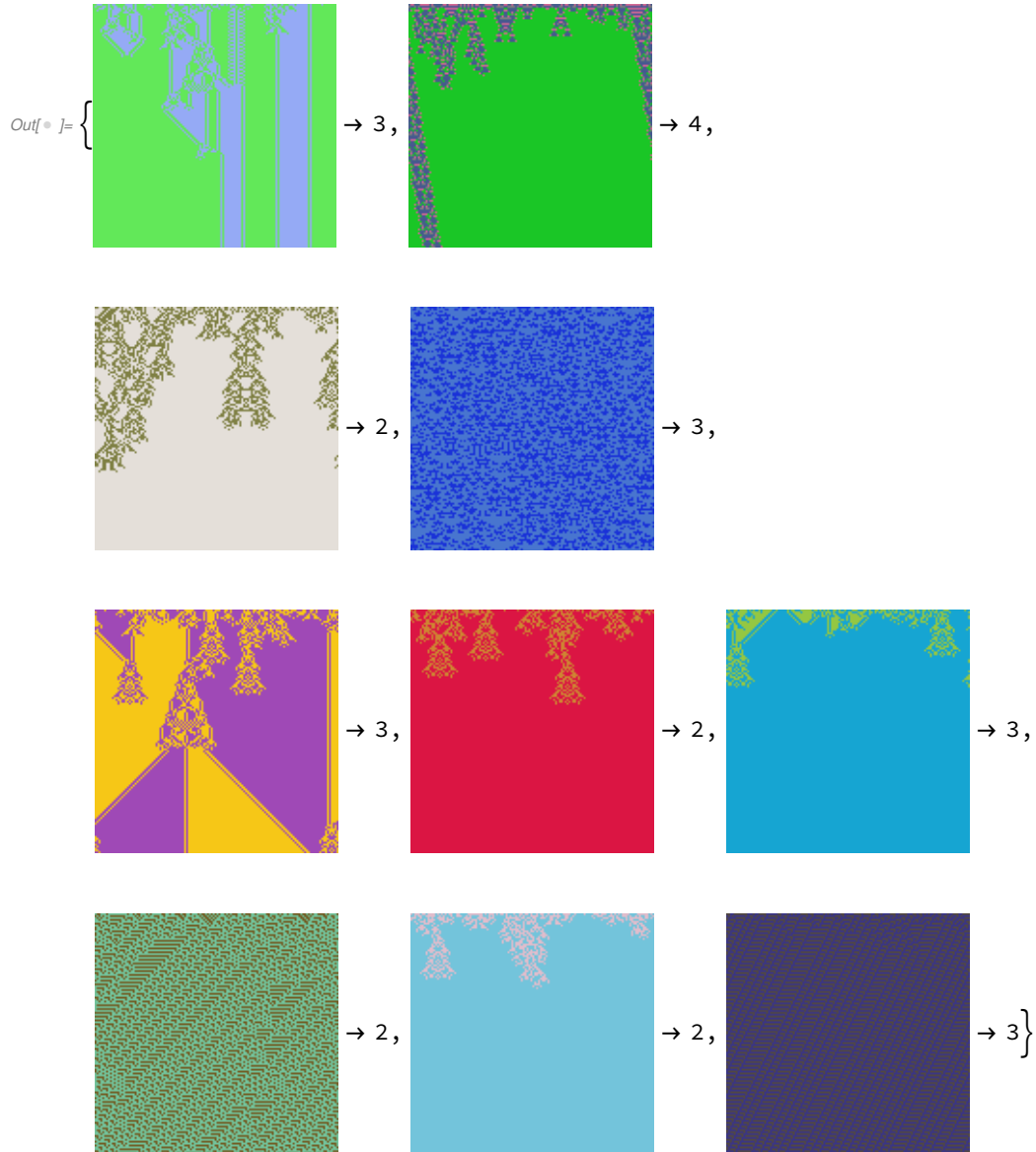


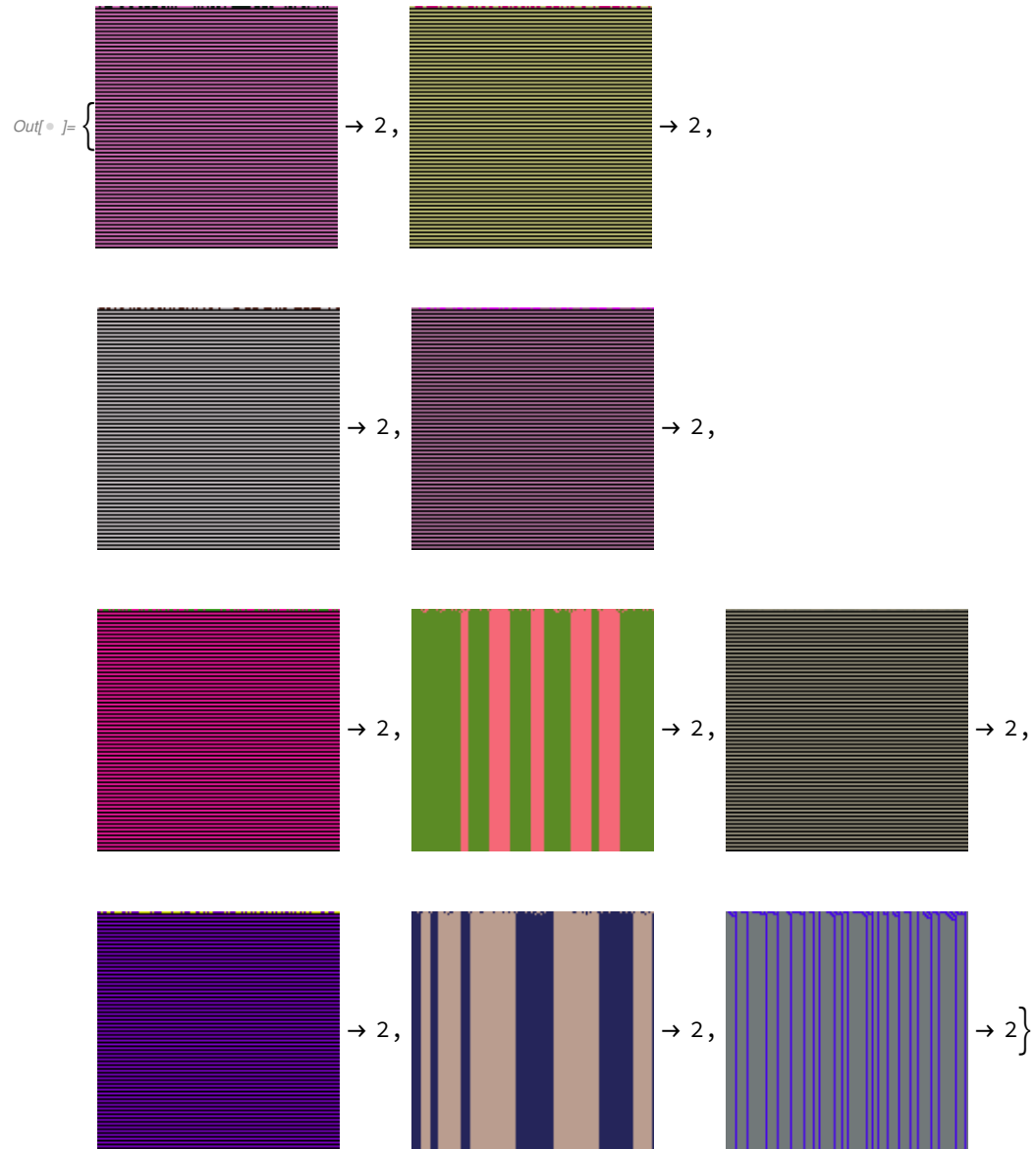
```
In[ ]:= NetMeasurements[netECA14, fullTestSetBigC,
  {"Accuracy", "Precision", "ConfusionMatrixPlot"}]
```

```
Out[ ]:= {0.637012, <| 1 → 0.801296, 2 → 0.627849, 3 → 0.499466, 4 → 0.875689 |>,
```



```
In[ ]:= entropyImagesBigC = RandomSample[Keys[fullTestSetBigC], 500];
  entropiesBigC = netECA14[entropyImagesBigC, "Entropy"];
  highEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, -10]]];
  lowEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, 10]]];
  Thread[highEntBigC → netECA14[highEntBigC]]
  Thread[lowEntBigC → netECA14[lowEntBigC]]
```



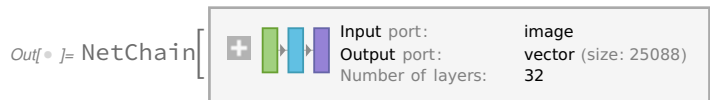


Network XV - Transfer learning with pre-trained image recognition net (VGG-16)

```
In[ ]:= netECA15 = NetModel["VGG-16 Trained on ImageNet Competition Data"]
```



```
In[ ]:= subNet = NetTake[netECA15, {"conv1_1", "flatten_0"}]
```



```
In[ ]:= joinedNet = NetJoin[subNet,
  NetChain@<{"linear_new" → LinearLayer[1024], "linear_out" → LinearLayer[4],
    "prob" → SoftmaxLayer[]}>, "Output" → NetDecoder[{"Class", Range[1, 4]}]]
```



```
In[ ]:= netECA15final = NetPrepend[joinedNet, {"augment" → ImageAugmentationLayer[{224, 224}]},
  "Input" → NetExtract[joinedNet, "Input"]]
```

```
Out[ ]:= NetChain[
  {
    + uninitialized
    Input port: image
    Output port: class
    Number of layers: 36
  }
]
```

```
In[ ]:= dataECA15 = dataC[224, 224, 8192];
```

```
In[ ]:= dataTotalistic2BigC15 = genData2r2C[224, 224, 1024];
```

```
In[ ]:= dataTotalistic3BigC15 = data3T2C[224, 224, 512];
```

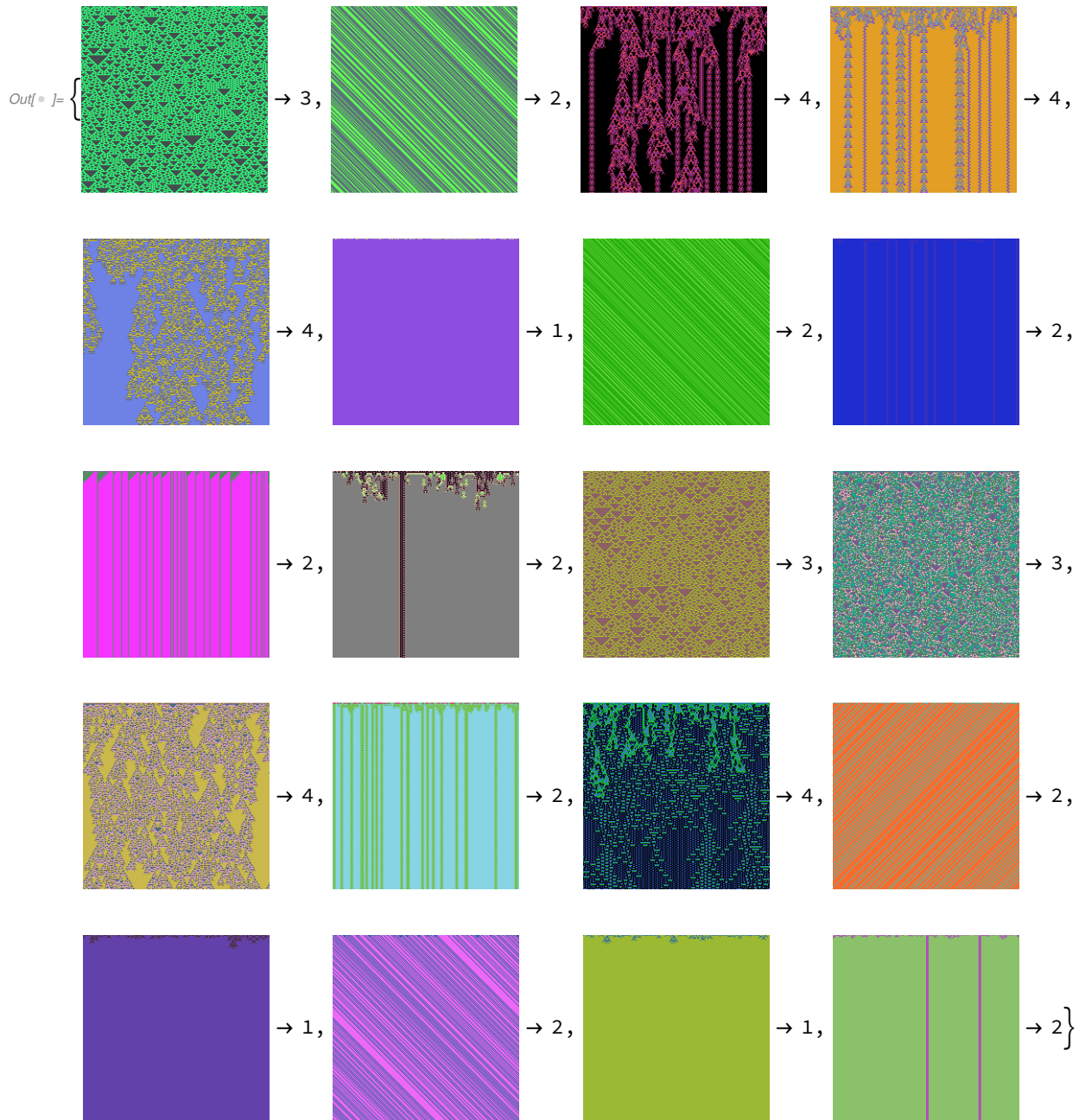
```
In[ ]:= dataTotalistic4BigC15 = data4TC[224, 224, 512];
```

```
In[ ]:= dataTotalistic5BigC15 = genData5TCC[224, 224, 1024];
```

```
In[ ]:= fullTrainingBigC15 = Join[dataECA15, dataTotalistic2BigC15,
  dataTotalistic3BigC15, dataTotalistic4BigC15, dataTotalistic5BigC15];
Length[fullTrainingBigC15]
```

```
Out[ ]:= 16384
```

```
In[ ]:= RandomSample[fullTrainingBigC15, 20]
```



```
In[ ]:= netECA15final =
```

```
NetTrain[netECA15final, fullTrainingBigC15, MaxTrainingRounds → 5, BatchSize → 256 * 4,
  TargetDevice → "CPU", TrainingProgressCheckpointing → {"Directory", dir},
  LearningRateMultipliers → {"linear_new" → 1, "linear_out" → 1, _ → 0}]
```

Network XVI - Three convolutions, dropout on linear only, BatchNorm

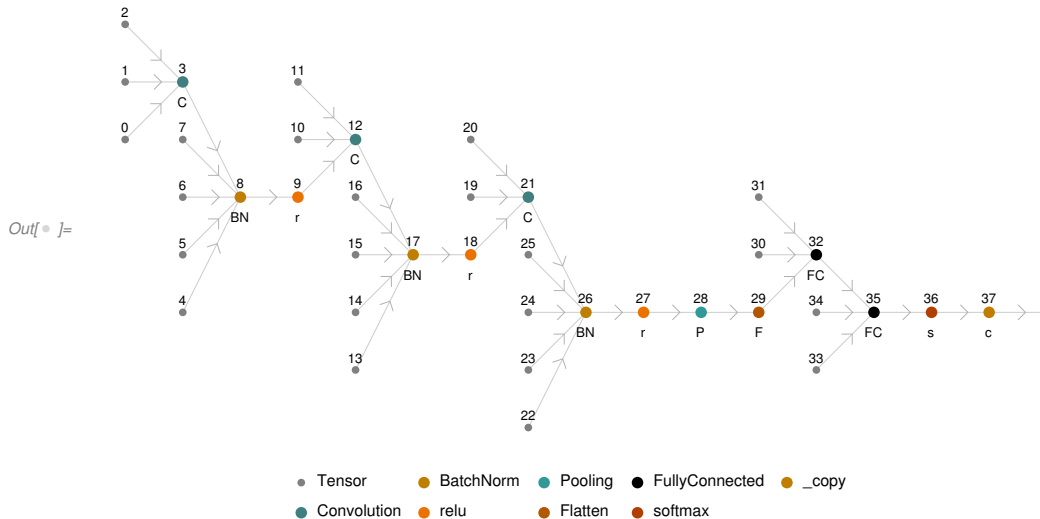
```
In[57]:= netECA16 = netNineCC512drop[128, 128]
```

```
Out[57]= NetChain[
```

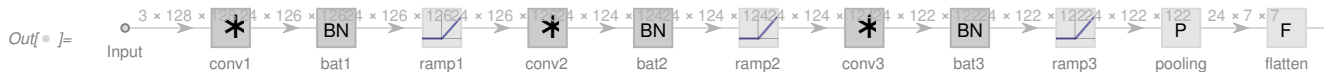


```
]
```

```
In[ ]:= NetInformation[netECA16, "MXNetNodeGraphPlot"]
```



```
In[ ]:= NetInformation[netECA16, "SummaryGraphic"]
```



```
In[58]:= dataECA16 = dataC[128, 128, 8192];
```

```
In[59]:= dataTotalistic2BigC16 = genData2r2C[128, 128, 1024];
```

```
In[60]:= dataTotalistic3BigC16 = data3T2C[128, 128, 1024];
```

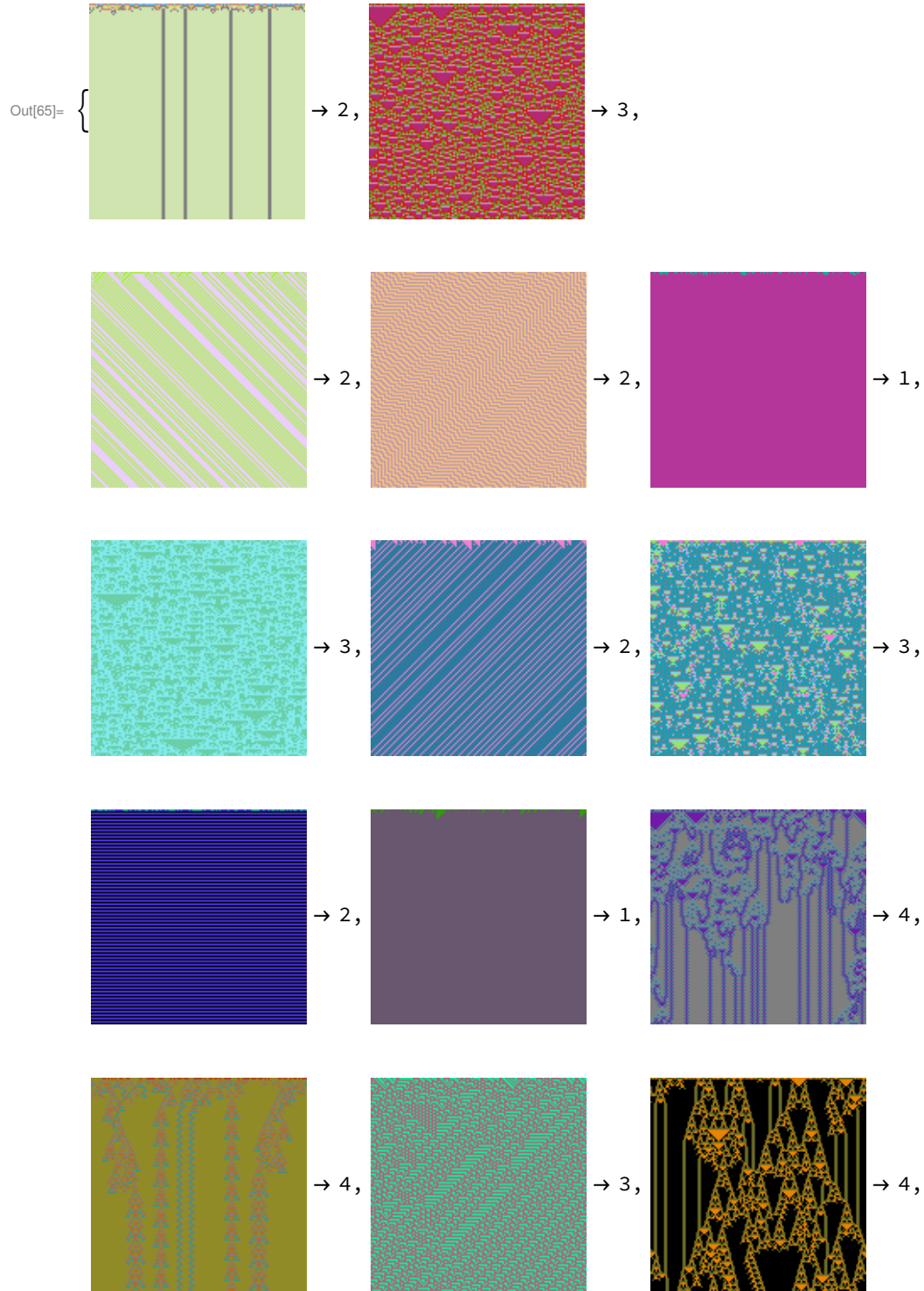
```
In[61]:= dataTotalistic4BigC16 = data4TC[128, 128, 1024];
```

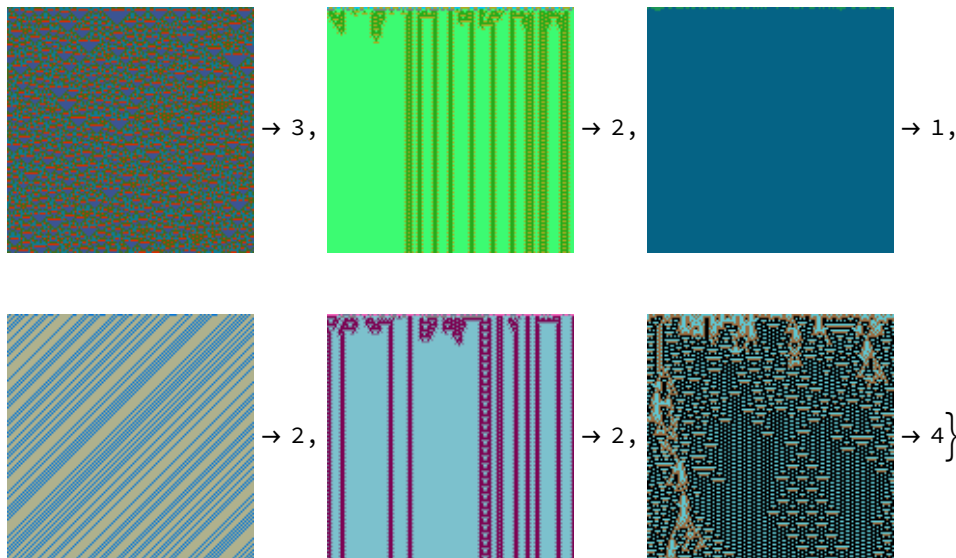
```
In[62]:= dataTotalistic5BigC16 = genData5TCC[128, 128, 4096];
```

```
In[63]:= fullTrainingBigC16 = Join[dataECA16, dataTotalistic2BigC16,
    dataTotalistic3BigC16, dataTotalistic4BigC16, dataTotalistic5BigC16];
Length[fullTrainingBigC16]
```

```
Out[64]= 26 624
```

```
In[65]:= RandomSample[fullTrainingBigC16, 20]
```






```
In[66]:= dir = SetDirectory[NotebookDirectory[]]
```

```
Out[66]= /home/esilverman/Documents
```

```
In[67]:= netECA16 =
```

```
NetTrain[netECA16, fullTrainingBigC16, MaxTrainingRounds → 200, BatchSize → 256,
  TargetDevice → "GPU", TrainingProgressCheckpointing → {"Directory", dir}]
```

Out[67]= NetChain[ Input port: image
Output port: class
Number of layers: 15

```
netECA16 = Import["netECA16-r20.wlnet"]
```

netECA16 =

```
NetTrain[netECA16, fullTrainingBigC16, MaxTrainingRounds → 20, BatchSize → 256 * 4,
  TargetDevice → "CPU", TrainingProgressCheckpointing → {"Directory", dir}]
```

Generate test data for Network XVI

```
In[ ]:= dir = SetDirectory[NotebookDirectory[]]
```

Out[•]= /Users/thorsilver/Downloads/Wolfram notebooks

```
In[9]: netECA16 = Import["netECA16-r20.wlnet"]
```

$Out[i..j] = \text{NetChain} \left[\begin{array}{l} \text{Input port: image} \\ \text{Output port: class} \\ \text{Number of layers: 15} \end{array} \right]$


```

In[68]:= testDataECABigC = dataC[128, 128, 1024];
testData2TBigC = genData2r2C[128, 128, 1024];
testData3TBigC = data3T2C[128, 128, 1024];
testData4TBigC = data4TC[128, 128, 1024];
testData5TBigC = genData5TCC[128, 128, 1024];
fullTestSetBigC = Join[testDataECABigC,
  testData2TBigC, testData3TBigC, testData4TBigC, testData5TBigC];
Length[fullTestSetBigC]

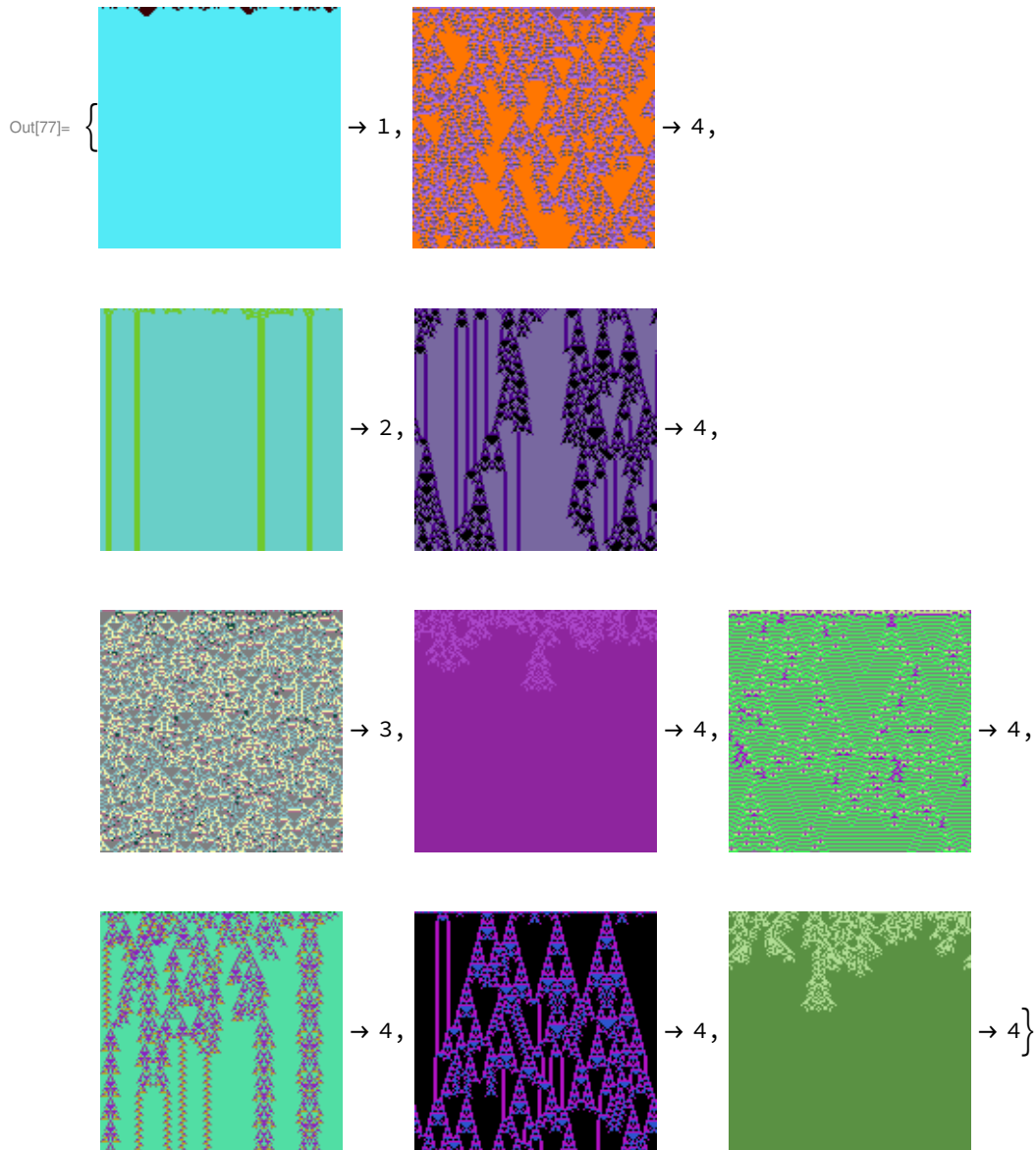
```

Out[74]= 10 240

```

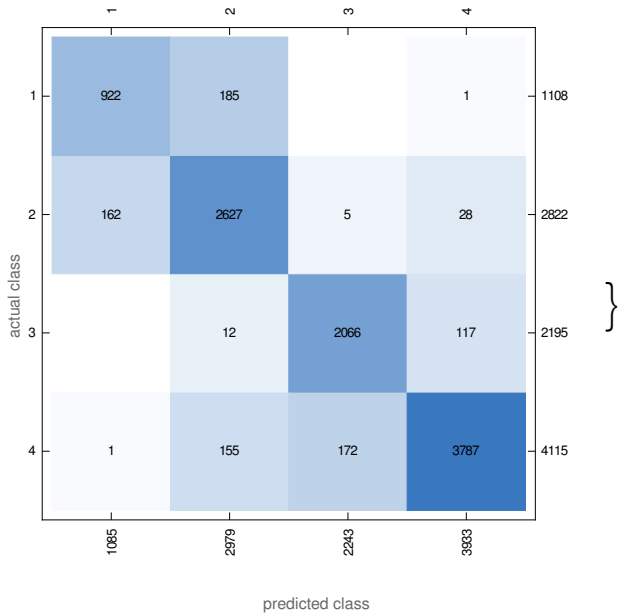
In[77]:= RandomSample[fullTestSetBigC, 10]

```

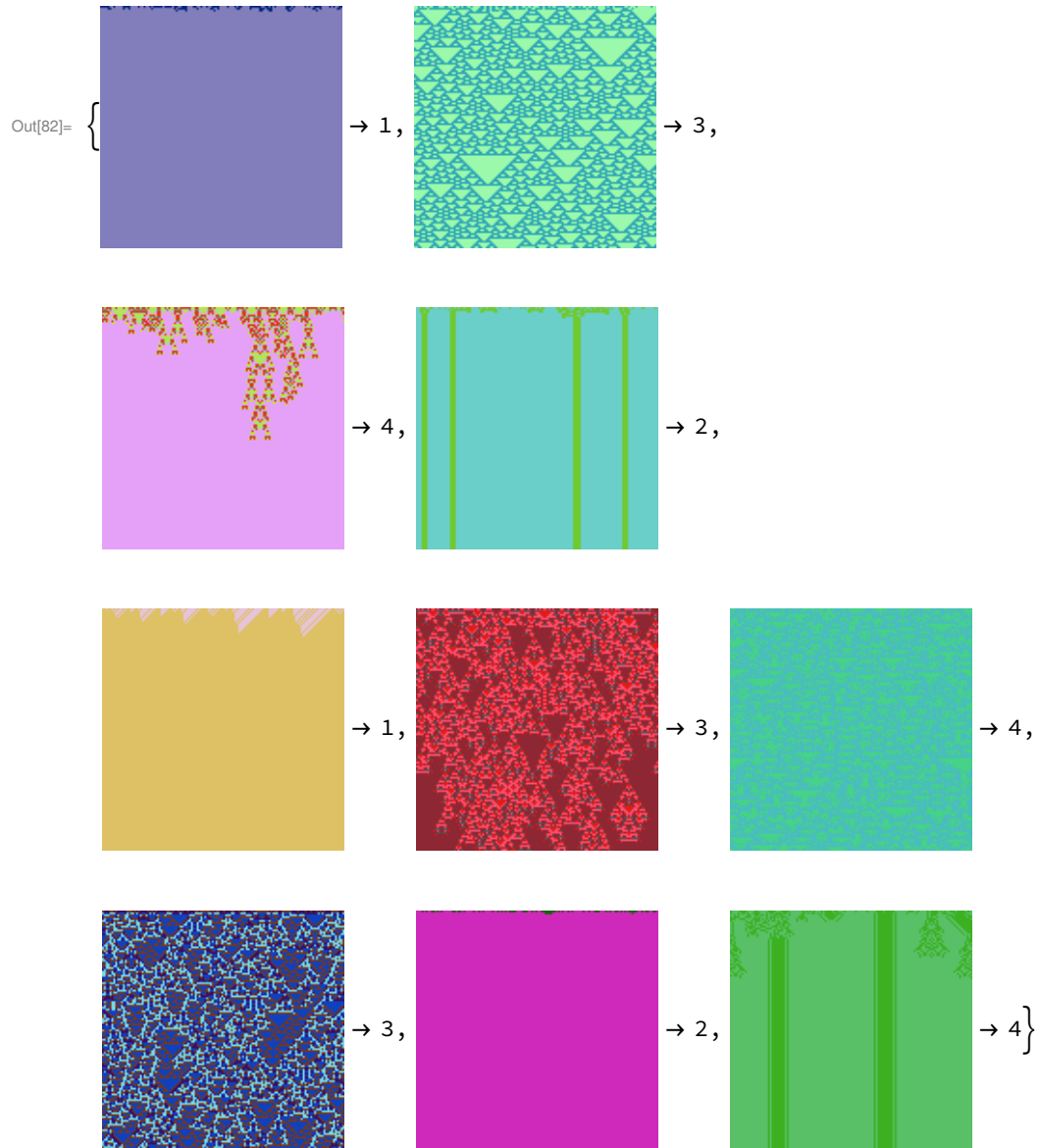


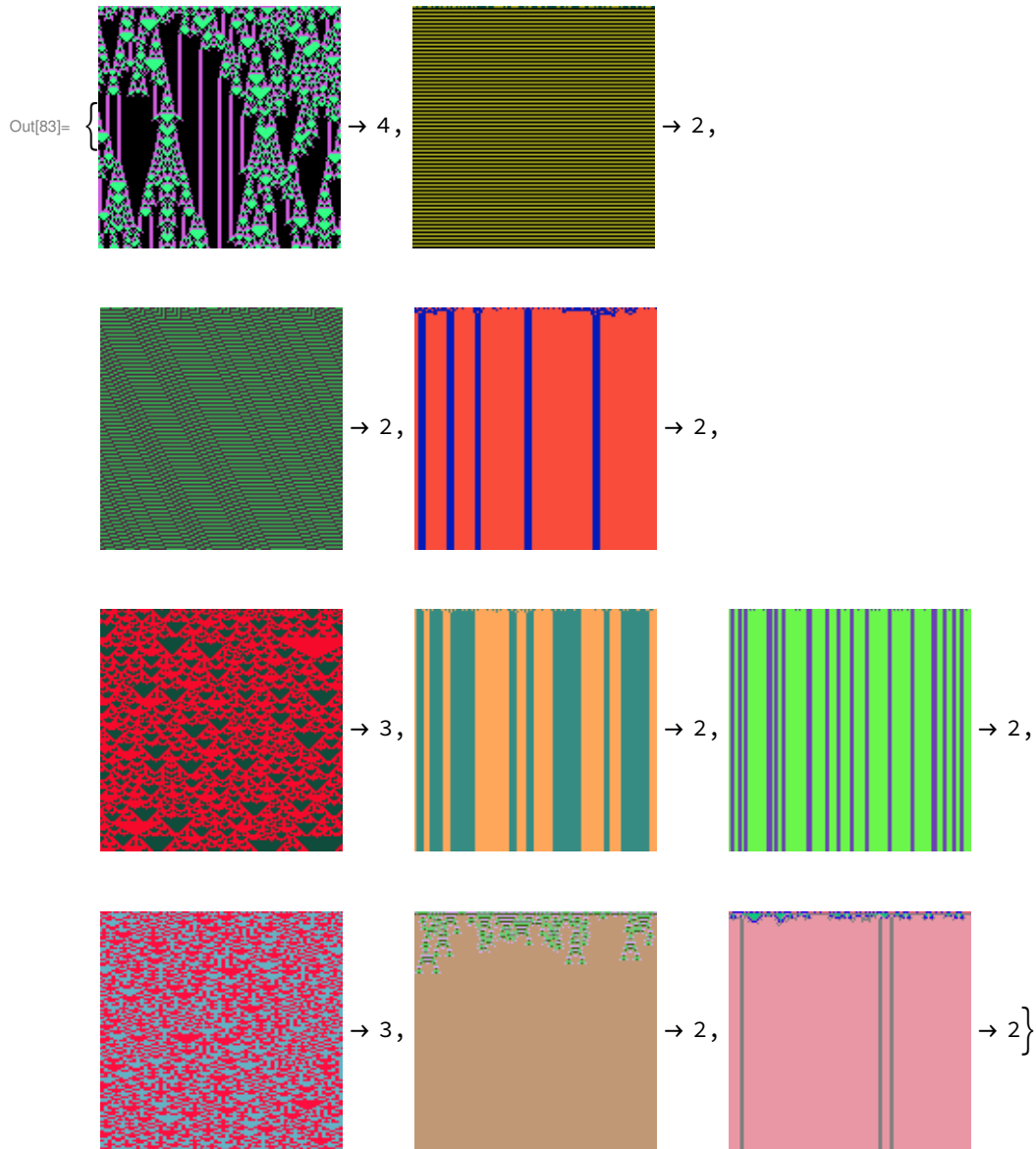
```
In[76]:= NetMeasurements[netECA16, fullTestSetBigC,
  {"Accuracy", "Precision", "ConfusionMatrixPlot"}]
```

```
Out[76]= {0.918164, <| 1 → 0.84977, 2 → 0.88184, 3 → 0.921088, 4 → 0.962878 |>,
```



```
In[78]:= entropyImagesBigC = RandomSample[Keys[fullTestSetBigC], 500];
entropiesBigC = netECA16[entropyImagesBigC, "Entropy"];
highEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, -10]]];
lowEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, 10]]];
Thread[highEntBigC → netECA16[highEntBigC]]
Thread[lowEntBigC → netECA16[lowEntBigC]]
```



Testing Network XVI on unseen CA rule spaces

2-colour non-totalistic, range 2

```
In[84]:= test4Data2kr2C16 = datak2r2C[128, 128, 8];
Thread[test4Data2kr2C16 → netECA16[Keys@test4Data2kr2C16, {"TopProbabilities", 2}]]
```

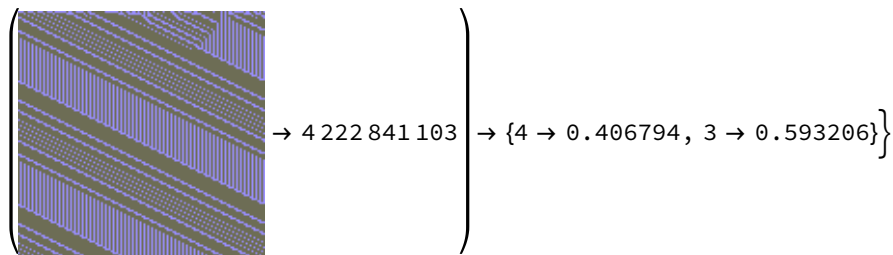
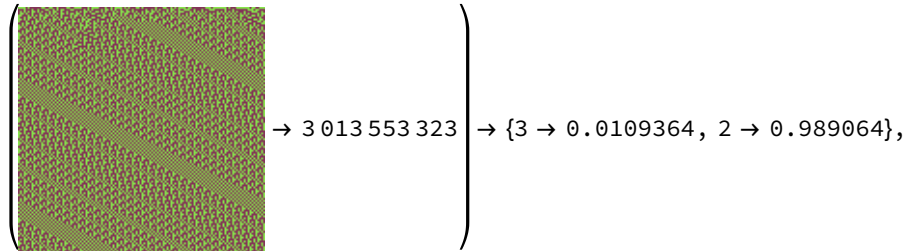
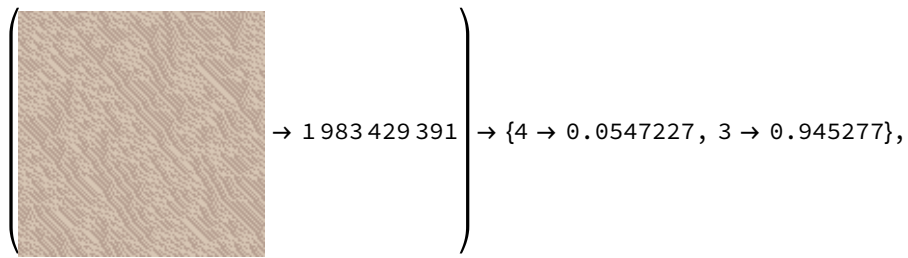
$$\text{Out[85]=} \left\{ \begin{array}{c} \text{[Green noisy image]} \\ \rightarrow 142\,978\,078 \end{array} \right\} \rightarrow \{4 \rightarrow 0.0000385332, 3 \rightarrow 0.999961\},$$

$$\left\{ \begin{array}{c} \text{[Magenta diagonal lines image]} \\ \rightarrow 2\,651\,048\,833 \end{array} \right\} \rightarrow \{4 \rightarrow 8.69455 \times 10^{-12}, 2 \rightarrow 1.\},$$

$$\left\{ \begin{array}{c} \text{[Magenta diagonal lines image]} \\ \rightarrow 2\,132\,867\,963 \end{array} \right\} \rightarrow \{4 \rightarrow 2.86202 \times 10^{-17}, 2 \rightarrow 1.\},$$

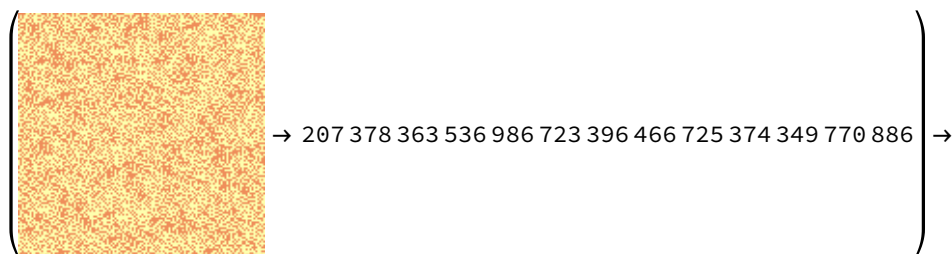
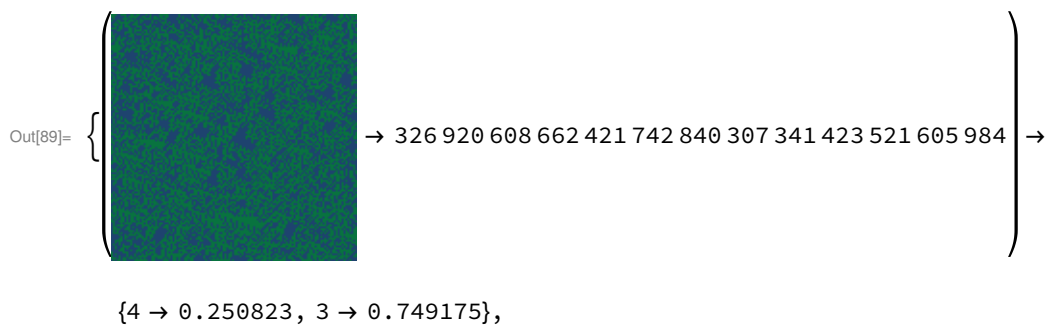
$$\left\{ \begin{array}{c} \text{[Brown noisy image]} \\ \rightarrow 3\,644\,758\,968 \end{array} \right\} \rightarrow \{4 \rightarrow 6.11899 \times 10^{-7}, 3 \rightarrow 0.999999\},$$

$$\left\{ \begin{array}{c} \text{[Blue and green diagonal lines image]} \\ \rightarrow 1\,762\,420\,096 \end{array} \right\} \rightarrow \{1 \rightarrow 2.34707 \times 10^{-9}, 2 \rightarrow 1.\},$$

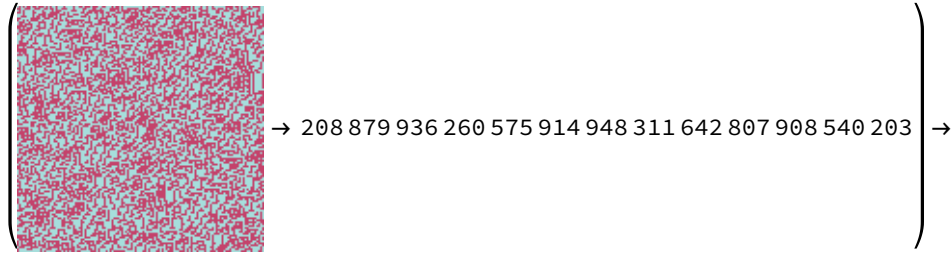


2-colour non-totalistic, range 3

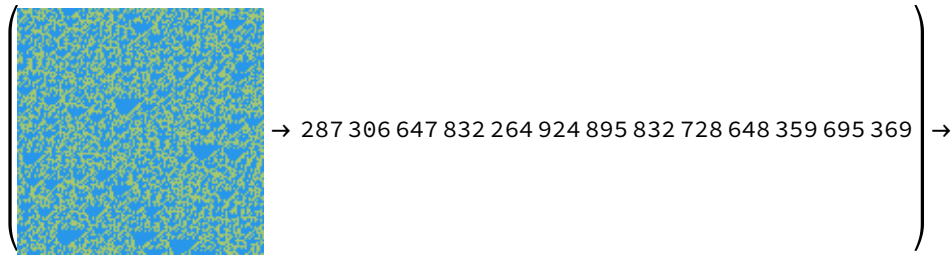
```
In[88]:= test4Data2kr3C16 = datak2r3NT[128, 128, 8];
Thread[test4Data2kr3C16 → netECA16[Keys@test4Data2kr3C16, {"TopProbabilities", 2}]]
```



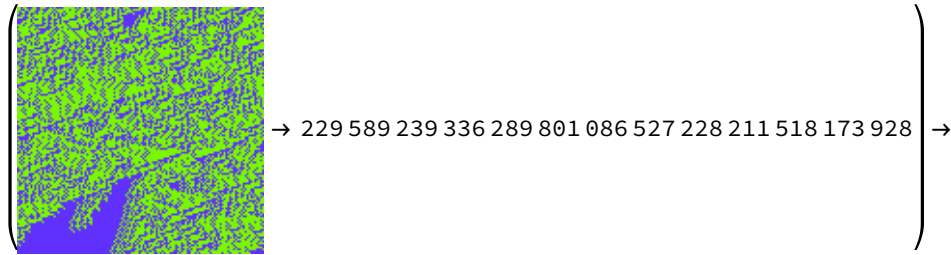
$$\{4 \rightarrow 3.99297 \times 10^{-14}, 3 \rightarrow 1.\},$$



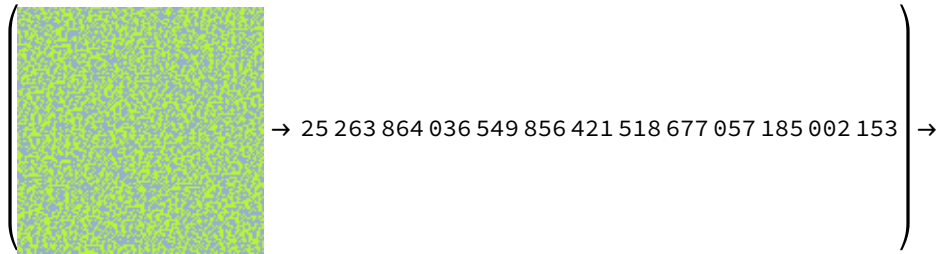
$$\{4 \rightarrow 1.58015 \times 10^{-11}, 3 \rightarrow 1.\},$$



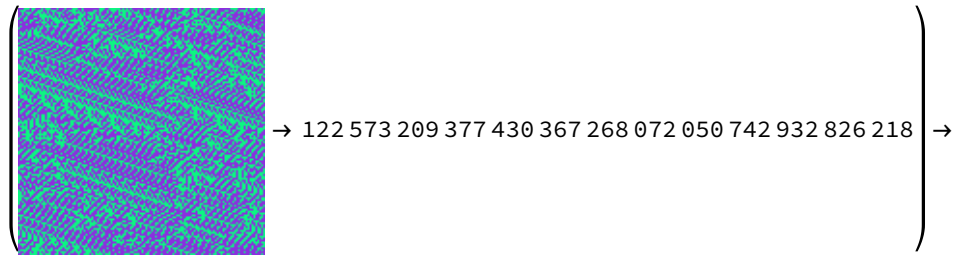
$$\{4 \rightarrow 1.21845 \times 10^{-8}, 3 \rightarrow 1.\},$$



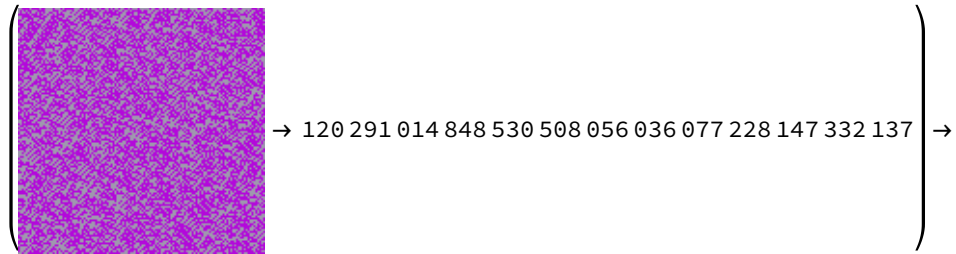
$$\{3 \rightarrow 0.0173989, 4 \rightarrow 0.982601\},$$



$$\{4 \rightarrow 2.486 \times 10^{-11}, 3 \rightarrow 1.\},$$



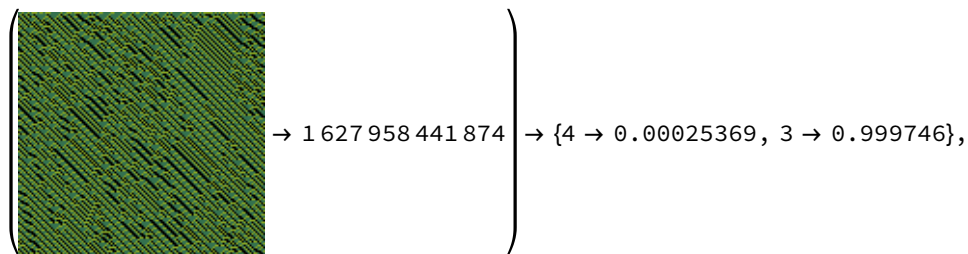
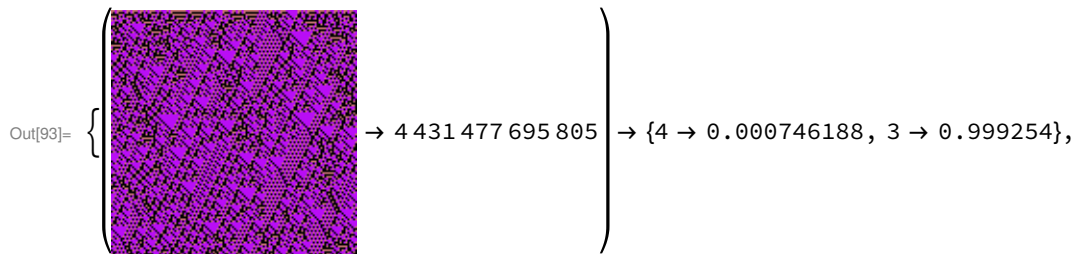
$\{4 \rightarrow 1.46881 \times 10^{-9}, 3 \rightarrow 1.\},$



$\{4 \rightarrow 0.00683298, 3 \rightarrow 0.993167\}$

3-colour non-totalistic, range 1

```
In[92]:= test4Data3kr1C16 = datak3r1NT[128, 128, 8];
Thread[test4Data3kr1C16 → netECA16[Keys@test4Data3kr1C16, {"TopProbabilities", 2}]]
```



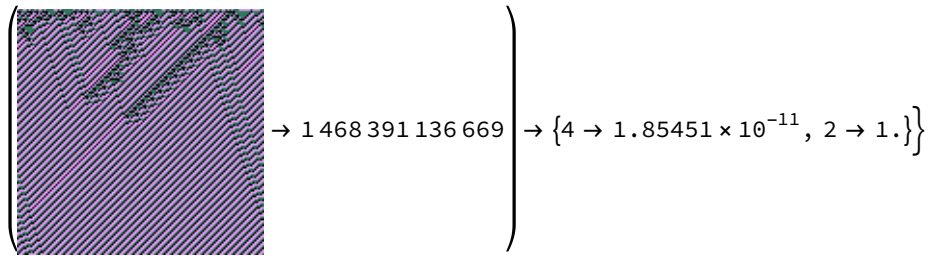
$$\left(\begin{array}{c} \text{Image 1: A square image with a complex, diagonal, wavy pattern of red, blue, and black lines.} \\ \rightarrow 4\,241\,674\,451\,024 \end{array} \right) \rightarrow \{3 \rightarrow 0.194892, 2 \rightarrow 0.805108\},$$

$$\left(\begin{array}{c} \text{Image 2: A square image with a noisy, pixelated pattern of yellow, green, and black.} \\ \rightarrow 4\,177\,916\,755\,057 \end{array} \right) \rightarrow \{3 \rightarrow 9.07174 \times 10^{-18}, 4 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image 3: A square image with a solid green background and several vertical black lines.} \\ \rightarrow 2\,504\,235\,138\,103 \end{array} \right) \rightarrow \{4 \rightarrow 1.3375 \times 10^{-21}, 2 \rightarrow 1.\},$$

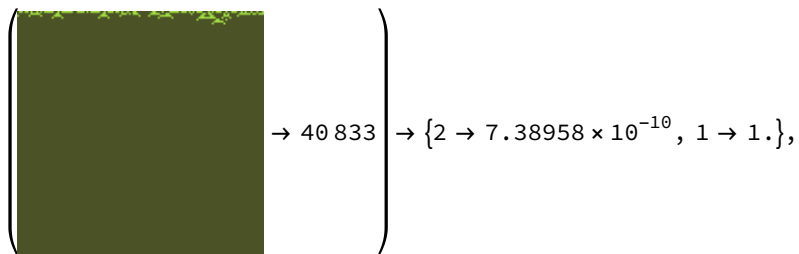
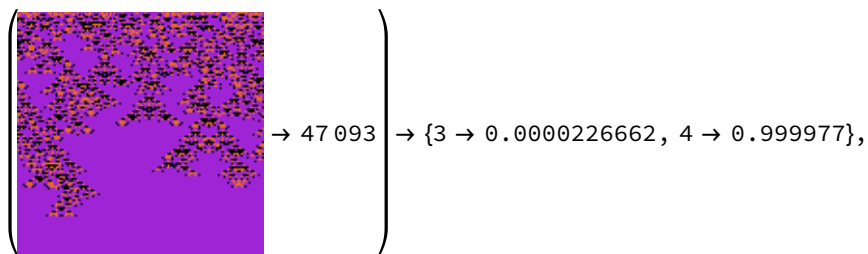
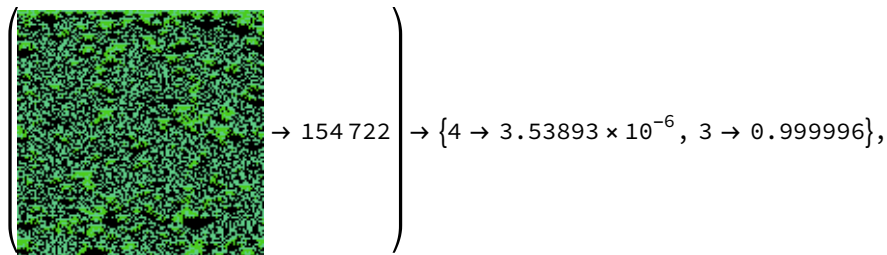
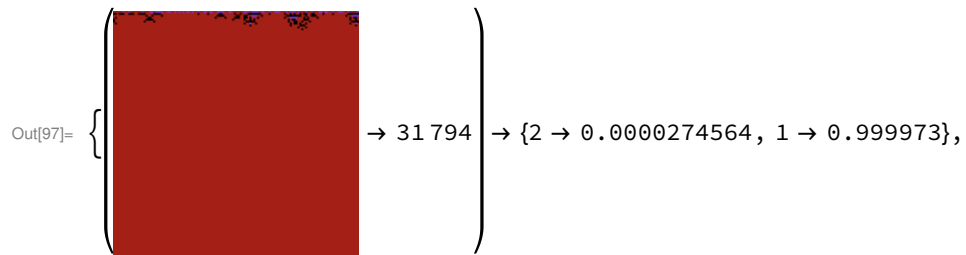
$$\left(\begin{array}{c} \text{Image 4: A square image with a noisy, pixelated pattern of red, green, and black.} \\ \rightarrow 2\,281\,646\,033\,785 \end{array} \right) \rightarrow \{4 \rightarrow 0.164883, 3 \rightarrow 0.835117\},$$

$$\left(\begin{array}{c} \text{Image 5: A square image with a solid cyan background and a vertical black line.} \\ \rightarrow 886\,946\,817\,375 \end{array} \right) \rightarrow \{2 \rightarrow 0.000352038, 1 \rightarrow 0.999648\},$$



3-colour totalistic, range 2

```
In[96]:= test4Data3kr2C16 = datak3r2C[128, 128, 8];
Thread[test4Data3kr2C16 → netECA16[Keys@test4Data3kr2C16, {"TopProbabilities", 2}]]
```



$$\left(\begin{array}{c} \text{Image} \\ \rightarrow 70\,499 \end{array} \right) \rightarrow \{4 \rightarrow 9.14168 \times 10^{-7}, 3 \rightarrow 0.999999\},$$

$$\left(\begin{array}{c} \text{Image} \\ \rightarrow 104\,031 \end{array} \right) \rightarrow \{2 \rightarrow 0.00469642, 1 \rightarrow 0.995304\},$$

$$\left(\begin{array}{c} \text{Image} \\ \rightarrow 102\,416 \end{array} \right) \rightarrow \{4 \rightarrow 0.00127827, 3 \rightarrow 0.998722\},$$

$$\left(\begin{array}{c} \text{Image} \\ \rightarrow 143\,812 \end{array} \right) \rightarrow \{3 \rightarrow 0.00152229, 4 \rightarrow 0.998478\}$$

3-colour totalistic, range 3

```
In[102]:= test4Data3kr3C16 = datak3r3C[128, 128, 8];
Thread[test4Data3kr3C16 → netECA16[Keys@test4Data3kr3C16, {"TopProbabilities", 2}]]
```

$$\text{Out[103]=} \left\{ \begin{array}{c} \text{Image} \\ \rightarrow 9\,694\,493 \end{array} \right\} \rightarrow \{3 \rightarrow 0.480724, 4 \rightarrow 0.519276\},$$

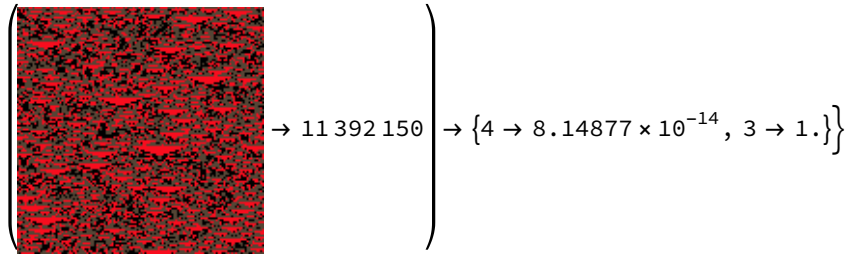
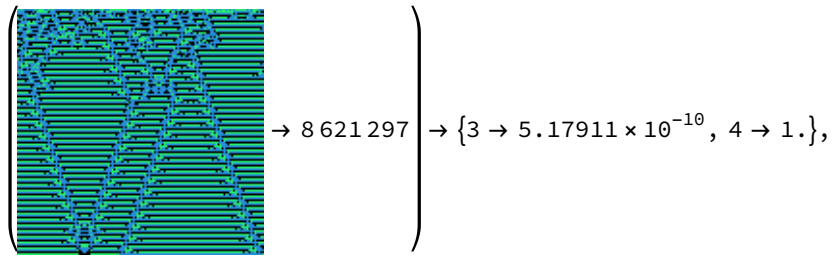
$$\left(\begin{array}{c} \text{Image 1} \\ \rightarrow 1\,266\,350 \end{array} \right) \rightarrow \{3 \rightarrow 2.07073 \times 10^{-17}, 4 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image 2} \\ \rightarrow 10\,922\,251 \end{array} \right) \rightarrow \{4 \rightarrow 0.0000302967, 3 \rightarrow 0.99997\},$$

$$\left(\begin{array}{c} \text{Image 3} \\ \rightarrow 10\,284\,081 \end{array} \right) \rightarrow \{4 \rightarrow 0.0000121386, 3 \rightarrow 0.999988\},$$

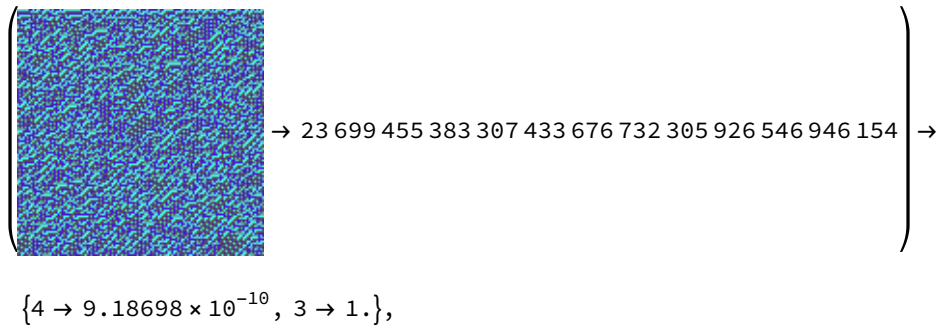
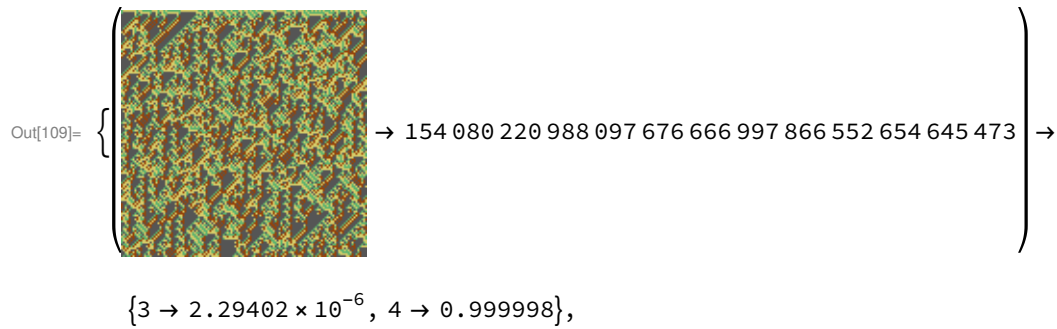
$$\left(\begin{array}{c} \text{Image 4} \\ \rightarrow 3\,664\,255 \end{array} \right) \rightarrow \{1 \rightarrow 0.0137727, 2 \rightarrow 0.986227\},$$

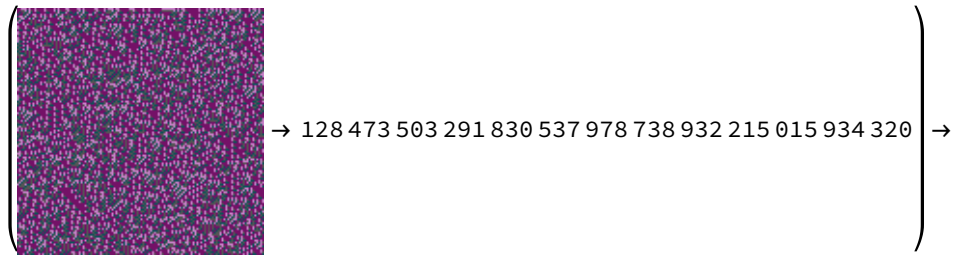
$$\left(\begin{array}{c} \text{Image 5} \\ \rightarrow 10\,298\,881 \end{array} \right) \rightarrow \{4 \rightarrow 0.000133186, 3 \rightarrow 0.999867\},$$



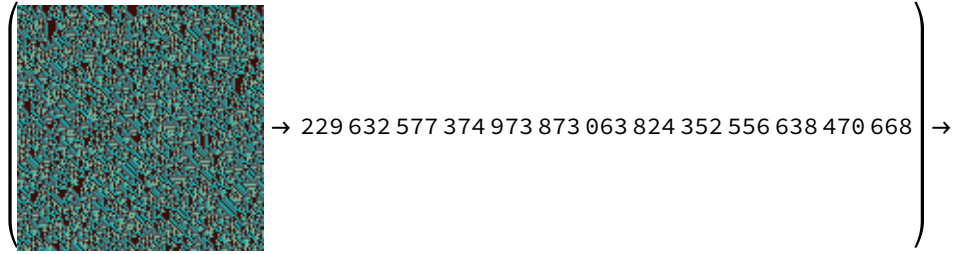
4-colour non-totalistic, range 1

```
In[108]:= test4Data4kr1C16 = datak4r1NT[128, 128, 8];
Thread[test4Data4kr1C16 → netECA16[Keys@test4Data4kr1C16, {"TopProbabilities", 2}]]
```

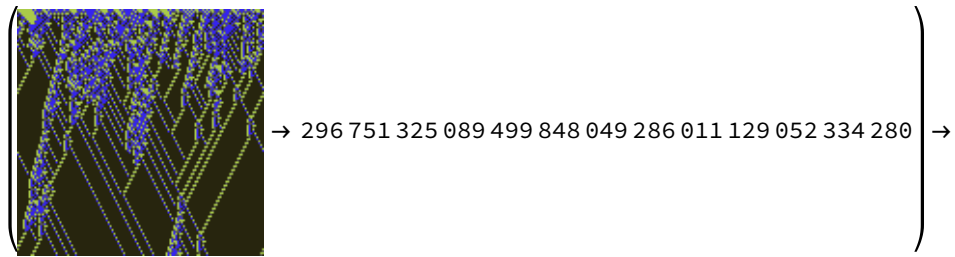




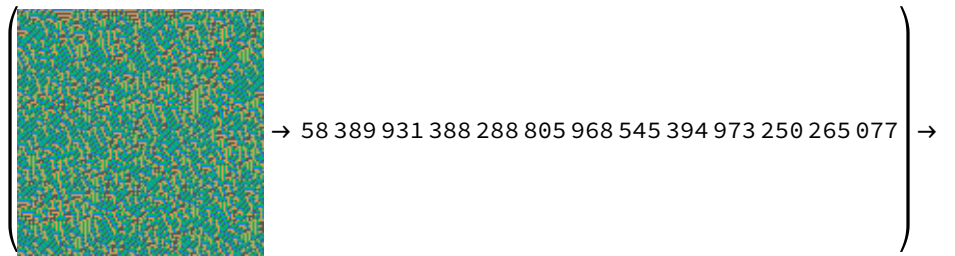
{4 → 0.016884, 3 → 0.983116},



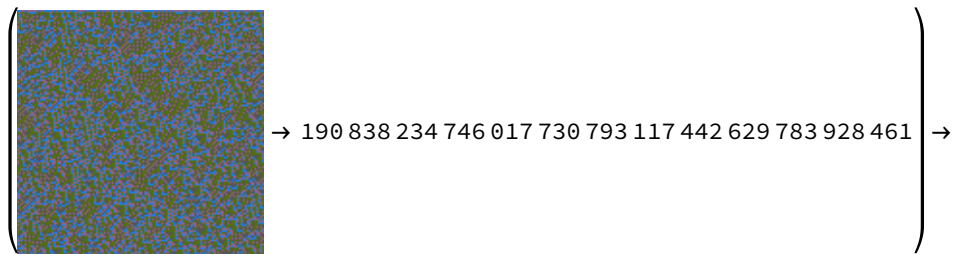
{3 → 3.66751×10^{-6} , 4 → 0.999996},



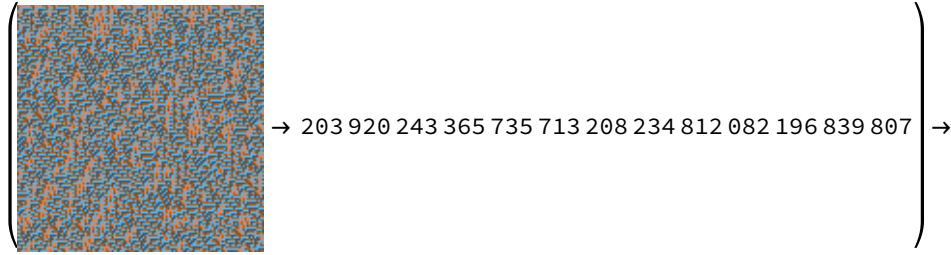
{2 → 0.0356663, 4 → 0.964334},



{4 → 0.392533, 3 → 0.607467},



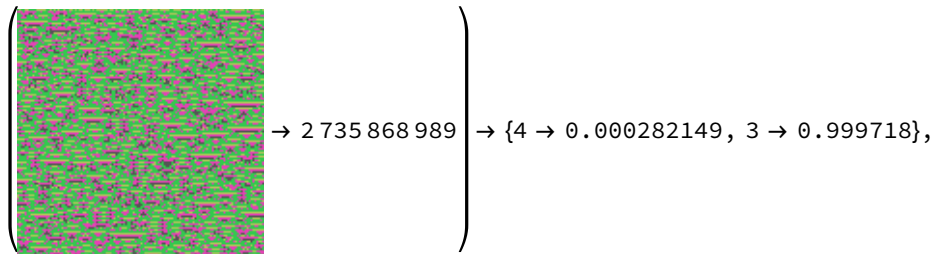
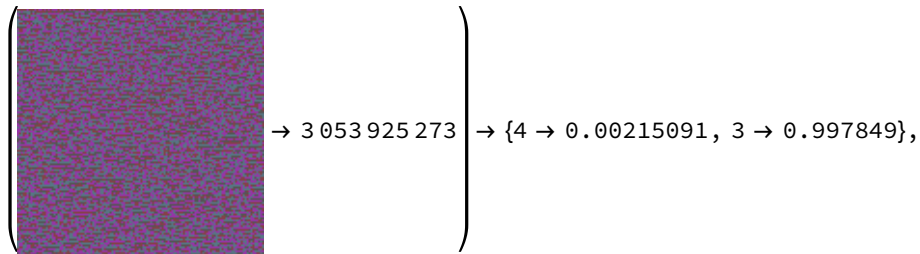
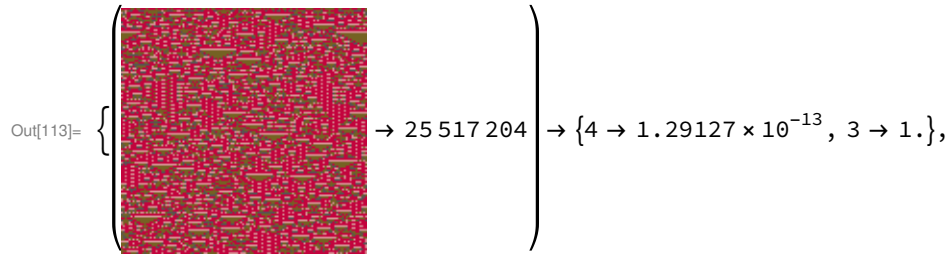
$\{3 \rightarrow 0.0000369307, 4 \rightarrow 0.999963\},$



$\{4 \rightarrow 0.00577653, 3 \rightarrow 0.994223\}$

4-colour totalistic, range 2

```
In[112]:= test4Data4kr2C16 = datak4r2C[128, 128, 8];
Thread[test4Data4kr2C16 → netECA16[Keys@test4Data4kr2C16, {"TopProbabilities", 2}]]
```



$$\left(\begin{array}{c} \text{Image} \\ \rightarrow 1\,440\,927\,950 \end{array} \right) \rightarrow \{4 \rightarrow 0.0889018, 3 \rightarrow 0.911098\},$$

$$\left(\begin{array}{c} \text{Image} \\ \rightarrow 3\,727\,816\,705 \end{array} \right) \rightarrow \{3 \rightarrow 2.78599 \times 10^{-7}, 4 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image} \\ \rightarrow 818\,963\,457 \end{array} \right) \rightarrow \{4 \rightarrow 4.45422 \times 10^{-19}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image} \\ \rightarrow 3\,948\,742\,311 \end{array} \right) \rightarrow \{4 \rightarrow 2.06369 \times 10^{-10}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image} \\ \rightarrow 1\,159\,108\,912 \end{array} \right) \rightarrow \{4 \rightarrow 0.431018, 2 \rightarrow 0.568975\}$$

5-colour totalistic, range 1

```
In[116]:= test4Data5kr1C16 = data5T2C[8, 128, 128];
Thread[test4Data5kr1C16 → netECA16[Keys@test4Data5kr1C16, {"TopProbabilities", 2}]]
```

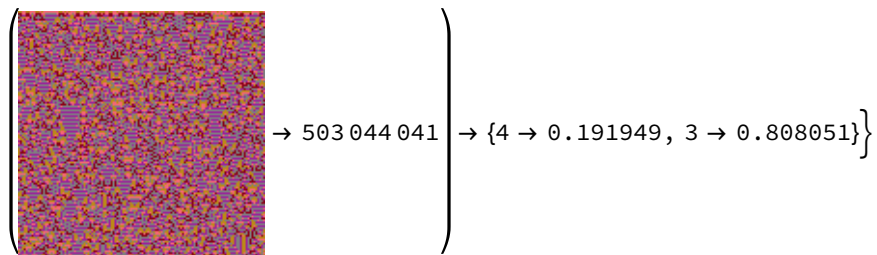
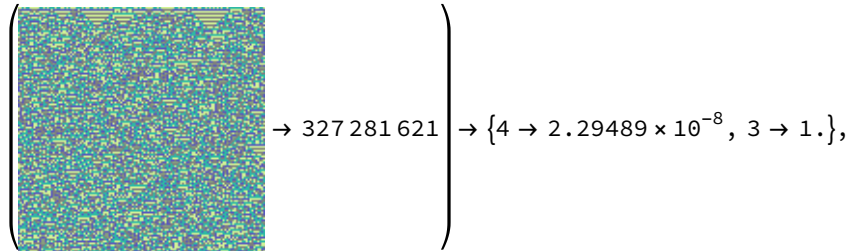
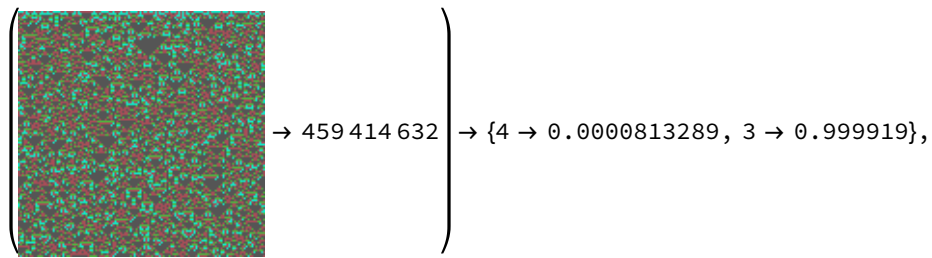

$$\text{Out}[117]= \left\{ \begin{array}{c} \left(\begin{array}{c} \text{Image} \end{array} \right) \rightarrow 81\,353\,109 \rightarrow \{4 \rightarrow 4.44391 \times 10^{-7}, 2 \rightarrow 1.\}, \end{array} \right.$$

$$\left(\begin{array}{c} \text{Image} \end{array} \right) \rightarrow 626\,536\,724 \rightarrow \{3 \rightarrow 3.46291 \times 10^{-8}, 4 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image} \end{array} \right) \rightarrow 129\,595\,314 \rightarrow \{4 \rightarrow 0.00257287, 3 \rightarrow 0.997427\},$$

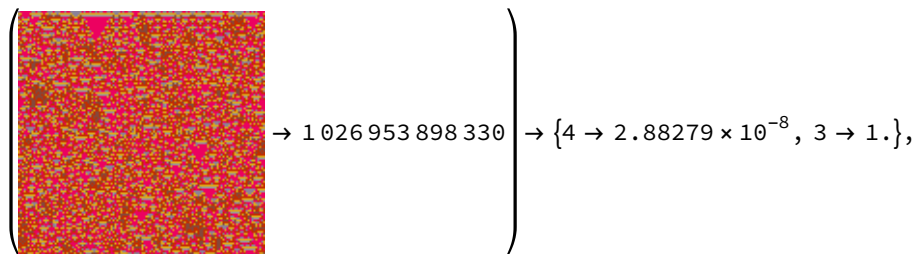
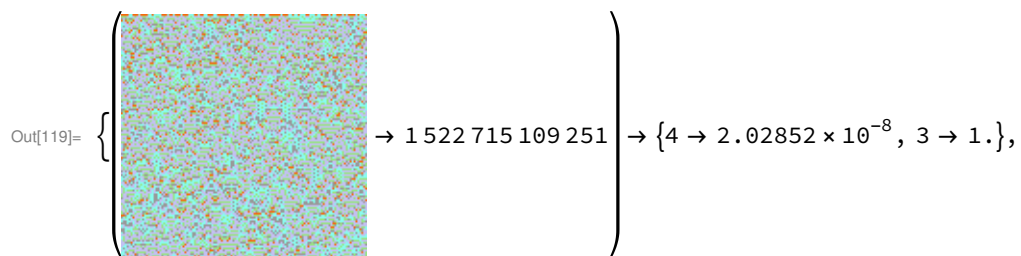
$$\left(\begin{array}{c} \text{Image} \end{array} \right) \rightarrow 513\,885\,470 \rightarrow \{1 \rightarrow 1.41572 \times 10^{-11}, 2 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image} \end{array} \right) \rightarrow 494\,894\,021 \rightarrow \{3 \rightarrow 0.0136503, 4 \rightarrow 0.98635\},$$



6-colour totalistic, range 1

```
In[118]:= test4Data6kr1C16 = data6TC[8, 128, 128];
Thread[test4Data6kr1C16 → netECA16[Keys@test4Data6kr1C16, {"TopProbabilities", 2}]]
```



$$\left(\begin{array}{c} \text{Image 1: Blue and red noise pattern} \\ \rightarrow 1\,583\,652\,682 \end{array} \right) \rightarrow \{3 \rightarrow 0.429972, 4 \rightarrow 0.570028\},$$

$$\left(\begin{array}{c} \text{Image 2: Purple and blue noise pattern} \\ \rightarrow 2\,123\,073\,201\,165 \end{array} \right) \rightarrow \{4 \rightarrow 6.23239 \times 10^{-10}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image 3: Green and yellow noise pattern} \\ \rightarrow 341\,591\,565\,791 \end{array} \right) \rightarrow \{4 \rightarrow 0.00212154, 3 \rightarrow 0.997878\},$$

$$\left(\begin{array}{c} \text{Image 4: Green and yellow noise pattern} \\ \rightarrow 2\,568\,539\,246\,083 \end{array} \right) \rightarrow \{4 \rightarrow 0.00197237, 3 \rightarrow 0.998028\},$$

$$\left(\begin{array}{c} \text{Image 5: Purple and green noise pattern} \\ \rightarrow 1\,213\,730\,554\,155 \end{array} \right) \rightarrow \{4 \rightarrow 0.0020281, 3 \rightarrow 0.997972\},$$

$$\left(\begin{array}{c} \text{[Random Noise Image]} \\ \rightarrow 389\,841\,312\,036 \end{array} \right) \rightarrow \{4 \rightarrow 2.91693 \times 10^{-11}, 3 \rightarrow 1.\}$$

6-colour totalistic, range 2

```
In[138]:= test4Data6kr2C16 = data6T2C[8, 128, 128];
Thread[test4Data6kr2C16 → netECA16[Keys@test4Data6kr2C16, {"TopProbabilities", 2}]]
```

$$\text{Out[139]=} \left\{ \begin{array}{c} \text{[Random Noise Image]} \\ \rightarrow 46\,177\,535\,535\,728\,053\,148 \end{array} \right\} \rightarrow \{4 \rightarrow 6.75757 \times 10^{-8}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[Random Noise Image]} \\ \rightarrow 35\,643\,164\,656\,729\,746\,413 \end{array} \right) \rightarrow \{4 \rightarrow 4.68349 \times 10^{-15}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[Random Noise Image]} \\ \rightarrow 151\,294\,335\,263\,255\,298\,785 \end{array} \right) \rightarrow \{4 \rightarrow 0.0673459, 3 \rightarrow 0.932654\},$$

$$\left(\begin{array}{c} \text{[Random Noise Image]} \\ \rightarrow 8\,803\,703\,818\,914\,948\,546 \end{array} \right) \rightarrow \{4 \rightarrow 0.00560205, 3 \rightarrow 0.994398\},$$

$$\left(\begin{array}{c} \text{[Image: Random noise pattern with purple, yellow, and red pixels]} \\ \rightarrow 46\,723\,275\,025\,483\,150\,950 \end{array} \right) \rightarrow \{4 \rightarrow 0.00307226, 3 \rightarrow 0.996928\},$$

$$\left(\begin{array}{c} \text{[Image: Random noise pattern with purple, blue, and red pixels]} \\ \rightarrow 72\,312\,079\,279\,485\,910\,528 \end{array} \right) \rightarrow \{4 \rightarrow 0.00153324, 3 \rightarrow 0.998467\},$$

$$\left(\begin{array}{c} \text{[Image: Random noise pattern with green, blue, and purple pixels]} \\ \rightarrow 22\,158\,237\,683\,799\,083\,047 \end{array} \right) \rightarrow \{4 \rightarrow 3.51784 \times 10^{-13}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[Image: Random noise pattern with green, blue, and yellow pixels]} \\ \rightarrow 142\,446\,781\,366\,136\,429\,283 \end{array} \right) \rightarrow \{4 \rightarrow 3.01302 \times 10^{-11}, 3 \rightarrow 1.\}$$

7-colour totalistic, range 1

```
In[154]:= test4Data7kr1C16 = data7TC[8, 128, 128];
Thread[test4Data7kr1C16 → netECA16[Keys@test4Data7kr1C16, {"TopProbabilities", 2}]]
```

$$\text{Out[155]=} \left\{ \begin{array}{c} \text{[Image: Patterned noise with pink, purple, and green pixels]} \\ \rightarrow 3\,109\,608\,593\,887\,262 \end{array} \right\} \rightarrow \{2 \rightarrow 0.0267983, 4 \rightarrow 0.973202\},$$

$$\left(\begin{array}{c} \text{Image 1} \end{array} \right) \rightarrow 10\,516\,337\,788\,191\,339 \rightarrow \{4 \rightarrow 0.202783, 3 \rightarrow 0.797217\},$$

$$\left(\begin{array}{c} \text{Image 2} \end{array} \right) \rightarrow 10\,218\,434\,972\,470\,056 \rightarrow \{4 \rightarrow 2.59313 \times 10^{-9}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image 3} \end{array} \right) \rightarrow 11\,301\,098\,979\,433\,534 \rightarrow \{4 \rightarrow 5.31247 \times 10^{-20}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image 4} \end{array} \right) \rightarrow 4\,222\,218\,586\,098\,008 \rightarrow \{4 \rightarrow 2.3505 \times 10^{-8}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image 5} \end{array} \right) \rightarrow 6\,272\,918\,110\,265\,620 \rightarrow \{4 \rightarrow 2.82334 \times 10^{-12}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[Image: Random noise pattern]} \\ \rightarrow 7\,237\,960\,144\,206\,103 \end{array} \right) \rightarrow \{4 \rightarrow 1.82804 \times 10^{-11}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[Image: Random noise pattern]} \\ \rightarrow 8\,157\,411\,943\,012\,914 \end{array} \right) \rightarrow \{4 \rightarrow 7.30163 \times 10^{-8}, 3 \rightarrow 1.\}$$

```
In[162]:= test4Data7kr1C16 = data7TC[8, 128, 128];
Thread[test4Data7kr1C16 → netECA16[Keys@test4Data7kr1C16, {"TopProbabilities", 2}]]
```

$$\text{Out[163]=} \left\{ \begin{array}{c} \text{[Image: Solid blue square]} \\ \rightarrow 2\,054\,187\,704\,193\,738 \end{array} \right\} \rightarrow \{2 \rightarrow 1.00393 \times 10^{-7}, 1 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[Image: Pattern with vertical lines and noise]} \\ \rightarrow 4\,502\,314\,670\,347\,259 \end{array} \right) \rightarrow \{1 \rightarrow 0.000272502, 2 \rightarrow 0.999727\},$$

$$\left(\begin{array}{c} \text{[Image: Random noise pattern]} \\ \rightarrow 6\,433\,286\,718\,439\,853 \end{array} \right) \rightarrow \{4 \rightarrow 3.57308 \times 10^{-13}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image 1: A noisy green and purple pattern} \end{array} \right) \rightarrow 10\,115\,271\,094\,201\,812 \rightarrow \{4 \rightarrow 1.83956 \times 10^{-14}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image 2: A green background with red and yellow vertical stripes} \end{array} \right) \rightarrow 2\,056\,629\,839\,849\,700 \rightarrow \{4 \rightarrow 7.03567 \times 10^{-6}, 2 \rightarrow 0.999993\},$$

$$\left(\begin{array}{c} \text{Image 3: A noisy purple and blue pattern} \end{array} \right) \rightarrow 6\,016\,684\,767\,156\,829 \rightarrow \{4 \rightarrow 0.0021258, 3 \rightarrow 0.997874\},$$

$$\left(\begin{array}{c} \text{Image 4: A noisy blue and green pattern} \end{array} \right) \rightarrow 1\,150\,898\,749\,617\,983 \rightarrow \{4 \rightarrow 5.05985 \times 10^{-9}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image 5: A purple background with blue diagonal stripes} \end{array} \right) \rightarrow 3\,441\,885\,208\,643\,463 \rightarrow \{3 \rightarrow 1.57168 \times 10^{-8}, 2 \rightarrow 1.\}$$

```
In[170]:= test4Data7kr1C16 = data7TC[8, 128, 128];
Thread[test4Data7kr1C16 → netECA16[Keys@test4Data7kr1C16, {"TopProbabilities", 2}]]
```

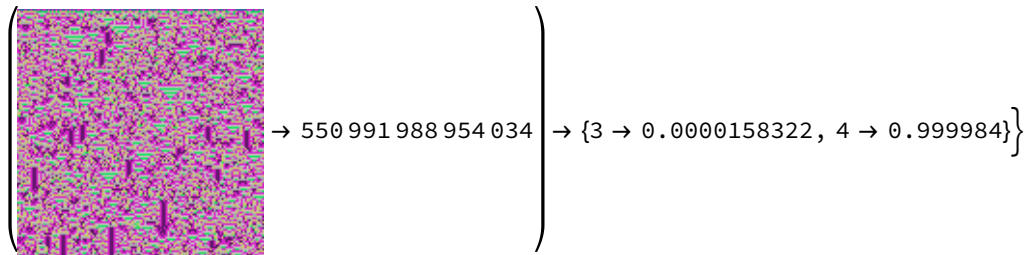
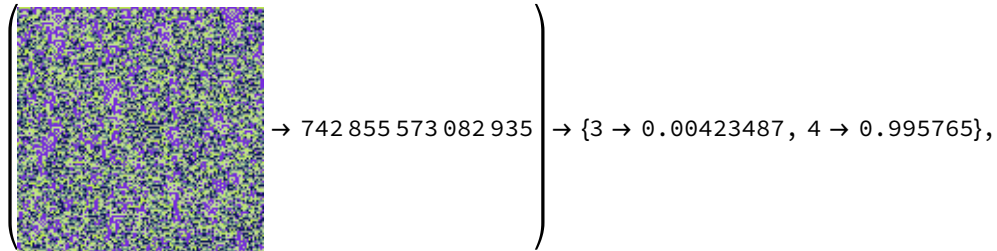
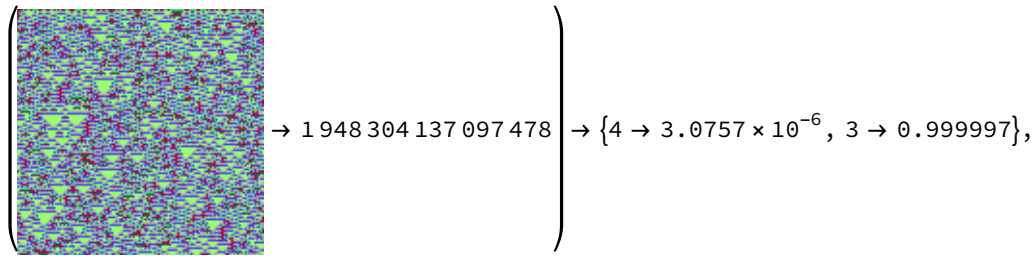
$$\text{Out}[171]= \left\{ \begin{array}{c} \text{Image} \\ \rightarrow 8\,718\,538\,805\,570\,808 \end{array} \right\} \rightarrow \{4 \rightarrow 0.0199047, 2 \rightarrow 0.980095\},$$

$$\left\{ \begin{array}{c} \text{Image} \\ \rightarrow 5\,687\,458\,247\,703\,346 \end{array} \right\} \rightarrow \{3 \rightarrow 3.931 \times 10^{-6}, 4 \rightarrow 0.999995\},$$

$$\left\{ \begin{array}{c} \text{Image} \\ \rightarrow 2\,004\,300\,484\,518\,722 \end{array} \right\} \rightarrow \{3 \rightarrow 0.0438658, 4 \rightarrow 0.956134\},$$

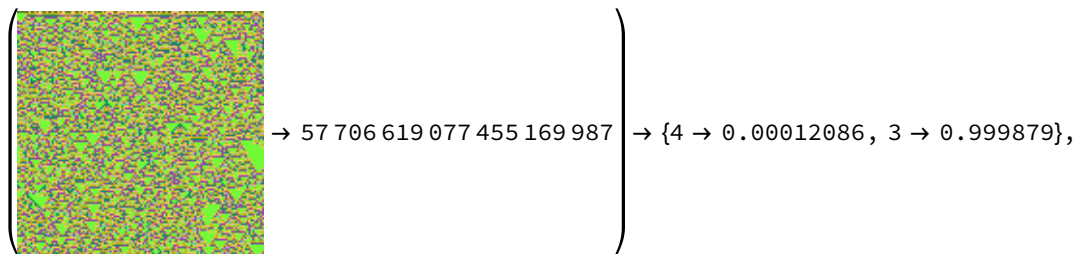
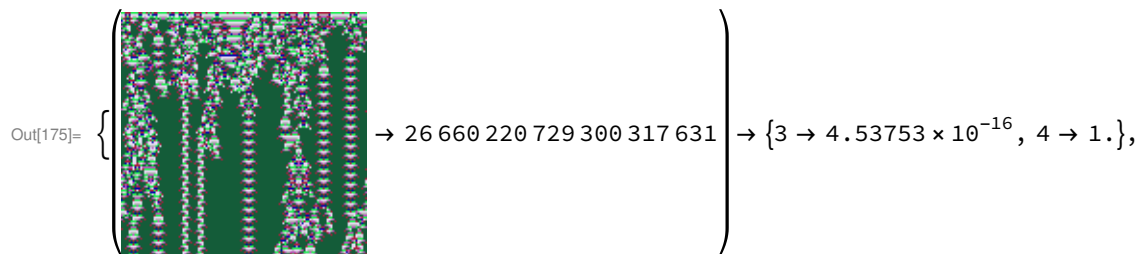
$$\left\{ \begin{array}{c} \text{Image} \\ \rightarrow 2\,106\,485\,862\,858\,275 \end{array} \right\} \rightarrow \{4 \rightarrow 3.36807 \times 10^{-10}, 3 \rightarrow 1.\},$$

$$\left\{ \begin{array}{c} \text{Image} \\ \rightarrow 10\,335\,102\,717\,390\,268 \end{array} \right\} \rightarrow \{4 \rightarrow 1.40275 \times 10^{-9}, 2 \rightarrow 1.\},$$



8-colour totalistic, range 1

```
In[174]:= test4Data8kr1C16 = data8TC[8, 128, 128];
Thread[test4Data8kr1C16 → netECA16[Keys@test4Data8kr1C16, {"TopProbabilities", 2}]]
```



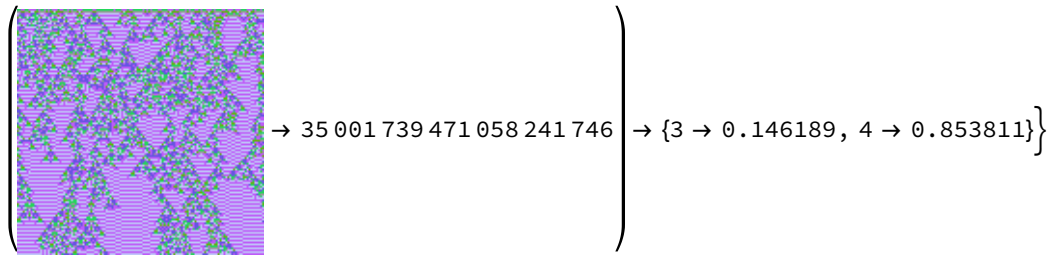
$$\left(\begin{array}{c} \text{Image 1: A noisy, abstract pattern with green, purple, and grey pixels.} \\ \rightarrow 64\,248\,301\,738\,433\,598\,883 \end{array} \right) \rightarrow \{4 \rightarrow 8.62498 \times 10^{-7}, 3 \rightarrow 0.999999\},$$

$$\left(\begin{array}{c} \text{Image 2: A noisy, abstract pattern with red, pink, and purple pixels.} \\ \rightarrow 38\,309\,191\,234\,358\,472\,181 \end{array} \right) \rightarrow \{3 \rightarrow 0.0920227, 4 \rightarrow 0.907977\},$$

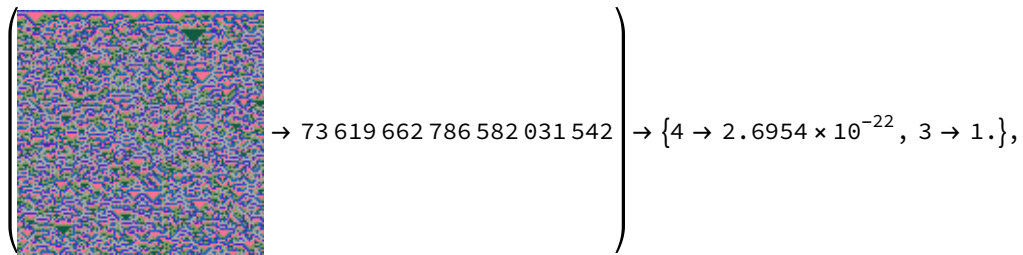
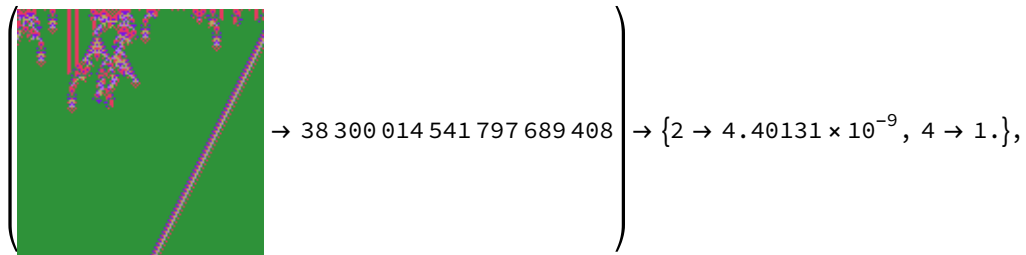
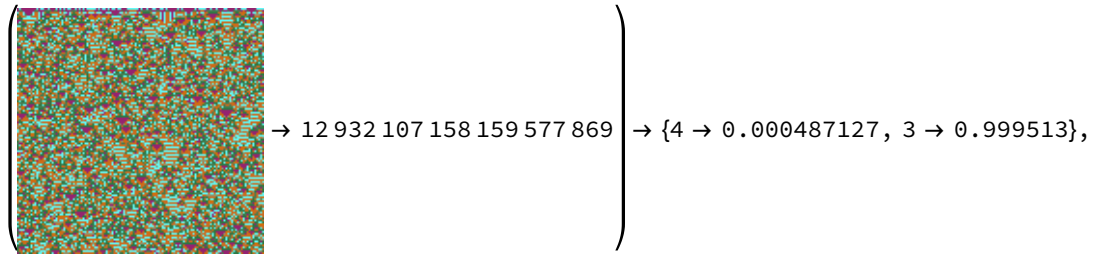
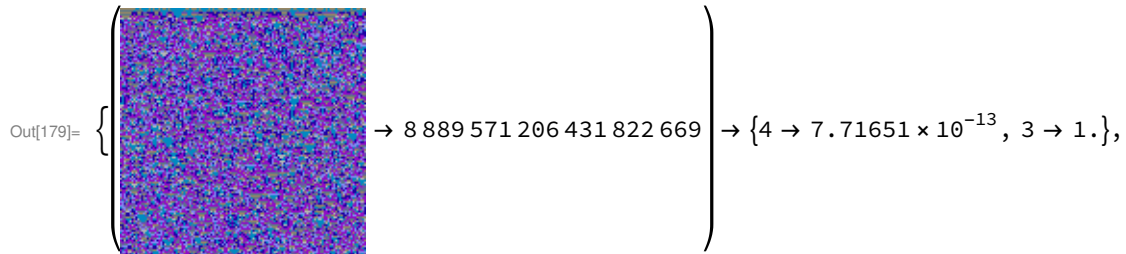
$$\left(\begin{array}{c} \text{Image 3: A noisy, abstract pattern with green, blue, and purple pixels.} \\ \rightarrow 10\,057\,418\,236\,647\,939\,786 \end{array} \right) \rightarrow \{3 \rightarrow 0.00153869, 4 \rightarrow 0.998461\},$$

$$\left(\begin{array}{c} \text{Image 4: A noisy, abstract pattern with blue, purple, and yellow pixels.} \\ \rightarrow 55\,038\,816\,396\,722\,824\,044 \end{array} \right) \rightarrow \{4 \rightarrow 7.93818 \times 10^{-11}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image 5: A noisy, abstract pattern with red, pink, and grey pixels.} \\ \rightarrow 13\,857\,790\,822\,319\,662\,750 \end{array} \right) \rightarrow \{4 \rightarrow 1.6375 \times 10^{-9}, 2 \rightarrow 1.\},$$



```
In[178]:= test4Data8kr1C16 = data8TC[8, 128, 128];
Thread[test4Data8kr1C16 → netECA16[Keys@test4Data8kr1C16, {"TopProbabilities", 2}]]
```



$$\left(\begin{array}{c} \text{[Image: A square image with a dense, noisy pattern of green and blue pixels.]}\end{array} \right) \rightarrow 25\,075\,664\,454\,379\,326\,631 \rightarrow \{4 \rightarrow 2.7484 \times 10^{-6}, 3 \rightarrow 0.999997\},$$

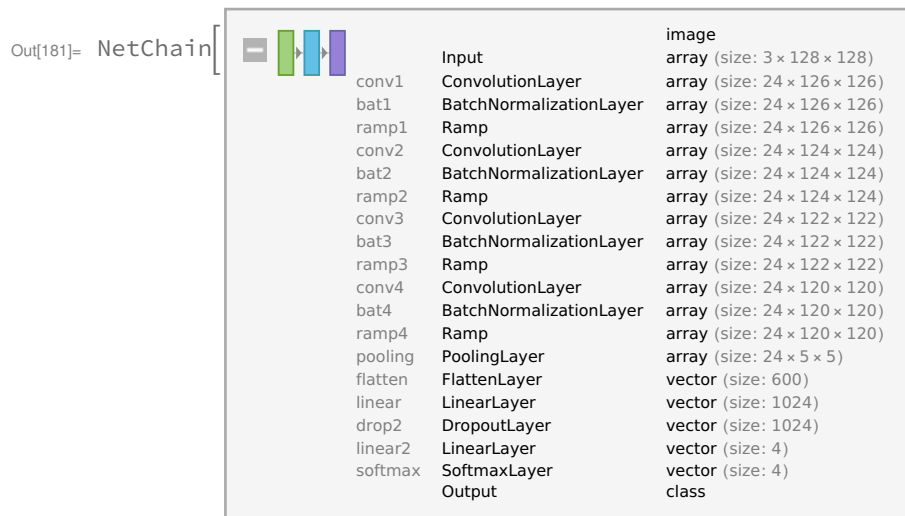
$$\left(\begin{array}{c} \text{[Image: A square image with a dense, noisy pattern of blue and purple pixels.]}\end{array} \right) \rightarrow 66\,251\,301\,754\,800\,867\,134 \rightarrow \{4 \rightarrow 0.045885, 3 \rightarrow 0.954115\},$$

$$\left(\begin{array}{c} \text{[Image: A square image with a dense, noisy pattern of pink and yellow pixels.]}\end{array} \right) \rightarrow 45\,939\,929\,171\,629\,412\,480 \rightarrow \{3 \rightarrow 0.0015837, 4 \rightarrow 0.998416\},$$

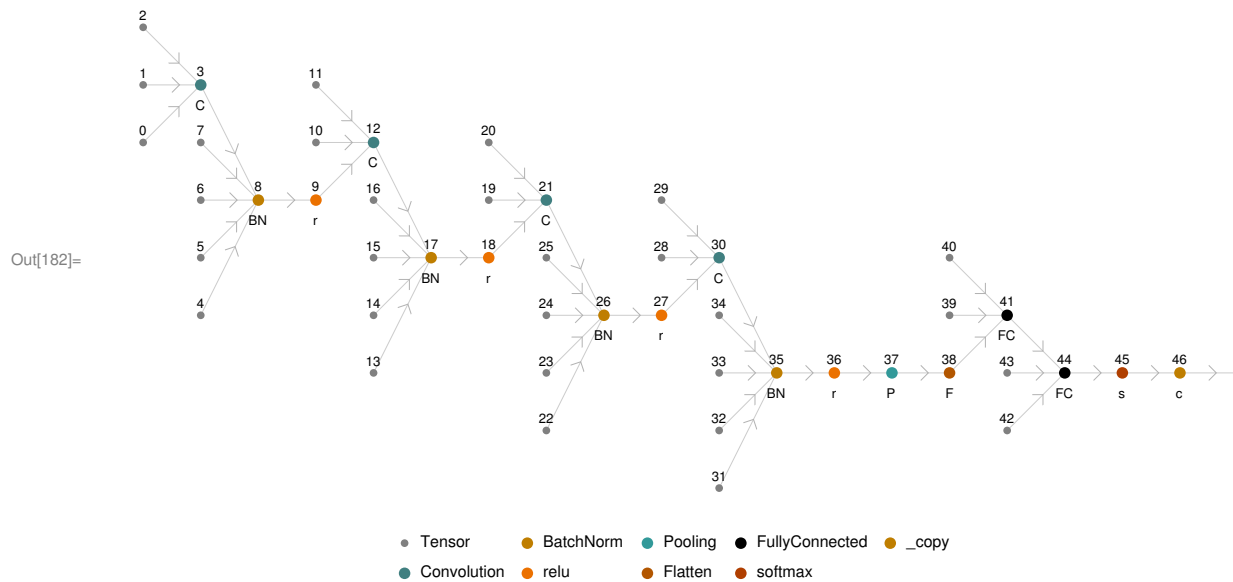
$$\left(\begin{array}{c} \text{[Image: A square image with a dense, noisy pattern of green and red pixels.]}\end{array} \right) \rightarrow 48\,918\,067\,825\,593\,479\,863 \rightarrow \{4 \rightarrow 0.000601606, 3 \rightarrow 0.999398\}$$

Network XVII - Four convolutions, dropout on linear only, BatchNorm

```
ln[181]:= netECA17 = netTenCC1024drop[128, 128]
```



In[182]:= NetInformation[netECA17, "MXNetNodeGraphPlot"]



In[183]:= NetInformation[netECA17, "SummaryGraphic"]



In[184]:= dataECA17 = dataC[128, 128, 16 384];

In[185]:= dataTotalistic2BigC17 = genData2r2C[128, 128, 2048];

In[186]:= dataTotalistic3BigC17 = data3T2C[128, 128, 2048];

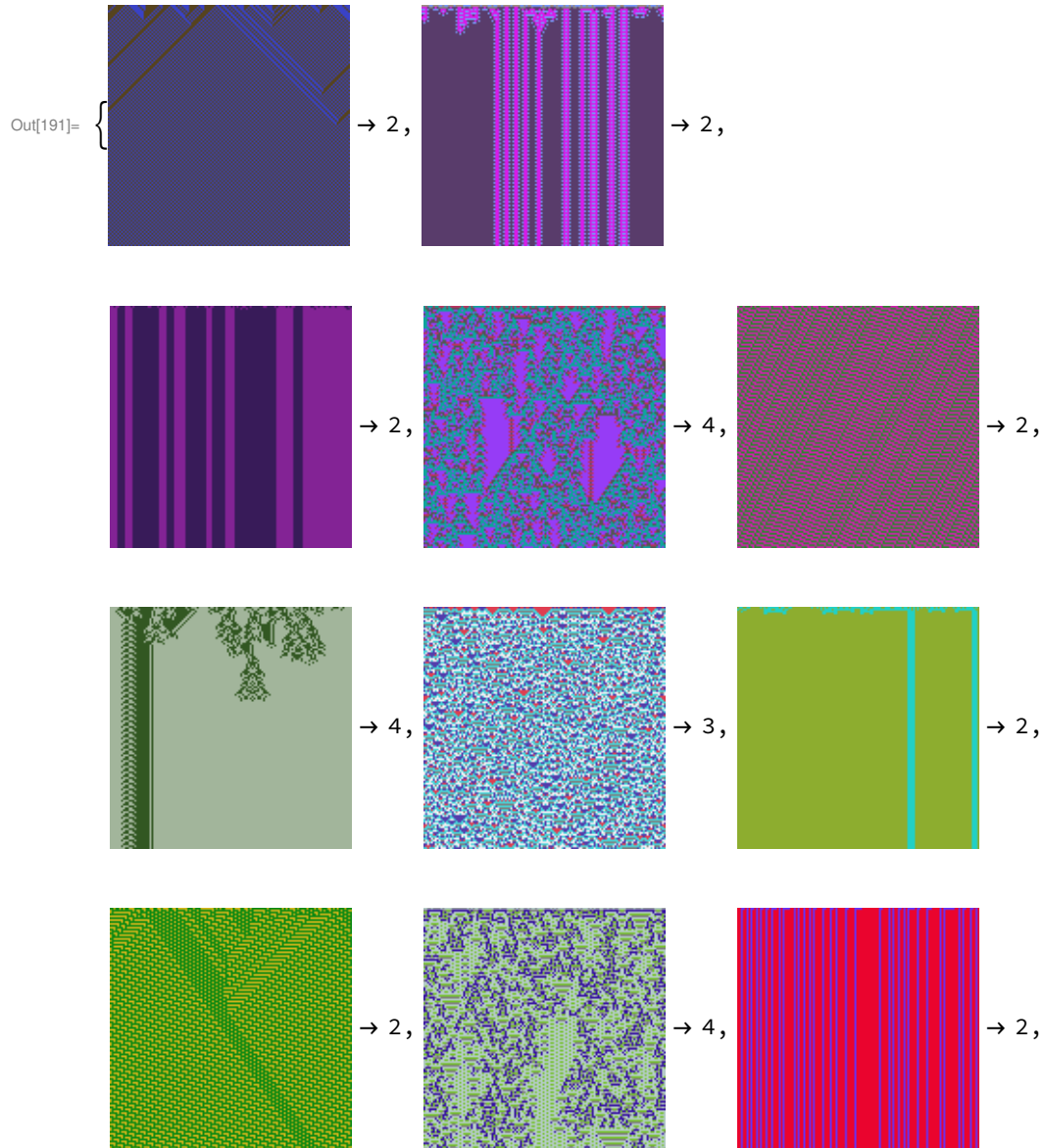
In[187]:= dataTotalistic4BigC17 = data4TC[128, 128, 2048];

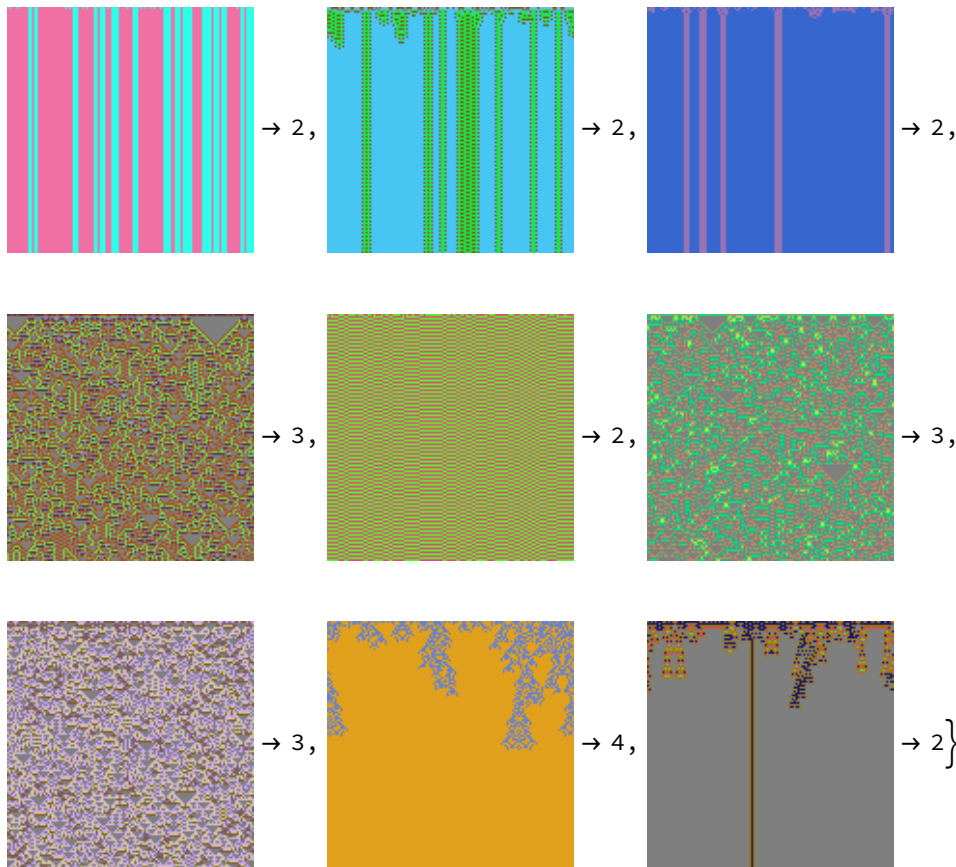
In[188]:= dataTotalistic5BigC17 = genData5TCC[128, 128, 8192];

```
In[189]:= fullTrainingBigC17 = Join[dataECA17, dataTotalistic2BigC17,
    dataTotalistic3BigC17, dataTotalistic4BigC17, dataTotalistic5BigC17];
Length[fullTrainingBigC17]
```

Out[190]= 53 248

```
In[191]:= RandomSample[fullTrainingBigC17, 20]
```





```
In[ ]:= dir = SetDirectory[NotebookDirectory[]]
```

```
In[192]:= "/home/esilverman/Documents"
```

```
Out[192]= /home/esilverman/Documents
```

```
In[193]:= netECA17 =
```

```
NetTrain[netECA17, fullTrainingBigC17, MaxTrainingRounds → 200, BatchSize → 256,  
TargetDevice → "GPU", TrainingProgressCheckpointing → {"Directory", dir}]
```

```
Out[193]= NetChain[  
  {  
    +,   
    →,   
    →,   
    Input port: image  
    Output port: class  
    Number of layers: 18  
  }  
]
```

```
netECA17 = Import["netECA17-r200.wlnet"]
```

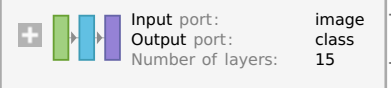
Generate test data for Network XVII (200 epochs)

```
In[ ]:= dir = SetDirectory[NotebookDirectory[]]
```

```
Out[ ]:= /Users/thorsilver/Downloads/Wolfram notebooks
```



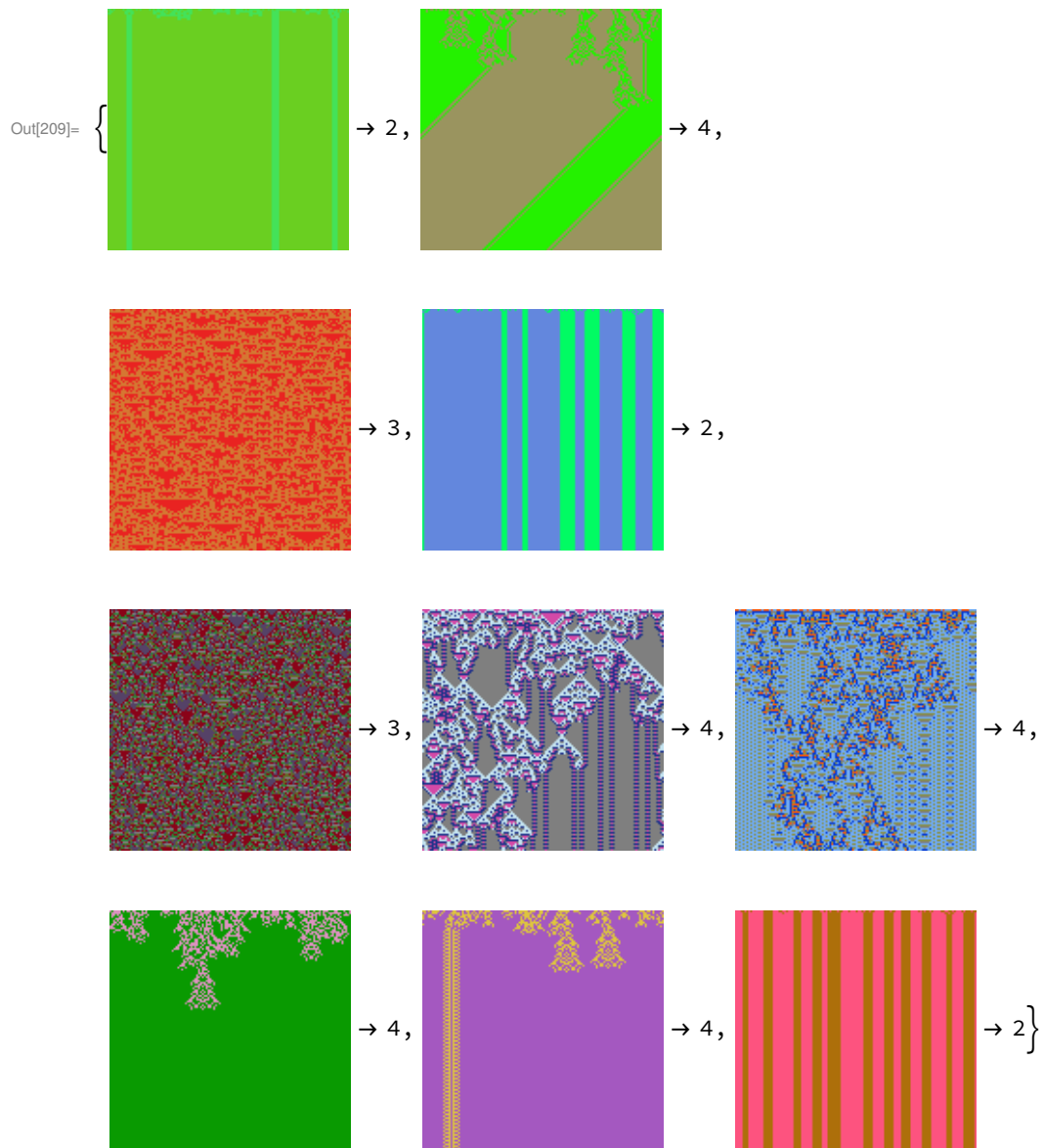
```
netECA17 = Import["netECA17-r200.wlnet"]
```

Out[] = J= NetChain[

```
In[202]:= testDataECABigC = dataC[128, 128, 1024];
testData2TBigC = genData2r2C[128, 128, 1024];
testData3TBigC = data3T2C[128, 128, 1024];
testData4TBigC = data4TC[128, 128, 1024];
testData5TBigC = genData5TCC[128, 128, 1024];
fullTestSetBigC = Join[testDataECABigC,
  testData2TBigC, testData3TBigC, testData4TBigC, testData5TBigC];
Length[fullTestSetBigC]
```

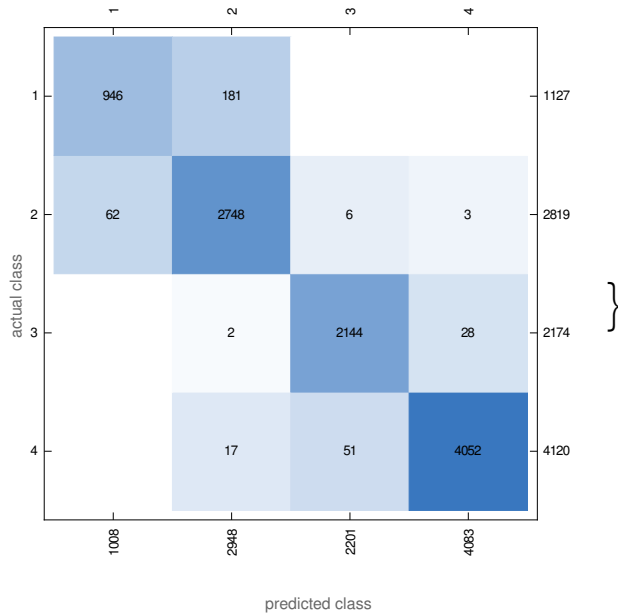
Out[208]= 10 240

In[209]:= RandomSample[fullTestSetBigC, 10]

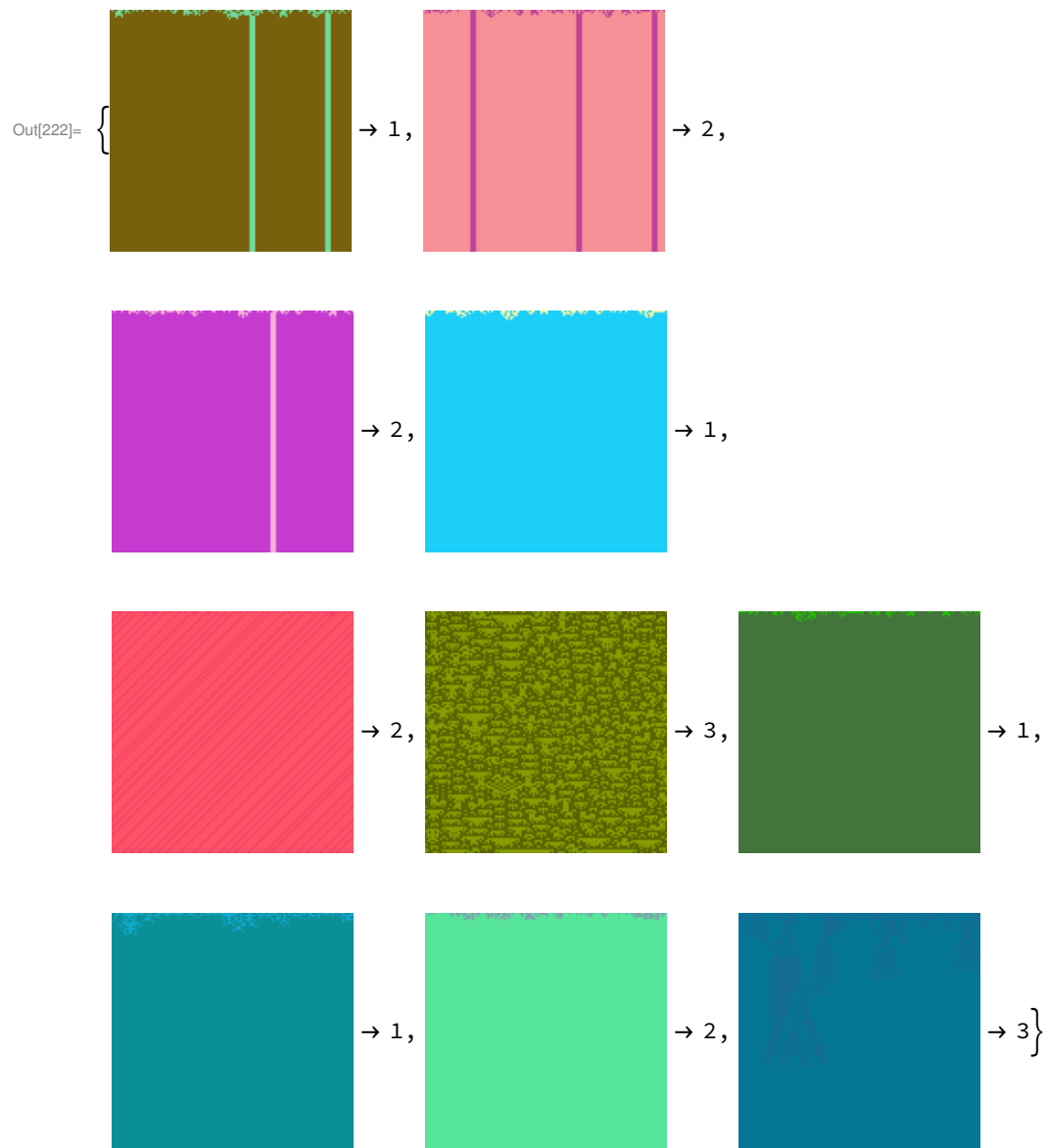


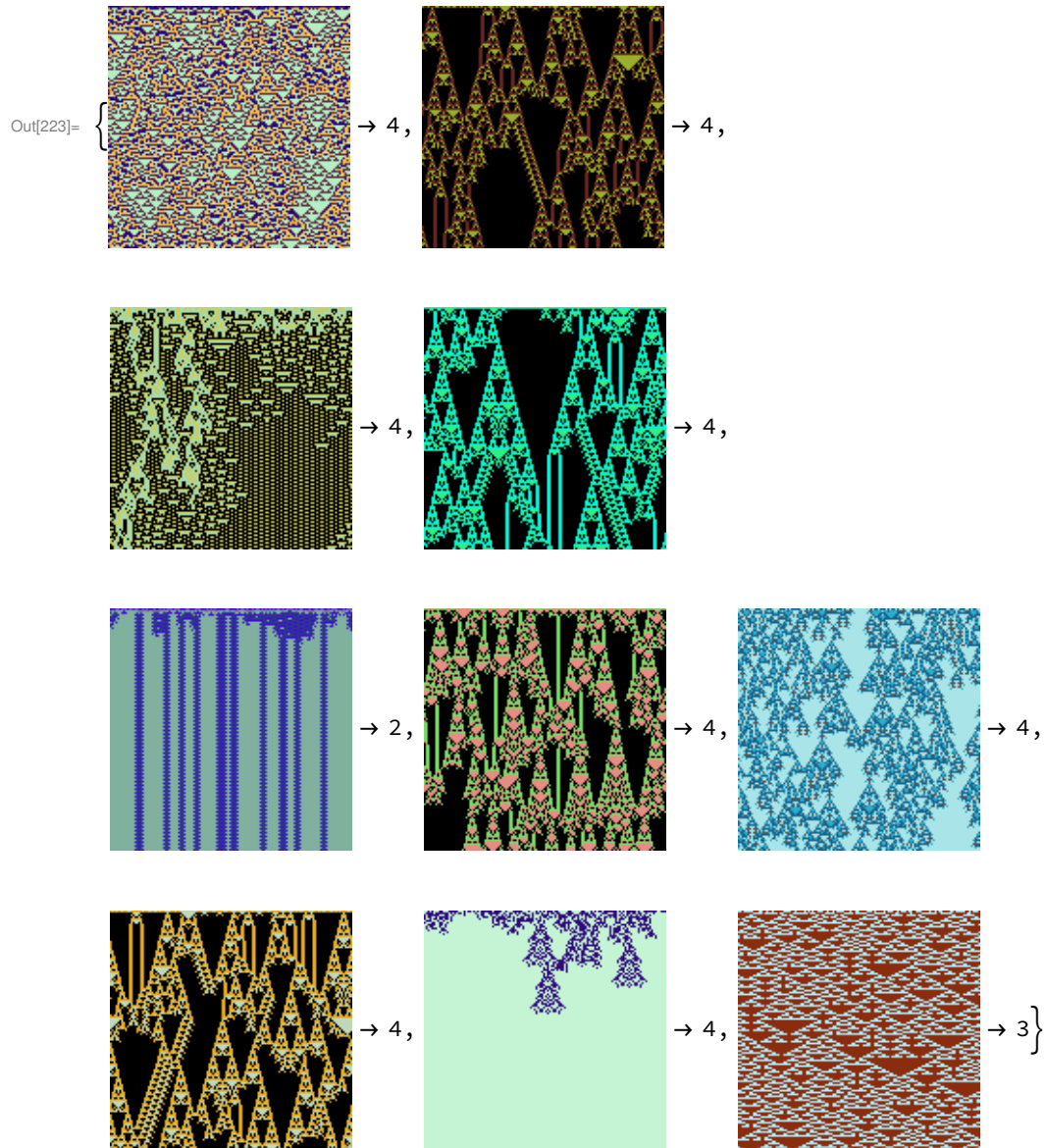

```
In[217]:= NetMeasurements[netECA17, fullTestSetBigC,
  {"Accuracy", "Precision", "ConfusionMatrixPlot"}]
```

```
Out[217]= {0.96582, <| 1 → 0.938492, 2 → 0.932157, 3 → 0.974103, 4 → 0.992408 |>,
```



```
In[218]:= entropyImagesBigC = RandomSample[Keys[fullTestSetBigC], 500];
entropiesBigC = netECA17[entropyImagesBigC, "Entropy"];
highEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, -10]]];
lowEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, 10]]];
Thread[highEntBigC → netECA17[highEntBigC]]
Thread[lowEntBigC → netECA17[lowEntBigC]]
```





Testing Network XVII (200 epochs) on unseen CA rule spaces

2-colour non-totalistic, range 2

```
In[224]:= test4Data2kr2C17 = datak2r2C[128, 128, 8];
Thread[test4Data2kr2C17 → netECA17[Keys@test4Data2kr2C17, {"TopProbabilities", 2}]]
```

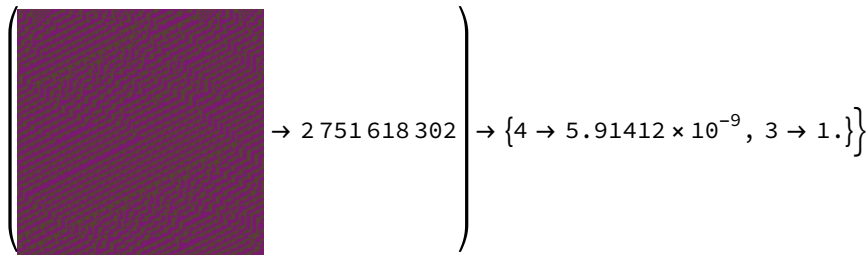
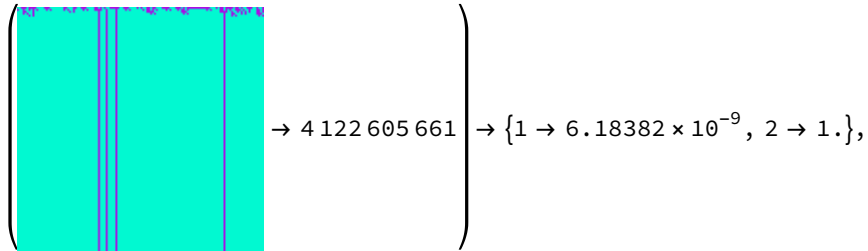
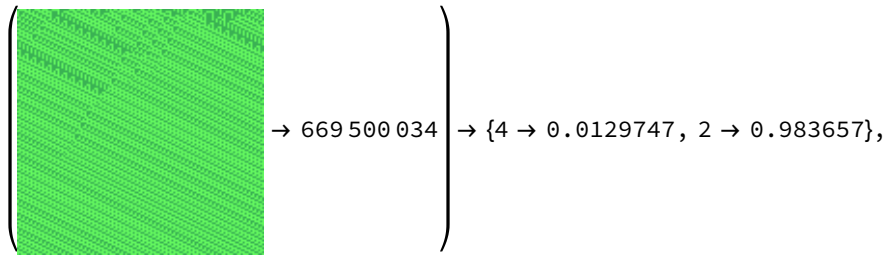
$$\text{Out}[225]= \left\{ \begin{array}{c} \left(\begin{array}{c} \text{[Orange Image]} \end{array} \right) \end{array} \right\} \rightarrow 3\,594\,886\,935 \rightarrow \{3 \rightarrow 1.19587 \times 10^{-7}, 2 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[Green/Yellow Image]} \end{array} \right) \rightarrow 4\,012\,014\,789 \rightarrow \{4 \rightarrow 0.00317589, 3 \rightarrow 0.996824\},$$

$$\left(\begin{array}{c} \text{[Purple Image]} \end{array} \right) \rightarrow 736\,342\,145 \rightarrow \{4 \rightarrow 0.000138652, 3 \rightarrow 0.999861\},$$

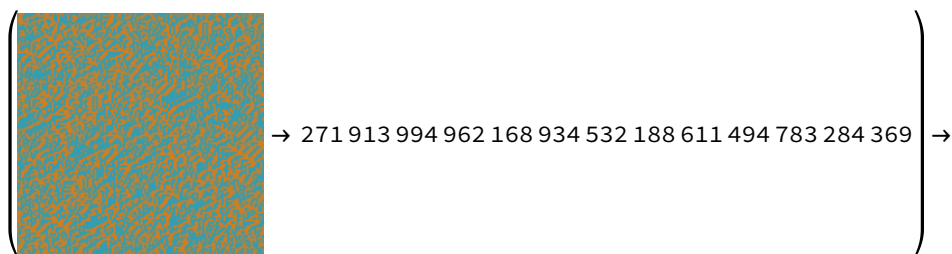
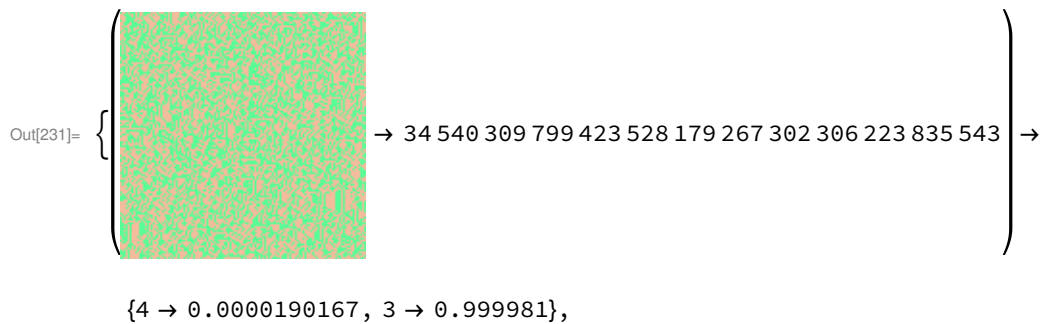
$$\left(\begin{array}{c} \text{[Yellow/Green Striped Image]} \end{array} \right) \rightarrow 3\,597\,938\,931 \rightarrow \{4 \rightarrow 5.42024 \times 10^{-16}, 2 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[Blue Striped Image]} \end{array} \right) \rightarrow 49\,406\,137 \rightarrow \{1 \rightarrow 4.03179 \times 10^{-30}, 2 \rightarrow 1.\},$$



2-colour non-totalistic, range 3

```
In[230]:= test4Data2kr3C17 = datak2r3NT[128, 128, 8];
Thread[test4Data2kr3C17 → netECA17[Keys@test4Data2kr3C17, {"TopProbabilities", 2}]]
```



$$\{4 \rightarrow 8.79258 \times 10^{-15}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image} \end{array} \right) \rightarrow 328\,899\,203\,265\,424\,040\,719\,063\,648\,351\,222\,904\,052 \rightarrow$$

$$\{3 \rightarrow 0.000609094, 4 \rightarrow 0.999391\},$$

$$\left(\begin{array}{c} \text{Image} \end{array} \right) \rightarrow 193\,952\,196\,319\,600\,964\,880\,345\,641\,761\,505\,849\,023 \rightarrow$$

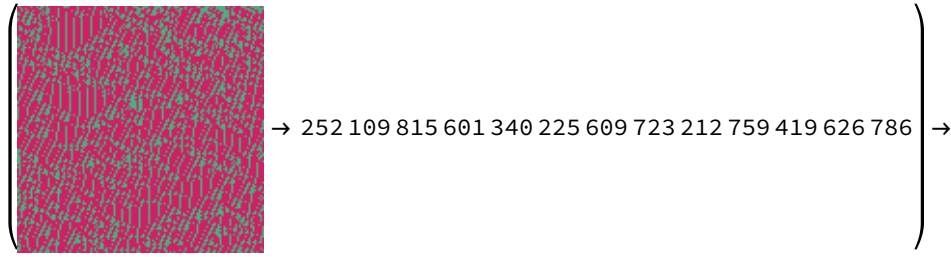
$$\{4 \rightarrow 8.96571 \times 10^{-10}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image} \end{array} \right) \rightarrow 196\,656\,308\,173\,162\,097\,107\,061\,836\,715\,379\,270\,739 \rightarrow$$

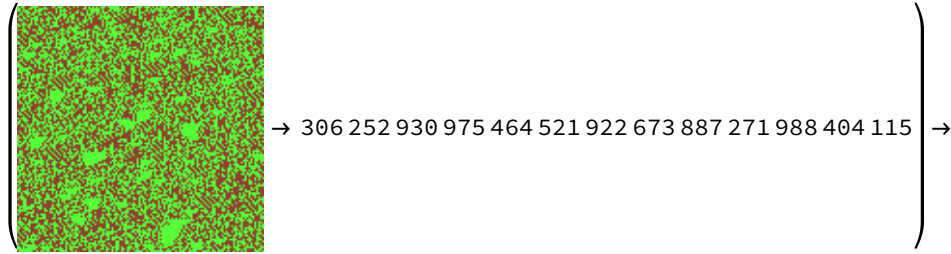
$$\{4 \rightarrow 3.36397 \times 10^{-6}, 3 \rightarrow 0.999997\},$$

$$\left(\begin{array}{c} \text{Image} \end{array} \right) \rightarrow 26\,038\,517\,878\,084\,050\,104\,120\,010\,197\,636\,533\,172 \rightarrow$$

$$\{3 \rightarrow 5.4757 \times 10^{-7}, 4 \rightarrow 0.999999\},$$



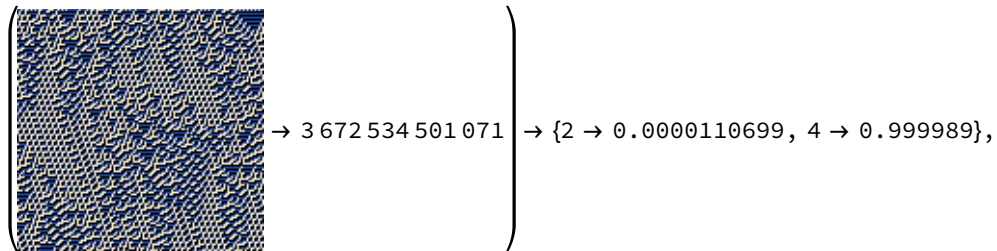
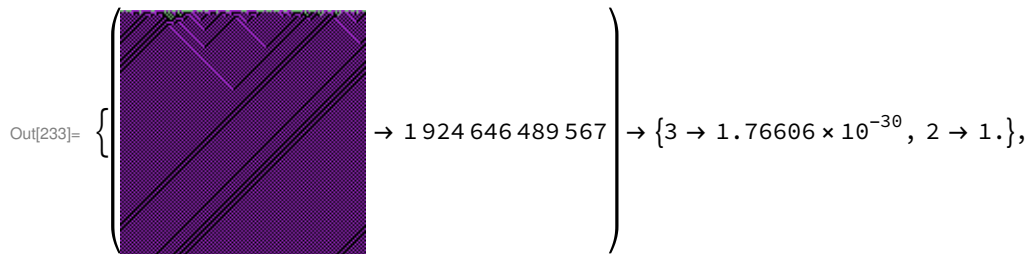
$\{4 \rightarrow 1.35911 \times 10^{-8}, 3 \rightarrow 1.\},$



$\{4 \rightarrow 5.68649 \times 10^{-7}, 3 \rightarrow 0.999999\}$

3-colour non-totalistic, range 1

```
In[232]:= test4Data3kr1C17 = datak3r1NT[128, 128, 8];
Thread[test4Data3kr1C17 → netECA17[Keys@test4Data3kr1C17, {"TopProbabilities", 2}]]
```



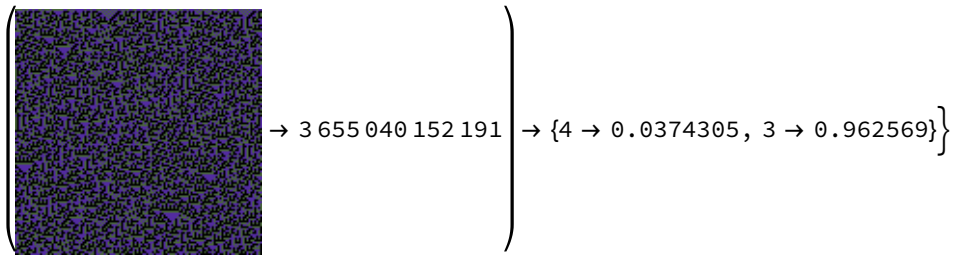
$$\left(\begin{array}{c} \text{Image 1: A square image with a complex, fractal-like pattern in shades of pink, red, and black.} \\ \rightarrow 5\,833\,330\,297\,781 \end{array} \right) \rightarrow \{2 \rightarrow 0.000232935, 4 \rightarrow 0.999767\},$$

$$\left(\begin{array}{c} \text{Image 2: A square image that is almost entirely black, with a thin horizontal band of yellow and green at the top.} \\ \rightarrow 7\,606\,192\,973\,798 \end{array} \right) \rightarrow \{2 \rightarrow 6.802 \times 10^{-10}, 1 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image 3: A square image with a dense, diagonal pattern of blue and orange lines.} \\ \rightarrow 7\,622\,301\,560\,954 \end{array} \right) \rightarrow \{3 \rightarrow 0.0391643, 2 \rightarrow 0.960836\},$$

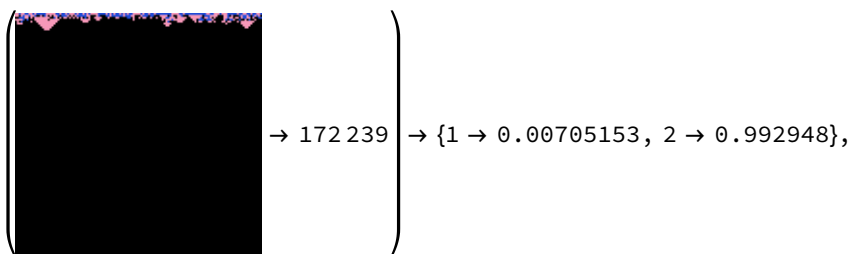
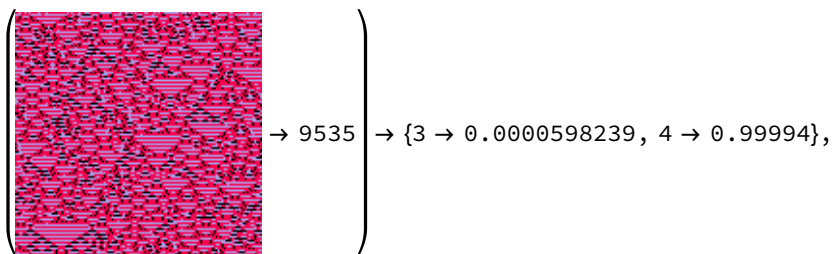
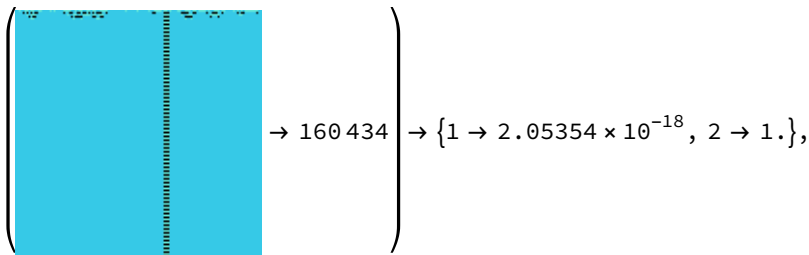
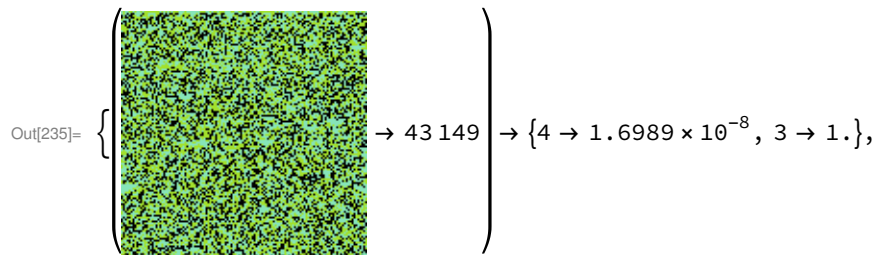
$$\left(\begin{array}{c} \text{Image 4: A square image with a dense, horizontal pattern of red and yellow lines.} \\ \rightarrow 3\,685\,910\,174\,297 \end{array} \right) \rightarrow \{3 \rightarrow 2.7602 \times 10^{-8}, 4 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image 5: A square image with a dense, wavy pattern of green and yellow lines.} \\ \rightarrow 5\,743\,838\,876\,456 \end{array} \right) \rightarrow \{1 \rightarrow 6.15406 \times 10^{-23}, 2 \rightarrow 1.\},$$



3-colour totalistic, range 2

```
In[234]:= test4Data3kr2C17 = datak3r2C[128, 128, 8];
Thread[test4Data3kr2C17 → netECA17[Keys@test4Data3kr2C17, {"TopProbabilities", 2}]]
```



$$\left(\begin{array}{c} \text{[Image: A dark, noisy image with a small light-colored shape at the top]} \\ \rightarrow 174\,680 \end{array} \right) \rightarrow \{2 \rightarrow 5.824 \times 10^{-11}, 1 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[Image: A noisy image with blue and white pixels]} \\ \rightarrow 55\,945 \end{array} \right) \rightarrow \{4 \rightarrow 0.0138349, 3 \rightarrow 0.986165\},$$

$$\left(\begin{array}{c} \text{[Image: A noisy image with blue and black pixels]} \\ \rightarrow 113\,483 \end{array} \right) \rightarrow \{4 \rightarrow 3.72822 \times 10^{-6}, 3 \rightarrow 0.999996\},$$

$$\left(\begin{array}{c} \text{[Image: A noisy image with green and black pixels]} \\ \rightarrow 67\,810 \end{array} \right) \rightarrow \{1 \rightarrow 6.91386 \times 10^{-17}, 2 \rightarrow 1.\}$$

3-colour totalistic, range 3

```
In[236]:= test4Data3kr3C17 = datak3r3C[128, 128, 8];
Thread[test4Data3kr3C17 → netECA17[Keys@test4Data3kr3C17, {"TopProbabilities", 2}]]
```

$$\text{Out[237]=} \left\{ \begin{array}{c} \text{[Image: A noisy image with green and black pixels]} \\ \rightarrow 3\,046\,610 \end{array} \right\} \rightarrow \{4 \rightarrow 7.58312 \times 10^{-7}, 3 \rightarrow 0.999999\},$$

$$\left(\begin{array}{c} \text{Image 1: Blue background with a vertical spiral pattern} \\ \rightarrow 7\,801\,434 \end{array} \right) \rightarrow \{1 \rightarrow 1.19167 \times 10^{-14}, 2 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image 2: Green and blue noisy pattern} \\ \rightarrow 5\,445\,843 \end{array} \right) \rightarrow \{4 \rightarrow 1.60992 \times 10^{-19}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image 3: Purple and black noisy pattern} \\ \rightarrow 1\,451\,413 \end{array} \right) \rightarrow \{4 \rightarrow 0.144413, 3 \rightarrow 0.855587\},$$

$$\left(\begin{array}{c} \text{Image 4: Green and black noisy pattern} \\ \rightarrow 10\,676\,790 \end{array} \right) \rightarrow \{3 \rightarrow 0.0738921, 4 \rightarrow 0.926108\},$$

$$\left(\begin{array}{c} \text{Image 5: Red and black noisy pattern} \\ \rightarrow 10\,375\,449 \end{array} \right) \rightarrow \{4 \rightarrow 1.04031 \times 10^{-17}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[Image: A 128x128 pixel image with a noisy, purple and black pattern]} \\ \rightarrow 5\,181\,761 \end{array} \right) \rightarrow \{4 \rightarrow 1.75908 \times 10^{-8}, 3 \rightarrow 1.\},$$

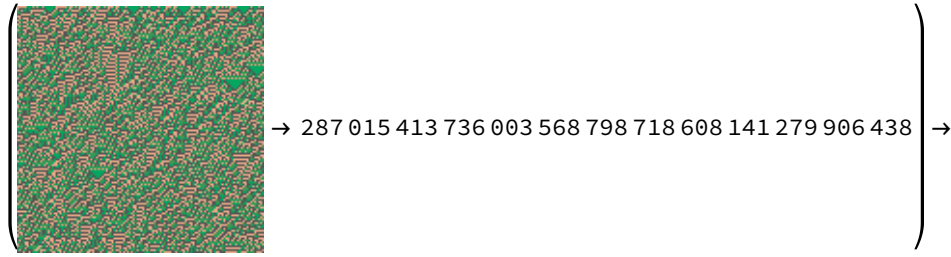
$$\left(\begin{array}{c} \text{[Image: A 128x128 pixel image with a noisy, orange and red pattern]} \\ \rightarrow 8\,884\,285 \end{array} \right) \rightarrow \{4 \rightarrow 7.91486 \times 10^{-6}, 3 \rightarrow 0.999992\}$$

4-colour non-totalistic, range 1

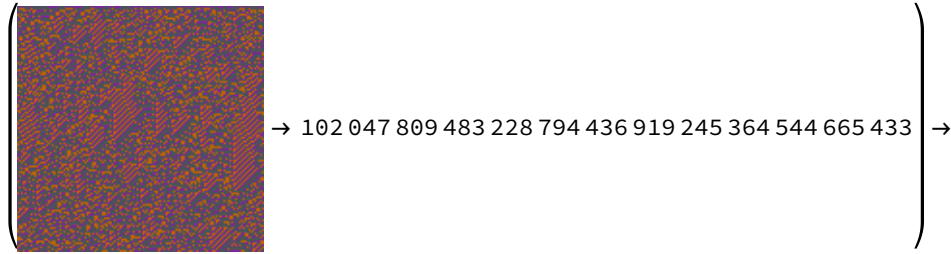
```
In[238]:= test4Data4kr1C17 = datak4r1NT[128, 128, 8];
Thread[test4Data4kr1C17 → netECA17[Keys@test4Data4kr1C17, {"TopProbabilities", 2}]]
```

$$\text{Out[239]=} \left\{ \begin{array}{c} \text{[Image: A 128x128 pixel image with a noisy, blue and green pattern]} \\ \rightarrow 255\,219\,118\,556\,246\,495\,764\,448\,982\,135\,818\,252\,673 \end{array} \right\} \rightarrow \{3 \rightarrow 2.62807 \times 10^{-6}, 4 \rightarrow 0.999997\},$$

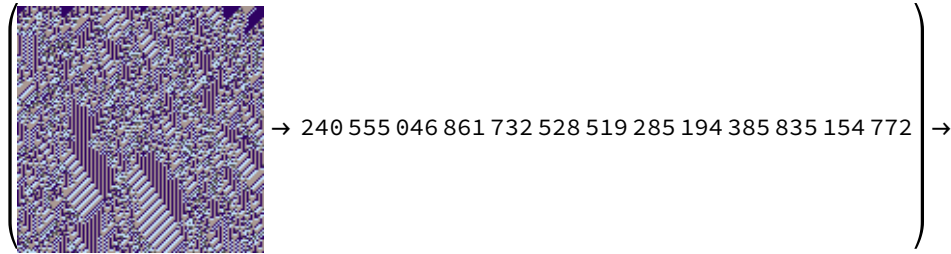
$$\left(\begin{array}{c} \text{[Image: A 128x128 pixel image with a noisy, cyan and blue pattern]} \\ \rightarrow 256\,372\,744\,774\,750\,994\,462\,308\,116\,064\,689\,670\,029 \end{array} \right) \rightarrow \{4 \rightarrow 1.66442 \times 10^{-17}, 3 \rightarrow 1.\},$$



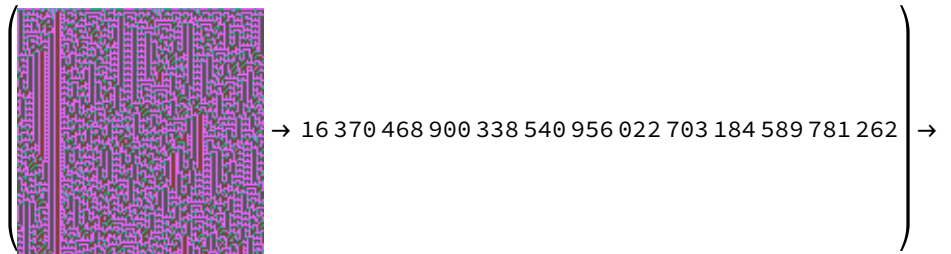
$\{4 \rightarrow 2.56385 \times 10^{-7}, 3 \rightarrow 1.\},$



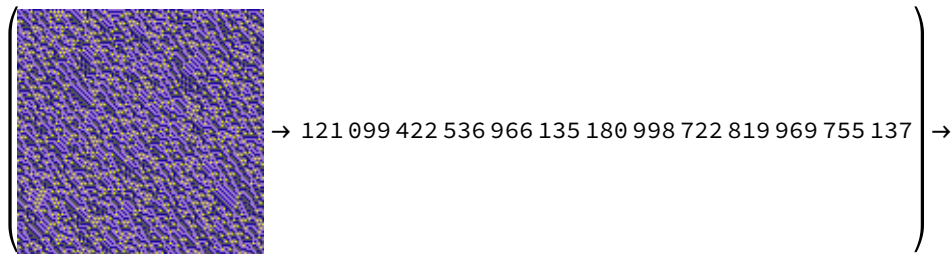
$\{4 \rightarrow 0.000696463, 3 \rightarrow 0.999304\},$



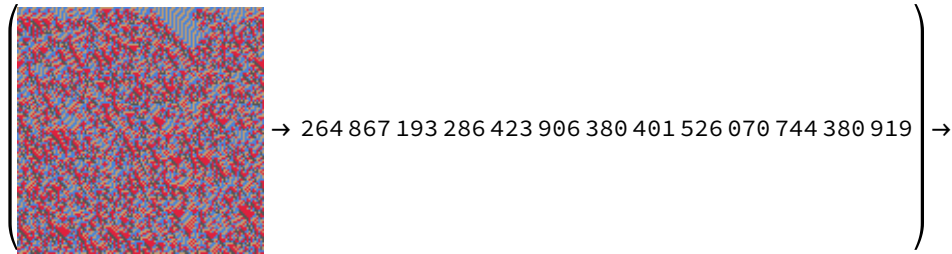
$\{4 \rightarrow 3.62136 \times 10^{-16}, 3 \rightarrow 1.\},$



$\{3 \rightarrow 1.45252 \times 10^{-15}, 4 \rightarrow 1.\},$



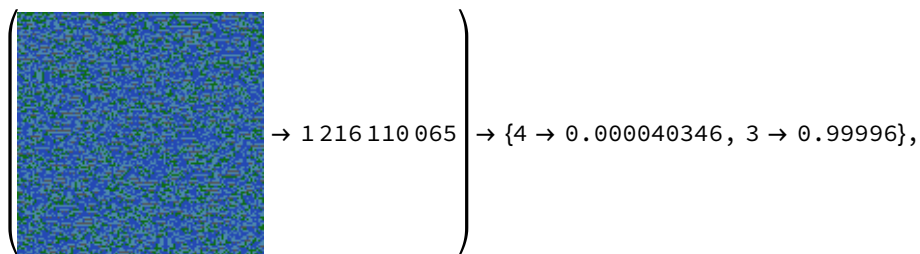
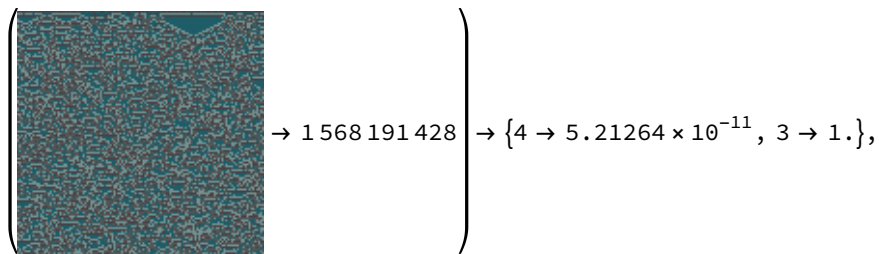
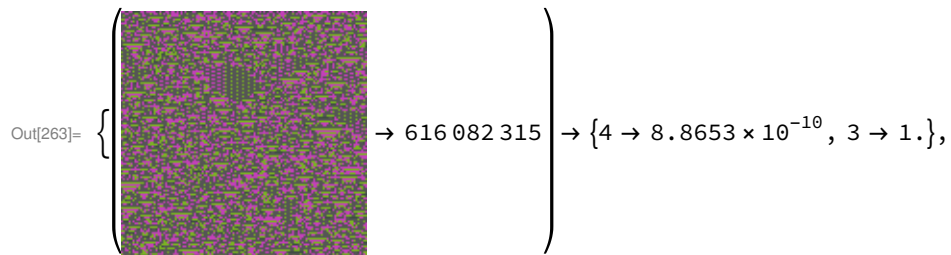
$\{4 \rightarrow 0.0000270873, 3 \rightarrow 0.999973\},$



$\{4 \rightarrow 0.105214, 3 \rightarrow 0.894786\}$

4-colour totalistic, range 2

```
In[262]:= test4Data4kr2C17 = data4kr2C[128, 128, 8];
Thread[test4Data4kr2C17 → netECA17[Keys@test4Data4kr2C17, {"TopProbabilities", 2}]]
```



$$\left(\begin{array}{c} \text{Image} \end{array} \right) \rightarrow 2\,419\,903\,949 \rightarrow \{4 \rightarrow 3.69897 \times 10^{-10}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image} \end{array} \right) \rightarrow 453\,961\,055 \rightarrow \{4 \rightarrow 3.89961 \times 10^{-8}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image} \end{array} \right) \rightarrow 3\,969\,029\,930 \rightarrow \{2 \rightarrow 0.0000237283, 4 \rightarrow 0.999976\},$$

$$\left(\begin{array}{c} \text{Image} \end{array} \right) \rightarrow 3\,970\,208\,335 \rightarrow \{4 \rightarrow 4.03487 \times 10^{-9}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image} \end{array} \right) \rightarrow 3\,418\,384\,250 \rightarrow \{4 \rightarrow 9.0126 \times 10^{-15}, 3 \rightarrow 1.\}$$

5-colour totalistic, range 1

```
In[242]:= test4Data5kr1C17 = data5T2C[8, 128, 128];
Thread[test4Data5kr1C17 → netECA17[Keys@test4Data5kr1C17, {"TopProbabilities", 2}]]
```


$$\text{Out}[243]= \left(\begin{array}{c} \text{Image} \\ \rightarrow 720\,503\,516 \end{array} \right) \rightarrow \{2 \rightarrow 0.000105936, 4 \rightarrow 0.999894\},$$

$$\left(\begin{array}{c} \text{Image} \\ \rightarrow 771\,013\,684 \end{array} \right) \rightarrow \{4 \rightarrow 1.94282 \times 10^{-8}, 2 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image} \\ \rightarrow 543\,872\,434 \end{array} \right) \rightarrow \{4 \rightarrow 6.11423 \times 10^{-7}, 3 \rightarrow 0.999999\},$$

$$\left(\begin{array}{c} \text{Image} \\ \rightarrow 341\,908\,586 \end{array} \right) \rightarrow \{4 \rightarrow 0.310854, 3 \rightarrow 0.689146\},$$

$$\left(\begin{array}{c} \text{Image} \\ \rightarrow 664\,036\,861 \end{array} \right) \rightarrow \{2 \rightarrow 0.00511847, 4 \rightarrow 0.994882\},$$

$$\left(\begin{array}{c} \text{Image} \end{array} \right) \rightarrow 1\,182\,110\,899 \rightarrow \{4 \rightarrow 0.039023, 3 \rightarrow 0.960977\},$$

$$\left(\begin{array}{c} \text{Image} \end{array} \right) \rightarrow 976\,082\,949 \rightarrow \{4 \rightarrow 9.09593 \times 10^{-19}, 2 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image} \end{array} \right) \rightarrow 1\,019\,517\,181 \rightarrow \{1 \rightarrow 6.47917 \times 10^{-10}, 2 \rightarrow 1.\}$$

6-colour totalistic, range 1

```
In[244]:= test4Data6kr1C17 = data6TC[8, 128, 128];
Thread[test4Data6kr1C17 → netECA17[Keys@test4Data6kr1C17, {"TopProbabilities", 2}]]
```

$$\text{Out}[245]= \left\{ \begin{array}{c} \text{Image} \end{array} \right\} \rightarrow 1\,128\,957\,409\,115 \rightarrow \{2 \rightarrow 0.387573, 1 \rightarrow 0.612427\},$$

$$\left(\begin{array}{c} \text{Image} \end{array} \right) \rightarrow 744\,151\,919\,694 \rightarrow \{3 \rightarrow 1.28454 \times 10^{-11}, 4 \rightarrow 1.\},$$

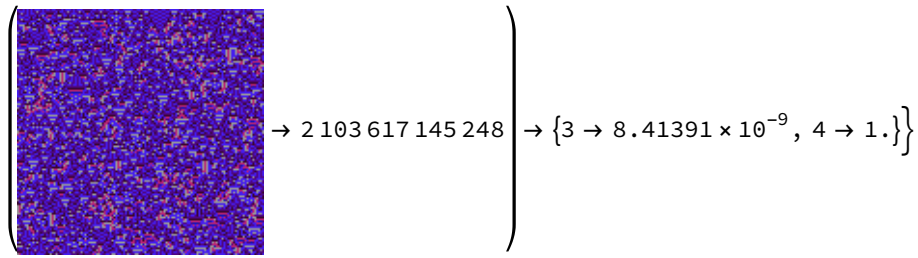
$$\left(\begin{array}{c} \text{Image 1} \\ \rightarrow 411\,482\,269\,593 \end{array} \right) \rightarrow \{4 \rightarrow 9.50671 \times 10^{-6}, 3 \rightarrow 0.99999\},$$

$$\left(\begin{array}{c} \text{Image 2} \\ \rightarrow 2\,122\,826\,252\,429 \end{array} \right) \rightarrow \{4 \rightarrow 4.58698 \times 10^{-10}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image 3} \\ \rightarrow 2\,443\,710\,325\,124 \end{array} \right) \rightarrow \{4 \rightarrow 5.97811 \times 10^{-9}, 3 \rightarrow 1.\},$$

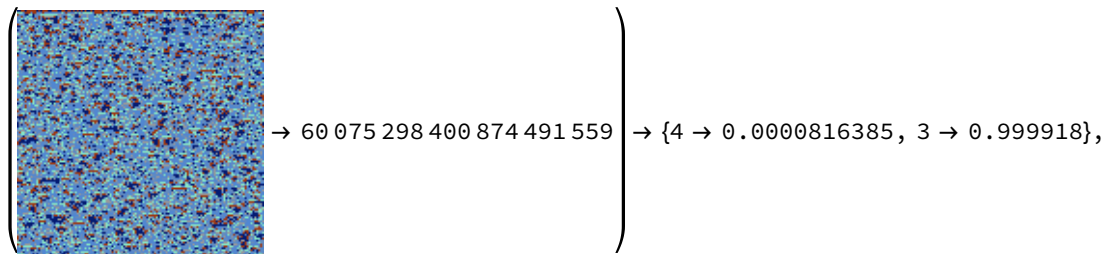
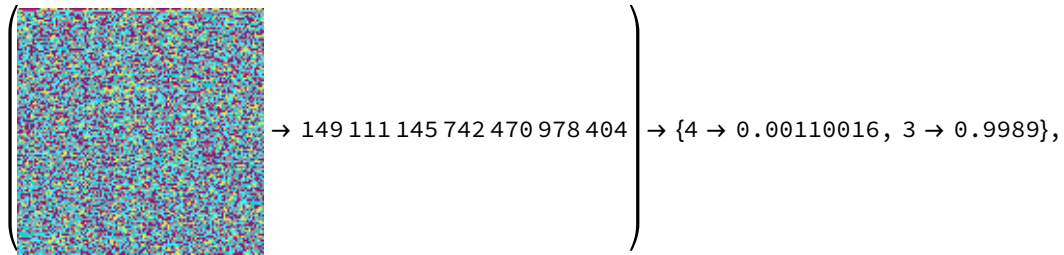
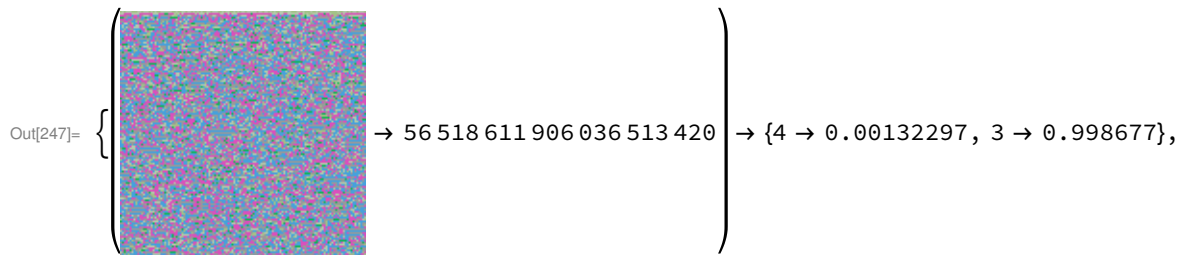
$$\left(\begin{array}{c} \text{Image 4} \\ \rightarrow 2\,519\,595\,515\,832 \end{array} \right) \rightarrow \{2 \rightarrow 0.396179, 4 \rightarrow 0.603821\},$$

$$\left(\begin{array}{c} \text{Image 5} \\ \rightarrow 572\,558\,234\,379 \end{array} \right) \rightarrow \{4 \rightarrow 1.63969 \times 10^{-11}, 3 \rightarrow 1.\},$$



6-colour totalistic, range 2

```
In[246]:= test4Data6kr2C17 = data6T2C[8, 128, 128];
Thread[test4Data6kr2C17 → netECA17[Keys@test4Data6kr2C17, {"TopProbabilities", 2}]]
```



$$\left(\begin{array}{c} \text{[Image: A noisy 128x128 pixel image with green, blue, and red pixels]} \end{array} \right) \rightarrow 138\,083\,937\,800\,052\,503\,915 \rightarrow \{4 \rightarrow 1.63338 \times 10^{-6}, 3 \rightarrow 0.999998\},$$

$$\left(\begin{array}{c} \text{[Image: A noisy 128x128 pixel image with red, green, and blue pixels]} \end{array} \right) \rightarrow 102\,848\,890\,668\,267\,918\,696 \rightarrow \{4 \rightarrow 4.51684 \times 10^{-8}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[Image: A noisy 128x128 pixel image with blue, green, and red pixels]} \end{array} \right) \rightarrow 52\,002\,759\,529\,482\,240\,344 \rightarrow \{4 \rightarrow 0.0161382, 3 \rightarrow 0.983862\},$$

$$\left(\begin{array}{c} \text{[Image: A noisy 128x128 pixel image with green, red, and blue pixels]} \end{array} \right) \rightarrow 3\,771\,326\,190\,903\,203\,597 \rightarrow \{4 \rightarrow 1.57635 \times 10^{-10}, 3 \rightarrow 1.\}$$

7-colour totalistic, range 1

```
In[248]:= test4Data7kr1C17 = data7TC[8, 128, 128];
Thread[test4Data7kr1C17 → netECA17[Keys@test4Data7kr1C17, {"TopProbabilities", 2}]]
```

$$\text{Out[249]=} \left\{ \begin{array}{c} \text{[Image: A noisy 128x128 pixel image with yellow, red, and blue pixels]} \end{array} \right. \rightarrow 249\,739\,897\,876\,317 \rightarrow \{4 \rightarrow 7.58753 \times 10^{-13}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image 1} \\ \rightarrow 6\,589\,873\,174\,284\,234 \end{array} \right) \rightarrow \{4 \rightarrow 3.70203 \times 10^{-21}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image 2} \\ \rightarrow 2\,838\,251\,451\,633\,386 \end{array} \right) \rightarrow \{3 \rightarrow 0.0000362001, 4 \rightarrow 0.999964\},$$

$$\left(\begin{array}{c} \text{Image 3} \\ \rightarrow 3\,069\,021\,856\,393\,877 \end{array} \right) \rightarrow \{4 \rightarrow 4.6982 \times 10^{-6}, 3 \rightarrow 0.999995\},$$

$$\left(\begin{array}{c} \text{Image 4} \\ \rightarrow 10\,282\,712\,720\,317\,214 \end{array} \right) \rightarrow \{3 \rightarrow 4.14045 \times 10^{-19}, 4 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image 5} \\ \rightarrow 203\,015\,413\,423\,084 \end{array} \right) \rightarrow \{4 \rightarrow 2.87431 \times 10^{-9}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[Image: 128x128 random noise with green and blue pixels]} \\ \rightarrow 9\,746\,864\,148\,555\,591 \end{array} \right) \rightarrow \{3 \rightarrow 1.53822 \times 10^{-7}, 4 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[Image: 128x128 random noise with purple and blue pixels]} \\ \rightarrow 8\,003\,062\,538\,664\,128 \end{array} \right) \rightarrow \{3 \rightarrow 2.05185 \times 10^{-8}, 4 \rightarrow 1.\}$$

8-colour totalistic, range 1

```
In[250]:= test4Data8kr1C17 = data8TC[8, 128, 128];
Thread[test4Data8kr1C17 → netECA17[Keys@test4Data8kr1C17, {"TopProbabilities", 2}]]
```

$$\text{Out[251]=} \left\{ \begin{array}{c} \text{[Image: 128x128 random noise with multi-colored pixels]} \\ \rightarrow 10\,266\,196\,594\,935\,096\,075 \end{array} \right\} \rightarrow \{4 \rightarrow 8.5791 \times 10^{-18}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[Image: 128x128 random noise with purple and blue pixels]} \\ \rightarrow 731\,338\,973\,990\,773\,560 \end{array} \right) \rightarrow \{2 \rightarrow 7.53019 \times 10^{-12}, 4 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[Image: 128x128 random noise with purple and blue pixels]} \\ \rightarrow 11\,247\,173\,012\,174\,218\,620 \end{array} \right) \rightarrow \{4 \rightarrow 0.0000380778, 3 \rightarrow 0.999962\},$$

$$\left(\begin{array}{c} \text{[Image: Random noise pattern with purple and blue tones]} \\ \rightarrow 63\,742\,472\,032\,617\,219\,918 \end{array} \right) \rightarrow \{4 \rightarrow 0.0000371126, 3 \rightarrow 0.999963\},$$

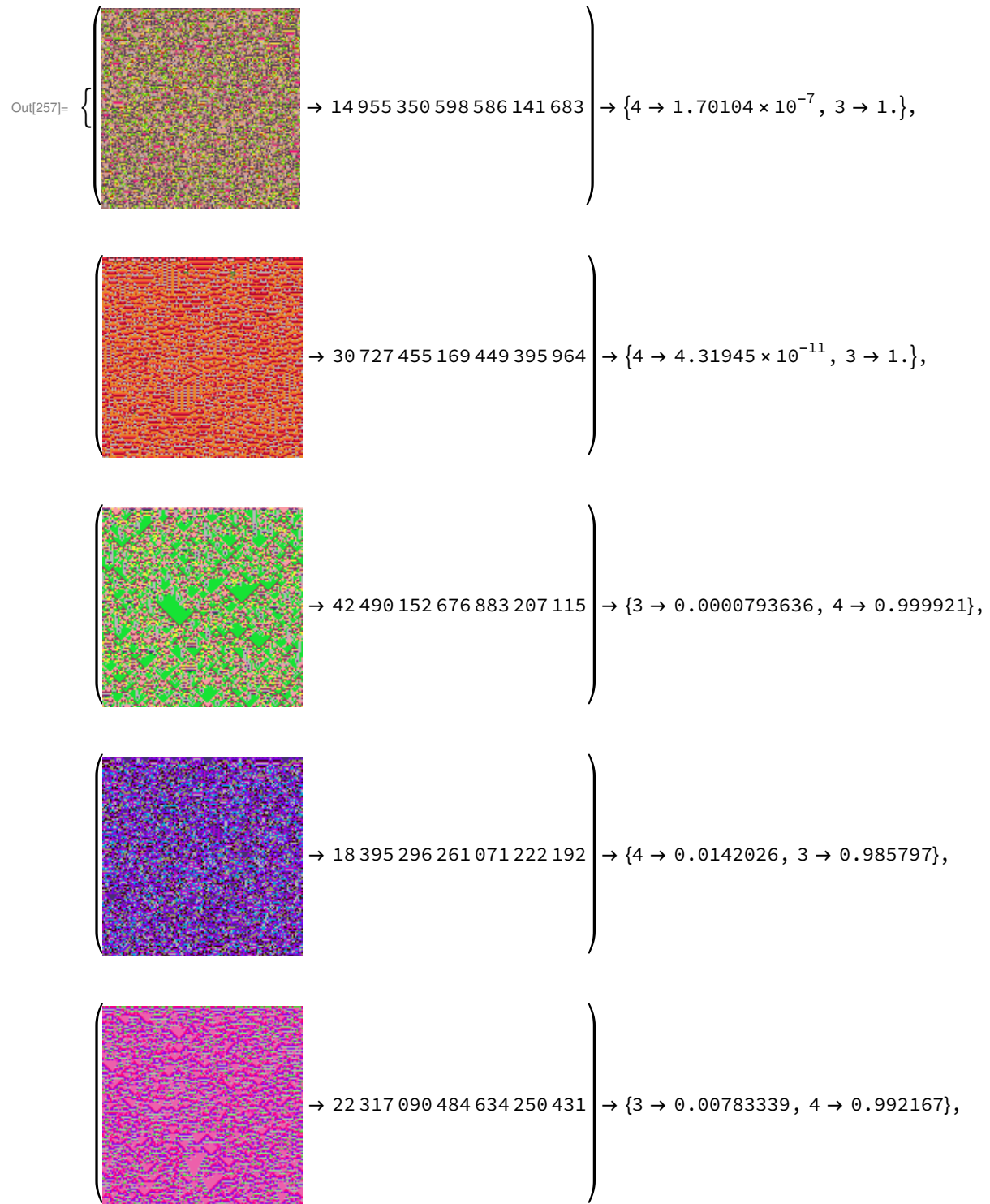
$$\left(\begin{array}{c} \text{[Image: Random noise pattern with green and blue tones]} \\ \rightarrow 7\,382\,455\,380\,800\,363\,015 \end{array} \right) \rightarrow \{4 \rightarrow 8.07468 \times 10^{-15}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[Image: Random noise pattern with green and blue tones]} \\ \rightarrow 59\,100\,651\,667\,569\,734\,000 \end{array} \right) \rightarrow \{4 \rightarrow 1.27228 \times 10^{-11}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[Image: Random noise pattern with green and blue tones]} \\ \rightarrow 24\,971\,306\,247\,396\,766\,335 \end{array} \right) \rightarrow \{4 \rightarrow 0.0333734, 3 \rightarrow 0.966627\},$$

$$\left(\begin{array}{c} \text{[Image: Random noise pattern with red and pink tones]} \\ \rightarrow 45\,946\,581\,080\,593\,555\,746 \end{array} \right) \rightarrow \{4 \rightarrow 1.08598 \times 10^{-15}, 3 \rightarrow 1.\}$$

```
In[256]:= test4Data8kr1C17 = data8TC[8, 128, 128];
Thread[test4Data8kr1C17 → netECA17[Keys@test4Data8kr1C17, {"TopProbabilities", 2}]]
```



$$\left(\begin{array}{c} \text{Image 1: A noisy, multi-colored pattern with purple, blue, and green pixels.} \\ \rightarrow 33\,329\,414\,465\,629\,594\,174 \end{array} \right) \rightarrow \{4 \rightarrow 0.00851294, 3 \rightarrow 0.991487\},$$

$$\left(\begin{array}{c} \text{Image 2: A pattern with a solid pink background and vertical yellow and blue lines.} \\ \rightarrow 68\,439\,232\,681\,205\,604\,962 \end{array} \right) \rightarrow \{2 \rightarrow 1.97568 \times 10^{-13}, 4 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image 3: A pattern with a solid pink background and horizontal yellow and blue lines.} \\ \rightarrow 53\,049\,830\,479\,062\,864\,751 \end{array} \right) \rightarrow \{4 \rightarrow 3.6815 \times 10^{-10}, 3 \rightarrow 1.\}$$