New CA Classifiers (random colours)

Wolfram Classes of ECAs

In[63]:=

```
CAclasses = {1, 2, 2, 2, 2, 2, 2, 2, 1, 2, 2, 2, 2, 2, 2, 2, 2, 3, 2, 2, 2, 3, 2, 2, 2, 2, 2,
   2, 2, 3, 2, 1, 2, 2, 2, 2, 2, 2, 2, 1, 3, 2, 2, 2, 3, 2, 2, 2, 2, 2, 2, 2, 2, 4, 2, 2,
   2, 2, 2, 3, 2, 2, 2, 1, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 3, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2,
   3, 2, 2, 3, 3, 2, 2, 2, 2, 2, 1, 3, 2, 2, 2, 3, 3, 2, 2, 3, 3, 3, 2, 2, 4, 2, 2, 2, 2,
   2, 2, 2, 2, 2, 3, 3, 3, 2, 4, 2, 3, 2, 1, 3, 2, 2, 2, 2, 2, 3, 1, 4, 2, 2, 2, 2, 2, 2,
   2, 2, 3, 4, 2, 3, 3, 3, 2, 3, 2, 2, 2, 2, 2, 2, 1, 3, 2, 2, 2, 3, 2, 2, 1, 3, 2, 2,
   2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 3, 3, 2, 2, 2, 2, 2, 2, 2, 2, 1, 4, 2, 3, 2, 2, 2, 2,
   2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 3, 2, 2,
   2, 2, 2, 2, 2, 2, 1, 1, 2, 2, 1, 1, 2, 2, 2, 2, 2, 2, 2, 2, 1, 1, 1, 1, 1, 1, 1, 1};
```

Functions for creating net and random datasets (ECAs, all 4 classes)

In[2]:=

```
RandomRuleC[n_Integer, W_Integer, H_Integer] :=
 Image[ArrayPlot[CellularAutomaton[n, RandomInteger[1, W], H - 1],
   ImageSize → {W, H}, ColorRules → {0 -> RandomColor[], 1 -> RandomColor[],
     3 -> RandomColor[], 4 → RandomColor[], 5 -> RandomColor[],
     6 -> RandomColor[], 7 -> RandomColor[]}, Frame → False]]
netC[W_Integer, H_Integer] := NetInitialize@NetChain[
   {ConvolutionLayer[16, {2, 3}], Ramp, PoolingLayer[{H, W} - {1, 2}], FlattenLayer[],
    LinearLayer[256], SoftmaxLayer[]}, "Input" → NetEncoder[{"Image", {W, H}}],
   "Output" → NetDecoder[{"Class", Range[0, 255]}]]
netTwoCC[W_Integer, H_Integer] := NetInitialize@
  NetChain[<|"conv1" → ConvolutionLayer[16, {2, 3}], "ramp1" → Ramp,
    "conv3" → ConvolutionLayer[16, {2, 3}], "ramp2" → Ramp,
    "pooling" → PoolingLayer[{H, W} - {2, 4}], "flatten" → FlattenLayer[],
    "linear" → 512, "linear2" → 4, "softmax" → SoftmaxLayer[]|>,
   "Input" → NetEncoder[{"Image", {W, H}}], "Output" → NetDecoder[{"Class", Range[1, 4]}]]
dataC[W_Integer, H_Integer, n_Integer] :=
 Table[RandomRuleC[i, W, H] → CAclasses[[i + 1]], {i, RandomChoice[Range[0, 255], n]}]
```

In[6]:=
```
netThreeCC[W_Integer, H_Integer] :=
 NetInitialize@NetChain[<|"conv1" → ConvolutionLayer[16, {2, 3}],
    "ramp1" → Ramp, "conv2" → ConvolutionLayer[16, {2, 3}],
    "ramp2" → Ramp, "conv3" → ConvolutionLayer[16, {2, 3}], "ramp3" → Ramp,
    "pooling" → PoolingLayer[{H, W} - {4, 8}], "flatten" → FlattenLayer[],
    "linear" → 512, "linear2" → 4, "softmax" → SoftmaxLayer[]|>,
   "Input" → NetEncoder[{"Image", {W, H}}], "Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

In[7]:=
```
netThreeCC1024[W_Integer, H_Integer] :=
 NetInitialize@NetChain[<|"conv1" → ConvolutionLayer[16, {2, 3}],
    "ramp1" → Ramp, "conv2" → ConvolutionLayer[16, {2, 3}],
    "ramp2" → Ramp, "conv3" → ConvolutionLayer[16, {2, 3}], "ramp3" → Ramp,
    "pooling" → PoolingLayer[{H, W} - {4, 8}], "flatten" → FlattenLayer[],
    "linear" → 1024, "linear2" → 4, "softmax" → SoftmaxLayer[]|>,
   "Input" → NetEncoder[{"Image", {W, H}}], "Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

In[8]:=
```
netFourCC512[W_Integer, H_Integer] :=
 NetInitialize@NetChain[<|"conv1" → ConvolutionLayer[32, {2, 3}],
    "ramp1" → Ramp, "conv3" → ConvolutionLayer[32, {2, 3}], "ramp2" → Ramp,
    "pooling" → PoolingLayer[{H, W} - {2, 4}], "flatten" → FlattenLayer[],
    "linear" → 512, "linear2" → 4, "softmax" → SoftmaxLayer[]|>,
   "Input" → NetEncoder[{"Image", {W, H}}], "Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

In[9]:=
```
netFiveCC512[W_Integer, H_Integer] := NetInitialize@
  NetChain[<|"conv1" → ConvolutionLayer[32, {2, 3}], "bat1" → BatchNormalizationLayer[],
    "ramp1" → Ramp, "conv3" → ConvolutionLayer[32, {2, 3}],
    "bat2" → BatchNormalizationLayer[], "ramp2" → Ramp,
    "pooling" → PoolingLayer[{H, W} - {2, 4}], "flatten" → FlattenLayer[],
    "linear" → 512, "linear2" → 4, "softmax" → SoftmaxLayer[]|>,
   "Input" → NetEncoder[{"Image", {W, H}}], "Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

In[10]:=
```
netSixCC512drop[W_Integer, H_Integer] := NetInitialize@
  NetChain[<|"drop1" → DropoutLayer[0.2], "conv1" → ConvolutionLayer[32, {3, 3}],
    "bat1" → BatchNormalizationLayer[], "ramp1" → Ramp,
    "conv3" → ConvolutionLayer[32, {3, 3}], "bat2" → BatchNormalizationLayer[],
    "ramp2" → Ramp, "pooling" → PoolingLayer[{H, W} - {4, 8}],
    "flatten" → FlattenLayer[], "linear" → 512, "drop2" → DropoutLayer[0.2],
    "linear2" → 4, "softmax" → SoftmaxLayer[]|>,
   "Input" → NetEncoder[{"Image", {W, H}}], "Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

In[11]:=
```
netSevenCC512drop[W_Integer, H_Integer] :=
 NetInitialize@NetChain[<|"conv1" → ConvolutionLayer[24, {3, 3}],
    "bat1" → BatchNormalizationLayer[], "ramp1" → Ramp,
    "conv3" → ConvolutionLayer[24, {3, 3}], "bat2" → BatchNormalizationLayer[],
    "ramp2" → Ramp, "pooling" → PoolingLayer[{H, W} - {4, 8}],
    "flatten" → FlattenLayer[], "linear" → 512, "drop2" → DropoutLayer[0.2],
    "linear2" → 4, "softmax" → SoftmaxLayer[]|>,
   "Input" → NetEncoder[{"Image", {W, H}}], "Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

In[12]:=
```
netEightCC512drop[W_Integer, H_Integer] :=
 NetInitialize@NetChain[<|"conv1" → ConvolutionLayer[24, {3, 3}],
    "bat1" → BatchNormalizationLayer[], "ramp1" → Ramp,
    "conv2" → ConvolutionLayer[16, {2, 3}], "bat2" → BatchNormalizationLayer[],
    "ramp2" → Ramp, "conv3" → ConvolutionLayer[24, {3, 3}],
    "bat3" → BatchNormalizationLayer[], "ramp3" → Ramp, "pooling" →
     PoolingLayer[{H, W} - {8, 16}], "flatten" → FlattenLayer[], "linear" → 1024,
    "drop2" → DropoutLayer[0.2], "linear2" → 4, "softmax" → SoftmaxLayer[]|>,
   "Input" → NetEncoder[{"Image", {W, H}}], "Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

In[13]:=
```
netNineCC512drop[W_Integer, H_Integer] :=
 NetInitialize@NetChain[<|"conv1" → ConvolutionLayer[24, {3, 3}],
    "bat1" → BatchNormalizationLayer[], "ramp1" → Ramp,
    "conv2" → ConvolutionLayer[24, {3, 3}], "bat2" → BatchNormalizationLayer[],
    "ramp2" → Ramp, "conv3" → ConvolutionLayer[24, {3, 3}],
    "bat3" → BatchNormalizationLayer[], "ramp3" → Ramp, "pooling" →
     PoolingLayer[{H, W} - {12, 12}], "flatten" → FlattenLayer[], "linear" → 512,
    "drop2" → DropoutLayer[0.2], "linear2" → 4, "softmax" → SoftmaxLayer[]|>,
   "Input" → NetEncoder[{"Image", {W, H}}], "Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

In[14]:=
```
netTenCC1024drop[W_Integer, H_Integer] :=
 NetInitialize@NetChain[<|"conv1" → ConvolutionLayer[24, {3, 3}],
    "bat1" → BatchNormalizationLayer[], "ramp1" → Ramp,
    "conv2" → ConvolutionLayer[24, {3, 3}], "bat2" → BatchNormalizationLayer[],
    "ramp2" → Ramp, "conv3" → ConvolutionLayer[24, {3, 3}],
    "bat3" → BatchNormalizationLayer[], "ramp3" → Ramp,
    "conv4" → ConvolutionLayer[24, {3, 3}], "bat4" → BatchNormalizationLayer[],
    "ramp4" → Ramp, "pooling" → PoolingLayer[{H, W} - {12, 12}],
    "flatten" → FlattenLayer[], "linear" → 1024,
    "drop2" → DropoutLayer[0.3], "linear2" → 4, "softmax" → SoftmaxLayer[]|>,
   "Input" → NetEncoder[{"Image", {W, H}}], "Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

In[112]:=
```
netElevenCC1024drop[W_Integer, H_Integer] :=
 NetInitialize@NetChain[<|"conv1" → ConvolutionLayer[24, {3, 3}],
    "bat1" → BatchNormalizationLayer[], "ramp1" → Ramp,
    "pooling1" → PoolingLayer[{2, 2}], "conv2" → ConvolutionLayer[16, {3, 3}],
    "bat2" → BatchNormalizationLayer[], "ramp2" → Ramp,
    "pooling2" → PoolingLayer[{2, 2}], "conv3" → ConvolutionLayer[12, {3, 3}],
    "bat3" → BatchNormalizationLayer[], "ramp3" → Ramp,
    "pooling3" → PoolingLayer[{2, 2}], "conv4" → ConvolutionLayer[6, {3, 3}],
    "bat4" → BatchNormalizationLayer[], "ramp4" → Ramp,
    "pooling4" → PoolingLayer[{32, 32}], "flatten" → FlattenLayer[], "linear" → 1024,
    "drop2" → DropoutLayer[0.3], "linear2" → 4, "softmax" → SoftmaxLayer[]|>,
   "Input" → NetEncoder[{"Image", {W, H}}], "Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

Functions for creating datasets (1D totalistic CAs)

k=3, r=1 totalistic (class 4 only)

In[16]:=
```
gen3TC[p_Integer, W_Integer, H_Integer] :=
 Image[ArrayPlot[CellularAutomaton[{p, {3, 1}}, RandomInteger[1, W], H - 1],
   ImageSize → {W, H}, ColorRules →
    {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 → RandomColor[],
     5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data3T2C[W_Integer, H_Integer, n_Integer] := Table[gen3TC[i, W, H] → 4,
  {i, RandomChoice[{1635, 1815, 2007, 2043, 2049, 1388, 1041}, n]}]
```

k=4, r=1 totalistic (class 4 only, 1 example)

In[18]:=
```
gen4TC[p_Integer, W_Integer, H_Integer] :=
 Image[ArrayPlot[CellularAutomaton[{p, {4, 1}}, RandomInteger[1, W], H - 1],
   ImageSize → {W, H}, ColorRules →
    {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 → RandomColor[],
     5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data4TC[W_Integer, H_Integer, n_Integer] := Table[gen4TC[1 004 600, W, H] → 4, n]
```

k=2, r=2 totalistic (all 4 classes)

In[20]:=
```
gen2r2C[p_Integer, W_Integer, H_Integer] :=
 Image[ArrayPlot[CellularAutomaton[{p, {2, 1}, 2}, RandomInteger[1, W], H - 1],
   ImageSize → {W, H}, ColorRules →
    {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 → RandomColor[],
     5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data2r2c4C[W_Integer, H_Integer, n_Integer] :=
 Table[gen2r2C[i, W, H] → 4, {i, RandomChoice[{20, 52}, n]}]
data2r2c3C[W_Integer, H_Integer, n_Integer] := Table[gen2r2C[i, W, H] → 3,
  {i, RandomChoice[{2, 6, 10, 12, 14, 18, 22, 26, 28, 30, 34, 38, 42, 44, 46, 50}, n]}]
data2r2c2C[W_Integer, H_Integer, n_Integer] :=
 Table[gen2r2C[i, W, H] → 2, {i, RandomChoice[{8, 24, 56}, n]}]
data2r2c1C[W_Integer, H_Integer, n_Integer] := Table[gen2r2C[i, W, H] → 1,
  {i, RandomChoice[{0, 4, 16, 32, 36, 40, 48, 54, 58, 60, 62}, n]}]
genData2r2C[W_Integer, H_Integer, n_Integer] :=
 Join[data2r2c4C[W, H, n], data2r2c3C[W, H, n], data2r2c2C[W, H, n], data2r2c1C[W, H, n]]
```

k=5, r=1 totalistic (class 4 only)

In[26]:=
```
gen5T4C[p_Integer, W_Integer, H_Integer] :=
 Image[ArrayPlot[CellularAutomaton[{p, {5, 1}}, RandomInteger[1, W], H - 1],
   ImageSize → {W, H}, ColorRules →
    {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 → RandomColor[],
     5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data5T4C[n_Integer, W_Integer, H_Integer] := Table[gen5T4C[i, W, H] → 4,
  {i, RandomChoice[{781 130 654, 772 514 435, 1 151 319 452, 309 095 787, 880 862 046,
     973 835 714, 779 446 817, 345 466 505, 535 500 975, 793 363 571, 1 052 373 865,
     455 984 785, 339 227 109, 1 050 973 846, 513 368 817, 91 315 820, 113 925 357}, n]}]
```

k=5, r=1 totalistic (classes 2/3/4)

In[28]:=
```
gen5TC[p_Integer, W_Integer, H_Integer] :=
 Image[ArrayPlot[CellularAutomaton[{p, {5, 1}, 1}, RandomInteger[1, W], H - 1],
   ImageSize → {W, H}, ColorRules →
    {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 → RandomColor[],
     5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data5T4CC[W_Integer, H_Integer, n_Integer] := Table[gen5TC[i, W, H] → 4,
  {i, RandomChoice[{644 218 533, 491 739 943, 6 889 640, 986 144 962, 1 099 816 682,
     988 971 204, 300 829 994, 272 622 024, 304 100 638, 626 595 633}, n]}]
data5T3CC[W_Integer, H_Integer, n_Integer] := Table[gen5TC[i, W, H] → 3,
  {i, RandomChoice[{889 082 395, 541 068 260, 807 907 479, 816 180 062, 650 485 139,
     643 827 745, 753 940 864, 871 525 323, 351 440 311, 83 501 460}, n]}]
data5T2CC[W_Integer, H_Integer, n_Integer] := Table[gen5TC[i, W, H] → 2,
  {i, RandomChoice[{525 735 659, 1 022 330 944, 1 007 796 739, 495 633 437, 1 036 827 943}, n]}]
genData5TCC[W_Integer, H_Integer, n_Integer] :=
 Join[data5T4CC[W, H, n], data5T3CC[W, H, n], data5T2CC[W, H, n]]
```

Generate test datasets

k=2, r=2 non-totalistic

In[33]:=
```
genk2r2C[p_Integer, W_Integer, H_Integer] :=
 Image[ArrayPlot[CellularAutomaton[{p, 2, 2}, RandomInteger[1, W], H - 1],
   ImageSize → {W, H}, ColorRules →
    {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 → RandomColor[],
     5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
datak2r2C[W_Integer, H_Integer, n_Integer] := Table[genk2r2C[i, W, H] → i,
  {i, RandomChoice[Range[0, 4 294 967 295], n]}]
```

k=2, r=3 non-totalistic

In[35]:=
```
genk2r3NT[p_Integer, W_Integer, H_Integer] :=
 Image[ArrayPlot[CellularAutomaton[{p, 2, 3}, RandomInteger[1, W], H - 1],
   ImageSize → {W, H}, ColorRules →
    {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 → RandomColor[],
     5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
datak2r3NT[W_Integer, H_Integer, n_Integer] :=
 Table[genk2r3NT[i, W, H] → i, {i, RandomInteger[2^2^7 - 1, n]}]
```

k=3, r=1 non-totalistic

In[37]:=
```
genk3r1NT[p_Integer, W_Integer, H_Integer] :=
 Image[ArrayPlot[CellularAutomaton[{p, 3}, RandomInteger[1, W], H - 1],
   ImageSize → {W, H}, ColorRules → {0 -> RandomColor[], 1 -> RandomColor[],
     3 -> RandomColor[], 4 → RandomColor[], 5 -> RandomColor[],
     6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
datak3r1NT[W_Integer, H_Integer, n_Integer] :=
 Table[genk3r1NT[i, W, H] → i, {i, RandomInteger[3^3^3 - 1, n]}]
```

k=3, r=2 totalistic

In[39]:=
```
genk3r2C[p_Integer, W_Integer, H_Integer] :=
 Image[ArrayPlot[CellularAutomaton[{p, {3, 1}, 2}, RandomInteger[1, W], H - 1],
   ImageSize → {W, H}, ColorRules →
    {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 → RandomColor[],
     5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
datak3r2C[W_Integer, H_Integer, n_Integer] := Table[genk3r2C[i, W, H] → i,
  {i, RandomChoice[Range[0, 177 146], n]}]
```

k=3, r=3 totalistic

In[41]:=
```
genk3r3C[p_Integer, W_Integer, H_Integer] :=
 Image[ArrayPlot[CellularAutomaton[{p, {3, 1}, 3}, RandomInteger[1, W], H - 1],
   ImageSize → {W, H}, ColorRules →
    {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 → RandomColor[],
     5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
datak3r3C[W_Integer, H_Integer, n_Integer] := Table[genk3r3C[i, W, H] → i,
  {i, RandomChoice[Range[0, 14 348 906], n]}]
```

k=4, r=1 non-totalistic

In[43]:=
```
genk4r1NT[p_Integer, W_Integer, H_Integer] :=
 Image[ArrayPlot[CellularAutomaton[{p, 4}, RandomInteger[1, W], H - 1],
   ImageSize → {W, H}, ColorRules → {0 -> RandomColor[], 1 -> RandomColor[],
     3 -> RandomColor[], 4 → RandomColor[], 5 -> RandomColor[],
     6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
datak4r1NT[W_Integer, H_Integer, n_Integer] :=
 Table[genk4r1NT[i, W, H] → i, {i, RandomInteger[4^4^3 - 1, n]}]
```

k=4, r=1 totalistic

In[45]:=
```
genk4r1C[p_Integer, W_Integer, H_Integer] :=
 Image[ArrayPlot[CellularAutomaton[{p, {4, 1}}, RandomInteger[1, W], H - 1],
   ImageSize → {W, H}, ColorRules →
    {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 → RandomColor[],
     5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
datak4r1C[W_Integer, H_Integer, n_Integer] := Table[genk4r1C[i, W, H] → i,
  {i, RandomChoice[Range[0, 1 048 575], n]}]
```

k=4, r=2 totalistic

In[47]:=
```
genk4r2C[p_Integer, W_Integer, H_Integer] :=
 Image[ArrayPlot[CellularAutomaton[{p, {4, 1}, 2}, RandomInteger[1, W], H - 1],
   ImageSize → {W, H}, ColorRules →
    {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 → RandomColor[],
     5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
datak4r2C[W_Integer, H_Integer, n_Integer] := Table[genk4r2C[i, W, H] → i,
  {i, RandomChoice[Range[0, 4 294 967 295], n]}]
```

k=5, r=1 totalistic

In[49]:=
```
gen5T2C[p_Integer, W_Integer, H_Integer] :=
 Image[ArrayPlot[CellularAutomaton[{p, {5, 1}, 1}, RandomInteger[1, W], H - 1],
   ImageSize → {W, H}, ColorRules →
    {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 → RandomColor[],
     5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data5T2C[n_Integer, W_Integer, H_Integer] := Table[gen5T2C[i, W, H] → i,
  {i, RandomChoice[Range[0, 1 220 703 125], n]}]
```

k=6, r=1 totalistic

In[51]:=
```
gen6TC[p_Integer, W_Integer, H_Integer] :=
 Image[ArrayPlot[CellularAutomaton[{p, {6, 1}, 1}, RandomInteger[1, W], H - 1],
   ImageSize → {W, H}, ColorRules →
    {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 → RandomColor[],
     5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data6TC[n_Integer, W_Integer, H_Integer] := Table[gen6TC[i, W, H] → i,
  {i, RandomInteger[2 821 109 907 455, n]}]
```

k=6, r=2 totalistic

In[53]:=
```
gen6T2C[p_Integer, W_Integer, H_Integer] :=
 Image[ArrayPlot[CellularAutomaton[{p, {6, 1}, 2}, RandomInteger[1, W], H - 1],
   ImageSize → {W, H}, ColorRules →
    {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 → RandomColor[],
     5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data6T2C[n_Integer, W_Integer, H_Integer] := Table[gen6T2C[i, W, H] → i,
  {i, RandomInteger[170 581 728 179 578 208 255, n]}]
```

k=7, r=1 totalistic

In[55]:=
```
gen7TC[p_Integer, W_Integer, H_Integer] :=
 Image[ArrayPlot[CellularAutomaton[{p, {7, 1}, 1}, RandomInteger[1, W], H - 1],
   ImageSize → {W, H}, ColorRules →
    {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 → RandomColor[],
     5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame → False]]
data7TC[n_Integer, W_Integer, H_Integer] := Table[gen7TC[i, W, H] → i,
  {i, RandomInteger[11 398 895 185 373 142, n]}]
```

k=8, r=1 totalistic

In[57]:=
```
gen8TC[p_Integer, W_Integer, H_Integer] :=
 Image[ArrayPlot[CellularAutomaton[{p, {8, 1}, 1}, RandomInteger[1, W], H - 1],
   ImageSize → {W, H}, ColorRules →
    {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 → RandomColor[],
     5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame → False]]
data8TC[n_Integer, W_Integer, H_Integer] := Table[gen8TC[i, W, H] → i,
  {i, RandomInteger[73 786 976 294 838 206 463, n]}]
```

k=8, r=2 totalistic

In[59]:=
```
gen8T2C[p_Integer, W_Integer, H_Integer] :=
 Image[ArrayPlot[CellularAutomaton[{p, {8, 1}, 2}, RandomInteger[1, W], H - 1],
   ImageSize → {W, H}, ColorRules →
    {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[], 4 → RandomColor[],
     5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[]}, Frame → False]]
data8T2C[n_Integer, W_Integer, H_Integer] := Table[gen8T2C[i, W, H] → i,
  {i, RandomInteger[324 518 553 658 426 726 783 156 020 576 255, n]}]
```

k=9, r=1 totalistic

In[61]:=
```
gen9TC[p_Integer, W_Integer, H_Integer] :=
 Image[ArrayPlot[CellularAutomaton[{p, {9, 1}, 1}, RandomInteger[1, W], H - 1],
   ImageSize → {W, H}, ColorRules → {0 -> RandomColor[], 1 -> RandomColor[],
     3 -> RandomColor[], 4 → RandomColor[], 5 -> RandomColor[],
     6 -> RandomColor[], 7 -> RandomColor[], 8 → RandomColor[]}, Frame → False]]
data9TC[n_Integer, W_Integer, H_Integer] := Table[gen9TC[i, W, H] → i,
  {i, RandomInteger[717 897 987 691 852 588 770 248, n]}]
```

k=10, r=1 totalistic

In[225]:=
```
gen10TC[p_Integer, W_Integer, H_Integer] :=
 Image[ArrayPlot[CellularAutomaton[{p, {10, 1}, 1}, RandomInteger[1, W], H - 1],
   ImageSize → {W, H}, ColorRules → {0 -> RandomColor[], 1 -> RandomColor[],
     3 -> RandomColor[], 4 → RandomColor[], 5 -> RandomColor[], 6 -> RandomColor[],
     7 -> RandomColor[], 8 → RandomColor[], 9 → RandomColor[]}, Frame → False]]
data10TC[n_Integer, W_Integer, H_Integer] := Table[gen10TC[i, W, H] → i,
  {i, RandomInteger[9 999 999 999 999 999 999 999 999 999, n]}]
```

k=11, r=1 totalistic

In[227]:=
```
gen11TC[p_Integer, W_Integer, H_Integer] := Image[ArrayPlot[
    CellularAutomaton[{p, {11, 1}, 1}, RandomInteger[1, W], H - 1], ImageSize → {W, H},
    ColorRules → {0 -> RandomColor[], 1 -> RandomColor[], 3 -> RandomColor[],
      4 → RandomColor[], 5 -> RandomColor[], 6 -> RandomColor[], 7 -> RandomColor[],
      8 → RandomColor[], 9 → RandomColor[], 10 → RandomColor[]}, Frame → False]]
data11TC[n_Integer, W_Integer, H_Integer] := Table[gen11TC[i, W, H] → i,
  {i, RandomInteger[191 943 424 957 750 480 504 146 841 291 809, n]}]
```

k=18, r=1 totalistic

In[229]:=
```
gen18TC[p_Integer, W_Integer, H_Integer] :=
 Image[ArrayPlot[CellularAutomaton[{p, {18, 1}, 1}, RandomInteger[1, W], H - 1],
   ImageSize → {W, H}, ColorRules → {0 -> RandomColor[], 1 -> RandomColor[],
     3 -> RandomColor[], 4 → RandomColor[], 5 -> RandomColor[], 6 -> RandomColor[],
     7 -> RandomColor[], 8 → RandomColor[], 9 → RandomColor[], 10 → RandomColor[],
     11 → RandomColor[], 12 → RandomColor[], 13 → RandomColor[], 14 → RandomColor[],
     15 → RandomColor[], 16 → RandomColor[], 17 → RandomColor[]}, Frame → False]]
data18TC[n_Integer, W_Integer, H_Integer] :=
 Table[gen18TC[i, W, H] → i, {i, RandomInteger[
    188 005 374 836 229 120 894 273 278 138 806 956 375 747 747 317 139 671 689 960 882 175, n]}]
```

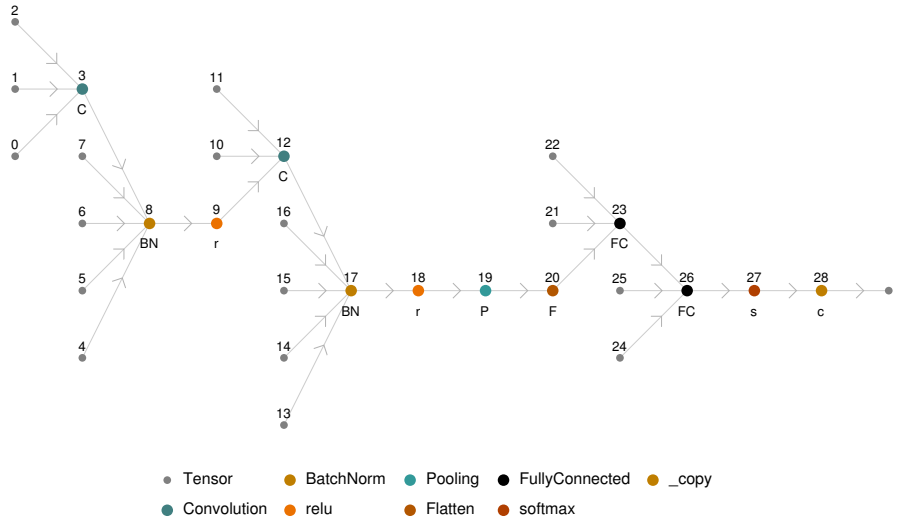
Network XIII - Two convolutions, dropout on linear only, BatchNorm

In[ ]:=
```
netECA13 = netSevenCC512drop[128, 128]
```

Out[ ]=
```
NetChain[ Input port: image
          Output port: class
          Number of layers: 12 ]
```

In[ ]:=
```
NetInformation[netECA13, "MXNetNodeGraphPlot"]
```

Out[ ]=



In[ ]:=
```
NetInformation[netECA13, "SummaryGraphic"]
```

Out[ ]=

In[ ]:=
```
dataECA13 = dataC[128, 128, 8192];
```

In[ ]:=
```
dataTotalistic2BigC13 = genData2r2C[128, 128, 1024];
```

In[ ]:=
```
dataTotalistic3BigC13 = data3T2C[128, 128, 1024];
```

In[ ]:=
```
dataTotalistic4BigC13 = data4TC[128, 128, 1024];
```

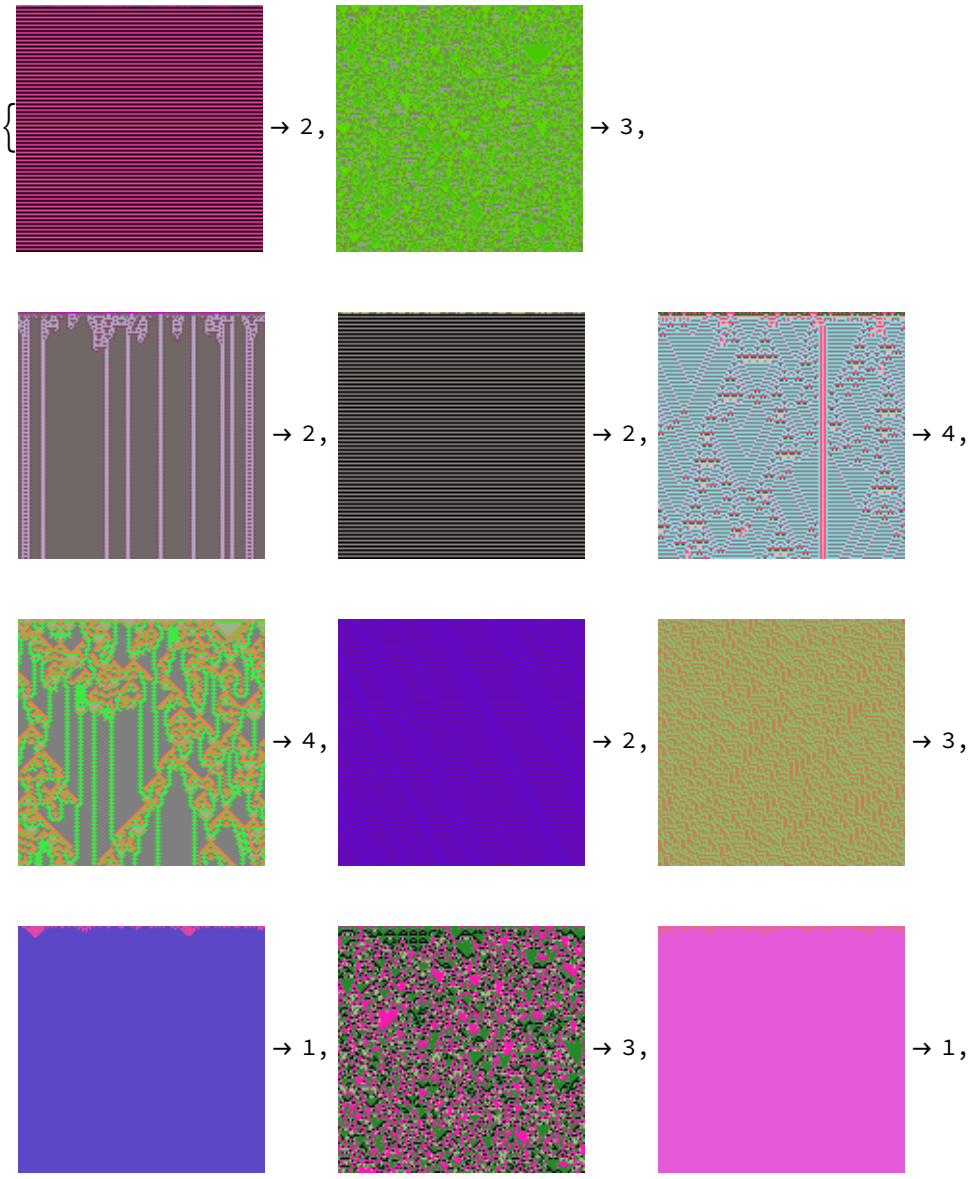
In[ ]:=
```
dataTotalistic5BigC13 = genData5TCC[128, 128, 4096];
```

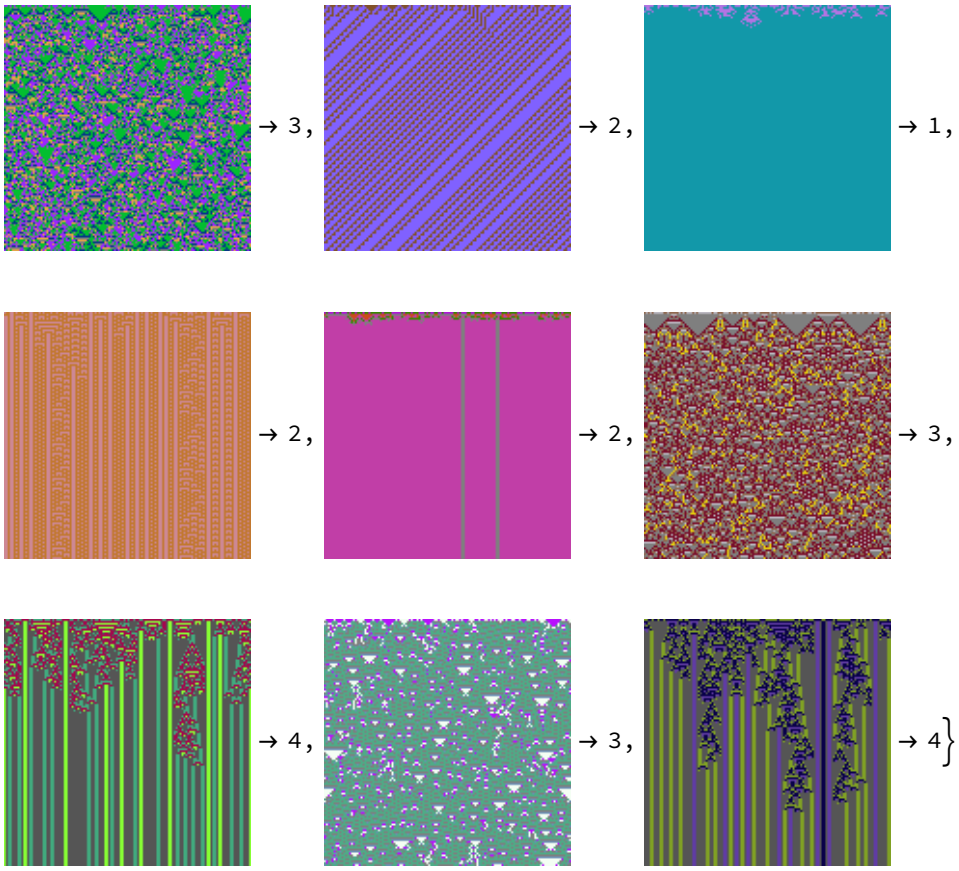
In[ ]:=
```
fullTrainingBigC13 = Join[dataECA13, dataTotalistic2BigC13,
    dataTotalistic3BigC13, dataTotalistic4BigC13, dataTotalistic5BigC13];
Length[fullTrainingBigC13]
```

Out[ ]= 26 624

In[ ]:=
```
RandomSample[fullTrainingBigC13, 20]
```

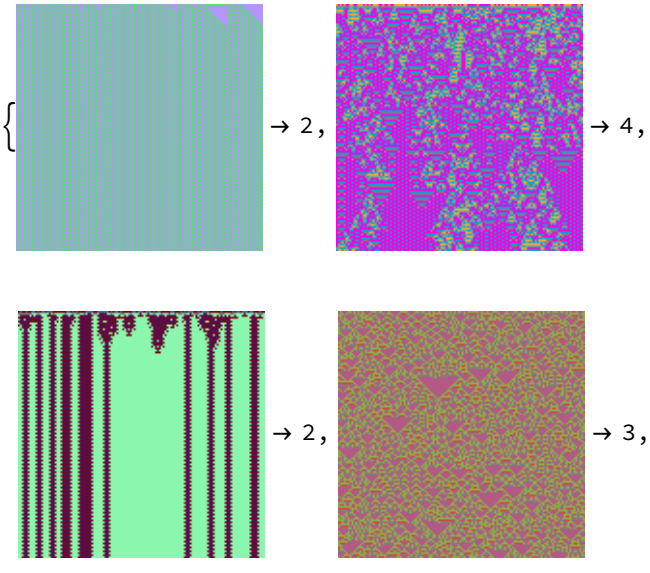
Out[ ]=

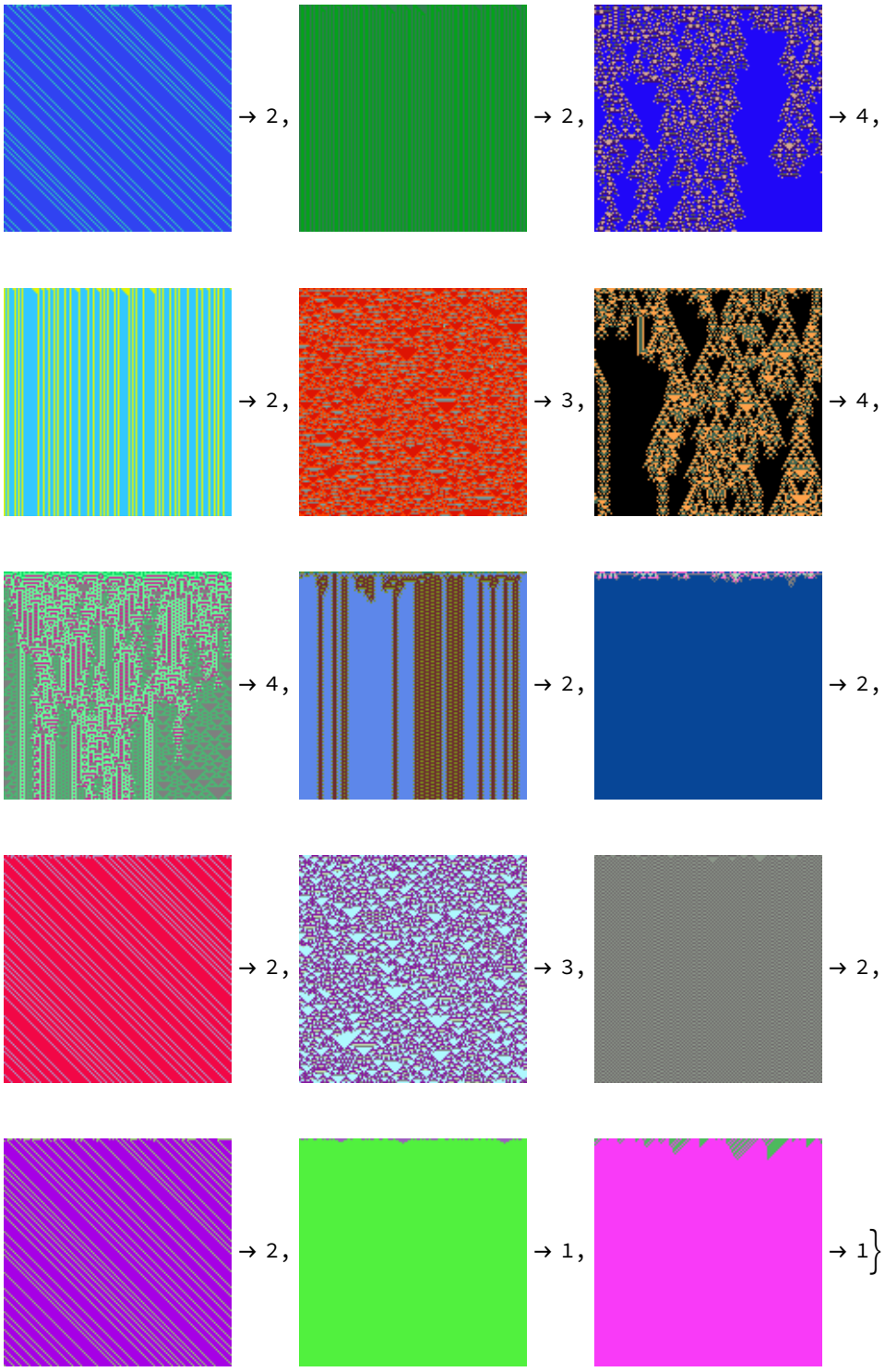




In[ ]:= **RandomSample[fullTrainingBigC13, 20]**

Out[ ]= {

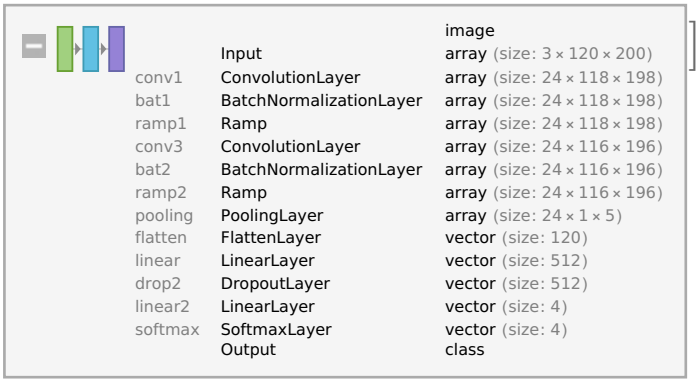




In[ ]:= **dir = SetDirectory[NotebookDirectory[]]**

Out[ ]= /Users/thorsilver/Downloads/Wolfram notebooks

In[ ]:=
```
netECA12 = Import["netECA12-r12.wlnet"]
```

Out[ ]=
```
NetChain[
```


	Input	image array (size: 3 × 120 × 200)
conv1	ConvolutionLayer	array (size: 24 × 118 × 198)
bat1	BatchNormalizationLayer	array (size: 24 × 118 × 198)
ramp1	Ramp	array (size: 24 × 118 × 198)
conv3	ConvolutionLayer	array (size: 24 × 116 × 196)
bat2	BatchNormalizationLayer	array (size: 24 × 116 × 196)
ramp2	Ramp	array (size: 24 × 116 × 196)
pooling	PoolingLayer	array (size: 24 × 1 × 5)
flatten	FlattenLayer	vector (size: 120)
linear	LinearLayer	vector (size: 512)
drop2	DropoutLayer	vector (size: 512)
linear2	LinearLayer	vector (size: 4)
softmax	SoftmaxLayer	vector (size: 4)
	Output	class

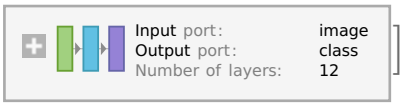
```
]
```

In[ ]:=
```
netECA13 =
  NetTrain[netECA13, fullTrainingBigC13, MaxTrainingRounds → 20, BatchSize → 256 * 4,
   TargetDevice → "CPU", TrainingProgressCheckpointing → {"Directory", dir}]
```

Out[ ]=
```
NetChain[
```

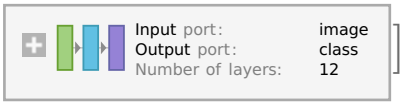

```
Input port:  image
Output port:  class
Number of layers:  12
]
```

In[ ]:=
```
netECA13 = Import["netECA13-r20.wlnet"]
```

Out[ ]=
```
NetChain[
```


```
Input port:  image
Output port:  class
Number of layers:  12
]
```

In[ ]:=
```
netECA13 =
  NetTrain[netECA13, fullTrainingBigC13, MaxTrainingRounds → 20, BatchSize → 256 * 4,
   TargetDevice → "CPU", TrainingProgressCheckpointing → {"Directory", dir}]
```

Out[ ]=
```
NetChain[
```


```
Input port:  image
Output port:  class
Number of layers:  12
]
```

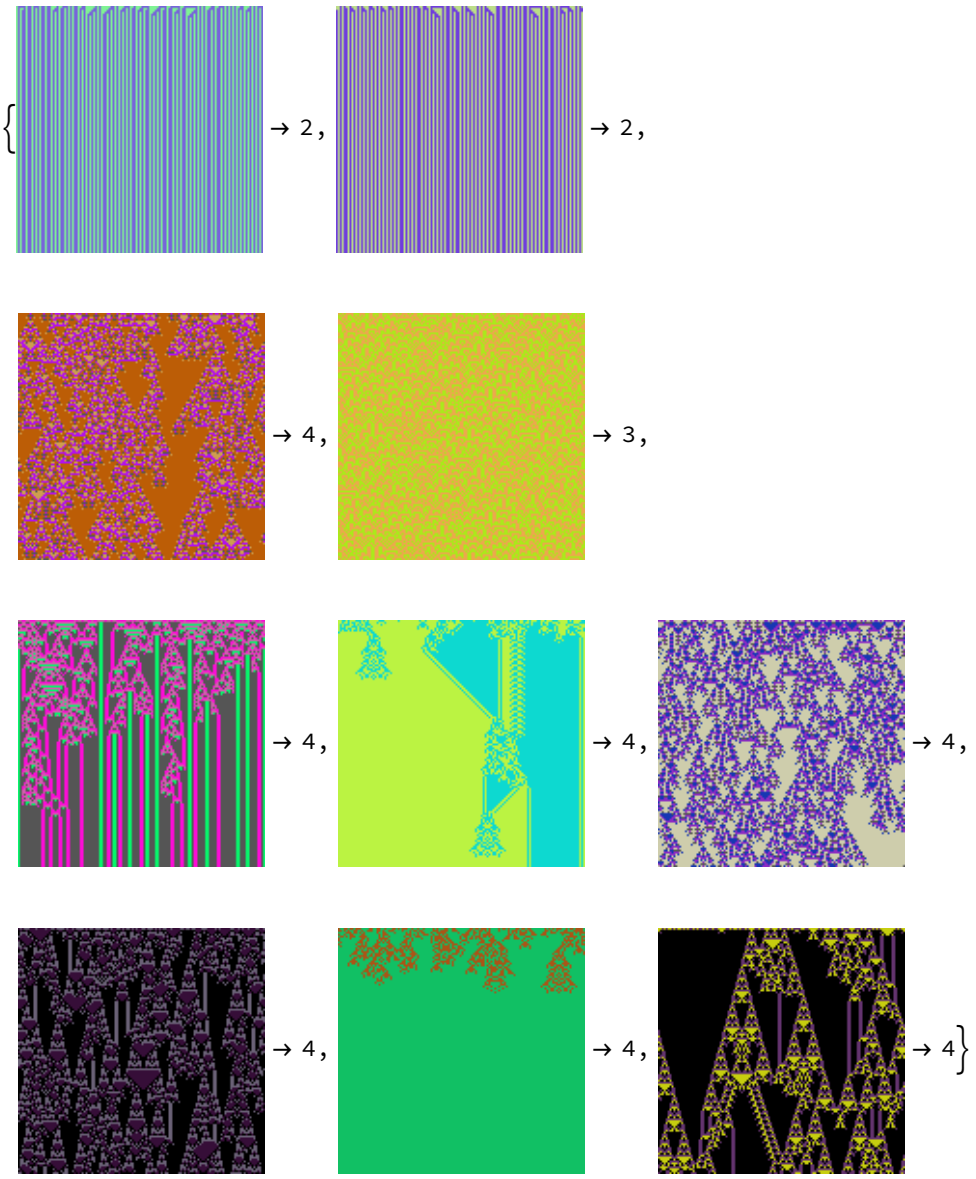
Generate test data for Network XIII

In[ ]:=
```
testDataECABigC = dataC[128, 128, 1024];
testData2TBigC = genData2r2C[128, 128, 1024];
testData3TBigC = data3T2C[128, 128, 1024];
testData4TBigC = data4TC[128, 128, 1024];
testData5TBigC = genData5TCC[128, 128, 1024];
fullTestSetBigC = Join[testDataECABigC,
   testData2TBigC, testData3TBigC, testData4TBigC, testData5TBigC];
Length[fullTestSetBigC]
```

Out[ ]=
```
10 240
```

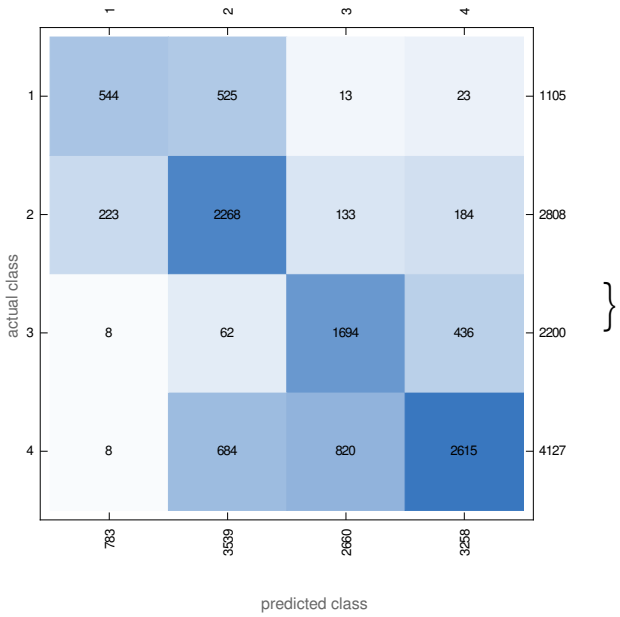
In[ ]:= `RandomSample[fullTestSetBigC, 10]`

Out[ ]=



In[ ]:=
```
NetMeasurements[netECA13, fullTestSetBigC,
 {"Accuracy", "Precision", "ConfusionMatrixPlot"}]
```

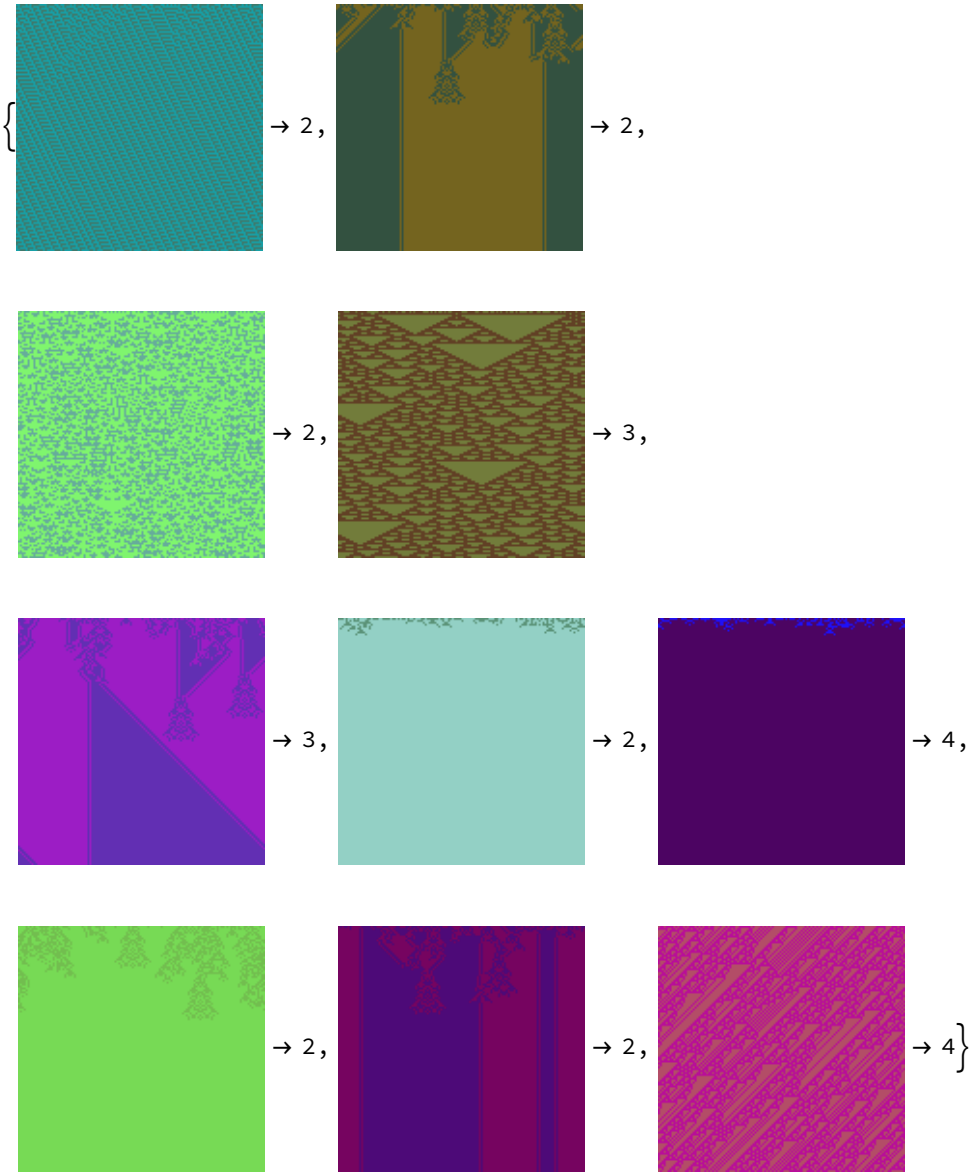
Out[ ]=
```
{0.69541, <|1 → 0.694764, 2 → 0.640859, 3 → 0.636842, 4 → 0.80264|>,
```



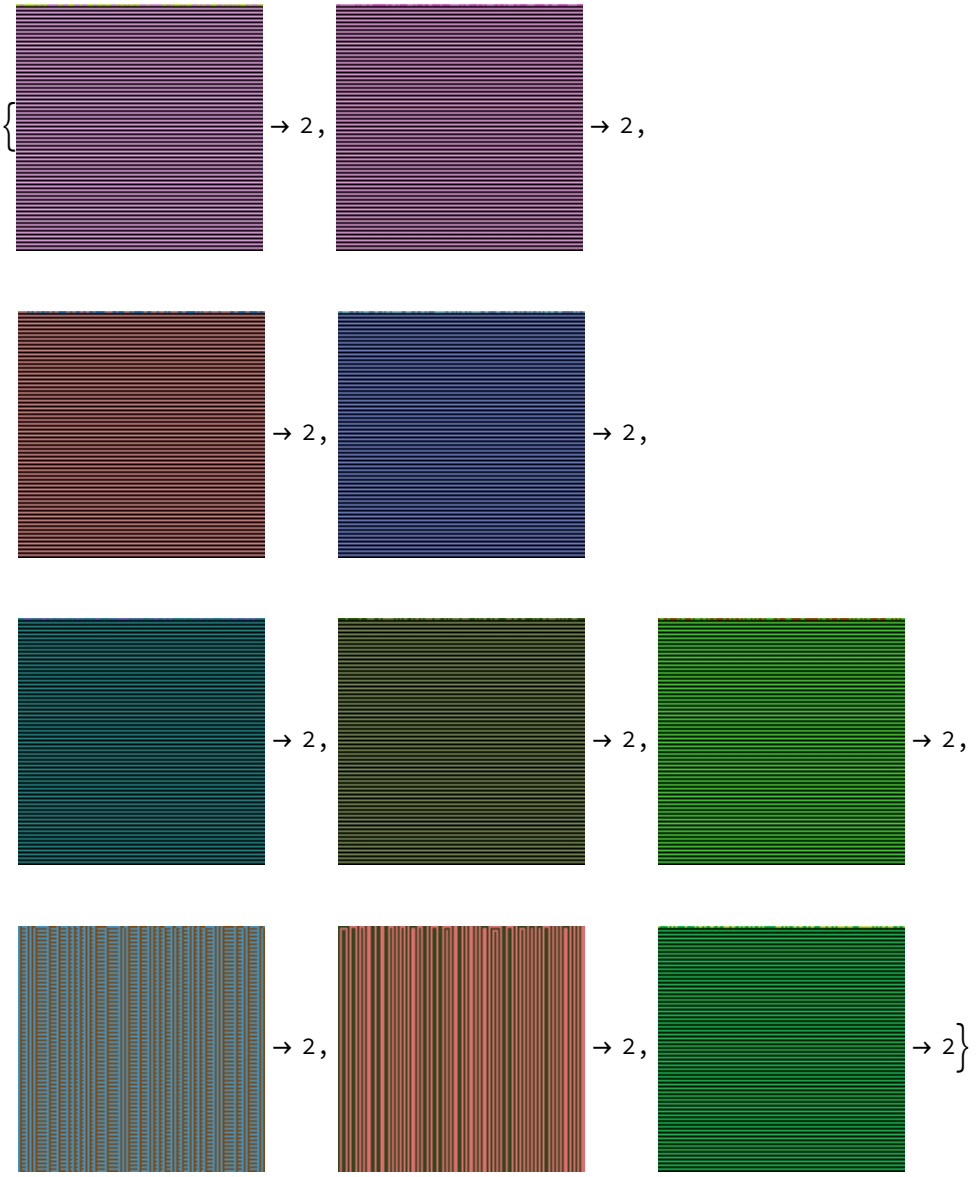

```
}
```

In[ ]:=
```
entropyImagesBigC = RandomSample[Keys[fullTestSetBigC], 500];
entropiesBigC = netECA13[entropyImagesBigC, "Entropy"];
highEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, -10]]];
lowEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, 10]]];
Thread[highEntBigC → netECA13[highEntBigC]]
Thread[lowEntBigC → netECA13[lowEntBigC]]
```

Out[ ]=



Out[ ]=



Network XIV - BatchNorm, 1024 linear, dropout

```
In[ ]:= netECA14 = netEightCC512drop[128, 128]
```

Out[ ]= NetChain

	Input	image array (size: 3 × 128 × 128)
conv1	ConvolutionLayer	array (size: 24 × 126 × 126)
bat1	BatchNormalizationLayer	array (size: 24 × 126 × 126)
ramp1	Ramp	array (size: 24 × 126 × 126)
conv2	ConvolutionLayer	array (size: 16 × 125 × 124)
bat2	BatchNormalizationLayer	array (size: 16 × 125 × 124)
ramp2	Ramp	array (size: 16 × 125 × 124)
conv3	ConvolutionLayer	array (size: 24 × 123 × 122)
bat3	BatchNormalizationLayer	array (size: 24 × 123 × 122)
ramp3	Ramp	array (size: 24 × 123 × 122)
pooling	PoolingLayer	array (size: 24 × 4 × 11)
flatten	FlattenLayer	vector (size: 1056)
linear	LinearLayer	vector (size: 1024)
drop2	DropoutLayer	vector (size: 1024)
linear2	LinearLayer	vector (size: 4)
softmax	SoftmaxLayer	vector (size: 4)
	Output	class

```
netECA14 =
 NetTrain[netECA14, fullTrainingBigC13, MaxTrainingRounds → 20, BatchSize → 256 * 4,
  TargetDevice → "CPU", TrainingProgressCheckpointing → {"Directory", dir}]
```

```
In[ ]:= dir = SetDirectory[NotebookDirectory[]]
```

```
Out[ ]= /Users/thorsilver/Downloads/Wolfram notebooks
```

```
In[ ]:= netECA14 = Import["netECA14-r20.wlnet"]
```

Out[ ]= NetChain

	Input	image array (size: 3 × 128 × 128)
conv1	ConvolutionLayer	array (size: 24 × 126 × 126)
bat1	BatchNormalizationLayer	array (size: 24 × 126 × 126)
ramp1	Ramp	array (size: 24 × 126 × 126)
conv2	ConvolutionLayer	array (size: 16 × 125 × 124)
bat2	BatchNormalizationLayer	array (size: 16 × 125 × 124)
ramp2	Ramp	array (size: 16 × 125 × 124)
conv3	ConvolutionLayer	array (size: 24 × 123 × 122)
bat3	BatchNormalizationLayer	array (size: 24 × 123 × 122)
ramp3	Ramp	array (size: 24 × 123 × 122)
pooling	PoolingLayer	array (size: 24 × 4 × 11)
flatten	FlattenLayer	vector (size: 1056)
linear	LinearLayer	vector (size: 1024)
drop2	DropoutLayer	vector (size: 1024)
linear2	LinearLayer	vector (size: 4)
softmax	SoftmaxLayer	vector (size: 4)
	Output	class

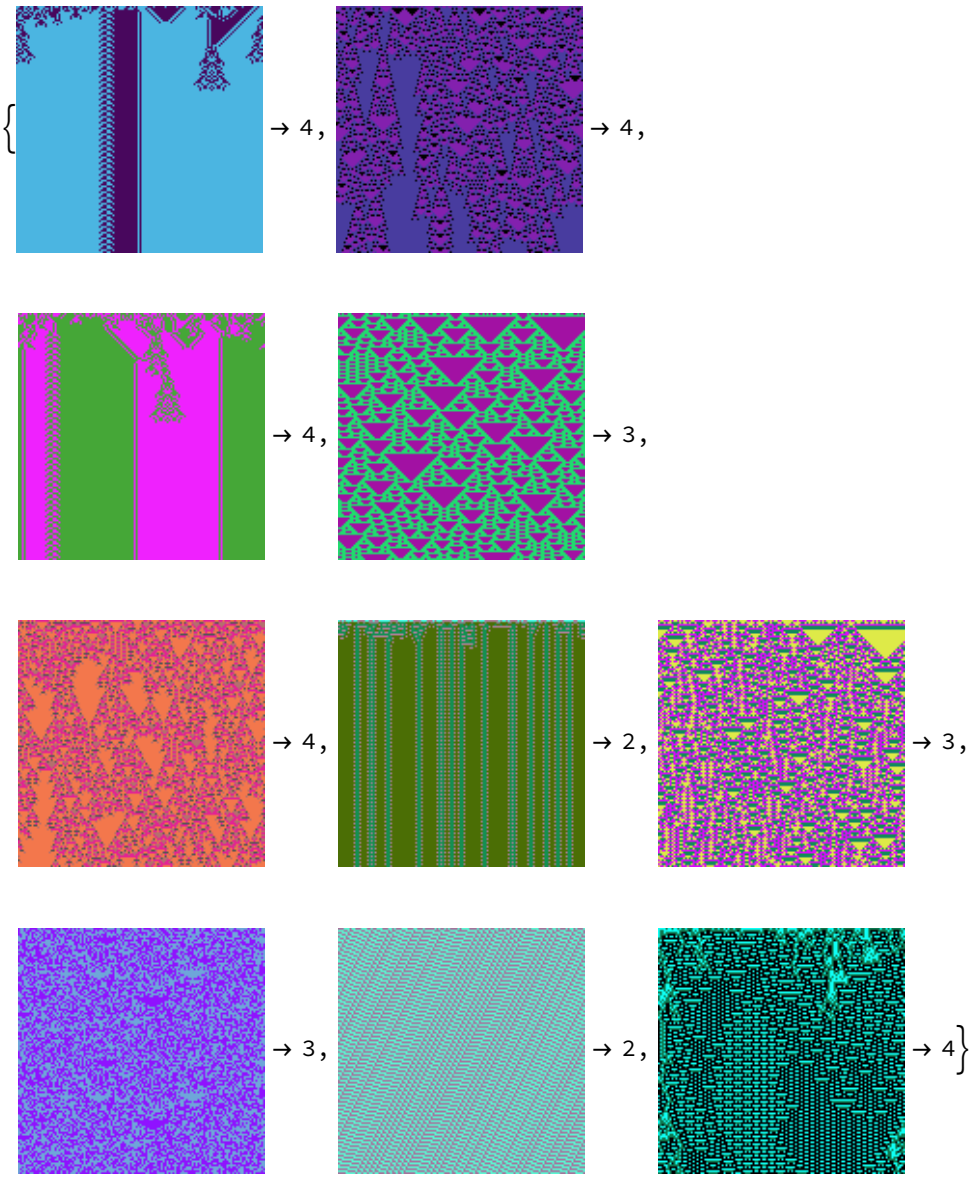
Generating test data for Network XIV

In[ ]:=
```
testDataECABigC = dataC[128, 128, 1024];
testData2TBigC = genData2r2C[128, 128, 1024];
testData3TBigC = data3T2C[128, 128, 1024];
testData4TBigC = data4TC[128, 128, 1024];
testData5TBigC = genData5TCC[128, 128, 1024];
fullTestSetBigC = Join[testDataECABigC,
   testData2TBigC, testData3TBigC, testData4TBigC, testData5TBigC];
Length[fullTestSetBigC]
```

Out[ ]=
```
10 240
```

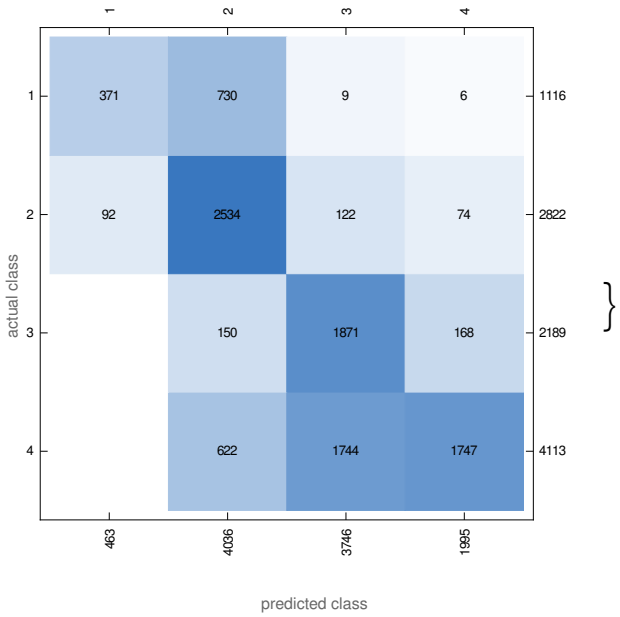
In[ ]:= `RandomSample[fullTestSetBigC, 10]`

Out[ ]=



In[ ]:=
```
NetMeasurements[netECA14, fullTestSetBigC,
 {"Accuracy", "Precision", "ConfusionMatrixPlot"}]
```

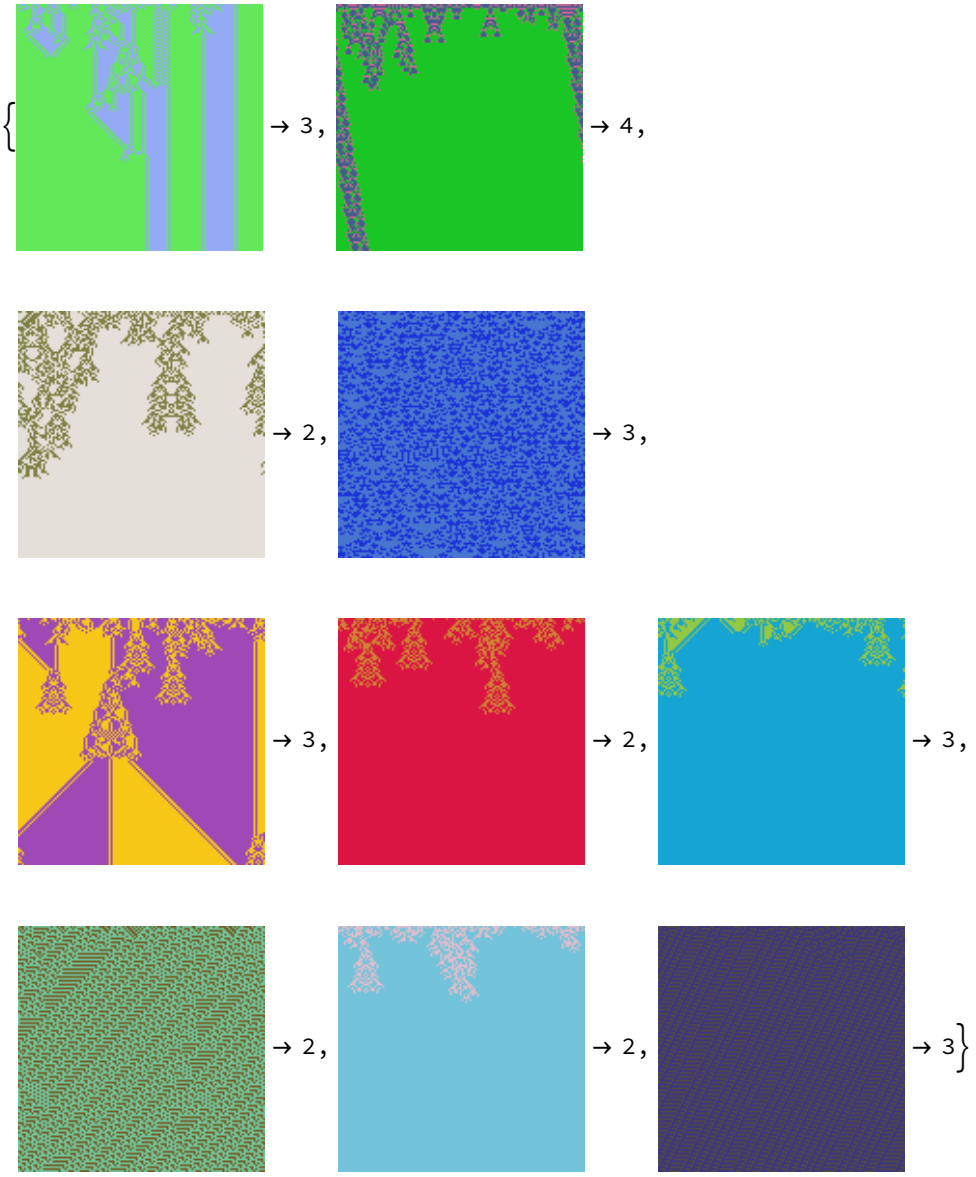
Out[ ]=
```
{0.637012, <|1 → 0.801296, 2 → 0.627849, 3 → 0.499466, 4 → 0.875689|>,
```



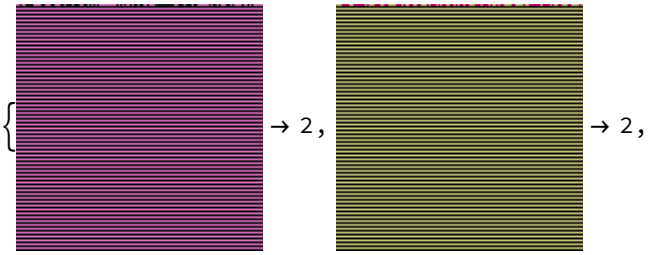

```
}
```

In[ ]:=
```
entropyImagesBigC = RandomSample[Keys[fullTestSetBigC], 500];
entropiesBigC = netECA14[entropyImagesBigC, "Entropy"];
highEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, -10]]];
lowEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, 10]]];
Thread[highEntBigC → netECA14[highEntBigC]]
Thread[lowEntBigC → netECA14[lowEntBigC]]
```

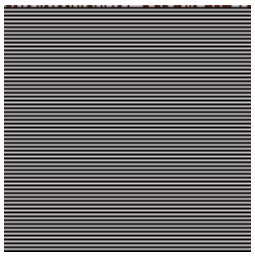
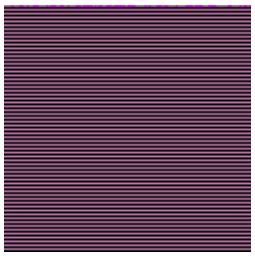
Out[ ]=

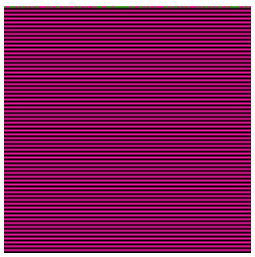


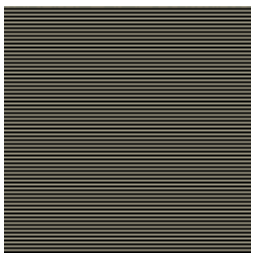
Out[ ]=

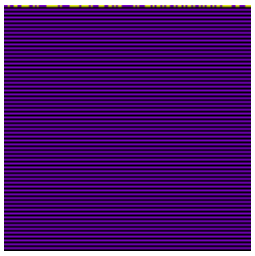

→ 2,

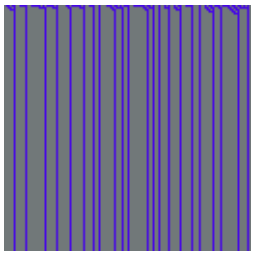
→ 2,


→ 2,

→ 2,


→ 2,

→ 2,

→ 2,


→ 2,

→ 2,

→ 2}

Network XV - Transfer learning with pre-trained image recognition net (VGG-16)

In[ ]:=
```
netECA15 = NetModel["VGG-16 Trained on ImageNet Competition Data"]
```

Out[ ]= NetChain

		image
	Input	array (size: 3 × 224 × 224)
conv1_1	ConvolutionLayer	array (size: 64 × 224 × 224)
relu1_1	Ramp	array (size: 64 × 224 × 224)
conv1_2	ConvolutionLayer	array (size: 64 × 224 × 224)
relu1_2	Ramp	array (size: 64 × 224 × 224)
pool1	PoolingLayer	array (size: 64 × 112 × 112)
conv2_1	ConvolutionLayer	array (size: 128 × 112 × 112)
relu2_1	Ramp	array (size: 128 × 112 × 112)
conv2_2	ConvolutionLayer	array (size: 128 × 112 × 112)
relu2_2	Ramp	array (size: 128 × 112 × 112)
pool2	PoolingLayer	array (size: 128 × 56 × 56)
conv3_1	ConvolutionLayer	array (size: 256 × 56 × 56)
relu3_1	Ramp	array (size: 256 × 56 × 56)
conv3_2	ConvolutionLayer	array (size: 256 × 56 × 56)
relu3_2	Ramp	array (size: 256 × 56 × 56)
conv3_3	ConvolutionLayer	array (size: 256 × 56 × 56)
relu3_3	Ramp	array (size: 256 × 56 × 56)
pool3	PoolingLayer	array (size: 256 × 28 × 28)
conv4_1	ConvolutionLayer	array (size: 512 × 28 × 28)
relu4_1	Ramp	array (size: 512 × 28 × 28)
conv4_2	ConvolutionLayer	array (size: 512 × 28 × 28)
relu4_2	Ramp	array (size: 512 × 28 × 28)
conv4_3	ConvolutionLayer	array (size: 512 × 28 × 28)
relu4_3	Ramp	array (size: 512 × 28 × 28)
pool4	PoolingLayer	array (size: 512 × 14 × 14)
conv5_1	ConvolutionLayer	array (size: 512 × 14 × 14)
relu5_1	Ramp	array (size: 512 × 14 × 14)
conv5_2	ConvolutionLayer	array (size: 512 × 14 × 14)
relu5_2	Ramp	array (size: 512 × 14 × 14)
conv5_3	ConvolutionLayer	array (size: 512 × 14 × 14)
relu5_3	Ramp	array (size: 512 × 14 × 14)
pool5	PoolingLayer	array (size: 512 × 7 × 7)
flatten_0	FlattenLayer	vector (size: 25088)
fc6	LinearLayer	vector (size: 4096)
relu6	Ramp	vector (size: 4096)
drop6	DropoutLayer	vector (size: 4096)
fc7	LinearLayer	vector (size: 4096)
relu7	Ramp	vector (size: 4096)
drop7	DropoutLayer	vector (size: 4096)
fc8	LinearLayer	vector (size: 1000)
prob	SoftmaxLayer	vector (size: 1000)
	Output	class

In[ ]:=
```
subNet = NetTake[netECA15, {"conv1_1", "flatten_0"}]
```

Out[ ]= NetChain

Input port:	image
Output port:	vector (size: 25088)
Number of layers:	32

In[ ]:=
```
joinedNet = NetJoin[subNet,
    NetChain@<|"linear_new" → LinearLayer[1024], "linear_out" → LinearLayer[4],
      "prob" → SoftmaxLayer[]|>, "Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

Out[ ]= NetChain

uninitialized

Input port:	image
Output port:	class
Number of layers:	35

```
In[ ]:= netECA15final = NetPrepend[joinedNet, {"augment" → ImageAugmentationLayer[{224, 224}]},
          "Input" → NetExtract[joinedNet, "Input"]]
```

```
Out[ ]= NetChain[ uninitialized | Input port: image
                                  Output port: class
                                  Number of layers: 36 ]
```

```
In[ ]:= dataECA15 = dataC[224, 224, 8192];
```

```
In[ ]:= dataTotalistic2BigC15 = genData2r2C[224, 224, 1024];
```

```
In[ ]:= dataTotalistic3BigC15 = data3T2C[224, 224, 512];
```

```
In[ ]:= dataTotalistic4BigC15 = data4TC[224, 224, 512];
```

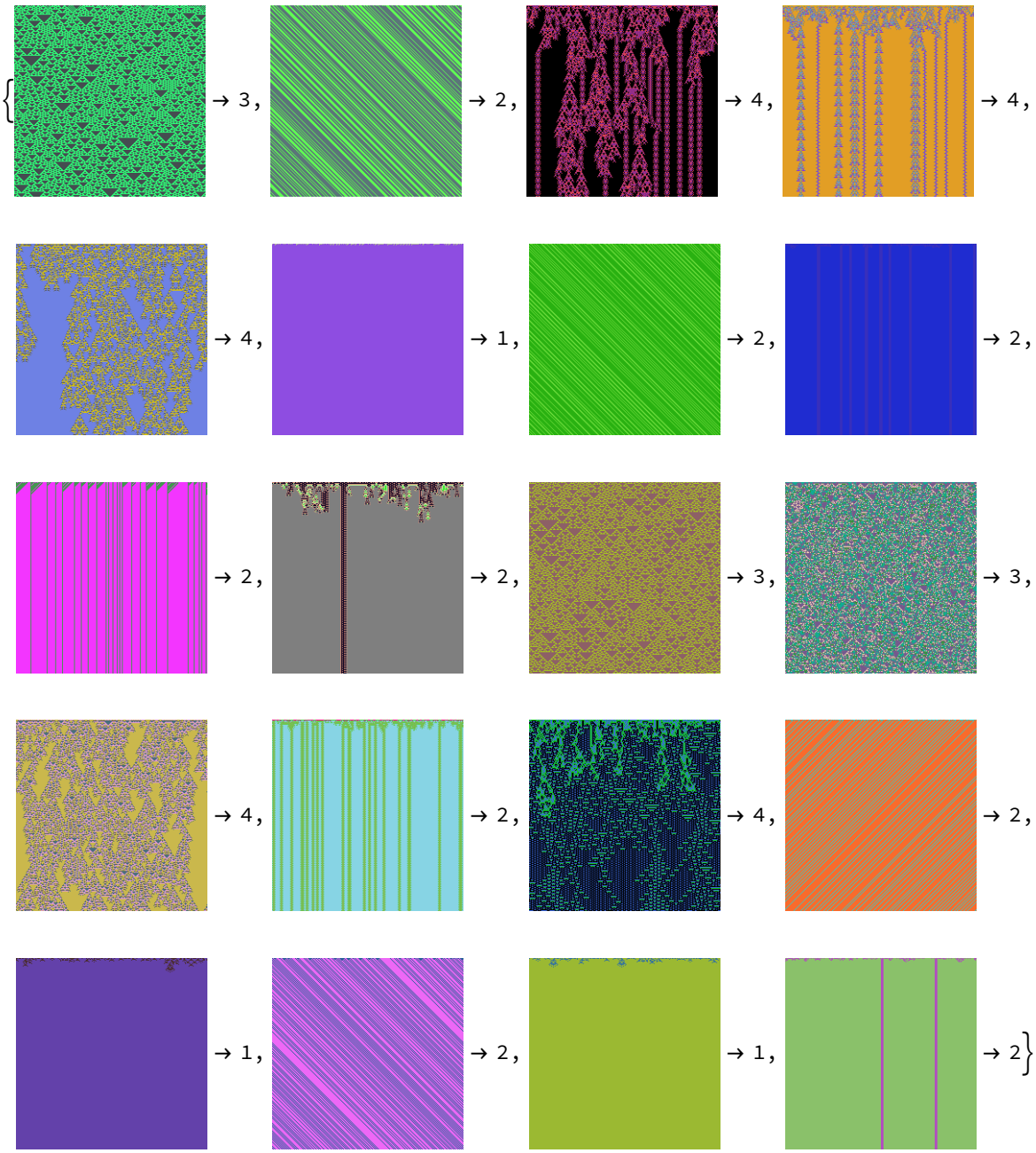
```
In[ ]:= dataTotalistic5BigC15 = genData5TCC[224, 224, 1024];
```

```
In[ ]:= fullTrainingBigC15 = Join[dataECA15, dataTotalistic2BigC15,
           dataTotalistic3BigC15, dataTotalistic4BigC15, dataTotalistic5BigC15];
        Length[fullTrainingBigC15]
```

```
Out[ ]= 16 384
```

In[ ]:=
```
RandomSample[fullTrainingBigC15, 20]
```

Out[ ]=



In[ ]:=
```
netECA15final =
  NetTrain[netECA15final, fullTrainingBigC15, MaxTrainingRounds → 5, BatchSize → 256 * 4,
   TargetDevice → "CPU", TrainingProgressCheckpointing → {"Directory", dir},
   LearningRateMultipliers → {"linear_new" → 1, "linear_out" → 1, _ → 0}]
```

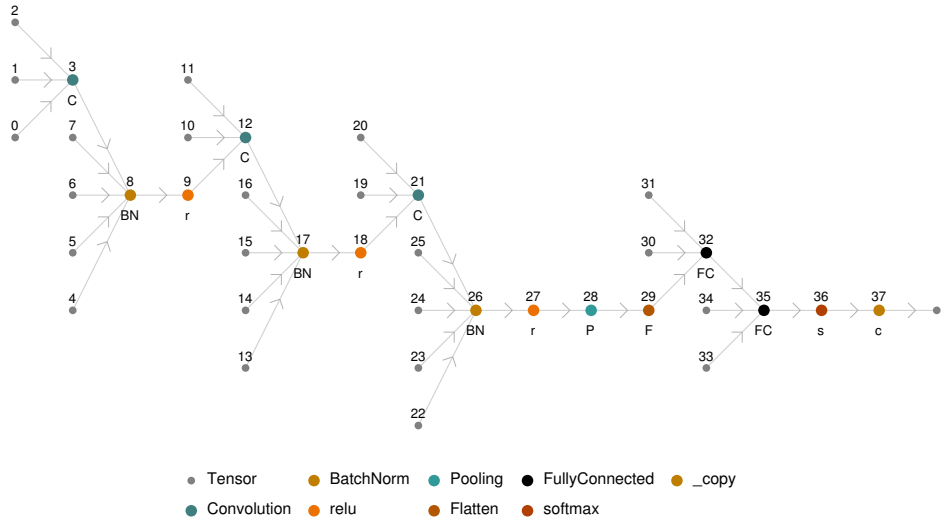
Network XVI - Three convolutions, dropout on linear only, BatchNorm

In[ ]:=
```
netECA16 = netNineCC512drop[128, 128]
```

Out[ ]=
```
NetChain[ Input port:  image
          Output port:  class
          Number of layers:  15 ]
```

In[ ]:=
```
NetInformation[netECA16, "MXNetNodeGraphPlot"]
```

Out[ ]=



In[ ]:=
```
NetInformation[netECA16, "SummaryGraphic"]
```

Out[ ]=

In[ ]:=
```
dataECA16 = dataC[128, 128, 8192];
```

In[ ]:=
```
dataTotalistic2BigC16 = genData2r2C[128, 128, 1024];
```

In[ ]:=
```
dataTotalistic3BigC16 = data3T2C[128, 128, 1024];
```

In[ ]:=
```
dataTotalistic4BigC16 = data4TC[128, 128, 1024];
```

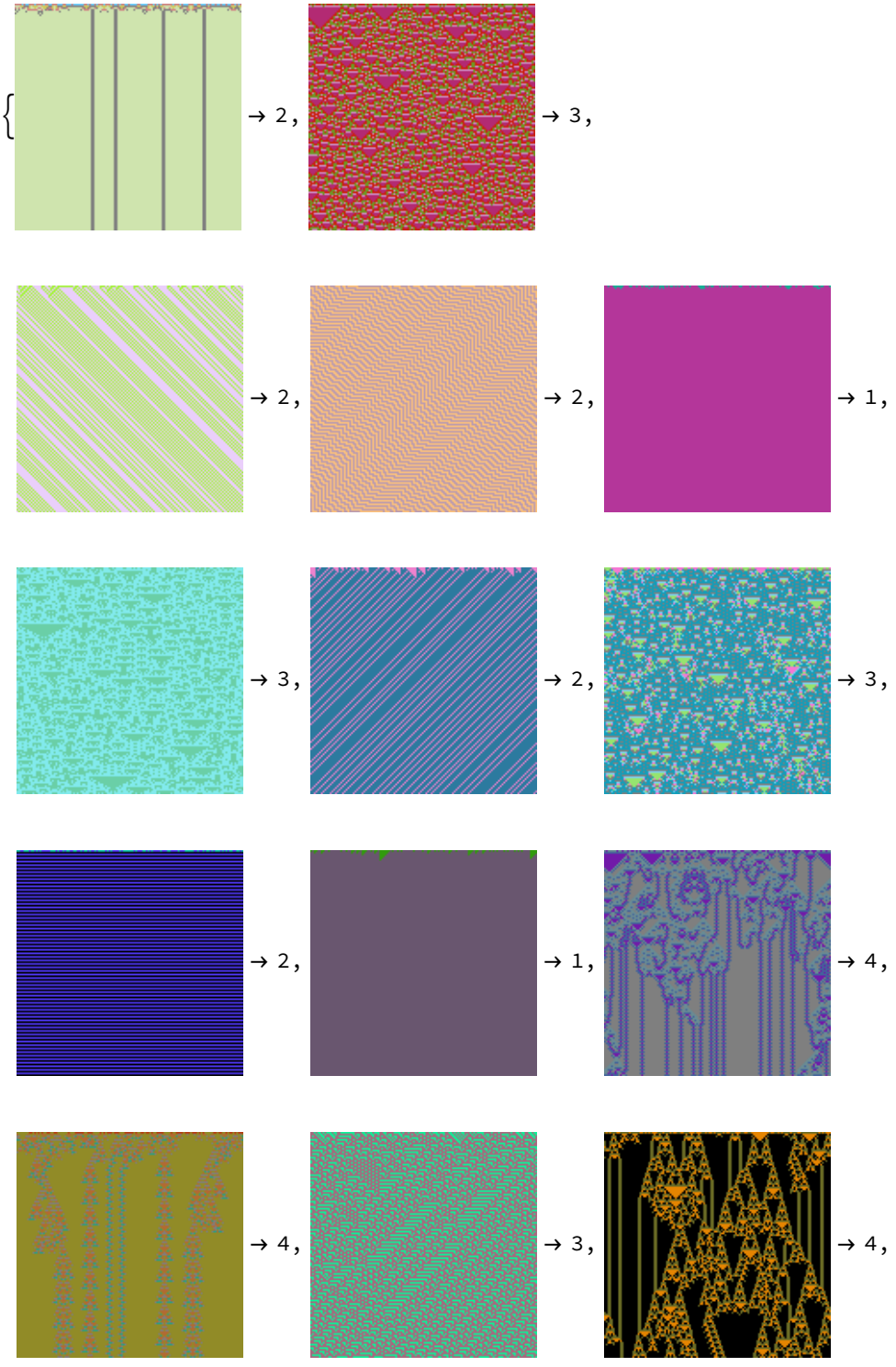
In[ ]:=
```
dataTotalistic5BigC16 = genData5TCC[128, 128, 4096];
```

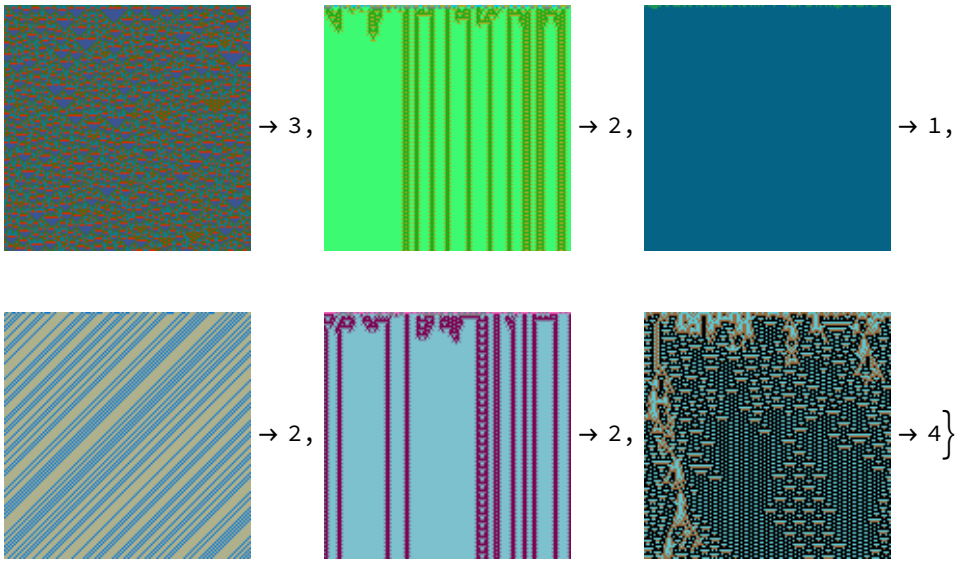
In[ ]:=
```
fullTrainingBigC16 = Join[dataECA16, dataTotalistic2BigC16,
    dataTotalistic3BigC16, dataTotalistic4BigC16, dataTotalistic5BigC16];
Length[fullTrainingBigC16]
```

Out[ ]=
```
26 624
```

In[ ]:=
```
RandomSample[fullTrainingBigC16, 20]
```

Out[ ]=





In[ ]:=
```
dir = SetDirectory[NotebookDirectory[]]
```

Out[ ]= /home/esilverman/Documents

In[ ]:=
```
netECA16 =
 NetTrain[netECA16, fullTrainingBigC16, MaxTrainingRounds → 200, BatchSize → 256,
  TargetDevice → "GPU", TrainingProgressCheckpointing → {"Directory", dir}]
```

Out[ ]= NetChain[Input port: image / Output port: class / Number of layers: 15]

```
netECA16 = Import["netECA16-r20.wlnet"]
```

```
netECA16 =
 NetTrain[netECA16, fullTrainingBigC16, MaxTrainingRounds → 20, BatchSize → 256 * 4,
  TargetDevice → "CPU", TrainingProgressCheckpointing → {"Directory", dir}]
```

Generate test data for Network XVI

In[ ]:=
```
dir = SetDirectory[NotebookDirectory[]]
```

Out[ ]= /Users/thorsilver/Downloads/Wolfram notebooks

In[ ]:=
```
netECA16 = Import["netECA16-r20.wlnet"]
```

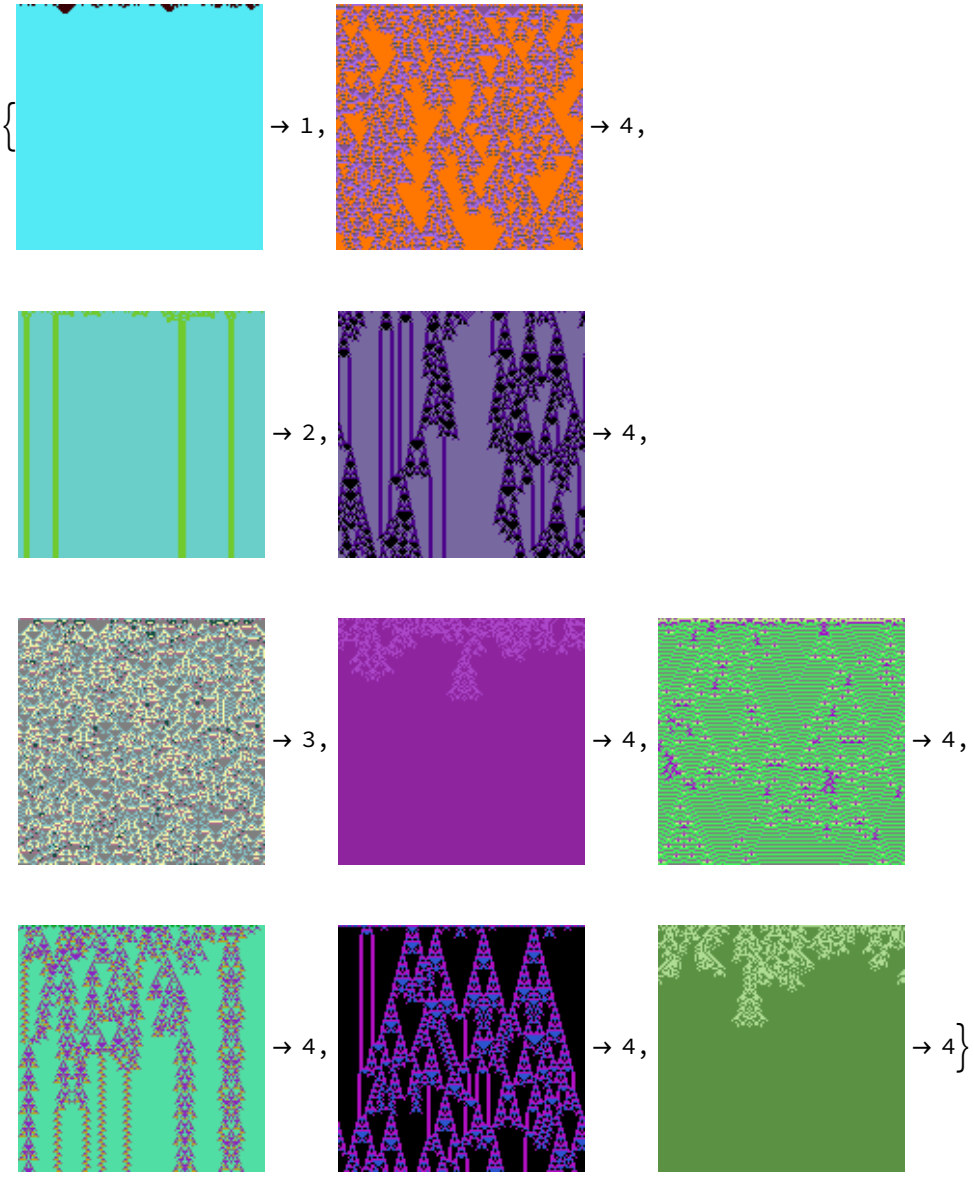
Out[ ]= NetChain[Input port: image / Output port: class / Number of layers: 15]

In[ ]:=
```
testDataECABigC = dataC[128, 128, 1024];
testData2TBigC = genData2r2C[128, 128, 1024];
testData3TBigC = data3T2C[128, 128, 1024];
testData4TBigC = data4TC[128, 128, 1024];
testData5TBigC = genData5TCC[128, 128, 1024];
fullTestSetBigC = Join[testDataECABigC,
   testData2TBigC, testData3TBigC, testData4TBigC, testData5TBigC];
Length[fullTestSetBigC]
```

Out[ ]=
```
10 240
```

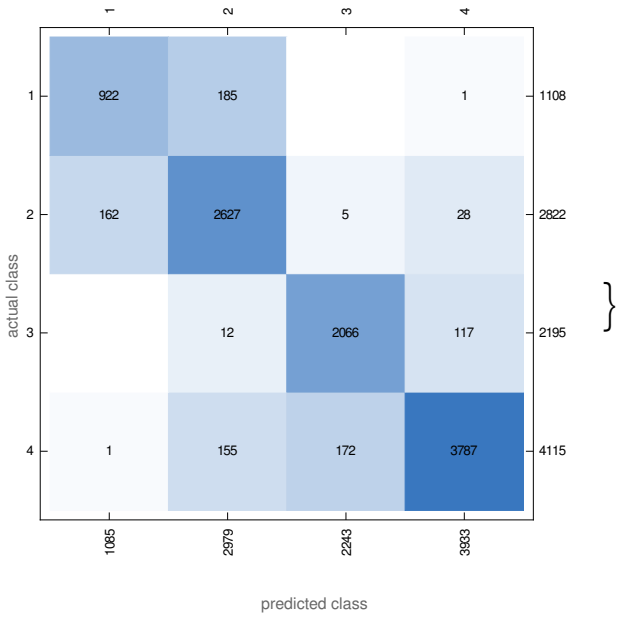
In[ ]:=
```
RandomSample[fullTestSetBigC, 10]
```

Out[ ]=



In[ ]:=
```
NetMeasurements[netECA16, fullTestSetBigC,
 {"Accuracy", "Precision", "ConfusionMatrixPlot"}]
```

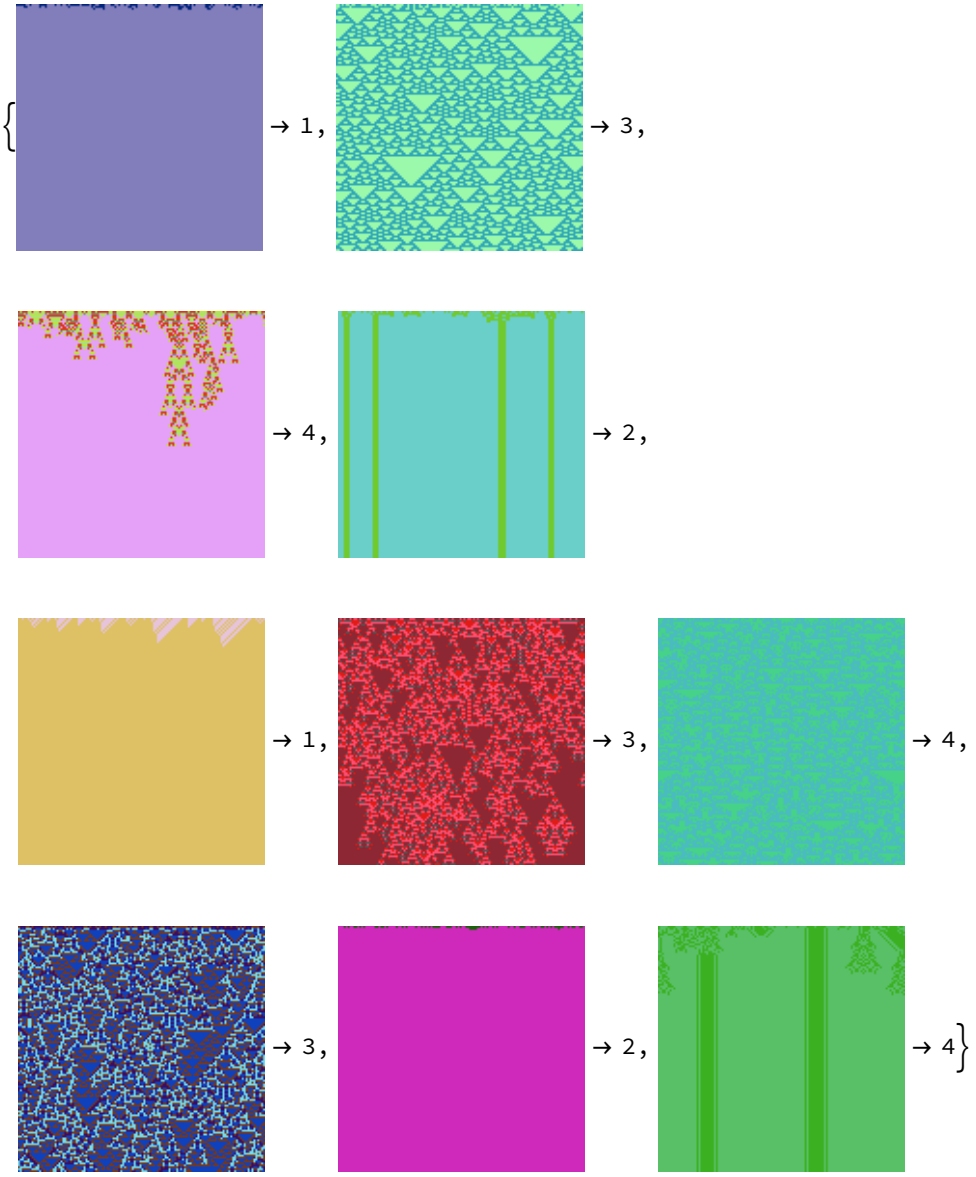
Out[ ]=
```
{0.918164, <|1 → 0.84977, 2 → 0.88184, 3 → 0.921088, 4 → 0.962878|>,
```



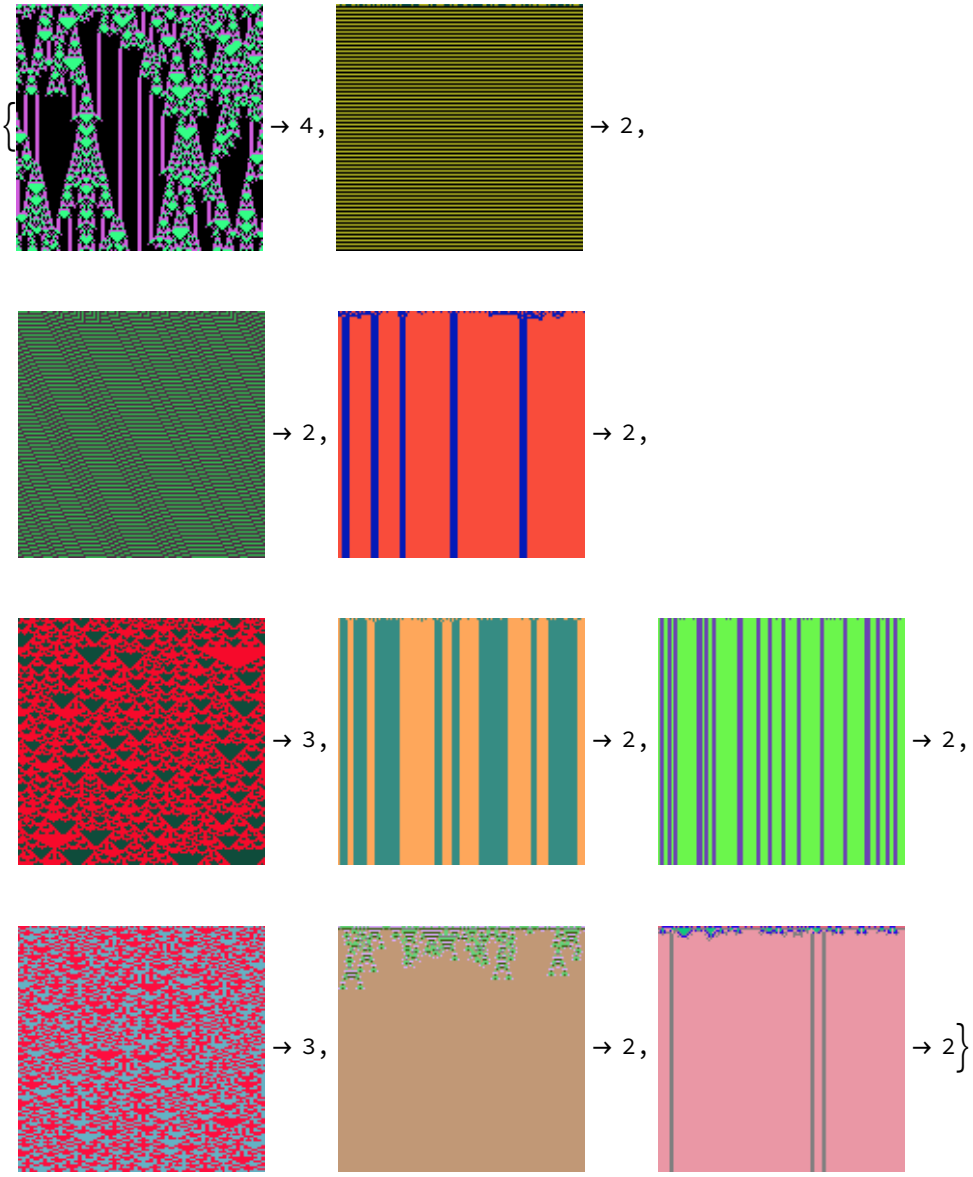

```
}
```

In[ ]:=
```
entropyImagesBigC = RandomSample[Keys[fullTestSetBigC], 500];
entropiesBigC = netECA16[entropyImagesBigC, "Entropy"];
highEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, -10]]];
lowEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, 10]]];
Thread[highEntBigC → netECA16[highEntBigC]]
Thread[lowEntBigC → netECA16[lowEntBigC]]
```

Out[ ]=



Out[ ]=

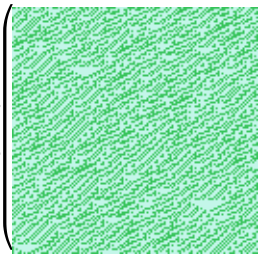


Testing Network XVI on unseen CA rule spaces

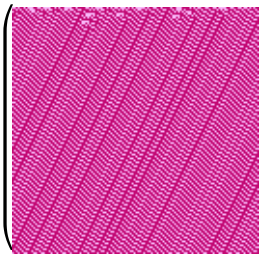
2-colour non-totalistic, range 2

In[ ]:=
```
test4Data2kr2C16 = datak2r2C[128, 128, 8];
Thread[test4Data2kr2C16 → netECA16[Keys@test4Data2kr2C16, {"TopProbabilities", 2}]]
```

Out[ ]=

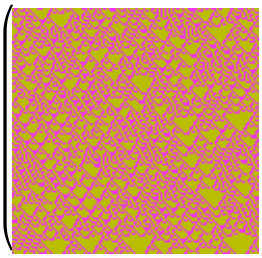


→ 142 978 078 → {4 → 0.0000385332, 3 → 0.999961},

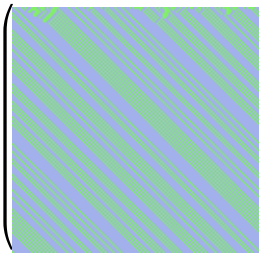


→ 2 651 048 833 → $\{4 \to 8.69455 \times 10^{-12}, 2 \to 1.\}$,

→ 2 132 867 963 → $\{4 \to 2.86202 \times 10^{-17}, 2 \to 1.\}$,

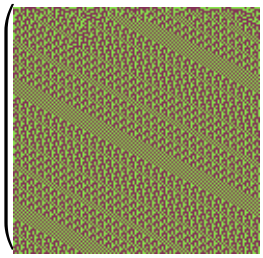


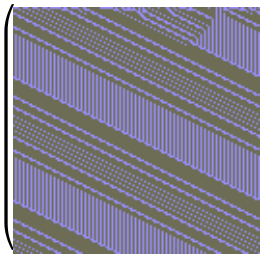
→ 3 644 758 968 → $\{4 \to 6.11899 \times 10^{-7}, 3 \to 0.999999\}$,



→ 1 762 420 096 → $\{1 \to 2.34707 \times 10^{-9}, 2 \to 1.\}$,

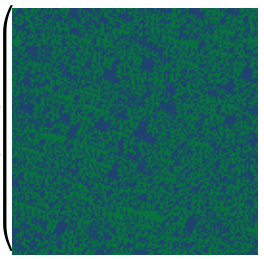

→ 1 983 429 391 → {4 → 0.0547227, 3 → 0.945277},


→ 3 013 553 323 → {3 → 0.0109364, 2 → 0.989064},

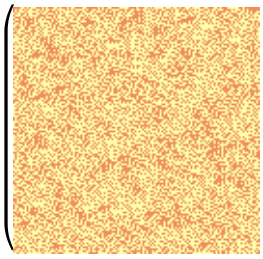

→ 4 222 841 103 → {4 → 0.406794, 3 → 0.593206}}

2-colour non-totalistic, range 3

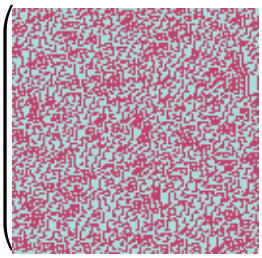
In[ ]:=
```
test4Data2kr3C16 = datak2r3NT[128, 128, 8];
Thread[test4Data2kr3C16 → netECA16[Keys@test4Data2kr3C16, {"TopProbabilities", 2}]]
```

Out[ ]=

→ 326 920 608 662 421 742 840 307 341 423 521 605 984 →

{4 → 0.250823, 3 → 0.749175},

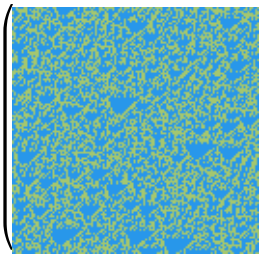

→ 207 378 363 536 986 723 396 466 725 374 349 770 886 →

$\{4 \to 3.99297 \times 10^{-14},\ 3 \to 1.\},$



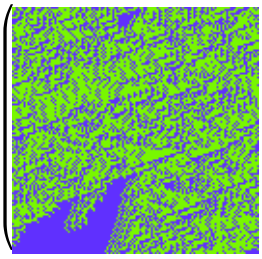
$\to 208\,879\,936\,260\,575\,914\,948\,311\,642\,807\,908\,540\,203 \to$

$\{4 \to 1.58015 \times 10^{-11},\ 3 \to 1.\},$



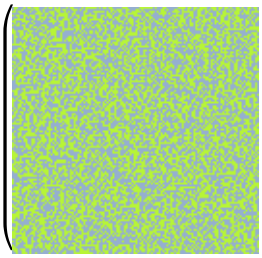
$\to 287\,306\,647\,832\,264\,924\,895\,832\,728\,648\,359\,695\,369 \to$

$\{4 \to 1.21845 \times 10^{-8},\ 3 \to 1.\},$



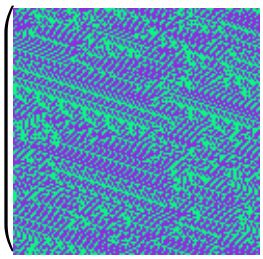
$\to 229\,589\,239\,336\,289\,801\,086\,527\,228\,211\,518\,173\,928 \to$

$\{3 \to 0.0173989,\ 4 \to 0.982601\},$



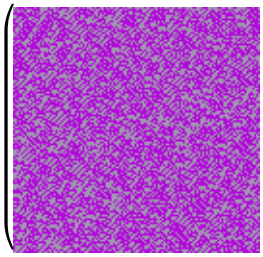
$\to 25\,263\,864\,036\,549\,856\,421\,518\,677\,057\,185\,002\,153 \to$

$\{4 \to 2.486 \times 10^{-11},\ 3 \to 1.\},$



→ 122 573 209 377 430 367 268 072 050 742 932 826 218 →

$\{4 \to 1.46881 \times 10^{-9}, 3 \to 1.\},$



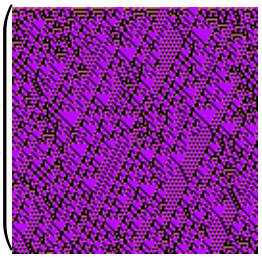
→ 120 291 014 848 530 508 056 036 077 228 147 332 137 →

$\{4 \to 0.00683298, 3 \to 0.993167\}\Big\}$

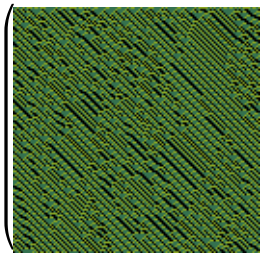
3-colour non-totalistic, range 1

In[ ]:=
```
test4Data3kr1C16 = datak3r1NT[128, 128, 8];
Thread[test4Data3kr1C16 → netECA16[Keys@test4Data3kr1C16, {"TopProbabilities", 2}]]
```

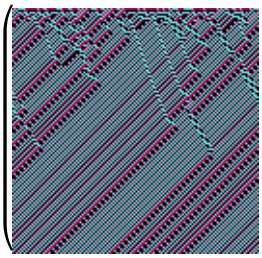
Out[ ]=



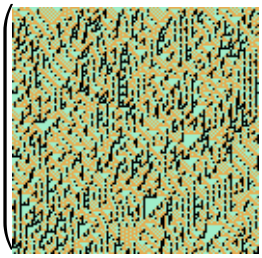
→ 4 431 477 695 805 → {4 → 0.000746188, 3 → 0.999254},



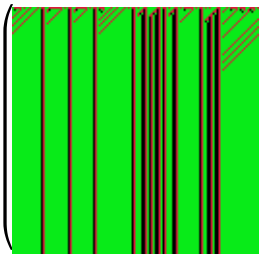
→ 1 627 958 441 874 → {4 → 0.00025369, 3 → 0.999746},



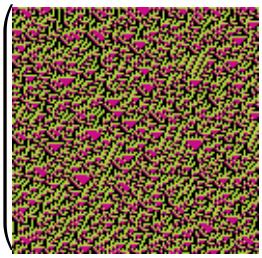
→ 4 241 674 451 024 → {3 → 0.194892, 2 → 0.805108},



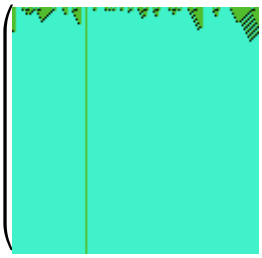
→ 4 177 916 755 057 → $\{3 \to 9.07174 \times 10^{-18}, 4 \to 1.\}$,



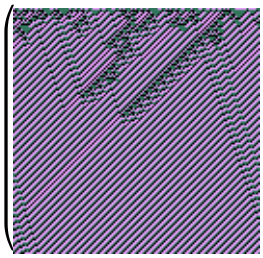
→ 2 504 235 138 103 → $\{4 \to 1.3375 \times 10^{-21}, 2 \to 1.\}$,



→ 2 281 646 033 785 → {4 → 0.164883, 3 → 0.835117},



→ 886 946 817 375 → {2 → 0.000352038, 1 → 0.999648},



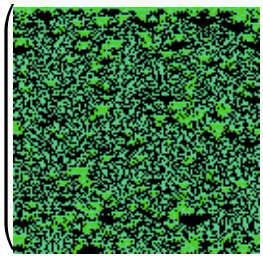
→ 1 468 391 136 669 → {4 → 1.85451 × 10^-11, 2 → 1.}}

3-colour totalistic, range 2

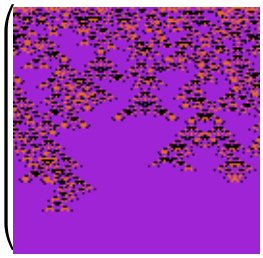
In[ ]:=
```
test4Data3kr2C16 = datak3r2C[128, 128, 8];
Thread[test4Data3kr2C16 → netECA16[Keys@test4Data3kr2C16, {"TopProbabilities", 2}]]
```

Out[ ]=

→ 31 794 → {2 → 0.0000274564, 1 → 0.999973},

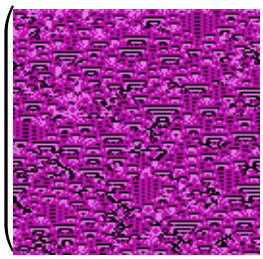


→ 154 722 → {4 → 3.53893 × 10^-6, 3 → 0.999996},



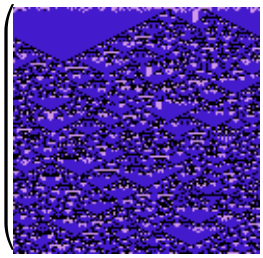
→ 47 093 → {3 → 0.0000226662, 4 → 0.999977},

→ 40 833 → {2 → 7.38958 × 10^-10, 1 → 1.},

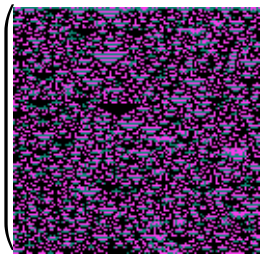


$\to 70\,499 \to \{4 \to 9.14168 \times 10^{-7}, 3 \to 0.999999\},$

$\to 104\,031 \to \{2 \to 0.00469642, 1 \to 0.995304\},$



$\to 102\,416 \to \{4 \to 0.00127827, 3 \to 0.998722\},$

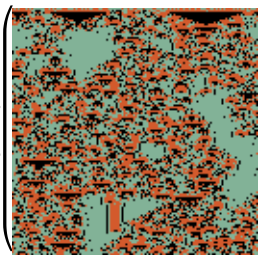


$\to 143\,812 \to \{3 \to 0.00152229, 4 \to 0.998478\}\}$

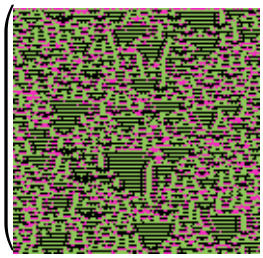
3-colour totalistic, range 3

In[ ]:=
```
test4Data3kr3C16 = datak3r3C[128, 128, 8];
Thread[test4Data3kr3C16 → netECA16[Keys@test4Data3kr3C16, {"TopProbabilities", 2}]]
```

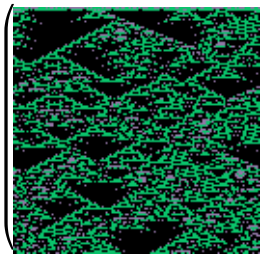
Out[ ]=



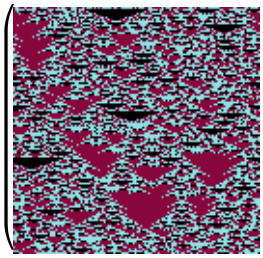
$\{\to 9\,694\,493 \to \{3 \to 0.480724, 4 \to 0.519276\},$



→ 1 266 350 → {3 → 2.07073 × 10^-17, 4 → 1.},

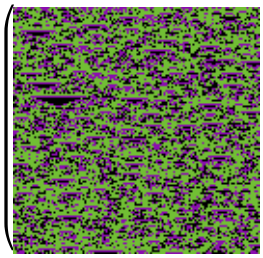


→ 10 922 251 → {4 → 0.0000302967, 3 → 0.99997},

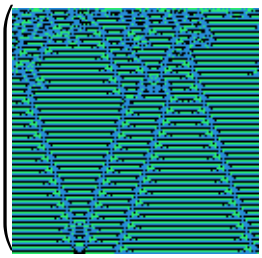


→ 10 284 081 → {4 → 0.0000121386, 3 → 0.999988},

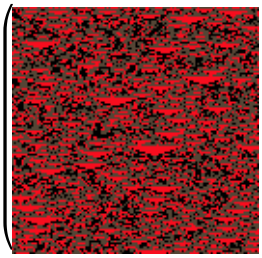
→ 3 664 255 → {1 → 0.0137727, 2 → 0.986227},



→ 10 298 881 → {4 → 0.000133186, 3 → 0.999867},



→ 8 621 297 → {3 → 5.17911 × 10^-10, 4 → 1.},

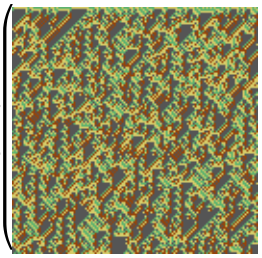


→ 11 392 150 → {4 → 8.14877 × 10^-14, 3 → 1.}}

4-colour non-totalistic, range 1

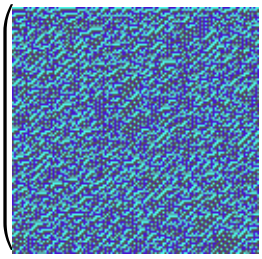
In[ ]:=
```
test4Data4kr1C16 = datak4r1NT[128, 128, 8];
Thread[test4Data4kr1C16 → netECA16[Keys@test4Data4kr1C16, {"TopProbabilities", 2}]]
```

Out[ ]=



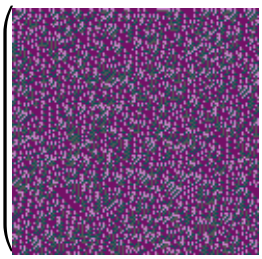
→ 154 080 220 988 097 676 666 997 866 552 654 645 473 →

{3 → 2.29402 × 10^-6, 4 → 0.999998},



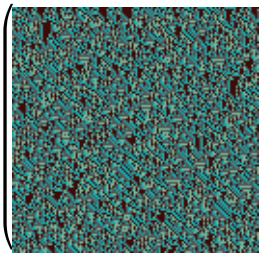
→ 23 699 455 383 307 433 676 732 305 926 546 946 154 →

{4 → 9.18698 × 10^-10, 3 → 1.},



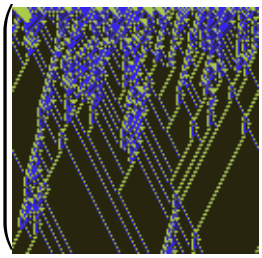
→ 128 473 503 291 830 537 978 738 932 215 015 934 320 →

{4 → 0.016884, 3 → 0.983116},



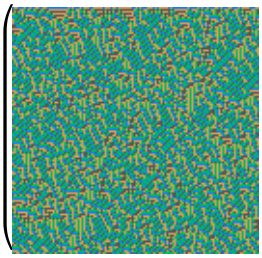
→ 229 632 577 374 973 873 063 824 352 556 638 470 668 →

$\{3 \to 3.66751 \times 10^{-6}, 4 \to 0.999996\}$,



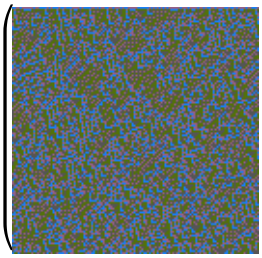
→ 296 751 325 089 499 848 049 286 011 129 052 334 280 →

{2 → 0.0356663, 4 → 0.964334},



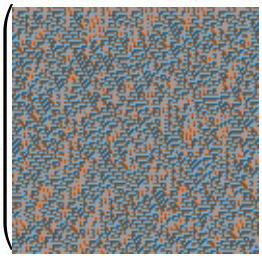
→ 58 389 931 388 288 805 968 545 394 973 250 265 077 →

{4 → 0.392533, 3 → 0.607467},



→ 190 838 234 746 017 730 793 117 442 629 783 928 461 →

{3 → 0.0000369307, 4 → 0.999963},



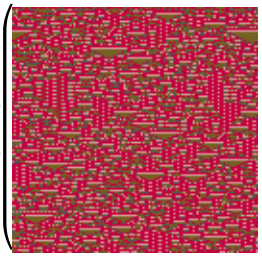
→ 203 920 243 365 735 713 208 234 812 082 196 839 807 →

{4 → 0.00577653, 3 → 0.994223}}

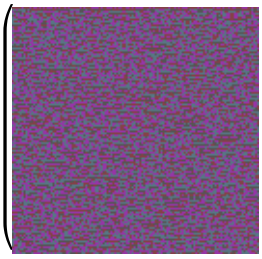
4-colour totalistic, range 2

In[ ]:=
```
test4Data4kr2C16 = datak4r2C[128, 128, 8];
Thread[test4Data4kr2C16 → netECA16[Keys@test4Data4kr2C16, {"TopProbabilities", 2}]]
```

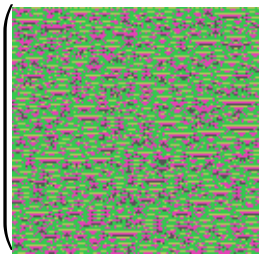
Out[ ]=



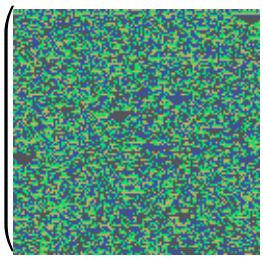
→ 25 517 204 → {4 → 1.29127 × 10^{-13}, 3 → 1.},



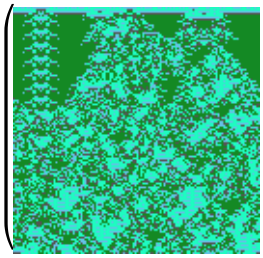
→ 3 053 925 273 → {4 → 0.00215091, 3 → 0.997849},



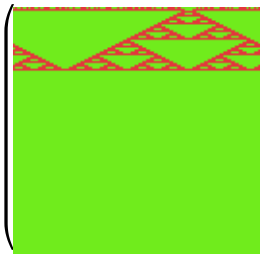
→ 2 735 868 989 → {4 → 0.000282149, 3 → 0.999718},



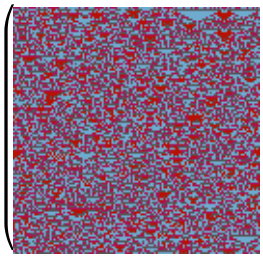
→ 1 440 927 950 → {4 → 0.0889018, 3 → 0.911098},



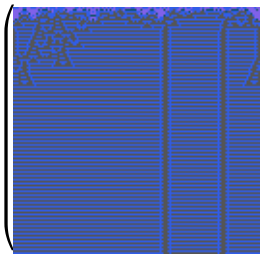
→ 3 727 816 705 → $\{3 \to 2.78599 \times 10^{-7}, 4 \to 1.\}$,



→ 818 963 457 → $\{4 \to 4.45422 \times 10^{-19}, 3 \to 1.\}$,



→ 3 948 742 311 → $\{4 \to 2.06369 \times 10^{-10}, 3 \to 1.\}$,

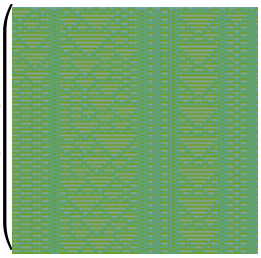


→ 1 159 108 912 → {4 → 0.431018, 2 → 0.568975}}

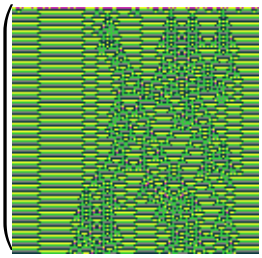
5-colour totalistic, range 1

In[ ]:=
```
test4Data5kr1C16 = data5T2C[8, 128, 128];
Thread[test4Data5kr1C16 → netECA16[Keys@test4Data5kr1C16, {"TopProbabilities", 2}]]
```

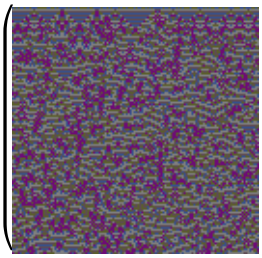
Out[ ]=



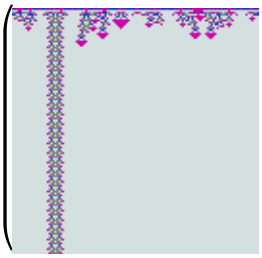
→ 81 353 109 → {4 → 4.44391 × 10^-7, 2 → 1.},



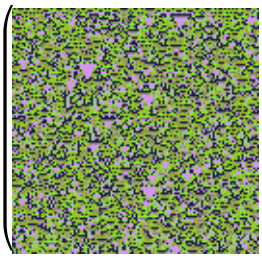
→ 626 536 724 → {3 → 3.46291 × 10^-8, 4 → 1.},



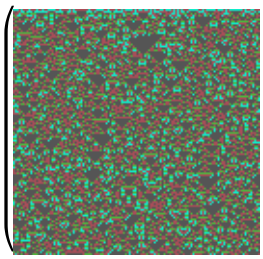
→ 129 595 314 → {4 → 0.00257287, 3 → 0.997427},



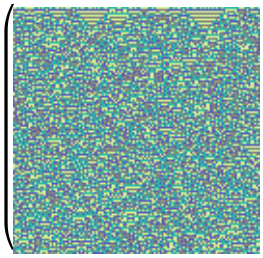
→ 513 885 470 → {1 → 1.41572 × 10^-11, 2 → 1.},



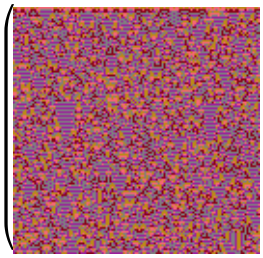
→ 494 894 021 → {3 → 0.0136503, 4 → 0.98635},



→ 459 414 632 → {4 → 0.0000813289, 3 → 0.999919},



→ 327 281 621 → {4 → 2.29489 × 10^−8, 3 → 1.},

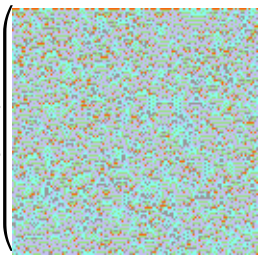


→ 503 044 041 → {4 → 0.191949, 3 → 0.808051}}

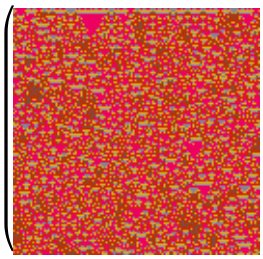
6-colour totalistic, range 1

In[ ]:=
```
test4Data6kr1C16 = data6TC[8, 128, 128];
Thread[test4Data6kr1C16 → netECA16[Keys@test4Data6kr1C16, {"TopProbabilities", 2}]]
```

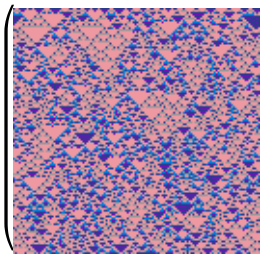
Out[ ]=



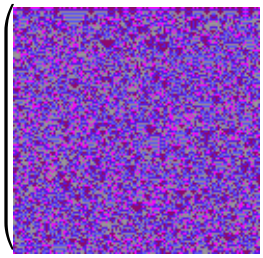
→ 1 522 715 109 251 → {4 → 2.02852 × 10^−8, 3 → 1.},



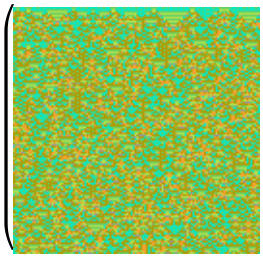
→ 1 026 953 898 330 → {4 → 2.88279 × 10^−8, 3 → 1.},



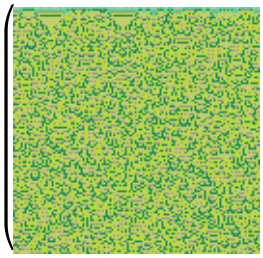
→ 1 583 652 682 → {3 → 0.429972, 4 → 0.570028},



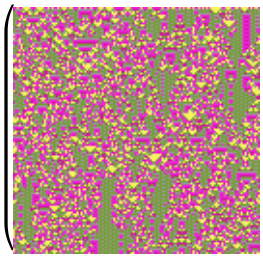
→ 2 123 073 201 165 → $\{4 \to 6.23239 \times 10^{-10}, 3 \to 1.\}$,



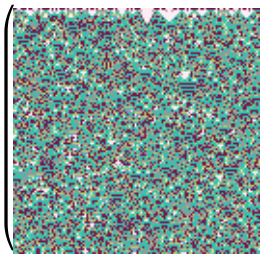
→ 341 591 565 791 → {4 → 0.00212154, 3 → 0.997878},



→ 2 568 539 246 083 → {4 → 0.00197237, 3 → 0.998028},



→ 1 213 730 554 155 → {4 → 0.0020281, 3 → 0.997972},

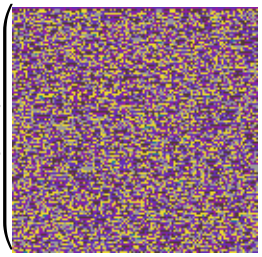


→ 389 841 312 036 → {4 → 2.91693 × 10^-11, 3 → 1.}}

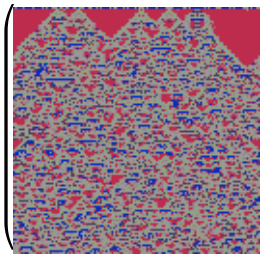
6-colour totalistic, range 2

In[ ]:=
```
test4Data6kr2C16 = data6T2C[8, 128, 128];
Thread[test4Data6kr2C16 → netECA16[Keys@test4Data6kr2C16, {"TopProbabilities", 2}]]
```

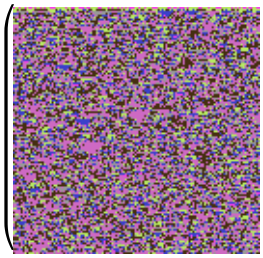
Out[ ]=



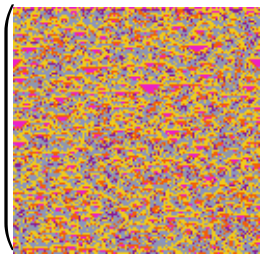
→ 46 177 535 535 728 053 148 → {4 → 6.75757 × 10^-8, 3 → 1.},



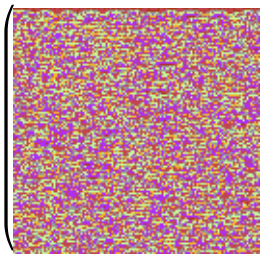
→ 35 643 164 656 729 746 413 → {4 → 4.68349 × 10^-15, 3 → 1.},

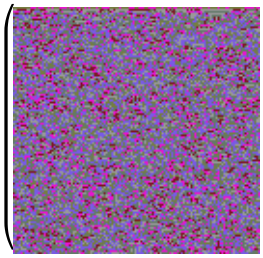


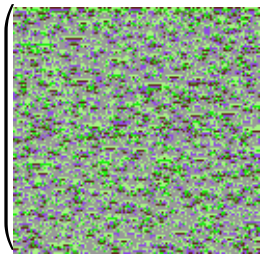
→ 151 294 335 263 255 298 785 → {4 → 0.0673459, 3 → 0.932654},

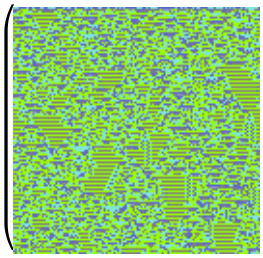


→ 8 803 703 818 914 948 546 → {4 → 0.00560205, 3 → 0.994398},


→ 46 723 275 025 483 150 950 → {4 → 0.00307226, 3 → 0.996928},


→ 72 312 079 279 485 910 528 → {4 → 0.00153324, 3 → 0.998467},

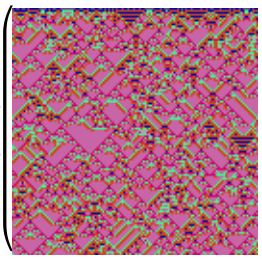

→ 22 158 237 683 799 083 047 → {4 → 3.51784 × 10^-13, 3 → 1.},

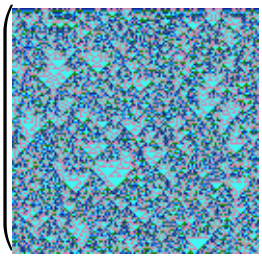

→ 142 446 781 366 136 429 283 → {4 → 3.01302 × 10^-11, 3 → 1.}

7-colour totalistic, range 1

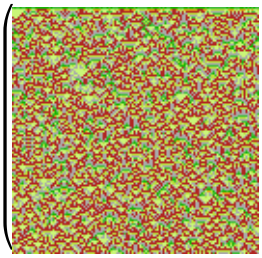
In[ ]:=
```
test4Data7kr1C16 = data7TC[8, 128, 128];
Thread[test4Data7kr1C16 → netECA16[Keys@test4Data7kr1C16, {"TopProbabilities", 2}]]
```

Out[ ]=

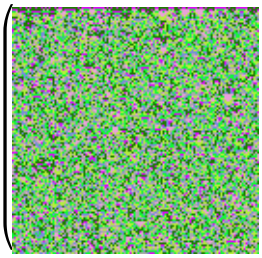

→ 3 109 608 593 887 262 → {2 → 0.0267983, 4 → 0.973202},



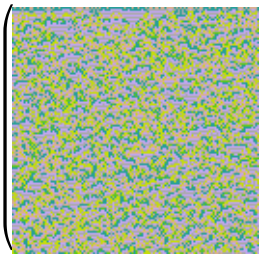
→ 10 516 337 788 191 339 → {4 → 0.202783, 3 → 0.797217},



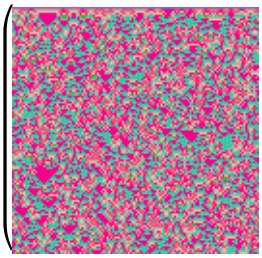
→ 10 218 434 972 470 056 → {4 → 2.59313 × 10^-9, 3 → 1.},



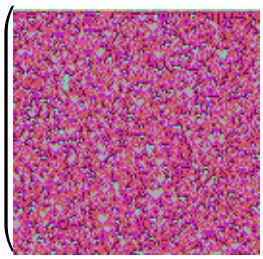
→ 11 301 098 979 433 534 → {4 → 5.31247 × 10^-20, 3 → 1.},



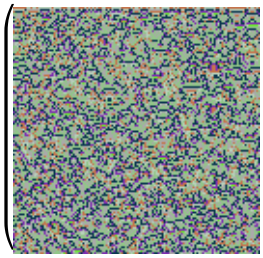
→ 4 222 218 586 098 008 → {4 → 2.3505 × 10^-8, 3 → 1.},



→ 6 272 918 110 265 620 → {4 → 2.82334 × 10^-12, 3 → 1.},



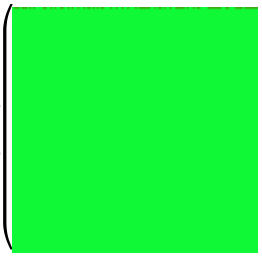
→ 7 237 960 144 206 103 → {4 → 1.82804 × 10^-11, 3 → 1.},



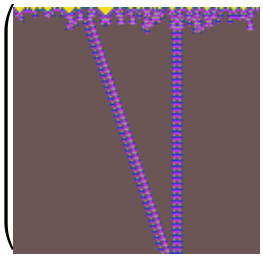
→ 8 157 411 943 012 914 → {4 → 7.30163 × 10^-8, 3 → 1.}}

In[ ]:=
```
test4Data7kr1C16 = data7TC[8, 128, 128];
Thread[test4Data7kr1C16 → netECA16[Keys@test4Data7kr1C16, {"TopProbabilities", 2}]]
```

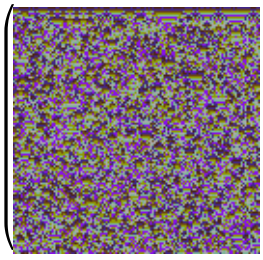
Out[ ]=



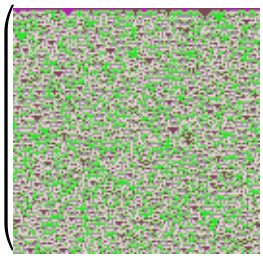
→ 2 054 187 704 193 738 → {2 → 1.00393 × 10^-7, 1 → 1.},



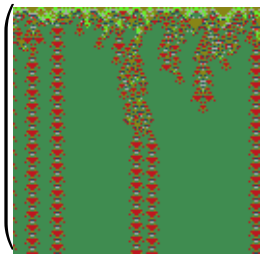
→ 4 502 314 670 347 259 → {1 → 0.000272502, 2 → 0.999727},



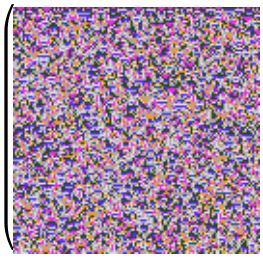
→ 6 433 286 718 439 853 → {4 → 3.57308 × 10^-13, 3 → 1.},



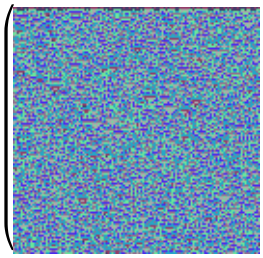
→ 10 115 271 094 201 812 → {4 → 1.83956 × 10^-14, 3 → 1.},



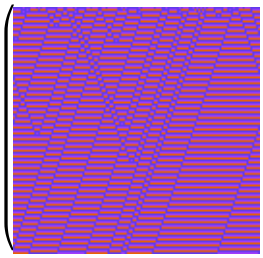
→ 2 056 629 839 849 700 → {4 → 7.03567 × 10^-6, 2 → 0.999993},



→ 6 016 684 767 156 829 → {4 → 0.0021258, 3 → 0.997874},



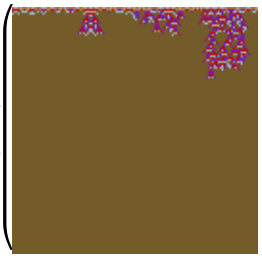
→ 1 150 898 749 617 983 → {4 → 5.05985 × 10^-9, 3 → 1.},



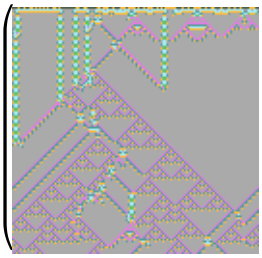
→ 3 441 885 208 643 463 → {3 → 1.57168 × 10^-8, 2 → 1.}}

In[ ]:=
```
test4Data7kr1C16 = data7TC[8, 128, 128];
Thread[test4Data7kr1C16 → netECA16[Keys@test4Data7kr1C16, {"TopProbabilities", 2}]]
```

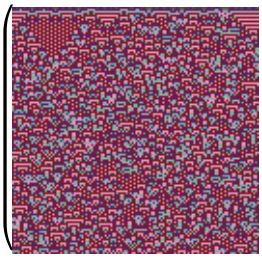
Out[ ]=



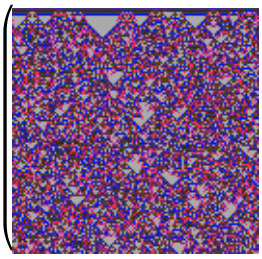
→ 8 718 538 805 570 808 → {4 → 0.0199047, 2 → 0.980095},



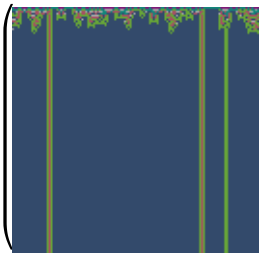
→ 5 687 458 247 703 346 → $\{3 \to 3.931 \times 10^{-6}, 4 \to 0.999995\}$,



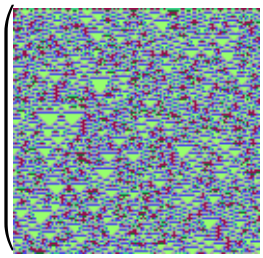
→ 2 004 300 484 518 722 → {3 → 0.0438658, 4 → 0.956134},



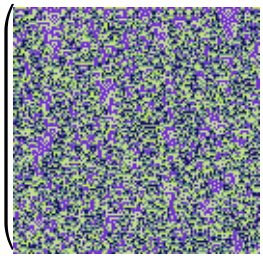
→ 2 106 485 862 858 275 → $\{4 \to 3.36807 \times 10^{-10}, 3 \to 1.\}$,



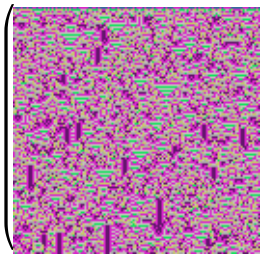
→ 10 335 102 717 390 268 → $\{4 \to 1.40275 \times 10^{-9}, 2 \to 1.\}$,



→ 1 948 304 137 097 478 → {4 → 3.0757 × 10^−6, 3 → 0.999997},



→ 742 855 573 082 935 → {3 → 0.00423487, 4 → 0.995765},

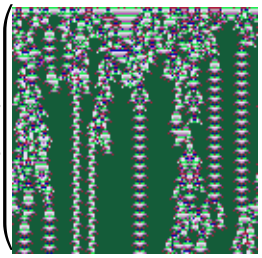


→ 550 991 988 954 034 → {3 → 0.0000158322, 4 → 0.999984}}

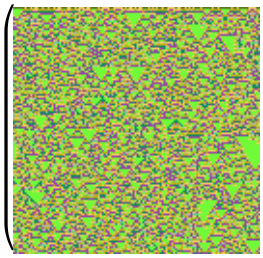
8-colour totalistic, range 1

In[ ]:=
```
test4Data8kr1C16 = data8TC[8, 128, 128];
Thread[test4Data8kr1C16 → netECA16[Keys@test4Data8kr1C16, {"TopProbabilities", 2}]]
```

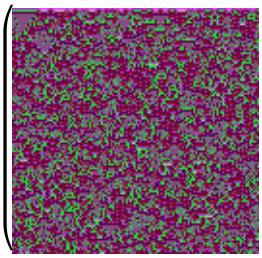
Out[ ]=



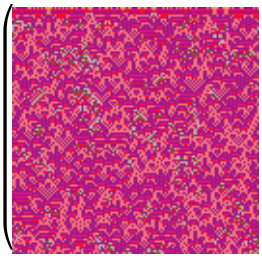
{→ 26 660 220 729 300 317 631 → {3 → 4.53753 × 10^−16, 4 → 1.},



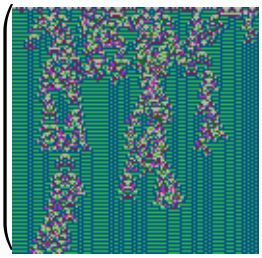
→ 57 706 619 077 455 169 987 → {4 → 0.00012086, 3 → 0.999879},



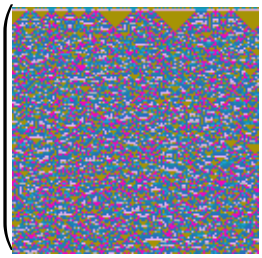
→ 64 248 301 738 433 598 883 → {4 → 8.62498 × 10^-7, 3 → 0.999999},



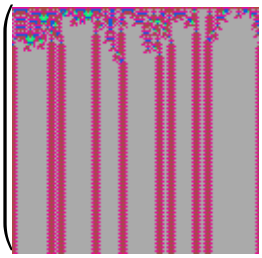
→ 38 309 191 234 358 472 181 → {3 → 0.0920227, 4 → 0.907977},



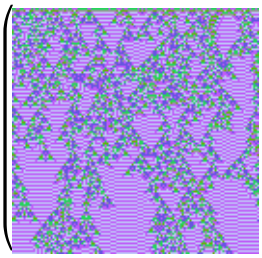
→ 10 057 418 236 647 939 786 → {3 → 0.00153869, 4 → 0.998461},



→ 55 038 816 396 722 824 044 → {4 → 7.93818 × 10^-11, 3 → 1.},



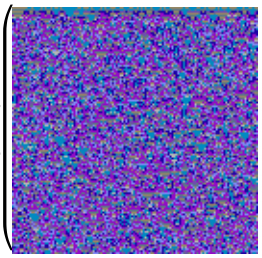
→ 13 857 790 822 319 662 750 → {4 → 1.6375 × 10^-9, 2 → 1.},



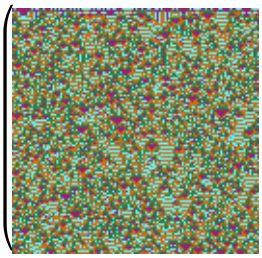
→ 35 001 739 471 058 241 746 → {3 → 0.146189, 4 → 0.853811}

In[ ]:=
```
test4Data8kr1C16 = data8TC[8, 128, 128];
Thread[test4Data8kr1C16 → netECA16[Keys@test4Data8kr1C16, {"TopProbabilities", 2}]]
```

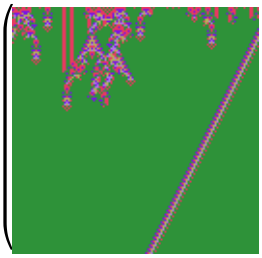
Out[ ]=



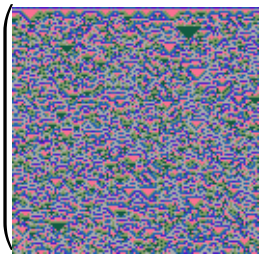
→ 8 889 571 206 431 822 669 → {4 → 7.71651 × 10^-13, 3 → 1.},



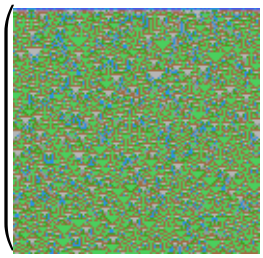
→ 12 932 107 158 159 577 869 → {4 → 0.000487127, 3 → 0.999513},



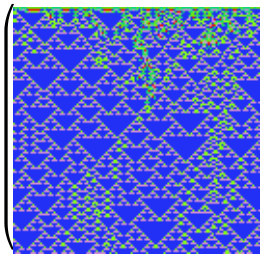
→ 38 300 014 541 797 689 408 → {2 → 4.40131 × 10^-9, 4 → 1.},



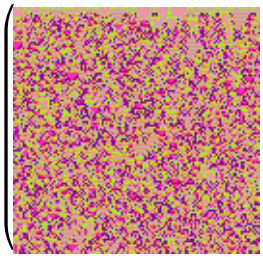
→ 73 619 662 786 582 031 542 → {4 → 2.6954 × 10^-22, 3 → 1.},



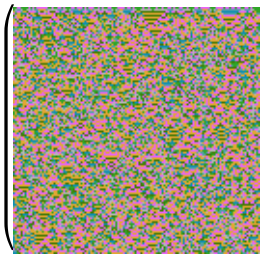
→ 25 075 664 454 379 326 631 → {4 → 2.7484 × 10^−6, 3 → 0.999997},



→ 66 251 301 754 800 867 134 → {4 → 0.045885, 3 → 0.954115},



→ 45 939 929 171 629 412 480 → {3 → 0.0015837, 4 → 0.998416},



→ 48 918 067 825 593 479 863 → {4 → 0.000601606, 3 → 0.999398}}

Network XVII - Four convolutions, dropout on linear only, BatchNorm

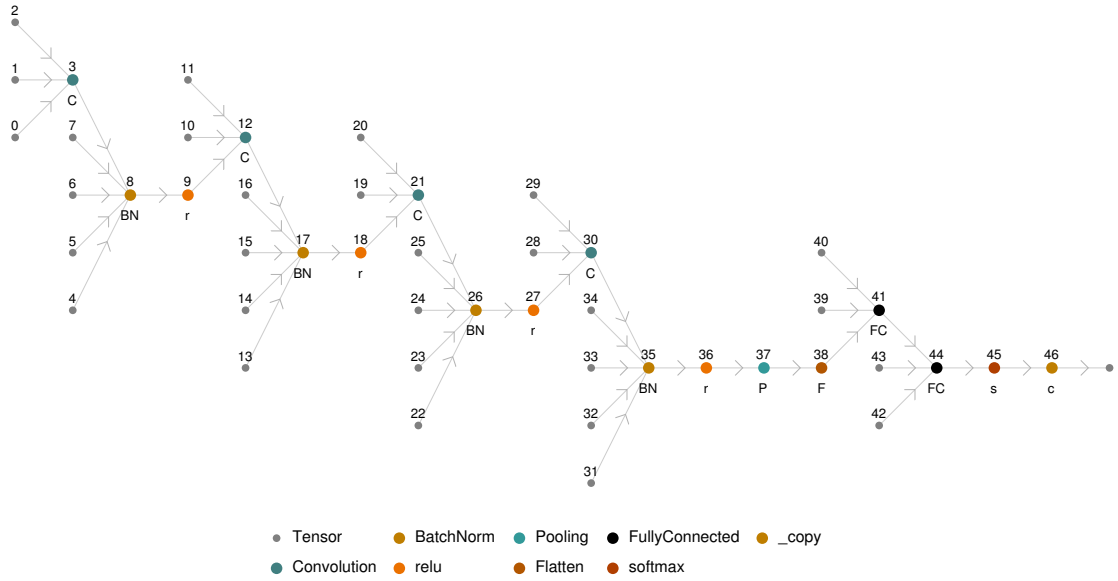
In[ ]:= **netECA17 = netTenCC1024drop[128, 128]**

Out[ ]= NetChain

	Input	image array (size: 3 × 128 × 128)
conv1	ConvolutionLayer	array (size: 24 × 126 × 126)
bat1	BatchNormalizationLayer	array (size: 24 × 126 × 126)
ramp1	Ramp	array (size: 24 × 126 × 126)
conv2	ConvolutionLayer	array (size: 24 × 124 × 124)
bat2	BatchNormalizationLayer	array (size: 24 × 124 × 124)
ramp2	Ramp	array (size: 24 × 124 × 124)
conv3	ConvolutionLayer	array (size: 24 × 122 × 122)
bat3	BatchNormalizationLayer	array (size: 24 × 122 × 122)
ramp3	Ramp	array (size: 24 × 122 × 122)
conv4	ConvolutionLayer	array (size: 24 × 120 × 120)
bat4	BatchNormalizationLayer	array (size: 24 × 120 × 120)
ramp4	Ramp	array (size: 24 × 120 × 120)
pooling	PoolingLayer	array (size: 24 × 5 × 5)
flatten	FlattenLayer	vector (size: 600)
linear	LinearLayer	vector (size: 1024)
drop2	DropoutLayer	vector (size: 1024)
linear2	LinearLayer	vector (size: 4)
softmax	SoftmaxLayer	vector (size: 4)
	Output	class

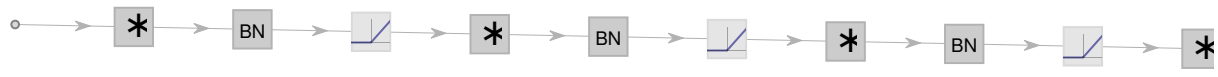
In[ ]:= NetInformation[netECA17, "MXNetNodeGraphPlot"]

Out[ ]=



In[ ]:= NetInformation[netECA17, "SummaryGraphic"]

Out[ ]=



In[ ]:= dataECA17 = dataC[128, 128, 16 384];

In[ ]:= dataTotalistic2BigC17 = genData2r2C[128, 128, 2048];

In[ ]:= dataTotalistic3BigC17 = data3T2C[128, 128, 2048];

In[ ]:= dataTotalistic4BigC17 = data4TC[128, 128, 2048];

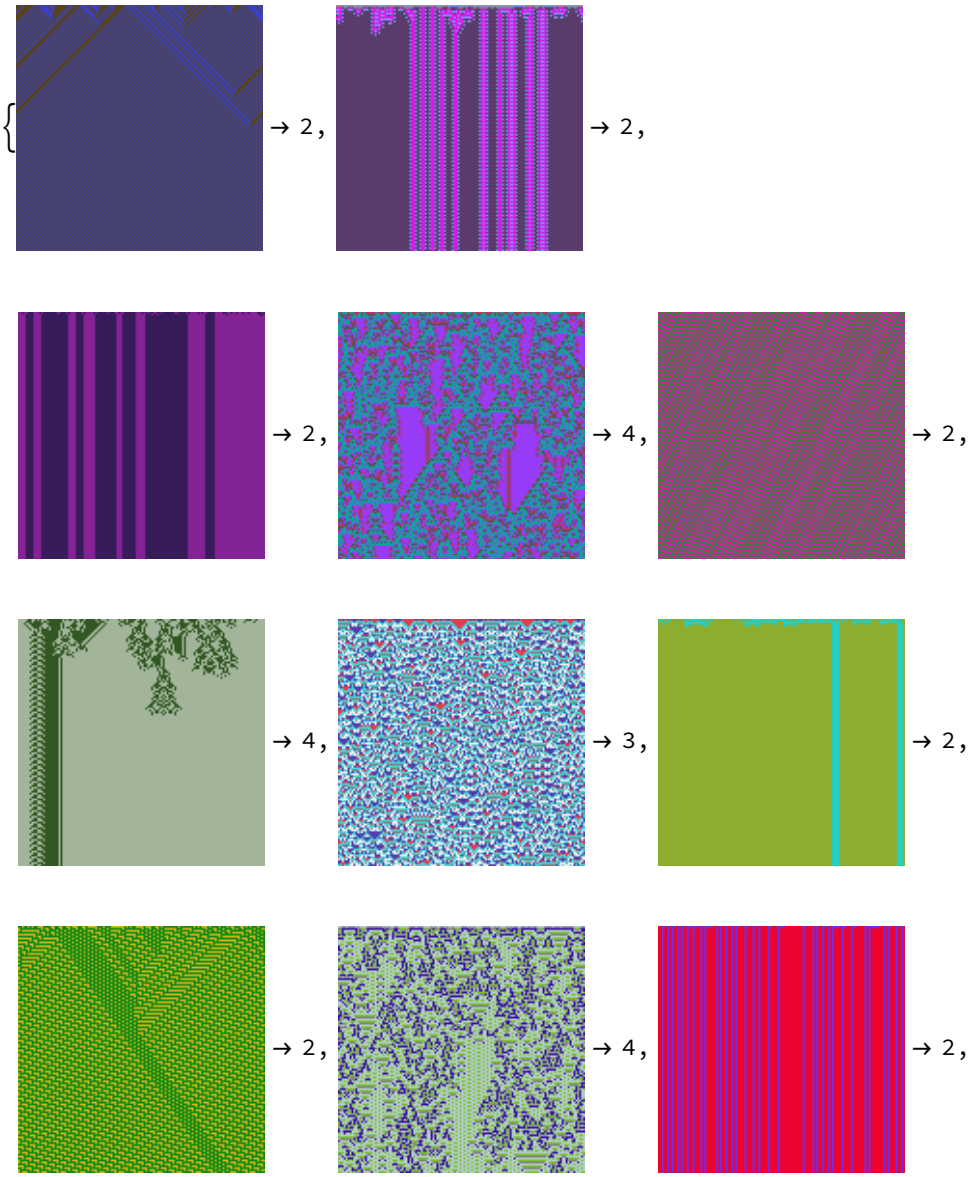
In[ ]:= dataTotalistic5BigC17 = genData5TCC[128, 128, 8192];

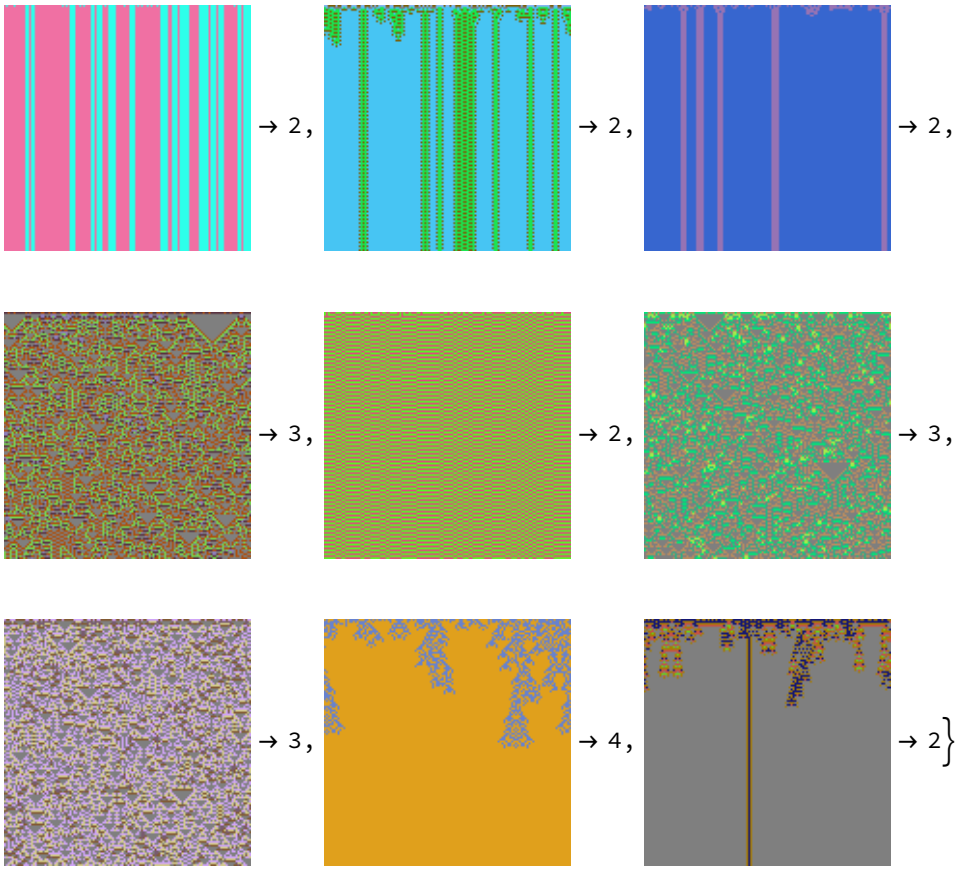
In[ ]:=
```
fullTrainingBigC17 = Join[dataECA17, dataTotalistic2BigC17,
    dataTotalistic3BigC17, dataTotalistic4BigC17, dataTotalistic5BigC17];
Length[fullTrainingBigC17]
```

Out[ ]= 53 248

In[ ]:=
```
RandomSample[fullTrainingBigC17, 20]
```

Out[ ]=





In[ ]:=
```
dir = SetDirectory[NotebookDirectory[]]
```

In[ ]:=
```
"/home/esilverman/Documents"
```

Out[ ]= /home/esilverman/Documents

In[ ]:=
```
netECA17 =
  NetTrain[netECA17, fullTrainingBigC17, MaxTrainingRounds → 200, BatchSize → 256,
   TargetDevice → "GPU", TrainingProgressCheckpointing → {"Directory", dir}]
```

Out[ ]= NetChain[Input port: image
Output port: class
Number of layers: 18]

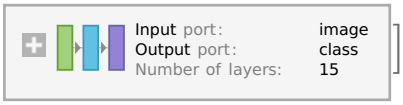
```
netECA17 = Import["netECA17-r200.wlnet"]
```

Generate test data for Network XVII (200 epochs)

In[ ]:=
```
dir = SetDirectory[NotebookDirectory[]]
```

Out[ ]= /Users/thorsilver/Downloads/Wolfram notebooks

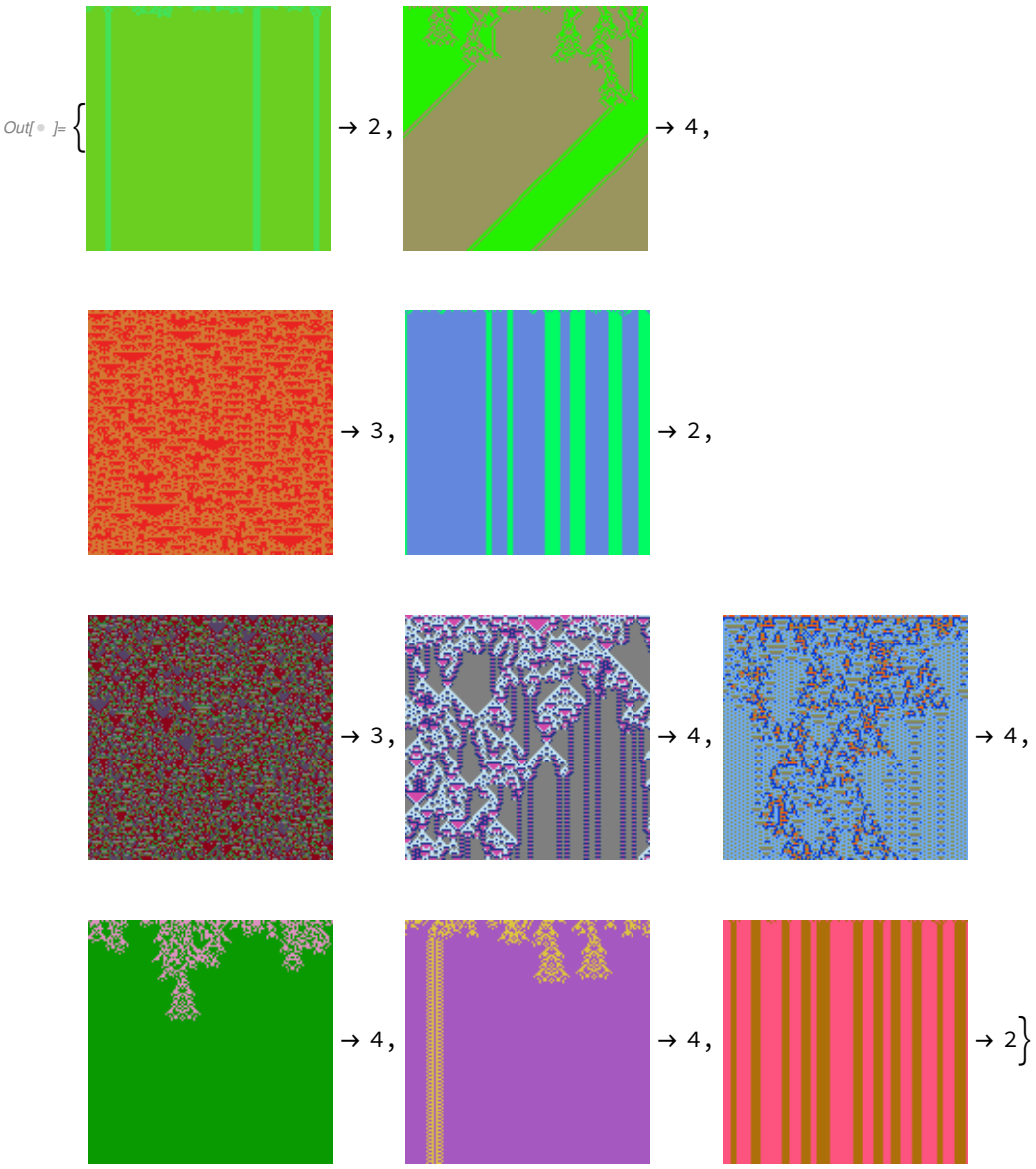
```
netECA17 = Import["netECA17-r200.wlnet"]
```

Out[ ]= NetChain[]

In[121]:=
```
testDataECABigC = dataC[128, 128, 1024];
testData2TBigC = genData2r2C[128, 128, 1024];
testData3TBigC = data3T2C[128, 128, 1024];
testData4TBigC = data4TC[128, 128, 1024];
testData5TBigC = genData5TCC[128, 128, 1024];
fullTestSetBigC = Join[testDataECABigC,
   testData2TBigC, testData3TBigC, testData4TBigC, testData5TBigC];
Length[fullTestSetBigC]
```

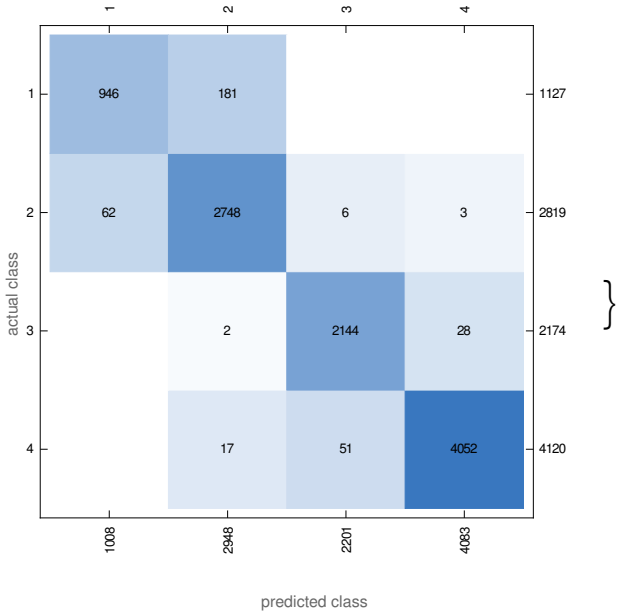
Out[127]= 10 240

In[ ]:= **RandomSample[fullTestSetBigC, 10]**

Out[ ]= 

In[ ]:=
```
NetMeasurements[netECA17, fullTestSetBigC,
 {"Accuracy", "Precision", "ConfusionMatrixPlot"}]
```

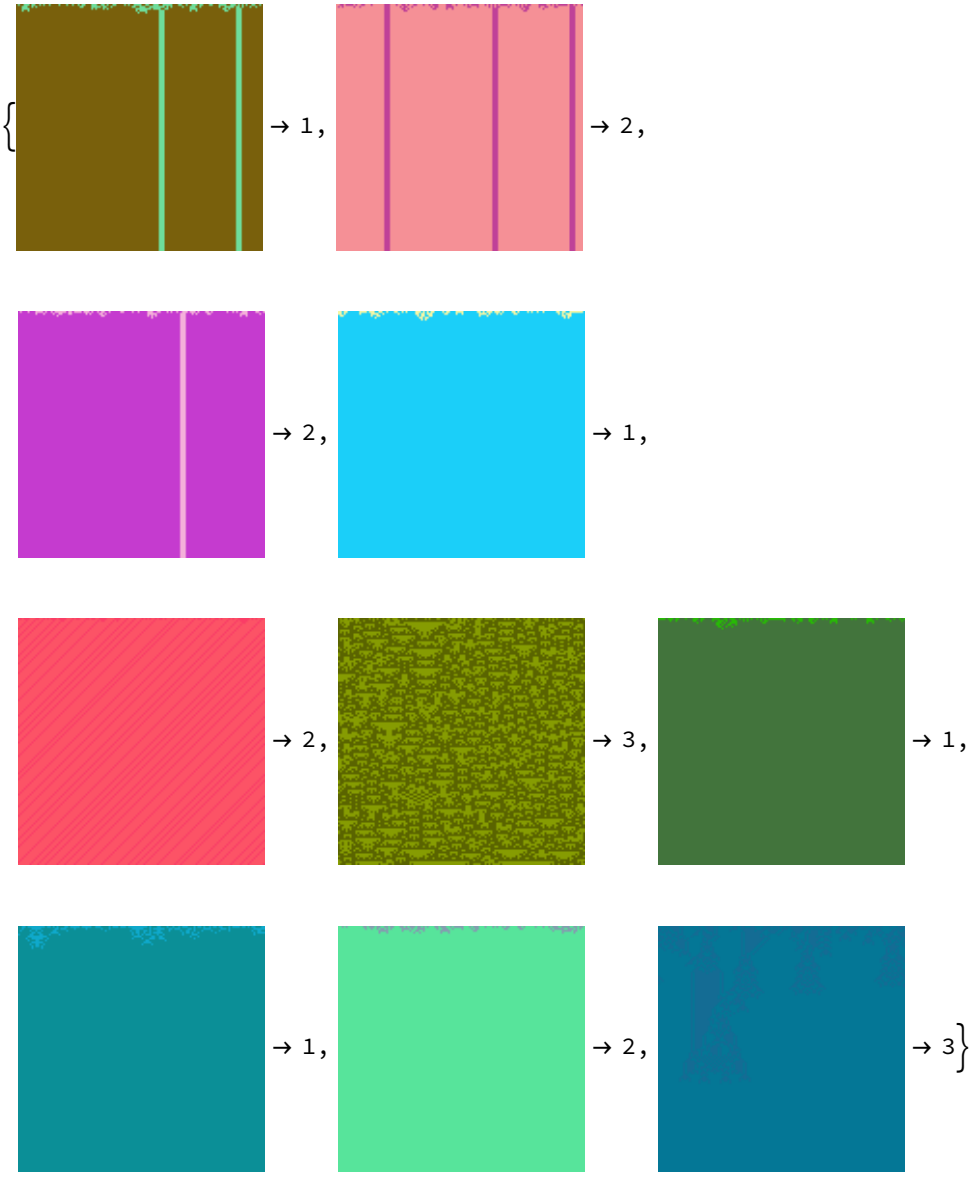
Out[ ]=
```
{0.96582, <|1 → 0.938492, 2 → 0.932157, 3 → 0.974103, 4 → 0.992408|>,
```



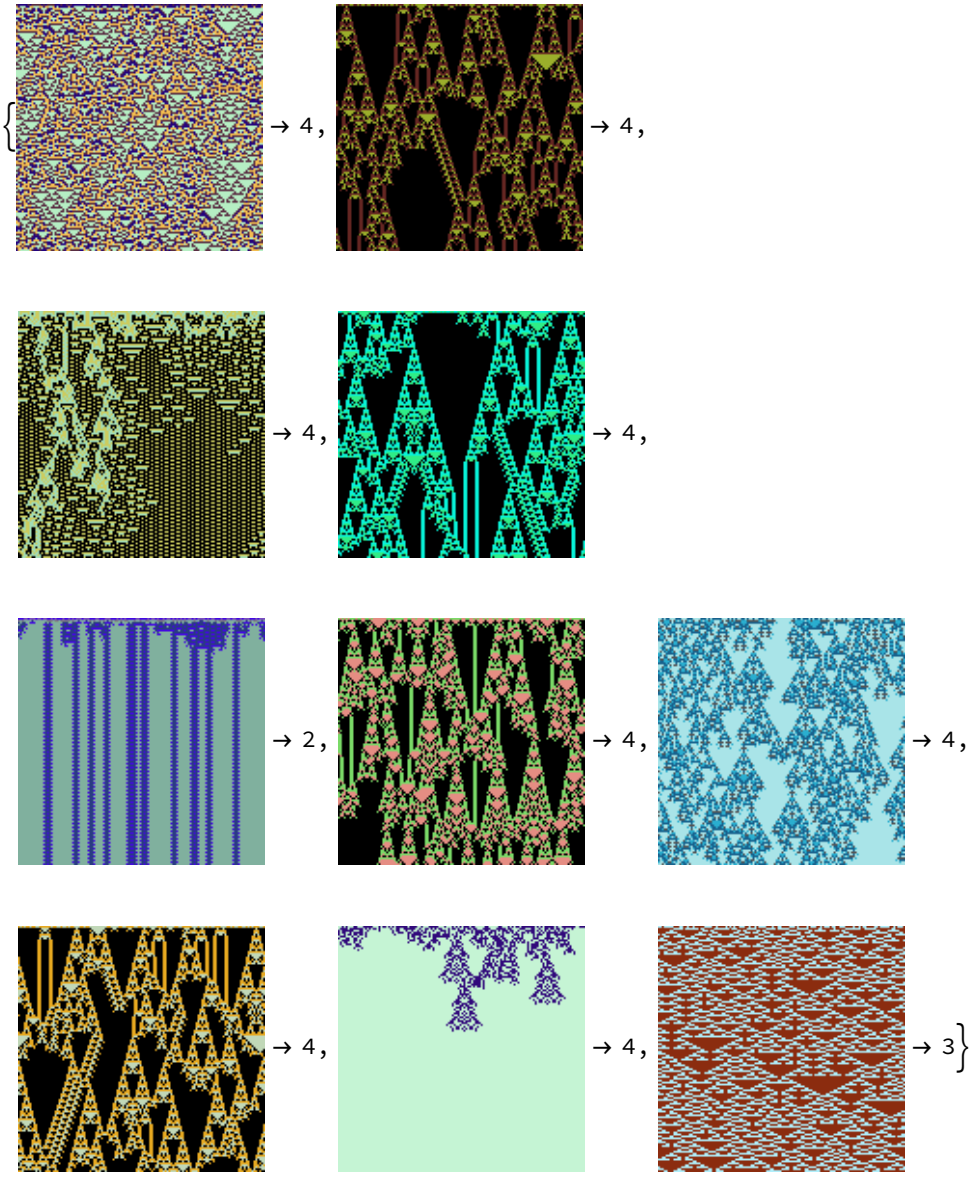

```
}
```

In[ ]:=
```
entropyImagesBigC = RandomSample[Keys[fullTestSetBigC], 500];
entropiesBigC = netECA17[entropyImagesBigC, "Entropy"];
highEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, -10]]];
lowEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, 10]]];
Thread[highEntBigC → netECA17[highEntBigC]]
Thread[lowEntBigC → netECA17[lowEntBigC]]
```

Out[ ]=



Out[ ]=



Testing Network XVII (200 epochs) on unseen CA rule spaces

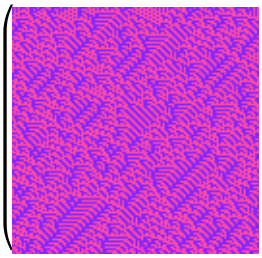
2-colour non-totalistic, range 2

In[ ]:=
```
test4Data2kr2C17 = datak2r2C[128, 128, 8];
Thread[test4Data2kr2C17 → netECA17[Keys@test4Data2kr2C17, {"TopProbabilities", 2}]]
```

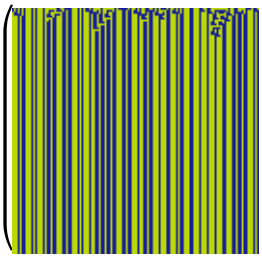
Out[ ]=

→ 3 594 886 935 → {3 → 1.19587 × 10^-7, 2 → 1.},

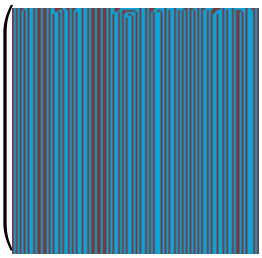
→ 4 012 014 789 → {4 → 0.00317589, 3 → 0.996824},



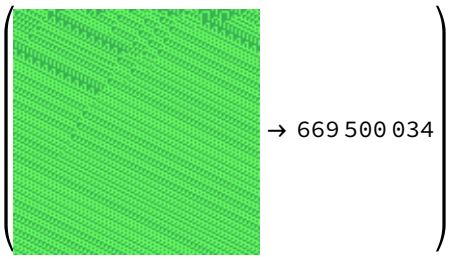
→ 736 342 145 → {4 → 0.000138652, 3 → 0.999861},

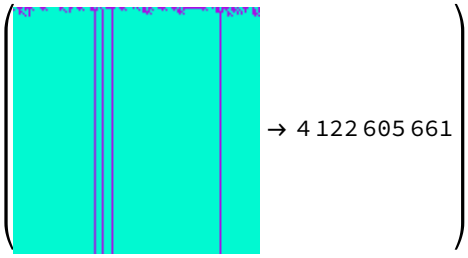


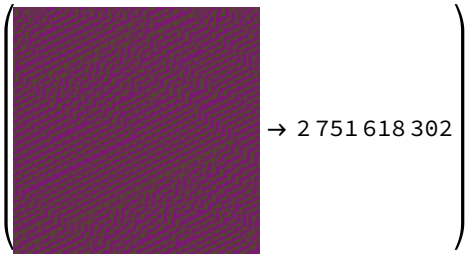
→ 3 597 938 931 → {4 → 5.42024 × 10^-16, 2 → 1.},



→ 49 406 137 → {1 → 4.03179 × 10^-30, 2 → 1.},

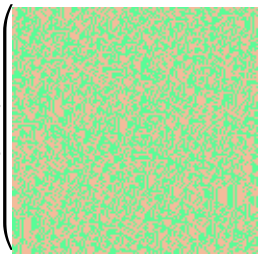

→ 669 500 034 → {4 → 0.0129747, 2 → 0.983657},


→ 4 122 605 661 → {1 → 6.18382 × 10^-9, 2 → 1.},

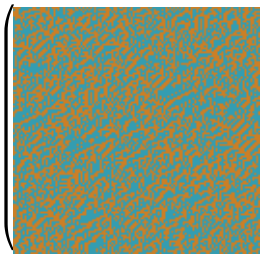

→ 2 751 618 302 → {4 → 5.91412 × 10^-9, 3 → 1.}}

2-colour non-totalistic, range 3

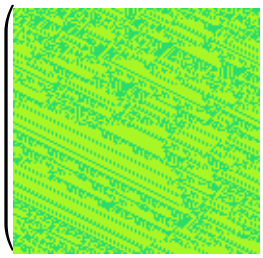
In[ ]:=
```
test4Data2kr3C17 = datak2r3NT[128, 128, 8];
Thread[test4Data2kr3C17 → netECA17[Keys@test4Data2kr3C17, {"TopProbabilities", 2}]]
```

Out[ ]=
{ 
→ 34 540 309 799 423 528 179 267 302 306 223 835 543 →

{4 → 0.0000190167, 3 → 0.999981},

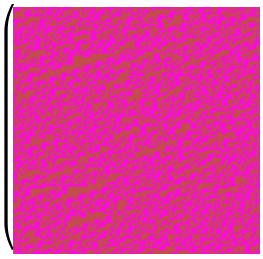

→ 271 913 994 962 168 934 532 188 611 494 783 284 369 →

$\{4 \to 8.79258 \times 10^{-15}, 3 \to 1.\},$



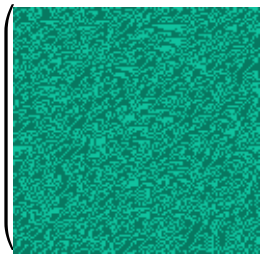
$\to 328\,899\,203\,265\,424\,040\,719\,063\,648\,351\,222\,904\,052 \to$

$\{3 \to 0.000609094, 4 \to 0.999391\},$



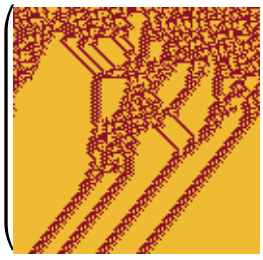
$\to 193\,952\,196\,319\,600\,964\,880\,345\,641\,761\,505\,849\,023 \to$

$\{4 \to 8.96571 \times 10^{-10}, 3 \to 1.\},$



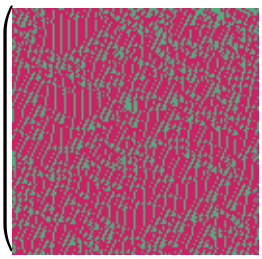
$\to 196\,656\,308\,173\,162\,097\,107\,061\,836\,715\,379\,270\,739 \to$

$\{4 \to 3.36397 \times 10^{-6}, 3 \to 0.999997\},$



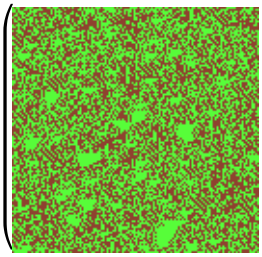
$\to 26\,038\,517\,878\,084\,050\,104\,120\,010\,197\,636\,533\,172 \to$

$\{3 \to 5.4757 \times 10^{-7}, 4 \to 0.999999\},$



→ 252 109 815 601 340 225 609 723 212 759 419 626 786 →

$\{4 \to 1.35911 \times 10^{-8}, 3 \to 1.\},$



→ 306 252 930 975 464 521 922 673 887 271 988 404 115 →

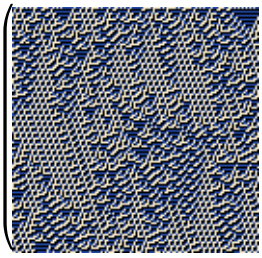
$\{4 \to 5.68649 \times 10^{-7}, 3 \to 0.999999\}\}$

3-colour non-totalistic, range 1

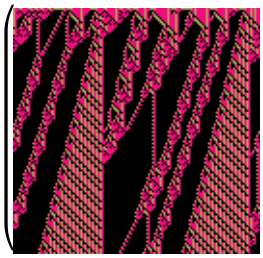
In[ ]:=
```
test4Data3kr1C17 = datak3r1NT[128, 128, 8];
Thread[test4Data3kr1C17 → netECA17[Keys@test4Data3kr1C17, {"TopProbabilities", 2}]]
```

Out[ ]=

→ 1 924 646 489 567 → $\{3 \to 1.76606 \times 10^{-30}, 2 \to 1.\},$

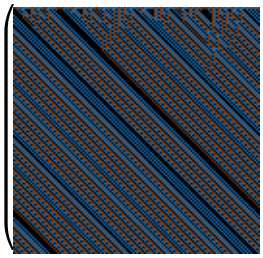


→ 3 672 534 501 071 → $\{2 \to 0.0000110699, 4 \to 0.999989\},$

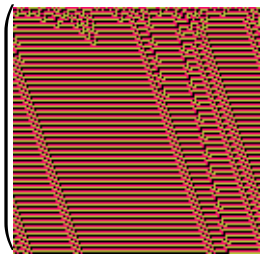


→ 5 833 330 297 781 → {2 → 0.000232935, 4 → 0.999767},

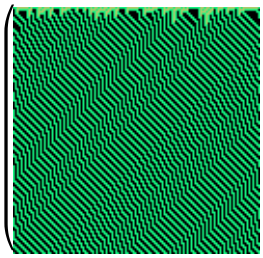
→ 7 606 192 973 798 → $\{2 \to 6.802 \times 10^{-10}, 1 \to 1.\}$,



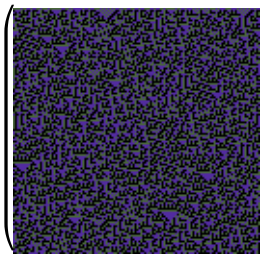
→ 7 622 301 560 954 → {3 → 0.0391643, 2 → 0.960836},



→ 3 685 910 174 297 → $\{3 \to 2.7602 \times 10^{-8}, 4 \to 1.\}$,



→ 5 743 838 876 456 → $\{1 \to 6.15406 \times 10^{-23}, 2 \to 1.\}$,

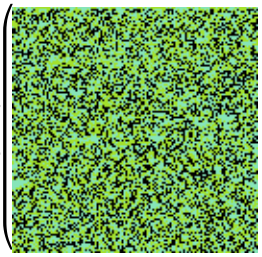


→ 3 655 040 152 191 | → {4 → 0.0374305, 3 → 0.962569}}

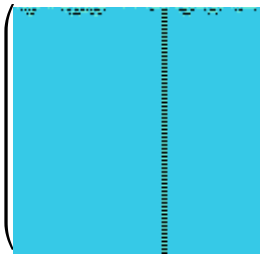
3-colour totalistic, range 2

In[ ]:=
```
test4Data3kr2C17 = datak3r2C[128, 128, 8];
Thread[test4Data3kr2C17 → netECA17[Keys@test4Data3kr2C17, {"TopProbabilities", 2}]]
```

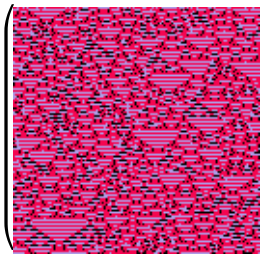
Out[ ]=



→ 43 149 | → {4 → 1.6989 × 10^−8, 3 → 1.},



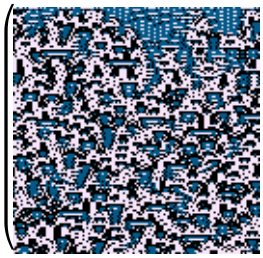
→ 160 434 | → {1 → 2.05354 × 10^−18, 2 → 1.},



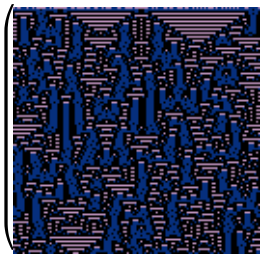
→ 9535 | → {3 → 0.0000598239, 4 → 0.99994},

→ 172 239 | → {1 → 0.00705153, 2 → 0.992948},

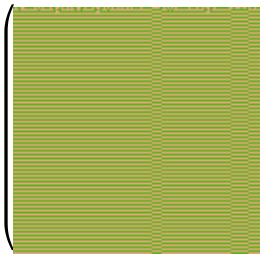
→ 174 680 → {2 → 5.824 × 10^-11, 1 → 1.},



→ 55 945 → {4 → 0.0138349, 3 → 0.986165},



→ 113 483 → {4 → 3.72822 × 10^-6, 3 → 0.999996},

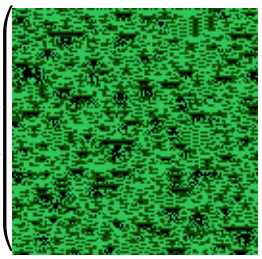


→ 67 810 → {1 → 6.91386 × 10^-17, 2 → 1.}}

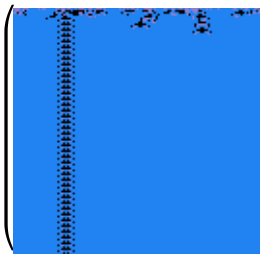
3-colour totalistic, range 3

In[ ]:=
```
test4Data3kr3C17 = datak3r3C[128, 128, 8];
Thread[test4Data3kr3C17 → netECA17[Keys@test4Data3kr3C17, {"TopProbabilities", 2}]]
```

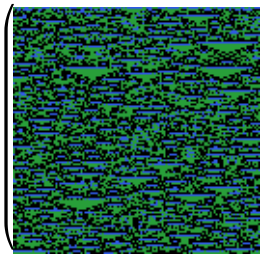
Out[ ]=



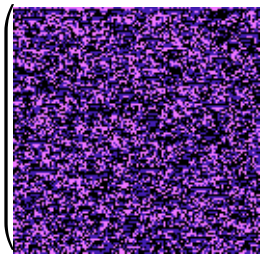
→ 3 046 610 → {4 → 7.58312 × 10^-7, 3 → 0.999999},



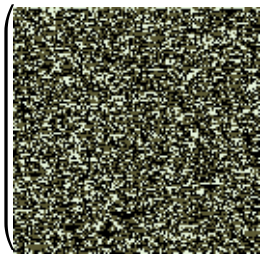
→ 7 801 434 → {1 → 1.19167 × 10^{-14}, 2 → 1.},



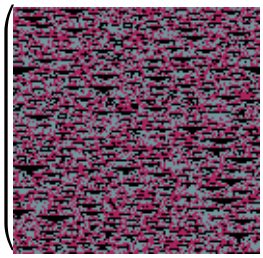
→ 5 445 843 → {4 → 1.60992 × 10^{-19}, 3 → 1.},



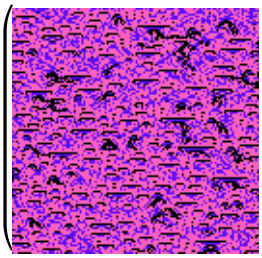
→ 1 451 413 → {4 → 0.144413, 3 → 0.855587},



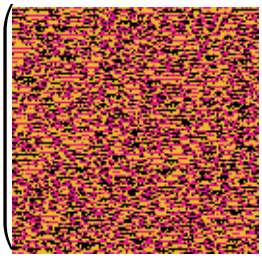
→ 10 676 790 → {3 → 0.0738921, 4 → 0.926108},



→ 10 375 449 → {4 → 1.04031 × 10^{-17}, 3 → 1.},



→ 5 181 761 → {4 → 1.75908 × 10^-8, 3 → 1.}},

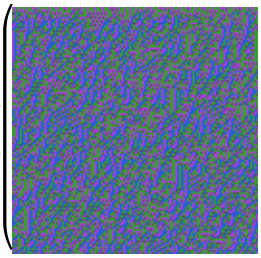


→ 8 884 285 → {4 → 7.91486 × 10^-6, 3 → 0.999992}}

4-colour non-totalistic, range 1

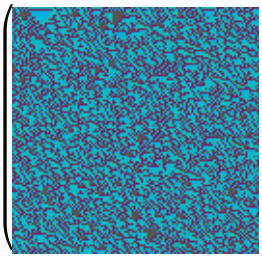
In[ ]:=
```
test4Data4kr1C17 = datak4r1NT[128, 128, 8];
Thread[test4Data4kr1C17 → netECA17[Keys@test4Data4kr1C17, {"TopProbabilities", 2}]]
```

Out[ ]=



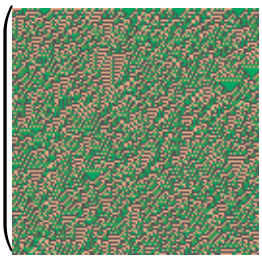
→ 255 219 118 556 246 495 764 448 982 135 818 252 673 →

{3 → 2.62807 × 10^-6, 4 → 0.999997},



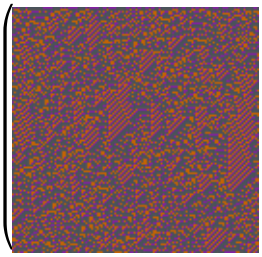
→ 256 372 744 774 750 994 462 308 116 064 689 670 029 →

{4 → 1.66442 × 10^-17, 3 → 1.},



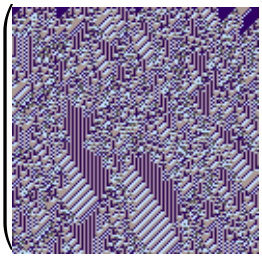
→ 287 015 413 736 003 568 798 718 608 141 279 906 438 →

$\{4 \to 2.56385 \times 10^{-7}, 3 \to 1.\}$,



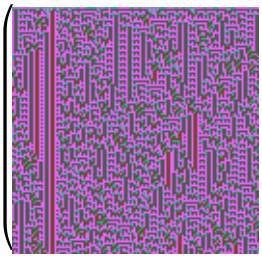
→ 102 047 809 483 228 794 436 919 245 364 544 665 433 →

$\{4 \to 0.000696463, 3 \to 0.999304\}$,



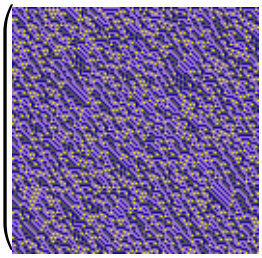
→ 240 555 046 861 732 528 519 285 194 385 835 154 772 →

$\{4 \to 3.62136 \times 10^{-16}, 3 \to 1.\}$,



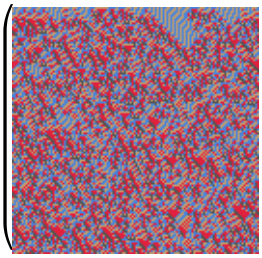
→ 16 370 468 900 338 540 956 022 703 184 589 781 262 →

$\{3 \to 1.45252 \times 10^{-15}, 4 \to 1.\}$,



→ 121 099 422 536 966 135 180 998 722 819 969 755 137 →

{4 → 0.0000270873, 3 → 0.999973},



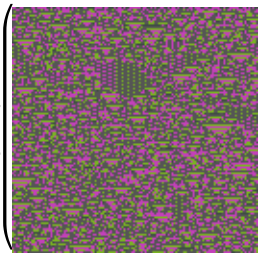
→ 264 867 193 286 423 906 380 401 526 070 744 380 919 →

{4 → 0.105214, 3 → 0.894786}}

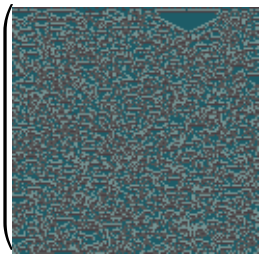
4-colour totalistic, range 2

In[ ]:=
```
test4Data4kr2C17 = datak4r2C[128, 128, 8];
Thread[test4Data4kr2C17 → netECA17[Keys@test4Data4kr2C17, {"TopProbabilities", 2}]]
```

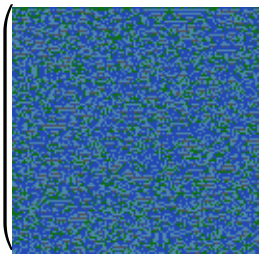
Out[ ]=



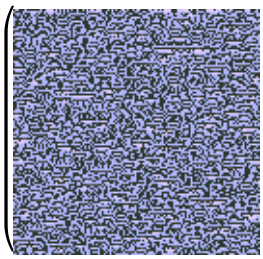
→ 616 082 315 → {4 → 8.8653 × 10^-10, 3 → 1.},



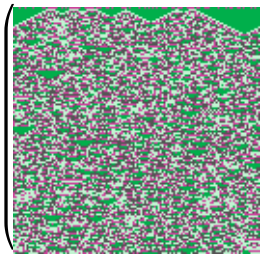
→ 1 568 191 428 → {4 → 5.21264 × 10^-11, 3 → 1.},



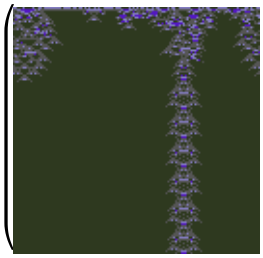
→ 1 216 110 065 → {4 → 0.000040346, 3 → 0.99996},



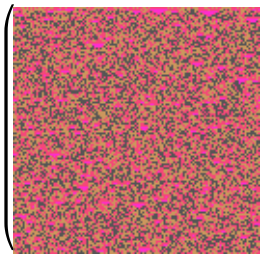
$\to 2\,419\,903\,949 \to \{4 \to 3.69897 \times 10^{-10}, 3 \to 1.\},$



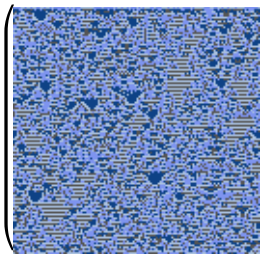
$\to 453\,961\,055 \to \{4 \to 3.89961 \times 10^{-8}, 3 \to 1.\},$



$\to 3\,969\,029\,930 \to \{2 \to 0.0000237283, 4 \to 0.999976\},$



$\to 3\,970\,208\,335 \to \{4 \to 4.03487 \times 10^{-9}, 3 \to 1.\},$

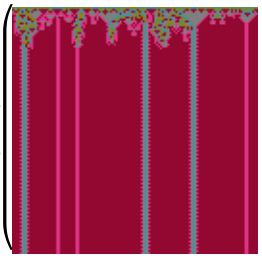


$\to 3\,418\,384\,250 \to \{4 \to 9.0126 \times 10^{-15}, 3 \to 1.\}\}$

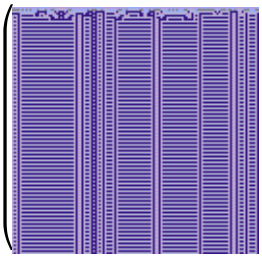
5-colour totalistic, range 1

In[ ]:=
```
test4Data5kr1C17 = data5T2C[8, 128, 128];
Thread[test4Data5kr1C17 → netECA17[Keys@test4Data5kr1C17, {"TopProbabilities", 2}]]
```

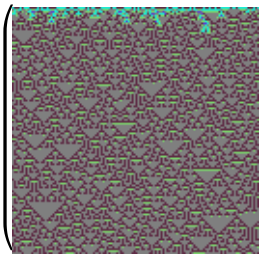
Out[ ]=



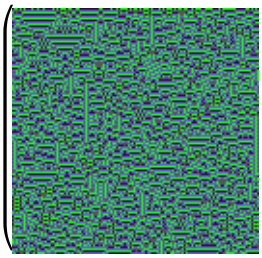
→ 720 503 516 → {2 → 0.000105936, 4 → 0.999894},



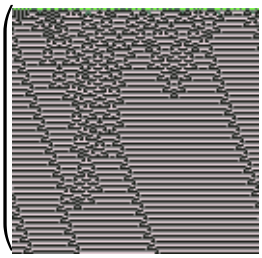
→ 771 013 684 → $\{4 \to 1.94282 \times 10^{-8}, 2 \to 1.\}$,



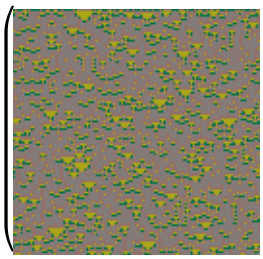
→ 543 872 434 → $\{4 \to 6.11423 \times 10^{-7}, 3 \to 0.999999\}$,



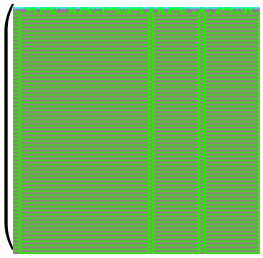
→ 341 908 586 → {4 → 0.310854, 3 → 0.689146},



→ 664 036 861 → {2 → 0.00511847, 4 → 0.994882},



→ 1 182 110 899 → {4 → 0.039023, 3 → 0.960977},



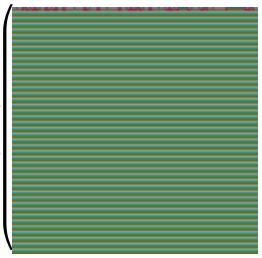
→ 976 082 949 → $\{4 \to 9.09593 \times 10^{-19}, 2 \to 1.\}$,

→ 1 019 517 181 → $\{1 \to 6.47917 \times 10^{-10}, 2 \to 1.\}\}$

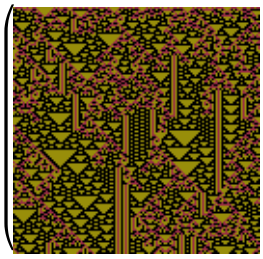
6-colour totalistic, range 1

In[ ]:=
```
test4Data6kr1C17 = data6TC[8, 128, 128];
Thread[test4Data6kr1C17 → netECA17[Keys@test4Data6kr1C17, {"TopProbabilities", 2}]]
```

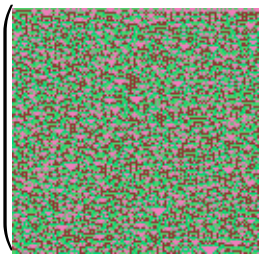
Out[ ]=



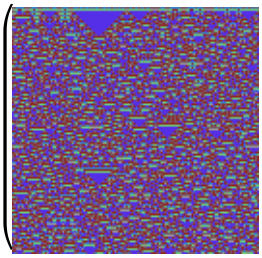
→ 1 128 957 409 115 → {2 → 0.387573, 1 → 0.612427},



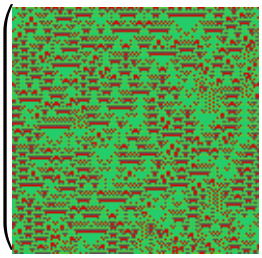
→ 744 151 919 694 → $\{3 \to 1.28454 \times 10^{-11}, 4 \to 1.\}$,



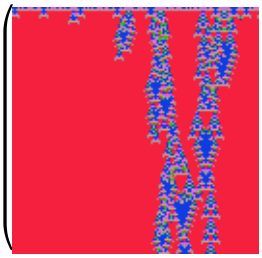
$\to 411\,482\,269\,593 \to \{4 \to 9.50671 \times 10^{-6},\ 3 \to 0.99999\},$



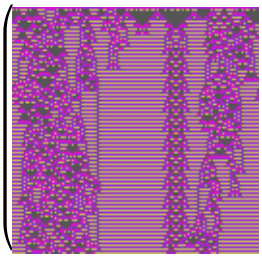
$\to 2\,122\,826\,252\,429 \to \{4 \to 4.58698 \times 10^{-10},\ 3 \to 1.\},$



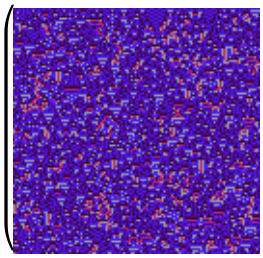
$\to 2\,443\,710\,325\,124 \to \{4 \to 5.97811 \times 10^{-9},\ 3 \to 1.\},$



$\to 2\,519\,595\,515\,832 \to \{2 \to 0.396179,\ 4 \to 0.603821\},$



$\to 572\,558\,234\,379 \to \{4 \to 1.63969 \times 10^{-11},\ 3 \to 1.\},$

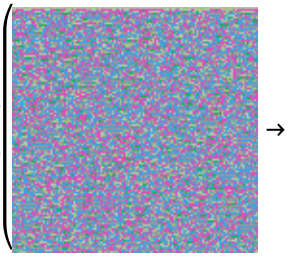


→ 2 103 617 145 248 → {3 → 8.41391 × 10^-9, 4 → 1.}}

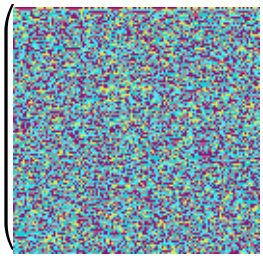
6-colour totalistic, range 2

In[ ]:=
```
test4Data6kr2C17 = data6T2C[8, 128, 128];
Thread[test4Data6kr2C17 → netECA17[Keys@test4Data6kr2C17, {"TopProbabilities", 2}]]
```

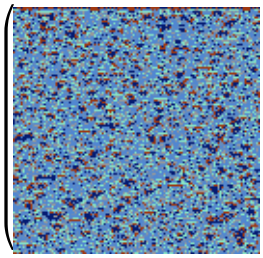
Out[ ]=



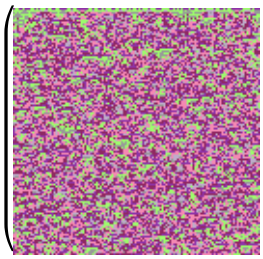
→ 56 518 611 906 036 513 420 → {4 → 0.00132297, 3 → 0.998677},



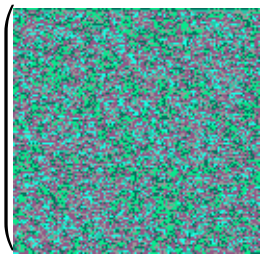
→ 149 111 145 742 470 978 404 → {4 → 0.00110016, 3 → 0.9989},



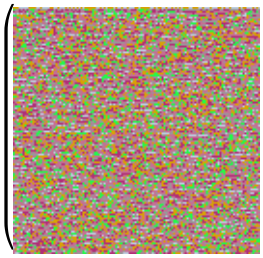
→ 60 075 298 400 874 491 559 → {4 → 0.0000816385, 3 → 0.999918},



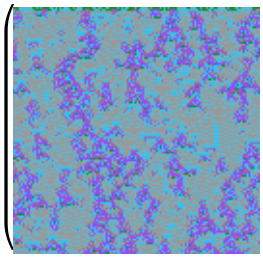
→ 61 137 219 885 741 406 688 → {4 → 6.01526 × 10^-9, 3 → 1.},



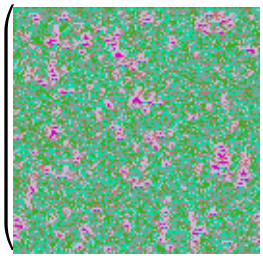
→ 138 083 937 800 052 503 915 → {4 → 1.63338 × 10^-6, 3 → 0.999998},



→ 102 848 890 668 267 918 696 → {4 → 4.51684 × 10^-8, 3 → 1.},



→ 52 002 759 529 482 240 344 → {4 → 0.0161382, 3 → 0.983862},

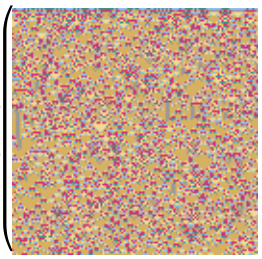


→ 3 771 326 190 903 203 597 → {4 → 1.57635 × 10^-10, 3 → 1.}}

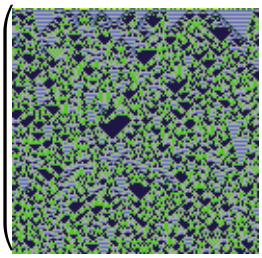
7-colour totalistic, range 1

In[ ]:=
```
test4Data7kr1C17 = data7TC[8, 128, 128];
Thread[test4Data7kr1C17 → netECA17[Keys@test4Data7kr1C17, {"TopProbabilities", 2}]]
```

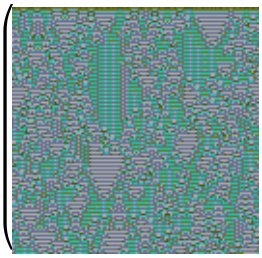
Out[ ]=



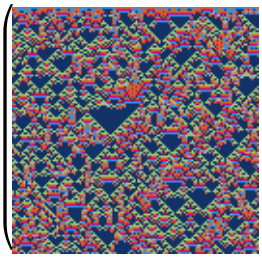
→ 249 739 897 876 317 → {4 → 7.58753 × 10^-13, 3 → 1.},



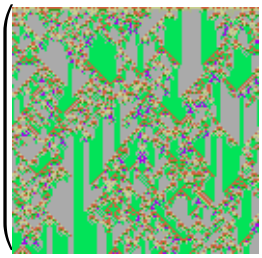
→ 6 589 873 174 284 234 → {4 → 3.70203 × 10^-21, 3 → 1.},



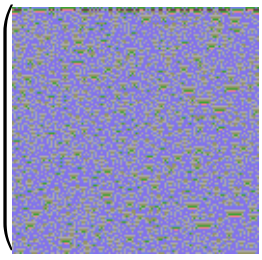
→ 2 838 251 451 633 386 → {3 → 0.0000362001, 4 → 0.999964},



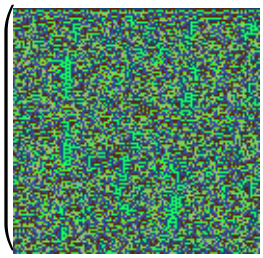
→ 3 069 021 856 393 877 → {4 → 4.6982 × 10^-6, 3 → 0.999995},



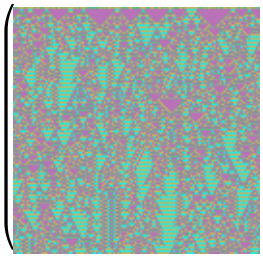
→ 10 282 712 720 317 214 → {3 → 4.14045 × 10^-19, 4 → 1.},



→ 203 015 413 423 084 → {4 → 2.87431 × 10^-9, 3 → 1.},



→ 9 746 864 148 555 591 → {3 → 1.53822 × 10^-7, 4 → 1.},

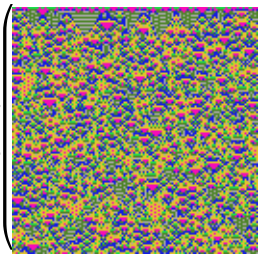


→ 8 003 062 538 664 128 → {3 → 2.05185 × 10^-8, 4 → 1.}}

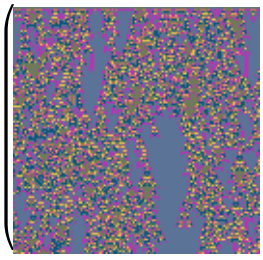
8-colour totalistic, range 1

In[ ]:=
```
test4Data8kr1C17 = data8TC[8, 128, 128];
Thread[test4Data8kr1C17 → netECA17[Keys@test4Data8kr1C17, {"TopProbabilities", 2}]]
```

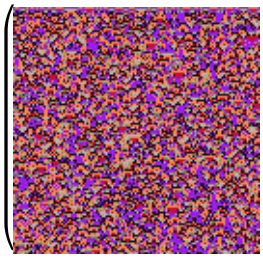
Out[ ]=



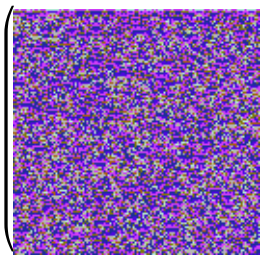
→ 10 266 196 594 935 096 075 → {4 → 8.5791 × 10^-18, 3 → 1.},



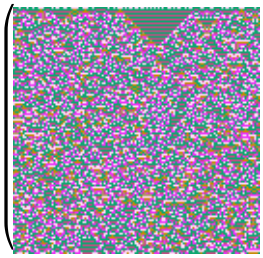
→ 731 338 973 990 773 560 → {2 → 7.53019 × 10^-12, 4 → 1.},



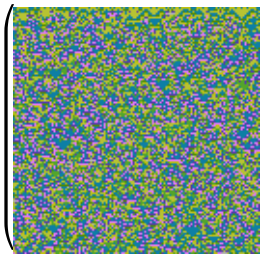
→ 11 247 173 012 174 218 620 → {4 → 0.0000380778, 3 → 0.999962},



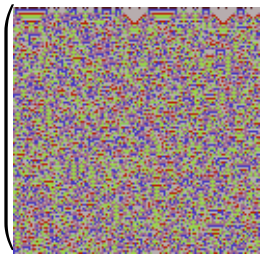
→ 63 742 472 032 617 219 918 → {4 → 0.0000371126, 3 → 0.999963},



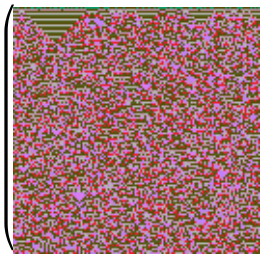
→ 7 382 455 380 800 363 015 → {4 → 8.07468 × 10^-15, 3 → 1.},



→ 59 100 651 667 569 734 000 → {4 → 1.27228 × 10^-11, 3 → 1.},



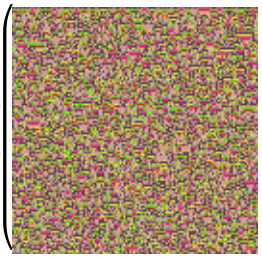
→ 24 971 306 247 396 766 335 → {4 → 0.0333734, 3 → 0.966627},



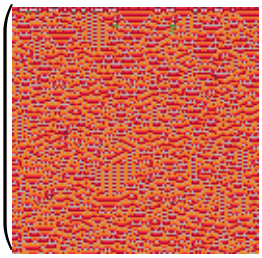
→ 45 946 581 080 593 555 746 → {4 → 1.08598 × 10^-15, 3 → 1.}}

In[ ]:=
```
test4Data8kr1C17 = data8TC[8, 128, 128];
Thread[test4Data8kr1C17 → netECA17[Keys@test4Data8kr1C17, {"TopProbabilities", 2}]]
```

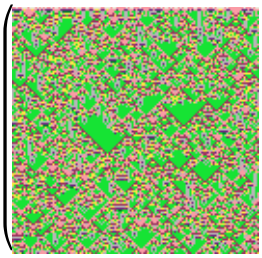
Out[ ]=



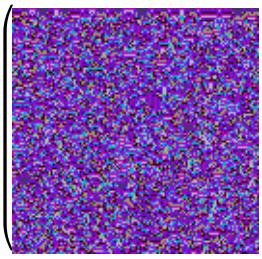
→ 14 955 350 598 586 141 683 → {4 → 1.70104 × 10^-7, 3 → 1.},



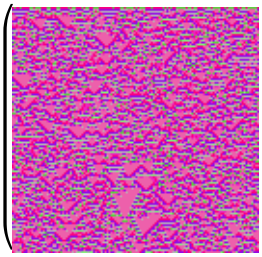
→ 30 727 455 169 449 395 964 → {4 → 4.31945 × 10^-11, 3 → 1.},



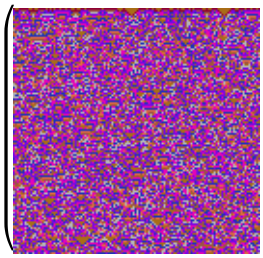
→ 42 490 152 676 883 207 115 → {3 → 0.0000793636, 4 → 0.999921},



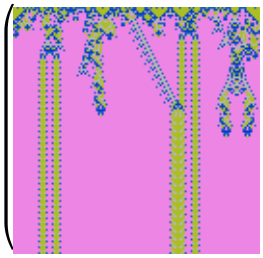
→ 18 395 296 261 071 222 192 → {4 → 0.0142026, 3 → 0.985797},



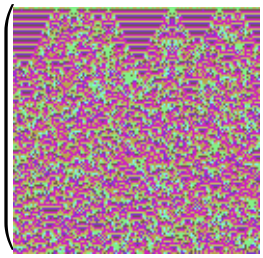
→ 22 317 090 484 634 250 431 → {3 → 0.00783339, 4 → 0.992167},



→ 33 329 414 465 629 594 174 → {4 → 0.00851294, 3 → 0.991487},



→ 68 439 232 681 205 604 962 → {2 → 1.97568 × 10^-13, 4 → 1.},



→ 53 049 830 479 062 864 751 → {4 → 3.6815 × 10^-10, 3 → 1.}}

Network XVIII- Four convolutions, dropout on linear only, BatchNorm

In[ ]:= **netECA18 = netTenCC1024drop[128, 128]**

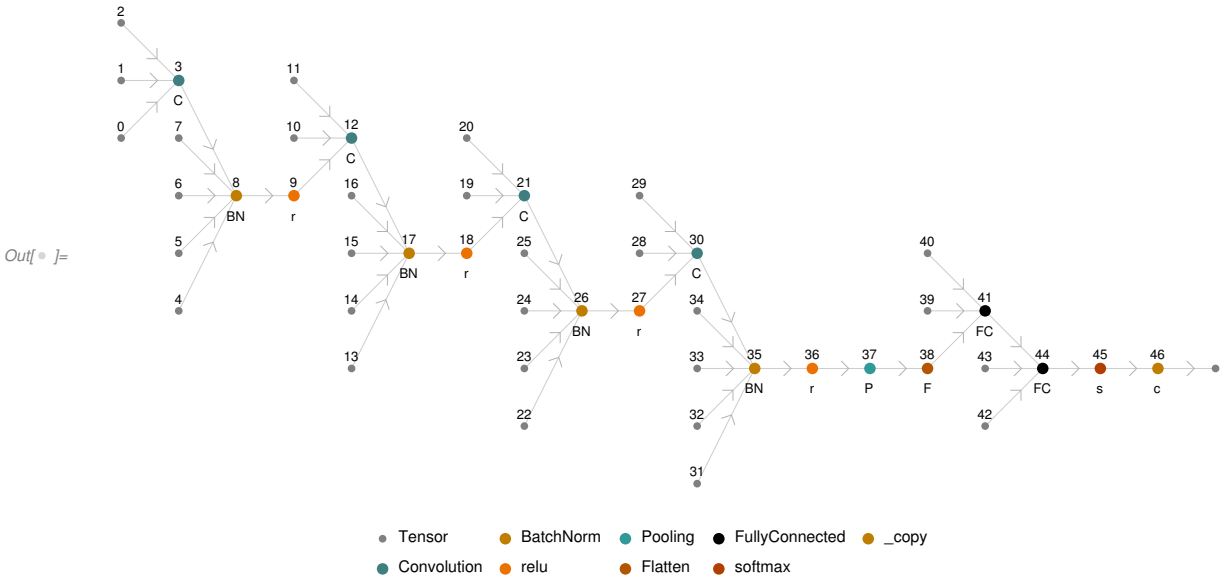
Out[ ]= NetChain[

		image
	Input	array (size: 3 × 128 × 128)
conv1	ConvolutionLayer	array (size: 24 × 126 × 126)
bat1	BatchNormalizationLayer	array (size: 24 × 126 × 126)
ramp1	Ramp	array (size: 24 × 126 × 126)
conv2	ConvolutionLayer	array (size: 24 × 124 × 124)
bat2	BatchNormalizationLayer	array (size: 24 × 124 × 124)
ramp2	Ramp	array (size: 24 × 124 × 124)
conv3	ConvolutionLayer	array (size: 24 × 122 × 122)
bat3	BatchNormalizationLayer	array (size: 24 × 122 × 122)
ramp3	Ramp	array (size: 24 × 122 × 122)
conv4	ConvolutionLayer	array (size: 24 × 120 × 120)
bat4	BatchNormalizationLayer	array (size: 24 × 120 × 120)
ramp4	Ramp	array (size: 24 × 120 × 120)
pooling	PoolingLayer	array (size: 24 × 5 × 5)
flatten	FlattenLayer	vector (size: 600)
linear	LinearLayer	vector (size: 1024)
drop2	DropoutLayer	vector (size: 1024)
linear2	LinearLayer	vector (size: 4)
softmax	SoftmaxLayer	vector (size: 4)
	Output	class

]

In[ ]:=
```
NetInformation[netECA18, "MXNetNodeGraphPlot"]
```

Out[ ]=



In[ ]:=
```
NetInformation[netECA18, "SummaryGraphic"]
```

Out[ ]=

In[ ]:=
```
dataECA18 = dataC[128, 128, 16 384];
```

In[ ]:=
```
dataTotalistic2BigC18 = genData2r2C[128, 128, 4096];
```

In[ ]:=
```
dataTotalistic3BigC18 = data3T2C[128, 128, 4096];
```

In[ ]:=
```
dataTotalistic4BigC18 = data4TC[128, 128, 4096];
```

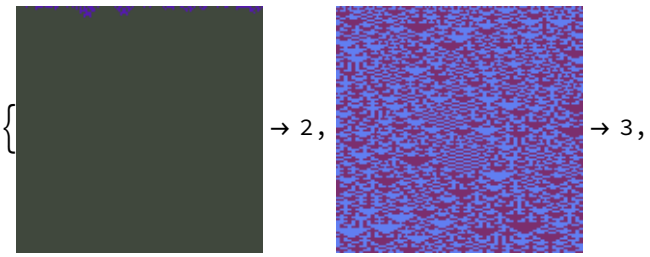
In[ ]:=
```
dataTotalistic5BigC18 = genData5TCC[128, 128, 16 384];
```

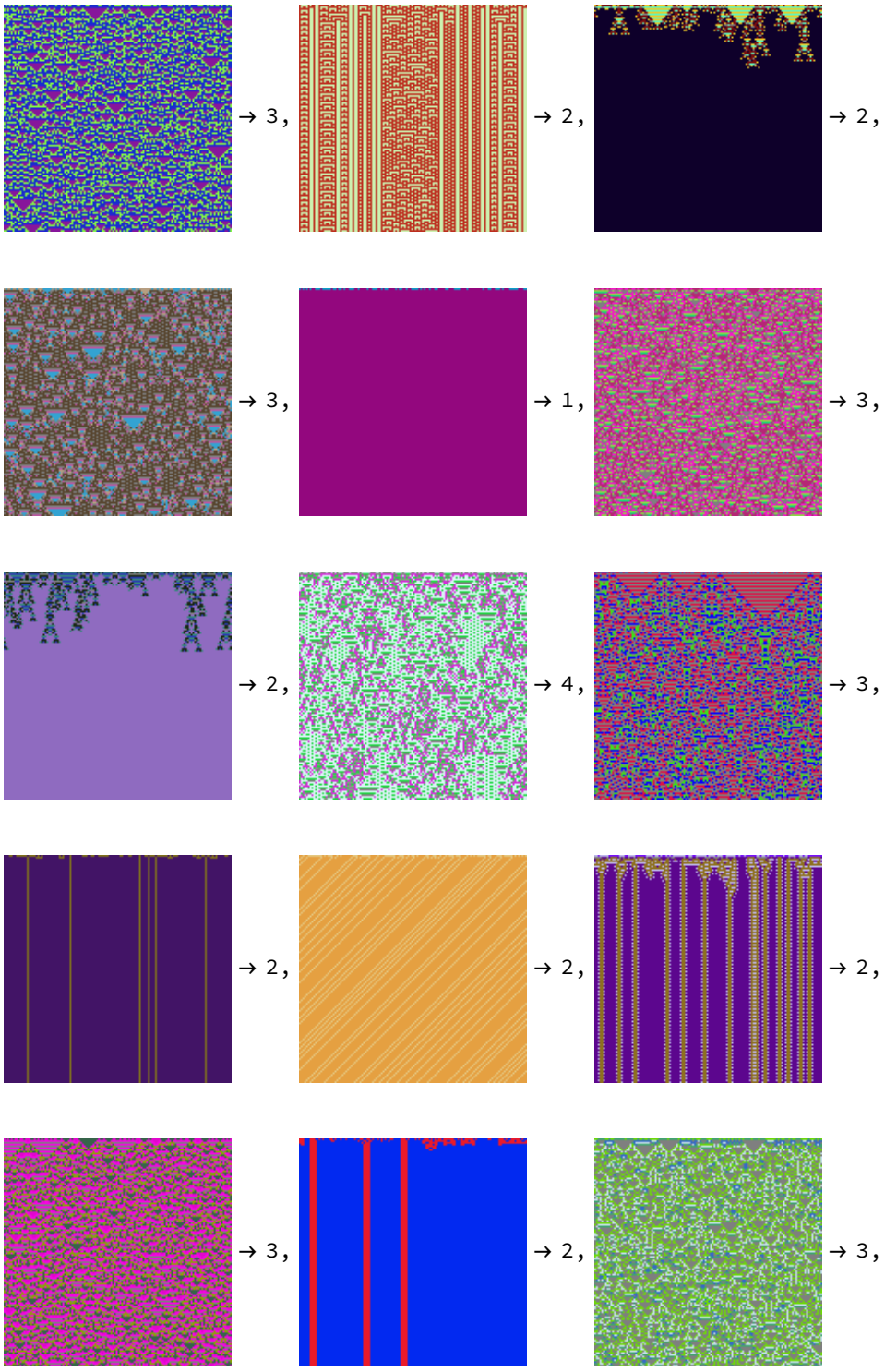
In[ ]:=
```
fullTrainingBigC18 = Join[dataECA18, dataTotalistic2BigC18,
    dataTotalistic3BigC18, dataTotalistic4BigC18, dataTotalistic5BigC18];
Length[fullTrainingBigC18]
```

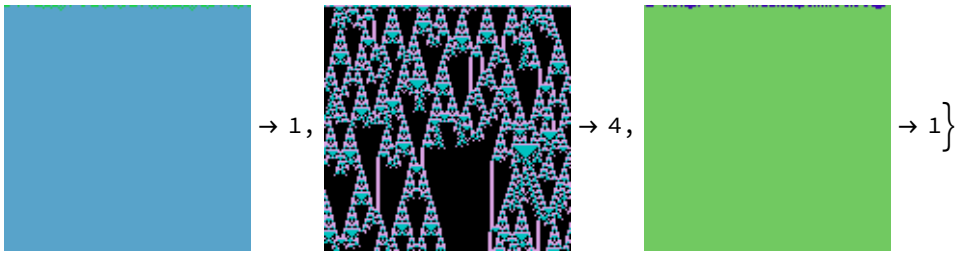
Out[ ]=
```
90 112
```

In[ ]:=
```
RandomSample[fullTrainingBigC18, 20]
```

Out[ ]=




→ 3,
→ 2,
→ 2,
→ 3,
→ 1,
→ 3,
→ 2,
→ 4,
→ 3,
→ 2,
→ 2,
→ 2,
→ 3,
→ 2,
→ 3,



In[ ]:= **dir = SetDirectory[NotebookDirectory[]]**

Out[ ]= /home/esilverman/Documents

In[ ]:= **"/home/esilverman/Documents"**

Out[ ]= /home/esilverman/Documents

In[ ]:=
```
netECA18 =
 NetTrain[netECA18, fullTrainingBigC18, MaxTrainingRounds → 200, BatchSize → 256,
  TargetDevice → "GPU", TrainingProgressCheckpointing → {"Directory", dir}]
```

Out[ ]= NetChain[Input port: image / Output port: class / Number of layers: 18]

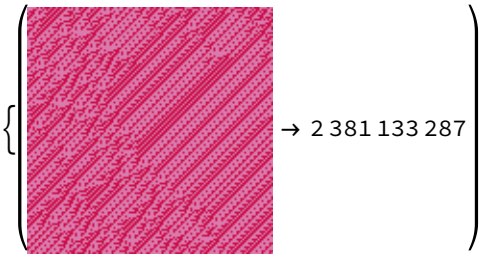
In[ ]:= **netECA18 = Import["netECA18-r200.wlnet"]**

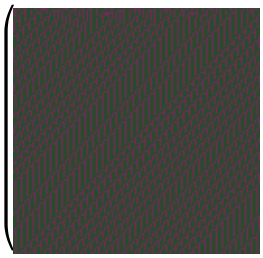
Out[ ]= NetChain[Input port: image / Output port: class / Number of layers: 18]

Testing Network XVIII (200 epochs) on unseen CA rule spaces

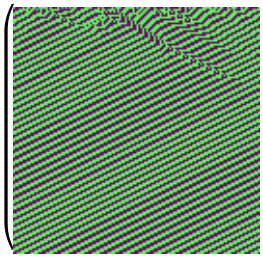
2-colour non-totalistic, range 2

In[ ]:=
```
test4Data2kr2C18 = datak2r2C[128, 128, 8];
Thread[test4Data2kr2C18 → netECA18[Keys@test4Data2kr2C18, {"TopProbabilities", 2}]]
```

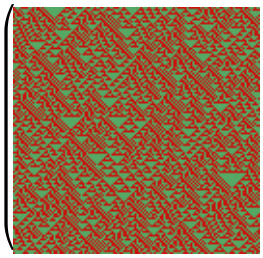
Out[ ]=  → 2 381 133 287 → {4 → 1.78812 × 10^-7, 3 → 1.},



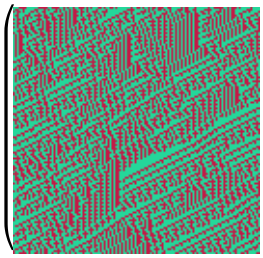
→ 2 956 498 967 → {2 → 0.00630379, 3 → 0.992493},



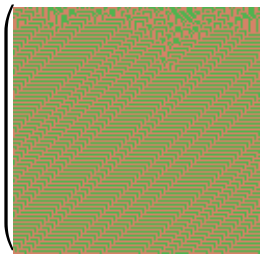
→ 677 038 591 → $\{4 \to 1.21175 \times 10^{-11}, 2 \to 1.\}$,



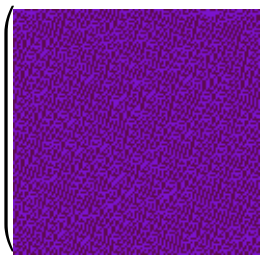
→ 3 273 379 163 → {4 → 0.34545, 3 → 0.65455},



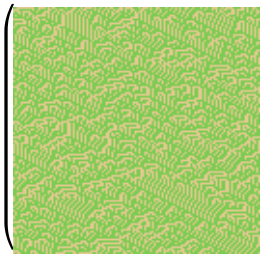
→ 2 209 740 989 → $\{2 \to 1.84144 \times 10^{-11}, 3 \to 1.\}$,



→ 939 607 251 → $\{3 \to 8.18048 \times 10^{-7}, 4 \to 0.999999\}$,



→ 1 148 523 078 → {4 → 8.98033 × 10^-7, 3 → 0.999999},

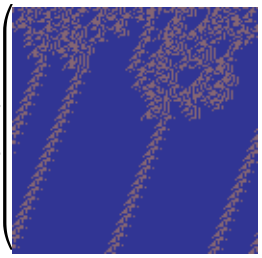


→ 297 019 595 → {4 → 1.32121 × 10^-12, 3 → 1.}}

2-colour non-totalistic, range 3

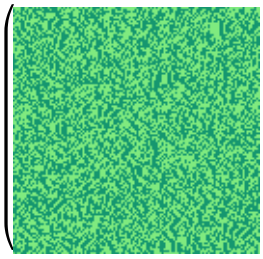
In[ ]:=
```
test4Data2kr3C18 = datak2r3NT[128, 128, 8];
Thread[test4Data2kr3C18 → netECA18[Keys@test4Data2kr3C18, {"TopProbabilities", 2}]]
```

Out[ ]=



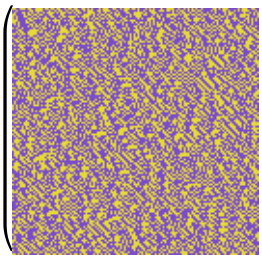
→ 330 416 984 885 540 388 017 354 162 041 951 825 587 →

{3 → 8.74296 × 10^-8, 4 → 1.},



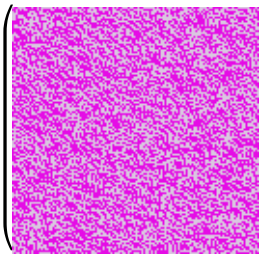
→ 279 656 361 264 376 888 074 030 685 915 728 704 181 →

{4 → 0.0213521, 3 → 0.978648},



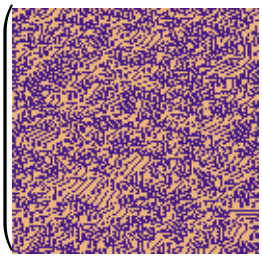
→ 197 632 068 292 332 388 955 030 541 940 304 062 122 →

$\{4 \to 5.0499 \times 10^{-16}, 3 \to 1.\}$,



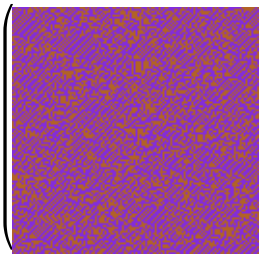
→ 188 082 660 194 176 799 122 844 083 244 865 677 445 →

$\{4 \to 2.34238 \times 10^{-6}, 3 \to 0.999998\}$,



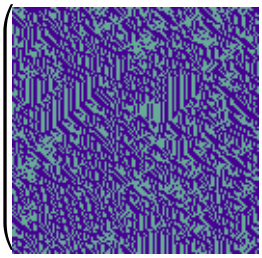
→ 99 467 121 511 183 621 679 443 804 486 384 512 063 →

{4 → 0.00329566, 3 → 0.996704},



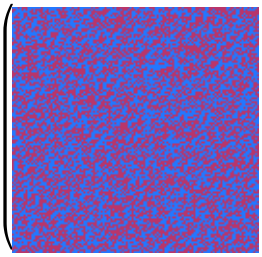
→ 56 219 309 346 455 872 630 743 597 889 899 213 800 →

$\{4 \to 1.38574 \times 10^{-10}, 3 \to 1.\}$,



→ 308 130 247 560 683 500 868 656 567 738 983 907 586 →

$\{4 \to 5.1263 \times 10^{-8}, 3 \to 1.\},$



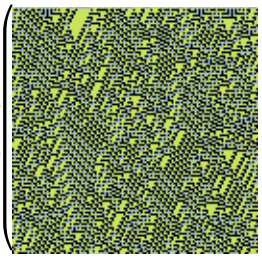
$\to 333\,388\,526\,947\,822\,905\,616\,741\,326\,831\,869\,137\,342 \to$

$\{4 \to 7.10494 \times 10^{-8}, 3 \to 1.\}\Big\}$

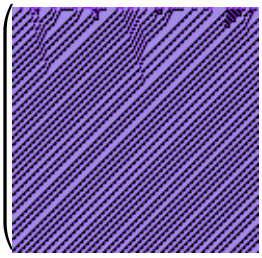
3-colour non-totalistic, range 1

In[ ]:=
```
test4Data3kr1C18 = datak3r1NT[128, 128, 8];
Thread[test4Data3kr1C18 → netECA18[Keys@test4Data3kr1C18, {"TopProbabilities", 2}]]
```

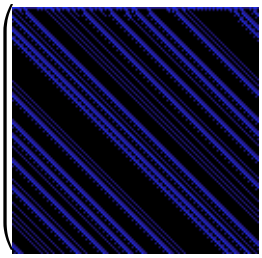
Out[ ]=



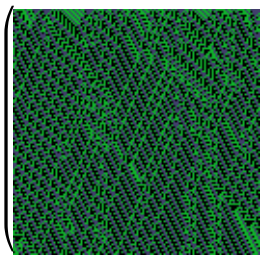
$\to 1\,592\,394\,332\,064 \to \{2 \to 7.59314 \times 10^{-6}, 4 \to 0.999992\},$



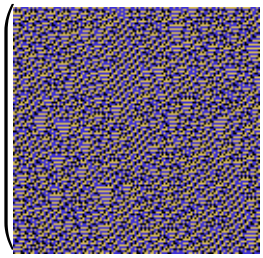
$\to 4\,098\,174\,485\,356 \to \{4 \to 8.44302 \times 10^{-20}, 2 \to 1.\},$



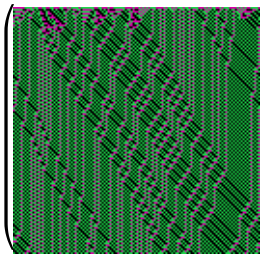
$\to 5\,930\,373\,291\,731 \to \{1 \to 2.34989 \times 10^{-7}, 2 \to 1.\},$



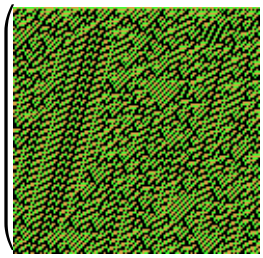
→ 6 363 744 081 807 → {3 → 0.0000390704, 4 → 0.999961},



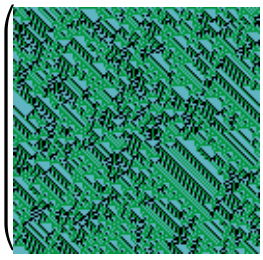
→ 1 193 083 886 293 → {4 → 0.0126455, 3 → 0.987355},



→ 1 957 822 902 340 → {3 → 0.0000561806, 2 → 0.999944},



→ 2 179 566 018 820 → $\{4 \to 1.10915 \times 10^{-6}, 3 \to 0.999999\}$,

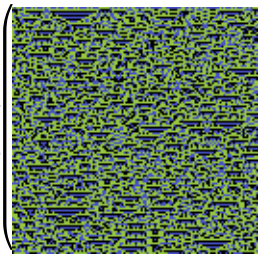


→ 4 111 476 009 175 → $\{4 \to 1.84666 \times 10^{-16}, 3 \to 1.\}$}

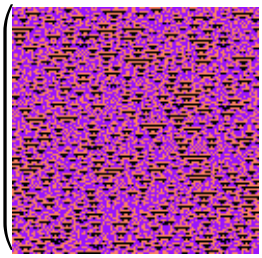
3-colour totalistic, range 2

In[ ]:=
```
test4Data3kr2C18 = datak3r2C[128, 128, 8];
Thread[test4Data3kr2C18 → netECA18[Keys@test4Data3kr2C18, {"TopProbabilities", 2}]]
```

Out[ ]=

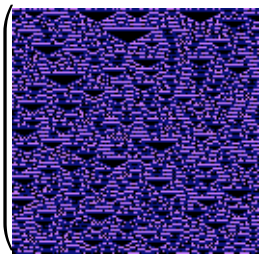


→ 101 105 → {4 → 1.49159 × 10^-7, 3 → 1.},

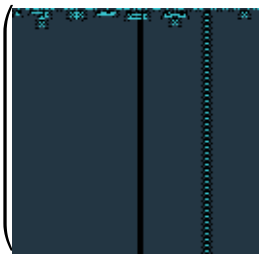


→ 48 212 → {4 → 3.39887 × 10^-8, 3 → 1.},

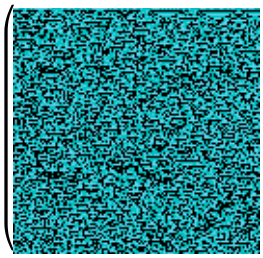
→ 81 243 → {2 → 6.61823 × 10^-15, 1 → 1.},



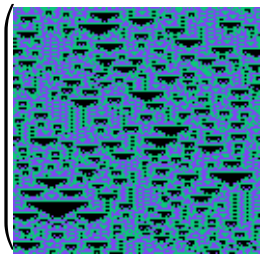
→ 144 952 → {4 → 5.58692 × 10^-14, 3 → 1.},



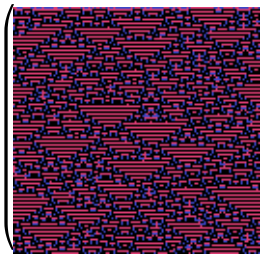
→ 167 730 → {1 → 3.79715 × 10^-7, 2 → 1.},



$\to 102\,220 \to \{4 \to 3.5215 \times 10^{-7},\ 3 \to 1.\},$



$\to 129\,071 \to \{4 \to 5.28522 \times 10^{-29},\ 3 \to 1.\},$

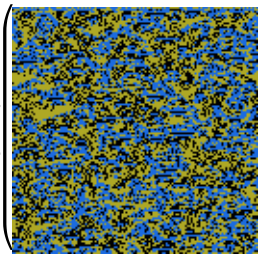


$\to 94\,027 \to \{4 \to 3.95426 \times 10^{-7},\ 3 \to 1.\}\}$

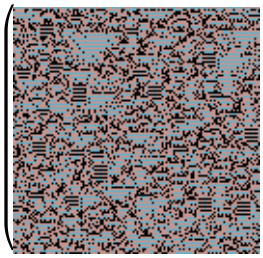
3-colour totalistic, range 3

In[ ]:=
```
test4Data3kr3C18 = datak3r3C[128, 128, 8];
Thread[test4Data3kr3C18 → netECA18[Keys@test4Data3kr3C18, {"TopProbabilities", 2}]]
```

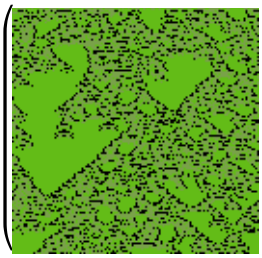
Out[ ]=



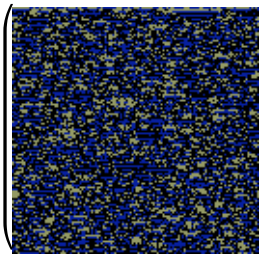
$\to 461\,960 \to \{4 \to 4.84455 \times 10^{-6},\ 3 \to 0.999995\},$



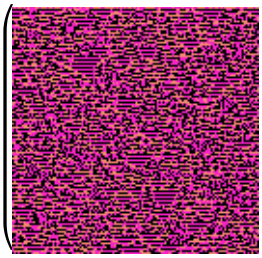
$\to 4\,823\,863 \to \{4 \to 1.80913 \times 10^{-22},\ 3 \to 1.\},$



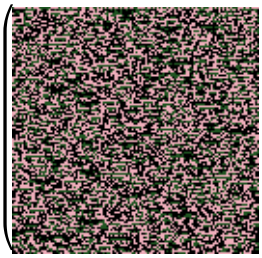
→ 7 272 180 → {3 → 3.43734 × 10^-9, 4 → 1.},



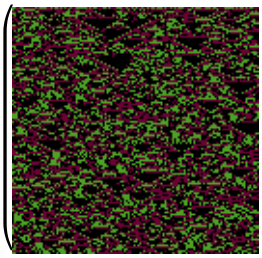
→ 8 672 980 → {4 → 6.70981 × 10^-6, 3 → 0.999993},



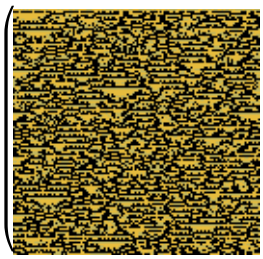
→ 254 357 → {4 → 2.17773 × 10^-6, 3 → 0.999998},



→ 9 226 537 → {4 → 1.70317 × 10^-12, 3 → 1.},



→ 13 913 899 → {4 → 1.88245 × 10^-14, 3 → 1.},

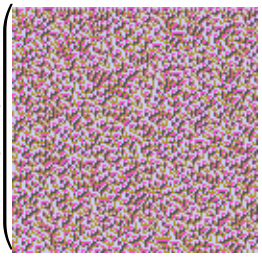


→ 2 641 642 → {4 → 1.17168 × 10^-16, 3 → 1.}

4-colour non-totalistic, range 1

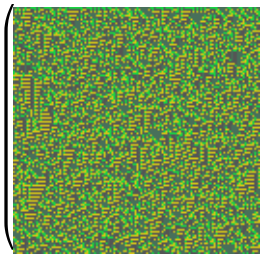
In[ ]:=
```
test4Data4kr1C18 = datak4r1NT[128, 128, 8];
Thread[test4Data4kr1C18 → netECA18[Keys@test4Data4kr1C18, {"TopProbabilities", 2}]]
```

Out[ ]=



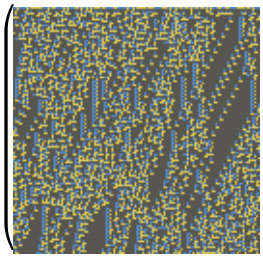
→ 102 061 531 028 325 101 056 411 203 373 159 921 153 →

{4 → 1.52655 × 10^-6, 3 → 0.999998},



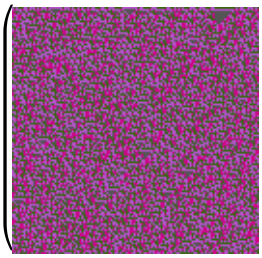
→ 220 826 430 777 843 014 546 276 939 581 509 597 468 →

{4 → 3.71156 × 10^-15, 3 → 1.},



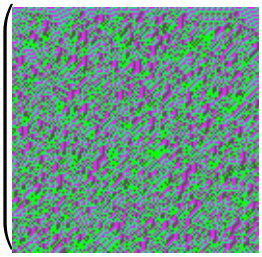
→ 189 759 227 742 452 338 669 016 752 488 159 725 978 →

{3 → 1.71606 × 10^-19, 4 → 1.},



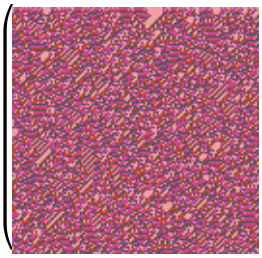
→ 39 086 343 891 936 177 646 298 077 938 677 400 893 →

{4 → 0.0000617923, 3 → 0.999938},



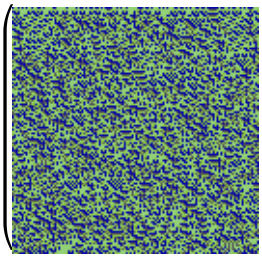
→ 325 561 419 730 770 765 208 110 988 081 624 688 453 →

$\{4 \to 4.25321 \times 10^{-7}, 3 \to 1.\}$,



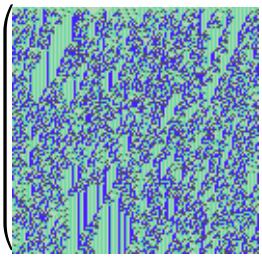
→ 247 405 682 417 519 114 838 497 454 468 289 242 544 →

$\{4 \to 3.94091 \times 10^{-12}, 3 \to 1.\}$,



→ 173 148 209 233 830 655 560 355 066 654 224 721 166 →

$\{4 \to 1.19081 \times 10^{-14}, 3 \to 1.\}$,



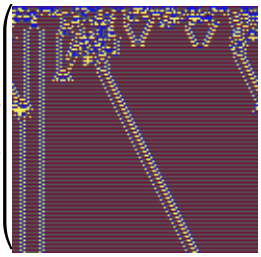
→ 272 790 974 570 863 467 026 653 486 918 315 112 723 →

$$\left\{3 \to 2.26679 \times 10^{-10},\ 4 \to 1.\right\}\Big\}$$

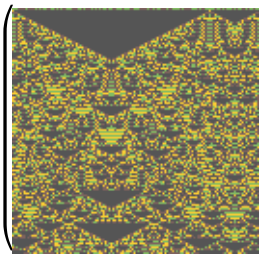
4-colour totalistic, range 2

In[ ]:=
```
test4Data4kr2C18 = datak4r2C[128, 128, 8];
Thread[test4Data4kr2C18 → netECA18[Keys@test4Data4kr2C18, {"TopProbabilities", 2}]]
```

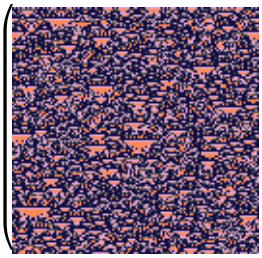
Out[ ]=



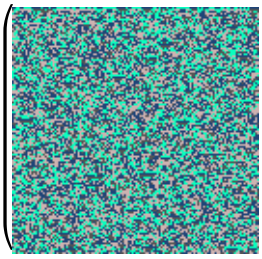
$\to 3\,511\,876\,239 \Big| \to \{2 \to 1.5807 \times 10^{-10},\ 4 \to 1.\},$



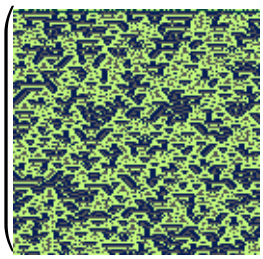
$\to 1\,629\,765\,289 \Big| \to \{4 \to 1.84811 \times 10^{-17},\ 3 \to 1.\},$

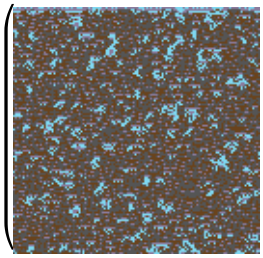


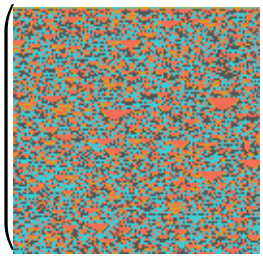
$\to 3\,309\,785\,711 \Big| \to \{4 \to 5.75659 \times 10^{-20},\ 3 \to 1.\},$

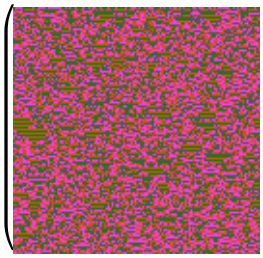


$\to 521\,880\,538 \Big| \to \{4 \to 2.42952 \times 10^{-8},\ 3 \to 1.\},$


→ 2 882 903 289 → {4 → 0.00262183, 3 → 0.997378},


→ 3 874 370 131 → {4 → 0.000817121, 3 → 0.999183},

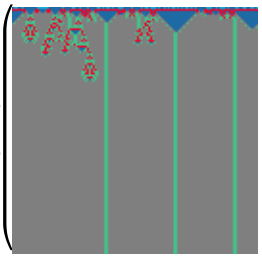

→ 3 978 874 812 → $\{4 \to 4.99897 \times 10^{-19}, 3 \to 1.\}$,

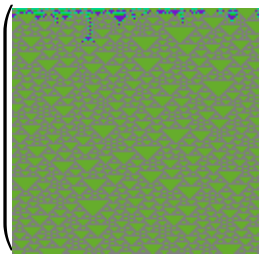

→ 1 758 609 338 → $\{4 \to 1.64955 \times 10^{-9}, 3 \to 1.\}$}

5-colour totalistic, range 1

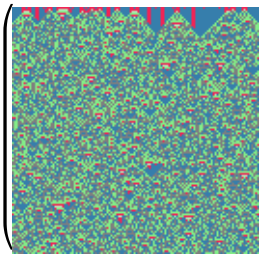
In[ ]:=
```
test4Data5kr1C18 = data5T2C[8, 128, 128];
Thread[test4Data5kr1C18 → netECA18[Keys@test4Data5kr1C18, {"TopProbabilities", 2}]]
```

Out[ ]=

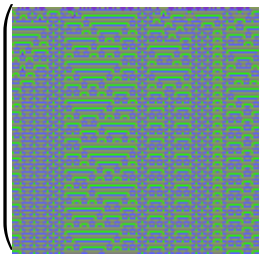

→ 419 338 996 → {4 → 0.471539, 2 → 0.528461},



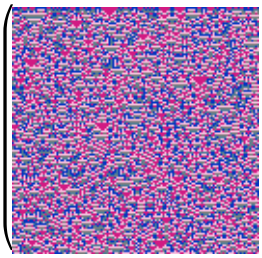
→ 884 788 964 → {4 → 0.0217201, 3 → 0.97828},



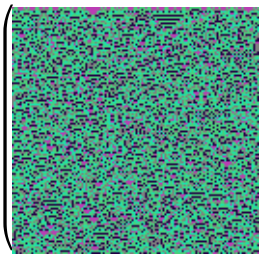
→ 743 542 029 → $\{3 \to 1.08355 \times 10^{-9}, 4 \to 1.\}$,



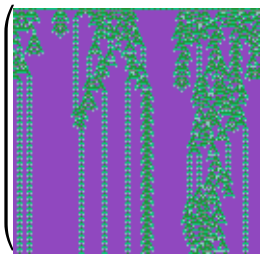
→ 782 108 342 → $\{4 \to 3.73846 \times 10^{-6}, 3 \to 0.999996\}$,



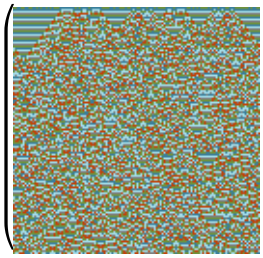
→ 785 621 045 → $\{4 \to 1.13554 \times 10^{-10}, 3 \to 1.\}$,



→ 540 834 160 → {4 → 0.0000100212, 3 → 0.99999},



→ 1 180 125 611 → {3 → 8.69272 × 10^-10, 4 → 1.},

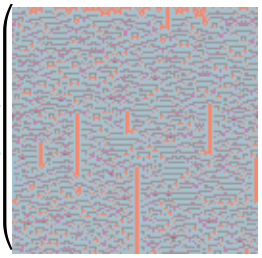


→ 604 699 906 → {4 → 5.02809 × 10^-11, 3 → 1.}}

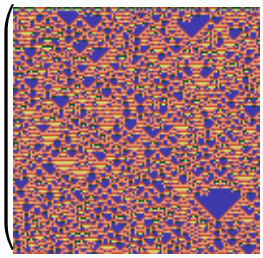
6-colour totalistic, range 1

In[ ]:=
```
test4Data6kr1C18 = data6TC[8, 128, 128];
Thread[test4Data6kr1C18 → netECA18[Keys@test4Data6kr1C18, {"TopProbabilities", 2}]]
```

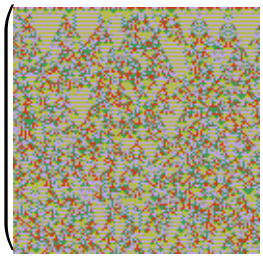
Out[ ]=



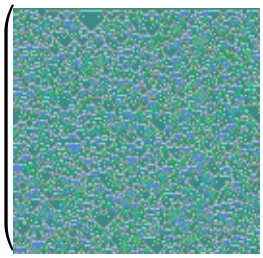
→ 1 598 104 240 744 → {4 → 0.385354, 3 → 0.614646},



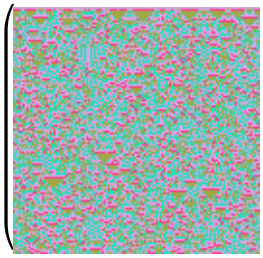
→ 2 744 610 103 617 → {4 → 4.14684 × 10^-12, 3 → 1.},



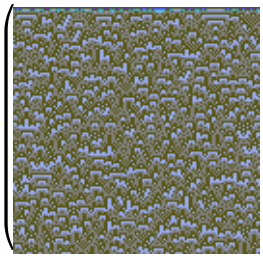
→ 2 679 723 007 553 → {4 → 0.0146554, 3 → 0.985345},



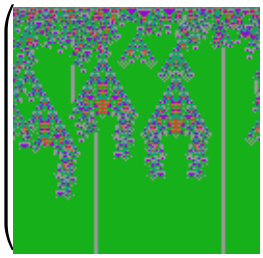
→ 333 206 194 422 → {4 → 1.77212 × 10^-6, 3 → 0.999998},



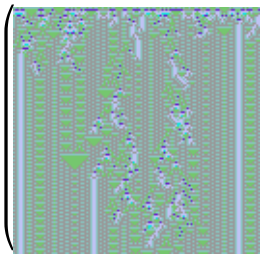
→ 385 745 608 648 → {4 → 4.96414 × 10^-18, 3 → 1.},



→ 1 376 556 791 013 → {4 → 1.60883 × 10^-6, 3 → 0.999998},



→ 1 497 722 744 619 → {2 → 5.2004 × 10^-22, 4 → 1.},

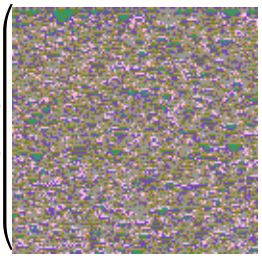


→ 1 461 122 595 667 → {4 → 0.0117104, 3 → 0.98829}}

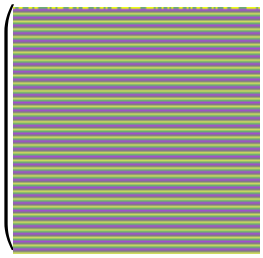
6-colour totalistic, range 2

In[ ]:=
```
test4Data6kr2C18 = data6T2C[8, 128, 128];
Thread[test4Data6kr2C18 → netECA18[Keys@test4Data6kr2C18, {"TopProbabilities", 2}]]
```

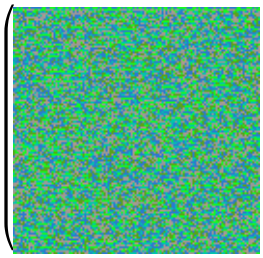
Out[ ]=



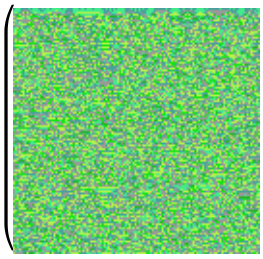
→ 94 758 619 520 606 075 339 → {4 → 3.45801 × 10^-14, 3 → 1.},



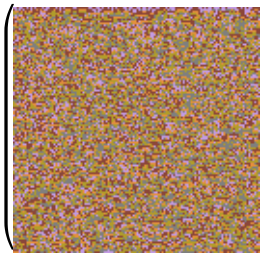
→ 20 009 329 597 666 396 569 → {1 → 0.000569901, 3 → 0.999395},



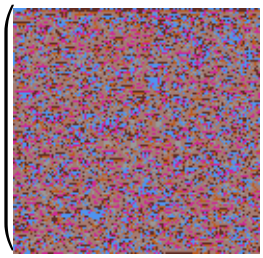
→ 143 751 744 015 528 766 387 → {4 → 4.63781 × 10^-12, 3 → 1.},



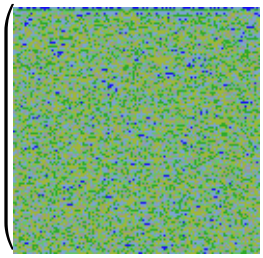
→ 14 907 007 420 911 525 245 → {4 → 2.71632 × 10^-7, 3 → 1.},



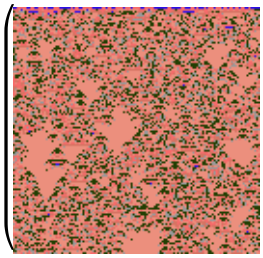
→ 153 725 842 134 059 084 151 → {4 → 8.53867 × 10^-11, 3 → 1.},



→ 21 849 107 846 366 361 856 → {4 → 4.26147 × 10^-8, 3 → 1.},



→ 39 897 609 306 289 130 946 → {4 → 3.43225 × 10^-8, 3 → 1.},

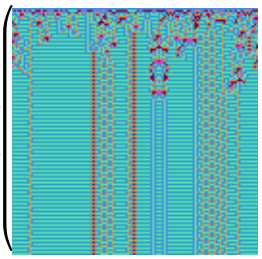


→ 24 452 844 112 980 510 505 → {3 → 2.30799 × 10^-17, 4 → 1.}}

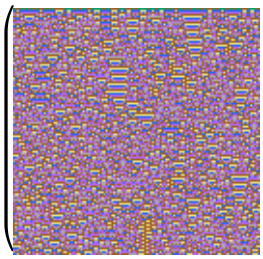
7-colour totalistic, range 1

In[ ]:=
```
test4Data7kr1C18 = data7TC[8, 128, 128];
Thread[test4Data7kr1C18 → netECA18[Keys@test4Data7kr1C18, {"TopProbabilities", 2}]]
```

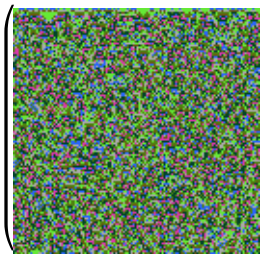
Out[ ]=



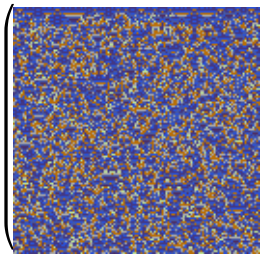
→ 9 377 524 399 313 965 → {3 → 1.74389 × 10^-8, 4 → 1.},



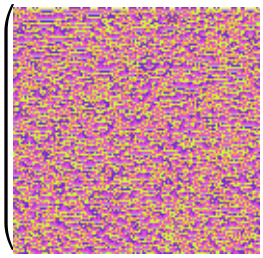
→ 4 962 953 862 340 599 → {4 → 0.0137316, 3 → 0.986268},



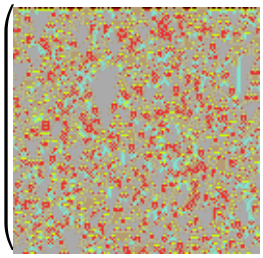
→ 8 745 570 953 687 246 → {4 → 2.19284 × 10^-7, 3 → 1.}},



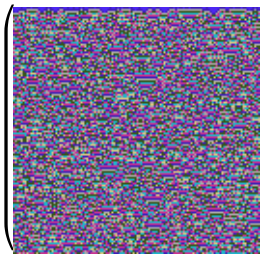
→ 5 868 018 872 447 407 → {4 → 0.000111761, 3 → 0.999888}},



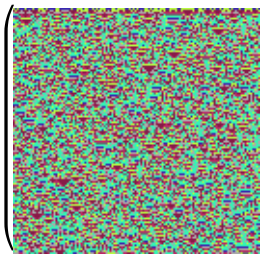
→ 4 309 418 628 605 253 → {4 → 1.75407 × 10^-6, 3 → 0.999998}},



→ 602 881 578 564 447 → {3 → 1.85106 × 10^-9, 4 → 1.}},



→ 2 664 890 136 425 923 → {4 → 3.52309 × 10^-12, 3 → 1.}},

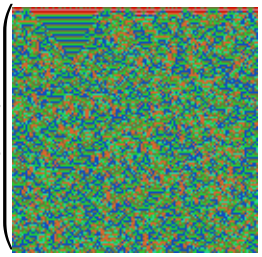


→ 2 116 828 975 265 896 → {4 → 3.12886 × 10^-9, 3 → 1.}}

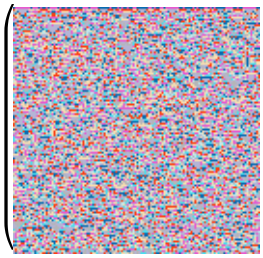
8-colour totalistic, range 1

In[ ]:=
```
test4Data8kr1C18 = data8TC[8, 128, 128];
Thread[test4Data8kr1C18 → netECA18[Keys@test4Data8kr1C18, {"TopProbabilities", 2}]]
```

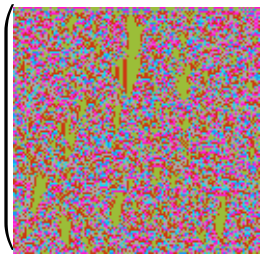
Out[ ]=



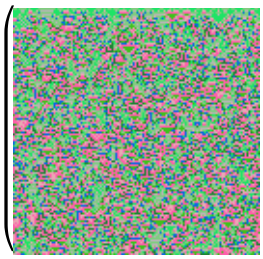
→ 4 354 635 422 940 040 188 → {4 → 0.0522672, 3 → 0.947733},



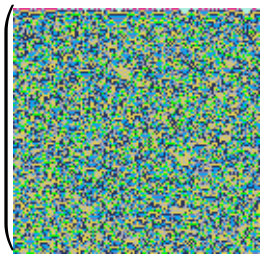
→ 69 178 369 869 620 121 447 → {4 → 1.13339 × 10^-12, 3 → 1.},

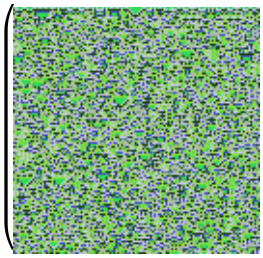


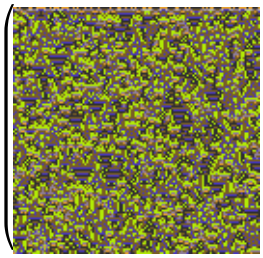
→ 52 954 223 906 783 093 008 → {3 → 7.29147 × 10^-15, 4 → 1.},

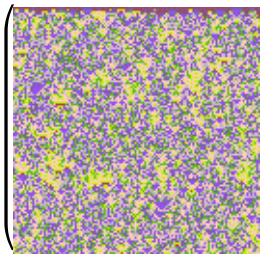


→ 68 658 165 468 973 438 000 → {4 → 1.9166 × 10^-11, 3 → 1.},

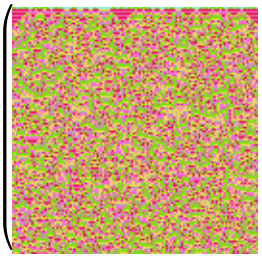

→ 40 882 704 313 683 534 715 → {4 → 0.0000183002, 3 → 0.999982},

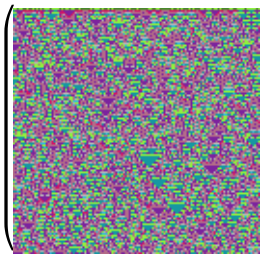

→ 4 334 236 228 138 547 400 → {4 → 1.8216 × 10^-12, 3 → 1.},


→ 38 056 813 477 139 716 563 → {4 → 0.025224, 3 → 0.974776},

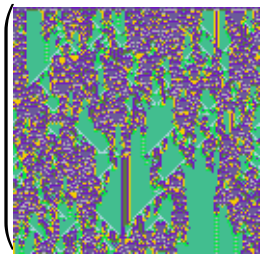

→ 17 144 034 197 046 476 300 → {4 → 1.1918 × 10^-10, 3 → 1.}}

In[ ]:=
```
test4Data8kr1C18 = data8TC[8, 128, 128];
Thread[test4Data8kr1C18 → netECA18[Keys@test4Data8kr1C18, {"TopProbabilities", 2}]]
```

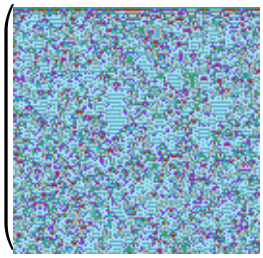
Out[ ]= { 
→ 27 295 602 810 117 462 452 → {4 → 1.93716 × 10^-14, 3 → 1.},



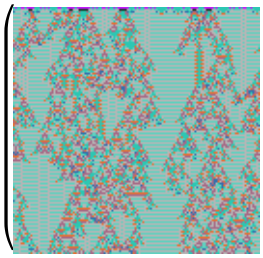
→ 68 187 226 482 692 112 227 → {4 → 1.97888 × 10^-15, 3 → 1.},



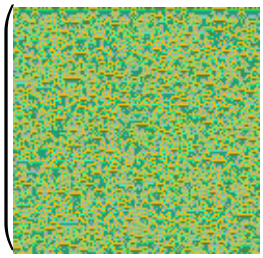
→ 26 338 422 679 712 858 793 → {2 → 1.54265 × 10^-15, 4 → 1.},



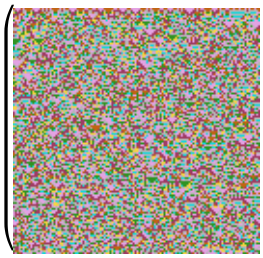
→ 20 106 191 194 925 098 456 → {4 → 1.32784 × 10^-9, 3 → 1.},



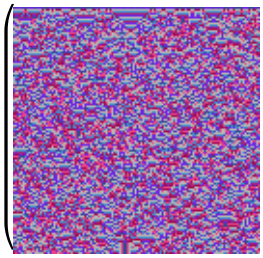
→ 27 427 530 853 867 733 909 → {3 → 7.69696 × 10^-6, 4 → 0.999992},



→ 67 626 281 665 658 424 537 → {4 → 1.31383 × 10^-8, 3 → 1.},



→ 25 326 375 293 896 897 208 → {4 → 9.39517 × 10^-8, 3 → 1.},

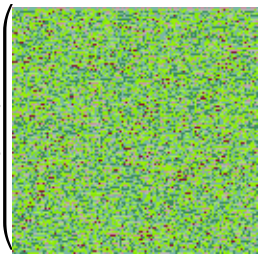


→ 17 284 363 590 068 343 962 → {4 → 0.000164327, 3 → 0.999836}}

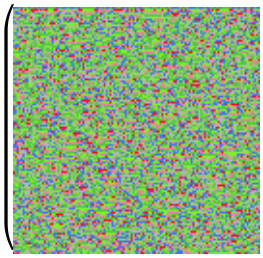
8-colour totalistic, range 2

In[ ]:=
```
test4Data8kr2C18 = data8T2C[8, 128, 128];
Thread[test4Data8kr2C18 → netECA18[Keys@test4Data8kr2C18, {"TopProbabilities", 2}]]
```

Out[ ]=

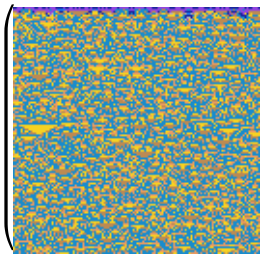


→ 91 605 229 994 459 866 473 701 555 510 459 → {4 → 8.95721 × 10^-9, 3 → 1.},



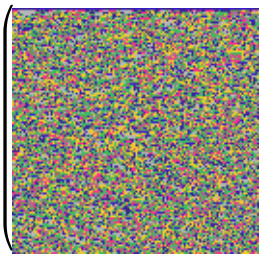
→ 148 194 329 210 486 766 360 332 149 681 908 →

{4 → 0.000259168, 3 → 0.999741},



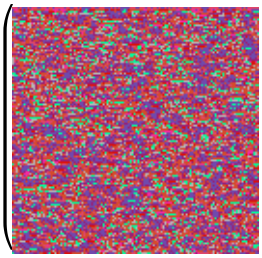
→ 312 941 122 843 853 005 350 894 081 598 045 →

$\{4 \to 3.01437 \times 10^{-25},\ 3 \to 1.\},$

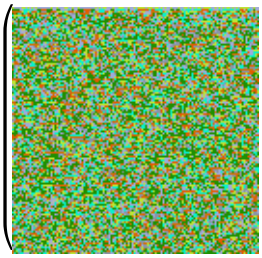


$\to 218\,758\,040\,018\,464\,082\,211\,209\,760\,600\,342 \to$

$\{4 \to 1.84707 \times 10^{-6},\ 3 \to 0.999998\},$

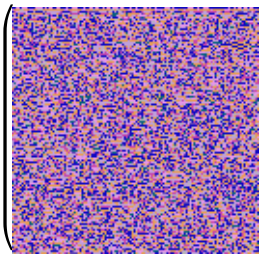


$\to 1\,618\,101\,134\,718\,809\,353\,656\,768\,953\,028 \to \{4 \to 8.91462 \times 10^{-12},\ 3 \to 1.\},$



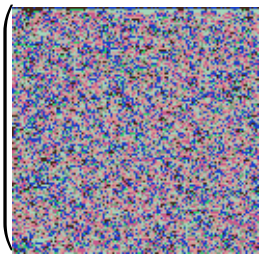
$\to 117\,778\,321\,396\,037\,048\,003\,724\,837\,215\,261 \to$

$\{4 \to 1.56349 \times 10^{-7},\ 3 \to 1.\},$



$\to 158\,334\,416\,764\,854\,082\,261\,529\,458\,487\,247 \to$

$\{3 \to 0.381514,\ 4 \to 0.618486\},$

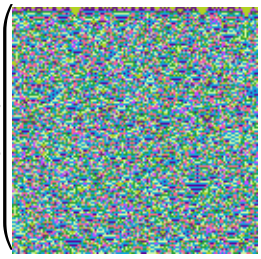


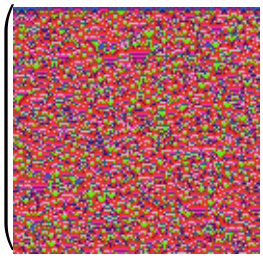
$\to 64\,962\,204\,199\,289\,039\,065\,352\,424\,560\,944 \to \{4 \to 3.15489 \times 10^{-10},\ 3 \to 1.\}\}$

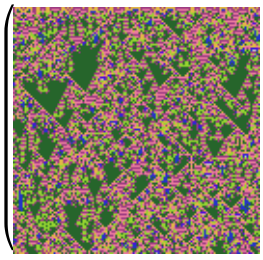
9-colour totalistic, range 1

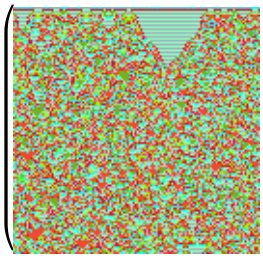
In[ ]:=
```
test4Data9kr1C18 = data9TC[8, 128, 128];
Thread[test4Data9kr1C18 → netECA18[Keys@test4Data9kr1C18, {"TopProbabilities", 2}]]
```

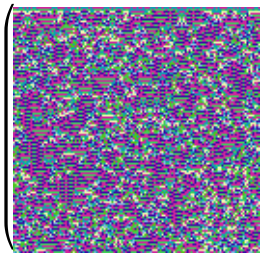
Out[ ]=

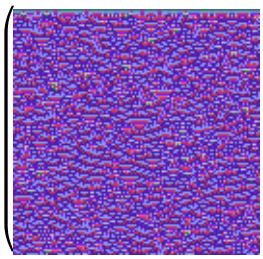

→ 522 568 741 028 775 861 250 602 → {4 → 1.89765 × 10^-9, 3 → 1.},

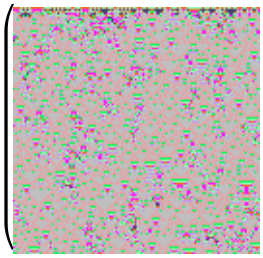

→ 150 105 663 552 960 221 109 656 → {4 → 8.50808 × 10^-11, 3 → 1.},

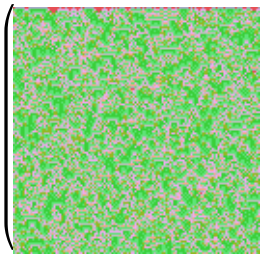

→ 177 646 283 305 699 098 325 471 → {3 → 2.75142 × 10^-13, 4 → 1.},


→ 649 888 623 407 447 388 665 878 → {4 → 9.1783 × 10^-8, 3 → 1.},


→ 572 736 978 221 231 214 545 140 → {4 → 1.19931 × 10^-8, 3 → 1.},

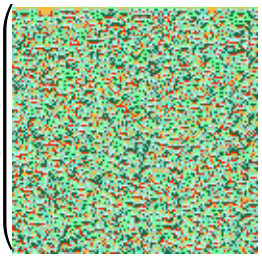

→ 577 735 506 397 144 743 916 701 → {4 → 5.16186 × 10^-6, 3 → 0.999995},

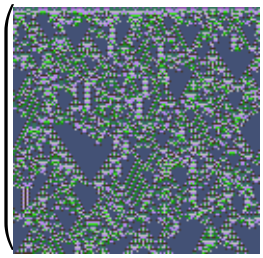

→ 38 290 460 957 561 945 226 664 → {4 → 0.0000332421, 3 → 0.999967},

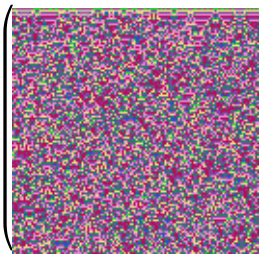

→ 65 266 980 214 577 653 296 276 → {4 → 2.0037 × 10^-9, 3 → 1.}}

In[ ]:=
```
test4Data9kr1C18 = data9TC[8, 128, 128];
Thread[test4Data9kr1C18 → netECA18[Keys@test4Data9kr1C18, {"TopProbabilities", 2}]]
```

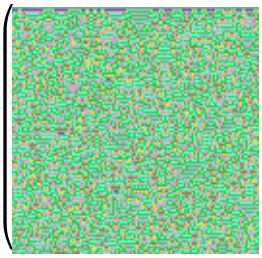
Out[ ]=


→ 376 251 875 419 739 043 750 089 → {4 → 8.56952 × 10^-8, 3 → 1.},

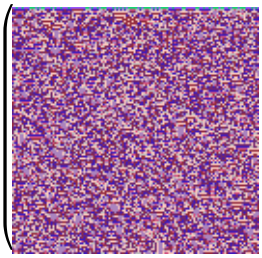

→ 292 480 217 936 066 672 681 870 → {3 → 5.77312 × 10^-11, 4 → 1.},



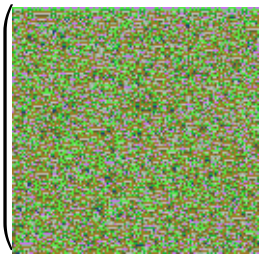
→ 641 652 971 419 956 634 593 698 → $\{4 \to 9.34668 \times 10^{-11}, 3 \to 1.\}$,



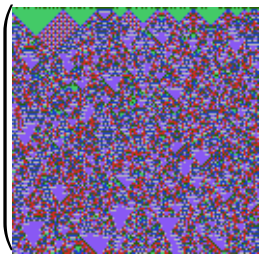
→ 560 384 664 222 257 507 134 238 → $\{4 \to 1.28321 \times 10^{-8}, 3 \to 1.\}$,



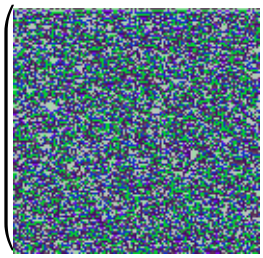
→ 431 262 759 200 417 990 085 248 → $\{4 \to 0.000429963, 3 \to 0.99957\}$,



→ 349 851 539 333 502 282 320 618 → $\{4 \to 5.50927 \times 10^{-7}, 3 \to 0.999999\}$,



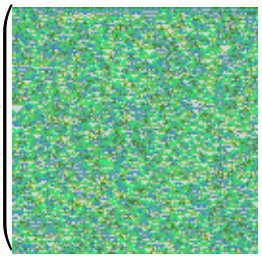
→ 141 618 270 878 027 879 702 319 → $\{4 \to 0.0000610287, 3 \to 0.999939\}$,



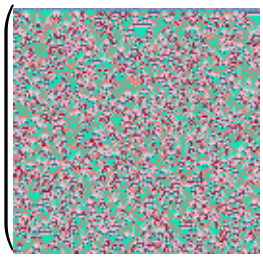
→ 401 516 309 538 894 848 288 118 → {4 → 6.7734 × 10^-12, 3 → 1.}}

In[ ]:=
```
test4Data9kr1C18 = data9TC[8, 128, 128];
Thread[test4Data9kr1C18 → netECA18[Keys@test4Data9kr1C18, {"TopProbabilities", 2}]]
```

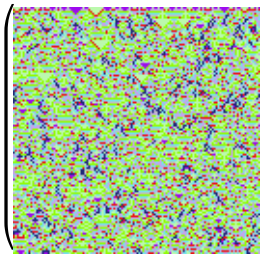
Out[ ]=

{ 

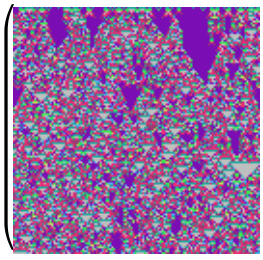
→ 102 484 955 339 910 707 201 065 → {4 → 2.85292 × 10^-12, 3 → 1.},



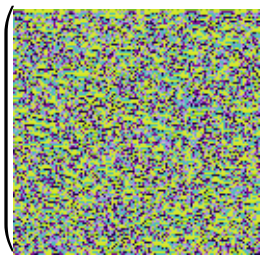
→ 225 104 493 515 167 213 968 116 → {4 → 2.59132 × 10^-19, 3 → 1.},



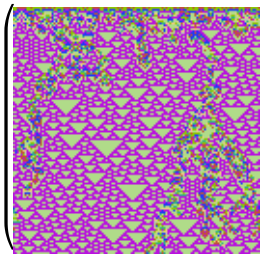
→ 82 955 736 870 484 114 072 206 → {4 → 7.69447 × 10^-10, 3 → 1.},



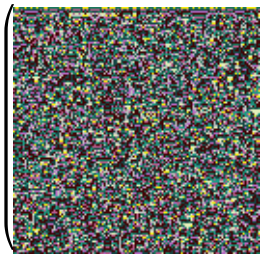
→ 671 885 429 563 685 913 440 220 → {3 → 0.0000324644, 4 → 0.999968},



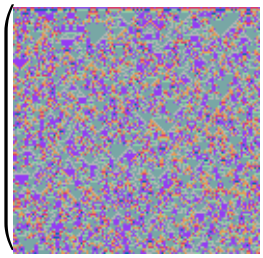
→ 319 540 285 313 900 469 182 543 → {4 → 1.25701 × 10^{-7}, 3 → 1.},



→ 472 683 159 387 864 865 560 932 → {4 → 0.0000136606, 3 → 0.999986},



→ 522 719 371 598 196 985 234 941 → {4 → 5.12875 × 10^{-11}, 3 → 1.},



→ 135 699 531 967 322 696 819 064 → {4 → 4.81907 × 10^{-12}, 3 → 1.}}

Network XX- Four convolutions, dropout on linear only, BatchNorm, MaxPool

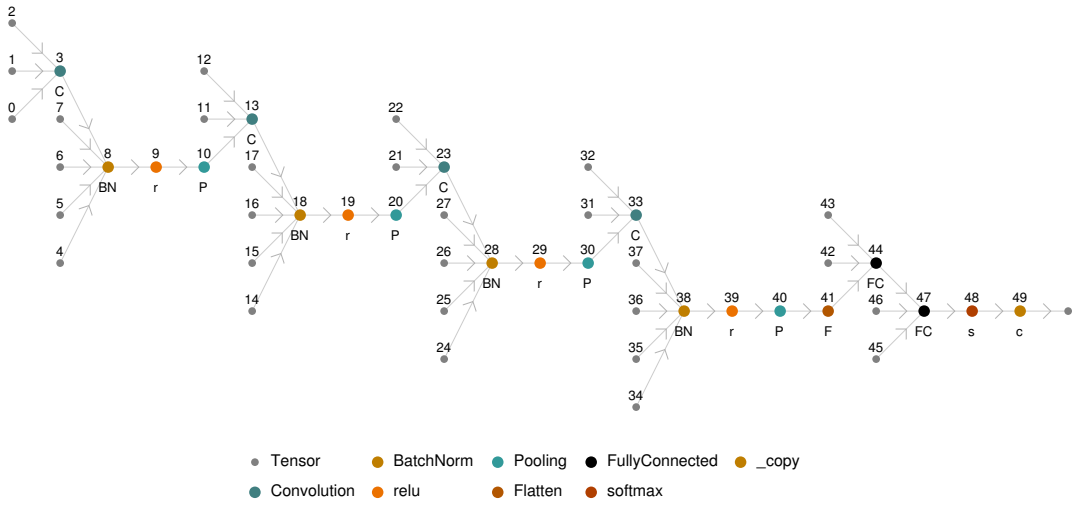
In[113]:=
```
netECA20 = netElevenCC1024drop[128, 128]
```

Out[113]= NetChain

	Input	image array (size: 3 × 128 × 128)
conv1	ConvolutionLayer	array (size: 24 × 126 × 126)
bat1	BatchNormalizationLayer	array (size: 24 × 126 × 126)
ramp1	Ramp	array (size: 24 × 126 × 126)
pooling1	PoolingLayer	array (size: 24 × 125 × 125)
conv2	ConvolutionLayer	array (size: 16 × 123 × 123)
bat2	BatchNormalizationLayer	array (size: 16 × 123 × 123)
ramp2	Ramp	array (size: 16 × 123 × 123)
pooling2	PoolingLayer	array (size: 16 × 122 × 122)
conv3	ConvolutionLayer	array (size: 12 × 120 × 120)
bat3	BatchNormalizationLayer	array (size: 12 × 120 × 120)
ramp3	Ramp	array (size: 12 × 120 × 120)
pooling3	PoolingLayer	array (size: 12 × 119 × 119)
conv4	ConvolutionLayer	array (size: 6 × 117 × 117)
bat4	BatchNormalizationLayer	array (size: 6 × 117 × 117)
ramp4	Ramp	array (size: 6 × 117 × 117)
pooling4	PoolingLayer	array (size: 6 × 86 × 86)
flatten	FlattenLayer	vector (size: 44376)
linear	LinearLayer	vector (size: 1024)
drop2	DropoutLayer	vector (size: 1024)
linear2	LinearLayer	vector (size: 4)
softmax	SoftmaxLayer	vector (size: 4)
	Output	class

In[114]:= `NetInformation[netECA20, "MXNetNodeGraphPlot"]`

Out[114]=



In[101]:= `NetInformation[netECA20, "SummaryGraphic"]`

Out[101]=

In[67]:= `dataECA19 = dataC[128, 128, 16 384];`

In[68]:= `dataTotalistic2BigC19 = genData2r2C[128, 128, 4096];`

In[69]:= `dataTotalistic3BigC19 = data3T2C[128, 128, 4096];`

In[70]:= `dataTotalistic4BigC19 = data4TC[128, 128, 4096];`

In[71]:= `dataTotalistic5BigC19 = genData5TCC[128, 128, 16 384];`

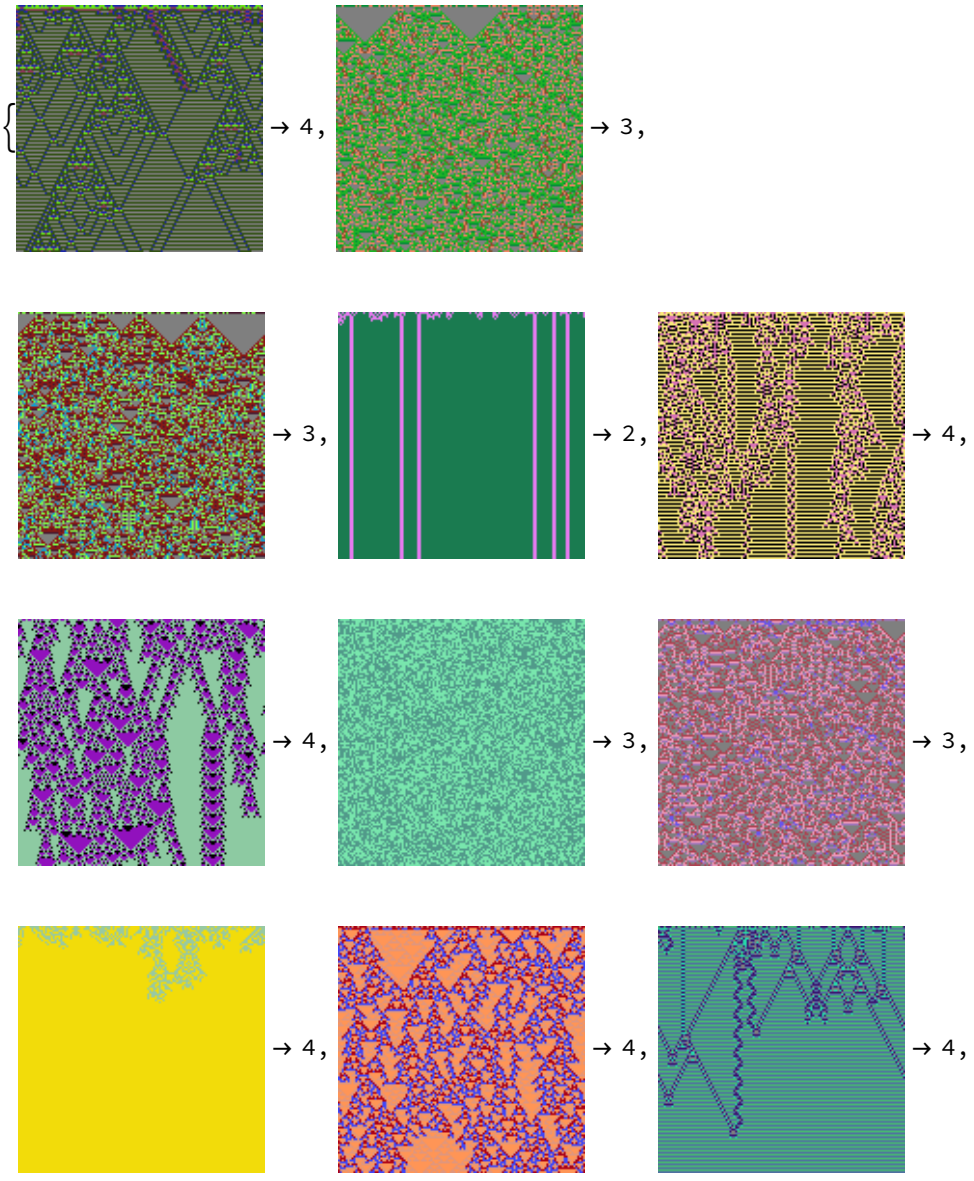
In[72]:=
```
fullTrainingBigC19 = Join[dataECA19, dataTotalistic2BigC19,
   dataTotalistic3BigC19, dataTotalistic4BigC19, dataTotalistic5BigC19];
```

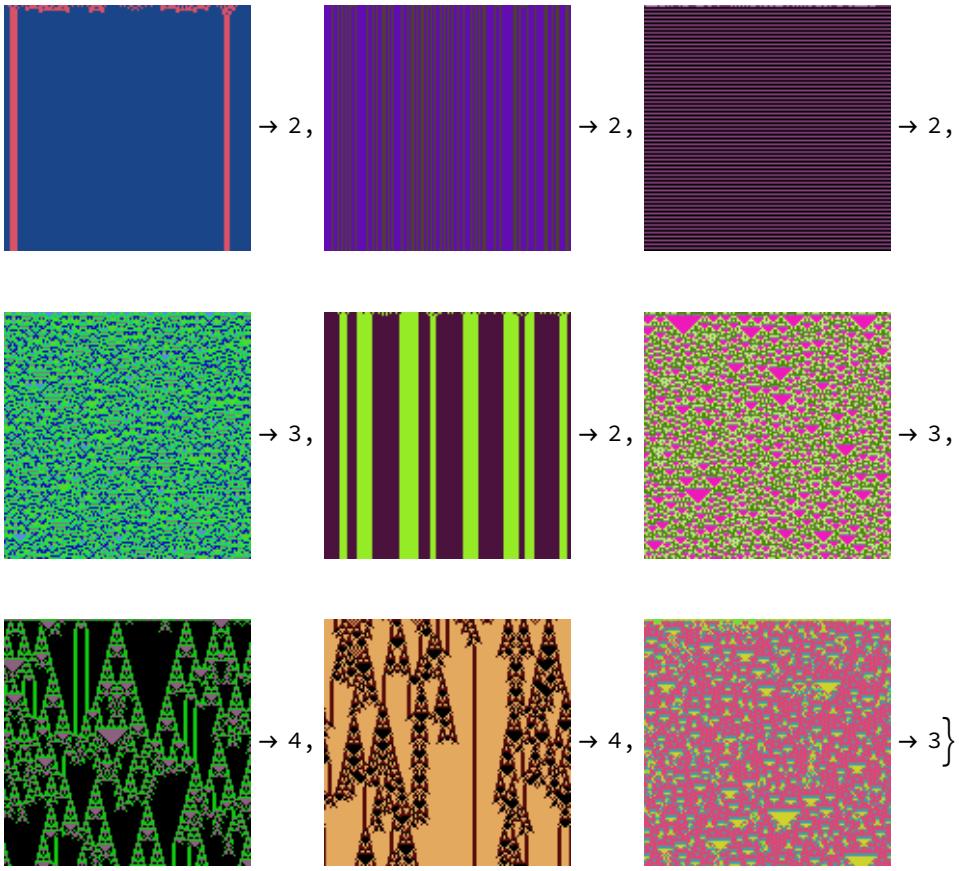
In[73]:=
```
Length[fullTrainingBigC19]
```

Out[73]= 90 112

In[89]:=
```
RandomSample[fullTrainingBigC19, 20]
```

Out[89]=





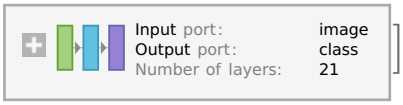
In[91]:=
```
dir = SetDirectory[NotebookDirectory[]]
```

Out[91]= /home/esilverman/Documents

In[ ]:=
```
"/home/esilverman/Documents"
```

Out[ ]= /home/esilverman/Documents

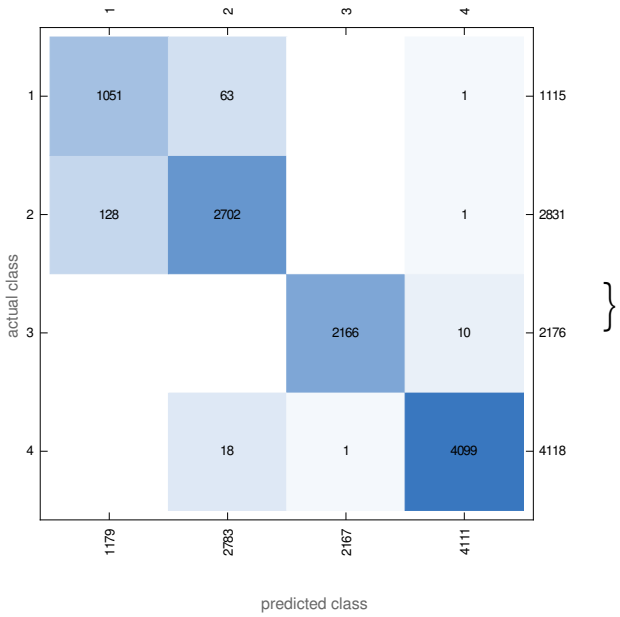
In[115]:=
```
netECA20 =
 NetTrain[netECA20, fullTrainingBigC19, MaxTrainingRounds → 200, BatchSize → 256,
  TargetDevice → "GPU", TrainingProgressCheckpointing → {"Directory", dir}]
```

Out[115]= NetChain[]

In[116]:=
```
netECA20 = Import["netECA20-r200.wlnet"]
```

In[128]:=
```
NetMeasurements[netECA20, fullTestSetBigC,
 {"Accuracy", "Precision", "ConfusionMatrixPlot"}]
```

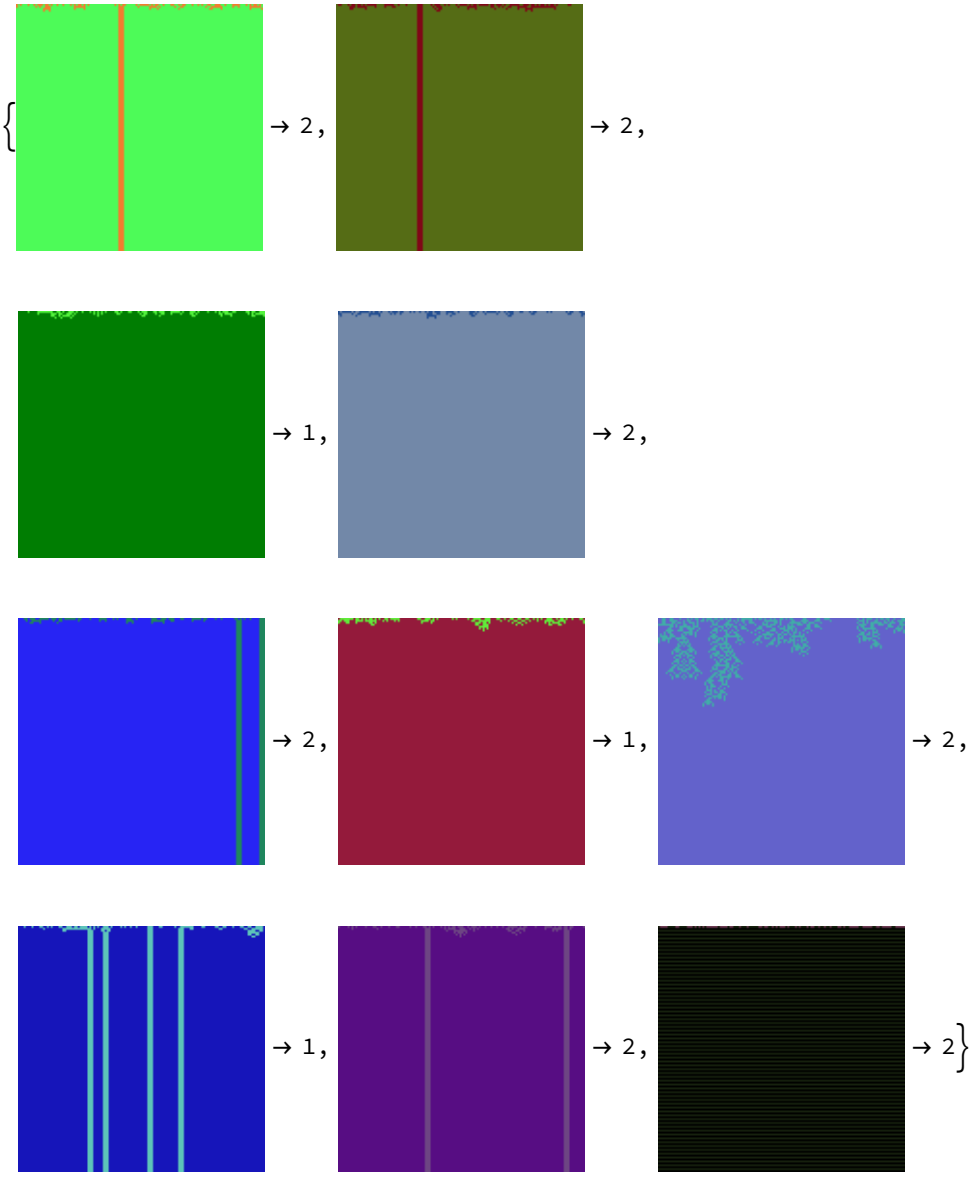
Out[128]=
```
{0.97832, <|1 → 0.891433, 2 → 0.970895, 3 → 0.999539, 4 → 0.997081|>,
```



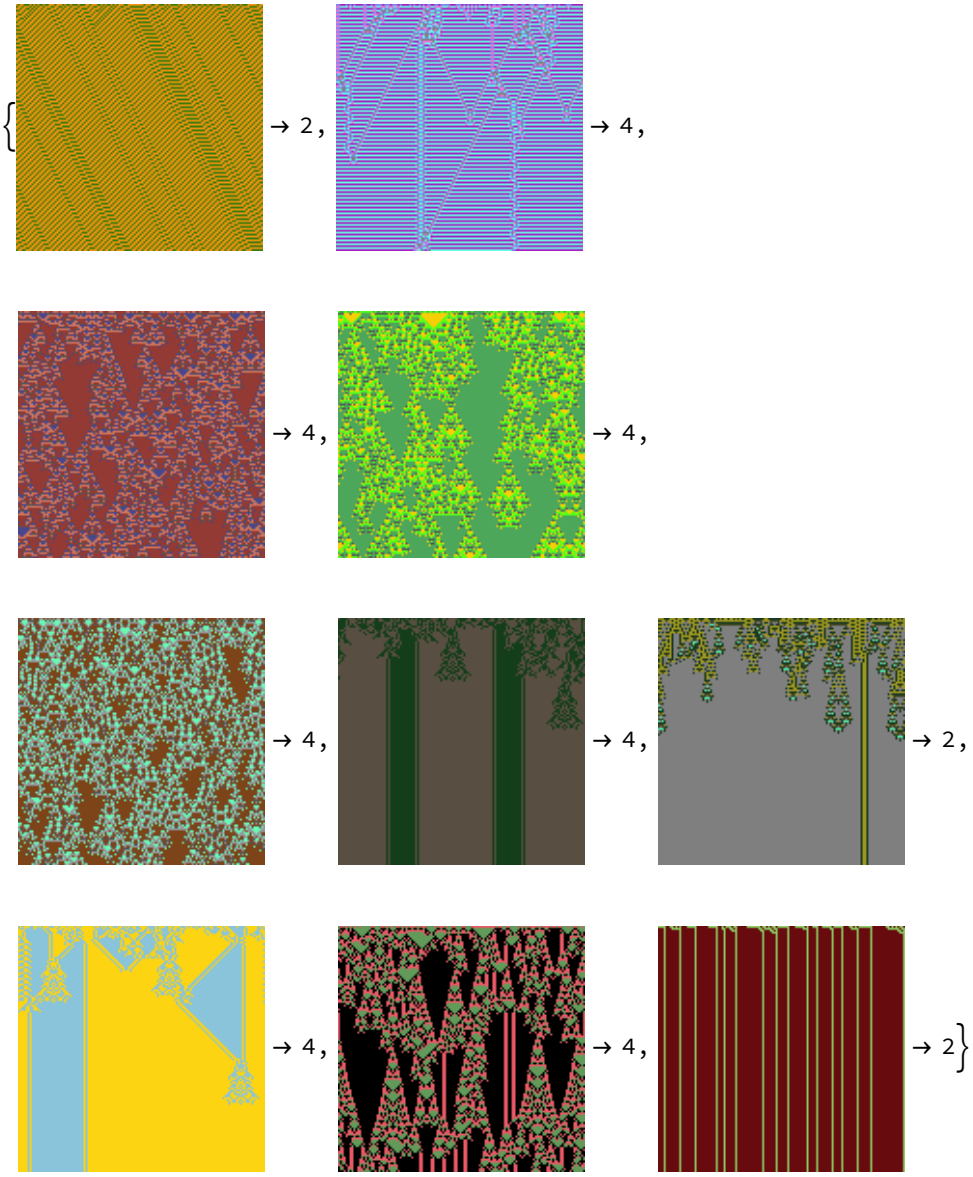

```
}
```

In[129]:=
```
entropyImagesBigC = RandomSample[Keys[fullTestSetBigC], 500];
entropiesBigC = netECA20[entropyImagesBigC, "Entropy"];
highEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, -10]]];
lowEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, 10]]];
Thread[highEntBigC → netECA20[highEntBigC]]
Thread[lowEntBigC → netECA20[lowEntBigC]]
```

Out[133]=



Out[134]=



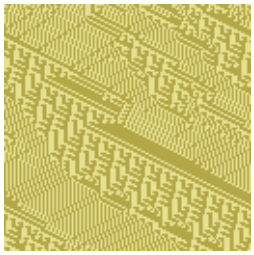
New Format for Unseen CA Testing

Testing Network XX (200 epochs) on unseen CA rule spaces - V2

2-colour non-totalistic, range 2

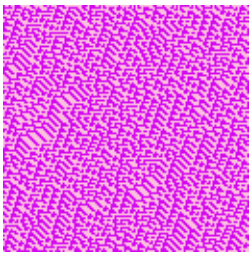
In[117]:=
```
test4Data2kr2C20 = datak2r2C[128, 128, 8];
test4Data2kr2C20labeled = Thread[
   Labeled[Keys@test4Data2kr2C20, Values@test4Data2kr2C20, LabelStyle → Small]];
Thread[test4Data2kr2C20labeled → netECA20[Keys@test4Data2kr2C20,
   {"TopProbabilities", 2}]]
```

Out[119]=



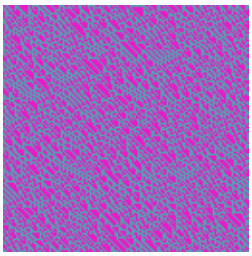
→ {4 → 2.2304 × 10^-29, 3 → 1.},

367 084 468



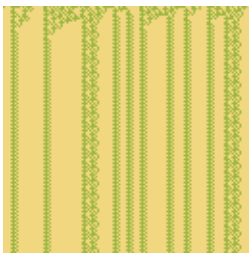
→ {4 → 0.0033, 3 → 0.9967},

1 379 242 519



→ {4 → 8.86727 × 10^-7, 3 → 0.999999},

4 162 051 619

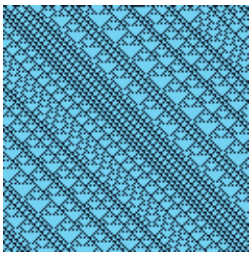


$\to \{1 \to 8.2126 \times 10^{-18}, 2 \to 1.\},$

3 514 891 567

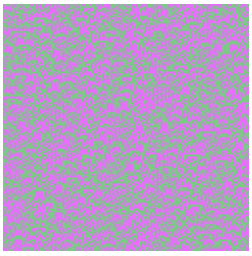
$\to \{4 \to 3.61159 \times 10^{-10}, 3 \to 1.\},$

866 396 076



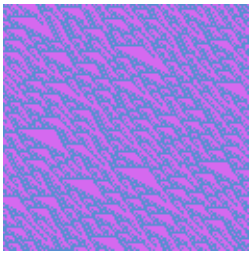
$\to \{1 \to 2.20806 \times 10^{-13}, 2 \to 1.\},$

3 744 518 143



$\to \{4 \to 4.93742 \times 10^{-17}, 3 \to 1.\},$

2 025 491 845



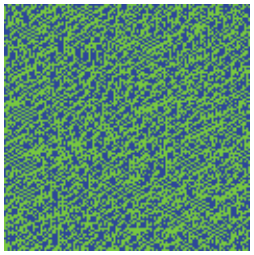
$\to \{2 \to 2.45739 \times 10^{-17}, 3 \to 1.\}\}$

4 265 753 027

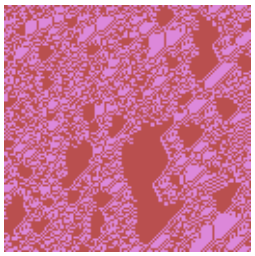
2-colour non-totalistic, range 3

In[135]:=
```
test4Data2kr3C20 = datak2r3NT[128, 128, 8];
test4Data2kr3C20labeled = Thread[
   Labeled[Keys@test4Data2kr3C20, Values@test4Data2kr3C20, LabelStyle → Small]];
Thread[test4Data2kr3C20labeled → netECA20[Keys@test4Data2kr3C20,
   {"TopProbabilities", 2}]]
```

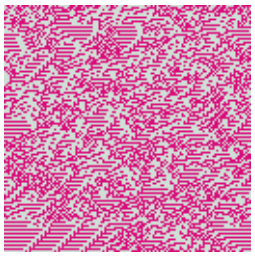
Out[137]=

{  → {4 → 5.58562 × 10^-16, 3 → 1.},

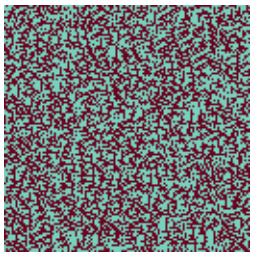
175 317 046 607 140 904 612 401 164 365 202 322 905

 → {3 → 1.03991 × 10^-17, 4 → 1.},

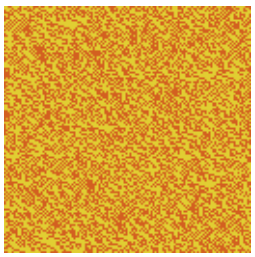
333 939 423 792 192 096 545 032 285 851 149 853 032

 → {4 → 4.23796 × 10^-36, 3 → 1.},

167 940 034 577 996 242 635 820 510 011 809 194 683

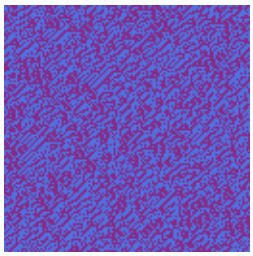
 → {4 → 4.92413 × 10^-22, 3 → 1.},

46 848 245 467 759 890 662 874 287 768 760 318 922



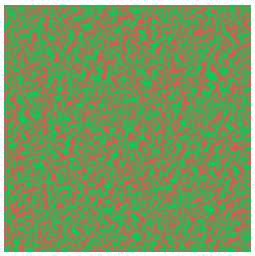
$\to \{4 \to 1.23357 \times 10^{-11}, 3 \to 1.\},$

285 094 920 214 522 408 031 701 099 217 938 232 744



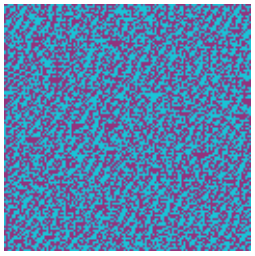
$\to \{4 \to 5.99548 \times 10^{-12}, 3 \to 1.\},$

75 936 807 861 750 066 397 325 972 543 865 321 227



$\to \{4 \to 1.45902 \times 10^{-6}, 3 \to 0.999999\},$

172 161 847 410 071 222 924 260 847 522 764 729 669



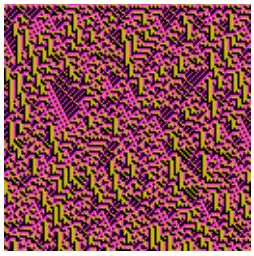
$\to \{4 \to 4.27078 \times 10^{-17}, 3 \to 1.\}\}$

260 689 717 174 866 318 397 438 350 620 887 242 168

3-colour non-totalistic, range 1

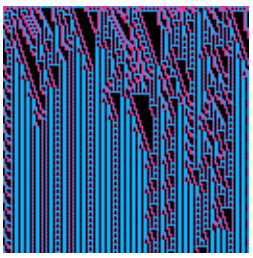
In[138]:=
```
test4Data3kr1C20 = datak3r1NT[128, 128, 8];
test4Data3kr1C20labeled = Thread[
   Labeled[Keys@test4Data3kr1C20, Values@test4Data3kr1C20, LabelStyle → Small]];
Thread[test4Data3kr1C20labeled → netECA20[Keys@test4Data3kr1C20,
   {"TopProbabilities", 2}]]
```

Out[140]=



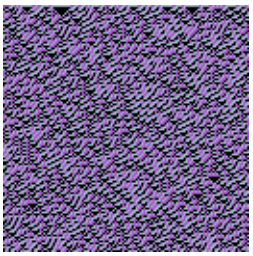
$\to \{4 \to 1.4644 \times 10^{-9}, 3 \to 1.\},$

1 943 525 046 013



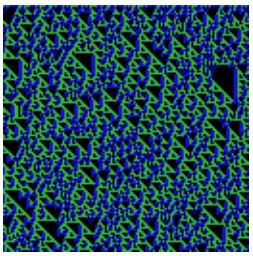
$\to \{2 \to 9.80909 \times 10^{-45}, 4 \to 1.\},$

7 420 171 714 826



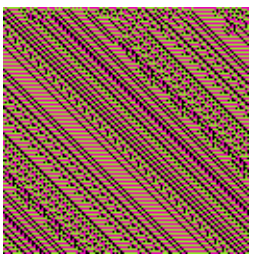
$\to \{4 \to 1.01109 \times 10^{-8}, 3 \to 1.\},$

6 476 551 191 581



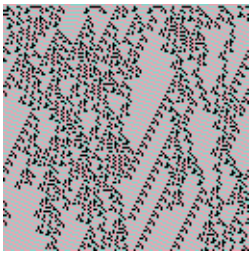
$\to \{4 \to 1.42896 \times 10^{-12}, 3 \to 1.\},$

5 667 424 638 140

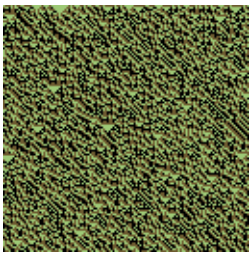


$\to \{4 \to 0.0000932045, 2 \to 0.999874\},$

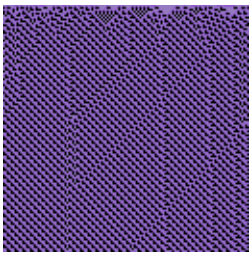
5 524 186 457 545



1 193 518 496 548 → {3 → 7.98056 × 10^-12, 4 → 1.},



1 606 486 300 315 → {4 → 1.45155 × 10^-15, 3 → 1.},

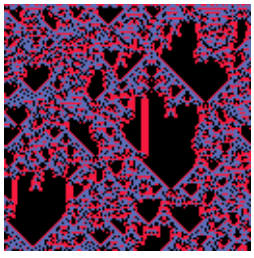


3 583 847 104 000 → {3 → 0.165043, 4 → 0.834957}

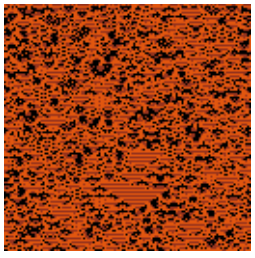
3-colour totalistic, range 2

In[141]:=
```
test4Data3kr2C20 = datak3r2C[128, 128, 8];
test4Data3kr2C20labeled = Thread[
   Labeled[Keys@test4Data3kr2C20, Values@test4Data3kr2C20, LabelStyle → Small]];
Thread[test4Data3kr2C20labeled → netECA20[Keys@test4Data3kr2C20,
   {"TopProbabilities", 2}]]
```

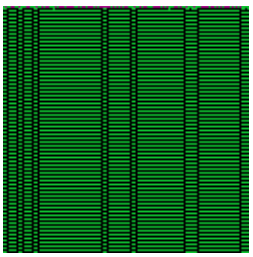
Out[143]=



173 671 → {1 → 0., 4 → 1.},

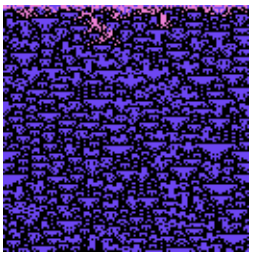


77 293 → {4 → 2.37724 × 10^-22, 3 → 1.},



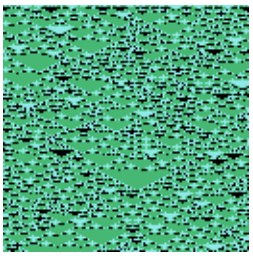
21 377

$\to \{1 \to 1.04919 \times 10^{-13}, 2 \to 1.\},$



56 667

$\to \{4 \to 2.82448 \times 10^{-10}, 3 \to 1.\},$

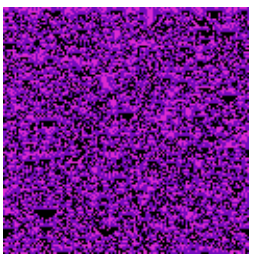


127 893

$\to \{1 \to 0., 3 \to 1.\},$

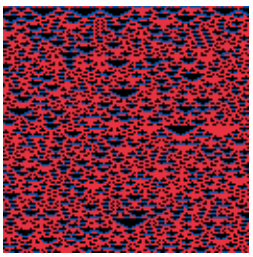
72 852

$\to \{3 \to 5.87496 \times 10^{-21}, 4 \to 1.\},$



134 006

$\to \{4 \to 5.31289 \times 10^{-37}, 3 \to 1.\},$



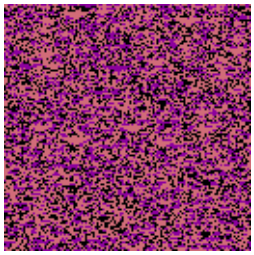
146 607

$\to \{4 \to 3.56902 \times 10^{-7}, 3 \to 1.\}\}$

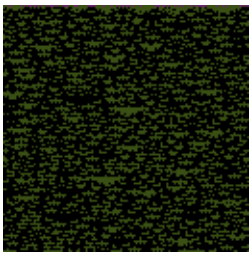
3-colour totalistic, range 3

In[144]:=
```
test4Data3kr3C20 = datak3r3C[128, 128, 8];
test4Data3kr3C20labeled = Thread[
   Labeled[Keys@test4Data3kr3C20, Values@test4Data3kr3C20, LabelStyle → Small]];
Thread[test4Data3kr3C20labeled → netECA20[Keys@test4Data3kr3C20,
   {"TopProbabilities", 2}]]
```

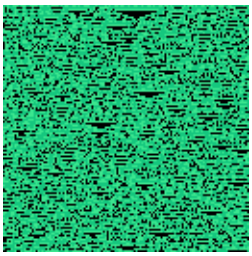
Out[146]=



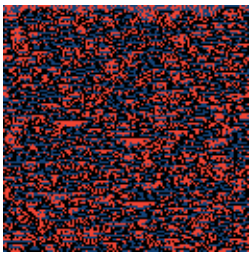
6 223 536 → {4 → 7.7582 × 10^-11, 3 → 1.},



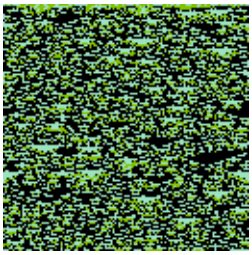
12 731 650 → {3 → 8.81735 × 10^-6, 4 → 0.999991},



9 770 921 → {4 → 2.7394 × 10^-28, 3 → 1.},

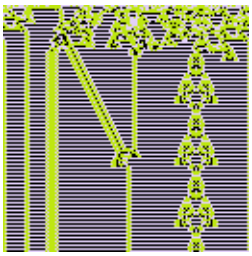


871 980 → {4 → 1.69056 × 10^-14, 3 → 1.},



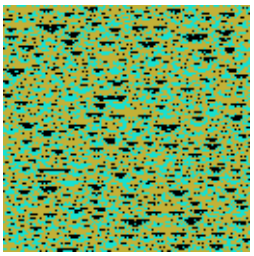
$\to \{4 \to 5.30067 \times 10^{-26}, 3 \to 1.\},$

13 165 143



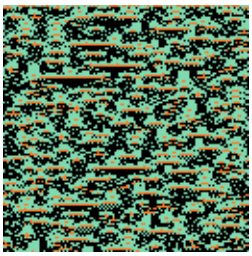
$\to \{1 \to 0., 4 \to 1.\},$

25 136



$\to \{4 \to 1.36329 \times 10^{-11}, 3 \to 1.\},$

9 450 771



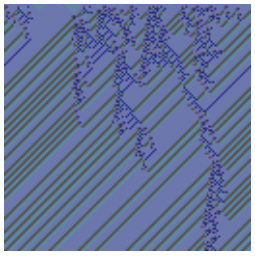
$\to \{4 \to 6.18499 \times 10^{-21}, 3 \to 1.\}\}$

11 473 546

4-colour non-totalistic, range 1

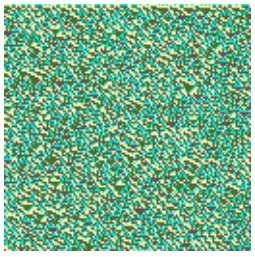
In[156]:=
```
test4Data4kr1C20 = datak4r1NT[128, 128, 8];
test4Data4kr1C20labeled = Thread[
   Labeled[Keys@test4Data4kr1C20, Values@test4Data4kr1C20, LabelStyle → Small]];
Thread[test4Data4kr1C20labeled → netECA20[Keys@test4Data4kr1C20,
   {"TopProbabilities", 2}]]
```

Out[158]=

$\{$ 

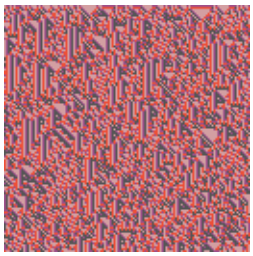
$\to \{4 \to 3.30248 \times 10^{-7}, 2 \to 1.\},$

66 798 888 009 362 444 760 733 244 837 359 231 165



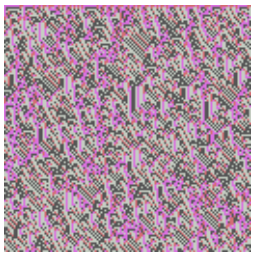
$\to \{4 \to 1.10829 \times 10^{-25}, 3 \to 1.\},$

306 719 859 071 756 487 947 088 377 520 725 503 027



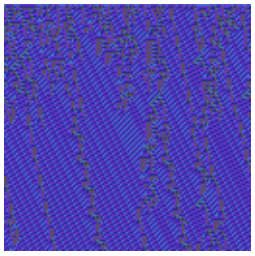
$\to \{3 \to 5.60172 \times 10^{-20}, 4 \to 1.\},$

31 243 239 385 070 099 510 344 350 901 399 068 656



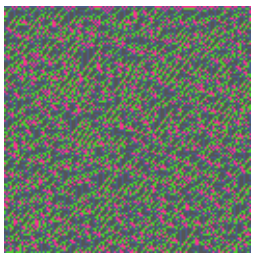
$\to \{4 \to 2.90225 \times 10^{-9}, 3 \to 1.\},$

255 083 844 223 499 044 791 265 916 871 791 704 013



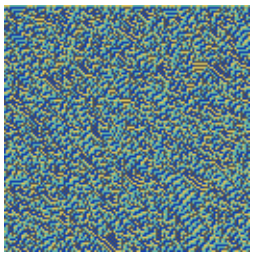
$\to \{4 \to 0.0131354, 3 \to 0.986863\},$

170 807 760 445 342 455 444 052 297 814 626 991 307



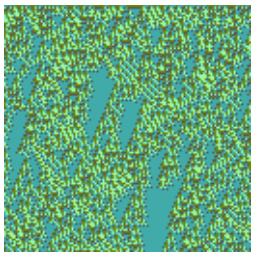
$\to \{4 \to 9.58918 \times 10^{-15}, 3 \to 1.\},$

234 183 748 902 969 287 076 764 247 530 943 795 214



$\to \{4 \to 1.92129 \times 10^{-6}, 3 \to 0.999998\},$

87 456 539 974 696 374 004 631 614 755 284 156 054



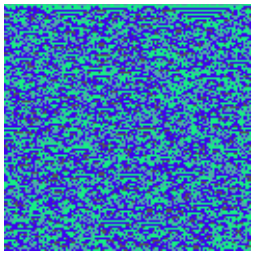
$\to \{3 \to 1.20497 \times 10^{-34}, 4 \to 1.\}\}$

259 436 914 968 037 895 094 402 944 856 604 631 010

4-colour totalistic, range 2

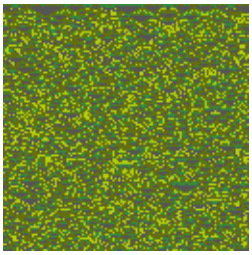
In[165]:=
```
test4Data4kr2C20 = datak4r2C[128, 128, 8];
test4Data4kr2C20labeled = Thread[
   Labeled[Keys@test4Data4kr2C20, Values@test4Data4kr2C20, LabelStyle → Small]];
Thread[test4Data4kr2C20labeled → netECA20[Keys@test4Data4kr2C20,
   {"TopProbabilities", 2}]]
```

Out[167]=



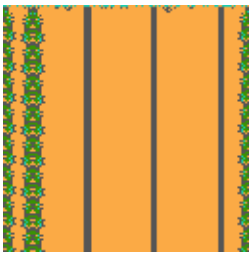
$\to \{4 \to 1.29089 \times 10^{-19}, 3 \to 1.\},$

852 327 439



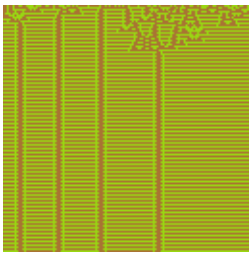
98 907 810

$\to \{4 \to 8.49412 \times 10^{-14}, 3 \to 1.\},$



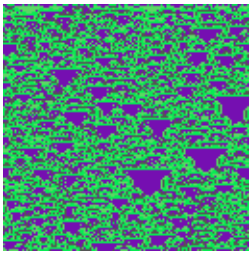
2 901 860 480

$\to \{3 \to 1.21847 \times 10^{-15}, 4 \to 1.\},$



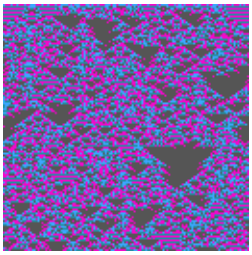
932 946 181

$\to \{2 \to 6.21748 \times 10^{-8}, 4 \to 1.\},$



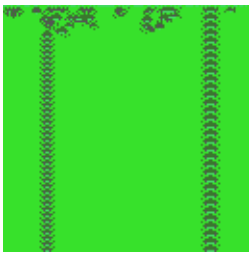
4 048 925 244

$\to \{4 \to 3.92905 \times 10^{-14}, 3 \to 1.\},$



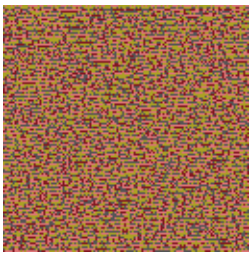
1 219 043 275

$\to \{4 \to 2.46516 \times 10^{-9}, 3 \to 1.\},$



3 616 075 824

$\to \{2 \to 0.0000874763, 4 \to 0.999913\},$

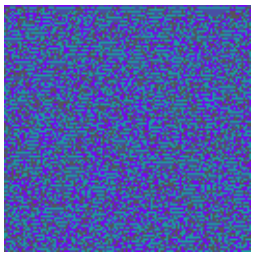


1 712 383 591

$\to \{4 \to 0.0000848748, 3 \to 0.999915\}\Big\}$

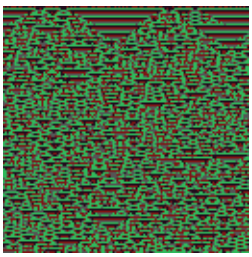
In[168]:=
```
test4Data4kr2C20 = datak4r2C[128, 128, 8];
test4Data4kr2C20labeled = Thread[
   Labeled[Keys@test4Data4kr2C20, Values@test4Data4kr2C20, LabelStyle → Small]];
Thread[test4Data4kr2C20labeled → netECA20[Keys@test4Data4kr2C20,
   {"TopProbabilities", 2}]]
```

Out[170]=

$\Big\{$ 

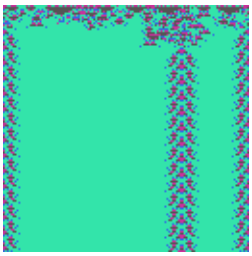
114 483 132

$\to \{4 \to 2.89317 \times 10^{-13}, 3 \to 1.\},$



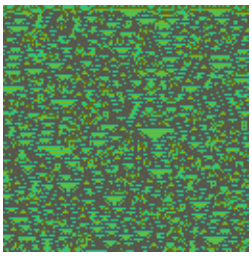
$\to \{4 \to 3.70507 \times 10^{-17}, 3 \to 1.\},$

1 354 752 510



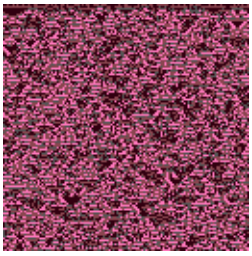
$\to \{2 \to 1.32739 \times 10^{-22}, 4 \to 1.\},$

1 348 564 386



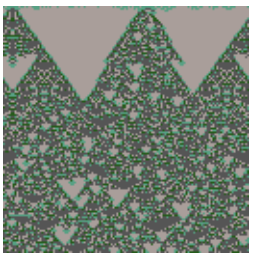
$\to \{4 \to 6.08254 \times 10^{-17}, 3 \to 1.\},$

1 502 784 775



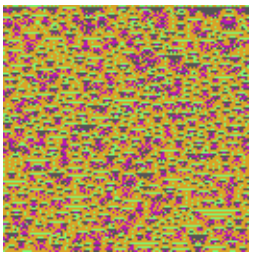
$\to \{4 \to 0.000100592, 3 \to 0.999899\},$

2 441 474 580



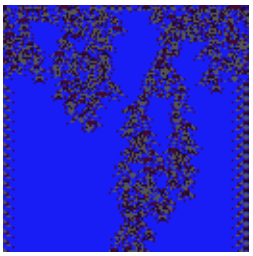
→ {4 → 0.00203915, 3 → 0.997961},

1 651 030 272



→ $\{4 \to 3.49291 \times 10^{-8}, 3 \to 1.\}$,

3 899 478 445



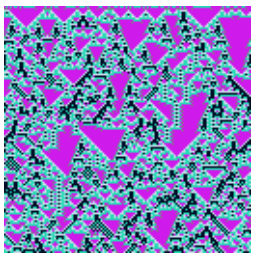
→ $\left\{3 \to 6.29676 \times 10^{-35}, 4 \to 1.\right\}\}$

690 898 352

5-colour totalistic, range 1

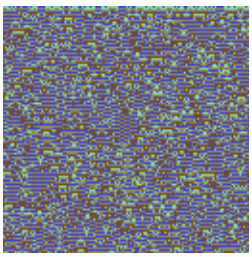
In[171]:=
```
test4Data5kr1C20 = data5T2C[8, 128, 128];
test4Data5kr1C20labeled = Thread[
   Labeled[Keys@test4Data5kr1C20, Values@test4Data5kr1C20, LabelStyle → Small]];
Thread[test4Data5kr1C20labeled → netECA20[Keys@test4Data5kr1C20,
   {"TopProbabilities", 2}]]
```

Out[173]=



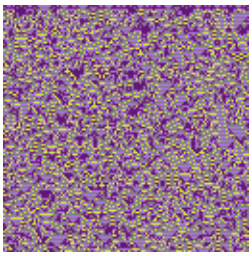
→ $\{3 \to 8.29153 \times 10^{-23}, 4 \to 1.\}$,

764 327 510



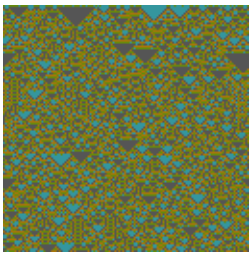
$\to \{4 \to 4.47792 \times 10^{-10}, 3 \to 1.\},$

490 295 289



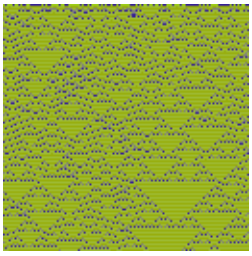
$\to \{4 \to 4.69638 \times 10^{-7}, 3 \to 1.\},$

1 162 664 732



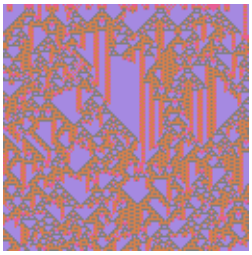
$\to \{4 \to 5.21527 \times 10^{-10}, 3 \to 1.\},$

304 808 425



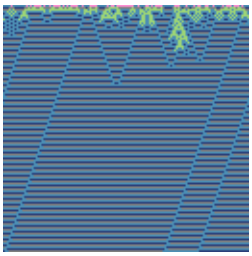
$\to \{4 \to 1.08461 \times 10^{-42}, 3 \to 1.\},$

907 022 973



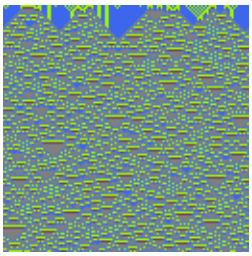
724 404 545

$\to \{3 \to 4.75025 \times 10^{-10}, 4 \to 1.\},$



560 019 942

$\to \{3 \to 1.58123 \times 10^{-11}, 4 \to 1.\},$



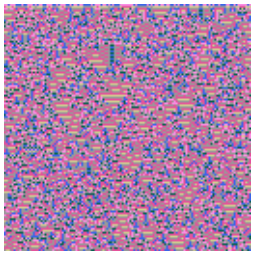
103 327 653

$\to \{4 \to 8.68805 \times 10^{-44}, 3 \to 1.\}\}$

6-colour totalistic, range 1

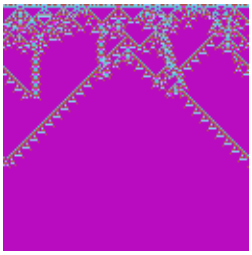
In[177]:=
```
test4Data6kr1C20 = data6TC[8, 128, 128];
test4Data6kr1C20labeled = Thread[
   Labeled[Keys@test4Data6kr1C20, Values@test4Data6kr1C20, LabelStyle → Small]];
Thread[test4Data6kr1C20labeled → netECA20[Keys@test4Data6kr1C20,
   {"TopProbabilities", 2}]]
```

Out[179]=



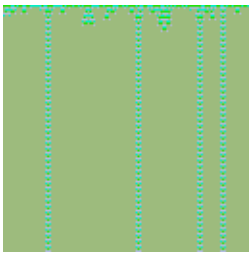
2 122 173 234 245

$\{\to \{4 \to 5.96215 \times 10^{-14}, 3 \to 1.\},$



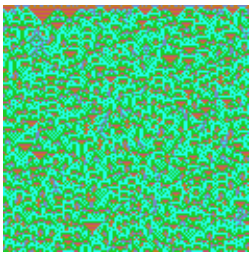
$\to \{2 \to 5.61713 \times 10^{-14}, 4 \to 1.\},$

884 722 928 890



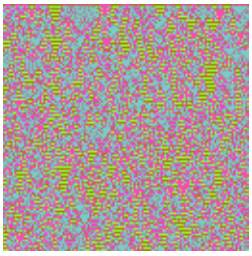
$\to \{2 \to 0.0284381, 4 \to 0.971562\},$

1 499 184 384 903



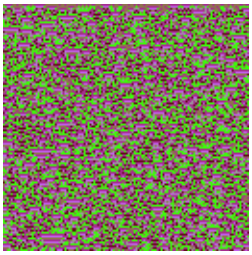
$\to \{4 \to 2.26852 \times 10^{-26}, 3 \to 1.\},$

2 025 733 343 548



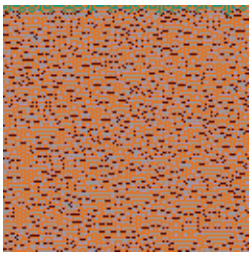
$\to \{4 \to 1.27025 \times 10^{-8}, 3 \to 1.\},$

475 359 235 938



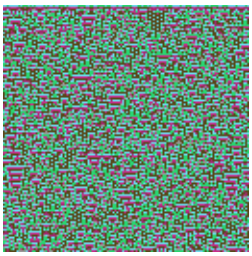
$\to \{4 \to 3.70575 \times 10^{-9}, 3 \to 1.\},$

263 650 594 825



$\to \{4 \to 2.29993 \times 10^{-16}, 3 \to 1.\},$

393 295 560 920



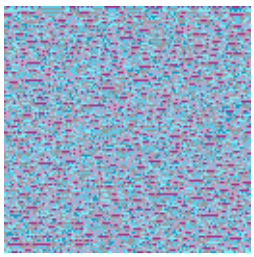
$\to \{4 \to 0.00013084, 3 \to 0.999869\}\Big\}$

2 012 563 000 751

6-colour totalistic, range 2

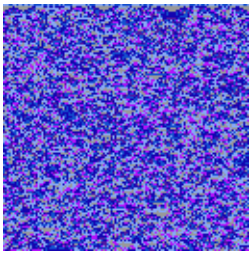
In[189]:=
```
test4Data6kr2C20 = data6T2C[8, 128, 128];
test4Data6kr2C20labeled = Thread[
   Labeled[Keys@test4Data6kr2C20, Values@test4Data6kr2C20, LabelStyle → Small]];
Thread[test4Data6kr2C20labeled → netECA20[Keys@test4Data6kr2C20,
   {"TopProbabilities", 2}]]
```

Out[191]=



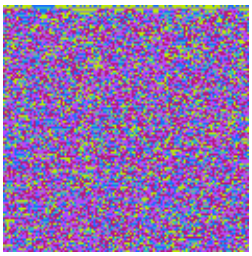
$\to \{4 \to 2.14776 \times 10^{-7}, 3 \to 1.\},$

1 621 502 426 955 534 427



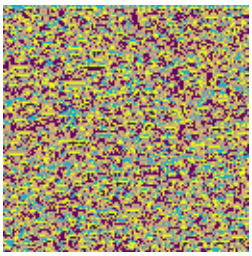
$\to \{4 \to 9.33202 \times 10^{-11}, 3 \to 1.\},$

131 338 484 536 441 330 961



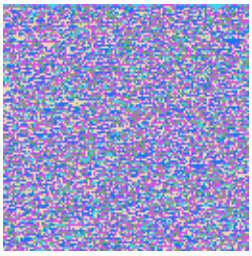
$\to \{4 \to 5.0397 \times 10^{-7}, 3 \to 1.\},$

158 918 292 961 883 595 722



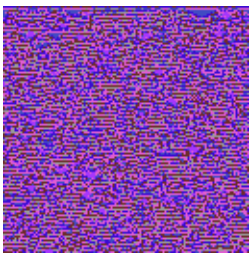
$\to \{4 \to 1.82161 \times 10^{-23}, 3 \to 1.\},$

106 403 272 815 247 748 066



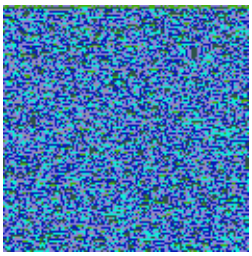
$\to \{4 \to 2.46028 \times 10^{-7}, 3 \to 1.\},$

168 311 878 705 436 456 573



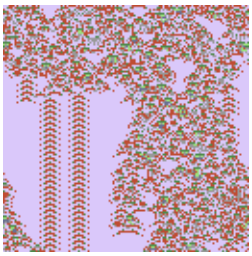
→ {4 → 0.00257098, 3 → 0.997429},

161 100 752 738 056 007 127



→ $\{4 \to 1.25412 \times 10^{-6}, 3 \to 0.999999\}$,

67 338 586 887 823 280 878



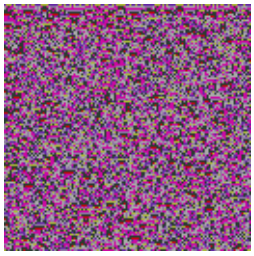
→ $\left\{3 \to 3.72349 \times 10^{-20}, 4 \to 1.\right\}\Big\}$

40 004 676 971 724 828 996

7-colour totalistic, range 1

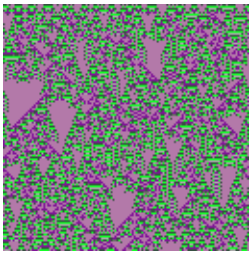
In[192]:=
```
test4Data7kr1C20 = data7TC[8, 128, 128];
test4Data7kr1C20labeled = Thread[
   Labeled[Keys@test4Data7kr1C20, Values@test4Data7kr1C20, LabelStyle → Small]];
Thread[test4Data7kr1C20labeled → netECA20[Keys@test4Data7kr1C20,
   {"TopProbabilities", 2}]]
```

Out[194]=



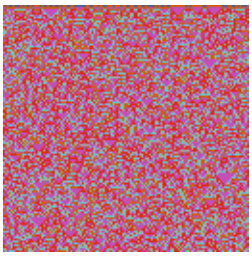
→ $\{4 \to 9.30343 \times 10^{-7}, 3 \to 0.999999\}$,

8 005 121 115 130 005



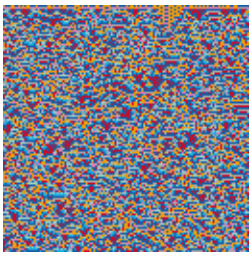
$\to \{3 \to 4.84794 \times 10^{-35}, 4 \to 1.\},$

4 335 901 976 609 098



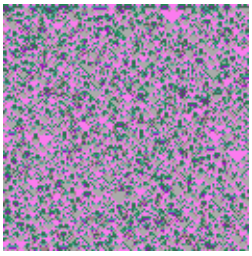
$\to \{4 \to 1.97203 \times 10^{-12}, 3 \to 1.\},$

10 508 822 606 686 953



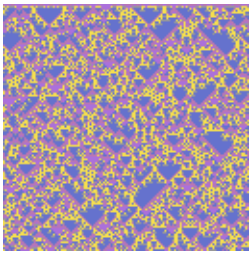
$\to \{4 \to 4.44739 \times 10^{-9}, 3 \to 1.\},$

1 596 925 239 801 768



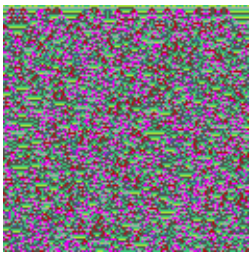
$\to \{4 \to 1.87004 \times 10^{-14}, 3 \to 1.\},$

10 215 244 325 708 880



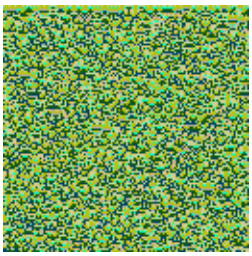
$\to \{4 \to 1.77311 \times 10^{-13}, 3 \to 1.\},$

7 040 224 636 385 774



$\to \{4 \to 9.65479 \times 10^{-8}, 3 \to 1.\},$

6 448 876 058 328 278



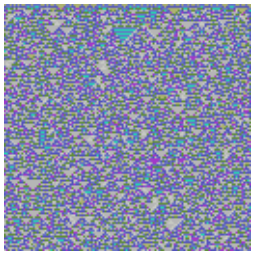
$\to \{4 \to 4.66881 \times 10^{-17}, 3 \to 1.\}\}$

8 488 970 361 710 764

8-colour totalistic, range 1

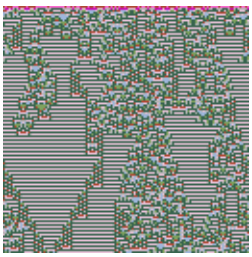
In[195]:=
```
test4Data8kr1C20 = data8TC[8, 128, 128];
test4Data8kr1C20labeled = Thread[
   Labeled[Keys@test4Data8kr1C20, Values@test4Data8kr1C20, LabelStyle → Small]];
Thread[test4Data8kr1C20labeled → netECA20[Keys@test4Data8kr1C20,
   {"TopProbabilities", 2}]]
```

Out[197]=



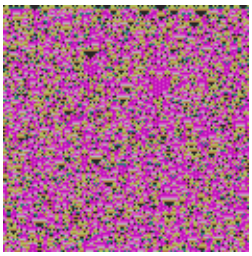
$\to \{4 \to 7.02129 \times 10^{-8}, 3 \to 1.\},$

17 622 595 304 491 307 972



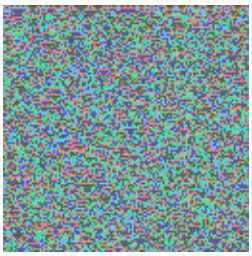
$\to \{3 \to 6.92144 \times 10^{-30}, 4 \to 1.\},$

34 241 353 322 287 229 398



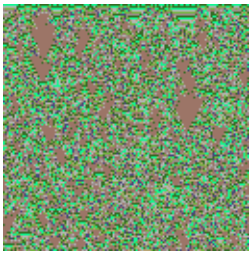
$\to \{4 \to 5.23277 \times 10^{-9}, 3 \to 1.\},$

2 060 768 124 912 791 136



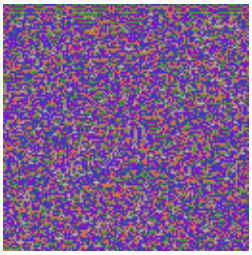
$\to \{4 \to 1.51806 \times 10^{-6}, 3 \to 0.999998\},$

61 211 199 906 993 871 933



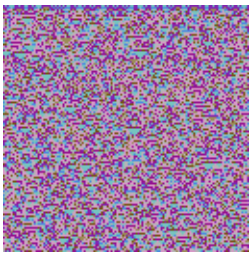
$\to \{4 \to 0.242177, 3 \to 0.757823\},$

64 867 558 234 168 550 441



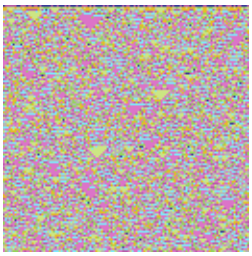
$\to \{4 \to 1.05298 \times 10^{-7}, 3 \to 1.\},$

48 804 732 770 089 589 599



$\to \{4 \to 3.27294 \times 10^{-9}, 3 \to 1.\},$

22 250 425 681 225 544 644



$\to \{4 \to 1.26372 \times 10^{-7}, 3 \to 1.\}\}$

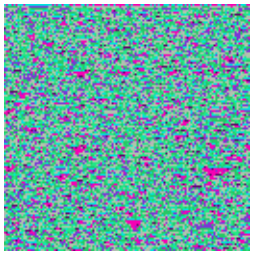
6 031 007 777 069 292 855

```
test4Data8kr1C20 = data8TC[8, 128, 128];
test4Data8kr1C20labeled = Thread[
   Labeled[Keys@test4Data8kr1C20, Values@test4Data8kr1C20, LabelStyle → Small]];
Thread[test4Data8kr1C20labeled → netECA20[Keys@test4Data8kr1C20,
   {"TopProbabilities", 2}]]
```

8-colour totalistic, range 2

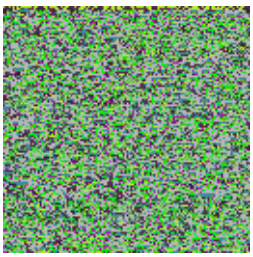
In[198]:=
```
test4Data8kr2C20 = data8T2C[8, 128, 128];
test4Data8kr2C20labeled = Thread[
   Labeled[Keys@test4Data8kr2C20, Values@test4Data8kr2C20, LabelStyle → Small]];
Thread[test4Data8kr2C20labeled → netECA20[Keys@test4Data8kr2C20,
   {"TopProbabilities", 2}]]
```

Out[200]= {



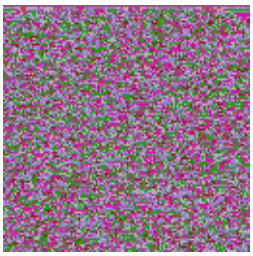
$\to \{4 \to 9.07147 \times 10^{-9}, 3 \to 1.\},$

34 654 596 361 113 019 068 625 927 861 588



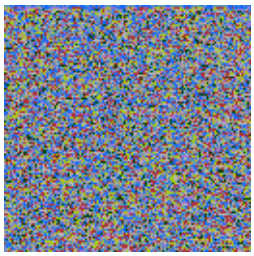
$\to \{4 \to 2.11931 \times 10^{-7}, 3 \to 1.\},$

281 482 922 380 025 038 886 593 272 382 401



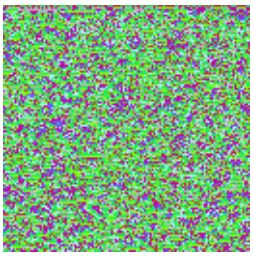
$\to \{4 \to 3.71128 \times 10^{-10}, 3 \to 1.\},$

136 834 659 229 241 596 913 590 173 599 070



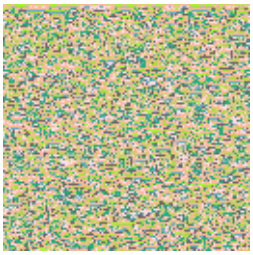
$\to \{4 \to 8.6463 \times 10^{-10}, 3 \to 1.\},$

99 039 415 938 616 855 241 596 711 134 078



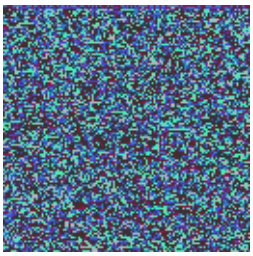
$\to \{4 \to 8.2174 \times 10^{-9}, 3 \to 1.\},$

229 246 662 605 553 621 164 874 696 175 286



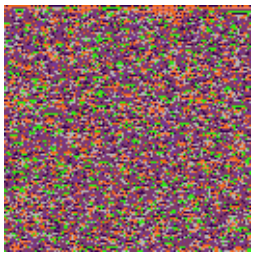
→ {4 → 0.0000763293, 3 → 0.999924},

179 241 943 887 588 895 040 248 748 590 135



→ $\{4 \to 1.05242 \times 10^{-9}, 3 \to 1.\}$,

159 919 994 014 568 400 575 667 683 478 858



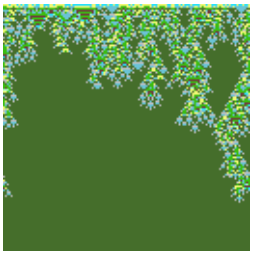
→ $\{4 \to 1.04627 \times 10^{-8}, 3 \to 1.\}\}$

65 542 614 726 689 378 130 235 771 767 178

9-colour totalistic, range 1

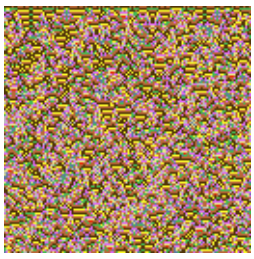
In[201]:=
```
test4Data9kr1C20 = data9TC[8, 128, 128];
test4Data9kr1C20labeled = Thread[
   Labeled[Keys@test4Data9kr1C20, Values@test4Data9kr1C20, LabelStyle → Small]];
Thread[test4Data9kr1C20labeled → netECA20[Keys@test4Data9kr1C20,
   {"TopProbabilities", 2}]]
```

Out[203]=



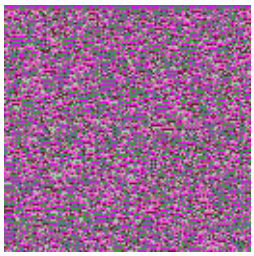
→ $\{2 \to 4.50007 \times 10^{-14}, 4 \to 1.\}$,

545 473 889 426 126 416 243 481



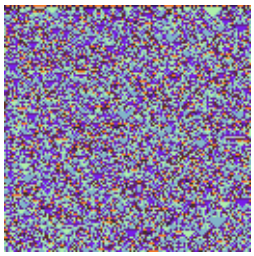
$\to \{4 \to 9.24149 \times 10^{-19}, 3 \to 1.\},$

502 210 816 307 654 598 488 514



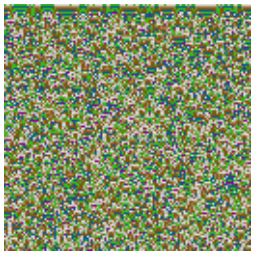
$\to \{4 \to 1.82232 \times 10^{-10}, 3 \to 1.\},$

252 071 869 730 596 894 533 775



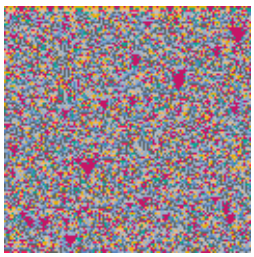
$\to \{4 \to 1.11817 \times 10^{-10}, 3 \to 1.\},$

214 330 265 025 126 729 457 970



$\to \{4 \to 8.69206 \times 10^{-10}, 3 \to 1.\},$

613 750 796 664 255 789 374 507

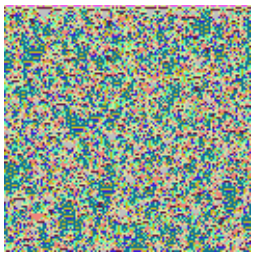


$\to \{4 \to 4.51773 \times 10^{-6}, 3 \to 0.999995\},$

229 941 589 923 423 647 251 209

$\to \{4 \to 1.4427 \times 10^{-9}, 3 \to 1.\},$

603 910 286 486 763 476 340 201

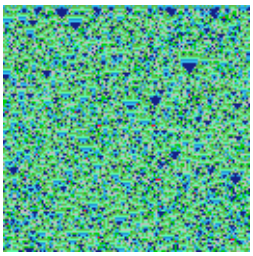


$\to \{4 \to 9.75566 \times 10^{-10}, 3 \to 1.\}\}$

212 234 742 362 166 511 987 715

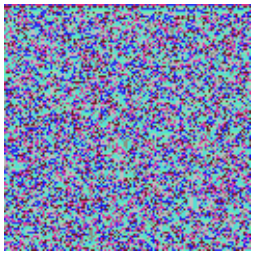
In[204]:=
```
test4Data9kr1C20 = data9TC[8, 128, 128];
test4Data9kr1C20labeled = Thread[
   Labeled[Keys@test4Data9kr1C20, Values@test4Data9kr1C20, LabelStyle → Small]];
Thread[test4Data9kr1C20labeled → netECA20[Keys@test4Data9kr1C20,
   {"TopProbabilities", 2}]]
```

Out[206]=



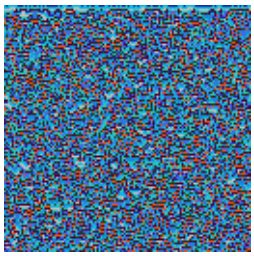
$\to \{4 \to 6.44658 \times 10^{-9}, 3 \to 1.\},$

632 243 116 302 958 616 080 766



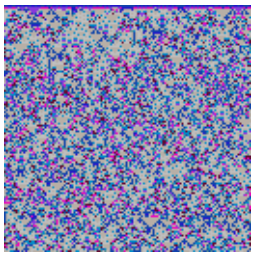
$\to \{4 \to 1.61253 \times 10^{-7}, 3 \to 1.\},$

397 550 570 643 234 170 502 037



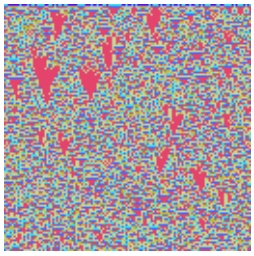
$\to \{4 \to 3.57356 \times 10^{-15}, 3 \to 1.\},$

210 090 422 560 296 622 071 412



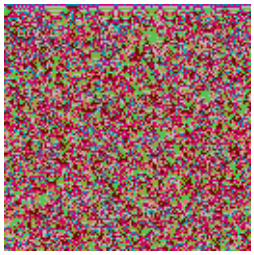
$\to \{4 \to 8.38878 \times 10^{-8}, 3 \to 1.\},$

211 510 167 579 945 323 093 293



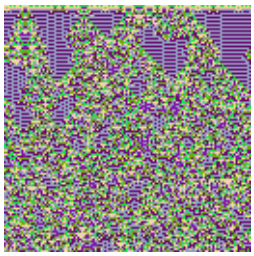
$\to \{3 \to 1.64811 \times 10^{-9}, 4 \to 1.\},$

358 720 881 018 661 807 902 186



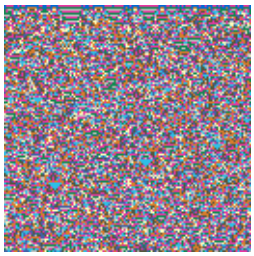
$\to \{4 \to 2.18409 \times 10^{-8}, 3 \to 1.\},$

138 775 222 971 002 819 176 049



$\to \{3 \to 7.59914 \times 10^{-7}, 4 \to 0.999999\},$

411 169 267 690 884 053 279 916

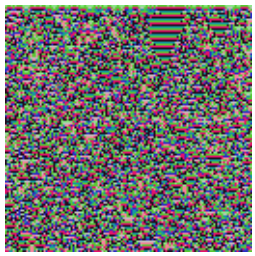


$\to \{4 \to 3.85116 \times 10^{-8}, 3 \to 1.\}\}$

177 060 381 259 418 538 511 307

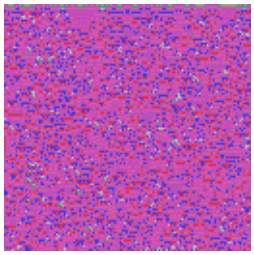
In[210]:=
```
test4Data9kr1C20 = data9TC[8, 128, 128];
test4Data9kr1C20labeled = Thread[
   Labeled[Keys@test4Data9kr1C20, Values@test4Data9kr1C20, LabelStyle → Small]];
Thread[test4Data9kr1C20labeled → netECA20[Keys@test4Data9kr1C20,
   {"TopProbabilities", 2}]]
```

Out[212]=



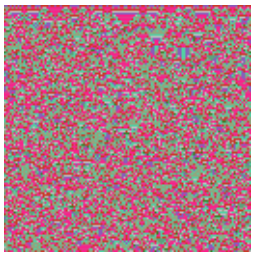
$\to \{4 \to 0.0000234349, 3 \to 0.999977\},$

259 588 662 506 132 867 744 548



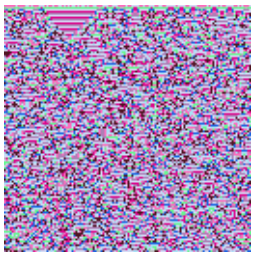
$\to \{4 \to 3.95801 \times 10^{-18}, 3 \to 1.\},$

399 714 464 052 713 002 443 244



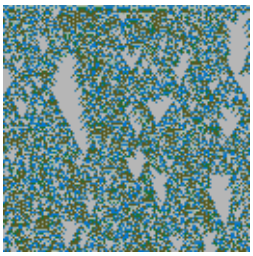
$\to \{4 \to 6.27675 \times 10^{-8}, 3 \to 1.\},$

444 874 973 288 043 518 720 987



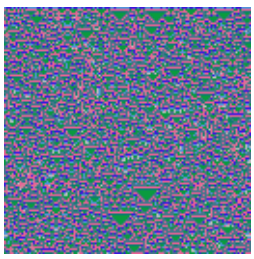
$\to \{4 \to 3.87381 \times 10^{-9}, 3 \to 1.\},$

243 239 750 322 177 213 694 175



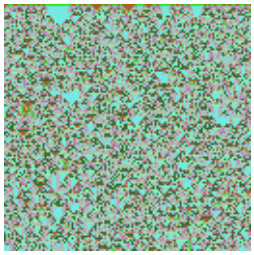
$\to \{1 \to 0., 4 \to 1.\},$

630 609 704 015 705 333 568 903



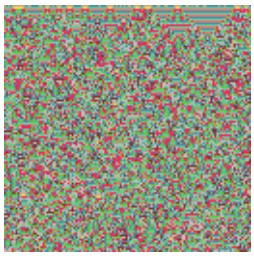
$\to \{4 \to 2.22592 \times 10^{-12}, 3 \to 1.\},$

259 051 458 785 907 037 572 167



$\to \{4 \to 1.61448 \times 10^{-6}, 3 \to 0.999998\},$

181 396 146 300 559 697 343 110

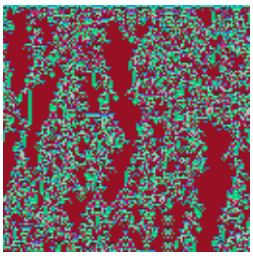


$\to \{4 \to 8.44342 \times 10^{-10}, 3 \to 1.\}\}$

590 603 799 910 104 521 604 359

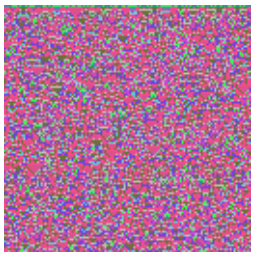
In[219]:=
```
test4Data9kr1C20 = data9TC[8, 128, 128];
test4Data9kr1C20labeled = Thread[
   Labeled[Keys@test4Data9kr1C20, Values@test4Data9kr1C20, LabelStyle → Small]];
Thread[test4Data9kr1C20labeled → netECA20[Keys@test4Data9kr1C20,
   {"TopProbabilities", 2}]]
```

Out[221]=



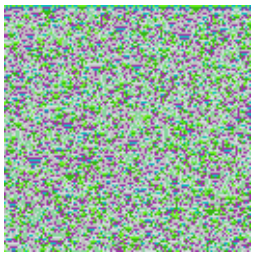
$\to \{1 \to 0., 4 \to 1.\},$

559 525 050 711 424 147 103 191



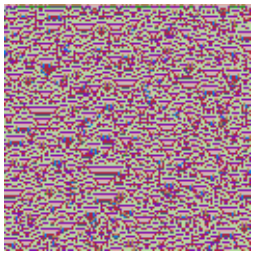
$\to \{4 \to 3.58462 \times 10^{-7}, 3 \to 1.\},$

381 031 691 994 576 244 742 372



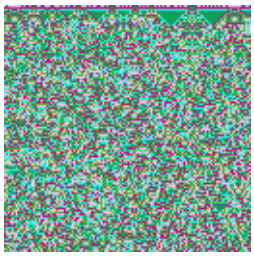
$\to \{4 \to 3.42679 \times 10^{-8}, 3 \to 1.\},$

176 193 088 198 065 357 484 722



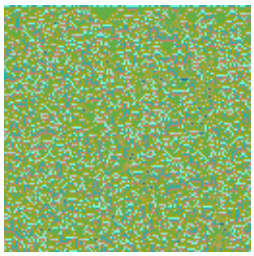
$\to \{4 \to 2.85477 \times 10^{-25}, 3 \to 1.\},$

424 983 346 694 267 584 684 002



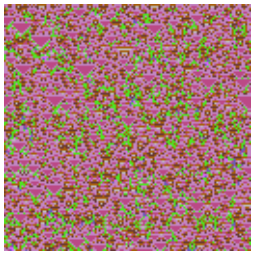
$\to \{4 \to 1.1626 \times 10^{-12}, 3 \to 1.\},$

401 281 846 717 180 232 569 288



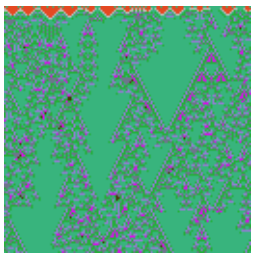
$\to \{4 \to 8.13265 \times 10^{-11}, 3 \to 1.\},$

527 622 550 933 327 483 302 175



$\to \{4 \to 6.60939 \times 10^{-9}, 3 \to 1.\},$

109 165 944 644 575 409 450 459



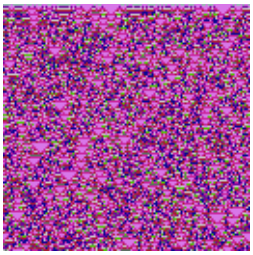
$\to \{3 \to 6.00677 \times 10^{-33}, 4 \to 1.\}\}$

466 105 670 797 185 959 312 718

10-colour totalistic, range 1

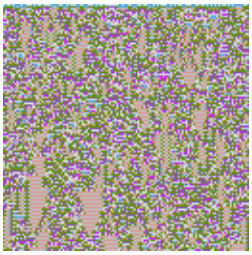
In[231]:=
```
test4Data10kr1C20 = data10TC[8, 128, 128];
test4Data10kr1C20labeled = Thread[
    Labeled[Keys@test4Data10kr1C20, Values@test4Data10kr1C20, LabelStyle → Small]];
Thread[test4Data10kr1C20labeled → netECA20[
    Keys@test4Data10kr1C20, {"TopProbabilities", 2}]]
```

Out[233]=



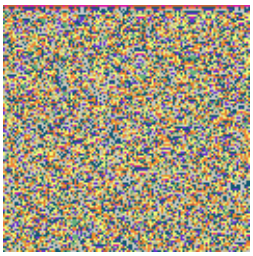
→ {4 → 0.0000763084, 3 → 0.999924},

1 312 438 879 231 379 999 597 551 818



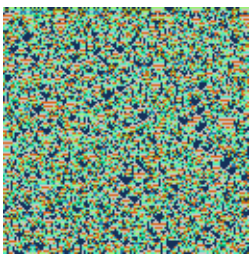
→ {3 → 0.0280082, 4 → 0.971992},

8 802 201 444 450 375 274 888 842 145



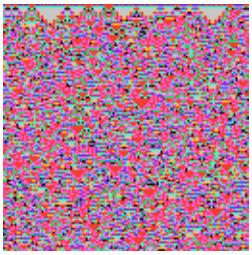
→ $\{4 \to 3.49283 \times 10^{-12}, 3 \to 1.\}$,

695 319 478 629 852 683 378 578 482



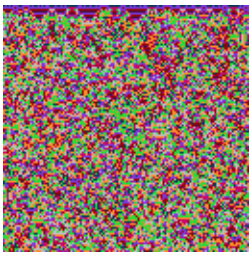
→ $\{4 \to 4.60576 \times 10^{-13}, 3 \to 1.\}$,

2 534 170 122 916 001 199 396 621 792



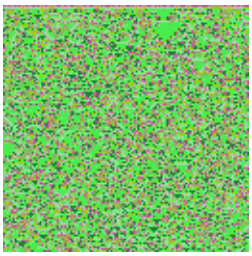
$\to \{4 \to 5.16076 \times 10^{-13}, 3 \to 1.\},$

6 402 030 110 956 009 099 812 379 880



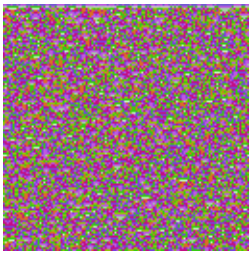
$\to \{4 \to 3.36832 \times 10^{-7}, 3 \to 1.\},$

8 056 627 540 848 327 134 024 377 008



$\to \{4 \to 1.99893 \times 10^{-9}, 3 \to 1.\},$

9 175 124 056 690 256 916 407 354 524

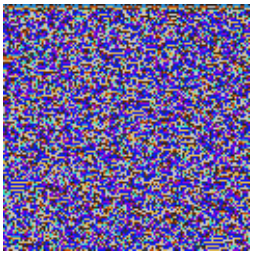


$\to \{4 \to 8.08514 \times 10^{-7}, 3 \to 0.999999\}\}$

9 446 873 547 431 883 154 485 119 281

In[249]:=
```
test4Data10kr1C20 = data10TC[8, 128, 128];
test4Data10kr1C20labeled = Thread[
   Labeled[Keys@test4Data10kr1C20, Values@test4Data10kr1C20, LabelStyle → Small]];
Thread[test4Data10kr1C20labeled → netECA20[
   Keys@test4Data10kr1C20, {"TopProbabilities", 2}]]
```

Out[251]= {

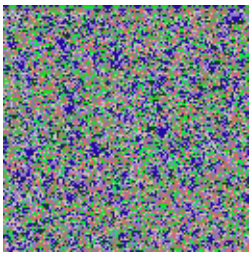


$\to \{4 \to 1.2805 \times 10^{-12}, 3 \to 1.\},$

4 099 129 486 982 529 374 716 532 304

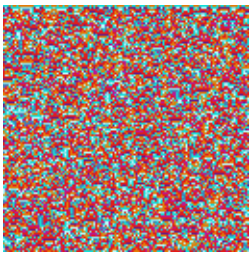
$\to \{2 \to 3.05239 \times 10^{-27}, 4 \to 1.\},$

5 178 229 202 161 056 818 928 741 804



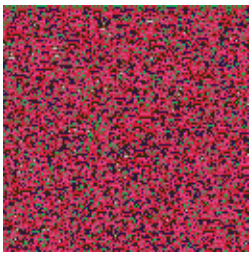
$\to \{4 \to 1.22816 \times 10^{-11}, 3 \to 1.\},$

1 958 204 953 984 761 521 473 671 845



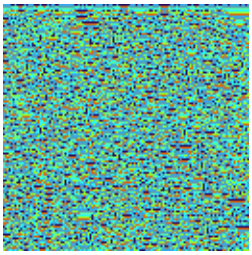
$\to \{4 \to 2.41992 \times 10^{-6}, 3 \to 0.999998\},$

3 846 804 511 187 008 038 498 195 063



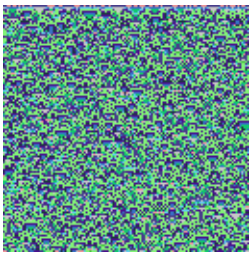
$\to \{4 \to 3.72526 \times 10^{-7}, 3 \to 1.\},$

5 943 294 755 181 741 046 165 887 635



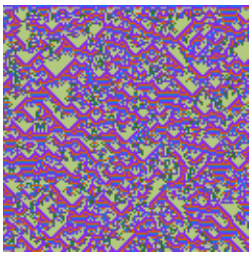
$\to \{4 \to 2.29086 \times 10^{-13}, 3 \to 1.\},$

1 379 195 931 173 118 078 894 037 759



$\to \{4 \to 8.98245 \times 10^{-18}, 3 \to 1.\},$

8 238 129 430 507 585 757 052 062 942



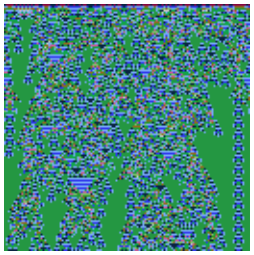
$\to \{4 \to 1.25814 \times 10^{-12}, 3 \to 1.\}\}$

3 700 381 629 363 093 603 170 760 087

11-colour totalistic, range 1

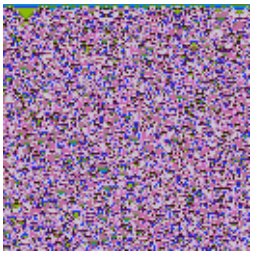
In[252]:=
```
test4Data11kr1C20 = data11TC[8, 128, 128];
test4Data11kr1C20labeled = Thread[
   Labeled[Keys@test4Data11kr1C20, Values@test4Data11kr1C20, LabelStyle → Small]];
Thread[test4Data11kr1C20labeled → netECA20[
   Keys@test4Data11kr1C20, {"TopProbabilities", 2}]]
```

Out[254]= $\{$



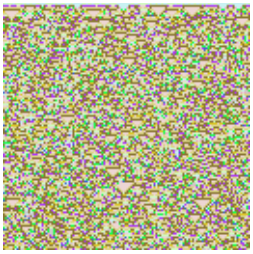
$\to \{1 \to 0., 4 \to 1.\},$

81 270 201 154 373 263 044 379 317 704 874



$\to \{4 \to 5.71573 \times 10^{-12}, 3 \to 1.\},$

179 897 284 365 900 959 311 332 077 089 987

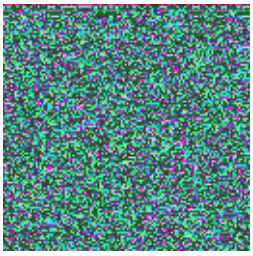


$\to \{4 \to 1.01114 \times 10^{-6}, 3 \to 0.999999\},$

35 123 924 118 216 489 757 803 859 991 151

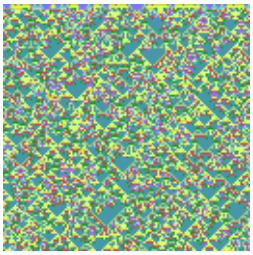
$\to \{4 \to 4.29644 \times 10^{-9}, 3 \to 1.\},$

131 712 843 883 972 330 326 889 146 741 015



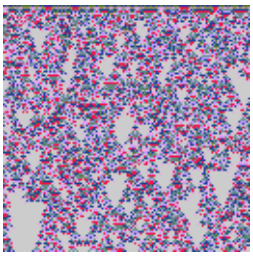
$\to \{4 \to 4.74543 \times 10^{-9}, 3 \to 1.\},$

181 377 425 870 102 192 541 033 392 752 135



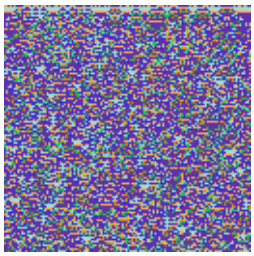
→ {4 → 0.000382702, 3 → 0.999617},

174 650 560 726 732 594 501 068 736 717 294



→ {1 → 0., 4 → 1.},

127 168 059 102 556 568 854 677 909 717 777

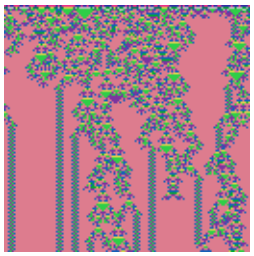


→ $\left\{4 \to 2.757 \times 10^{-9}, 3 \to 1.\right\}\}$

37 971 389 738 506 976 388 161 689 344 929

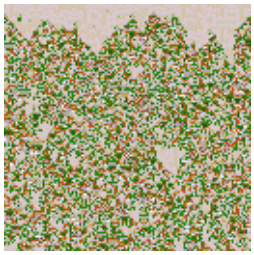
In[255]:=
```
test4Data11kr1C20 = data11TC[8, 128, 128];
test4Data11kr1C20labeled = Thread[
   Labeled[Keys@test4Data11kr1C20, Values@test4Data11kr1C20, LabelStyle → Small]];
Thread[test4Data11kr1C20labeled → netECA20[
   Keys@test4Data11kr1C20, {"TopProbabilities", 2}]]
```

Out[257]= {



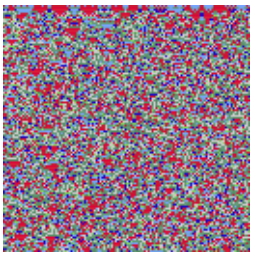
→ {1 → 0., 4 → 1.},

75 528 821 621 970 557 523 532 255 357 581



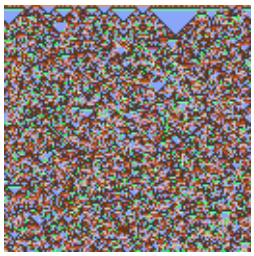
$\to \{4 \to 8.41156 \times 10^{-9}, 3 \to 1.\},$

99 826 099 470 711 656 538 450 065 618 641



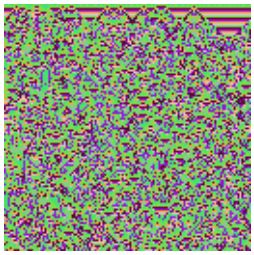
$\to \{4 \to 2.84243 \times 10^{-7}, 3 \to 1.\},$

100 390 219 568 920 591 260 363 922 695 811



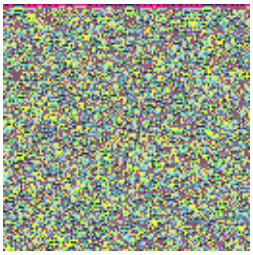
$\to \{4 \to 1.41461 \times 10^{-11}, 3 \to 1.\},$

17 077 054 181 389 965 369 404 988 478 854



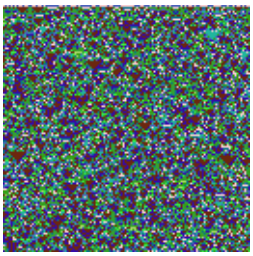
$\to \{4 \to 2.9442 \times 10^{-16}, 3 \to 1.\},$

46 622 934 574 362 974 007 509 756 139 546



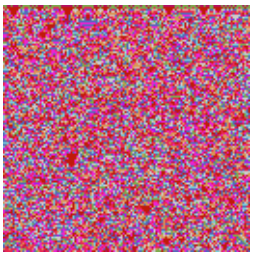
$\to \{4 \to 4.8596 \times 10^{-6}, 3 \to 0.999995\},$

185 822 863 976 379 061 933 630 911 988 252



$\to \{4 \to 2.43169 \times 10^{-11}, 3 \to 1.\},$

142 216 988 940 391 283 032 233 853 211 890



$\to \{4 \to 7.02143 \times 10^{-8}, 3 \to 1.\}\}$

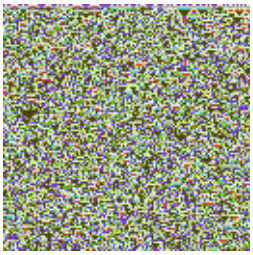
117 200 940 384 907 043 343 466 231 887 360

In[270]:=
```
test4Data11kr1C20 = data11TC[8, 128, 128];
test4Data11kr1C20labeled = Thread[
   Labeled[Keys@test4Data11kr1C20, Values@test4Data11kr1C20, LabelStyle → Small]];
Thread[test4Data11kr1C20labeled → netECA20[
   Keys@test4Data11kr1C20, {"TopProbabilities", 2}]]
```

Out[272]=

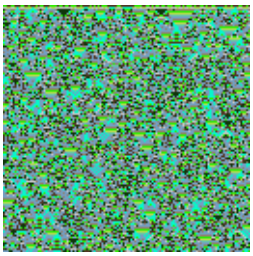
$\to \{2 \to 2.02047 \times 10^{-30}, 4 \to 1.\},$

178 363 666 301 844 176 896 902 943 988 858



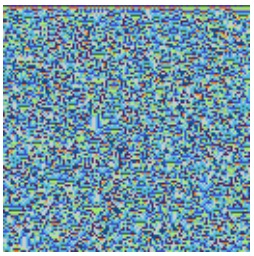
$\to \{4 \to 2.6887 \times 10^{-11}, 3 \to 1.\},$

177 027 294 830 625 404 290 680 474 451 217



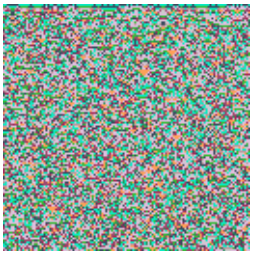
$\to \{4 \to 7.40175 \times 10^{-7}, 3 \to 0.999999\},$

126 906 237 354 515 632 704 558 856 267 857



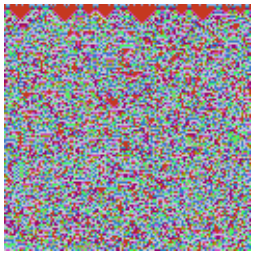
$\to \{4 \to 3.38035 \times 10^{-14}, 3 \to 1.\},$

22 613 266 992 527 162 362 852 892 587 199



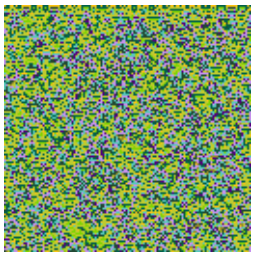
$\to \{4 \to 6.06419 \times 10^{-11}, 3 \to 1.\},$

142 349 637 421 779 073 192 832 714 618 325



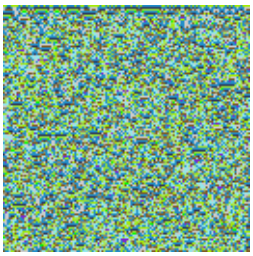
→ $\{4 \to 1.00889 \times 10^{-7}, 3 \to 1.\}$,

34 656 815 267 107 399 874 295 185 977 282



→ $\{4 \to 1.909 \times 10^{-6}, 3 \to 0.999998\}$,

96 858 366 685 806 367 009 587 399 868 548



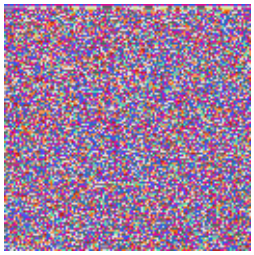
→ $\{4 \to 0.0000288415, 3 \to 0.999971\}\Big\}$

175 943 823 986 781 537 144 565 001 846 691

18-colour totalistic, range 1

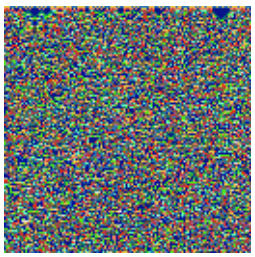
In[378]:=
```
test4Data20kr1C20 = data18TC[8, 128, 128];
test4Data20kr1C20labeled = Thread[
   Labeled[Keys@test4Data20kr1C20, Values@test4Data20kr1C20, LabelStyle → Small]];
Thread[test4Data20kr1C20labeled → netECA20[
   Keys@test4Data20kr1C20, {"TopProbabilities", 2}]]
```

Out[380]= $\Big\{$



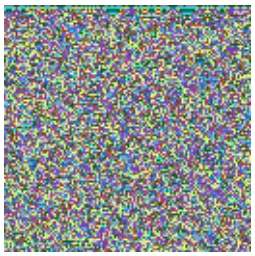
→ $\{4 \to 7.7597 \times 10^{-6}, 3 \to 0.999992\}$,

23 434 974 086 189 670 666 096 286 332 995 102 915 874 032 470 682 037 180 644 183 358



$\to \{4 \to 1.24071 \times 10^{-10}, 3 \to 1.\},$

93 300 872 509 057 852 420 655 736 582 598 566 638 857 748 607 015 346 208 998 324 828

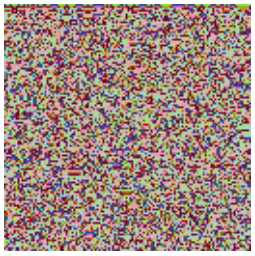


$\to \{4 \to 1.9872 \times 10^{-8}, 3 \to 1.\},$

79 235 904 011 269 637 953 999 347 456 714 134 435 497 259 754 903 807 290 486 739 641

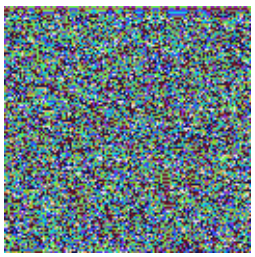
$\to \{4 \to 1.38992 \times 10^{-8}, 3 \to 1.\},$

124 928 833 699 436 712 033 508 328 112 867 712 446 945 561 347 885 859 615 379 006 993



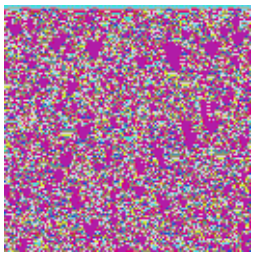
$\to \{4 \to 1.40564 \times 10^{-8}, 3 \to 1.\},$

71 497 848 082 533 087 615 004 763 266 651 143 491 779 360 582 072 239 959 247 110 947



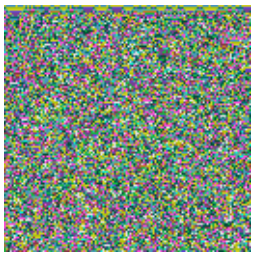
$\to \{4 \to 2.25592 \times 10^{-8}, 3 \to 1.\},$

66 657 161 305 697 641 636 859 556 902 357 240 625 573 715 904 096 692 790 632 509 282



$\to \{3 \to 5.26172 \times 10^{-12}, 4 \to 1.\},$

97 510 296 511 360 330 782 963 218 744 654 973 820 671 525 366 153 156 999 860 511 261



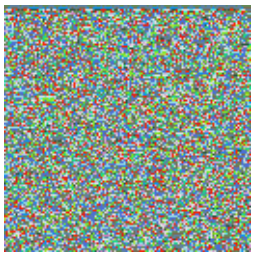
$\to \{4 \to 4.09566 \times 10^{-7}, 3 \to 1.\}\}$

76 689 254 701 118 307 477 071 077 030 538 715 222 860 413 402 089 977 280 198 311 120

In[594]:=
```
test4Data20kr1C20 = data18TC[8, 128, 128];
test4Data20kr1C20labeled = Thread[
   Labeled[Keys@test4Data20kr1C20, Values@test4Data20kr1C20, LabelStyle → Small]];
Thread[test4Data20kr1C20labeled → netECA20[
   Keys@test4Data20kr1C20, {"TopProbabilities", 2}]]
```

Out[596]=

$\{$

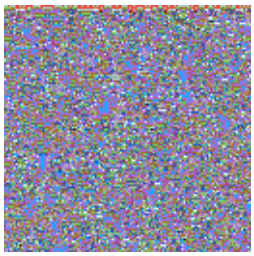


$\to \{4 \to 4.92206 \times 10^{-8}, 3 \to 1.\},$

13 895 444 763 919 059 979 046 331 431 883 669 791 694 898 698 400 119 270 281 702 758

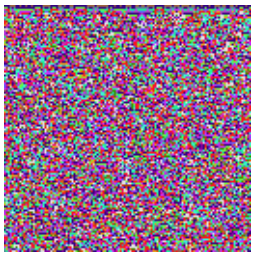
$\to \{4 \to 1.48082 \times 10^{-6}, 3 \to 0.999999\},$

106 368 420 586 570 822 019 872 523 445 604 218 834 533 098 216 287 365 943 030 756 788



$\to \{4 \to 0.00538366, 3 \to 0.994616\},$

67 433 993 272 154 407 393 640 986 822 973 341 944 172 352 119 634 590 667 454 136 225

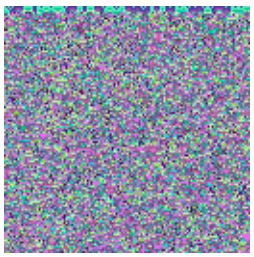


$\to \{4 \to 8.86493 \times 10^{-7}, 3 \to 0.999999\},$

37 430 509 440 865 924 347 471 414 529 586 779 254 418 867 442 023 297 930 793 363 029

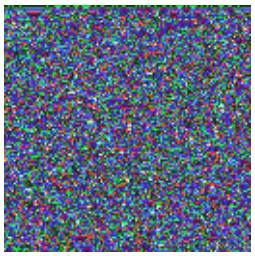
$\to \{3 \to 5.23049 \times 10^{-13}, 4 \to 1.\},$

102 974 792 016 961 301 874 082 998 899 289 451 594 446 816 624 822 058 274 997 622 818



$\to \{4 \to 9.10167 \times 10^{-8}, 3 \to 1.\},$

145 174 403 817 984 288 422 936 771 763 187 187 336 914 549 329 772 734 771 983 326 775



$\to \{4 \to 7.12584 \times 10^{-7}, 3 \to 0.999999\},$

93 615 186 269 380 003 910 578 033 332 307 326 434 318 188 079 815 292 928 055 199 809

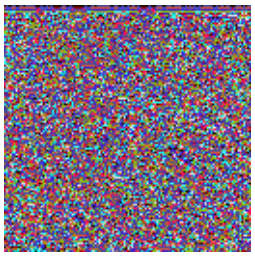
$\to \{4 \to 3.48093 \times 10^{-8}, 3 \to 1.\}\}$

32 482 775 703 171 155 706 697 146 175 003 665 260 068 895 561 499 679 040 679 495 679

In[735]:=
```
test4Data20kr1C20 = data18TC[8, 128, 128];
test4Data20kr1C20labeled = Thread[
   Labeled[Keys@test4Data20kr1C20, Values@test4Data20kr1C20, LabelStyle → Small]];
Thread[test4Data20kr1C20labeled → netECA20[
   Keys@test4Data20kr1C20, {"TopProbabilities", 2}]]
```

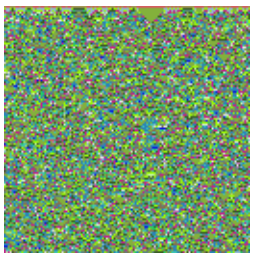
Out[737]=

$\{$



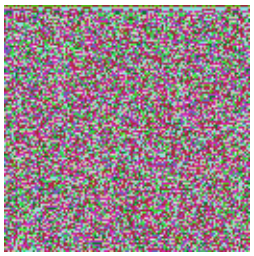
$\to \{4 \to 6.32741 \times 10^{-10}, 3 \to 1.\},$

28 175 454 977 997 067 214 463 043 253 352 871 085 211 575 190 195 708 701 636 959 137



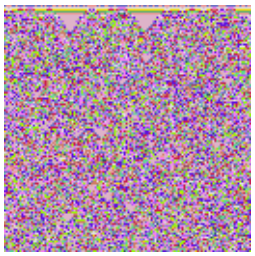
$\to \{4 \to 3.07251 \times 10^{-7}, 3 \to 1.\},$

161 284 150 023 404 885 560 160 057 467 573 309 877 857 614 125 061 936 417 217 016 949



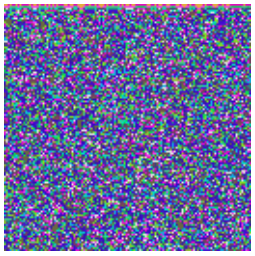
$\to \{4 \to 0.000044006, 3 \to 0.999956\},$

151 710 806 654 537 069 327 117 479 927 915 521 078 255 157 993 672 649 653 114 936 045



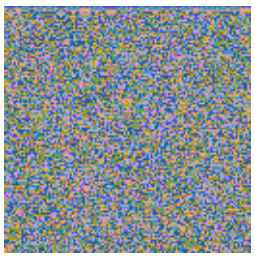
$\to \{4 \to 4.47639 \times 10^{-14}, 3 \to 1.\},$

57 209 847 886 539 446 213 625 540 790 032 240 443 171 463 705 053 200 907 659 136 468



$\to \{4 \to 7.94511 \times 10^{-7}, 3 \to 0.999999\},$

56 999 308 162 524 401 421 461 871 315 116 359 624 875 220 113 356 377 177 821 386 904



$\to \{4 \to 3.02405 \times 10^{-7}, 3 \to 1.\},$

41 972 268 231 226 443 316 650 829 849 557 027 452 476 658 864 600 631 820 342 213 926

$\to \{3 \to 4.02173 \times 10^{-43}, 4 \to 1.\},$

78 622 215 754 414 568 219 556 752 884 065 329 997 322 688 396 678 939 373 108 341 338

$\to \{4 \to 2.39354 \times 10^{-9}, 3 \to 1.\}\}$

34 644 471 185 301 269 917 453 937 405 067 621 603 052 014 212 415 913 610 137 608 144