

New CA Classifiers (random colours)

Wolfram Classes of ECAs

Functions for creating net and random datasets (ECAs, all 4 classes)

```

In[2]:= RandomRuleC[n_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[n, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[],
      3 -> RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[],
      6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]

netC[W_Integer, H_Integer] := NetInitialize@
  NetChain[{ConvolutionLayer[16, {2, 3}], Ramp, PoolingLayer[{H, W} - {1, 2}],
    FlattenLayer[], LinearLayer[256], SoftmaxLayer[]},
   "Input" -> NetEncoder[{"Image", {W, H}}],
   "Output" -> NetDecoder[{"Class", Range[0, 255]}]]

netTwoCC[W_Integer, H_Integer] := NetInitialize@
  NetChain[<|"conv1" -> ConvolutionLayer[16, {2, 3}], "ramp1" -> Ramp,
   "conv3" -> ConvolutionLayer[16, {2, 3}], "ramp2" -> Ramp,
   "pooling" -> PoolingLayer[{H, W} - {2, 4}], "flatten" -> FlattenLayer[],
   "linear" -> 512, "linear2" -> 4, "softmax" -> SoftmaxLayer[]|>,
   "Input" -> NetEncoder[{"Image", {W, H}}],
   "Output" -> NetDecoder[{"Class", Range[1, 4]}]]

dataC[W_Integer, H_Integer, n_Integer] := Table[
  RandomRuleC[i, W, H] -> CAclasses[[i + 1]], {i, RandomChoice[Range[0, 255], n]}]

```

```
In[6]:= netThreeCC[W_Integer, H_Integer] :=
NetInitialize@NetChain[<|"conv1" → ConvolutionLayer[16, {2, 3}],
 "ramp1" → Ramp, "conv2" → ConvolutionLayer[16, {2, 3}],
 "ramp2" → Ramp, "conv3" → ConvolutionLayer[16, {2, 3}], "ramp3" → Ramp,
 "pooling" → PoolingLayer[{H, W} - {4, 8}], "flatten" → FlattenLayer[],
 "linear" → 512, "linear2" → 4, "softmax" → SoftmaxLayer[]|>,
 "Input" → NetEncoder[{"Image", {W, H}}],
 "Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

```
In[7]:= netThreeCC1024[W_Integer, H_Integer] :=
NetInitialize@NetChain[<|"conv1" → ConvolutionLayer[16, {2, 3}],
 "ramp1" → Ramp, "conv2" → ConvolutionLayer[16, {2, 3}],
 "ramp2" → Ramp, "conv3" → ConvolutionLayer[16, {2, 3}], "ramp3" → Ramp,
 "pooling" → PoolingLayer[{H, W} - {4, 8}], "flatten" → FlattenLayer[],
 "linear" → 1024, "linear2" → 4, "softmax" → SoftmaxLayer[]|>,
 "Input" → NetEncoder[{"Image", {W, H}}],
 "Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

```
In[8]:= netFourCC512[W_Integer, H_Integer] :=
NetInitialize@NetChain[<|"conv1" → ConvolutionLayer[32, {2, 3}],
 "ramp1" → Ramp, "conv3" → ConvolutionLayer[32, {2, 3}], "ramp2" → Ramp,
 "pooling" → PoolingLayer[{H, W} - {2, 4}], "flatten" → FlattenLayer[],
 "linear" → 512, "linear2" → 4, "softmax" → SoftmaxLayer[]|>,
 "Input" → NetEncoder[{"Image", {W, H}}],
 "Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

```
In[9]:= netFiveCC512[W_Integer, H_Integer] :=
NetInitialize@NetChain[<|"conv1" → ConvolutionLayer[32, {2, 3}],
 "bat1" → BatchNormalizationLayer[], "ramp1" → Ramp,
 "conv3" → ConvolutionLayer[32, {2, 3}],
 "bat2" → BatchNormalizationLayer[], "ramp2" → Ramp,
 "pooling" → PoolingLayer[{H, W} - {2, 4}], "flatten" → FlattenLayer[],
 "linear" → 512, "linear2" → 4, "softmax" → SoftmaxLayer[]|>,
 "Input" → NetEncoder[{"Image", {W, H}}],
 "Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

```
In[10]:= netSixCC512drop[W_Integer, H_Integer] :=
NetInitialize@NetChain[<|"drop1" → DropoutLayer[0.2], "conv1" →
ConvolutionLayer[32, {3, 3}], "bat1" → BatchNormalizationLayer[],
 "ramp1" → Ramp, "conv3" → ConvolutionLayer[32, {3, 3}],
 "bat2" → BatchNormalizationLayer[], "ramp2" → Ramp,
 "pooling" → PoolingLayer[{H, W} - {4, 8}], "flatten" → FlattenLayer[],
 "linear" → 512, "drop2" → DropoutLayer[0.2], "linear2" → 4,
 "softmax" → SoftmaxLayer[]|>, "Input" → NetEncoder[{"Image", {W, H}}],
 "Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

```
In[1]:= netSevenCC512drop[W_Integer, H_Integer] :=
NetInitialize@NetChain[<|"conv1" → ConvolutionLayer[24, {3, 3}],
"bat1" → BatchNormalizationLayer[], "ramp1" → Ramp,
"conv3" → ConvolutionLayer[24, {3, 3}],
"bat2" → BatchNormalizationLayer[], "ramp2" → Ramp,
"pooling" → PoolingLayer[{H, W} - {4, 8}], "flatten" → FlattenLayer[],
"linear" → 512, "drop2" → DropoutLayer[0.2], "linear2" → 4,
"softmax" → SoftmaxLayer[]|>, "Input" → NetEncoder[{"Image", {W, H}}],
"Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

```
In[12]:= netEightCC512drop[W_Integer, H_Integer] :=
NetInitialize@NetChain[<|"conv1" → ConvolutionLayer[24, {3, 3}],
"bat1" → BatchNormalizationLayer[], "ramp1" → Ramp,
"conv2" → ConvolutionLayer[16, {2, 3}], "bat2" → BatchNormalizationLayer[],
"ramp2" → Ramp, "conv3" → ConvolutionLayer[24, {3, 3}],
"bat3" → BatchNormalizationLayer[], "ramp3" → Ramp,
"pooling" → PoolingLayer[{H, W} - {8, 16}], "flatten" → FlattenLayer[],
"linear" → 1024, "drop2" → DropoutLayer[0.2], "linear2" → 4,
"softmax" → SoftmaxLayer[]|>, "Input" → NetEncoder[{"Image", {W, H}}],
"Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

```
In[13]:= netNineCC512drop[W_Integer, H_Integer] :=
NetInitialize@NetChain[<|"conv1" → ConvolutionLayer[24, {3, 3}],
"bat1" → BatchNormalizationLayer[], "ramp1" → Ramp,
"conv2" → ConvolutionLayer[24, {3, 3}], "bat2" → BatchNormalizationLayer[],
"ramp2" → Ramp, "conv3" → ConvolutionLayer[24, {3, 3}],
"bat3" → BatchNormalizationLayer[], "ramp3" → Ramp,
"pooling" → PoolingLayer[{H, W} - {12, 12}], "flatten" → FlattenLayer[],
"linear" → 512, "drop2" → DropoutLayer[0.2], "linear2" → 4,
"softmax" → SoftmaxLayer[]|>, "Input" → NetEncoder[{"Image", {W, H}}],
"Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

```
In[14]:= netTenCC1024drop[W_Integer, H_Integer] :=
NetInitialize@NetChain[<|"conv1" → ConvolutionLayer[24, {3, 3}],
"bat1" → BatchNormalizationLayer[], "ramp1" → Ramp,
"conv2" → ConvolutionLayer[24, {3, 3}], "bat2" → BatchNormalizationLayer[],
"ramp2" → Ramp, "conv3" → ConvolutionLayer[24, {3, 3}],
"bat3" → BatchNormalizationLayer[], "ramp3" → Ramp,
"conv4" → ConvolutionLayer[24, {3, 3}],
"bat4" → BatchNormalizationLayer[], "ramp4" → Ramp,
"pooling" → PoolingLayer[{H, W} - {12, 12}], "flatten" → FlattenLayer[],
"linear" → 1024, "drop2" → DropoutLayer[0.3], "linear2" → 4,
"softmax" → SoftmaxLayer[]|>, "Input" → NetEncoder[{"Image", {W, H}}],
"Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

```
In[15]:= netElevenCC1024drop[W_Integer, H_Integer] :=
  NetInitialize@NetChain[<|"conv1" → ConvolutionLayer[48, {3, 3}],
    "bat1" → BatchNormalizationLayer[], "ramp1" → Ramp,
    "pooling1" → PoolingLayer[{2, 2}], "conv2" → ConvolutionLayer[24, {3, 3}],
    "bat2" → BatchNormalizationLayer[], "ramp2" → Ramp,
    "pooling2" → PoolingLayer[{2, 2}], "conv3" → ConvolutionLayer[24, {3, 3}],
    "bat3" → BatchNormalizationLayer[], "ramp3" → Ramp,
    "pooling3" → PoolingLayer[{2, 2}], "conv4" → ConvolutionLayer[12, {3, 3}],
    "bat4" → BatchNormalizationLayer[], "ramp4" → Ramp,
    "pooling4" → PoolingLayer[{2, 2}], "flatten" → FlattenLayer[],
    "linear" → 1024, "drop2" → DropoutLayer[0.3], "linear2" → 4,
    "softmax" → SoftmaxLayer[]|>, "Input" → NetEncoder[{"Image", {W, H}}],
    "Output" → NetDecoder[{"Class", Range[1, 4]}]]
```

Functions for creating datasets (1D totalistic CAs)

k=3, r=1 totalistic (class 4 only)

```
In[16]:= gen3TC[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {3, 1}}, RandomInteger[1, W], H - 1],
    ImageSize → {W, H}, ColorRules → {0 → RandomColor[], 1 → RandomColor[],
      3 → RandomColor[], 4 → RandomColor[], 5 → RandomColor[],
      6 → RandomColor[], 7 → RandomColor[]}, Frame → False]]
data3T2C[W_Integer, H_Integer, n_Integer] := Table[gen3TC[i, W, H] → 4,
  {i, RandomChoice[{1635, 1815, 2007, 2043, 2049, 1388, 1041}], n}]
```

k=4, r=1 totalistic (class 4 only, 1 example)

```
In[18]:= gen4TC[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {4, 1}}, RandomInteger[1, W], H - 1],
    ImageSize → {W, H}, ColorRules → {0 → RandomColor[], 1 → RandomColor[],
      3 → RandomColor[], 4 → RandomColor[], 5 → RandomColor[],
      6 → RandomColor[], 7 → RandomColor[]}, Frame → False]]
data4TC[W_Integer, H_Integer, n_Integer] := Table[gen4TC[1004600, W, H] → 4, n]
```

k=2, r=2 totalistic (all 4 classes)

```
In[20]:= gen2r2C[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {2, 1}, 2}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[],
      3 -> RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[],
      6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data2r2c4C[W_Integer, H_Integer, n_Integer] :=
  Table[gen2r2C[i, W, H] -> 4, {i, RandomChoice[{20, 52}, n]}]
data2r2c3C[W_Integer, H_Integer, n_Integer] :=
  Table[gen2r2C[i, W, H] -> 3, {i, RandomChoice[
    {2, 6, 10, 12, 14, 18, 22, 26, 28, 30, 34, 38, 42, 44, 46, 50}, n]}]
data2r2c2C[W_Integer, H_Integer, n_Integer] :=
  Table[gen2r2C[i, W, H] -> 2, {i, RandomChoice[{8, 24, 56}, n]}]
data2r2c1C[W_Integer, H_Integer, n_Integer] := Table[gen2r2C[i, W, H] -> 1,
  {i, RandomChoice[{0, 4, 16, 32, 36, 40, 48, 54, 58, 60, 62}, n]}]
genData2r2C[W_Integer, H_Integer, n_Integer] := Join[data2r2c4C[W, H, n],
  data2r2c3C[W, H, n], data2r2c2C[W, H, n], data2r2c1C[W, H, n]]
```

k=5, r=1 totalistic (class 4 only)

```
In[26]:= gen5T4C[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {5, 1}}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[],
      3 -> RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[],
      6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data5T4C[n_Integer, W_Integer, H_Integer] :=
  Table[gen5T4C[i, W, H] -> 4, {i, RandomChoice[
    {781 130 654, 772 514 435, 1 151 319 452, 309 095 787, 880 862 046, 973 835 714,
      779 446 817, 345 466 505, 535 500 975, 793 363 571, 1 052 373 865, 455 984 785,
      339 227 109, 1 050 973 846, 513 368 817, 91 315 820, 113 925 357}, n]}]
```

k=5, r=1 totalistic (classes 2/3/4)

```
In[28]:= gen5TC[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {5, 1}, 1}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[],
      3 -> RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[],
      6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data5T4CC[W_Integer, H_Integer, n_Integer] := Table[gen5TC[i, W, H] -> 4,
  {i, RandomChoice[{644 218 533, 491 739 943, 6 889 640, 986 144 962, 1 099 816 682,
    988 971 204, 300 829 994, 272 622 024, 304 100 638, 626 595 633}, n]}]
data5T3CC[W_Integer, H_Integer, n_Integer] := Table[gen5TC[i, W, H] -> 3,
  {i, RandomChoice[{889 082 395, 541 068 260, 807 907 479, 816 180 062, 650 485 139,
    643 827 745, 753 940 864, 871 525 323, 351 440 311, 83 501 460}, n]}]
data5T2CC[W_Integer, H_Integer, n_Integer] :=
  Table[gen5TC[i, W, H] -> 2, {i, RandomChoice[
    {525 735 659, 1 022 330 944, 1 007 796 739, 495 633 437, 1 036 827 943}, n]}]
genData5TCC[W_Integer, H_Integer, n_Integer] :=
  Join[data5T4CC[W, H, n], data5T3CC[W, H, n], data5T2CC[W, H, n]]
```

Generate test datasets

k=2, r=2 non-totalistic

```
In[33]:= genk2r2C[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, 2, 2}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[],
      3 -> RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[],
      6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
datak2r2C[W_Integer, H_Integer, n_Integer] :=
  Table[genk2r2C[i, W, H] -> i, {i, RandomChoice[Range[0, 4 294 967 295], n]}]
```

k=2, r=3 non-totalistic

```
In[35]:= genk2r3NT[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, 2, 3}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[],
      3 -> RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[],
      6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
datak2r3NT[W_Integer, H_Integer, n_Integer] :=
  Table[genk2r3NT[i, W, H] -> i, {i, RandomInteger[2^2^7 - 1, n]}]
```

k=3, r=1 non-totalistic

```
In[37]:= genk3r1NT[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, 3}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[],
      3 -> RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[],
      6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
datak3r1NT[W_Integer, H_Integer, n_Integer] :=
  Table[genk3r1NT[i, W, H] -> i, {i, RandomInteger[3^3^3 - 1, n]}]
```

k=3, r=2 totalistic

```
In[39]:= genk3r2C[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {3, 1}, 2}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[],
      3 -> RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[],
      6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
datak3r2C[W_Integer, H_Integer, n_Integer] :=
  Table[genk3r2C[i, W, H] -> i, {i, RandomChoice[Range[0, 177146], n]}]
```

k=3, r=3 totalistic

```
In[41]:= genk3r3C[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {3, 1}, 3}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[],
      3 -> RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[],
      6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
datak3r3C[W_Integer, H_Integer, n_Integer] :=
  Table[genk3r3C[i, W, H] -> i, {i, RandomChoice[Range[0, 14348906], n]}]
```

k=4, r=1 non-totalistic

```
In[43]:= genk4r1NT[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, 4}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[],
      3 -> RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[],
      6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
datak4r1NT[W_Integer, H_Integer, n_Integer] :=
  Table[genk4r1NT[i, W, H] -> i, {i, RandomInteger[4^4^3 - 1, n]}]
```

k=4, r=1 totalistic

```
In[45]:= genk4r1C[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {4, 1}}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[],
      3 -> RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[],
      6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
datak4r1C[W_Integer, H_Integer, n_Integer] :=
  Table[genk4r1C[i, W, H] -> i, {i, RandomChoice[Range[0, 1048575], n]}]
```

k=4, r=2 totalistic

```
In[47]:= genk4r2C[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {4, 1}, 2}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[],
      3 -> RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[],
      6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
datak4r2C[W_Integer, H_Integer, n_Integer] :=
  Table[genk4r2C[i, W, H] -> i, {i, RandomChoice[Range[0, 4294967295], n]}]
```

k=5, r=1 totalistic

```
In[49]:= gen5T2C[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {5, 1}, 1}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[],
      3 -> RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[],
      6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data5T2C[n_Integer, W_Integer, H_Integer] := Table[gen5T2C[i, W, H] -> i,
  {i, RandomChoice[Range[0, 1220703125], n]}]
```

k=6, r=1 totalistic

```
In[51]:= gen6TC[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {6, 1}, 1}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[],
      3 -> RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[],
      6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data6TC[n_Integer, W_Integer, H_Integer] := Table[gen6TC[i, W, H] -> i,
  {i, RandomInteger[2821109907455, n]}]
```

k=6, r=2 totalistic

```
In[53]:= gen6T2C[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {6, 1}, 2}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[],
      3 -> RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[],
      6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data6T2C[n_Integer, W_Integer, H_Integer] := Table[gen6T2C[i, W, H] -> i,
  {i, RandomInteger[170 581 728 179 578 208 255, n]}]
```

k=7, r=1 totalistic

```
In[55]:= gen7TC[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {7, 1}, 1}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[],
      3 -> RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[],
      6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data7TC[n_Integer, W_Integer, H_Integer] := Table[gen7TC[i, W, H] -> i,
  {i, RandomInteger[11 398 895 185 373 142, n]}]
```

k=8, r=1 totalistic

```
In[57]:= gen8TC[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {8, 1}, 1}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[],
      3 -> RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[],
      6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data8TC[n_Integer, W_Integer, H_Integer] := Table[gen8TC[i, W, H] -> i,
  {i, RandomInteger[73 786 976 294 838 206 463, n]}]
```

k=8, r=2 totalistic

```
In[59]:= gen8T2C[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {8, 1}, 2}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[],
      3 -> RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[],
      6 -> RandomColor[], 7 -> RandomColor[]}, Frame -> False]]
data8T2C[n_Integer, W_Integer, H_Integer] := Table[gen8T2C[i, W, H] -> i,
  {i, RandomInteger[324 518 553 658 426 726 783 156 020 576 255, n]}]
```

k=9, r=1 totalistic

```
In[61]:= gen9TC[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {9, 1}, 1}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[],
      3 -> RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[],
      6 -> RandomColor[], 7 -> RandomColor[], 8 -> RandomColor[]}, Frame -> False]]
data9TC[n_Integer, W_Integer, H_Integer] := Table[gen9TC[i, W, H] -> i,
  {i, RandomInteger[717897987691852588770248, n]}]
```

k=10, r=1 totalistic

```
In[1418]:= gen10TC[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {10, 1}, 1}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[], 3 ->
      RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[], 6 -> RandomColor[],
      7 -> RandomColor[], 8 -> RandomColor[], 9 -> RandomColor[]}, Frame -> False]]
data10TC[n_Integer, W_Integer, H_Integer] := Table[gen10TC[i, W, H] -> i,
  {i, RandomInteger[9999999999999999999999999999999999999999999, n]}]
```

k=11, r=1 totalistic

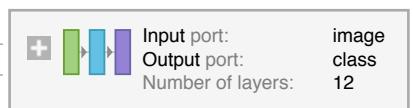
```
In[1446]:= gen11TC[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {11, 1}, 1}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[],
      3 -> RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[],
      6 -> RandomColor[], 7 -> RandomColor[], 8 -> RandomColor[],
      9 -> RandomColor[], 10 -> RandomColor[]}, Frame -> False]]
data11TC[n_Integer, W_Integer, H_Integer] := Table[gen11TC[i, W, H] -> i,
  {i, RandomInteger[191943424957750480504146841291809, n]}]
```

k=18, r=1 totalistic

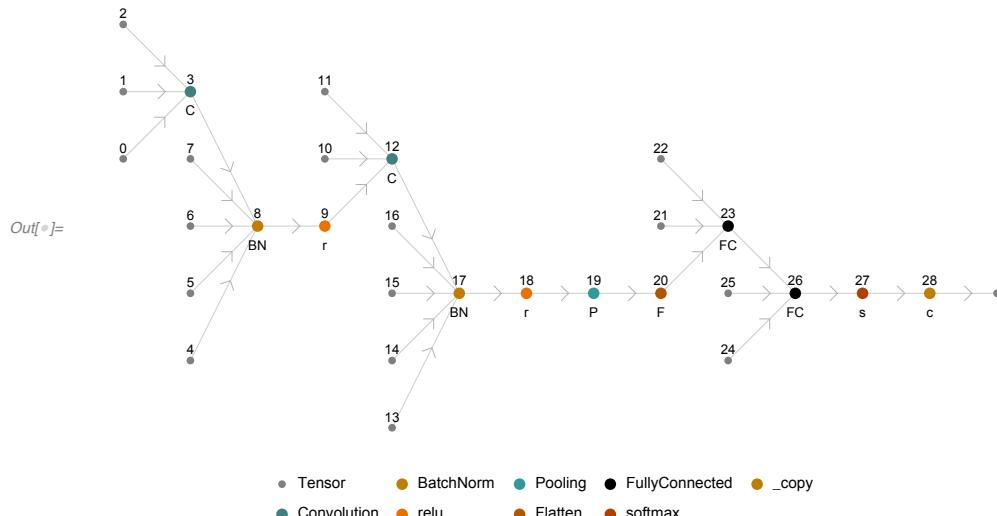
```
In[1448]:= gen18TC[p_Integer, W_Integer, H_Integer] :=
  Image[ArrayPlot[CellularAutomaton[{p, {18, 1}, 1}, RandomInteger[1, W], H - 1],
    ImageSize -> {W, H}, ColorRules -> {0 -> RandomColor[], 1 -> RandomColor[],
      3 -> RandomColor[], 4 -> RandomColor[], 5 -> RandomColor[], 6 ->
      RandomColor[], 7 -> RandomColor[], 8 -> RandomColor[], 9 -> RandomColor[],
      10 -> RandomColor[], 11 -> RandomColor[], 12 -> RandomColor[],
      13 -> RandomColor[], 14 -> RandomColor[], 15 -> RandomColor[],
      16 -> RandomColor[], 17 -> RandomColor[]}], Frame -> False]
data18TC[n_Integer, W_Integer, H_Integer] :=
  Table[gen18TC[i, W, H] -> i, {i, RandomInteger[
    188 005 374 836 229 120 894 273 278 138 806 956 375 747 747 317 139 671 689 960 882 175
    , n]}]
```

Network XIII - Two convolutions, dropout on linear only, BatchNorm

```
In[1]:= netECA13 = netSevenCC512drop[128, 128]
```

Out[1]= NetChain[ Input port: Output port: Number of layers:
image class 12

```
In[2]:= NetInformation[netECA13, "MXNetNodeGraphPlot"]
```



```
In[3]:= NetInformation[netECA13, "SummaryGraphic"]
```



```
In[4]:= dataECA13 = dataC[128, 128, 8192];
```

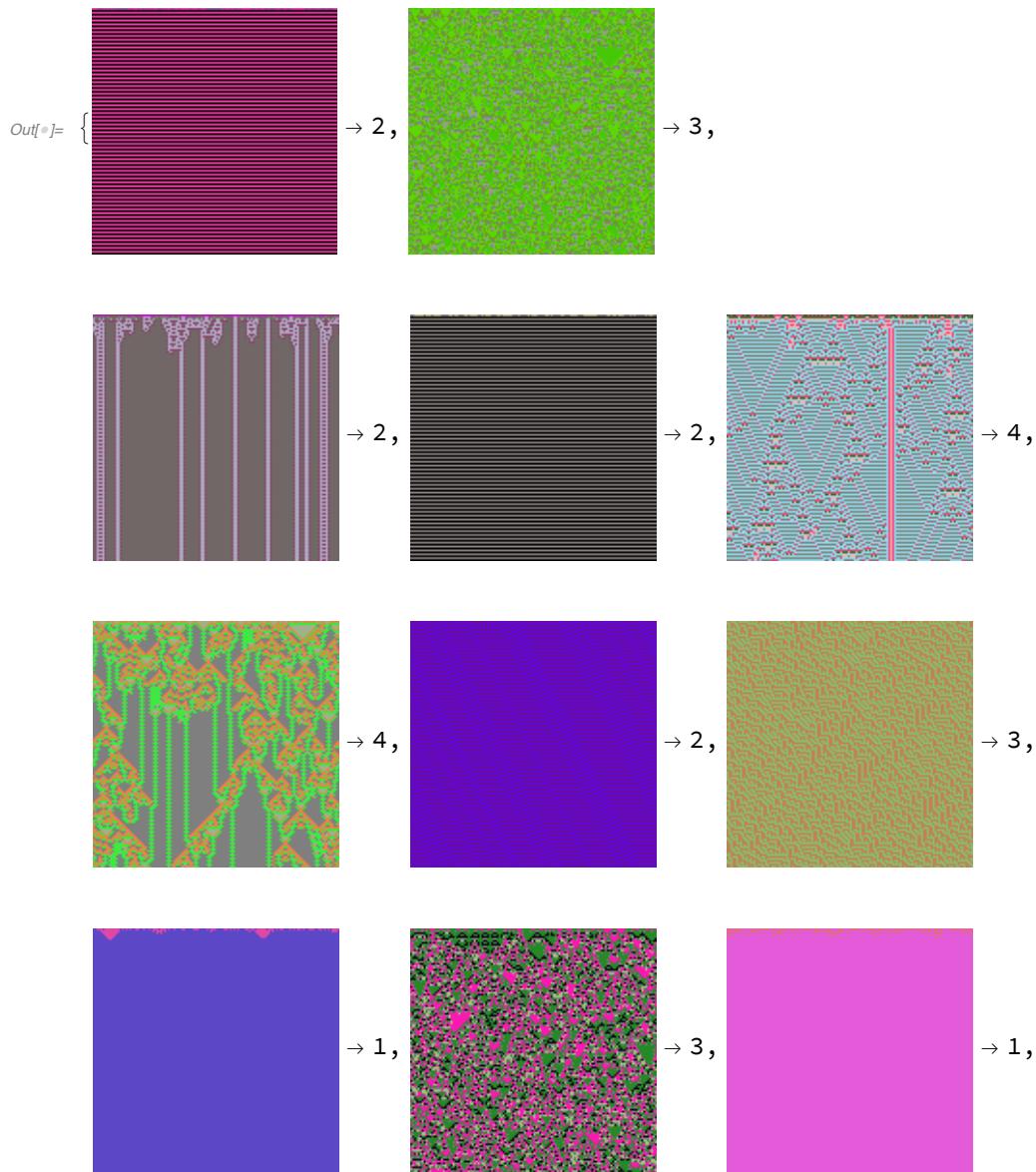
```
In[5]:= dataTotalistic2BigC13 = genData2r2C[128, 128, 1024];
```

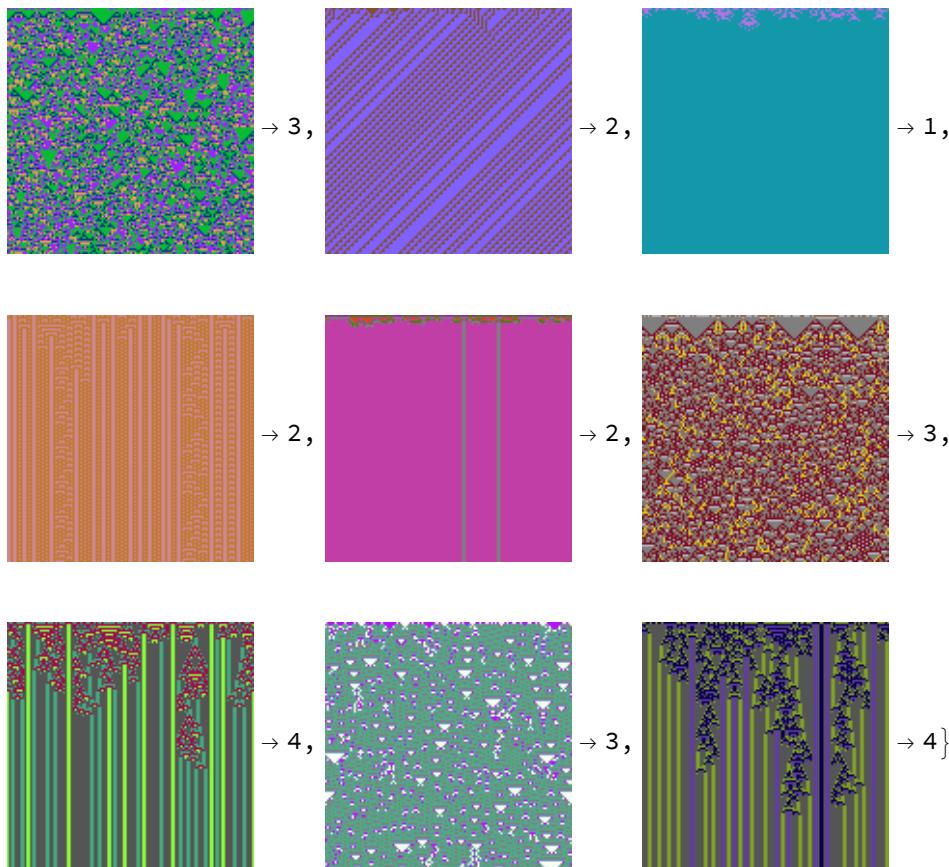
```
In[6]:= dataTotalistic3BigC13 = data3T2C[128, 128, 1024];
```

```
In[]:= dataTotalistic4BigC13 = data4TC[128, 128, 1024];
In[]:= dataTotalistic5BigC13 = genData5TCC[128, 128, 4096];
In[]:= fullTrainingBigC13 = Join[dataECA13, dataTotalistic2BigC13,
      dataTotalistic3BigC13, dataTotalistic4BigC13, dataTotalistic5BigC13];
Length[fullTrainingBigC13]

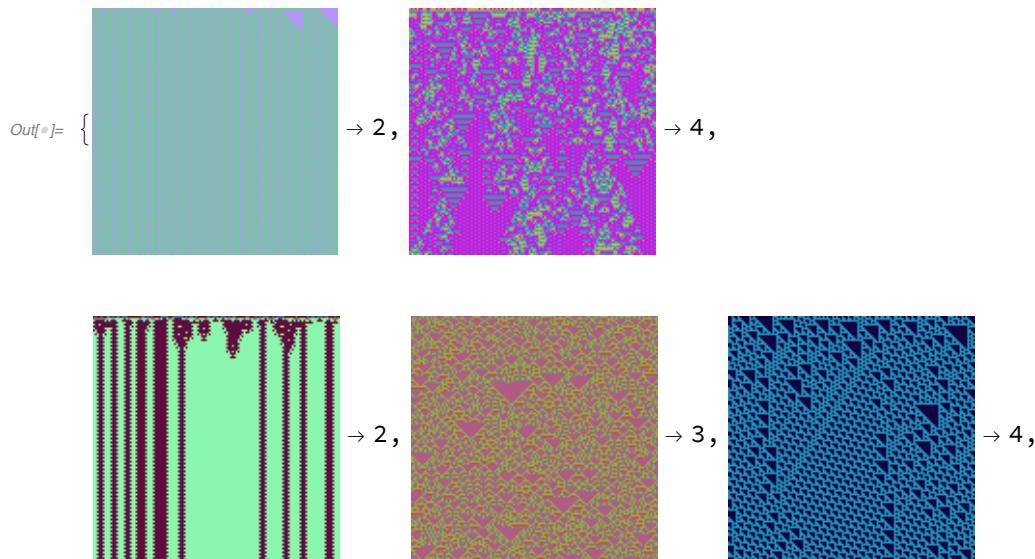
Out[]= 26624
```

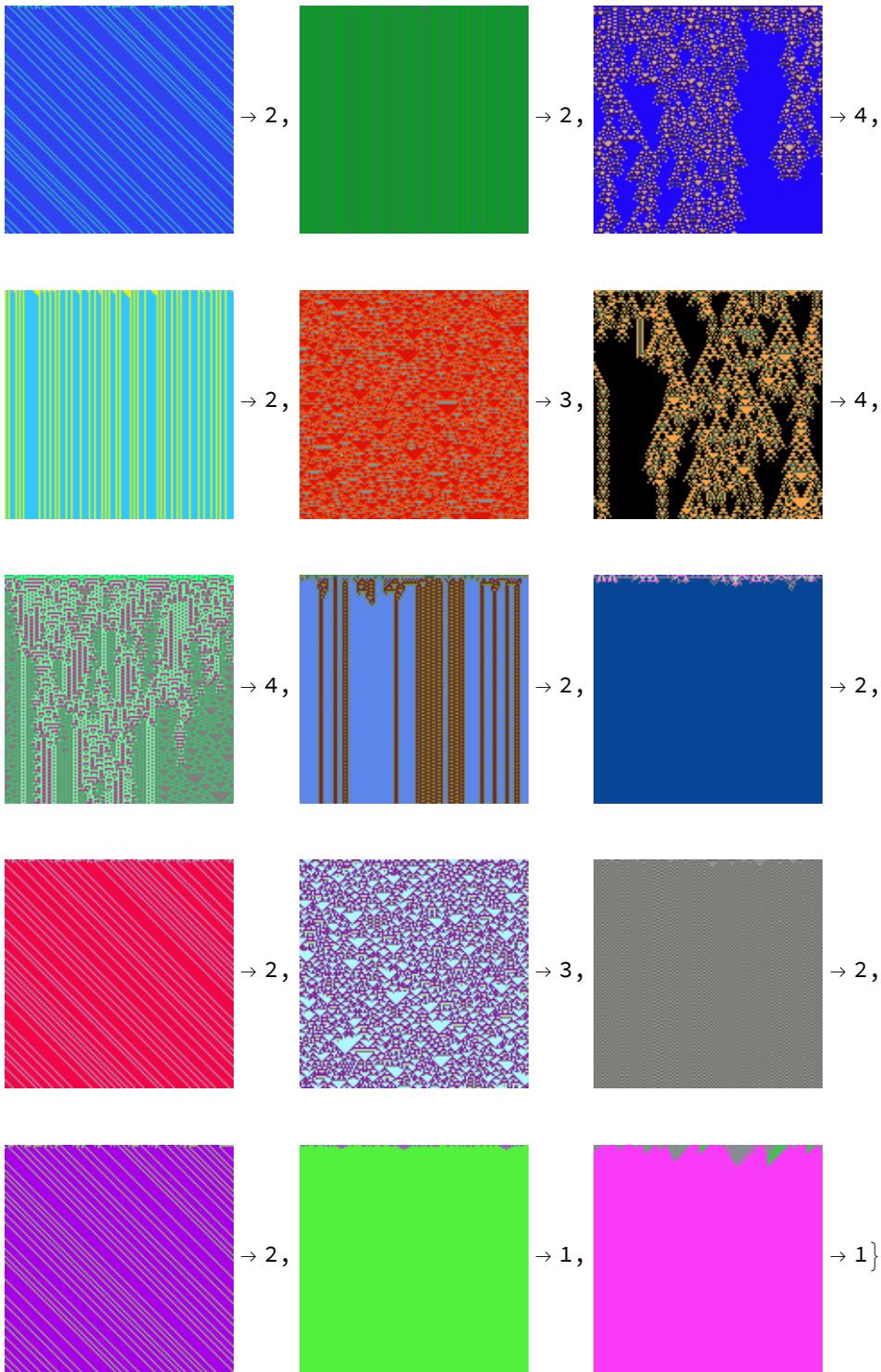
```
In[]:= RandomSample[fullTrainingBigC13, 20]
```





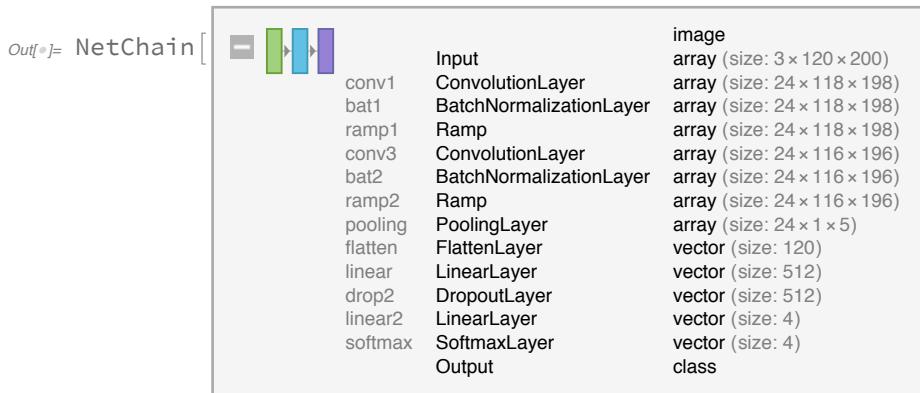
```
In[6]:= RandomSample[fullTrainingBigC13, 20]
```





```
In[®]:= dir = SetDirectory[NotebookDirectory[]]
Out[®]= /Users/thorsilver/Downloads/Wolfram notebooks
```

```
In[®]:= netECA12 = Import["netECA12-r12.wlnet"]
```



```
In[®]:= netECA13 = NetTrain[netECA13, fullTrainingBigC13,
  MaxTrainingRounds → 20, BatchSize → 256 * 4, TargetDevice → "CPU",
  TrainingProgressCheckpointing → {"Directory", dir}]
```



```
In[®]:= netECA13 = Import["netECA13-r20.wlnet"]
```



```
In[®]:= netECA13 = NetTrain[netECA13, fullTrainingBigC13,
  MaxTrainingRounds → 20, BatchSize → 256 * 4, TargetDevice → "CPU",
  TrainingProgressCheckpointing → {"Directory", dir}]
```



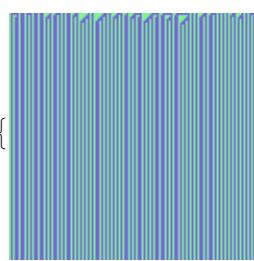
Generate test data for Network XIII

```
In[®]:= testDataECABigC = dataC[128, 128, 1024];
testData2TBigC = genData2r2C[128, 128, 1024];
testData3TBigC = data3T2C[128, 128, 1024];
testData4TBigC = data4TC[128, 128, 1024];
testData5TBigC = genData5TCC[128, 128, 1024];
fullTestSetBigC = Join[testDataECABigC,
  testData2TBigC, testData3TBigC, testData4TBigC, testData5TBigC];
Length[fullTestSetBigC]
```

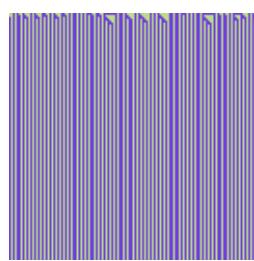
Out[®]= 10 240

```
In[®]:= RandomSample[fullTestSetBigC, 10]
```

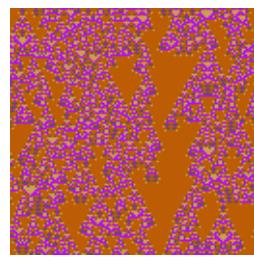
Out[®]= {



$\rightarrow 2,$



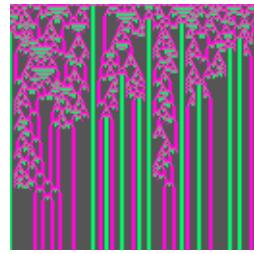
$\rightarrow 2,$



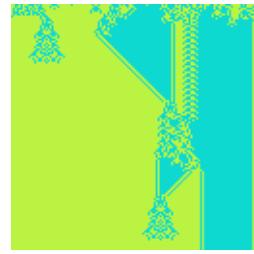
$\rightarrow 4,$



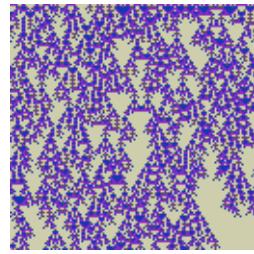
$\rightarrow 3,$



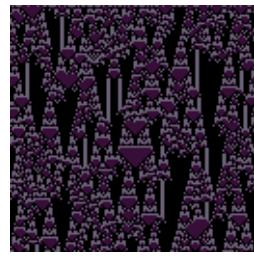
$\rightarrow 4,$



$\rightarrow 4,$



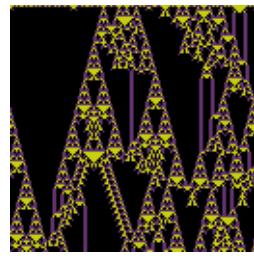
$\rightarrow 4,$



$\rightarrow 4,$



$\rightarrow 4,$

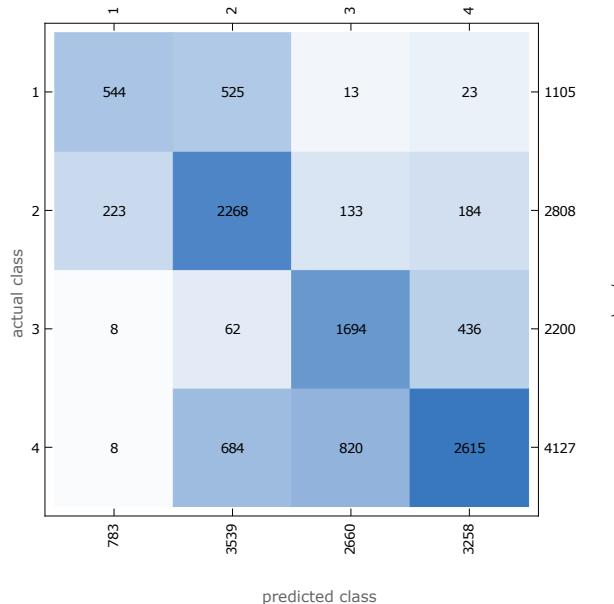


$\rightarrow 4\}$

```
In[8]:= NetMeasurements[netECA13, fullTestSetBigC,
```

```
{ "Accuracy", "Precision", "ConfusionMatrixPlot"}]
```

```
Out[8]= {0.69541, {1 → 0.694764, 2 → 0.640859, 3 → 0.636842, 4 → 0.80264},
```



```
In[9]:= entropyImagesBigC = RandomSample[Keys[fullTestSetBigC], 500];
```

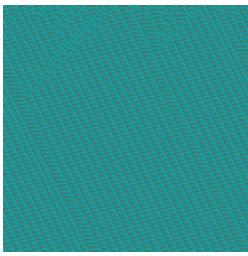
```
entropiesBigC = netECA13[entropyImagesBigC, "Entropy"];
```

```
highEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, -10]]];
```

```
lowEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, 10]]];
```

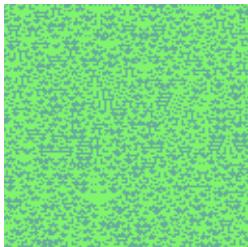
```
Thread[highEntBigC → netECA13[highEntBigC]]
```

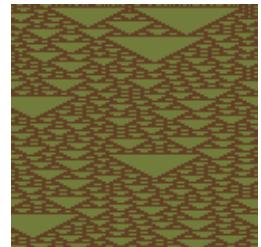
```
Thread[lowEntBigC → netECA13[lowEntBigC]]
```

Out[8]= { → 2,



→ 2,

 → 2,



→ 3,

 → 3,

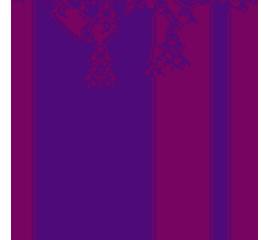


→ 2,

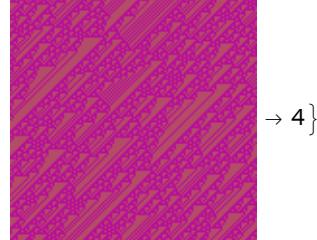


→ 4,

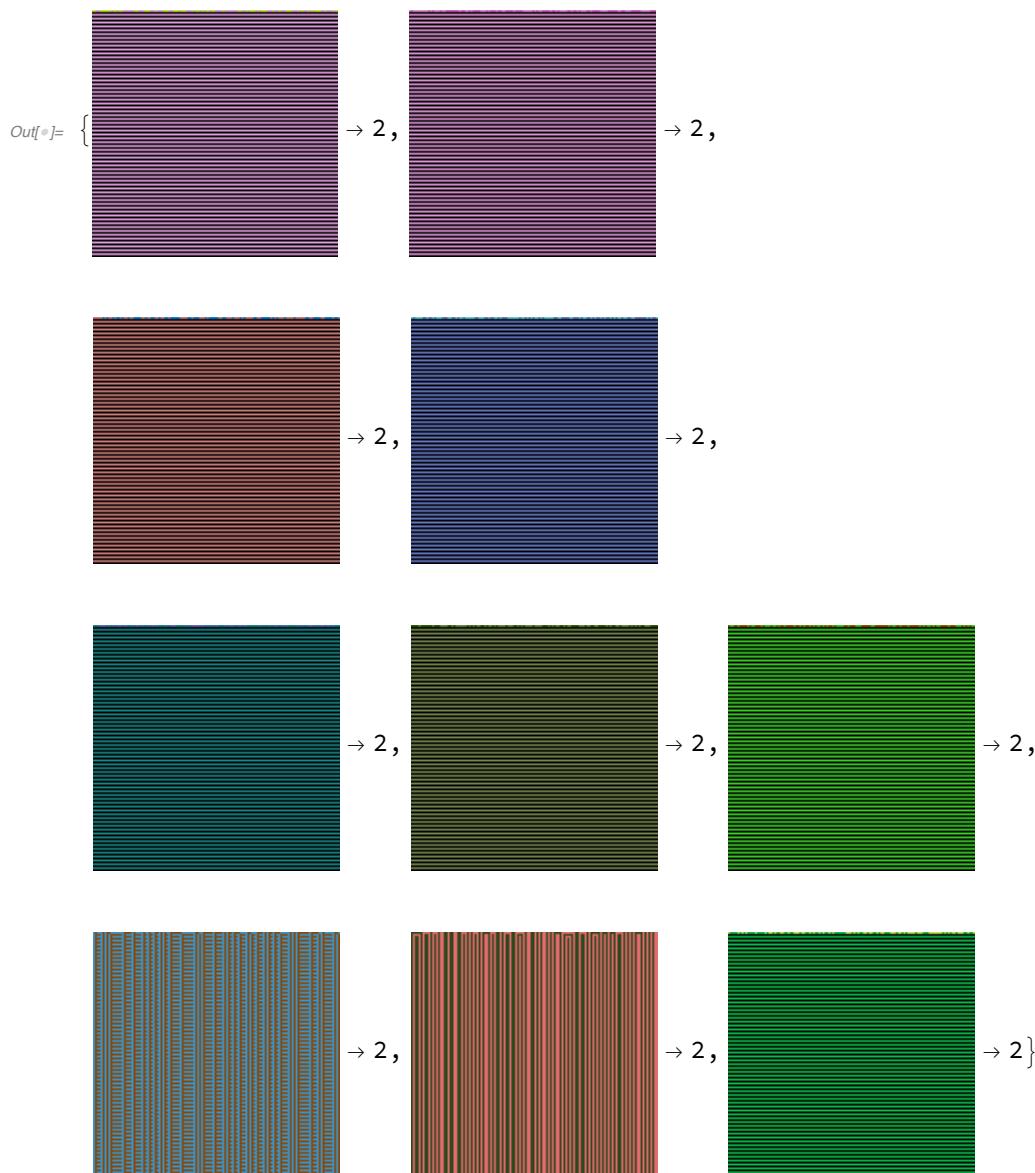
 → 2,



→ 2,

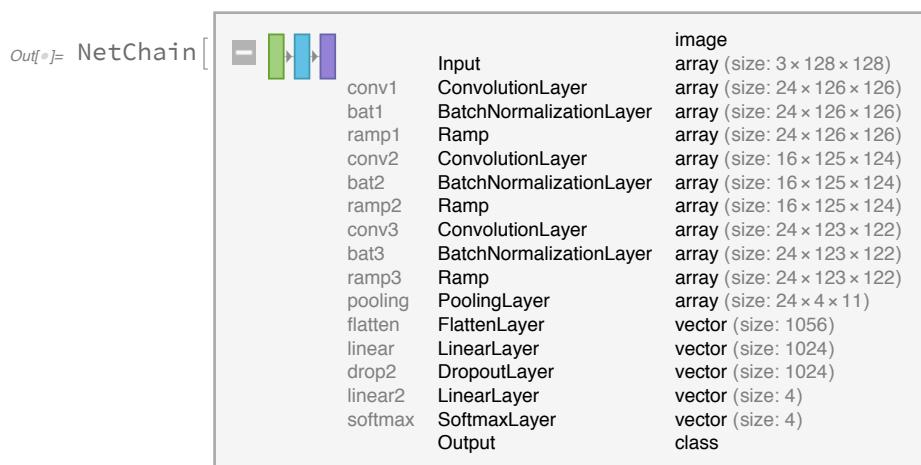


→ 4}



Network XIV - BatchNorm, 1024 linear, dropout

In[•]:= netECA14 = netEightCC512drop[128, 128]



```

netECA14 = NetTrain[netECA14, fullTrainingBigC13,
  MaxTrainingRounds → 20, BatchSize → 256 * 4, TargetDevice → "CPU",
  TrainingProgressCheckpointing → {"Directory", dir}]

In[]:= dir = SetDirectory[NotebookDirectory[]]
Out[]:= /Users/thorsilver/Downloads/Wolfram notebooks

In[]:= netECA14 = Import["netECA14-r20.wlnet"]

```

	Input	
conv1	ConvolutionLayer	array (size: 3 × 128 × 128)
bat1	BatchNormalizationLayer	array (size: 24 × 126 × 126)
ramp1	Ramp	array (size: 24 × 126 × 126)
conv2	ConvolutionLayer	array (size: 24 × 125 × 124)
bat2	BatchNormalizationLayer	array (size: 16 × 125 × 124)
ramp2	Ramp	array (size: 16 × 125 × 124)
conv3	ConvolutionLayer	array (size: 24 × 123 × 122)
bat3	BatchNormalizationLayer	array (size: 24 × 123 × 122)
ramp3	Ramp	array (size: 24 × 123 × 122)
pooling	PoolingLayer	array (size: 24 × 4 × 11)
flatten	FlattenLayer	vector (size: 1056)
linear	LinearLayer	vector (size: 1024)
drop2	DropoutLayer	vector (size: 1024)
linear2	LinearLayer	vector (size: 4)
softmax	SoftmaxLayer	vector (size: 4)
Output		class

Generating test data for Network XIV

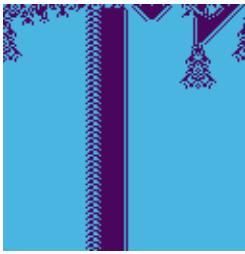
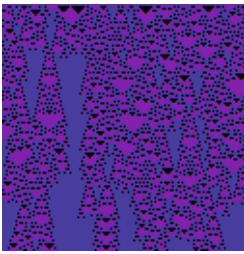
```

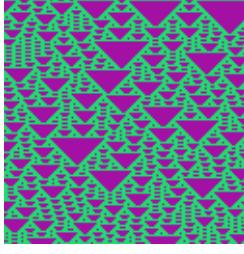
In[]:= testDataECABigC = dataC[128, 128, 1024];
testData2TBigC = genData2r2C[128, 128, 1024];
testData3TBigC = data3T2C[128, 128, 1024];
testData4TBigC = data4TC[128, 128, 1024];
testData5TBigC = genData5TCC[128, 128, 1024];
fullTestSetBigC = Join[testDataECABigC,
  testData2TBigC, testData3TBigC, testData4TBigC, testData5TBigC];
Length[fullTestSetBigC]

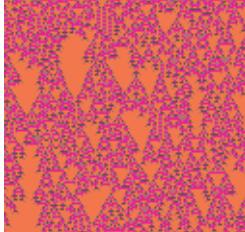
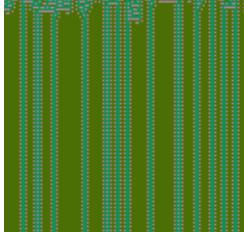
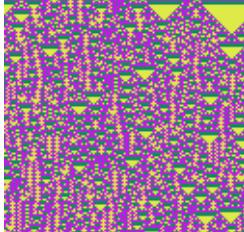
Out[]:= 10 240

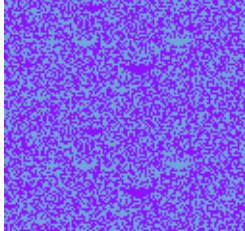
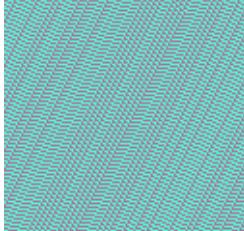
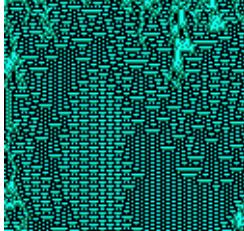
```

```
In[®]:= RandomSample[fullTestSetBigC, 10]
```

Out[®]= { → 4,  → 4,

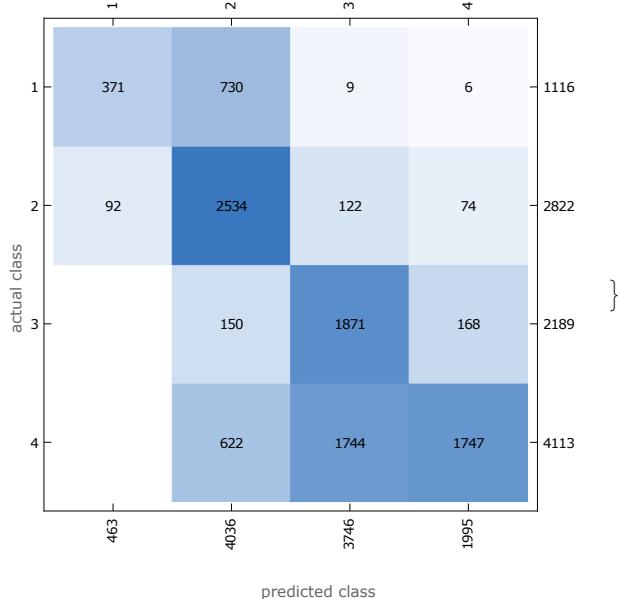
 → 4,  → 3,

 → 4,  → 2,  → 3,

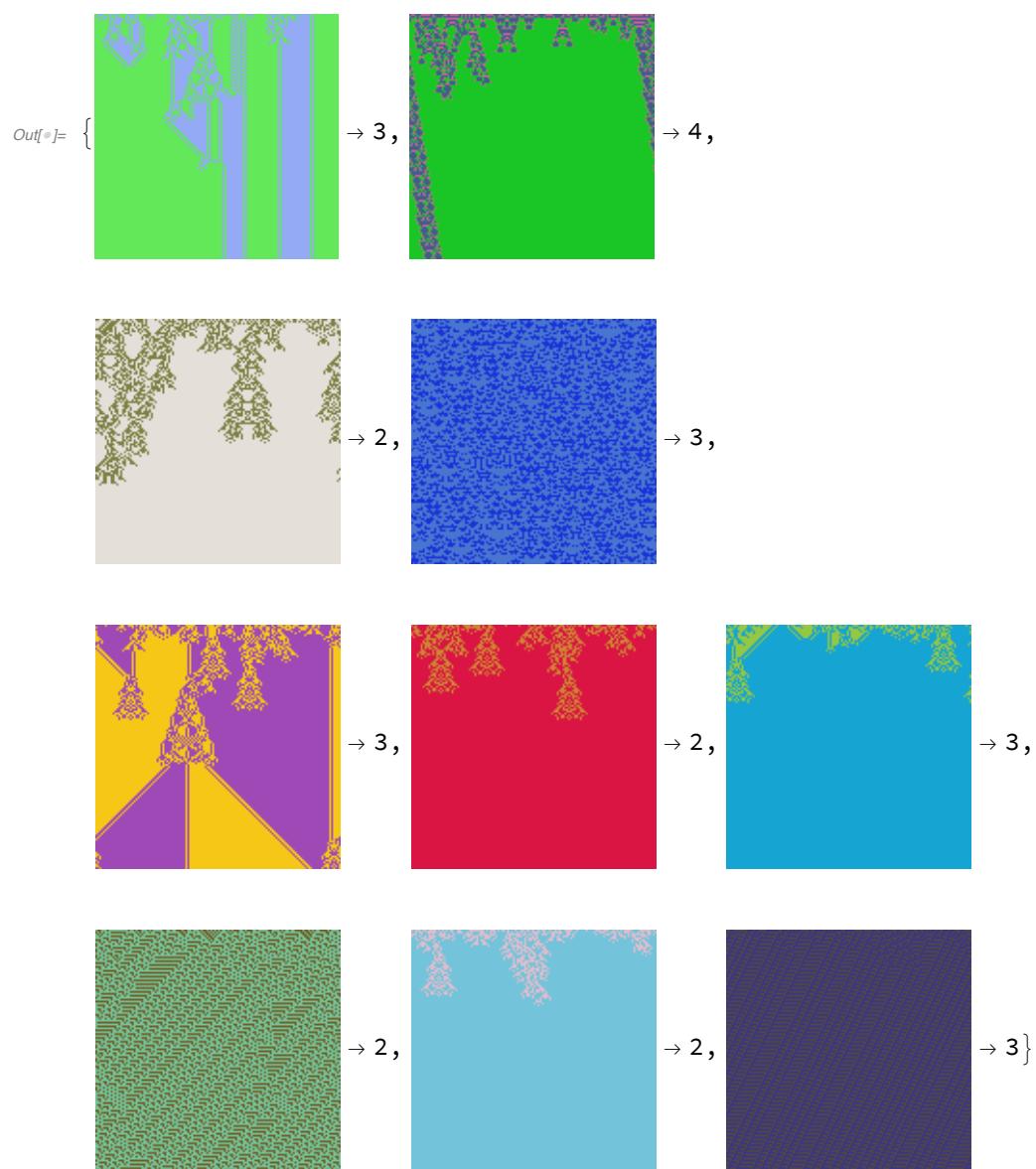
 → 3,  → 2,  → 4}

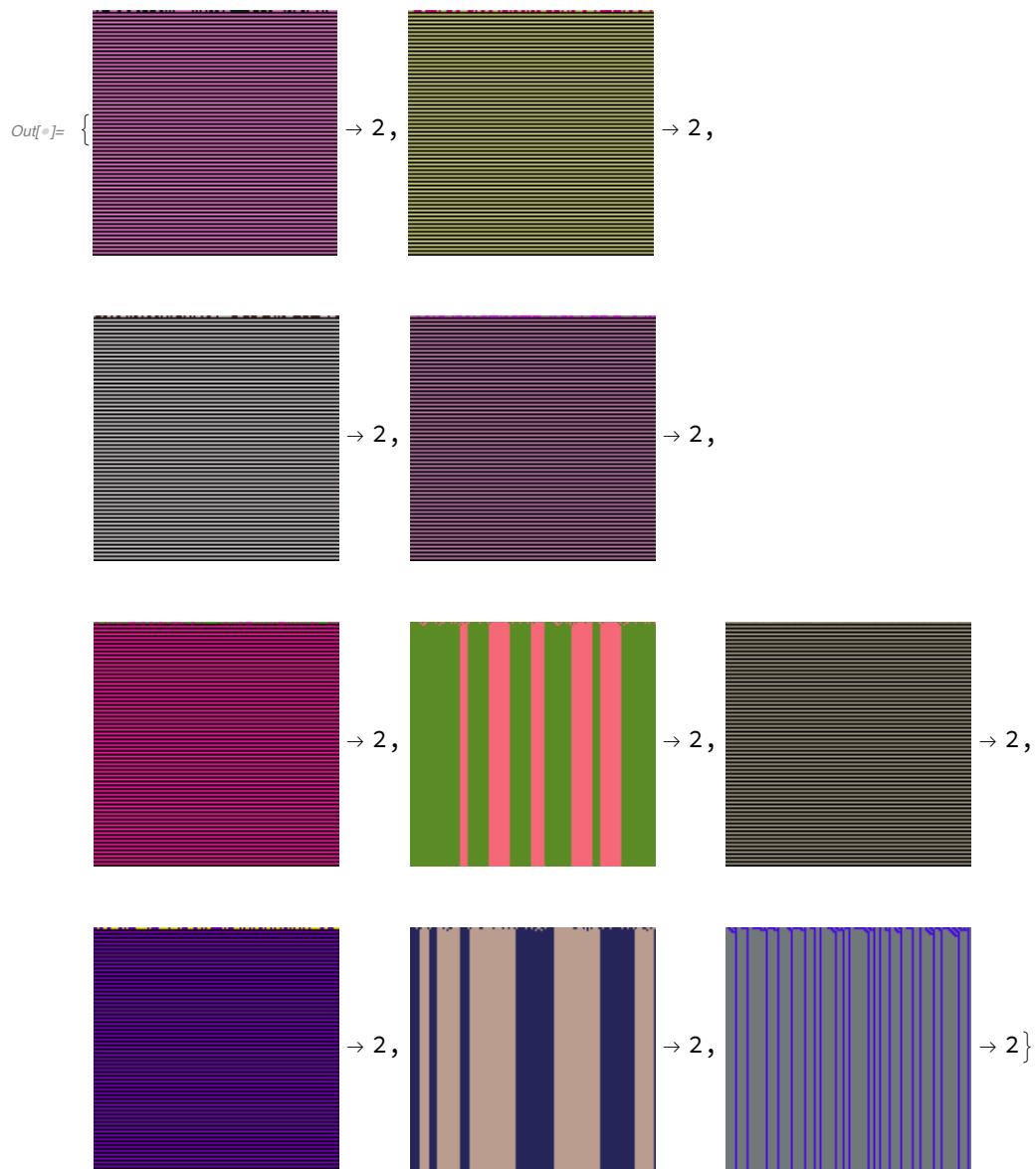
```
In[®]:= NetMeasurements[netECA14, fullTestSetBigC,
 {"Accuracy", "Precision", "ConfusionMatrixPlot"}]

Out[®]= {0.637012, <| 1 → 0.801296, 2 → 0.627849, 3 → 0.499466, 4 → 0.875689 |>, }
```



```
In[®]:= entropyImagesBigC = RandomSample[Keys[fullTestSetBigC], 500];
entropiesBigC = netECA14[entropyImagesBigC, "Entropy"];
highEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, -10]]];
lowEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, 10]]];
Thread[highEntBigC → netECA14[highEntBigC]]
Thread[lowEntBigC → netECA14[lowEntBigC]]
```





Network XV - Transfer learning with pre-trained image recognition net (VGG-16)

```
In[⑩]:= netECA15 = NetModel["VGG-16 Trained on ImageNet Competition Data"]
```



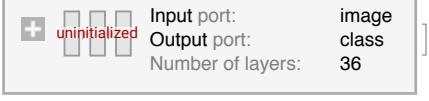
```
In[⑪]:= subNet = NetTake[netECA15, {"conv1_1", "flatten_0"}]
```



```
In[⑫]:= joinedNet = NetJoin[subNet,
  NetChain@<|"linear_new" → LinearLayer[1024], "linear_out" → LinearLayer[4],
  "prob" → SoftmaxLayer[]|>, "Output" → NetDecoder[{"Class", Range[1, 4]}]]
```



```
In[®]:= netECA15final =
NetPrepend[joinedNet, {"augment" → ImageAugmentationLayer[{224, 224}]}],
"Input" → NetExtract[joinedNet, "Input"]]

Out[®]= NetChain[]
  Input port: image class
  Output port: image class
  Number of layers: 36
```

In[®]:= dataECA15 = dataC[224, 224, 8192];

In[®]:= dataTotalistic2BigC15 = genData2r2C[224, 224, 1024];

In[®]:= dataTotalistic3BigC15 = data3T2C[224, 224, 512];

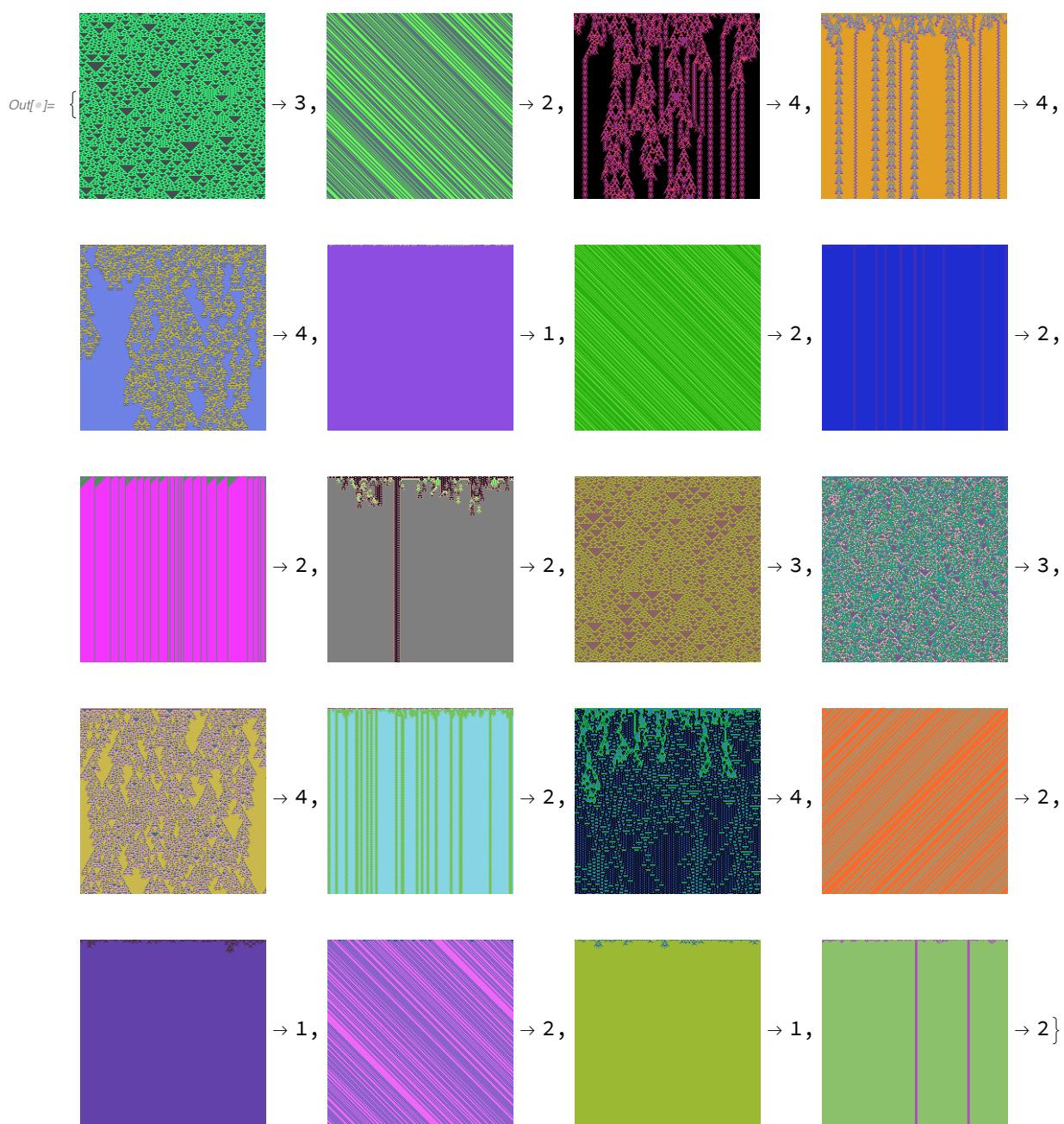
In[®]:= dataTotalistic4BigC15 = data4TC[224, 224, 512];

In[®]:= dataTotalistic5BigC15 = genData5TCC[224, 224, 1024];

In[®]:= fullTrainingBigC15 = Join[dataECA15, dataTotalistic2BigC15,
 dataTotalistic3BigC15, dataTotalistic4BigC15, dataTotalistic5BigC15];
Length[fullTrainingBigC15]

Out[®]= 16 384

In[8]:= RandomSample[fullTrainingBigC15, 20]



In[9]:= netECA15final = NetTrain[netECA15final, fullTrainingBigC15,
MaxTrainingRounds → 5, BatchSize → 256 * 4, TargetDevice → "CPU",
TrainingProgressCheckpointing → {"Directory", dir},
LearningRateMultipliers → {"linear_new" → 1, "linear_out" → 1, _ → 0}]

Network XVI - Three convolutions, dropout on linear only, BatchNorm

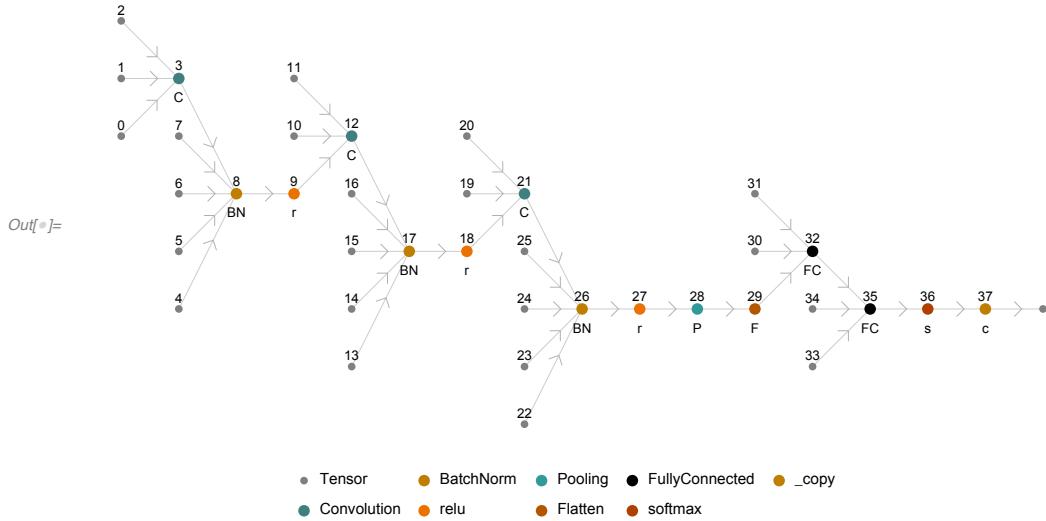
In[10]:= netECA16 = netNineCC512drop[128, 128]

Out[10]= NetChain[

	Input port:	image
	Output port:	class
	Number of layers:	15

]

```
In[④]:= NetInformation[netECA16, "MXNetNodeGraphPlot"]
```



```
In[⑤]:= NetInformation[netECA16, "SummaryGraphic"]
```



```
In[⑥]:= dataECA16 = dataC[128, 128, 8192];
```

```
In[⑦]:= dataTotalistic2BigC16 = genData2r2C[128, 128, 1024];
```

```
In[⑧]:= dataTotalistic3BigC16 = data3T2C[128, 128, 1024];
```

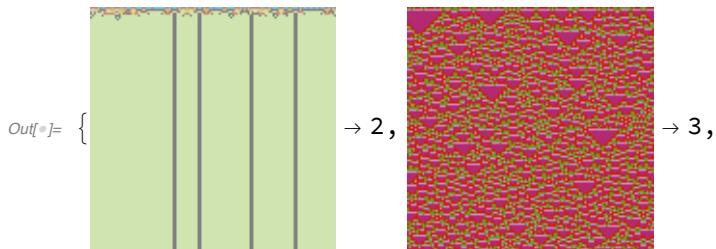
```
In[⑨]:= dataTotalistic4BigC16 = data4TC[128, 128, 1024];
```

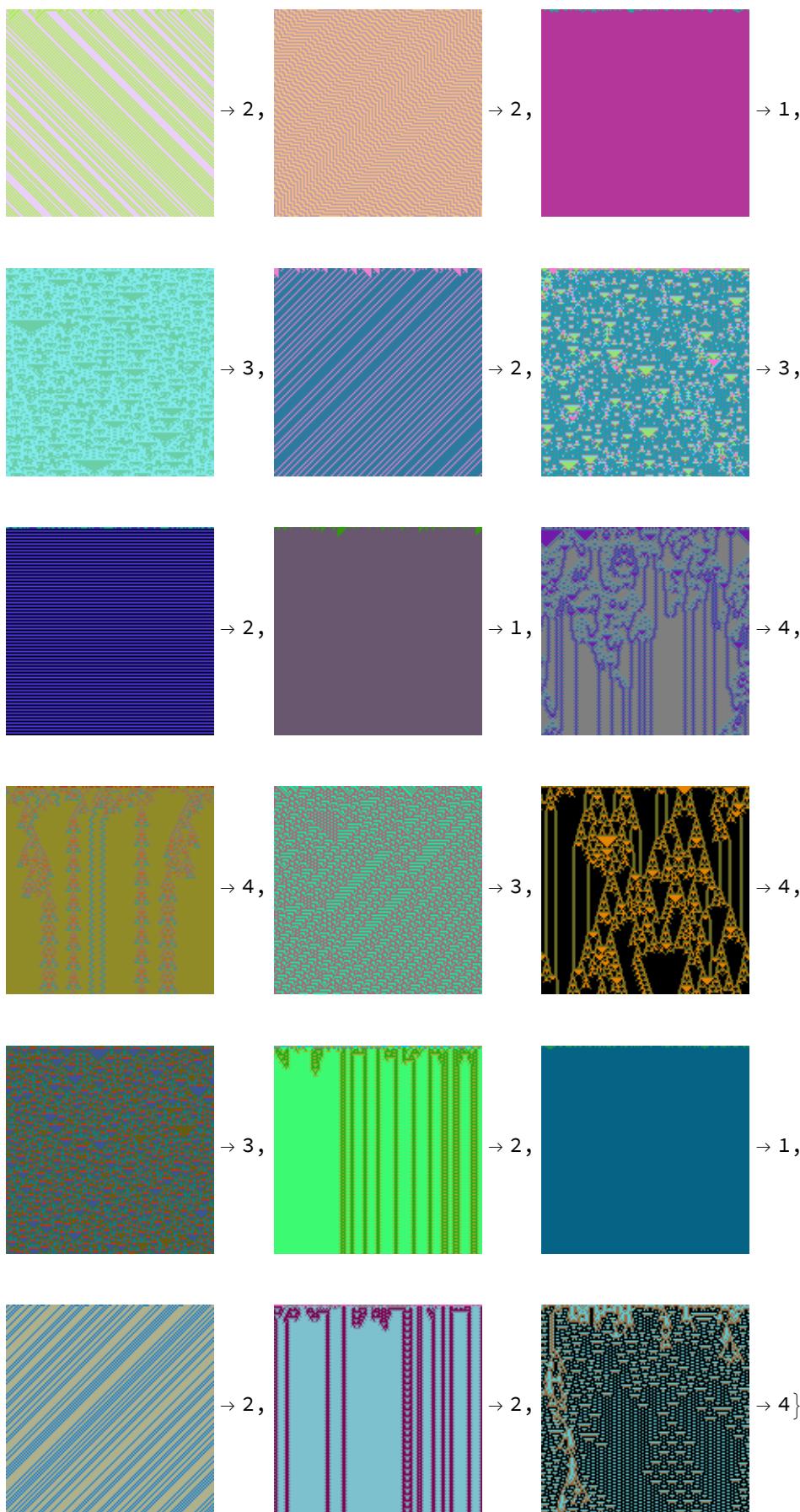
```
In[⑩]:= dataTotalistic5BigC16 = genData5TCC[128, 128, 4096];
```

```
In[⑪]:= fullTrainingBigC16 = Join[dataECA16, dataTotalistic2BigC16,
    dataTotalistic3BigC16, dataTotalistic4BigC16, dataTotalistic5BigC16];
Length[fullTrainingBigC16]
```

Out[⑪]= 26 624

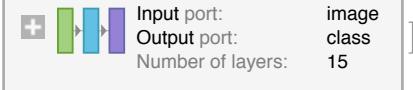
```
In[⑫]:= RandomSample[fullTrainingBigC16, 20]
```





```
In[®]:= dir = SetDirectory[NotebookDirectory[]]
Out[®]= /home/esilverman/Documents

In[®]:= netECA16 = NetTrain[netECA16, fullTrainingBigC16,
  MaxTrainingRounds → 200, BatchSize → 256, TargetDevice → "GPU",
  TrainingProgressCheckpointing → {"Directory", dir}]

Out[®]= NetChain[]
```

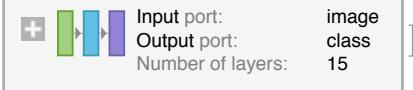
```
netECA16 = Import["netECA16-r20.wlnet"]

netECA16 = NetTrain[netECA16, fullTrainingBigC16,
  MaxTrainingRounds → 20, BatchSize → 256 * 4, TargetDevice → "CPU",
  TrainingProgressCheckpointing → {"Directory", dir}]
```

Generate test data for Network XVI

```
In[®]:= dir = SetDirectory[NotebookDirectory[]]
Out[®]= /Users/thorsilver/Downloads/Wolfram notebooks

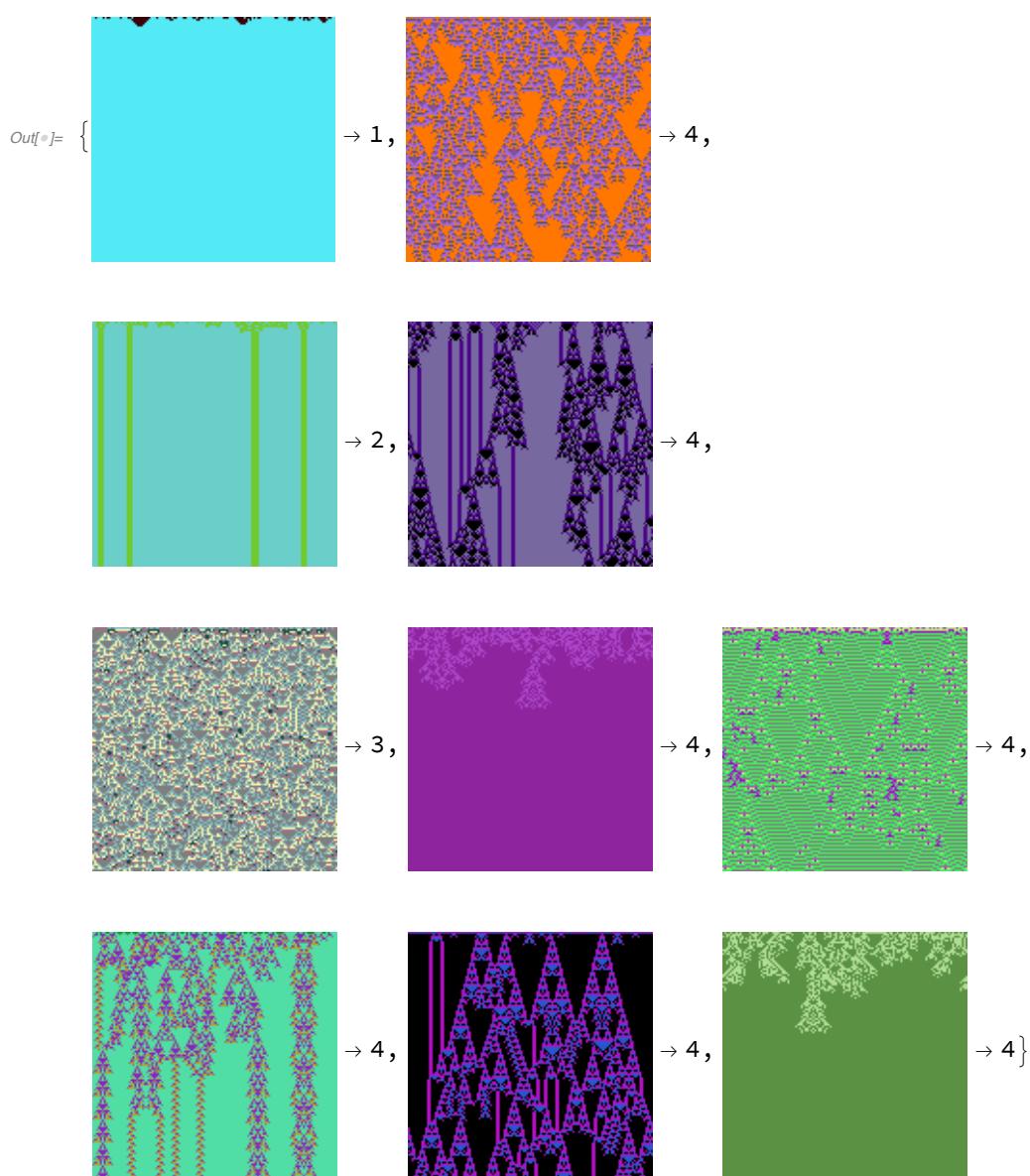
In[®]:= netECA16 = Import["netECA16-r20.wlnet"]

Out[®]= NetChain[]
```

```
In[®]:= testDataECABigC = dataC[128, 128, 1024];
testData2TBigC = genData2r2C[128, 128, 1024];
testData3TBigC = data3T2C[128, 128, 1024];
testData4TBigC = data4TC[128, 128, 1024];
testData5TBigC = genData5TCC[128, 128, 1024];
fullTestSetBigC = Join[testDataECABigC,
  testData2TBigC, testData3TBigC, testData4TBigC, testData5TBigC];
Length[fullTestSetBigC]

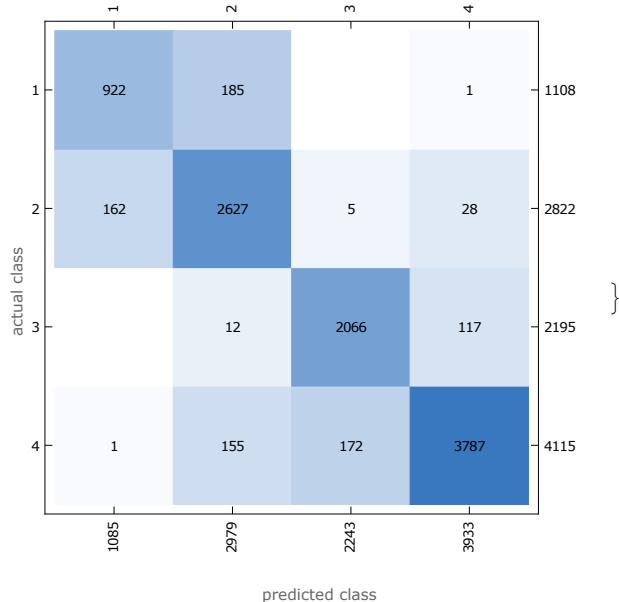
Out[®]= 10 240
```

```
In[®]:= RandomSample[fullTestSetBigC, 10]
```

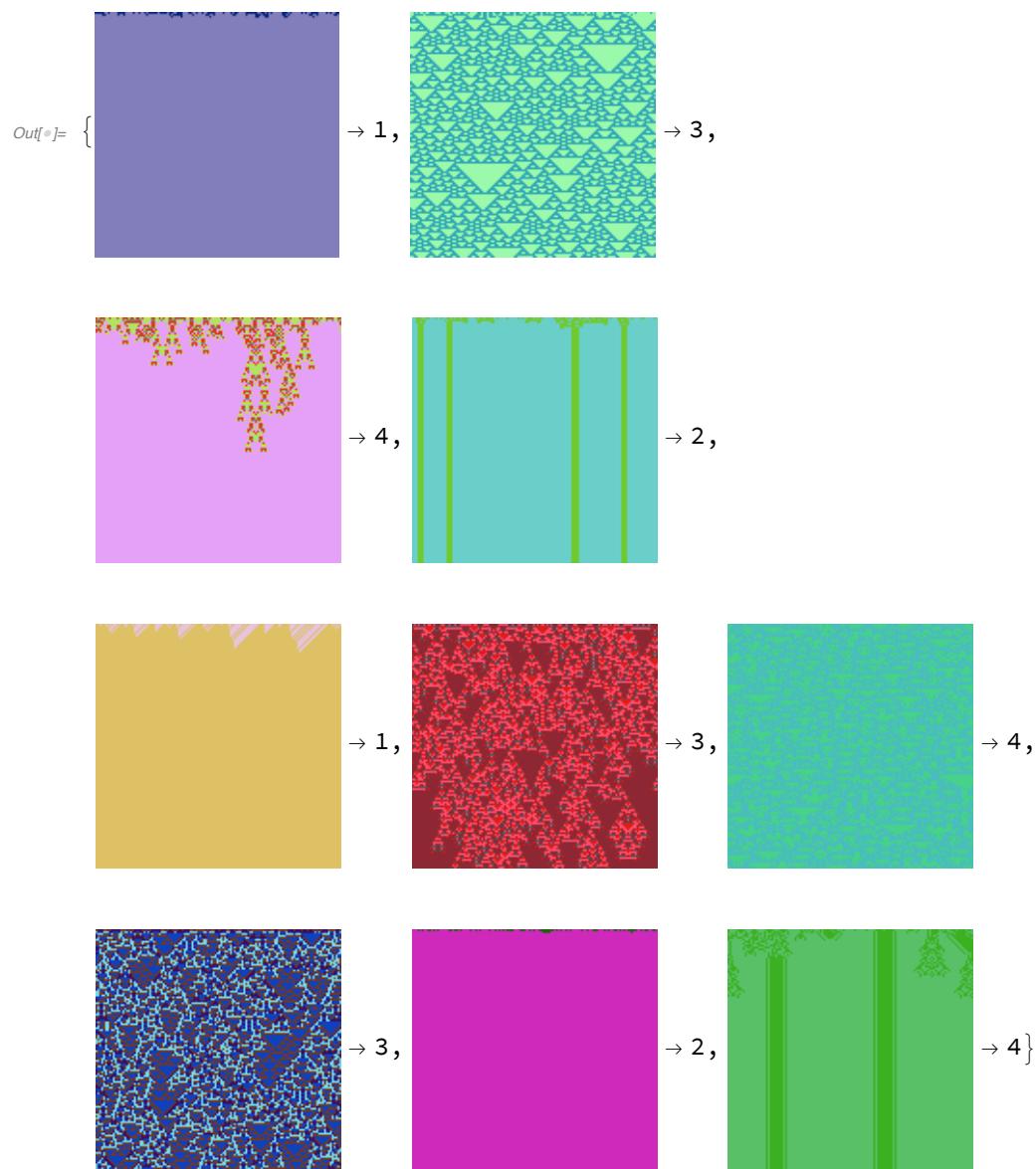


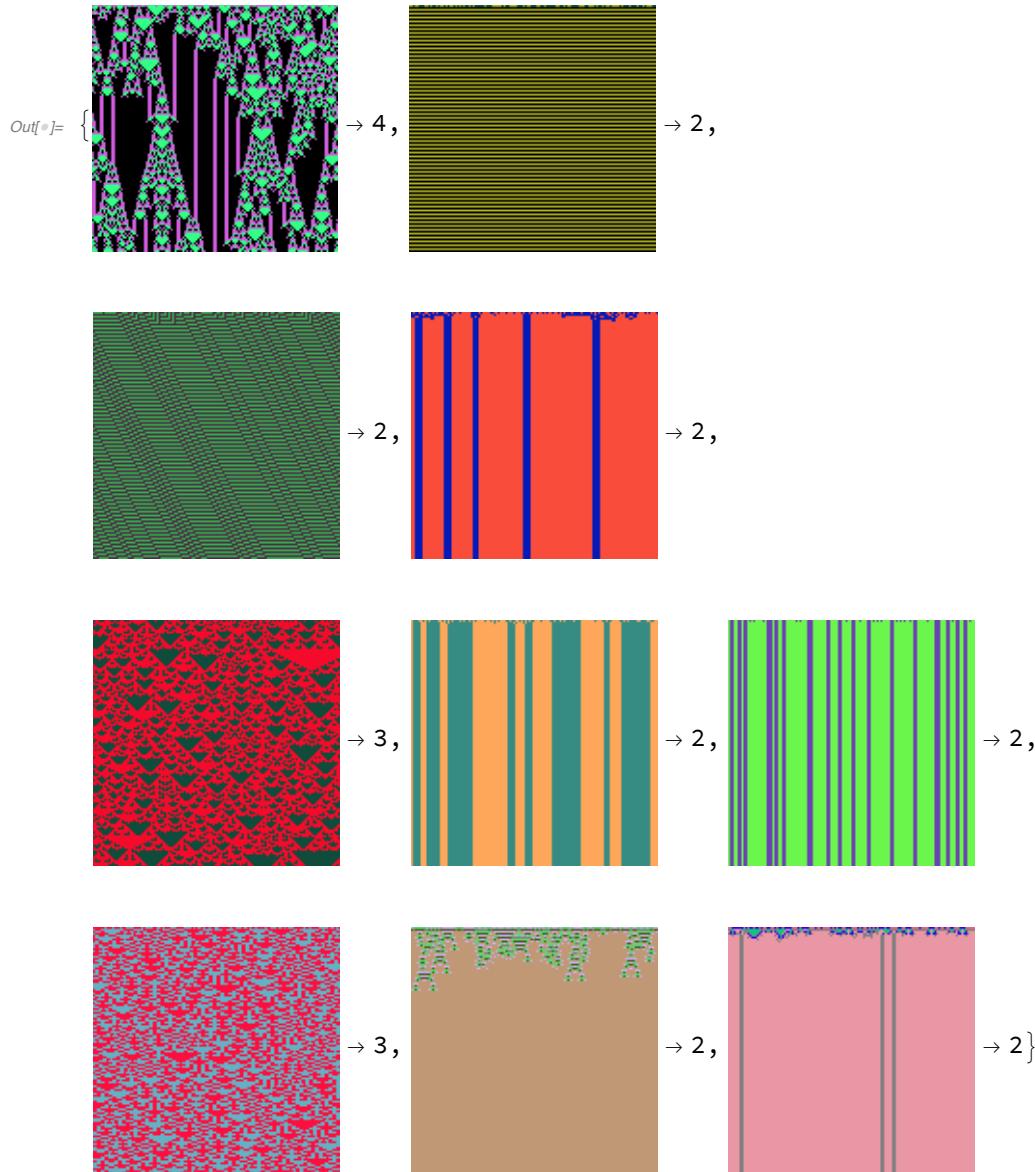
```
In[®]:= NetMeasurements[netECA16, fullTestSetBigC,
 {"Accuracy", "Precision", "ConfusionMatrixPlot"}]

Out[®]= {0.918164, <| 1 → 0.84977, 2 → 0.88184, 3 → 0.921088, 4 → 0.962878 |>, }
```



```
In[®]:= entropyImagesBigC = RandomSample[Keys[fullTestSetBigC], 500];
entropiesBigC = netECA16[entropyImagesBigC, "Entropy"];
highEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, -10]]];
lowEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, 10]]];
Thread[highEntBigC → netECA16[highEntBigC]]
Thread[lowEntBigC → netECA16[lowEntBigC]]
```





Testing Network XVI on unseen CA rule spaces

2-colour non-totalistic, range 2

```
In[•]:= test4Data2kr2C16 = datak2r2C[128, 128, 8];
Thread[
  test4Data2kr2C16 → netECA16[Keys@test4Data2kr2C16, {"TopProbabilities", 2}]]
```

Out[•]:= {

→ 142 978 078 → {4 → 0.0000385332, 3 → 0.999961},

$$\left(\begin{array}{c} \text{[A 4x4 grid of red dots]} \\ \rightarrow 2\ 651\ 048\ 833 \end{array} \right) \rightarrow \{ 4 \rightarrow 8.69455 \times 10^{-12}, 2 \rightarrow 1. \},$$

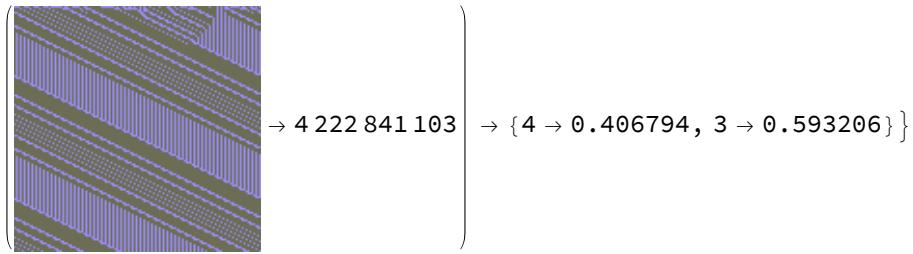
$$\left(\begin{array}{c} \text{[A 4x4 grid of blue dots]} \\ \rightarrow 2\ 132\ 867\ 963 \end{array} \right) \rightarrow \{ 4 \rightarrow 2.86202 \times 10^{-17}, 2 \rightarrow 1. \},$$

$$\left(\begin{array}{c} \text{[A 4x4 grid of yellow dots]} \\ \rightarrow 3\ 644\ 758\ 968 \end{array} \right) \rightarrow \{ 4 \rightarrow 6.11899 \times 10^{-7}, 3 \rightarrow 0.999999 \},$$

$$\left(\begin{array}{c} \text{[A 4x4 grid of green and blue diagonal stripes]} \\ \rightarrow 1\ 762\ 420\ 096 \end{array} \right) \rightarrow \{ 1 \rightarrow 2.34707 \times 10^{-9}, 2 \rightarrow 1. \},$$

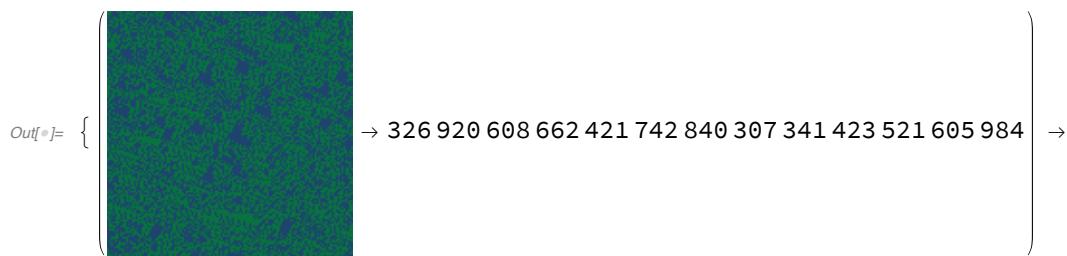
$$\left(\begin{array}{c} \text{[A 4x4 grid of brown dots]} \\ \rightarrow 1\ 983\ 429\ 391 \end{array} \right) \rightarrow \{ 4 \rightarrow 0.0547227, 3 \rightarrow 0.945277 \},$$

$$\left(\begin{array}{c} \text{[A 4x4 grid of dark green dots]} \\ \rightarrow 3\ 013\ 553\ 323 \end{array} \right) \rightarrow \{ 3 \rightarrow 0.0109364, 2 \rightarrow 0.989064 \},$$

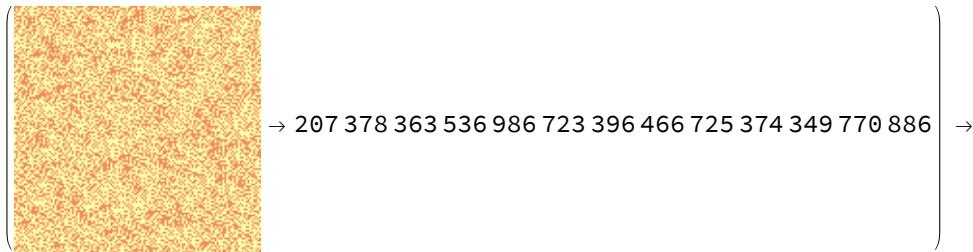


2-colour non-totalistic, range 3

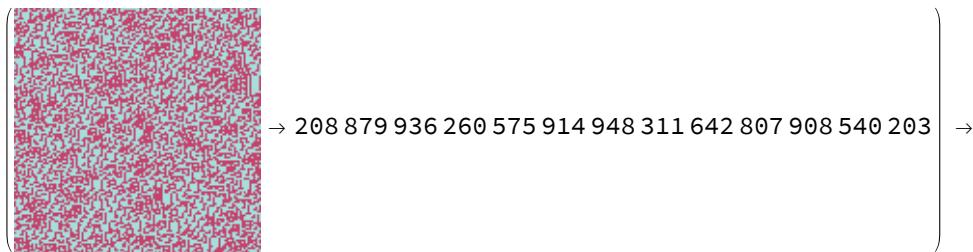
```
In[6]:= test4Data2kr3C16 = datak2r3NT[128, 128, 8];
Thread[
test4Data2kr3C16 → netECA16[Keys@test4Data2kr3C16, {"TopProbabilities", 2}]]
```



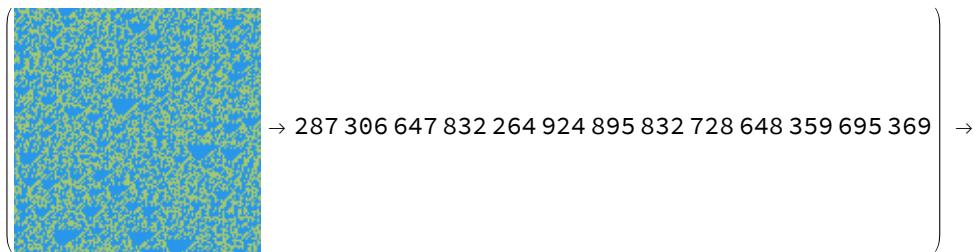
{4 → 0.250823, 3 → 0.749175},



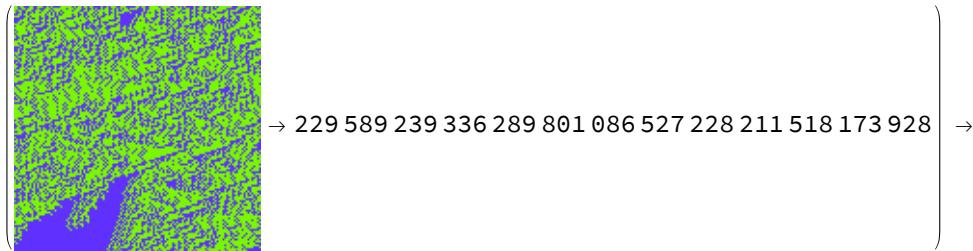
{4 → 3.99297 × 10⁻¹⁴, 3 → 1.},



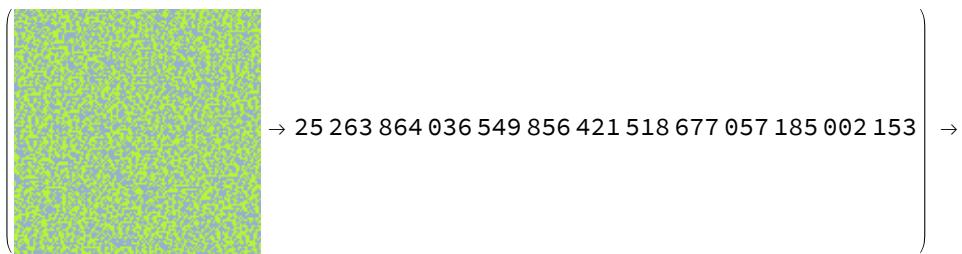
{4 → 1.58015 × 10⁻¹¹, 3 → 1.},



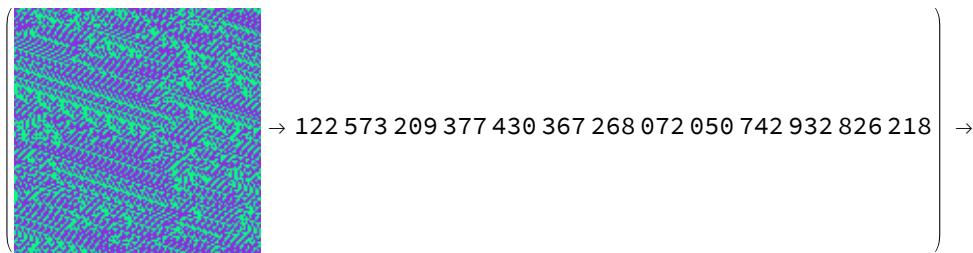
$\{4 \rightarrow 1.21845 \times 10^{-8}, 3 \rightarrow 1.\}$,



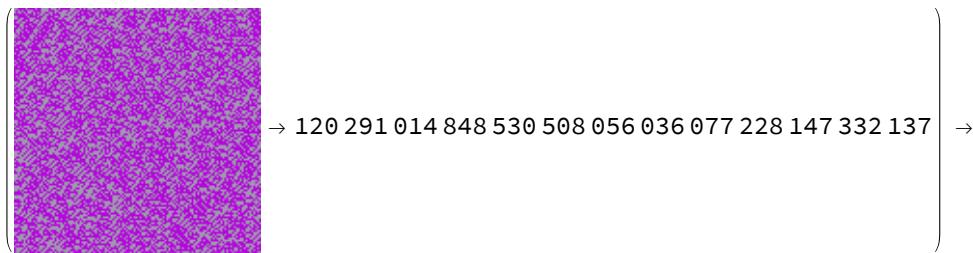
$\{3 \rightarrow 0.0173989, 4 \rightarrow 0.982601\}$,



$\{4 \rightarrow 2.486 \times 10^{-11}, 3 \rightarrow 1.\}$,



$\{4 \rightarrow 1.46881 \times 10^{-9}, 3 \rightarrow 1.\}$,



$\{4 \rightarrow 0.00683298, 3 \rightarrow 0.993167\}\}$

3-colour non-totalistic, range 1

```
In[6]:= test4Data3kr1C16 = datak3r1NT[128, 128, 8];
Thread[
test4Data3kr1C16 → netECA16[Keys@test4Data3kr1C16, {"TopProbabilities", 2}]]
```

Out[•]= $\left\{ \begin{array}{c} \text{A 2D grid of black and white dots} \\ \rightarrow 4\ 431\ 477\ 695\ 805 \end{array} \right\} \rightarrow \{ 4 \rightarrow 0.000746188, 3 \rightarrow 0.999254 \},$

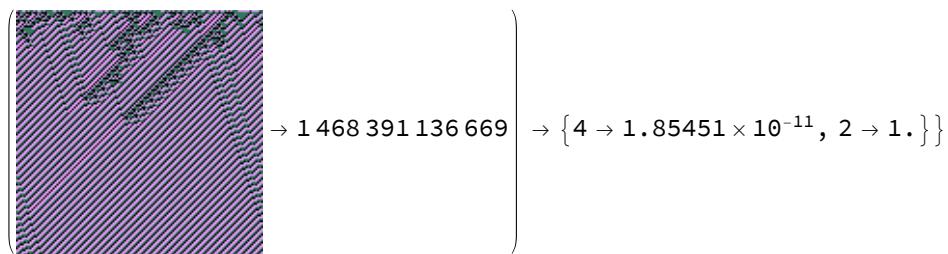
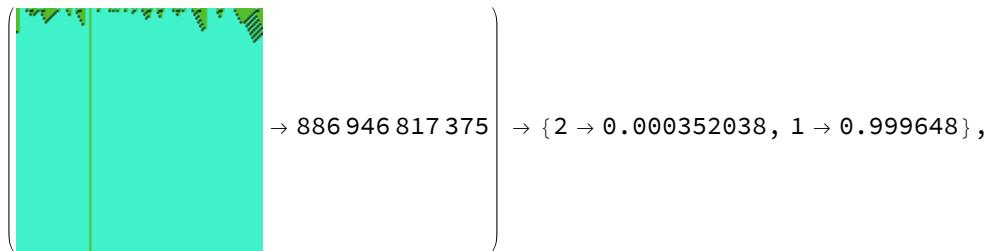
$\left\{ \begin{array}{c} \text{A 2D grid of green and black dots} \\ \rightarrow 1\ 627\ 958\ 441\ 874 \end{array} \right\} \rightarrow \{ 4 \rightarrow 0.00025369, 3 \rightarrow 0.999746 \},$

$\left\{ \begin{array}{c} \text{A 2D grid of blue, red, and black dots} \\ \rightarrow 4\ 241\ 674\ 451\ 024 \end{array} \right\} \rightarrow \{ 3 \rightarrow 0.194892, 2 \rightarrow 0.805108 \},$

$\left\{ \begin{array}{c} \text{A 2D grid of orange, green, and black dots} \\ \rightarrow 4\ 177\ 916\ 755\ 057 \end{array} \right\} \rightarrow \{ 3 \rightarrow 9.07174 \times 10^{-18}, 4 \rightarrow 1. \},$

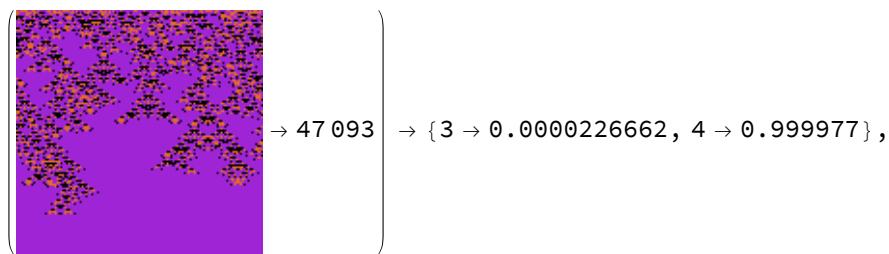
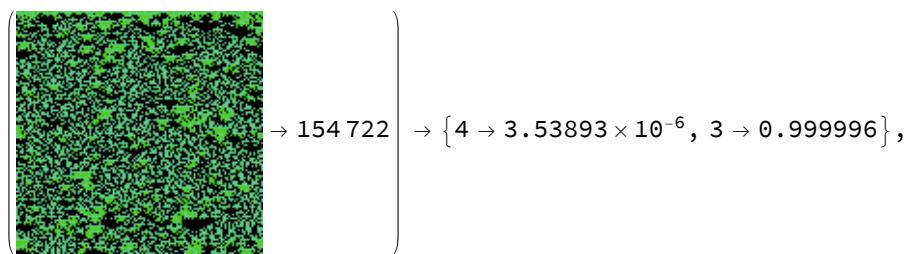
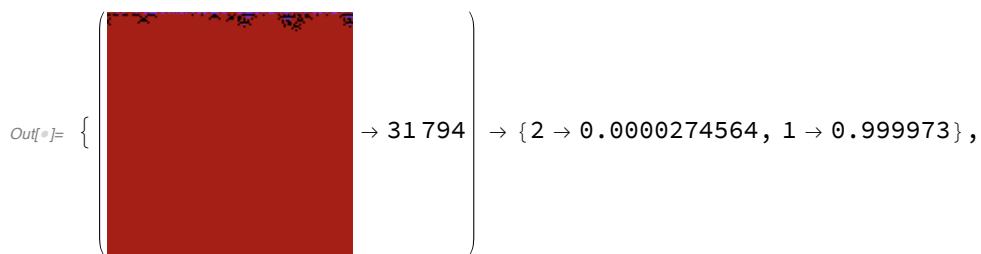
$\left\{ \begin{array}{c} \text{A 2D grid of red and green vertical stripes} \\ \rightarrow 2\ 504\ 235\ 138\ 103 \end{array} \right\} \rightarrow \{ 4 \rightarrow 1.3375 \times 10^{-21}, 2 \rightarrow 1. \},$

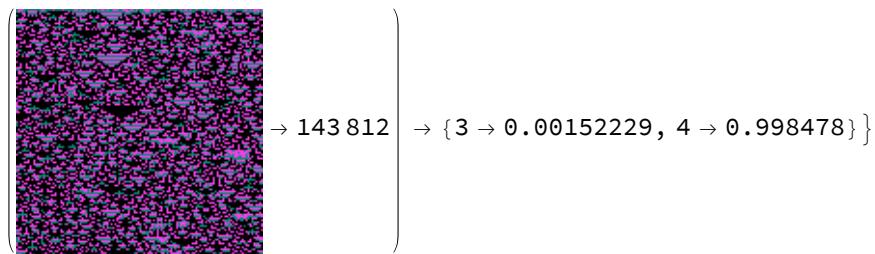
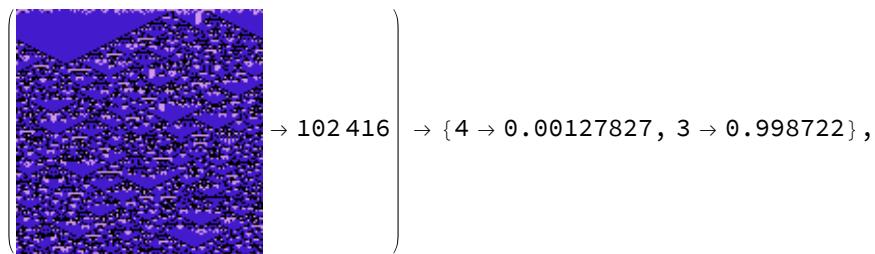
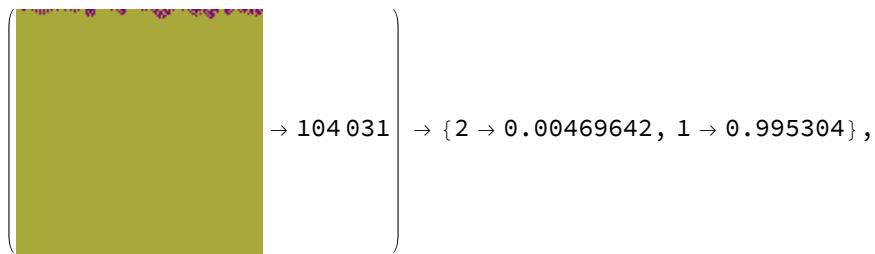
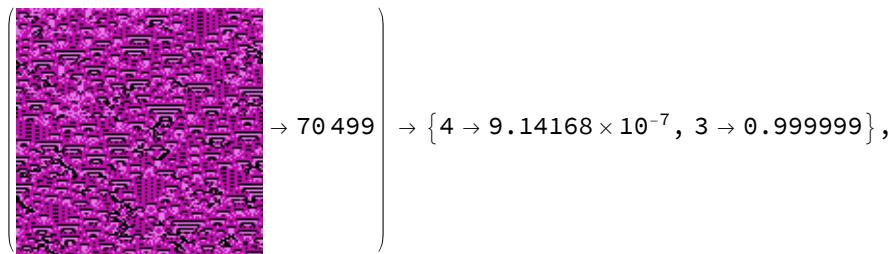
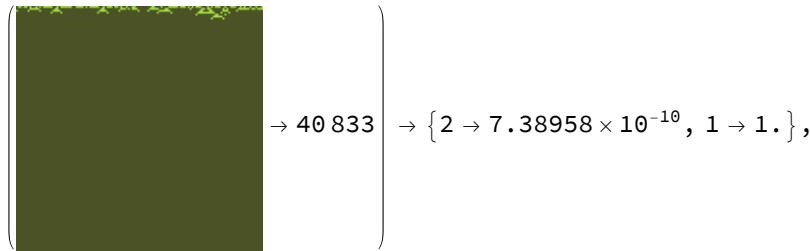
$\left\{ \begin{array}{c} \text{A 2D grid of yellow and pink dots} \\ \rightarrow 2\ 281\ 646\ 033\ 785 \end{array} \right\} \rightarrow \{ 4 \rightarrow 0.164883, 3 \rightarrow 0.835117 \},$



3-colour totalistic, range 2

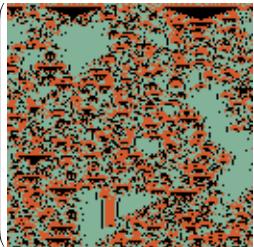
```
In[]:= test4Data3kr2C16 = datak3r2C[128, 128, 8];
Thread[
  test4Data3kr2C16 \[Function] netECA16[Keys@test4Data3kr2C16, {"TopProbabilities", 2}]]
```

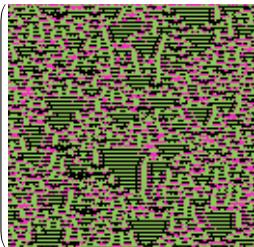


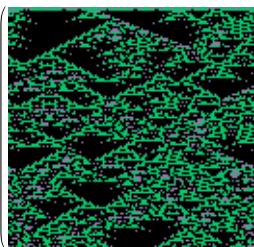


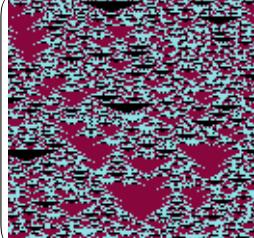
3-colour totalistic, range 3

```
In[④]:= test4Data3kr3C16 = datak3r3C[128, 128, 8];
Thread[
test4Data3kr3C16 → netECA16[Keys@test4Data3kr3C16, {"TopProbabilities", 2}]]
```

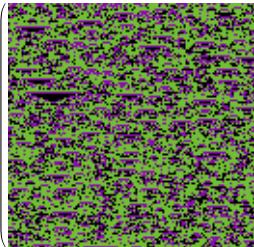
Out[•]= { → 9 694 493} → {3 → 0.480724, 4 → 0.519276},

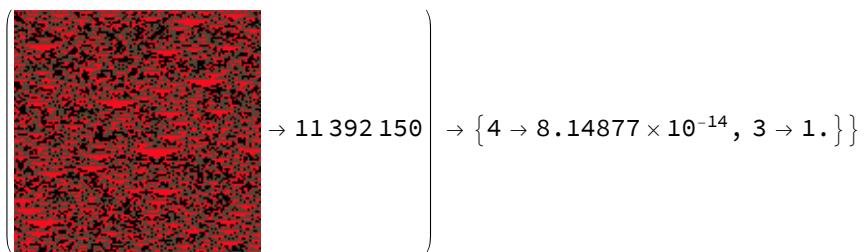
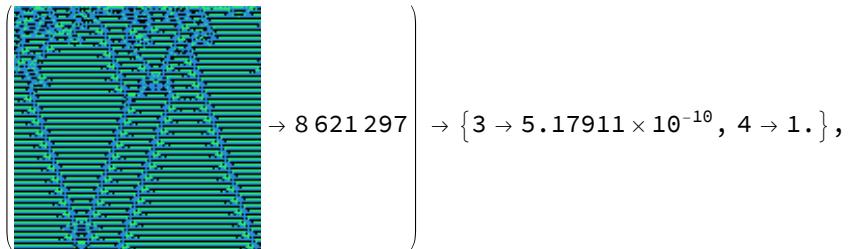
{ → 1 266 350} → {3 → 2.07073 × 10⁻¹⁷, 4 → 1.},

{ → 10 922 251} → {4 → 0.0000302967, 3 → 0.99997},

{ → 10 284 081} → {4 → 0.0000121386, 3 → 0.999988},

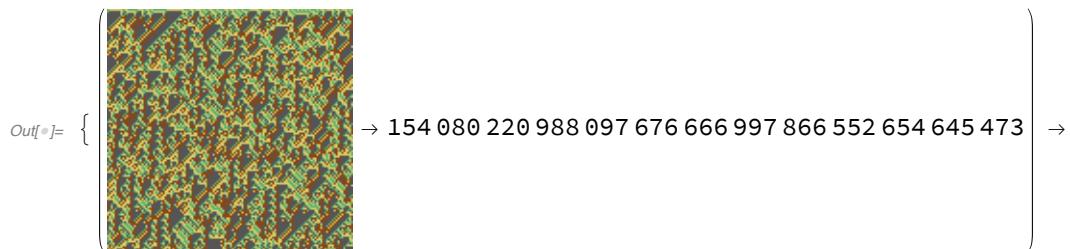
{ → 3 664 255} → {1 → 0.0137727, 2 → 0.986227},

{ → 10 298 881} → {4 → 0.000133186, 3 → 0.999867},

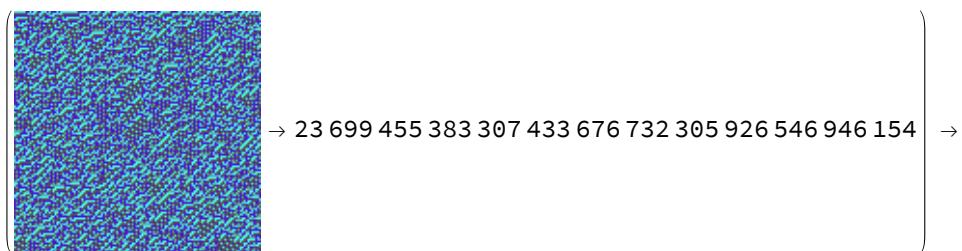


4-colour non-totalistic, range 1

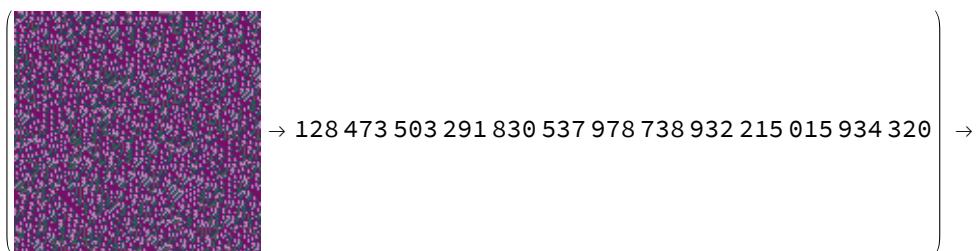
```
In[]:= test4Data4kr1C16 = datak4r1NT[128, 128, 8];
Thread[
  test4Data4kr1C16 → netECA16[Keys@test4Data4kr1C16, {"TopProbabilities", 2}]]
```



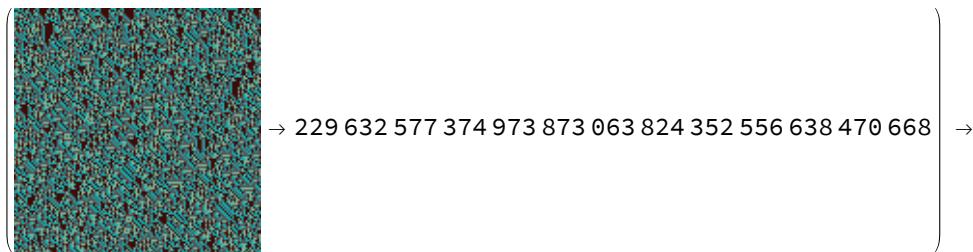
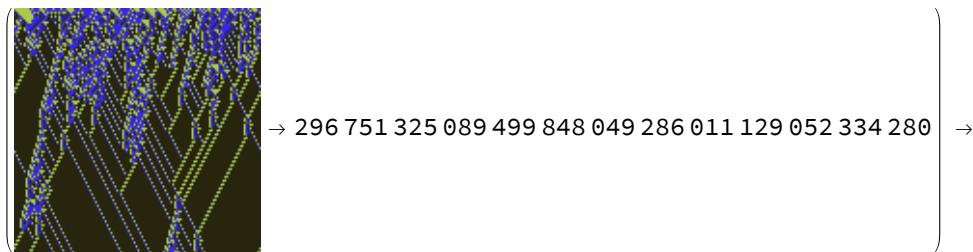
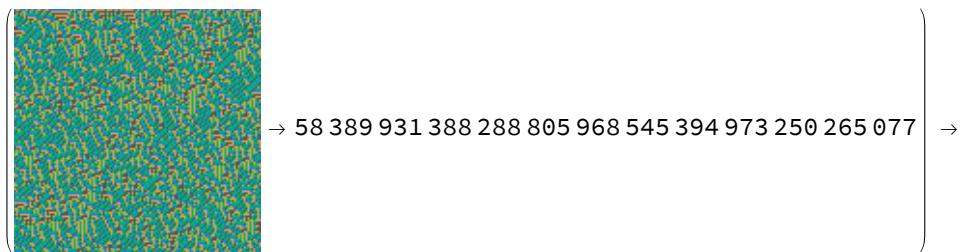
$$\{3 \rightarrow 2.29402 \times 10^{-6}, 4 \rightarrow 0.999998\},$$

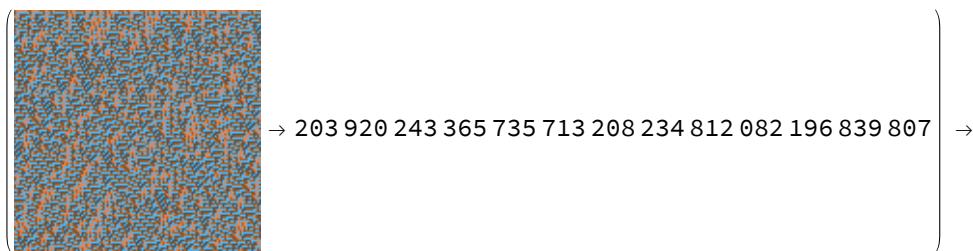


$$\{4 \rightarrow 9.18698 \times 10^{-10}, 3 \rightarrow 1.\},$$



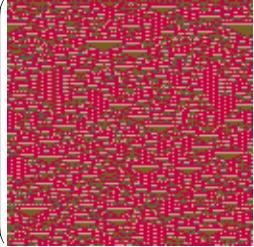
$$\{4 \rightarrow 0.016884, 3 \rightarrow 0.983116\},$$

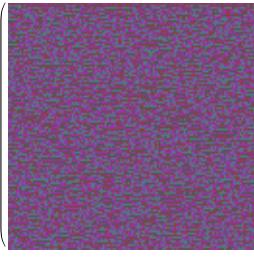

 $\{3 \rightarrow 3.66751 \times 10^{-6}, 4 \rightarrow 0.999996\},$

 $\{2 \rightarrow 0.03566663, 4 \rightarrow 0.964334\},$

 $\{4 \rightarrow 0.392533, 3 \rightarrow 0.607467\},$

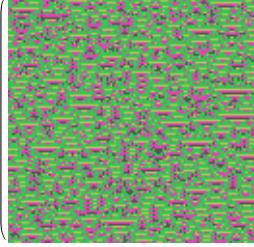
 $\{3 \rightarrow 0.0000369307, 4 \rightarrow 0.999963\},$

 $\{4 \rightarrow 0.00577653, 3 \rightarrow 0.994223\}\}$

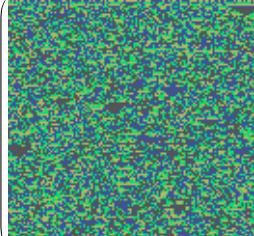
4-colour totalistic, range 2

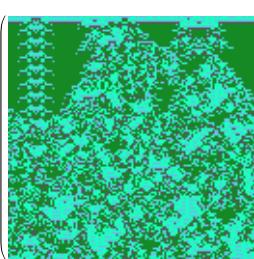
```
In[®]:= test4Data4kr2C16 = datak4r2C[128, 128, 8];
Thread[
  test4Data4kr2C16 → netECA16[Keys@test4Data4kr2C16, {"TopProbabilities", 2}]]
```

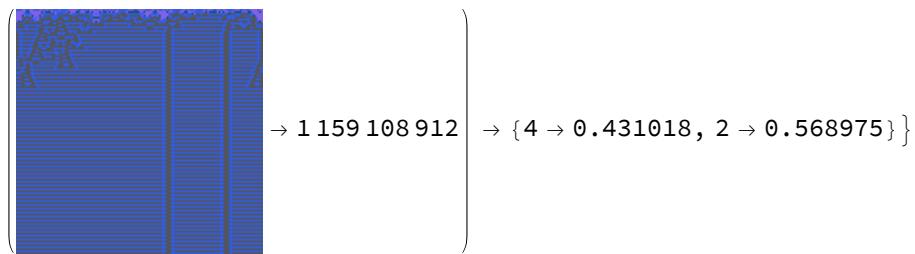
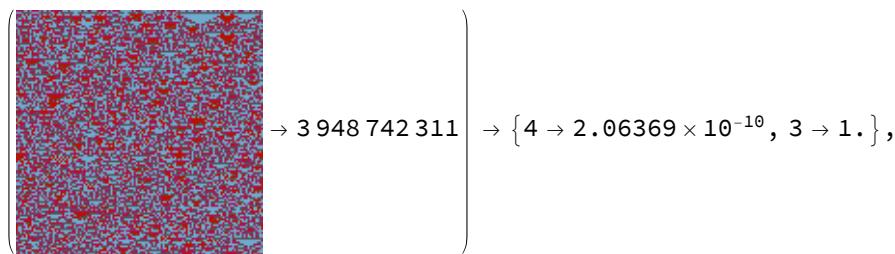
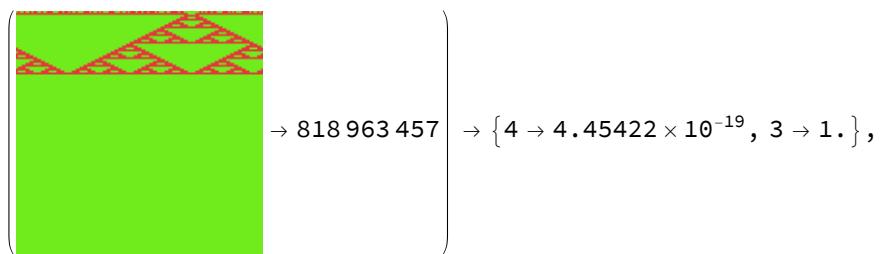
Out[®]= { → 25 517 204} → {4 → 1.29127 × 10⁻¹³, 3 → 1.},

{ → 3 053 925 273} → {4 → 0.00215091, 3 → 0.997849},

{ → 2 735 868 989} → {4 → 0.000282149, 3 → 0.999718},

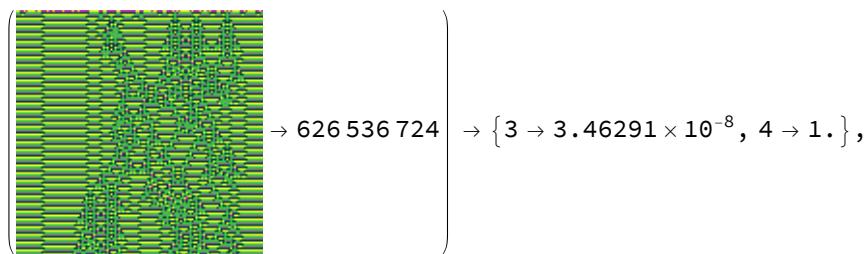
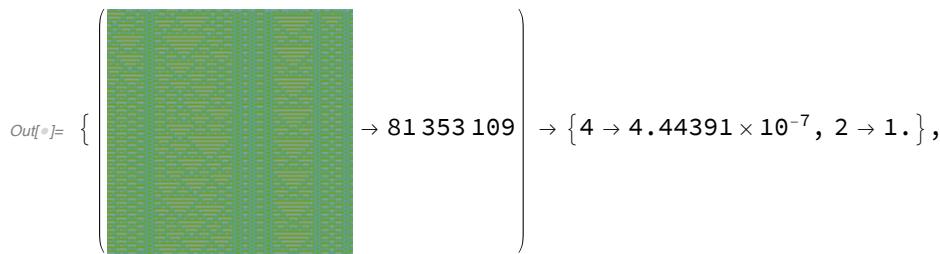
{ → 1 440 927 950} → {4 → 0.0889018, 3 → 0.911098},

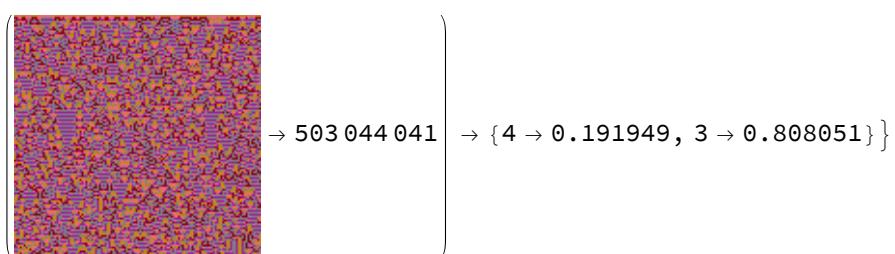
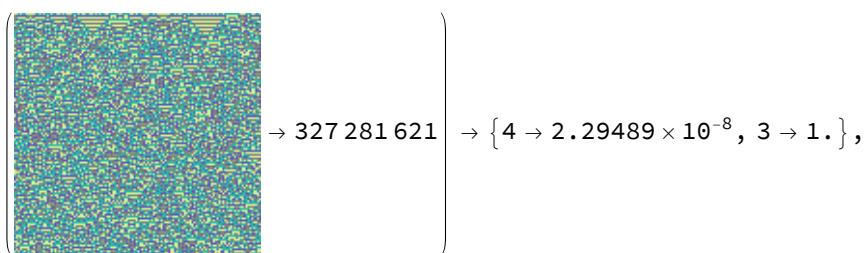
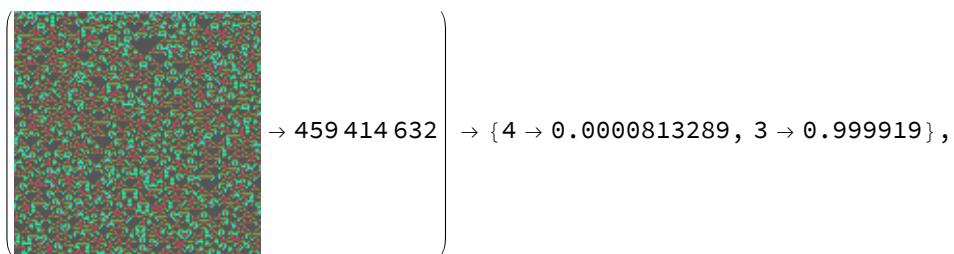
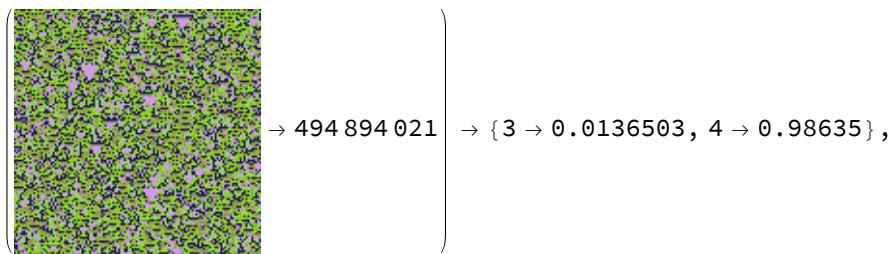
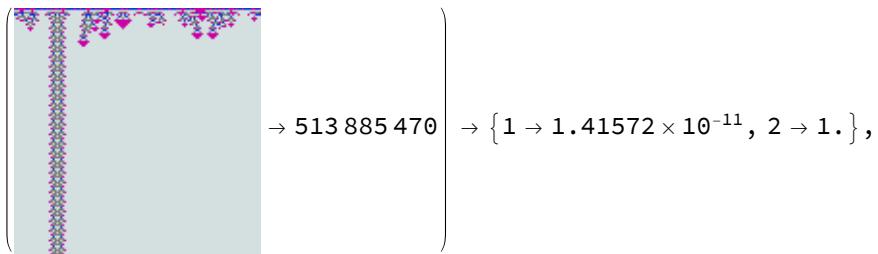
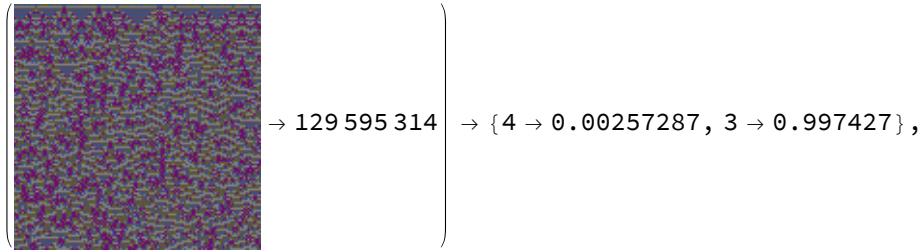
{ → 3 727 816 705} → {3 → 2.78599 × 10⁻⁷, 4 → 1.},



5-colour totalistic, range 1

```
In[8]:= test4Data5kr1C16 = data5T2C[8, 128, 128];
Thread[
  test4Data5kr1C16 → netECA16[Keys@test4Data5kr1C16, {"TopProbabilities", 2}]]
```





6-colour totalistic, range 1

```
In[]:= test4Data6kr1C16 = data6TC[8, 128, 128];
Thread[
  test4Data6kr1C16 → netECA16[Keys@test4Data6kr1C16, {"TopProbabilities", 2}]]
```

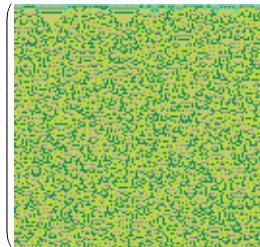
$$\text{Out}[]= \left\{ \begin{array}{l} \text{(A 128x128 grid of random colors)} \\ \rightarrow 1522715109251 \end{array} \right\} \rightarrow \{4 \rightarrow 2.02852 \times 10^{-8}, 3 \rightarrow 1.\},$$

$$\left\{ \begin{array}{l} \text{(A 128x128 grid of random colors)} \\ \rightarrow 1026953898330 \end{array} \right\} \rightarrow \{4 \rightarrow 2.88279 \times 10^{-8}, 3 \rightarrow 1.\},$$

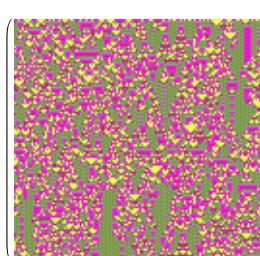
$$\left\{ \begin{array}{l} \text{(A 128x128 grid of random colors)} \\ \rightarrow 1583652682 \end{array} \right\} \rightarrow \{3 \rightarrow 0.429972, 4 \rightarrow 0.570028\},$$

$$\left\{ \begin{array}{l} \text{(A 128x128 grid of random colors)} \\ \rightarrow 2123073201165 \end{array} \right\} \rightarrow \{4 \rightarrow 6.23239 \times 10^{-10}, 3 \rightarrow 1.\},$$

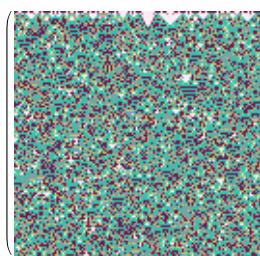
$$\left\{ \begin{array}{l} \text{(A 128x128 grid of random colors)} \\ \rightarrow 341591565791 \end{array} \right\} \rightarrow \{4 \rightarrow 0.00212154, 3 \rightarrow 0.997878\},$$

 $\rightarrow 2\ 568\ 539\ 246\ 083$

$\left. \right\} \rightarrow \{4 \rightarrow 0.00197237, 3 \rightarrow 0.998028\},$

 $\rightarrow 1\ 213\ 730\ 554\ 155$

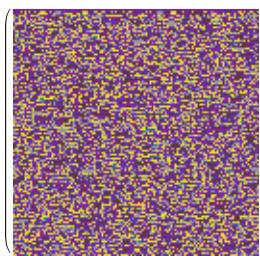
$\left. \right\} \rightarrow \{4 \rightarrow 0.0020281, 3 \rightarrow 0.997972\},$

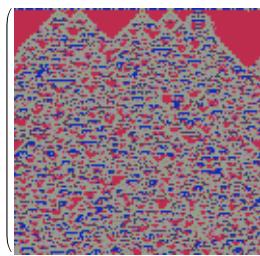
 $\rightarrow 389\ 841\ 312\ 036$

$\left. \right\} \rightarrow \{4 \rightarrow 2.91693 \times 10^{-11}, 3 \rightarrow 1.\}$

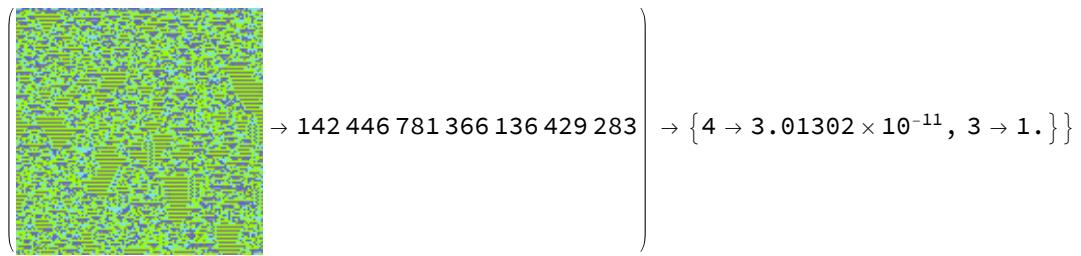
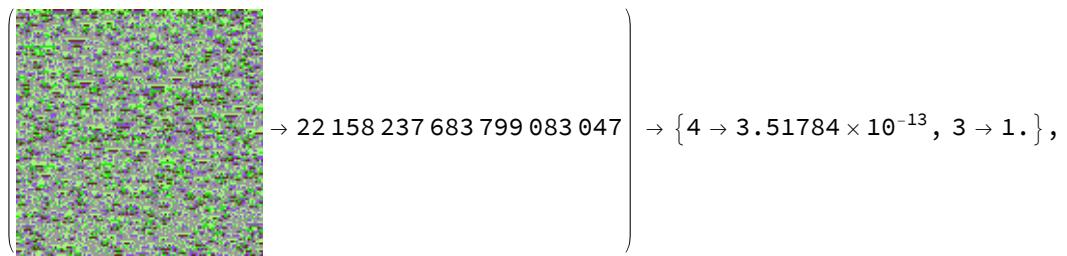
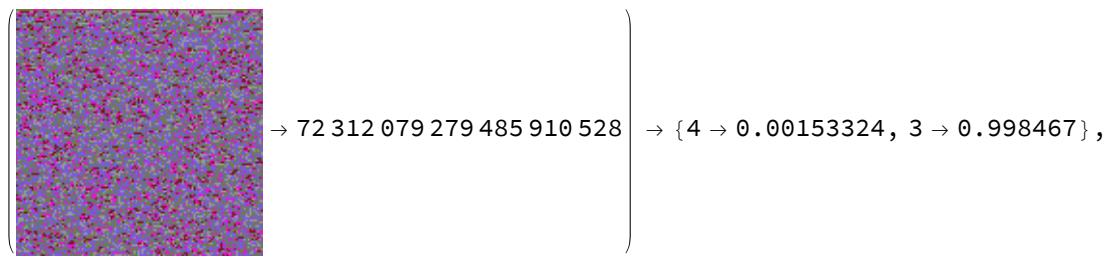
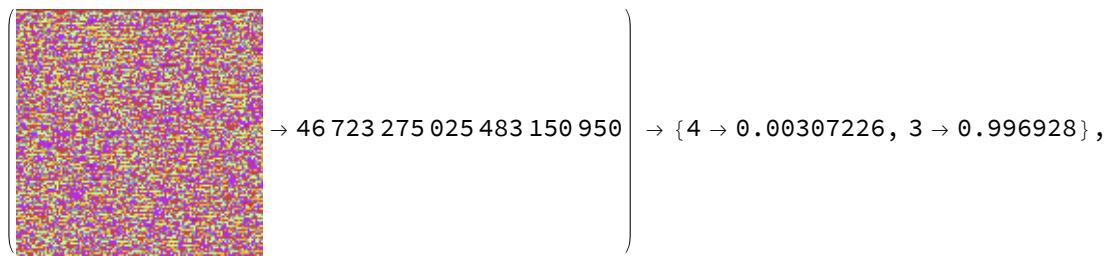
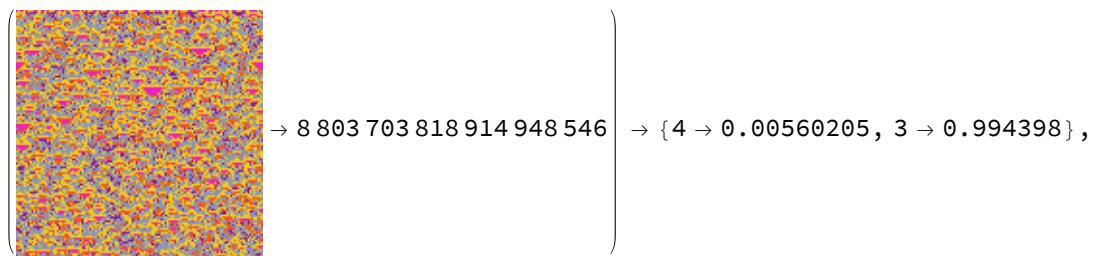
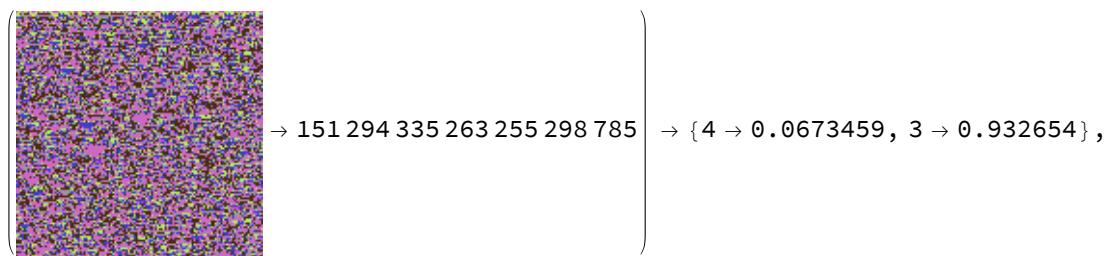
6-colour totalistic, range 2

```
In[8]:= test4Data6kr2C16 = data6T2C[8, 128, 128];
Thread[
  test4Data6kr2C16 \rightarrow netECA16[Keys@test4Data6kr2C16, {"TopProbabilities", 2}]]
```

Out[8]= $\left\{ \begin{array}{l} \text{ } \rightarrow 46\ 177\ 535\ 535\ 728\ 053\ 148 \\ \end{array} \right\} \rightarrow \{4 \rightarrow 6.75757 \times 10^{-8}, 3 \rightarrow 1.\},$

 $\rightarrow 35\ 643\ 164\ 656\ 729\ 746\ 413$

$\left. \right\} \rightarrow \{4 \rightarrow 4.68349 \times 10^{-15}, 3 \rightarrow 1.\},$



7-colour totalistic, range 1

```
In[]:= test4Data7kr1C16 = data7TC[8, 128, 128];
Thread[
test4Data7kr1C16 → netECA16[Keys@test4Data7kr1C16, {"TopProbabilities", 2}]]
```

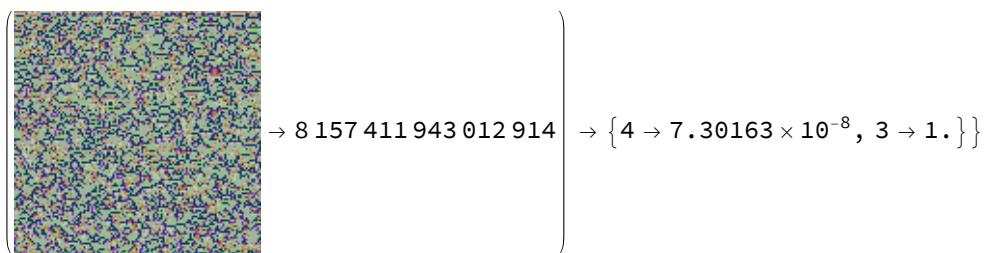
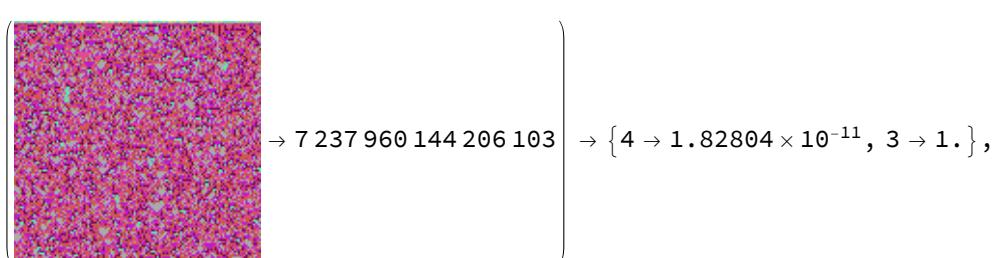
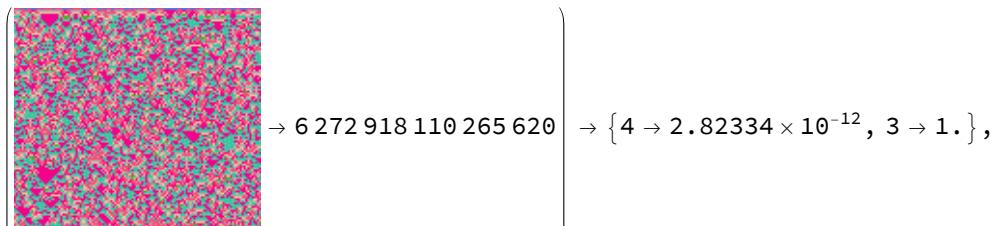
$$\text{Out}[]= \left\{ \begin{array}{l} \text{A 128x128 grid of 7 colors (red, green, blue, cyan, magenta, yellow, black) showing a complex, chaotic pattern.} \\ \rightarrow 3109608593887262 \end{array} \right\} \rightarrow \{2 \rightarrow 0.0267983, 4 \rightarrow 0.973202\},$$

$$\left\{ \begin{array}{l} \text{A 128x128 grid of 7 colors showing a more uniform, noisy pattern.} \\ \rightarrow 10516337788191339 \end{array} \right\} \rightarrow \{4 \rightarrow 0.202783, 3 \rightarrow 0.797217\},$$

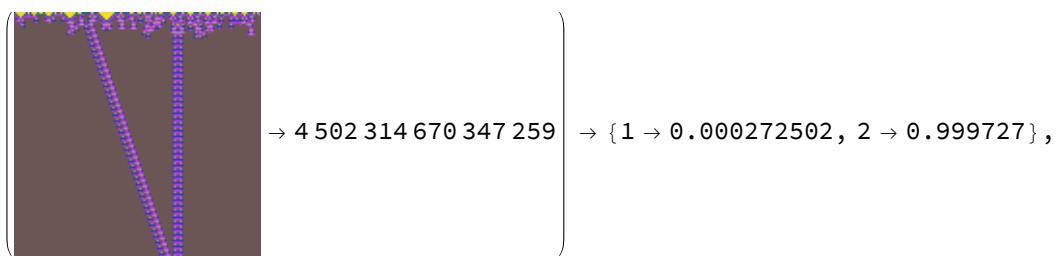
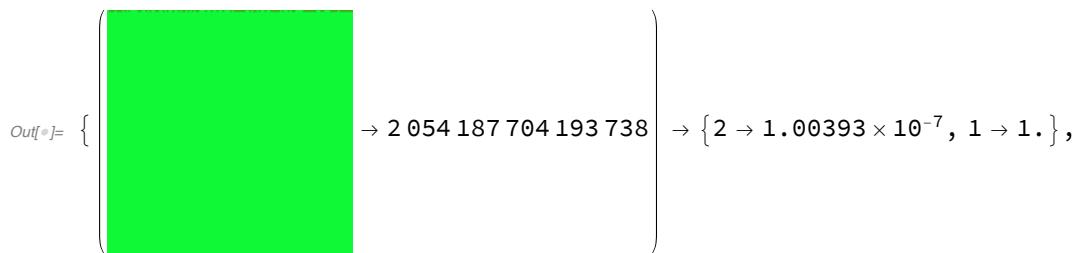
$$\left\{ \begin{array}{l} \text{A 128x128 grid of 7 colors showing a sparse, scattered pattern.} \\ \rightarrow 10218434972470056 \end{array} \right\} \rightarrow \{4 \rightarrow 2.59313 \times 10^{-9}, 3 \rightarrow 1.\},$$

$$\left\{ \begin{array}{l} \text{A 128x128 grid of 7 colors showing a sparse, scattered pattern.} \\ \rightarrow 11301098979433534 \end{array} \right\} \rightarrow \{4 \rightarrow 5.31247 \times 10^{-20}, 3 \rightarrow 1.\},$$

$$\left\{ \begin{array}{l} \text{A 128x128 grid of 7 colors showing a sparse, scattered pattern.} \\ \rightarrow 4222218586098008 \end{array} \right\} \rightarrow \{4 \rightarrow 2.3505 \times 10^{-8}, 3 \rightarrow 1.\},$$



```
In[8]:= test4Data7kr1C16 = data7TC[8, 128, 128];
Thread[
  test4Data7kr1C16 → netECA16[Keys@test4Data7kr1C16, {"TopProbabilities", 2}]]
```



$$\left(\begin{array}{c} \text{[A 2x2 grid of random colors]} \\ \rightarrow 6\ 433\ 286\ 718\ 439\ 853 \end{array} \right) \rightarrow \left\{ 4 \rightarrow 3.57308 \times 10^{-13}, 3 \rightarrow 1. \right\},$$

$$\left(\begin{array}{c} \text{[A 2x2 grid of random colors]} \\ \rightarrow 10\ 115\ 271\ 094\ 201\ 812 \end{array} \right) \rightarrow \left\{ 4 \rightarrow 1.83956 \times 10^{-14}, 3 \rightarrow 1. \right\},$$

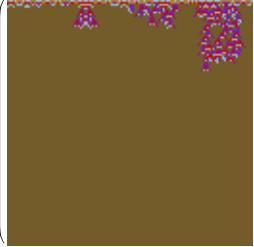
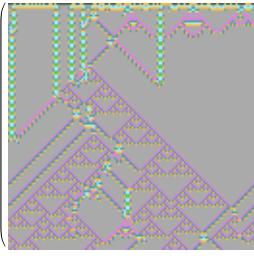
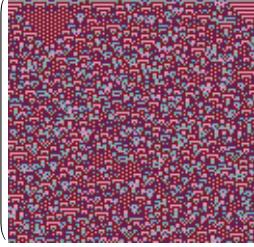
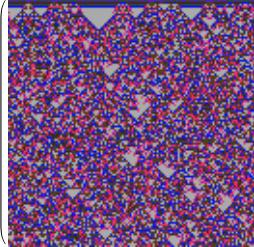
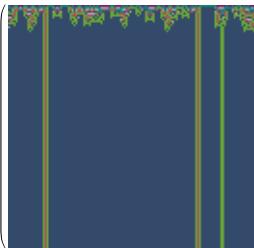
$$\left(\begin{array}{c} \text{[A 2x2 grid of random colors]} \\ \rightarrow 2\ 056\ 629\ 839\ 849\ 700 \end{array} \right) \rightarrow \left\{ 4 \rightarrow 7.03567 \times 10^{-6}, 2 \rightarrow 0.999993 \right\},$$

$$\left(\begin{array}{c} \text{[A 2x2 grid of random colors]} \\ \rightarrow 6\ 016\ 684\ 767\ 156\ 829 \end{array} \right) \rightarrow \left\{ 4 \rightarrow 0.0021258, 3 \rightarrow 0.997874 \right\},$$

$$\left(\begin{array}{c} \text{[A 2x2 grid of random colors]} \\ \rightarrow 1\ 150\ 898\ 749\ 617\ 983 \end{array} \right) \rightarrow \left\{ 4 \rightarrow 5.05985 \times 10^{-9}, 3 \rightarrow 1. \right\},$$

$$\left(\begin{array}{c} \text{[A 2x2 grid of random colors]} \\ \rightarrow 3\ 441\ 885\ 208\ 643\ 463 \end{array} \right) \rightarrow \left\{ 3 \rightarrow 1.57168 \times 10^{-8}, 2 \rightarrow 1. \right\}$$

```
In[8]:= test4Data7kr1C16 = data7TC[8, 128, 128];
Thread[
  test4Data7kr1C16 → netECA16[Keys@test4Data7kr1C16, {"TopProbabilities", 2}]]
```

Out[8]= { → 8 718 538 805 570 808,  → 5 687 458 247 703 346,  → 2 004 300 484 518 722,  → 2 106 485 862 858 275,  → 10 335 102 717 390 268} → {4 → 0.0199047, 2 → 0.980095}, {3 → 3.931 × 10⁻⁶, 4 → 0.999995}, {3 → 0.0438658, 4 → 0.956134}, {4 → 3.36807 × 10⁻¹⁰, 3 → 1.}, {4 → 1.40275 × 10⁻⁹, 2 → 1.},

$$\left(\begin{array}{c} \text{[A 128x128 grid of random colors]} \\ \rightarrow 1\ 948\ 304\ 137\ 097\ 478 \end{array} \right) \rightarrow \{ 4 \rightarrow 3.0757 \times 10^{-6}, 3 \rightarrow 0.999997 \},$$

$$\left(\begin{array}{c} \text{[A 128x128 grid of random colors]} \\ \rightarrow 742\ 855\ 573\ 082\ 935 \end{array} \right) \rightarrow \{ 3 \rightarrow 0.00423487, 4 \rightarrow 0.995765 \},$$

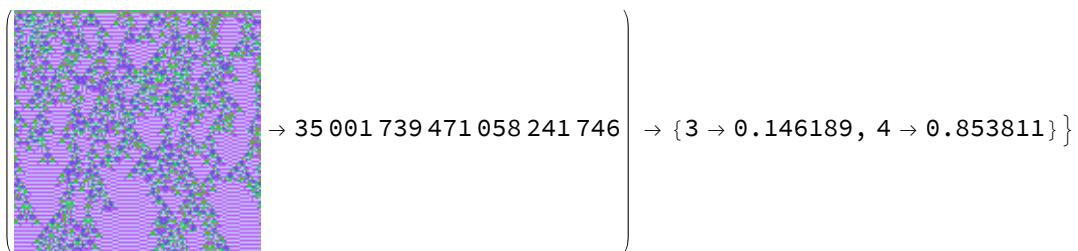
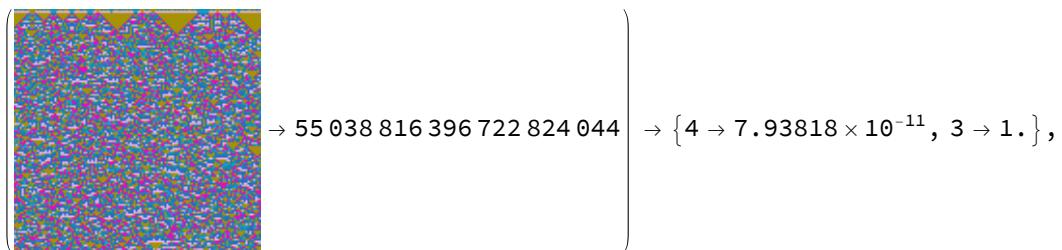
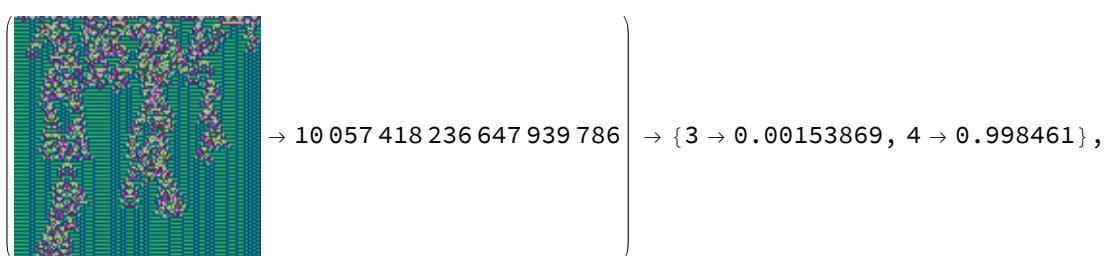
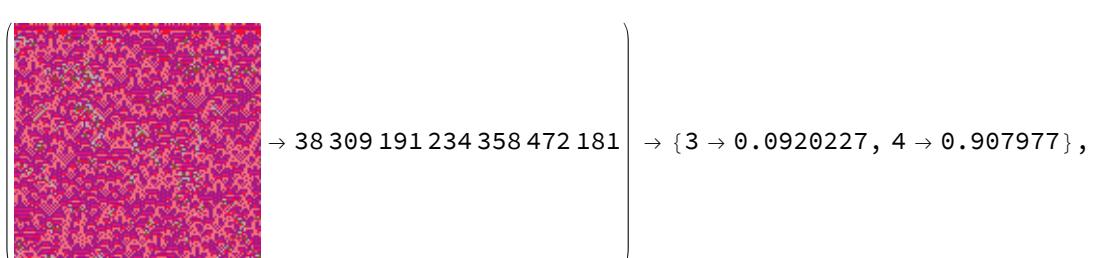
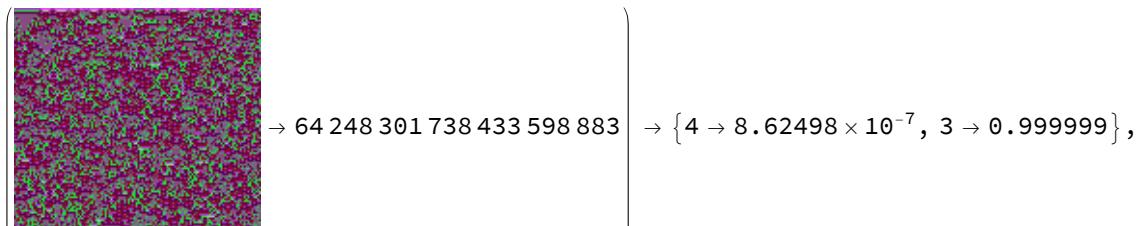
$$\left(\begin{array}{c} \text{[A 128x128 grid of random colors]} \\ \rightarrow 550\ 991\ 988\ 954\ 034 \end{array} \right) \rightarrow \{ 3 \rightarrow 0.0000158322, 4 \rightarrow 0.999984 \}$$

8-colour totalistic, range 1

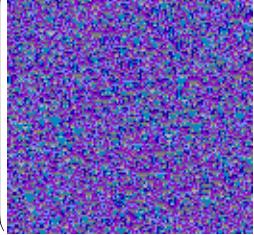
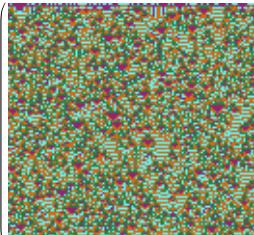
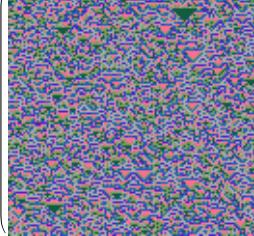
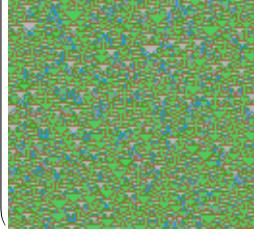
```
In[]:= test4Data8kr1C16 = data8TC[8, 128, 128];
Thread[
  test4Data8kr1C16 → netECA16[Keys@test4Data8kr1C16, {"TopProbabilities", 2}]]
```

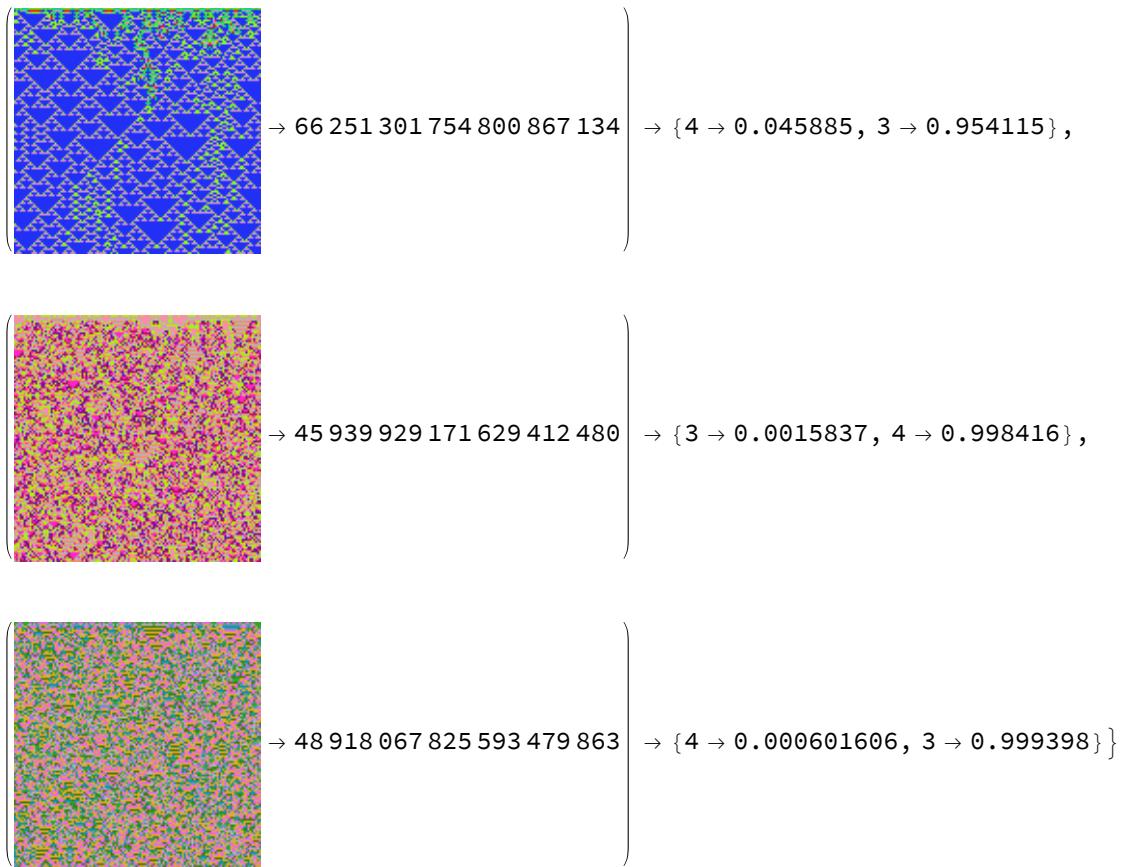
$$\text{Out}[=] = \left\{ \begin{array}{c} \text{[A 128x128 grid of 8-color totalistic CA pattern]} \\ \rightarrow 26\ 660\ 220\ 729\ 300\ 317\ 631 \end{array} \right\} \rightarrow \{ 3 \rightarrow 4.53753 \times 10^{-16}, 4 \rightarrow 1. \},$$

$$\left(\begin{array}{c} \text{[A 128x128 grid of 8-color totalistic CA pattern]} \\ \rightarrow 57\ 706\ 619\ 077\ 455\ 169\ 987 \end{array} \right) \rightarrow \{ 4 \rightarrow 0.00012086, 3 \rightarrow 0.999879 \},$$



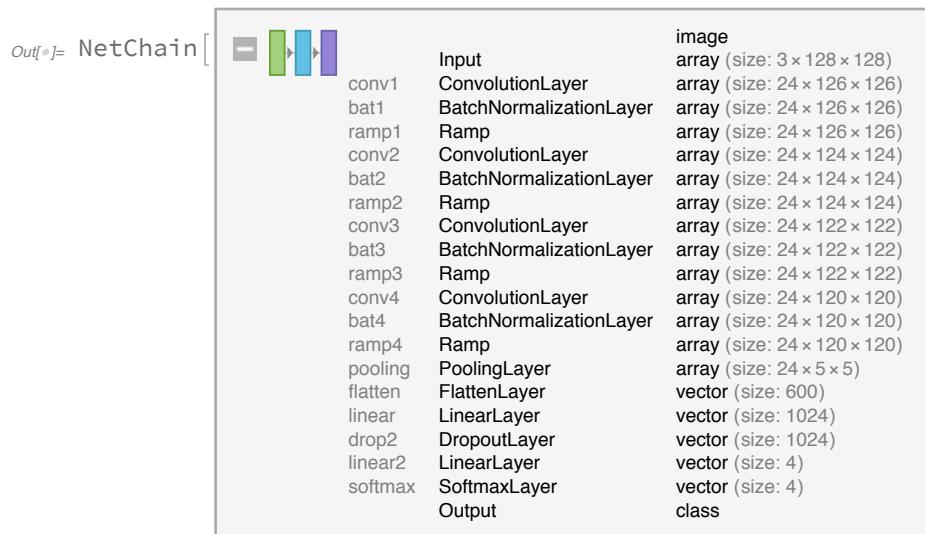
```
In[®]:= test4Data8kr1C16 = data8TC[8, 128, 128];
Thread[
  test4Data8kr1C16 → netECA16[Keys@test4Data8kr1C16, {"TopProbabilities", 2}]]
```

Out[®]= { → 8 889 571 206 431 822 669,  → 12 932 107 158 159 577 869,  → 38 300 014 541 797 689 408,  → 73 619 662 786 582 031 542,  → 25 075 664 454 379 326 631}

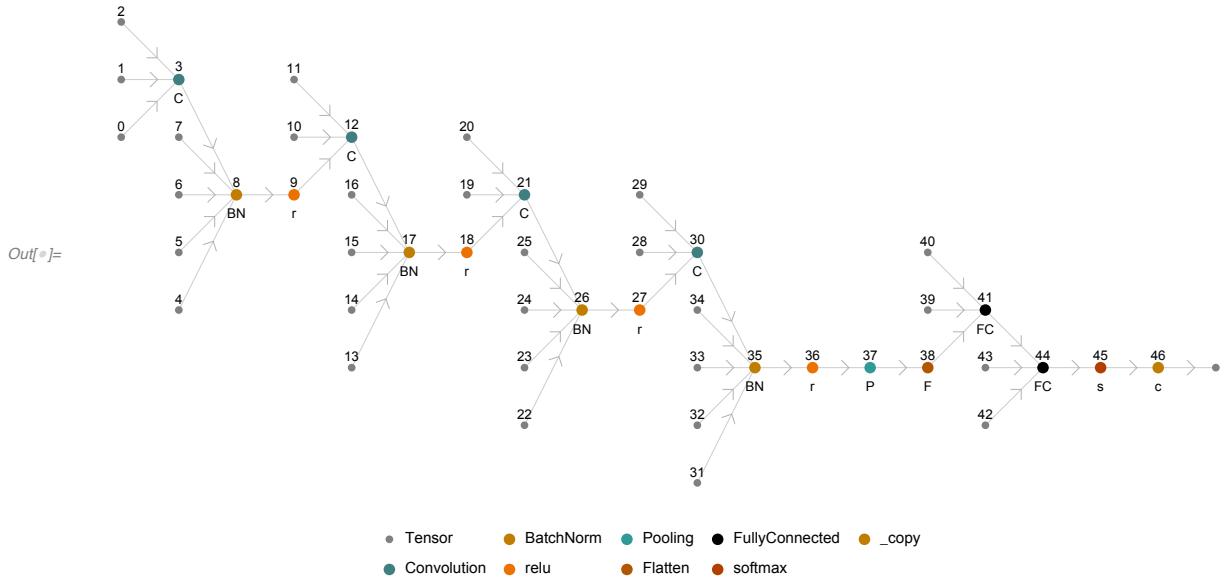


Network XVII - Four convolutions, dropout on linear only, BatchNorm

```
In[6]:= netECA17 = netTenCC1024drop[128, 128]
```



In[8]:= NetInformation[netECA17, "MXNetNodeGraphPlot"]



In[9]:= NetInformation[netECA17, "SummaryGraphic"]



In[10]:= dataECA17 = dataC[128, 128, 16 384];

In[11]:= dataTotalistic2BigC17 = genData2r2C[128, 128, 2048];

In[12]:= dataTotalistic3BigC17 = data3T2C[128, 128, 2048];

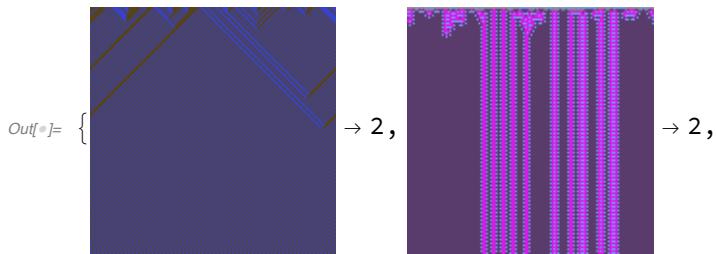
In[13]:= dataTotalistic4BigC17 = data4TC[128, 128, 2048];

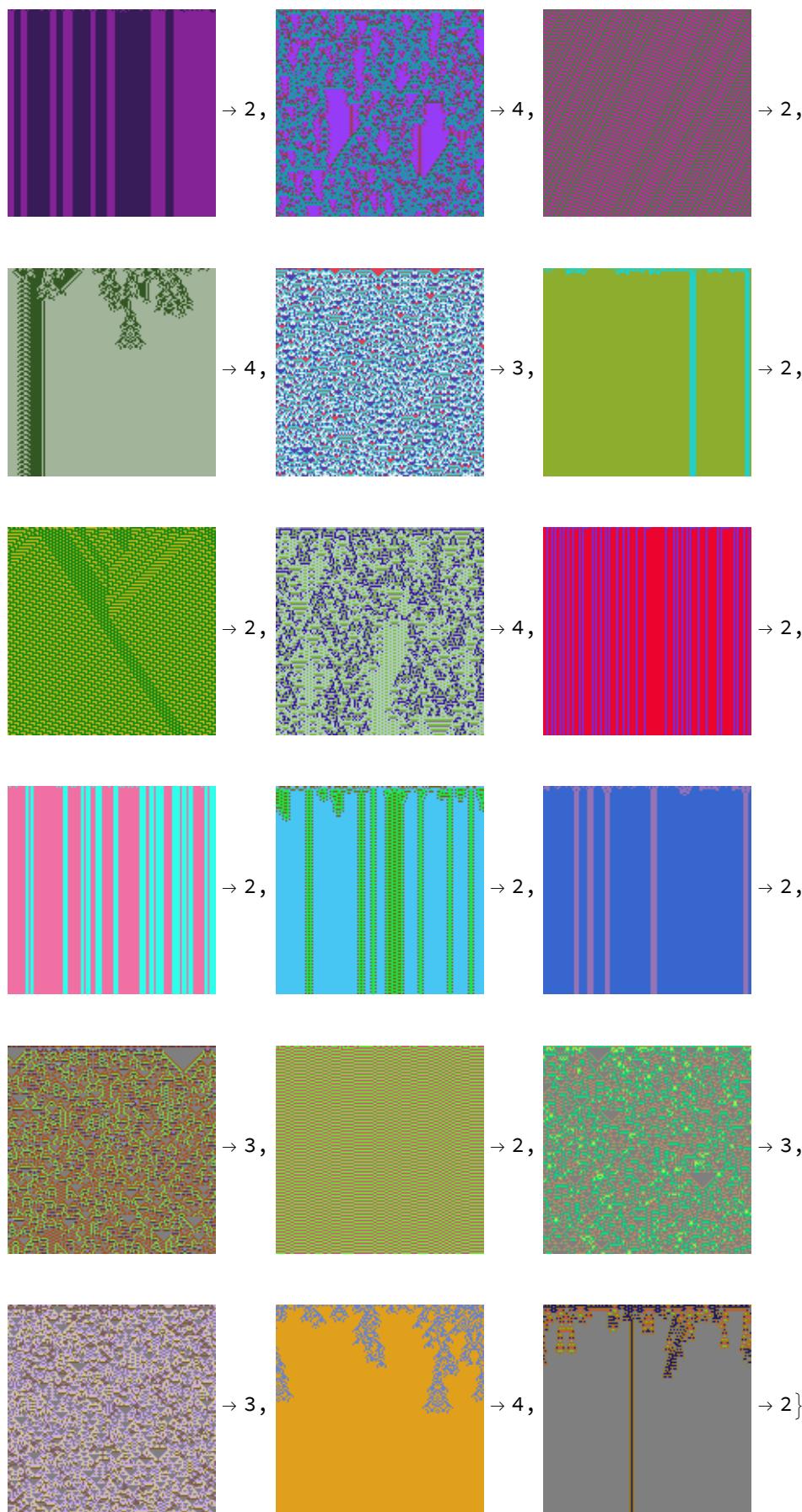
In[14]:= dataTotalistic5BigC17 = genData5TCC[128, 128, 8192];

In[15]:= fullTrainingBigC17 = Join[dataECA17, dataTotalistic2BigC17,
dataTotalistic3BigC17, dataTotalistic4BigC17, dataTotalistic5BigC17];
Length[fullTrainingBigC17]

Out[15]= 53 248

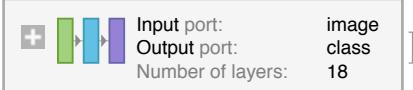
In[16]:= RandomSample[fullTrainingBigC17, 20]





```
In[®]:= dir = SetDirectory[NotebookDirectory[]]
In[®]:= "/home/esilverman/Documents"
Out[®]= /home/esilverman/Documents

In[®]:= netECA17 = NetTrain[netECA17, fullTrainingBigC17,
  MaxTrainingRounds → 200, BatchSize → 256, TargetDevice → "GPU",
  TrainingProgressCheckpointing → {"Directory", dir}]
```

Out[®]= NetChain[]

Input port: Output port: Number of layers:

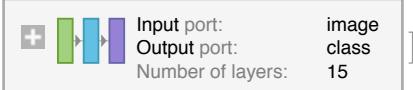
image class 18

```
netECA17 = Import["netECA17-r200.wlnet"]
```

Generate test data for Network XVII (200 epochs)

```
In[®]:= dir = SetDirectory[NotebookDirectory[]]
Out[®]= /Users/thorsilver/Downloads/Wolfram notebooks
```

```
netECA17 = Import["netECA17-r200.wlnet"]
```

Out[®]= NetChain[]

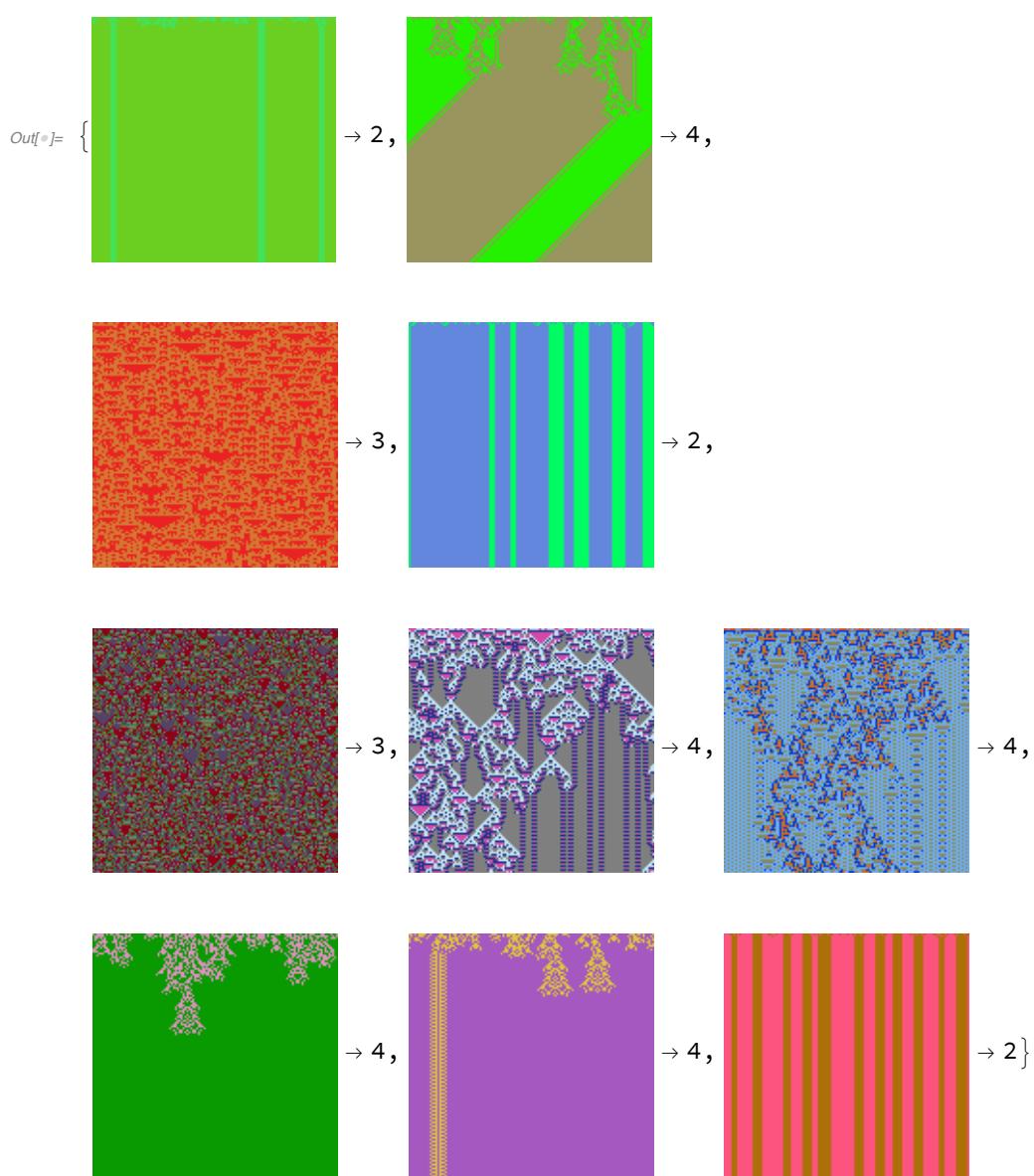
Input port: Output port: Number of layers:

image class 15

```
In[®]:= testDataECABigC = dataC[128, 128, 1024];
testData2TBigC = genData2r2C[128, 128, 1024];
testData3TBigC = data3T2C[128, 128, 1024];
testData4TBigC = data4TC[128, 128, 1024];
testData5TBigC = genData5TCC[128, 128, 1024];
fullTestSetBigC = Join[testDataECABigC,
  testData2TBigC, testData3TBigC, testData4TBigC, testData5TBigC];
Length[fullTestSetBigC]
```

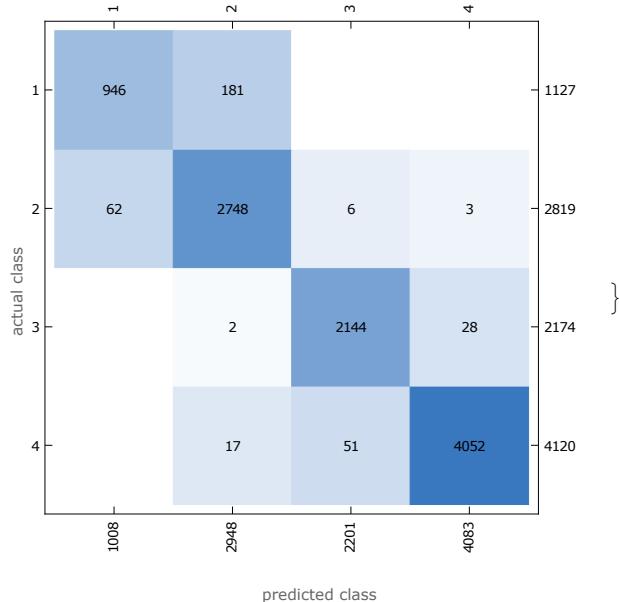
Out[®]= 10 240

```
In[]:= RandomSample[fullTestSetBigC, 10]
```

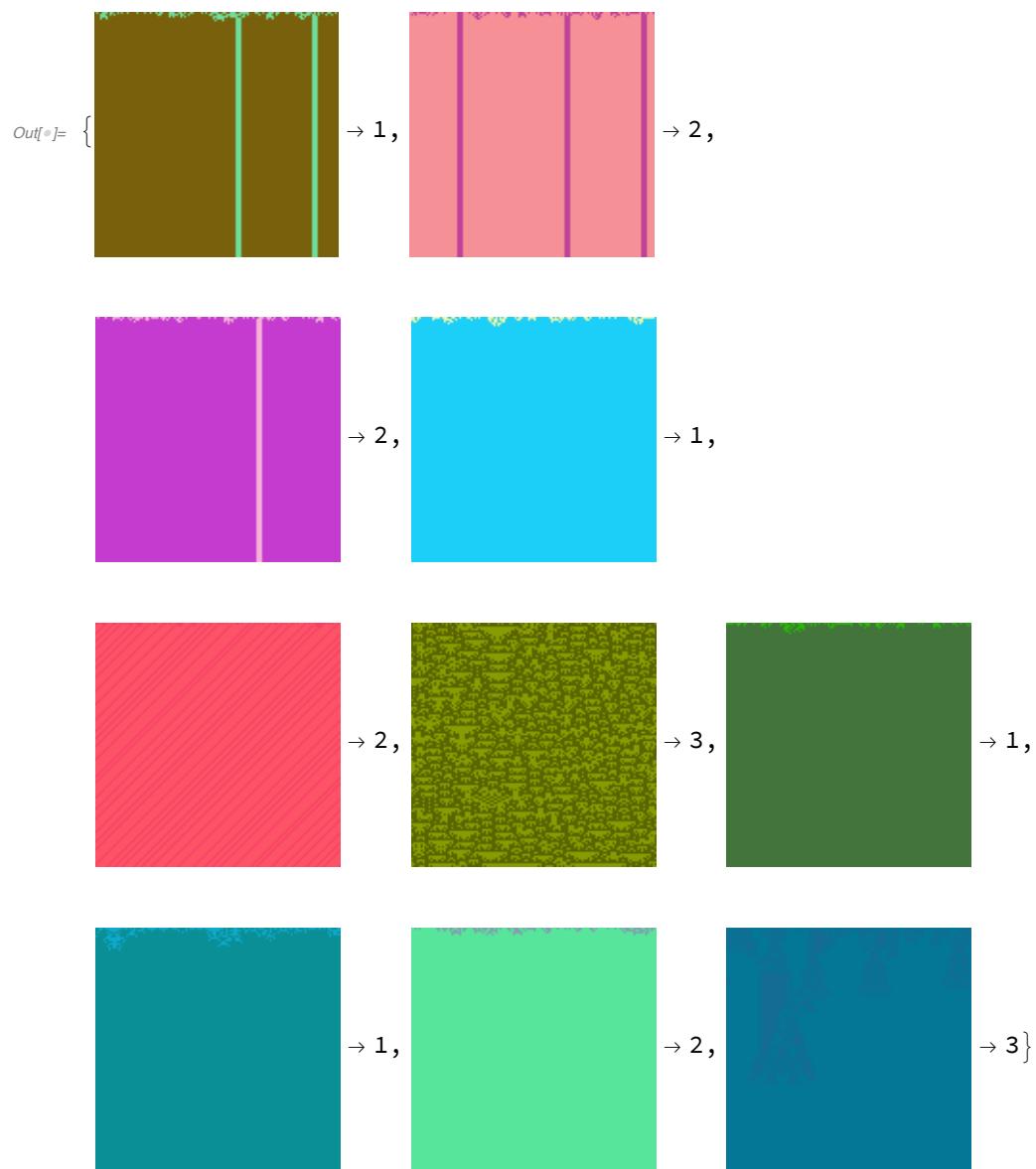


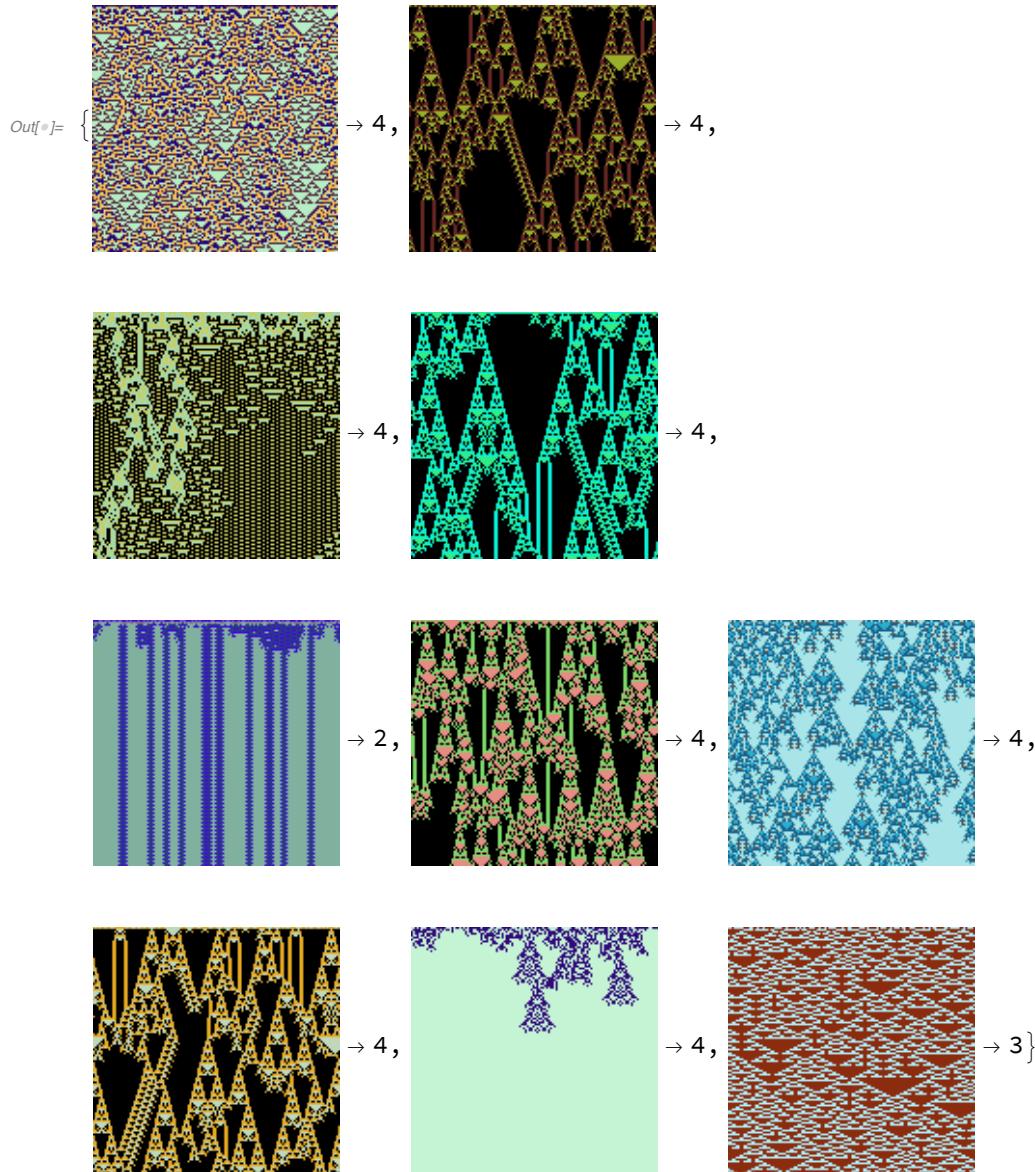
```
In[®]:= NetMeasurements[netECA17, fullTestSetBigC,
 {"Accuracy", "Precision", "ConfusionMatrixPlot"}]

Out[®]= {0.96582, {1 → 0.938492, 2 → 0.932157, 3 → 0.974103, 4 → 0.992408}, }
```



```
In[®]:= entropyImagesBigC = RandomSample[Keys[fullTestSetBigC], 500];
entropiesBigC = netECA17[entropyImagesBigC, "Entropy"];
highEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, -10]]];
lowEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, 10]]];
Thread[highEntBigC → netECA17[highEntBigC]]
Thread[lowEntBigC → netECA17[lowEntBigC]]
```





Testing Network XVII (200 epochs) on unseen CA rule spaces

2-colour non-totalistic, range 2

```
In[•]:= test4Data2kr2C17 = datak2r2C[128, 128, 8];
Thread[
  test4Data2kr2C17 → netECA17[Keys@test4Data2kr2C17, {"TopProbabilities", 2}]]
```

Out[•]:= {

→ 3 594 886 935 → {3 → 1.19587 × 10⁻⁷, 2 → 1.},

$$\left(\begin{array}{c} \text{[A 4x4 grid of yellow pixels]} \\ \rightarrow 4\ 012\ 014\ 789 \end{array} \right) \rightarrow \{ 4 \rightarrow 0.00317589, 3 \rightarrow 0.996824 \},$$

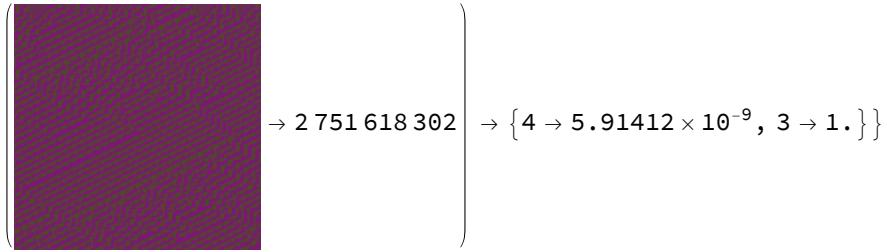
$$\left(\begin{array}{c} \text{[A 4x4 grid of red/pink pixels]} \\ \rightarrow 736\ 342\ 145 \end{array} \right) \rightarrow \{ 4 \rightarrow 0.000138652, 3 \rightarrow 0.999861 \},$$

$$\left(\begin{array}{c} \text{[A 4x4 grid of vertical blue and yellow bars]} \\ \rightarrow 3\ 597\ 938\ 931 \end{array} \right) \rightarrow \{ 4 \rightarrow 5.42024 \times 10^{-16}, 2 \rightarrow 1. \},$$

$$\left(\begin{array}{c} \text{[A 4x4 grid of horizontal blue and black bars]} \\ \rightarrow 49\ 406\ 137 \end{array} \right) \rightarrow \{ 1 \rightarrow 4.03179 \times 10^{-30}, 2 \rightarrow 1. \},$$

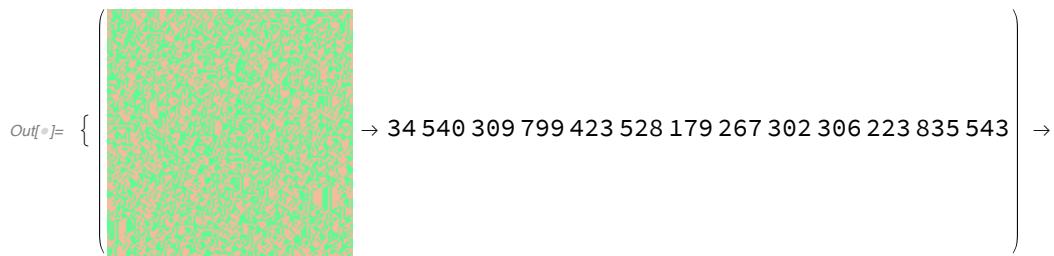
$$\left(\begin{array}{c} \text{[A 4x4 grid of green pixels with diagonal patterns]} \\ \rightarrow 669\ 500\ 034 \end{array} \right) \rightarrow \{ 4 \rightarrow 0.0129747, 2 \rightarrow 0.983657 \},$$

$$\left(\begin{array}{c} \text{[A 4x4 grid of cyan pixels with vertical patterns]} \\ \rightarrow 4\ 122\ 605\ 661 \end{array} \right) \rightarrow \{ 1 \rightarrow 6.18382 \times 10^{-9}, 2 \rightarrow 1. \},$$

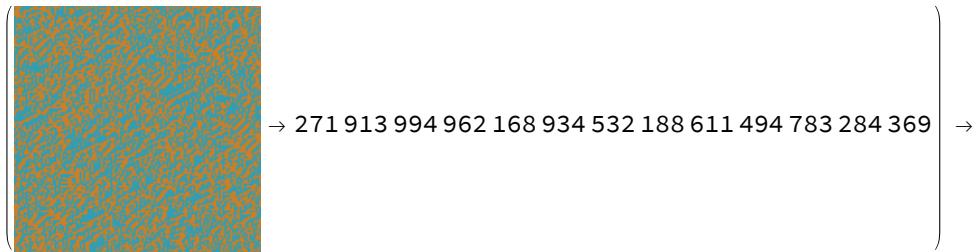


2-colour non-totalistic, range 3

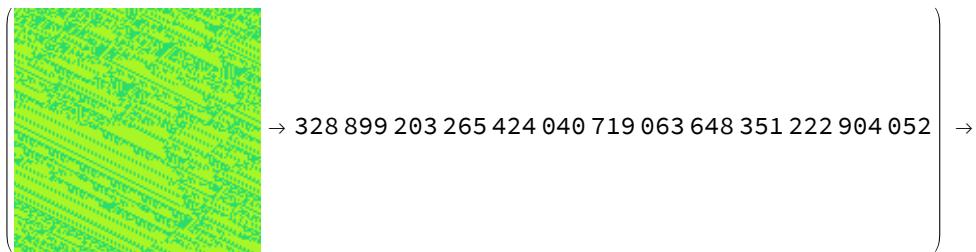
```
In[6]:= test4Data2kr3C17 = datak2r3NT[128, 128, 8];
Thread[
test4Data2kr3C17 → netECA17[Keys@test4Data2kr3C17, {"TopProbabilities", 2}]]
```



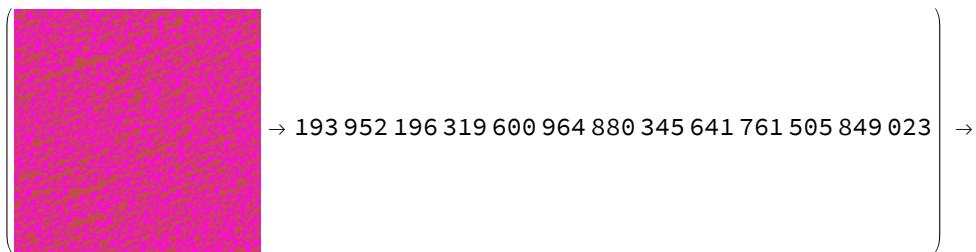
{4 → 0.0000190167, 3 → 0.999981},



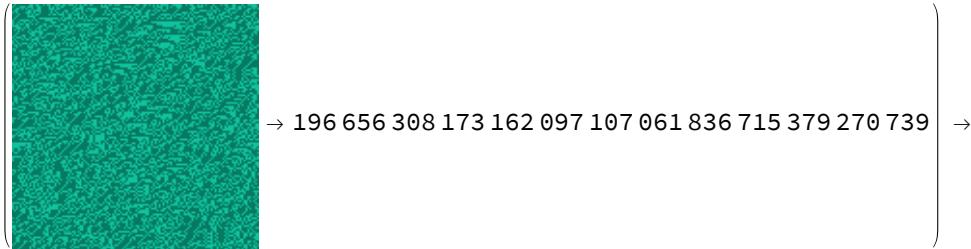
{4 → 8.79258 × 10⁻¹⁵, 3 → 1.},



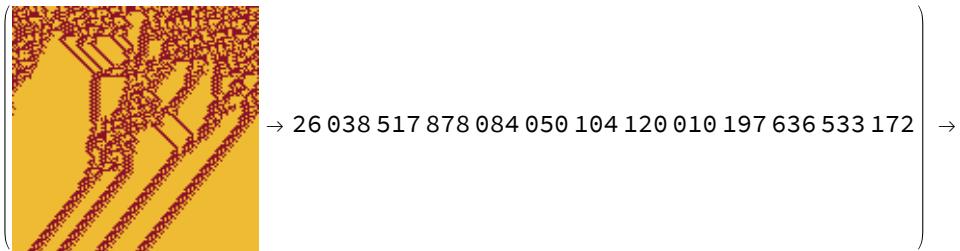
{3 → 0.000609094, 4 → 0.999391},



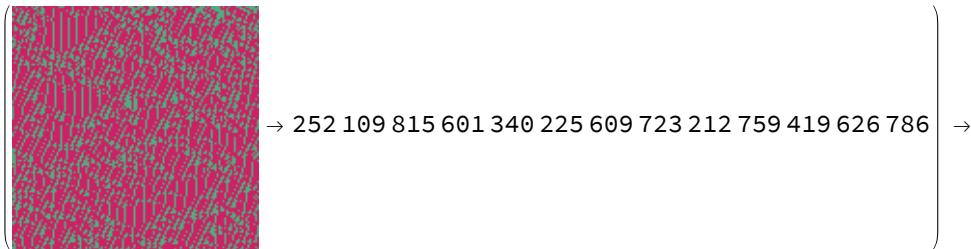
$\{4 \rightarrow 8.96571 \times 10^{-10}, 3 \rightarrow 1.\}$,



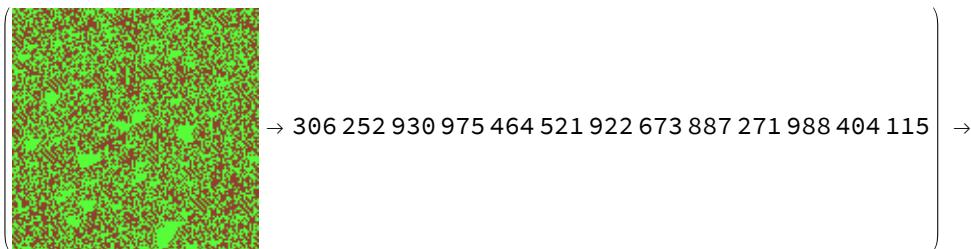
$\{4 \rightarrow 3.36397 \times 10^{-6}, 3 \rightarrow 0.999997\}$,



$\{3 \rightarrow 5.4757 \times 10^{-7}, 4 \rightarrow 0.999999\}$,



$\{4 \rightarrow 1.35911 \times 10^{-8}, 3 \rightarrow 1.\}$,



$\{4 \rightarrow 5.68649 \times 10^{-7}, 3 \rightarrow 0.999999\}\}$

3-colour non-totalistic, range 1

```
In[6]:= test4Data3kr1C17 = datak3r1NT[128, 128, 8];
Thread[
test4Data3kr1C17 → netECA17[Keys@test4Data3kr1C17, {"TopProbabilities", 2}]]
```

$$Out[\textcolor{brown}{\#}]= \left\{ \begin{array}{c} \text{Image} \\ \rightarrow 1924646489567 \end{array} \right\} \rightarrow \{3 \rightarrow 1.76606 \times 10^{-30}, 2 \rightarrow 1.\},$$

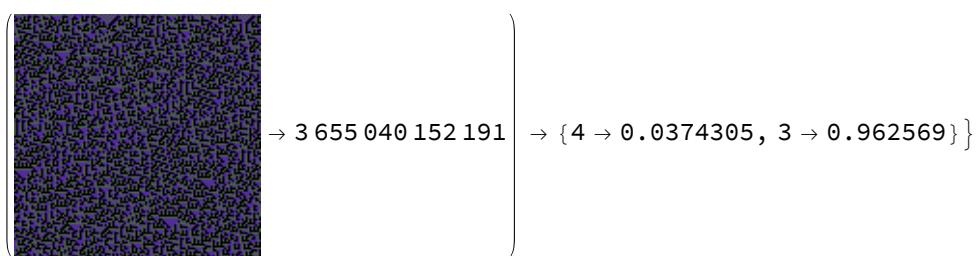
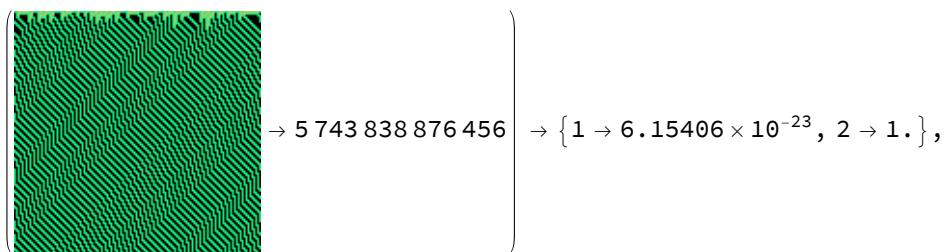
$$\left\{ \begin{array}{c} \text{Image} \\ \rightarrow 3672534501071 \end{array} \right\} \rightarrow \{2 \rightarrow 0.0000110699, 4 \rightarrow 0.999989\},$$

$$\left\{ \begin{array}{c} \text{Image} \\ \rightarrow 5833330297781 \end{array} \right\} \rightarrow \{2 \rightarrow 0.000232935, 4 \rightarrow 0.999767\},$$

$$\left\{ \begin{array}{c} \text{Image} \\ \rightarrow 7606192973798 \end{array} \right\} \rightarrow \{2 \rightarrow 6.802 \times 10^{-10}, 1 \rightarrow 1.\},$$

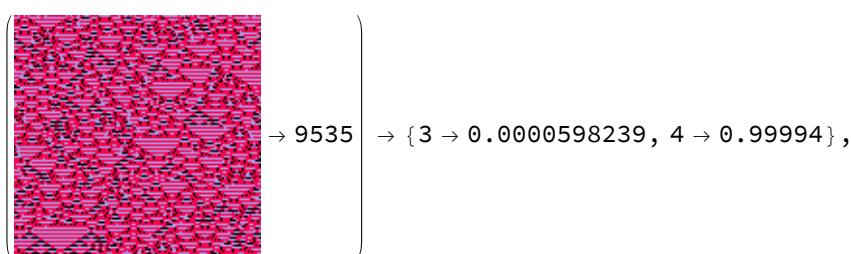
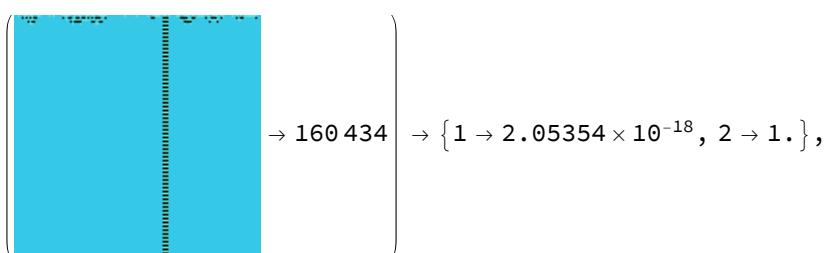
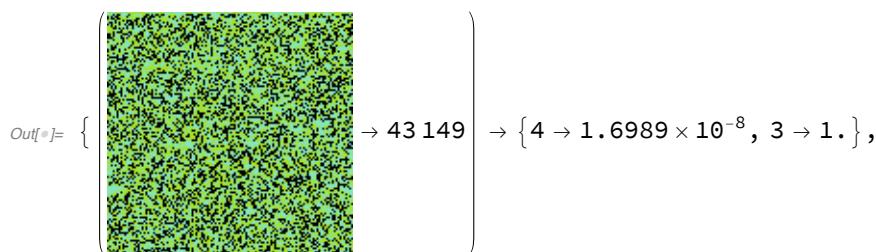
$$\left\{ \begin{array}{c} \text{Image} \\ \rightarrow 7622301560954 \end{array} \right\} \rightarrow \{3 \rightarrow 0.0391643, 2 \rightarrow 0.960836\},$$

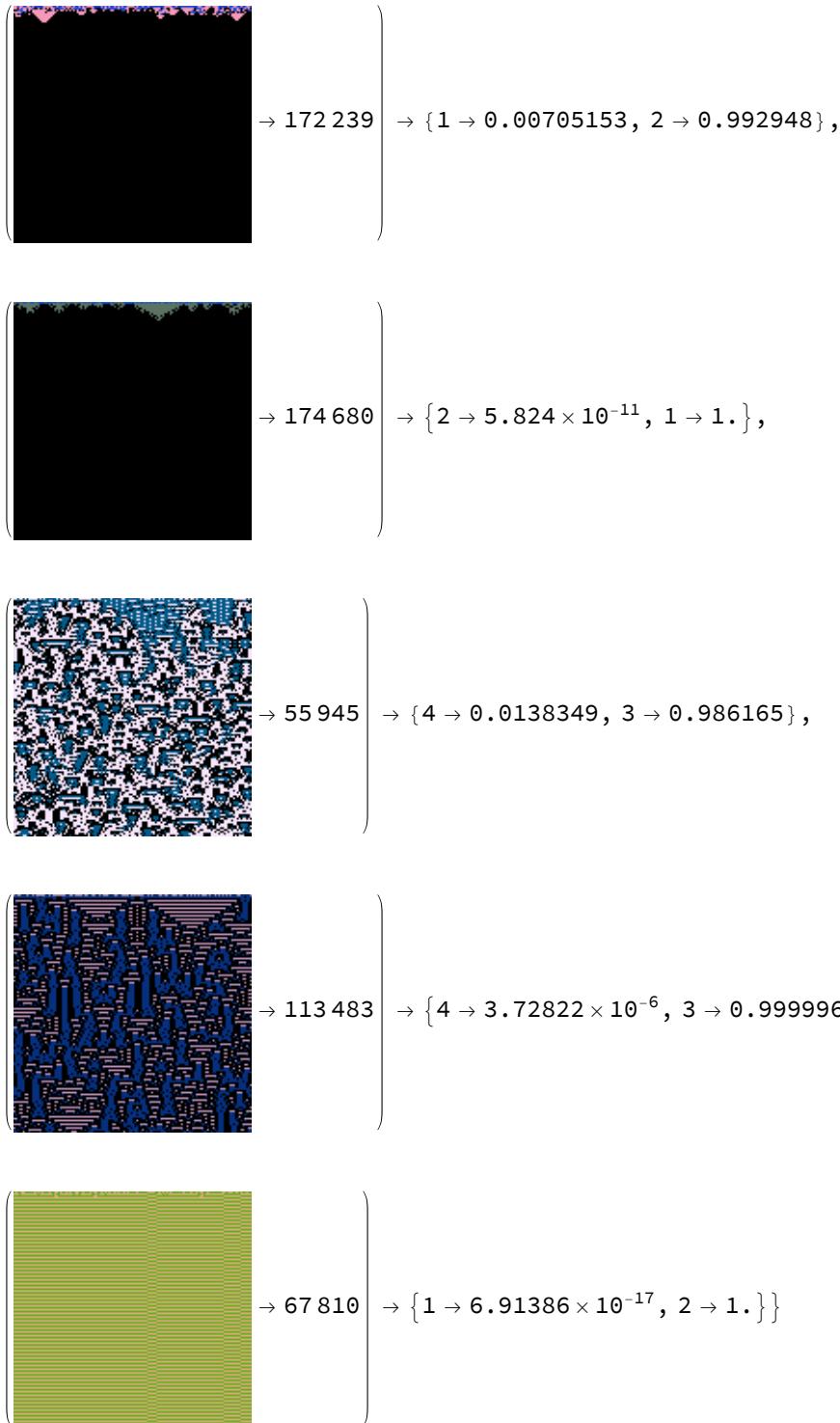
$$\left\{ \begin{array}{c} \text{Image} \\ \rightarrow 3685910174297 \end{array} \right\} \rightarrow \{3 \rightarrow 2.7602 \times 10^{-8}, 4 \rightarrow 1.\},$$



3-colour totalistic, range 2

```
In[]:= test4Data3kr2C17 = datak3r2C[128, 128, 8];
Thread[
  test4Data3kr2C17 \[Rightarrow] netECA17[Keys@test4Data3kr2C17, {"TopProbabilities", 2}]]
```





3-colour totalistic, range 3

```

In[④]:= test4Data3kr3C17 = datak3r3C[128, 128, 8];
Thread[
test4Data3kr3C17 → netECA17[Keys@test4Data3kr3C17, {"TopProbabilities", 2}]]
```

Out[1]= $\left\{ \begin{array}{l} \text{A green noisy pattern} \\ \rightarrow 3\ 046\ 610 \end{array} \right\} \rightarrow \{4 \rightarrow 7.58312 \times 10^{-7}, 3 \rightarrow 0.999999\},$

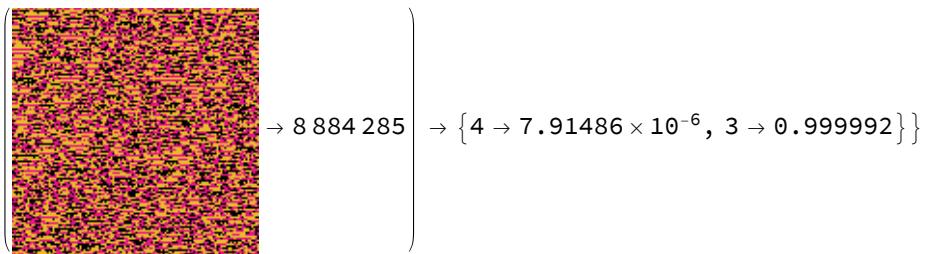
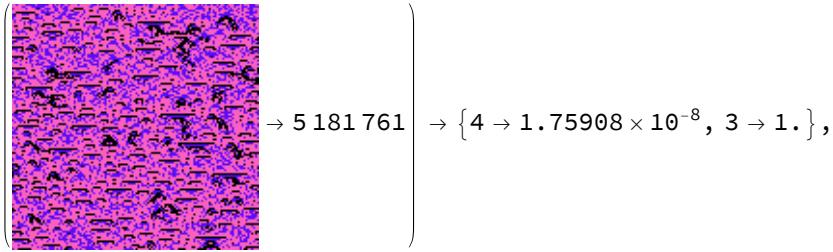
$\left\{ \begin{array}{l} \text{A blue pattern with vertical} \\ \text{black dots} \\ \rightarrow 7\ 801\ 434 \end{array} \right\} \rightarrow \{1 \rightarrow 1.19167 \times 10^{-14}, 2 \rightarrow 1.\},$

$\left\{ \begin{array}{l} \text{A blue pattern with horizontal} \\ \text{black lines} \\ \rightarrow 5\ 445\ 843 \end{array} \right\} \rightarrow \{4 \rightarrow 1.60992 \times 10^{-19}, 3 \rightarrow 1.\},$

$\left\{ \begin{array}{l} \text{A purple pattern} \\ \rightarrow 1\ 451\ 413 \end{array} \right\} \rightarrow \{4 \rightarrow 0.144413, 3 \rightarrow 0.855587\},$

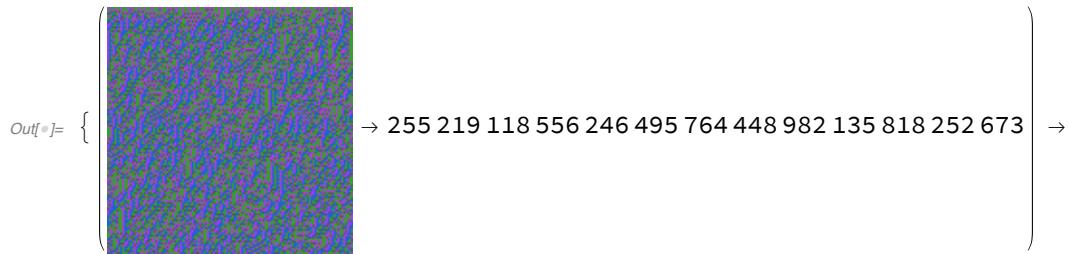
$\left\{ \begin{array}{l} \text{A brown pattern} \\ \rightarrow 10\ 676\ 790 \end{array} \right\} \rightarrow \{3 \rightarrow 0.0738921, 4 \rightarrow 0.926108\},$

$\left\{ \begin{array}{l} \text{A pink pattern} \\ \rightarrow 10\ 375\ 449 \end{array} \right\} \rightarrow \{4 \rightarrow 1.04031 \times 10^{-17}, 3 \rightarrow 1.\},$

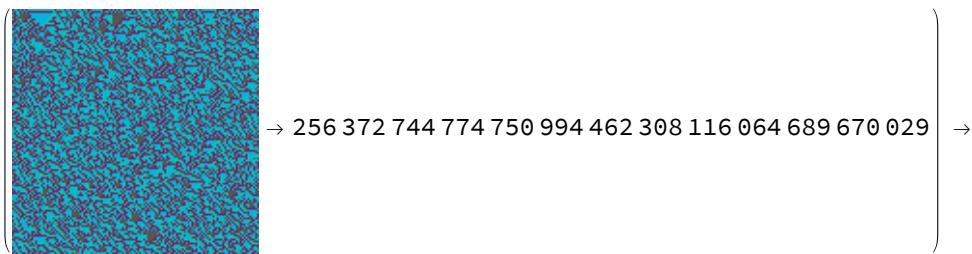


4-colour non-totalistic, range 1

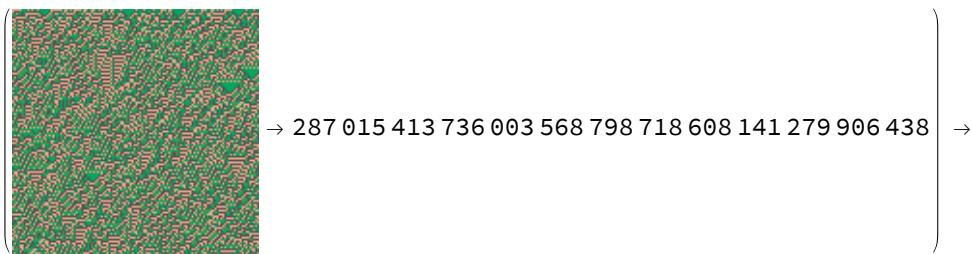
```
In[]:= test4Data4kr1C17 = datak4r1NT[128, 128, 8];
Thread[
test4Data4kr1C17 → netECA17[Keys@test4Data4kr1C17, {"TopProbabilities", 2}]]
```



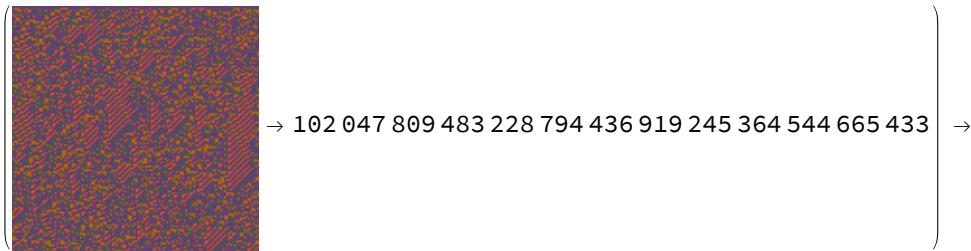
{3 → 2.62807 × 10⁻⁶, 4 → 0.999997},



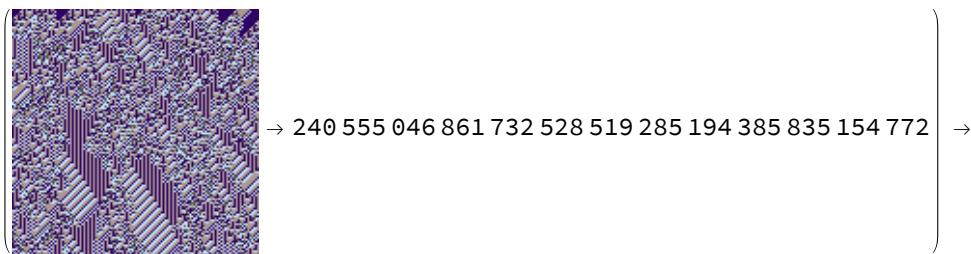
{4 → 1.66442 × 10⁻¹⁷, 3 → 1.},



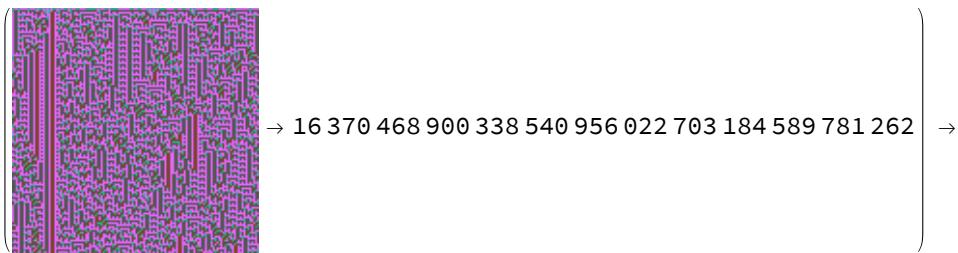
$\{4 \rightarrow 2.56385 \times 10^{-7}, 3 \rightarrow 1.\}$,



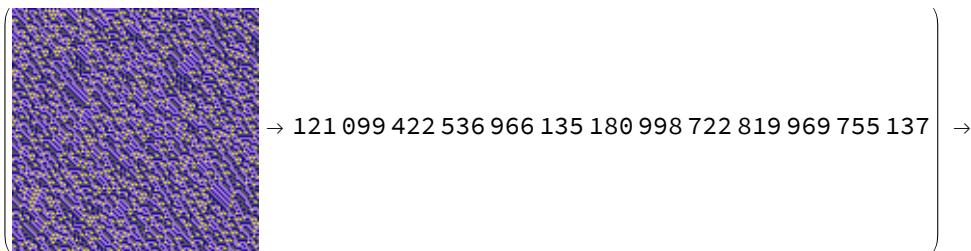
$\{4 \rightarrow 0.000696463, 3 \rightarrow 0.999304\}$,



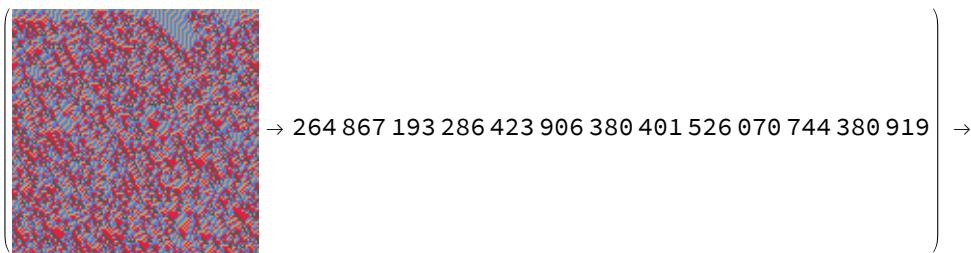
$\{4 \rightarrow 3.62136 \times 10^{-16}, 3 \rightarrow 1.\}$,



$\{3 \rightarrow 1.45252 \times 10^{-15}, 4 \rightarrow 1.\}$,



$\{4 \rightarrow 0.0000270873, 3 \rightarrow 0.999973\}$,



$\{4 \rightarrow 0.105214, 3 \rightarrow 0.894786\}$

4-colour totalistic, range 2

```
In[]:= test4Data4kr2C17 = datak4r2C[128, 128, 8];
Thread[
  test4Data4kr2C17 → netECA17[Keys@test4Data4kr2C17, {"TopProbabilities", 2}]]
```

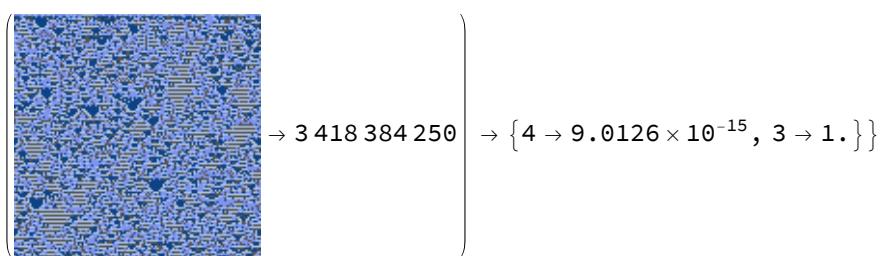
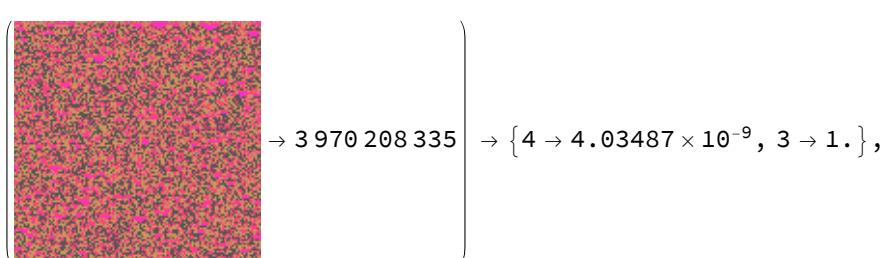
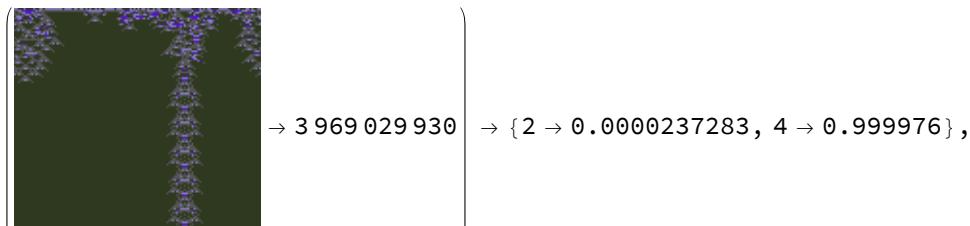
$$\text{Out}[]= \left\{ \begin{array}{l} \text{A 128x128 grid of colored pixels (purple, green, yellow, red)} \\ \rightarrow 616\ 082\ 315 \end{array} \right\} \rightarrow \{4 \rightarrow 8.8653 \times 10^{-10}, 3 \rightarrow 1.\},$$

$$\left\{ \begin{array}{l} \text{A 128x128 grid of colored pixels (purple, green, yellow, red)} \\ \rightarrow 1\ 568\ 191\ 428 \end{array} \right\} \rightarrow \{4 \rightarrow 5.21264 \times 10^{-11}, 3 \rightarrow 1.\},$$

$$\left\{ \begin{array}{l} \text{A 128x128 grid of colored pixels (purple, green, yellow, red)} \\ \rightarrow 1\ 216\ 110\ 065 \end{array} \right\} \rightarrow \{4 \rightarrow 0.000040346, 3 \rightarrow 0.99996\},$$

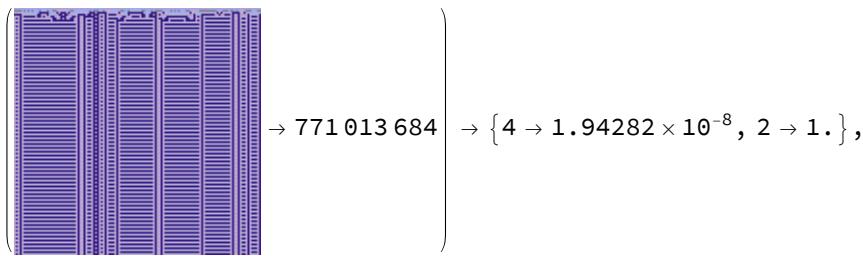
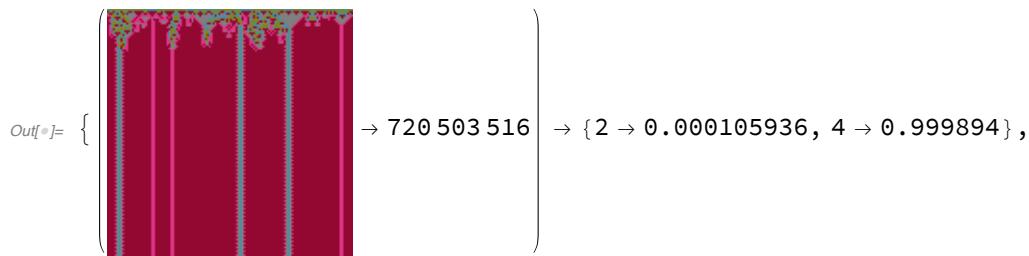
$$\left\{ \begin{array}{l} \text{A 128x128 grid of colored pixels (purple, green, yellow, red)} \\ \rightarrow 2\ 419\ 903\ 949 \end{array} \right\} \rightarrow \{4 \rightarrow 3.69897 \times 10^{-10}, 3 \rightarrow 1.\},$$

$$\left\{ \begin{array}{l} \text{A 128x128 grid of colored pixels (purple, green, yellow, red)} \\ \rightarrow 453\ 961\ 055 \end{array} \right\} \rightarrow \{4 \rightarrow 3.89961 \times 10^{-8}, 3 \rightarrow 1.\},$$



5-colour totalistic, range 1

```
In[8]:= test4Data5kr1C17 = data5T2C[8, 128, 128];
Thread[
  test4Data5kr1C17 &gt; netECA17[Keys@test4Data5kr1C17, {"TopProbabilities", 2}]]
```



$$\left(\begin{array}{c} \text{[A 19x20 grid of random colors]} \\ \rightarrow 543\ 872\ 434 \end{array} \right) \rightarrow \{4 \rightarrow 6.11423 \times 10^{-7}, 3 \rightarrow 0.999999\},$$

$$\left(\begin{array}{c} \text{[A 19x20 grid of random colors]} \\ \rightarrow 341\ 908\ 586 \end{array} \right) \rightarrow \{4 \rightarrow 0.310854, 3 \rightarrow 0.689146\},$$

$$\left(\begin{array}{c} \text{[A 19x20 grid of random colors]} \\ \rightarrow 664\ 036\ 861 \end{array} \right) \rightarrow \{2 \rightarrow 0.00511847, 4 \rightarrow 0.994882\},$$

$$\left(\begin{array}{c} \text{[A 19x20 grid of random colors]} \\ \rightarrow 1\ 182\ 110\ 899 \end{array} \right) \rightarrow \{4 \rightarrow 0.039023, 3 \rightarrow 0.960977\},$$

$$\left(\begin{array}{c} \text{[A 19x20 grid of random colors]} \\ \rightarrow 976\ 082\ 949 \end{array} \right) \rightarrow \{4 \rightarrow 9.09593 \times 10^{-19}, 2 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[A 19x20 grid of random colors]} \\ \rightarrow 1\ 019\ 517\ 181 \end{array} \right) \rightarrow \{1 \rightarrow 6.47917 \times 10^{-10}, 2 \rightarrow 1.\}$$

6-colour totalistic, range 1

```
In[]:= test4Data6kr1C17 = data6TC[8, 128, 128];
Thread[
  test4Data6kr1C17 → netECA17[Keys@test4Data6kr1C17, {"TopProbabilities", 2}]]
```

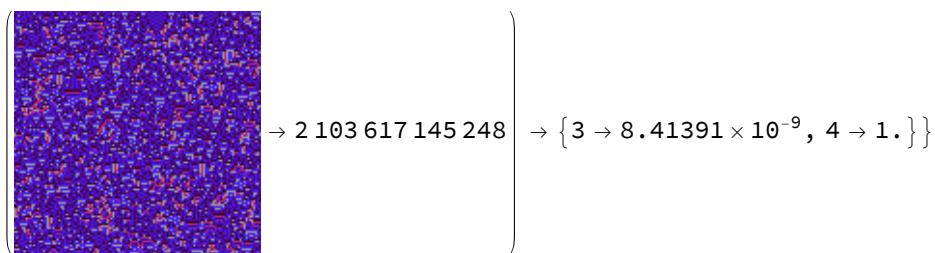
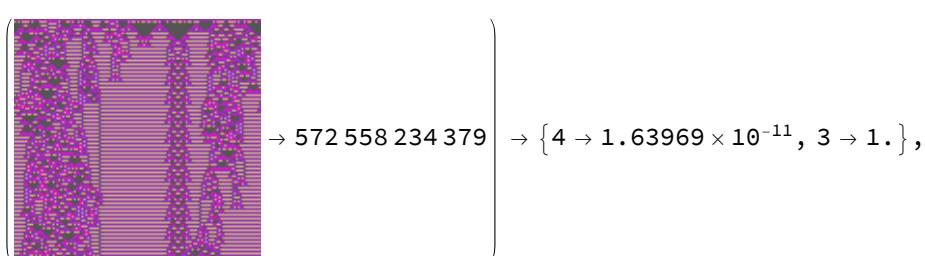
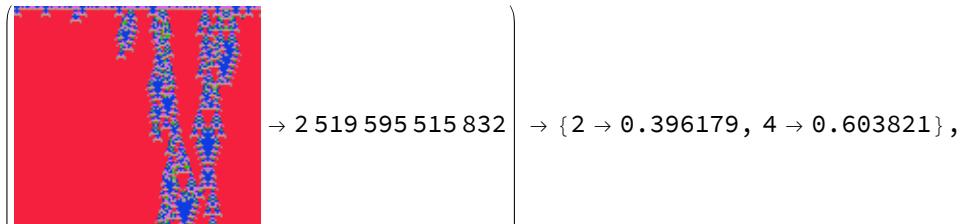
Out[]:= $\left\{ \begin{array}{c} \text{[A 128x128 grid of horizontal green and blue bars]} \\ \rightarrow 1\ 128\ 957\ 409\ 115 \end{array} \right\} \rightarrow \{2 \rightarrow 0.387573, 1 \rightarrow 0.612427\},$

$\left\{ \begin{array}{c} \text{[A 128x128 grid of complex, multi-colored patterns]} \\ \rightarrow 744\ 151\ 919\ 694 \end{array} \right\} \rightarrow \{3 \rightarrow 1.28454 \times 10^{-11}, 4 \rightarrow 1.\},$

$\left\{ \begin{array}{c} \text{[A 128x128 grid of mostly red and green pixels]} \\ \rightarrow 411\ 482\ 269\ 593 \end{array} \right\} \rightarrow \{4 \rightarrow 9.50671 \times 10^{-6}, 3 \rightarrow 0.99999\},$

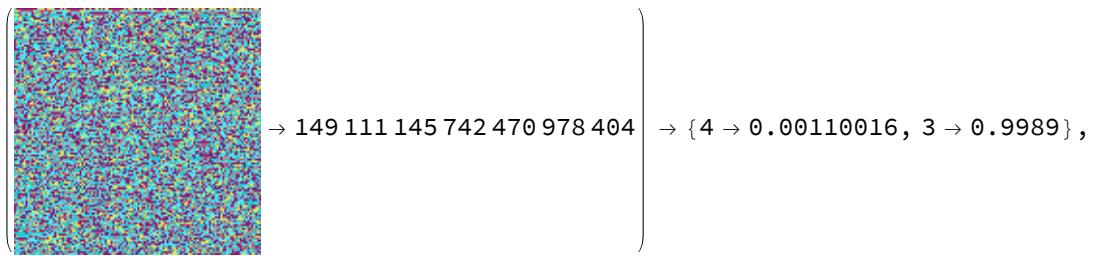
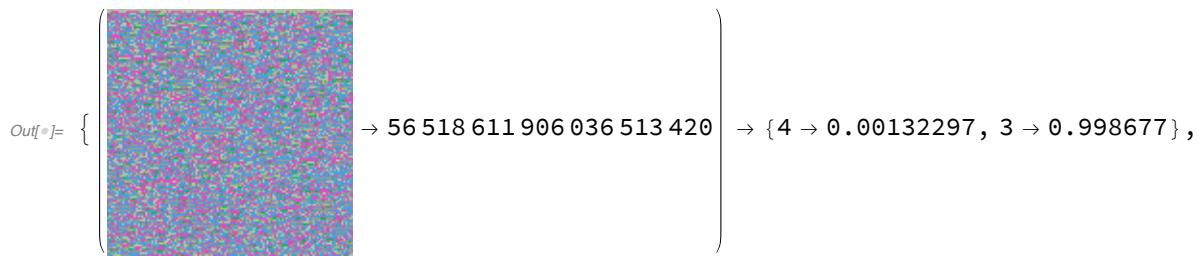
$\left\{ \begin{array}{c} \text{[A 128x128 grid of blue and yellow pixels]} \\ \rightarrow 2\ 122\ 826\ 252\ 429 \end{array} \right\} \rightarrow \{4 \rightarrow 4.58698 \times 10^{-10}, 3 \rightarrow 1.\},$

$\left\{ \begin{array}{c} \text{[A 128x128 grid of red and green pixels]} \\ \rightarrow 2\ 443\ 710\ 325\ 124 \end{array} \right\} \rightarrow \{4 \rightarrow 5.97811 \times 10^{-9}, 3 \rightarrow 1.\},$



6-colour totalistic, range 2

```
In[]:= test4Data6kr2C17 = data6T2C[8, 128, 128];
Thread[
  test4Data6kr2C17 → netECA17[Keys@test4Data6kr2C17, {"TopProbabilities", 2}]]
```



$$\left(\begin{array}{c} \text{[A 10x10 grid of blue and orange dots]} \\ \rightarrow 60\ 075\ 298\ 400\ 874\ 491\ 559 \end{array} \right) \rightarrow \{4 \rightarrow 0.0000816385, 3 \rightarrow 0.999918\},$$

$$\left(\begin{array}{c} \text{[A 10x10 grid of green and purple dots]} \\ \rightarrow 61\ 137\ 219\ 885\ 741\ 406\ 688 \end{array} \right) \rightarrow \{4 \rightarrow 6.01526 \times 10^{-9}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[A 10x10 grid of green and red dots]} \\ \rightarrow 138\ 083\ 937\ 800\ 052\ 503\ 915 \end{array} \right) \rightarrow \{4 \rightarrow 1.63338 \times 10^{-6}, 3 \rightarrow 0.999998\},$$

$$\left(\begin{array}{c} \text{[A 10x10 grid of red and yellow dots]} \\ \rightarrow 102\ 848\ 890\ 668\ 267\ 918\ 696 \end{array} \right) \rightarrow \{4 \rightarrow 4.51684 \times 10^{-8}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[A 10x10 grid of blue and purple dots]} \\ \rightarrow 52\ 002\ 759\ 529\ 482\ 240\ 344 \end{array} \right) \rightarrow \{4 \rightarrow 0.0161382, 3 \rightarrow 0.983862\},$$

$$\left(\begin{array}{c} \text{[A 10x10 grid of green and pink dots]} \\ \rightarrow 3\ 771\ 326\ 190\ 903\ 203\ 597 \end{array} \right) \rightarrow \{4 \rightarrow 1.57635 \times 10^{-10}, 3 \rightarrow 1.\}\}$$

7-colour totalistic, range 1

```
In[]:= test4Data7kr1C17 = data7TC[8, 128, 128];
Thread[
test4Data7kr1C17 → netECA17[Keys@test4Data7kr1C17, {"TopProbabilities", 2}]]
```

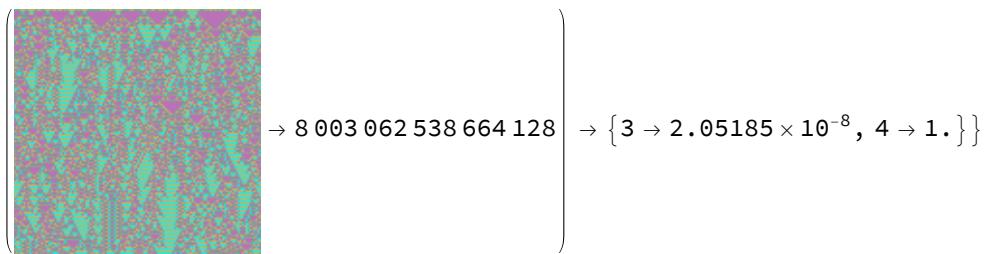
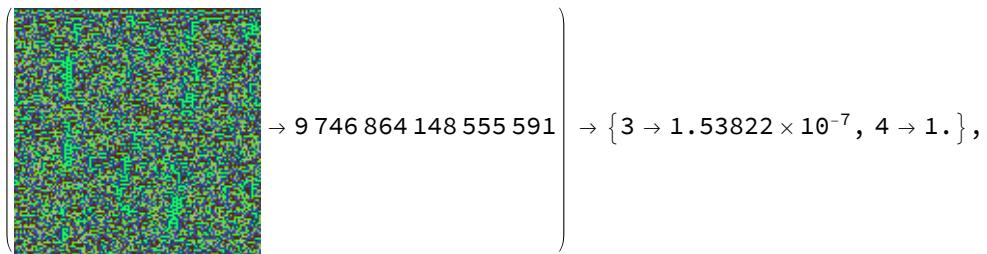
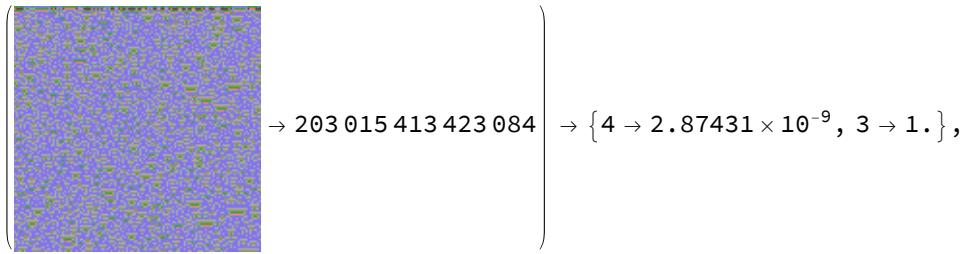
$$\left. \begin{array}{l} \text{Out}[1]= \left\{ \begin{array}{l} \text{A 128x128 pixel grid with various colors (yellow, red, blue, green, etc.)} \\ \rightarrow 249\,739\,897\,876\,317 \end{array} \right\} \rightarrow \left\{ 4 \rightarrow 7.58753 \times 10^{-13}, 3 \rightarrow 1. \right\}, \end{array} \right.$$

$$\left. \begin{array}{l} \text{Out}[2]= \left\{ \begin{array}{l} \text{A 128x128 pixel grid with various colors (yellow, red, blue, green, etc.)} \\ \rightarrow 6\,589\,873\,174\,284\,234 \end{array} \right\} \rightarrow \left\{ 4 \rightarrow 3.70203 \times 10^{-21}, 3 \rightarrow 1. \right\}, \end{array} \right.$$

$$\left. \begin{array}{l} \text{Out}[3]= \left\{ \begin{array}{l} \text{A 128x128 pixel grid with various colors (yellow, red, blue, green, etc.)} \\ \rightarrow 2\,838\,251\,451\,633\,386 \end{array} \right\} \rightarrow \left\{ 3 \rightarrow 0.0000362001, 4 \rightarrow 0.999964 \right\}, \end{array} \right.$$

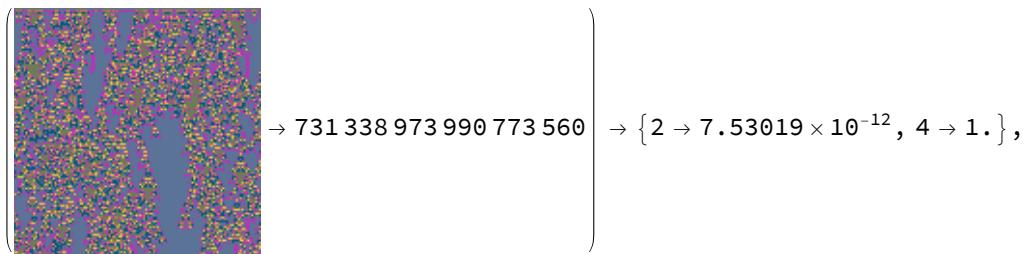
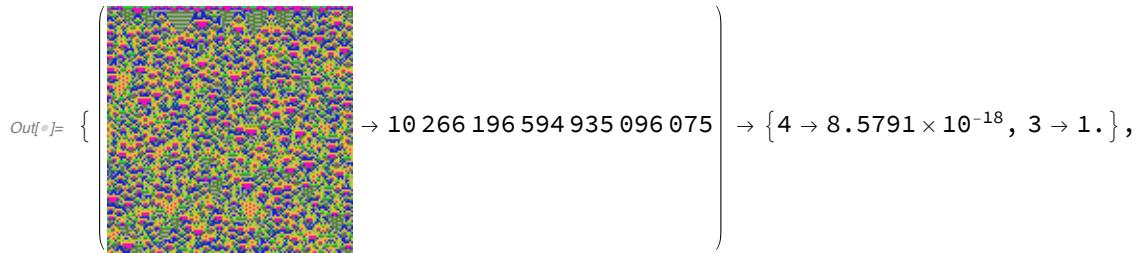
$$\left. \begin{array}{l} \text{Out}[4]= \left\{ \begin{array}{l} \text{A 128x128 pixel grid with various colors (yellow, red, blue, green, etc.)} \\ \rightarrow 3\,069\,021\,856\,393\,877 \end{array} \right\} \rightarrow \left\{ 4 \rightarrow 4.6982 \times 10^{-6}, 3 \rightarrow 0.999995 \right\}, \end{array} \right.$$

$$\left. \begin{array}{l} \text{Out}[5]= \left\{ \begin{array}{l} \text{A 128x128 pixel grid with various colors (yellow, red, blue, green, etc.)} \\ \rightarrow 10\,282\,712\,720\,317\,214 \end{array} \right\} \rightarrow \left\{ 3 \rightarrow 4.14045 \times 10^{-19}, 4 \rightarrow 1. \right\}, \end{array} \right.$$



8-colour totalistic, range 1

```
In[]:= test4Data8kr1C17 = data8TC[8, 128, 128];
Thread[
  test4Data8kr1C17 &gt;> netECA17[Keys@test4Data8kr1C17, {"TopProbabilities", 2}]]
```



$$\left(\begin{array}{c} \text{[A 2x2 grid of colored pixels]} \\ \rightarrow 11\ 247\ 173\ 012\ 174\ 218\ 620 \end{array} \right) \rightarrow \{4 \rightarrow 0.0000380778, 3 \rightarrow 0.999962\},$$

$$\left(\begin{array}{c} \text{[A 2x2 grid of colored pixels]} \\ \rightarrow 63\ 742\ 472\ 032\ 617\ 219\ 918 \end{array} \right) \rightarrow \{4 \rightarrow 0.0000371126, 3 \rightarrow 0.999963\},$$

$$\left(\begin{array}{c} \text{[A 2x2 grid of colored pixels]} \\ \rightarrow 7\ 382\ 455\ 380\ 800\ 363\ 015 \end{array} \right) \rightarrow \{4 \rightarrow 8.07468 \times 10^{-15}, 3 \rightarrow 1.\},$$

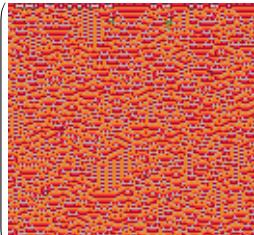
$$\left(\begin{array}{c} \text{[A 2x2 grid of colored pixels]} \\ \rightarrow 59\ 100\ 651\ 667\ 569\ 734\ 000 \end{array} \right) \rightarrow \{4 \rightarrow 1.27228 \times 10^{-11}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[A 2x2 grid of colored pixels]} \\ \rightarrow 24\ 971\ 306\ 247\ 396\ 766\ 335 \end{array} \right) \rightarrow \{4 \rightarrow 0.0333734, 3 \rightarrow 0.966627\},$$

$$\left(\begin{array}{c} \text{[A 2x2 grid of colored pixels]} \\ \rightarrow 45\ 946\ 581\ 080\ 593\ 555\ 746 \end{array} \right) \rightarrow \{4 \rightarrow 1.08598 \times 10^{-15}, 3 \rightarrow 1.\}$$

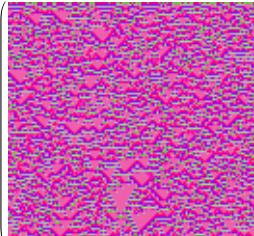
```
In[8]:= test4Data8kr1C17 = data8TC[8, 128, 128];
Thread[
  test4Data8kr1C17 → netECA17[Keys@test4Data8kr1C17, {"TopProbabilities", 2}]]
```

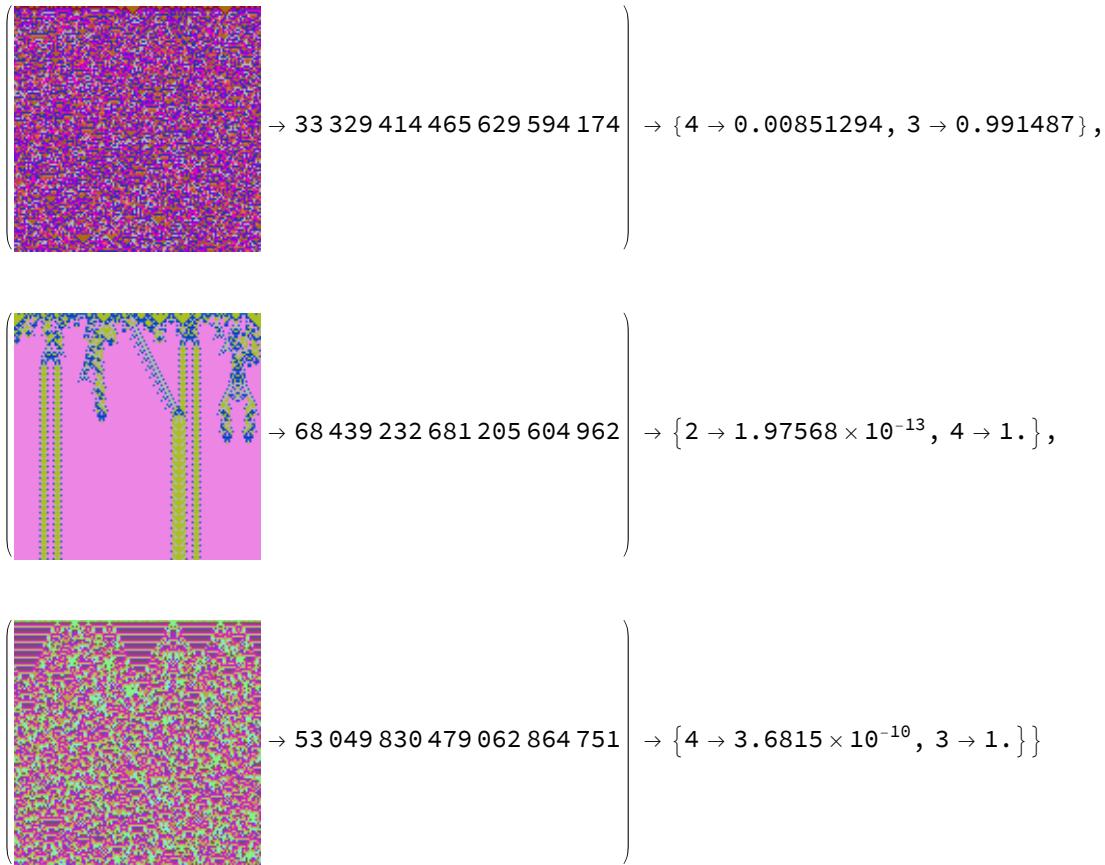
Out[8]= { → 14 955 350 598 586 141 683}

{ → 30 727 455 169 449 395 964}

{ → 42 490 152 676 883 207 115}

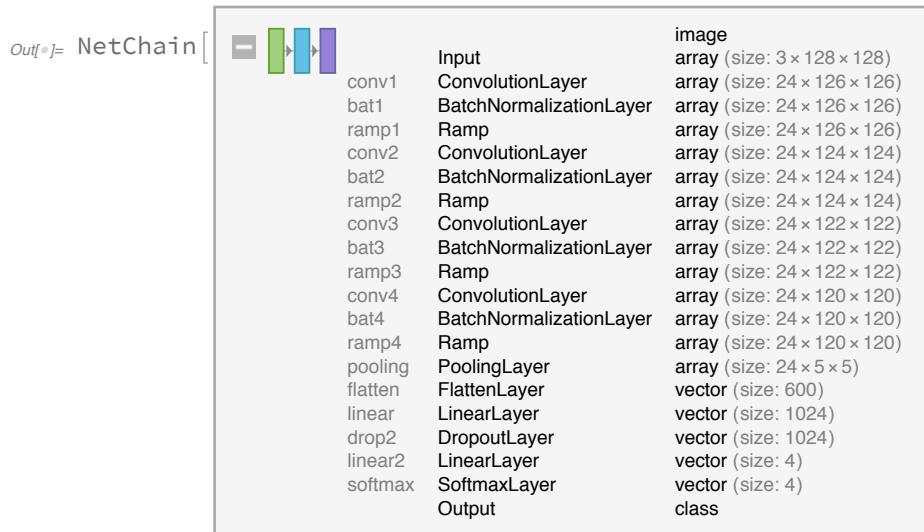
{ → 18 395 296 261 071 222 192}

{ → 22 317 090 484 634 250 431}

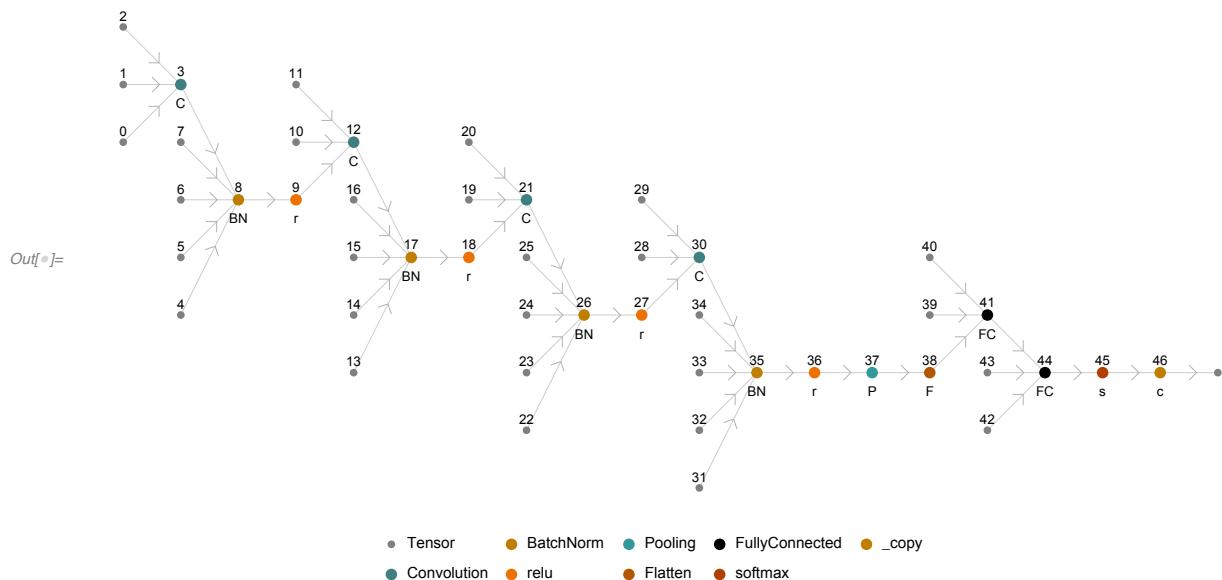


Network XVIII- Four convolutions, dropout on linear only, BatchNorm

```
In[®]:= netECA18 = netTenCC1024drop[128, 128]
```



```
In[6]:= NetInformation[netECA18, "MXNetNodeGraphPlot"]
```



```
In[526]:= NetInformation[netECA18, "SummaryGraphic"]
```



```
In[6]:= dataECA18 = dataC[128, 128, 16 384];
```

```
In[6]:= dataTotalistic2BigC18 = genData2r2C[128, 128, 4096];
```

```
In[6]:= dataTotalistic3BigC18 = data3T2C[128, 128, 4096];
```

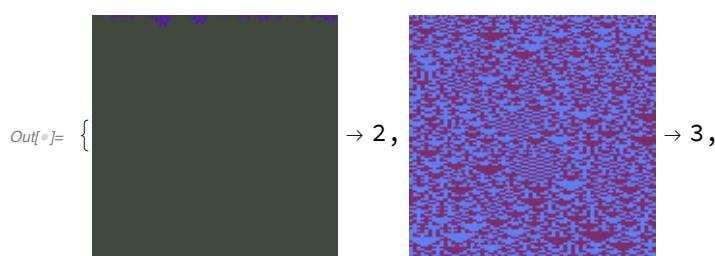
```
In[6]:= dataTotalistic4BigC18 = data4TC[128, 128, 4096];
```

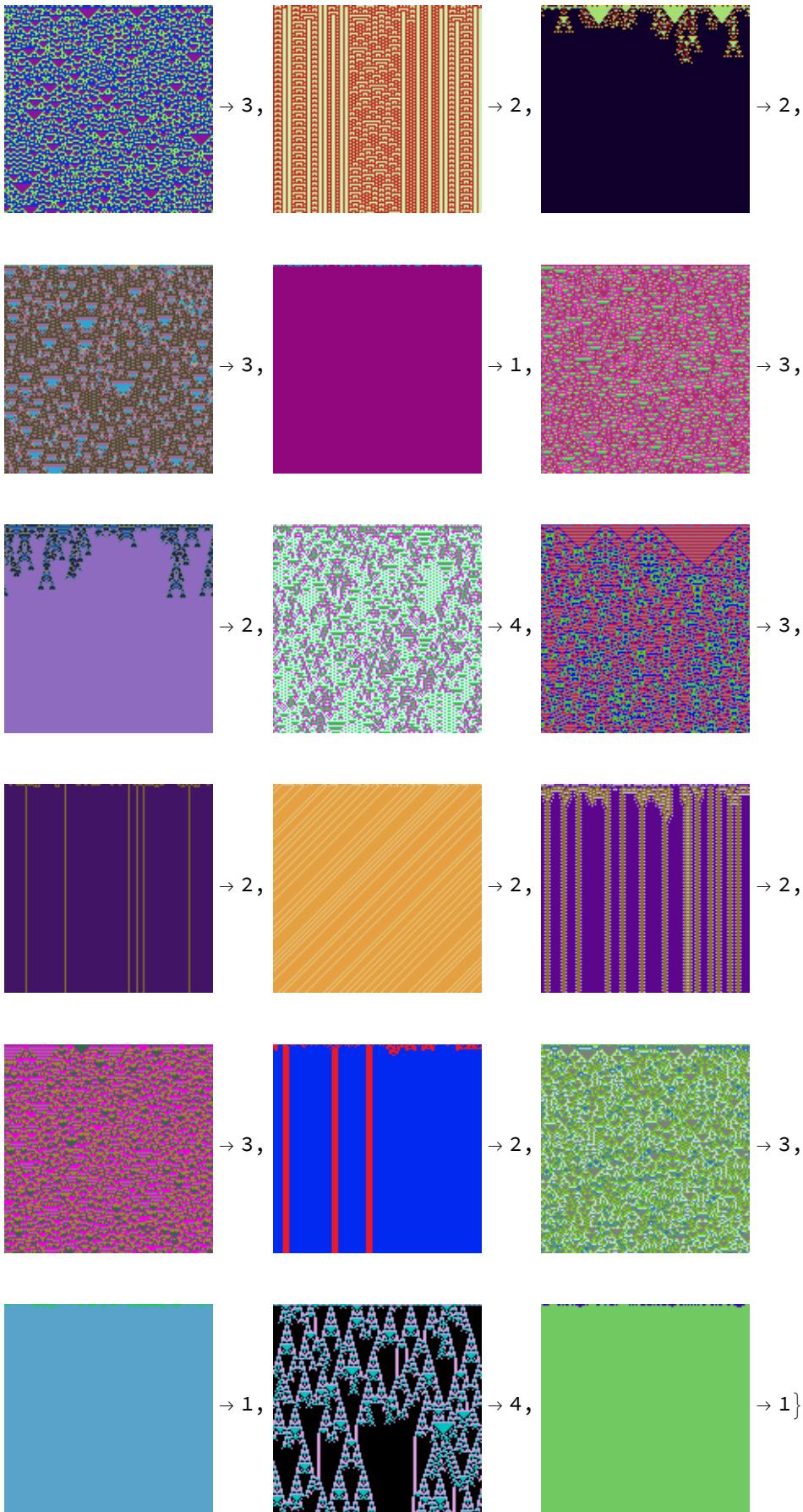
```
In[6]:= dataTotalistic5BigC18 = genData5TCC[128, 128, 16 384];
```

```
In[6]:= fullTrainingBigC18 = Join[dataECA18, dataTotalistic2BigC18,
    dataTotalistic3BigC18, dataTotalistic4BigC18, dataTotalistic5BigC18];
Length[fullTrainingBigC18]
```

```
Out[6]= 90112
```

```
In[6]:= RandomSample[fullTrainingBigC18, 20]
```





```
In[⑩]:= dir = SetDirectory[NotebookDirectory[]]
Out[⑩]= /home/esilverman/Documents

In[⑪]:= "/home/esilverman/Documents"
Out[⑪]= /home/esilverman/Documents

In[⑫]:= netECA18 = NetTrain[netECA18, fullTrainingBigC18,
  MaxTrainingRounds → 200, BatchSize → 256, TargetDevice → "GPU",
  TrainingProgressCheckpointing → {"Directory", dir}]
```

Out[⑫]= NetChain[ Input port: image
Output port: class
Number of layers: 18]

```
In[⑬]:= netECA18 = Import["netECA18-r200.wlnet"]
Out[⑬]= NetChain[ Input port: image  
Output port: class  
Number of layers: 18]
```

Generate test data for Network XVII (200 epochs)

```
In[⑭]:= dir = SetDirectory[NotebookDirectory[]]
Out[⑭]= /Users/thorsilver/Downloads/Wolfram notebooks
```

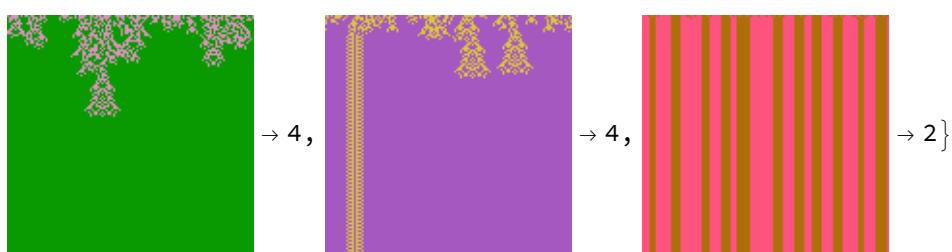
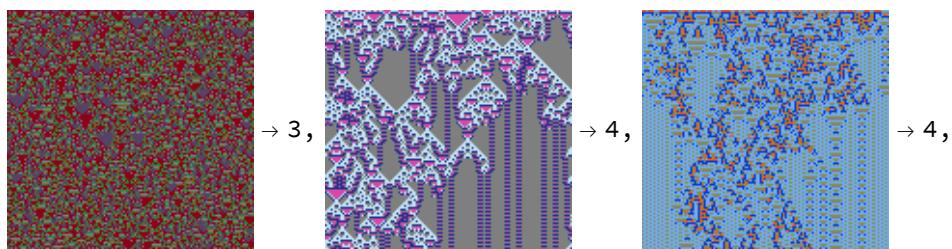
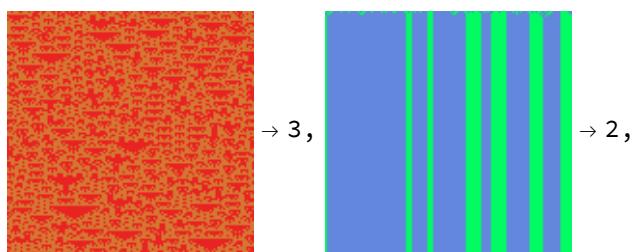
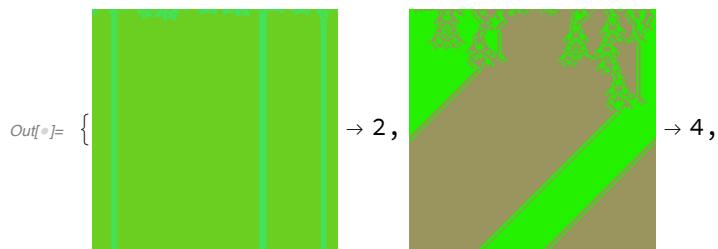
```
In[180]:= netECA18 = Import["netECA18-r200.wlnet"]
```

Out[180]= NetChain[ Input image
conv1 ConvolutionLayer array (size: 3 × 128 × 128)
bat1 BatchNormalizationLayer array (size: 24 × 126 × 126)
ramp1 Ramp array (size: 24 × 126 × 126)
conv2 ConvolutionLayer array (size: 24 × 124 × 124)
bat2 BatchNormalizationLayer array (size: 24 × 124 × 124)
ramp2 Ramp array (size: 24 × 124 × 124)
conv3 ConvolutionLayer array (size: 24 × 122 × 122)
bat3 BatchNormalizationLayer array (size: 24 × 122 × 122)
ramp3 Ramp array (size: 24 × 122 × 122)
conv4 ConvolutionLayer array (size: 24 × 120 × 120)
bat4 BatchNormalizationLayer array (size: 24 × 120 × 120)
ramp4 Ramp array (size: 24 × 120 × 120)
pooling PoolingLayer array (size: 24 × 5 × 5)
flatten FlattenLayer vector (size: 600)
linear LinearLayer vector (size: 1024)
drop2 DropoutLayer vector (size: 1024)
linear2 LinearLayer vector (size: 4)
softmax SoftmaxLayer vector (size: 4)
Output class]

```
In[®]:= testDataECABigC = dataC[128, 128, 1024];
testData2TBigC = genData2r2C[128, 128, 1024];
testData3TBigC = data3T2C[128, 128, 1024];
testData4TBigC = data4TC[128, 128, 1024];
testData5TBigC = genData5TCC[128, 128, 1024];
fullTestSetBigC = Join[testDataECABigC,
  testData2TBigC, testData3TBigC, testData4TBigC, testData5TBigC];
Length[fullTestSetBigC]
```

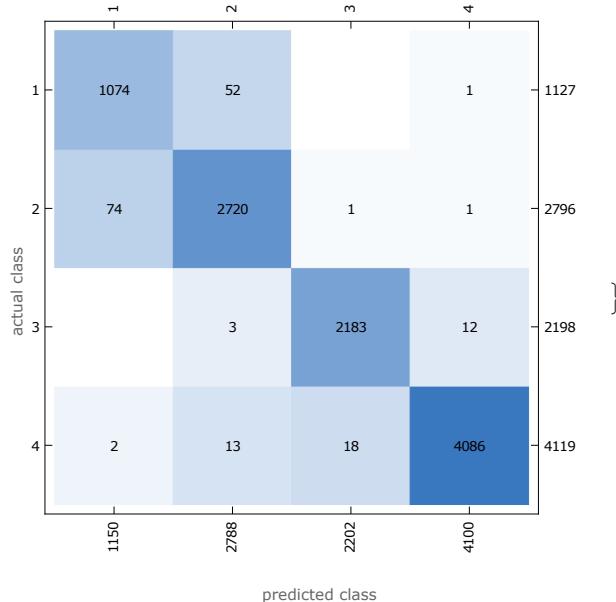
Out[®]= 10240

```
In[®]:= RandomSample[fullTestSetBigC, 10]
```

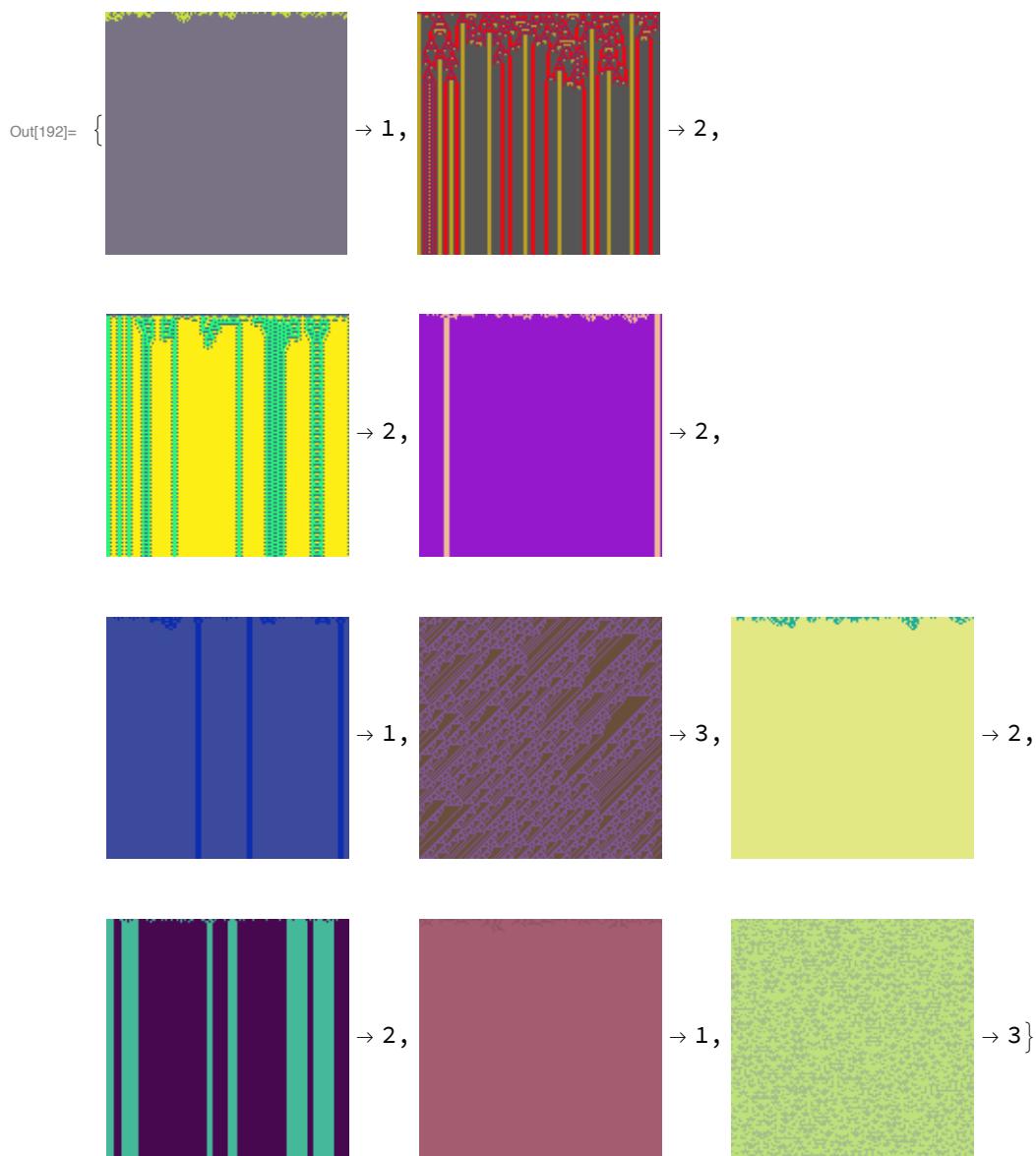


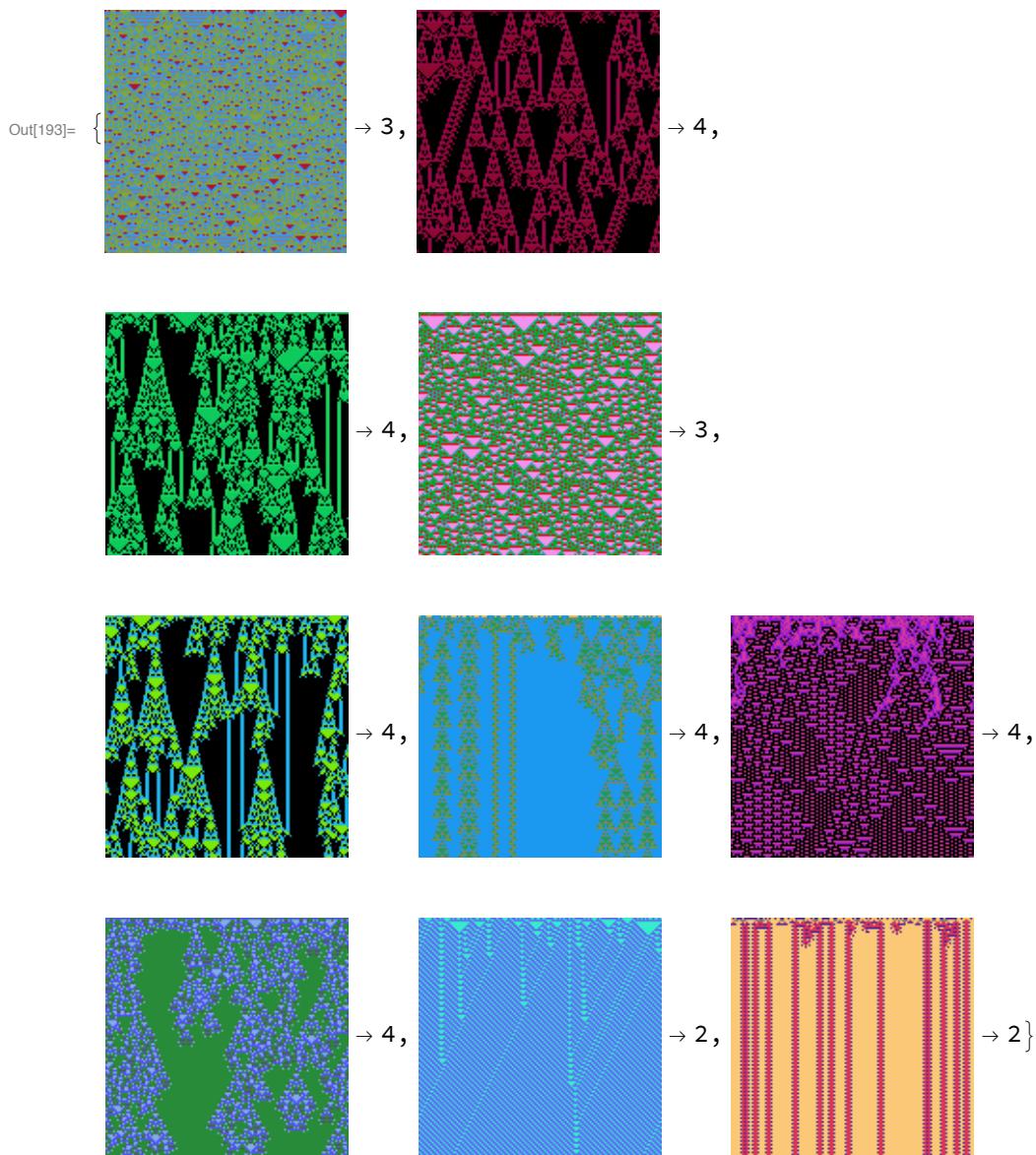
```
In[181]:= NetMeasurements[netECA18, fullTestSetBigC,
 {"Accuracy", "Precision", "ConfusionMatrixPlot"}]

Out[181]= {0.982715, {1 → 0.933913, 2 → 0.97561, 3 → 0.991371, 4 → 0.996585}, }
```



```
In[188]:= entropyImagesBigC = RandomSample[Keys[fullTestSetBigC], 500];
entropiesBigC = netECA18[entropyImagesBigC, "Entropy"];
highEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, -10]]];
lowEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, 10]]];
Thread[highEntBigC → netECA18[highEntBigC]]
Thread[lowEntBigC → netECA18[lowEntBigC]]
```





Testing Network XVIII (200 epochs) on unseen CA rule spaces

2-colour non-totalistic, range 2

```
In[527]:= test4Data2kr2C18 = datak2r2C[128, 128, 8];
Thread[
  test4Data2kr2C18 → netECA18[Keys@test4Data2kr2C18, {"TopProbabilities", 2}]]
```

Out[528]= {

$\rightarrow 1\ 370\ 260\ 644$

$\rightarrow \{4 \rightarrow 0.0166854, 2 \rightarrow 0.983315\},$

$$\left(\begin{array}{c} \text{[A 2x2 grid of small black dots on a white background]} \\ \rightarrow 1\ 807\ 990\ 148 \end{array} \right) \rightarrow \{2 \rightarrow 3.85446 \times 10^{-17}, 3 \rightarrow 1.\},$$

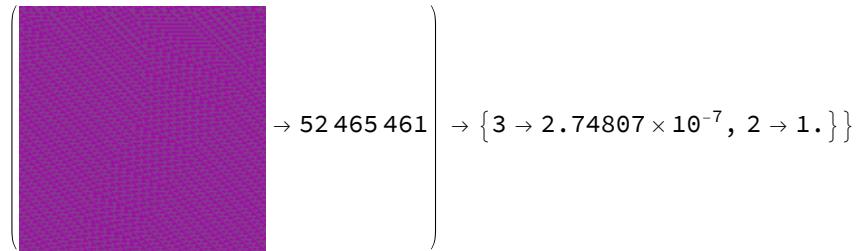
$$\left(\begin{array}{c} \text{[A 2x2 grid of small green dots on a white background]} \\ \rightarrow 2\ 530\ 190\ 276 \end{array} \right) \rightarrow \{4 \rightarrow 2.53726 \times 10^{-6}, 3 \rightarrow 0.999997\},$$

$$\left(\begin{array}{c} \text{[A 2x2 grid of small blue dots on a white background]} \\ \rightarrow 2\ 788\ 659\ 278 \end{array} \right) \rightarrow \{4 \rightarrow 7.89003 \times 10^{-11}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[A 2x2 grid of small red dots on a white background]} \\ \rightarrow 1\ 183\ 464\ 169 \end{array} \right) \rightarrow \{4 \rightarrow 8.12001 \times 10^{-9}, 3 \rightarrow 1.\},$$

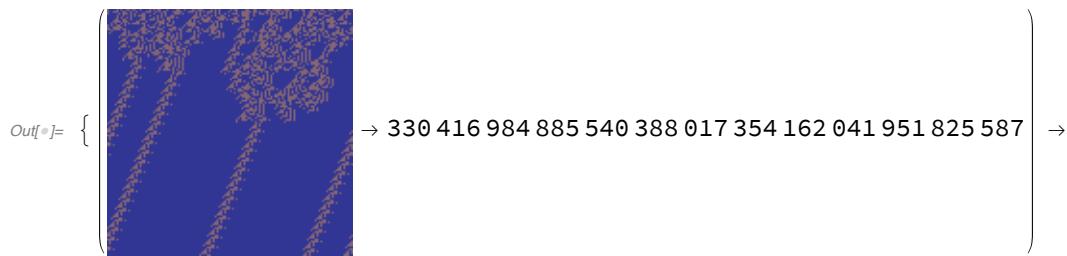
$$\left(\begin{array}{c} \text{[A 2x2 grid of small orange dots on a white background]} \\ \rightarrow 3\ 203\ 768\ 679 \end{array} \right) \rightarrow \{4 \rightarrow 1.44395 \times 10^{-7}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[A 2x2 grid of vertical bars in red, green, and blue]} \\ \rightarrow 1\ 424\ 091\ 569 \end{array} \right) \rightarrow \{2 \rightarrow 2.16345 \times 10^{-7}, 4 \rightarrow 1.\},$$

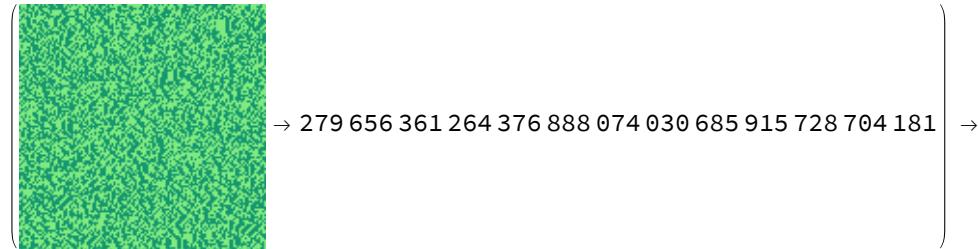


2-colour non-totalistic, range 3

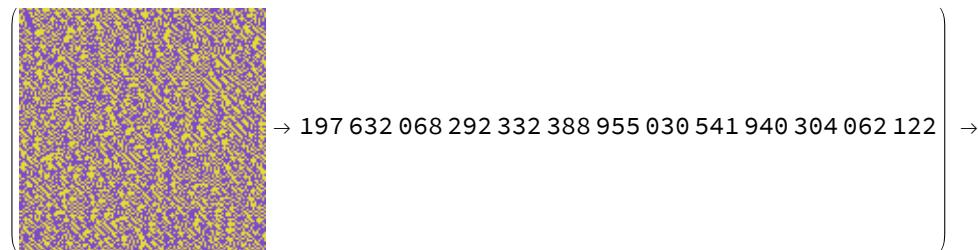
```
In[]:= test4Data2kr3C18 = datak2r3NT[128, 128, 8];
Thread[
test4Data2kr3C18 → netECA18[Keys@test4Data2kr3C18, {"TopProbabilities", 2}]]
```



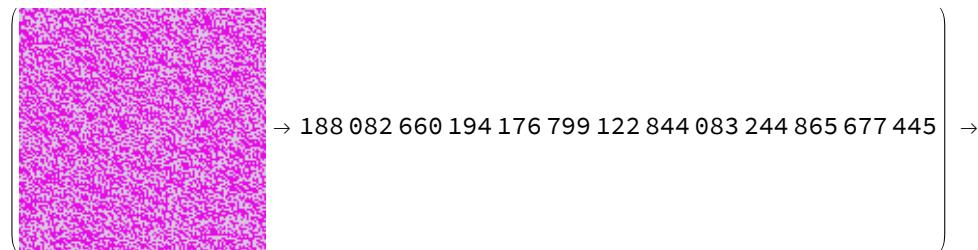
$$\{ 3 \rightarrow 8.74296 \times 10^{-8}, 4 \rightarrow 1. \},$$

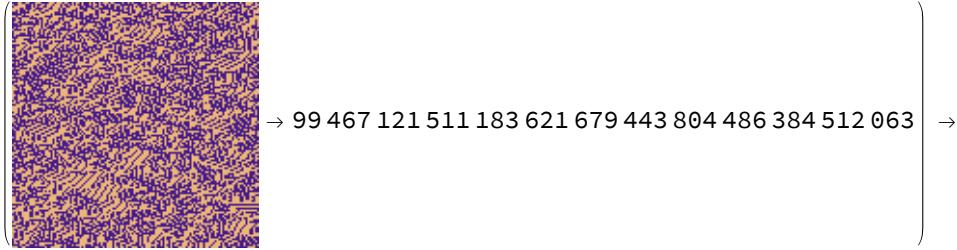
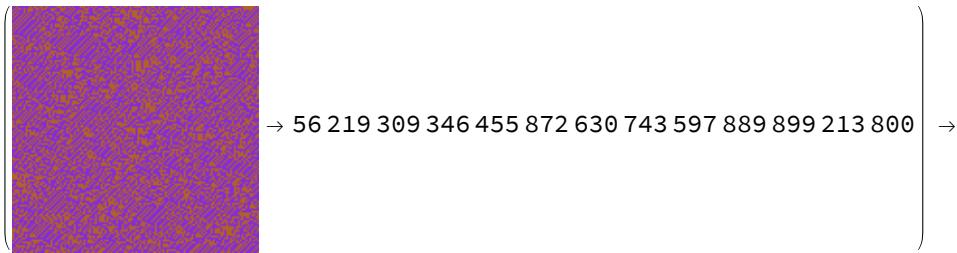


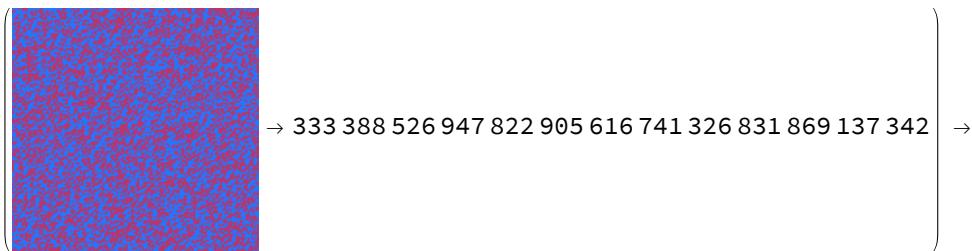
$$\{ 4 \rightarrow 0.0213521, 3 \rightarrow 0.978648 \},$$



$$\{ 4 \rightarrow 5.0499 \times 10^{-16}, 3 \rightarrow 1. \},$$



$\{4 \rightarrow 2.34238 \times 10^{-6}, 3 \rightarrow 0.999998\},$

 $\{4 \rightarrow 0.00329566, 3 \rightarrow 0.996704\},$

 $\{4 \rightarrow 1.38574 \times 10^{-10}, 3 \rightarrow 1.\},$

 $\{4 \rightarrow 5.1263 \times 10^{-8}, 3 \rightarrow 1.\},$

 $\{4 \rightarrow 7.10494 \times 10^{-8}, 3 \rightarrow 1.\}\}$

3-colour non-totalistic, range 1

```
In[6]:= test4Data3kr1C18 = datak3r1NT[128, 128, 8];
Thread[
test4Data3kr1C18 → netECA18[Keys@test4Data3kr1C18, {"TopProbabilities", 2}]]
```

$$Out[1]= \left\{ \begin{array}{l} \text{(A 10x10 grid of yellow dots)} \\ \rightarrow 1\ 592\ 394\ 332\ 064 \end{array} \right\} \rightarrow \{2 \rightarrow 7.59314 \times 10^{-6}, 4 \rightarrow 0.999992\},$$

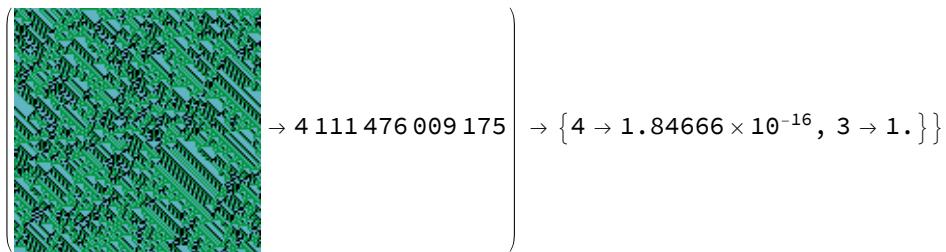
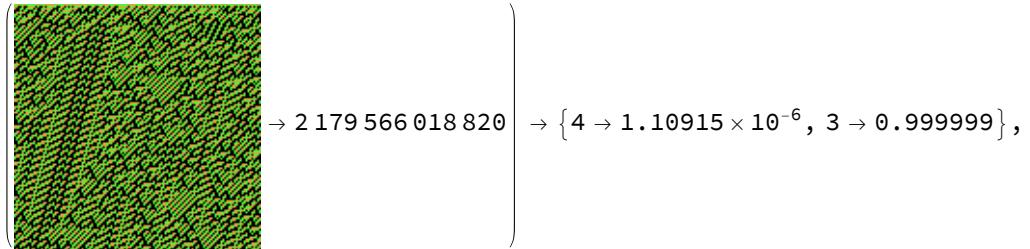
$$\left\{ \begin{array}{l} \text{(A 10x10 grid of purple dots)} \\ \rightarrow 4\ 098\ 174\ 485\ 356 \end{array} \right\} \rightarrow \{4 \rightarrow 8.44302 \times 10^{-20}, 2 \rightarrow 1.\},$$

$$\left\{ \begin{array}{l} \text{(A 10x10 grid of blue dots)} \\ \rightarrow 5\ 930\ 373\ 291\ 731 \end{array} \right\} \rightarrow \{1 \rightarrow 2.34989 \times 10^{-7}, 2 \rightarrow 1.\},$$

$$\left\{ \begin{array}{l} \text{(A 10x10 grid of green dots)} \\ \rightarrow 6\ 363\ 744\ 081\ 807 \end{array} \right\} \rightarrow \{3 \rightarrow 0.0000390704, 4 \rightarrow 0.999961\},$$

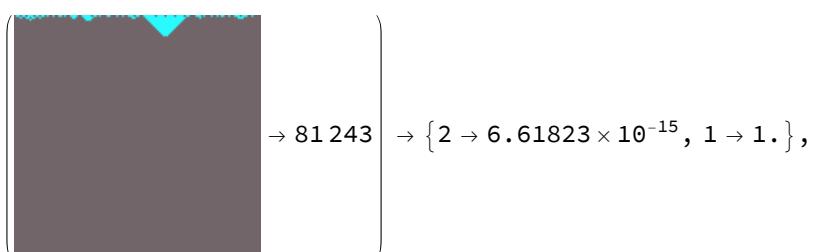
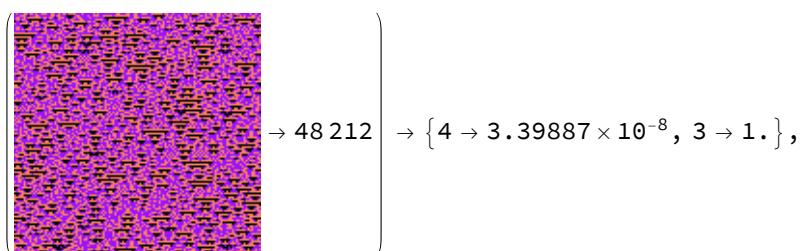
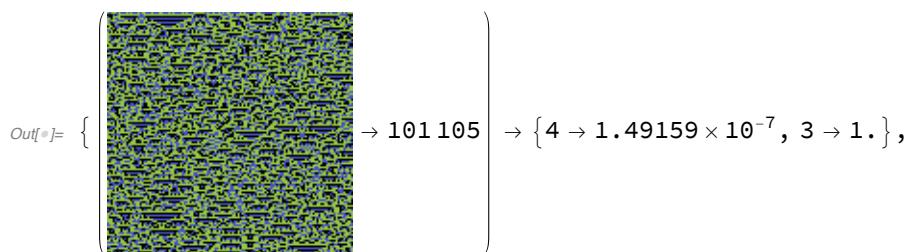
$$\left\{ \begin{array}{l} \text{(A 10x10 grid of blue and yellow dots)} \\ \rightarrow 1\ 193\ 083\ 886\ 293 \end{array} \right\} \rightarrow \{4 \rightarrow 0.0126455, 3 \rightarrow 0.987355\},$$

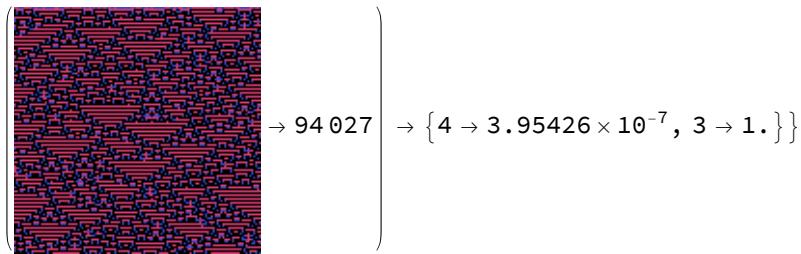
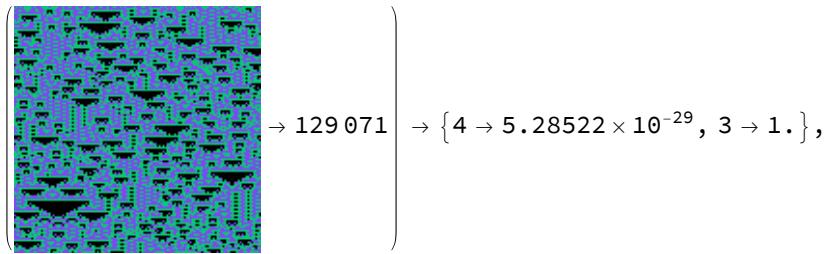
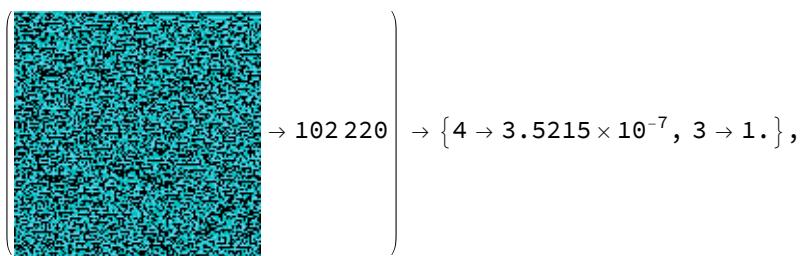
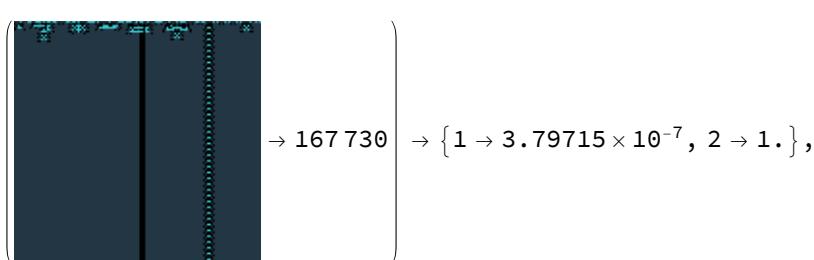
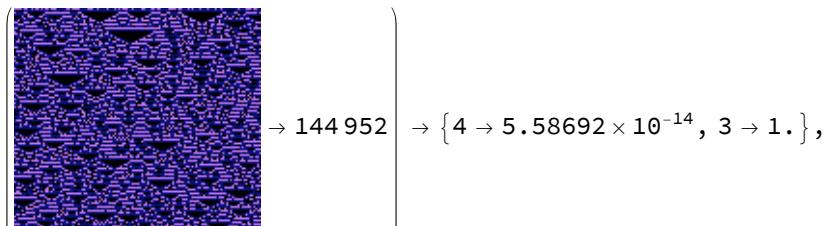
$$\left\{ \begin{array}{l} \text{(A 10x10 grid of green and black dots)} \\ \rightarrow 1\ 957\ 822\ 902\ 340 \end{array} \right\} \rightarrow \{3 \rightarrow 0.0000561806, 2 \rightarrow 0.999944\},$$



3-colour totalistic, range 2

```
In[]:= test4Data3kr2C18 = datak3r2C[128, 128, 8];
Thread[
  test4Data3kr2C18 → netECA18[Keys@test4Data3kr2C18, {"TopProbabilities", 2}]]
```





3-colour totalistic, range 3

```
In[⑩]:= test4Data3kr3C18 = datak3r3C[128, 128, 8];
Thread[
test4Data3kr3C18 → netECA18[Keys@test4Data3kr3C18, {"TopProbabilities", 2}]]
```

Out[•]= $\left\{ \begin{array}{l} \text{A 10x10 grid of blue and yellow cells} \\ \rightarrow 461960 \end{array} \right\} \rightarrow \{4 \rightarrow 4.84455 \times 10^{-6}, 3 \rightarrow 0.999995\},$

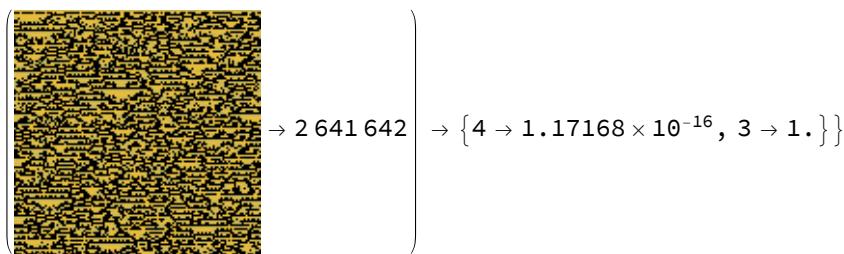
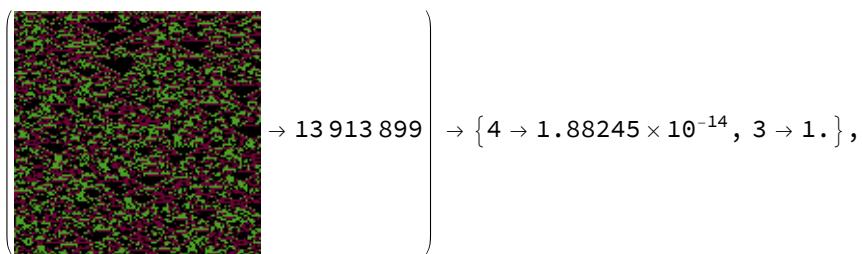
$\left\{ \begin{array}{l} \text{A 10x10 grid of blue, red, and black cells} \\ \rightarrow 4823863 \end{array} \right\} \rightarrow \{4 \rightarrow 1.80913 \times 10^{-22}, 3 \rightarrow 1.\},$

$\left\{ \begin{array}{l} \text{A 10x10 grid of green and black cells} \\ \rightarrow 7272180 \end{array} \right\} \rightarrow \{3 \rightarrow 3.43734 \times 10^{-9}, 4 \rightarrow 1.\},$

$\left\{ \begin{array}{l} \text{A 10x10 grid of blue and black cells} \\ \rightarrow 8672980 \end{array} \right\} \rightarrow \{4 \rightarrow 6.70981 \times 10^{-6}, 3 \rightarrow 0.999993\},$

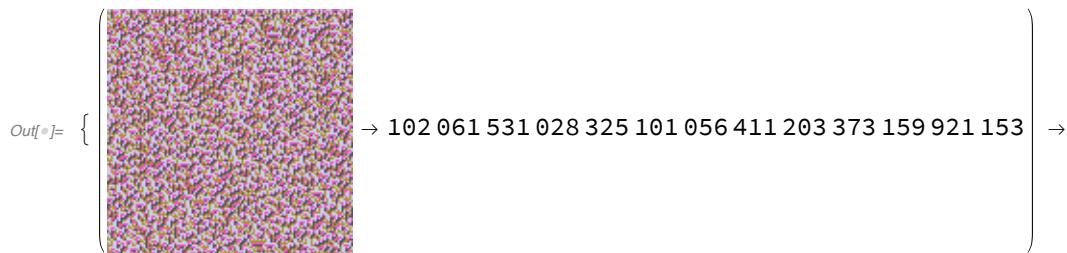
$\left\{ \begin{array}{l} \text{A 10x10 grid of pink and black cells} \\ \rightarrow 254357 \end{array} \right\} \rightarrow \{4 \rightarrow 2.17773 \times 10^{-6}, 3 \rightarrow 0.999998\},$

$\left\{ \begin{array}{l} \text{A 10x10 grid of green and black cells} \\ \rightarrow 9226537 \end{array} \right\} \rightarrow \{4 \rightarrow 1.70317 \times 10^{-12}, 3 \rightarrow 1.\},$

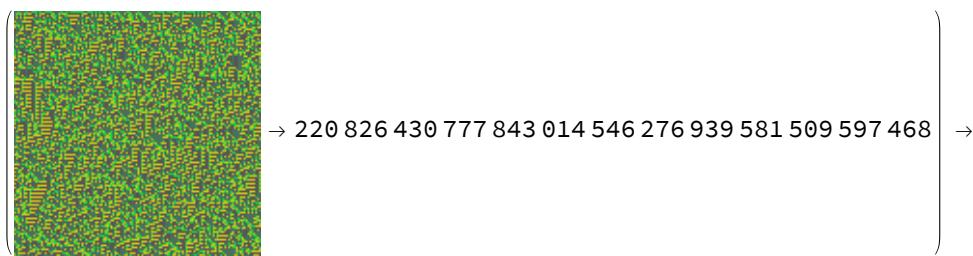


4-colour non-totalistic, range 1

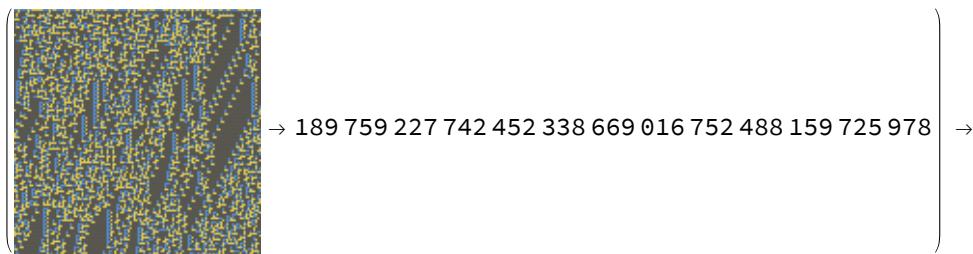
```
In[]:= test4Data4kr1C18 = datak4r1NT[128, 128, 8];
Thread[
  test4Data4kr1C18 → netECA18[Keys@test4Data4kr1C18, {"TopProbabilities", 2}]]
```



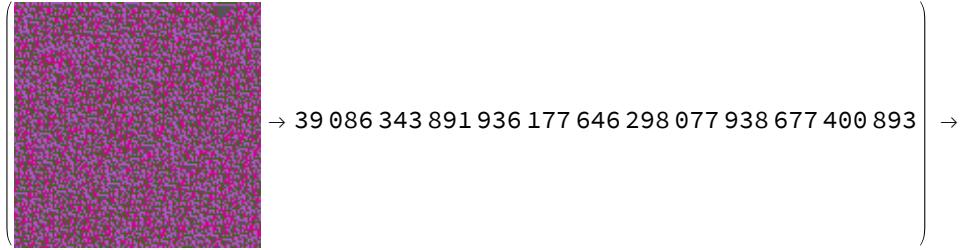
$\{4 \rightarrow 1.52655 \times 10^{-6}, 3 \rightarrow 0.999998\}$,



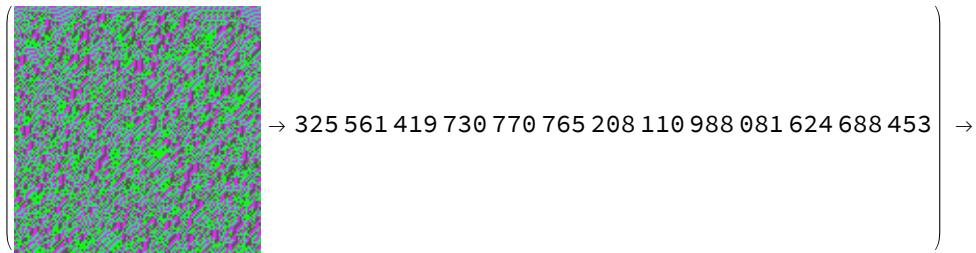
$\{4 \rightarrow 3.71156 \times 10^{-15}, 3 \rightarrow 1.\}$,



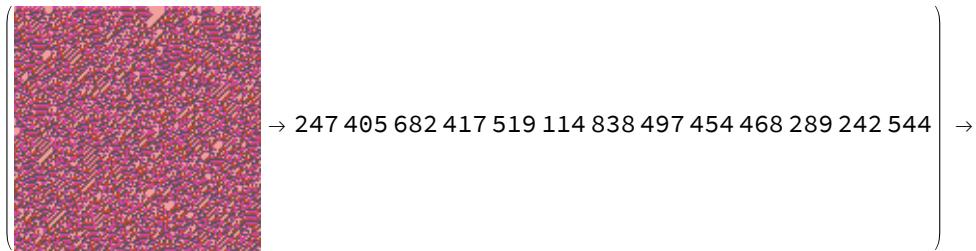
$$\{3 \rightarrow 1.71606 \times 10^{-19}, 4 \rightarrow 1.\},$$



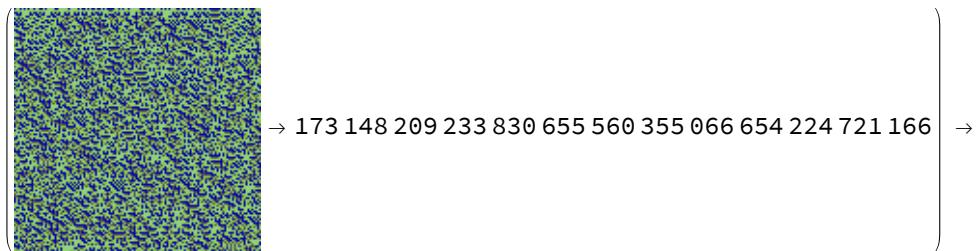
$$\{4 \rightarrow 0.0000617923, 3 \rightarrow 0.999938\},$$



$$\{4 \rightarrow 4.25321 \times 10^{-7}, 3 \rightarrow 1.\},$$



$$\{4 \rightarrow 3.94091 \times 10^{-12}, 3 \rightarrow 1.\},$$



$$\{4 \rightarrow 1.19081 \times 10^{-14}, 3 \rightarrow 1.\},$$



$$\{3 \rightarrow 2.26679 \times 10^{-10}, 4 \rightarrow 1.\}$$

4-colour totalistic, range 2

```
In[]:= test4Data4kr2C18 = datak4r2C[128, 128, 8];
Thread[
  test4Data4kr2C18 → netECA18[Keys@test4Data4kr2C18, {"TopProbabilities", 2}]]
```

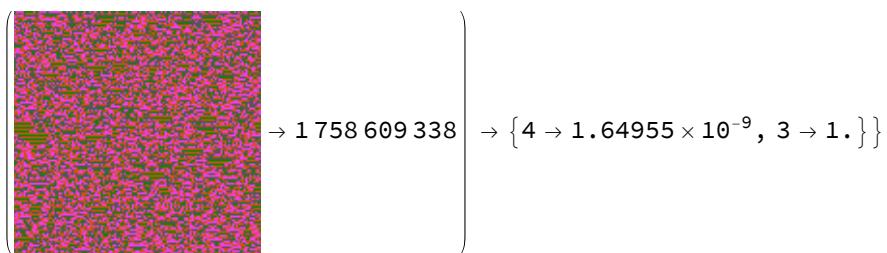
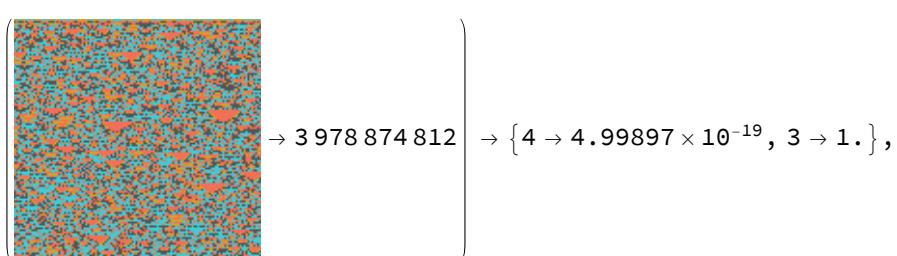
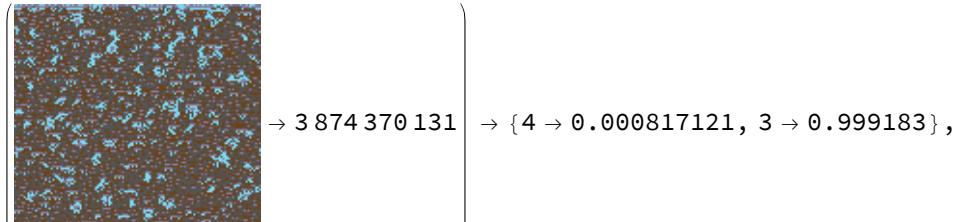
Out[]:= $\left\{ \begin{array}{l} \text{A 128x128 grid of dots in blue, yellow, and red colors.} \\ \rightarrow 3511876239 \end{array} \right\} \rightarrow \{2 \rightarrow 1.5807 \times 10^{-10}, 4 \rightarrow 1.\},$

Out[]:= $\left\{ \begin{array}{l} \text{A 128x128 grid showing a complex, symmetric pattern of yellow, green, and black cells.} \\ \rightarrow 1629765289 \end{array} \right\} \rightarrow \{4 \rightarrow 1.84811 \times 10^{-17}, 3 \rightarrow 1.\},$

Out[]:= $\left\{ \begin{array}{l} \text{A 128x128 grid showing a dense, noisy pattern of orange, red, and purple cells.} \\ \rightarrow 3309785711 \end{array} \right\} \rightarrow \{4 \rightarrow 5.75659 \times 10^{-20}, 3 \rightarrow 1.\},$

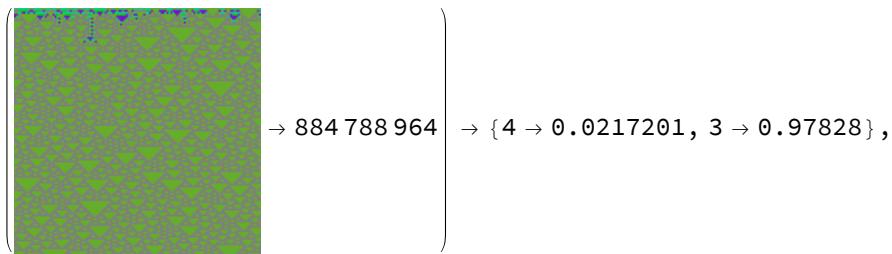
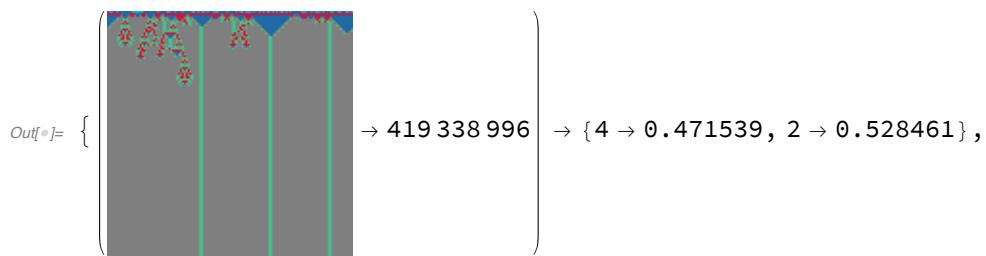
Out[]:= $\left\{ \begin{array}{l} \text{A 128x128 grid showing a sparse, scattered pattern of cyan and black cells.} \\ \rightarrow 521880538 \end{array} \right\} \rightarrow \{4 \rightarrow 2.42952 \times 10^{-8}, 3 \rightarrow 1.\},$

Out[]:= $\left\{ \begin{array}{l} \text{A 128x128 grid showing a highly irregular, noisy pattern of black, green, and yellow cells.} \\ \rightarrow 2882903289 \end{array} \right\} \rightarrow \{4 \rightarrow 0.00262183, 3 \rightarrow 0.997378\},$



5-colour totalistic, range 1

```
In[]:= test4Data5kr1C18 = data5T2C[8, 128, 128];
Thread[
  test4Data5kr1C18 → netECA18[Keys@test4Data5kr1C18, {"TopProbabilities", 2}]]
```



$$\left(\begin{array}{c} \text{[A 2x2 grid of random colors]} \\ \rightarrow 743\ 542\ 029 \end{array} \right) \rightarrow \{3 \rightarrow 1.08355 \times 10^{-9}, 4 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[A 2x2 grid of random colors]} \\ \rightarrow 782\ 108\ 342 \end{array} \right) \rightarrow \{4 \rightarrow 3.73846 \times 10^{-6}, 3 \rightarrow 0.999996\},$$

$$\left(\begin{array}{c} \text{[A 2x2 grid of random colors]} \\ \rightarrow 785\ 621\ 045 \end{array} \right) \rightarrow \{4 \rightarrow 1.13554 \times 10^{-10}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[A 2x2 grid of random colors]} \\ \rightarrow 540\ 834\ 160 \end{array} \right) \rightarrow \{4 \rightarrow 0.0000100212, 3 \rightarrow 0.99999\},$$

$$\left(\begin{array}{c} \text{[A 2x2 grid of random colors]} \\ \rightarrow 1\ 180\ 125\ 611 \end{array} \right) \rightarrow \{3 \rightarrow 8.69272 \times 10^{-10}, 4 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[A 2x2 grid of random colors]} \\ \rightarrow 604\ 699\ 906 \end{array} \right) \rightarrow \{4 \rightarrow 5.02809 \times 10^{-11}, 3 \rightarrow 1.\}$$

6-colour totalistic, range 1

```
In[]:= test4Data6kr1C18 = data6TC[8, 128, 128];
Thread[
  test4Data6kr1C18 → netECA18[Keys@test4Data6kr1C18, {"TopProbabilities", 2}]]
```

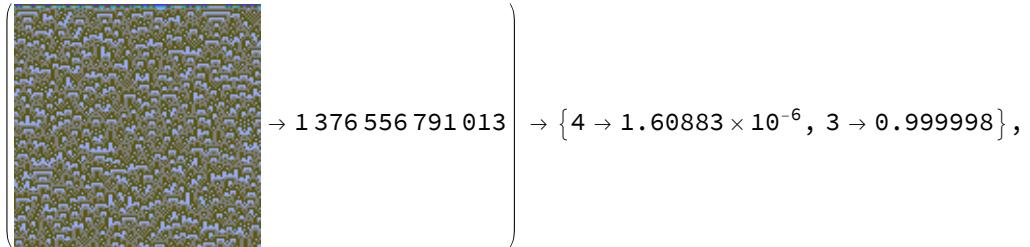
Out[]:= $\left\{ \begin{array}{c} \text{A 128x128 grid of 6 colors (red, blue, green, yellow, cyan, magenta) showing a sparse pattern of red cells.} \\ \rightarrow 1\ 598\ 104\ 240\ 744 \end{array} \right\} \rightarrow \{4 \rightarrow 0.385354, 3 \rightarrow 0.614646\},$

$\left\{ \begin{array}{c} \text{A 128x128 grid of 6 colors showing a more complex, dense pattern of red, blue, and yellow cells.} \\ \rightarrow 2\ 744\ 610\ 103\ 617 \end{array} \right\} \rightarrow \{4 \rightarrow 4.14684 \times 10^{-12}, 3 \rightarrow 1.\},$

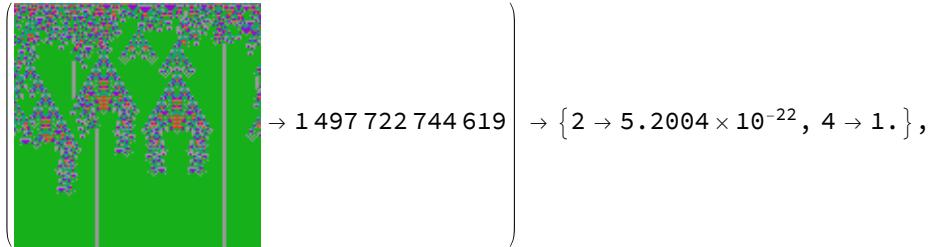
$\left\{ \begin{array}{c} \text{A 128x128 grid of 6 colors showing a very dense and noisy pattern of all six colors.} \\ \rightarrow 2\ 679\ 723\ 007\ 553 \end{array} \right\} \rightarrow \{4 \rightarrow 0.0146554, 3 \rightarrow 0.985345\},$

$\left\{ \begin{array}{c} \text{A 128x128 grid of 6 colors showing a uniform distribution of all six colors.} \\ \rightarrow 333\ 206\ 194\ 422 \end{array} \right\} \rightarrow \{4 \rightarrow 1.77212 \times 10^{-6}, 3 \rightarrow 0.999998\},$

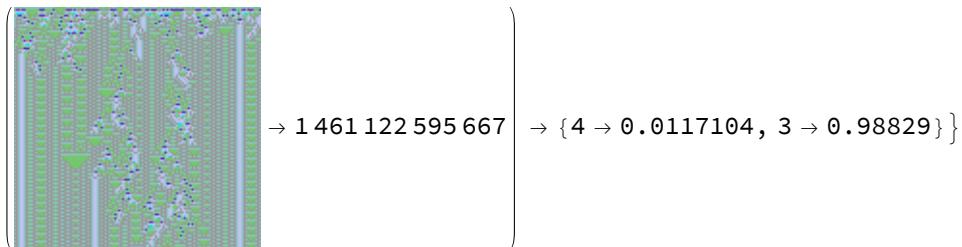
$\left\{ \begin{array}{c} \text{A 128x128 grid of 6 colors showing a sparse pattern of cyan and magenta cells.} \\ \rightarrow 385\ 745\ 608\ 648 \end{array} \right\} \rightarrow \{4 \rightarrow 4.96414 \times 10^{-18}, 3 \rightarrow 1.\},$



$\rightarrow \{4 \rightarrow 1.60883 \times 10^{-6}, 3 \rightarrow 0.999998\},$



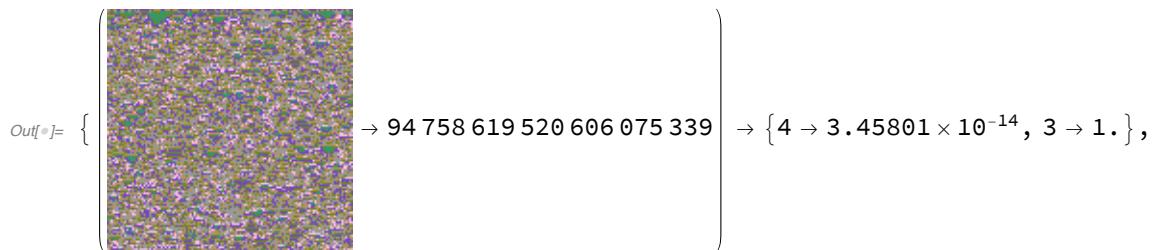
$\rightarrow \{2 \rightarrow 5.2004 \times 10^{-22}, 4 \rightarrow 1.\},$



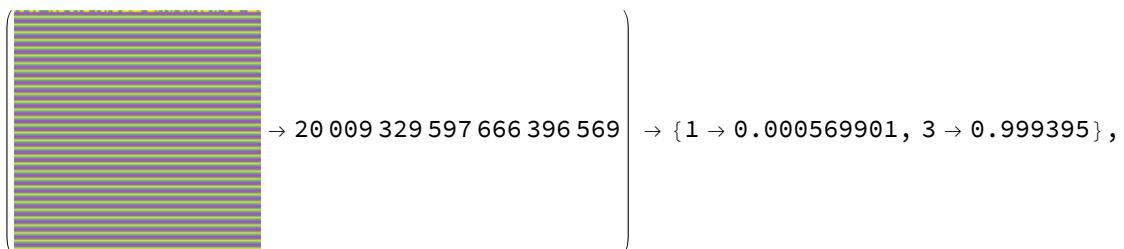
$\rightarrow \{4 \rightarrow 0.0117104, 3 \rightarrow 0.98829\}\}$

6-colour totalistic, range 2

```
In[]:= test4Data6kr2C18 = data6T2C[8, 128, 128];
Thread[
  test4Data6kr2C18 &gt;> netECA18[Keys@test4Data6kr2C18, {"TopProbabilities", 2}]]
```



$\rightarrow \{4 \rightarrow 3.45801 \times 10^{-14}, 3 \rightarrow 1.\},$



$\rightarrow \{1 \rightarrow 0.000569901, 3 \rightarrow 0.999395\},$

$$\left(\begin{array}{c} \text{[A 4x4 grid of green and blue dots]} \\ \rightarrow 143\ 751\ 744\ 015\ 528\ 766\ 387 \end{array} \right) \rightarrow \{4 \rightarrow 4.63781 \times 10^{-12}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[A 4x4 grid of green and blue dots]} \\ \rightarrow 14\ 907\ 007\ 420\ 911\ 525\ 245 \end{array} \right) \rightarrow \{4 \rightarrow 2.71632 \times 10^{-7}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[A 4x4 grid of green, blue, and yellow dots]} \\ \rightarrow 153\ 725\ 842\ 134\ 059\ 084\ 151 \end{array} \right) \rightarrow \{4 \rightarrow 8.53867 \times 10^{-11}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[A 4x4 grid of red, blue, and green dots]} \\ \rightarrow 21\ 849\ 107\ 846\ 366\ 361\ 856 \end{array} \right) \rightarrow \{4 \rightarrow 4.26147 \times 10^{-8}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[A 4x4 grid of green and blue dots]} \\ \rightarrow 39\ 897\ 609\ 306\ 289\ 130\ 946 \end{array} \right) \rightarrow \{4 \rightarrow 3.43225 \times 10^{-8}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[A 4x4 grid of red and green dots]} \\ \rightarrow 24\ 452\ 844\ 112\ 980\ 510\ 505 \end{array} \right) \rightarrow \{3 \rightarrow 2.30799 \times 10^{-17}, 4 \rightarrow 1.\}\}$$

7-colour totalistic, range 1

```
In[]:= test4Data7kr1C18 = data7TC[8, 128, 128];
Thread[
  test4Data7kr1C18 → netECA18[Keys@test4Data7kr1C18, {"TopProbabilities", 2}]]
```

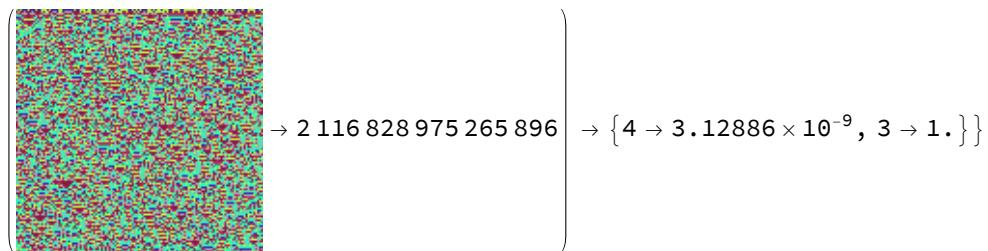
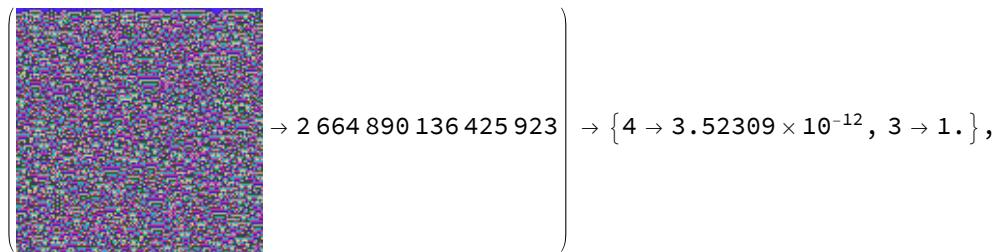
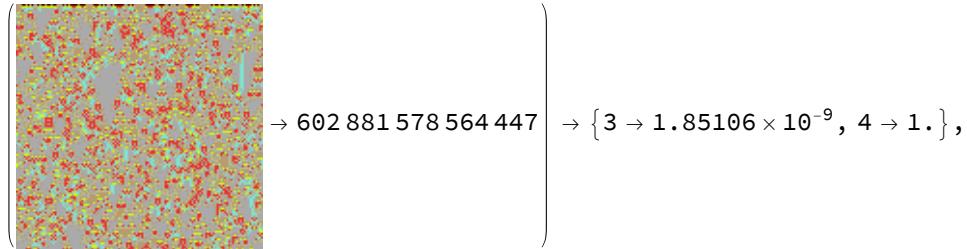
Out[]:= $\left\{ \begin{array}{c} \text{[A 128x128 grid of 7 colors]} \\ \rightarrow 9377524399313965 \end{array} \right\} \rightarrow \{3 \rightarrow 1.74389 \times 10^{-8}, 4 \rightarrow 1.\},$

Out[]:= $\left\{ \begin{array}{c} \text{[A 128x128 grid of 7 colors]} \\ \rightarrow 4962953862340599 \end{array} \right\} \rightarrow \{4 \rightarrow 0.0137316, 3 \rightarrow 0.986268\},$

Out[]:= $\left\{ \begin{array}{c} \text{[A 128x128 grid of 7 colors]} \\ \rightarrow 8745570953687246 \end{array} \right\} \rightarrow \{4 \rightarrow 2.19284 \times 10^{-7}, 3 \rightarrow 1.\},$

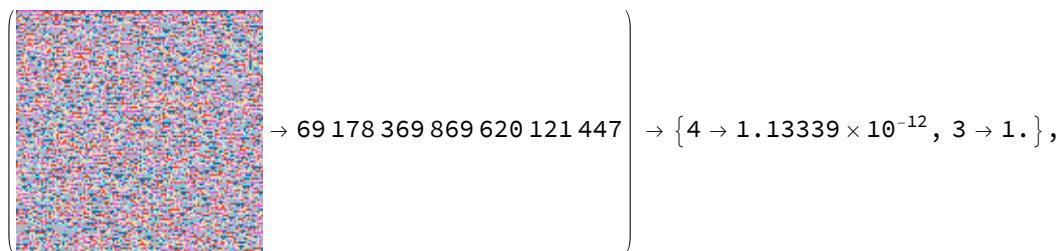
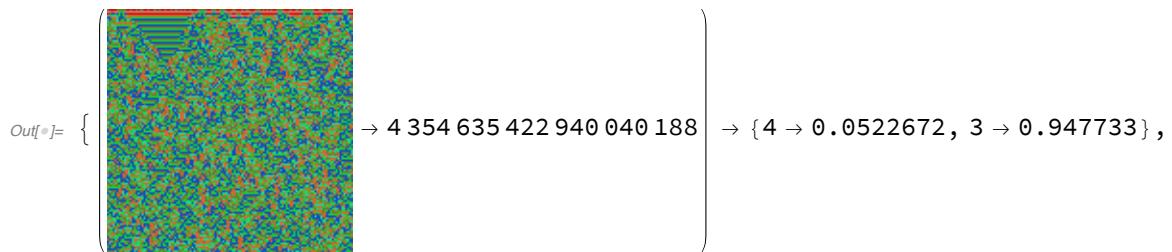
Out[]:= $\left\{ \begin{array}{c} \text{[A 128x128 grid of 7 colors]} \\ \rightarrow 5868018872447407 \end{array} \right\} \rightarrow \{4 \rightarrow 0.000111761, 3 \rightarrow 0.999888\},$

Out[]:= $\left\{ \begin{array}{c} \text{[A 128x128 grid of 7 colors]} \\ \rightarrow 4309418628605253 \end{array} \right\} \rightarrow \{4 \rightarrow 1.75407 \times 10^{-6}, 3 \rightarrow 0.999998\},$



8-colour totalistic, range 1

```
In[8]:= test4Data8kr1C18 = data8TC[8, 128, 128];
Thread[
  test4Data8kr1C18 → netECA18[Keys@test4Data8kr1C18, {"TopProbabilities", 2}]]
```



$$\left(\begin{array}{c} \text{Image 1: A 10x10 grid with various colored cells (red, green, blue, yellow, purple)} \\ \rightarrow 52\ 954\ 223\ 906\ 783\ 093\ 008 \end{array} \right) \rightarrow \{3 \rightarrow 7.29147 \times 10^{-15}, 4 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image 2: A 10x10 grid with mostly red and green cells, some blue and yellow} \\ \rightarrow 68\ 658\ 165\ 468\ 973\ 438\ 000 \end{array} \right) \rightarrow \{4 \rightarrow 1.9166 \times 10^{-11}, 3 \rightarrow 1.\},$$

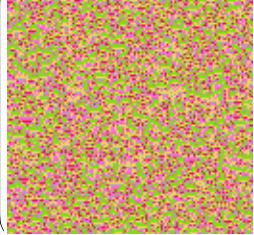
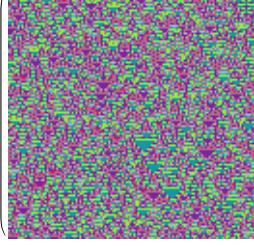
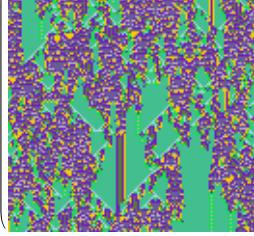
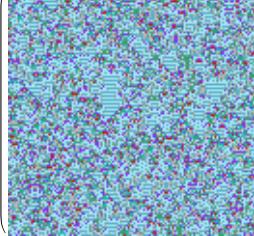
$$\left(\begin{array}{c} \text{Image 3: A 10x10 grid with mostly blue and green cells, some red and yellow} \\ \rightarrow 40\ 882\ 704\ 313\ 683\ 534\ 715 \end{array} \right) \rightarrow \{4 \rightarrow 0.0000183002, 3 \rightarrow 0.999982\},$$

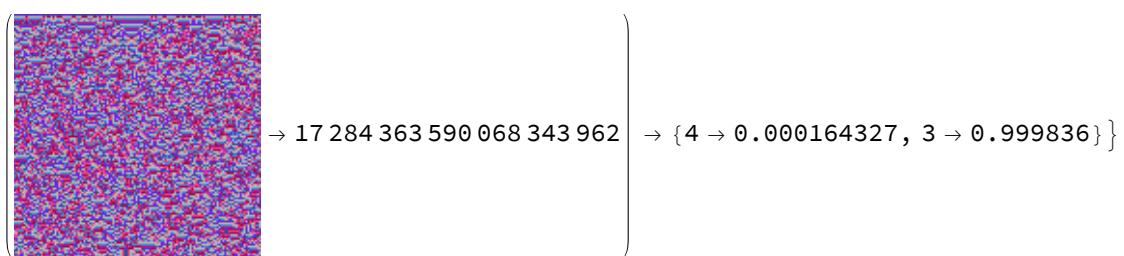
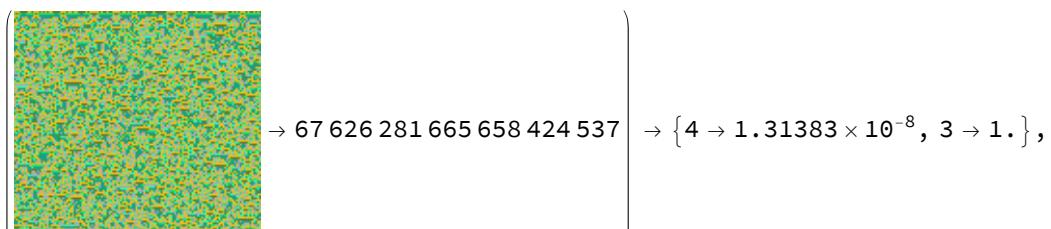
$$\left(\begin{array}{c} \text{Image 4: A 10x10 grid with mostly green and blue cells, some red and yellow} \\ \rightarrow 4\ 334\ 236\ 228\ 138\ 547\ 400 \end{array} \right) \rightarrow \{4 \rightarrow 1.8216 \times 10^{-12}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{Image 5: A 10x10 grid with mostly yellow and green cells, some red and blue} \\ \rightarrow 38\ 056\ 813\ 477\ 139\ 716\ 563 \end{array} \right) \rightarrow \{4 \rightarrow 0.025224, 3 \rightarrow 0.974776\},$$

$$\left(\begin{array}{c} \text{Image 6: A 10x10 grid with mostly purple and yellow cells, some red and blue} \\ \rightarrow 17\ 144\ 034\ 197\ 046\ 476\ 300 \end{array} \right) \rightarrow \{4 \rightarrow 1.1918 \times 10^{-10}, 3 \rightarrow 1.\}$$

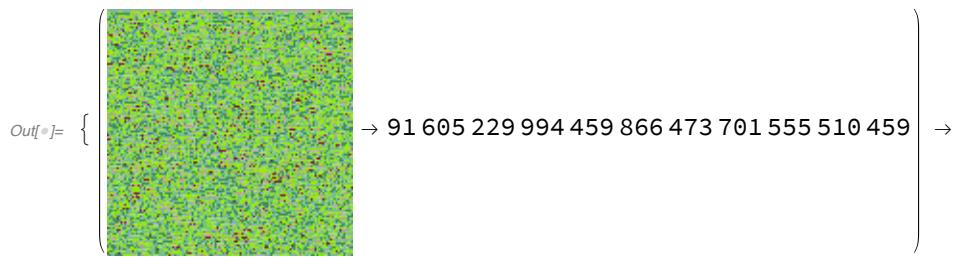
```
In[8]:= test4Data8kr1C18 = data8TC[8, 128, 128];
Thread[
  test4Data8kr1C18 → netECA18[Keys@test4Data8kr1C18, {"TopProbabilities", 2}]]
```

Out[8]= { → 27 295 602 810 117 462 452,  → 68 187 226 482 692 112 227,  → 26 338 422 679 712 858 793,  → 20 106 191 194 925 098 456,  → 27 427 530 853 867 733 909}

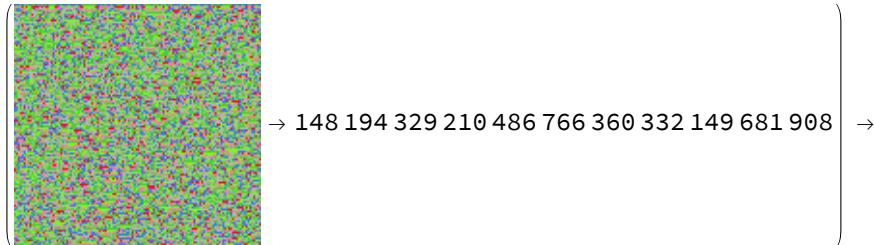


8-colour totalistic, range 2

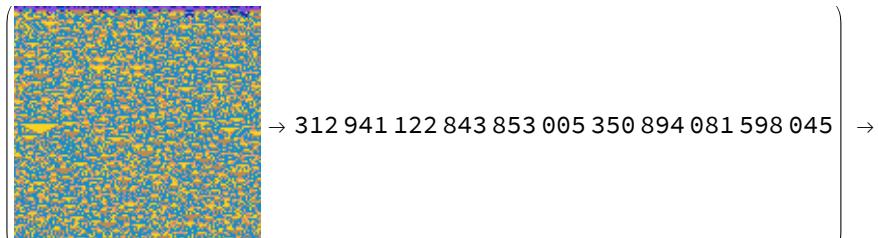
```
In[]:= test4Data8kr2C18 = data8T2C[8, 128, 128];
Thread[
  test4Data8kr2C18 \rightarrow netECA18[Keys@test4Data8kr2C18, {"TopProbabilities", 2}]]
```



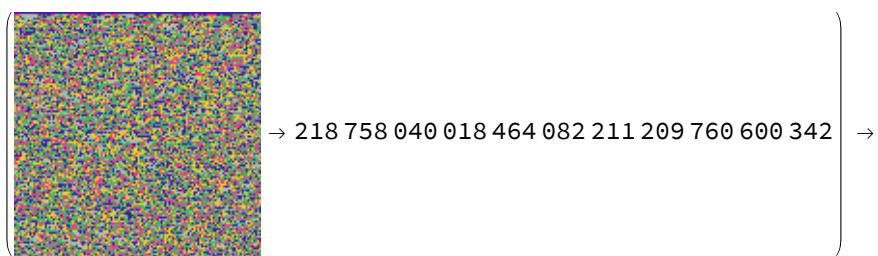
$$\{4 \rightarrow 8.95721 \times 10^{-9}, 3 \rightarrow 1.\},$$



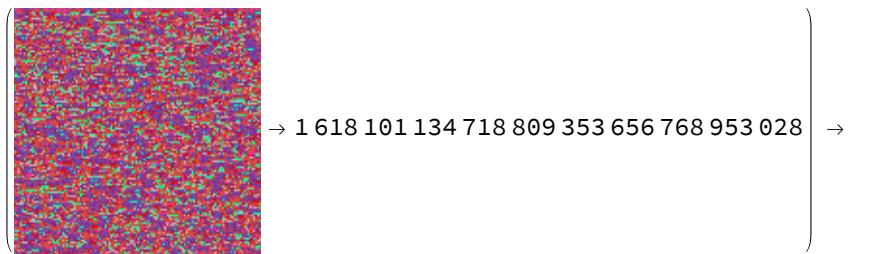
$$\{4 \rightarrow 0.000259168, 3 \rightarrow 0.999741\},$$



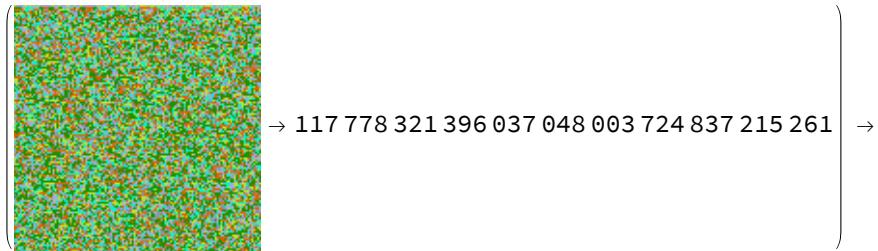
$\{4 \rightarrow 3.01437 \times 10^{-25}, 3 \rightarrow 1.\},$



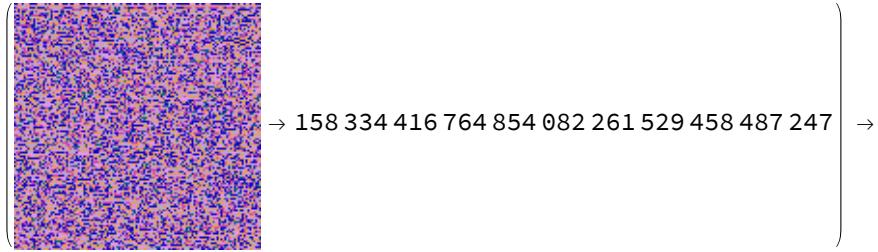
$\{4 \rightarrow 1.84707 \times 10^{-6}, 3 \rightarrow 0.999998\},$



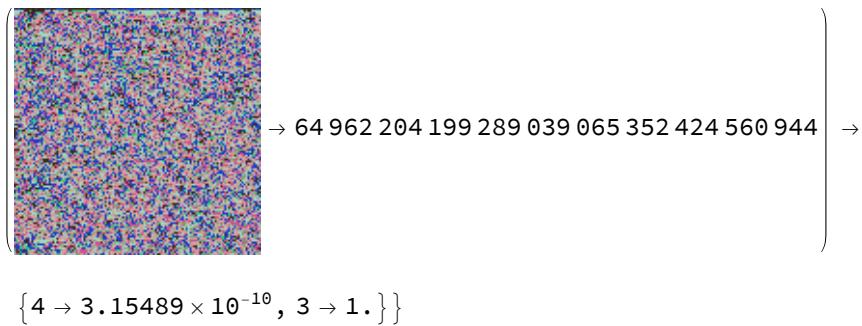
$\{4 \rightarrow 8.91462 \times 10^{-12}, 3 \rightarrow 1.\},$



$\{4 \rightarrow 1.56349 \times 10^{-7}, 3 \rightarrow 1.\},$

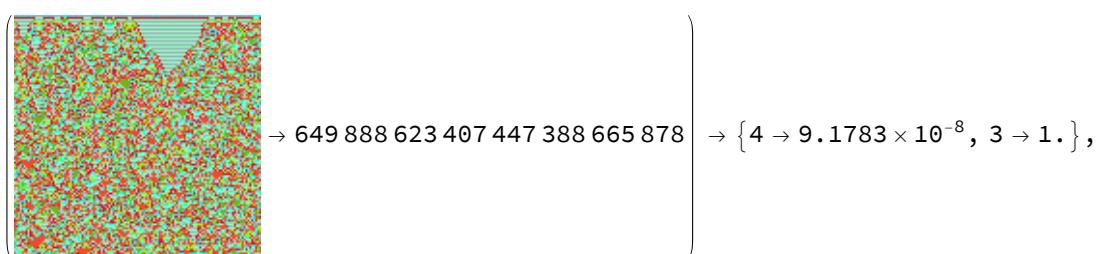
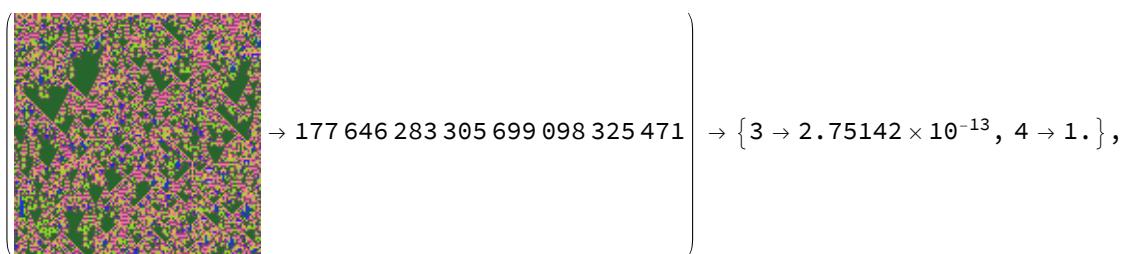
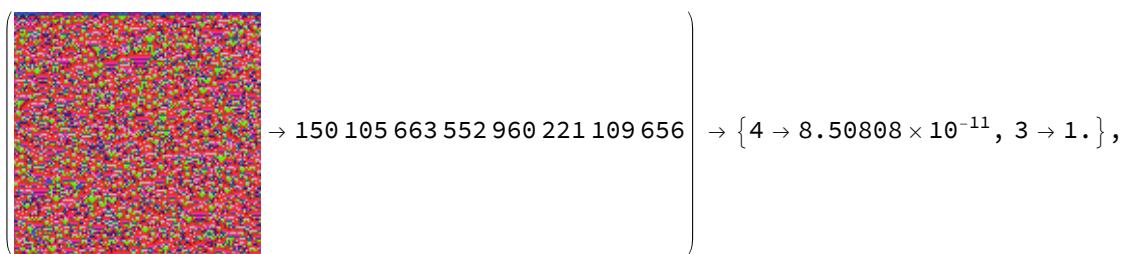
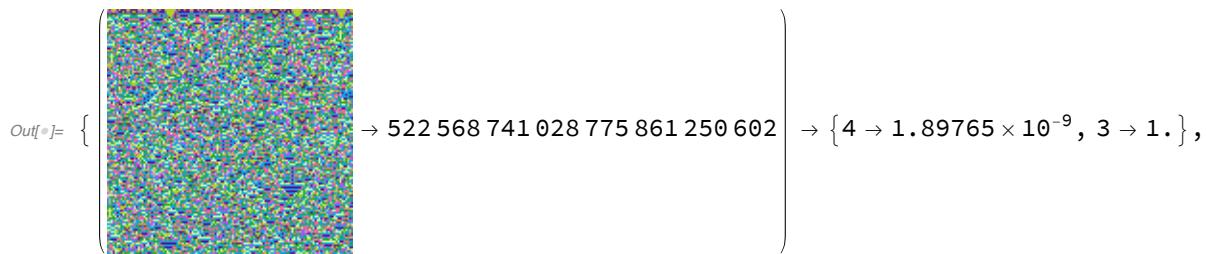


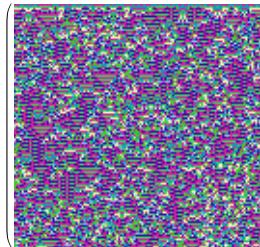
$\{3 \rightarrow 0.381514, 4 \rightarrow 0.618486\},$

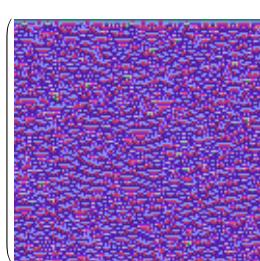


9-colour totalistic, range 1

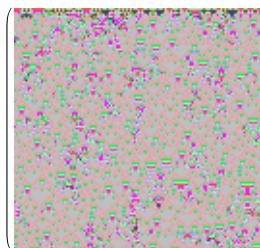
```
In[8]:= test4Data9kr1C18 = data9TC[8, 128, 128];
Thread[
  test4Data9kr1C18 &gt;> netECA18[Keys@test4Data9kr1C18, {"TopProbabilities", 2}]]
```



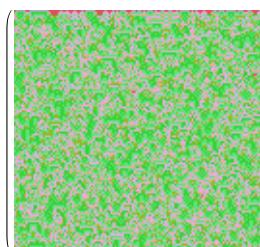

 $\rightarrow 572\ 736\ 978\ 221\ 231\ 214\ 545\ 140 \quad \left. \right\} \rightarrow \{4 \rightarrow 1.19931 \times 10^{-8}, 3 \rightarrow 1.\},$


 $\rightarrow 577\ 735\ 506\ 397\ 144\ 743\ 916\ 701 \quad \left. \right\} \rightarrow$

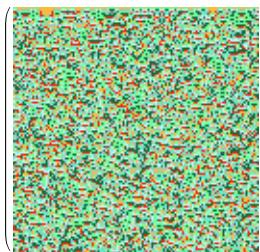
$\{4 \rightarrow 5.16186 \times 10^{-6}, 3 \rightarrow 0.999995\},$

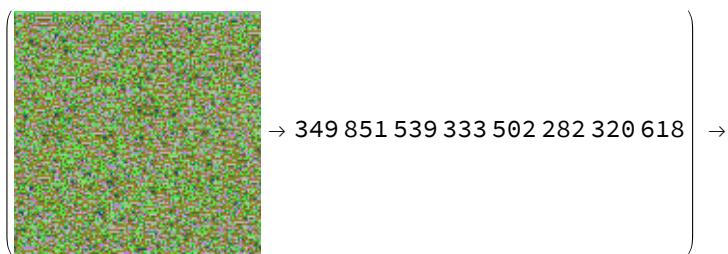
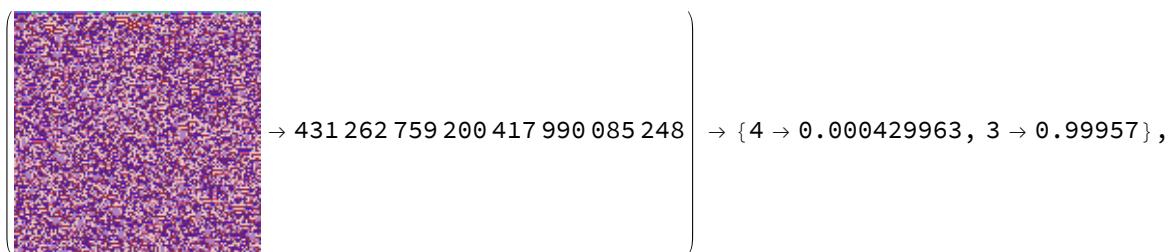
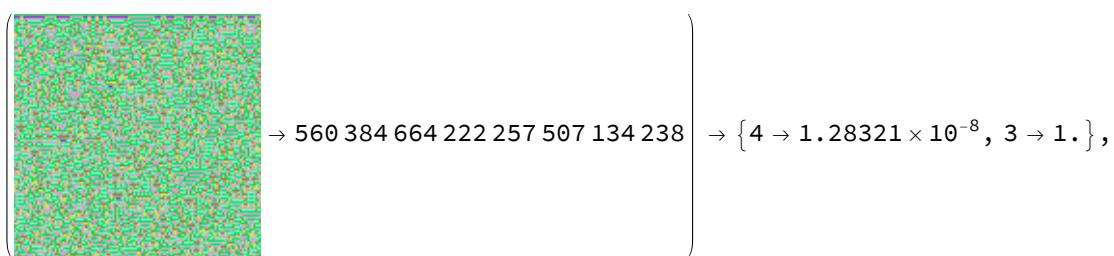
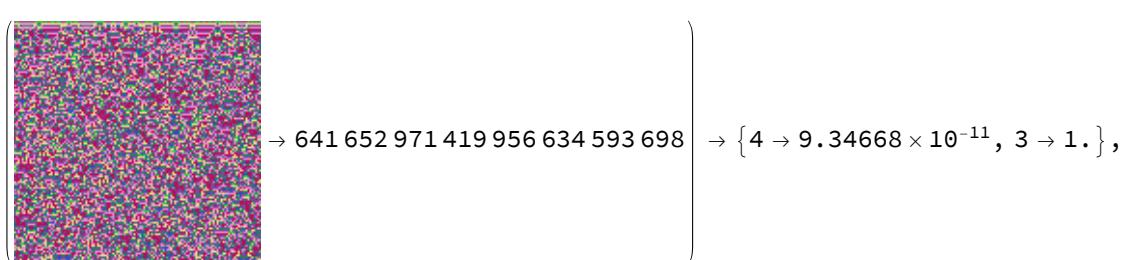
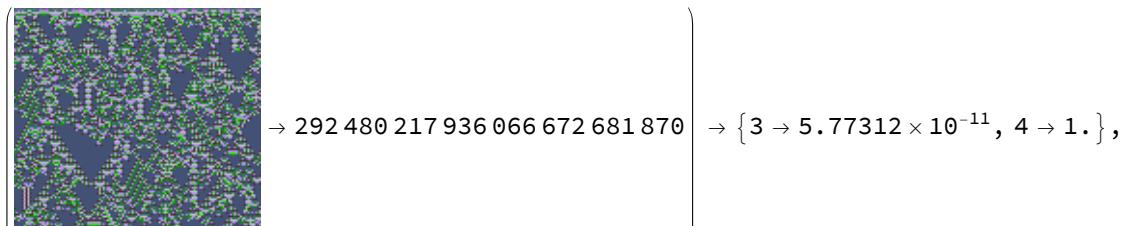

 $\rightarrow 38\ 290\ 460\ 957\ 561\ 945\ 226\ 664 \quad \left. \right\} \rightarrow$

$\{4 \rightarrow 0.0000332421, 3 \rightarrow 0.999967\},$

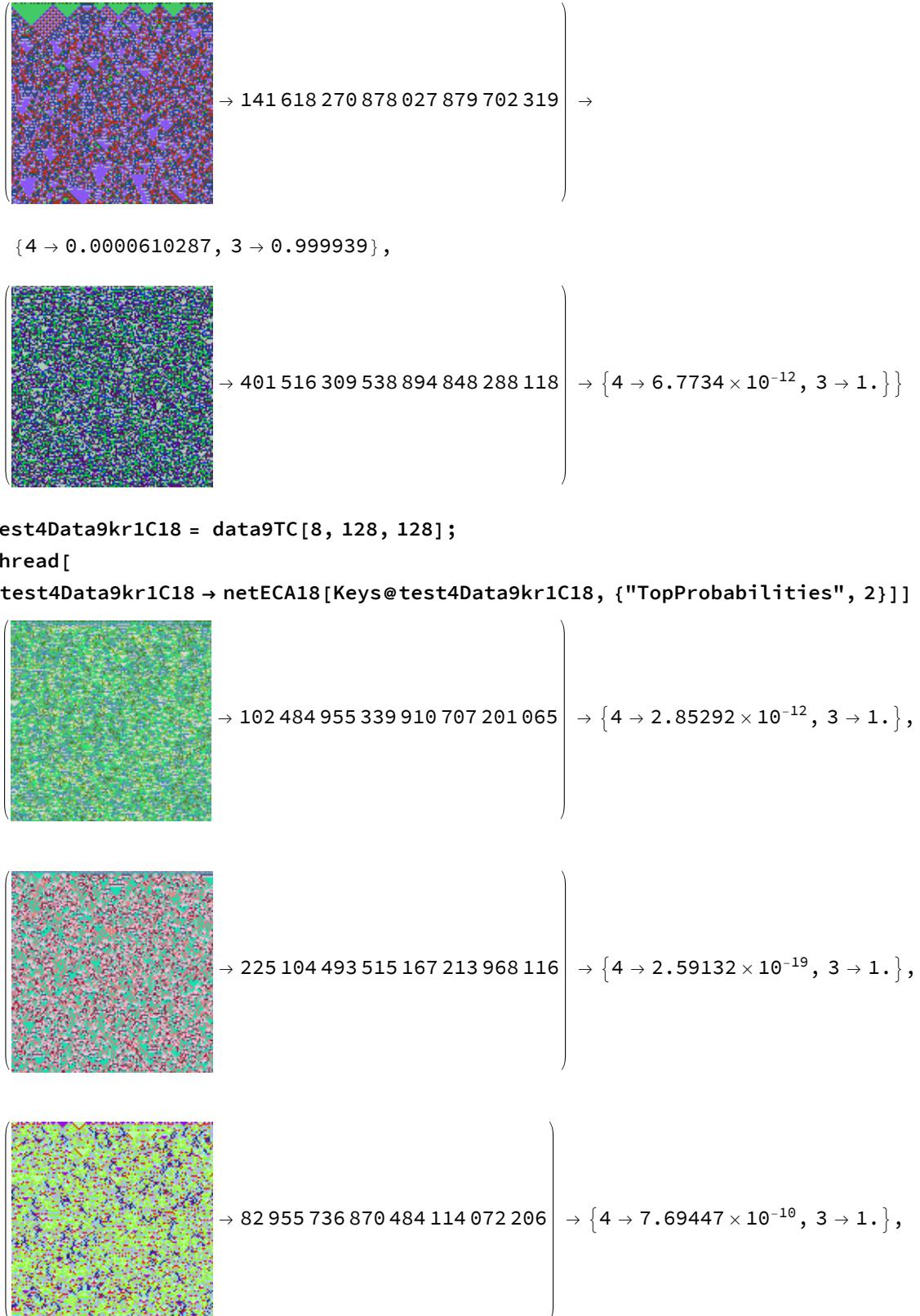

 $\rightarrow 65\ 266\ 980\ 214\ 577\ 653\ 296\ 276 \quad \left. \right\} \rightarrow \{4 \rightarrow 2.0037 \times 10^{-9}, 3 \rightarrow 1.\}$

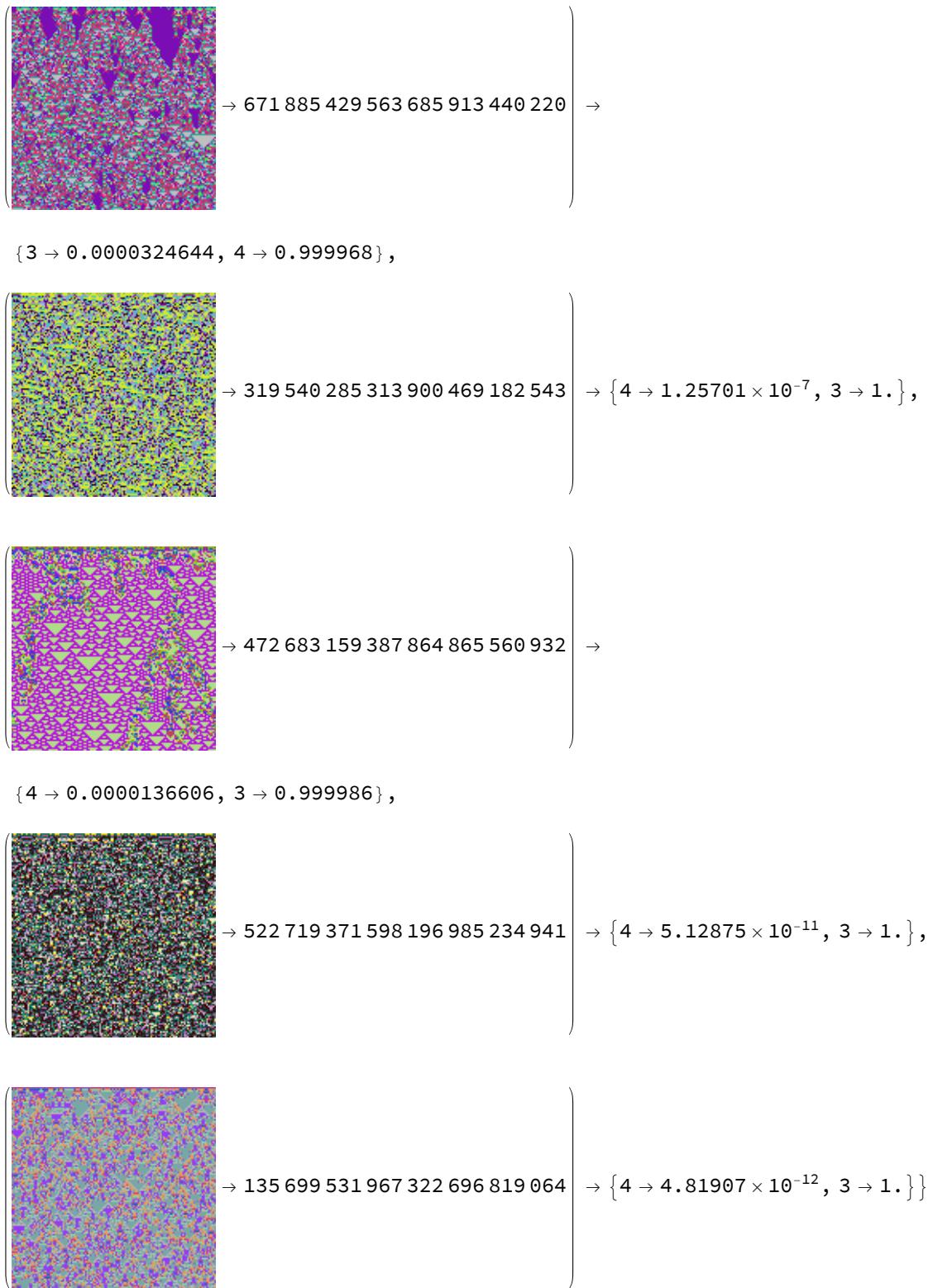
```
In[6]:= test4Data9kr1C18 = data9TC[8, 128, 128];
Thread[
  test4Data9kr1C18 \[Function] netECA18[Keys@test4Data9kr1C18, {"TopProbabilities", 2}]]
```


 $\rightarrow 376\ 251\ 875\ 419\ 739\ 043\ 750\ 089 \quad \left. \right\} \rightarrow \{4 \rightarrow 8.56952 \times 10^{-8}, 3 \rightarrow 1.\},$



$\{4 \rightarrow 5.50927 \times 10^{-7}, 3 \rightarrow 0.999999\},$

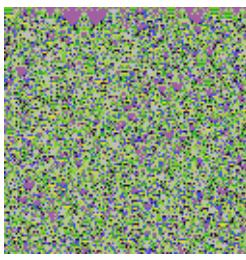


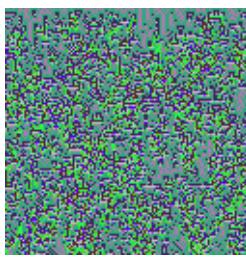


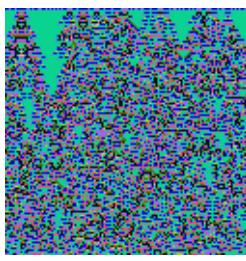
```

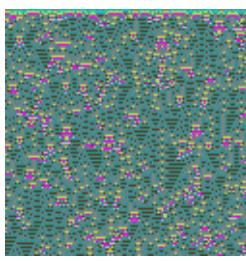
In[313]:= test4Data9kr1C18 = data9TC[8, 128, 128];
test4Data9kr1C18labeled = Thread[Labeled[
  Keys@test4Data9kr1C18, Values@test4Data9kr1C18, LabelStyle -> Small]];
Thread[test4Data9kr1C18labeled -> netECA18[Keys@test4Data9kr1C18,
 {"TopProbabilities", 2}]]

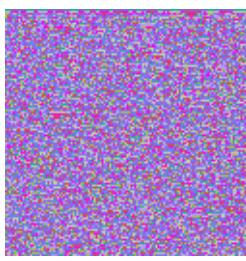
```

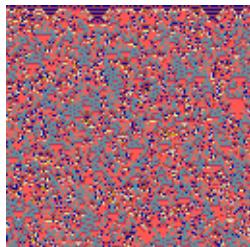
Out[315]= 
 $\rightarrow \{4 \rightarrow 3.42626 \times 10^{-14}, 3 \rightarrow 1.\},$
349 053 945 078 960 182 984 058


 $\rightarrow \{4 \rightarrow 2.76129 \times 10^{-8}, 3 \rightarrow 1.\},$
436 609 066 684 808 759 301 987


 $\rightarrow \{3 \rightarrow 3.31294 \times 10^{-20}, 4 \rightarrow 1.\},$
109 306 125 150 234 096 172 548

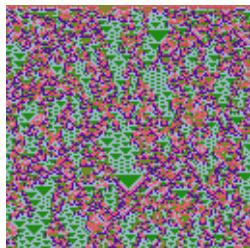

 $\rightarrow \{4 \rightarrow 0.00193157, 3 \rightarrow 0.998068\},$
418 672 174 548 024 537 683 242


 $\rightarrow \{4 \rightarrow 5.19538 \times 10^{-7}, 3 \rightarrow 0.999999\},$
384 634 547 406 938 511 788 486



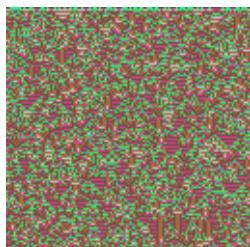
$\rightarrow \{ 4 \rightarrow 6.78179 \times 10^{-9}, 3 \rightarrow 1. \},$

395 758 960 768 423 349 691 715



$\rightarrow \{ 4 \rightarrow 8.80994 \times 10^{-6}, 3 \rightarrow 0.999991 \},$

396 890 553 438 981 909 112 518



$\rightarrow \{ 4 \rightarrow 0.00035471, 3 \rightarrow 0.999645 \} \}$

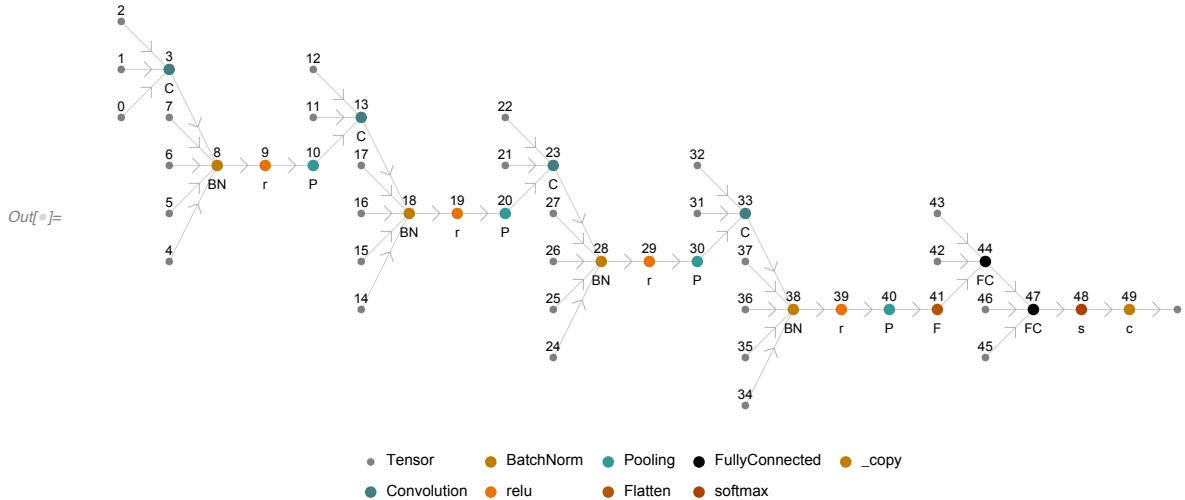
221 637 308 166 169 056 395 230

Network XIX - Four convolutions, dropout on linear only, BatchNorm, MaxPool

In[⑩]:= **netECA19 = netElevenCC1024drop[128, 128]**

Out[⑩]= NetChain[Input	image
	conv1	array (size: 3 x 128 x 128)
	bat1	array (size: 48 x 126 x 126)
	ramp1	array (size: 48 x 126 x 126)
	pooling1	array (size: 48 x 126 x 126)
	conv2	array (size: 24 x 123 x 123)
	bat2	array (size: 24 x 123 x 123)
	ramp2	array (size: 24 x 123 x 123)
	pooling2	array (size: 24 x 122 x 122)
	conv3	array (size: 24 x 120 x 120)
	bat3	array (size: 24 x 120 x 120)
	ramp3	array (size: 24 x 120 x 120)
	pooling3	array (size: 24 x 119 x 119)
	conv4	array (size: 12 x 117 x 117)
	bat4	array (size: 12 x 117 x 117)
	ramp4	array (size: 12 x 117 x 117)
	pooling4	array (size: 12 x 116 x 116)
	flatten	vector (size: 161472)
	linear	vector (size: 1024)
	drop2	vector (size: 1024)
	linear2	vector (size: 4)
	softmax	vector (size: 4)
	Output	class

```
In[⑩]:= NetInformation[netECA19, "MXNetNodeGraphPlot"]
```



```
In[⑪]:= NetInformation[netECA19, "SummaryGraphic"]
```



```
In[⑫]:= dataECA19 = dataC[128, 128, 16 384];
```

```
In[⑬]:= dataTotalistic2BigC19 = genData2r2C[128, 128, 4096];
```

```
In[⑭]:= dataTotalistic3BigC19 = data3T2C[128, 128, 4096];
```

```
In[⑮]:= dataTotalistic4BigC19 = data4TC[128, 128, 4096];
```

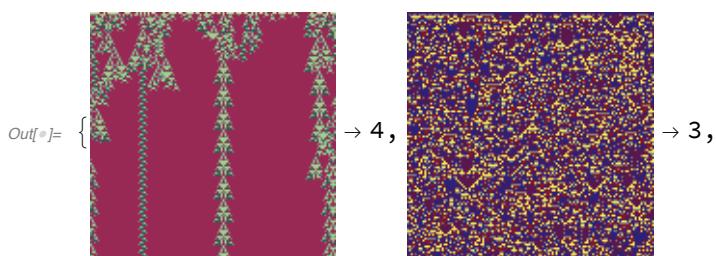
```
In[⑯]:= dataTotalistic5BigC19 = genData5TCC[128, 128, 16 384];
```

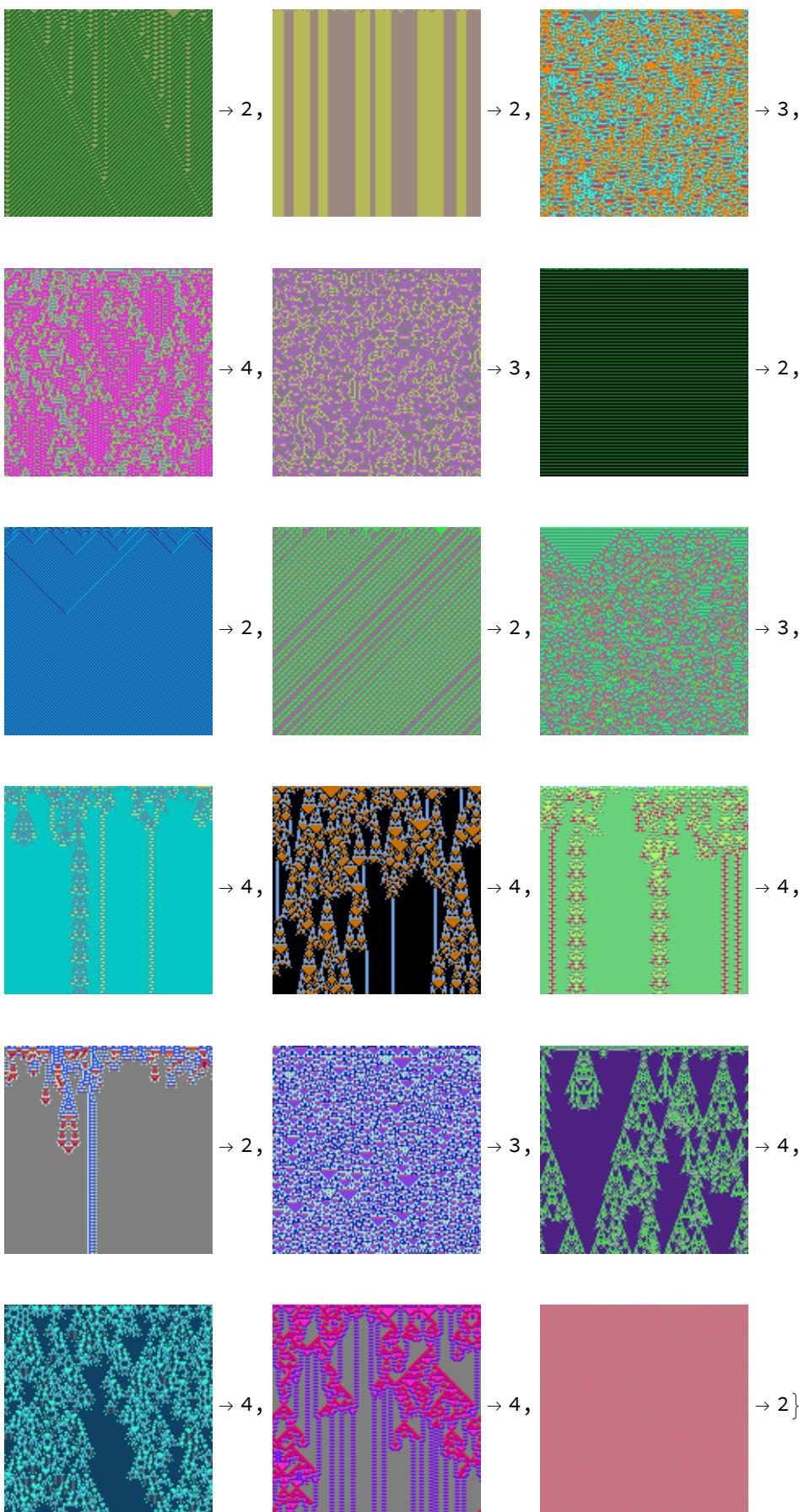
```
In[⑰]:= fullTrainingBigC19 = Join[dataECA19, dataTotalistic2BigC19,
    dataTotalistic3BigC19, dataTotalistic4BigC19, dataTotalistic5BigC19];
```

```
In[⑱]:= Length[fullTrainingBigC19]
```

```
Out[⑱]= 90112
```

```
In[⑲]:= RandomSample[fullTrainingBigC19, 20]
```





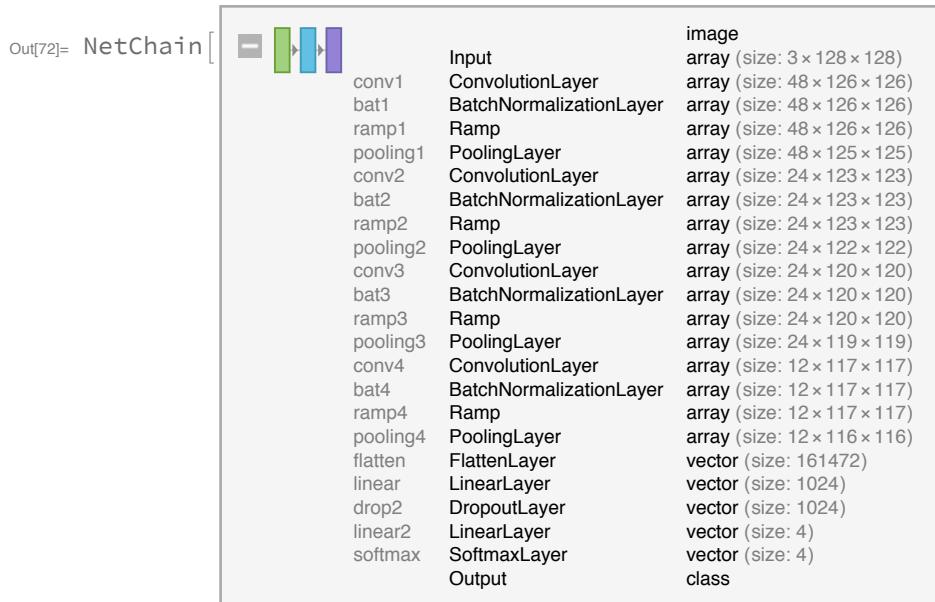
```
In[6]:= dir = SetDirectory[NotebookDirectory[]]
Out[6]= /home/esilverman/Documents

In[7]:= netECA19 = NetTrain[netECA19, fullTrainingBigC19,
  MaxTrainingRounds → 200, BatchSize → 256, TargetDevice → "GPU",
  TrainingProgressCheckpointing → {"Directory", dir}]
```

Generate test data for Network XIX (200 epochs)

```
In[71]:= dir = SetDirectory[NotebookDirectory[]]
Out[71]= /Users/thorsilver/Downloads/Wolfram notebooks
```

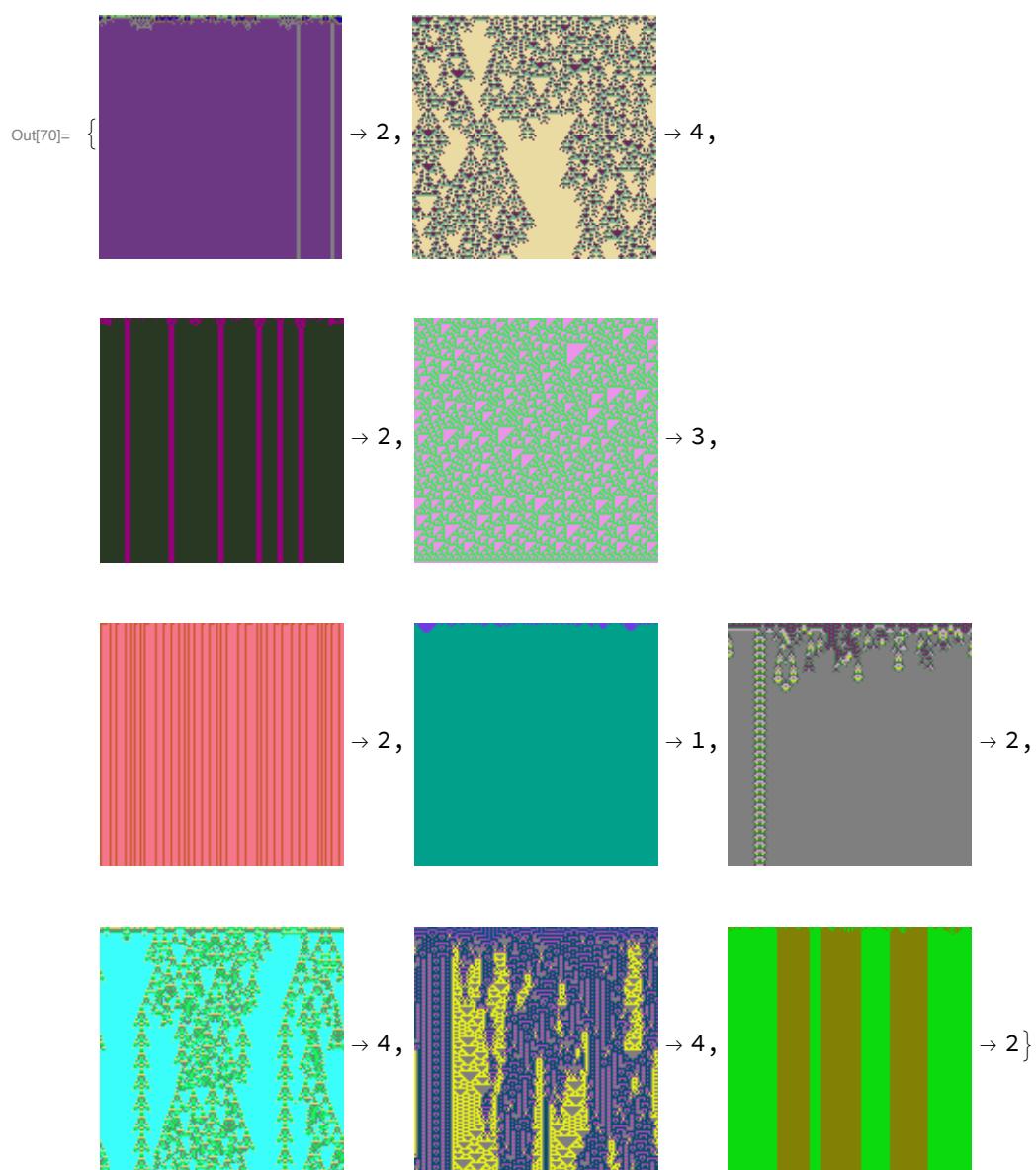
```
In[72]:= netECA19 = Import["netECA19-r200.wlnet"]
```



```
In[63]:= testDataECABigC = dataC[128, 128, 1024];
testData2TBigC = genData2r2C[128, 128, 1024];
testData3TBigC = data3T2C[128, 128, 1024];
testData4TBigC = data4TC[128, 128, 1024];
testData5TBigC = genData5TCC[128, 128, 1024];
fullTestSetBigC = Join[testDataECABigC,
  testData2TBigC, testData3TBigC, testData4TBigC, testData5TBigC];
Length[fullTestSetBigC]
```

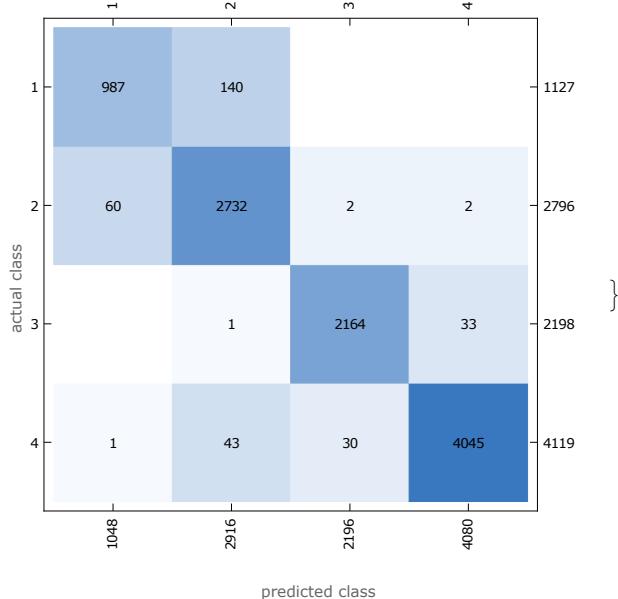
```
Out[69]= 10 240
```

```
In[70]:= RandomSample[fullTestSetBigC, 10]
```

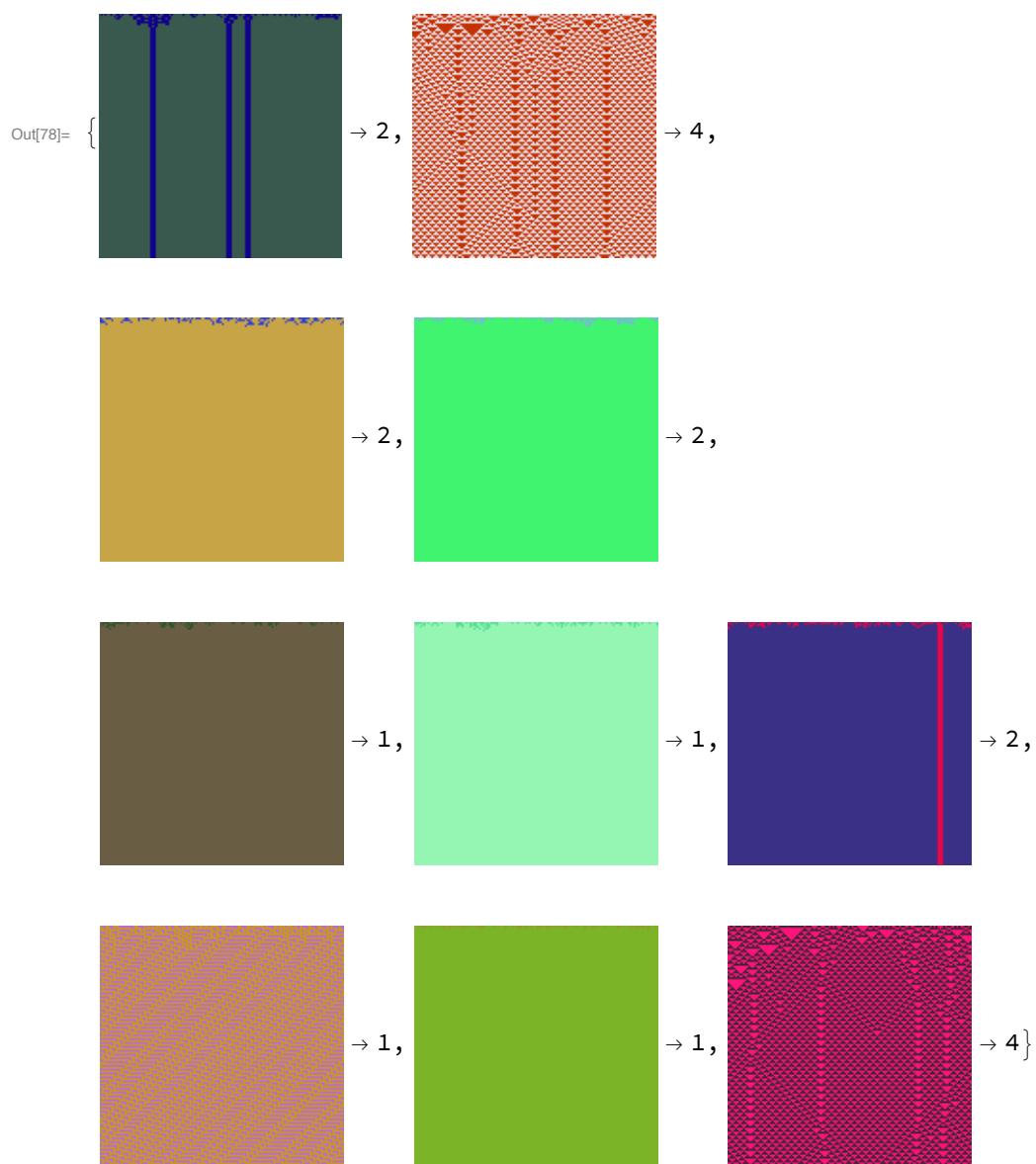


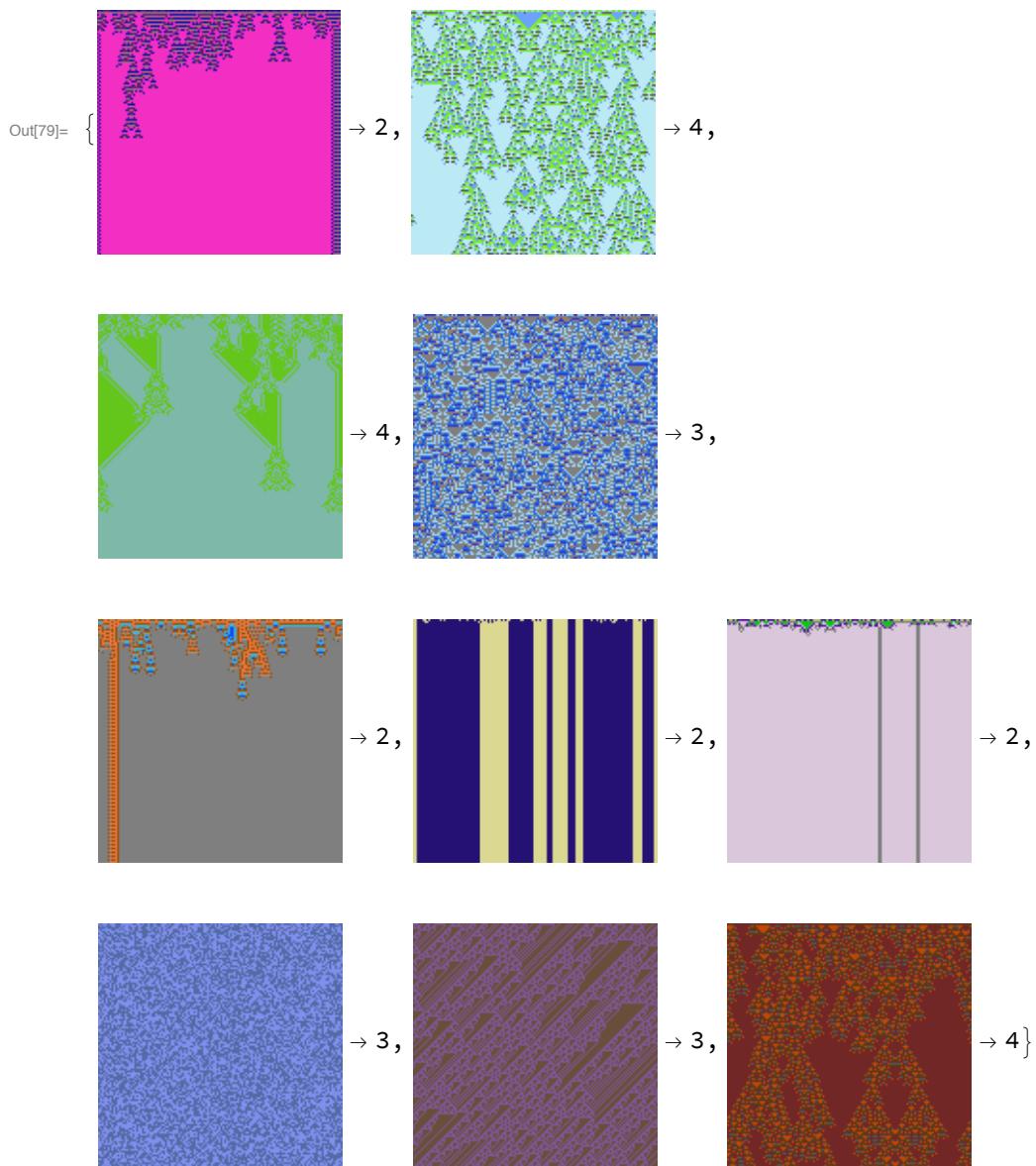
```
In[73]:= NetMeasurements[netECA19, fullTestSetBigC,
 {"Accuracy", "Precision", "ConfusionMatrixPlot"}]

Out[73]= {0.969531, {1 → 0.941794, 2 → 0.9369, 3 → 0.985428, 4 → 0.991422}, }
```



```
In[74]:= entropyImagesBigC = RandomSample[Keys[fullTestSetBigC], 500];
entropiesBigC = netECA19[entropyImagesBigC, "Entropy"];
highEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, -10]]];
lowEntBigC = entropyImagesBigC[[Ordering[entropiesBigC, 10]]];
Thread[highEntBigC → netECA19[highEntBigC]]
Thread[lowEntBigC → netECA19[lowEntBigC]]
```





Testing Network XIX (200 epochs) on unseen CA rule spaces

2-colour non-totalistic, range 2

```
In[84]:= test4Data2kr2C19 = datak2r2C[128, 128, 8];
Thread[
  test4Data2kr2C19 \[Function] netECA19[Keys@test4Data2kr2C19, {"TopProbabilities", 2}]]
```

Out[85]= {

$\rightarrow 3623639841 \rightarrow \{4 \rightarrow 5.92466 \times 10^{-19}, 3 \rightarrow 1.\},$

$$\left(\begin{array}{c} \text{[A green square with blue vertical stripes]} \\ \rightarrow 4\ 204\ 902\ 033 \end{array} \right) \rightarrow \{4 \rightarrow 2.56823 \times 10^{-8}, 2 \rightarrow 1.\},$$

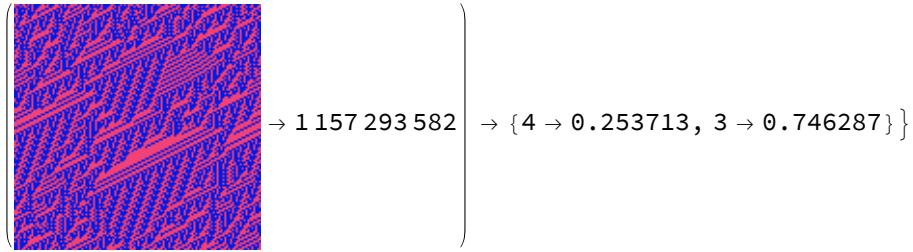
$$\left(\begin{array}{c} \text{[A pink square with a diagonal pattern of black and white dots]} \\ \rightarrow 3\ 766\ 586\ 648 \end{array} \right) \rightarrow \{1 \rightarrow 0., 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[A green square with small black dots]} \\ \rightarrow 3\ 083\ 711\ 710 \end{array} \right) \rightarrow \{4 \rightarrow 2.17708 \times 10^{-25}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[A purple square with diagonal lines and a central green line]} \\ \rightarrow 3\ 912\ 062\ 127 \end{array} \right) \rightarrow \{1 \rightarrow 0., 2 \rightarrow 1.\},$$

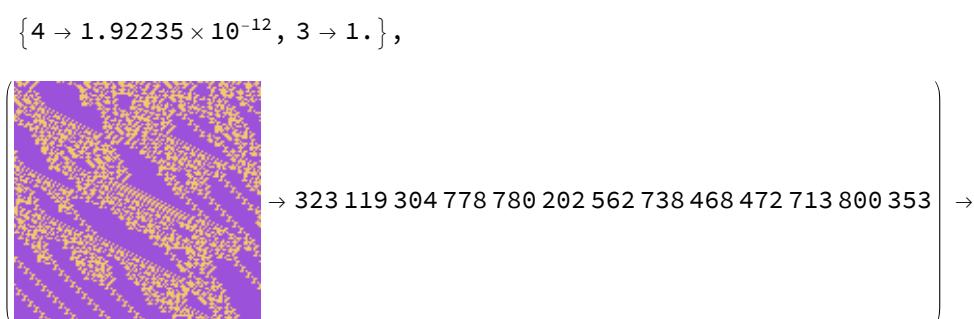
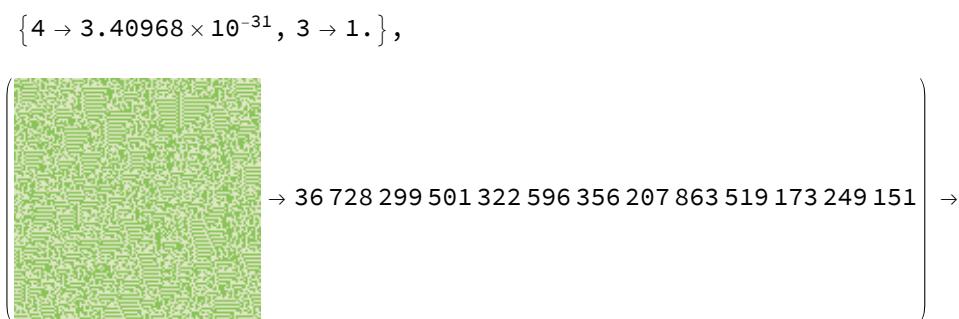
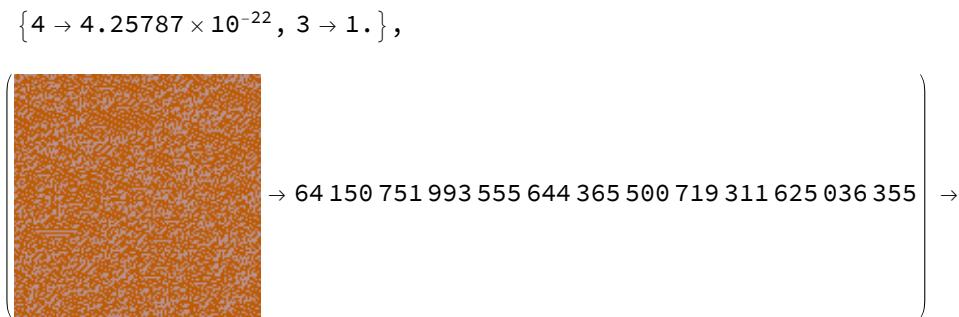
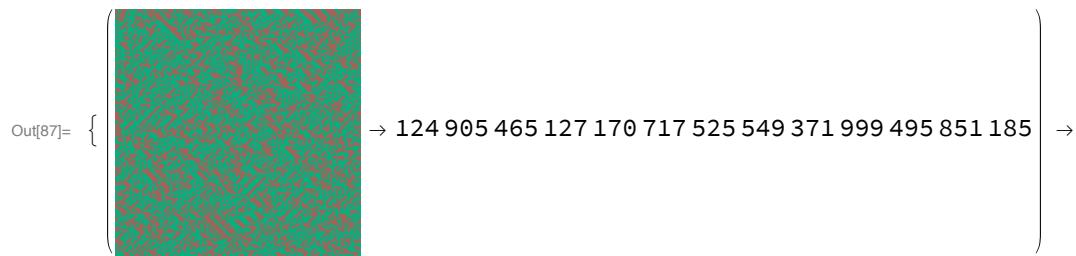
$$\left(\begin{array}{c} \text{[A pink square with a complex pattern of black and white dots]} \\ \rightarrow 3\ 127\ 103\ 417 \end{array} \right) \rightarrow \{1 \rightarrow 0., 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[A blue square with a fine grid pattern]} \\ \rightarrow 1\ 368\ 223\ 734 \end{array} \right) \rightarrow \{3 \rightarrow 0.0375692, 4 \rightarrow 0.962431\},$$

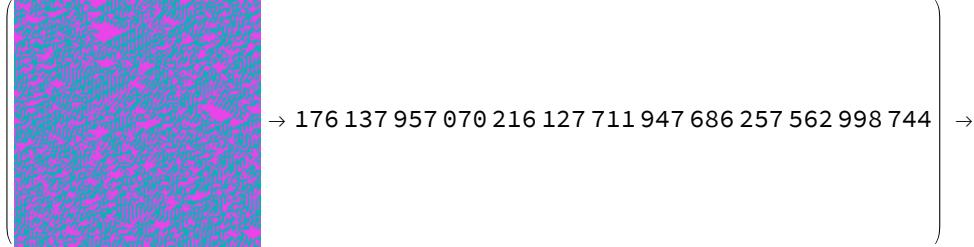


2-colour non-totalistic, range 3

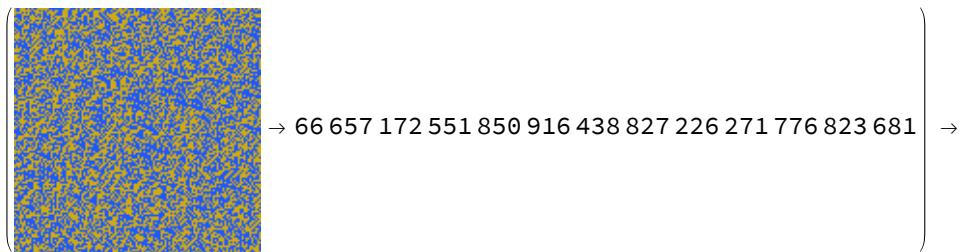
```
In[86]:= test4Data2kr3C19 = datak2r3NT[128, 128, 8];
Thread[
test4Data2kr3C19 → netECA19[Keys@test4Data2kr3C19, {"TopProbabilities", 2}]]
```



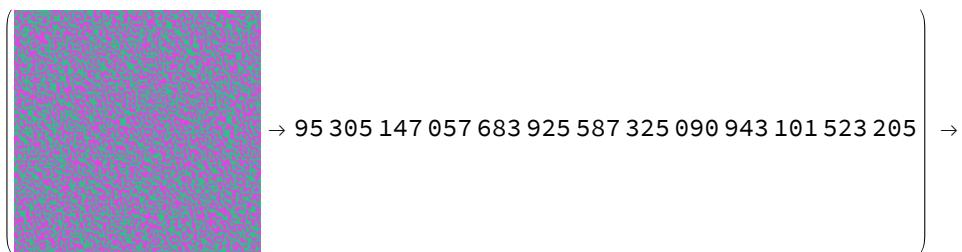
$\{3 \rightarrow 0.190559, 4 \rightarrow 0.809441\},$



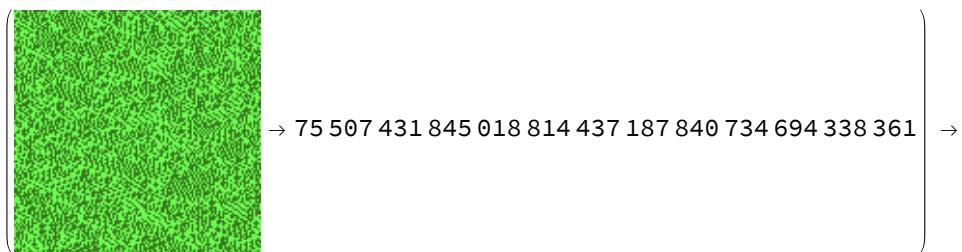
$\{1 \rightarrow 0., 3 \rightarrow 1.\},$



$\{4 \rightarrow 9.37229 \times 10^{-18}, 3 \rightarrow 1.\},$



$\{4 \rightarrow 1.7544 \times 10^{-26}, 3 \rightarrow 1.\},$



$\{4 \rightarrow 1.14088 \times 10^{-28}, 3 \rightarrow 1.\}\}$

3-colour non-totalistic, range 1

```
In[90]:= test4Data3kr1C19 = datak3r1NT[128, 128, 8];
Thread[
test4Data3kr1C19 → netECA19[Keys@test4Data3kr1C19, {"TopProbabilities", 2}]]
```

Out[91]= $\left\{ \begin{array}{c} \text{(A 10x10 grid of black dots on a white background)} \\ \rightarrow 903\ 740\ 772\ 813 \end{array} \right\} \rightarrow \{4 \rightarrow 1.43387 \times 10^{-14}, 3 \rightarrow 1.\},$

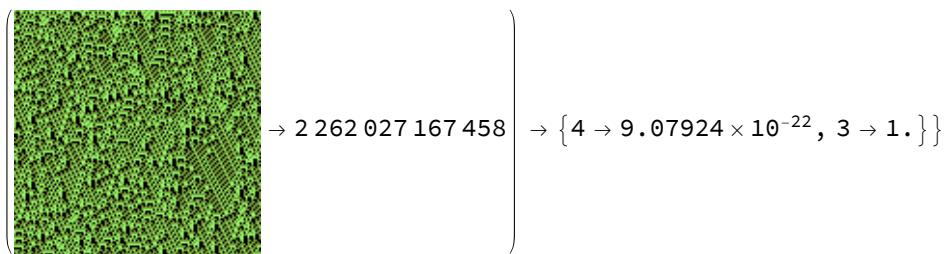
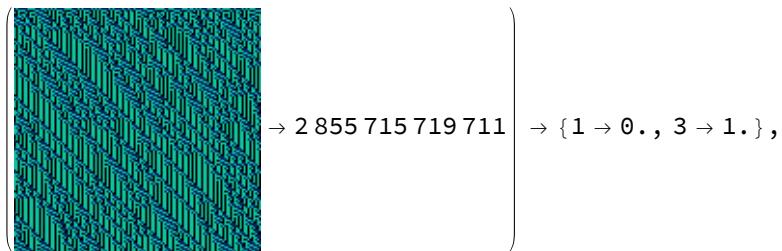
$\left\{ \begin{array}{c} \text{(A 10x10 grid of black dots on a white background with diagonal stripes of red dots)} \\ \rightarrow 4\ 969\ 181\ 144\ 217 \end{array} \right\} \rightarrow \{2 \rightarrow 0.0805151, 4 \rightarrow 0.919485\},$

$\left\{ \begin{array}{c} \text{(A 10x10 grid of black dots on a white background with diagonal stripes of purple dots)} \\ \rightarrow 7\ 038\ 367\ 528\ 689 \end{array} \right\} \rightarrow \{3 \rightarrow 8.64922 \times 10^{-26}, 4 \rightarrow 1.\},$

$\left\{ \begin{array}{c} \text{(A 10x10 grid of black dots on a white background with vertical stripes of red dots)} \\ \rightarrow 432\ 813\ 174\ 387 \end{array} \right\} \rightarrow \{4 \rightarrow 1.4013 \times 10^{-45}, 2 \rightarrow 1.\},$

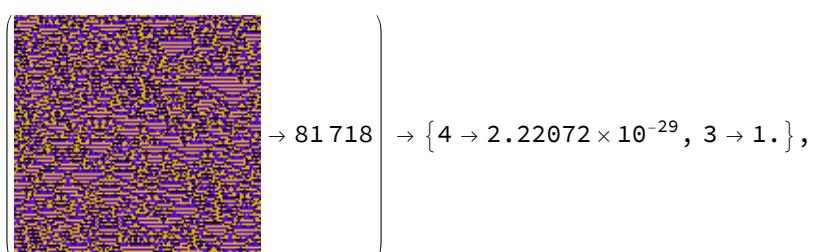
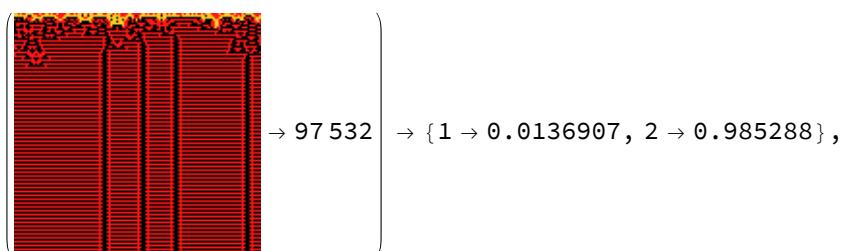
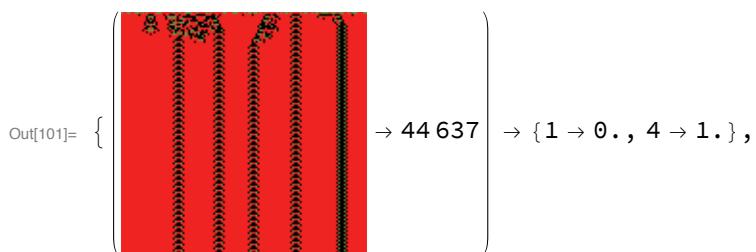
$\left\{ \begin{array}{c} \text{(A 10x10 grid of black dots on a white background with a complex pattern of green dots)} \\ \rightarrow 2\ 083\ 475\ 355\ 420 \end{array} \right\} \rightarrow \{4 \rightarrow 1.38076 \times 10^{-8}, 3 \rightarrow 1.\},$

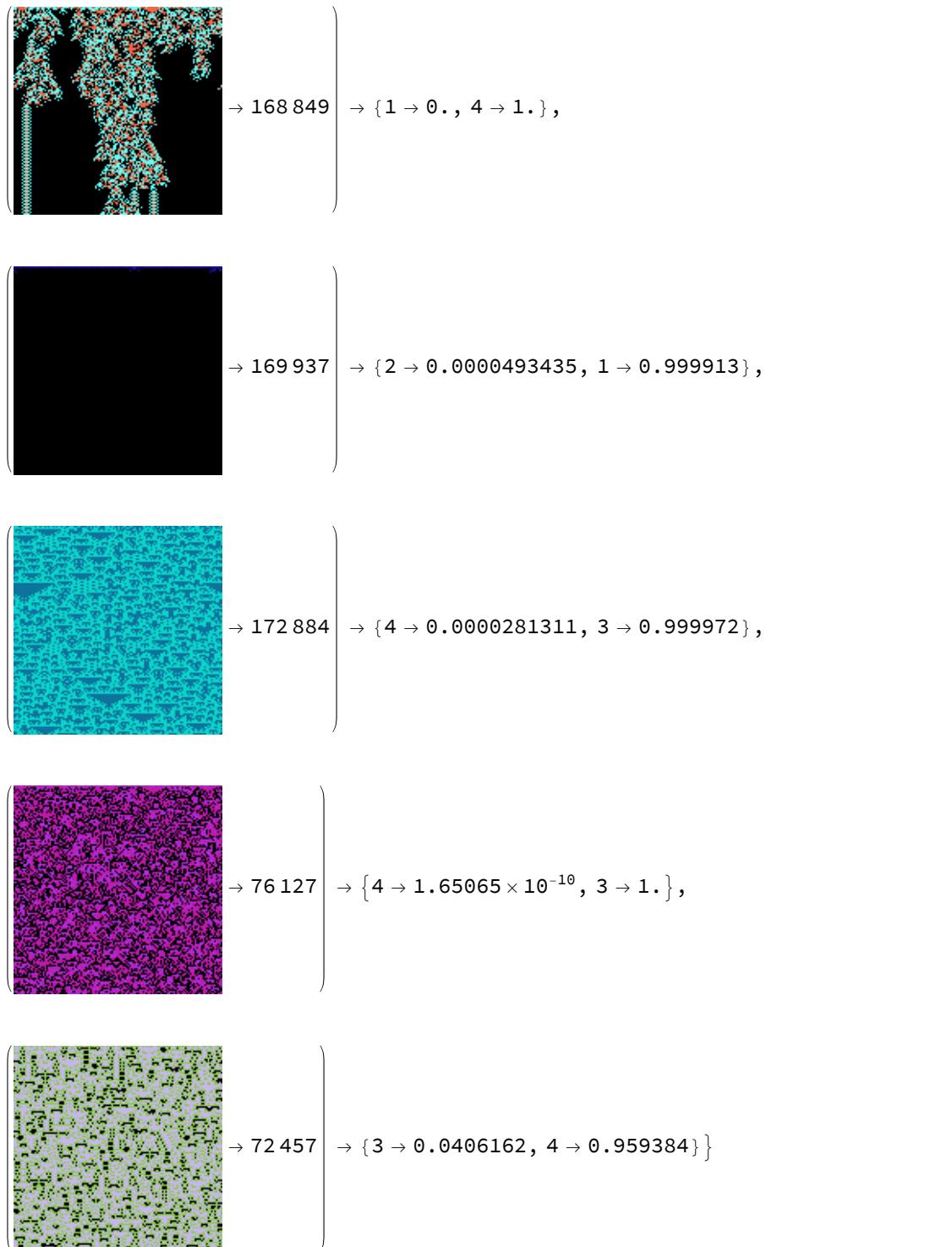
$\left\{ \begin{array}{c} \text{(A 10x10 grid of black dots on a white background with a complex pattern of green dots)} \\ \rightarrow 966\ 244\ 316\ 659 \end{array} \right\} \rightarrow \{4 \rightarrow 8.30269 \times 10^{-33}, 3 \rightarrow 1.\},$



3-colour totalistic, range 2

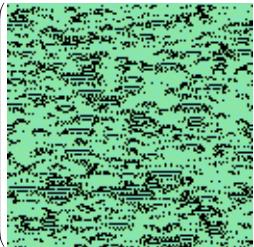
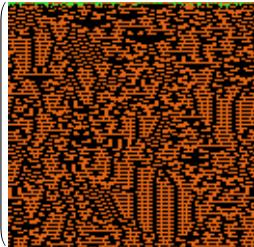
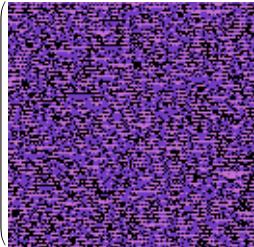
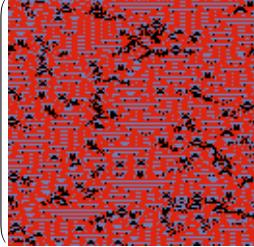
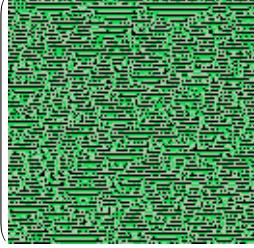
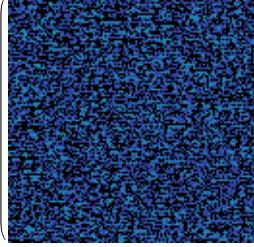
```
In[100]:= test4Data3kr2C19 = datak3r2C[128, 128, 8];
Thread[
  test4Data3kr2C19 → netECA19[Keys@test4Data3kr2C19, {"TopProbabilities", 2}]]
```

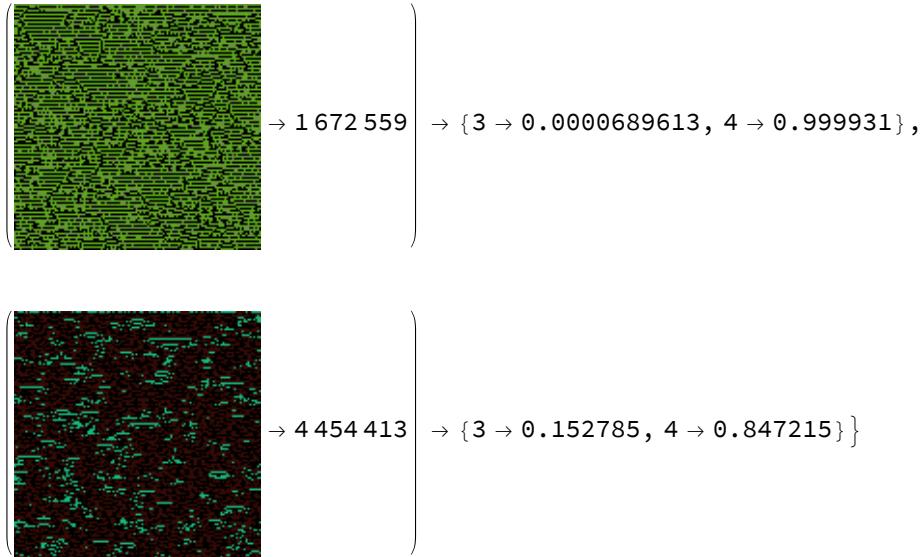




3-colour totalistic, range 3

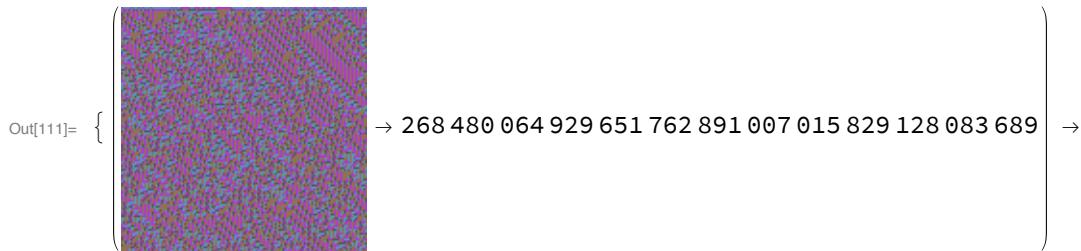
```
In[104]:= test4Data3kr3C19 = datak3r3C[128, 128, 8];
Thread[
  test4Data3kr3C19 → netECA19[Keys@test4Data3kr3C19, {"TopProbabilities", 2}]]
```

Out[105]=	{		→ 5 332 402	}	→ {1 → 0., 3 → 1.},
			→ 12 215 348	}	→ {3 → 0.0215091, 4 → 0.978491},
			→ 5 882 266	}	→ {4 → 7.74599 × 10⁻¹⁰, 3 → 1.},
			→ 3 262 519	}	→ {1 → 0., 3 → 1.},
			→ 4 981 094	}	→ {4 → 0.000228014, 3 → 0.999772},
			→ 9 082 439	}	→ {4 → 1.88074 × 10⁻¹³, 3 → 1.},

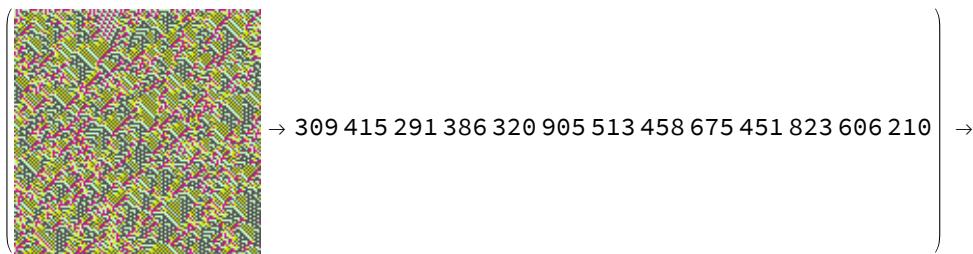


4-colour non-totalistic, range 1

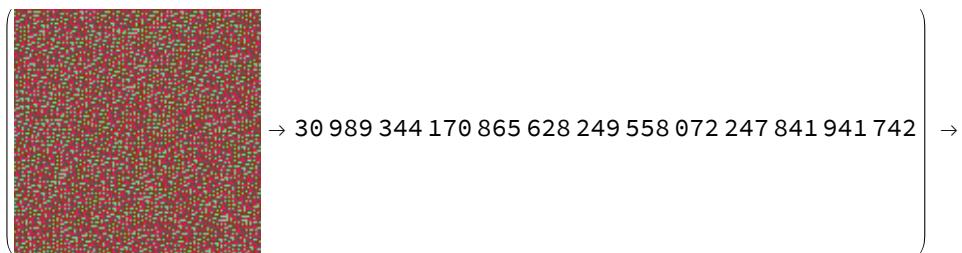
```
In[110]:= test4Data4kr1C19 = datak4r1NT[128, 128, 8];
Thread[
  test4Data4kr1C19 &gt; netECA19[Keys@test4Data4kr1C19, {"TopProbabilities", 2}]]
```



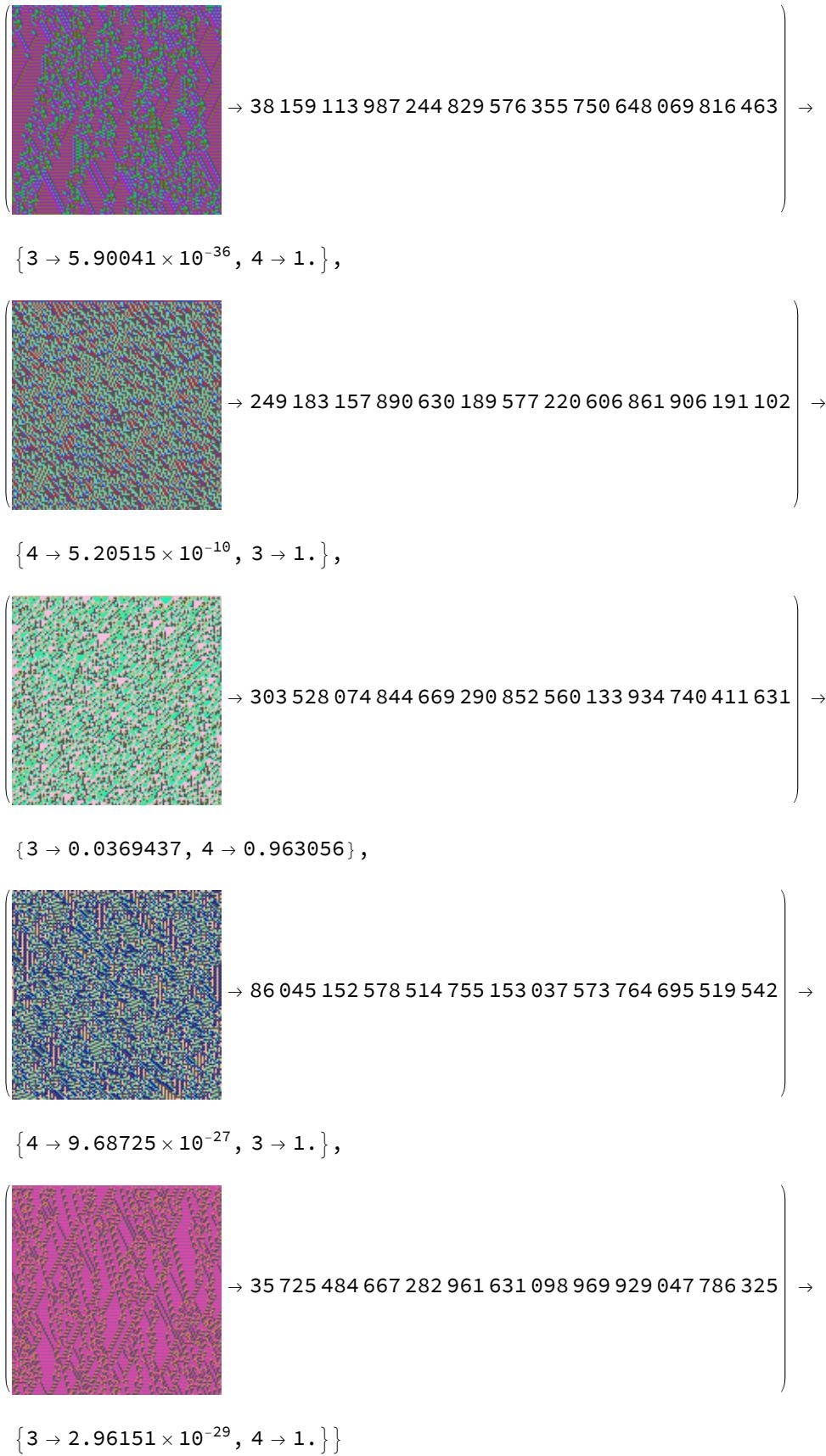
$$\{4 \rightarrow 5.90905 \times 10^{-31}, 3 \rightarrow 1.\},$$



$$\{3 \rightarrow 0.0527879, 4 \rightarrow 0.947212\},$$



$$\{4 \rightarrow 1.13198 \times 10^{-13}, 3 \rightarrow 1.\},$$



4-colour totalistic, range 2

```
In[112]:= test4Data4kr2C19 = data4r2C[128, 128, 8];
Thread[
  test4Data4kr2C19 → netECA19[Keys@test4Data4kr2C19, {"TopProbabilities", 2}]]
```

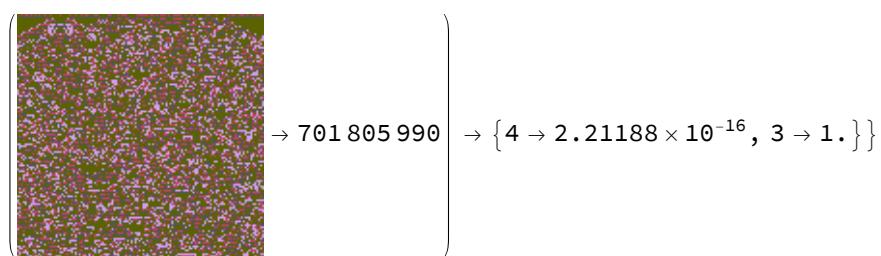
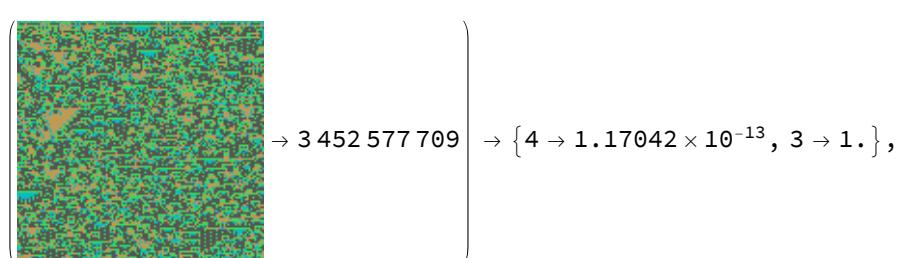
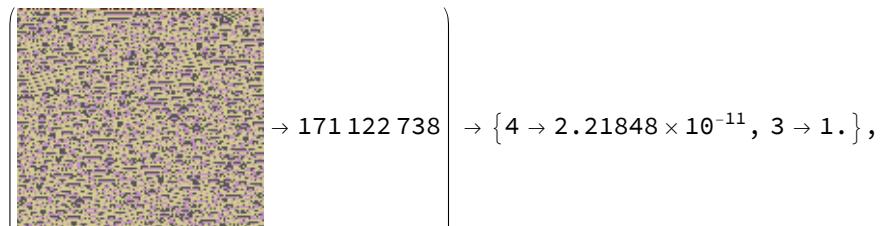
Out[113]= $\left\{ \begin{array}{c} \text{(A 128x128 red square)} \\ \rightarrow 3\ 039\ 279\ 908 \end{array} \right\} \rightarrow \{4 \rightarrow 1.99769 \times 10^{-22}, 3 \rightarrow 1.\},$

Out[114]= $\left\{ \begin{array}{c} \text{(A 128x128 green square)} \\ \rightarrow 1\ 004\ 857\ 722 \end{array} \right\} \rightarrow \{4 \rightarrow 2.69276 \times 10^{-14}, 3 \rightarrow 1.\},$

Out[115]= $\left\{ \begin{array}{c} \text{(A 128x128 yellow square)} \\ \rightarrow 1\ 136\ 086\ 050 \end{array} \right\} \rightarrow \{4 \rightarrow 5.1036 \times 10^{-14}, 3 \rightarrow 1.\},$

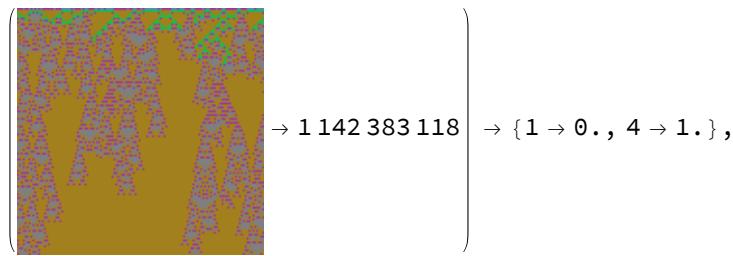
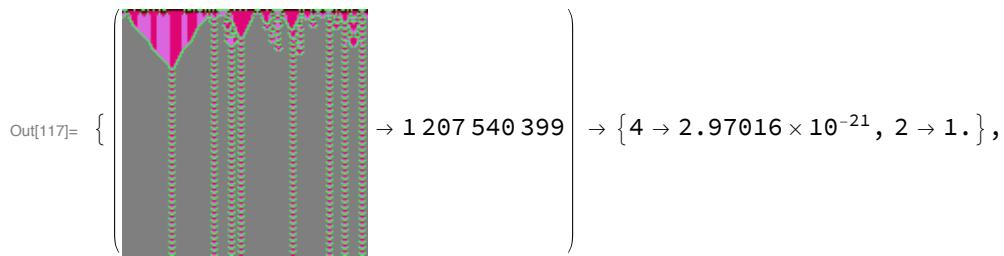
Out[116]= $\left\{ \begin{array}{c} \text{(A 128x128 black square with a diagonal pattern)} \\ \rightarrow 3\ 492\ 358\ 882 \end{array} \right\} \rightarrow \{3 \rightarrow 1.56014 \times 10^{-7}, 4 \rightarrow 1.\},$

Out[117]= $\left\{ \begin{array}{c} \text{(A 128x128 blue square)} \\ \rightarrow 1\ 069\ 866\ 717 \end{array} \right\} \rightarrow \{4 \rightarrow 8.91689 \times 10^{-21}, 3 \rightarrow 1.\},$



5-colour totalistic, range 1

```
In[116]:= test4Data5kr1C19 = data5T2C[8, 128, 128];
Thread[
  test4Data5kr1C19 → netECA19[Keys@test4Data5kr1C19, {"TopProbabilities", 2}]]
```



$$\left(\begin{array}{c} \text{[A 10x10 grid with red, yellow, and black cells]} \\ \rightarrow 1\ 123\ 443\ 123 \end{array} \right) \rightarrow \{ 4 \rightarrow 0.0000133564, 2 \rightarrow 0.999987 \},$$

$$\left(\begin{array}{c} \text{[A 10x10 grid with cyan and black cells]} \\ \rightarrow 179\ 147\ 268 \end{array} \right) \rightarrow \{ 3 \rightarrow 0.00253984, 4 \rightarrow 0.99746 \},$$

$$\left(\begin{array}{c} \text{[A 10x10 grid with purple and pink cells]} \\ \rightarrow 1\ 070\ 088\ 188 \end{array} \right) \rightarrow \{ 4 \rightarrow 5.16433 \times 10^{-17}, 2 \rightarrow 1. \},$$

$$\left(\begin{array}{c} \text{[A 10x10 grid with green and black cells]} \\ \rightarrow 839\ 709\ 526 \end{array} \right) \rightarrow \{ 1 \rightarrow 1.99965 \times 10^{-42}, 2 \rightarrow 1. \},$$

$$\left(\begin{array}{c} \text{[A 10x10 grid with cyan, magenta, and black cells]} \\ \rightarrow 1\ 029\ 145\ 401 \end{array} \right) \rightarrow \{ 4 \rightarrow 4.63463 \times 10^{-18}, 3 \rightarrow 1. \},$$

$$\left(\begin{array}{c} \text{[A 10x10 grid with blue and magenta cells]} \\ \rightarrow 153\ 105\ 290 \end{array} \right) \rightarrow \{ 3 \rightarrow 4.82742 \times 10^{-35}, 4 \rightarrow 1. \}$$

6-colour totalistic, range 1

```
In[124]:= test4Data6kr1C19 = data6TC[8, 128, 128];
Thread[
  test4Data6kr1C19 → netECA19[Keys@test4Data6kr1C19, {"TopProbabilities", 2}]]
```

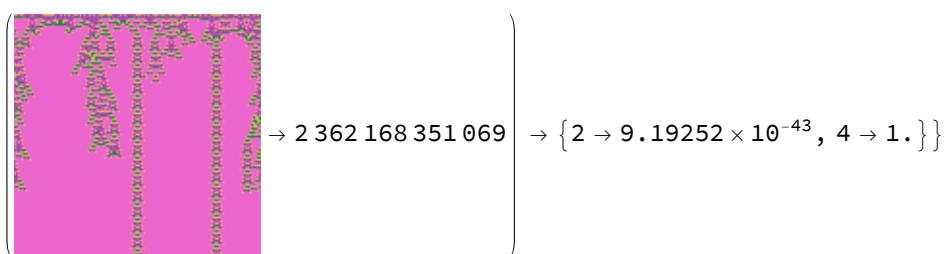
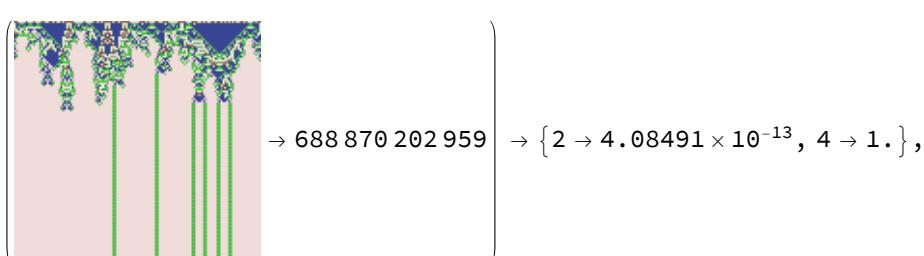
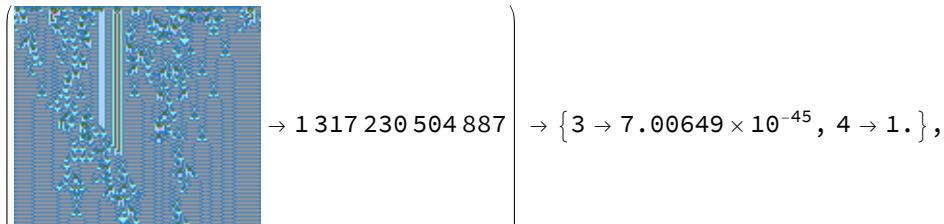
$$\text{Out}[125]= \left\{ \begin{array}{c} \text{[A 128x128 grid of green, blue, and cyan pixels]} \\ \rightarrow 521\ 151\ 757\ 166 \end{array} \right\} \rightarrow \{4 \rightarrow 4.2538 \times 10^{-27}, 3 \rightarrow 1.\},$$

$$\left\{ \begin{array}{c} \text{[A 128x128 grid of green, blue, and cyan pixels]} \\ \rightarrow 1\ 148\ 948\ 615\ 051 \end{array} \right\} \rightarrow \{3 \rightarrow 1.05684 \times 10^{-11}, 4 \rightarrow 1.\},$$

$$\left\{ \begin{array}{c} \text{[A 128x128 grid of green, blue, and cyan pixels]} \\ \rightarrow 1\ 701\ 138\ 861\ 521 \end{array} \right\} \rightarrow \{3 \rightarrow 0.344279, 4 \rightarrow 0.655721\},$$

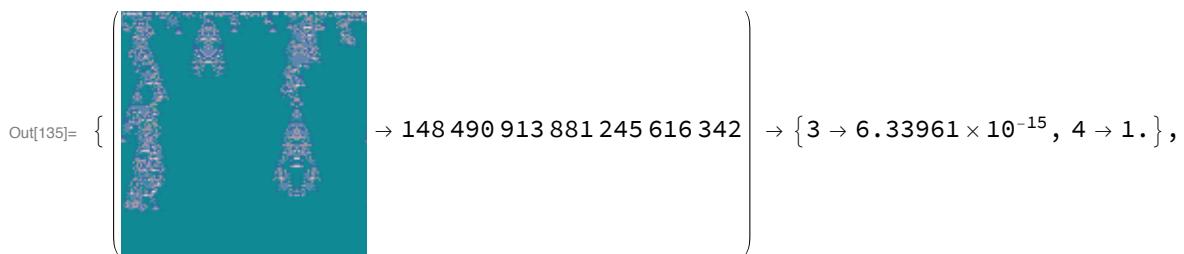
$$\left\{ \begin{array}{c} \text{[A 128x128 grid of red pixels]} \\ \rightarrow 772\ 044\ 852\ 372 \end{array} \right\} \rightarrow \{4 \rightarrow 3.00861 \times 10^{-22}, 2 \rightarrow 1.\},$$

$$\left\{ \begin{array}{c} \text{[A 128x128 grid of red, green, and blue pixels]} \\ \rightarrow 401\ 641\ 356\ 701 \end{array} \right\} \rightarrow \{4 \rightarrow 1.64612 \times 10^{-16}, 3 \rightarrow 1.\},$$



6-colour totalistic, range 2

```
In[134]:= test4Data6kr2C19 = data6T2C[8, 128, 128];
Thread[
  test4Data6kr2C19 → netECA19[Keys@test4Data6kr2C19, {"TopProbabilities", 2}]]
```



$$\left(\begin{array}{c} \text{[A 4x4 grid of random colors]} \\ \rightarrow 145\ 612\ 570\ 579\ 789\ 266\ 485 \end{array} \right) \rightarrow \{4 \rightarrow 1.52405 \times 10^{-9}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[A 4x4 grid of random colors]} \\ \rightarrow 57\ 362\ 919\ 586\ 594\ 306\ 710 \end{array} \right) \rightarrow \{4 \rightarrow 0.031388, 3 \rightarrow 0.968612\},$$

$$\left(\begin{array}{c} \text{[A 4x4 grid of random colors]} \\ \rightarrow 24\ 770\ 952\ 214\ 224\ 040\ 296 \end{array} \right) \rightarrow \{4 \rightarrow 5.16516 \times 10^{-16}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[A 4x4 grid of random colors]} \\ \rightarrow 143\ 600\ 862\ 017\ 240\ 236\ 453 \end{array} \right) \rightarrow \{4 \rightarrow 1.30214 \times 10^{-22}, 3 \rightarrow 1.\},$$

$$\left(\begin{array}{c} \text{[A 4x4 grid of random colors]} \\ \rightarrow 160\ 410\ 817\ 633\ 450\ 677\ 074 \end{array} \right) \rightarrow \{4 \rightarrow 0.000231853, 3 \rightarrow 0.999768\},$$

$$\left(\begin{array}{c} \text{[A 4x4 grid of random colors]} \\ \rightarrow 99\ 035\ 735\ 849\ 117\ 353\ 433 \end{array} \right) \rightarrow \{4 \rightarrow 7.72208 \times 10^{-20}, 3 \rightarrow 1.\}\}$$

7-colour totalistic, range 1

```
In[140]:= test4Data7kr1C19 = data7TC[8, 128, 128];
Thread[
  test4Data7kr1C19 → netECA19[Keys@test4Data7kr1C19, {"TopProbabilities", 2}]]
```

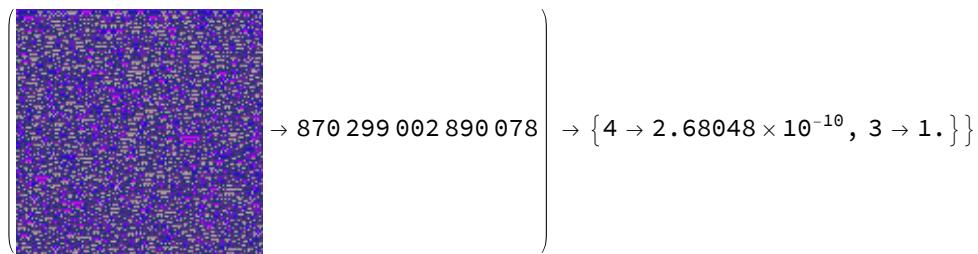
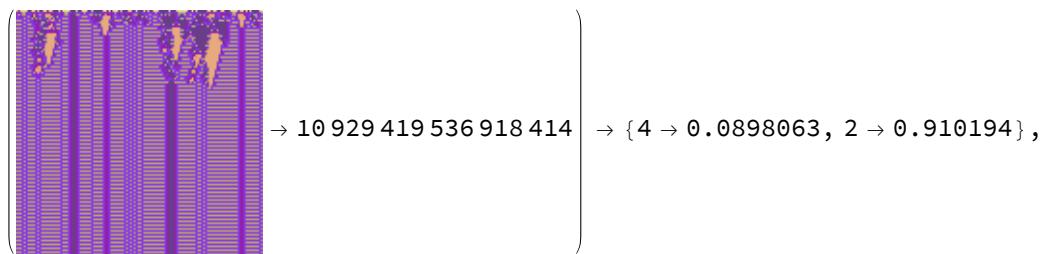
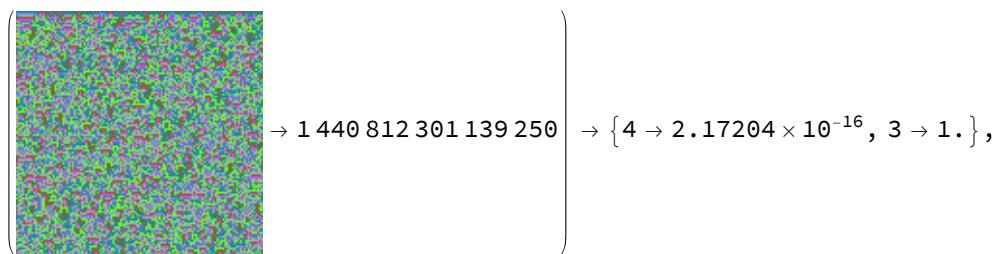
Out[141]= $\left\{ \begin{array}{c} \text{A 128x128 grid of 7 colors (blue, green, red, yellow, cyan, magenta, black)} \\ \rightarrow 7905962486151833 \end{array} \right\} \rightarrow \{4 \rightarrow 0.000554173, 3 \rightarrow 0.999446\},$

$\left\{ \begin{array}{c} \text{A 128x128 grid of 7 colors (blue, green, red, yellow, cyan, magenta, black)} \\ \rightarrow 5986825348569542 \end{array} \right\} \rightarrow \{4 \rightarrow 0.0000562114, 3 \rightarrow 0.999944\},$

$\left\{ \begin{array}{c} \text{A 128x128 grid of 7 colors (blue, green, red, yellow, cyan, magenta, black)} \\ \rightarrow 5160779372988604 \end{array} \right\} \rightarrow \{3 \rightarrow 1.30743 \times 10^{-8}, 4 \rightarrow 1.\},$

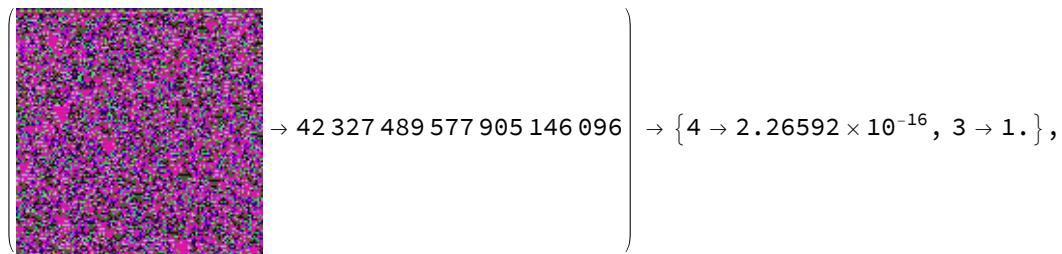
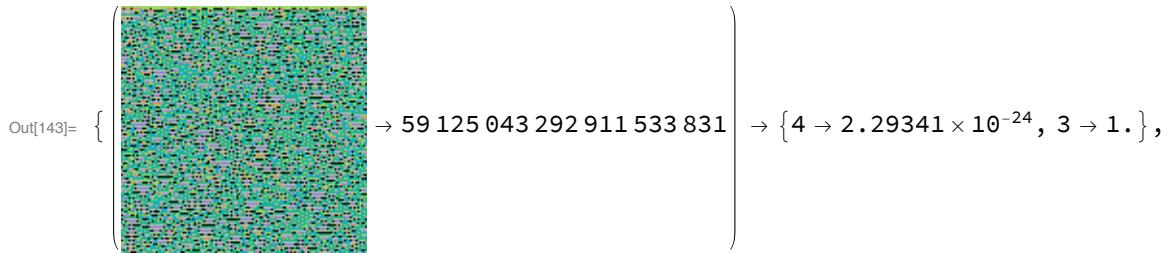
$\left\{ \begin{array}{c} \text{A 128x128 grid of 7 colors (blue, green, red, yellow, cyan, magenta, black)} \\ \rightarrow 2668104076298035 \end{array} \right\} \rightarrow \{4 \rightarrow 3.94844 \times 10^{-18}, 3 \rightarrow 1.\},$

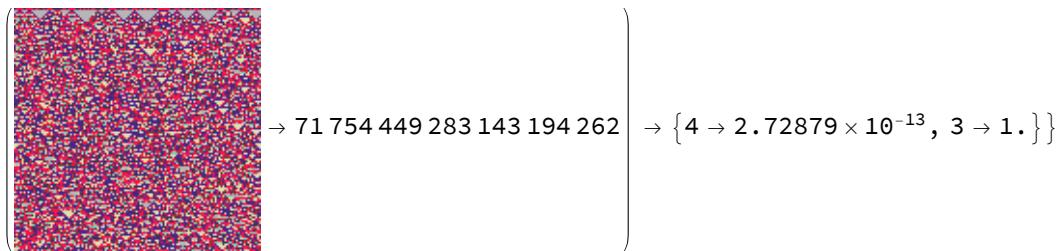
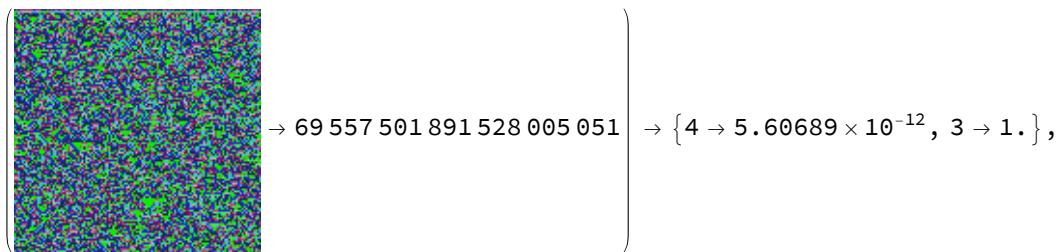
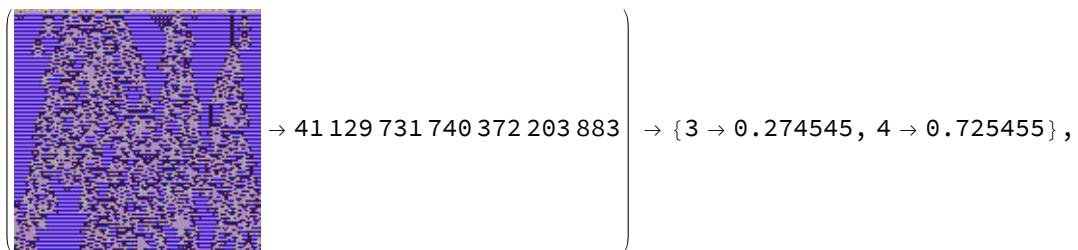
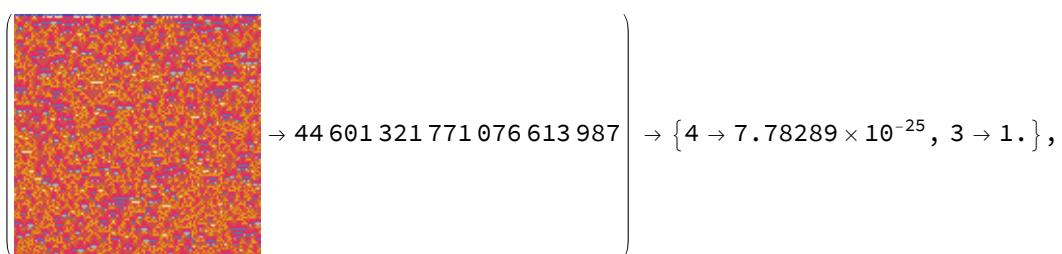
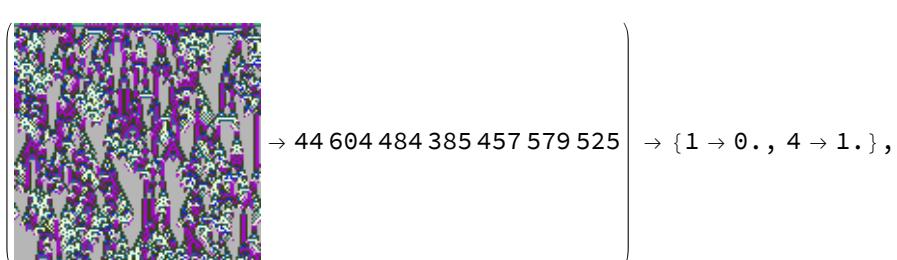
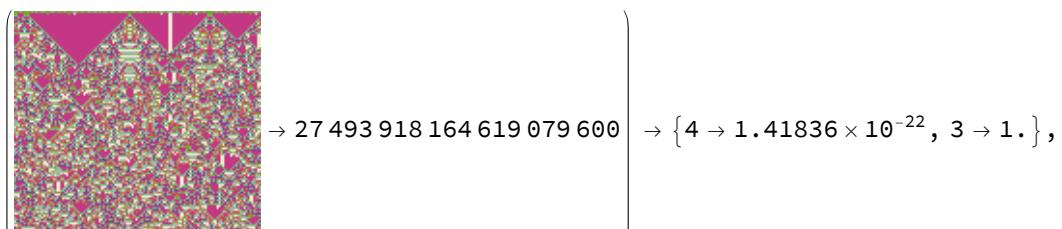
$\left\{ \begin{array}{c} \text{A 128x128 grid of 7 colors (blue, green, red, yellow, cyan, magenta, black)} \\ \rightarrow 3691759700407743 \end{array} \right\} \rightarrow \{4 \rightarrow 4.45377 \times 10^{-16}, 3 \rightarrow 1.\},$



8-colour totalistic, range 1

```
In[142]:= test4Data8kr1C19 = data8TC[8, 128, 128];
Thread[
  test4Data8kr1C19 → netECA19[Keys@test4Data8kr1C19, {"TopProbabilities", 2}]]
```





```
In[146]:= test4Data8kr1C19 = data8TC[8, 128, 128];
Thread[
  test4Data8kr1C19 → netECA19[Keys@test4Data8kr1C19, {"TopProbabilities", 2}]]
```

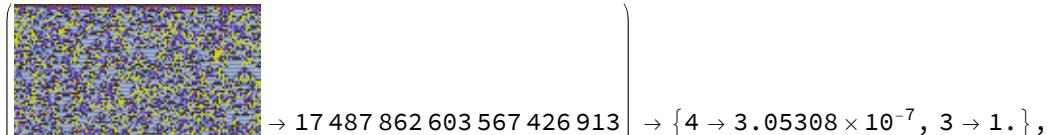
Out[147]= $\left\{ \begin{array}{c} \text{[A 128x128 pixel image showing a pattern of red, blue, and green dots]} \\ \rightarrow 30\ 958\ 781\ 818\ 328\ 214\ 442 \end{array} \right\} \rightarrow \left\{ 4 \rightarrow 4.62524 \times 10^{-15}, 3 \rightarrow 1. \right\},$

Out[147]= $\left\{ \begin{array}{c} \text{[A 128x128 pixel image showing a pattern of red, blue, and green dots]} \\ \rightarrow 61\ 018\ 914\ 870\ 782\ 867\ 384 \end{array} \right\} \rightarrow \left\{ 4 \rightarrow 1.13687 \times 10^{-12}, 3 \rightarrow 1. \right\},$

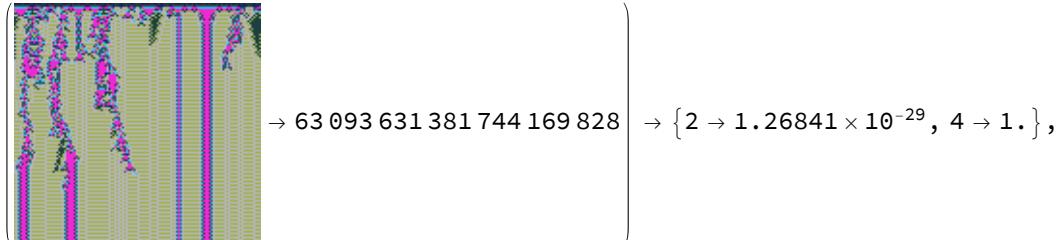
Out[147]= $\left\{ \begin{array}{c} \text{[A 128x128 pixel image showing a pattern of red, blue, and green dots]} \\ \rightarrow 20\ 705\ 257\ 985\ 378\ 094\ 677 \end{array} \right\} \rightarrow \left\{ 4 \rightarrow 1.82975 \times 10^{-19}, 3 \rightarrow 1. \right\},$

Out[147]= $\left\{ \begin{array}{c} \text{[A 128x128 pixel image showing a pattern of red, blue, and green dots]} \\ \rightarrow 43\ 941\ 374\ 463\ 684\ 638\ 030 \end{array} \right\} \rightarrow \left\{ 4 \rightarrow 1.04552 \times 10^{-6}, 3 \rightarrow 0.999999 \right\},$

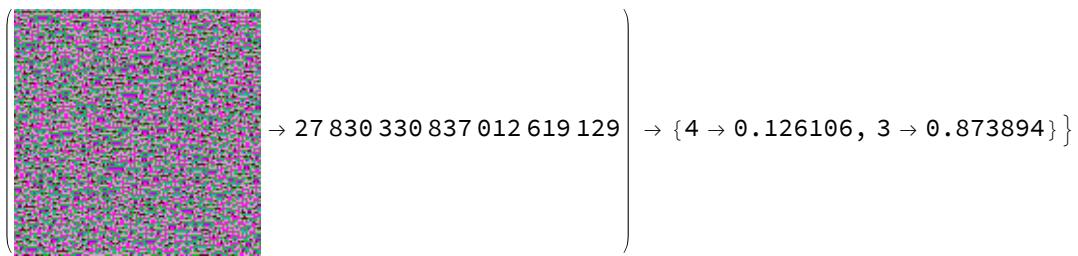
Out[147]= $\left\{ \begin{array}{c} \text{[A 128x128 pixel image showing a pattern of red, blue, and green dots]} \\ \rightarrow 3\ 024\ 227\ 929\ 898\ 264\ 848 \end{array} \right\} \rightarrow \left\{ 4 \rightarrow 1.85219 \times 10^{-8}, 3 \rightarrow 1. \right\},$



$$\left. \begin{array}{l} \text{→ } 17\ 487\ 862\ 603\ 567\ 426\ 913 \\ \end{array} \right\} \rightarrow \{4 \rightarrow 3.05308 \times 10^{-7}, 3 \rightarrow 1.\},$$



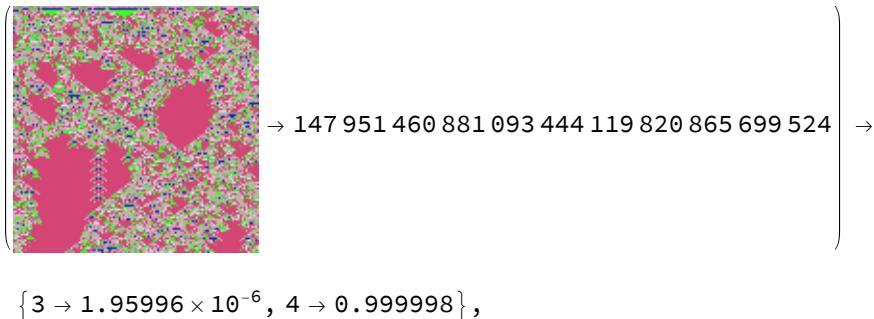
$$\left. \begin{array}{l} \text{→ } 63\ 093\ 631\ 381\ 744\ 169\ 828 \\ \end{array} \right\} \rightarrow \{2 \rightarrow 1.26841 \times 10^{-29}, 4 \rightarrow 1.\},$$



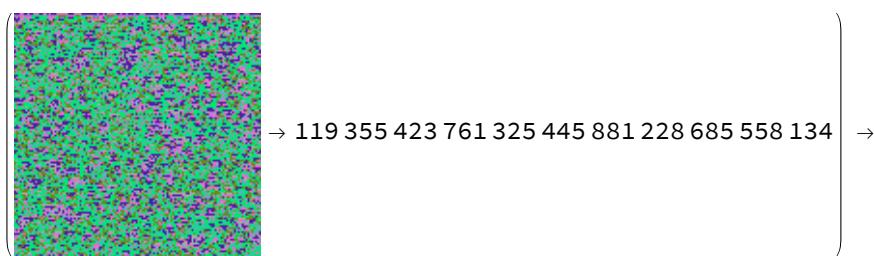
$$\left. \begin{array}{l} \text{→ } 27\ 830\ 330\ 837\ 012\ 619\ 129 \\ \end{array} \right\} \rightarrow \{4 \rightarrow 0.126106, 3 \rightarrow 0.873894\}$$

8-colour totalistic, range 2

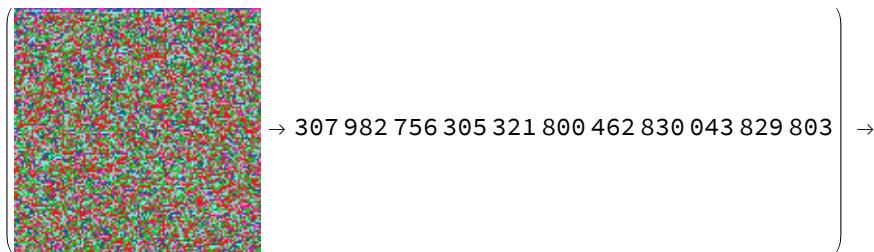
```
In[162]:= test4Data8kr2C19 = data8T2C[8, 128, 128];
Thread[
  test4Data8kr2C19 → netECA19[Keys@test4Data8kr2C19, {"TopProbabilities", 2}]]
```

Out[163]= 

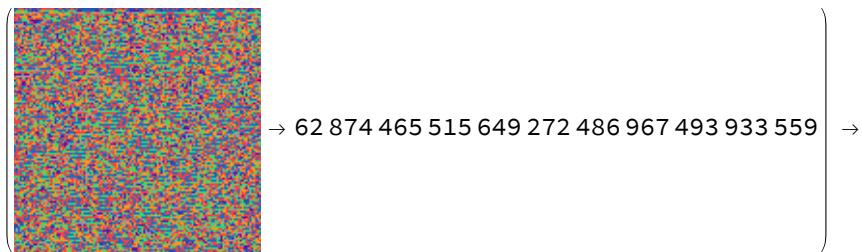
$$\left. \begin{array}{l} \text{→ } 147\ 951\ 460\ 881\ 093\ 444\ 119\ 820\ 865\ 699\ 524 \\ \end{array} \right\} \rightarrow \{3 \rightarrow 1.95996 \times 10^{-6}, 4 \rightarrow 0.999998\},$$



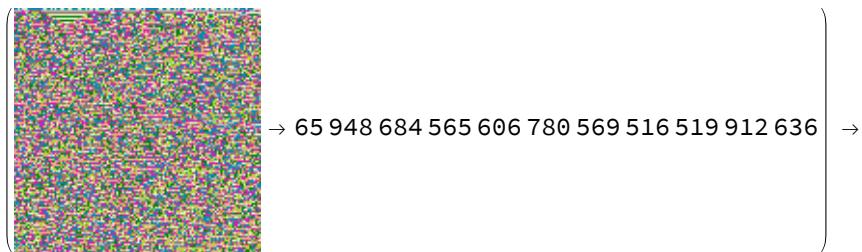
$$\left. \begin{array}{l} \text{→ } 119\ 355\ 423\ 761\ 325\ 445\ 881\ 228\ 685\ 558\ 134 \\ \end{array} \right\} \rightarrow \{4 \rightarrow 0.060776, 3 \rightarrow 0.939224\},$$



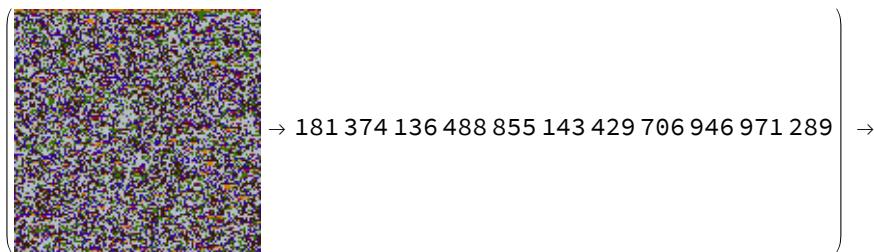
$\{4 \rightarrow 2.91468 \times 10^{-9}, 3 \rightarrow 1.\},$



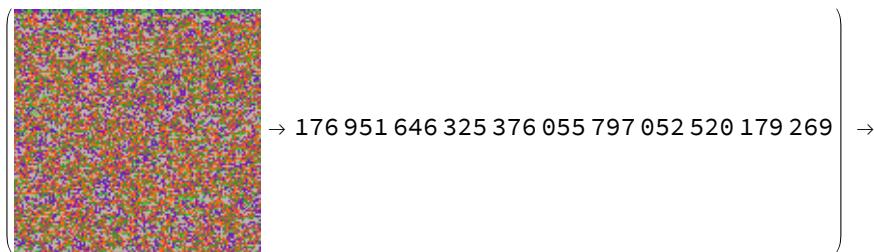
$\{4 \rightarrow 5.81908 \times 10^{-7}, 3 \rightarrow 0.999999\},$



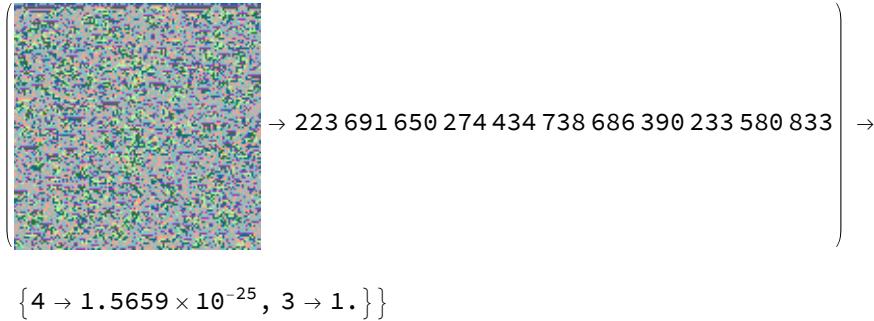
$\{4 \rightarrow 0.0000545016, 3 \rightarrow 0.999946\},$



$\{4 \rightarrow 2.66552 \times 10^{-19}, 3 \rightarrow 1.\},$

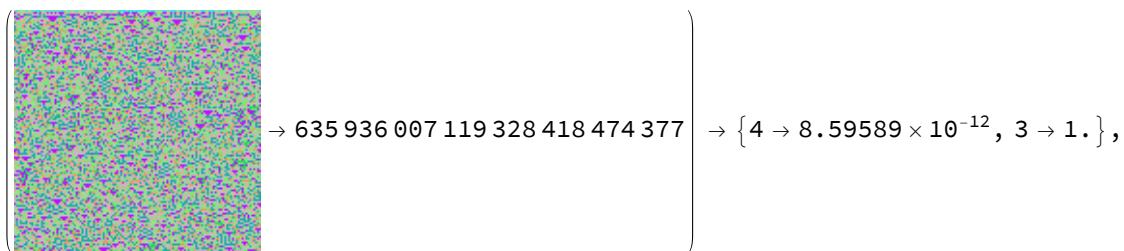
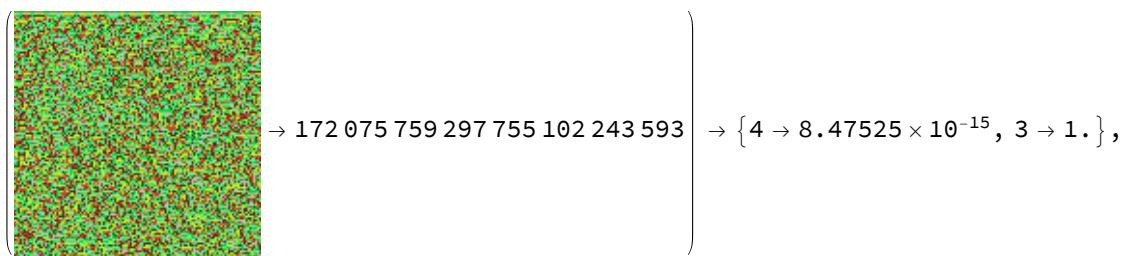
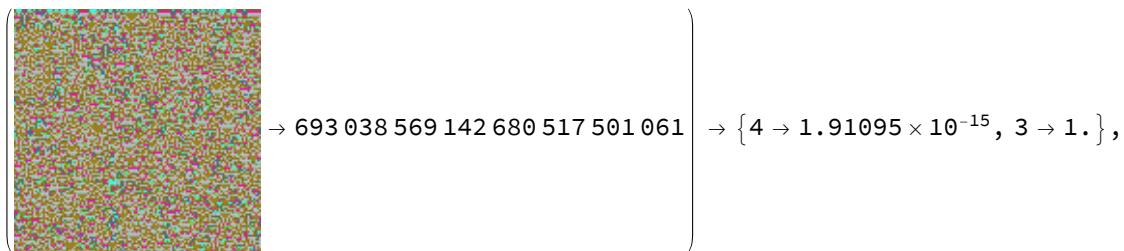
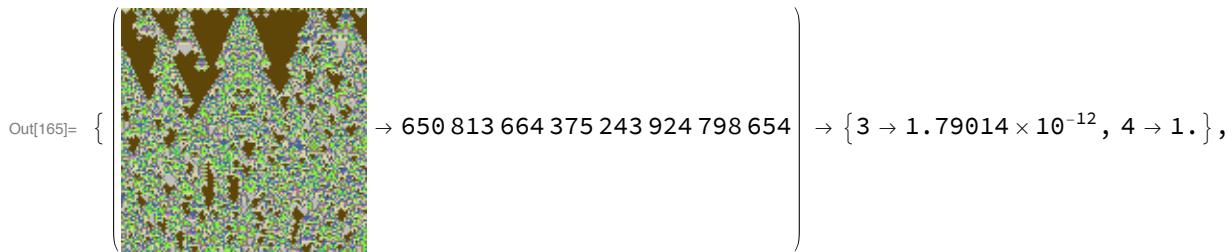


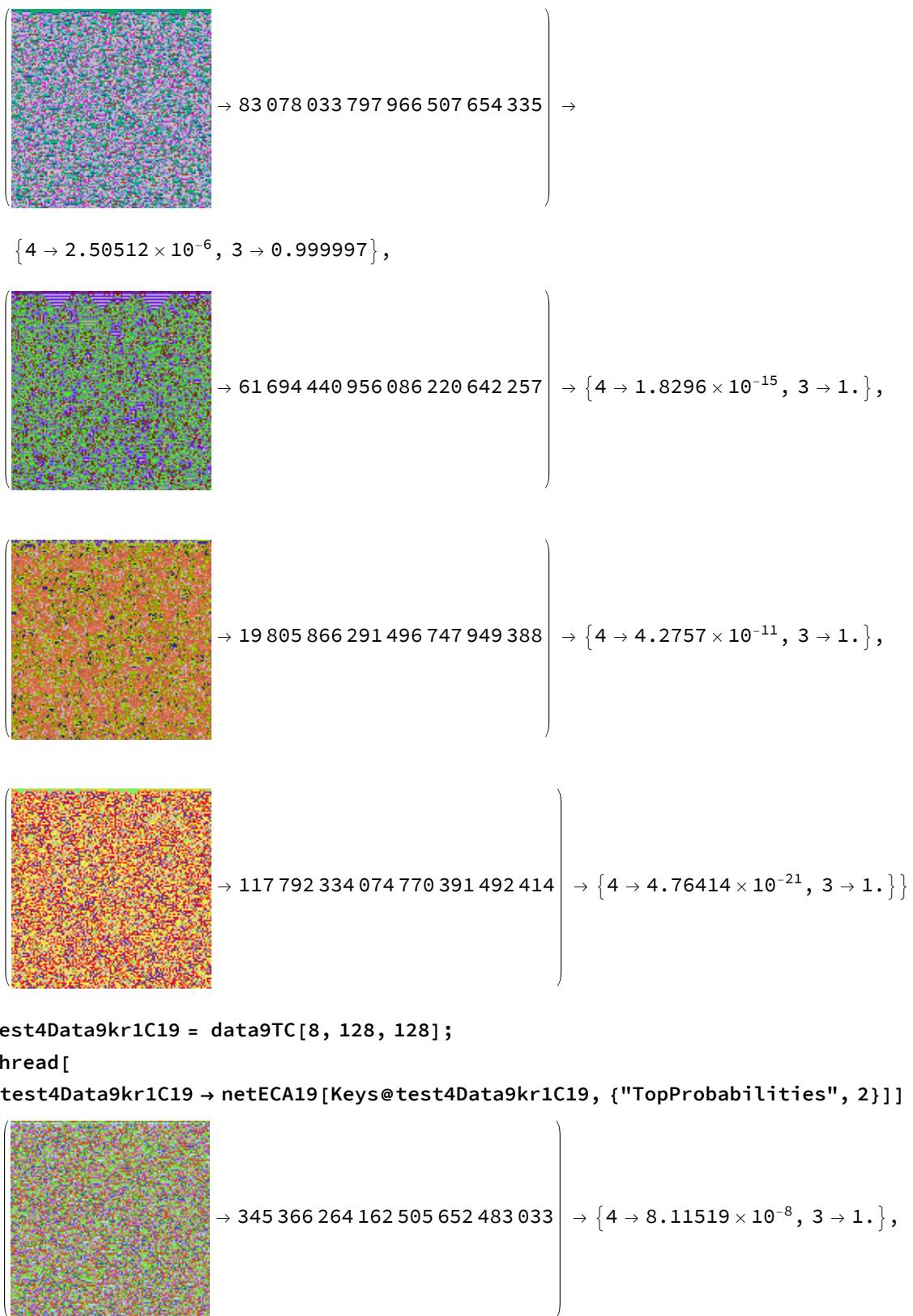
$\{4 \rightarrow 1.80483 \times 10^{-11}, 3 \rightarrow 1.\},$

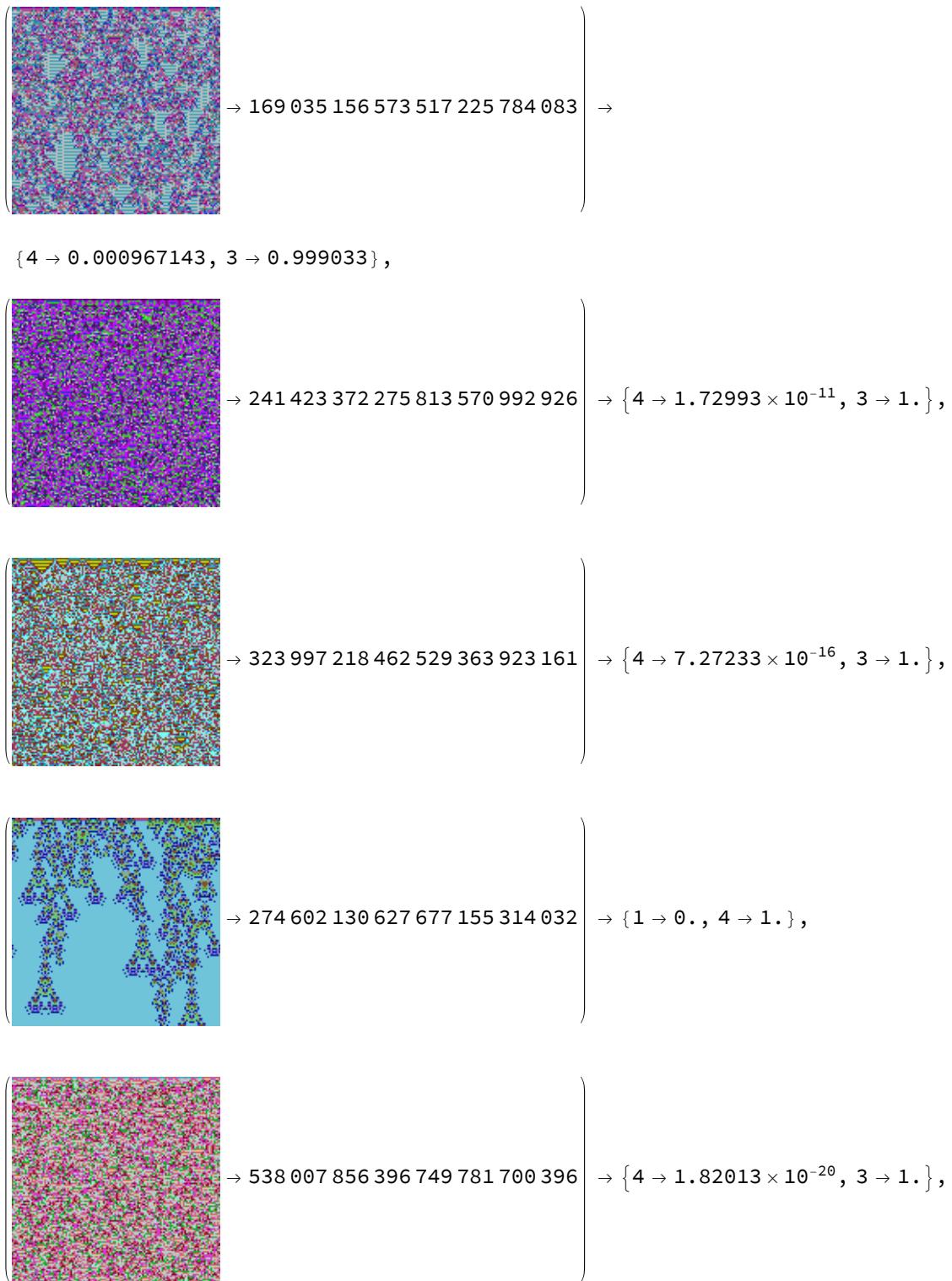


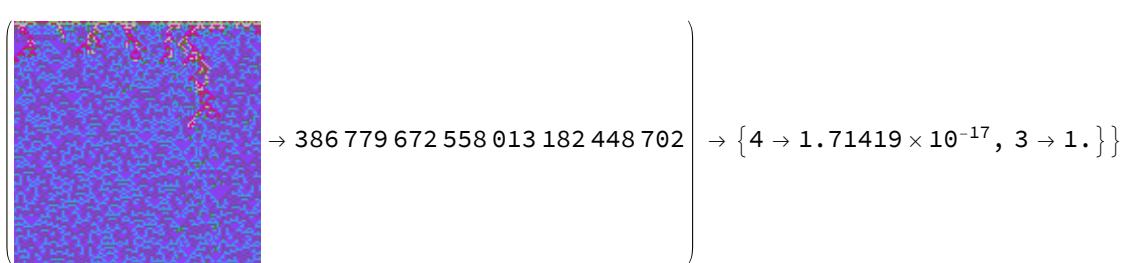
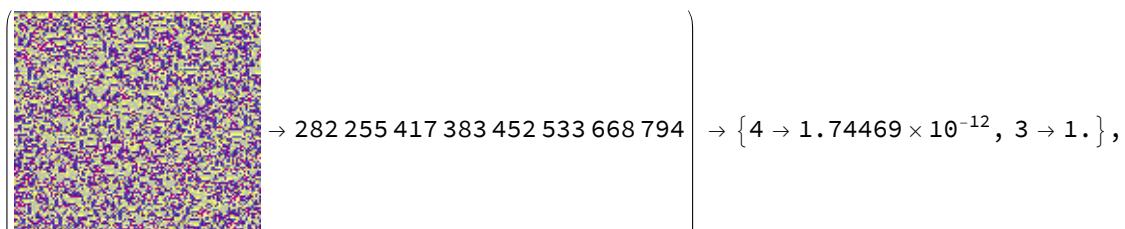
9-colour totalistic, range 1

```
In[164]:= test4Data9kr1C19 = data9TC[8, 128, 128];
Thread[
  test4Data9kr1C19 &gt;> netECA19[Keys@test4Data9kr1C19, {"TopProbabilities", 2}]]
```

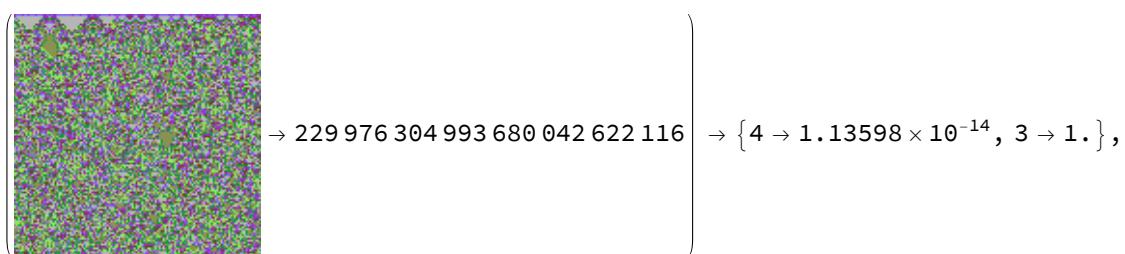
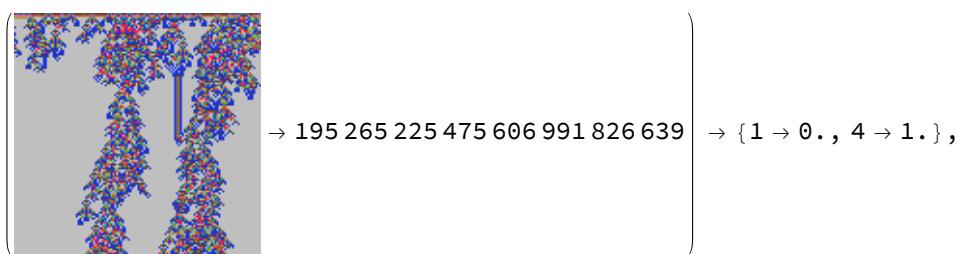
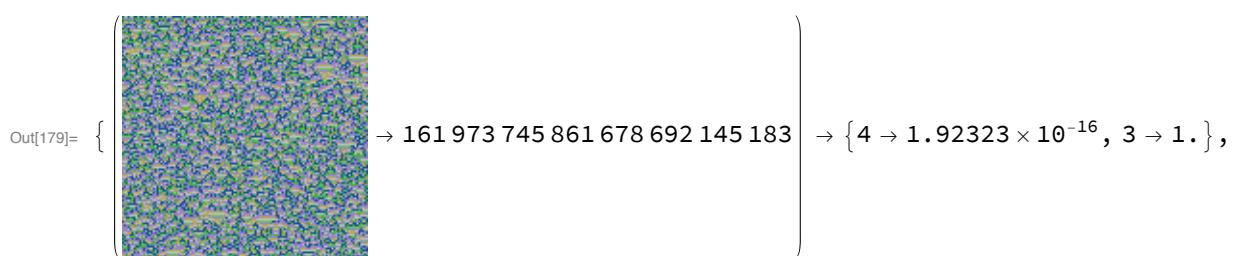


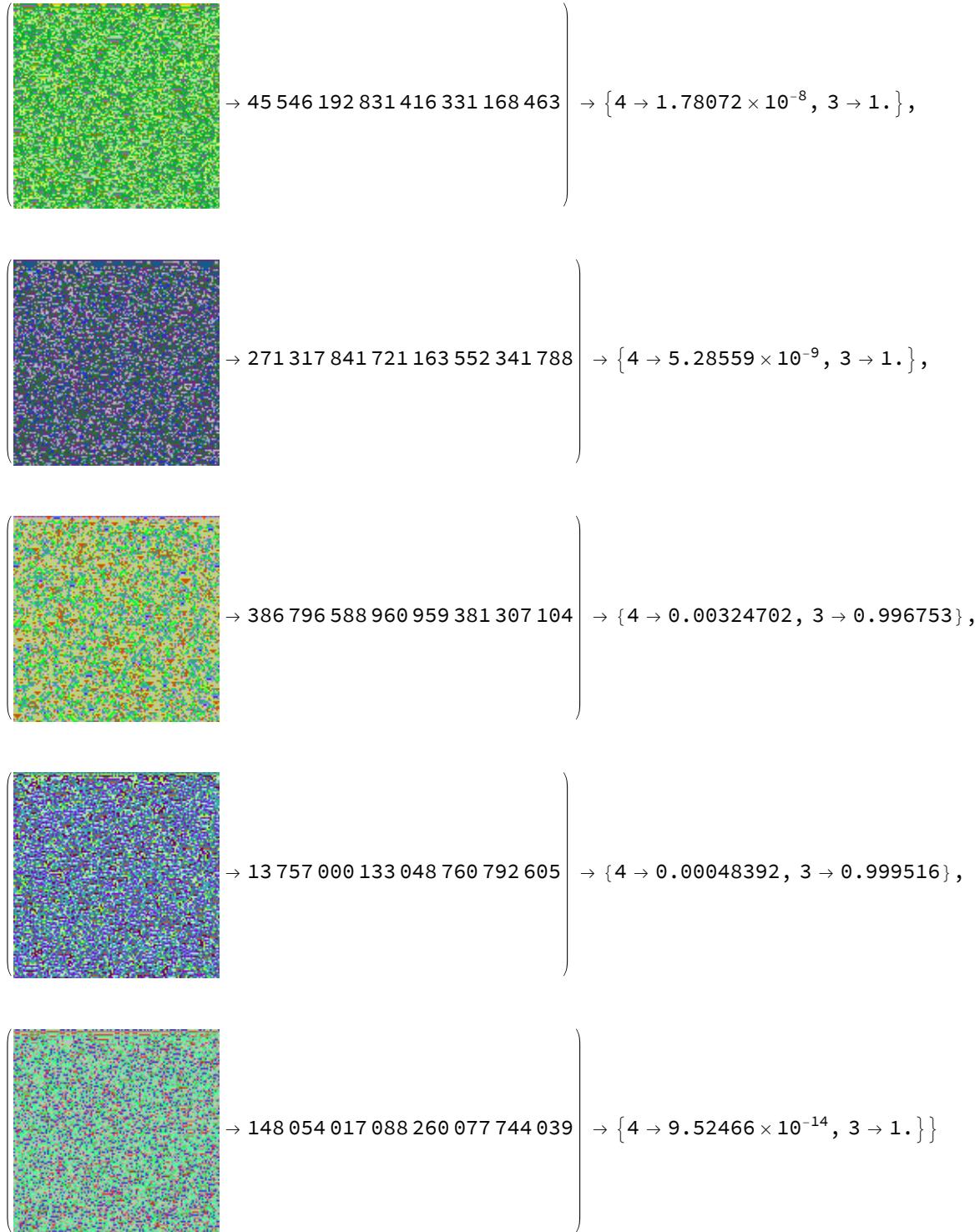






```
In[178]:= test4Data9kr1C19 = data9TC[8, 128, 128];
Thread[
test4Data9kr1C19 → netECA19[Keys@test4Data9kr1C19, {"TopProbabilities", 2}]]
```



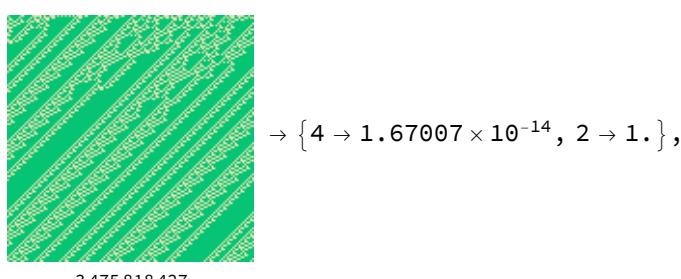
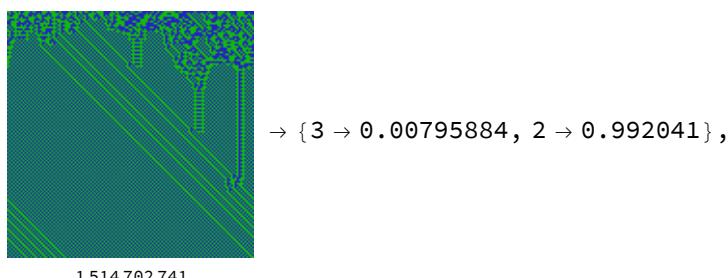
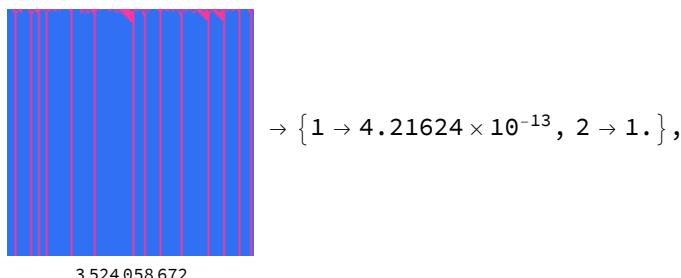
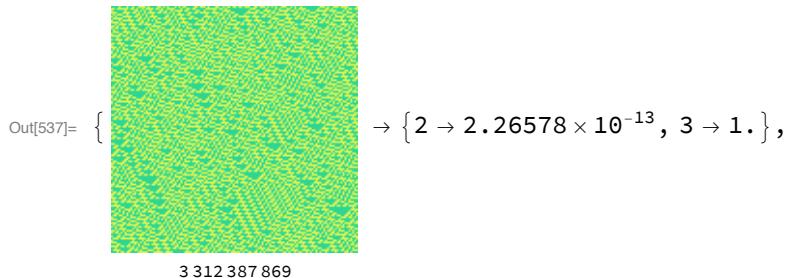


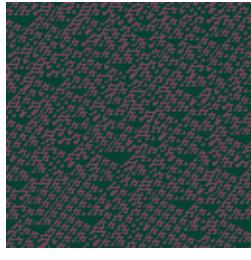
New Format for Unseen CA Testing

Testing Network XVIII (200 epochs) on unseen CA rule spaces - V2

2-colour non-totalistic, range 2

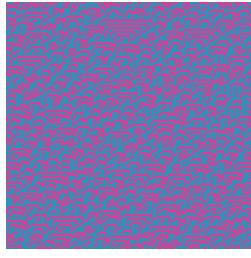
```
In[535]:= test4Data2kr2C18 = datak2r2C[128, 128, 8];
test4Data2kr2C18labeled = Thread[Labeled[
  Keys@test4Data2kr2C18, Values@test4Data2kr2C18, LabelStyle -> Small]];
Thread[test4Data2kr2C18labeled -> netECA18[Keys@test4Data2kr2C18,
 {"TopProbabilities", 2}]]
```





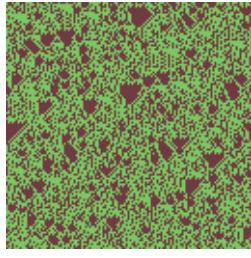
$$\rightarrow \{4 \rightarrow 1.01054 \times 10^{-21}, 3 \rightarrow 1.\},$$

1 083 655 580



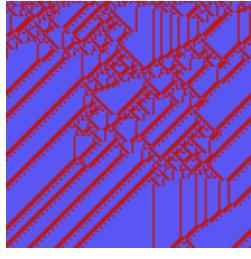
$$\rightarrow \{4 \rightarrow 3.28444 \times 10^{-8}, 3 \rightarrow 1.\},$$

1 874 576 323



$$\rightarrow \{4 \rightarrow 2.23374 \times 10^{-7}, 3 \rightarrow 1.\},$$

3 605 674 388

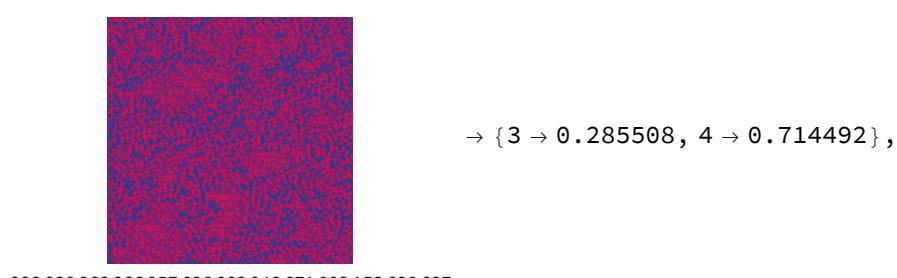
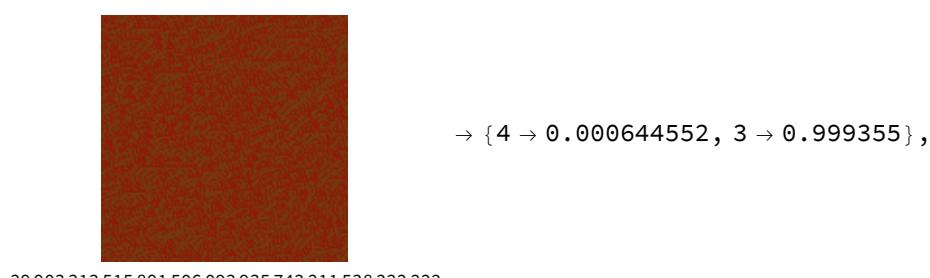
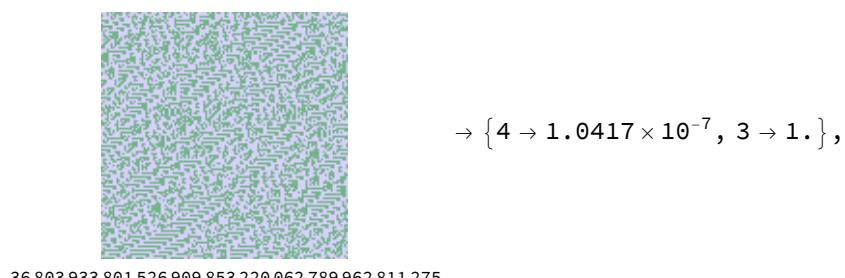
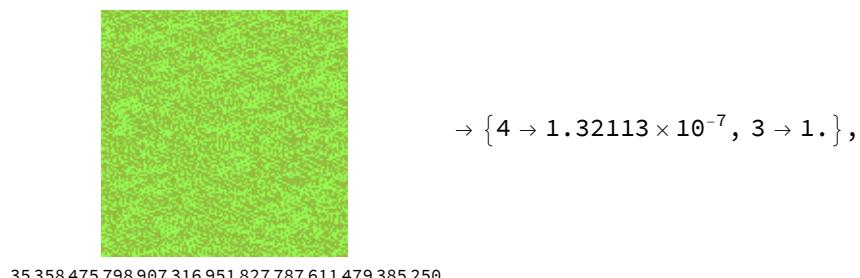
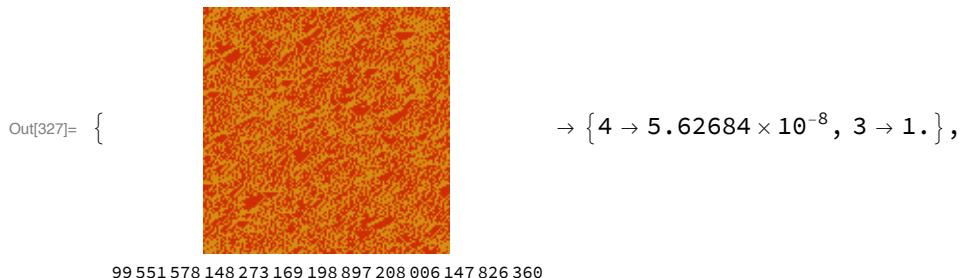


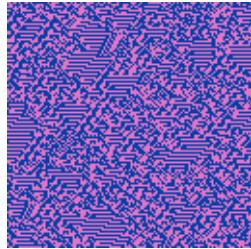
$$\rightarrow \{3 \rightarrow 2.80205 \times 10^{-10}, 4 \rightarrow 1.\}\}$$

1 126 749 880

2-colour non-totalistic, range 3

```
In[325]:= test4Data2kr3C18 = datak2r3NT[128, 128, 8];
test4Data2kr3C18labeled = Thread[Labeled[
  Keys@test4Data2kr3C18, Values@test4Data2kr3C18, LabelStyle -> Small]];
Thread[test4Data2kr3C18labeled -> netECA18[Keys@test4Data2kr3C18,
 {"TopProbabilities", 2}]]
```

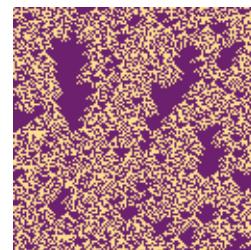



 $\rightarrow \{4 \rightarrow 1.83681 \times 10^{-10}, 3 \rightarrow 1.\},$

12 468 494 678 383 889 361 821 753 917 325 448 539


 $\rightarrow \{4 \rightarrow 1.0842 \times 10^{-19}, 3 \rightarrow 1.\},$

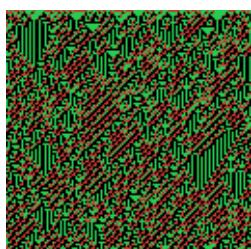
44 305 856 055 937 701 345 862 540 328 298 186 550


 $\rightarrow \{3 \rightarrow 9.105 \times 10^{-6}, 4 \rightarrow 0.999991\}\}$

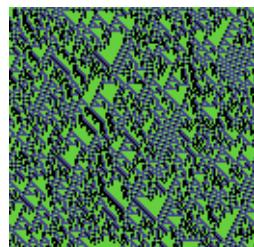
267 617 510 768 053 109 256 323 006 038 446 324 056

3-colour non-totalistic, range 1

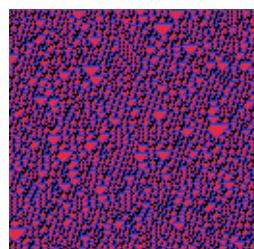
```
In[331]:= test4Data3kr1C18 = datak3r1NT[128, 128, 8];
test4Data3kr1C18labeled = Thread[Labeled[
  Keys@test4Data3kr1C18, Values@test4Data3kr1C18, LabelStyle -> Small]];
Thread[test4Data3kr1C18labeled -> netECA18[Keys@test4Data3kr1C18,
  {"TopProbabilities", 2}]]
```


 $\rightarrow \{3 \rightarrow 0.0917874, 4 \rightarrow 0.908213\},$

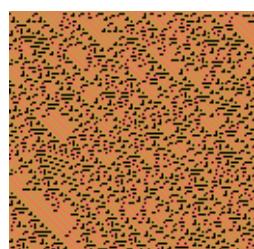
1 571 302 467 213


$$\rightarrow \{3 \rightarrow 4.22647 \times 10^{-10}, 4 \rightarrow 1.\},$$

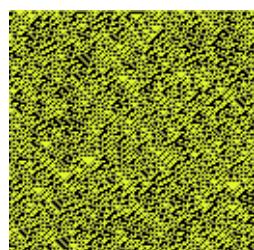
3 341 423 193 643


$$\rightarrow \{4 \rightarrow 1.09209 \times 10^{-6}, 3 \rightarrow 0.999999\},$$

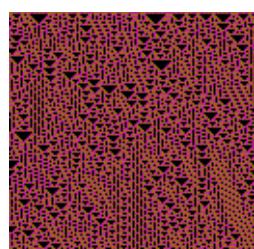
6 038 131 516 158


$$\rightarrow \{4 \rightarrow 0.0019874, 3 \rightarrow 0.998013\},$$

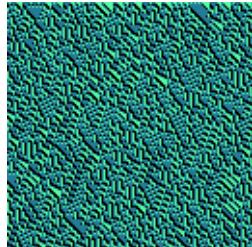
2 964 330 506 711


$$\rightarrow \{4 \rightarrow 0.149341, 3 \rightarrow 0.850659\},$$

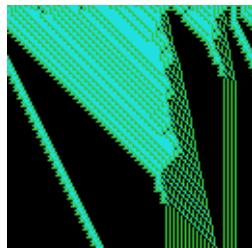
2 043 795 596 664


$$\rightarrow \{4 \rightarrow 4.64997 \times 10^{-15}, 3 \rightarrow 1.\},$$

6 229 038 683 407


 $\rightarrow \{4 \rightarrow 1.23256 \times 10^{-6}, 3 \rightarrow 0.999999\},$

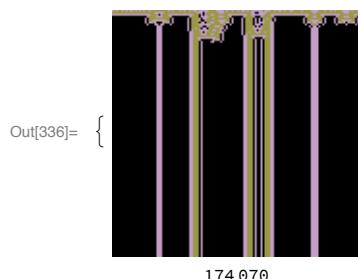
2 323 009 082 805


 $\rightarrow \{2 \rightarrow 5.05033 \times 10^{-6}, 4 \rightarrow 0.999995\}$

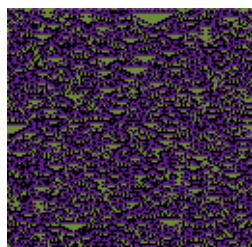
7 237 003 779 873

3-colour totalistic, range 2

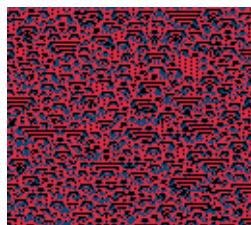
```
In[334]:= test4Data3kr2C18 = datak3r2C[128, 128, 8];
test4Data3kr2C18labeled = Thread[Labeled[
  Keys@test4Data3kr2C18, Values@test4Data3kr2C18, LabelStyle \[Rule] Small]];
Thread[test4Data3kr2C18labeled \[Rule] netECA18[Keys@test4Data3kr2C18,
 {"TopProbabilities", 2}]]
```


 $\rightarrow \{4 \rightarrow 3.78844 \times 10^{-13}, 2 \rightarrow 1.\},$

174 070

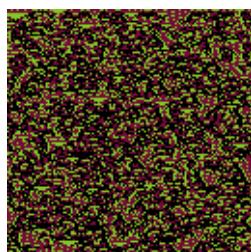

 $\rightarrow \{4 \rightarrow 4.95807 \times 10^{-12}, 3 \rightarrow 1.\},$

108 828



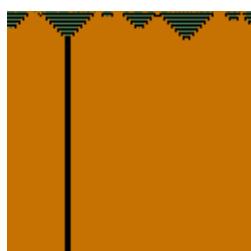
27 791

$$\rightarrow \{4 \rightarrow 7.17529 \times 10^{-14}, 3 \rightarrow 1.\},$$



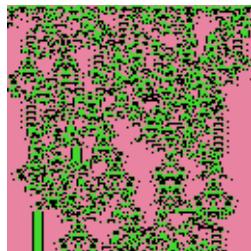
130 620

$$\rightarrow \{4 \rightarrow 3.4037 \times 10^{-10}, 3 \rightarrow 1.\},$$



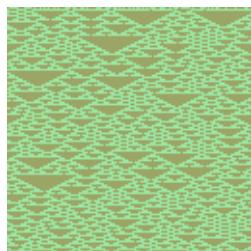
36 125

$$\rightarrow \{1 \rightarrow 2.30518 \times 10^{-32}, 2 \rightarrow 1.\},$$



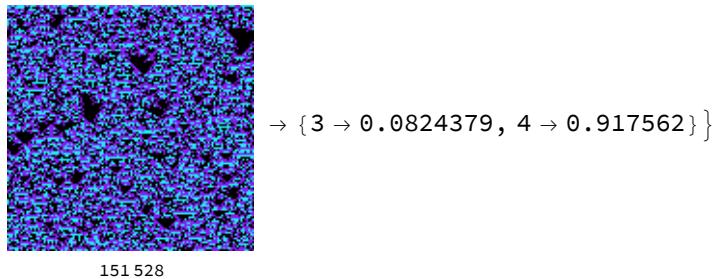
92 996

$$\rightarrow \{3 \rightarrow 1.06918 \times 10^{-9}, 4 \rightarrow 1.\},$$



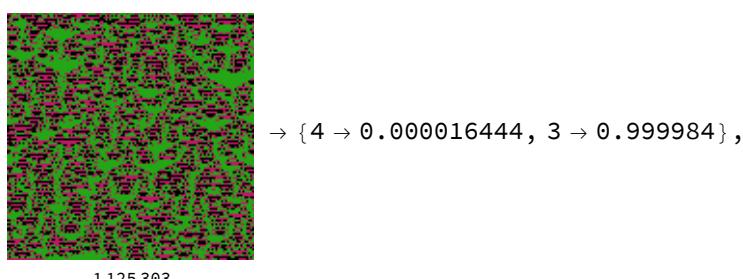
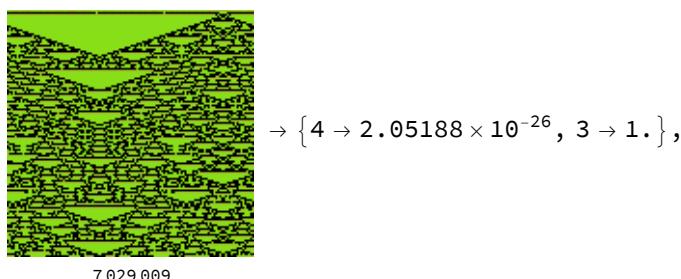
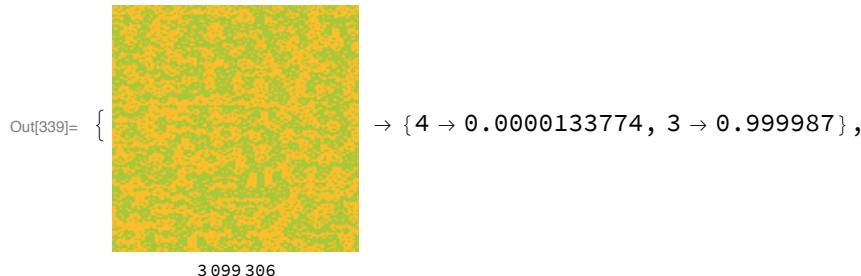
121 053

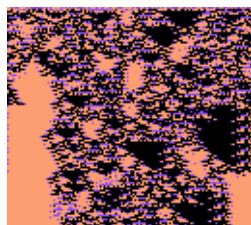
$$\rightarrow \{4 \rightarrow 9.93266 \times 10^{-17}, 3 \rightarrow 1.\},$$



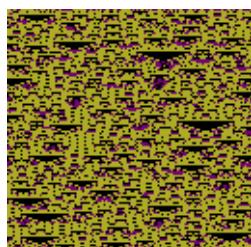
3-colour totalistic, range 3

```
In[337]:= test4Data3kr3C18 = datak3r3C[128, 128, 8];
test4Data3kr3C18labeled = Thread[Labeled[
  Keys@test4Data3kr3C18, Values@test4Data3kr3C18, LabelStyle -> Small]];
Thread[test4Data3kr3C18labeled -> netECA18[Keys@test4Data3kr3C18,
 {"TopProbabilities", 2}]]
```

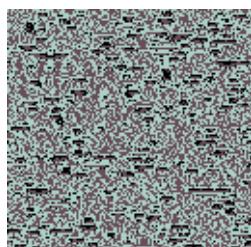


 $\rightarrow \{3 \rightarrow 1.2371 \times 10^{-15}, 4 \rightarrow 1.\},$

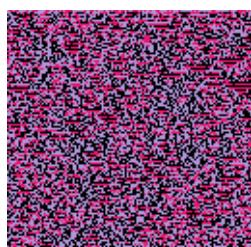
13 655 070

 $\rightarrow \{4 \rightarrow 1.94068 \times 10^{-11}, 3 \rightarrow 1.\},$

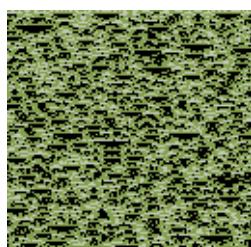
9 614 108

 $\rightarrow \{4 \rightarrow 1.5376 \times 10^{-9}, 3 \rightarrow 1.\},$

11 960 980

 $\rightarrow \{4 \rightarrow 4.52632 \times 10^{-9}, 3 \rightarrow 1.\},$

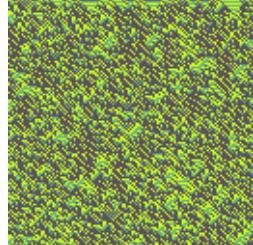
8 698 120

 $\rightarrow \{4 \rightarrow 4.75949 \times 10^{-25}, 3 \rightarrow 1.\}\}$

13 126 418

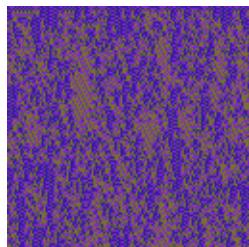
4-colour non-totalistic, range 1

```
In[340]:= test4Data4kr1C18 = datak4r1NT[128, 128, 8];
test4Data4kr1C18labeled = Thread[Labeled[
  Keys@test4Data4kr1C18, Values@test4Data4kr1C18, LabelStyle -> Small]];
Thread[test4Data4kr1C18labeled -> netECA18[Keys@test4Data4kr1C18,
 {"TopProbabilities", 2}]]
```



$$\rightarrow \{4 \rightarrow 3.30619 \times 10^{-13}, 3 \rightarrow 1.\},$$

47 363 336 282 129 006 026 820 981 542 521 963 471



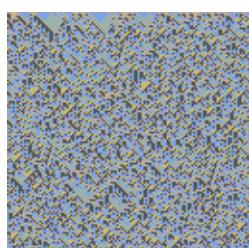
$$\rightarrow \{4 \rightarrow 5.80167 \times 10^{-10}, 3 \rightarrow 1.\},$$

329 817 774 570 860 109 019 844 624 987 993 225 974



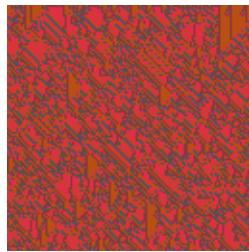
$$\rightarrow \{4 \rightarrow 0.00309639, 3 \rightarrow 0.996904\},$$

296 989 328 924 775 435 626 986 693 102 679 269 368



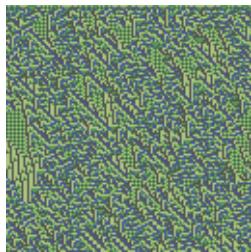
$$\rightarrow \{4 \rightarrow 4.8693 \times 10^{-12}, 3 \rightarrow 1.\},$$

277 043 840 053 627 505 746 917 475 000 616 813 220



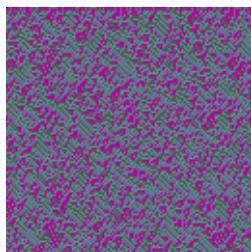
$\rightarrow \{3 \rightarrow 0.000043137, 4 \rightarrow 0.999957\},$

297 372 458 771 516 273 056 931 610 077 577 840 227



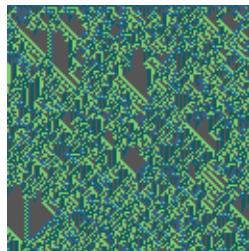
$\rightarrow \{4 \rightarrow 0.0000362744, 3 \rightarrow 0.999964\},$

26 912 895 002 299 472 576 733 451 589 891 132 584



$\rightarrow \{4 \rightarrow 0.000179133, 3 \rightarrow 0.999821\},$

45 190 769 914 069 167 984 586 974 565 370 938 754

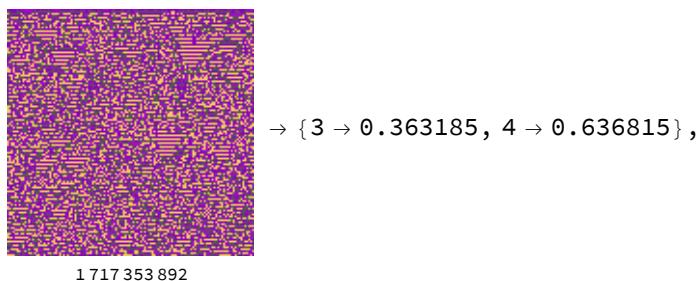
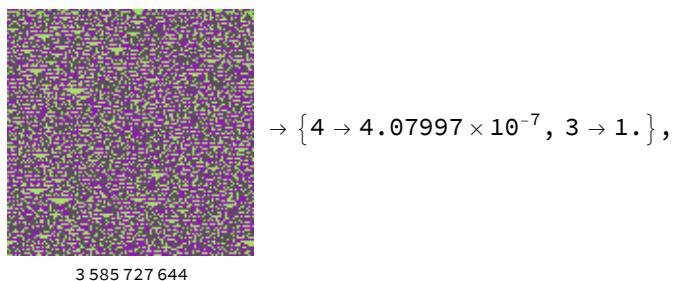
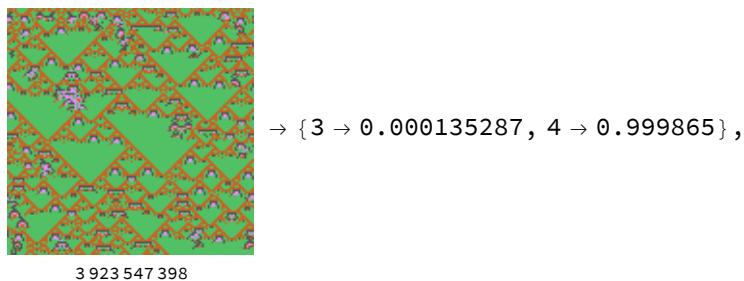
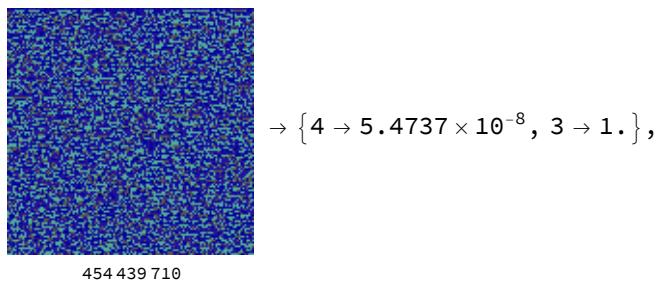
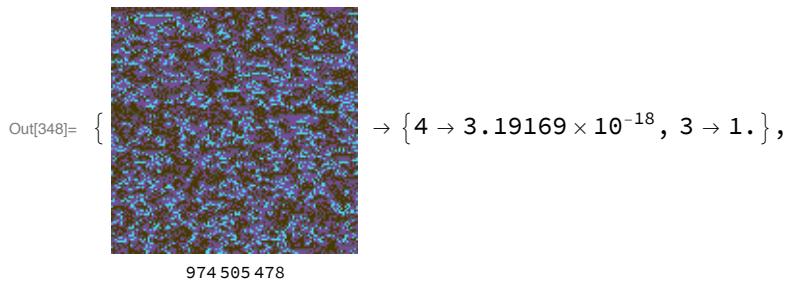


$\rightarrow \{3 \rightarrow 5.37614 \times 10^{-19}, 4 \rightarrow 1.\}\}$

162 808 182 811 890 428 892 567 565 752 290 349 790

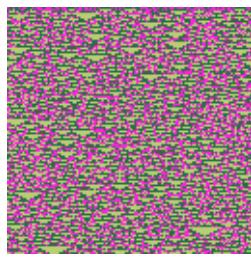
4-colour totalistic, range 2

```
In[346]:= test4Data4kr2C18 = datak4r2C[128, 128, 8];
test4Data4kr2C18labeled = Thread[Labeled[
  Keys@test4Data4kr2C18, Values@test4Data4kr2C18, LabelStyle -> Small]];
Thread[test4Data4kr2C18labeled -> netECA18[Keys@test4Data4kr2C18,
 {"TopProbabilities", 2}]]
```

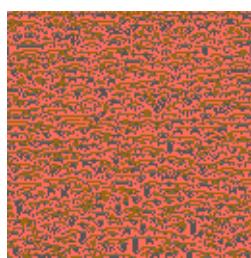




$$\rightarrow \{3 \rightarrow 5.64166 \times 10^{-15}, 4 \rightarrow 1.\},$$



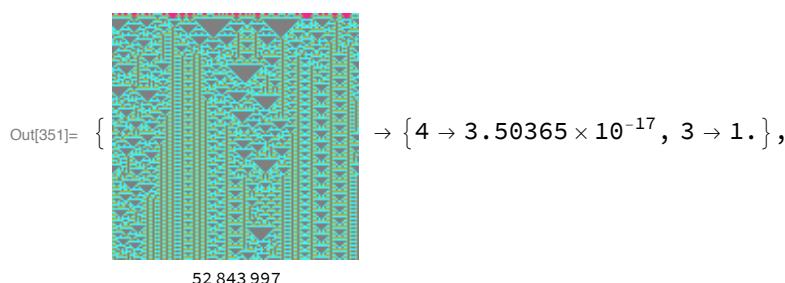
$$\rightarrow \{4 \rightarrow 2.15542 \times 10^{-17}, 3 \rightarrow 1.\},$$



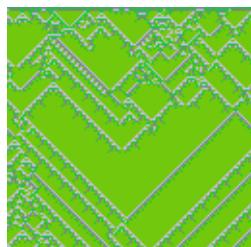
$$\rightarrow \{4 \rightarrow 1.07391 \times 10^{-8}, 3 \rightarrow 1.\}\}$$

5-colour totalistic, range 1

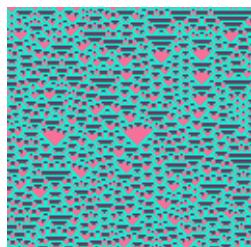
```
In[349]:= test4Data5kr1C18 = data5T2C[8, 128, 128];
test4Data5kr1C18labeled = Thread[Labeled[
  Keys@test4Data5kr1C18, Values@test4Data5kr1C18, LabelStyle -> Small]];
Thread[test4Data5kr1C18labeled -> netECA18[Keys@test4Data5kr1C18,
 {"TopProbabilities", 2}]]
```



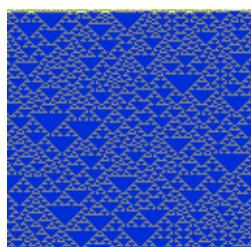
$$\rightarrow \{4 \rightarrow 3.50365 \times 10^{-17}, 3 \rightarrow 1.\},$$

 $\rightarrow \{3 \rightarrow 0.000149786, 4 \rightarrow 0.99985\},$

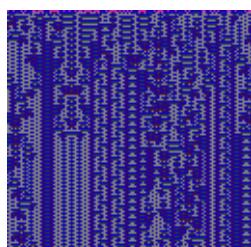
191 855 511

 $\rightarrow \{4 \rightarrow 6.7807 \times 10^{-17}, 3 \rightarrow 1.\},$

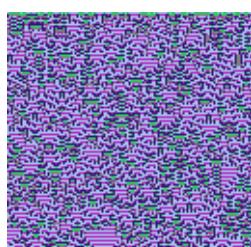
132 578 878

 $\rightarrow \{4 \rightarrow 0.0000493967, 3 \rightarrow 0.999951\},$

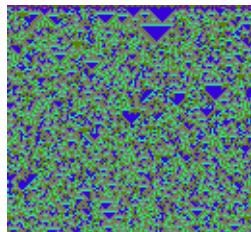
1 050 460 689

 $\rightarrow \{2 \rightarrow 3.37816 \times 10^{-13}, 4 \rightarrow 1.\},$

521 486 054

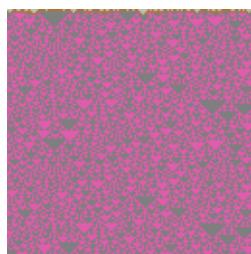
 $\rightarrow \{4 \rightarrow 9.39393 \times 10^{-8}, 3 \rightarrow 1.\},$

208 155 477



$\rightarrow \{4 \rightarrow 2.54559 \times 10^{-18}, 3 \rightarrow 1.\},$

1 151 305 852

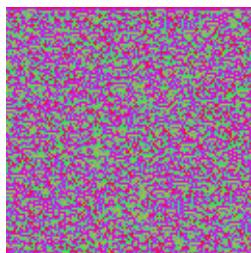


$\rightarrow \{4 \rightarrow 1.2891 \times 10^{-27}, 3 \rightarrow 1.\}\}$

1 054 499 680

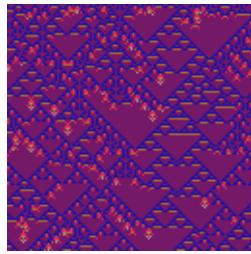
6-colour totalistic, range 1

```
In[352]:= test4Data6kr1C18 = data6TC[8, 128, 128];
test4Data6kr1C18labeled = Thread[Labeled[
  Keys@test4Data6kr1C18, Values@test4Data6kr1C18, LabelStyle -> Small]];
Thread[test4Data6kr1C18labeled -> netECA18[Keys@test4Data6kr1C18,
 {"TopProbabilities", 2}]]
```



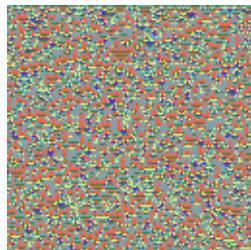
$\rightarrow \{4 \rightarrow 0.000143323, 3 \rightarrow 0.999857\},$

2 087 706 472 301



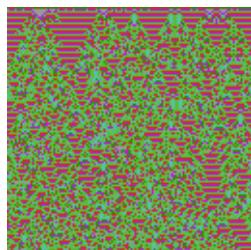
$\rightarrow \{3 \rightarrow 4.24896 \times 10^{-11}, 4 \rightarrow 1.\},$

1 359 662 596 278



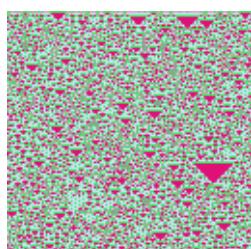
101 715 726 127

$$\rightarrow \{4 \rightarrow 2.22334 \times 10^{-10}, 3 \rightarrow 1.\},$$



626 135 479 216

$$\rightarrow \{4 \rightarrow 0.00949019, 3 \rightarrow 0.99051\},$$



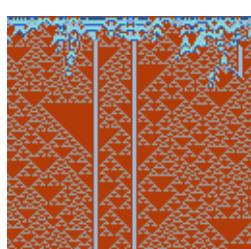
236 160 187 623

$$\rightarrow \{4 \rightarrow 2.7105 \times 10^{-17}, 3 \rightarrow 1.\},$$



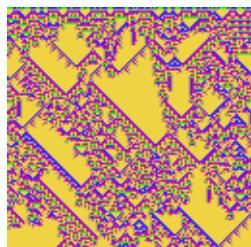
2 194 216 283 700

$$\rightarrow \{2 \rightarrow 0.000408826, 1 \rightarrow 0.999591\},$$



282 791 124 711

$$\rightarrow \{3 \rightarrow 1.58059 \times 10^{-15}, 4 \rightarrow 1.\},$$

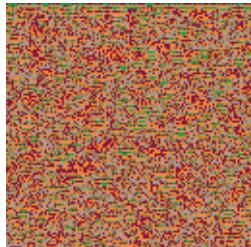


$$\rightarrow \{3 \rightarrow 2.46304 \times 10^{-19}, 4 \rightarrow 1.\} \}$$

585 122 220 446

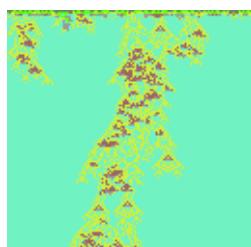
6-colour totalistic, range 2

```
In[355]:= test4Data6kr2C18 = data6T2C[8, 128, 128];
test4Data6kr2C18labeled = Thread[Labeled[
  Keys@test4Data6kr2C18, Values@test4Data6kr2C18, LabelStyle -> Small]];
Thread[test4Data6kr2C18labeled -> netECA18[Keys@test4Data6kr2C18,
  {"TopProbabilities", 2}]]
```



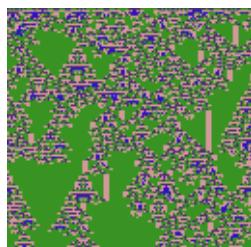
$$\rightarrow \{4 \rightarrow 1.56299 \times 10^{-6}, 3 \rightarrow 0.999998\},$$

Out[357]= { }



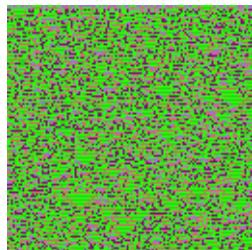
$$\rightarrow \{3 \rightarrow 1.71257 \times 10^{-19}, 4 \rightarrow 1.\},$$

170 164 089 950 923 780 299



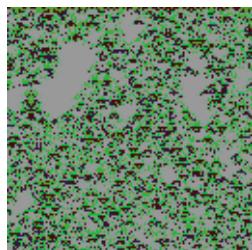
$$\rightarrow \{3 \rightarrow 8.95514 \times 10^{-13}, 4 \rightarrow 1.\},$$

155 892 327 712 219 067 638



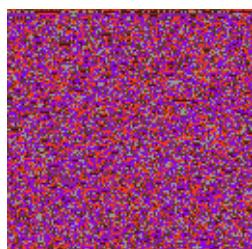
$$\rightarrow \{4 \rightarrow 1.25818 \times 10^{-8}, 3 \rightarrow 1.\},$$

93 368 100 412 663 805 755



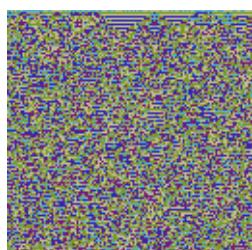
$$\rightarrow \{4 \rightarrow 4.75288 \times 10^{-6}, 3 \rightarrow 0.999995\},$$

135 899 886 200 004 305 929



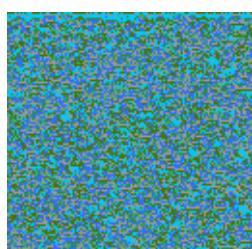
$$\rightarrow \{4 \rightarrow 3.28831 \times 10^{-13}, 3 \rightarrow 1.\},$$

40 491 495 414 090 990 843



$$\rightarrow \{4 \rightarrow 0.00354854, 3 \rightarrow 0.996451\},$$

52 482 358 297 896 098 096

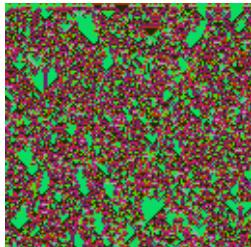


$$\rightarrow \{4 \rightarrow 9.04766 \times 10^{-8}, 3 \rightarrow 1.\}\}$$

126 066 113 157 629 415 623

7-colour totalistic, range 1

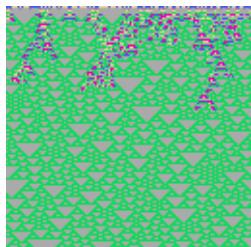
```
In[373]:= test4Data7kr1C18 = data7TC[8, 128, 128];
test4Data7kr1C18labeled = Thread[Labeled[
  Keys@test4Data7kr1C18, Values@test4Data7kr1C18, LabelStyle -> Small]];
Thread[test4Data7kr1C18labeled -> netECA18[Keys@test4Data7kr1C18,
 {"TopProbabilities", 2}]]
```



```
Out[375]= {
```

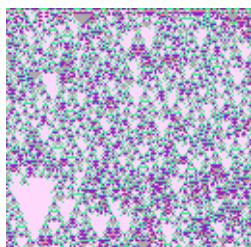
$$\rightarrow \{4 \rightarrow 0.000603501, 3 \rightarrow 0.999397\},$$

5 419 415 476 292 874



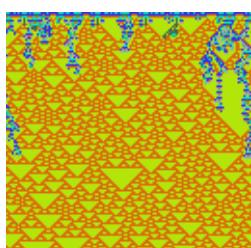
$$\rightarrow \{4 \rightarrow 1.58323 \times 10^{-9}, 3 \rightarrow 1.\},$$

5 263 032 896 718 823



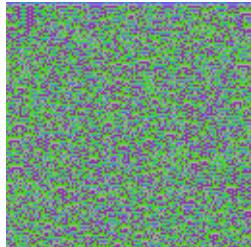
$$\rightarrow \{2 \rightarrow 4.05481 \times 10^{-11}, 4 \rightarrow 1.\},$$

7 020 291 676 264 106

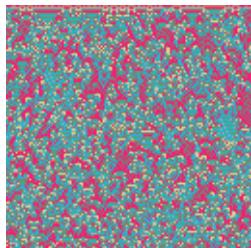


$$\rightarrow \{2 \rightarrow 7.7001 \times 10^{-21}, 4 \rightarrow 1.\},$$

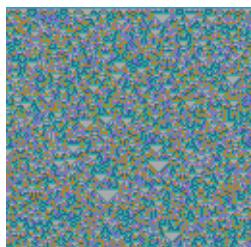
1 156 837 474 592 456


 $\rightarrow \{4 \rightarrow 0.00665255, 3 \rightarrow 0.993347\},$

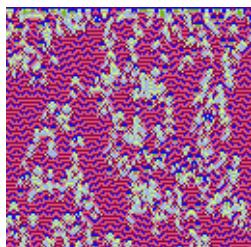
975 822 040 535 045


 $\rightarrow \{4 \rightarrow 2.9215 \times 10^{-8}, 3 \rightarrow 1.\},$

6 831 445 863 597 275


 $\rightarrow \{4 \rightarrow 4.22974 \times 10^{-19}, 3 \rightarrow 1.\},$

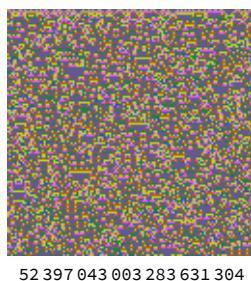
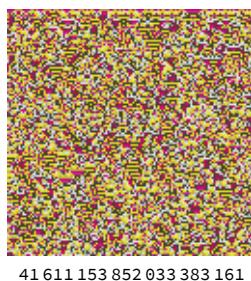
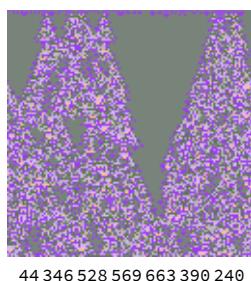
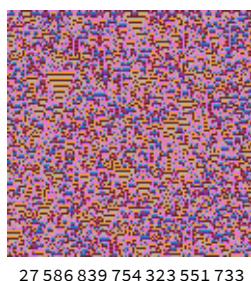
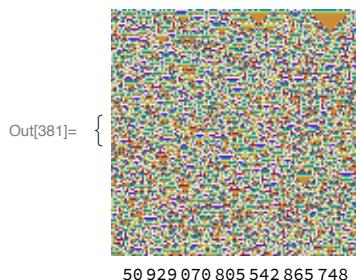
2 999 900 742 201 901

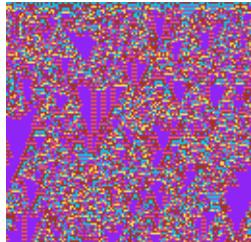

 $\rightarrow \{4 \rightarrow 1.14567 \times 10^{-16}, 3 \rightarrow 1.\}\}$

4 165 489 127 562 489

8-colour totalistic, range 1

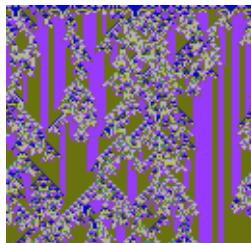
```
In[379]:= test4Data8kr1C18 = data8TC[8, 128, 128];
test4Data8kr1C18labeled = Thread[Labeled[
  Keys@test4Data8kr1C18, Values@test4Data8kr1C18, LabelStyle -> Small]];
Thread[test4Data8kr1C18labeled -> netECA18[Keys@test4Data8kr1C18,
 {"TopProbabilities", 2}]]
```





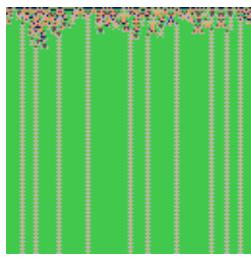
$$\rightarrow \{3 \rightarrow 3.53547 \times 10^{-13}, 4 \rightarrow 1.\},$$

4 859 584 663 297 976 265



$$\rightarrow \{3 \rightarrow 1.23709 \times 10^{-23}, 4 \rightarrow 1.\},$$

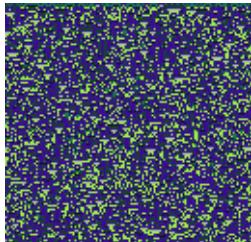
40 462 293 174 819 572 784



$$\rightarrow \{1 \rightarrow 4.45234 \times 10^{-14}, 2 \rightarrow 1.\}\}$$

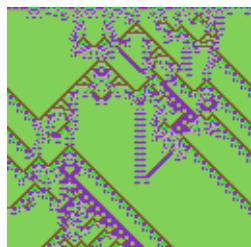
31 565 401 331 503 942 033

```
In[382]:= test4Data8kr1C18 = data8TC[8, 128, 128];
test4Data8kr1C18labeled = Thread[Labeled[
  Keys@test4Data8kr1C18, Values@test4Data8kr1C18, LabelStyle -> Small]];
Thread[test4Data8kr1C18labeled -> netECA18[Keys@test4Data8kr1C18,
  {"TopProbabilities", 2}]]
```

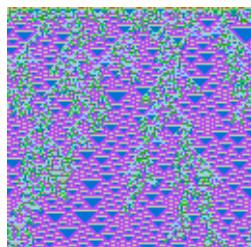


$$\rightarrow \{4 \rightarrow 1.29992 \times 10^{-6}, 3 \rightarrow 0.999999\},$$

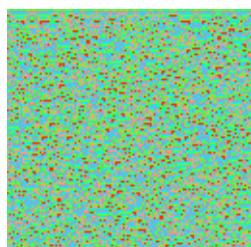
37 704 545 164 847 890 018

 $\rightarrow \{3 \rightarrow 9.65757 \times 10^{-15}, 4 \rightarrow 1.\},$

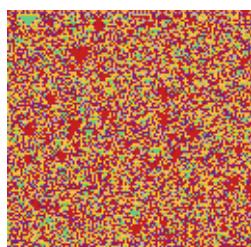
27 648 091 129 795 825 837

 $\rightarrow \{4 \rightarrow 3.23122 \times 10^{-6}, 3 \rightarrow 0.999997\},$

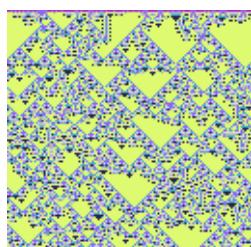
60 505 018 748 296 148 542

 $\rightarrow \{4 \rightarrow 3.09422 \times 10^{-6}, 3 \rightarrow 0.999997\},$

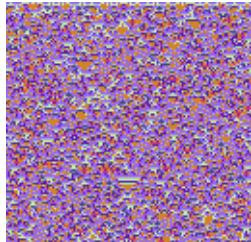
54 287 354 911 476 152 107

 $\rightarrow \{4 \rightarrow 1.61319 \times 10^{-13}, 3 \rightarrow 1.\},$

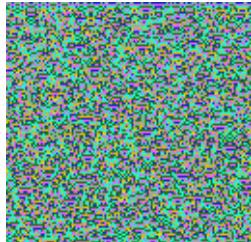
51 683 500 767 429 363 920

 $\rightarrow \{4 \rightarrow 0.0000932216, 3 \rightarrow 0.999907\},$

41 609 680 851 379 694 800


 $\rightarrow \{4 \rightarrow 1.21235 \times 10^{-9}, 3 \rightarrow 1.\},$

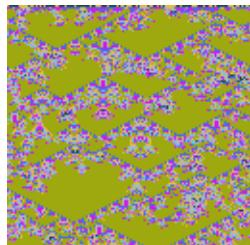
63 509 679 527 843 614 538


 $\rightarrow \{4 \rightarrow 1.98827 \times 10^{-9}, 3 \rightarrow 1.\}\}$

6 460 427 784 035 907 917

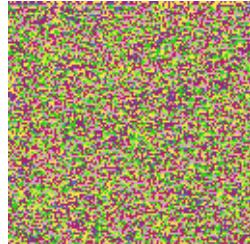
8-colour totalistic, range 2

```
In[487]:= test4Data8kr2C18 = data8T2C[8, 128, 128];
test4Data8kr2C18labeled = Thread[Labeled[
  Keys@test4Data8kr2C18, Values@test4Data8kr2C18, LabelStyle -> Small]];
Thread[test4Data8kr2C18labeled -> netECA18[Keys@test4Data8kr2C18,
 {"TopProbabilities", 2}]]
```

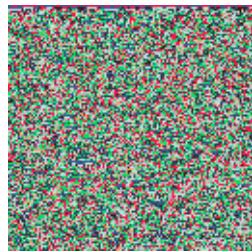

 $\rightarrow \{3 \rightarrow 7.88283 \times 10^{-12}, 4 \rightarrow 1.\},$

Out[489]= {

229 321 369 541 173 903 171 226 198 126 330

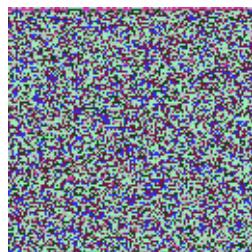

 $\rightarrow \{4 \rightarrow 0.00109673, 3 \rightarrow 0.998903\},$

291 185 141 089 185 274 214 583 413 507 046



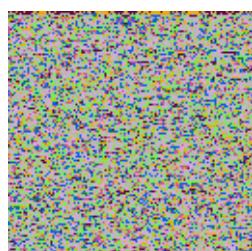
$\rightarrow \{4 \rightarrow 0.000326178, 3 \rightarrow 0.999674\},$

282 186 565 988 139 310 685 504 387 498 444



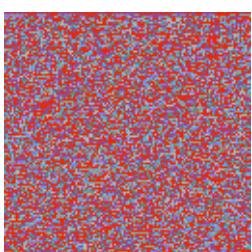
$\rightarrow \{4 \rightarrow 1.02374 \times 10^{-9}, 3 \rightarrow 1.\},$

112 532 574 870 883 354 099 356 064 113 252



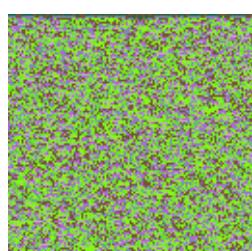
$\rightarrow \{4 \rightarrow 1.24142 \times 10^{-11}, 3 \rightarrow 1.\},$

236 991 826 693 416 819 134 399 943 087 298



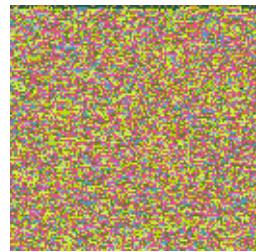
$\rightarrow \{4 \rightarrow 1.45662 \times 10^{-13}, 3 \rightarrow 1.\},$

63 680 569 239 782 716 398 778 656 016 965



$\rightarrow \{4 \rightarrow 6.68537 \times 10^{-7}, 3 \rightarrow 0.999999\},$

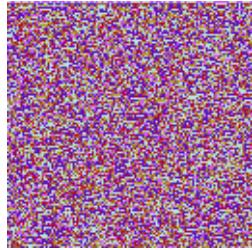
308 344 304 481 068 219 036 959 151 470 092


 $\rightarrow \{4 \rightarrow 1.57705 \times 10^{-8}, 3 \rightarrow 1.\}\}$

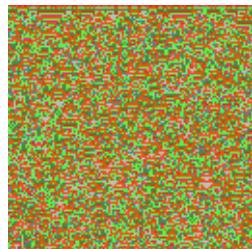
105 724 215 011 096 612 281 834 858 043 422

9-colour totalistic, range 1

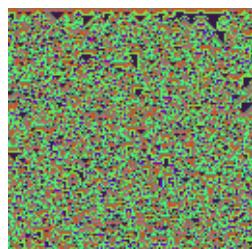
```
In[496]:= test4Data9kr1C18 = data9TC[8, 128, 128];
test4Data9kr1C18labeled = Thread[Labeled[
  Keys@test4Data9kr1C18, Values@test4Data9kr1C18, LabelStyle -> Small]];
Thread[test4Data9kr1C18labeled -> netECA18[Keys@test4Data9kr1C18,
 {"TopProbabilities", 2}]]
```


 $\rightarrow \{4 \rightarrow 5.83823 \times 10^{-9}, 3 \rightarrow 1.\},$

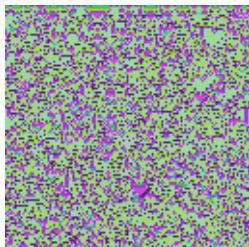
457 094 757 911 682 583 135 513


 $\rightarrow \{4 \rightarrow 0.0000180204, 3 \rightarrow 0.999982\},$

425 392 860 893 969 211 015 901

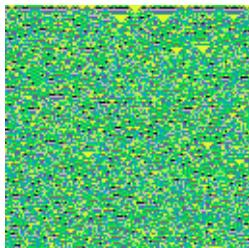

 $\rightarrow \{4 \rightarrow 4.45654 \times 10^{-7}, 3 \rightarrow 1.\},$

619 273 769 732 372 476 607 237



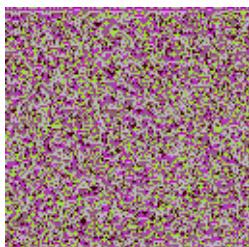
$$\rightarrow \{4 \rightarrow 8.57981 \times 10^{-11}, 3 \rightarrow 1.\},$$

529 952 216 513 222 451 975 404



$$\rightarrow \{4 \rightarrow 2.43131 \times 10^{-7}, 3 \rightarrow 1.\},$$

180 356 719 388 510 007 067 549



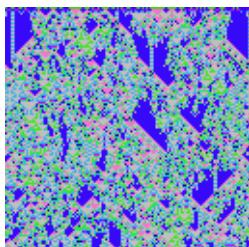
$$\rightarrow \{4 \rightarrow 1.51658 \times 10^{-8}, 3 \rightarrow 1.\},$$

433 148 230 728 762 736 100 900



$$\rightarrow \{4 \rightarrow 6.70076 \times 10^{-10}, 3 \rightarrow 1.\},$$

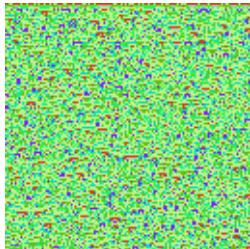
396 827 895 882 577 775 438 185



$$\rightarrow \{2 \rightarrow 4.02659 \times 10^{-6}, 4 \rightarrow 0.999996\}\}$$

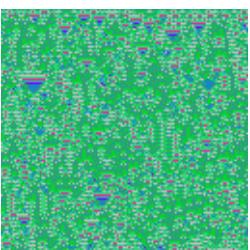
351 429 815 695 311 172 396 620

```
In[511]:= test4Data9kr1C18 = data9TC[8, 128, 128];
test4Data9kr1C18labeled = Thread[Labeled[
  Keys@test4Data9kr1C18, Values@test4Data9kr1C18, LabelStyle -> Small]];
Thread[test4Data9kr1C18labeled -> netECA18[Keys@test4Data9kr1C18,
 {"TopProbabilities", 2}]]
```



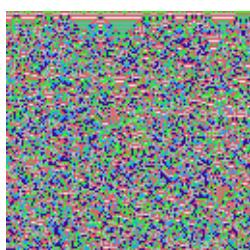
Out[513]= $\{ \rightarrow \{4 \rightarrow 2.58219 \times 10^{-8}, 3 \rightarrow 1.\},$

571 898 225 263 709 171 935 181



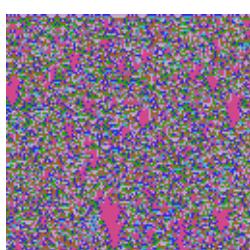
$\rightarrow \{4 \rightarrow 4.17492 \times 10^{-16}, 3 \rightarrow 1.\},$

16 416 436 883 866 903 040 539



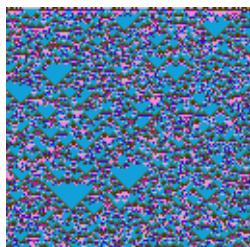
$\rightarrow \{4 \rightarrow 6.31934 \times 10^{-11}, 3 \rightarrow 1.\},$

505 080 187 994 424 945 599 908



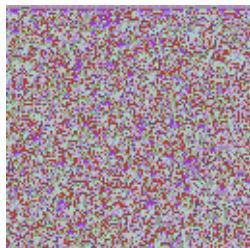
$\rightarrow \{3 \rightarrow 9.02887 \times 10^{-6}, 4 \rightarrow 0.999991\},$

405 543 563 336 574 719 930 798



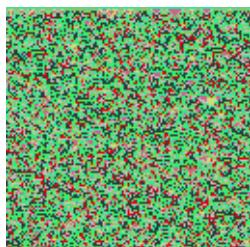
$$\rightarrow \{ 4 \rightarrow 1.01538 \times 10^{-9}, 3 \rightarrow 1. \},$$

640 899 150 274 978 311 294 101



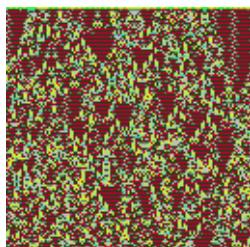
$$\rightarrow \{ 4 \rightarrow 1.45824 \times 10^{-11}, 3 \rightarrow 1. \},$$

477 880 861 207 247 090 323 396



$$\rightarrow \{ 4 \rightarrow 9.03987 \times 10^{-7}, 3 \rightarrow 0.999999 \},$$

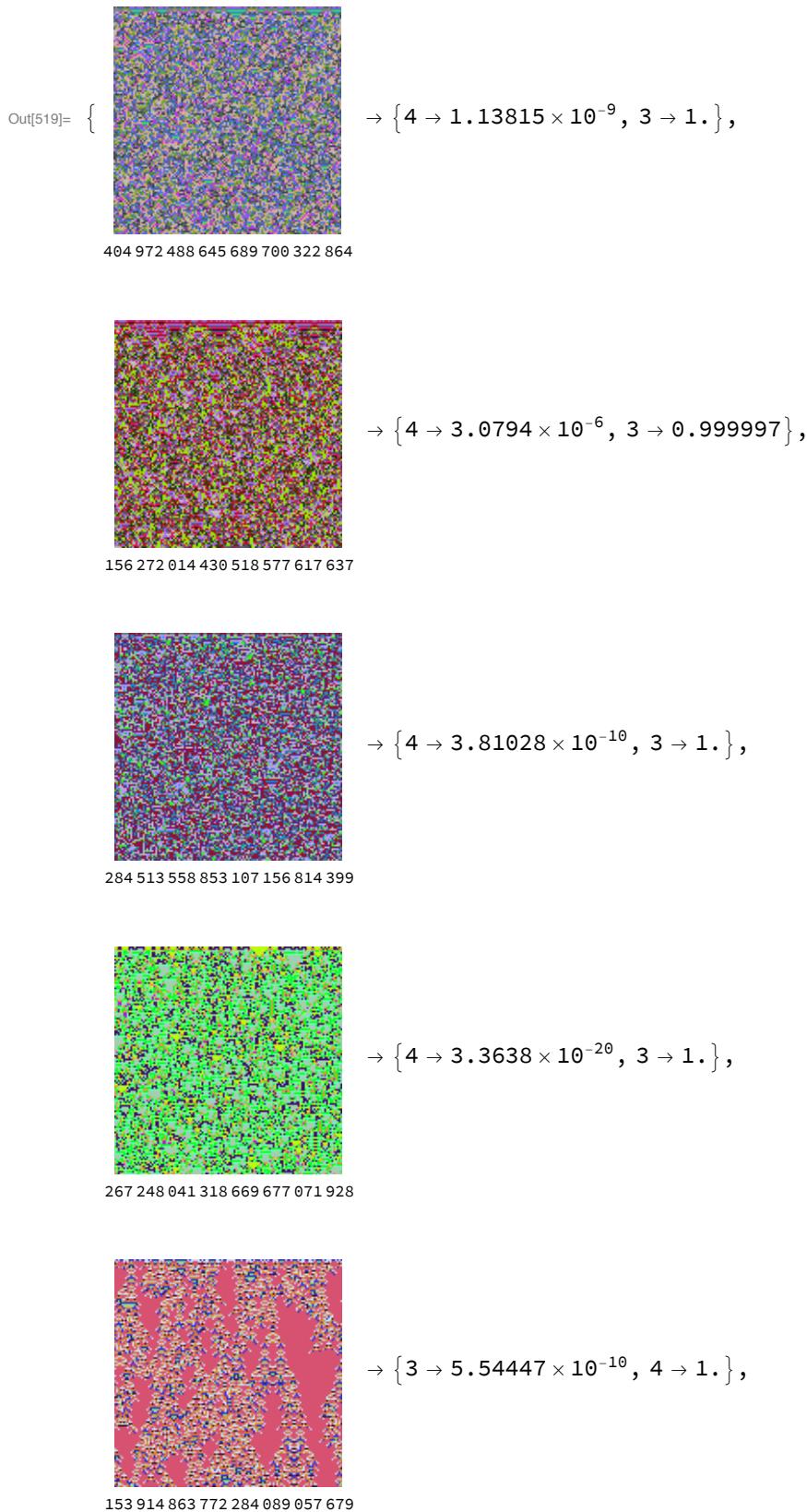
356 314 942 681 551 111 282 584

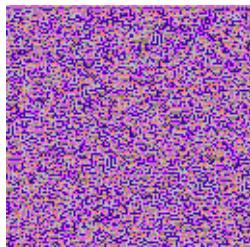


$$\rightarrow \{ 3 \rightarrow 0.000582645, 4 \rightarrow 0.999417 \}$$

298 013 848 612 651 157 159 625

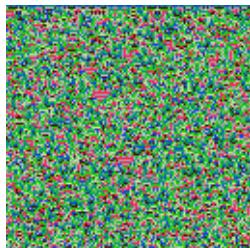
```
In[517]:= test4Data9kr1C18 = data9TC[8, 128, 128];
test4Data9kr1C18labeled = Thread[Labeled[
  Keys@test4Data9kr1C18, Values@test4Data9kr1C18, LabelStyle -> Small]];
Thread[test4Data9kr1C18labeled -> netECA18[Keys@test4Data9kr1C18,
  {"TopProbabilities", 2}]]
```





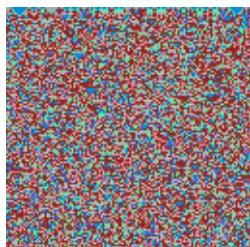
$$\rightarrow \{4 \rightarrow 1.13692 \times 10^{-9}, 3 \rightarrow 1.\},$$

254 141 771 646 448 052 827 109



$$\rightarrow \{4 \rightarrow 5.3356 \times 10^{-12}, 3 \rightarrow 1.\},$$

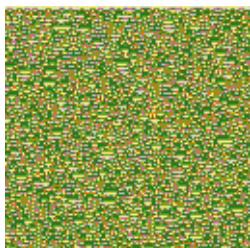
404 793 401 643 156 100 738 375



$$\rightarrow \{4 \rightarrow 6.60115 \times 10^{-9}, 3 \rightarrow 1.\}\}$$

670 268 613 476 400 266 631 186

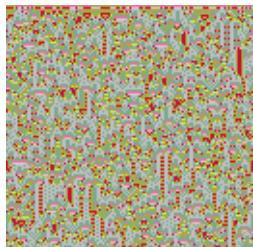
```
In[523]:= test4Data9kr1C18 = data9TC[8, 128, 128];
test4Data9kr1C18labeled = Thread[Labeled[
  Keys@test4Data9kr1C18, Values@test4Data9kr1C18, LabelStyle -> Small]];
Thread[test4Data9kr1C18labeled -> netECA18[Keys@test4Data9kr1C18,
 {"TopProbabilities", 2}]]
```



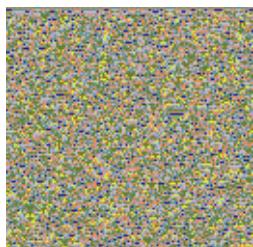
$$\rightarrow \{4 \rightarrow 2.4276 \times 10^{-9}, 3 \rightarrow 1.\},$$

Out[525]= {

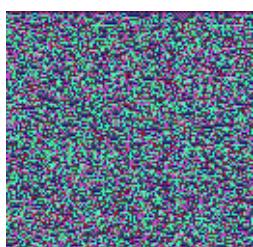
355 971 169 427 388 040 424 582

 $\rightarrow \{3 \rightarrow 0.059592, 4 \rightarrow 0.940408\},$

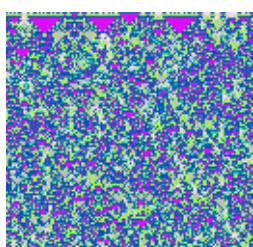
533 897 222 146 305 160 363 448

 $\rightarrow \{4 \rightarrow 2.29648 \times 10^{-11}, 3 \rightarrow 1.\},$

691 506 306 126 519 782 511 638

 $\rightarrow \{4 \rightarrow 0.0929386, 3 \rightarrow 0.907061\},$

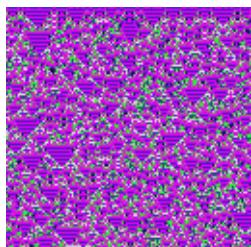
323 208 263 876 392 814 574 412

 $\rightarrow \{4 \rightarrow 7.66009 \times 10^{-12}, 3 \rightarrow 1.\},$

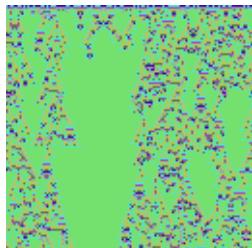
616 227 181 029 580 959 691 458

 $\rightarrow \{4 \rightarrow 6.44332 \times 10^{-9}, 3 \rightarrow 1.\},$

190 650 889 368 707 191 921 149


 $\rightarrow \{4 \rightarrow 1.31887 \times 10^{-21}, 3 \rightarrow 1.\},$

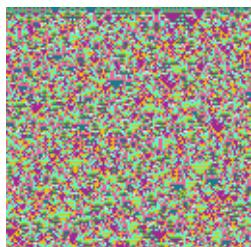
73 319 162 863 689 362 047 643


 $\rightarrow \{3 \rightarrow 6.58991 \times 10^{-13}, 4 \rightarrow 1.\}\}$

287 724 570 221 091 851 404 918

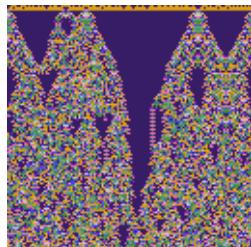
10-colour totalistic, range 1

```
In[1428]:= test4Data10kr1C18 = data10TC[8, 128, 128];
test4Data10kr1C18labeled = Thread[Labeled[
  Keys@test4Data10kr1C18, Values@test4Data10kr1C18, LabelStyle -> Small]];
Thread[test4Data10kr1C18labeled -> netECA18[Keys@test4Data10kr1C18,
  {"TopProbabilities", 2}]]
```

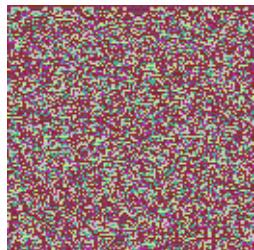

 $\rightarrow \{4 \rightarrow 6.66216 \times 10^{-6}, 3 \rightarrow 0.999993\},$

Out[1430]= {

1 903 096 544 443 096 393 988 581 973

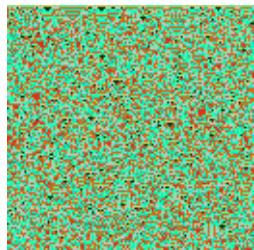

 $\rightarrow \{3 \rightarrow 8.7366 \times 10^{-26}, 4 \rightarrow 1.\},$

4 036 261 294 900 174 856 088 230 770



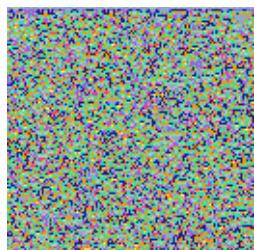
$\rightarrow \{4 \rightarrow 5.38208 \times 10^{-7}, 3 \rightarrow 0.999999\},$

5 776 611 602 355 309 071 925 208 128



$\rightarrow \{4 \rightarrow 0.0000249653, 3 \rightarrow 0.999975\},$

9 368 607 075 136 056 205 288 539 286



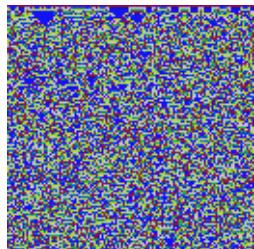
$\rightarrow \{4 \rightarrow 4.39227 \times 10^{-11}, 3 \rightarrow 1.\},$

1 159 609 440 706 048 934 937 421 381



$\rightarrow \{4 \rightarrow 0.0000298941, 3 \rightarrow 0.99997\},$

9 585 758 006 399 290 542 154 306 334



$\rightarrow \{4 \rightarrow 8.01368 \times 10^{-14}, 3 \rightarrow 1.\},$

7 176 425 566 624 142 460 503 296 528

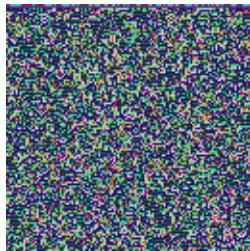


$$\rightarrow \{4 \rightarrow 2.83049 \times 10^{-14}, 3 \rightarrow 1.\} \}$$

3 224 320 499 780 698 506 582 500 278

11-colour totalistic, range 1

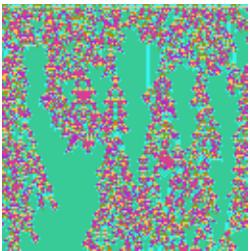
```
In[1440]:= test4Data11kr1C18 = data11TC[8, 128, 128];
test4Data11kr1C18labeled = Thread[Labeled[
  Keys@test4Data11kr1C18, Values@test4Data11kr1C18, LabelStyle -> Small]];
Thread[test4Data11kr1C18labeled -> netECA18[Keys@test4Data11kr1C18,
  {"TopProbabilities", 2}]]
```



$$\rightarrow \{4 \rightarrow 9.41752 \times 10^{-9}, 3 \rightarrow 1.\},$$

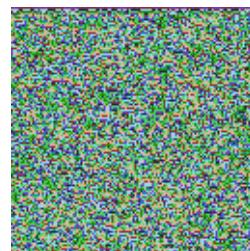
Out[1442]= {

27 602 157 973 840 641 007 105 652 106 671



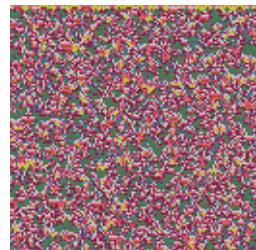
$$\rightarrow \{2 \rightarrow 1.96872 \times 10^{-15}, 4 \rightarrow 1.\},$$

9 422 428 048 625 511 295 094 670 912 285



$$\rightarrow \{4 \rightarrow 1.70571 \times 10^{-6}, 3 \rightarrow 0.999998\},$$

152 007 042 234 913 357 388 586 460 753 588



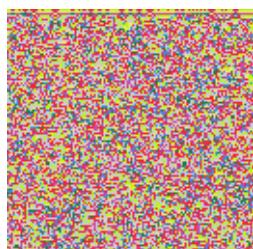
$$\rightarrow \{4 \rightarrow 3.79533 \times 10^{-12}, 3 \rightarrow 1.\},$$

177 741 547 512 091 115 527 598 027 282 597



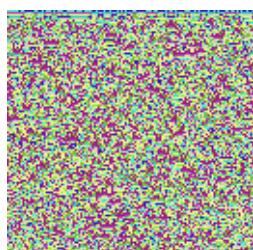
$$\rightarrow \{4 \rightarrow 2.11903 \times 10^{-11}, 3 \rightarrow 1.\},$$

6 410 005 958 600 172 029 712 985 812 034



$$\rightarrow \{4 \rightarrow 0.0000280034, 3 \rightarrow 0.999972\},$$

62 674 162 164 599 079 657 718 948 002 220



$$\rightarrow \{4 \rightarrow 0.000625919, 3 \rightarrow 0.999374\},$$

54 565 635 982 317 707 368 048 715 194 998

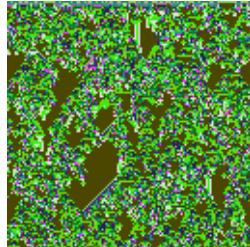


$$\rightarrow \{4 \rightarrow 0.0318018, 3 \rightarrow 0.968198\} \}$$

106 166 310 463 190 697 380 502 476 410 631

18-colour totalistic, range 1

```
In[1450]:= test4Data18kr1C18 = data18TC[8, 128, 128];
test4Data18kr1C18labeled = Thread[Labeled[
  Keys@test4Data18kr1C18, Values@test4Data18kr1C18, LabelStyle -> Small]];
Thread[test4Data18kr1C18labeled -> netECA18[Keys@test4Data18kr1C18,
 {"TopProbabilities", 2}]]
```

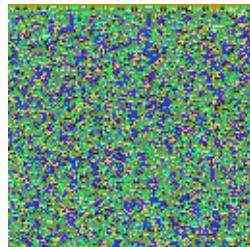


→

Out[1452]= {

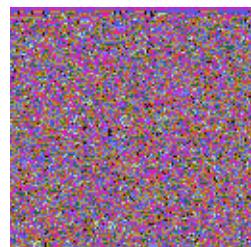
100 432 709 745 221 968 471 400 004 161 272 421 785 313 175 864 424 392 860 092 443 780

{2 → 9.88542 × 10⁻¹⁶, 4 → 1.},



→ {4 → 9.2871 × 10⁻¹², 3 → 1.},

107 101 642 185 879 469 855 619 597 786 715 865 594 446 574 702 301 683 198 426 820 028



→ {4 → 3.28886 × 10⁻⁹, 3 → 1.},

4 694 181 392 858 132 208 106 823 918 969 450 417 444 631 398 095 827 854 395 585 117



→

77 700 327 286 014 060 041 114 089 271 941 524 874 778 257 975 616 225 192 759 868 025

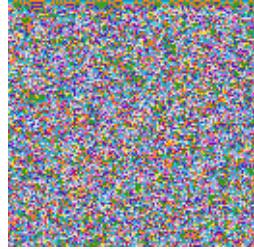
{4 → 0.000136886, 3 → 0.999863},



→

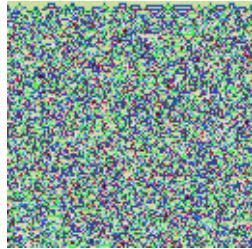
101 275 737 719 588 313 499 958 188 776 684 645 488 887 964 763 703 077 870 951 309 667

{4 → 0.00148989, 3 → 0.99851},



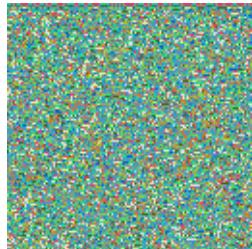
→ {4 → 4.94333 × 10⁻¹², 3 → 1.},

31 330 139 254 828 030 520 812 274 076 452 349 678 165 064 863 828 483 555 288 280 047



→ {3 → 0.28896, 4 → 0.71104},

160 047 496 270 492 329 204 041 848 237 376 187 065 045 724 082 331 147 631 919 936 795



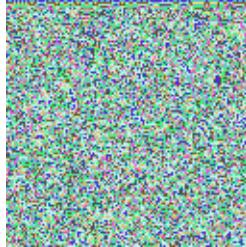
→

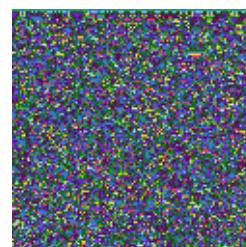
131 248 368 813 783 732 937 063 439 793 510 226 771 975 010 899 085 872 633 783 660 532

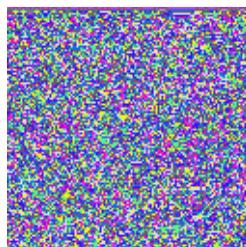
{4 → 0.0000118765, 3 → 0.999988} }

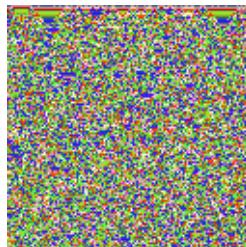
```
In[1459]:= test4Data18kr1C18 = data18TC[8, 128, 128];
test4Data18kr1C18labeled = Thread[Labeled[
  Keys@test4Data18kr1C18, Values@test4Data18kr1C18, LabelStyle → Small]];
Thread[test4Data18kr1C18labeled → netECA18[Keys@test4Data18kr1C18,
 {"TopProbabilities", 2}]]
```

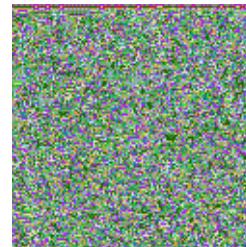
```

Out[1461]= { →
84 407 891 860 608 186 800 342 925 777 103 111 012 730 709 614 871 448 322 966 842 743
{4 → 0.000107331, 3 → 0.999893},  

 →
161 424 174 456 430 728 167 518 922 554 123 708 832 493 894 459 273 117 300 803 992 860
{4 → 1.09406 × 10-10, 3 → 1.},  

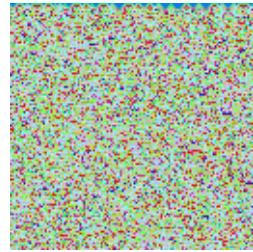
 →
78 032 217 344 344 330 867 403 680 915 204 373 154 822 648 823 501 092 588 035 610 835
{4 → 4.26104 × 10-6, 3 → 0.999996},  

 →
17 514 930 310 957 860 289 760 217 211 982 312 893 914 895 733 884 156 147 675 071 979
{4 → 3.02896 × 10-6, 3 → 0.999997},  

 →
126 337 368 684 499 452 874 800 008 665 847 585 515 559 961 310 661 358 461 150 478 987

```

$$\{4 \rightarrow 6.83088 \times 10^{-11}, 3 \rightarrow 1.\},$$



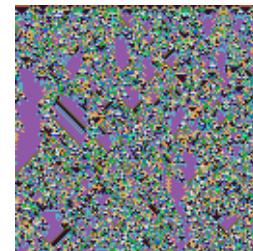
$$\rightarrow \{4 \rightarrow 4.53993 \times 10^{-9}, 3 \rightarrow 1.\},$$

40 213 870 254 046 402 060 993 100 884 679 132 055 568 662 380 628 182 270 851 703 964



$$\rightarrow \{4 \rightarrow 1.55591 \times 10^{-10}, 3 \rightarrow 1.\},$$

51 884 643 645 127 688 338 260 865 508 261 671 962 402 238 325 831 463 126 617 291 758

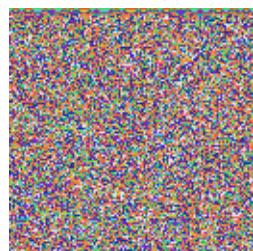


\rightarrow

105 981 239 442 692 171 040 307 215 500 165 460 050 735 782 946 669 540 434 861 001 557

$$\{2 \rightarrow 1.37062 \times 10^{-16}, 4 \rightarrow 1.\}\}$$

```
In[1516]:= test4Data18kr1C18 = data18TC[8, 128, 128];
test4Data18kr1C18labeled = Thread[Labeled[
  Keys@test4Data18kr1C18, Values@test4Data18kr1C18, LabelStyle -> Small]];
Thread[test4Data18kr1C18labeled -> netECA18[Keys@test4Data18kr1C18,
 {"TopProbabilities", 2}]]
```

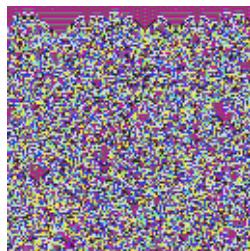


\rightarrow

Out[1518]= {

67 097 332 073 690 877 096 462 393 318 551 121 105 627 611 874 073 821 346 080 316 259

$$\{4 \rightarrow 5.10358 \times 10^{-11}, 3 \rightarrow 1.\},$$



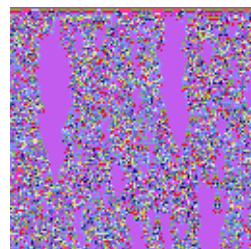
$$\rightarrow \{4 \rightarrow 6.51776 \times 10^{-10}, 3 \rightarrow 1.\},$$

469 341 525 975 528 605 442 938 764 400 684 210 544 509 817 697 780 635 610 240 385



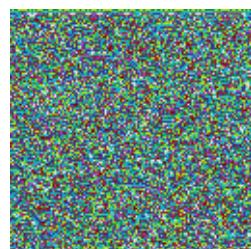
$$\rightarrow \{4 \rightarrow 5.69048 \times 10^{-9}, 3 \rightarrow 1.\},$$

92 797 071 861 825 599 650 393 018 230 465 068 427 103 727 472 152 026 271 875 491 041



$$\rightarrow \{2 \rightarrow 4.64192 \times 10^{-12}, 4 \rightarrow 1.\},$$

48 707 525 714 524 878 716 517 127 579 370 682 054 079 882 568 456 080 106 934 725 549



\rightarrow

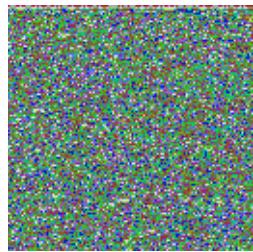
44 770 759 776 338 013 160 561 529 662 542 939 808 723 595 235 004 541 281 157 081 136

$$\{4 \rightarrow 9.2328 \times 10^{-7}, 3 \rightarrow 0.999999\},$$



$$\rightarrow \{4 \rightarrow 1.19647 \times 10^{-8}, 3 \rightarrow 1.\},$$

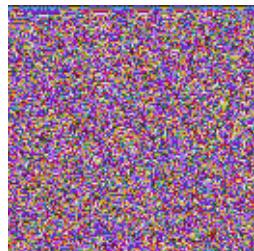
860 018 757 961 576 225 864 410 760 233 199 100 592 057 684 375 923 534 430 897 683



→

164 751 184 453 635 689 907 701 761 887 389 137 319 437 941 824 750 165 777 001 238 660

{ 4 → 0.000073185 , 3 → 0.999927 } ,



→

30 824 548 023 101 519 695 632 494 294 594 245 489 101 989 183 582 883 081 905 253 160

{ 4 → 0.00834654 , 3 → 0.991653 } }