

Assignment - 4(a)

Iteration - 0

Sample - 1

x_i	y_i
7.6	157
7.1	170

Step 1:- $(7.6, 157)$, $\eta = 0.01$, $m = 1$, $c = -1$

$$\begin{aligned} \text{Step 2:- } \frac{\partial E}{\partial m} \bigg|_{m=1} &= -(y_i^a - mx_i^a - c) \times (-x_i^a) \\ &= +(157 - 1 \times 7.6 - (-1)) \times (7.6) \\ &= (158 - 7.6) (7.6) \\ &= (150.4) (7.6) \\ &= 1143.04 \end{aligned}$$

$$\begin{aligned} \frac{\partial E}{\partial c} \bigg|_{c=-1} &= -(y_i^a - mx_i^a - c) \\ &= -(157 - 1 \times 7.6 - (-1)) \\ &= -(158 - 7.6) \\ &= -150.4 \end{aligned}$$

$$\begin{aligned} \text{Step 3: } \Delta m &= -\eta \frac{\partial E}{\partial m} = -(0.01) (1143.04) \\ &= -11.4304 \end{aligned}$$

$$\begin{aligned} \Delta c &= -\eta \frac{\partial E}{\partial c} = -(0.01) (-150.4) \\ &= 1.504 \end{aligned}$$

$$\begin{aligned} \text{Step 4:- } m &= m + \Delta m = 1 + (-11.43) = -10.43 \\ c &= c + \Delta c = -1 + (1.504) = 0.504 \end{aligned}$$

~~step 2~~
Sample - 2

step-1:- $(7.1, 174)$, $\eta = 0.01$, $m = 1$, $c = -1$

$$\begin{aligned}\text{step 2:- } \frac{\partial E}{\partial m} \Big|_{m=1} &= -(y_i^a - m x_i^a - c) \cdot x_i^a \\ &= (174 - 1 \cdot (7.1) - (-1)) \cdot 7.1 \\ &= (175 - 7.1) \cdot (7.1) \\ &= 167.9 \times 7.1 = 1192.09\end{aligned}$$

$$\begin{aligned}\frac{\partial E}{\partial c} \Big|_{c=-1} &= -(y_i^a - m x_i^a - c) \\ &= -(174 - 1(7.1) - (-1)) \\ &= -167.9\end{aligned}$$

step 3r $\Delta m = -\eta \frac{\partial E}{\partial m} = -(0.01) 1192.09$
 $= -11.920$

$$\begin{aligned}\Delta c &= -\eta \frac{\partial E}{\partial c} = -(0.01) (-167.9) \\ &= 1.679\end{aligned}$$

step 4r $m = m + \Delta m = 1 + (-11.920)$
 $= -10.920$
 $c = c + \Delta c = -1 + 1.679$
 $= 0.679$

Iteration - 2

sample - 1

step 1:- $[7.61, 157]$, $n=0.01$, $m=-10.43$, $c=0.504$

step 2:- $\frac{\partial E}{\partial m} \Big|_{m=-10.43} = (157 - (-10.43)(7.61) - 0.504)(7.61)$

$$= (157 + (10.43)(7.61) - 0.504)(7.61)$$

$$= (156.496 + (10.43 \times 7.61))7.61$$

$$= (156.496 + 79.372)7.61$$

$$= (235.868)7.61$$

$$= 1794.955$$

$$\frac{\partial E}{\partial c} \Big|_{c=0.504} = -(157 - (-10.43)(7.61) - 0.504)$$
$$= -235.868$$

step 3:- $\Delta m = n \frac{\partial E}{\partial m} = (-0.01 \times 1794.955)$

$$= -17.949$$

$$\Delta c = -n \frac{\partial E}{\partial c} = (-0.01) \times -235.868$$

$$= 2.358$$

step 4:-

$$m = m + \Delta m = -10.43 + (-17.949)$$

$$= -28.379$$

$$c = c + \Delta c = 0.504 + 2.358$$

$$= 2.862$$

sample-2

step 1 :- $(7.1, 174)$, $n = 0.01$, $m = -10.92$, $c = 0.679$

step 2 :- $\frac{\partial F}{\partial m} \bigg|_{m=-10.92} = (174 - (-10.92)(7.1) - 0.679(7.1))$
 $= (173.321 + (10.92 \times 7.1)) \times 7.1$
 $= 1781.056$

$\frac{\partial E}{\partial c} \bigg|_{c=0.679} = - (174 - (-10.92)(7.1) - (-0.679)(7.1))$
 $= -250.853$

step 3 :- $m = n \frac{\partial E}{\partial m} = -(0.01) \times 1781.056$
 $= -17.810$

$\Delta c = -n \frac{\partial E}{\partial c} = -(0.01)(-250.853)$
 $= 2.508$

step 4 :- $m = m + \Delta m$
 $= -10.92 - 17.81$
 $= -28.73$

$c = c + \Delta c$
 $= 0.679 + 2.508$
 $= 3.187$