

## Binomial Heap

In this task you have to implement a binomial heap data structure. You need to implement the following functions:

1. **MakeHeap ()**: Creates and returns a new heap containing no elements. Time complexity:  $O(1)$ .
2. **Union ( $H_1, H_2$ )**: Combines two binomial heaps  $H_1$  and  $H_2$  into one binomial heap. Time complexity:  $O(\log n)$ .
3. **Insert ( $x, H$ )**: Inserts a key  $x$  into the binomial heap data structure  $H$ . Time complexity:  $O(\log n)$ .
4. **FindMin ( $H$ )**: Returns the pointer to the minimum key in  $H$  but does not remove the key. Time complexity:  $O(\log n)$ . Another overloaded function can be optimized to  $O(1)$ .
5. **ExtractMin ( $H$ )**: Returns the pointer to the minimum key in  $H$  and delete the key from  $H$ . Time complexity:  $O(\log n)$ .
6. **IncreaseKey ( $x, newKey, H$ )**: Increase the new key value  $newKey$  to the key  $x$  within the binomial heap  $H$ . The  $newKey$  should not be smaller than the current key. Time complexity:  $O(\log n)$ .
7. **DecreaseKey ( $x, newKey, H$ )**: Decrease the new key value  $newKey$  to the key  $x$  within the binomial heap  $H$ . The  $newKey$  should not be greater than the current key. Time complexity:  $O(\log n)$ .
8. **Delete ( $x, H$ )**: Deletes the key  $x$  from  $H$ . Time complexity:  $O(\log n)$ .
9. **Print ()**: Print the heap.

You should write your program using features of object-oriented programming.

### Input:

Create a menu for the nine operations. Use 1-9 for the above operations sequentially and 10 for quit. Ask user to select an operation until option 10 is selected. Also prompt user for input any value which is required for the corresponding operations, i.e., insert, increaseKey, etc.

### Submission Guidelines:

- a. In your local machine, create a new folder; **the name of the folder should be your 7 digit roll number.**
- b. Put all the source code files in the folder created in step (a).
- c. Finally, compress the folder created in (a) to produce a .zip file. **The name of the .zip file should be your 7 digit roll number.**
- d. Submit the .zip file.

### Policy:

Copying from internet, classmate, seniors, or from any other source is strongly prohibited. - **100% marks will be 'rewarded' if any such copying is detected.**

### Deadline:

Deadline is set at 24 August 2019, 11:00 pm BDT for all subsections.