

Excursions in METAPOST

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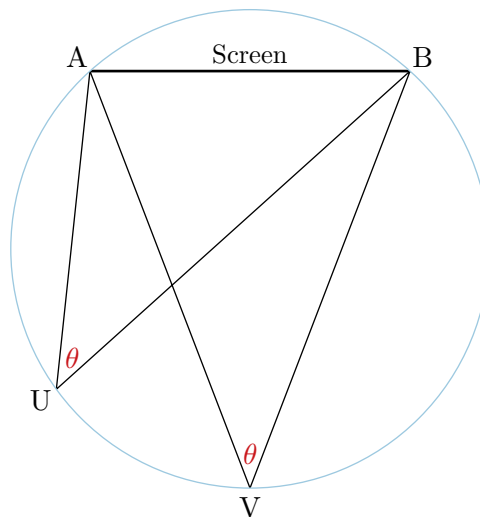
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This example document includes geometric illustrations inspired by *Excursions in Geometry*, C. Stanley Ogilvy, OUP 1968. The illustrations are presented roughly in the same order as the book, with notes about how you can use METAPOST to produce similar. The section heading also approximately follow the book. You might like to read the PDF of this document side by side with the source code, so that you can see how each illustration is done. Each illustration is included as in-line METAPOST code, there are no external graphics files used.

1 A bit of background

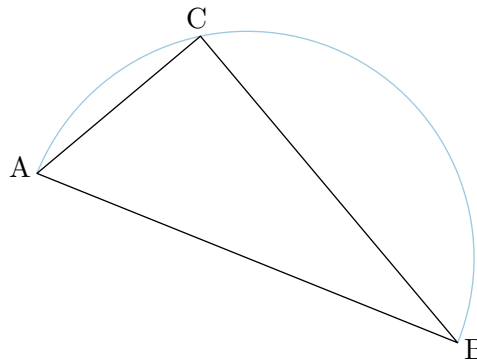
Ogilvie starts with a review of some circle theorems. In fact most of the book is about circles in one way or another.

In this first diagram, you are given the width AB of the screen and the ideal viewing angle θ . The METAPOST code works out the rest from that, including a useful routine for a circle through three points.

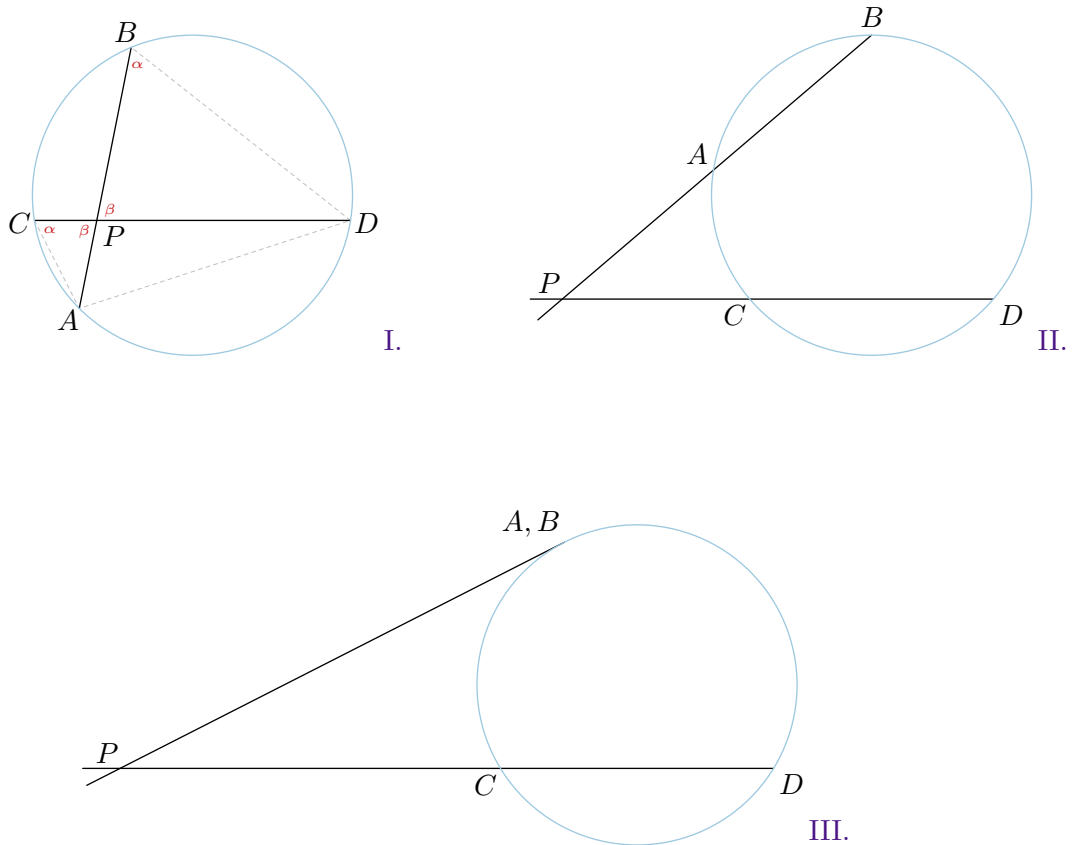


Here θ is half the angle measured by the intercepted arc, which gives us the useful corollary that any angle inscribed in a semicircle is a right angle, and conversely that if

you can show that some angle ACB is a right angle, then the semicircle drawn with AB as a diameter must pass through C .



A basic theorem: If two chords intersect, the product of the lengths of the segments of the one equals the product of the lengths of the segments of the other. In all three cases below you have $PA/PD = PC/PB$ by similar triangles, hence $PA \cdot PB = PC \cdot PD$.



This example also shows how to arrange sub-figures into one.

2 Harmonic division and Apollonian circles

Can we find C and D on the line AB so that $AC/CB = AD/BD$?

Yes:

