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## 1 CArL

This is the documentation of CArL, an Open Source C++ Library for Computer Arithmetic and Logic. On this page, you can find introductory information on how to obtain and compile CArL, discussion of some core features of CArL as well as traditional doxygen API documentation.

If you are new to CArL and want to have a look around, we recommend reading the User Documentation. This section gives a gentle introduction to basic concepts like number types, polynomials and alike.

If you want to use CArL and want to know how to get and install it, have a look at Getting Started. It covers the most important steps including obtaining the actual source code, obtaining dependencies, building the library and running our test suite.

If you already use CArL and want to dig deeper or submit new code, you can read the Developers' Guide. It contains information about supplementary features like our logging framework and some basic guidelines for our code like how we use doxygen.

Note that this documentation is, and will probably always be, work in progress. If you feel that some topic that is important to you is missing or some explanation is unclear, please let us know!

## 1.0.1 Contact

• github: https://github.com/ths-rwth/carl

## 2 Developers' Guide

- Documentation
- Logging
- · Finding and Reporting Bugs
- Code style

#### 2.1 Documentation

On this page, we refer to some internal documentation rules. We use doxygen to generate our documentation and code reference. The most important conventions for documentation in CArL are collected here.

Note that some of the documentation may be incomplete or rendered incorrectly, especially if you use an old version of doxygen. Here is a list of known problems:

- Comments in code blocks (see below) may not work correctly (e.g. with doxygen 1.8.1.2). See <a href="here">here</a> for a workaround. This will however look ugly for newer doxygen versions, hence we do not use it.
- Files with static\_assert statements will be incomplete. A patch is pending and will hopefully make it into doxygen 1.8.9.
- Member groups (usually used to group operators) may or may not work. There still seem to be a few cases
  where doxygen messes up.
- Documenting unnamed parameters is not possible. A corresponding ticket exists for several years.

#### 2.1.1 Modules

In order to structure the reference, we use the concept of <code>Doxygen modules</code>. Such modules are best thought of as a hierarchical set of tags, called groups. We define those groups in <code>/doc/markdown/codedocs/groups.dox</code>. Please make sure to put new files and classes in the appropriate groups.

#### 2.1.2 Literature references

Literature references should be provided when appropriate.

We use a bibtex database located at /doc/literature.bib with the following conventions:

- Label for one author: LastnameYY, for example Ducos00 for ? .
- Label for multiple authors: ABCYY where ABC are the first letters of the authors last names. For example GCL92 for ? .
- · Order the bibtex entrys by label.

These references can be used with @cite label, for example like this:

```
* Checks whether the polynomial is unit normal
* @see @cite GCL92, page 39
* @return If polynomial is normal.
*/
bool is_normal() const;
```

## 2.1.3 Code comments

```
2.1.3.1 File headers
 * @file <filename>
 * @ingroup <groupidl>
 * @ingroup <groupid2>
 * @author <author1>
 * @author <author2>
 *
 * [ Short description ]
 */
```

Descriptions may be omitted when the file contains a single class, either implementation or declaration.

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2.1.3.2 Namespaces Namespaces are documented in a separate file, found at '/doc/markdown/codedocs/namespaces.dox'

```
2.1.3.3 Class headers /**
    * @ingroup <groupid>
    * [ Description ]
    * @see <reference>
    * @see <OtherClass>
    */

2.1.3.4 Method headers /**
    * [ Usage Description ]
    * @param <p1> [ Short description for first parameter ]
    * @param <p2> [ Short description for second parameter ]
    * @return [ Short description of return value ]
    * @see <reference>
    * @see <otherMethod>
    */
```

These method headers are written directly above the method declaration. Comments about the implementation are written above the or inside the implementation.

The see command is used likewise as for classes.

**2.1.3.5 Method groups** There are some cases when documenting each method is tedious and meaningless, for example operators. In this case, we use doxygen method groups.

For member operators (for example operator+=), this works as follows:

```
/// @name In-place addition operators
/// @{
/**
   * Add something to this polynomial and return the changed polynomial.
   * @param rhs Right hand side.
   * @return Changed polynomial.
   */
   MultivariatePolynomial& operator+=(const MultivariatePolynomial& rhs);
   MultivariatePolynomial& operator+=(const Term<Coeff>& rhs);
   MultivariatePolynomial& operator+=(const Monomial& rhs);
   MultivariatePolynomial& operator+=(Variable::Arg rhs);
   MultivariatePolynomial& operator+=(const Coeff& rhs);
   /// @}
```

#### 2.1.4 Writing out-of-source documentation

Documentation not directly related to the source code is written in Markdown format, and is located in /doc/markdown/.

### 2.2 Logging

#### 2.2.1 Logging frontend

The frontend for logging is defined in logging.h.

It provides the following macros for logging:

- LOGMSG\_TRACE(channel, msg)
- LOGMSG\_DEBUG(channel, msg)
- LOGMSG\_INFO(channel, msg)
- · LOGMSG\_WARN(channel, msg)

- LOGMSG\_ERROR(channel, msg)
- · LOGMSG\_FATAL(channel, msg)
- LOG\_FUNC(channel, args)
- LOG\_FUNC(channel, args, msg)
- LOG\_ASSERT(channel, condition, msg)
- LOG\_NOTIMPLEMENTED()
- LOG\_INEFFICIENT()

Where the arguments mean the following:

- channel: A string describing the context. For example "carl.core".
- msg: The actual message as an expression that can be sent to a std::stringstream. For example "foo: "
   foo.
- args: A description of the function arguments as an expression like msg.
- condition: A boolean expression that can be passed to assert ().

```
Typically, logging looks like this:
```

```
bool checkStuff(Object o, bool flag) {
   LOG.FUNC("carl", o << ", " << flag);
   bool result = o.property(flag);
   LOGMSG.TRACE("carl", "Result: " << result);
   return result;
}</pre>
```

Logging is enabled (or disabled) by the LOGGING macro in CMake.

### 2.2.2 Logging configuration

As of now, there is no frontend interface to configure logging. Hence, configuration is performed directly on the backend.

## 2.2.3 Logging backends

As of now, only two logging backends exist.

- **2.2.3.1 CArL logging** CArL provides a custom logging mechanism defined in carl::logging.
- **2.2.3.2 Fallback logging** If logging is enabled, but no real logging backend is selected, all logging of level WARN or above goes to std::cerr.

## 2.3 Finding and Reporting Bugs

This page is meant as a guide for the case that you find a bug or any unexpected behaviour. We consider any of the following events a (potential) bug:

- · CArL crashes.
- · A library used through CArL crashes.
- · CArL gives incorrect results.
- · CArL does not terminate (for reasonably sized inputs).
- CArL does not provide a method or functionality that should be available according to this documentation.
- CArL does not provide a method or functionality that you consider crucial or trivial for some of the datastructures.
- · Compiling the CArL library fails.
- Compiling your code using CArL fails and you are pretty sure that you use CArL according to this documentation.

In any of the above cases, make sure that:

- You have installed all necessary Dependencies in the required versions.
- · You work on something that is similar to a system listed as supported platform at Getting Started.
- You can (somewhat reliably) reproduce the error with a (somewhat) clean build of CArL. (i.e., you did not screw up the CMake flags, see Building with CMake for more information)
- You compile either with CMAKE\_BUILD\_TYPE=DEBUG or DEVELOPER=ON. This will give additional warnings during compilation and enable assertions during runtime. This will slow down CArL significantly, but detect errors before an actual crash happens and give a meaningful error message in many cases.

If you are unable to solve issue yourself or you find the issue to be an actual bug in CArL, please do not hesitate to contact us. You can either contact us via email (if you suspect a configuration or usage issue on your side) or create a ticket in our bug tracker (if you suspect an error that is to be fixed by us). We use the github bug tracker at https://github.com/ths-rwth/carl/issues.

When sending us a mail or creating a ticket, please provide us with:

- · Your system specifications, including versions of compilers and libraries listed in the dependencies.
- The CArL version (release version or git commit id).
- · A minimal working example.
- · A description of what you would expect to happen.
- · A description of what actually happens.

## 2.4 Code style

Please follow these guidelines for new code. We are migrating old code over the time.

**2.4.0.1 Code formatting** ClangFormat allows to define code style rules and format source files automatically. A .clang-format file is provided with the repository. Please use this file to format all sources.

#### 2.4.0.2 Naming conventions For all new code, the following rules apply.

• type names and template parameter: CamelCase

• variable and function names: snake\_case

• compiler macros and defines: ALL\_UPPERCASE

• enum values: UPPERCASE

(private) class members: start with m\_ respectively mp\_ for pointers and mr\_ for references

• type traits: snake\_case and end with \_type

• namespace: snake\_case

**2.4.0.3** Use of classes, structs and functions We follow a Rust-style approach where we define data structures and attach basic operations that as methods to it. All functionality that can be considered optional is realized via free functions.

#### 2.4.0.4 Directory structure and namespaces

- Libraries
  - Dependencies between libraries are acyclic!
- · Folders and files
  - A folder represents a module.
  - A file contains either of the following:
    - \* a data structure, a collection of related data structures and basic functionality,
    - \* free functions that operate on data structures.
  - Dependencies between folders on the same level need to be acyclic.
  - Either all files in a directory depend on subdirectories in the same folder or subdirectories depend on files from the parent directory, but not both.
- Namespaces
  - CArL lives within the carl namespace.
  - Each library has its own sub-namespace, except carl-common, carl-arithmetic, carl-formula, carl-extpolys.
  - Auxiliary functions are in an appropriate sub-namespace.

#### 2.4.0.5 C++ features

- As of now, please stick to C++17 features.
- Use enum class instead of enum.

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## 3 Getting Started

#### 3.1 Download

We mirror our master branch to github.com. If you want to use the newest bleeding edge version, you can checkout from <a href="https://github.com/ths-rwth/carl">https://github.com/ths-rwth/carl</a>. Although we try to keep the master branch stable, there is a chance that the current revision is broken. You can check <a href="here">here</a> if the current revision compiles and all the unit tests work.

We regularly tag reasonably stable versions. You can find them at <a href="https://github.com/ths-rwth/carl/releases">https://github.com/ths-rwth/carl/releases</a>.

## 3.2 Quick installation guide

- Make sure all dependencies are available.
- Download the latest release or clone the git repository from https://github.com/ths-rwth/carl.
- Prepare the build.
   \$ mkdir build && cd build && cmake ../
- Build carl (with tests and documentation).

```
$ make
$ make test doc
```

### 3.3 Using CArL

CArL registers itself in the CMake system, hence to include CArL in any other CMake project, just use find.

package (carl).

To use CArL in other projects, link against the shared or static library created in build/.

## 3.4 Supported platforms

We test carl on the following platforms:

Ubuntu 22.04 LTS with several compilers

We usually support at least all clang and gcc versions starting from those shipped with the latest Ubuntu LTS or Debian stable releases. As of now, this is clang-13 and newer and gcc-11 and newer.

## 3.5 Advanced building topics

· Building with CMake

## 3.6 Troubleshooting

If you're experiencing problems, take a look at our Troubleshooting section. If that doesn't help you, feel free to contact us.

## 3.7 Dependencies

To build and use CArL, you need the following other software:

- git to checkout the git repository.
- · cmake to generate the make files.
- g++ or clang to compile.

We use C++17 and thus need at least g++7 or clang 5.

Optional dependencies

- · ccmake to set cmake flags.
- doxygen and doxygen-latex to build the documentation.
- · gtest to build the test cases.

Additionally, CArL requires a few external libraries, which are installed automatically by CMake if no local version is available:

- · boost for several additional libraries.
- gmp for calculations with large numbers.
- Eigen3 for numerical computations.

To simplify the installation process, all these libraries can be built by CArL automatically if it is not available on your system. You can do this manually by running make resources

# 3.8 Building with CMake

We use CMake to support the building process. CMake is a command line tool available for all major platforms. To simplify the building process on Unix, we suggest using CCMake.

CMake generates a Makefile likewise to Autotools' configure. We suggest initiating this procedure from a separate build directory, called 'out-of-source' building. This keeps the source directory free from files created during the building process.

#### 3.8.1 CMake Options for building CArL.

```
Run ccmake to obtain a list of all available options or change them. $ cd build/
$ ccmake ../
```

Using [t], you can enable the *advanced mode* that shows all options. Most of these should not be changed by the average user.

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#### 3.8.1.1 General

- CMAKE\_BUILD\_TYPE [Release, Debug]
  - Release
  - Debug
- CMAKE\_CXX\_COMPILER < compiler command>
  - /usr/bin/c++: Default for most linux distributions, will probably be an alias for g++.
  - /usr/bin/g++: Uses g++.
  - /usr/bin/clang++: Uses clang.
- USE\_CLN\_NUMBERS [ON, OFF]

If set to ON, CLN number types can be used in addition to GMP number types.

• USE\_COCOA [ON, OFF]

If set to ON, CoCoALib can be used for advanced polynomial operations, for example multivariate gcd or factorization.

• USE\_GINAC [ON, OFF]

If set to ON, GiNaC can be used for some polynomial operations. Note that this implies  $USE\_CLN\_NUMBERS = ON$ .

#### 3.8.1.2 Debugging

DEVELOPER

Enables additional compiler warnings.

• LOGGING [ON, OFF]

Setting *LOGGING* to *OFF* disables all logging output. It is recommended if the performance should be maximized, but notice that this also prevents important warnings and error messages to be generated.

#### 3.8.2 CMake Targets

There are a few important targets in the CArL CMakeLists:

- doc: Builds the doxygen documentation.
- libs: Builds all libraries.
- runXTests: Builds the tests for the X module.
- test: Build and run all tests.

### 3.9 Troubleshooting

#### 3.9.1 General

CArL tries to make use of modern C++ features. Though we try to be compatible with the stock versions of all dependencies of Debian stable and the latest Ubuntu LTS, this does not always work out.

### 4 User Documentation

This is the introductory user documentation of CArL. It explains the basic concepts and classes that CArL provides.

· CArL module structure

## 4.1 Basic concepts

- Numbers
- · Polynomials
- Numbers

#### 4.2 Tutorial

There are some introductory code examples how CArL can be used. You find them at Tutorial.

#### 4.3 CArL module structure

CArL is separated into several libraries implementing functionality on different abstraction levels.

## 4.3.1 General utilities

- carl-common: Basic data structures, helper methods, etc.
- carl-logging: Logging funtionality. Depends on carl-common.
- carl-statistics: Collect statistics about a run of a program. Depends on carl-common.
- carl-checkpoints: Collect the trace of the run of a programm and compare it with certain checkpoints. *Depends on carl-common and carl-logging.*
- · carl-settings: Runtime settings infrastructure.

#### 4.3.2 Core libraries

- carl-arithmetic: Arithmetic package. Does not do sophisticated memory management. *Depends on carl-common and carl-logging.*
- carl-formula: Logical formulas with support for arithmetic, bitvector and uninterpreted function constraints. Does pooling of some types for memory efficiency. *Depends on carl-arithmetic.*
- carl-vs: Implements virtual substitution. For legecy reasons, this depends on carl-formula.
- carl-extpolys: Extended polynomial types: factorized polynomials, rational functions. *Depends on carl-arithmetic.*

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#### 4.3.3 Higher level

- carl-io: Input/output functionality for CArL types from/to different file formats. Depends on carl-formula.
- carl-covering: Data structures and heuristics for computing coverings. *Depends on carl-common and carl-logging*.

#### 4.4 Numbers

The higher-level datastructures in CArL are templated with respect to their underlying number type and can therefore be used with any number type that fulfills some common requirements. This is the case, for example, for carl::Term, carl::MultivariatePolynomial, carl::UnivariatePolynomial or carl::Interval objects.

Everything related to number types resides in the /carl/numbers/ directory. For each group of supported number types T, a folder  $adaption_T$  exists that contains the following:

- Include of the library (if necessary)
- · Type traits according to Type Traits.
- · Static constants for zero and one.
- · Operations to fulfill our common interface.

From the outside, that is also the rest of the CArL library, only the central numbers/numbers.h shall be included. This file includes all available adaptions and takes care of disabling adaptions if the respective library is unavailable.

#### 4.4.1 Adaptions

As of now, we provide adaptions of the following types:

- CLN (cln::cl\_I and cln::cl\_RA).
- FLOAT\_T<mpfr\_t>, our own wrapper for mpfr\_t
- · GMPxx, the C++ interface of GMP.
- · Native datatypes as defined by ?

Note that these adaptions may not fully implement all methods described below, but only to some extend that is used. Finishing these adaptions is work in progress.

#### 4.4.2 Interface

The following interface should be implemented for every number type T.

- Type Traits if applicable.
- carl::constant\_zero<T> and carl::constant\_one<T> if the generic definition from carl/numbers/constants.h does not fit.
- Specialization of std::hash<T>
- · Arithmetic operators:

```
    T operator+(const T&, const T&) and T& operator+=(const T&, const T&)
    T operator-(const T&, const T&) and T& operator-=(const T&, const T&)
    T operator-(const T&)
    T operator*(const T&, const T&) and T& operator*=(const T&, const T&)
    T& operator=(const T&)
    bool carl::is_zero(const T&) and bool carl::is_one(const T&)
```

- | f carl::is\_rational\_type<T>::value:
  - carl::get\_num(const T&) and carl::get\_denom(const T&)
  - T carl::rationalize(double)
- bool carl::is\_integer(const T&)
- std::size\_t carl::bitsize(const T&)
- double carl::to\_double(const T&) and I carl::to\_int<I>(const T&) for some integer types I.
- T carl::abs(const T&)
- T carl::floor(const T&) and T carl::ceil(const T&)
- If carl::is\_integer\_type<T>::value:

```
- T carl::gcd(const T&, const T&) and T carl::lcm(const T&, const T&)
```

- T carl::mod(const T&, const T&)
- T carl::pow(const T&, unsigned)
- std::pair<T,T> carl::sqrt(const T&) where the result represents an interval containing the exact result.
- T carl::div(const T&, const T&) asserting that exact division is possible.
- T carl::quotient(const T&, const T&) and T carl::remainder(const T&, const T&)

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## 4.5 Polynomials

In order to represent polynomials, we define the following hierarchy of classes:

- · Coefficient: Represents the numeric coefficient..
- · Variable: Represents a variable.
- · Monomial: Represents a product of variables.
- · Term: Represents a product of a constant factor and a Monomial.
- MultivariatePolynomial: Represents a polynomial in multiple variables with numeric coefficients.

We consider these types to be embedded in a hierarchy like this:

- · MultivariatePolynomial
  - Term
    - \* Monomial
      - · Variable
    - \* Coefficient

We will abbreviate these types as C, V, M, T, MP.

#### 4.5.1 UnivariatePolynomial

Additionally, we define a UnivariatePolynomial class. It is meant to represent either a univariate polynomial in a single variable, or a multivariate polynomial with a distinguished main variable.

In the former case, a number type is used as template argument. We call this a univariate polynomial.

In the latter case, the template argument is instantiated with a multivariate polynomial. We call this a *univariately* represented polynomial.

A UnivariatePolynomial, regardless if univariate or univariately represented, is mostly compatible to the above types.

Operators

#### 4.5.2 Operators

The classes used to build polynomials are (almost) fully compatible with respect to the following operators, that means that any two objects of these types can be combined if there is a directed path between them within the class hierarchy. The exception are shown and explained below. All the operators have the usual meaning.

· Comparison operators

```
- operator==(lhs, rhs)
- operator!=(lhs, rhs)
- operator<=(lhs, rhs)
- operator>=(lhs, rhs)
- operator>=(lhs, rhs)
```

## Arithmetic operators

```
- operator+(lhs, rhs)
- operator+=(lhs, rhs)
- operator-(lhs, rhs)
- operator-(rhs)
- operator-=(lhs, rhs)
- operator*(lhs, rhs)
- operator*=(lhs, rhs)
```

- **4.5.2.1 Comparison operators** All of these operators are defined for all combination of types. We use the following ordering:
  - For two variables x and y, x < y if the id of x is smaller then the id of y. The id is generated automatically by the VariablePool.
  - For two monomials a and b, we use a lexicographical ordering with total degree, that is a < b if
    - the total degree of a is smaller than the total degree of b, or
    - the total degrees are the same and
      - $\star$  the exponent of some variable v in a is greater than in b and
      - $\star$  the exponents of all variables smaller than v are the same in a and in b.
    - The intuition is that the monomials are considered as a sorted product of plain variables.
  - For two terms a and b, a < b if
    - the monomial of a is smaller than the monomial of b, or
    - the monomials of a and b are the same and the coefficient of a is smaller than the coefficient of b.
  - ullet For two polynomials a and b, we use a lexicographical ordering, that is a < b if
    - term(a,i) < term(b,i) and
    - term(a, j) = term(b, j) for all j=0, ..., i-1, where term(a, 0) is the leading term of a, that is the largest term with respect to the term ordering.
- **4.5.2.2 Arithmetic operators** We now give a table for all (classes of) operators with the result type or a reason why it is not implemented for any combination of these types.

| +  | С  | ٧  | M  | Т  | MP |
|----|----|----|----|----|----|
| С  | С  | MP | MP | MP | MP |
| V  | MP | 1) | 1) | MP | MP |
| М  | MP | 1) | 1) | MP | MP |
| Т  | MP | MP | MP | MP | MP |
| MP | MP | MP | MP | MP | MP |

4.5.2.2.1 <tt>operator+(lhs, rhs)</tt>, <tt>operator-(lhs, rhs)</tt>

| - | С | ٧  | M  | Т | MP |
|---|---|----|----|---|----|
| - | С | 1) | 1) | Т | MP |

#### 4.5.2.2.2 <tt>operator-(lhs)</tt> (unary minus)

| *  | С  | ٧  | M  | Т  | MP |
|----|----|----|----|----|----|
| С  | С  | Т  | Т  | Т  | MP |
| V  | Т  | М  | М  | Т  | MP |
| М  | Т  | М  | М  | Т  | MP |
| Т  | Т  | Т  | Т  | Т  | MP |
| MP | MP | MP | MP | MP | MP |

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#### 4.5.2.2.3 operator\*(lhs, rhs)

| += | С  | ٧  | M  | Т  | MP |
|----|----|----|----|----|----|
| С  | С  | 2) | 2) | 2) | 2) |
| ٧  | 2) | 2) | 2) | 2) | 2) |
| М  | 2) | 2) | 2) | 2) | 2) |
| Т  | 2) | 2) | 2) | 2) | 2) |
| MP | MP | MP | MP | MP | MP |

#### 4.5.2.2.4 <tt>operator+=(rhs)</tt>, <tt>operator-=(rhs)</tt>

| *= | С  | V  | M  | Т  | MP |
|----|----|----|----|----|----|
| С  | С  | 3) | 3) | 3) | 3) |
| V  | 3) | 3) | 3) | 3) | 3) |
| М  | 3) | М  | М  | 3) | 3) |
| Т  | Т  | Т  | Т  | Т  | 3) |
| MP | MP | MP | MP | MP | MP |

## 4.5.2.2.5 <tt>operator\*=(rhs)</tt>

- 1. A coefficient type is needed to construct the desired result type, but none can be extracted from the argument types.
- 2. The type of the left hand side can not represent sums of these objects.
- 3. The type of the left hand side can not represent products of these objects.

#### 4.5.2.3 UnivariatePolynomial operators

#### **4.5.2.4 Implementation** We follow a few rules when implementing these operators:

- Of the comparison operators, only operator== and operator< contain a real implementation. The others are implemented like this:
  - operator!=(lhs, rhs):!(lhs == rhs)
  - operator<=(lhs, rhs):!(rhs < lhs)</pre>
  - operator>(lhs, rhs):rhs < lhs
  - operator>=(lhs, rhs):rhs <= lhs
- Of all operator==, only those where lhs is the most general type contain a real implementation. The others are implemented like this:
  - operator == (lhs, rhs): rhs == lhs
- · They are ordered like in the list above.
- Operators are implemented in the file of the most general type involved (either an argument or the return type).

- Operators are not implemented as friend methods. Those are usually only found by the compiler due to ADL, but as we need to declare operator+(Term, Term) -> MultivariatePolynomial next to the MultivariatePolynomial, this will not work. If a friend declaration is necessary, it will be done as a forward declaration.
- Overloaded versions of the same operator are ordered in decreasing lexicographical order, like in this example:
  - operator(Term, Term)
  - operator(Term, Monomial)
  - operator(Term, Variable)
  - operator(Term, Coefficient)
  - operator (Monomial, Term)
  - operator (Variable, Term)
  - operator (Coefficient, Term)
- · Other versions are below those.
- **4.5.2.5 Testing the operators** There are two stages for testing these operators: a syntactical check that these operators exist and have the correct signature and a semantical check that they actually work as expected.
- **4.5.2.5.1 Syntactical checks** The syntactical check for all operators specified here is done in  $tests/core/\leftarrow Test\_Operators.cpp$ . We use boost::concept\\_check to check the existence of the operators. There are the following concepts:
  - Comparison: Checks for all comparison operators. (==, !=, <, <=, >, >=)
  - Addition: Checks for out-of-place addition operators. (+, -)
  - UnaryMinus: Checks for unary minus operators. (-)
  - Multiplication: Checks for out-of-place multiplication operators. (\*)
  - InplaceAddition: Checks for all in-place addition operators. (+=, -=)
  - InplaceMultiplication: Checks for all in-place multiplication operators. (\*=)
- **4.5.2.5.2 Semantical checks** Semantical checking is done within the test for each class.

## 4.6 Numbers

### 4.7 Tutorial

As a tutorial, we have a number of small programs that show certain features of CArL. The code is explained using normal comments and can be compiled using make tutorial.

Whenever we want to state that a certain property holds at some point, we will use assert () to do so.

- · Creating Variables
- Creating Monomials
- · Creating Polynomials

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#### 5 Todo List

```
Global carl::DiophantineEquations < Integer >::solveMultivariateDiophantine (const std::vector < Polyno-
   mial > &a, const MultiPoly &c, const std::map< Variable, GFNumber< Integer >> &I, unsigned d)
   const
   implement
Global carl::EEA< IntegerType >::calculate_recursive (const IntegerType &a, const IntegerType &b,
   IntegerType &s, IntegerType &t)
   a iterative implementation might be faster
Global carl::FactorizedPolynomial < P >::derivative (const carl::Variable &_var, unsigned _nth=1) const
   only _nth == 1 is supported
   we do not use factorization currently
Global carl::FactorizedPolynomial < P >::pow (unsigned _exp) const
   uses multiplication -> bad idea.
Global carl::FLOAT_T < FloatType >::root (FLOAT_T &, std::size_t, CARL_RND=CARL_RND::N) const
   implement root for FLOAT_T
Global carl::FLOAT_T< FloatType >::root_assign (std::size_t, CARL_RND=CARL_RND::N)
   implement root_assign for FLOAT_T
Global carl::ldealDatastructureVector< Polynomial >::getDivisor (const Term< typename Polynomial::CoeffType >
   &t) const
   delete divres?
Global carl::IntegralType < RationalType >::type
   Should any type have an integral type?
Global carl::Interval < Number >::div (const Interval < Number > &rhs) const
   Correctly determine if bounds are strict or weak.
Global carl::is_integer (const GFNumber < IntegerT > &)
   Implement this
Global carl::Monomial::drop_variable (Variable v) const
   this should work on the shared_ptr directly. Then we could directly return this shared_ptr instead of the ugly
   copying.
\textbf{Global} \quad \textbf{carl::MultivariatePolynomial} < \textbf{Coeff, Ordering, Policies} > :: \textbf{erase\_term} \quad \textbf{(typename} \quad \textbf{TermsType} \leftarrow \textbf{(typename)} 
   ::iterator pos)
   find new Iterm or constant term
Global carl::MultivariatePolynomial < Coeff, Ordering, Policies >::numeric_content () const
   gcd needed for fractions
Global carl::MultivariatePolynomial < Coeff, Ordering, Policies >::operator*= (const Term < Coeff > &rhs)
   more efficient.
Global carl::MultivariatePolynomial < Coeff, Ordering, Policies >::operator*= (const Monomial::Arg &rhs)
   more efficient.
Global carl::MultivariatePolynomial < Coeff, Ordering, Policies >::operator*= (Variable::Arg rhs)
   more efficient.
Global carl::MultivariatePolynomial < Coeff, Ordering, Policies >::operator*= (const Coeff &rhs)
   more efficient.
Global carl::MultivariatePolynomial < Coeff, Ordering, Policies >::operator+= (const Monomial::Arg &rhs)
   insert at correct position if already ordered
```

| Global carl::MultivariatePolynomial < Coeff, Ordering, Policies >::operator-= (const Monomial: Check if this works with ordering.   | Arg &rhs)     |
|---|---------------|
| Global carl::MultivariatePolynomial < Coeff, Ordering, Policies >::operator-= (const Term < Coeff Check if this works with ordering.  | eff > &rhs)   |
| Global carl::MultivariatePolynomial < Coeff, Ordering, Policies >::strip_Iterm () find new Iterm  |               |
| Global carl::RationalFunction < Pol, AutoSimplify >::derivative (const Variable &x, unsigned not Currently only nth = 1 is supported  Curretnly only factorized polynomials are supported | h=1) const    |
| Global carl::SortManager::exportDefinitions (std::ostream &os) const fix this   |               |
| Global carl::UnivariatePolynomial < Coefficient >::divides (const UnivariatePolynomial &divisor ls this correct?  | r) const      |
| 6 Runtime Complexity Bounds   |               |
| Global carl::detail_sign_variations::reverse (UnivariatePolynomial< Coefficient > &&p) O(n)   |               |
| Global carl::detail_sign_variations::scale (UnivariatePolynomial< Coefficient > &&p, const Coeffort  tor)  O(n)   | ficient &fac- |
| $ \begin{tabular}{lllllllllllllllllllllllllllllllllll$  | t Coefficient |
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# 8 Hierarchical Index

## 8.1 Class Hierarchy

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| $\mbox{ carl::GBProcedure} < \mbox{ Polynomial, Procedure, AddingPolynomialPolicy} > \\ \mbox{ AddingPolicy}$ | 718 |
| carl::Buchberger< Polynomial, AddingPolicy >  | 510 |
| carl::tree_detail::BaseIterator< T, Iterator, reverse >   | 490 |
| ${\tt carl::tree\_detail::BaseIterator} < {\tt T, ChildrenIterator} < {\tt T, false} >, {\tt false} >$        | 490 |
| carl::tree_detail::ChildrenIterator< T, reverse >   | 559 |
| ${\tt carl::tree\_detail::BaseIterator} < {\tt T, DepthIterator} < {\tt T, false} >, {\tt false} >$           | 490 |
| carl::tree_detail::DepthIterator< T, reverse >  | 597 |
| ${\tt carl::tree\_detail::Baselterator} < {\tt T, Leaflterator} < {\tt T, false} >, {\tt false} >$            | 490 |
| carl::tree_detail::LeafIterator< T, reverse >   | 842 |
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| carl::tree_detail::BaseIterator < T, PostorderIterator < T, false >, false >                                  | 490 |

| carl::tree_detail::PostorderIterator< T, reverse >  | 990         |
|---|-------------|
| ${\bf carl::} {\bf tree\_detail::} {\bf BaseIterator} {\bf < T,  PreorderIterator} {\bf < T,  false >},  {\bf false >}$ | 490         |
| carl::tree_detail::PreorderIterator< T, reverse >   | 994         |
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| carl::helper::BitvectorSubstitutor < Pol > Bool   | 509         |
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| carl::CompactTree < Entry, Configuration::fastIndex >   | 564  |
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| carl::all< Head, Tail >   | 490  |
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| carl::Constraint < Pol >  | 570  |
| carl::Context   | 577  |
| ${\sf carl::ContextPolynomial}{<}\ {\sf Coeff,Ordering,Policies}>$  | 578  |
| ${\bf carl::contractor::Contractor} < {\bf Origin, Polynomial, Number} >$   | 584  |
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| carl::tree_detail::LeafIterator< T, reverse > Iterator class for iterations over all leaf elements   | 842          |
| carl::less< T, mayBeNull > Alternative specialization of std::less for pointer types   | 846          |
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| carl::ModelSubstitution< Rational, Poly > Represent a expression for a ModelValue with variables as placeholders, where the final expression's value depends on the bindings/values of these variables                    | 875 |
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| carl::MultivariateHorner< PolynomialType, strategy >  | 911 |
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| carl::tree_detail::PathIterator< T >     Iterator class for iterations from a given element to the root              | 963 |
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| carl::policies< Number, Interval > Struct which holds the rounding and checking policies required for boost interval | 976 |
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| carl::PolynomialFactorizationPair< P >   | 978 |
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| carl::tree_detail::PostorderIterator< T, reverse > Iterator class for post-order iterations over all elements  | 990  |
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| carl::io::parser::RationalPolicies < Coeff >   | 1024 |
| carl::parser::RationalPolicies< T > Specialization of qi::real_policies for our rational types   | 1024 |
| carl::RealAlgebraicNumber < Number >   | 1026 |
| carl::RealAlgebraicNumberThom< Number >  | 1026 |
| carl::RealRadicalAwareAdding< Polynomial >   | 1029 |
| carl::ran::interval::RealRootIsolation< Number > Compact class to isolate real roots from a univariate polynomial using bisection  | 1030 |
| carl::RealRootsResult< RAN >   | 1031 |
| carl::logging::RecordInfo Additional information about a log message   | 1032 |
| carl::Reductor< InputPolynomial, PolynomialInIdeal, Datastructure, Configuration > A dedicated algorithm for calculating the remainder of a polynomial modulo a set of other polynomials | 1033 |
| carl::ReductorConfiguration < Polynomial > Class with the settings for the reduction algorithm   | 1036 |

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| carl::covering::SetCover Represents a set cover problem  | 1056 |
| carl::settings::Settings Base class for central settings class                                       | 1059 |
| carl::settings::SettingsParser  Base class for a settings parser                                     | 1059 |
| carl::settings::SettingsPrinter Helper class to nicely print the settings that were parsed           | 1064 |
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| carl::SimpleNewton< Polynomial >   | 1068 |
| carl::Singleton < T > Base class that implements a singleton   | 1068 |
| carl::logging::Sink Base class for a logging sink  | 1070 |
| carl::io::detail::SMTLIBOutputContainer< Args >  | 1071 |
| carl::io::detail::SMTLIBScriptContainer< Pol > Shorthand to allow writing SMTLIB scripts in one line | 1071 |
| carl::io::SMTLIBStream Allows to print carl data structures in SMTLIB syntax                         | 1073 |
| carl::Sort Implements a sort (for defining types of variables and functions)                         | 1078 |
| sortByLeadingTerm< Polynomial > Sorts generators of an ideal by their leading terms                  | 1080 |
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| carl::SortContent The actual content of a sort   | 1082 |

| carl::SortManager Implements a manager for sorts, containing the actual contents of these sort and allocating their ids            | 1<br>1084 |
|--|-----------|
| carl::SortValue Implements a sort value, being a value of the uninterpreted domain specified by this sort                          | 1091      |
| carl::SortValueManager Implements a manager for sort values, containing the actual contents of these sort and allocating their ids | 1092      |
| carl::SPolPair Basic spol-pair   | 1094      |
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| carl::StdAdding< Polynomial >  | 1106      |
| carl::StdMultivariatePolynomialPolicies < ReasonsAdaptor, Allocator > The default policy for polynomials                           | 1106      |
| carl::strategy   | 1108      |
| carl::detail::stream_joined_impl< T, F >   | 1108      |
| carl::logging::StreamSink Logging sink that wraps an arbitrary std::ostream  | 1109      |
| carl::io::StringParser   | 1110      |
| carl::vs::detail::Substitution < Poly >  | 1112      |
| carl::helper::Substitutor< Pol >   | 1113      |
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| carl::TarskiQueryManager< Number >   | 1115      |
| carl::TaylorExpansion < Integer >  | 1116      |
| carl::Term< Coefficient > Represents a single term, that is a numeric coefficient and a monomial                                   | 1116      |
| carl::vs::Term< Poly >   | 1127      |
| carl::TermAdditionManager< Polynomial, Ordering >  | 1129      |
| carl::ThomEncoding< Number >   | 1132      |
| carl::statistics::timer  | 1138      |
| carl::Timer  This classes provides an easy way to obtain the current number of milliseconds that the program has been running      | 1139      |

| carl::ToGiNaC  | 1139             |
|--|------------------|
| carl::tree< T > This class represents a tree   | 1142             |
| carl::detail::tuple_accumulate_impl< Tuple, T, F > Helper functor for carl::tuple_accumulate that actually does the work   | 1155             |
| carl::tuple_convert< Converter, Information, FOut, TOut >  | 1155             |
| carl::tuple_convert< Converter, Information, Out >   | 1156             |
| carl::covering::TypedSetCover< Set > Represents a set cover problem where a set is represented by some type  | 1157             |
| carl::UEquality Implements an uninterpreted equality, that is an equality of either two uninterpreted function instances, two uninterpreted variables, or an uninterpreted function instance and an uninterpreted variable |                  |
| carl::UFContent The actual content of an uninterpreted function instance   | 1162             |
| carl::UFInstance Implements an uninterpreted function instance   | 1164             |
| carl::UFInstanceContent The actual content of an uninterpreted function instance   | 1165             |
| carl::UFInstanceManager Implements a manager for uninterpreted function instances, containing their actual contents and allocating their ids   | 1168             |
| carl::UFManager Implements a manager for uninterpreted functions, containing their actual contents and allocating their ids  | 1170             |
| carl::UFModel Implements a sort value, being a value of the uninterpreted domain specified by this sort  | 1173             |
| carl::UnderlyingNumberType< T > Gives the underlying number type of a complex object   | 1174             |
| carl::UnderlyingNumberType< MultivariatePolynomial< C, O, P > >     States that UnderlyingNumberType of MultivariatePolynomial <c,o,p> is UnderlyingNumberType 1174</c,o,p>  | oe <c>::type</c> |
| carl::UnderlyingNumberType< UnivariatePolynomial< C >> States that UnderlyingNumberType of UnivariatePolynomial <t> is UnderlyingNumberType<c> 1175</c></t>  | >::type          |
| carl::UninterpretedFunction Implements an uninterpreted function   | 1176             |
| carl::helper::UninterpretedSubstitutor< Pol >  | 1177             |
| carl::UnivariatePolynomial < Coefficient > This class represents a univariate polynomial with coefficients of an arbitrary type  | 1178             |
| carl::UndateEnc  | 1216             |

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| carl::UpdateFnct< BuchbergerProc >  | 1217 |
|---|------|
| carl::UpperBound< Number >  | 1217 |
| carl::UTerm Implements an uninterpreted term, that is either an uninterpreted variable or an uninterpreted function instance  | 1218 |
| carl::UVariable Implements an uninterpreted variable  | 1220 |
| carl::Variable  A Variable represents an algebraic variable that can be used throughout carl  | 1222 |
| carl::variable_type_filter  | 1230 |
| carl::VariableAssignment< Poly >  | 1231 |
| carl::VariableComparison< Poly > Represent a sum type/variant of an (in)equality between a variable on the left-hand side and multivariateRoot or algebraic real on the right-hand side | 1234 |
| carl::VariablePool This class generates new variables and stores human-readable names for them  | 1236 |
| carl::detail::variant_extend_visitor< Target >  | 1240 |
| carl::detail::variant_hash  | 1241 |
| carl::detail::variant_is_type_visitor< T >  | 1241 |
| carl::VarInfo < CoeffType >   | 1241 |
| carl::VarsInfo < CoeffType >  | 1243 |
| carl::VarSolutionFormula < Polynomial >   | 1245 |
| carl::Void < typename >   | 1246 |
| carl::vs::zero< Poly > A square root expression with side conditions  | 1246 |

# 10 Module Documentation

# 10.1 Polynomials

### **Modules**

- Multivariate Represented Polynomials
- Univariate Represented Polynomials

# 10.1.1 Detailed Description

# 10.2 Multivariate Represented Polynomials

## **Files**

• file Monomial.h

- · file MultivariatePolynomial.h
- file MultivariatePolynomialPolicy.h
- file MultivariatePolynomial.tpp
- file MonomialOrdering.h
- file EZGCD.h

· class carl::Monomial

The general-purpose monomials.

class carl::MultivariatePolynomial< Coeff, Ordering, Policies >

The general-purpose multivariate polynomial class.

struct carl::StdMultivariatePolynomialPolicies< ReasonsAdaptor, Allocator >

The default policy for polynomials.

class carl::Term< Coefficient >

Represents a single term, that is a numeric coefficient and a monomial.

struct carl::MonomialComparator< f, degreeOrdered >

A class for term orderings.

class carl::EZGCD< Coeff, Ordering, Policies >

Extended Zassenhaus algorithm for multivariate GCD calculation.

### 10.2.1 Detailed Description

# 10.3 Univariate Represented Polynomials

#### Files

• file UnivariatePolynomial.h

### **Data Structures**

class carl::UnivariatePolynomial < Coefficient >

This class represents a univariate polynomial with coefficients of an arbitrary type.

### 10.3.1 Detailed Description

### 10.4 Constraints

### **Files**

- · file Relation.h
- file ConstraintOperations.h

10.5 Algorithms 53

# 10.4.1 Detailed Description

# 10.5 Algorithms

#### **Modules**

- Greatest Common Divisor
- · Groebner Bases
- Cylindrical Algebraic Decomposition

### 10.5.1 Detailed Description

## 10.6 Greatest Common Divisor

#### **Files**

• file EZGCD.h

# **Data Structures**

• class carl::EZGCD< Coeff, Ordering, Policies >

Extended Zassenhaus algorithm for multivariate GCD calculation.

## 10.6.1 Detailed Description

# 10.7 Groebner Bases

## Files

- file DivisionLookupResult.h
- file Buchberger.h
- · file CriticalPairs.h
- file CriticalPairsEntry.h
- file SPolPair.h
- file GBProcedure.h
- file GBUpdateProcedures.h
- file Ideal.h
- file ReductorEntry.h

- struct carl::UpdateFnct< BuchbergerProc >
- struct carl::DefaultBuchbergerSettings

Standard settings used if the Buchberger object is not instantiated with another template parameter.

class carl::Buchberger< Polynomial, AddingPolicy >

Gebauer and Moeller style implementation of the Buchberger algorithm.

class carl::CriticalPairsEntry
 Compare >

A list of SPol pairs which have to be checked by the Buchberger algorithm.

class carl::GBProcedure
 Polynomial
 Procedure
 AddingPolynomialPolicy

A general class for Groebner Basis calculation.

- class carl::Ideal
   Polynomial, Datastructure, CacheSize >
- class carl::ReductorConfiguration< Polynomial >

Class with the settings for the reduction algorithm.

class carl::Reductor < InputPolynomial, PolynomialInIdeal, Datastructure, Configuration >

A dedicated algorithm for calculating the remainder of a polynomial modulo a set of other polynomials.

class carl::ReductorEntry< Polynomial >

An entry in the reduction polynomial.

### 10.7.1 Detailed Description

# 10.8 Cylindrical Algebraic Decomposition

# 10.9 Number Types

### **Modules**

- GMPxx Usage
- · CLN Usage

### 10.9.1 Detailed Description

# 10.10 GMPxx Usage

### Files

- · file hash.h
- · file operations.h
- · file typetraits.h

#### **Data Structures**

struct carl::is\_integer\_type< mpz\_class >

States that mpz\_class has the trait is\_integer\_type.

struct carl::is\_rational\_type< mpq\_class >

States that mpq\_class has the trait is\_rational\_type .

struct carl::IntegralType< mpq\_class >

States that IntegralType of mpg\_class is mpz\_class.

struct carl::IntegralType< mpz\_class >

States that IntegralType of mpz\_class is mpz\_class.

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### 10.10.1 Detailed Description

# 10.11 CLN Usage

#### **Files**

- · file hash.h
- · file operations.h
- · file typetraits.h

#### **Data Structures**

struct carl::is\_integer\_type< cln::cl\_l >

States that cln::cl\_I has the trait is\_integer\_type .

struct carl::is\_rational\_type< cln::cl\_RA >

States that cln::cl\_RA has the trait is\_rational\_type .

struct carl::IntegralType< cln::cl\_l >

States that IntegralType of cln::cl\_I is cln::cl\_I.

struct carl::IntegralType< cln::cl\_RA >

States that IntegralType of cln::cl\_RA is cln::cl\_I.

#### 10.11.1 Detailed Description

## 10.12 Type Traits

We define custom type traits for number types we use.

### Modules

• is\_field\_type

All types that represent a field are marked with is\_field\_type.

• is\_finite\_type

All types that can represent only numbers from a finite domain are marked with is\_finite\_type.

• is\_float\_type

All types that represent floating point numbers are marked with is\_float\_type.

• is\_integer\_type

All integral types that can (in theory) represent all integers are marked with is\_integer\_type.

• is\_number\_type

All types that represent any kind of number are marked with is\_number\_type.

is\_rational\_type

All integral types that can (in theory) represent all rationals are marked with is\_rational\_type.

IntegralType

The associated integral type of any type can be defined with IntegralType.

• UnderlyingNumberType

The number type that some type is built upon can be defined with UnderlyingNumberType.

#### **Files**

- · file typetraits.h
- · file typetraits.h
- file typetraits.h
- · file typetraits.h

#### **Data Structures**

struct carl::has\_subtype< T >

This template is designed to provide types that are related to other types.

### 10.12.1 Detailed Description

We define custom type traits for number types we use.

We use the notation conventions of the STL, being lower cases with underscores.

We define the following type traits:

- is\_field\_type: Types that represent elements from a field.
- is\_finite\_type: Types that represent only a finite domain.
- is\_float\_type: Types that represent real numbers using a floating point representation.
- is\_integer\_type: Types that represent the set of integral numbers.
- is\_subset\_of\_integers\_type: Types that may represent some integral numbers.
- is\_number\_type: Types that represent numbers.
- is\_rational\_type: Types that may represent any rational number.
- is\_subset\_of\_rationals\_type: Types that may represent some rational numbers.

A more exact definition for each of these type traits can be found in their own documentation.

Additionally, we define related types in a type traits like manner:

- IntegralType: Integral type, that the given type is based on. For fractions, this would be the type of the numerator and denominator.
- UnderlyingNumberType: Number type that is used within a more complex type. For polynomials, this would be the number type of the coefficients.

Note that we keep away from similar type traits defined in the standard ? (20.9) (like std::is\_integral or std::is\_floating\_point, as they are not meant to be specialized for custom types.

### 10.13 is\_field\_type

All types that represent a field are marked with is\_field\_type.

10.14 is\_finite\_type 57

#### **Data Structures**

```
    struct carl::is_field_type < T >
        States if a type is a field.
    struct carl::is_field_type < GFNumber < C > >
        States that a Gallois field is a field.
```

### 10.13.1 Detailed Description

All types that represent a field are marked with is\_field\_type.

To be a field, the type must satisfy the common axioms for fields (and their technical interpretation):

- · It represents some (not empty) set of numbers.
- It defines the basic operators  $+,-,\cdot,/$ , implemented as operator+(), operator-(), operator\*(), operator/(). The result of these operators is of the same type, i.e. the type is closed under the given operations.
- · It's operations are associative and commutative. Multiplication and addition are distributive.
- There are identity elements for addition and multiplication.
- For every element of the type, there are *inverse elements* for addition and multiplication.

All types that are marked with is\_rational\_type represent a field.

# 10.14 is\_finite\_type

All types that can represent only numbers from a finite domain are marked with is\_finite\_type.

### **Data Structures**

```
    struct carl::is_finite_type< T >
        States if a type represents only a finite domain.
    struct carl::is_finite_type< GFNumber< C > >
```

Type trait is\_finite\_type\_domain.

### 10.14.1 Detailed Description

All types that can represent only numbers from a finite domain are marked with is\_finite\_type.

All fundamental types are also finite.

### 10.15 is\_float\_type

All types that represent floating point numbers are marked with is\_float\_type.

struct carl::is\_float\_type < T >
 States if a type is a floating point type.

#### 10.15.1 Detailed Description

All types that represent floating point numbers are marked with is\_float\_type.

A floating point type is used to approximate real number and in general behaves like a field. However, it does not guarantee exact computation and may be subject to rounding errors or overflows.

# 10.16 is\_integer\_type

All integral types that can (in theory) represent all integers are marked with is\_integer\_type.

#### **Modules**

• is\_subset\_of\_integers\_type

All integral types are marked with is\_subset\_of\_integers\_type.

#### **Data Structures**

struct carl::is\_integer\_type< T >

States if a type is an integer type.

struct carl::is\_integer\_type< mpz\_class >

States that mpz\_class has the trait is\_integer\_type .

struct carl::is\_integer\_type< cln::cl\_l >

States that cln::cl\_I has the trait is\_integer\_type .

#### 10.16.1 Detailed Description

All integral types that can (in theory) represent all integers are marked with is\_integer\_type.

To be an integer type, the type must satisfy the following conditions:

- · It represents exactly all integer numbers.
- It defines the basic operators  $+, -, \cdot$  by implementing operator+(), operator-() and operator\*() which are closed.
- It's operations are associative and commutative. Multiplication and addition are distributive.
- There are identity elements for addition and multiplication.
- For every element of the type, there is an inverse element for addition.
- · Additionally, it defines the following operations:
  - div (): Performs an integer division, asserting that the remainder is zero.
  - quotient (): Calculates the quotient of an integer division.
  - remainder (): Calculates the remainder of an integer division.
  - mod (): Calculated the modulus of an integer.
  - operator/() shall be an alias for quotient().

# 10.17 is\_subset\_of\_integers\_type

All integral types are marked with is\_subset\_of\_integers\_type.

#### **Data Structures**

struct carl::is\_subset\_of\_integers\_type< Type >

States if a type represents a subset of all integers.

struct carl::is\_subset\_of\_integers\_type< signed char >

States that signed char has the trait is\_subset\_of\_integers\_type .

struct carl::is\_subset\_of\_integers\_type< short int >

States that short int has the trait is\_subset\_of\_integers\_type .

struct carl::is\_subset\_of\_integers\_type< int >

States that int has the trait is\_subset\_of\_integers\_type .

struct carl::is\_subset\_of\_integers\_type< long int >

States that long int has the trait is\_subset\_of\_integers\_type .

struct carl::is\_subset\_of\_integers\_type< long long int >

States that long long int has the trait is\_subset\_of\_integers\_type .

struct carl::is\_subset\_of\_integers\_type< unsigned char >

States that unsigned char has the trait is\_subset\_of\_integers\_type .

struct carl::is\_subset\_of\_integers\_type< unsigned short int >

States that unsigned short int has the trait is\_subset\_of\_integers\_type.

struct carl::is\_subset\_of\_integers\_type< unsigned int >

States that unsigned int has the trait is\_subset\_of\_integers\_type .

struct carl::is\_subset\_of\_integers\_type< unsigned long int >

States that unsigned long int has the trait is\_subset\_of\_integers\_type.

- struct carl::is\_subset\_of\_integers\_type< unsigned long long int >

States that unsigned long long int has the trait is\_subset\_of\_integers\_type .

### 10.17.1 Detailed Description

All integral types are marked with is\_subset\_of\_integers\_type.

They must satisfy the same conditions as for is\_integer\_type, except that they may represent only a subset of all integer numbers. If this is the case, std::numeric\_limits must be specialized. If the limits are exceeded, the type may behave arbitrarily and the type is not obliged to check for this.

# 10.18 is\_number\_type

All types that represent any kind of number are marked with is\_number\_type.

- struct carl::is\_number\_type< T >
  - States if a type is a number type.
- struct carl::is\_number\_type< GFNumber< C >>

### 10.18.1 Detailed Description

All types that represent any kind of number are marked with is\_number\_type.

All number types are required to implement the following methods:

- abs (): Returns the absolute value.
- floor(): Returns the nearest integer below.
- ceil (): Returns the nearest integer above.
- pow (): Returns the power.

### 10.19 is\_rational\_type

All integral types that can (in theory) represent all rationals are marked with is\_rational\_type.

#### **Modules**

· is\_subset\_of\_rationals\_type

All rational types that can represent a subset of all rationals are marked with is\_subset\_of\_rationals\_type.

# **Data Structures**

- struct carl::is\_rational\_type < mpq\_class >
   States that mpq\_class has the trait is\_rational\_type .
- struct carl::is\_rational\_type< cln::cl\_RA >

States that cln::cl\_RA has the trait is\_rational\_type .

# 10.19.1 Detailed Description

All integral types that can (in theory) represent all rationals are marked with is\_rational\_type.

It is assumed that a fractional representation is used. A type that is rational must satisfy all requirements of is\_field\_type. Additionally, it must implement the following methods:

- get\_num(): Returns the numerator of a fraction.
- get\_denom(): Return the denominator of a fraction.
- rationalize (): Converts a native floating point number to the rational type.

### 10.20 is\_subset\_of\_rationals\_type

All rational types that can represent a subset of all rationals are marked with  $is\_subset\_of\_rationals\_type$ .

10.21 IntegralType 61

### **Data Structures**

struct carl::is\_subset\_of\_rationals\_type< T >

States if a type represents a subset of all rationals and the representation is similar to a rational.

#### 10.20.1 Detailed Description

All rational types that can represent a subset of all rationals are marked with is\_subset\_of\_rationals\_type.

It is assumed that a fractional representation is used and the restriction to a subset of all rationals is due to the type of the numerator and the denominator.

# 10.21 IntegralType

The associated integral type of any type can be defined with IntegralType.

#### **Data Structures**

```
    struct carl::IntegralType
    RationalType >
```

Gives the corresponding integral type.

struct carl::IntegralType< float >

States that IntegralType of float is sint.

struct carl::IntegralType< double >

States that IntegralType of double is sint .

struct carl::IntegralType< long double >

States that IntegralType of long double is sint .

struct carl::IntegralType< mpq\_class >

States that IntegralType of mpq\_class is mpz\_class.

struct carl::IntegralType< mpz\_class >

States that IntegralType of mpz\_class is mpz\_class.

• struct carl::IntegralType< cln::cl\_l >

States that IntegralType of cln::cl\_I is cln::cl\_I.

struct carl::IntegralType< cln::cl\_RA >

States that IntegralType of cln::cl\_RA is cln::cl\_I.

### 10.21.1 Detailed Description

The associated integral type of any type can be defined with IntegralType.

Any function that operates on the type and naturally returns an integer, regardless whether the input was actually integral, uses the associated integral type as result type. Simple examples for this are <a href="mailto:get\_num">get\_num</a>() and <a href="mailto:get\_num">get\_num</a>() and <a href="mailto:get\_num">get\_num</a>() which return the numerator and denominator respectively of a fraction.

### 10.22 UnderlyingNumberType

The number type that some type is built upon can be defined with UnderlyingNumberType.

- struct carl::UnderlyingNumberType< T >
  - Gives the underlying number type of a complex object.
- struct carl::UnderlyingNumberType< MultivariatePolynomial< C, O, P >>
  - $States\ that\ Underlying Number Type\ of\ Multivariate Polynomial < C, O, P>\ is\ Underlying Number Type < C>::type.$
- struct carl::UnderlyingNumberType< UnivariatePolynomial< C >>

States that UnderlyingNumberType of UnivariatePolynomial<T> is UnderlyingNumberType<C>::type.

#### 10.22.1 Detailed Description

The number type that some type is built upon can be defined with UnderlyingNumberType.

Any function that operates on the (more complex) type and returns a number can use this trait. The function can thereby easily retrieve the exact number type that is used within the complex type.

# 11 Namespace Documentation

## 11.1 carl Namespace Reference

carl is the main namespace for the library.

#### **Namespaces**

- · benchmarks
- · checkpoints
- constraint
- · constraints
- contractor
- convert\_poly
- convert\_ran
- · covering
- detail
- detail\_derivative
- · detail\_sign\_variations
- dtl
- formula
- formula\_to\_cnf
- · gcd\_detail
- · helper
- io
- logging

Contains a custom logging facility.

- model
- · parser
- poly\_helper

Helpers due to the shortcomings of libpoly's C++ API.

- pool
- ran
- · resultant\_debug
- roots
- · settings
- · statistics
- tree\_detail
- VS

· class Variable

A Variable represents an algebraic variable that can be used throughout carl.

class VariablePool

This class generates new variables and stores human-readable names for them.

class Singleton

Base class that implements a singleton.

class BuchbergerStats

A little class for gathering statistics about the Buchberger algorithm calls.

- struct constant\_zero
- struct constant\_one
- struct remove\_all
- struct remove\_all
   T, T >
- struct has\_subtype

This template is designed to provide types that are related to other types.

class GFNumber

Galois Field numbers, i.e.

· class UnivariatePolynomial

This class represents a univariate polynomial with coefficients of an arbitrary type.

· class MultivariatePolynomial

The general-purpose multivariate polynomial class.

struct is\_rational\_type

States if a type is a rational type.

struct is\_subset\_of\_rationals\_type

States if a type represents a subset of all rationals and the representation is similar to a rational.

struct is\_field\_type

States if a type is a field.

struct is\_field\_type< GFNumber< C >>

States that a Gallois field is a field.

struct is\_finite\_type

States if a type represents only a finite domain.

• struct is\_finite\_type< GFNumber< C >>

Type trait is\_finite\_type\_domain.

struct is\_float\_type

States if a type is a floating point type.

• struct is\_integer\_type

States if a type is an integer type.

struct is\_subset\_of\_integers\_type

States if a type represents a subset of all integers.

struct is\_number\_type

States if a type is a number type.

- struct is\_number\_type< GFNumber< C >>
- · struct characteristic

Type trait for the characteristic of the given field (template argument).

struct IntegralType

Gives the corresponding integral type.

- struct IntegralType< GFNumber< C >>
- struct UnderlyingNumberType

Gives the underlying number type of a complex object.

• class PreventConversion

 struct is\_subset\_of\_integers\_type< signed char > States that signed char has the trait is\_subset\_of\_integers\_type . struct is\_subset\_of\_integers\_type< short int > States that short int has the trait is\_subset\_of\_integers\_type . struct is\_subset\_of\_integers\_type< int > States that int has the trait is\_subset\_of\_integers\_type . struct is\_subset\_of\_integers\_type< long int > States that long int has the trait is\_subset\_of\_integers\_type . struct is\_subset\_of\_integers\_type< long long int > States that long long int has the trait is\_subset\_of\_integers\_type . struct is\_subset\_of\_integers\_type< unsigned char > States that unsigned char has the trait is\_subset\_of\_integers\_type . struct is\_subset\_of\_integers\_type< unsigned short int > States that unsigned short int has the trait is\_subset\_of\_integers\_type . struct is\_subset\_of\_integers\_type< unsigned int > States that unsigned int has the trait is\_subset\_of\_integers\_type . struct is\_subset\_of\_integers\_type< unsigned long int > States that unsigned long int has the trait is\_subset\_of\_integers\_type . struct is\_subset\_of\_integers\_type< unsigned long long int > States that unsigned long long int has the trait is\_subset\_of\_integers\_type . struct IntegralType< float > States that IntegralType of float is sint . struct IntegralType< double > States that IntegralType of double is sint . struct IntegralType< long double > States that Integral Type of long double is sint. struct is\_integer\_type< mpz\_class > States that mpz\_class has the trait is\_integer\_type . struct is\_rational\_type< mpq\_class > States that mpq\_class has the trait is\_rational\_type . struct IntegralType< mpq\_class > States that IntegralType of mpq\_class is mpz\_class. struct IntegralType< mpz\_class > States that IntegralType of mpz\_class is mpz\_class. · class Interval The class which contains the interval arithmetic including trigonometric functions. class FLOAT\_T Templated wrapper class which allows universal usage of different IEEE 754 implementations. struct FloatConv point implementations. • struct IntegralType< carl::FLOAT $_{-}$ T< F > > struct is\_rational\_type< FLOAT\_T< C >>

Struct which holds the conversion operator for any two instanciations of FLOAT\_T with different underlying floating

- struct is\_float\_type< carl::FLOAT\_T< C >>
- struct IntegerPairCompare
- · class GaloisField

A finite field.

- · class GaloisFieldManager
- struct is\_interval\_type

States whether a given type is an Interval.

· struct overloaded

- struct dependent\_bool\_type
- · struct any

Meta-logical disjunction.

- struct any< Head, Tail... >
- struct all

Meta-logical conjunction.

- struct all
   Head, Tail...
- struct Void
- struct is\_instantiation\_of
- struct is\_instantiation\_of< Template, Template< Args... >>
- struct hash\_inserter

Utility functor to hash a sequence of object using an output iterator.

- struct convRnd
- · class MonomialPool
- · class Monomial

The general-purpose monomials.

- struct hashLess
- struct hashEqual
- class IDPool
- · class Bitset

This class is a simple wrapper around boost::dynamic\_bitset.

struct EEA

Extended euclidean algorithm for numbers.

- class variable\_type\_filter
- · class carlVariables
- struct CompileInfo

Compile time generated structure holding information about compiler and system version.

- struct CMakeOptionPrinter
- · class BitVector
- class BVConstraint
- class BVConstraintPool
- class Pool
- class BVTerm
- struct is\_from\_variant
- struct convertible\_to\_variant
- · class BVValue
- class BVVariable

Represent a BitVector-Variable.

- struct BVUnaryContent
- struct BVBinaryContent
- struct BVExtractContent
- struct BVTermContent
- class BVTermPool
- struct SortContent

The actual content of a sort.

class SortManager

Implements a manager for sorts, containing the actual contents of these sort and allocating their ids.

• class Sort

Implements a sort (for defining types of variables and functions).

• struct equal\_to

Alternative specialization of std::equal\_to for pointer types.

- struct equal\_to < T \*, mayBeNull >
- struct equal\_to< std::shared\_ptr< T >, mayBeNull >

- · struct not\_equal\_to
- struct not\_equal\_to < T \*, mayBeNull >
- struct not\_equal\_to< std::shared\_ptr< T >, mayBeNull >
- struct less

Alternative specialization of std::less for pointer types.

- struct less< T \*, mayBeNull >
- struct less< std::shared\_ptr< T >, mayBeNull >
- · struct greater
- struct greater< T \*, mayBeNull >
- struct greater< std::shared\_ptr< T >, mayBeNull >
- · struct hash

Alternative specialization of std::hash for pointer types.

- struct hash< T \*, mayBeNull >
- struct hash< std::shared\_ptr< T >, mayBeNull >
- · class UEquality

Implements an uninterpreted equality, that is an equality of either two uninterpreted function instances, two uninterpreted variables, or an uninterpreted function instance and an uninterpreted variable.

· class UFInstance

Implements an uninterpreted function instance.

· class UFInstanceContent

The actual content of an uninterpreted function instance.

class UFInstanceManager

Implements a manager for uninterpreted function instances, containing their actual contents and allocating their ids.

· class UVariable

Implements an uninterpreted variable.

· class UninterpretedFunction

Implements an uninterpreted function.

class UTerm

Implements an uninterpreted term, that is either an uninterpreted variable or an uninterpreted function instance.

class UFContent

The actual content of an uninterpreted function instance.

class UFManager

Implements a manager for uninterpreted functions, containing their actual contents and allocating their ids.

class UFModel

Implements a sort value, being a value of the uninterpreted domain specified by this sort.

class SortValueManager

Implements a manager for sort values, containing the actual contents of these sort and allocating their ids.

- struct rounding
- struct is\_polynomial\_type< carl::MultivariatePolynomial< T, O, P >>
- struct UnderlyingNumberType< MultivariatePolynomial< C, O, P >>

 $States\ that\ Underlying Number Type\ of\ Multivariate Polynomial < C,O,P>\ is\ Underlying Number Type < C>::type.$ 

class Timer

This classes provides an easy way to obtain the current number of milliseconds that the program has been running.

- · class MultivariateHorner
- struct StdMultivariatePolynomialPolicies

The default policy for polynomials.

· class Term

Represents a single term, that is a numeric coefficient and a monomial.

- class TermAdditionManager
- struct is\_polynomial\_type
- struct needs\_cache\_type
- struct needs\_context\_type

- struct is\_factorized\_type
- · struct MonomialComparator

A class for term orderings.

- struct NoAllocator
- struct NoReasons
- struct BVReasons
- class IntRepRealAlgebraicNumber
- struct is\_polynomial\_type< carl::UnivariatePolynomial< T > >
- struct UnderlyingNumberType
   UnivariatePolynomial
   C >>

States that UnderlyingNumberType of UnivariatePolynomial<T> is UnderlyingNumberType<C>::type.

- struct is\_interval\_type< carl::Interval< Number > >
- struct is\_interval\_type< const carl::Interval< Number >>
- · struct policies

Struct which holds the rounding and checking policies required for boost interval.

struct policies < double, Interval >

Template specialization for rounding and checking policies for native double.

- · struct LowerBound
- struct UpperBound
- struct is\_number\_type< Interval< T >>
- · struct checking
- struct rounding
   FLOAT\_T
   FloatType
- · class VarSolutionFormula
- · class Contraction
- class SimpleNewton
- · struct DivisionResult

A strongly typed pair encoding the result of a division, being a quotient and a remainder.

· class BasicConstraint

Represent a polynomial (in)equality against zero.

- · class CArLConverter
- class ConvertTo
- class ConvertFrom
- · class GiNaCConversion
- class ToGiNaC
- class FromGiNaC
- · class MultivariateRoot
- class VariableAssignment
- · class VariableComparison

Represent a sum type/variant of an (in)equality between a variable on the left-hand side and multivariateRoot or algebraic real on the right-hand side.

· struct DivisionLookupResult

The result of.

- struct UpdateFnct
- struct DefaultBuchbergerSettings

Standard settings used if the Buchberger object is not instantiated with another template parameter.

· class Buchberger

Gebauer and Moeller style implementation of the Buchberger algorithm.

- class CriticalPairConfiguration
- · class CriticalPairs

A data structure to store all the SPolynomial pairs which have to be checked.

class CriticalPairsEntry

A list of SPol pairs which have to be checked by the Buchberger algorithm.

struct SPolPair

Basic spol-pair.

- · struct SPolPairCompare
- · class AbstractGBProcedure
- · class GBProcedure

A general class for Groebner Basis calculation.

- struct UpdateFnc
- struct StdAdding
- · struct RadicalAwareAdding
- · struct RealRadicalAwareAdding
- · class IdealDatastructureVector
- · class Ideal
- class ReductorConfiguration

Class with the settings for the reduction algorithm.

· class Reductor

A dedicated algorithm for calculating the remainder of a polynomial modulo a set of other polynomials.

class ReductorEntry

An entry in the reduction polynomial.

struct is\_integer\_type< cln::cl\_l >

States that cln::cl\_l has the trait is\_integer\_type .

struct is\_rational\_type< cln::cl\_RA >

States that cln::cl\_RA has the trait is\_rational\_type .

struct IntegralType< cln::cl\_l >

States that IntegralType of cln::cl\_I is cln::cl\_I.

struct IntegralType< cln::cl\_RA >

States that IntegralType of cln::cl\_RA is cln::cl\_I.

class FactorizationFactory

This class provides a cached factorization for numbers.

class FactorizationFactory< uint >

This class provides a cached prime factorization for std::size\_t.

class PrimeFactory

This class provides a convenient way to enumerate primes.

- class Context
- class ContextPolynomial
- struct needs\_context\_type< ContextPolynomial< Coeff, Ordering, Policies > >
- struct is\_polynomial\_type< ContextPolynomial< Coeff, Ordering, Policies >>
- struct Chebyshev

Implements a generator for Chebyshev polynomials.

class EZGCD

Extended Zassenhaus algorithm for multivariate GCD calculation.

- struct strategy
- · class DiophantineEquations

Includes the algorithms 6.2 and 6.3 from the book Algorithms for Computer Algebra by Geddes, Czaper, Labahn.

- · class MultivariateHensel
- · class TaylorExpansion
- · class VarInfo
- · class VarsInfo
- struct is\_ran\_type
- class RealRootsResult
- struct is\_ran\_type< IntRepRealAlgebraicNumber< Number > >
- struct RealAlgebraicNumberThom
- struct is\_ran\_type< RealAlgebraicNumberThom< Number >>
- class SignCondition
- class SignDetermination

- · class GroebnerBase
- struct BaseRepresentation
- · class MultiplicationTable
- · class TarskiQueryManager
- class ThomEncoding
- class RealAlgebraicNumber
- class SqrtEx
- · class tree

This class represents a tree.

class CompactTree

This class packs a complete binary tree in a vector.

class Heap

A heap priority queue.

- · class Cache
- struct mpl\_unique
- struct mpl\_concatenate\_impl
- struct mpl\_concatenate\_impl< 1, Front, Tail... >
- struct mpl\_concatenate
- struct mpl\_variant\_of\_impl
- struct mpl\_variant\_of\_impl< true, Vector, Unpacked... >
- struct mpl\_variant\_of
- · class tuple\_convert
- class tuple\_convert< Converter, Information, Out >
- class FactorizedPolynomial
- struct needs\_cache\_type< FactorizedPolynomial< P > >
- struct is\_factorized\_type< FactorizedPolynomial< P >>
- · class Factorization
- · class PolynomialFactorizationPair
- · class RationalFunction
- class Constraint

Represent a polynomial (in)equality against zero.

- struct CachedConstraintContent
- · class Condition
- · class Formula

Represent an SMT formula, which can be an atom for some background theory or a boolean combination of (sub)formulas.

- class FormulaPool
- · struct QuantifierContent

Stores the variables and the formula bound by a quantifier.

- class FormulaContent
- class Model

Represent a collection of assignments/mappings from variables to values.

- class ModelFormulaSubstitution
- class ModelMVRootSubstitution
- · class ModelPolynomialSubstitution
- · class ModelSubstitution

Represent a expression for a ModelValue with variables as placeholders, where the final expression's value depends on the bindings/values of these variables.

class ModelValue

Represent a sum type/variant over the different kinds of values that can be assigned to the different kinds of variables that exist in CARL and to use them in a more uniform way, e.g.

struct InfinityValue

This class represents infinity or minus infinity, depending on its flag positive.

· class ModelVariable

Represent a sum type/variant over the different kinds of variables that exist in CARL to use them in a more uniform way, e.g.

- · class ModelConditionalSubstitution
- class SortValue

Implements a sort value, being a value of the uninterpreted domain specified by this sort.

### **Typedefs**

```
 using uint = std::uint64_t

• using sint = std::int64_t
template<typename C >
  using IntegralTypeIfDifferent = typename std::enable_if<!std::is_same< C, typename IntegralType< C >←
  ::type >::value, typename IntegralType < C >::type >::type

    using precision_t = std::size_t

- template<br/>bool If, typename Then , typename Else >
  using Conditional = typename std::conditional < If, Then, Else >::type
• template<bool B, typename... T>
  using Bool = typename dependent_bool_type< B, T... >::type
template<typename T >
  using Not = Bool<!T::value >
     Meta-logical negation.
• template<typename... Condition>
  using EnableIf = typename std::enable_if < all < Condition... >::value, dtl::enabled >::type
• template<typename... Condition>
  using DisableIf = typename std::enable_if < Not < any < Condition... > >::value, dtl::enabled >::type
· template<bool Condition>
  using EnableIfBool = typename std::enable_if< Condition, dtl::enabled >::type
• using exponent = std::size_t
      Type of an exponent.
• template<typename T >
  using pointerEqual = carl::equal_to < const T *, false >

    template<typename T >

  using pointerEqualWithNull = carl::equal_to < const T *, true >

    template<typename T >

  using sharedPointerEqual = carl::equal_to < std::shared_ptr < const T >, false >
• template<typename T >
  using sharedPointerEqualWithNull = carl::equal_to< std::shared_ptr< const T >, true >

    template<typename T >

  using pointerLess = carl::less < const T *, false >

    template<typename T >

  using pointerLessWithNull = carl::less< const T *, true >

    template<typename T >

  using sharedPointerLess = carl::less< std::shared_ptr< const T > *, false >
template<typename T >
  using sharedPointerLessWithNull = carl::less< std::shared_ptr< const T >, true >
• template<typename T >
  using pointerHash = carl::hash < T *, false >

    template<typename T >

  using pointerHashWithNull = carl::hash< T *, true >
• template<typename T >
  using sharedPointerHash = carl::hash< std::shared_ptr< const T > *, false >
\bullet \ \ template\!<\!typename\ T>
  using sharedPointerHashWithNull = carl::hash< std::shared_ptr< const T > *, true >
```

```
• template<typename T >
  using PointerSet = std::set< const T *, pointerLess< T >>
template<typename T >
  using PointerMultiSet = std::multiset < const T *, pointerLess < T > >

    template<typename T1, typename T2 >

  using PointerMap = std::map < const T1 *, T2, pointerLess < T1 > >
template<typename T >
  using SharedPointerSet = std::set< std::shared_ptr< const T >, sharedPointerLess< T >>
• template<typename T >
  using SharedPointerMultiSet = std::multiset < std::shared_ptr < const T >, sharedPointerLess < T > >
• template<typename T1 , typename T2 >
  using SharedPointerMap = std::map < std::shared_ptr < const T1 >, T2, sharedPointerLess < T1 > >
• template<typename T >
  using FastSet = std::unordered_set< T, std::hash< T >>

    template<typename T1 , typename T2 >

  using FastMap = std::unordered_map< T1, T2, std::hash< T1 >>

    template<typename T >

  using FastPointerSet = std::unordered_set< const T *, pointerHash< T >, pointerEqual< T > >
• template<typename T1 , typename T2 >
  using FastPointerMap = std::unordered_map < const T1 *, T2, pointerHash < T1 >, pointerEqual < T1 > >

    template<typename T >

  using FastSharedPointerSet = std::unordered_set< std::shared_ptr< const T >, sharedPointerHash< T >,
  sharedPointerEqual< T >>
• template<typename T1 , typename T2 >
  using FastSharedPointerMap = std::unordered_map < std::shared_ptr < const T1 >, T2, sharedPointerHash <
  T1 >, sharedPointerEqual < T1 > >

    template<typename T >

  using FastPointerSetB = std::unordered_set< const T *, pointerHashWithNull< T >, pointerEqualWithNull<
  T > >

    template<typename T1, typename T2 >

  using FastPointerMapB = std::unordered_map< const T1 *, T2, pointerHashWithNull< T1 >, pointerEqualWithNull<
  T1 > >
template<typename T >
  using FastSharedPointerSetB = std::unordered_set< std::shared_ptr< const T >, sharedPointerHashWithNull<
  T >, pointerEqualWithNull< T >
• template<typename T1 , typename T2 >
  using FastSharedPointerMapB = std::unordered_map< std::shared_ptr< const T1 >, T2, sharedPointerHashWithNull<
  T1 >, pointerEqualWithNull< T1 >>

    using MonomialOrderingFunction = CompareResult(*)(const Monomial::Arg &, const Monomial::Arg &)

    using LexOrdering = MonomialComparator< Monomial::compareLexical, false >

    using GrLexOrdering = MonomialComparator< Monomial::compareGradedLexical, true >

    template<typename Coefficient >

  using UnivariatePolynomialPtr = std::shared_ptr< UnivariatePolynomial< Coefficient > >

    template<typename Coefficient >

  using FactorMap = std::map < UnivariatePolynomial < Coefficient >, uint >
template<typename T >
  using Assignment = std::map< Variable, T >

    template<typename T >

  using OrderedAssignment = std::vector< std::pair< Variable, T >>
using Variables = std::set< Variable >

    template<typename Pol >

  using Factors = std::map < Pol, uint >

    template<typename Poly >

  using EncodingCache = std::map< MultivariateRoot< Poly >, std::pair< std::vector< BasicConstraint< Poly
  >>, Variable >>

    typedef CriticalPairs< Heap, CriticalPairConfiguration< GrLexOrdering > > CritPairs
```

template<typename Coeff >

This class represents the sign of a number n.

enum class BoundType { STRICT = 0 , WEAK = 1 , INFTY = 2 }

using CoeffMatrix = Eigen::Matrix < Coeff, Eigen::Dynamic, Eigen::Dynamic >

```
• template<typename T , class I >
      using TypeInfoPair = std::pair < T *, I >
    template<typename P >
      using Coeff = typename UnderlyingNumberType< P >::type

    template<typename Poly >

     using Constraints = std::set< Constraint< Poly >, carl::less< Constraint< Poly >, false > >
    • template<typename Pol >
      using ConstraintPool = pool::Pool < CachedConstraintContent < Pol > >

    template<typename Poly >

      using Formulas = std::vector< Formula< Poly >>

    template<typename Poly >

      using FormulaSet = std::set < Formula < Poly > >
    template<typename Poly >
      using FormulasMulti = std::multiset< Formula< Poly >>

    template<typename Pol >

      using ConstraintBounds = FastMap < Pol, std::map < typename Pol::NumberType, std::pair < Relation,
      Formula < Pol > >> >
         A map from formula pointers to a map of rationals to a pair of a constraint relation and a formula pointer. (internally
         used)
    • template<typename Rational , typename Poly >
      using ModelSubstitutionPtr = std::unique_ptr< ModelSubstitution< Rational, Poly >>
Enumerations

    enum class VariableType {

      VT_BOOL = 0, VT_REAL = 1, VT_INT = 2, VT_UNINTERPRETED = 3,
      VT_BITVECTOR = 4, MIN_TYPE = VT_BOOL, MAX_TYPE = VT_BITVECTOR, TYPE_SIZE = MAX_TYPE -
      MIN_TYPE + 1 }
         Several types of variables are supported.

    enum Str2Double_Error { FLOAT_SUCCESS , FLOAT_OVERFLOW , FLOAT_UNDERFLOW , FLOAT_INCONVERTIBLE

    enum class CARL_RND : int {
     N = 0, Z = 1, U = 2, D = 3,
      A = 4

    enum class CompareResult { LESS = -1 , EQUAL = 0 , GREATER = 1 }

    enum class BVCompareRelation : unsigned {

      EQ, NEQ, ULT, ULE,
      UGT, UGE, SLT, SLE,
      SGT, SGE }

    enum class BVTermType {

      CONSTANT, VARIABLE, CONCAT, EXTRACT,
      NOT, NEG, AND, OR,
      XOR, NAND, NOR, XNOR,
      ADD, SUB, MUL, DIV_U,
      DIV_S . MOD_U . MOD_S1 . MOD_S2 .
      EQ, LSHIFT, RSHIFT_LOGIC, RSHIFT_ARITH,
     LROTATE, RROTATE, EXT_U, EXT_S,
      REPEAT }
    • enum class PolynomialComparisonOrder { CauchyBound , LowDegree , Memory , Default = LowDegree }

    enum class Sign { NEGATIVE = -1 , ZERO = 0 , POSITIVE = 1 }
```

```
    enum class Relation {

 EQ = 0, NEQ = 1, LESS = 2, LEQ = 4,
 GREATER = 3, GEQ = 5

    enum class Definiteness {

 NEGATIVE = 0, NEGATIVE_SEMI = 1, NON = 2, POSITIVE_SEMI = 3,
 POSITIVE = 4 }
     Regarding a polynomial p as a function p: X \to Y, its definiteness gives information about the codomain Y.

    enum variableSelectionHeurisics { GREEDY_I = 0 , GREEDY_Is = 1 , GREEDY_II = 2 , GREEDY_IIs = 3 }

    enum class SubresultantStrategy { Generic , Lazard , Ducos , Default = Lazard }

    enum ThomComparisonResult {

 LESS, LESS = -1, LESS = 2, EQUAL,
 EQUAL = 0, GREATER, GREATER = 1, GREATER = 3 }
enum FormulaType {
 ITE, EXISTS, FORALL, TRUE,
 FALSE, BOOL, NOT, NOT,
 IMPLIES, AND, AND, OR,
 OR, XOR, XOR, IFF,
 CONSTRAINT, VARCOMPARE, VARASSIGN, BITVECTOR,
 UEQ }
     Represent the type of a formula to allow faster/specialized processing.

    enum class Logic {

 QF_BV, QF_IDL, QF_LIA, QF_LIRA,
 QF_LRA, QF_NIA, QF_NIRA, QF_NRA,
 QF_PB, QF_RDL, QF_UF, UNDEFINED }
```

## **Functions**

std::ostream & operator<< (std::ostream &os, const VariableType &t)</li>

Streaming operator for VariableType.

std::ostream & operator<< (std::ostream &os, Variable rhs)</li>

Streaming operator for Variable.

- Variable fresh\_variable (VariableType vt) noexcept
- Variable fresh\_variable (const std::string &name, VariableType vt)
- Variable fresh\_bitvector\_variable () noexcept
- Variable fresh\_bitvector\_variable (const std::string &name)
- Variable fresh\_boolean\_variable () noexcept
- Variable fresh\_boolean\_variable (const std::string &name)
- Variable fresh\_real\_variable () noexcept
- Variable fresh\_real\_variable (const std::string &name)
- Variable fresh\_integer\_variable () noexcept
- Variable fresh\_integer\_variable (const std::string &name)
- Variable fresh\_uninterpreted\_variable () noexcept
- Variable fresh\_uninterpreted\_variable (const std::string &name)
- template<typename Enum >
   constexpr Enum invalid\_enum\_value ()

Returns an enum value that is (most probably) not a valid enum value.

 template<typename Enum > constexpr auto underlying\_enum\_value (Enum e)

Casts an enum value to a value of the underlying number type.

int init ()

The routine for initializing the carl library.

• int initialize ()

Method to ensure that upon inclusion, init() is called exactly once.

```
• template<typename T , typename T2 >
  bool fits_within (const T2 &t)
• template<typename T >
  T rationalize (double n)
• template<typename T >
  T rationalize (float n)
• template<typename T >
  T rationalize (int n)
• template<typename T >
  T rationalize (sint n)
• template<typename T >
  T rationalize (uint n)
• template<typename From , typename To , carl::DisableIf< std::is_same< From, To >> = dummy>
  To convert (const From &)

    template<typename Number >

  int to_int (const Number &n)
template<typename T >
  T parse (const std::string &n)

    template<typename T >

  bool try_parse (const std::string &n, T &res)
template<typename T >
  bool is_zero (const T &t)
• template<typename T >
  bool is_one (const T &t)
• template<typename T , EnableIf< has_is_positive< T >> >
  bool is_positive (const T &t)
• template<typename T , EnableIf< has_is_negative< T >> >
  bool is_negative (const T &t)
• template<typename T , Disablelf< is_interval_type< T >> = dummy>
  T pow (const T &basis, std::size_t exp)
      Implements a fast exponentiation on an arbitrary type T.
• template<typename T >
  void pow_assign (T &t, std::size_t exp)
      Implements a fast exponentiation on an arbitrary type T.
• bool is_zero (double n)
      Informational functions.
• bool is_positive (double n)

    bool is_negative (double n)

    bool isNaN (double d)

• bool isInf (double d)
• bool is_number (double d)

    bool is_integer (double d)

    bool is_integer (sint)

    std::size_t bitsize (unsigned)

• double to_double (sint n)
      Conversion functions.

    double to_double (double n)

• template<typename Integer >
  Integer to_int (double n)

    template<> sint to_int< sint > (double n)

    template<> uint to_int< uint > (double n)

    template<> double rationalize (double n)

• template<typename T >
  std::enable_if< std::is_arithmetic< typename remove_all< T >::type >::value, std::string >::type toString
  (const T &n, bool)
```

double floor (double n)

Basic Operators.

- double ceil (double n)
- double abs (double n)
- uint mod (uint n, uint m)
- sint mod (sint n, sint m)
- sint remainder (sint n, sint m)
- sint div (sint n, sint m)
- sint quotient (sint n, sint m)
- void divide (sint dividend, sint divisor, sint &quo, sint &rem)
- double sin (double in)
- double cos (double in)
- double acos (double in)
- double sqrt (double in)
- std::pair< double, double > sqrt\_safe (double in)
- double pow (double in, uint exp)
- double log (double in)
- double log10 (double in)
- template<typename Number>

Number highestPower (const Number &n)

Returns the highest power of two below n.

bool is\_zero (const mpz\_class &n)

Informational functions.

- bool is\_zero (const mpq\_class &n)
- bool is\_one (const mpz\_class &n)
- bool is\_one (const mpq\_class &n)
- bool is\_positive (const mpz\_class &n)
- bool is\_positive (const mpq\_class &n)
- bool is\_negative (const mpz\_class &n)
- bool is\_negative (const mpq\_class &n)
- mpz\_class get\_num (const mpq\_class &n)
- mpz\_class get\_num (const mpz\_class &n)
- mpz\_class get\_denom (const mpq\_class &n)
- mpz\_class get\_denom (const mpz\_class &n)
- bool is\_integer (const mpq\_class &n)
- bool is\_integer (const mpz\_class &)
- std::size\_t bitsize (const mpz\_class &n)

Get the bit size of the representation of a integer.

std::size\_t bitsize (const mpq\_class &n)

Get the bit size of the representation of a fraction.

• double to\_double (const mpq\_class &n)

Conversion functions.

- double to\_double (const mpz\_class &n)
- ullet template<typename Integer >

Integer to\_int (const mpz\_class &n)

- template<> sint to\_int< sint > (const mpz\_class &n)
- template<> uint to\_int< uint > (const mpz\_class &n)
- template<typename Integer >

Integer to\_int (const mpq\_class &n)

template<> mpz\_class to\_int< mpz\_class > (const mpq\_class &n)

Convert a fraction to an integer.

• template<typename To , typename From >

To from\_int (const From &n)

template<> mpz\_class from\_int (const uint &n)

```
    template<> mpz_class from_int (const sint &n)

    template<> sint to_int< sint > (const mpq_class &n)

      Convert a fraction to an unsigned.

    template<> uint to_int< uint > (const mpq_class &n)

    template<typename T >

  T rationalize (const PreventConversion < mpq_class > &)

    template<> mpq_class rationalize< mpq_class > (float n)

    template<> mpq_class rationalize< mpq_class > (double n)

    template<> mpg_class rationalize< mpg_class > (int n)

    template<> mpq_class rationalize< mpq_class > (uint n)

    template<> mpq_class rationalize< mpq_class > (sint n)

    template<> mpq_class rationalize< mpq_class > (const PreventConversion< mpq_class > &n)

    template<> mpz_class parse< mpz_class > (const std::string &n)

• template<> bool try_parse< mpz_class > (const std::string &n, mpz_class &res)
• template<> mpg_class parse< mpg_class > (const std::string &n)

    template<> bool try_parse< mpq_class > (const std::string &n, mpq_class &res)

    mpz_class abs (const mpz_class &n)

     Basic Operators.
• mpq_class abs (const mpq_class &n)

    mpz_class round (const mpg_class &n)

    mpz_class round (const mpz_class &n)

    mpz_class floor (const mpq_class &n)

    mpz_class floor (const mpz_class &n)

    mpz_class ceil (const mpq_class &n)

    mpz_class ceil (const mpz_class &n)

    mpz_class gcd (const mpz_class &a, const mpz_class &b)

    mpz_class lcm (const mpz_class &a, const mpz_class &b)

    mpq_class gcd (const mpq_class &a, const mpq_class &b)

    mpz_class & gcd_assign (mpz_class &a, const mpz_class &b)

      Calculate the greatest common divisor of two integers.

    mpq_class & gcd_assign (mpq_class &a, const mpq_class &b)

      Calculate the greatest common divisor of two integers.

    mpq_class lcm (const mpq_class &a, const mpq_class &b)

    mpq_class log (const mpq_class &n)

    mpq_class log10 (const mpq_class &n)

    mpq_class sin (const mpq_class &n)

• mpq_class cos (const mpq_class &n)

    template<> mpz_class pow (const mpz_class &basis, std::size_t exp)

    template<> mpq_class pow (const mpq_class &basis, std::size_t exp)

    bool sqrt_exact (const mpq_class &a, mpq_class &b)

     Calculate the square root of a fraction if possible.

    mpq_class sqrt (const mpq_class &a)

    std::pair< mpq_class, mpq_class > sqrt_safe (const mpq_class &a)
```

std::pair< mpq\_class, mpq\_class > root\_safe (const mpq\_class &a, uint n)

Calculate the nth root of a fraction.

std::pair< mpq\_class, mpq\_class > sqrt\_fast (const mpq\_class &a)

Compute square root in a fast but less precise way.

- mpz\_class mod (const mpz\_class &n, const mpz\_class &m)
- mpz\_class remainder (const mpz\_class &n, const mpz\_class &m)
- mpz\_class quotient (const mpz\_class &n, const mpz\_class &d)
- mpz\_class operator/ (const mpz\_class &n, const mpz\_class &d)
- mpq\_class quotient (const mpq\_class &n, const mpq\_class &d)
- mpq\_class operator/ (const mpq\_class &n, const mpq\_class &d)

```
    void divide (const mpz_class &dividend, const mpz_class &divisor, mpz_class &quotient, mpz_class

  &remainder)

    mpq_class div (const mpq_class &a, const mpq_class &b)

     Divide two fractions.

    mpz_class div (const mpz_class &a, const mpz_class &b)

     Divide two integers.

    mpz_class & div_assign (mpz_class &a, const mpz_class &b)

     Divide two integers.

    mpq_class & div_assign (mpq_class &a, const mpq_class &b)

     Divide two integers.

    mpq_class reciprocal (const mpq_class &a)

    mpq_class operator* (const mpq_class &lhs, const mpq_class &rhs)

    std::string toString (const mpq_class &_number, bool _infix=true)

    std::string toString (const mpz_class &_number, bool _infix=true)

    Str2Double_Error str2double (double &d, char const *s)

template<typename Number >
  bool AlmostEqual2sComplement (const Number &A, const Number &B, unsigned=128)
• template<> bool AlmostEqual2sComplement< double > (const double &A, const double &B, unsigned
  maxUlps)

    template<typename FloatType >

  bool is_integer (const FLOAT_T< FloatType > &in)

    template<typename FloatType >

  FLOAT_T< FloatType > div (const FLOAT_T< FloatType > &_lhs, const FLOAT_T< FloatType > &_rhs)
     Implements the division which assumes that there is no remainder.

    template<typename FloatType >

  FLOAT_T < FloatType > quotient (const FLOAT_T < FloatType > &_lhs, const FLOAT_T < FloatType > &_rhs)
     Implements the division with remainder.
- template<typename Integer , typename FloatType >
  Integer to_int (const FLOAT_T< FloatType > &_float)
     Casts the FLOAT_T to an arbitrary integer type which has a constructor for a native int.

    template<typename FloatType >

  double to_double (const FLOAT_T< FloatType > &_float)

    template<typename FloatType >

  FLOAT_T< FloatType > abs (const FLOAT_T< FloatType > &_in)
     Method which returns the absolute value of the passed number.

    template<typename FloatType >

  FLOAT_T< FloatType > log (const FLOAT_T< FloatType > &_in)
     Method which returns the logarithm of the passed number.

    template<typename FloatType >

  FLOAT_T< FloatType > sqrt (const FLOAT_T< FloatType > &_in)
     Method which returns the square root of the passed number.

    template<typename FloatType >

  std::pair< FLOAT_T< FloatType >, FLOAT_T< FloatType > sqrt_safe (const FLOAT_T< FloatType > &_in)

    template<typename FloatType >

  FLOAT_T< FloatType > pow (const FLOAT_T< FloatType > &_in, size_t _exp)

    template<typename FloatType >

  FLOAT_T< FloatType > sin (const FLOAT_T< FloatType > &_in)

    template<typename FloatType >
```

FLOAT\_T< FloatType > cos (const FLOAT\_T< FloatType > &\_in)

FLOAT\_T< FloatType > asin (const FLOAT\_T< FloatType > &\_in)

FLOAT\_T< FloatType > acos (const FLOAT\_T< FloatType > &\_in)

template<typename FloatType >

template<typename FloatType >

```
    template<typename FloatType >

  FLOAT_T< FloatType > atan (const FLOAT_T< FloatType > &_in)

    template<typename FloatType >

  FLOAT_T< FloatType > floor (const FLOAT_T< FloatType > &_in)
     Method which returns the next smaller integer of this number or the number itself, if it is already an integer.

    template<typename FloatType >

  FLOAT_T< FloatType > ceil (const FLOAT_T< FloatType > &_in)
     Method which returns the next larger integer of the passed number or the number itself, if it is already an integer.

    template<> FLOAT_T< double > rationalize< FLOAT_T< double >> (double n)

    template<> FLOAT_T< float > rationalize< FLOAT_T< float >> (float n)

    template<>> FLOAT_T< mpq_class > rationalize< FLOAT_T< mpq_class >> (double n)

    mpz_class get_denom (const FLOAT_T< mpq_class > &_in)

      Implicitly converts the number to a rational and returns the denominator.

    mpz_class get_num (const FLOAT_T< mpq_class > &_in)

      Implicitly converts the number to a rational and returns the nominator.

    template<typename FloatType >

  bool is_zero (const FLOAT_T< FloatType > &_in)

    template<typename FloatType >

  bool isInfinity (const FLOAT_T< FloatType > &_in)

    template<typename FloatType >

  bool isNan (const FLOAT_T< FloatType > &_in)

    template<> bool AlmostEqual2sComplement< FLOAT_T< double >> (const FLOAT_T< double > &A,

  const FLOAT_T< double > &B, unsigned maxUlps)

    template<typename IntegerT >

  bool is_zero (const GFNumber < IntegerT > &_in)

    template<typename IntegerT >

  bool is_one (const GFNumber< IntegerT > &_in)

    template<typename IntegerT >

  GFNumber < IntegerT > quotient (const GFNumber < IntegerT > &lhs, const GFNumber < IntegerT > &rhs)

    template<typename IntegerT >

  GFNumber< IntegerT > abs (const GFNumber< IntegerT > &n)

    template<typename IntegerT >

  bool is_integer (const GFNumber< IntegerT > &)

    template<typename IntegerType >

  std::string toString (const GFNumber< IntegerType > &_number, bool)
      Creates the string representation to the given galois field number.

    template < class... Ts >

  overloaded (Ts...) -> overloaded< Ts... >

    has_method_struct (normalize) has_method_struct(is_negative) has_method_struct(is_positive) has_function←

  _overload(is_one) has_function_overload(is_zero) template< template< typename... > class Template

    void hash_combine (std::size_t &seed, std::size_t value)

     Add a value to the given hash seed.
template<typename T >
  void hash_add (std::size_t &seed, const T &value)
     Add hash of the given value to the hash seed.

    template<> void hash_add (std::size_t &seed, const std::size_t &value)

     Add hash of the given value to the hash seed.
• template<typename T1 , typename T2 >
  void hash_add (std::size_t &seed, const std::pair< T1, T2 > &p)
     Add hash of both elements of a std::pair to the seed.

    template<typename T >

  void hash_add (std::size_t &seed, const std::vector< T > &v)
```

Add hash of all elements of a std::vector to the seed.

```
• template<typename First , typename... Tail>
   void hash_add (std::size_t &seed, const First &value, Tail &&... tail)
          Variadic version of hash_add to add an arbitrary number of values to the seed.
template<typename... Args>
   std::size_t hash_all (Args &&... args)
         Hashes an arbitrary number of values.

    template<typename IntegerT >

   bool operator== (const GFNumber < IntegerT > &lhs, const GFNumber < IntegerT > &rhs)

    template<typename IntegerT >

   bool operator== (const GFNumber < IntegerT > &lhs, const IntegerT &rhs)

    template<typename IntegerT >

   bool operator== (const IntegerT &lhs, const GFNumber < IntegerT > &rhs)

    template<typename IntegerT >

   bool operator== (const GFNumber < IntegerT > &lhs, int rhs)

    template<typename IntegerT >

   bool operator== (int lhs, const GFNumber < IntegerT > &rhs)

    template<typename IntegerT >

   bool operator!= (const GFNumber < IntegerT > &Ihs, const GFNumber < IntegerT > &rhs)

    template<typename IntegerT >

   bool operator!= (const GFNumber < IntegerT > &lhs, const IntegerT &rhs)

    template<typename IntegerT >

   bool operator!= (const IntegerT &lhs, const GFNumber < IntegerT > &rhs)

    template<typename IntegerT >

   bool operator!= (const GFNumber < IntegerT > &lhs, int rhs)

    template<typename IntegerT >

   bool operator!= (int lhs, const GFNumber < IntegerT > &rhs)

    template < typename IntegerT >

   {\sf GFNumber} < {\sf IntegerT} > {\sf operator+} \; ({\sf const} \; {\sf GFNumber} < \; {\sf IntegerT} > \& {\sf lhs}, \; {\sf const} \; {\sf GFNumber} < \; {\sf IntegerT} > \& {\sf Inte
   &rhs)

    template<typename IntegerT >

   GFNumber< IntegerT > operator+ (const GFNumber< IntegerT > &lhs, const IntegerT &rhs)

    template<typename IntegerT >

   GFNumber < IntegerT > operator+ (const IntegerT &lhs, const GFNumber < IntegerT > &rhs)

    template<typename IntegerT >

   GFNumber < IntegerT > operator- (const GFNumber < IntegerT > &lhs, const GFNumber < IntegerT > &rhs)

    template<typename IntegerT >

    GFNumber< IntegerT > operator- (const GFNumber< IntegerT > &lhs, const IntegerT &rhs)
• template<typename IntegerT >
   GFNumber < IntegerT > operator- (const IntegerT & lhs, const GFNumber < IntegerT > &rhs)

    template<typename IntegerT >

   GFNumber< IntegerT > operator* (const GFNumber< IntegerT > &lhs, const GFNumber< IntegerT >
   &rhs)

    template<typename IntegerT >

   GFNumber< IntegerT > operator* (const GFNumber< IntegerT > &lhs, const IntegerT &rhs)

    template<typename IntegerT >

   GFNumber < IntegerT > operator* (const IntegerT &lhs, const GFNumber < IntegerT > &rhs)

    template<typename IntegerT >

   GFNumber < IntegerT > operator/ (const GFNumber < IntegerT > &lhs, const GFNumber < IntegerT > &rhs)

    template<typename Rational >

   double roundDown (const Rational &o, bool overapproximate=false)
          Returns a down-rounded representation of the given numeric.

    template<typename Rational >

   double roundUp (const Rational &o, bool overapproximate=false)
          Returns a up-rounded representation of the given numeric.

    template<> mpq_class convert< double, mpq_class > (const double &n)
```

template<> double convert< mpq\_class, double > (const mpq\_class &n)

```
    template<>> FLOAT_T< mpq_class > convert< double, FLOAT_T< mpq_class >> (const double &n)

    template<> double convert< FLOAT_T< mpq_class >, double > (const FLOAT_T< mpq_class > &n)

    template<>> FLOAT_T< double > convert< mpq_class, FLOAT_T< double > > (const mpq_class &n)

    template<> mpq_class convert< FLOAT_T< double >, mpq_class > (const FLOAT_T< double > &n)

    template<> mpq_class convert< FLOAT_T< mpq_class >, mpq_class > (const FLOAT_T< mpq_class >

  &n)

    template<> FLOAT_T< mpq_class > convert< mpq_class, FLOAT_T< mpq_class >> (const mpq_class

    template<> double convert< FLOAT_T< double >, double > (const FLOAT_T< double > &n)

    template<>> FLOAT_T< double > convert< double, FLOAT_T< double >> (const double &n)

    Monomial::Arg gcd (const Monomial::Arg &lhs, const Monomial::Arg &rhs)

      Calculates the least common multiple of two monomial pointers.

    std::size_t hash_value (const carl::Monomial &monomial)

    std::ostream & operator<< (std::ostream &os, const MonomialPool &mp)</li>

    template<typename... T>

  Monomial::Arg createMonomial (T &&... t)

    Monomial::Arg pow (Variable v, std::size_t exp)

    bool operator== (const std::pair< Variable, std::size_t > &p, Variable v)

      Compare a pair of variable and exponent with a variable.

    std::ostream & operator<< (std::ostream &os, const Monomial &rhs)</li>

      Streaming operator for Monomial.

    std::ostream & operator<< (std::ostream &os, const Monomial::Arg &rhs)</li>

      Streaming operator for std::shared_ptr< Monomial>.

    void variables (const Monomial &m, carlVariables &vars)

     Add the variables of the given monomial to the variables.

    std::ostream & operator<< (std::ostream &os, CompareResult cr)</li>

    void swap (Variable &lhs, Variable &rhs)

    bool operator== (const carlVariables &lhs, const carlVariables &rhs)

    std::ostream & operator<< (std::ostream &os, const carlVariables &vars)</li>

• template<typename T >
  carlVariables variables (const T &t)
     Return the variables as collected by the methods above.
• template<typename T >
  carlVariables boolean_variables (const T &t)
template<typename T >
  carlVariables integer_variables (const T &t)

    template<typename T >

  carlVariables real_variables (const T &t)
template<typename T >
  carlVariables arithmetic_variables (const T &t)

    template<typename T >

  carlVariables bitvector_variables (const T &t)
template<typename T >
  carlVariables uninterpreted_variables (const T &t)

    template<typename T >

  std::ostream & operator<< (std::ostream &os, const std::forward_list< T > &I)
     Output a std::forward_list with arbitrary content.

    template<typename T >

  std::ostream & operator<< (std::ostream &os, const std::initializer_list< T > &I)
      Output a std::initializer_list with arbitrary content.

    template<typename T >

  std::ostream & operator<< (std::ostream &os, const std::list< T > &I)
     Output a std::list with arbitrary content.
```

```
    template<typename Key , typename Value , typename Comparator >

  std::ostream & operator << (std::ostream &os, const std::map < Key, Value, Comparator > &m)
      Output a std::map with arbitrary content.

    template<typename Key , typename Value , typename Comparator >

  std::ostream & operator << (std::ostream &os, const std::multimap < Key, Value, Comparator > &m)
      Output a std::multimap with arbitrary content.

    template<tvpename T >

  std::ostream & operator<< (std::ostream &os, const std::optional< T > &o)
      Output a std::optional with arbitrary content.
• template<typename U , typename V >
  std::ostream & operator<< (std::ostream &os, const std::pair< U, V > &p)
      Output a std::pair with arbitrary content.
• template<typename T , typename C >
  std::ostream & operator<< (std::ostream &os, const std::set< T, C > &s)
      Output a std::set with arbitrary content.
• template<typename... T>
  std::ostream & operator<< (std::ostream &os, const std::tuple< T... > &t)
      Output a std::tuple with arbitrary content.
• template<typename Key, typename Value, typename H, typename E, typename A>
  std::ostream & operator << (std::ostream &os, const std::unordered_map < Key, Value, H, E, A > &m)
      Output a std::unordered_map with arbitrary content.

    template < typename T, typename H, typename K, typename A >

  std::ostream & operator << (std::ostream &os, const std::unordered_set < T, H, K, A > &s)
      Output a std::unordered_set with arbitrary content.

    template<typename T, typename... Tail>

  std::ostream & operator<< (std::ostream &os, const std::variant< T, Tail... > &v)
      Output a std::variant with arbitrary content.
• template<typename T >
  std::ostream & operator << (std::ostream &os, const std::vector < T > &v)
      Output a std::vector with arbitrary content.

    template<typename T >

  std::ostream & operator<< (std::ostream &os, const std::deque< T > &v)
      Output a std::deque with arbitrary content.

    template<tvpename T >

  auto stream_joined (const std::string &glue, const T &v)
      Allows to easily output some container with all elements separated by some string.
• template<typename T , typename F >
  auto stream_joined (const std::string &glue, const T &v, F &&f)
      Allows to easily output some container with all elements separated by some string.
• template<typename T , typename C >
  std::ostream & operator << (std::ostream &os, const boost::container::flat_set < T, C > &s)
      Output a boost::container::flat_set with arbitrary content.

    std::ostream & operator<< (std::ostream &os, CMakeOptionPrinter cmop)</li>

    constexpr CMakeOptionPrinter CMakeOptions (bool advanced=false) noexcept

• BitVector operator (const BitVector &lhs, const BitVector &rhs)

    bool operator== (const BitVector &lhs, const BitVector &rhs)

    bool operator== (const BitVector::forward_iterator &fi1, const BitVector::forward_iterator &fi2)

    std::ostream & operator<< (std::ostream &os, const BitVector &bv)</li>

    std::string demangle (const char *name)

    void printStacktrace ()

      Uses GDB to print a stack trace.

    std::string callingFunction ()

    static void handle_signal (int signal)
```

## Actual signal handler.

static bool install\_signal\_handler () noexcept

Installs the signal handler.

- template < typename T > std::string typeString ()
- bool operator== (const BVConstraint &lhs, const BVConstraint &rhs)
- bool operator< (const BVConstraint &lhs, const BVConstraint &rhs)</li>
- std::ostream & operator<< (std::ostream &os, const BVConstraint &c)</li>
- std::string toString (BVCompareRelation \_r)
- std::ostream & operator<< (std::ostream &\_os, const BVCompareRelation &\_r)
- std::size\_t told (const BVCompareRelation \_relation)
- BVCompareRelation inverse (BVCompareRelation \_c)
- bool relationIsStrict (BVCompareRelation \_r)
- bool relationIsSigned (BVCompareRelation \_r)
- bool operator== (const BVTerm &lhs, const BVTerm &rhs)
- bool operator< (const BVTerm &lhs, const BVTerm &rhs)</li>
- std::ostream & operator<< (std::ostream &os, const BVTerm &term)</li>
- template<typename T, typename Variant >
   bool variant\_is\_type (const Variant &variant) noexcept

Checks whether a variant contains a value of a fiven type.

- template<typename Target , typename... Args>
   Target variant\_extend (const boost::variant< Args... > &variant)
- template < typename... T>
   std::size\_t variant\_hash (const boost::variant < T... > &value)
- auto typeld (BVTermType type)
- std::ostream & operator<< (std::ostream &os, BVTermType type)</li>
- bool typeIsUnary (BVTermType type)
- bool typeIsBinary (BVTermType type)
- bool operator== (const BVValue &lhs, const BVValue &rhs)
- bool operator< (const BVValue &lhs, const BVValue &rhs)</li>
- BVValue operator ~ (const BVValue &val)
- BVValue operator+ (const BVValue &lhs, const BVValue &rhs)
- BVValue operator\* (const BVValue &lhs, const BVValue &rhs)
- BVValue operator- (const BVValue &val)
- BVValue operator- (const BVValue &lhs, const BVValue &rhs)
- BVValue operator% (const BVValue &lhs, const BVValue &rhs)
- BVValue operator/ (const BVValue &lhs, const BVValue &rhs)
- BVValue operator& (const BVValue &lhs, const BVValue &rhs)
- BVValue operator (const BVValue &lhs, const BVValue &rhs)
- BVValue operator<sup>^</sup> (const BVValue &lhs, const BVValue &rhs)
- BVValue operator<< (const BVValue &lhs, const BVValue &rhs)</li>
- BVValue operator>> (const BVValue &lhs, const BVValue &rhs)
- std::ostream & operator<< (std::ostream &os, const BVValue &val)</li>
- bool operator== (const BVVariable &lhs, const BVVariable &rhs)
- bool operator== (const BVVariable &lhs, const Variable &rhs)
- bool operator== (const Variable &lhs, const BVVariable &rhs)
- bool operator< (const BVVariable &lhs, const BVVariable &rhs)
- bool operator< (const BVVariable &lhs, const Variable &rhs)</li>
- bool operator< (const Variable &lhs, const BVVariable &rhs)</li>
- bool operator== (const BVTermContent &lhs, const BVTermContent &rhs)
- bool operator< (const BVTermContent &lhs, const BVTermContent &rhs)</li>
- std::ostream & operator<< (std::ostream &os, const BVTermContent &term)</li>

The output operator of a term.

bool operator< (const SortContent &lhs, const SortContent &rhs)</li>

template<typename... Args>
 Sort getSort (Args &&... args)

Gets the sort specified by the arguments.

- std::ostream & operator<< (std::ostream &\_os, const Sort &\_sort)</li>
- bool operator== (Sort lhs, Sort rhs)
- bool operator!= (Sort lhs, Sort rhs)
- bool operator< (Sort lhs, Sort rhs)</li>

Checks whether one sort is smaller than another.

- void collectUFVars (std::set< UVariable > &uvars, UFInstance ufi)
- bool operator== (const UEquality &lhs, const UEquality &rhs)
- bool operator!= (const UEquality &lhs, const UEquality &rhs)
- bool operator< (const UEquality &lhs, const UEquality &rhs)</li>
- std::ostream & operator<< (std::ostream &os, const UEquality &ueq)</li>

Prints the given uninterpreted equality on the given output stream.

std::ostream & operator<< (std::ostream &os, const UFInstance &ufun)</li>

Prints the given uninterpreted function instance on the given output stream.

- bool operator== (const UFInstance &lhs, const UFInstance &rhs)
- bool operator< (const UFInstance &lhs, const UFInstance &rhs)</li>
- UFInstance newUFInstance (const UninterpretedFunction &uf, std::vector< UTerm > &&args)

Gets the uninterpreted function instance with the given name, domain, arguments and codomain.

UFInstance newUFInstance (const UninterpretedFunction &uf, const std::vector < UTerm > &args)

Gets the uninterpreted function instance with the given name, domain, arguments and codomain.

std::ostream & operator<< (std::ostream &os, UVariable uvar)</li>

Prints the given uninterpreted variable on the given output stream.

- bool operator== (UVariable lhs, UVariable rhs)
- bool operator< (UVariable lhs, UVariable rhs)</li>
- bool operator== (const UninterpretedFunction &lhs, const UninterpretedFunction &rhs)

Check whether two uninterpreted functions are equal.

bool operator< (const UninterpretedFunction &lhs, const UninterpretedFunction &rhs)</li>

Check whether one uninterpreted function is smaller than another.

• std::ostream & operator<< (std::ostream &os, const UninterpretedFunction &ufun)

Prints the given uninterpreted function on the given output stream.

- bool operator== (const UTerm &lhs, const UTerm &rhs)
- bool operator!= (const UTerm &lhs, const UTerm &rhs)
- bool operator< (const UTerm &lhs, const UTerm &rhs)
- std::ostream & operator<< (std::ostream &os, const UTerm &ut)</li>

Prints the given uninterpreted term on the given output stream.

- bool operator== (const UFContent &lhs, const UFContent &rhs)
- bool operator< (const UFContent &lhs, const UFContent &rhs)
- UninterpretedFunction newUninterpretedFunction (std::string name, std::vector< Sort > domain, Sort codomain)

Gets the uninterpreted function with the given name, domain, arguments and codomain.

std::ostream & operator<< (std::ostream &os, const UFModel &ufm)</li>

Prints the given uninterpreted function model on the given output stream.

bool operator== (const UFModel &lhs, const UFModel &rhs)

Compares two UFModel objects for equality.

bool operator< (const UFModel &lhs, const UFModel &rhs)</li>

Checks whether one UFModel is smaller than another.

SortValue newSortValue (const Sort &sort)

Creates a new value for the given sort.

SortValue defaultSortValue (const Sort &sort)

Returns the default value for the given sort.

template<typename Numeric >

```
    template<typename T >

   std::string binary (const T &a, const bool &spacing=true)
         Return the binary representation given value as bit string.

    std::string basename (const std::string &filename)

          Return the basename of a given filename.
• template<typename C , typename O , typename P >
   bool is_one (const MultivariatePolynomial < C, O, P > &p)
• template<typename C , typename O , typename P >
   bool is_zero (const MultivariatePolynomial < C, O, P > &p)
• template<typename C , typename O , typename P >
   std::pair< MultivariatePolynomial< C, O, P >, MultivariatePolynomial< C, O, P >> lazyDiv (const
   MultivariatePolynomial < C, O, P > &_polyA, const MultivariatePolynomial < C, O, P > &_polyB)

    template<typename C , typename O , typename P >

   std::ostream & operator << (std::ostream &os, const MultivariatePolynomial < C, O, P > &rhs)
          Streaming operator for multivariate polynomials.
• template<typename Coeff , typename Ordering , typename Policies >
   void variables (const MultivariatePolynomial < Coeff, Ordering, Policies > &p, carlVariables &vars)
         Add the variables of the given polynomial to the variables.

    std::ostream & operator<< (std::ostream &os, const Timer &t)</li>

         Streaming operator for a Timer.
template<typename Coeff >
   bool is_zero (const Term < Coeff > &term)
         Checks whether a term is zero.
template<typename Coeff >
   void variables (const Term < Coeff > &t, carlVariables &vars)
         Add the variables of the given term to the variables.

    template<typename Coeff >

   bool is_one (const Term < Coeff > &term)
          Checks whether a term is one.

    template<typename Coeff >

   Term < Coeff > operator- (const Term < Coeff > &rhs)
• template<typename C , typename O , typename P >
   \label{eq:multivariatePolynomial} \mbox{MultivariatePolynomial} < C > \&, \mbox{const MultivariatePolynomial} 
   C, O, P > \&)
• template<typename C , typename O , typename P >
   MultivariatePolynomial < C, O, P > operator+ (const MultivariatePolynomial < C, O, P > &, const
   UnivariatePolynomial < C > &)

    template<typename C , typename O , typename P >

   MultivariatePolynomial < C, O, P > operator+ (const UnivariatePolynomial < MultivariatePolynomial < C >>
   &, const MultivariatePolynomial < C, O, P > &)
• template<typename C , typename O , typename P >
   \label{eq:multivariatePolynomial} \textit{MultivariatePolynomial} < C, \ O, \ P \ > \ \&, \ const
   UnivariatePolynomial < MultivariatePolynomial < C >> &)
• template<typename C , typename O , typename P >
   const MultivariatePolynomial < C, O, P > operator* (const UnivariatePolynomial < C > &, const
   MultivariatePolynomial < C, O, P > \&)

    template<typename C , typename O , typename P >

   const MultivariatePolynomial < C, O, P > operator* (const MultivariatePolynomial < C, O, P > &lhs, const
   UnivariatePolynomial < C > &rhs)

    template<typename C , typename O , typename P >

   MultivariatePolynomial < C, O, P > operator/ (const MultivariatePolynomial < C, O, P > &lhs, unsigned long
   rhs)
```

Interval < Numeric > evaluate (const Monomial &m, const std::map < Variable, Interval < Numeric >> &map)

```
    template < typename Coeff , typename Numeric , EnableIf < std::is_same < Numeric, Coeff >> = dummy >

  Interval < Numeric > evaluate (const Term < Coeff > &t, const std::map < Variable, Interval < Numeric >>
  &map)

    template<typename Coeff , typename Policy , typename Ordering , typename Numeric >

  Interval < Numeric > evaluate (const MultivariatePolynomial < Coeff, Policy, Ordering > &p, const std::map <
  Variable, Interval < Numeric >> &map)

    template<typename Numeric, typename Coeff, EnableIf< std::is_same< Numeric, Coeff>> = dummy>

  Interval < Numeric > evaluate (const UnivariatePolynomial < Coeff > &p, const std::map < Variable, Interval <
  Numeric >> &map)

    template<typename Coeff >

  bool operator== (const Term < Coeff > &lhs, const Monomial::Arg &rhs)

    template<typename Coeff >

  const Term < Coeff > operator/ (const Term < Coeff > &lhs, uint rhs)

    template<typename Coeff >

  std::ostream & operator << (std::ostream &os, const Term < Coeff > &rhs)

    template<typename Coeff >

  std::ostream & operator<< (std::ostream &os, const std::shared_ptr< const Term< Coeff >> &rhs)

    template<typename Coefficient >

  bool is_zero (const UnivariatePolynomial < Coefficient > &p)
      Checks if the polynomial is equal to zero.

    template<typename Coefficient >

  bool is_one (const UnivariatePolynomial < Coefficient > &p)
      Checks if the polynomial is equal to one.
• template<typename Coeff >
  void variables (const UnivariatePolynomial < Coeff > &p, carlVariables &vars)
      Add the variables of the given polynomial to the variables.
 \bullet \ \ \text{template}{<} \text{typename Number} >
  std::ostream & operator << (std::ostream &os, const LowerBound < Number > &lb)

    template<typename Number >

  std::ostream & operator<< (std::ostream &os, const UpperBound< Number > &lb)

    template<typename Number >

  bool is_integer (const Interval< Number > &n)

    template<typename Number >

  bool is_zero (const Interval < Number > &i)
      Check if this interval is a point-interval containing 0.
template<typename Number >
  bool is_one (const Interval < Number > &i)
      Check if this interval is a point-interval containing 1.

    template<typename Number >

  Interval < Number > div (const \ Interval < Number > \&\_lhs, \ const \ Interval < Number > \&\_rhs)
      Implements the division which assumes that there is no remainder.

    template<typename Number >

  Interval < Number > quotient (const Interval < Number > &_Ihs, const Interval < Number > &_rhs)
      Implements the division with remainder.

    template<typename Integer , typename Number >

  Integer to_int (const Interval < Number > &_floatInterval)
      Casts the Interval to an arbitrary integer type which has a constructor for a native int.

    template<typename Number >

  Interval < Number > abs (const Interval < Number > &_in)
      Method which returns the absolute value of the passed number.
template<typename Number >
  Interval < Number > floor (const Interval < Number > &_in)
      Method which returns the next smaller integer of this number or the number itself, if it is already an integer.
 \bullet \ \ \text{template}{<} \text{typename Number} >
  Interval < Number > ceil (const Interval < Number > &_in)
```

Method which returns the next larger integer of the passed number or the number itself, if it is already an integer.

- std::ostream & operator<< (std::ostream &os, const Sign &sign)</li>
- template<typename Number >

Sign sgn (const Number &n)

Obtain the sign of the given number.

template<typename InputIterator >

std::size\_t sign\_variations (InputIterator begin, InputIterator end)

Counts the number of sign variations in the given object range.

- template<typename InputIterator , typename Function >

std::size\_t sign\_variations (InputIterator begin, InputIterator end, const Function &f)

Counts the number of sign variations in the given object range.

- std::ostream & operator<< (std::ostream &os, BoundType b)</li>
- static BoundType get\_weakest\_bound\_type (BoundType type1, BoundType type2)
- static BoundType get\_strictest\_bound\_type (BoundType type1, BoundType type2)
- static BoundType get\_other\_bound\_type (BoundType type)
- template<typename Number >

Number center (const Interval < Number > &i)

Returns the center point of the interval.

template<typename Number >

Number sample (const Interval < Number > &i, bool includingBounds=true)

Searches for some point in this interval, preferably near the midpoint and with a small representation.

template<typename Number >

Number sample\_stern\_brocot (const Interval < Number > &i, bool includingBounds=true)

Searches for some point in this interval, preferably near the midpoint and with a small representation.

template<tvpename Number >

Number sample\_left (const Interval < Number > &i)

Searches for some point in this interval, preferably near the left endpoint and with a small representation.

 $\bullet \ \ \text{template}{<} \text{typename Number}{>}$ 

Number sample\_right (const Interval < Number > &i)

Searches for some point in this interval, preferably near the right endpoint and with a small representation.

template<typename Number >

Number sample\_zero (const Interval < Number > &i)

Searches for some point in this interval, preferably near zero and with a small representation.

• template<typename Number >

Number sample\_infty (const Interval < Number > &i)

Searches for some point in this interval, preferably far aways from zero and with a small representation.

template<typename Number >

bool operator< (const LowerBound< Number > &lhs, const LowerBound< Number > &rhs)

Operators for LowerBound and UpperBound.

template<typename Number >

bool operator <= (const LowerBound < Number > &lhs, const LowerBound < Number > &rhs)

 $\bullet \ \ \text{template}{<} \text{typename Number} >$ 

bool operator< (const UpperBound< Number > &lhs, const LowerBound< Number > &rhs)

template<typename Number >

bool operator <= (const LowerBound < Number > &lhs, const UpperBound < Number > &rhs)

• template<typename Number >

bool operator < (const UpperBound < Number > &lhs, const UpperBound < Number > &rhs)

• template<typename Number >

bool operator <= (const UpperBound < Number > &lhs, const UpperBound < Number > &rhs)

• template<typename Number >

bool bounds\_connect (const UpperBound < Number > &lhs, const LowerBound < Number > &rhs)

Check whether the two bounds connect, for example as for ...3),[3...

• template<typename Number>

bool operator== (const Interval < Number > &Ihs, const Interval < Number > &rhs)

Operator for the comparison of two intervals. template<> bool operator== (const Interval< double > &lhs, const Interval< double > &rhs) • template<typename Number > bool operator== (const Interval < Number > &lhs, const Number &rhs) template<typename Number > bool operator== (const Number &lhs, const Interval < Number > &rhs) template<typename Number > bool operator!= (const Interval < Number > &lhs, const Interval < Number > &rhs) Operator for the comparison of two intervals. template<typename Number > bool operator!= (const Interval < Number > &lhs, const Number &rhs) template<typename Number > bool operator!= (const Number &lhs, const Interval < Number > &rhs) template<typename Number > bool operator< (const Interval< Number > &lhs, const Interval< Number > &rhs) Operator for the comparison of two intervals. template<typename Number > bool operator (const Interval Number > &lhs, const Number &rhs) template<typename Number > bool operator< (const Number &lhs, const Interval< Number > &rhs) template<typename Number > bool operator> (const Interval< Number > &lhs, const Interval< Number > &rhs) Operator for the comparison of two intervals. template<typename Number > bool operator> (const Interval< Number > &lhs, const Number &rhs) template<typename Number > bool operator> (const Number &lhs, const Interval< Number > &rhs) template<typename Number > bool operator<= (const Interval< Number > &lhs, const Interval< Number > &rhs) Operator for the comparison of two intervals. template<typename Number > bool operator<= (const Interval< Number > &lhs, const Number &rhs) template<typename Number > bool operator<= (const Number &lhs, const Interval< Number > &rhs) template<typename Number > bool operator>= (const Interval < Number > &Ihs, const Interval < Number > &rhs) Operator for the comparison of two intervals. template<typename Number > bool operator>= (const Interval < Number > &lhs, const Number &rhs) template < typename Number > bool operator>= (const Number &lhs, const Interval< Number > &rhs) template < typename Number > Interval < Number > operator+ (const Interval < Number > &lhs, const Interval < Number > &rhs) Operator for the addition of two intervals. template<typename Number > Interval < Number > operator+ (const Interval < Number > &lhs, const Number &rhs) Operator for the addition of an interval and a number. template<typename Number > Interval < Number > operator+ (const Number &lhs, const Interval < Number > &rhs) Operator for the addition of an interval and a number. template<typename Number >

```
    template<typename Number >
        Interval < Number > & operator+= (Interval < Number > &Ihs, const Number &rhs)
```

Operator for the addition of an interval and a number with assignment.

Interval < Number > & operator+= (Interval < Number > &lhs, const Interval < Number > &rhs)

C > &rhs)

template<typename C >

Operator for the addition of an interval and a number with assignment. • template<typename Number > Interval < Number > operator- (const Interval < Number > &rhs) Unary minus. template<typename Number > Interval < Number > operator- (const Interval < Number > &lhs, const Interval < Number > &rhs) Operator for the subtraction of two intervals. • template<typename Number > Interval < Number > operator- (const Interval < Number > &lhs, const Number &rhs) Operator for the subtraction of an interval and a number. • template<typename Number > Interval < Number > operator- (const Number &lhs, const Interval < Number > &rhs) Operator for the subtraction of an interval and a number. template<typename Number > Interval < Number > & operator = (Interval < Number > &Ihs, const Interval < Number > &rhs) Operator for the subtraction of two intervals with assignment. template<typename Number > Interval < Number > & operator-= (Interval < Number > &lhs, const Number &rhs) Operator for the subtraction of an interval and a number with assignment. template<typename Number > Interval < Number > operator\* (const Interval < Number > &lhs, const Interval < Number > &rhs) Operator for the multiplication of two intervals. template<typename Number > Interval < Number > operator\* (const Interval < Number > &lhs, const Number &rhs) Operator for the multiplication of an interval and a number. template<typename Number > Interval < Number > operator\* (const Number & lhs, const Interval < Number > & rhs) Operator for the multiplication of an interval and a number. template<typename Number > Interval < Number > & operator\*= (Interval < Number > &lhs, const Interval < Number > &rhs) Operator for the multiplication of an interval and a number with assignment. template<typename Number > Interval < Number > & operator\*= (Interval < Number > &Ihs, const Number &rhs) Operator for the multiplication of an interval and a number with assignment. template<typename Number > Interval < Number > operator/ (const Interval < Number > &lhs, const Number &rhs) Operator for the division of an interval and a number. template<typename Number > Interval < Number > & operator/= (Interval < Number > &lhs, const Number &rhs) Operator for the division of an interval and a number with assignment. template<typename From , typename To , carl::DisableIf< std::is\_same< From , To >> = dummy> Interval < To > convert (const Interval < From > &i) template<typename C > UnivariatePolynomial < C > operator+ (const UnivariatePolynomial < C > &lhs, const UnivariatePolynomial < C > & rhs) template<typename C > UnivariatePolynomial < C > operator+ (const UnivariatePolynomial < C > &lhs, const C &rhs) template<typename C > UnivariatePolynomial < C > operator+ (const C &lhs, const UnivariatePolynomial < C > &rhs) template<typename C >

UnivariatePolynomial < C > operator- (const UnivariatePolynomial < C > &lhs, const UnivariatePolynomial <

UnivariatePolynomial < C > operator- (const UnivariatePolynomial < C > &lhs, const C &rhs)

```
template<typename C >
  UnivariatePolynomial < C > operator- (const C &lhs, const UnivariatePolynomial < C > &rhs)
• template<typename C >
  UnivariatePolynomial < C > operator* (const UnivariatePolynomial < C > &lhs, const UnivariatePolynomial <
  C > &rhs)
template<typename C >
  UnivariatePolynomial < C > operator* (const UnivariatePolynomial < C > &lhs, Variable rhs)
template<typename C >
  UnivariatePolynomial < C > operator* (Variable lhs, const UnivariatePolynomial < C > &rhs)
template<typename C >
  UnivariatePolynomial < C > operator* (const UnivariatePolynomial < C > &lhs, const C &rhs)
template<typename C >
  UnivariatePolynomial < C > operator* (const C &lhs, const UnivariatePolynomial < C > &rhs)

    template<typename C >

  UnivariatePolynomial < C > operator* (const UnivariatePolynomial < C > &lhs, const IntegralTypeIfDifferent <
  C > &rhs

    template<typename C >

  UnivariatePolynomial < C > operator* (const IntegralTypeIfDifferent < C > &lhs, const UnivariatePolynomial <
  C > &rhs)

    template<typename C >

  UnivariatePolynomial < C > operator/ (const UnivariatePolynomial < C > &lhs, const C &rhs)
template<typename C >
  bool operator== (const UnivariatePolynomial < C > &lhs, const UnivariatePolynomial < C > &rhs)
• template<typename C >
  bool operator== (const UnivariatePolynomialPtr< C > &lhs, const UnivariatePolynomialPtr< C > &rhs)
• template<typename C >
  bool operator== (const UnivariatePolynomial < C > &lhs, const C &rhs)

    template<typename C >

  bool operator== (const C &lhs, const UnivariatePolynomial < C > &rhs)

    template<typename C >

  bool operator!= (const UnivariatePolynomial < C > &lhs, const UnivariatePolynomial < C > &rhs)

    template<typename C >

  bool operator!= (const UnivariatePolynomialPtr< C > &lhs, const UnivariatePolynomialPtr< C > &rhs)
template<typename C >
  bool operator < (const UnivariatePolynomial < C > &lhs, const UnivariatePolynomial < C > &rhs)

    template<typename C >

  std::ostream & operator << (std::ostream &os, const UnivariatePolynomial < C > &rhs)

    template<typename Number, typename Integer >

  Interval < Number > pow (const Interval < Number > &i, Integer exp)

    template<typename Number, typename Integer >

  void pow_assign (Interval < Number > &i, Integer exp)

    template<typename Number , Enablelf< std::is_floating_point< Number >> = dummy>

  Interval < Number > sqrt (const Interval < Number > &i)

    template<typename Number , EnableIf< std::is_floating_point< Number >> = dummy>

  void sqrt_assign (Interval< Number > &i)

    template<typename T, EnableIf< is_number_type< T>> = dummy>

  const T & derivative (const T &t, Variable, std::size_t n=1)
      Computes the n'th derivative of a number, which is either the number itself (for n = 0) or zero.

    std::pair < std::size_t, Monomial::Arg > derivative (const Monomial::Arg &m, Variable v, std::size_t n=1)

     Computes the (partial) n'th derivative of this monomial with respect to the given variable.
template<typename C >
  Term< C > derivative (const Term< C > &t, Variable v, std::size_t n=1)
     Computes the n'th derivative of t with respect to v.
• template<typename C , typename O , typename P >
  MultivariatePolynomial < C, O, P > derivative (const MultivariatePolynomial < C, O, P > &p, Variable v, std\leftarrow
  ::size_t n=1)
```

Computes the n'th derivative of p with respect to v.

• template<typename C >

UnivariatePolynomial < C > derivative (const UnivariatePolynomial < C > &p, std::size\_t n=1)

Computes the n'th derivative of p with respect to the main variable of p.

template<typename C >

UnivariatePolynomial < C > derivative (const UnivariatePolynomial < C > &p, Variable v, std::size\_t n=1)

Computes the n'th derivative of p with respect to v.

template<typename Coeff >

Term < Coeff > divide (const Term < Coeff > &t, const Coeff &c)

• template<typename Coeff >

bool try\_divide (const Term < Coeff > &t, const Coeff &c, Term < Coeff > &res)

template<typename Coeff >

bool try\_divide (const Term< Coeff > &t, Variable v, Term< Coeff > &res)

template<typename Coeff , typename Ordering , typename Policies >

MultivariatePolynomial < Coeff, Ordering, Policies > divide (const MultivariatePolynomial < Coeff, Ordering, Policies > &p, const Coeff &divisor)

Divides the polynomial by the given coefficient.

- template<typename Coeff , typename Ordering , typename Policies >

bool try\_divide (const MultivariatePolynomial < Coeff, Ordering, Policies > &dividend, const MultivariatePolynomial < Coeff, Ordering, Policies > &divisor, MultivariatePolynomial < Coeff, Ordering, Policies > &quotient)

Divides the polynomial by another polynomial.

template<typename Coeff , typename Ordering , typename Policies >

DivisionResult< MultivariatePolynomial< Coeff, Ordering, Policies >> divide (const MultivariatePolynomial< Coeff, Ordering, Policies > & dividend, const MultivariatePolynomial< Coeff, Ordering, Policies > & divisor)

Calculating the quotient and the remainder, such that for a given polynomial p we have p = divisor \* quotient + remainder.

template<typename Coeff >

bool try\_divide (const UnivariatePolynomial < Coeff > &dividend, const Coeff &divisor, UnivariatePolynomial < Coeff > &quotient)

• template<typename Coeff >

DivisionResult< UnivariatePolynomial< Coeff > > divide (const UnivariatePolynomial< Coeff > &p, const Coeff &divisor)

• template<typename Coeff >

DivisionResult< UnivariatePolynomial< Coeff > > divide (const UnivariatePolynomial< Coeff > &p, const typename UnderlyingNumberType< Coeff >::type &divisor)

• template<typename Coeff >

DivisionResult< UnivariatePolynomial< Coeff > > divide (const UnivariatePolynomial< Coeff > &dividend, const UnivariatePolynomial< Coeff > &divisor)

Divides the polynomial by another polynomial.

• template < typename  $\,$  C  $\,$  , typename  $\,$  O  $\,$  , typename  $\,$  P  $\,$ 

MultivariatePolynomial < C, O, P > operator/ (const MultivariatePolynomial < C, O, P > &lhs, const MultivariatePolynomial < C, O, P > &rhs)

• template<typename P >

bool operator== (const BasicConstraint < P > &lhs, const BasicConstraint < P > &rhs)

• template<typename P >

bool operator!= (const BasicConstraint< P > &lhs, const BasicConstraint< P > &rhs)

template<typename P >

bool operator< (const BasicConstraint< P > &lhs, const BasicConstraint< P > &rhs)

template<typename P >

bool operator<= (const BasicConstraint< P > &lhs, const BasicConstraint< P > &rhs)

template<typename P >

bool operator> (const BasicConstraint< P > &lhs, const BasicConstraint< P > &rhs)

• template<typename P >

bool operator>= (const BasicConstraint< P > &lhs, const BasicConstraint< P > &rhs)

template<typename Pol >

void variables (const BasicConstraint< Pol > &c, carlVariables &vars)

• template<typename Poly > std::ostream & operator<< (std::ostream &os, const BasicConstraint< Poly > &c)

Prints the given constraint on the given stream.

• template<typename Pol >

bool is\_bound (const BasicConstraint < Pol > &constr)

template<typename Pol >

bool is\_lower\_bound (const BasicConstraint < Pol > &constr)

template<typename Pol >

bool is\_upper\_bound (const BasicConstraint< Pol > &constr)

template<typename Pol >

signed compare (const BasicConstraint < Pol > &\_constraint A, const BasicConstraint < Pol > &\_constraint B)

Compares \_constraintA with \_constraintB.

 $\bullet \ \ \mathsf{template}{<} \mathsf{typename} \ \mathsf{Poly} >$ 

std::size\_t complexity (const BasicConstraint < Poly > &c)

- template<typename ToPoly , typename FromPoly , typename = std::enable\_if\_t<!needs\_context\_type<ToPoly>::value>>
   BasicConstraint< ToPoly > convert (const BasicConstraint< FromPoly > &c)
- template<typename Number, typename Poly, typename = std::enable\_if\_t<is\_number\_type<Number>::value>> bool evaluate (const BasicConstraint< Poly > &c, const Assignment< Number > &m)
- template<typename Pol >

unsigned satisfied\_by (const BasicConstraint< Pol > &c, const Assignment< typename Pol::NumberType > &\_assignment)

Checks whether the given assignment satisfies this constraint.

template<typename Number, typename Poly >
 boost::tribool evaluate (const BasicConstraint< Poly > &c, const Assignment< Interval< Number >> &map)

template<typename Pol >
 static unsigned consistent\_with (const BasicConstraint< Pol > &c, const Assignment< Interval< double >>
 &\_solutionInterval)

Checks whether this constraint is consistent with the given assignment from the its variables to interval domains.

template<typename Pol >

static unsigned consistent\_with (const BasicConstraint< Pol > &c, const Assignment< Interval< double >> &\_solutionInterval, Relation &\_stricterRelation)

Checks whether this constraint is consistent with the given assignment from the its variables to interval domains.

template<typename Pol >

std::optional < std::pair < Variable, Pol > > get\_substitution (const BasicConstraint < Pol > &c, bool  $\leftarrow$  \_negated=false, Variable \_exclude=carl::Variable::NO\_VARIABLE, std::optional < VarsInfo < Pol >> var\_info=std::nullopt)

If this constraint represents a substitution (equation, where at least one variable occurs only linearly), this method detects a (there could be various possibilities) corresponding substitution variable and term.

template<typename Pol >

std::optional < std::pair < Variable, typename Pol::NumberType > > get\_assignment (const BasicConstraint < Pol > &c)

- std::ostream & operator<< (std::ostream &os, const Relation &r)</li>
- Relation inverse (Relation r)

Inverts the given relation symbol.

Relation turn\_around (Relation r)

Turns around the given relation symbol, in the sense that LESS (LEQ) and GREATER (GEQ) are swapped.

- std::string toString (Relation r)
- bool is\_strict (Relation r)
- bool is\_weak (Relation r)
- bool evaluate (Sign s, Relation r)
- template<typename T >
   bool evaluate (const T &t, Relation r)

```
    template<typename T1 , typename T2 >

   bool evaluate (const T1 &lhs, Relation r, const T2 &rhs)
• template < typename ToPoly, typename FromPoly, typename = std::enable_if_t < needs_context_type < ToPoly >::value >>
   VariableComparison < ToPoly > convert (const typename ToPoly::ContextType &context, const VariableComparison <
   FromPoly > &c)
• template<typename ToPoly, typename FromPoly, typename = std::enable_if_t<!needs_context_type<ToPoly>::value>>
   VariableComparison < ToPoly > convert (const VariableComparison < FromPoly > &c)
template<typename Poly >
   void encode_as_constraints_simple (const MultivariateRoot< Poly > &f, Assignment< typename
   VariableComparison< Poly >::RAN > ass, Variable var, std::vector< BasicConstraint< Poly >> &out)

    template<typename Poly >

   void encode_as_constraints_thom (const MultivariateRoot < Poly > &f, Assignment < typename VariableComparison <
   Poly >::RAN > ass, Variable var, std::vector < BasicConstraint < Poly >> &out)

    template<typename Poly >

   std::pair < std::vector < BasicConstraint < Poly >> , Variable > encode\_as\_constraints \ (const \ MultivariateRoot < Constraint < Constraint < Constraint < Constraint < Constraint < Const \ MultivariateRoot < Constraint < Co
   Poly > &f, Assignment< typename VariableComparison< Poly >::RAN > ass, EncodingCache< Poly >
   cache)

    template<typename Poly >

   std::pair< std::vector< BasicConstraint< Poly > >, BasicConstraint< Poly > > encode_as_constraints
   (const VariableComparison < Poly > &f, const Assignment < typename VariableComparison < Poly >::RAN
   > &ass, EncodingCache < Poly > cache)
• template<typename Poly >
   bool operator== (const MultivariateRoot< Poly > &lhs, const MultivariateRoot< Poly > &rhs)
• template<typename Poly >
   bool operator< (const MultivariateRoot< Poly > &lhs, const MultivariateRoot< Poly > &rhs)

    template<typename P >

   std::ostream & operator << (std::ostream &os, const MultivariateRoot < P > &mr)

    template<typename Poly >

   void variables (const MultivariateRoot< Poly > &mr, carlVariables &vars)
         Add the variables mentioned in underlying polynomial, excluding the root-variable "_z".
template<typename Poly >
   void substitute_inplace (MultivariateRoot< Poly > &mr, Variable var, const Poly &poly)
         Create a copy of the underlying polynomial with the given variable replaced by the given polynomial.

    template<typename Poly >

   MultivariateRoot< Poly > convert_to_mvroot (const typename MultivariateRoot< Poly >::RAN &ran, Variable
   var)

    template<typename Poly >

   std::optional< typename MultivariateRoot< Poly >::RAN > evaluate (const MultivariateRoot< Poly > &mr,
   const carl::Assignment< typename MultivariateRoot< Poly >::RAN > &m)
         Return the emerging algebraic real after pluggin in a subpoint to replace all variables with algebraic reals that are not
        the root-variable "_z".
• template<typename Pol >
   void variables (const VariableAssignment< Pol > &f, carlVariables &vars)

    template<typename Poly >

   bool operator== (const VariableAssignment< Poly > &lhs, const VariableAssignment< Poly > &rhs)

    template<typename Poly >

   bool operator < (const VariableAssignment < Poly > &lhs, const VariableAssignment < Poly > &rhs)
   std::ostream & operator << (std::ostream &os, const VariableAssignment < Poly > &va)

    template<typename Poly >

   std::optional < BasicConstraint < Poly > > as_constraint (const VariableComparison < Poly > &f)
         Convert this variable comparison "v < root(..)" into a simpler polynomial (in)equality against zero "p(..) < 0" if that is
```

template<typename Poly, std::enable\_if\_t<!needs\_context\_type< Poly >::value, bool > = true>
 Poly defining\_polynomial (const VariableComparison< Poly > &f)

possible.

Return a polynomial containing the Ihs-variable that has a same root for the this Ihs-variable as the value that rhs represent, e.g.

template<typename Poly >

boost::tribool evaluate (const VariableComparison < Poly > &f, const Assignment < typename VariableComparison < Poly >::RAN > &a)

template<typename Pol >

void variables (const VariableComparison < Pol > &f, carlVariables &vars)

template<typename Poly >

bool operator== (const VariableComparison < Poly > &lhs, const VariableComparison < Poly > &rhs)

template<typename Poly >

bool operator < (const VariableComparison < Poly > &lhs, const VariableComparison < Poly > &rhs)

• template<typename Poly >

std::ostream & operator << (std::ostream &os, const VariableComparison < Poly > &vc)

template < class C >

std::ostream & operator << (std::ostream &os, const ReductorEntry < C > rhs)

template<typename Number >

boost::tribool evaluate (Interval < Number > interval, Relation relation)

template < typename Number , Enablelf < std::is\_floating\_point < Number >> = dummy > Interval < Number > exp (const Interval < Number > &i)

template<typename Number , EnableIf< std::is\_floating\_point< Number >> = dummy>
 void exp\_assign (Interval< Number > &i)

template < typename Number , EnableIf < std::is\_floating\_point < Number >> = dummy > Interval < Number > log (const Interval < Number > &i)

template<typename Number , EnableIf< std::is\_floating\_point< Number >> = dummy> void log\_assign (Interval< Number > &i)

template<typename Number >

bool set\_complement (const Interval < Number > &interval < Number > &resA, Interval < Number > &resB)

Calculates the complement in a set-theoretic manner (can result in two distinct intervals).

template<typename Number >

bool set\_difference (const Interval < Number > &lhs, const Interval < Number > &rhs, Interval < Number > &resA, Interval < Number > &resB)

Calculates the difference of two intervals in a set-theoretic manner: Ihs \ rhs (can result in two distinct intervals).

• template<typename Number >

Interval < Number > set\_intersection (const Interval < Number > &lhs, const Interval < Number > &rhs)

Intersects two intervals in a set-theoretic manner.

• template<typename Number >

bool set\_have\_intersection (const Interval < Number > &lhs, const Interval < Number > &rhs)

template<typename Number >

 $bool \ set\_is\_proper\_subset \ (const \ Interval < Number > \&lhs, \ const \ Interval < Number > \&rhs)$ 

Checks whether lhs is a proper subset of rhs.

• template<typename Number >

bool set\_is\_subset (const Interval < Number > &lhs, const Interval < Number > &rhs)

Checks whether lhs is a subset of rhs.

• template<typename Number >

bool  $set\_symmetric\_difference$  (const Interval < Number > &lhs, const Interval < Number > &rhs, Interval < Number > &resA, Interval < Number > &resB)

Calculates the symmetric difference of two intervals in a set-theoretic manner (can result in two distinct intervals).

template<typename Number >

bool  $set\_union$  (const Interval < Number > &Ihs, const Interval < Number > &rhs, Interval < Number > &resA, Interval < Number > &resB)

Computes the union of two intervals (can result in two distinct intervals).

- template < typename Number , Enablelf < std::is\_floating\_point < Number >> = dummy > Interval < Number > sin (const Interval < Number > &i)
- template<typename Number, EnableIf< std::is\_floating\_point< Number >> = dummy> void sin\_assign (Interval< Number > &i)

- template < typename Number , EnableIf < std::is\_floating\_point < Number >> = dummy > Interval < Number > cos (const Interval < Number > &i)
- template<typename Number, Enablelf< std::is\_floating\_point< Number >> = dummy> void cos\_assign (Interval< Number > &i)
- template < typename Number , EnableIf < std::is\_floating\_point < Number >> = dummy > Interval < Number > tan (const Interval < Number > &i)
- template < typename Number , Enablelf < std::is\_floating\_point < Number >> = dummy > void tan\_assign (Interval < Number > &i)
- template < typename Number , Enablelf < std::is.floating.point < Number >> = dummy > Interval < Number > asin (const Interval < Number > &i)
- template<typename Number, EnableIf< std::is\_floating\_point< Number >> = dummy> void asin\_assign (Interval< Number > &i)
- template<typename Number, EnableIf< std::is\_floating\_point< Number >> = dummy>
   Interval< Number > acos (const Interval< Number > &i)
- template<typename Number, EnableIf< std::is\_floating\_point< Number >> = dummy> void acos\_assign (Interval< Number > &i)
- template < typename Number , Enablelf < std::is\_floating\_point < Number >> = dummy > Interval < Number > atan (const Interval < Number > &i)
- template < typename Number , Enablelf < std::is\_floating\_point < Number >> = dummy > void atan\_assign (Interval < Number > &i)
- template < typename Number , Enablelf < std::is.floating.point < Number >> = dummy > Interval < Number > sinh (const Interval < Number > &i)
- template<typename Number, EnableIf< std::is\_floating\_point< Number >> = dummy>
   void sinh\_assign (Interval< Number > &i)
- template < typename Number , Enablelf < std::is\_floating\_point < Number >> = dummy > Interval < Number > cosh (const Interval < Number > &i)
- template < typename Number , Enablelf < std::is\_floating\_point < Number >> = dummy > void cosh\_assign (Interval < Number > &i)
- template < typename Number , EnableIf < std::is\_floating\_point < Number >> = dummy >
   Interval < Number > tanh (const Interval < Number > &i)
- template < typename Number , Enablelf < std::is\_floating\_point < Number >> = dummy > void tanh\_assign (Interval < Number > &i)
- template<typename Number, EnableIf< std::is\_floating\_point< Number >> = dummy>
   Interval< Number > asinh (const Interval< Number > &i)
- template<typename Number, EnableIf< std::is\_floating\_point< Number >> = dummy> void asinh\_assign (Interval< Number > &i)
- template < typename Number , Enablelf < std::is\_floating\_point < Number >> = dummy > Interval < Number > acosh (const Interval < Number > &i)
- template<typename Number, EnableIf< std::is\_floating\_point< Number >> = dummy> void acosh\_assign (Interval< Number > &i)
- template < typename Number , Enablelf < std::is\_floating\_point < Number >> = dummy > Interval < Number > atanh (const Interval < Number > &i)
- template<typename Number , EnableIf< std::is\_floating\_point< Number >> = dummy>
   void atanh\_assign (Interval< Number > &i)
- bool is\_zero (const cln::cl\_l &n)
- bool is\_zero (const cln::cl\_RA &n)
- bool is\_one (const cln::cl\_l &n)
- bool is\_one (const cln::cl\_RA &n)
- bool is\_positive (const cln::cl\_l &n)
- bool is\_positive (const cln::cl\_RA &n)
- bool is\_negative (const cln::cl\_l &n)
- bool is\_negative (const cln::cl\_RA &n)
- cln::cl\_I get\_num (const cln::cl\_RA &n)

Extract the numerator from a fraction.

cln::cl\_l get\_denom (const cln::cl\_RA &n)

Extract the denominator from a fraction.

 bool is\_integer (const cln::cl\_l &) Check if a number is integral. bool is\_integer (const cln::cl\_RA &n) Check if a fraction is integral. std::size\_t bitsize (const cln::cl\_l &n) Get the bit size of the representation of a integer. std::size\_t bitsize (const cln::cl\_RA &n) Get the bit size of the representation of a fraction. double to\_double (const cln::cl\_RA &n) Converts the given fraction to a double. double to\_double (const cln::cl\_l &n) Converts the given integer to a double. • template<typename Integer > Integer to\_int (const cln::cl\_l &n) template<typename Integer > Integer to\_int (const cln::cl\_RA &n) template<> sint to\_int< sint > (const cln::cl\_l &n) template<> uint to\_int< uint > (const cln::cl\_l &n) template<> cln::cl\_l to\_int< cln::cl\_l > (const cln::cl\_RA &n) Convert a fraction to an integer. template<> sint to\_int< sint > (const cln::cl\_RA &n) template<> uint to\_int< uint > (const cln::cl\_RA &n) cln::cl\_LF to\_lf (const cln::cl\_RA &n) Convert a cln fraction to a cln long float. template<> cln::cl\_RA rationalize< cln::cl\_RA > (double n) template<> cln::cl\_RA rationalize< cln::cl\_RA > (float n) template<> cln::cl\_RA rationalize< cln::cl\_RA > (int n) template<> cln::cl\_RA rationalize< cln::cl\_RA > (uint n) template<> cln::cl\_RA rationalize< cln::cl\_RA > (sint n) • template<> cln::cl\_l parse< cln::cl\_l > (const std::string &n) template<> bool try\_parse< cln::cl\_l > (const std::string &n, cln::cl\_l &res) template<> cln::cl\_RA parse< cln::cl\_RA > (const std::string &n) template<> bool try\_parse< cln::cl\_RA > (const std::string &n, cln::cl\_RA &res) cln::cl\_l abs (const cln::cl\_l &n) Get absolute value of an integer. cln::cl\_RA abs (const cln::cl\_RA &n) Get absolute value of a fraction. cln::cl\_I round (const cln::cl\_RA &n) Round a fraction to next integer. cln::cl\_l round (const cln::cl\_l &n) Round an integer to next integer, that is do nothing. cln::cl\_I floor (const cln::cl\_RA &n) Round down a fraction. cln::cl\_l floor (const cln::cl\_l &n) Round down an integer. cln::cl\_l ceil (const cln::cl\_RA &n) Round up a fraction.

 cln::cl\_l ceil (const cln::cl\_l &n) Round up an integer.

cln::cl\_l gcd (const cln::cl\_l &a, const cln::cl\_l &b)

Calculate the greatest common divisor of two integers.

cln::cl\_l & gcd\_assign (cln::cl\_l &a, const cln::cl\_l &b)

Calculate the greatest common divisor of two integers.

- void divide (const cln::cl\_l &dividend, const cln::cl\_l &divisor, cln::cl\_l &quotient, cln::cl\_l &remainder)
- cln::cl\_RA & gcd\_assign (cln::cl\_RA &a, const cln::cl\_RA &b)

Calculate the greatest common divisor of two fractions.

cln::cl\_RA gcd (const cln::cl\_RA &a, const cln::cl\_RA &b)

Calculate the greatest common divisor of two fractions.

• cln::cl\_l lcm (const cln::cl\_l &a, const cln::cl\_l &b)

Calculate the least common multiple of two integers.

cln::cl\_RA lcm (const cln::cl\_RA &a, const cln::cl\_RA &b)

Calculate the least common multiple of two fractions.

template<> cln::cl\_RA pow (const cln::cl\_RA &basis, std::size\_t exp)

Calculate the power of some fraction to some positive integer.

- cln::cl\_RA log (const cln::cl\_RA &n)
- cln::cl\_RA log10 (const cln::cl\_RA &n)
- cln::cl\_RA sin (const cln::cl\_RA &n)
- cln::cl\_RA cos (const cln::cl\_RA &n)
- bool sqrt\_exact (const cln::cl\_RA &a, cln::cl\_RA &b)

Calculate the square root of a fraction if possible.

- cln::cl\_RA sqrt (const cln::cl\_RA &a)
- std::pair< cln::cl\_RA, cln::cl\_RA > sqrt\_safe (const cln::cl\_RA &a)

Calculate the square root of a fraction.

std::pair< cln::cl\_RA, cln::cl\_RA > sqrt\_fast (const cln::cl\_RA &a)

Compute square root in a fast but less precise way.

- std::pair < cln::cl\_RA, cln::cl\_RA > root\_safe (const cln::cl\_RA &a, uint n)
- cln::cl\_l mod (const cln::cl\_l &a, const cln::cl\_l &b)

Calculate the remainder of the integer division.

• cln::cl\_RA div (const cln::cl\_RA &a, const cln::cl\_RA &b)

Divide two fractions.

cln::cl\_l div (const cln::cl\_l &a, const cln::cl\_l &b)

Divide two integers.

cln::cl\_RA & div\_assign (cln::cl\_RA &a, const cln::cl\_RA &b)

Divide two fractions.

cln::cl\_l & div\_assign (cln::cl\_l &a, const cln::cl\_l &b)

Divide two integers.

cln::cl\_RA quotient (const cln::cl\_RA &a, const cln::cl\_RA &b)

Divide two fractions.

• cln::cl\_l quotient (const cln::cl\_l &a, const cln::cl\_l &b)

Divide two integers.

• cln::cl\_l remainder (const cln::cl\_l &a, const cln::cl\_l &b)

Calculate the remainder of the integer division.

• cln::cl\_l operator/ (const cln::cl\_l &a, const cln::cl\_l &b)

Divide two integers.

- cln::cl\_I operator/ (const cln::cl\_I &lhs, const int &rhs)
- cln::cl\_RA reciprocal (const cln::cl\_RA &a)
- std::string toString (const cln::cl\_RA &\_number, bool \_infix=true)
- std::string toString (const cln::cl\_I &\_number, bool \_infix=true)
- template<typename T , typename S , std::enable\_if\_t< is\_polynomial\_type< T >::value &&is\_polynomial\_type< S >::value &&!needs  $\hookleftarrow$  \_context\_type< T >::value, int > = 0>

T convert (const S &r)

• template<typename T , typename S , std::enable\_if\_t< is\_polynomial\_type< T >::value &&is\_polynomial\_type< S >::value &&needs ← context\_type< T >::value, int > = 0>

T convert (const typename T::ContextType &c, const S &r)

Gives the total degree, i.e.

• bool is\_constant (const Monomial &m)

```
    std::ostream & operator<< (std::ostream &os, const Context &ctx)</li>

ullet template<typename Coeff , typename Ordering , typename Policies >
  bool is_constant (const ContextPolynomial < Coeff, Ordering, Policies > &p)

    template<typename Coeff , typename Ordering , typename Policies >

  bool is_zero (const ContextPolynomial < Coeff, Ordering, Policies > &p)
• template<typename Coeff , typename Ordering , typename Policies >
  bool is_linear (const ContextPolynomial < Coeff, Ordering, Policies > &p)
ullet template<typename Coeff , typename Ordering , typename Policies >
  bool is_number (const ContextPolynomial < Coeff, Ordering, Policies > &p)
ullet template<typename Coeff , typename Ordering , typename Policies >
  std::size_t level_of (const ContextPolynomial < Coeff, Ordering, Policies > &p)
ullet template<typename Coeff , typename Ordering , typename Policies >
  void variables (const ContextPolynomial < Coeff, Ordering, Policies > &p, carlVariables &vars)
- template<typename Coeff , typename Ordering , typename Policies >
  bool operator< (const ContextPolynomial< Coeff, Ordering, Policies > &lhs, const ContextPolynomial<
  Coeff, Ordering, Policies > &rhs)

    template<typename Coeff , typename Ordering , typename Policies >

  bool operator== (const ContextPolynomial < Coeff, Ordering, Policies > &lhs, const ContextPolynomial <
  Coeff, Ordering, Policies > &rhs)

    template<typename Coeff , typename Ordering , typename Policies >

  std::ostream & operator<< (std::ostream &os, const ContextPolynomial< Coeff, Ordering, Policies > &rhs)

    template<typename Coeff , typename Ordering , typename Policies >

  auto irreducible_factors (const ContextPolynomial < Coeff, Ordering, Policies > &p, bool constants=true)

    template<typename Coeff , typename Ordering , typename Policies >

  auto discriminant (const ContextPolynomial Coeff, Ordering, Policies > &p)

    template<typename Coeff , typename Ordering , typename Policies >

  auto resultant (const ContextPolynomial < Coeff, Ordering, Policies > &p, const ContextPolynomial < Coeff,
  Ordering, Policies > &q)

    std::size_t bitsize (const Monomial &m)

template<typename Coeff >
  std::size_t bitsize (const Term < Coeff > &t)

    template<typename Coeff , typename Ordering , typename Policies >

  std::size_t bitsize (const MultivariatePolynomial < Coeff, Ordering, Policies > &p)

    std::size_t complexity (const Monomial &m)

template<typename Coeff >
  std::size_t complexity (const Term < Coeff > &t)

    template<typename Coeff , typename Ordering , typename Policies >

  std::size_t complexity (const MultivariatePolynomial < Coeff, Ordering, Policies > &p)

    template<typename Coeff >

  std::size_t complexity (const UnivariatePolynomial < Coeff > &p)
template<typename Coeff >
  Coeff content (const UnivariatePolynomial < Coeff > &p)
      The content of a polynomial is the gcd of the coefficients of the normal part of a polynomial.
• template<typename C , typename O , typename P >
  MultivariatePolynomial < C, O, P > coprimePart (const MultivariatePolynomial < C, O, P > &p, const
  MultivariatePolynomial < C, O, P > &q)
      Calculates the coprime part of p and q.

    std::ostream & operator<< (std::ostream &os, Definiteness d)</li>

    template<typename Coeff >

  Definiteness definiteness (const Term < Coeff > &t)
- template<typename C , typename O , typename P >
  Definiteness definiteness (const MultivariatePolynomial < C, O, P > &p, bool full_effort=true)

    auto total_degree (const Monomial &m)
```

template<typename Coeff >

bool includeConstants=true)

• template<typename C , typename O , typename P >

bool is\_root\_of (const UnivariatePolynomial < Coeff > &p, const Coeff &value)

 $Factors < \ Multivariate Polynomial < C, O, P >> factorization \ (const \ Multivariate Polynomial < C, O, P > \&p, \\$ 

Checks whether the monomial is a constant. • bool is\_linear (const Monomial &m) Checks whether the monomial has exactly degree one. bool is\_at\_most\_linear (const Monomial &m) Checks whether the monomial has at most degree one. template<tvpename Coeff >  $std::size\_t\ total\_degree\ (const\ Term < Coeff > \&t)$ Gives the total degree, i.e. template<typename Coeff > bool is\_constant (const Term< Coeff > &t) Checks whether the monomial is a constant.  $\bullet \ \ {\sf template}{<} {\sf typename Coeff}>$ bool is\_linear (const Term < Coeff > &t) Checks whether the monomial has exactly the degree one. template<typename Coeff > bool is\_at\_most\_linear (const Term < Coeff > &t) Checks whether the monomial has at most degree one. • template<typename Coeff , typename Ordering , typename Policies > std::size\_t total\_degree (const MultivariatePolynomial < Coeff, Ordering, Policies > &p) Calculates the max. • template<typename Coeff , typename Ordering , typename Policies > bool is\_constant (const MultivariatePolynomial < Coeff, Ordering, Policies > &p) Check if the polynomial is linear. template<typename Coeff , typename Ordering , typename Policies > bool is\_linear (const MultivariatePolynomial < Coeff, Ordering, Policies > &p) Check if the polynomial is linear. template<typename Coeff > std::size\_t total\_degree (const UnivariatePolynomial < Coeff > &p) Returns the total degree of the polynomial, that is the maximum degree of any monomial. template<typename Coeff > bool is\_constant (const UnivariatePolynomial < Coeff > &p) Checks whether the polynomial is constant with respect to the main variable. template<typename Coeff > bool is\_linear (const UnivariatePolynomial < Coeff > &p) • template<typename T > std::vector< T > solveDiophantine (MultivariatePolynomial< T > &p) Diophantine Equations solver. template<typename T > T extended\_gcd\_integer (T a, T b, T &s, T &t) template<typename Coefficient > Coefficient evaluate (const Monomial &m, const std::map < Variable, Coefficient > &substitutions) template<typename Coefficient > Coefficient evaluate (const Term < Coefficient > &t, const std::map < Variable, Coefficient > &map) template < typename C , typename O , typename P , typename SubstitutionType > SubstitutionType evaluate (const MultivariatePolynomial < C, O, P > &p, const std::map < Variable, SubstitutionType > &substitutions) Like substitute, but expects substitutions for all variables. template<typename Coeff > Coeff evaluate (const UnivariatePolynomial < Coeff > &p, const Coeff &value)

Try to factorize a multivariate polynomial.

template<typename C, typename O, typename P >
 bool is\_trivial (const Factors< MultivariatePolynomial< C, O, P >> &f)

template < typename C, typename O, typename P >
 std::vector < Multivariate Polynomial < C, O, P >> irreducible\_factors (const Multivariate Polynomial < C, O, P >> &p, bool include Constants=true)

Try to factorize a multivariate polynomial and return the irreducible factors (without multiplicities).

template<typename Coeff >

std::map< uint, UnivariatePolynomial< Coeff > > squareFreeFactorization (const UnivariatePolynomial< Coeff > &p)

template<typename Coeff >

FactorMap < Coeff > factorization (const UnivariatePolynomial < Coeff > &p)

template<typename Coeff >

UnivariatePolynomial < Coeff > gcd (const UnivariatePolynomial < Coeff > &a, const UnivariatePolynomial < Coeff > &b)

Calculates the greatest common divisor of two polynomials.

• template<typename C , typename O , typename P >

Term< C > gcd (const MultivariatePolynomial< C, O, P > &a, const Term< C > &b)

• template<typename C , typename O , typename P >

 $\textit{Term} < \textit{C} > \textit{gcd} \; (\textit{const Term} < \textit{C} > \textit{\&a}, \, \textit{const MultivariatePolynomial} < \textit{C}, \, \textit{O}, \, \textit{P} > \textit{\&b})$ 

• template<typename C , typename O , typename P >

Monomial::Arg gcd (const MultivariatePolynomial< C, O, P > &a, const Monomial::Arg &b)

- template<typename C , typename O , typename P >

Monomial::Arg gcd (const Monomial::Arg &a, const MultivariatePolynomial < C, O, P > &b)

 $\bullet \ \ {\sf template}{<} {\sf typename Coeff}>$ 

Term< Coeff > gcd (const Term< Coeff > &t1, const Term< Coeff > &t2)

Calculates the gcd of (t1, t2).

• template<typename Coeff >

Univariate Polynomial < Coeff > gcd\_recursive (const Univariate Polynomial < Coeff > &a, const Univariate Polynomial < Coeff > &b)

• template<typename Coeff >

 $\label{lem:coeff} \mbox{ UnivariatePolynomial< Coeff > extended\_gcd (const UnivariatePolynomial< Coeff > \&a, const UnivariatePolynomial< Coeff > \&b, UnivariatePolynomial< Coeff > \&s, UnivariatePolynomial< Coeff > \&t) \\$ 

Calculates the extended greatest common divisor g of two polynomials.

- template<typename C , typename O , typename P >

Multivariate Polynomial < C, O, P > lcm (const Multivariate Polynomial < C, O, P > &a, const Multivariate Polynomial < C, O, P > &b)

Monomial::Arg pow (const Monomial &m, uint exp)

Calculates the given power of a monomial m.

- Monomial::Arg pow (const Monomial::Arg &m, uint exp)
- template<typename Coeff >

Term < Coeff > pow (const Term < Coeff > &t, uint exp)

• template<typename C , typename O , typename P >

MultivariatePolynomial < C, O, P > pow (const MultivariatePolynomial < C, O, P > &p, std::size\_t exp)

• template<typename C , typename O , typename P >

MultivariatePolynomial < C, O, P > pow\_naive (const MultivariatePolynomial < C, O, P > &p, std::size\_t exp)

template<typename Coeff >

UnivariatePolynomial < Coeff > pow (const UnivariatePolynomial < Coeff > &p, std::size\_t exp)

Returns a polynomial to the given power.

• template<typename Coeff >

 $\label{lem:univariatePolynomial} \mbox{ Coeff } > \mbox{ primitive\_euclidean (const UnivariatePolynomial} < \mbox{ Coeff } > \mbox{ \&a, const UnivariatePolynomial} < \mbox{ Coeff } > \mbox{ \&b)}$ 

Computes the GCD of two univariate polynomial with coefficients from a unique factorization domain using the primitive euclidean algorithm.

template<typename Coeff >

UnivariatePolynomial < Coeff > primitive\_part (const UnivariatePolynomial < Coeff > &p)

The primitive part of p is the normal part of p divided by the content of p.

template<typename Coeff >

UnivariatePolynomial < Coeff > pseudo\_primitive\_part (const UnivariatePolynomial < Coeff > &p)

Returns this/divisor where divisor is the numeric content of this polynomial.

• template<typename C , typename O , typename P >

 $\label{eq:multivariatePolynomial} \mbox{MultivariatePolynomial} < C, O, P > \mbox{dividend, const MultivariatePolynomial} < C, O, P > \mbox{\&divisor)}$ 

Calculates the quotient of a polynomial division.

template<typename Coeff >

UnivariatePolynomial < Coeff > remainder\_helper (const UnivariatePolynomial < Coeff > &dividend, const UnivariatePolynomial < Coeff > &divisor, const Coeff \*prefactor=nullptr)

Does the heavy lifting for the remainder computation of polynomial division.

• template<typename Coeff >

UnivariatePolynomial < Coeff > remainder (const UnivariatePolynomial < Coeff > &dividend, const UnivariatePolynomial < Coeff > &divisor, const Coeff &prefactor)

template<typename Coeff >

UnivariatePolynomial< Coeff > remainder (const UnivariatePolynomial< Coeff > &dividend, const UnivariatePolynomial< Coeff > &divisor)

• template<typename Coeff >

UnivariatePolynomial < Coeff > pseudo\_remainder (const UnivariatePolynomial < Coeff > &dividend, const UnivariatePolynomial < Coeff > &divisor)

Calculates the pseudo-remainder.

• template<typename Coeff >

UnivariatePolynomial < Coeff > signed\_pseudo\_remainder (const UnivariatePolynomial < Coeff > &dividend, const UnivariatePolynomial < Coeff > &divisor)

Compute the signed pseudo-remainder.

template<typename C , typename O , typename P >

 $\label{eq:multivariatePolynomial} \begin{tabular}{ll} MultivariatePolynomial< C, O, P > & dividend, const \\ MultivariatePolynomial< C, O, P > & divisor) \end{tabular}$ 

• template<typename C , typename O , typename P >

 $\label{eq:multivariatePolynomial} \begin{tabular}{ll} MultivariatePolynomial< C, O, P> pseudo\_remainder (const MultivariatePolynomial< C, O, P> & divisor, Variable var) \end{tabular}$ 

template<typename Coeff >

UnivariatePolynomial< MultivariatePolynomial< typename UnderlyingNumberType< Coeff >::type > > switch\_main\_variable (const UnivariatePolynomial< Coeff > &p, Variable newVar)

Switches the main variable using a purely syntactical restructuring.

template<typename Coeff >

UnivariatePolynomial < Coeff > replace\_main\_variable (const UnivariatePolynomial < Coeff > &p, Variable newVar)

Replaces the main variable in a polynomial.

- template<typename C, typename O, typename P>
   MultivariatePolynomial< C, O, P > switch\_variable (const MultivariatePolynomial< C, O, P > &p, Variable old\_var, Variable new\_var)
- template<typename Coeff >

std::list< UnivariatePolynomial< Coeff > > subresultants (const UnivariatePolynomial< Coeff > &pol1, const UnivariatePolynomial< Coeff > &pol2, SubresultantStrategy strategy)

Implements a subresultants algorithm with optimizations described in ? .

template < typename Coeff >
 std::vector < UnivariatePolynomial < Coeff > > principalSubresultantsCoefficients (const UnivariatePolynomial <</li>

Coeff > &, const UnivariatePolynomial < Coeff > &, SubresultantStrategy=SubresultantStrategy::Default)

• template<typename Coeff >

UnivariatePolynomial < Coeff > resultant (const UnivariatePolynomial < Coeff > &, const UnivariatePolynomial < Coeff > &, SubresultantStrategy=SubresultantStrategy::Default)

template<typename Coeff >

UnivariatePolynomial Coeff > discriminant (const UnivariatePolynomial Coeff > &, SubresultantStrategy=SubresultantStrategy

• template<typename Coeff >

Coeff cauchyBound (const UnivariatePolynomial < Coeff > &p)

template<typename Coeff >

 $\label{lem:coeff} \textbf{Coeff hirstMaceyBound (const UnivariatePolynomial} < \textbf{Coeff} > \& \textbf{p}) \\$ 

template<typename Coeff >

Coeff lagrangeBound (const UnivariatePolynomial < Coeff > &p)

template<typename Coeff >

Coeff lagrangePositiveUpperBound (const UnivariatePolynomial < Coeff > &p)

template<typename Coeff >

Coeff lagrangePositiveLowerBound (const UnivariatePolynomial < Coeff > &p)

Computes a lower bound on the value of the positive real roots of the given univariate polynomial.

template<typename Coeff >

Coeff lagrangeNegativeUpperBound (const UnivariatePolynomial < Coeff > &p)

Computes an upper bound on the value of the negative real roots of the given univariate polynomial.

template < typename Coefficient >

int count\_real\_roots (const std::vector< UnivariatePolynomial< Coefficient >> &seq, const Interval< Coefficient > &i)

Calculate the number of real roots of a polynomial within a given interval based on a sturm sequence of this polynomial.

template<typename Coefficient >

int count\_real\_roots (const UnivariatePolynomial < Coefficient > &p, const Interval < Coefficient > &i)

Count the number of real roots of p within the given interval using Sturm sequences.

template<typename Coeff >

void eliminate\_zero\_root (UnivariatePolynomial< Coeff > &p)

Reduces the given polynomial such that zero is not a root anymore.

template<typename Coeff >

void eliminate\_root (UnivariatePolynomial < Coeff > &p, const Coeff &root)

Reduces the polynomial such that the given root is not a root anymore.

Monomial::Arg separable\_part (const Monomial &m)

Calculates the separable part of this monomial.

• template<typename Coefficient >

uint sign\_variations (const UnivariatePolynomial< Coefficient > &polynomial, const Interval< Coefficient > &interval)

Counts the sign variations (i.e.

- template<typename C , typename O , typename P >

std::vector< std::pair< C, MultivariatePolynomial< C, O, P > > sos\_decomposition (const MultivariatePolynomial< C, O, P > &p, bool not\_trivial=false)

• template<typename C , typename O , typename P >

Multivariate Polynomial < C, O, P > S Polynomial (const Multivariate Polynomial < C, O, P > &p, const Multivariate Polynomial < C, O, P > &q)

Calculates the S-Polynomial of two polynomials.

template<typename C , typename O , typename P >

MultivariatePolynomial < C, O, P > squareFreePart (const MultivariatePolynomial < C, O, P > &polynomial)

• template<typename Coeff , EnableIf< is\_subset\_of\_rationals\_type< Coeff >> = dummy>

UnivariatePolynomial < Coeff > squareFreePart (const UnivariatePolynomial < Coeff > &p)

• template<typename Coeff >

 $std::vector < Univariate Polynomial < Coeff >> sturm\_sequence \ (const \ Univariate Polynomial < Coeff > \&p, const \ Univariate Polynomial < Coeff > \&q)$ 

Computes the sturm sequence of two polynomials.

• template<typename Coeff >

std::vector< UnivariatePolynomial< Coeff > > sturm\_sequence (const UnivariatePolynomial< Coeff > &p)

Computes the sturm sequence of a polynomial as defined at ?, page 333, example 22.

template<typename Coeff >

Coeff substitute (const Monomial &m, const std::map < Variable, Coeff > &substitutions)

Applies the given substitutions to a monomial.

template<typename Coeff >

Term < Coeff > substitute (const Term < Coeff > &t, const std::map < Variable, Coeff > &substitutions)

template<typename Coeff >

Term < Coeff > substitute (const Term < Coeff > &t, const std::map < Variable, Term < Coeff >> &substitutions)

template<typename C, typename O, typename P>
 void substitute\_inplace (MultivariatePolynomial< C, O, P > &p, Variable var, const MultivariatePolynomial<
 C, O, P > &value)

template<typename C, typename O, typename P>
 MultivariatePolynomial< C, O, P > substitute (const MultivariatePolynomial< C, O, P > &p, Variable var, const MultivariatePolynomial< C, O, P > &value)

template<typename C, typename O, typename P, typename S>
 MultivariatePolynomial< C, O, P > substitute (const MultivariatePolynomial< C, O, P > &p, const std::map
 Variable, S > &substitutions)

template<typename C, typename O, typename P>
 MultivariatePolynomial< C, O, P > substitute (const MultivariatePolynomial< C, O, P > &p, const std::map
 Variable, Term< C >> &substitutions)

template<typename C, typename O, typename P>
 MultivariatePolynomial< C, O, P > substitute (const MultivariatePolynomial< C, O, P > &p, const std::map
 Variable, MultivariatePolynomial< C, O, P >> &substitutions)

template < typename Coeff > void substitute\_inplace (UnivariatePolynomial < Coeff > &p, Variable var, const Coeff &value)

template<typename Coeff >
 UnivariatePolynomial< Coeff > substitute (const UnivariatePolynomial< Coeff > &p, Variable var, const Coeff &value)

template<typename Rational > void substitute\_inplace (MultivariatePolynomial< Rational > &p, Variable var, const Rational &r)

Substitutes a variable with a rational within a polynomial.

template<typename Poly , typename Rational > void substitute\_inplace (UnivariatePolynomial< Poly > &p, Variable var, const Rational &r)

template < typename C, typename O, typename P >
 UnivariatePolynomial < C > to\_univariate\_polynomial (const MultivariatePolynomial < C, O, P > &p)

Convert a univariate polynomial that is currently (mis)represented by a 'MultivariatePolynomial' into a more appropriate 'UnivariatePolynomial' representation.

template < typename C, typename O, typename P >
 UnivariatePolynomial < MultivariatePolynomial < C, O, P > > to\_univariate\_polynomial (const MultivariatePolynomial < C, O, P > &p, Variable v)

Convert a multivariate polynomial that is currently represented by a MultivariatePolynomial into a UnivariatePolynomial representation.

template<typename Coeff, typename Ordering, typename Policies >
 VarInfo< MultivariatePolynomial< Coeff, Ordering, Policies > > var\_info (const MultivariatePolynomial
 Coeff, Ordering, Policies > &poly, const Variable var, bool collect\_coeff=false)

template<typename Coeff, typename Ordering, typename Policies >
 VarsInfo< MultivariatePolynomial< Coeff, Ordering, Policies > > vars\_info (const MultivariatePolynomial
 Coeff, Ordering, Policies > &poly, bool collect\_coeff=false)

- template<typename Number, typename = std::enable\_if\_t<is\_number\_type<Number>::value>>
  const Number & branching\_point (const Number &n)
- template<typename Number, typename = std::enable\_if\_t<is\_number\_type<Number>::value>>
  Number sample\_above (const Number &n)

- template<typename Number, typename = std::enable\_if\_t<is\_number\_type<Number>::value>>
  Number sample\_below (const Number &n)
- template<typename Number, typename = std::enable\_if\_t<is\_number\_type<Number>::value>>
  Number sample\_between (const Number &lower, const Number &upper)
- template < typename Number, typename RAN, typename = std::enable\_if\_t < is\_ran\_type < RAN>::value>> Number is\_root\_of (const UnivariatePolynomial < Number > &p, const RAN &value)
- template<typename Number , typename RAN , typename = std::enable\_if\_t<is\_ran\_type<RAN>::value>> bool operator== (const RAN &lhs, const Number &rhs)
- template < typename Number , typename RAN , typename = std::enable\_if\_t < is\_ran\_type < RAN >::value >> bool operator! = (const RAN &lhs, const Number &rhs)
- template<typename Number, typename RAN, typename = std::enable\_if\_t<is\_ran\_type<RAN>::value>> bool operator<= (const RAN &lhs, const Number &rhs)</li>
- template < typename Number, typename RAN, typename = std::enable.if\_t < is\_ran\_type < RAN > ::value >> bool operator >= (const RAN &lhs, const Number &rhs)
- template < typename Number , typename RAN , typename = std::enable\_if\_t < is\_ran\_type < RAN >::value >> bool operator < (const RAN &lhs, const Number &rhs)</li>
- template<typename Number , typename RAN , typename = std::enable\_if\_t<is\_ran\_type<RAN>::value>> bool operator> (const RAN &lhs, const Number &rhs)
- template < typename Number , typename RAN , typename = std::enable\_if\_t < is\_ran\_type < RAN>::value>> bool operator == (const Number & lhs, const RAN & rhs)
- template<typename Number, typename RAN, typename = std::enable\_if\_t<is\_ran\_type<RAN>::value>> bool operator!= (const Number &lhs, const RAN &rhs)
- template<typename Number, typename RAN, typename = std::enable\_if\_t<is\_ran\_type<RAN>::value>> bool operator<= (const Number &lhs, const RAN &rhs)</li>
- template<typename Number , typename RAN , typename = std::enable\_if\_t<is\_ran\_type<RAN>::value>> bool operator>= (const Number &lhs, const RAN &rhs)
- template<typename Number, typename RAN, typename = std::enable\_if\_t<is\_ran\_type<RAN>::value>> bool operator< (const Number &lhs, const RAN &rhs)</li>
- template<typename Number, typename RAN, typename = std::enable\_if\_t<is\_ran\_type<RAN>::value>> bool operator> (const Number &lhs, const RAN &rhs)
- template < typename RAN, EnableIf < is\_ran\_type < RAN >> = dummy > bool operator == (const RAN &Ihs, const RAN &rhs)
- template < typename RAN, Enablelf < is\_ran\_type < RAN >> = dummy > bool operator! = (const RAN &lhs, const RAN &rhs)
- template < typename RAN, Enablelf < is\_ran\_type < RAN >> = dummy > bool operator <= (const RAN &lhs, const RAN &rhs)</li>
- template<typename RAN, EnableIf< is\_ran\_type< RAN >> = dummy> bool operator>= (const RAN &lhs, const RAN &rhs)
- template<typename RAN, EnableIf< is\_ran\_type< RAN >> = dummy> bool operator< (const RAN &Ihs, const RAN &rhs)</li>
- template < typename RAN, Enablelf < is\_ran\_type < RAN >> = dummy > bool operator > (const RAN &lhs, const RAN &rhs)
- template<typename T , std::enable\_if\_t< is\_ran\_type< T >::value, int > = 0>
  T convert (const T &r)
- template<typename Number >
   std::optional< IntRepRealAlgebraicNumber< Number > > evaluate (MultivariatePolynomial< Number > p,
   const Assignment< IntRepRealAlgebraicNumber< Number >> &m, bool refine\_model=true)

Evaluate the given polynomial with the given values for the variables.

- template<typename Number >
   boost::tribool evaluate (const BasicConstraint< MultivariatePolynomial< Number >> &c, const
   Assignment< IntRepRealAlgebraicNumber< Number >> &m, bool refine\_model=true, bool use\_root\_
   bounds=true)
- template < typename Coeff, typename Ordering, typename Policies >
   auto evaluate (const ContextPolynomial < Coeff, Ordering, Policies > &p, const Assignment < typename
   ContextPolynomial < Coeff, Ordering, Policies > ::RootType > &a)

```
    template<typename Coeff , typename Ordering , typename Policies >

  auto evaluate (const BasicConstraint< ContextPolynomial< Coeff, Ordering, Policies >> &p, const
  Assignment < typename ContextPolynomial < Coeff, Ordering, Policies >::RootType > &a)
template<typename Number >
  Number branching_point (const IntRepRealAlgebraicNumber < Number > &n)
• template<typename Number >
  Number sample_above (const IntRepRealAlgebraicNumber < Number > &n)

    template<typename Number >

  Number sample_below (const IntRepRealAlgebraicNumber < Number > &n)

    template<typename Number >

  Number sample_between (const IntRepRealAlgebraicNumber < Number > &lower, const IntRepRealAlgebraicNumber <
  Number > &upper)

    template<typename Number >

  Number sample_between (const IntRepRealAlgebraicNumber < Number > &lower, const Number &upper)

    template<typename Number >

  Number sample_between (const Number &lower, const IntRepRealAlgebraicNumber < Number > &upper)

    template < typename Number >

  Number floor (const IntRepRealAlgebraicNumber < Number > &n)
template<typename Number >
  Number ceil (const IntRepRealAlgebraicNumber < Number > &n)
template<typename Number >
  bool is_zero (const IntRepRealAlgebraicNumber < Number > &n)

    template<typename Number >

  bool is_integer (const IntRepRealAlgebraicNumber < Number > &n)

    template<typename Number >

  Number integer_below (const IntRepRealAlgebraicNumber < Number > &n)

    template<typename Number >

  static IntRepRealAlgebraicNumber < Number > abs (const IntRepRealAlgebraicNumber < Number > &n)

    template<typename Number >

  std::size_t bitsize (const IntRepRealAlgebraicNumber < Number > &n)

    template < typename Number >

  Sign sgn (const IntRepRealAlgebraicNumber < Number > &n)
template<typename Number >
  Sign sgn (const IntRepRealAlgebraicNumber < Number > &n, const UnivariatePolynomial < Number > &p)
\bullet \ \ \text{template}{<} \text{typename Number}{>}
  bool contained_in (const IntRepRealAlgebraicNumber < Number > &n, const Interval < Number > &i)
template<typename Number >
  bool compare (const IntRepRealAlgebraicNumber < Number > &lhs, const IntRepRealAlgebraicNumber <
  Number > &rhs, const Relation relation)

    template<typename Number >

  bool compare (const IntRepRealAlgebraicNumber < Number > &lhs, const Number &rhs, const Relation
  relation)
\bullet \ \ \text{template}{<} \text{typename Num} >
  std::ostream & operator<< (std::ostream &os, const IntRepRealAlgebraicNumber< Num > &ran)
• template<typename Coeff, typename Number = typename UnderlyingNumberType<Coeff>::type, EnableIf< std::is_same< Coeff,
  Number >> = dummy>
  RealRootsResult< IntRepRealAlgebraicNumber< Number > > real_roots (const UnivariatePolynomial<
  Coeff > &polynomial, const Interval < Number > &interval = Interval < Number >::unbounded_interval())
```

Find all real roots of a univariate 'polynomial' with numeric coefficients within a given 'interval'.

template<typename Coeff, typename Number >
 RealRootsResult
 IntRepRealAlgebraicNumber
 Number > real\_roots (const UnivariatePolynomial
 Coeff > &poly, const Assignment
 IntRepRealAlgebraicNumber
 Number >> &varToRANMap, const Interval
 Number > &interval=Interval
 Number >::unbounded\_interval())

Replace all variables except one of the multivariate polynomial 'p' by numbers as given in the mapping 'm', which creates a univariate polynomial, and return all roots of that created polynomial.

 template<typename Coeff , typename Ordering , typename Policies > auto real\_roots (const ContextPolynomial < Coeff, Ordering, Policies > &p, const Assignment < typename ContextPolynomial < Coeff, Ordering, Policies >::RootType > &a) • template<typename Number > Number branching\_point (const RealAlgebraicNumberThom < Number > &n) template<typename Number > Number evaluate (const MultivariatePolynomial < Number > &p, std::map < Variable, RealAlgebraicNumberThom < Number >> &m) template<typename Number , typename Poly > bool evaluate (const BasicConstraint< Poly > &c, std::map< Variable, RealAlgebraicNumberThom< Number >> &m) template<typename Number > RealAlgebraicNumberThom< Number > abs (const RealAlgebraicNumberThom< Number > &n) template<typename Number > RealAlgebraicNumberThom< Number > sample\_above (const RealAlgebraicNumberThom< Number > &n) template<typename Number > RealAlgebraicNumberThom< Number > sample\_below (const RealAlgebraicNumberThom< Number > &n) template<typename Number > RealAlgebraicNumberThom < Number > sample\_between (const RealAlgebraicNumberThom < Number > &lower, const RealAlgebraicNumberThom< Number > &upper) template<typename Number > Number sample\_between (const RealAlgebraicNumberThom< Number > &lower, const Number &upper) template<typename Number > Number sample\_between (const Number &lower, const RealAlgebraicNumberThom< Number > &upper) template<typename Number > Number floor (const RealAlgebraicNumberThom< Number > &n) template<typename Number > Number ceil (const RealAlgebraicNumberThom< Number > &n) template<typename Number > bool operator== (const RealAlgebraicNumberThom< Number > &lhs, const RealAlgebraicNumberThom< Number > &rhs) template<typename Number > bool operator== (const RealAlgebraicNumberThom< Number > &lhs, const Number &rhs) template<typename Number > bool operator== (const Number &lhs, const RealAlgebraicNumberThom< Number > &rhs) template<typename Number > bool operator< (const RealAlgebraicNumberThom< Number > &lhs, const RealAlgebraicNumberThom< Number > &rhs) template<typename Number > bool operator< (const RealAlgebraicNumberThom< Number > &lhs, const Number &rhs) template<typename Number > bool operator< (const Number &lhs, const RealAlgebraicNumberThom< Number > &rhs) • template<typename Num>std::ostream & operator << (std::ostream &os, const RealAlgebraicNumberThom < Num > &rhs) template<typename N > std::ostream & operator<< (std::ostream &os, const SignDetermination< N > &rhs) template<typename Coeff > std::vector< Coeff > newtonSums (const std::vector< Coeff > &newtonSums) template<typename Coeff > void printMatrix (const CoeffMatrix < Coeff > &m) template<typename Coeff > std::vector < Coeff > charPol (const CoeffMatrix < Coeff > &m) template<typename C > std::ostream & operator<< (std::ostream &o, const MultiplicationTable< C > &table) template<typename Number > int multivariateTarskiQuery (const MultivariatePolynomial < Number > &Q, const MultiplicationTable < Number > &table)

```
    template<typename Number >

  Sign signAtMinusInf (const UnivariatePolynomial < Number > &p)
template<typename Number >
  Sign signAtPlusInf (const UnivariatePolynomial < Number > &p)

    template<typename Number >

  int univariateTarskiQuery (const UnivariatePolynomial < Number > &p, const UnivariatePolynomial < Number
  > &q, const UnivariatePolynomial < Number > &der_q)
template<typename Number >
  int univariateTarskiQuery (const UnivariatePolynomial < Number > &p, const UnivariatePolynomial < Number
  > &q)

    template<typename N >

  bool operator< (const ThomEncoding< N > &lhs, const ThomEncoding< N > &rhs)

    template<typename N >

  bool operator<= (const ThomEncoding< N > &lhs, const ThomEncoding< N > &rhs)

    template<typename N >

  bool operator> (const ThomEncoding< N > &lhs, const ThomEncoding< N > &rhs)

    template<typename N >

  bool operator>= (const ThomEncoding < N > &lhs, const ThomEncoding < N > &rhs)

    template<typename N >

  bool operator== (const ThomEncoding < N > &Ihs, const ThomEncoding < N > &rhs)

    template<typename N >

  bool operator!= (const ThomEncoding < N >  &lhs, const ThomEncoding < N >  &rhs)

    template<typename N >

  bool operator< (const ThomEncoding< N > &lhs, const N &rhs)

    template<typename N >

  bool operator<= (const ThomEncoding< N > &lhs, const N &rhs)

    template<typename N >

  bool operator> (const ThomEncoding< N > &lhs, const N &rhs)

    template<typename N >

  bool operator>= (const ThomEncoding < N > &Ihs, const N &rhs)

    template<typename N >

  bool operator== (const ThomEncoding < N > &Ihs, const N &rhs)

    template<typename N >

  bool operator!= (const ThomEncoding< N > &lhs, const N &rhs)
• template<typename N >
  bool operator< (const N &lhs, const ThomEncoding< N > &rhs)

    template<typename N >

  bool operator <= (const N &lhs, const ThomEncoding < N > &rhs)

    template<typename N >

  bool operator> (const N &lhs, const ThomEncoding< N > &rhs)
 template<typename N >
  bool operator>= (const N &lhs, const ThomEncoding < N > &rhs)

    template<typename N >

  bool operator== (const N &lhs, const ThomEncoding < N > &rhs)

    template<typename N >

  bool operator!= (const N &lhs, const ThomEncoding < N > &rhs)

    template<typename N >

  ThomEncoding< N > operator+ (const N &lhs, const ThomEncoding< N > &rhs)

    template<typename N >

  std::ostream & operator<< (std::ostream &os, const ThomEncoding< N > &rhs)
template<typename Number >
  RealAlgebraicNumber < Number > evaluateTE (const MultivariatePolynomial < Number > &p, std::map <
  Variable, RealAlgebraicNumber < Number >> &m)

    template<typename Number >

  std::list< ThomEncoding< Number > > realRootsThom (const MultivariatePolynomial< Number > &p,
  Variable::Arg mainVar, std::shared_ptr< ThomEncoding< Number >> point_ptr, const Interval< Number
  > &interval=Interval < Number >::unbounded_interval())
```

```
• template<typename Number >
  std::list< ThomEncoding< Number > > realRootsThom (const MultivariatePolynomial< Number > &p,
  Variable::Arg mainVar, const std::map< Variable, ThomEncoding< Number >> &m={}, const Interval<
  Number > &interval=Interval < Number >::unbounded_interval())
• template<typename Coeff , typename Number >
  std::list< RealAlgebraicNumber < Number > > realRootsThom (const UnivariatePolynomial < Coeff > &p,
  const std::map < Variable, RealAlgebraicNumber < Number >> &m, const Interval < Number > &interval)
template<typename Number >
  std::list< MultivariatePolynomial< Number > > der (const MultivariatePolynomial< Number > &p,
  Variable::Arg var, uint from, uint upto)
template<typename Poly >
  std::pair< typename SqrtEx< Poly >::Rational, bool > evaluate (const SqrtEx< Poly > &sqrt_ex, const
  std::map< Variable, typename SqrtEx< Poly >::Rational > &eval_map, int rounding)
     Evaluates the square root expression.
• template<typename Poly >
  void variables (const SqrtEx< Poly > &ex, carlVariables &vars)

    template<typename Poly >

  SqrtEx< Poly > substitute (const SqrtEx< Poly > &sqrt_ex, const std::map< Variable, typename SqrtEx<
  Poly >::Rational > &eval_map)
template<typename Poly >
  SqrtEx< Poly > substitute (const Poly &_substituteIn, const carl::Variable _varToSubstitute, const SqrtEx<
  Poly > &_substituteBy)
     Substitutes a variable in an expression by a square root expression, which results in a square root expression.
template<typename TT >
  std::ostream & operator << (std::ostream &os, const tree < TT > &tree)

    template<class E , bool FI>

  std::ostream & operator << (std::ostream &out, const CompactTree < E, FI > &tree)

    template<typename T , class I >

  bool operator== (const TypeInfoPair< T, I > &_tipA, const TypeInfoPair< T, I > &_tipB)
template<typename T >
  bool returnFalse (const T &, const T &)
• template<typename T >
  void doNothing (const T &, const T &)
• template<typename Tuple1 , typename Tuple2 >
  auto tuple_cat (Tuple1 &&t1, Tuple2 &&t2)
• template<typename Tuple >
  auto tuple_tail (Tuple &&t)
     Returns a new tuple containing everything but the first element.

    template<typename F, typename Tuple >

  auto tuple_apply (F &&f, Tuple &&t)
     Invokes a callable object f on a tuple of arguments.
• template<typename F , typename Tuple >
  auto tuple_foreach (F &&f, Tuple &&t)
     Invokes a callable object f on every element of a tuple and returns a tuple containing the results.

    template<typename Tuple , typename T , typename F >

  T tuple_accumulate (Tuple &&t, T &&init, F &&f)
     Implements a functional fold (similar to std::accumulate) for std::tuple.

    template<typename Coeff , typename Subst >

  Subst evaluate (const FactorizedPolynomial < Coeff > &p, const std::map < Variable, Subst > &substitutions)
     Like substitute, but expects substitutions for all variables.
• template<typename P , typename Numeric >
  Interval < Numeric > evaluate (const FactorizedPolynomial < P > &p, const std::map < Variable, Interval <
  Numeric >> &map)

    template<typename P >

  bool is_one (const FactorizedPolynomial < P > &fp)
```

 template<typename P > bool is\_zero (const FactorizedPolynomial < P > &fp) • template<typename P > P computePolynomial (const FactorizedPolynomial < P > &\_fpoly) Obtains the polynomial (representation) of this factorized polynomial. template<typename P > std::ostream & operator << (std::ostream &\_out, const FactorizedPolynomial < P > &\_fpoly) Prints the factorization representation of the given factorized polynomial on the given output stream. • template<typename P > std::string factorizationToString (const Factorization< P > &\_factorization, bool \_infix=true, bool \_friendly ← VarNames=true) template<typename P > std::ostream & operator<< (std::ostream &\_out, const Factorization< P > &\_factorization) template<typename P > bool factorizationsEqual (const Factorization< P > & factorizationA, const Factorization< P > & ← factorizationB) template<typename P > P computePolynomial (const PolynomialFactorizationPair< P > &\_pfPair) Compute the polynomial from the given polynomial-factorization pair. • template<typename Pol , bool AS> RationalFunction< Pol, AS > operator+ (const RationalFunction< Pol, AS > &lhs, const RationalFunction< Pol. AS > &rhs) template<typename Pol , bool AS> RationalFunction < Pol, AS > operator+ (const RationalFunction < Pol, AS > &lhs, const Pol &rhs) template<typename Pol , bool AS, Disablelf< needs\_cache\_type< Pol >> = dummy> RationalFunction < Pol, AS > operator+ (const RationalFunction < Pol, AS > &lhs, const Term < typename Pol::CoeffType > &rhs) template<typename Pol , bool AS, Disablelf< needs\_cache\_type< Pol >> = dummy> RationalFunction < Pol, AS > operator+ (const RationalFunction < Pol, AS > &lhs, const Monomial::Arg &rhs) template<typename Pol, bool AS, Disablelf< needs\_cache\_type< Pol >> = dummy> RationalFunction < Pol, AS > operator+ (const RationalFunction < Pol, AS > &lhs, Variable rhs) template<typename Pol , bool AS> RationalFunction< Pol, AS > operator+ (const RationalFunction< Pol, AS > &lhs, const typename Pol:: ← CoeffType &rhs) template<typename Pol , bool AS> RationalFunction < Pol, AS > operator- (const RationalFunction < Pol, AS > &lhs) template<typename Pol , bool AS> RationalFunction < Pol, AS > operator- (const RationalFunction < Pol, AS > &lhs, const RationalFunction < Pol, AS > &rhs) • template<typename Pol , bool AS> RationalFunction < Pol, AS > operator- (const RationalFunction < Pol, AS > &lhs, const Pol &rhs) template<typename Pol , bool AS, Disablelf< needs\_cache\_type< Pol >> = dummy> RationalFunction< Pol, AS > operator- (const RationalFunction< Pol, AS > &lhs, const Term< typename Pol::CoeffType > &rhs) template<typename Pol , bool AS, Disablelf< needs\_cache\_type< Pol >> = dummy> RationalFunction < Pol, AS > operator- (const RationalFunction < Pol, AS > &lhs, const Monomial::Arg &rhs) template<typename Pol , bool AS, Disablelf< needs\_cache\_type< Pol >> = dummy> RationalFunction< Pol, AS > operator- (const RationalFunction< Pol, AS > &lhs, Variable rhs) template<typename Pol , bool AS> RationalFunction< Pol, AS > operator- (const RationalFunction< Pol, AS > &lhs, const typename Pol::←

Pol, AS > &rhs)

• template<typename Pol, bool AS>
RationalFunction
 Pol, AS > operator\* (const RationalFunction
 Pol, AS > &lhs, const Pol &rhs)

RationalFunction < Pol, AS > operator\* (const RationalFunction < Pol, AS > &lhs, const RationalFunction <

CoeffType &rhs)

template<typename Pol , bool AS>

```
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    template<typename Pol , bool AS, Disablelf< needs_cache_type< Pol >> = dummy>

      RationalFunction< Pol, AS > operator* (const RationalFunction< Pol, AS > &lhs, const Term< typename
      Pol::CoeffType > &rhs)
    • template<typename Pol , bool AS, DisableIf< needs_cache_type< Pol >> = dummy>
      RationalFunction < Pol, AS > operator* (const RationalFunction < Pol, AS > &lhs, const Monomial::Arg &rhs)

    template<typename Pol , bool AS, Disablelf< needs_cache_type< Pol >> = dummy>

      RationalFunction < Pol, AS > operator* (const RationalFunction < Pol, AS > &lhs, Variable rhs)

    template<typename Pol , bool AS>

      RationalFunction< Pol, AS > operator* (const RationalFunction< Pol, AS > &lhs, const typename Pol::←
      CoeffType &rhs)

    template<typename Pol , bool AS>

      RationalFunction < Pol, AS > operator* (const typename Pol::CoeffType &lhs, const RationalFunction < Pol,
      AS > &rhs)

    template<typename Pol , bool AS>

      RationalFunction < Pol, AS > operator* (const RationalFunction < Pol, AS > &lhs, carl::sint rhs)

    template<typename Pol , bool AS>

      RationalFunction < Pol, AS > operator* (carl::sint lhs, const RationalFunction < Pol, AS > &rhs)
    • template<typename Pol , bool AS>
      RationalFunction < Pol, AS > operator/ (const RationalFunction < Pol, AS > &lhs, const RationalFunction <
      Pol, AS > &rhs)

    template<typename Pol , bool AS>

      RationalFunction < Pol, AS > operator/ (const RationalFunction < Pol, AS > &lhs, const Pol &rhs)

    template<typename Pol , bool AS, Disablelf< needs_cache_type< Pol >> = dummy>

      RationalFunction< Pol, AS > operator/ (const RationalFunction< Pol, AS > &lhs, const Term< typename
      Pol::CoeffType > &rhs)

    template<typename Pol , bool AS, DisableIf< needs_cache_type< Pol >> = dummy>

      RationalFunction < Pol, AS > operator/ (const RationalFunction < Pol, AS > &lhs, const Monomial::Arg &rhs)
```

template<typename Pol , bool AS, Disablelf< needs\_cache\_type< Pol >> = dummy>

template<typename Pol , bool AS>

• template<typename Pol , bool AS>

template<typename Pol , bool AS>

• template<typename Pol, bool AS>

FactorizedPolynomial < P > &value)

template<typename P , typename Subs >

Subs > &substitutions)

template<typename P >

Replace the given variable by the given value.

FactorizedPolynomial < P >> &substitutions)

Replace all variables by a value given in their map.

Replace all variables by a value given in their map.

Replace all variables by a value given in their map.

bool operator== (const Constraint < P > &lhs, const Constraint < P > &rhs)

CoeffType &rhs)

template<typename P >

template<typename P >

• template<typename P >

RationalFunction < Pol, AS > operator/ (const RationalFunction < Pol, AS > &lhs, Variable rhs)

RationalFunction< Pol, AS > operator/ (const RationalFunction< Pol, AS > &lhs, const typename Pol::←

RationalFunction < Pol, AS > operator/ (const RationalFunction < Pol, AS > &lhs, unsigned long rhs)

bool operator!= (const RationalFunction < Pol, AS > &lhs, const RationalFunction < Pol, AS > &rhs)

FactorizedPolynomial < P > substitute (const FactorizedPolynomial < P > &p, Variable var, const

FactorizedPolynomial < P > substitute (const FactorizedPolynomial < P > &p, const std::map < Variable,

FactorizedPolynomial < P > substitute (const FactorizedPolynomial < P > &p, const std::map < Variable,

FactorizedPolynomial < P > substitute (const FactorizedPolynomial < P > &p, const std::map < Variable,

FactorizedPolynomial < P >> &substitutions, const std::map < Variable, P > &substitutionsAsP)

RationalFunction < Pol, AS > pow (unsigned exp, const RationalFunction < Pol, AS > &rf)

```
    template<typename P >

  bool operator!= (const Constraint < P > &lhs, const Constraint < P > &rhs)
template<typename P >
  bool operator< (const Constraint< P > &lhs, const Constraint< P > &rhs)

    template<typename P >

  bool operator <= (const Constraint < P > &lhs, const Constraint < P > &rhs)

    template<typename P >

  bool operator> (const Constraint< P > &Ihs, const Constraint< P > &rhs)
template<typename P >
  bool operator>= (const Constraint< P > &lhs, const Constraint< P > &rhs)

    template<typename Poly >

  std::ostream & operator << (std::ostream &os, const Constraint < Poly > &c)
     Prints the given constraint on the given stream.

    template<typename Pol >

  void variables (const Constraint < Pol > &c, carlVariables &vars)

    template<typename Pol >

  std::optional < std::pair < Variable, Pol > > get_substitution (const Constraint < Pol > &c, bool _ \Leftarrow
  negated=false, Variable _exclude=carl::Variable::NO_VARIABLE)

    template<typename Pol >

  auto get_assignment (const Constraint< Pol > &c)

    template<typename Pol >

  auto compare (const Constraint < Pol > &c1, const Constraint < Pol > &c2)

    template<typename Pol >

  auto satisfied_by (const Constraint < Pol > &c, const Assignment < typename Pol::NumberType > &a)

    template<typename Pol >

  bool is_bound (const Constraint < Pol > &constr, bool negated=false)

    template<typename Pol >

  bool is_lower_bound (const Constraint < Pol > &constr)

    template<typename Pol >

  bool is_upper_bound (const Constraint < Pol > &constr)

    bool operator<= (const Condition &lhs, const Condition &rhs)</li>

      Check whether the bits of one condition are always set if the corresponding bit of another condition is set.

    template<typename P >

  std::ostream & operator<< (std::ostream &os, const Formula< P > &f)
      The output operator of a formula.

    std::string formulaTypeToString (FormulaType _type)

    std::ostream & operator<< (std::ostream &os, FormulaType t)</li>

    template<typename Pol >

  std::ostream & operator<< (std::ostream &os, const FormulaContent< Pol > &f)
      The output operator of a formula.

    template<typename Pol >

  std::ostream & operator << (std::ostream &os, const FormulaContent < Pol > *fc)

    template<typename Pol >

  std::size_t hash_value (const carl::FormulaContent< Pol > &content)

    template<typename Poly >

  Formula < Poly > to_cnf (const Formula < Poly > &f, bool keep_constraints=true, bool simplify_ <--
  combinations=false, bool tseitin_equivalence=true)
     Converts the given formula to CNF.

    template<typename Pol >

  size_t complexity (const Formula < Pol > &f)

    template<typename Pol >

  Formula < Pol > addConstraintBound (ConstraintBounds < Pol > &_constraintBounds, const Formula < Pol
  > &_constraint, bool _inConjunction)
```

Adds the bound to the bounds of the polynomial specified by this constraint.

template<typename Pol >

bool swapConstraintBounds (ConstraintBounds < Pol > &\_constraintBounds, Formulas < Pol > &\_into $\leftarrow$  Formulas, bool \_inConjunction)

Stores for every polynomial for which we determined bounds for given constraints a minimal set of constraints representing these bounds into the given set of sub-formulas of a conjunction (\_inConjunction == true) or disjunction (\_inConjunction == false) to construct.

template<typename Pol >

Formula < Pol > resolve\_negation (const Formula < Pol > &f, bool \_keepConstraint=true)

Resolves the outermost negation of this formula.

template<typename Poly >

Formula < Poly > to\_nnf (const Formula < Poly > &formula)

template<typename Poly >

Formula < Poly > toQF (std::vector < Variables > &variables, unsigned level=0, bool negated=false)

Transforms this formula to its quantifier free equivalent.

• template<typename Pol , typename Source , typename Target >

Formula < Pol > substitute (const Formula < Pol > &formula, const Source &source, const Target &target)

template<typename Pol >

Formula < Pol > substitute (const Formula < Pol > &formula, const std::map < Formula < Pol >, Formula < Pol >> &replacements)

• template<typename Pol >

Formula < Pol > substitute (const Formula < Pol > &formula, const std::map < Variable, typename Formula < Pol > ::PolynomialType > &replacements)

template<typename Pol >

Formula < Pol > substitute (const Formula < Pol > &formula, const std::map < BVVariable, BVTerm > &replacements)

template<typename Pol >

Formula < Pol > substitute (const Formula < Pol > &formula, const std::map < UVariable, UFInstance > &replacements)

• template<typename Pol >

void variables (const Formula < Pol > &f, carlVariables &vars)

 $\bullet \;\; {\sf template}{<} {\sf typename} \; {\sf Pol} >$ 

 $void\ uninterpreted\_functions\ (const\ Formula < Pol > \&f,\ std::set < UninterpretedFunction > \&ufs)$ 

template<typename Pol >

void uninterpreted\_variables (const Formula < Pol > &f, std::set < UVariable > &uvs)

template<typename Pol >

 $void \ bitvector\_variables \ (const \ Formula < Pol > \&f, \ std::set < BVVariable > \&bvvs)$ 

• template<typename Pol >

void arithmetic\_constraints (const Formula < Pol > &f, std::vector < Constraint < Pol >> &constraints)

Collects all constraint occurring in this formula.

• template<typename Pol>

void arithmetic\_constraints (const Formula < Pol > &f, std::vector < Formula < Pol >> &constraints)

Collects all constraint occurring in this formula.

• template<typename Pol , typename Visitor >

void visit (const Formula < Pol > &formula, Visitor func)

Recursively calls func on every subformula.

• template<typename Pol , typename Visitor >

Formula < Pol > visit\_result (const Formula < Pol > &formula, Visitor func)

Recursively calls func on every subformula and return a new formula.

- std::ostream & operator<< (std::ostream &os, const Logic &I)</li>
- template<typename Rational , typename Poly >

bool getRationalAssignmentsFromModel (const Model < Rational, Poly > &\_model, std::map < Variable, Rational > &\_rationalAssigns)

Obtains all assignments which can be transformed to rationals and stores them in the passed map.

template<typename Rational , typename Poly >

 $unsigned \ satisfies \ (const \ Model < \ Rational, \ Poly > \&\_assignment, \ const \ Formula < Poly > \&\_formula)$ 

```
    template<typename Rational , typename Poly >

  bool isPartOf (const std::map < Variable, Rational > & assignment, const Model < Rational, Poly > & model)
• template<typename Rational , typename Poly >
  unsigned satisfies (const Model< Rational, Poly > &_model, const std::map< Variable, Rational > &_←
  assignment, const std::map< BVVariable, BVTerm > &bvAssigns, const Formula< Poly > & formula)

    template<typename Rational , typename Poly >

  void getDefaultModel (Model < Rational, Poly > &_defaultModel, const UEquality &_constraint, bool _←
  overwrite=true, size_t _seed=0)

    template<typename Rational , typename Poly >

  void getDefaultModel (Model< Rational, Poly > &_defaultModel, const BVTerm &_constraint, bool _←
  overwrite=true, size_t _seed=0)

    template<typename Rational , typename Poly >

  void getDefaultModel (Model < Rational, Poly > &_defaultModel, const Constraint < Poly > &_constraint, bool
  _overwrite=true, size_t _seed=0)

    template<typename Rational , typename Poly >

  void getDefaultModel (Model < Rational, Poly > &_defaultModel, const Formula < Poly > &_formula, bool
  _overwrite=true, size_t _seed=0)
• template<typename Rational , typename Poly >
  Formula < Poly > representingFormula (const ModelVariable &mv, const Model < Rational, Poly > &model)

    template<typename Rational , typename Poly >

  std::optional < Assignment < typename Poly::RootType > > get_ran_assignment (const carlVariables &vars,
  const Model < Rational, Poly > & model)

    template<typename Rational , typename Poly >

  Assignment< typename Poly::RootType > get_ran_assignment (const Model< Rational, Poly > &model)
ullet template<typename T , typename Rational , typename Poly >
  T substitute (const T &t, const Model < Rational, Poly > &m)
     Substitutes a model into an expression t.
ullet template<typename T , typename Rational , typename Poly >
  ModelValue < Rational, Poly > evaluate (const T &t, const Model < Rational, Poly > &m)
      Evaluates a given expression t over a model.
• template<typename T , typename Rational , typename Poly >
  unsigned satisfied_by (const T &t, const Model < Rational, Poly > &m)

    template<typename Rational , typename Poly >

  void substitute_inplace (BVTerm &bvt, const Model < Rational, Poly > &m)
     Substitutes all variables from a model within a bitvector term.
• template<typename Rational , typename Poly >
  void substitute_inplace (BVConstraint &bvc, const Model < Rational, Poly > &m)
     Substitutes all variables from a model within a bitvector constraint.

    template<typename Rational , typename Poly >

  void evaluate_inplace (ModelValue < Rational, Poly > &res, BVTerm &bvt, const Model < Rational, Poly >
  &m)
     Evaluates a bitvector term to a ModelValue over a Model.
ullet template<typename Rational , typename Poly >
  void evaluate_inplace (ModelValue < Rational, Poly > &res, BVConstraint &bvc, const Model < Rational, Poly
  > &m)
      Evaluates a bitvector constraint to a ModelValue over a Model.

    template<typename Rational , typename Poly >

  void substitute_inplace (Constraint< Poly > &c, const Model< Rational, Poly > &m)
      Substitutes all variables from a model within a constraint.

    template<typename Rational , typename Poly >

  void evaluate_inplace (ModelValue < Rational, Poly > &res, Constraint < Poly > &c, const Model < Rational,
  Poly > \&m)
     Evaluates a constraint to a ModelValue over a Model.
```

template<typename Rational , typename Poly >

void substitute\_inplace (Formula< Poly > &f, const Model< Rational, Poly > &m)

Substitutes all variables from a model within a formula.

template<typename Rational, typename Poly > void evaluate\_inplace (ModelValue< Rational, Poly > &res, Formula< Poly > &f, const Model< Rational, Poly > &m)

Evaluates a formula to a ModelValue over a Model.

- template<typename Rational , typename Poly >

void substitute\_inplace (MultivariateRoot< Poly > &mvr, const Model< Rational, Poly > &m)

Substitutes all variables from a model within a MultivariateRoot.

template<typename Rational , typename Poly >

void evaluate\_inplace (ModelValue< Rational, Poly > &res, MultivariateRoot< Poly > &mvr, const Model< Rational, Poly > &m)

Evaluates a MultivariateRoot to a ModelValue over a Model.

template < typename Rational, typename Poly, typename ModelPoly > void substitute\_inplace (Poly &p, const Model < Rational, ModelPoly > &m)

Substitutes all variables from a model within a polynomial.

• template<typename Rational , typename Poly >

void evaluate\_inplace (ModelValue< Rational, Poly > &res, Poly &p, const Model< Rational, Poly > &m)

Evaluates a polynomial to a ModelValue over a Model.

• template<typename Rational , typename Poly >

void evaluate\_inplace (ModelValue< Rational, Poly > &res, const UVariable &uv, const Model< Rational, Poly > &m)

Evaluates a uninterpreted variable to a ModelValue over a Model.

• template<typename Rational , typename Poly >

void evaluate\_inplace (ModelValue< Rational, Poly > &res, const UFInstance &ufi, const Model< Rational, Poly > &m)

Evaluates a uninterpreted function instance to a ModelValue over a Model.

• template<typename Rational , typename Poly >

void evaluate\_inplace (ModelValue< Rational, Poly > &res, const UEquality &ue, const Model< Rational, Poly > &m)

Evaluates a uninterpreted variable to a ModelValue over a Model.

- template<typename Rational , typename Poly >

std::ostream & operator<< (std::ostream &os, const Model< Rational, Poly > &model)

• template<typename Rational , typename Poly >

std::ostream & operator << (std::ostream &os, const ModelSubstitution < Rational, Poly > &ms)

• template<typename Rational , typename Poly >

std::ostream & operator<< (std::ostream &os, const ModelSubstitutionPtr< Rational, Poly > &ms)

 $\bullet \ \ \text{template} < \text{typename Rational , typename Poly , typename Substitution , typename...} \ \text{Args} >$ 

ModelValue < Rational, Poly > createSubstitution (Args &&... args)

template<typename Rational , typename Poly , typename Substitution , typename... Args>
 ModelSubstitutionPtr< Rational, Poly > createSubstitutionPtr (Args &&... args)

template < typename Rational , typename Poly >

ModelValue < Rational, Poly > createSubstitution (const MultivariateRoot < Poly > &mr)

- bool operator== (InfinityValue Ihs, InfinityValue rhs)
- std::ostream & operator<< (std::ostream &os, const InfinityValue &iv)
- template<typename Rational , typename Poly >

bool operator== (const ModelValue < Rational, Poly > &lhs, const ModelValue < Rational, Poly > &rhs)

Check if two Assignments are equal.

• template<typename Rational , typename Poly >

 $bool\ operator < (const\ Model Value < Rational,\ Poly > \&lhs,\ const\ Model Value < Rational,\ Poly > \&rhs)$ 

• template<typename R , typename P >

std::ostream & operator<< (std::ostream &os, const ModelValue< R, P > &mv)

• bool operator== (const ModelVariable &lhs, const ModelVariable &rhs)

Return true if lhs is equal to rhs.

bool operator< (const ModelVariable &lhs, const ModelVariable &rhs)</li>

Return true if Ihs is smaller than rhs.

- std::ostream & operator<< (std::ostream &os, const ModelVariable &mv)</li>
- std::ostream & operator<< (std::ostream &os, const SortValue &sv)</li>

Prints the given sort value on the given output stream.

bool operator== (const SortValue &lhs, const SortValue &rhs)

Compares two sort values for equality.

bool operator< (const SortValue &lhs, const SortValue &rhs)</li>

Orders two sort values.

#### **Multiplication operators**

Monomial::Arg operator\* (const Monomial::Arg &lhs, const Monomial::Arg &rhs)

Perform a multiplication involving a monomial.

• Monomial::Arg operator\* (const Monomial::Arg &lhs, Variable rhs)

Perform a multiplication involving a monomial.

• Monomial::Arg operator\* (Variable Ihs, const Monomial::Arg &rhs)

Perform a multiplication involving a monomial.

Monomial::Arg operator\* (Variable lhs, Variable rhs)

Perform a multiplication involving a monomial.

template<typename Coeff >

```
Term < Coeff > operator* (Term < Coeff > lhs, const Term < Coeff > &rhs)
```

Perform a multiplication involving a term.

template<typename Coeff >

```
Term < Coeff > operator* (Term < Coeff > lhs, const Monomial::Arg &rhs)
```

Perform a multiplication involving a term.

• template<typename Coeff >

```
Term< Coeff > operator* (Term< Coeff > lhs, Variable rhs)
```

Perform a multiplication involving a term.

template<typename Coeff >

```
Term < Coeff > operator* (Term < Coeff > lhs, const Coeff &rhs)
```

Perform a multiplication involving a term.

template<typename Coeff >

```
Term < Coeff > operator* (const Monomial::Arg &lhs, const Term < Coeff > &rhs)
```

Perform a multiplication involving a term.

template<typename Coeff , EnableIf< carl::is\_number\_type< Coeff >> = dummy>

```
Term < Coeff > operator* (const Monomial::Arg &lhs, const Coeff &rhs)
```

Perform a multiplication involving a term.

• template<typename Coeff >

```
Term < Coeff > operator* (Variable lhs, const Term < Coeff > &rhs)
```

Perform a multiplication involving a term.

template<typename Coeff >

```
Term < Coeff > operator* (Variable lhs, const Coeff &rhs)
```

Perform a multiplication involving a term.

• template<typename Coeff >

```
Term < Coeff > operator* (const Coeff &lhs, const Term < Coeff > &rhs)
```

Perform a multiplication involving a term.

template<typename Coeff , EnableIf< carl::is\_number\_type< Coeff >> = dummy>

```
Term < Coeff > operator* (const Coeff &lhs, const Monomial::Arg &rhs)
```

Perform a multiplication involving a term.

template<typename Coeff >

```
Term < Coeff > operator* (const Coeff &lhs, Variable rhs)
```

Perform a multiplication involving a term.

• template<typename Coeff , EnableIf< carl::is\_subset\_of\_rationals\_type< Coeff >> = dummy>

```
Term < Coeff > operator/ (const Term < Coeff > &lhs, const Coeff &rhs)
```

Perform a multiplication involving a term.

template<typename Coeff , EnableIf< carl::is\_subset\_of\_rationals\_type< Coeff >> = dummy>

```
Term < Coeff > operator/ (const Monomial::Arg &lhs, const Coeff &rhs)
```

Perform a multiplication involving a term. template<typename Coeff , EnableIf< carl::is\_subset\_of\_rationals\_type< Coeff >> = dummy> Term < Coeff > operator/ (Variable &lhs, const Coeff &rhs) Perform a multiplication involving a term. • template<typename C , typename O , typename P >auto operator\* (const MultivariatePolynomial < C, O, P > &lhs, const MultivariatePolynomial < C, O, P > Perform a multiplication involving a polynomial using operator\*=(). - template<typename C , typename O , typename P >auto operator\* (const MultivariatePolynomial < C, O, P > &lhs, const Term < C > &rhs) Perform a multiplication involving a polynomial using operator\*=(). - template<typename C , typename O , typename P >auto operator\* (const MultivariatePolynomial < C, O, P > &lhs, const Monomial::Arg &rhs) Perform a multiplication involving a polynomial using operator\*=(). template<typename C , typename O , typename P > auto operator\* (const MultivariatePolynomial < C, O, P > &lhs, Variable rhs) Perform a multiplication involving a polynomial using operator\*=(). template<typename C , typename O , typename P > auto operator\* (const MultivariatePolynomial < C, O, P > &lhs, const C &rhs) Perform a multiplication involving a polynomial using operator\*=(). • template<typename C , typename O , typename P > auto operator\* (const Term< C > &lhs, const MultivariatePolynomial< C, O, P > &rhs) Perform a multiplication involving a polynomial using operator\*=(). - template<typename C , typename O , typename P >auto operator\* (const Monomial::Arg &lhs, const MultivariatePolynomial < C, O, P > &rhs) Perform a multiplication involving a polynomial using operator\*=(). • template<typename C , typename O , typename P >auto operator\* (Variable lhs, const MultivariatePolynomial< C, O, P > &rhs) Perform a multiplication involving a polynomial using operator\*=(). template<typename C, typename O, typename P> auto operator\* (const C &lhs, const MultivariatePolynomial < C, O, P > &rhs) Perform a multiplication involving a polynomial using operator\*=(). template<typename P >

 $\label{eq:polynomial} \textbf{FactorizedPolynomial} < P > \textbf{a\_lhs}, \textbf{const FactorizedPolynomial} < P > \textbf{a\_lhs}, \textbf{const FactorizedPolynomial} < P > \textbf{a\_rhs})$ 

Perform a multiplication involving a polynomial.

template<typename P >

 $\label{eq:power_problem} Factorized Polynomial < P > operator* (const Factorized Polynomial < P > \&\_lhs, const typename Factorized Polynomial < P > ::Coeff Type \&\_rhs)$ 

Perform a multiplication involving a polynomial.

template<typename P >

 $\label{eq:polynomial} \textbf{FactorizedPolynomial} < P > \textbf{operator*} \ \, (\textbf{const typename FactorizedPolynomial} < P > \textbf{::CoeffType \&\_lhs, const FactorizedPolynomial} < P > \textbf{\&\_rhs}) \\$ 

Perform a multiplication involving a polynomial.

template<typename P >

Perform a multiplication involving a polynomial.

#### Comparison operators

• bool operator== (const Monomial &lhs, const Monomial &rhs)

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

bool operator== (const Monomial::Arg &lhs, const Monomial::Arg &rhs)

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

• bool operator== (const Monomial::Arg &lhs, Variable rhs)

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

bool operator== (Variable lhs, const Monomial::Arg &rhs)

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

bool operator!= (const Monomial::Arg &lhs, const Monomial::Arg &rhs)

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

bool operator!= (const Monomial::Arg &lhs, Variable rhs)

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

bool operator!= (Variable lhs, const Monomial::Arg &rhs)

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

bool operator< (const Monomial::Arg &lhs, const Monomial::Arg &rhs)</li>

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

bool operator< (const Monomial::Arg &lhs, Variable rhs)</li>

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

bool operator< (Variable lhs, const Monomial::Arg &rhs)</li>

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

bool operator<= (const Monomial::Arg &lhs, const Monomial::Arg &rhs)</li>

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

bool operator<= (const Monomial::Arg &lhs, Variable rhs)</li>

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

bool operator<= (Variable lhs, const Monomial::Arg &rhs)</li>

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

bool operator> (const Monomial::Arg &lhs, const Monomial::Arg &rhs)

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

bool operator> (const Monomial::Arg &lhs, Variable rhs)

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

• bool operator> (Variable lhs, const Monomial::Arg &rhs)

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

bool operator>= (const Monomial::Arg &lhs, const Monomial::Arg &rhs)

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

bool operator>= (const Monomial::Arg &lhs, Variable rhs)

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

bool operator>= (Variable lhs, const Monomial::Arg &rhs)

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

template<typename Coeff >

```
bool operator== (const Term < Coeff > &lhs, const Term < Coeff > &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

• template<typename Coeff >

```
bool operator== (const Term < Coeff > &lhs, const Monomial &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

 $\bullet \;\; {\sf template}{<} {\sf typename} \; {\sf Coeff} >$ 

```
bool operator== (const Term < Coeff > &lhs, Variable rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

```
bool operator== (const Term < Coeff > &lhs, const Coeff &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

• template<typename Coeff >

```
bool operator== (const Monomial::Arg &lhs, const Term < Coeff > &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

• template<typename Coeff >

```
bool operator== (Variable lhs, const Term < Coeff > &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

```
bool operator== (const Coeff &lhs, const Term < Coeff > &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

```
bool operator!= (const Term < Coeff > &lhs, const Term < Coeff > &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

```
bool operator!= (const Term< Coeff > &lhs, const Monomial::Arg &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

• template<typename Coeff >

bool operator!= (const Term< Coeff > &lhs, Variable rhs)

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

bool operator!= (const Term< Coeff > &lhs, const Coeff &rhs)

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

bool operator!= (const Monomial::Arg &lhs, const Term< Coeff > &rhs)

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

bool operator!= (Variable lhs, const Term < Coeff > &rhs)

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

bool operator!= (const Coeff &lhs, const Term < Coeff > &rhs)

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

bool operator< (const Term< Coeff > &lhs, const Term< Coeff > &rhs)

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

bool operator< (const Term< Coeff > &lhs, const Monomial::Arg &rhs)

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

bool operator< (const Term< Coeff > &Ihs, Variable rhs)

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

bool operator< (const Term< Coeff > &lhs, const Coeff &rhs)

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

bool operator< (const Monomial::Arg &lhs, const Term< Coeff > &rhs)

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

bool operator< (Variable Ihs, const Term< Coeff > &rhs)

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

bool operator< (const Coeff &lhs, const Term< Coeff > &rhs)

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

```
bool operator<= (const Term< Coeff > &lhs, const Term< Coeff > &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

```
bool operator<= (const Term< Coeff > &lhs, const Monomial::Arg &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

• template<typename Coeff >

```
bool operator <= (const Term < Coeff > &lhs, Variable rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

• template<typename Coeff >

```
bool operator<= (const Term< Coeff > &lhs, const Coeff &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

```
bool operator<= (const Monomial::Arg &lhs, const Term< Coeff > &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

```
bool operator<= (Variable lhs, const Term< Coeff > &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

• template<typename Coeff >

```
bool operator<= (const Coeff &lhs, const Term< Coeff > &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

```
bool operator> (const Term< Coeff > &lhs, const Term< Coeff > &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

```
bool operator> (const Term< Coeff > &lhs, const Monomial::Arg &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

• template<typename Coeff >

```
bool operator> (const Term< Coeff > &lhs, Variable rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

```
bool operator > (const Term < Coeff > &lhs, const Coeff &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

```
bool operator> (const Monomial::Arg &lhs, const Term< Coeff > &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

```
bool operator> (Variable Ihs, const Term< Coeff > &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

```
bool operator> (const Coeff &lhs, const Term< Coeff > &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

```
bool operator>= (const Term< Coeff > &lhs, const Term< Coeff > &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

```
bool operator>= (const Term< Coeff > &lhs, const Monomial::Arg &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

```
bool operator>= (const Term< Coeff > &lhs, Variable rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

• template<typename Coeff >

```
bool operator>= (const Term< Coeff > &lhs, const Coeff &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

```
bool operator>= (const Monomial::Arg &lhs, const Term< Coeff > &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

```
bool operator>= (Variable lhs, const Term< Coeff > &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

template<typename Coeff >

```
bool operator>= (const Coeff &lhs, const Term< Coeff > &rhs)
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

#### **Division operators**

template<typename C, typename O, typename P, Enablelf< carl::is\_number\_type< C>> = dummy>
 MultivariatePolynomial< C, O, P > operator/ (const MultivariatePolynomial< C, O, P > &lhs, const C &rhs)
 Perform a division involving a polynomial.

#### In-place multiplication operators

• template<typename Coeff >

```
Term< Coeff > & operator*= (Term< Coeff > &lhs, const Coeff &rhs)
```

Multiply a term with something and return the changed term.

template<typename Coeff >

```
Term< Coeff > & operator*= (Term< Coeff > &lhs, Variable rhs)
```

Multiply a term with something and return the changed term.

template<typename Coeff >

```
Term < Coeff > & operator*= (Term < Coeff > &lhs, const Monomial::Arg &rhs)
```

Multiply a term with something and return the changed term.

 template<typename Coeff >
 Term< Coeff > & operator\*= (Term< Coeff > &lhs, const Term< Coeff > &rhs)
 Multiply a term with something and return the changed term.

#### **Equality comparison operators**

```
- template<typename C , typename O , typename P >
 bool operator== (const MultivariatePolynomial < C, O, P > &lhs, const MultivariatePolynomial < C, O, P >
  &rhs)
     Checks if the two arguments are equal.
• template<typename C , typename O , typename P >
 bool operator== (const MultivariatePolynomial < C, O, P > &lhs, const Term < C > &rhs)
      Checks if the two arguments are equal.

    template<typename C , typename O , typename P >

  bool operator== (const MultivariatePolynomial < C, O, P > &lhs, const Monomial::Arg &rhs)
     Checks if the two arguments are equal.
- template<typename C , typename O , typename P >
 bool operator== (const MultivariatePolynomial < C, O, P > &lhs, Variable rhs)
      Checks if the two arguments are equal.
- template<typename C , typename O , typename P >
  bool operator== (const MultivariatePolynomial < C, O, P > &lhs, const C &rhs)
     Checks if the two arguments are equal.

    template<typename C , typename O , typename P , DisableIf< std::is.integral< C >> = dummy>

 bool operator== (const MultivariatePolynomial < C, O, P > &lhs, int rhs)
     Checks if the two arguments are equal.

    template<typename C , typename O , typename P >

 bool operator== (const Term < C > &lhs, const MultivariatePolynomial < C, O, P > &rhs)
      Checks if the two arguments are equal.
- template<typename C , typename O , typename P >
  bool operator== (const Monomial::Arg &lhs, const MultivariatePolynomial < C, O, P > &rhs)
      Checks if the two arguments are equal.
• template<typename C , typename O , typename P >
 bool operator== (Variable lhs, const MultivariatePolynomial < C, O, P > &rhs)
     Checks if the two arguments are equal.

    template<typename C , typename O , typename P >

 bool operator== (const C &lhs, const MultivariatePolynomial < C, O, P > &rhs)
      Checks if the two arguments are equal.
 template<typename C , typename O , typename P >
 bool operator== (const UnivariatePolynomial < C > &lhs, const MultivariatePolynomial < C, O, P > &rhs)
     Checks if the two arguments are equal.
- template<typename C , typename O , typename P >
 bool operator== (const MultivariatePolynomial < C, O, P > &lhs, const UnivariatePolynomial < C > &rhs)
     Checks if the two arguments are equal.
• template<typename C , typename O , typename P >
  bool operator== (const UnivariatePolynomial < MultivariatePolynomial < C >> &lhs, const MultivariatePolynomial <
  C, O, P > &rhs
      Checks if the two arguments are equal.
 template<typename C , typename O , typename P >
  bool operator== (const MultivariatePolynomial< C, O, P > &lhs, const UnivariatePolynomial<
 MultivariatePolynomial < C >> &rhs)
     Checks if the two arguments are equal.

    template<typename P >
```

bool operator== (const FactorizedPolynomial < P > &\_lhs, const FactorizedPolynomial < P > &\_rhs)

bool operator== (const FactorizedPolynomial < P > & Lhs, const typename FactorizedPolynomial < P > ↔

Checks if the two arguments are equal.

Checks if the two arguments are equal.

template<typename P >

::CoeffType &\_rhs)

```
template<typename P >
     bool operator== (const typename FactorizedPolynomial < P >::CoeffType &.lhs, const FactorizedPolynomial <
     P > \&_rhs)
        Checks if the two arguments are equal.
Inequality comparison operators
  - template<typename C , typename O , typename P >
     bool operator!= (const MultivariatePolynomial < C, O, P > &lhs, const MultivariatePolynomial < C, O, P >
     &rhs)
        Checks if the two arguments are not equal.
    template<typename C , typename O , typename P >
    bool operator!= (const MultivariatePolynomial < C, O, P > &Ihs, const Term < C > &rhs)
        Checks if the two arguments are not equal.

    template<typename C , typename O , typename P >

    bool operator!= (const MultivariatePolynomial < C, O, P > &lhs, const Monomial::Arg &rhs)
        Checks if the two arguments are not equal.
  - template<typename C , typename O , typename P >
     bool operator!= (const MultivariatePolynomial < C, O, P > &lhs, Variable rhs)
        Checks if the two arguments are not equal.
    template<typename C, typename O, typename P>
     bool operator!= (const MultivariatePolynomial < C, O, P > &Ihs, const C &rhs)
        Checks if the two arguments are not equal.
   • template<typename C , typename O , typename P >
    bool operator!= (const Term< C > &lhs, const MultivariatePolynomial< C, O, P > &rhs)
        Checks if the two arguments are not equal.

    template<typename C , typename O , typename P >

    bool operator!= (const Monomial::Arg &lhs, const MultivariatePolynomial < C, O, P > &rhs)
        Checks if the two arguments are not equal.
  • template<typename C , typename O , typename P >
     bool operator!= (Variable lhs, const MultivariatePolynomial < C, O, P > &rhs)
        Checks if the two arguments are not equal.
  - template<typename C , typename O , typename P >
    bool operator!= (const C &lhs, const MultivariatePolynomial < C, O, P > &rhs)
        Checks if the two arguments are not equal.
  • template<typename C , typename O , typename P >
    bool operator!= (const UnivariatePolynomial < C > &lhs, const MultivariatePolynomial < C, O, P > &rhs)
        Checks if the two arguments are not equal.
  - template<typename C , typename O , typename P >
     bool operator!= (const MultivariatePolynomial < C, O, P > &lhs, const UnivariatePolynomial < C > &rhs)
        Checks if the two arguments are not equal.
    template<typename C, typename O, typename P>
     bool operator!= (const UnivariatePolynomial < MultivariatePolynomial < C >> &lhs, const MultivariatePolynomial <
    C, O, P > &rhs
        Checks if the two arguments are not equal.

    template<typename C , typename O , typename P >

    bool operator!= (const MultivariatePolynomial< C, O, P > &lhs, const UnivariatePolynomial<
    MultivariatePolynomial < C >> &rhs)
        Checks if the two arguments are not equal.

    template<typename P >

    bool operator!= (const FactorizedPolynomial < P > & lhs, const FactorizedPolynomial < P > & rhs)
        Checks if the two arguments are not equal.

    template<typename P >

    bool operator!= (const FactorizedPolynomial < P > & lhs, const typename FactorizedPolynomial < P > ←
     ::CoeffType &_rhs)
        Checks if the two arguments are not equal.

    template<typename P >
```

bool operator!= (const typename FactorizedPolynomial < P >::CoeffType & lhs, const FactorizedPolynomial <

 $P > \&_rhs$ 

Checks if the two arguments are not equal.

#### Less than comparison operators

template<typename C, typename O, typename P >
 bool operator< (const MultivariatePolynomial< C, O, P > &lhs, const MultivariatePolynomial< C, O, P >
 &rhs)

Checks if the first arguments is less than the second.

• template<typename C , typename O , typename P >

bool operator< (const MultivariatePolynomial< C, O, P > &lhs, const Term< C > &rhs)

Checks if the first arguments is less than the second.

template<typename C , typename O , typename P >

bool operator < (const MultivariatePolynomial < C, O, P > &lhs, const Monomial::Arg &rhs)

Checks if the first arguments is less than the second.

- template<typename C , typename O , typename P >

bool operator< (const MultivariatePolynomial< C, O, P > &lhs, Variable rhs)

Checks if the first arguments is less than the second.

template<typename C , typename O , typename P >

bool operator< (const MultivariatePolynomial< C, O, P > &lhs, const C &rhs)

Checks if the first arguments is less than the second.

- template<typename C , typename O , typename P >

bool operator< (const Term< C > &lhs, const MultivariatePolynomial< C, O, P > &rhs)

Checks if the first arguments is less than the second.

• template<typename C , typename O , typename P >

bool operator < (const Monomial::Arg &lhs, const MultivariatePolynomial < C, O, P > &rhs)

Checks if the first arguments is less than the second.

template<typename C , typename O , typename P >

bool operator< (Variable lhs, const MultivariatePolynomial< C, O, P > &rhs)

Checks if the first arguments is less than the second.

• template<typename C , typename O , typename P >

bool operator< (const C &lhs, const MultivariatePolynomial< C, O, P > &rhs)

Checks if the first arguments is less than the second.

template<typename P >

bool operator< (const FactorizedPolynomial<  $P > \&\_lhs$ , const FactorizedPolynomial<  $P > \&\_rhs$ )

Checks if the first arguments is less than the second.

template<typename P >

bool operator< (const FactorizedPolynomial< P > & lhs, const typename FactorizedPolynomial<  $P > \leftarrow :: CoeffType \& rhs$ )

Checks if the first arguments is less than the second.

template<typename P >

bool operator < (const typename FactorizedPolynomial < P >::CoeffType &\_lhs, const FactorizedPolynomial < P > &\_rhs)

Checks if the first arguments is less than the second.

#### Greater than comparison operators

template < typename C, typename O, typename P >
 bool operator > (const MultivariatePolynomial < C, O, P > &Ihs, const MultivariatePolynomial < C, O, P >
 &rhs)

Checks if the first argument is greater than the second.

template<typename C , typename O , typename P >

bool operator> (const MultivariatePolynomial< C, O, P > &lhs, const Term< C > &rhs)

Checks if the first argument is greater than the second.

• template<typename C , typename O , typename P >

bool operator> (const MultivariatePolynomial< C, O, P > &lhs, const Monomial::Arg &rhs)

Checks if the first argument is greater than the second.

• template<typename C , typename O , typename P >

bool operator> (const MultivariatePolynomial< C, O, P > &lhs, Variable rhs)

```
Checks if the first argument is greater than the second.
```

• template<typename C , typename O , typename P>

```
bool operator> (const MultivariatePolynomial< C, O, P > &lhs, const C &rhs)
```

Checks if the first argument is greater than the second.

- template<typename C , typename O , typename P >

```
bool operator> (const Term< C > &lhs, const MultivariatePolynomial< C, O, P > &rhs)
```

Checks if the first argument is greater than the second.

• template<typename C , typename O , typename P >

```
bool operator> (const Monomial::Arg &lhs, const MultivariatePolynomial< C, O, P > &rhs)
```

Checks if the first argument is greater than the second.

• template<typename C , typename O , typename P >

```
bool operator> (Variable lhs, const MultivariatePolynomial< C, O, P > &rhs)
```

Checks if the first argument is greater than the second.

• template<typename C , typename O , typename P >

```
bool operator> (const C &lhs, const MultivariatePolynomial< C, O, P > &rhs)
```

Checks if the first argument is greater than the second.

• template<typename C , typename O , typename P >

bool operator> (const UnivariatePolynomial < C > &lhs, const MultivariatePolynomial < C, O, P > &rhs)

Checks if the first argument is greater than the second.

• template<typename C , typename O , typename P >

```
bool\ operator{>}\ (const\ Multivariate Polynomial < C,\ O,\ P > \&lhs,\ const\ Univariate Polynomial < C > \&rhs)
```

Checks if the first argument is greater than the second.

• template<typename C , typename O , typename P >

 $bool\ operator{>>}\ (const\ UnivariatePolynomial{<}\ C>> \&lhs,\ const\ MultivariatePolynomial{<}\ C,\ O,\ P>\&rhs)$ 

Checks if the first argument is greater than the second.

• template<typename C , typename O , typename P >

```
bool operator> (const MultivariatePolynomial< C, O, P > &lhs, const UnivariatePolynomial< MultivariatePolynomial< C >> &rhs)
```

Checks if the first argument is greater than the second.

template<typename P >

```
bool operator> (const FactorizedPolynomial < P > & lhs, const FactorizedPolynomial < P > & rhs)
```

Checks if the first arguments is greater than the second.

template<typename P >

bool operator> (const FactorizedPolynomial < P > & lhs, const typename FactorizedPolynomial  $< P > \Leftrightarrow lhs$ )

Checks if the first arguments is greater than the second.

template<typename P >

bool operator> (const typename FactorizedPolynomial < P >::CoeffType &\_lhs, const FactorizedPolynomial < P > &\_rhs)

Checks if the first arguments is greater than the second.

## Less or equal comparison operators

template<typename C, typename O, typename P >
 bool operator<= (const MultivariatePolynomial< C, O, P > &lhs, const MultivariatePolynomial< C, O, P > &rhs)

Checks if the first argument is less or equal than the second.

• template<typename C , typename O , typename P >

```
bool operator<= (const MultivariatePolynomial< C, O, P > &lhs, const Term< C > &rhs)
```

Checks if the first argument is less or equal than the second.

• template<typename C , typename O , typename P >

```
bool operator <= (const MultivariatePolynomial < C, O, P > &lhs, const Monomial::Arg &rhs)
```

Checks if the first argument is less or equal than the second.

template<typename C , typename O , typename P >

```
bool operator<= (const MultivariatePolynomial< C, O, P > &lhs, Variable rhs)
```

Checks if the first argument is less or equal than the second.

template < typename C, typename O, typename P >
 bool operator <= (const Multivariate Polynomial < C, O, P > &Ihs, const C &rhs)
 Checks if the first argument is less or equal than the second.

- template<typename C , typename O , typename P >

bool operator<= (const Term< C > &lhs, const MultivariatePolynomial< C, O, P > &rhs)

Checks if the first argument is less or equal than the second.

• template<typename C , typename O , typename P >

bool operator <= (const Monomial:: Arg &lhs, const MultivariatePolynomial < C, O, P > &rhs)

Checks if the first argument is less or equal than the second.

template<typename C , typename O , typename P >

bool operator<= (Variable Ihs, const MultivariatePolynomial< C, O, P > &rhs)

Checks if the first argument is less or equal than the second.

- template<typename C , typename O , typename P >

bool operator<= (const C &lhs, const MultivariatePolynomial< C, O, P > &rhs)

Checks if the first argument is less or equal than the second.

• template<typename C , typename O , typename P>

bool operator<= (const UnivariatePolynomial< C > &lhs, const MultivariatePolynomial< C, O, P > &rhs)

Checks if the first argument is less or equal than the second.

- template<typename C , typename O , typename P >

bool operator <= (const MultivariatePolynomial < C, O, P > &lhs, const UnivariatePolynomial < C > &rhs)

Checks if the first argument is less or equal than the second.

• template<typename C , typename O , typename P >

bool operator<= (const UnivariatePolynomial< MultivariatePolynomial< C >> &lhs, const MultivariatePolynomial< C, O, P > &rhs)

Checks if the first argument is less or equal than the second.

• template<typename C , typename O , typename P >

bool operator<= (const MultivariatePolynomial< C, O, P > &lhs, const UnivariatePolynomial< MultivariatePolynomial< C >> &rhs)

Checks if the first argument is less or equal than the second.

template<typename P >

bool operator<= (const FactorizedPolynomial< P > &\_Ihs, const FactorizedPolynomial< P > &\_rhs)

Checks if the first arguments is less or equal than the second.

template<typename P >

 $bool\ operator <= (const\ Factorized Polynomial < P > \&\_lhs,\ const\ typename\ Factorized Polynomial < P > \hookleftarrow :: Coeff Type\ \&\_rhs)$ 

Checks if the first arguments is less or equal than the second.

• template<typename P >

 $bool\ operator <= (const\ typename\ Factorized Polynomial < P>:: Coeff Type\ \&\_lhs,\ const\ Factorized Polynomial < P>\&\_rhs)$ 

Checks if the first arguments is less or equal than the second.

#### Greater or equal comparison operators

template < typename C, typename O, typename P >
 bool operator >= (const MultivariatePolynomial < C, O, P > &Ihs, const MultivariatePolynomial < C, O, P > &rhs)

Checks if the first argument is greater or equal than the second.

template<typename C , typename O , typename P >

bool operator>= (const MultivariatePolynomial < C, O, P > &lhs, const Term < C > &rhs)

Checks if the first argument is greater or equal than the second.

template<typename C , typename O , typename P >

bool operator>= (const MultivariatePolynomial < C, O, P > &Ihs, const Monomial::Arg &rhs)

Checks if the first argument is greater or equal than the second.

- template<typename C , typename O , typename P >

bool operator>= (const MultivariatePolynomial < C, O, P > &lhs, Variable rhs)

Checks if the first argument is greater or equal than the second.

• template < typename C , typename O , typename P >

bool operator>= (const MultivariatePolynomial < C, O, P > &lhs, const C &rhs)

```
Checks if the first argument is greater or equal than the second.
   • template<typename C , typename O , typename P >
     bool operator>= (const Term< C > &lhs, const MultivariatePolynomial< C, O, P > &rhs)
        Checks if the first argument is greater or equal than the second.
  • template<typename C , typename O , typename P >
    bool operator>= (const Monomial::Arg &lhs, const MultivariatePolynomial< C, O, P > &rhs)
         Checks if the first argument is greater or equal than the second.

    template<typename C , typename O , typename P >

     bool operator>= (Variable lhs, const MultivariatePolynomial < C, O, P > &rhs)
         Checks if the first argument is greater or equal than the second.
    template<typename C , typename O , typename P >
     bool operator>= (const C &lhs, const MultivariatePolynomial< C, O, P > &rhs)
         Checks if the first argument is greater or equal than the second.
    template<typename C , typename O , typename P>
     bool operator>= (const UnivariatePolynomial < C > &lhs, const MultivariatePolynomial < C, O, P > &rhs)
         Checks if the first argument is greater or equal than the second.

    template<typename C , typename O , typename P >

    bool operator>= (const MultivariatePolynomial < C, O, P > &lhs, const UnivariatePolynomial < C > &rhs)
        Checks if the first argument is greater or equal than the second.

    template<typename C , typename O , typename P >

     bool operator>= (const UnivariatePolynomial < MultivariatePolynomial < C >> &lhs, const MultivariatePolynomial <
     C, O, P > & rhs
         Checks if the first argument is greater or equal than the second.
    template<typename C , typename O , typename P >
     bool operator>= (const MultivariatePolynomial< C, O, P > &lhs, const UnivariatePolynomial<
    MultivariatePolynomial < C >> &rhs)
         Checks if the first argument is greater or equal than the second.
    template<typename P >
     bool operator>= (const FactorizedPolynomial < P > &_lhs, const FactorizedPolynomial < P > &_rhs)
        Checks if the first arguments is greater or equal than the second.

    template<typename P >

    bool operator>= (const FactorizedPolynomial < P > & lhs, const typename FactorizedPolynomial < P > ←
     ::CoeffType &_rhs)
         Checks if the first arguments is greater or equal than the second.

    template<typename P >

     bool operator>= (const typename FactorizedPolynomial < P >::CoeffType & Lhs, const FactorizedPolynomial <
    P > \&_rhs)
         Checks if the first arguments is greater or equal than the second.
Addition operators
  - template<typename C , typename O , typename P >
     auto operator+ (const MultivariatePolynomial < C, O, P > &lhs, const MultivariatePolynomial < C, O, P >
     &rhs)
        Performs an addition involving a polynomial using operator+= ().
  - template<typename C , typename O , typename P >
     auto operator+ (const MultivariatePolynomial < C, O, P > &lhs, const Term < C > &rhs)
        Performs an addition involving a polynomial using operator+= ().
    template<typename C , typename O , typename P >
     auto operator+ (const MultivariatePolynomial < C, O, P > &lhs, const Monomial::Arg &rhs)
        Performs an addition involving a polynomial using operator+= ().
   • template<typename C , typename O , typename P >
     auto operator+ (const MultivariatePolynomial < C, O, P > &lhs, Variable rhs)
         Performs an addition involving a polynomial using operator+= ().

    template<typename C , typename O , typename P >

     auto operator+ (const MultivariatePolynomial < C, O, P > &lhs, const C &rhs)
```

Performs an addition involving a polynomial using operator+= ().

```
    template<typename C , typename O , typename P >

  auto operator+ (const Term < C > &lhs, const MultivariatePolynomial < C, O, P > &rhs)
     Performs an addition involving a polynomial using operator+=().

    template<typename C >

 auto operator+ (const Term< C > &lhs, const Term< C > &rhs)
     Performs an addition involving a polynomial using operator+= ().
template<typename C >
  auto operator+ (const Term< C > &lhs, const Monomial::Arg &rhs)
      Performs an addition involving a polynomial using operator+=().
template<typename C >
  auto operator+ (const Term < C > &lhs, Variable rhs)
     Performs an addition involving a polynomial using operator+= ().

    template<tvpename C >

  auto operator+ (const Term< C > &lhs, const C &rhs)
     Performs an addition involving a polynomial using operator+=().
- template<typename C , typename O , typename P >
  auto operator+ (const Monomial::Arg &lhs, const MultivariatePolynomial < C, O, P > &rhs)
     Performs an addition involving a polynomial using operator+=().

    template<typename C >

  auto operator+ (const Monomial::Arg &lhs, const Term< C > &rhs)
      Performs an addition involving a polynomial using operator+= ().

    template<typename C , EnableIf< carl::is_number_type< C >> = dummy>

  auto operator+ (const Monomial::Arg &lhs, const C &rhs)
     Performs an addition involving a polynomial using operator+= ().

    template<typename C , typename O , typename P >

  auto operator+ (Variable lhs, const MultivariatePolynomial< C, O, P > &rhs)
     Performs an addition involving a polynomial using operator+= ().

    template<typename C >

  auto operator+ (Variable lhs, const Term< C > &rhs)
      Performs an addition involving a polynomial using operator+= ().
• template<typename C , EnableIf< carl::is_number_type< C >> = dummy>
  auto operator+ (Variable lhs, const C &rhs)
     Performs an addition involving a polynomial using operator+= ().
 template<typename C , typename O , typename P >
  auto operator+ (const C &lhs, const MultivariatePolynomial < C, O, P > &rhs)
     Performs an addition involving a polynomial using operator+= ().

    template<typename C >

  auto operator+ (const C &lhs, const Term< C > &rhs)
     Performs an addition involving a polynomial using operator+= ().

    template<typename C , EnableIf< carl::is_number_type< C >> = dummy>

  auto operator+ (const C &lhs, const Monomial::Arg &rhs)
      Performs an addition involving a polynomial using operator+= ().

    template<typename C , EnableIf< carl::is_number_type< C >> = dummy>

  auto operator+ (const C &lhs, Variable rhs)
     Performs an addition involving a polynomial using operator+=().
• template<typename P >
  FactorizedPolynomial < P > operator+ (const FactorizedPolynomial < P > & lhs, const FactorizedPolynomial <
  P > \&_rhs
     Performs an addition involving a polynomial.

    template<typename P >

  FactorizedPolynomial < P > operator+ (const FactorizedPolynomial < P > & lhs, const typename
 FactorizedPolynomial < P >::CoeffType &_rhs)
      Performs an addition involving a polynomial.

    template<typename P >

  FactorizedPolynomial < P > operator+ (const typename FactorizedPolynomial < P >::CoeffType & lhs,
  const FactorizedPolynomial < P > &_rhs)
     Performs an addition involving a polynomial.
```

```
    template<typename C , typename O , typename P >

  auto operator- (const MultivariatePolynomial < C, O, P > &lhs, const MultivariatePolynomial < C, O, P >
  &rhs)
     Performs a subtraction involving a polynomial using operator -= ().
• template<typename C , typename O , typename P >
  auto operator- (const MultivariatePolynomial < C, O, P > &lhs, const Term < C > &rhs)
      Performs a subtraction involving a polynomial using operator -= ().

    template<typename C , typename O , typename P >

 auto operator- (const MultivariatePolynomial < C, O, P > &lhs, const Monomial::Arg &rhs)
     Performs a subtraction involving a polynomial using operator -= ().
 template<typename C , typename O , typename P >
 auto operator- (const MultivariatePolynomial < C, O, P > &lhs, Variable rhs)
      Performs a subtraction involving a polynomial using operator -= ().
 template<typename C , typename O , typename P >
  auto operator- (const MultivariatePolynomial < C, O, P > &Ihs, const C &rhs)
     Performs a subtraction involving a polynomial using operator -= ().

    template<typename C , typename O , typename P >

  auto operator- (const Term< C > &lhs, const MultivariatePolynomial< C, O, P > &rhs)
     Performs a subtraction involving a polynomial using operator -= ().

    template<typename C >

  auto operator- (const Term < C > &lhs, const Term < C > &rhs)
     Performs a subtraction involving a polynomial using operator —= ().
 template<typename C >
  auto operator- (const Term< C > &lhs, const Monomial::Arg &rhs)
     Performs a subtraction involving a polynomial using operator -= ().

    template<tvpename C >

  auto operator- (const Term< C > &lhs, Variable rhs)
     Performs a subtraction involving a polynomial using operator -= ().
 template<tvpename C >
  auto operator- (const Term< C > &lhs, const C &rhs)
     Performs a subtraction involving a polynomial using operator -= ().
• template<typename C , typename O , typename P >
  auto operator- (const Monomial::Arg &lhs, const MultivariatePolynomial < C, O, P > &rhs)
      Performs a subtraction involving a polynomial using operator -= ().
 template<typename C >
  auto operator- (const Monomial::Arg &lhs, const Term< C > &rhs)
     Performs a subtraction involving a polynomial using operator == ().
 template<typename C , EnableIf< carl::is_number_type< C >> = dummy>
  auto operator- (const Monomial::Arg &lhs, const C &rhs)
      Performs a subtraction involving a polynomial using operator = ().
 template<typename C , typename O , typename P >
  auto operator- (Variable lhs, const MultivariatePolynomial < C, O, P > &rhs)
     Performs a subtraction involving a polynomial using operator -= ().
template<typename C >
 auto operator- (Variable lhs, const Term< C > &rhs)
     Performs a subtraction involving a polynomial using operator —= ().

    template<typename C , EnableIf< carl::is_number_type< C >> = dummy>

  auto operator- (Variable lhs, const C &rhs)
     Performs a subtraction involving a polynomial using operator -= ().
 template<typename C , typename O , typename P>
  auto operator- (const C &lhs, const MultivariatePolynomial < C, O, P > &rhs)
     Performs a subtraction involving a polynomial using operator -= ().
template<typename C >
  auto operator- (const C &lhs, const Term< C > &rhs)
     Performs a subtraction involving a polynomial using operator = ().

    template<typename C , EnableIf< carl::is_number_type< C >> = dummy>

  auto operator- (const C &lhs, const Monomial::Arg &rhs)
```

Performs a subtraction involving a polynomial using operator = ().

 template<typename C , EnableIf< carl::is\_number\_type< C >> = dummy> auto operator- (const C &lhs, Variable rhs)

Performs a subtraction involving a polynomial using operator -= ().

template<typename P >

FactorizedPolynomial < P > operator- (const FactorizedPolynomial < P > &\_Ihs, const FactorizedPolynomial < P > &\_rhs)

Performs an subtraction involving a polynomial.

template<typename P >

FactorizedPolynomial < P > operator (const FactorizedPolynomial  $< P > \&_lhs$ , const typename FactorizedPolynomial  $< P > ::CoeffType \&_rhs$ )

Performs an subtraction involving a polynomial.

template<typename P >

FactorizedPolynomial < P > operator- (const typename FactorizedPolynomial < P >::CoeffType &\_lhs, const FactorizedPolynomial < P > &\_rhs)

Performs an subtraction involving a polynomial.

#### **Variables**

• static int initvariable = initialize()

Call to initialize.

- const dtl::enabled dummy = {}
- template<class>

constexpr bool dependent\_false\_v = false

- constexpr unsigned sizeOfUnsigned = sizeof(unsigned)
- std::string last\_assertion\_string

Stores a textual representation of the last assertion that was registered via REGISTER\_ASSERT.

int last\_assertion\_code = 23

Stores an integer representation of the last assertion that was registered via REGISTER\_ASSERT.

static bool signal\_installed = install\_signal\_handler()

Static variable that ensures that install\_signal\_handler is called.

- static std::map< Variable, Interval< double >> mMap = {{ Variable::NO\_VARIABLE, Interval< double>(0)}}
- const signed A\_IFF\_B = 2
- const signed A\_IMPLIES\_B = 1
- const signed B\_IMPLIES\_A = -1
- const signed NOT\_A\_AND\_B = -2
- const signed A\_AND\_B\_\_IFF\_C = -3
- const signed A\_XOR\_B = -4
- static const cln::cl\_RA ONE\_DIVIDED\_BY\_10\_TO\_THE\_POWER\_OF\_23 = cln::cl\_RA(1)/cln::expt(cln::cl\_← RA(10), 23)
- static const cln::cl\_RA ONE\_DIVIDED\_BY\_10\_TO\_THE\_POWER\_OF\_52 = cln::cl\_RA(1)/cln::expt(cln::cl\_ $\leftarrow$  RA(10), 52)
- static constexpr std::size\_t CONDITION\_SIZE = 64
- static constexpr Condition PROP\_TRUE = Condition()
- static constexpr Condition PROP\_IS\_IN\_NNF = Condition( 0 )
- static constexpr Condition PROP\_IS\_IN\_CNF = Condition(1)
- static constexpr Condition PROP\_IS\_PURE\_CONJUNCTION = Condition(2)
- static constexpr Condition PROP\_IS\_A\_CLAUSE = Condition(3)
- static constexpr Condition PROP\_IS\_A\_LITERAL = Condition(4)
- static constexpr Condition PROP\_IS\_AN\_ATOM = Condition(5)
- static constexpr Condition PROP\_IS\_LITERAL\_CONJUNCTION = Condition(6)
- static const Condition STRONG\_CONDITIONS
- static constexpr Condition PROP\_CONTAINS\_EQUATION = Condition( 16 )
- static constexpr Condition PROP\_CONTAINS\_INEQUALITY = Condition(17)
- static constexpr Condition PROP\_CONTAINS\_STRICT\_INEQUALITY = Condition( 18 )

- static constexpr Condition PROP\_CONTAINS\_LINEAR\_POLYNOMIAL = Condition(19)
- static constexpr Condition PROP\_CONTAINS\_NONLINEAR\_POLYNOMIAL = Condition( 20 )
- static constexpr Condition PROP\_CONTAINS\_MULTIVARIATE\_POLYNOMIAL = Condition(21)
- static constexpr Condition PROP\_CONTAINS\_BOOLEAN = Condition(22)
- static constexpr Condition PROP\_CONTAINS\_INTEGER\_VALUED\_VARS = Condition(23)
- static constexpr Condition PROP\_CONTAINS\_REAL\_VALUED\_VARS = Condition(24)
- static constexpr Condition PROP\_CONTAINS\_UNINTERPRETED\_EQUATIONS = Condition(25)
- static constexpr Condition PROP\_CONTAINS\_BITVECTOR = Condition( 26 )
- static constexpr Condition PROP\_CONTAINS\_PSEUDOBOOLEAN = Condition(27)
- static constexpr Condition PROP\_VARIABLE\_DEGREE\_GREATER\_THAN\_TWO = Condition(28)
- static constexpr Condition PROP\_VARIABLE\_DEGREE\_GREATER\_THAN\_THREE = Condition(29)
- static constexpr Condition PROP\_VARIABLE\_DEGREE\_GREATER\_THAN\_FOUR = Condition(30)
- static constexpr Condition PROP\_CONTAINS\_WEAK\_INEQUALITY = Condition(31)
- static const Condition WEAK\_CONDITIONS

#### 11.1.1 Detailed Description

carl is the main namespace for the library.

This file provides mechanisms to substitute a model into an expression and to evaluate an expression over a model.

#### Condition.h.

Class to create a square root expression object.

Everything included in this library is found in this namespace.

**Author** 

Florian Corzilius

Since

2011-05-26

Version

2013-10-22

**Author** 

Florian Corzilius corzilius@cs.rwth-aachen.de

Since

2012-06-11

Version

2014-10-30

### 11.1.2 Typedef Documentation

```
11.1.2.1 Assignment template<typename T >
using carl::Assignment = typedef std::map<Variable, T>
11.1.2.2 Bool template<br/>bool B, typename... T>
using carl::Bool = typedef typename dependent_bool_type<B, T...>::type
11.1.2.3 Coeff template<typename P >
using carl::Coeff = typedef typename UnderlyingNumberType<P>::type
11.1.2.4 CoeffMatrix template<typename Coeff >
using carl::CoeffMatrix = typedef Eigen::Matrix<Coeff, Eigen::Dynamic, Eigen::Dynamic>
11.1.2.5 Conditional template<br/>bool If, typename Then , typename Else >
using carl::Conditional = typedef typename std::conditional<If, Then, Else>::type
11.1.2.6 ConstraintBounds template<typename Pol >
using carl::ConstraintBounds = typedef FastMap<Pol, std::map<typename Pol::NumberType, std↔
::pair<Relation,Formula<Pol> >> >
A map from formula pointers to a map of rationals to a pair of a constraint relation and a formula pointer. (internally
used)
11.1.2.7 ConstraintPool template<typename Pol >
using carl::ConstraintPool = typedef pool::Pool<CachedConstraintContent<Pol> >
11.1.2.8 Constraints template<typename Poly >
using carl::Constraints = typedef std::set<Constraint<Poly>, carl::less<Constraint<Poly>,
false> >
```

```
11.1.2.9 CritPairs typedef CriticalPairs<Heap, CriticalPairConfiguration<GrLexOrdering> >
carl::CritPairs
11.1.2.10 DisableIf template<typename... Condition>
::type
11.1.2.11 EnableIf template<typename... Condition>
using \ carl:: Enable If = type def \ type name \ std:: enable if < all < Condition...>:: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition...>: value, \ dtl:: enable d > \leftrightarrow all < condition
 ::type
11.1.2.12 EnableIfBool template<bool Condition>
using carl::EnableIfBool = typedef typename std::enable_if<Condition, dtl::enabled>::type
11.1.2.13 EncodingCache template<typename Poly >
using carl::EncodingCache = typedef std::map<MultivariateRoot<Poly>, std::pair<std::vector<BasicConstraint<Number | Std::vector<BasicConstraint<Number | S
>, Variable> >
11.1.2.14 exponent using carl::exponent = typedef std::size_t
Type of an exponent.
11.1.2.15 FactorMap template<typename Coefficient >
using carl::FactorMap = typedef std::map<UnivariatePolynomial<Coefficient>, uint>
11.1.2.16 Factors template<typename Pol >
using carl::Factors = typedef std::map<Pol,uint>
11.1.2.17 FastMap template<typename T1 , typename T2 >
using carl::FastMap = typedef std::unordered_map<T1, T2, std::hash<T1> >
```

```
11.1.2.18 FastPointerMap template<typename T1 , typename T2 >
using carl::FastPointerMap = typedef std::unordered_map<const T1*, T2, pointerHash<T1>, pointerEqual<T1>
11.1.2.19 FastPointerMapB template<typename T1 , typename T2 >
using carl::FastPointerMapB = typedef std::unordered_map<const T1*, T2, pointerHashWithNull<T1>,
pointerEqualWithNull<T1> >
11.1.2.20 FastPointerSet template<typename T >
using carl::FastPointerSet = typedef std::unordered_set<const T*, pointerHash<T>, pointerEqual<T>
\textbf{11.1.2.21} \quad \textbf{FastPointerSetB} \quad \texttt{template} < \texttt{typename} \ \texttt{T} \ > \\
using carl::FastPointerSetB = typedef std::unordered.set<const T*, pointerHashWithNull<T>,
pointerEqualWithNull<T> >
11.1.2.22 FastSet template<typename T >
using carl::FastSet = typedef std::unordered_set<T, std::hash<T> >
11.1.2.23 FastSharedPointerMap template<typename T1 , typename T2 >
using carl::FastSharedPointerMap = typedef std::unordered_map<std::shared_ptr<const T1>, T2,
sharedPointerHash<T1>, sharedPointerEqual<T1> >
\textbf{11.1.2.24} \quad \textbf{FastSharedPointerMapB} \quad \texttt{template} < \texttt{typename T1} \text{ , typename T2} >
using carl::FastSharedPointerMapB = typedef std::unordered.map<std::shared.ptr<const T1>, T2,
\verb| sharedPointerHashWithNull<| T1>, pointerEqualWithNull<| T1> > |
11.1.2.25 FastSharedPointerSet template<typename T >
using carl::FastSharedPointerSet = typedef std::unordered_set<std::shared_ptr<const T>, sharedPointerHash<T>,
sharedPointerEqual<T> >
```

```
11.1.2.26 FastSharedPointerSetB template<typename T >
using carl::FastSharedPointerSetB = typedef std::unordered_set<std::shared_ptr<const T>, sharedPointerHashWitt
{\tt pointerEqualWithNull<T>} >
11.1.2.27 Formulas template<typename Poly >
using carl::Formulas = typedef std::vector<Formula<Poly> >
11.1.2.28 FormulaSet template<typename Poly >
using carl::FormulaSet = typedef std::set<Formula<Poly> >
11.1.2.29 FormulasMulti template<typename Poly >
using carl::FormulasMulti = typedef std::multiset<Formula<Poly> >
11.1.2.30 GrLexOrdering using carl::GrLexOrdering = typedef MonomialComparator<Monomial::compareGradedLexical
true >
11.1.2.31 IntegralTypelfDifferent template<typename C >
using carl::IntegralTypeIfDifferent = typedef typename std::enable_if<!std::is_same<C, typename
IntegralType<C>::type>::type<::type</pre>
11.1.2.32 LexOrdering using carl::LexOrdering = typedef MonomialComparator<Monomial::compareLexical,
false >
11.1.2.33 ModelSubstitutionPtr template<typename Rational , typename Poly >
using carl::ModelSubstitutionPtr = typedef std::unique_ptr<ModelSubstitution<Rational,Poly> >
11.1.2.34 MonomialOrderingFunction using carl::MonomialOrderingFunction = typedef CompareResult(*)(const
Monomial::Arg&, const Monomial::Arg&)
```

```
11.1.2.35 Not template<typename T >
using carl::Not = typedef Bool<!T::value>
Meta-logical negation.
11.1.2.36 OrderedAssignment template<typename T >
using carl::OrderedAssignment = typedef std::vector<std::pair<Variable, T> >
11.1.2.37 pointerEqual template<typename T >
using carl::pointerEqual = typedef carl::equal_to<const T*, false>
11.1.2.38 pointerEqualWithNull template<typename T >
using carl::pointerEqualWithNull = typedef carl::equal.to<const T*, true>
11.1.2.39 pointerHash template<typename T >
using carl::pointerHash = typedef carl::hash<T*, false>
11.1.2.40 pointerHashWithNull template<typename T >
using carl::pointerHashWithNull = typedef carl::hash<T*, true>
11.1.2.41 pointerLess template<typename T >
using carl::pointerLess = typedef carl::less<const T*, false>
11.1.2.42 pointerLessWithNull template<typename T >
using carl::pointerLessWithNull = typedef carl::less<const T*, true>
11.1.2.43 PointerMap template<typename T1 , typename T2 >
using carl::PointerMap = typedef std::map<const T1*, T2, pointerLess<T1> >
```

```
11.1.2.44 PointerMultiSet template<typename T >
using carl::PointerMultiSet = typedef std::multiset<const T*, pointerLess<T> >
11.1.2.45 PointerSet template<typename T >
using carl::PointerSet = typedef std::set<const T*, pointerLess<T> >
11.1.2.46 precision_t using carl::precision_t = typedef std::size_t
11.1.2.47 sharedPointerEqual template<typename T >
using carl::sharedPointerEqual = typedef carl::equal_to<std::shared_ptr<const T>, false>
11.1.2.48 sharedPointerEqualWithNull template<typename T >
using carl::sharedPointerEqualWithNull = typedef carl::equal_to<std::shared.ptr<const T>,
true>
11.1.2.49 sharedPointerHash template<typename T >
using carl::sharedPointerHash = typedef carl::hash<std::shared.ptr<const T>*, false>
11.1.2.50 sharedPointerHashWithNull template<typename T >
using carl::sharedPointerHashWithNull = typedef carl::hash<std::shared_ptr<const T>*, true>
11.1.2.51 sharedPointerLess template<typename T >
using carl::sharedPointerLess = typedef carl::less<std::shared.ptr<const T>*, false>
11.1.2.52 sharedPointerLessWithNull template<typename T >
using carl::sharedPointerLessWithNull = typedef carl::less<std::shared.ptr<const T>, true>
```

```
11.1.2.53 SharedPointerMap template<typename T1 , typename T2 >
using carl::SharedPointerMap = typedef std::map<std::shared.ptr<const T1>, T2, sharedPointerLess<T1>
11.1.2.54 SharedPointerMultiSet template<typename T >
using carl::SharedPointerMultiSet = typedef std::multiset<std::shared_ptr<const T>, sharedPointerLess<T>
11.1.2.55 SharedPointerSet template<typename T >
using carl::SharedPointerSet = typedef std::set<std::shared_ptr<const T>, sharedPointerLess<T>
11.1.2.56 sint using carl::sint = typedef std::int64_t
11.1.2.57 TypeInfoPair template<typename T , class I >
using carl::TypeInfoPair = typedef std::pair<T*,I>
11.1.2.58 uint using carl::uint = typedef std::uint64_t
11.1.2.59 UnivariatePolynomialPtr template<typename Coefficient >
using carl::UnivariatePolynomialPtr = typedef std::shared_ptr<UnivariatePolynomial<Coefficient>
11.1.2.60 Variables using carl::Variables = typedef std::set<Variable>
11.1.3 Enumeration Type Documentation
11.1.3.1 BoundType enum carl::BoundType [strong]
```

# Enumerator

| STRICT | the given bound is compared by a strict ordering relation   |
|--------|---|
| WEAK   | the given bound is compared by a weak ordering relation   |
| INFTY  | the given bound is interpreted as minus or plus infinity depending on whether it is the left or the right bound |

# 11.1.3.2 BVCompareRelation enum carl::BVCompareRelation : unsigned [strong]

### Enumerator

| EQ  |  |
|-----|--|
| NEQ |  |
| ULT |  |
| ULE |  |
| UGT |  |
| UGE |  |
| SLT |  |
| SLE |  |
| SGT |  |
| SGE |  |

# 11.1.3.3 BVTermType enum carl::BVTermType [strong]

| CONSTANT |  |
|----------|--|
| VARIABLE |  |
| CONCAT   |  |
| EXTRACT  |  |
| NOT      |  |
| NEG      |  |
| AND      |  |
| OR       |  |
| XOR      |  |
| NAND     |  |
| NOR      |  |
| XNOR     |  |
| ADD      |  |
| SUB      |  |
| MUL      |  |
| DIV_U    |  |
| DIV₋S    |  |
| MOD_U    |  |
| MOD₋S1   |  |
| MOD₋S2   |  |
|          |  |

# Enumerator

| EQ           |  |
|--------------|--|
| LSHIFT       |  |
| RSHIFT_LOGIC |  |
| RSHIFT₋ARITH |  |
| LROTATE      |  |
| RROTATE      |  |
| EXT₋U        |  |
| EXT₋S        |  |
| REPEAT       |  |
|              |  |

# 11.1.3.4 CARL\_RND enum carl::CARL\_RND : int [strong]

# Enumerator

| N |  |
|---|--|
| Z |  |
| U |  |
| D |  |
| Α |  |

# 11.1.3.5 CompareResult enum carl::CompareResult [strong]

# Enumerator

| LESS    |  |
|---------|--|
| EQUAL   |  |
| GREATER |  |

# 11.1.3.6 Definiteness enum carl::Definiteness [strong]

Regarding a polynomial p as a function  $p:X\to Y$ , its definiteness gives information about the codomain Y.

| NEGATIVE      | Indicates that $y < 0 \forall y \in Y$ .            |
|---------------|---|
| NEGATIVE_SEMI | Indicates that $y \leq 0 \forall y \in Y$ .         |
| NON           | Indicates that values may be positive and negative. |
| POSITIVE_SEMI | Indicates that $y \ge 0 \forall y \in Y$ .          |
| POSITIVE      | Indicates that $y > 0 \forall y \in Y$ .            |

# 11.1.3.7 FormulaType enum carl::FormulaType

Represent the type of a formula to allow faster/specialized processing.

For each (supported) SMTLIB theory, we have

- Constants
- Variables
- Functions
- Additional functions (not specified, but used in the wild)

# Enumerator

| ITE        |  |
|------------|--|
| EXISTS     |  |
| FORALL     |  |
| TRUE       |  |
| FALSE      |  |
| BOOL       |  |
| NOT        |  |
| NOT        |  |
| IMPLIES    |  |
| AND        |  |
| AND        |  |
| OR         |  |
| OR         |  |
| XOR        |  |
| XOR        |  |
| IFF        |  |
| CONSTRAINT |  |
| VARCOMPARE |  |
| VARASSIGN  |  |
| BITVECTOR  |  |
| UEQ        |  |
|            |  |

# 11.1.3.8 Logic enum carl::Logic [strong]

| QF₋BV   |  |
|---------|--|
| QF_IDL  |  |
| QF_LIA  |  |
| QF_LIRA |  |
| QF₋LRA  |  |

# Enumerator

| QF_NIA    |  |
|-----------|--|
| QF₋NIRA   |  |
| QF₋NRA    |  |
| QF₋PB     |  |
| QF_RDL    |  |
| QF₋UF     |  |
| UNDEFINED |  |

# 11.1.3.9 PolynomialComparisonOrder enum carl::PolynomialComparisonOrder [strong]

### Enumerator

| CauchyBound |  |
|-------------|--|
| LowDegree   |  |
| Memory      |  |
| Default     |  |

# 11.1.3.10 Relation enum carl::Relation [strong]

# Enumerator

| EQ      |  |
|---------|--|
| NEQ     |  |
| LESS    |  |
| LEQ     |  |
| GREATER |  |
| GEQ     |  |

# 11.1.3.11 Sign enum carl::Sign [strong]

This class represents the sign of a number n.

| NEGATIVE | Indicates that $n < 0$ . |
|----------|--------------------------|
| ZERO     | Indicates that $n=0$ .   |
| POSITIVE | Indicates that $n > 0$ . |

# 11.1.3.12 Str2Double\_Error enum carl::Str2Double\_Error

### Enumerator

| FLOAT_SUCCESS       |  |
|---------------------|--|
| FLOAT_OVERFLOW      |  |
| FLOAT_UNDERFLOW     |  |
| FLOAT_INCONVERTIBLE |  |

# 11.1.3.13 SubresultantStrategy enum carl::SubresultantStrategy [strong]

#### Enumerator

| Generic |  |
|---------|--|
| Lazard  |  |
| Ducos   |  |
| Default |  |

# 11.1.3.14 ThomComparisonResult enum carl::ThomComparisonResult

#### Enumerator

| LESS    |  |
|---------|--|
| LESS    |  |
| LESS    |  |
| EQUAL   |  |
| EQUAL   |  |
| GREATER |  |
| GREATER |  |
| GREATER |  |

# 11.1.3.15 variableSelectionHeurisics enum carl::variableSelectionHeurisics

| _ |            |  |
|---|------------|--|
|   | GREEDY_I   |  |
| ſ | GREEDY_Is  |  |
| ſ | GREEDY_II  |  |
| Ī | GREEDY_IIs |  |

# 11.1.3.16 VariableType enum carl::VariableType [strong]

Several types of variables are supported.

BOOL: the Booleans REAL: the reals INT: the integers UNINTERPRETED: all uninterpreted types BITVECTOR: bitvectors of any length

#### Enumerator

| VT_BOOL          |  |
|------------------|--|
| VT_REAL          |  |
| VT_INT           |  |
| VT_UNINTERPRETED |  |
| VT_BITVECTOR     |  |
| MIN_TYPE         |  |
| MAX_TYPE         |  |
| TYPE_SIZE        |  |

### 11.1.4 Function Documentation

Get absolute value of an integer.

**Parameters** 

```
n An integer.
```

Returns

|n|.

Get absolute value of a fraction.

**Parameters** 

```
n A fraction.
```

#### Returns

|n|.

Method which returns the absolute value of the passed number.

#### **Parameters**

| $\leftarrow$ | Number. |
|--------------|---------|
| _←           |         |
| in           |         |

#### Returns

Number which holds the result.

```
11.1.4.4 abs() [4/10] template<typename IntegerT > GFNumber<IntegerT> carl::abs ( const GFNumber< IntegerT > & n)
```

Method which returns the absolute value of the passed number.

### **Parameters**

| $\leftarrow$ | Number. |
|--------------|---------|
| _←           |         |
| in           |         |

### Returns

Number which holds the result.

```
11.1.4.6 abs() [6/10] template<typename Number >
static IntRepRealAlgebraicNumber<Number> carl::abs (
             \verb|const IntRepRealAlgebraicNumber< Number > & n | [static]|
11.1.4.7 abs() [7/10] mpq_class carl::abs (
             const mpq_class & n ) [inline]
11.1.4.8 abs() [8/10] mpz_class carl::abs (
             \verb|const mpz_class & n | | [inline]|
Basic Operators.
The following functions implement simple operations on the given numbers.
11.1.4.9 abs() [9/10] template<typename Number >
RealAlgebraicNumberThom<Number> carl::abs (
             const RealAlgebraicNumberThom< Number > \& n)
11.1.4.10 abs() [10/10] double carl::abs (
             double n ) [inline]
11.1.4.11 acos() [1/3] template<typename FloatType >
FLOAT_T<FloatType> carl::acos (
             const FLOAT_T< FloatType > \& \_in ) [inline]
11.1.4.12 acos() [2/3] template<typename Number , EnableIf< std::is.floating.point< Number >>
= dummy>
Interval<Number> carl::acos (
            const Interval< Number > & i )
11.1.4.13 acos() [3/3] double carl::acos (
             double in ) [inline]
```

```
11.1.4.14 acos_assign() template<typename Number , EnableIf< std::is_floating_point< Number >>
= dummv>
void carl::acos_assign (
            Interval< Number > & i )
11.1.4.15 acosh() template<typename Number , EnableIf< std::is_floating_point< Number >> =
dummy>
Interval<Number> carl::acosh (
            const Interval< Number > & i )
11.1.4.16 acosh_assign() template<typename Number , EnableIf< std::is_floating_point< Number
>> = dummy>
void carl::acosh_assign (
            Interval< Number > & i )
11.1.4.17 addConstraintBound() template<typename Pol >
Formula<Pol> carl::addConstraintBound (
            ConstraintBoundsPol > & _constraintBounds,
            const Formula< Pol > & _constraint,
            bool _inConjunction )
```

Adds the bound to the bounds of the polynomial specified by this constraint.

E.g., if the constraint is p+b $\sim$ 0, where p is a sum of terms, being a rational (actually integer) coefficient times a non-trivial (!=1) monomial( product of variables to the power of an exponent), b is a rational and  $\sim$  is any constraint relation. Furthermore, the leading coefficient of p is 1. Then we add the bound -b to the bounds of p (means that p  $\sim$  -b) stored in the given constraint bounds.

#### **Parameters**

| ₋constraintBounds | An object collecting bounds of polynomials.   |  |
|-------------------|---|--|
| _constraint       | The constraint to find a bound for a polynomial for.  |  |
| ₋inConjunction    | inConjunction true, if the constraint is part of a conjunction. false, if the constraint is part of a disjunc |  |

# Returns

Formula<Pol>( FALSE ), if the yet determined bounds imply that the conjunction (\_inConjunction == true) or disjunction (\_inConjunction == false) of which we got the given constraint is invalid resp. valid; false, the added constraint.

```
const Number & A,
const Number & B,
unsigned = 128 ) [inline]
```

# 11.1.4.19 AlmostEqual2sComplement< double >() template<>

## 11.1.4.20 AlmostEqual2sComplement< FLOAT\_T< double >>() template<>

# 11.1.4.21 arithmetic\_constraints() [1/2] template<typename Pol >

```
void carl::arithmetic_constraints ( const\ Formula <\ Pol\ >\ \&\ f, std::vector <\ Constraint <\ Pol\ >>\ \&\ constraints\ )
```

Collects all constraint occurring in this formula.

**Parameters** 

constraints The container to insert the constraint into.

# 11.1.4.22 arithmetic\_constraints() [2/2] template<typename Pol >

Collects all constraint occurring in this formula.

**Parameters** 

constraints The container to insert the constraint into.

```
carlVariables carl::arithmetic_variables ( {\tt const\ T\ \&\ t\ )} \quad [{\tt inline}]
```

```
11.1.4.24 as_constraint() template<typename Poly > std::optional<BasicConstraint<Poly> > carl::as_constraint ( const VariableComparison< Poly > & f )
```

Convert this variable comparison "v < root(..)" into a simpler polynomial (in)equality against zero "p(..) < 0" if that is possible.

**Returns** 

std::nullopt if conversion impossible.

```
11.1.4.25 asin() [1/2] template<typename FloatType >
FLOAT_T<FloatType> carl::asin (
            const FLOAT_T< FloatType > & _in ) [inline]
11.1.4.26 asin() [2/2] template<typename Number , EnableIf< std::is_floating_point< Number >>
= dummy >
Interval<Number> carl::asin (
            const Interval< Number > & i )
11.1.4.27 asin_assign() template<typename Number , EnableIf< std::is_floating_point< Number >>
= dummy>
void carl::asin_assign (
            Interval< Number > & i )
11.1.4.28 asinh() template<typename Number , EnableIf< std::is_floating_point< Number >> =
dummy>
Interval<Number> carl::asinh (
           const Interval< Number > & i )
11.1.4.29 asinh_assign() template<typename Number , EnableIf< std::is_floating_point< Number
>> = dummy>
void carl::asinh_assign (
            Interval < Number > & i )
```

```
11.1.4.30 atan() [1/2] template<typename FloatType >
FLOAT_T<FloatType> carl::atan (
            \verb|const FLOAT_T| < \verb|FloatType| > \& \_in | ) | [inline]
11.1.4.31 atan() [2/2] template<typename Number , EnableIf< std::is_floating_point< Number >>
= dummy>
Interval<Number> carl::atan (
            const Interval< Number > & i )
11.1.4.32 atan_assign() template<typename Number , EnableIf< std::is_floating_point< Number >>
= dummy>
void carl::atan_assign (
            Interval< Number > & i )
11.1.4.33 atanh() template<typename Number , EnableIf< std::is_floating_point< Number >> =
dummy>
Interval<Number> carl::atanh (
            const Interval< Number > & i )
11.1.4.34 atanh_assign() template<typename Number , EnableIf< std::is_floating_point< Number
>> = dummy>
void carl::atanh_assign (
            Interval< Number > & i )
11.1.4.35 basename() std::string carl::basename (
             const std::string & filename ) [inline]
Return the basename of a given filename.
11.1.4.36 binary() template<typename T >
std::string carl::binary (
             const T & a,
```

Return the binary representation given value as bit string.

const bool & spacing = true )

Note that this method is tailored to little endian systems.

| а       | A value of any type                                   |  |
|---------|---|--|
| spacing | Specifies if the bytes shall be separated by a space. |  |

### Returns

Bit string representing a.

Get the bit size of the representation of a integer.

## **Parameters**

```
n An integer.
```

### **Returns**

Bit size of n.

Get the bit size of the representation of a fraction.

### **Parameters**

```
n A fraction.
```

### Returns

Bit size of n.

```
11.1.4.40 bitsize() [4/9] std::size_t carl::bitsize (

const Monomial & m ) [inline]
```

An approximation of the bitsize of this monomial.

Get the bit size of the representation of a fraction.

**Parameters** 

```
n A fraction.
```

Returns

Bit size of n.

```
11.1.4.42 bitsize() [6/9] std::size_t carl::bitsize ( const mpz_class & n ) [inline]
```

Get the bit size of the representation of a integer.

**Parameters** 

```
n An integer.
```

Returns

Bit size of n.

Returns

An approximation of the bitsize of this polynomial.

An approximation of the bitsize of this term.

```
11.1.4.45 bitsize() [9/9] std::size_t carl::bitsize (
             unsigned ) [inline]
11.1.4.46 bitvector_variables() [1/2] template<typename Pol >
void carl::bitvector_variables (
             const Formula < Pol > & f,
             std::set< BVVariable > & bvvs )
11.1.4.47 bitvector_variables() [2/2] template<typename T >
carlVariables carl::bitvector_variables (
            const T & t ) [inline]
11.1.4.48 boolean_variables() template<typename T >
carlVariables carl::boolean_variables (
            const T & t ) [inline]
11.1.4.49 bounds_connect() template<typename Number >
bool carl::bounds_connect (
             const UpperBound< Number > & lhs,
             \verb|const LowerBound| < \verb|Number| > \& rhs | | [inline]|
```

Check whether the two bounds connect, for example as for ...3),[3...

```
11.1.4.50 branching_point() [1/3] template<typename Number > Number carl::branching_point ( const IntRepRealAlgebraicNumber< Number > & n)
```

```
\textbf{11.1.4.51} \quad \textbf{branching\_point()} \; \texttt{[2/3]} \quad \texttt{template} < \texttt{typename} \; \texttt{Number} \; \text{,} \; \texttt{typename} \; \texttt{=} \; \texttt{std::enable\_if\_t} < \texttt{is\_} \leftarrow \texttt{-} \; \texttt{-} \;
number_type<Number>::value>>
const Number& carl::branching_point (
                                                                             const Number & n )
11.1.4.52 branching_point() [3/3] template<typename Number >
Number carl::branching_point (
                                                                                  const RealAlgebraicNumberThom< Number > & n)
11.1.4.53 callingFunction() std::string carl::callingFunction ( )
11.1.4.54 cauchyBound() template<typename Coeff >
Coeff carl::cauchyBound (
                                                                                  const UnivariatePolynomial < Coeff > & p )
11.1.4.55 ceil() [1/9] cln::cl_I carl::ceil (
                                                                                   const cln::cl_I & n ) [inline]
Round up an integer.
 Parameters
                               An integer.
 Returns
                               \lceil n \rceil.
11.1.4.56 ceil() [2/9] cln::cl_I carl::ceil (
                                                                                  \verb|const cln::cl_RA & n | [inline]|
Round up a fraction.
 Parameters
                                A fraction.
```

 $\lceil n \rceil$ .

Method which returns the next larger integer of the passed number or the number itself, if it is already an integer.

#### **Parameters**

| $\leftarrow$ | Number. |
|--------------|---------|
| _←           |         |
| in           |         |

### Returns

Number which holds the result.

Method which returns the next larger integer of the passed number or the number itself, if it is already an integer.

### **Parameters**

### Returns

Number which holds the result.

```
11.1.4.60 ceil() [6/9] mpz_class carl::ceil ( const mpq_class & n ) [inline]
```

```
11.1.4.61 ceil() [7/9] mpz_class carl::ceil (
             const mpz_class & n ) [inline]
11.1.4.62 ceil() [8/9] template<typename Number >
Number carl::ceil (
            const RealAlgebraicNumberThom< Number > \& n)
11.1.4.63 ceil() [9/9] double carl::ceil (
             double n ) [inline]
11.1.4.64 center() template<typename Number >
Number carl::center (
            const Interval< Number > & i )
Returns the center point of the interval.
Returns
    Center.
11.1.4.65 charPol() template<typename Coeff >
std::vector<Coeff> carl::charPol (
            const CoeffMatrix< Coeff > & m )
11.1.4.66 CMakeOptions() constexpr CMakeOptionPrinter carl::CMakeOptions (
             bool advanced = false ) [constexpr], [noexcept]
11.1.4.67 collectUFVars() void carl::collectUFVars (
             std::set< UVariable > & uvars,
             UFInstance ufi )
```

Compares \_constraintA with \_constraintB.

### Returns

2, if it is easy to decide that \_constraintA and \_constraintB have the same solutions. \_constraintA = \_constraintB 1, if it is easy to decide that \_constraintB includes all solutions of \_constraintA; \_constraintA -> \_constraintB -1, if it is easy to decide that \_constraintA includes all solutions of \_constraintB; \_constraintB -> \_constraintA -2, if it is easy to decide that \_constraintA has no solution common with \_constraintB; not(\_constraintA and \_constraintB) -3, if it is easy to decide that \_constraintA and \_constraintB can be intersected; \_constraintA and \_constraintB = \_constraintC -4, if it is easy to decide that \_constraintA is the inverse of \_constraintB; \_constraintA xor \_constraintB 0, otherwise.

```
11.1.4.69 compare() [2/4] template<typename Pol >
auto carl::compare (
             const Constraint < Pol > & c1,
             const Constraint< Pol > & c2 )
11.1.4.70 compare() [3/4] template<typename Number >
bool carl::compare (
             const IntRepRealAlgebraicNumber < Number > & lhs,
             const IntRepRealAlgebraicNumber < Number > & rhs,
             const Relation relation )
11.1.4.71 compare() [4/4] template<typename Number >
bool carl::compare (
             const IntRepRealAlgebraicNumber < Number > & lhs,
             const Number & rhs,
             const Relation relation )
11.1.4.72 complexity() [1/6] template<typename Poly >
std::size_t carl::complexity (
             const BasicConstraint < Poly > & c )
```

## Returns

An approximation of the complexity of this constraint.

```
11.1.4.73 complexity() [2/6] template<typename Pol > size t carl::complexity ( const Formula< Pol > & f )
```

An approximation of the complexity of this monomial.

```
11.1.4.75 complexity() [4/6] template<typename Coeff , typename Ordering , typename Policies > std::size_t carl::complexity ( const MultivariatePolynomial< Coeff, Ordering, Policies > & p )
```

Returns

An approximation of the complexity of this polynomial.

Returns

An approximation of the complexity of this term.

Returns

An approximation of the complexity of this polynomial.

Obtains the polynomial (representation) of this factorized polynomial.

Note, that the result won't be stored in the factorized polynomial, hence, this method should only be called for debug purpose.

| £ 1    | The feet wine does be a consider a set it and the continue and a feet will be a continue and the continue an |
|--------|--|
| _fpoly | The factorized polynomial to get its polynomial (representation) for.  |
|        |  |

## Returns

The polynomial (representation) of this factorized polynomial

Compute the polynomial from the given polynomial-factorization pair.

### **Parameters**

| ₋fpPair | A polynomial-factorization pair. |
|---------|----------------------------------|
|---------|----------------------------------|

#### Returns

The polynomial.

Checks whether this constraint is consistent with the given assignment from the its variables to interval domains.

## **Parameters**

```
_solutionInterval | The interval domains of the variables.
```

### Returns

1, if this constraint is consistent with the given intervals; 0, if this constraint is not consistent with the given intervals; 2, if it cannot be decided whether this constraint is consistent with the given intervals.

```
11.1.4.81 consistent_with() [2/2] template<typename Pol > static unsigned carl::consistent_with ( const BasicConstraint< Pol > & c,
```

```
const Assignment< Interval< double >> & _solutionInterval,
Relation & _stricterRelation ) [static]
```

Checks whether this constraint is consistent with the given assignment from the its variables to interval domains.

| ₋solutionInterval | The interval domains of the variables.   |  |
|-------------------|--|--|
| _stricterRelation | This relation is set to a relation R such that this constraint and the given variable bounds |  |
|                   | imply the constraint formed by R, comparing this constraint's left-hand side to zero.        |  |

### Returns

1, if this constraint is consistent with the given intervals; 0, if this constraint is not consistent with the given intervals; 2, if it cannot be decided whether this constraint is consistent with the given intervals.

The content of a polynomial is the gcd of the coefficients of the normal part of a polynomial.

The content of zero is zero.

See also

?, page 53, definition 2.18

### Returns

The content of the polynomial.

```
11.1.4.86 convert() [3/9] template<typename From , typename To , carl::DisableIf< std::is_same<
From, To > = dummy>
Interval< To > carl::convert (
                                                       const Interval < From > & i ) [inline]
11.1.4.87 convert() [4/9] template<typename T , typename S , std::enable_if_t< is_polynomial.←
type< T >::value &&is_polynomial_type< S >::value &&!needs_context_type< T >::value, int > =
0>
T carl::convert (
                                                         const S & r ) [inline]
\textbf{11.1.4.88} \quad \textbf{convert()} \; \texttt{[5/9]} \quad \texttt{template} < \texttt{typename T} \; \text{, std::enable\_if\_t} < \; \texttt{is\_ran\_type} < \; \texttt{T} > :: \texttt{value, int} 
> = 0>
T carl::convert (
                                                       const T & r ) [inline]
\textbf{11.1.4.89} \quad \textbf{convert()} \; \texttt{[6/9]} \quad \texttt{template} < \texttt{typename} \; \texttt{T} \; \text{, } \; \texttt{typename} \; \texttt{S} \; \text{, } \; \texttt{std::enable\_if\_t} < \; \texttt{is\_polynomial} \leftarrow \; \texttt{Convert()} \; \texttt{Std::enable\_if\_t} < \;
 \texttt{\_type} < \texttt{T} > :: \texttt{value \&\&is\_polynomial\_type} < \texttt{S} > :: \texttt{value \&\&needs\_context\_type} < \texttt{T} > :: \texttt{value, int} > = \texttt{S} < \texttt{value, int} > \texttt{value, int} >
0>
T carl::convert (
                                                         const typename T::ContextType & c,
                                                          const S & r ) [inline]
11.1.4.90 convert() [7/9] template<typename ToPoly , typename FromPoly , typename = std::enable \leftarrow
_if_t<needs_context_type<ToPoly>::value>>
BasicConstraint<ToPoly> carl::convert (
                                                          const typename ToPoly::ContextType & context,
                                                          const BasicConstraint< FromPoly > \& c ) [inline]
11.1.4.91 convert() [8/9] template<typename ToPoly , typename FromPoly , typename = std::enable \leftarrow
_if_t<needs_context_type<ToPoly>::value>>
VariableComparison<ToPoly> carl::convert (
                                                          const typename ToPoly::ContextType & context,
                                                          const VariableComparison<br/>< FromPoly > & c ) [inline]
11.1.4.92 convert() [9/9] template<typename ToPoly , typename FromPoly , typename = std::enable \leftarrow
_if_t<!needs_context_type<ToPoly>::value>>
VariableComparison<ToPoly> carl::convert (
                                                          const VariableComparison<br/>< FromPoly > \& c ) [inline]
```

```
11.1.4.93 convert< double, FLOAT_T< double > >() template<>
FLOAT_T < double > carl::convert < double, FLOAT_T < double > > (
            const double & n ) [inline]
11.1.4.94 convert< double, FLOAT_T< mpq_class >>() template<>
FLOAT_T<mpq_class> carl::convert< double, FLOAT_T< mpq_class > > (
            const double & n ) [inline]
11.1.4.95 convert< double, mpq_class >() template<>
mpq_class carl::convert< double, mpq_class > (
            const double & n ) [inline]
11.1.4.96 convert< FLOAT_T< double >, double >() template<>
double carl::convert< FLOAT_T< double >, double > (
            const FLOAT_T< double > & n ) [inline]
11.1.4.97 convert< FLOAT_T< double >, mpq_class >() template<>
mpq_class carl::convert< FLOAT.T< double >, mpq_class > (
            const FLOAT_T< double > & n ) [inline]
11.1.4.98 convert< FLOAT_T< mpq_class >, double >() template<>
double carl::convert< FLOAT_T< mpq_class >, double > (
            const FLOAT_T< mpq_class > & n ) [inline]
11.1.4.99 convert< FLOAT_T< mpq_class >, mpq_class >() template<>
mpq.class carl::convert< FLOAT.T< mpq.class >, mpq.class > (
            const FLOAT_T< mpq_class > & n ) [inline]
11.1.4.100 convert< mpq_class, double >() template<>
double carl::convert< mpq_class, double > (
           const mpq_class & n ) [inline]
```

```
11.1.4.101 convert< mpq_class, FLOAT_T< double > >() template<>
const mpq_class & n ) [inline]
11.1.4.102 convert< mpq_class, FLOAT_T< mpq_class >>() template<>
FLOAT_T<mpq_class> carl::convert< mpq_class, FLOAT_T< mpq_class > > (
            \verb|const mpq-class & n | | [inline]|
11.1.4.103 convert_to_mvroot() template<typename Poly >
MultivariateRoot<Poly> carl::convert_to_mvroot (
            const typename MultivariateRoot< Poly >::RAN & ran,
            Variable var )
11.1.4.104 coprimePart() template<typename C , typename O , typename P >
MultivariatePolynomial<C,O,P> carl::coprimePart (
            const MultivariatePolynomial < C, O, P > & p,
            const Multivariate
Polynomial<br/>< C, O, P > & q )
Calculates the coprime part of p and q.
11.1.4.105 cos() [1/5] cln::cl_RA carl::cos (
            const cln::cl_RA & n ) [inline]
11.1.4.106 cos() [2/5] template<typename FloatType >
FLOAT_T<FloatType> carl::cos (
            const FLOAT_T< FloatType > & _in ) [inline]
11.1.4.107 cos() [3/5] template<typename Number , EnableIf< std::is_floating_point< Number >>
= dummy>
Interval<Number> carl::cos (
           const Interval< Number > & i )
11.1.4.108 cos() [4/5] mpq_class carl::cos (
            const mpq\_class \& n) [inline]
```

```
11.1.4.109 cos() [5/5] double carl::cos (
            double in ) [inline]
11.1.4.110 cos_assign() template<typename Number , EnableIf< std::is_floating_point< Number >>
= dummy>
void carl::cos_assign (
            Interval< Number > & i )
11.1.4.111 cosh() template<typename Number , EnableIf< std::is.floating_point< Number >> =
dummy>
Interval<Number> carl::cosh (
            const Interval< Number > & i )
11.1.4.112 cosh_assign() template<typename Number , EnableIf< std::is_floating_point< Number
>> = dummy>
void carl::cosh_assign (
            Interval< Number > & i )
11.1.4.113 count_real_roots() [1/2] template<typename Coefficient >
int carl::count_real_roots (
            const std::vector< UnivariatePolynomial< Coefficient >> & seq,
            const Interval< Coefficient > & i )
```

Calculate the number of real roots of a polynomial within a given interval based on a sturm sequence of this polynomial.

### **Parameters**

| seq | Sturm sequence. |
|-----|-----------------|
| i   | Interval.       |

# Returns

Number of real roots in the interval.

Count the number of real roots of p within the given interval using Sturm sequences.

| р | The polynomial.                   |  |
|---|-----------------------------------|--|
| i | Count roots within this interval. |  |

#### Returns

Number of real roots within the interval.

```
11.1.4.115 createMonomial() template<typename... T>
Monomial::Arg carl::createMonomial (
                                                          T &&... t ) [inline]
\textbf{11.1.4.116} \quad \textbf{createSubstitution()} \; \texttt{[1/2]} \quad \texttt{template} < \texttt{typename} \; \texttt{Rational} \; \text{, typename} \; \texttt{Poly} \; \text{, typename} \; \text{, typename} \; \texttt{Poly} \; \text{, typen
Substitution , typename... Args>
ModelValue< Rational, Poly > carl::createSubstitution (
                                                        Args &&... args ) [inline]
11.1.4.117 createSubstitution() [2/2] template<typename Rational , typename Poly >
ModelValue< Rational, Poly > carl::createSubstitution (
                                                         const MultivariateRoot< Poly > & mr ) [inline]
11.1.4.118 createSubstitutionPtr() template<typename Rational , typename Poly , typename Substitution
 , typename... Args>
ModelSubstitutionPtr< Rational, Poly > carl::createSubstitutionPtr (
                                                      Args &&... args ) [inline]
11.1.4.119 defaultSortValue() SortValue carl::defaultSortValue (
                                                          const Sort & sort ) [inline]
```

# Parameters

sort The sort to return the default value for.

Returns the default value for the given sort.

The resulting sort value.

Return a polynomial containing the lhs-variable that has a same root for the this lhs-variable as the value that rhs represent, e.g.

if this variable comparison is 'v < 3' then a defining polynomial could be 'v-3', because it has the same root for variable v, i.e., v=3.

```
11.1.4.121 definiteness() [1/2] template<typename C , typename O , typename P >
Definiteness carl::definiteness (
            const MultivariatePolynomial < C, O, P > & p,
             bool full_effort = true )
11.1.4.122 definiteness() [2/2] template<typename Coeff >
Definiteness carl::definiteness (
            const Term< Coeff > & t)
11.1.4.123 demangle() std::string carl::demangle (
             const char * name )
11.1.4.124 der() template<typename Number >
std::list<MultivariatePolynomial<Number> > carl::der (
            const MultivariatePolynomial< Number > & p,
            Variable::Arg var,
            uint from,
             uint upto )
11.1.4.125 derivative() [1/6] std::pair<std::size_t,Monomial::Arg> carl::derivative (
             const Monomial::Arg & m,
             Variable v,
             std::size_t n = 1) [inline]
```

Computes the (partial) n'th derivative of this monomial with respect to the given variable.

| m | Monomial to derive. |  |
|---|---------------------|--|
| V | Variable.           |  |
| n | n.                  |  |

### **Returns**

Partial n'th derivative, consisting of constant factor and the remaining monomial.

Computes the n'th derivative of p with respect to v.

Computes the n'th derivative of a number, which is either the number itself (for n = 0) or zero.

Computes the n'th derivative of t with respect to v.

```
11.1.4.129 derivative() [5/6] template<typename C > UnivariatePolynomial<C> carl::derivative ( const UnivariatePolynomial< C > & p, std::size_t n=1)
```

Computes the n'th derivative of p with respect to the main variable of p.

Computes the n'th derivative of p with respect to v.

Divide two integers.

Asserts that the remainder is zero.

const cln::cl\_I & b ) [inline]

#### **Parameters**

| а | First argument.  |  |
|---|------------------|--|
| b | Second argument. |  |

## Returns

a/b.

Divide two fractions.

| а | First argument.  |  |
|---|------------------|--|
| b | Second argument. |  |

### Returns

a/b.

Implements the division which assumes that there is no remainder.

### **Parameters**

| ₋lhs |  |
|------|--|
| ₋rhs |  |

## Returns

Number which holds the result.

Implements the division which assumes that there is no remainder.

## **Parameters**

| _lhs |  |
|------|--|
| ₋rhs |  |

#### Returns

Interval which holds the result.

```
11.1.4.137 div() [5/7] mpq_class carl::div (

const mpq_class & a,

const mpq_class & b) [inline]
```

Divide two fractions.

## **Parameters**

| а | First argument.  |
|---|------------------|
| b | Second argument. |

### **Returns**

a/b.

Divide two integers.

Asserts that the remainder is zero.

## **Parameters**

| а | First argument.  |
|---|------------------|
| b | Second argument. |

## Returns

a/b.

Divide two integers.

Asserts that the remainder is zero. Stores the result in the first argument.

| а | First argument.  |
|---|------------------|
| b | Second argument. |

### Returns

a/b.

Divide two fractions.

Stores the result in the first argument.

## **Parameters**

| а | First argument.  |
|---|------------------|
| b | Second argument. |

### Returns

a/b.

Divide two integers.

Asserts that the remainder is zero. Stores the result in the first argument.

## **Parameters**

|   | а | First argument.  |
|---|---|------------------|
| ſ | b | Second argument. |

## Returns

a/b.

Divide two integers.

Asserts that the remainder is zero. Stores the result in the first argument.

#### **Parameters**

| а | First argument.  |
|---|------------------|
| b | Second argument. |

### Returns

a/b.

Calculating the quotient and the remainder, such that for a given polynomial p we have p = divisor \* quotient + remainder.

## **Parameters**

| divisor Another polynor | nial |
|-------------------------|------|
|-------------------------|------|

## Returns

A divisionresult, holding the quotient and the remainder.

See also

Note

Division is only defined on fields

Divides the polynomial by the given coefficient.

Applies if the coefficients are from a field.

**Parameters** 

divisor

Returns

```
11.1.4.148 divide() [5/9] template<typename Coeff > Term<Coeff> carl::divide ( const Term< Coeff > & t, const Coeff & c)
```

Divides the polynomial by another polynomial.

### **Parameters**

| dividend | Dividend. |
|----------|-----------|
| divisor  | Divisor.  |

dividend / divisor.

```
11.1.4.150 divide() [7/9] template<typename Coeff >
DivisionResult<UnivariatePolynomial<Coeff> > carl::divide (
            const UnivariatePolynomial< Coeff > & p,
            const Coeff & divisor )
11.1.4.151 divide() [8/9] template<typename Coeff >
DivisionResult<UnivariatePolynomial<Coeff> > carl::divide (
            const UnivariatePolynomial < Coeff > & p,
            const typename UnderlyingNumberType< Coeff >::type & divisor )
11.1.4.152 divide() [9/9] void carl::divide (
             sint dividend,
             sint divisor,
             sint & quo,
             sint & rem ) [inline]
11.1.4.153 doNothing() template<typename T >
void carl::doNothing (
            const T & ,
            const T & )
11.1.4.154 eliminate_root() template<typename Coeff >
void carl::eliminate_root (
            UnivariatePolynomial < Coeff > & p,
             const Coeff & root )
```

Reduces the polynomial such that the given root is not a root anymore.

The reduction is achieved by removing the linear factor (mainVar - root) from the polynomial, possibly multiple times.

This method assumes that the given root is an actual real root of this polynomial. If this is not the case, i.e. evaluate(root) != 0, the polynomial will contain meaningless garbage.

### **Parameters**

| р    | The polynomial.        |
|------|------------------------|
| root | Root to be eliminated. |

::RootType > & a)

```
11.1.4.155 eliminate_zero_root() template<typename Coeff >
void carl::eliminate_zero_root (
             UnivariatePolynomial< Coeff > & p )
Reduces the given polynomial such that zero is not a root anymore.
Is functionally equivalent to eliminate_root(0), but faster.
11.1.4.156 encode_as_constraints() [1/2] template<typename Poly >
std::pair<std::vector<BasicConstraint<Poly> >, Variable> carl::encode_as_constraints (
             const MultivariateRoot< Poly > & f,
             Assignment< typename VariableComparison< Poly >::RAN > ass,
             EncodingCache< Poly > cache )
11.1.4.157 encode_as_constraints() [2/2] template<typename Poly >
\verb|std::pair<std::vector<| BasicConstraint<| Poly>>, | BasicConstraint<| Poly>> | carl::encode_as_{\leftarrow}|
constraints (
             const VariableComparison< Poly > & f,
             const Assignment< typename VariableComparison< Poly >::RAN > & ass,
             EncodingCache< Poly > cache )
11.1.4.158 encode_as_constraints_simple() template<typename Poly >
void carl::encode_as_constraints_simple (
             const MultivariateRoot < Poly > & f_{i}
             Assignment< typename VariableComparison< Poly >::RAN > ass,
             Variable var,
             std::vector< BasicConstraint< Poly >> & out )
11.1.4.159 encode_as_constraints_thom() template<typename Poly >
void carl::encode_as_constraints_thom (
             const MultivariateRoot< Poly > & f,
             Assignment< typename VariableComparison< Poly >::RAN > ass,
             Variable var,
             std::vector < BasicConstraint < Poly >> & out )
11.1.4.160 evaluate() [1/27] template<typename Coeff , typename Ordering , typename Policies >
auto carl::evaluate (
             const BasicConstraint< ContextPolynomial< Coeff, Ordering, Policies >> & p,
```

const Assignment< typename ContextPolynomial< Coeff, Ordering, Policies  $> \leftarrow$ 

```
11.1.4.161 evaluate() [2/27] template<typename Number >
boost::tribool carl::evaluate (
             const BasicConstraint<br/>< MultivariatePolynomial<br/>< Number >> & c \mbox{,}
             const Assignment<br/>< IntRepRealAlgebraicNumber<br/>< Number >> & \textit{m,}
             bool refine_model = true,
             bool use_root_bounds = true )
11.1.4.162 evaluate() [3/27] template<typename Number , typename Poly >
boost::tribool carl::evaluate (
             const BasicConstraint < Poly > & c,
             const Assignment< Interval< Number >> & map ) [inline]
11.1.4.163 evaluate() [4/27] template<typename Number , typename Poly , typename = std::enable←
_if_t<is_number_type<Number>::value>>
bool carl::evaluate (
             const BasicConstraint< Poly > & c,
             const Assignment< Number > & m )
11.1.4.164 evaluate() [5/27] template<typename Number , typename Poly >
bool carl::evaluate (
             const BasicConstraint < Poly > & c,
             std::map< Variable, RealAlgebraicNumberThom< Number >> & m )
11.1.4.165 evaluate() [6/27] template<typename Coeff , typename Ordering , typename Policies >
auto carl::evaluate (
             const ContextPolynomial< Coeff, Ordering, Policies > & p,
             \verb|const Assignment| < \verb|typename ContextPolynomial| < \verb|coeff|, Ordering|, Policies > \leftarrow \\
::RootType > & a)
11.1.4.166 evaluate() [7/27] template<typename Coeff , typename Subst >
Subst carl::evaluate (
             const FactorizedPolynomial< Coeff > & p,
             const std::map< Variable, Subst > & substitutions )
```

Like substitute, but expects substitutions for all variables.

# Returns

For a polynomial p, the function value  $p(x_1,...,x_n)$ .

```
11.1.4.167 evaluate() [8/27] template<typename P , typename Numeric >
Interval<Numeric> carl::evaluate (
            const FactorizedPolynomial < P > & p,
             const std::map< Variable, Interval< Numeric >> & map )
11.1.4.168 evaluate() [9/27] template<typename Coefficient >
Coefficient carl::evaluate (
            const Monomial & m,
             const std::map< Variable, Coefficient > & substitutions )
11.1.4.169 evaluate() [10/27] template<typename Numeric >
Interval<Numeric> carl::evaluate (
            const Monomial & m,
            const std::map< Variable, Interval< Numeric >> & map ) [inline]
11.1.4.170 evaluate() [11/27] template<typename PolynomialType , typename Number , class strategy
Interval<Number> carl::evaluate (
            const MultivariateHorner< PolynomialType, strategy > & mvH,
             const std::map< Variable, Interval< Number >> & map ) [inline]
11.1.4.171 evaluate() [12/27] template<typename C , typename P , typename P , typename Substitution↔
Type >
SubstitutionType carl::evaluate (
             const MultivariatePolynomial < C, O, P > & p,
             const std::map< Variable, SubstitutionType > & substitutions )
Like substitute, but expects substitutions for all variables.
Returns
    For a polynomial p, the function value p(x_1,...,x_n).
11.1.4.172 evaluate() [13/27] template<typename Coeff , typename Policy , typename Ordering ,
typename Numeric >
Interval<Numeric> carl::evaluate (
            const MultivariatePolynomial< Coeff, Policy, Ordering > & p,
             const std::map< Variable, Interval< Numeric >> & map ) [inline]
```

Return the emerging algebraic real after pluggin in a subpoint to replace all variables with algebraic reals that are not the root-variable ".z".

#### **Parameters**

m must contain algebraic real assignments for all variables that are not "\_z".

### Returns

std::nullopt if the underlying polynomial has no root with index 'rootldx' at the given subpoint.

Evaluates the square root expression.

Might be not exact when a square root is rounded.

# **Template Parameters**



## **Parameters**

| sqrt_ex  | The square root expression to be evaluated.   |
|----------|---|
| eval_map | Assignments for all variables.  |
| rounding | -1 if square root should be rounded downwards, 1 if the square root should be rounded upwards, 0 if double precision is fine. |

# Returns

std::pair<SqrtEx<Poly>::Rational, bool> The first component is the evaluation result, the second indicates whether the result is exact (true) or rounded (false).

The result is always a ModelValue, though it may be a ModelSubstitution in some cases.

```
11.1.4.177 evaluate() [18/27] template<typename T >
bool carl::evaluate (
            const T & t,
             Relation r ) [inline]
11.1.4.178 evaluate() [19/27] template<typename T1 , typename T2 >
bool carl::evaluate (
            const T1 & lhs,
            Relation r,
            const T2 & rhs ) [inline]
11.1.4.179 evaluate() [20/27] template<typename Coeff , typename Numeric , EnableIf< std::is-\leftarrow
same< Numeric, Coeff >> = dummy>
Interval < Numeric > carl::evaluate (
            const Term< Coeff > & t,
            const std::map< Variable, Interval< Numeric >> & map ) [inline]
11.1.4.180 evaluate() [21/27] template<typename Coefficient >
Coefficient carl::evaluate (
            const Term< Coefficient > & t,
            const std::map< Variable, Coefficient > & map )
11.1.4.181 evaluate() [22/27] template<typename Coeff >
Coeff carl::evaluate (
             const UnivariatePolynomial< Coeff > & p,
             const Coeff & value )
11.1.4.182 evaluate() [23/27] template<typename Numeric , typename Coeff , EnableIf< std::is.↔
same< Numeric, Coeff >> = dummy>
Interval<Numeric> carl::evaluate (
            const UnivariatePolynomial< Coeff > & p,
             const std::map< Variable, Interval< Numeric >> & map ) [inline]
```

Evaluate the given polynomial with the given values for the variables.

Asserts that all variables of p have an assignment in m and that m has no additional assignments.

Returns std::nullopt if some unassigned variables are still contained in p after plugging in m.

### **Parameters**

| р | Polynomial to be evaluated |
|---|----------------------------|
| m | Variable assignment        |

## Returns

Evaluation result

Evaluates a bitvector constraint to a ModelValue over a Model.

Evaluates a bitvector term to a ModelValue over a Model.

Evaluates a uninterpreted variable to a ModelValue over a Model.

Evaluates a uninterpreted function instance to a ModelValue over a Model.

Evaluates a uninterpreted variable to a ModelValue over a Model.

Evaluates a constraint to a ModelValue over a Model.

If evaluation can not be done for some variables, the result may actually be a Constraint again.

Evaluates a formula to a ModelValue over a Model.

If evaluation can not be done for some variables, the result may actually be a ModelPolynomialSubstitution.

Evaluates a MultivariateRoot to a ModelValue over a Model.

If evaluation can not be done for some variables, the result may actually be a ModelMVRootSubstitution.

Evaluates a polynomial to a ModelValue over a Model.

If evaluation can not be done for some variables, the result may actually be a ModelPolynomialSubstitution.

```
11.1.4.196 evaluateTE() template<typename Number >
RealAlgebraicNumber<Number> carl::evaluateTE (
              const MultivariatePolynomial< Number > & p,
              std::map< Variable, RealAlgebraicNumber< Number >> & m )
11.1.4.197 exp() template<typename Number , EnableIf< std::is_floating_point< Number >> =
dummy>
Interval < Number > carl::exp (
              const Interval < Number > & i )
\textbf{11.1.4.198} \quad \textbf{exp\_assign()} \quad \texttt{template} < \texttt{typename Number , EnableIf} < \textit{std} :: \texttt{is\_floating\_point} < \textit{Number } >> \\
= dummy>
void carl::exp_assign (
              Interval< Number > & i )
11.1.4.199 extended_gcd() template<typename Coeff >
UnivariatePolynomial<Coeff> carl::extended_gcd (
              const UnivariatePolynomial< Coeff > & a,
              const UnivariatePolynomial < Coeff > & b,
              UnivariatePolynomial < Coeff > & s,
              UnivariatePolynomial< Coeff > \& t )
```

Calculates the extended greatest common divisor q of two polynomials.

The output polynomials s and t are computed such that  $g = s \cdot a + t \cdot b$ .

## **Parameters**

| а | First polynomial.         |
|---|---------------------------|
| b | Second polynomial.        |
| s | First output polynomial.  |
| t | Second output polynomial. |

## See also

?, Algorithm 2.2

# Returns

```
gcd(a,b)
```

```
11.1.4.200 extended_gcd_integer() template<typename T >
```

Try to factorize a multivariate polynomial.

Uses CoCoALib and GiNaC, if available, depending on the coefficient type of the polynomial.

```
11.1.4.202 factorization() [2/2] template<typename Coeff > FactorMap<Coeff> carl::factorization ( const UnivariatePolynomial < Coeff > & p)
```

```
11.1.4.204 factorizationToString() template<typename P >
std::string carl::factorizationToString (
             const Factorization< P > & _factorization,
             bool _infix = true,
             bool _friendlyVarNames = true )
11.1.4.205 fits_within() template<typename T , typename T2 >
bool carl::fits_within (
             const T2 & t )
11.1.4.206 floor() [1/9] cln::cl_I carl::floor (
             const cln::cl_I & n ) [inline]
Round down an integer.
Parameters
     An integer.
Returns
     |n|.
11.1.4.207 floor() [2/9] cln::cl_I carl::floor (
             const cln::cl_RA & n ) [inline]
Round down a fraction.
Parameters
     A fraction.
Returns
     |n|.
11.1.4.208 floor() [3/9] template<typename FloatType >
FLOAT_T<FloatType> carl::floor (
```

Method which returns the next smaller integer of this number or the number itself, if it is already an integer.

const FLOAT\_T< FloatType  $> \& \_in$  ) [inline]

## **Parameters**

| $\leftarrow$ | Number. |
|--------------|---------|
| _←           |         |
| in           |         |

# Returns

Number which holds the result.

```
11.1.4.209 floor() [4/9] template<typename Number > Interval<Number> carl::floor ( const Interval< Number > & _in ) [inline]
```

Method which returns the next smaller integer of this number or the number itself, if it is already an integer.

## **Parameters**

| $\leftarrow$ | Number. |
|--------------|---------|
| _←           |         |
| in           |         |

# Returns

Number which holds the result.

```
11.1.4.214 floor() [9/9] double carl::floor ( double n ) [inline]
```

Basic Operators.

The following functions implement simple operations on the given numbers.

## **Parameters**

| _typ | oe . | The formula type to get the string representation for. |
|------|------|--|
|------|------|--|

#### Returns

The string representation of the given type.

```
11.1.4.216 fresh_bitvector_variable() [1/2] Variable carl::fresh_bitvector_variable ( ) [inline], [noexcept]
```

```
11.1.4.217 fresh_bitvector_variable() [2/2] Variable carl::fresh_bitvector_variable (
const std::string & name ) [inline]
```

```
11.1.4.218 fresh_boolean_variable() [1/2] Variable carl::fresh_boolean_variable ( ) [inline], [noexcept]
```

```
11.1.4.219 fresh_boolean_variable() [2/2] Variable carl::fresh_boolean_variable (
const std::string & name ) [inline]
```

```
11.1.4.220 fresh_integer_variable() [1/2] Variable carl::fresh_integer_variable ( ) [inline], [noexcept]
```

```
11.1.4.221 fresh_integer_variable() [2/2] Variable carl::fresh_integer_variable ( const std::string & name ) [inline]
```

```
11.1.4.222 fresh_real_variable() [1/2] Variable carl::fresh_real_variable ( ) [inline], [noexcept]
11.1.4.223 fresh_real_variable() [2/2] Variable carl::fresh_real_variable (
             const std::string & name ) [inline]
11.1.4.224 fresh_uninterpreted_variable() [1/2] Variable carl::fresh_uninterpreted_variable ( )
[inline], [noexcept]
11.1.4.225 fresh_uninterpreted_variable() [2/2] Variable carl::fresh_uninterpreted_variable (
             const std::string & name ) [inline]
11.1.4.226 fresh_variable() [1/2] Variable carl::fresh_variable (
             const std::string & name,
             VariableType vt ) [inline]
11.1.4.227 fresh_variable() [2/2] Variable carl::fresh_variable (
             VariableType vt ) [inline], [noexcept]
11.1.4.228 from_int() [1/3] template<typename To , typename From >
To carl::from_int (
            const From & n ) [inline]
11.1.4.229 from_int() [2/3] template<>
cln::cl_RA carl::from_int (
            const sint & n ) [inline]
11.1.4.230 from_int() [3/3] template<>
cln::cl_RA carl::from_int (
            const uint & n ) [inline]
11.1.4.231 gcd() [1/12] cln::cl_I carl::gcd (
             const cln::cl_I & a,
             \verb|const cln::cl_I & b | | [inline]|
```

Calculate the greatest common divisor of two integers.

# **Parameters**

| а | First argument.  |
|---|------------------|
| b | Second argument. |

## Returns

Gcd of a and b.

Calculate the greatest common divisor of two fractions.

Asserts that the arguments are integral.

## **Parameters**

| а | First argument.  |
|---|------------------|
| b | Second argument. |

## Returns

Gcd of a and b.

Calculates the least common multiple of two monomial pointers.

If both are valid objects, the gcd of both is calculated. If only one is a valid object, this one is returned. If both are invalid objects, an empty monomial is returned.

## **Parameters**

| lhs | First monomial.  |
|-----|------------------|
| rhs | Second monomial. |

```
Returns
```

gcd of lhs and rhs.

```
11.1.4.235 gcd() [5/12] mpq_class carl::gcd (
            const mpq_class & a,
            const mpq_class & b ) [inline]
11.1.4.236 gcd() [6/12] mpz_class carl::gcd (
            const mpz_class & a,
            const mpz_class & b ) [inline]
11.1.4.237 gcd() [7/12] template<typename C , typename O , typename P >
Monomial::Arg carl::gcd (
            const MultivariatePolynomial < C, O, P > & a,
            const Monomial::Arg & b )
11.1.4.238 gcd() [8/12] template<typename C , typename O , typename P >
MultivariatePolynomial< C, O, P > carl::gcd (
            const MultivariatePolynomial < C, O, P > & a,
            const MultivariatePolynomial< C, O, P > & b )
11.1.4.239 gcd() [9/12] template<typename C , typename O , typename P >
Term<C> carl::gcd (
            const MultivariatePolynomial < C, O, P > & a,
            const Term < C > \& b)
11.1.4.240 gcd() [10/12] template<typename C , typename O , typename P >
Term<C> carl::gcd (
            const Term < C > & a,
            const MultivariatePolynomial< C, O, P > & b )
11.1.4.241 gcd() [11/12] template<typename Coeff >
Term<Coeff> carl::gcd (
            const Term< Coeff > & t1,
             const Term< Coeff > & t2)
Calculates the gcd of (t1, t2).
```

If t1 or t2 is zero, undefined.

# **Parameters**

| t1 | first term  |
|----|-------------|
| t2 | second term |

# Returns

gcd of t1 and t2.

Calculates the greatest common divisor of two polynomials.

# **Parameters**

| а | First polynomial.  |
|---|--------------------|
| b | Second polynomial. |

# Returns

gcd(a,b)

```
11.1.4.243 gcd_assign() [1/4] cln::cl_I & carl::gcd_assign ( cln::cl_I & a, const cln::cl_I & b ) [inline]
```

Calculate the greatest common divisor of two integers.

Stores the result in the first argument.

# **Parameters**

| а | First argument.  |
|---|------------------|
| b | Second argument. |

# Returns

Updated a.

Calculate the greatest common divisor of two fractions.

Stores the result in the first argument. Asserts that the arguments are integral.

## **Parameters**

| а | First argument.  |
|---|------------------|
| b | Second argument. |

# Returns

Updated a.

```
11.1.4.245 gcd_assign() [3/4] mpq_class\& carl::gcd_assign ( <math>mpq_class\& a, const mpq_class\& b) [inline]
```

Calculate the greatest common divisor of two integers.

Stores the result in the first argument.

# Parameters

| а | First argument.  |
|---|------------------|
| b | Second argument. |

# Returns

Updated a.

```
11.1.4.246 gcd_assign() [4/4] mpz_class\& carl::gcd_assign ( <math>mpz_class\& a, const mpz_class\& b) [inline]
```

Calculate the greatest common divisor of two integers.

Stores the result in the first argument.

# **Parameters**

| а | First argument.  |
|---|------------------|
| b | Second argument. |

```
Returns
```

Updated a.

Extract the denominator from a fraction.

# **Parameters**

n Fraction.

# Returns

Denominator.

```
11.1.4.251 get_denom() [2/4] mpz_class carl::get_denom ( const FLOAT_T< mpq_class > \& _in ) [inline]
```

Implicitly converts the number to a rational and returns the denominator.

# **Parameters**

| $\leftarrow$ | Number. |
|--------------|---------|
| _←           |         |
| in           |         |

Returns

GMP interger which holds the result.

```
11.1.4.252 get\_denom() [3/4] mpz_class carl::get_denom ( const mpq_class & n ) [inline]
```

```
11.1.4.253 get_denom() [4/4] mpz_class carl::get_denom ( const mpz_class & n ) [inline]
```

```
11.1.4.254 get_num() [1/4] cln::cl_I carl::get_num ( const cln::cl_RA & n ) [inline]
```

Extract the numerator from a fraction.

## **Parameters**

```
n Fraction.
```

Returns

Numerator.

```
11.1.4.255 get_num() [2/4] mpz_class carl::get_num ( const FLOAT_T< mpq_class > \& _in ) [inline]
```

Implicitly converts the number to a rational and returns the nominator.

# **Parameters**

| $\leftarrow$ | Number. |
|--------------|---------|
| _←           |         |
| in           |         |

# Returns

GMP interger which holds the result.

```
11.1.4.256 get_num() [3/4] mpz_class carl::get_num (
              const mpq_class & n ) [inline]
11.1.4.257 get_num() [4/4] mpz_class carl::get_num (
              const mpz\_class \& n) [inline]
11.1.4.258 get_other_bound_type() static BoundType carl::get_other_bound_type (
              BoundType type ) [inline], [static]
\textbf{11.1.4.259} \quad \textbf{get\_ran\_assignment()} \; \texttt{[1/2]} \quad \texttt{template} < \texttt{typename} \; \texttt{Rational} \; \; \text{,} \; \; \texttt{typename} \; \; \texttt{Poly} \; > \; \\
\verb|std::optional<| Assignment<| typename Poly::RootType> > carl::get\_ran\_assignment (
              const carlVariables & vars,
              const Model < Rational, Poly > & model)
11.1.4.260 get_ran_assignment() [2/2] template<typename Rational , typename Poly >
Assignment<typename Poly::RootType> carl::get_ran_assignment (
              const Model< Rational, Poly > & model )
11.1.4.261 get_strictest_bound_type() static BoundType carl::get_strictest_bound_type (
              BoundType type1,
              BoundType type2 ) [inline], [static]
11.1.4.262 get_substitution() [1/2] template<typename Pol >
std::optional<std::pair<Variable, Pol> > carl::get_substitution (
              const BasicConstraint< Pol > & c,
              bool _negated = false,
              Variable _exclude = carl::Variable::NO_VARIABLE,
              std::optional< VarsInfo< Pol >> var_info = std::nullopt )
```

If this constraint represents a substitution (equation, where at least one variable occurs only linearly), this method detects a (there could be various possibilities) corresponding substitution variable and term.

# Parameters

| _substitutionVariable | Is set to the substitution variable, if this constraint represents a substitution. |
|-----------------------|--|
| ₋substitutionTerm     | Is set to the substitution term, if this constraint represents a substitution.     |

#### Returns

true, if this constraints represents a substitution; false, otherwise.

```
11.1.4.263 get_substitution() [2/2] template<typename Pol >
std::optional<std::pair<Variable, Pol> > carl::get_substitution (
                                  const Constraint < Pol > & c,
                                  bool _negated = false,
                                  Variable _exclude = carl::Variable::NO_VARIABLE )
11.1.4.264 get_weakest_bound_type() static BoundType carl::get_weakest_bound_type (
                                   BoundType type1,
                                  BoundType type2 ) [inline], [static]
\textbf{11.1.4.265} \quad \textbf{getDefaultModel()} \; \texttt{[1/4]} \quad \texttt{template} < \texttt{typename} \; \texttt{Rational} \; \; \text{,} \; \; \texttt{typename} \; \texttt{Poly} \; > \; \texttt{(instable of the poly of th
void carl::getDefaultModel (
                                  Model < Rational, Poly > & _defaultModel,
                                  const BVTerm & _constraint,
                                  bool _overwrite = true,
                                  size_t _seed = 0 )
\textbf{11.1.4.266} \quad \textbf{getDefaultModel()} \  \, \textbf{[2/4]} \quad \text{template} < \text{typename Rational , typename Poly} > \\
void carl::getDefaultModel (
                                 Model < Rational, Poly > & _defaultModel,
                                  const Constraint< Poly > & _constraint,
                                  bool _overwrite = true,
                                   size_t _seed = 0 )
11.1.4.267 getDefaultModel() [3/4] template<typename Rational , typename Poly >
void carl::getDefaultModel (
                                 Model < Rational, Poly > & _defaultModel,
                                  const Formula Poly > & _formula,
                                  bool _overwrite = true,
                                  size_t = seed = 0)
11.1.4.268 getDefaultModel() [4/4] template<typename Rational , typename Poly >
void carl::getDefaultModel (
                                  Model< Rational, Poly > & _defaultModel,
                                   const UEquality & _constraint,
                                  bool _overwrite = true,
                                   size_t _seed = 0 )
```

```
11.1.4.269 getRationalAssignmentsFromModel() template<typename Rational , typename Poly > bool carl::getRationalAssignmentsFromModel ( const Model< Rational, Poly > & model, std::map< Variable, Rational > & rationalAssigns)
```

Obtains all assignments which can be transformed to rationals and stores them in the passed map.

## **Parameters**

| ₋model           | The model from which to obtain the rational assignments. |
|------------------|--|
| ₋rationalAssigns | The map to store the rational assignments in.            |

## Returns

true, if the entire model could be transformed to rational assignments. (not possible if, e.g., sqrt is contained)

Gets the sort specified by the arguments.

Forwards to SortManager::getSort().

Actual signal handler.

Variadic version of hash-add to add an arbitrary number of values to the seed.

Add hash of both elements of a std::pair to the seed.

Add hash of the given value to the hash seed.

```
11.1.4.276 hash_add() [4/5] template<typename T > void carl::hash_add ( std::size\_t \ \& \ seed, const \ std::vector< T > \& v ) \ [inline]
```

Add hash of all elements of a std::vector to the seed.

Add hash of the given value to the hash seed.

Used hash\_combine with the result of std::hash<T>.

Hashes an arbitrary number of values.

Uses hash\_add with a seed of 0.

Add a value to the given hash seed.

This method is a copy of boost::hash\_combine(). It is reimplemented here to avoid including all of boost/functional/hash.hpp for this single line of code.

Returns the highest power of two below n.

Can also be seen as the highest bit set in n.

## **Parameters**

n

Returns

```
11.1.4.283 hirstMaceyBound() template<typename Coeff > Coeff carl::hirstMaceyBound ( const UnivariatePolynomial< Coeff > & p )
```

```
11.1.4.284 init() int carl::init ( ) [inline]
```

The routine for initializing the carl library.

Which is called automatically by including this header. TODO prevent outside access.

```
11.1.4.285 initialize() int carl::initialize ( ) [inline]
```

Method to ensure that upon inclusion, init() is called exactly once.

TODO prevent outside access.

11.1.4.286 install\_signal\_handler() static bool carl::install\_signal\_handler ( ) [static], [noexcept] Installs the signal handler.

```
11.1.4.288 integer_variables() template<typename T > carlVariables carl::integer_variables ( const T & t ) [inline]
```

```
11.1.4.289 invalid_enum_value() template<typename Enum > constexpr Enum carl::invalid_enum_value () [constexpr]
```

Returns an enum value that is (most probably) not a valid enum value.

This can be used to check whether methods that take enums properly handle invalid values.

```
11.1.4.290 inverse() [1/2] BVCompareRelation carl::inverse (
BVCompareRelation _c ) [inline]
```

```
11.1.4.291 inverse() [2/2] Relation carl::inverse (

Relation r) [inline]
```

Inverts the given relation symbol.

Try to factorize a multivariate polynomial and return the irreducible factors (without multiplicities).

Uses CoCoALib and GiNaC, if available, depending on the coefficient type of the polynomial.

bool includeConstants = true )

Checks whether the monomial has at most degree one.

# Returns

If monomial is linear or constant.

Checks whether the monomial has at most degree one.

## Returns

If monomial is linear or constant.

# Returns

true, if this constraint is a bound.

Checks whether the monomial is a constant.

Returns

If monomial is constant.

Check if the polynomial is linear.

```
11.1.4.301 is_constant() [4/5] template<typename Coeff > bool carl::is_constant ( const Term< Coeff > & t )
```

Checks whether the monomial is a constant.

Returns

```
11.1.4.302 is_constant() [5/5] template<typename Coeff > bool carl::is_constant ( const UnivariatePolynomial < Coeff > & p)
```

Checks whether the polynomial is constant with respect to the main variable.

Returns

If polynomial is constant.

Check if a number is integral.

As cln::cl\_l are always integral, this method returns true.

Returns

true.

Check if a fraction is integral.

```
Parameters
 n A fraction.
Returns
    true.
11.1.4.305 is_integer() [3/10] template<typename FloatType >
bool carl::is_integer (
             \verb|const FLOAT_T| < \verb|FloatType| > \& in | | [inline]
11.1.4.306 is_integer() [4/10] template<typename IntegerT >
bool carl::is_integer (
             const GFNumber< IntegerT > & ) [inline]
Todo Implement this
Parameters
11.1.4.307 is_integer() [5/10] template<typename Number >
bool carl::is_integer (
             const Interval< Number > & n ) [inline]
11.1.4.308 is_integer() [6/10] template<typename Number >
bool carl::is_integer (
             const IntRepRealAlgebraicNumber< Number > \& n ) [inline]
11.1.4.309 is_integer() [7/10] bool carl::is_integer (
```

const mpq\_class & n ) [inline]

```
11.1.4.310 is_integer() [8/10] bool carl::is_integer (
             const mpz_class & ) [inline]
11.1.4.311 is_integer() [9/10] bool carl::is_integer (
             double d ) [inline]
11.1.4.312 is_integer() [10/10] bool carl::is_integer (
             sint ) [inline]
11.1.4.313 is_linear() [1/5] template<typename Coeff , typename Ordering , typename Policies >
bool carl::is_linear (
             const ContextPolynomial< Coeff, Ordering, Policies > & p ) [inline]
11.1.4.314 is_linear() [2/5] bool carl::is_linear (
             const Monomial & m ) [inline]
Checks whether the monomial has exactly degree one.
Returns
     If monomial is linear.
11.1.4.315 is_linear() [3/5] template<typename Coeff , typename Ordering , typename Policies >
bool carl::is_linear (
             const MultivariatePolynomial< Coeff, Ordering, Policies > & p )
Check if the polynomial is linear.
11.1.4.316 is_linear() [4/5] template<typename Coeff >
bool carl::is_linear (
             const Term< Coeff > \& t )
Checks whether the monomial has exactly the degree one.
```

Returns

```
11.1.4.317 is_linear() [5/5] template<typename Coeff >
bool carl::is_linear (
             const UnivariatePolynomial < Coeff > & p )
11.1.4.318 is_lower_bound() [1/2] template<typename Pol >
bool carl::is_lower_bound (
            const BasicConstraint< Pol > & constr )
Returns
    true, if this constraint is a lower bound.
11.1.4.319 is_lower_bound() [2/2] template<typename Pol >
bool carl::is_lower_bound (
             const Constraint< Pol > & constr )
11.1.4.320 is_negative() [1/6] bool carl::is_negative (
             const cln::cl_I & n ) [inline]
11.1.4.321 is_negative() [2/6] bool carl::is_negative (
             const cln::cl_RA & n ) [inline]
11.1.4.322 is_negative() [3/6] bool carl::is_negative (
             const mpq_class & n ) [inline]
11.1.4.323 is_negative() [4/6] bool carl::is_negative (
             const mpz_class & n ) [inline]
11.1.4.324 is_negative() [5/6] template<typename T , EnableIf< has_is_negative< T >> >
bool carl::is_negative (
           const T & t ) [inline]
```

```
11.1.4.325 is_negative() [6/6] bool carl::is_negative (
             double n ) [inline]
11.1.4.326 is_number() [1/2] template<typename Coeff , typename Ordering , typename Policies >
bool carl::is_number (
            const ContextPolynomial< Coeff, Ordering, Policies > & p ) [inline]
11.1.4.327 is_number() [2/2] bool carl::is_number (
             double d ) [inline]
11.1.4.328 is_one() [1/11] bool carl::is_one (
            const cln::cl_I & n ) [inline]
11.1.4.329 is_one() [2/11] bool carl::is_one (
             const cln::cl_RA & n ) [inline]
11.1.4.330 is_one() [3/11] template<typename P >
bool carl::is_one (
             const FactorizedPolynomial< P > & fp )
Returns
    true, if the factorized polynomial is one.
11.1.4.331 is_one() [4/11] template<typename IntegerT >
bool carl::is_one (
             const GFNumber< IntegerT > & _in )
11.1.4.332 is_one() [5/11] template<typename Number >
bool carl::is_one (
            const Interval< Number > & i )
```

Check if this interval is a point-interval containing 1.

```
11.1.4.333 is_one() [6/11] bool carl::is_one (
             const mpq\_class \& n) [inline]
11.1.4.334 is_one() [7/11] bool carl::is_one (
             const mpz_class & n ) [inline]
11.1.4.335 is_one() [8/11] template<typename C , typename O , typename P >
bool carl::is_one (
             const MultivariatePolynomial < C, O, P > & p )
11.1.4.336 is_one() [9/11] template<typename T >
bool carl::is_one (
            const T & t ) [inline]
11.1.4.337 is_one() [10/11] template<typename Coeff >
bool carl::is_one (
             const Term< Coeff > & term ) [inline]
Checks whether a term is one.
11.1.4.338 is_one() [11/11] template<typename Coefficient >
bool carl::is_one (
             const UnivariatePolynomial< Coefficient > \& p)
Checks if the polynomial is equal to one.
Returns
     If polynomial is one.
11.1.4.339 is_positive() [1/6] bool carl::is_positive (
             const cln::cl_I & n ) [inline]
11.1.4.340 is_positive() [2/6] bool carl::is_positive (
             const cln::cl_RA & n ) [inline]
```

```
11.1.4.341 is_positive() [3/6] bool carl::is_positive (
             const mpq_class & n ) [inline]
11.1.4.342 is_positive() [4/6] bool carl::is_positive (
             const mpz_class & n ) [inline]
11.1.4.343 is_positive() [5/6] template<typename T , EnableIf< has_is_positive< T >> >
bool carl::is_positive (
             const T & t ) [inline]
11.1.4.344 is_positive() [6/6] bool carl::is_positive (
             double n ) [inline]
11.1.4.345 is_root_of() [1/2] template<typename Coeff >
bool carl::is_root_of (
            const UnivariatePolynomial< Coeff > & p,
            const Coeff & value )
11.1.4.346 is_root_of() [2/2] template<typename Number , typename RAN , typename = std::enable. \leftarrow
if_t<is_ran_type<RAN>::value>>
Number carl::is_root_of (
             const UnivariatePolynomial < Number > & p,
             const RAN & value )
11.1.4.347 is_strict() bool carl::is_strict (
             Relation r ) [inline]
11.1.4.348 is_trivial() template<typename C , typename O , typename P >
bool carl::is_trivial (
             const Factors< MultivariatePolynomial< C, O, P >> \& f)
```

11.1.4.349 is\_upper\_bound() [1/2] template<typename Pol >

```
bool carl::is_upper_bound (
            const BasicConstraint< Pol > & constr )
Returns
    true, if this constraint is an upper bound.
11.1.4.350 is_upper_bound() [2/2] template<typename Pol >
bool carl::is_upper_bound (
            const Constraint< Pol > & constr )
11.1.4.351 is_weak() bool carl::is_weak (
             Relation r ) [inline]
11.1.4.352 is_zero() [1/15] bool carl::is_zero (
             const cln::cl_I & n ) [inline]
11.1.4.353 is_zero() [2/15] bool carl::is_zero (
             const cln::cl_RA & n ) [inline]
11.1.4.354 is_zero() [3/15] template<typename Coeff , typename Ordering , typename Policies >
bool carl::is_zero (
             const ContextPolynomial < Coeff, Ordering, Policies > & p ) [inline]
11.1.4.355 is zero() [4/15] template<typename P >
bool carl::is_zero (
            const FactorizedPolynomial< P > & fp )
```

Returns

true, if the factorized polynomial is zero.

```
11.1.4.356 is_zero() [5/15] template<typename FloatType >
bool carl::is_zero (
             const FLOAT_T< FloatType > & _in ) [inline]
11.1.4.357 is_zero() [6/15] template<typename IntegerT >
bool carl::is_zero (
            const GFNumber< IntegerT > & _in )
11.1.4.358 is_zero() [7/15] template<typename Number >
bool carl::is-zero (
             const Interval< Number > & i )
Check if this interval is a point-interval containing 0.
11.1.4.359 is_zero() [8/15] template<typename Number >
bool carl::is_zero (
             const IntRepRealAlgebraicNumber < Number > & n ) [inline]
11.1.4.360 is_zero() [9/15] bool carl::is_zero (
             const mpq_class & n ) [inline]
11.1.4.361 is_zero() [10/15] bool carl::is_zero (
             const mpz_class & n ) [inline]
Informational functions.
The following functions return informations about the given numbers.
11.1.4.362 is zero() [11/15] template<typename C , typename O , typename P >
bool carl::is_zero (
             const MultivariatePolynomial< C, O, P > & p )
11.1.4.363 is_zero() [12/15] template<typename T >
bool carl::is_zero (
            const T & t ) [inline]
```

Checks whether a term is zero.

Checks if the polynomial is equal to zero.

Returns

If polynomial is zero.

```
11.1.4.366 is_zero() [15/15] bool carl::is_zero ( double n ) [inline]
```

Informational functions.

The following functions return informations about the given numbers.

```
11.1.4.367 islnf() bool carl::isInf ( double d ) [inline]
```

```
11.1.4.370 isNaN() bool carl::isNaN (
double d ) [inline]
```

Computes an upper bound on the value of the negative real roots of the given univariate polynomial.

Note that the positive roots of P(-x) are the negative roots of P(x).

Computes a lower bound on the value of the positive real roots of the given univariate polynomial.

Let  $Q(x) = x^q * P(1/x)$ . Then  $P(1/a) = 0 \to Q(a) = 0$ . Thus for any b it holds  $(\forall a > 0, Q(a) = 0.a <= b) \to (\forall a > 0, P(a) = 0.1/b <= a)$ , that is, if b is an upper bound of the positive real roots of Q, then 1/b is a lower bound on the positive real roots of P. Note that the coefficients of Q are the ones of P in reverse order.

Calculate the least common multiple of two integers.

# **Parameters**

| а | First argument.  |
|---|------------------|
| b | Second argument. |

## Returns

Lcm of a and b.

Calculate the least common multiple of two fractions.

Asserts that the arguments are integral.

# **Parameters**

| а | First argument.  |
|---|------------------|
| b | Second argument. |

# Returns

Lcm of a and b.

Method which returns the logarithm of the passed number.

#### **Parameters**

| $\downarrow$ | Number. |
|--------------|---------|
| _←           |         |
| in           |         |

## Returns

Number which holds the result.

```
11.1.4.389 log10() [2/3] mpq_class carl::log10 (
             const mpq_class & n ) [inline]
11.1.4.390 log10()[3/3] double carl::log10 (
             double in ) [inline]
11.1.4.391 log_assign() template<typename Number , EnableIf< std::is_floating_point< Number >>
= dummy>
void carl::log_assign (
            Interval< Number > & i )
11.1.4.392 mod() [1/4] cln::cl_I carl::mod (
            const cln::cl_I & a,
             const cln::cl_I & b ) [inline]
Calculate the remainder of the integer division.
Parameters
 a First argument.
 b Second argument.
Returns
    a\%b.
11.1.4.393 mod() [2/4] mpz_class carl::mod (
            const mpz_class & n,
             const mpz_class & m ) [inline]
11.1.4.394 mod() [3/4] sint carl::mod (
            sint n,
             sint m ) [inline]
11.1.4.395 mod() [4/4] uint carl::mod (
             uint n,
             uint m ) [inline]
```

Creates a new value for the given sort.

## **Parameters**

| cort | The sort to create a new value for. |
|------|-------------------------------------|
| SULL | The sort to create a new value for. |

## Returns

The resulting sort value.

Gets the uninterpreted function instance with the given name, domain, arguments and codomain.

# **Parameters**

| uf   | The underlying function of the uninterpreted function instance to get. |
|------|--|
| args | The arguments of the uninterpreted function instance to get.           |

# Returns

The resulting uninterpreted function instance.

Gets the uninterpreted function instance with the given name, domain, arguments and codomain.

# **Parameters**

| uf   | The underlying function of the uninterpreted function instance to get. |
|------|--|
| args | The arguments of the uninterpreted function instance to get.           |

# Returns

The resulting uninterpreted function instance.

Gets the uninterpreted function with the given name, domain, arguments and codomain.

## **Parameters**

| name     | The name of the uninterpreted function of the uninterpreted function to get.     |
|----------|--|
| domain   | The domain of the uninterpreted function of the uninterpreted function to get.   |
| codomain | The codomain of the uninterpreted function of the uninterpreted function to get. |

## Returns

The resulting uninterpreted function.

Checks if the two arguments are not equal.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs != rhs
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\,\sim\,$  rhs,  $\sim$  being the relation that is checked.

```
11.1.4.405 operator"!=() [4/48] template<typename P > bool carl::operator!= ( const\ Constraint< \ P > \&\ lhs, \\ const\ Constraint< \ P > \&\ rhs\ )
```

Checks if the two arguments are not equal.

# **Parameters**

| ₋lhs | First argument.  |
|------|------------------|
| ₋rhs | Second argument. |

# Returns

```
_lhs != _rhs
```

#### **Parameters**

| _lhs | First argument.  |
|------|------------------|
| ₋rhs | Second argument. |

## Returns

```
_lhs != _rhs
```

```
11.1.4.408 operator"!=() [7/48] template<typename IntegerT >
bool carl::operator!= (
            const GFNumber< IntegerT > & lhs,
            const GFNumber< IntegerT > & rhs )
11.1.4.409 operator"!=() [8/48] template<typename IntegerT >
bool carl::operator!= (
            const GFNumber< IntegerT > & lhs,
             const IntegerT & rhs )
11.1.4.410 operator"!=() [9/48] template<typename IntegerT >
bool carl::operator!= (
            const GFNumber< IntegerT > & lhs,
             int rhs )
11.1.4.411 operator"!=() [10/48] template<typename IntegerT >
bool carl::operator!= (
            const IntegerT & lhs,
            const GFNumber< IntegerT > & rhs )
11.1.4.412 operator"!=() [11/48] template<typename Number >
bool carl::operator!= (
            const Interval< Number > & lhs,
             const Interval< Number > & rhs ) [inline]
```

Operator for the comparison of two intervals.

| lhs | Lefthand side.  |
|-----|-----------------|
| rhs | Righthand side. |

## Returns

True if both intervals are unequal.

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

# Parameters

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

lhs  $\,\sim\,$  rhs,  $\sim$  being the relation that is checked.

Checks if the two arguments are not equal.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs != rhs
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

lhs  $\,\sim\,$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

# **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Checks if the two arguments are not equal.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs != rhs
```

Checks if the two arguments are not equal.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs != rhs
```

Checks if the two arguments are not equal.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs != rhs
```

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs != rhs
```

Checks if the two arguments are not equal.

### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs != rhs
```

Checks if the two arguments are not equal.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
Returns
```

```
lhs != rhs
```

11.1.4.425 operator"!=() [24/48] template<typename N >

const RAN & rhs )

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs != rhs
```

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs != rhs

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\,\sim\,$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## **Returns**

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Checks if the two arguments are not equal.

## **Parameters**

| ₋lhs | First argument.  |
|------|------------------|
| _rhs | Second argument. |

# Returns

```
_lhs != _rhs
```

| lhs | The left hand side.  |
|-----|----------------------|
| rhs | The right hand side. |

true, if lhs and rhs are not equal.

Checks if the two arguments are not equal.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

```
lhs != rhs
```

### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs != rhs
```

Checks if the two arguments are not equal.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
Returns
```

```
lhs != rhs
```

| lhs | The left sort.  |
|-----|-----------------|
| rhs | The right sort. |

# Returns

true, if the sorts are different.

Sort rhs ) [inline]

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Checks if the two arguments are not equal.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

```
lhs != rhs
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

11.1.4.451 operator&() BVValue carl::operator& (

```
const BVValue & 1hs,
             const BVValue & rhs ) [inline]
11.1.4.452 operator*() [1/53] template<typename Pol , bool AS>
RationalFunction<Pol, AS> carl::operator* (
             carl::sint lhs,
             const RationalFunction< Pol, AS > & rhs )
11.1.4.453 operator*() [2/53] BVValue carl::operator* (
             const BVValue & 1hs,
             const BVValue & rhs )
11.1.4.454 operator*()[3/53] template<typename C , typename O , typename P >
auto carl::operator* (
             const C & lhs,
             const MultivariatePolynomial < C, O, P > & rhs > [inline]
Perform a multiplication involving a polynomial using operator*=().
Parameters
 lhs
      Left hand side.
      Right hand side.
Returns
    lhs * rhs
11.1.4.455 operator*() [4/53] template<typename C >
UnivariatePolynomial<C> carl::operator* (
             const C & lhs,
             const UnivariatePolynomial<br/>< C > & rhs )
11.1.4.456 operator*() [5/53] template<typename Coeff , EnableIf< carl::is_number_type< Coeff
>> = dummy>
Term<Coeff> carl::operator* (
             const Coeff & lhs,
             const Monomial::Arg & rhs ) [inline]
```

Perform a multiplication involving a term.

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

# Returns

```
lhs * rhs
```

Perform a multiplication involving a term.

# **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

# Returns

```
lhs * rhs
```

Perform a multiplication involving a term.

# **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

```
lhs * rhs
```

Perform a multiplication involving a polynomial.

#### **Parameters**

| ₋lhs | Left hand side.  |
|------|------------------|
| ₋rhs | Right hand side. |

## **Returns**

```
_{	ext{lhs}} * _{	ext{rhs}}
```

Perform a multiplication involving a polynomial.

# **Parameters**

| _lhs | Left hand side.  |
|------|------------------|
| ₋rhs | Right hand side. |

```
_lhs * _rhs
```

const Interval< Number > & lhs,

const Interval< Number > & rhs ) [inline]

Operator for the multiplication of two intervals.

Interval < Number > carl::operator\* (

## **Parameters**

| lhs | Lefthand side.  |
|-----|-----------------|
| rhs | Righthand side. |

## Returns

Resulting interval.

Operator for the multiplication of an interval and a number.

# **Parameters**

| lhs | Lefthand side.  |
|-----|-----------------|
| rhs | Righthand side. |

# Returns

Resulting interval.

Perform a multiplication involving a term.

## **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

## Returns

```
lhs * rhs
```

Perform a multiplication involving a monomial.

# **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

## Returns

```
lhs * rhs
```

Perform a multiplication involving a polynomial using operator\*=().

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

```
lhs * rhs
```

Perform a multiplication involving a term.

## **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

# Returns

```
lhs * rhs
```

Perform a multiplication involving a monomial.

# **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

```
lhs * rhs
```

Perform a multiplication involving a polynomial using operator\*=().

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

# Returns

```
lhs * rhs
```

Perform a multiplication involving a polynomial using operator\*=().

## **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

# Returns

```
lhs * rhs
```

Perform a multiplication involving a polynomial using operator\*=().

### **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

```
lhs * rhs
```

Perform a multiplication involving a polynomial using operator\*=().

#### **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

## **Returns**

lhs \* rhs

Perform a multiplication involving a polynomial using operator\*=().

### **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

## Returns

lhs \* rhs

Operator for the multiplication of an interval and a number.

| lhs | Lefthand side.  |
|-----|-----------------|
| rhs | Righthand side. |

#### Returns

Resulting interval.

```
11.1.4.480 operator*() [29/53] template<typename Pol , bool AS>
RationalFunction<Pol, AS> carl::operator* (
            const RationalFunction < Pol, AS > & lhs,
             carl::sint rhs )
11.1.4.481 operator*() [30/53] template<typename Pol , bool AS, DisableIf< needs_cache_type<
Pol >> = dummy>
RationalFunction<Pol, AS> carl::operator* (
            const RationalFunction < Pol, AS > & lhs,
            const Monomial::Arg & rhs )
11.1.4.482 operator*() [31/53] template<typename Pol , bool AS>
RationalFunction<Pol, AS> carl::operator* (
            const RationalFunction < Pol, AS > & lhs,
            const Pol & rhs )
11.1.4.483 operator*() [32/53] template<typename Pol , bool AS>
RationalFunction<Pol, AS> carl::operator* (
           const RationalFunction < Pol, AS > & lhs,
            const RationalFunction< Pol, AS > & rhs )
11.1.4.484 operator*() [33/53] template<typename Pol , bool AS, DisableIf< needs_cache_type<
Pol >> = dummy>
RationalFunction<Pol, AS> carl::operator* (
            const RationalFunction< Pol, AS > & lhs,
            const Term< typename Pol::CoeffType > & rhs )
```

Perform a multiplication involving a polynomial using operator\*=().

#### **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

# Returns

lhs \* rhs

Perform a multiplication involving a polynomial.

# **Parameters**

| ₋lhs | Left hand side.  |
|------|------------------|
| _rhs | Right hand side. |

#### Returns

\_lhs \* \_rhs

```
11.1.4.489 operator*() [38/53] template<typename Pol , bool AS>
RationalFunction<Pol, AS> carl::operator* (
            const typename Pol::CoeffType & lhs,
            const RationalFunction< Pol, AS > & rhs )
11.1.4.490 operator*() [39/53] template<typename C , typename O , typename P >
const MultivariatePolynomial<C,O,P> carl::operator* (
            const UnivariatePolynomial< C > & ,
             const MultivariatePolynomial < C, O, P > & )
11.1.4.491 operator*() [40/53] template<typename C >
UnivariatePolynomial<C> carl::operator* (
            const UnivariatePolynomial< C > & lhs,
            const C & rhs )
11.1.4.492 operator*() [41/53] template<typename C >
UnivariatePolynomial<C> carl::operator* (
             const UnivariatePolynomial< C > & lhs,
            const IntegralTypeIfDifferent< C > & rhs )
11.1.4.493 operator*() [42/53] template<typename C >
UnivariatePolynomial<C> carl::operator* (
            const UnivariatePolynomial < C > & lhs,
            const UnivariatePolynomial< C > & rhs )
Parameters
      Left hand side.
 lhs
 rhs
      Right hand side.
Returns
    lhs * rhs
11.1.4.494 operator*() [43/53] template<typename C >
UnivariatePolynomial<C> carl::operator* (
            const UnivariatePolynomial< C > & lhs,
```

Variable rhs )

Perform a multiplication involving a term.

## **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

# Returns

lhs \* rhs

Perform a multiplication involving a term.

# **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

# Returns

lhs \* rhs

Perform a multiplication involving a term.

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

```
lhs * rhs
```

Perform a multiplication involving a term.

## **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

# Returns

```
lhs * rhs
```

Perform a multiplication involving a term.

# **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

# Returns

```
lhs * rhs
```

```
11.1.4.500 operator*() [49/53] Monomial::Arg carl::operator* (

Variable lhs,

const Monomial::Arg & rhs )
```

Perform a multiplication involving a monomial.

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

# Returns

```
lhs * rhs
```

Perform a multiplication involving a polynomial using operator\*=().

# **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

# Returns

```
lhs * rhs
```

Perform a multiplication involving a term.

# **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

```
lhs * rhs
```

Perform a multiplication involving a monomial.

#### **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

## Returns

```
lhs * rhs
```

Operator for the multiplication of an interval and a number with assignment.

#### **Parameters**

| lhs | Lefthand side.  |
|-----|-----------------|
| rhs | Righthand side. |

# Returns

Resulting interval.

Operator for the multiplication of an interval and a number with assignment.

| lhs | Lefthand side.  |
|-----|-----------------|
| rhs | Righthand side. |

# Returns

Resulting interval.

Multiply a term with something and return the changed term.

# **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

# Returns

Changed lhs.

Multiply a term with something and return the changed term.

# **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

# Returns

Changed lhs.

Multiply a term with something and return the changed term.

## **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

# Returns

Changed lhs.

Multiply a term with something and return the changed term.

# **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

# Returns

Changed lhs.

Performs an addition involving a polynomial using operator+= ().

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs + rhs
```

```
11.1.4.513 operator+() [3/44] template<typename C , typename O , typename P > auto carl::operator+ ( const\ C\ \&\ lhs, const\ MultivariatePolynomial< C, O, P > \&\ rhs\ ) \ [inline]
```

Performs an addition involving a polynomial using operator+= ().

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs + rhs
```

Performs an addition involving a polynomial using operator+= ().

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs + rhs
```

Performs an addition involving a polynomial using operator+= ().

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

```
lhs + rhs
```

Performs an addition involving a polynomial.

#### **Parameters**

| ₋lhs | First argument.  |
|------|------------------|
| _rhs | Second argument. |

#### Returns

```
_lhs + _rhs
```

Performs an addition involving a polynomial.

| ₋lhs | First argument.  |
|------|------------------|
| ₋rhs | Second argument. |

#### Returns

```
_lhs + _rhs
```

```
11.1.4.519 operator+() [9/44] template<typename IntegerT >
GFNumber<IntegerT> carl::operator+ (
           const GFNumber < IntegerT > & lhs,
            const GFNumber< IntegerT > & rhs )
11.1.4.520 operator+() [10/44] template<typename IntegerT >
GFNumber<IntegerT> carl::operator+ (
            const GFNumber< IntegerT > & lhs,
            const IntegerT & rhs )
11.1.4.521 operator+() [11/44] template<typename IntegerT >
GFNumber<IntegerT> carl::operator+ (
            const IntegerT & lhs,
            const GFNumber< IntegerT > & rhs )
11.1.4.522 operator+() [12/44] template<typename Number >
Interval<Number> carl::operator+ (
            const Interval< Number > & lhs,
            const Interval< Number > & rhs ) [inline]
```

Operator for the addition of two intervals.

### **Parameters**

| lhs | Lefthand side.  |
|-----|-----------------|
| rhs | Righthand side. |

# Returns

Resulting interval.

Operator for the addition of an interval and a number.

## **Parameters**

| lhs | Lefthand side.  |
|-----|-----------------|
| rhs | Righthand side. |

# Returns

Resulting interval.

Performs an addition involving a polynomial using operator+= ().

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs + rhs
```

Performs an addition involving a polynomial using operator+= ().

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs + rhs
```

Performs an addition involving a polynomial using operator+= ().

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

lhs + rhs

Performs an addition involving a polynomial using operator+= ().

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs + rhs
```

Performs an addition involving a polynomial using operator+= ().

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

```
lhs + rhs
```

Performs an addition involving a polynomial using operator+= ().

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

### Returns

```
lhs + rhs
```

Performs an addition involving a polynomial using operator += ().

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

### Returns

```
lhs + rhs
```

Performs an addition involving a polynomial using operator+= ().

### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs + rhs
```

```
11.1.4.534 operator+() [24/44] template<typename N > ThomEncoding<N> carl::operator+ ( const\ N\ \&\ lhs, const\ ThomEncoding<\ N\ >\ \&\ rhs\ )
```

Operator for the addition of an interval and a number.

### **Parameters**

| lhs | Lefthand side.  |
|-----|-----------------|
| rhs | Righthand side. |

Returns

Resulting interval.

```
11.1.4.536 operator+() [26/44] template<typename Pol , bool AS, DisableIf< needs_cache_type<
Pol >> = dummy>
RationalFunction<Pol, AS> carl::operator+ (
            const RationalFunction < Pol, AS > & lhs,
            const Monomial::Arg & rhs )
11.1.4.537 operator+() [27/44] template<typename Pol , bool AS>
RationalFunction<Pol, AS> carl::operator+ (
            const RationalFunction < Pol, AS > & lhs,
            const Pol & rhs )
11.1.4.538 operator+() [28/44] template<typename Pol , bool AS>
RationalFunction<Pol, AS> carl::operator+ (
            const RationalFunction< Pol, AS > & lhs,
             const RationalFunction< Pol, AS > & rhs )
11.1.4.539 operator+() [29/44] template<typename Pol , bool AS, DisableIf< needs_cache_type<
Pol >> = dummy>
RationalFunction<Pol, AS> carl::operator+ (
           const RationalFunction < Pol, AS > & lhs,
            const Term< typename Pol::CoeffType > & rhs )
11.1.4.540 operator+() [30/44] template<typename Pol , bool AS>
RationalFunction<Pol, AS> carl::operator+ (
            const RationalFunction < Pol, AS > & lhs,
            const typename Pol::CoeffType & rhs )
11.1.4.541 operator+() [31/44] template<typename Pol , bool AS, DisableIf< needs_cache_type<
Pol >> = dummy>
RationalFunction<Pol, AS> carl::operator+ (
            const RationalFunction < Pol, AS > & lhs,
            Variable rhs )
11.1.4.542 operator+() [32/44] template<typename C >
auto carl::operator+ (
            const Term< C > & 1hs,
             const C & rhs ) [inline]
Performs an addition involving a polynomial using operator+= ().
```

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs + rhs
```

Performs an addition involving a polynomial using operator+= ().

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs + rhs
```

```
11.1.4.544 operator+() [34/44] template<typename C , typename O , typename P > auto carl::operator+ (  const\ Term<\ C > \&\ lhs, \\ const\ MultivariatePolynomial<\ C,\ O,\ P > \&\ rhs\ ) \ [inline]
```

Performs an addition involving a polynomial using operator+= ().

# **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs + rhs
```

```
11.1.4.545 operator+() [35/44] template<typename C > auto carl::operator+ (  const \ Term < C > \& \ lhs, \\ const \ Term < C > \& \ rhs \ ) \ [inline]
```

Performs an addition involving a polynomial using operator+= ().

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs + rhs
```

Performs an addition involving a polynomial using operator+= ().

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs + rhs
```

Performs an addition involving a polynomial.

### **Parameters**

| ₋lhs | First argument.  |
|------|------------------|
| ₋rhs | Second argument. |

```
Returns
```

```
_{lhs} + _{rhs}
```

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs + rhs
```

Performs an addition involving a polynomial using operator+= ().

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs + rhs
```

Performs an addition involving a polynomial using operator+= ().

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs + rhs
```

Performs an addition involving a polynomial using operator+= ().

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs + rhs
```

Operator for the addition of an interval and a number with assignment.

# **Parameters**

| lhs | Lefthand side.  |
|-----|-----------------|
| rhs | Righthand side. |

## Returns

Resulting interval.

Operator for the addition of an interval and a number with assignment.

# **Parameters**

| lhs | Lefthand side.  |
|-----|-----------------|
| rhs | Righthand side. |

### Returns

Resulting interval.

Performs a subtraction involving a polynomial using operator=().

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs - rhs
```

Performs a subtraction involving a polynomial using operator = ().

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs - rhs
```

Performs a subtraction involving a polynomial using operator == ().

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs - rhs
```

Performs a subtraction involving a polynomial using operator == ().

### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

### Returns

```
lhs - rhs
```

Performs an subtraction involving a polynomial.

### **Parameters**

| ₋lhs | First argument.  |
|------|------------------|
| _rhs | Second argument. |

### Returns

```
_lhs - _rhs
```

Performs an subtraction involving a polynomial.

| ₋lhs | First argument.  |
|------|------------------|
| ₋rhs | Second argument. |

### Returns

```
_lhs - _rhs
```

const Interval< Number > & rhs ) [inline]

Operator for the subtraction of two intervals.

### **Parameters**

| lhs | Lefthand side.  |
|-----|-----------------|
| rhs | Righthand side. |

### Returns

Resulting interval.

Operator for the subtraction of an interval and a number.

## **Parameters**

| lhs | Lefthand side.  |
|-----|-----------------|
| rhs | Righthand side. |

# Returns

Resulting interval.

Unary minus.

# **Parameters**

```
rhs The operand.
```

# Returns

Resulting interval.

Performs a subtraction involving a polynomial using operator == ().

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

### Returns

```
lhs - rhs
```

Performs a subtraction involving a polynomial using operator == ().

### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

### Returns

```
lhs - rhs
```

Performs a subtraction involving a polynomial using operator == ().

### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs - rhs
```

Performs a subtraction involving a polynomial using operator == ().

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

### Returns

```
lhs - rhs
```

Performs a subtraction involving a polynomial using operator = ().

### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs - rhs
```

Performs a subtraction involving a polynomial using operator == ().

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs - rhs
```

Performs a subtraction involving a polynomial using operator = ().

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs - rhs
```

Performs a subtraction involving a polynomial using operator == ().

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs - rhs
```

Operator for the subtraction of an interval and a number.

# **Parameters**

| lhs | Lefthand side.  |
|-----|-----------------|
| rhs | Righthand side. |

```
Returns
```

Resulting interval.

```
11.1.4.581 operator-() [25/43] template<typename Pol , bool AS>
RationalFunction<Pol, AS> carl::operator- (
             const RationalFunction< Pol, AS > & lhs)
11.1.4.582 operator-() [26/43] template<typename Pol , bool AS, DisableIf< needs_cache_type< Pol
>> = dummy>
RationalFunction<Pol, AS> carl::operator- (
           const RationalFunction < Pol, AS > & lhs,
            const Monomial::Arg & rhs )
11.1.4.583 operator-() [27/43] template<typename Pol , bool AS>
RationalFunction<Pol, AS> carl::operator- (
            const RationalFunction< Pol, AS > & lhs,
            const Pol & rhs )
11.1.4.584 operator-() [28/43] template<typename Pol , bool AS>
RationalFunction<Pol, AS> carl::operator- (
            const RationalFunction< Pol, AS > & lhs,
            const RationalFunction< Pol, AS > & rhs )
11.1.4.585 operator-() [29/43] template<typename Pol , bool AS, DisableIf< needs_cache_type< Pol
>> = dummy>
RationalFunction<Pol, AS> carl::operator- (
            const RationalFunction < Pol, AS > & lhs,
             const Term< typename Pol::CoeffType > & rhs )
11.1.4.586 operator-() [30/43] template<typename Pol , bool AS>
RationalFunction<Pol, AS> carl::operator- (
            const RationalFunction< Pol, AS > & lhs,
            const typename Pol::CoeffType & rhs )
```

Performs a subtraction involving a polynomial using operator == ().

### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

### Returns

```
lhs - rhs
```

Performs a subtraction involving a polynomial using operator == ().

### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

### Returns

```
lhs - rhs
```

```
11.1.4.590 operator-() [34/43] template<typename C , typename O , typename P > auto carl::operator- ( const\ Term<\ C\ >\ \&\ lhs, const\ MultivariatePolynomial<\ C,\ O,\ P\ >\ \&\ rhs\ )\ [inline]
```

Performs a subtraction involving a polynomial using operator == ().

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs - rhs
```

Performs a subtraction involving a polynomial using operator == ().

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

lhs - rhs

Performs a subtraction involving a polynomial using operator == ().

# **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs - rhs
```

```
11.1.4.593 operator-() [37/43] template<typename Coeff > Term<Coeff> carl::operator- ( const Term< Coeff > & rhs )
```

Performs an subtraction involving a polynomial.

### **Parameters**

| _lhs | First argument.  |
|------|------------------|
| _rhs | Second argument. |

### Returns

```
_lhs - _rhs
```

# Parameters

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs - rhs
```

```
11.1.4.597 operator-() [41/43] template<typename C , EnableIf< carl::is_number_type< C >> = dummy>
```

Performs a subtraction involving a polynomial using operator == ().

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs - rhs
```

Performs a subtraction involving a polynomial using operator == ().

### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs - rhs
```

Performs a subtraction involving a polynomial using operator == ().

# **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs - rhs
```

Operator for the subtraction of two intervals with assignment.

### **Parameters**

| lhs | Lefthand side.  |
|-----|-----------------|
| rhs | Righthand side. |

## **Returns**

Resulting interval.

Operator for the subtraction of an interval and a number with assignment.

# Parameters

| lhs | Lefthand side.  |
|-----|-----------------|
| rhs | Righthand side. |

## Returns

Resulting interval.

```
11.1.4.602 operator/() [1/23] BVValue carl::operator/ (

const BVValue & lhs,

const BVValue & rhs) [inline]
```

Divide two integers.

Discards the remainder of the division.

### **Parameters**

| а | First argument.  |
|---|------------------|
| b | Second argument. |

## **Returns**

a/b.

Perform a multiplication involving a polynomial.

# **Parameters**

| ₋lhs | Left hand side.  |
|------|------------------|
| ₋rhs | Right hand side. |

```
_lhs * _rhs
```

Operator for the division of an interval and a number.

## **Parameters**

| lhs | Lefthand side.  |
|-----|-----------------|
| rhs | Righthand side. |

# Returns

Resulting interval.

Perform a multiplication involving a term.

### **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

```
lhs * rhs
```

```
11.1.4.609 operator/() [8/23] mpq_class carl::operator/ ( const mpq_class & n, const mpq_class & d ) [inline]
```

```
11.1.4.610 operator/() [9/23] mpz_class carl::operator/ ( const mpz_class & n, const mpz_class & d) [inline]
```

Perform a division involving a polynomial.

### **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

## Returns

lhs / rhs

## **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

# Returns

lhs / rhs

```
11.1.4.615 operator/() [14/23] template<typename Pol , bool AS>
RationalFunction<Pol, AS> carl::operator/ (
            const RationalFunction < Pol, AS > & lhs,
            const Pol & rhs )
11.1.4.616 operator/() [15/23] template<typename Pol , bool AS>
RationalFunction<Pol, AS> carl::operator/ (
            const RationalFunction< Pol, AS > & lhs,
             const RationalFunction< Pol, AS > & rhs )
11.1.4.617 operator/() [16/23] template<typename Pol , bool AS, DisableIf< needs_cache_type< Pol
>> = dummy>
RationalFunction<Pol, AS> carl::operator/ (
             const RationalFunction< Pol, AS > & lhs,
            const Term< typename Pol::CoeffType > & rhs )
11.1.4.618 operator/() [17/23] template<typename Pol , bool AS>
RationalFunction<Pol, AS> carl::operator/ (
            const RationalFunction < Pol, AS > & lhs,
            const typename Pol::CoeffType & rhs )
11.1.4.619 operator/() [18/23] template<typename Pol , bool AS> \,
RationalFunction<Pol, AS> carl::operator/ (
            const RationalFunction < Pol, AS > & lhs,
            unsigned long rhs )
11.1.4.620 operator/() [19/23] template<typename Pol , bool AS, DisableIf< needs_cache_type< Pol
>> = dummy>
RationalFunction<Pol, AS> carl::operator/ (
             const RationalFunction < Pol, AS > & lhs,
             Variable rhs )
11.1.4.621 operator/() [20/23] template<typename Coeff , EnableIf< carl::is_subset_of_rationals↔
_type< Coeff >> = dummy>
Term<Coeff> carl::operator/ (
            const Term< Coeff > & lhs,
             const Coeff & rhs ) [inline]
```

Perform a multiplication involving a term.

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

# Returns

```
lhs * rhs
```

## **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

# Returns

lhs / rhs

# **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

# Returns

```
lhs / rhs
```

Perform a multiplication involving a term.

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

# Returns

```
lhs * rhs
```

Operator for the division of an interval and a number with assignment.

## **Parameters**

| lhs | Lefthand side.  |
|-----|-----------------|
| rhs | Righthand side. |

## **Returns**

Resulting interval.

const BVTerm & rhs )

```
11.1.4.629 operator<() [4/63] bool carl::operator< (
             const BVTermContent & 1hs,
            const BVTermContent & rhs ) [inline]
11.1.4.630 operator<() [5/63] bool carl::operator< (
            const BVValue & lhs,
             const BVValue & rhs ) [inline]
11.1.4.631 operator<() [6/63] bool carl::operator< (
            const BVVariable & lhs,
             const BVVariable & rhs ) [inline]
11.1.4.632 operator<() [7/63] bool carl::operator< (
            const BVVariable & lhs,
             const Variable & rhs ) [inline]
11.1.4.633 operator<() [8/63] template<typename C , typename O , typename P >
bool carl::operator< (</pre>
            const C & lhs,
             const MultivariatePolynomial< C, O, P > & rhs ) [inline]
```

Checks if the first arguments is less than the second.

### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

lhs < rhs

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

### Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

```
11.1.4.635 operator<() [10/63] template<typename P > bool carl::operator< ( const\ Constraint<\ P > \&\ lhs, \\ const\ Constraint<<\ P > \&\ rhs\ )
```

Checks if the first arguments is less than the second.

## **Parameters**

| ₋lhs | First argument.  |
|------|------------------|
| ₋rhs | Second argument. |

### Returns

```
_lhs < _rhs
```

Checks if the first arguments is less than the second.

| ₋lhs | First argument.  |
|------|------------------|
| ₋rhs | Second argument. |

### Returns

```
_lhs < _rhs
```

Operator for the comparison of two intervals.

### **Parameters**

| lhs | Lefthand side.  |
|-----|-----------------|
| rhs | Righthand side. |

### Returns

True if the lefthand side is smaller than the righthand side.

11.1.4.640 operator<() [15/63] template<typename Number >

Operators for LowerBound and UpperBound.

Return true if lhs is smaller than rhs.

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

### Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

```
11.1.4.645 operator<() [20/63] template<typename C , typename O , typename P > bool carl::operator< ( const Monomial::Arg & lhs, const MultivariatePolynomial< C, O, P > & rhs) [inline]
```

Checks if the first arguments is less than the second.

# **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs < rhs
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Checks if the first arguments is less than the second.

### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs < rhs

```
11.1.4.649 operator<() [24/63] template<typename C , typename O , typename P > bool carl::operator< ( const MultivariatePolynomial< C, O, P > & lhs, const Monomial::Arg & rhs) [inline]
```

Checks if the first arguments is less than the second.

### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs < rhs

```
11.1.4.650 operator<() [25/63] template<typename C , typename O , typename P > bool carl::operator< ( const MultivariatePolynomial< C, O, P > & lhs, const MultivariatePolynomial< C, O, P > & rhs) [inline]
```

Checks if the first arguments is less than the second.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs < rhs

```
11.1.4.651 operator<() [26/63] template<typename C , typename O , typename P > bool carl::operator< ( const MultivariatePolynomial< C, O, P > & lhs, const Term< C > & rhs) [inline]
```

Checks if the first arguments is less than the second.

### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
Returns
```

```
lhs < rhs
```

Checks if the first arguments is less than the second.

### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

### Returns

lhs < rhs

```
11.1.4.654 operator<() [29/63] template<typename N > bool carl::operator< ( const N & lhs, const ThomEncoding< N > & rhs)
```

```
11.1.4.657 operator<() [32/63] template<typename Number >
bool carl::operator< (</pre>
             const Number & 1hs,
             const RealAlgebraicNumberThom< Number > & rhs )
11.1.4.658 operator<() [33/63] template<typename Number , typename RAN , typename = std::enable↔
_if_t<is_ran_type<RAN>::value>>
bool carl::operator< (</pre>
            const RAN & lhs,
             const Number & rhs )
11.1.4.659 operator<() [34/63] template<typename RAN , EnableIf< is_ran_type< RAN >> = dummy>
bool carl::operator< (</pre>
             const RAN & lhs,
             const RAN & rhs )
11.1.4.660 operator<() [35/63] template<typename Number >
bool carl::operator< (</pre>
             const RealAlgebraicNumberThom< Number > & lhs,
             const Number & rhs )
11.1.4.661 operator<() [36/63] template<typename Number >
bool carl::operator< (</pre>
             const RealAlgebraicNumberThom< Number > & lhs,
             const RealAlgebraicNumberThom< Number > & rhs )
11.1.4.662 operator<() [37/63] bool carl::operator< (
             const SortContent & 1hs,
             const SortContent & rhs ) [inline]
Parameters
 lhs
      Left SortContent
 rhs | Right SortContent
```

### Returns

lhs < rhs

Orders two sort values.

```
11.1.4.664 operator<() [39/63] template<typename C , typename O , typename P > bool carl::operator< ( const Term< C > & lhs, const MultivariatePolynomial< C, O, P > & rhs) [inline]
```

Checks if the first arguments is less than the second.

### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

### Returns

```
lhs < rhs
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

# **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\,\sim\,$  rhs,  $\sim$  being the relation that is checked.

Checks if the first arguments is less than the second.

#### **Parameters**

| ₋lhs | First argument.  |  |
|------|------------------|--|
| ₋rhs | Second argument. |  |

## Returns

```
_lhs < _rhs
```

# Parameters

| lhs | The left hand side.  |
|-----|----------------------|
| rhs | The right hand side. |

## Returns

true, if the left equality is less than the right one.

| lhs | Left UFContent.  |
|-----|------------------|
| rhs | Right UFContent. |

## Returns

true, if lhs is smaller than rhs.

# **Parameters**

| lhs | The left function instance.  |
|-----|------------------------------|
| rhs | The right function instance. |

## Returns

true, if lhs < rhs.

Checks whether one **UFModel** is smaller than another.

## Returns

true, if one uninterpreted function model is less than the other.

Check whether one uninterpreted function is smaller than another.

## Returns

true, if one uninterpreted function is less than the other one.

```
11.1.4.677 operator<() [52/63] template<typename C >
bool carl::operator< (</pre>
             const UnivariatePolynomial< C > & lhs,
             const UnivariatePolynomial< C > & rhs )
11.1.4.678 operator<() [53/63] template<typename Number >
bool carl::operator< (</pre>
             const UpperBound< Number > & lhs,
             const LowerBound< Number > & rhs ) [inline]
11.1.4.679 operator<() [54/63] template<typename Number >
bool carl::operator< (</pre>
             const UpperBound< Number > & 1hs,
             const UpperBound< Number > & rhs ) [inline]
11.1.4.680 operator<() [55/63] bool carl::operator< (
             const UTerm & 1hs,
             const UTerm & rhs )
Parameters
       The uninterpreted term to the left.
 lhs
 rhs
       The uninterpreted term to the right.
Returns
     true, if lhs is smaller than rhs.
11.1.4.681 operator<() [56/63] bool carl::operator< (
             const Variable & lhs,
             const BVVariable & rhs ) [inline]
```

11.1.4.682 operator<() [57/63] template<typename Poly >

const VariableAssignment< Poly > & lhs,
const VariableAssignment< Poly > & rhs )

bool carl::operator< (</pre>

Checks whether one sort is smaller than another.

# Returns

true, if lhs is less than rhs.

#### **Parameters**

| lhs | The left variable.  |
|-----|---------------------|
| rhs | The right variable. |

## Returns

true, if the left variable is smaller.

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

#### **Parameters**

| lhs | First argument.  |  |
|-----|------------------|--|
| rhs | Second argument. |  |

# Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Checks if the first arguments is less than the second.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

```
lhs < rhs
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

## **Parameters**

| lhs | First argument.  |  |
|-----|------------------|--|
| rhs | Second argument. |  |

# Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

| _OS   | The output stream to print on. |
|-------|--------------------------------|
| ₋sort | The sort to print.             |

## Returns

The output stream after printing the given sort on it.

Prints the factorization representation of the given factorized polynomial on the given output stream.

# Parameters

| ₋out   | The stream to print on.             |
|--------|-------------------------------------|
| _fpoly | The factorized polynomial to print. |

# Returns

The output stream after inserting the output.

Prints the given constraint on the given stream.

## **Parameters**

| os | The stream to print the given constraint on. |
|----|--|
| С  | The formula to print.                        |

## Returns

The stream after printing the given constraint on it.

| os | Output stream.     |
|----|--------------------|
| s  | set to be printed. |

#### Returns

Output stream.

The output operator of a term.

| os   | Output stream.               |
|------|------------------------------|
| term | Content of a bitvector term. |

```
11.1.4.707 operator <<() [19/78] template < typename Poly > std::ostream & carl::operator << ( std::ostream & os, const Constraint < Poly > & c)
```

Prints the given constraint on the given stream.

#### **Parameters**

| os | The stream to print the given constraint on. |
|----|--|
| С  | The formula to print.                        |

## Returns

The stream after printing the given constraint on it.

The output operator of a formula.

```
os The stream to print on.f The formula to print.
```

```
11.1.4.711 operator<<() [23/78] template<typename Pol >
std::ostream& carl::operator<< (</pre>
```

```
std::ostream & os,
const FormulaContent< Pol > & f )
```

The output operator of a formula.

| os | The stream to print on. |
|----|-------------------------|
| f  |                         |

```
11.1.4.712 operator <<() [24/78] template < typename Pol >
std::ostream& carl::operator<< (</pre>
             std::ostream & os,
             const FormulaContent< Pol > * fc)
11.1.4.713 operator << () [25/78] std::ostream& carl::operator << (
             std::ostream & os,
             const InfinityValue & iv ) [inline]
11.1.4.714 operator <<() [26/78] template < typename Num >
std::ostream& carl::operator<< (</pre>
            std::ostream & os,
             const IntRepRealAlgebraicNumber< Num > & ran )
11.1.4.715 operator<<() [27/78] std::ostream& carl::operator<< (
             std::ostream & os,
             const Logic & 1 ) [inline]
11.1.4.716 operator <<() [28/78] template < typename Number >
std::ostream& carl::operator<< (</pre>
            std::ostream & os,
             const LowerBound< Number > & 1b )
11.1.4.717 operator <<() [29/78] template < typename Rational , typename Poly >
std::ostream& carl::operator<< (</pre>
             std::ostream & os,
             const Model < Rational, Poly > & model)
```

```
11.1.4.718 operator <<() [30/78] template < typename Rational , typename Poly >
std::ostream& carl::operator<< (</pre>
            std::ostream & os,
             const ModelSubstitution< Rational, Poly > & ms ) [inline]
11.1.4.719 operator << () [31/78] template < typename Rational , typename Poly >
std::ostream& carl::operator<< (</pre>
             std::ostream & os,
             const ModelSubstitutionPtr< Rational, Poly > & ms ) [inline]
11.1.4.720 operator << () [32/78] template < typename R , typename P >
std::ostream& carl::operator<< (</pre>
             std::ostream & os,
             const ModelValue< R, P > & mv ) [inline]
11.1.4.721 operator<<() [33/78] std::ostream& carl::operator<< (
             std::ostream & os,
             const ModelVariable & mv ) [inline]
11.1.4.722 operator << () [34/78] std::ostream& carl::operator << (
             std::ostream & os,
             const Monomial & rhs ) [inline]
Streaming operator for Monomial.
Parameters
      Output stream.
 os
 rhs
      Monomial.
Returns
    os
```

Streaming operator for std::shared\_ptr<Monomial>.

| os  | Output stream. |
|-----|----------------|
| rhs | Monomial.      |

## Returns

os

const MultivariatePolynomial< C, O, P > & rhs ) [inline]

Streaming operator for multivariate polynomials.

std::ostream & os,

std::ostream & os,

std::ostream& carl::operator<< (</pre>

# Parameters

| os  | Output stream. |
|-----|----------------|
| rhs | Polynomial.    |

#### Returns

os.

const RealAlgebraicNumberThom< Num > & rhs )

```
11.1.4.728 operator <<() [40/78] template < class C >
std::ostream& carl::operator<< (</pre>
            std::ostream & os,
             const ReductorEntry< C > rhs )
11.1.4.729 operator <<() [41/78] std::ostream& carl::operator << (
             std::ostream & os,
             const Relation & r ) [inline]
11.1.4.730 operator<<() [42/78] std::ostream& carl::operator<< (
             std::ostream & os,
             const Sign & sign ) [inline]
11.1.4.731 operator <<() [43/78] template < typename N >
std::ostream& carl::operator<< (</pre>
             std::ostream & os,
             const SignDetermination< N > & rhs )
11.1.4.732 operator << () [44/78] std::ostream& carl::operator << (
             std::ostream & os,
             const SortValue & sv ) [inline]
Prints the given sort value on the given output stream.
```

| os | The output stream to print on. |
|----|--------------------------------|
| sv | The sort value to print.       |

## Returns

The output stream after printing the given sort value on it.

```
11.1.4.733 operator <<() [45/78] template < typename T > std::ostream & carl::operator << ( std::ostream & os, const std::deque < T > & v) [inline]
```

Output a std::deque with arbitrary content.

```
The format is [<length>: <item>, <item>, ...]
```

| os | Output stream.        |
|----|-----------------------|
| V  | vector to be printed. |

# Returns

Output stream.

```
11.1.4.734 operator << () [46/78] template < typename T > std::ostream & carl::operator << ( std::ostream & os, const std::forward_list < T > & l ) [inline]
```

Output a std::forward\_list with arbitrary content.

```
The format is [<item>, <item>, ...]
```

## **Parameters**

| os | Output stream.      |
|----|---------------------|
| 1  | list to be printed. |

# Returns

Output stream.

Output a std::initializer\_list with arbitrary content.

```
The format is [<item>, <item>, ...]
```

# **Parameters**

| os | Output stream.      |
|----|---------------------|
| 1  | list to be printed. |

#### Returns

Output stream.

```
11.1.4.736 operator << () [48/78] template < typename T > std::ostream & carl::operator << ( std::ostream & os, const std::list < T > & l ) [inline]
```

Output a std::list with arbitrary content.

```
The format is [<length>: <item>, <item>, ...]
```

#### **Parameters**

| os | Output stream.      |
|----|---------------------|
| 1  | list to be printed. |

## Returns

Output stream.

```
11.1.4.737 operator <<() [49/78] template<typename Key , typename Value , typename Comparator > std::ostream & carl::operator << ( std::ostream & os, const std::map< Key, Value, Comparator > & m ) [inline]
```

Output a std::map with arbitrary content.

```
The format is {<key>:<value>, <key>:<value>, ...}
```

# **Parameters**

| os | Output stream.     |
|----|--------------------|
| m  | map to be printed. |

#### Returns

Output stream.

Output a std::multimap with arbitrary content.

```
The format is \{<key>:<value>, <key>:<value>, \ldots \}
```

| os | Output stream.          |
|----|-------------------------|
| m  | multimap to be printed. |

## Returns

Output stream.

```
11.1.4.739 operator << () [51/78] template < typename T > std::ostream & carl::operator << ( std::ostream & os, const std::optional < T > & o ) [inline]
```

Output a std::optional with arbitrary content.

Prints empty if the optional holds no value and forwards the call to the content otherwise.

# **Parameters**

| os | Output stream.          |
|----|-------------------------|
| 0  | optional to be printed. |

# Returns

Output stream.

```
11.1.4.740 operator <<() [52/78] template < typename U , typename V > std::ostream & carl::operator << ( std::ostream \& os, \\ const std::pair < U, V > \& p ) [inline]
```

Output a std::pair with arbitrary content.

```
The format is (<first>, <second>)
```

## **Parameters**

| os | Output stream.      |
|----|---------------------|
| р  | pair to be printed. |

## Returns

Output stream.

```
11.1.4.741 operator <<() [53/78] template < typename T , typename C > std::ostream & carl::operator << ( std::ostream \& os, \\ const std::set < T, C > \& s ) [inline]
```

Output a std::set with arbitrary content.

```
The format is {<length>: <item>, <item>, ...}
```

## **Parameters**

| os | Output stream.     |
|----|--------------------|
| s  | set to be printed. |

#### Returns

Output stream.

```
11.1.4.743 operator << () [55/78] template < typename... T> std::ostream & carl::operator << ( std::ostream & os, const std::tuple < T... > & t )
```

Output a std::tuple with arbitrary content.

```
The format is (<item>, <item>, ...)
```

## **Parameters**

| os | Output stream.       |
|----|----------------------|
| t  | tuple to be printed. |

# Returns

Output stream.

```
11.1.4.744 operator << () [56/78] template < typename Key , typename Value , typename H , typename E , typename A >
```

Output a std::unordered\_map with arbitrary content.

```
The format is \{<key>:<value>, <key>:<value>, \ldots \}
```

#### **Parameters**

| os | Output stream.     |
|----|--------------------|
| m  | map to be printed. |

#### Returns

Output stream.

```
11.1.4.745 operator <<() [57/78] template < typename T , typename H , typename K , typename A > std::ostream & carl::operator << ( std::ostream & os, const std::unordered_set < T, H, K, A > & s ) [inline]
```

Output a std::unordered\_set with arbitrary content.

```
The format is {<length>: <item>, <item>, ...}
```

# **Parameters**

| os | Output stream.               |
|----|------------------------------|
| s  | unordered_set to be printed. |

# Returns

Output stream.

```
11.1.4.746 operator < () [58/78] template < typename T , typename... Tail> std::ostream & carl::operator < ( std::ostream & os, const std::variant < T, Tail... > & v ) [inline]
```

Output a std::variant with arbitrary content.

The call is simply forwarded to whatever content is currently stored in the variant.

| os | Output stream.         |
|----|------------------------|
| V  | variant to be printed. |

## Returns

Output stream.

```
11.1.4.747 operator <<() [59/78] template < typename T > std::ostream & carl::operator << ( std::ostream & os, const std::vector < T > & v ) [inline]
```

Output a std::vector with arbitrary content.

```
The format is [<length>: <item>, <item>, ...]
```

#### **Parameters**

| os | Output stream.        |
|----|-----------------------|
| V  | vector to be printed. |

# Returns

Output stream.

## **Parameters**

| os  | Output stream. |
|-----|----------------|
| rhs | Term.          |

## Returns

os

```
11.1.4.749 operator << () [61/78] template < typename N > std::ostream & carl::operator << ( std::ostream \ \& \ os, const\ ThomEncoding < \ N > \& \ rhs \ )
```

```
11.1.4.750 operator << () [62/78] std::ostream& carl::operator << ( std::ostream & os, const Timer & t ) [inline]
```

Streaming operator for a Timer.

Prints the result of t.passed().

#### **Parameters**

| os | Output stream. |
|----|----------------|
| t  | Timer.         |

#### Returns

os.

Prints the given uninterpreted equality on the given output stream.

## **Parameters**

| os  | The output stream to print on.       |
|-----|--------------------------------------|
| ueq | The uninterpreted equality to print. |

## Returns

The output stream after printing the given uninterpreted equality on it.

```
11.1.4.753 operator << () [65/78] std::ostream & carl::operator << ( std::ostream & os, const UFInstance & ufun )
```

Prints the given uninterpreted function instance on the given output stream.

| os   | The output stream to print on.                |
|------|---|
| ufun | The uninterpreted function instance to print. |

#### Returns

The output stream after printing the given uninterpreted function instance on it.

Prints the given uninterpreted function model on the given output stream.

## **Parameters**

| os  | The output stream to print on.             |
|-----|--|
| ufm | The uninterpreted function model to print. |

## Returns

The output stream after printing the given uninterpreted function model on it.

Prints the given uninterpreted function on the given output stream.

# Parameters

| os   | The output stream to print on.       |
|------|--------------------------------------|
| ufun | The uninterpreted function to print. |

#### Returns

The output stream after printing the given uninterpreted function on it.

| os  | Output stream. |
|-----|----------------|
| rhs | Polynomial.    |

#### Returns

os

Prints the given uninterpreted term on the given output stream.

const UTerm & ut )

## **Parameters**

| os | The output stream to print on.   |
|----|----------------------------------|
| ut | The uninterpreted term to print. |

## Returns

The output stream after printing the given uninterpreted term on it.

```
11.1.4.761 operator << () [73/78] std::ostream& carl::operator << ( std::ostream & os, const VariableType & t ) [inline]
```

Streaming operator for VariableType.

## **Parameters**

| os | Output Stream. |
|----|----------------|
| t  | VariableType.  |

Returns

os.

Prints the given uninterpreted variable on the given output stream.

## **Parameters**

| os   | The output stream to print on.       |
|------|--------------------------------------|
| uvar | The uninterpreted variable to print. |

# Returns

The output stream after printing the given uninterpreted variable on it.

Streaming operator for Variable.

| os  | Output stream. |
|-----|----------------|
| rhs | Variable.      |

## Returns

os

Checks if the first argument is less or equal than the second.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs <= rhs
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Check whether the bits of one condition are always set if the corresponding bit of another condition is set.

Essentially checks for an implication.

#### **Parameters**

| lhs | The first condition.  |
|-----|-----------------------|
| rhs | The second condition. |

## Returns

true, if all bits of lhs are set if the corresponding bit of rhs are set; false, otherwise.

Checks if the first arguments is less or equal than the second.

| _lhs | First argument.  |
|------|------------------|
| ₋rhs | Second argument. |

#### Returns

```
_lhs <= _rhs
```

Checks if the first arguments is less or equal than the second.

#### **Parameters**

| ₋lhs | First argument.  |
|------|------------------|
| ₋rhs | Second argument. |

#### Returns

```
_lhs <= _rhs
```

Operator for the comparison of two intervals.

#### **Parameters**

| lhs | Lefthand side.  |
|-----|-----------------|
| rhs | Righthand side. |

## Returns

True if the righthand side has maximal one intersection with the lefthand side at the upper bound of lhs.

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Checks if the first argument is less or equal than the second.

# **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs <= rhs
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Checks if the first argument is less or equal than the second.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs <= rhs
```

Checks if the first argument is less or equal than the second.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

```
lhs <= rhs
```

Checks if the first argument is less or equal than the second.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

```
lhs <= rhs
```

Checks if the first argument is less or equal than the second.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

```
lhs <= rhs
```

Checks if the first argument is less or equal than the second.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs <= rhs
```

Checks if the first argument is less or equal than the second.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs <= rhs
```

Checks if the first argument is less or equal than the second.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

```
lhs <= rhs
```

```
11.1.4.789 operator<=() [23/41] template<typename N > bool carl::operator<= ( const N & lhs, const ThomEncoding< N > & rhs)
```

Checks if the first argument is less or equal than the second.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

```
lhs <= rhs
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\,\sim\,$  rhs,  $\sim$  being the relation that is checked.

Checks if the first arguments is less or equal than the second.

#### **Parameters**

| ₋lhs | First argument.  |
|------|------------------|
| ₋rhs | Second argument. |

## Returns

```
_lhs <= _rhs
```

Checks if the first argument is less or equal than the second.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## **Returns**

```
lhs <= rhs
```

Checks if the first argument is less or equal than the second.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

```
lhs <= rhs
```

const Monomial::Arg & rhs ) [inline]

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

Variable lhs,

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Checks if the first argument is less or equal than the second.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

```
lhs <= rhs
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

```
11.1.4.811 operator==() [4/81] bool carl::operator== (
            const BVConstraint & 1hs,
            const BVConstraint & rhs )
11.1.4.812 operator==() [5/81] bool carl::operator== (
             const BVTerm & 1hs,
             const BVTerm & rhs )
11.1.4.813 operator==() [6/81] bool carl::operator== (
            const BVTermContent & lhs,
             const BVTermContent & rhs ) [inline]
11.1.4.814 operator==() [7/81] bool carl::operator== (
            const BVValue & lhs,
             const BVValue & rhs ) [inline]
11.1.4.815 operator==() [8/81] bool carl::operator== (
            const BVVariable & lhs,
             const BVVariable & rhs ) [inline]
11.1.4.816 operator==() [9/81] bool carl::operator== (
            const BVVariable & lhs,
             const Variable & rhs ) [inline]
11.1.4.817 operator==() [10/81] template<typename C , typename O , typename P >
bool carl::operator== (
            const C & lhs,
             const MultivariatePolynomial< C, O, P > & rhs ) [inline]
```

Checks if the two arguments are equal.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs == rhs
```

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs == rhs
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Checks if the two arguments are equal.

#### **Parameters**

| ₋lhs | First argument.  |
|------|------------------|
| ₋rhs | Second argument. |

#### Returns

```
_lhs == _rhs
```

Checks if the two arguments are equal.

#### **Parameters**

| ₋lhs | First argument.  |
|------|------------------|
| _rhs | Second argument. |

```
_lhs == _rhs
```

Returns

Returns

Operator for the comparison of two intervals.

| lhs | Lefthand side.  |
|-----|-----------------|
| rhs | Righthand side. |

True if both intervals are equal.

Check if two Assignments are equal.

Two Assignments are considered equal, if both are either bool or not bool and their value is the same.

If both Assignments are not bools, the check may return false although they represent the same value. If both are numbers in different representations, this comparison is only done as a "best effort".

#### **Parameters**

| lhs | First Assignment.  |
|-----|--------------------|
| rhs | Second Assignment. |

## Returns

Ihs == rhs.

Return true if lhs is equal to rhs.

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Checks if the two arguments are equal.

### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs == rhs
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Checks if the two arguments are equal.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs == rhs
```

Checks if the two arguments are equal.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

```
lhs == rhs
```

Checks if the two arguments are equal.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs == rhs
```

Checks if the two arguments are equal.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs == rhs
```

Checks if the two arguments are equal.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs == rhs
```

Checks if the two arguments are equal.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs == rhs
```

Checks if the two arguments are equal.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs == rhs
```

Checks if the two arguments are equal.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs == rhs
```

```
11.1.4.848 operator==() [41/81] template<typename N > bool carl::operator== ( const N & lhs, const ThomEncoding< N > & rhs)
```

```
11.1.4.849 operator==() [42/81] template<typename Number >
bool carl::operator== (
                                             const Number & lhs,
                                               const Interval < Number > & rhs ) [inline]
11.1.4.850 operator==() [43/81] template<typename Number , typename RAN , typename = std\leftrightarrow
 ::enable_if_t<is_ran_type<RAN>::value>>
bool carl::operator== (
                                             const Number & lhs,
                                              const RAN & rhs )
11.1.4.851 operator==() [44/81] template<typename Number >
bool carl::operator== (
                                              const Number & lhs,
                                               const RealAlgebraicNumberThom< Number > & rhs )
11.1.4.852 operator==() [45/81] template<typename Number , typename RAN , typename = std \leftarrow
 ::enable_if_t<is_ran_type<RAN>::value>>
bool carl::operator== (
                                             const RAN & lhs,
                                              const Number & rhs )
\textbf{11.1.4.853} \quad \textbf{operator==()} \; \texttt{[46/81]} \quad \texttt{template} < \texttt{typename} \; \texttt{RAN} \; \text{,} \; \texttt{EnableIf} < \; \texttt{is\_ran\_type} < \; \texttt{RAN} \; >> \; = \; \texttt{dummy} > \; \texttt{
bool carl::operator== (
                                             const RAN & lhs,
                                              const RAN & rhs )
11.1.4.854 operator==() [47/81] template<typename Number >
bool carl::operator== (
                                              const RealAlgebraicNumberThom< Number > & lhs,
                                               const Number & rhs )
11.1.4.855 operator==() [48/81] template<typename Number >
bool carl::operator== (
                                              const RealAlgebraicNumberThom< Number > & lhs,
                                               const RealAlgebraicNumberThom< Number > & rhs )
```

Compares two sort values for equality.

Compare a pair of variable and exponent with a variable.

Returns true, if both variables are the same.

#### **Parameters**

| р | Pair of variable and exponent. |  |
|---|--------------------------------|--|
| V | Variable.                      |  |

#### Returns

```
p.first == v
```

Checks if the two arguments are equal.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs == rhs
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

```
11.1.4.864 operator==() [57/81] template<typename N >
bool carl::operator== (
            const ThomEncoding < N > & lhs,
            const N & rhs )
11.1.4.865 operator==() [58/81] template<typename N >
bool carl::operator== (
            const ThomEncoding< N > & lhs,
            const ThomEncoding< N > & rhs )
11.1.4.866 operator==() [59/81] template<typename T , class I >
bool carl::operator== (
            const TypeInfoPair< T, I > & _tipA,
             const TypeInfoPair< T, I > & _tipB )
11.1.4.867 operator==() [60/81] template<typename P >
bool carl::operator== (
            const typename FactorizedPolynomial< P >::CoeffType & _lhs,
             const FactorizedPolynomial< P > & \_rhs ) [inline]
```

Checks if the two arguments are equal.

| ₋lhs | First argument.  |
|------|------------------|
| ₋rhs | Second argument. |

## Returns

```
_lhs == _rhs
```

## **Parameters**

| lhs | The left hand side.  |
|-----|----------------------|
| rhs | The right hand side. |

## Returns

true, if lhs and rhs are equal.

# **Parameters**

| lhs | Left UFContent.  |
|-----|------------------|
| rhs | Right UFContent. |

# Returns

true, if lhs and rhs are the same.

| lhs | The left function instance.  |
|-----|------------------------------|
| rhs | The right function instance. |

true, if lhs == rhs.

Compares two **UFModel** objects for equality.

#### Returns

true, if the two uninterpreted function models are equal.

Check whether two uninterpreted functions are equal.

## Returns

true, if the two given uninterpreted functions are equal.

Checks if the two arguments are equal.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
Returns
```

```
lhs == rhs
```

Checks if the two arguments are equal.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

```
lhs == rhs
```

| lhs | The uninterpreted term to the left.  |
|-----|--------------------------------------|
| rhs | The uninterpreted term to the right. |

true, if the given uninterpreted terms are equal.

```
11.1.4.879 operator==() [72/81] bool carl::operator== (
             const Variable & lhs,
             const BVVariable & rhs ) [inline]
11.1.4.880 operator==() [73/81] template<typename Poly >
bool carl::operator== (
            const VariableAssignment < Poly > & lhs,
            const VariableAssignment< Poly > & rhs )
11.1.4.881 operator==() [74/81] template<typename Poly >
bool carl::operator== (
            const VariableComparison< Poly > & lhs,
            const VariableComparison< Poly > & rhs )
11.1.4.882 operator==() [75/81] bool carl::operator== (
             InfinityValue 1hs,
             InfinityValue rhs ) [inline]
11.1.4.883 operator==() [76/81] template<typename IntegerT >
bool carl::operator== (
            int lhs,
            const GFNumber< IntegerT > & rhs )
Returns
11.1.4.884 operator==() [77/81] bool carl::operator== (
             Sort lhs,
             Sort rhs ) [inline]
```

| lhs | The left sort.  |
|-----|-----------------|
| rhs | The right sort. |

true, if the sorts are the same.

## **Parameters**

| lhs | The left variable.  |
|-----|---------------------|
| rhs | The right variable. |

## Returns

true, if the variable are equal.

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Checks if the two arguments are equal.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs == rhs
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

lhs  $\,\sim\,$  rhs,  $\sim$  being the relation that is checked.

```
11.1.4.889 operator>() [1/37] template<typename P > bool carl::operator> ( const\ BasicConstraint< P > \&\ lhs, \\ const\ BasicConstraint< P > \&\ rhs\ )
```

Checks if the first argument is greater than the second.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs > rhs
```

```
11.1.4.891 operator>() [3/37] template<typename Coeff > bool carl::operator> ( const Coeff & lhs, const Term< Coeff > & rhs) [inline]
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Checks if the first arguments is greater than the second.

## **Parameters**

| _lhs | First argument.  |
|------|------------------|
| _rhs | Second argument. |

# Returns

```
_{\rm lhs} > _{\rm rhs}
```

Checks if the first arguments is greater than the second.

| ₋lhs | First argument.  |
|------|------------------|
| ₋rhs | Second argument. |

## Returns

```
_{\rm lhs} > _{\rm rhs}
```

Operator for the comparison of two intervals.

#### **Parameters**

| lhs | Lefthand side.  |
|-----|-----------------|
| rhs | Righthand side. |

## Returns

True if the lefthand side is larger than the righthand side.

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Checks if the first argument is greater than the second.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

lhs > rhs

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Checks if the first argument is greater than the second.

### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs > rhs
```

Checks if the first argument is greater than the second.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs > rhs
```

Checks if the first argument is greater than the second.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs > rhs

Checks if the first argument is greater than the second.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs > rhs

Checks if the first argument is greater than the second.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs > rhs
```

Checks if the first argument is greater than the second.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

lhs > rhs

Checks if the first argument is greater than the second.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs > rhs
```

```
11.1.4.908 operator>() [20/37] template<typename N > bool carl::operator> ( const N & lhs, const ThomEncoding< N > & rhs)
```

```
11.1.4.909 operator>() [21/37] template<typename Number >
bool carl::operator> (
            const Number & lhs,
             const Interval< Number > & rhs ) [inline]
11.1.4.910 operator>() [22/37] template<typename Number , typename RAN , typename = std::enable \leftarrow
_if_t<is_ran_type<RAN>::value>>
bool carl::operator> (
            const Number & lhs,
            const RAN & rhs )
11.1.4.911 operator>() [23/37] template<typename Number , typename RAN , typename = std::enable←
_if_t<is_ran_type<RAN>::value>>
bool carl::operator> (
            const RAN & lhs,
            const Number & rhs )
11.1.4.912 operator>() [24/37] template<typename RAN , EnableIf< is_ran_type< RAN >> = dummy>
bool carl::operator> (
            const RAN & lhs,
             const RAN & rhs )
11.1.4.913 operator>() [25/37] template<typename C , typename O , typename P >
bool carl::operator> (
             const Term< C > & lhs,
             const MultivariatePolynomial< C, O, P > & rhs ) [inline]
Checks if the first argument is greater than the second.
Parameters
 lhs
      First argument.
 rhs
      Second argument.
```

lhs > rhs

```
11.1.4.914 operator>() [26/37] template<typename Coeff > bool carl::operator> (
```

```
const Term< Coeff > & lhs,
const Coeff & rhs ) [inline]
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

# **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

```
11.1.4.919 operator>() [31/37] template<typename N > bool carl::operator> ( const\ ThomEncoding<\ N\ >\ \&\ lhs, const\ ThomEncoding<\ N\ >\ \&\ rhs\ )
```

Checks if the first arguments is greater than the second.

# **Parameters**

| ₋lhs | First argument.  |
|------|------------------|
| ₋rhs | Second argument. |

```
_lhs > _rhs
```

Checks if the first argument is greater than the second.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs > rhs

Checks if the first argument is greater than the second.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

lhs > rhs

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Checks if the first argument is greater than the second.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

lhs > rhs

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Checks if the first argument is greater or equal than the second.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

```
lhs >= rhs
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Checks if the first arguments is greater or equal than the second.

| ₋lhs | First argument.  |
|------|------------------|
| ₋rhs | Second argument. |

## Returns

```
_lhs >= _rhs
```

Checks if the first arguments is greater or equal than the second.

#### **Parameters**

| ₋lhs | First argument.  |
|------|------------------|
| ₋rhs | Second argument. |

## Returns

```
_lhs >= _rhs
```

Operator for the comparison of two intervals.

#### **Parameters**

| lhs | Lefthand side.  |
|-----|-----------------|
| rhs | Righthand side. |

## Returns

True if the lefthand side has maximal one intersection with the righthand side at the lower bound of lhs.

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Checks if the first argument is greater or equal than the second.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs >= rhs
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Checks if the first argument is greater or equal than the second.

### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

lhs >= rhs

Checks if the first argument is greater or equal than the second.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

#### Returns

```
lhs >= rhs
```

Checks if the first argument is greater or equal than the second.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs >= rhs
```

Checks if the first argument is greater or equal than the second.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs >= rhs
```

Checks if the first argument is greater or equal than the second.

# **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs >= rhs
```

Checks if the first argument is greater or equal than the second.

# **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs >= rhs
```

Checks if the first argument is greater or equal than the second.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs >= rhs
```

```
11.1.4.945 operator>=() [20/37] template<typename N >
bool carl::operator>= (
            const N & lhs,
            const ThomEncoding< N > & rhs )
11.1.4.946 operator>=() [21/37] template<typename Number >
bool carl::operator>= (
            const Number & lhs,
            const Interval < Number > & rhs ) [inline]
11.1.4.947 operator>=() [22/37] template<typename Number , typename RAN , typename = std\leftrightarrow
::enable_if_t<is_ran_type<RAN>::value>>
bool carl::operator>= (
            const Number & lhs,
            const RAN & rhs )
11.1.4.948 operator>=() [23/37] template<typename Number , typename RAN , typename = std\leftrightarrow
::enable_if_t<is_ran_type<RAN>::value>>
bool carl::operator>= (
            const RAN & lhs,
            const Number & rhs )
11.1.4.949 operator>=() [24/37] template<typename RAN , EnableIf< is_ran_type< RAN >> = dummy>
bool carl::operator>= (
            const RAN & lhs,
            const RAN & rhs )
11.1.4.950 operator>=() [25/37] template<typename C , typename O , typename P >
bool carl::operator>= (
            const Term< C > & lhs,
             const MultivariatePolynomial< C, O, P > & rhs ) [inline]
```

Checks if the first argument is greater or equal than the second.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs >= rhs
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

# **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

# **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

lhs  $\,\sim\,$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

# **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

# **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Checks if the first arguments is greater or equal than the second.

# **Parameters**

| _lhs | First argument.  |
|------|------------------|
| ₋rhs | Second argument. |

# Returns

```
_{\rm lhs} >= _{\rm rhs}
```

Checks if the first argument is greater or equal than the second.

# **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs >= rhs
```

Checks if the first argument is greater or equal than the second.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs >= rhs
```

Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

# **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Checks if the first argument is greater or equal than the second.

# **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# Returns

```
lhs >= rhs
```

Compares two arguments where one is a term and the other is either a term, a monomial or a variable.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

# **Returns**

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

```
11.1.4.963 operator>>() BVValue carl::operator>> (
            const BVValue & 1hs,
             const BVValue & rhs ) [inline]
11.1.4.964 operator^{\wedge}() BVValue carl::operator^{\wedge} (
            const BVValue & lhs,
             const BVValue & rhs ) [inline]
11.1.4.965 operator" | () [1/2] BitVector carl::operator| (
            const BitVector & lhs,
             const BitVector & rhs )
11.1.4.966 operator" | () [2/2] BVValue carl::operator (
             const BVValue & 1hs,
             const BVValue & rhs ) [inline]
11.1.4.967 operator~() BVValue carl::operator~ (
            const BVValue & val ) [inline]
11.1.4.968 overloaded() template<class... Ts>
carl::overloaded (
             Ts... ) -> overloaded< Ts... >
```

```
11.1.4.969 parse() template<typename T >
T carl::parse (
            const std::string & n ) [inline]
11.1.4.970 parse < cln::cl_l >() template <>
cln::cl_I carl::parse< cln::cl_I > (
            const std::string & n )
11.1.4.971 parse < cln::cl_RA >() template <>
cln::cl_RA carl::parse< cln::cl_RA > (
           const std::string & n )
11.1.4.972 parse< mpq_class >() template<>
mpq_class carl::parse< mpq_class > (
           const std::string & n )
11.1.4.973 parse< mpz_class >() template<>
mpz_class carl::parse< mpz_class > (
           const std::string & n )
11.1.4.974 pow() [1/14] template<>
cln::cl_RA carl::pow (
            const cln::cl_RA & basis,
            std::size_t exp ) [inline]
```

Calculate the power of some fraction to some positive integer.

# **Parameters**

| basis | Basis.    |
|-------|-----------|
| exp   | Exponent. |

Returns

 $n^e$ 

```
11.1.4.975 pow() [2/14] template<typename FloatType >
FLOAT_T<FloatType> carl::pow (
           const FLOAT_T< FloatType > & _in,
            size_t _exp ) [inline]
11.1.4.976 pow()[3/14] template<typename Number , typename Integer >
Interval<Number> carl::pow (
            const Interval< Number > & i,
            Integer exp )
11.1.4.977 pow() [4/14] Monomial::Arg carl::pow (
             const Monomial & m,
             uint exp ) [inline]
Calculates the given power of a monomial m.
Parameters
       The monomial.
      Exponent.
 exp
Returns
    m to the power of exp.
11.1.4.978 pow() [5/14] Monomial::Arg carl::pow (
            const Monomial::Arg & m,
             uint exp ) [inline]
11.1.4.979 pow() [6/14] template<>
mpq_class carl::pow (
            const mpq_class & basis,
            std::size_t exp ) [inline]
11.1.4.980 pow() [7/14] template<>
mpz_class carl::pow (
            const mpz_class & basis,
```

std::size\_t exp ) [inline]

11.1.4.982 pow() [9/14] template<typename T , DisableIf< is\_interval\_type< T >> = dummy>

Implements a fast exponentiation on an arbitrary type T.

const T & basis,
std::size\_t exp )

To use carl::pow() on a type T, the following must be defined:

- carl::constant\_one<T>,
- T::operator=(const T&) and
- operator\*(const T&, const T&). Alternatively, carl::pow() can be specialized for T explicitly.

# **Parameters**

T carl::pow (

| basis | A number.     |
|-------|---------------|
| exp   | The exponent. |

# Returns

basis to the power of  $\exp$ .

```
11.1.4.983 pow() [10/14] template<typename Coeff > Term<Coeff> carl::pow ( const Term< Coeff > & t, uint exp)
```

Returns a polynomial to the given power.

| р   | The polynomial. |
|-----|-----------------|
| exp | Exponent.       |

# Returns

The polynomial to the power of exp.

```
11.1.4.985 pow() [12/14] double carl::pow (
            double in,
            uint exp ) [inline]
11.1.4.986 pow() [13/14] template<typename Pol , bool AS>
RationalFunction<Pol, AS> carl::pow (
            unsigned exp,
            const RationalFunction< Pol, AS > & rf )
11.1.4.987 pow() [14/14] Monomial::Arg carl::pow (
            Variable v,
             std::size_t exp )
11.1.4.988 pow_assign() [1/2] template<typename Number , typename Integer >
void carl::pow_assign (
            Interval< Number > & i,
            Integer exp )
11.1.4.989 pow_assign() [2/2] template<typename T >
void carl::pow_assign (
            T & t,
             std::size_t exp )
```

Implements a fast exponentiation on an arbitrary type T.

The result is stored in the given number. To use carl::pow\_assign() on a type T, the following must be defined:

- carl::constant\_one<T>,
- T::operator=(const T&) and
- operator\*(const T&, const T&). Alternatively, carl::pow() can be specialized for T explicitly.

| t   | A number.     |
|-----|---------------|
| exp | The exponent. |

Computes the GCD of two univariate polynomial with coefficients from a unique factorization domain using the primitive euclidean algorithm.

See also

?, page 57, Algorithm 2.3

```
11.1.4.992 primitive_part() template<typename Coeff > UnivariatePolynomial<Coeff> carl::primitive_part ( const UnivariatePolynomial< Coeff > & p)
```

The primitive part of p is the normal part of p divided by the content of p.

The primitive part of zero is zero.

See also

?, page 53, definition 2.18

Returns

The primitive part of the polynomial.

11.1.4.995 printStacktrace() void carl::printStacktrace ( )

Uses GDB to print a stack trace.

Returns this/divisor where divisor is the numeric content of this polynomial.

Returns

Calculates the pseudo-remainder.

See also

?, page 55, Pseudo-Division Property

Divide two integers.

Discards the remainder of the division.

| а | First argument.  |
|---|------------------|
| b | Second argument. |

# Returns

a/b.

Divide two fractions.

# **Parameters**

| а | First argument.  |
|---|------------------|
| b | Second argument. |

# Returns

a/b.

Implements the division with remainder.

# **Parameters**

| ₋lhs |  |
|------|--|
| _rhs |  |

# Returns

Number which holds the result.

```
11.1.4.1002 quotient() [4/9] template<typename IntegerT >
GFNumber<IntegerT> carl::quotient (
```

```
const GFNumber< IntegerT > & lhs,
const GFNumber< IntegerT > & rhs )
```

Implements the division with remainder.

# **Parameters**

| ₋lhs |  |
|------|--|
| ₋rhs |  |

# Returns

Interval which holds the result.

```
11.1.4.1004 quotient() [6/9] mpq_class carl::quotient ( const mpq_class & n, const mpq_class & d) [inline]
```

```
11.1.4.1005 quotient() [7/9] mpz_class carl::quotient ( const mpz_class & n, const mpz_class & d) [inline]
```

```
11.1.4.1006 quotient() [8/9] template<typename C , typename O , typename P > MultivariatePolynomial<C,O,P> carl::quotient ( const\ MultivariatePolynomial<\ C,\ O,\ P>\ \&\ dividend,\\ const\ MultivariatePolynomial<\ C,\ O,\ P>\ \&\ divisor\ )
```

Calculates the quotient of a polynomial division.

```
11.1.4.1008 rationalize() [1/7] template<typename T >
T carl::rationalize (
            const PreventConversion< mpq_class > & ) [inline]
11.1.4.1009 rationalize() [2/7] template<>
double carl::rationalize (
           double n ) [inline]
11.1.4.1010 rationalize() [3/7] template<typename T >
T carl::rationalize (
            double n ) [inline]
11.1.4.1011 rationalize() [4/7] template<typename T >
T carl::rationalize (
            float n ) [inline]
11.1.4.1012 rationalize() [5/7] template<typename T >
T carl::rationalize (
           int n ) [inline]
11.1.4.1013 rationalize() [6/7] template<typename T >
T carl::rationalize (
            sint n ) [inline]
11.1.4.1014 rationalize() [7/7] template<typename T >
T carl::rationalize (
            uint n ) [inline]
11.1.4.1015 rationalize < cln::cl_RA >() [1/5] template <>
cln::cl_RA carl::rationalize< cln::cl_RA > (
            double n )
```

```
11.1.4.1016 rationalize < cln::cl_RA >() [2/5] template <>
cln::cl_RA carl::rationalize< cln::cl_RA > (
            float n)
11.1.4.1017 rationalize < cln::cl_RA >() [3/5] template <>
cln::cl_RA carl::rationalize< cln::cl_RA > (
           int n ) [inline]
11.1.4.1018 rationalize < cln::cl_RA >() [4/5] template <>
cln::cl_RA carl::rationalize< cln::cl_RA > (
            sint n ) [inline]
11.1.4.1019 rationalize < cln::cl_RA >() [5/5] template <>
cln::cl_RA carl::rationalize< cln::cl_RA > (
            uint n ) [inline]
11.1.4.1020 rationalize < FLOAT_T < double > >() template <>
FLOAT_T<double> carl::rationalize< FLOAT_T< double > > (
           double n ) [inline]
11.1.4.1021 rationalize < FLOAT_T < float > >() template <>
FLOAT_T<float> carl::rationalize< FLOAT_T< float > > (
            float n ) [inline]
11.1.4.1022 rationalize < FLOAT_T < mpq_class > >() template <>
double n ) [inline]
11.1.4.1023 rationalize < mpq_class >() [1/6] template <>
mpq_class carl::rationalize< mpq_class > (
           const PreventConversion< mpq_class > \& n ) [inline]
```

```
11.1.4.1024 rationalize < mpq_class >() [2/6] template <>
mpq_class carl::rationalize< mpq_class > (
             double n ) [inline]
11.1.4.1025 rationalize < mpq_class >() [3/6] template <>
mpq_class carl::rationalize< mpq_class > (
             float n ) [inline]
11.1.4.1026 rationalize < mpq_class >() [4/6] template <>
mpq_class carl::rationalize< mpq_class > (
             int n ) [inline]
11.1.4.1027 rationalize < mpq_class >() [5/6] template <>
mpq_class carl::rationalize< mpq_class > (
             sint n ) [inline]
11.1.4.1028 rationalize < mpq_class >() [6/6] template <>
mpq_class carl::rationalize< mpq_class > (
            uint n ) [inline]
11.1.4.1029 real_roots() [1/3] template<typename Coeff , typename Ordering , typename Policies >
auto carl::real_roots (
             const ContextPolynomial< Coeff, Ordering, Policies > & p,
             const Assignment< typename ContextPolynomial< Coeff, Ordering, Policies > \leftarrow
::RootType > & a )
11.1.4.1030 real_roots() [2/3] template<typename Coeff , typename Number >
RealRootsResult<IntRepRealAlgebraicNumber<Number> > carl::real_roots (
             const UnivariatePolynomial< Coeff > & poly,
             const Assignment< IntRepRealAlgebraicNumber< Number >> & varToRANMap,
             const Interval < Number > & interval = Interval < Number >::unbounded_interval() )
```

Replace all variables except one of the multivariate polynomial 'p' by numbers as given in the mapping 'm', which creates a univariate polynomial, and return all roots of that created polynomial.

Note that 'p' is represented as a univariate polynomial with polynomial coefficients. Its main variable is not replaced and stays the main variable of the created polynomial. However, all variables in the polynomial coefficients are replaced, which is why

- the main variable of 'p' must not be in 'm'
- · all variables from the coefficients of 'p' must be in 'm'

The roots are sorted in ascending order. Returns a RealRootsResult indicating whether the roots could be isolated or the polynomial was not univariate or is nullified.

Find all real roots of a univariate 'polynomial' with numeric coefficients within a given 'interval'.

Find all real roots of a univariate 'polynomial' with non-numeric coefficients within a given 'interval'.

The roots are sorted in ascending order.

However, all coefficients must be types that contain numeric numbers that are retrievable by using .constant\_part(); The roots are sorted in ascending order.

```
11.1.4.1032 real_variables() template<typename T >
carlVariables carl::real_variables (
            const T & t ) [inline]
11.1.4.1033 realRootsThom() [1/3] template<typename Number >
std::list<ThomEncoding<Number> > carl::realRootsThom (
             const MultivariatePolynomial< Number > & p,
             Variable::Arg mainVar,
             const std::map< Variable, ThomEncoding< Number >> & m = {},
             const Interval < Number > & interval = Interval < Number>::unbounded_interval() )
11.1.4.1034 realRootsThom() [2/3] template<typename Number >
std::list< ThomEncoding< Number > > carl::realRootsThom (
             const MultivariatePolynomial< Number > & p,
             Variable::Arg mainVar,
             std::shared_ptr< ThomEncoding< Number >> point_ptr,
             const Interval < Number > & interval = Interval < Number >::unbounded_interval() )
11.1.4.1035 realRootsThom() [3/3] template<typename Coeff , typename Number >
\verb|std::list<RealAlgebraicNumber<Number>> carl::realRootsThom (|
            const UnivariatePolynomial< Coeff > & p,
            const std::map< Variable, RealAlgebraicNumber >> & m,
             const Interval < Number > & interval )
11.1.4.1036 reciprocal() [1/2] cln::cl_RA carl::reciprocal (
             const cln::cl_RA & a ) [inline]
```

```
11.1.4.1037 reciprocal() [2/2] mpq_class carl::reciprocal (
              const mpq_class & a ) [inline]
\textbf{11.1.4.1038} \quad \textbf{relationIsSigned()} \quad \texttt{bool carl::relationIsSigned ()}
              BVCompareRelation \_r) [inline]
11.1.4.1039 relationIsStrict() bool carl::relationIsStrict (
              BVCompareRelation _r ) [inline]
11.1.4.1040 remainder() [1/6] cln::cl_I carl::remainder (
              const cln::cl_I & a,
              const cln::cl_I & b ) [inline]
Calculate the remainder of the integer division.
Parameters
     First argument.
     Second argument.
Returns
     a\%b.
\textbf{11.1.4.1041} \quad \textbf{remainder()} \; \texttt{[2/6]} \quad \texttt{mpz\_class carl::remainder} \; \; \texttt{(}
              const mpz_class & n,
              const mpz_class & m ) [inline]
11.1.4.1042 remainder() [3/6] template<typename C , typename O , typename P >
MultivariatePolynomial<C,O,P> carl::remainder (
              const MultivariatePolynomial < C, O, P > & dividend,
              const MultivariatePolynomial< C, O, P > & divisor )
11.1.4.1043 remainder() [4/6] template<typename Coeff >
UnivariatePolynomial<Coeff> carl::remainder (
              const UnivariatePolynomial< Coeff > & dividend,
              const UnivariatePolynomial< Coeff > & divisor )
```

Does the heavy lifting for the remainder computation of polynomial division.

const Coeff \* prefactor = nullptr )

# **Parameters**

| divisor   |  |
|-----------|--|
| prefactor |  |

# See also

?, page 55, Pseudo-Division Property

Returns

Replaces the main variable in a polynomial.

| р      | The polynomial.    |  |
|--------|--------------------|--|
| newVar | New main variable. |  |

# Returns

New polynomial.

Resolves the outermost negation of this formula.

### **Parameters**

bool carl::returnFalse (

const T & ,
const T & )

```
_keepConstraint A flag indicating whether to change constraints in order to resolve the negation in front of them, or to keep the constraints and leave the negation.
```

```
11.1.4.1053 root_safe() [1/2] std::pair<cln::cl_RA, cln::cl_RA> carl::root_safe ( const cln::cl_RA & a, uint n)
```

```
11.1.4.1054 root_safe() [2/2] std::pair< mpq_class, mpq_class > carl::root_safe ( const mpq_class & a, uint n)
```

Calculate the nth root of a fraction.

The precise result is contained in the resulting interval.

Round an integer to next integer, that is do nothing.

# **Parameters**

```
n An integer.
```

# Returns

The next integer.

Round a fraction to next integer.

# **Parameters**

```
n A fraction.
```

# **Returns**

The next integer.

```
11.1.4.1057 round() [3/4] mpz_class carl::round ( const mpq_class & n ) [inline]
```

Returns a down-rounded representation of the given numeric.

#### **Parameters**

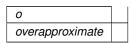
| 0               | Number to round.                               |
|-----------------|--|
| overapproximate | Flag if overapproximation shall be guaranteed. |

# Returns

Double representation of o.

Returns a up-rounded representation of the given numeric.

# **Parameters**



# Returns

double representation of o (overapprox) Note, that it can return the double INFINITY.

Searches for some point in this interval, preferably near the midpoint and with a small representation.

Checks the integers next to the midpoint, uses the midpoint if both are outside.

# Returns

Some point within this interval.

```
11.1.4.1062 sample_above() [1/3] template<typename Number >
Number carl::sample_above (
             const IntRepRealAlgebraicNumber < Number > & n )
11.1.4.1063 sample_above() [2/3] template<typename Number , typename = std::enable_if_t<is_\leftarrow
number_type<Number>::value>>
Number carl::sample_above (
            const Number & n )
11.1.4.1064 sample_above() [3/3] template<typename Number >
RealAlgebraicNumberThom<Number> carl::sample_above (
             const RealAlgebraicNumberThom< Number > & n)
11.1.4.1065 sample_below() [1/3] template<typename Number >
Number carl::sample_below (
             const IntRepRealAlgebraicNumber < Number > & n )
11.1.4.1066 sample_below() [2/3] template<typename Number , typename = std::enable_if_t<is_\leftarrow
number_type<Number>::value>>
Number carl::sample_below (
            const Number & n )
11.1.4.1067 sample_below() [3/3] template<typename Number >
RealAlgebraicNumberThom<Number> carl::sample_below (
             const RealAlgebraicNumberThom< Number > & n)
11.1.4.1068 sample_between() [1/7] template<typename Number >
Number carl::sample_between (
            const IntRepRealAlgebraicNumber < Number > & lower,
             const IntRepRealAlgebraicNumber < Number > & upper )
11.1.4.1069 sample_between() [2/7] template<typename Number >
Number carl::sample_between (
             const IntRepRealAlgebraicNumber< Number > & lower,
             const Number & upper )
```

```
11.1.4.1070 sample_between() [3/7] template<typename Number >
Number carl::sample_between (
            const Number & lower,
            \verb|const IntRepRealAlgebraicNumber< Number> & upper | |
11.1.4.1071 sample_between() [4/7] template<typename Number , typename = std::enable_if_t<is_←
number_type<Number>::value>>
Number carl::sample_between (
            const Number & lower,
            const Number & upper )
11.1.4.1072 sample_between() [5/7] template<typename Number >
Number carl::sample_between (
            const Number & lower,
            const RealAlgebraicNumberThom< Number > & upper )
11.1.4.1073 sample_between() [6/7] template<typename Number >
Number carl::sample_between (
            const RealAlgebraicNumberThom< Number > & lower,
            const Number & upper )
11.1.4.1074 sample_between() [7/7] template<typename Number >
RealAlgebraicNumberThom<Number> carl::sample_between (
            const RealAlgebraicNumberThom< Number > & lower,
             const RealAlgebraicNumberThom< Number > & upper )
11.1.4.1075 sample_infty() template<typename Number >
Number carl::sample_infty (
             const Interval< Number > & i )
```

Searches for some point in this interval, preferably far aways from zero and with a small representation.

Checks the integer next to the right endpoint if the interval is semi-positive. Checks the integer next to the left endpoint if the interval is semi-negative. Uses zero otherwise.

# Returns

Some point within this interval.

Searches for some point in this interval, preferably near the left endpoint and with a small representation.

Checks the integer next to the left endpoint, uses the midpoint if it is outside.

Returns

Some point within this interval.

Searches for some point in this interval, preferably near the right endpoint and with a small representation.

Checks the integer next to the right endpoint, uses the midpoint if it is outside.

Returns

Some point within this interval.

Searches for some point in this interval, preferably near the midpoint and with a small representation.

Uses a binary search based on the Stern-Brocot tree starting from the integer below the midpoint.

Returns

Some point within this interval.

```
11.1.4.1079 sample_zero() template<typename Number > Number carl::sample_zero ( const Interval< Number > & i)
```

Searches for some point in this interval, preferably near zero and with a small representation.

Checks the integer next to the left endpoint if the interval is semi-positive. Checks the integer next to the right endpoint if the interval is semi-negative. Uses zero otherwise.

Returns

Some point within this interval.

Checks whether the given assignment satisfies this constraint.

| _assignment The assignment. |
|-----------------------------|
|-----------------------------|

# Returns

1, if the given assignment satisfies this constraint. 0, if the given assignment contradicts this constraint. 2, otherwise (possibly not defined for all variables in the constraint, even then it could be possible to obtain the first two results.)

```
11.1.4.1081 satisfied_by() [2/3] template<typename Pol >
auto carl::satisfied_by (
             const Constraint < Pol > & c,
             const Assignment< typename Pol::NumberType > & a )
11.1.4.1082 satisfied_by() [3/3] template<typename T , typename Rational , typename Poly >
unsigned carl::satisfied_by (
             const T & t,
             const Model< Rational, Poly > & m )
11.1.4.1083 satisfies() [1/2] template<typename Rational , typename Poly >
unsigned carl::satisfies (
             const Model < Rational, Poly > & _assignment,
             const Formula<br/>< Poly > & \_formula )
Parameters
```

| ₋assignment | The assignment for which to check whether the given formula is satisfied by it. |  |
|-------------|---|--|
| ₋formula    | The formula to be satisfied.  |  |

# Returns

0, if this formula is violated by the given assignment; 1, if this formula is satisfied by the given assignment; 2, otherwise.

```
11.1.4.1084 satisfies() [2/2] template<typename Rational , typename Poly >
unsigned carl::satisfies (
            const Model< Rational, Poly > & _model,
             const std::map< Variable, Rational > & _assignment,
             const std::map< BVVariable, BVTerm > & bvAssigns,
             const Formula < Poly > & \_formula )
```

| ₋model      | The assignment for which to check whether the given formula is satisfied by it. |  |
|-------------|---|--|
| ₋assignment | The map to store the rational assignments in.                                   |  |
| bvAssigns   | The map to store the bitvector assignments in.                                  |  |
| ₋formula    | The formula to be satisfied.  |  |

# Returns

0, if this formula is violated by the given assignment; 1, if this formula is satisfied by the given assignment; 2, otherwise.

Calculates the separable part of this monomial.

```
For a monomial prod_i x_i^{e_i} \text{ with } e_i \neq 0 \text{, this is } \\ prod_i x_i^1.
```

# Returns

Separable part.

Calculates the complement in a set-theoretic manner (can result in two distinct intervals).

# **Parameters**

| interval | Interval. |
|----------|-----------|
| resA     | Result a. |
| resB     | Result b. |

# Returns

True, if the result is twofold.

Calculates the difference of two intervals in a set-theoretic manner: lhs \ rhs (can result in two distinct intervals).

# **Parameters**

| lhs  | First interval.  |
|------|------------------|
| rhs  | Second interval. |
| resA | Result a.        |
| resB | Result b.        |

# Returns

True, if the result is twofold.

Intersects two intervals in a set-theoretic manner.

# Parameters

| lhs | Lefthand side.  |
|-----|-----------------|
| rhs | Righthand side. |

# Returns

Result.

```
11.1.4.1090 set_is_proper_subset() template<typename Number >
bool carl::set_is_proper_subset (
```

```
const Interval< Number > & lhs,
const Interval< Number > & rhs )
```

Checks whether lhs is a proper subset of rhs.

Checks whether lhs is a subset of rhs.

Calculates the symmetric difference of two intervals in a set-theoretic manner (can result in two distinct intervals).

# **Parameters**

| lhs  | First interval.  |
|------|------------------|
| rhs  | Second interval. |
| resA | Result a.        |
| resB | Result b.        |

# Returns

True, if the result is twofold.

Computes the union of two intervals (can result in two distinct intervals).

| lhs  | First interval.  |
|------|------------------|
| rhs  | Second interval. |
| resA | Result a.        |
| resB | Result b.        |

# Returns

True, if the result is twofold.

Obtain the sign of the given number.

This method relies on the comparison operators for the type of the given number.

# Parameters

```
n Number
```

# Returns

Sign of n

Counts the sign variations (i.e.

an upper bound for the number of real roots) via Descarte's rule of signs. This is an upper bound for countReal ← Roots().

| polynomial | A polynomial.                     |
|------------|-----------------------------------|
| interval   | Count roots within this interval. |

# Returns

Upper bound for number of real roots within the interval.

Counts the number of sign variations in the given object range.

The function accepts an range of Sign objects.

# **Parameters**

| begin | Start of object range. |
|-------|------------------------|
| end   | End of object range.   |

# Returns

Sign variations of objects.

Counts the number of sign variations in the given object range.

The function accepts an object range and an additional function f. If the objects are not of type Sign, the function f can be used to convert the objects to a Sign on the fly. As for the number of sign variations in the evaluations of polynomials p at a position x, this might look like this:  $signVariations(p.begin(), p.end(), [\&x] (const Polynomial\& p) { return <math>sgn(p.evaluate(x)); });$ 

# Parameters

| begin | Start of object range.                      |
|-------|---|
| end   | End of object range.                        |
| f     | Function object to convert objects to Sign. |

# Returns

Sign variations of objects.

```
11.1.4.1100 signAtMinusInf() template<typename Number >
Sign carl::signAtMinusInf (
             const UnivariatePolynomial< Number > & p )
11.1.4.1101 signAtPlusInf() template<typename Number >
Sign carl::signAtPlusInf (
             const UnivariatePolynomial< Number > & p )
11.1.4.1102 signed_pseudo_remainder() template<typename Coeff >
UnivariatePolynomial < Coeff > carl::signed_pseudo_remainder (
             const UnivariatePolynomial< Coeff > & dividend,
             const UnivariatePolynomial< Coeff > & divisor )
Compute the signed pseudo-remainder.
11.1.4.1103 sin() [1/5] cln::cl_RA carl::sin (
             const cln::cl_RA & n ) [inline]
11.1.4.1104 sin() [2/5] template<typename FloatType >
FLOAT_T<FloatType> carl::sin (
             const FLOAT_T< FloatType > & _in ) [inline]
11.1.4.1105 \sin() [3/5] template<typename Number , EnableIf< std::is_floating_point< Number >>
= dummy>
Interval<Number> carl::sin (
            const Interval< Number > & i )
11.1.4.1106 sin() [4/5] mpq_class carl::sin (
             const mpq_class & n ) [inline]
11.1.4.1107 sin() [5/5] double carl::sin (
             double in ) [inline]
```

```
11.1.4.1108 sin_assign() template<typename Number , EnableIf< std::is_floating_point< Number
>> = dummy>
void carl::sin_assign (
             Interval< Number > & i )
11.1.4.1109 sinh() template<typename Number , EnableIf< std::is_floating_point< Number >> =
dummv>
Interval<Number> carl::sinh (
             const Interval< Number > & i )
11.1.4.1110 sinh_assign() template<typename Number , EnableIf< std::is_floating_point< Number
>> = dummy>
void carl::sinh_assign (
             Interval< Number > & i )
11.1.4.1111 solveDiophantine() template<typename T >
std::vector<T> carl::solveDiophantine (
             MultivariatePolynomial < T > & p )
Diophantine Equations solver.
11.1.4.1112 sos_decomposition() template<typename C , typename O , typename P >
\verb|std::vector| < \verb|std::pair| < C, \verb|MultivariatePolynomial| < C, O, \verb|P>| > carl::sos_decomposition (|state | C, O, P|) < 0.
             const MultivariatePolynomial < C, O, P > & p,
             bool not_trivial = false )
11.1.4.1113 SPolynomial() template<typename C , typename O , typename P >
MultivariatePolynomial <C,O,P > carl::SPolynomial (
             const MultivariatePolynomial< C, O, P > & p,
             const MultivariatePolynomial< C, O, P > & q )
Calculates the S-Polynomial of two polynomials.
11.1.4.1114 sqrt() [1/5] cln::cl_RA carl::sqrt (
             const cln::cl_RA & a )
11.1.4.1115 sqrt() [2/5] template<typename FloatType >
FLOAT_T<FloatType> carl::sqrt (
             \verb|const FLOAT_T| < \verb|FloatType| > \& \_in | ) [inline]
```

Method which returns the square root of the passed number.

| $\leftarrow$ | Number. |
|--------------|---------|
| _←           |         |
| in           |         |

# Returns

Number which holds the result.

Calculate the square root of a fraction if possible.

cln::cl\_RA & b )

| а | The fraction to calculate the square root for.              |  |
|---|---|--|
| b | A reference to the rational, in which the result is stored. |  |

### Returns

true, if the number to calculate the square root for is a square; false, otherwise.

Calculate the square root of a fraction if possible.

### **Parameters**

| а | The fraction to calculate the square root for.              |
|---|---|
| b | A reference to the rational, in which the result is stored. |

## Returns

true, if the number to calculate the square root for is a square; false, otherwise.

Compute square root in a fast but less precise way.

Use cln::sqrt() to obtain an approximation. If the result is rational, i.e. the result is exact, use this result. Otherwise use the nearest integers as bounds on the square root.

### **Parameters**

```
a Some number.
```

## Returns

[x,x] if sqrt(a) = x is rational, otherwise [y,z] for y,z integer and y < sqrt(a) < z.

Compute square root in a fast but less precise way.

Use cln::sqrt() to obtain an approximation. If the result is rational, i.e. the result is exact, use this result. Otherwise use the nearest integers as bounds on the square root.

#### **Parameters**

```
a Some number.
```

## Returns

[x,x] if sqrt(a) = x is rational, otherwise [y,z] for y,z integer and y < sqrt(a) < z.

Calculate the square root of a fraction.

If we are able to find a an x such that x is the exact root of a, (x,x) is returned. If we can not find such a number (note that such a number might not even exist), (x,y) is returned with  $x<\sqrt{a}< y$ . Note that we try to find bounds that are very close to the actual square root. If a small representation is more important than a small interval, sqrt\_fast should be used.

### **Parameters**

```
a A fraction.
```

## Returns

Interval containing the square root of a.

const UnivariatePolynomial< Coeff > & p )

Allows to easily output some container with all elements separated by some string.

```
Usage: os << stream_joined(" ", container).</pre>
```

### **Parameters**

| glue | The intermediate string.     |
|------|------------------------------|
| V    | The container to be printed. |

### Returns

A temporary object that implements operator<< ().

```
11.1.4.1133 stream_joined() [2/2] template<typename T , typename F > auto carl::stream_joined ( const std::string & glue, const T & v, F && f ) [inline]
```

Allows to easily output some container with all elements separated by some string.

An additional callable f takes care of writing an individual element to the stream. Usage: os << stream\_ $\leftarrow$  joined(" ", container).

### **Parameters**

| glue | The intermediate string.                        |  |
|------|---|--|
| V    | The container to be printed.                    |  |
| f    | A callable taking a stream and an element of v. |  |

### Returns

A temporary object that implements operator<< ().

```
11.1.4.1134 sturm_sequence() [1/2] template<typename Coeff > std::vector<UnivariatePolynomial<Coeff> > carl::sturm_sequence ( const UnivariatePolynomial< Coeff > & p )
```

Computes the sturm sequence of a polynomial as defined at ?, page 333, example 22.

The sturm sequence of p is defined as:

```
• p_0 = p
```

•  $p_1 = p'$ 

•  $p_k = -rem(p_{k-2}, p_{k-1})$ 

```
11.1.4.1135 sturm_sequence() [2/2] template<typename Coeff > std::vector<UnivariatePolynomial<Coeff> > carl::sturm_sequence ( const UnivariatePolynomial< Coeff > & p, const UnivariatePolynomial< Coeff > & q)
```

Computes the sturm sequence of two polynomials.

Compared to the regular sturm sequence, we use the second polynomial as p\_1.

Implements a subresultants algorithm with optimizations described in ? .

### **Parameters**

| pol1     | First polynomial. |
|----------|-------------------|
| pol2     | First polynomial. |
| strategy | Strategy.         |

#### Returns

Subresultants of pol1 and pol2.

Case distinction on delta: either we choose b as next subresultant or we could reduce b (delta > 1) and add the reduced version c as next subresultant. The reduction is done by division, which depends on the internal variable order of GiNaC and might fail although for some order it would succeed. In this case, we just do not reduce b. (A relaxed reduction could also be applied.)

After the if-else block, bDeg is the degree of the front-most element of subresultants, be it c or b.

Replace all variables by a value given in their map.

### Returns

A new factorized polynomial without the variables in map.

Replace all variables by a value given in their map.

## Returns

A new factorized polynomial without the variables in map.

Replace all variables by a value given in their map.

### Returns

A new factorized polynomial without the variables in map.

Replace the given variable by the given value.

Returns

A new factorized polynomial resulting from this substitution.

```
11.1.4.1141 substitute() [5/20] template<typename Pol , typename Source , typename Target >
Formula<Pol> carl::substitute (
            const Formula< Pol > & formula,
            const Source & source,
            const Target & target )
11.1.4.1142 substitute() [6/20] template<typename Pol >
Formula<Pol> carl::substitute (
             const Formula< Pol > & formula,
             const std::map< BVVariable, BVTerm > & replacements )
11.1.4.1143 substitute() [7/20] template<typename Pol >
Formula<Pol> carl::substitute (
             const Formula< Pol > & formula,
             const std::map< Formula< Pol >, Formula< Pol >> & replacements )
11.1.4.1144 substitute() [8/20] template<typename Pol >
Formula<Pol> carl::substitute (
            const Formula< Pol > & formula,
            const std::map< UVariable, UFInstance > & replacements )
11.1.4.1145 substitute() [9/20] template<typename Pol >
Formula<Pol> carl::substitute (
            const Formula< Pol > & formula,
            const std::map< Variable, typename Formula< Pol >::PolynomialType > & replacements
11.1.4.1146 substitute() [10/20] template<typename Coeff >
Coeff carl::substitute (
             const Monomial & m,
             const std::map< Variable, Coeff > & substitutions )
```

Applies the given substitutions to a monomial.

Every variable may be substituted by some value.

### **Parameters**

| m             | The monomial.              |
|---------------|----------------------------|
| substitutions | Maps variables to numbers. |

### Returns

```
this[< substitutions>]
```

```
11.1.4.1147 substitute() [11/20] template<typename C , typename O , typename P >
MultivariatePolynomial<C,O,P> carl::substitute (
             const MultivariatePolynomial< C, O, P > & p,
             const std::map< Variable, MultivariatePolynomial< C, O, P >> & substitutions)
11.1.4.1148 substitute() [12/20] template<typename C , typename O , typename P , typename S >
MultivariatePolynomial<C,O,P> carl::substitute (
             const MultivariatePolynomial < C, O, P > & p,
             const std::map< Variable, S > & substitutions )
11.1.4.1149 substitute() [13/20] template<typename C , typename O , typename P >
MultivariatePolynomial<C,O,P> carl::substitute (
            const MultivariatePolynomial < C, O, P > & p,
             const std::map< Variable, Term< C >> & substitutions)
11.1.4.1150 substitute() [14/20] template<typename C , typename O , typename P >
MultivariatePolynomial<C,O,P> carl::substitute (
            const MultivariatePolynomial < C, O, P > & p,
            Variable var,
             const MultivariatePolynomial< C, O, P > & value )
11.1.4.1151 substitute() [15/20] template<typename Poly >
SqrtEx<Poly> carl::substitute (
            const Poly & _substituteIn,
             const carl::Variable _varToSubstitute,
             const SqrtEx< Poly > & _substituteBy )
```

Substitutes a variable in an expression by a square root expression, which results in a square root expression.

### **Parameters**

| ₋substituteIn    | The polynomial to substitute in.                                   |
|------------------|--|
| ₋varToSubstitute | The variable to substitute.  |
| ₋substituteBy    | The square root expression by which the variable gets substituted. |

### Returns

The resulting square root expression.

Substitutes a model into an expression t.

The result is always an expression of the same type. This may not be possible for some expressions, for example for uninterpreted equalities.

Substitutes all variables from a model within a bitvector constraint.

Substitutes all variables from a model within a bitvector term.

Substitutes all variables from a model within a constraint.

May fail to substitute some variables, for example if the values are RANs or SqrtEx.

```
11.1.4.1160 substitute_inplace() [4/11] template<typename Rational , typename Poly > void carl::substitute_inplace ( Formula < Poly > \& f, \\ const \ Model < Rational, Poly > \& m )
```

Substitutes all variables from a model within a formula.

May fail to substitute some variables, for example if the values are RANs or SqrtEx.

Substitutes a variable with a rational within a polynomial.

Create a copy of the underlying polynomial with the given variable replaced by the given polynomial.

Substitutes all variables from a model within a MultivariateRoot.

May fail to substitute some variables, for example if the values are RANs or SqrtEx.

```
11.1.4.1165 substitute_inplace() [9/11] template<typename Rational , typename Poly , typename ModelPoly > void carl::substitute_inplace (  Poly \ \& \ p, \\ const \ Model< \ Rational, \ ModelPoly > \& \ m \ )
```

Substitutes all variables from a model within a polynomial.

bool \_inConjunction )

May fail to substitute some variables, for example if the values are RANs or SqrtEx.

```
11.1.4.1166 substitute_inplace() [10/11] template<typename Coeff >
void carl::substitute_inplace (
            UnivariatePolynomial < Coeff > & p,
            Variable var,
             const Coeff & value )
11.1.4.1167 substitute_inplace() [11/11] template<typename Poly , typename Rational >
void carl::substitute_inplace (
            UnivariatePolynomial < Poly > & p,
             Variable var,
             const Rational & r )
11.1.4.1168 swap() void carl::swap (
             Variable & lhs,
             Variable & rhs ) [inline]
11.1.4.1169 swapConstraintBounds() template<typename Pol >
bool carl::swapConstraintBounds (
             ConstraintBounds < Pol > & _constraintBounds,
             Formulas< Pol > & _intoFormulas,
```

Stores for every polynomial for which we determined bounds for given constraints a minimal set of constraints representing these bounds into the given set of sub-formulas of a conjunction (\_inConjunction == true) or disjunction (\_inConjunction == false) to construct.

### **Parameters**

| _constraintBounds | An object collecting bounds of polynomials.  |
|-------------------|--|
| ₋intoAsts         | A set of sub-formulas of a conjunction (_inConjunction == true) or disjunction (_inConjunction == false) to construct.   |
| ₋inConjunction    | true, if constraints representing the polynomial's bounds are going to be part of a conjunction. false, if constraints representing the polynomial's bounds are going to be part of a disjunction. |

## Returns

true, if the yet added bounds imply that the conjunction (\_inConjunction == true) or disjunction (\_inConjunction == false) to which the bounds are added is invalid resp. valid; false, otherwise.

Switches the main variable using a purely syntactical restructuring.

The resulting polynomial will be algebraicly identical, but have the given variable as its main variable.

### **Parameters**

| p      | The polynomial.    |
|--------|--------------------|
| newVar | New main variable. |

## Returns

Restructured polynomial.

```
11.1.4.1173 tan_assign() template<typename Number , EnableIf< std::is_floating_point< Number
>> = dummy>
void carl::tan_assign (
            Interval< Number > & i )
11.1.4.1174 tanh() template<typename Number , EnableIf< std::is_floating_point< Number >> =
dummy>
Interval<Number> carl::tanh (
            const Interval< Number > & i )
11.1.4.1175 tanh_assign() template<typename Number , EnableIf< std::is_floating_point< Number
>> = dummy>
void carl::tanh_assign (
            Interval< Number > & i )
11.1.4.1176 to_cnf() template<typename Poly >
Formula<Poly> carl::to_cnf (
            const Formula < Poly > & f,
            bool keep_constraints = true,
            bool simplify_combinations = false,
            bool tseitin_equivalence = true )
```

# Converts the given formula to CNF.

## **Parameters**

| f   | Formula to convert.  |
|---|--|
| keep_constraints  | Indicates whether to keep constraints or allow to change them in resolve_negation(). |
| simplify_combinations Indicates whether we attempt to simplify combinations of constraints with |  |
|   | ConstraintBounds.  |
| tseitin_equivalence   | Indicates whether we use implications or equivalences for tseitin variables.         |

## Returns

The formula in CNF.

Converts the given integer to a double.

| Da |    |   |    |   |    |
|----|----|---|----|---|----|
| ra | ra | m | eı | œ | rs |

```
n An integer.
```

Returns

Double.

```
11.1.4.1178 to_double() [2/7] double carl::to_double ( const cln::cl_RA & n ) [inline]
```

Converts the given fraction to a double.

# **Parameters**

```
n A fraction.
```

Returns

Double.

Conversion functions.

The following function convert types to other types.

```
11.1.4.1182 to_double() [6/7] double carl::to_double ( double n ) [inline]
```

```
11.1.4.1183 to_double() [7/7] double carl::to_double ( sint n ) [inline]
```

Conversion functions.

The following function convert types to other types.

```
11.1.4.1184 to_int() [1/8] template<typename Integer > Integer carl::to_int ( const cln::cl_I & n ) [inline]
```

```
11.1.4.1185 to_int() [2/8] template<typename Integer > Integer carl::to_int ( const cln::cl_RA & n ) [inline]
```

Casts the FLOAT\_T to an arbitrary integer type which has a constructor for a native int.

## **Parameters**

₋float

# Returns

Integer type which holds floor(\_float).

Casts the Interval to an arbitrary integer type which has a constructor for a native int.

## **Parameters**

₋floatInterval

## Returns

Integer type which holds floor(\_float).

Convert a fraction to an integer.

This method assert, that the given fraction is an integer, i.e. that the denominator is one.

## **Parameters**

```
n A fraction.
```

# Returns

An integer.

Convert a fraction to an integer.

This method assert, that the given fraction is an integer, i.e. that the denominator is one.

```
Parameters
```

```
n A fraction.
```

Returns

An integer.

```
11.1.4.1194 to_int< sint > () [1/5] template<> sint carl::to_int < sint > ( const cln::cl_I & n ) [inline]
```

```
11.1.4.1195 to_int< sint >() [2/5] template<> sint carl::to_int< sint > ( const cln::cl_RA & n ) [inline]
```

```
11.1.4.1196 to int < sint >() [3/5] template <> sint carl::to-int < sint > (

const mpq_class & n) [inline]
```

Convert a fraction to an unsigned.

## **Parameters**

```
n A fraction.
```

Returns

n as unsigned.

```
11.1.4.1197 to_int< sint > () [4/5] template<> sint carl::to_int < sint > ( const mpz_class & n ) [inline]
```

```
11.1.4.1199 to_int< uint >() [1/5] template<>
uint carl::to_int< uint > (
           const cln::cl_I & n ) [inline]
11.1.4.1200 to_int< uint >() [2/5] template<>
uint carl::to_int< uint > (
            const cln::cl_RA & n ) [inline]
11.1.4.1201 to_int< uint >() [3/5] template<>
uint carl::to_int< uint > (
            const mpq_class & n ) [inline]
11.1.4.1202 to_int< uint >() [4/5] template<>
uint carl::to_int< uint > (
            const mpz_class & n ) [inline]
11.1.4.1203 to_int< uint >() [5/5] template<>
uint carl::to_int< uint > (
            double n ) [inline]
11.1.4.1204 to_lf() cln::cl_LF carl::to_lf (
             const cln::cl_RA & n ) [inline]
Convert a cln fraction to a cln long float.
Parameters
 n A fraction.
Returns
    n as cln::cl_LF.
11.1.4.1205 to_nnf() template<typename Poly >
Formula<Poly> carl::to_nnf (
```

const Formula< Poly > & formula )

```
11.1.4.1206 to_univariate_polynomial() [1/2] template<typename C , typename O , typename P > UnivariatePolynomial<C> carl::to_univariate_polynomial ( const MultivariatePolynomial< C, O, P > & p)
```

Convert a univariate polynomial that is currently (mis)represented by a 'MultivariatePolynomial' into a more appropiate 'UnivariatePolynomial' representation.

Note that the current polynomial must mention one and only one variable, i.e., be indeed univariate.

Convert a multivariate polynomial that is currently represented by a MultivariatePolynomial into a UnivariatePolynomial representation.

The main variable of the resulting polynomial is given as second argument.

Transforms this formula to its quantifier free equivalent.

bool negated = false )

The quantifiers are represented by the parameter variables. Each entry in variables contains all variables between two quantifier alternations. The even entries (starting with 0) are quantified existentially, the odd entries are quantified universally.

## **Parameters**

| variables | Contains the quantified variables. |
|-----------|------------------------------------|
| level     | Used for internal recursion.       |
| negated   | Used for internal recursion.       |

## Returns

The quantifier-free version of this formula.

```
11.1.4.1210 toString() [1/8] std::string carl::toString (

BVCompareRelation -r ) [inline]
```

```
11.1.4.1211 toString() [2/8] std::string carl::toString (
              const cln::cl_I & _number,
              bool \_infix = true)
11.1.4.1212 toString() [3/8] std::string carl::toString (
              const cln::cl_RA & _number,
              bool _infix = true )
11.1.4.1213 toString() [4/8] template<typename IntegerType >
std::string carl::toString (
             const GFNumber< IntegerType > & _number,
             bool )
Creates the string representation to the given galois field number.
Parameters
 ₋number
            The galois field number to get its string representation for.
Returns
     The string representation to the given galois field number.
11.1.4.1214 toString() [5/8] std::string carl::toString (
              const mpq_class & _number,
             bool _infix = true )
11.1.4.1215 toString() [6/8] std::string carl::toString (
             const mpz_class & _number,
```

std::enable\_if<std::is\_arithmetic<typename remove\_all<T>::type>::value, std::string>::type

bool \_infix = true )

11.1.4.1216 toString() [7/8] template<typename T >

const T & n,
bool ) [inline]

carl::toString (

```
11.1.4.1217 toString() [8/8] std::string carl::toString (

Relation r) [inline]
```

Gives the total degree, i.e.

the sum of all exponents.

**Returns** 

Total degree.

Calculates the max.

degree over all monomials occurring in the polynomial. As the degree of the zero polynomial is  $-\infty$ , we assert that this polynomial is not zero. This must be checked by the caller before calling this method.

See also

?, page 48

Returns

Total degree.

```
11.1.4.1220 total_degree() [3/4] template<typename Coeff > std::size_t carl::total_degree ( const Term< Coeff > & t )
```

Gives the total degree, i.e.

the sum of all exponents.

Returns

Total degree.

Returns the total degree of the polynomial, that is the maximum degree of any monomial.

As the degree of the zero polynomial is  $-\infty$ , we assert that this polynomial is not zero. This must be checked by the caller before calling this method.

See also

?, page 38

Returns

Total degree.

Divides the polynomial by another polynomial.

If the divisor divides this polynomial, quotient contains the result of the division and true is returned. Otherwise, false is returned and the content of quotient remains unchanged. Applies if the coefficients are from a field. Note that the quotient must not be \*this.

## **Parameters**



Returns

```
11.1.4.1224 try_divide() [3/4] template<typename Coeff >
bool carl::try_divide (
            const Term< Coeff > & t,
             Variable v,
             Term< Coeff > & res )
11.1.4.1225 try_divide() [4/4] template<typename Coeff >
bool carl::try_divide (
            const UnivariatePolynomial< Coeff > & dividend,
            const Coeff & divisor,
            UnivariatePolynomial < Coeff > & quotient )
11.1.4.1226 try_parse() template<typename T >
bool carl::try_parse (
           const std::string & n,
            T & res ) [inline]
11.1.4.1227 try_parse < cln::cl_l >() template <>
bool carl::try_parse< cln::cl_I > (
            const std::string & n,
            cln::cl_I & res )
11.1.4.1228 try_parse < cln::cl_RA >() template <>
bool carl::try_parse< cln::cl_RA > (
           const std::string & n,
            cln::cl_RA & res )
11.1.4.1229 try_parse< mpq_class >() template<>
bool carl::try_parse< mpq_class > (
            const std::string & n,
            mpq_class & res )
11.1.4.1230 try_parse< mpz_class >() template<>
bool carl::try_parse< mpz_class > (
            const std::string & n,
            mpz_class & res )
```

Implements a functional fold (similar to std::accumulate) for std::tuple.

Combines all tuple elements using a combinator function f and an initial value init.

```
11.1.4.1232 tuple_apply() template<typename F , typename Tuple > auto carl::tuple_apply (  F \ \&\& \ f,  Tuple && t )
```

Invokes a callable object f on a tuple of arguments.

This is basically std::apply (available with C++17).

Invokes a callable object f on every element of a tuple and returns a tuple containing the results.

This basically corresponds to the functional map (func, list).

Returns a new tuple containing everything but the first element.

```
11.1.4.1236 turn\_around() Relation carl::turn\_around (
Relation r) [inline]
```

Turns around the given relation symbol, in the sense that LESS (LEQ) and GREATER (GEQ) are swapped.

```
11.1.4.1237 typeld() auto carl::typeId (
             BVTermType type ) [inline]
11.1.4.1238 typelsBinary() bool carl::typeIsBinary (
             BVTermType type ) [inline]
11.1.4.1239 typelsUnary() bool carl::typeIsUnary (
             BVTermType type ) [inline]
11.1.4.1240 typeString() template<typename T >
std::string carl::typeString ( )
11.1.4.1241 underlying_enum_value() template<typename Enum >
constexpr auto carl::underlying_enum_value (
             Enum e ) [constexpr]
Casts an enum value to a value of the underlying number type.
11.1.4.1242 uninterpreted_functions() template<typename Pol >
void carl::uninterpreted_functions (
            const Formula < Pol > & f,
             std::set < UninterpretedFunction > & ufs)
11.1.4.1243 uninterpreted_variables() [1/2] template<typename Pol >
void carl::uninterpreted_variables (
            const Formula < Pol > & f,
            std::set< UVariable > & uvs )
11.1.4.1244 uninterpreted_variables() [2/2] template<typename T >
carlVariables carl::uninterpreted_variables (
            const T & t ) [inline]
```

```
11.1.4.1245 univariateTarskiQuery() [1/2] template<typename Number >
int carl::univariateTarskiQuery (
            const UnivariatePolynomial< Number > \& p,
             const UnivariatePolynomial< Number > \& q)
11.1.4.1246 univariateTarskiQuery() [2/2] template<typename Number >
int carl::univariateTarskiQuery (
            const UnivariatePolynomial< Number > & p,
             const UnivariatePolynomial< Number > & q,
             const UnivariatePolynomial< Number > & der_q )
11.1.4.1247 var_info() template<typename Coeff , typename Ordering , typename Policies >
VarInfo<MultivariatePolynomial<Coeff,Ordering,Policies> > carl::var.info (
             const MultivariatePolynomial< Coeff, Ordering, Policies > & poly,
             const Variable var,
             bool collect_coeff = false ) [inline]
11.1.4.1248 variables() [1/13] template<typename Pol >
void carl::variables (
             const BasicConstraint < Pol > & c,
             carlVariables & vars )
11.1.4.1249 variables() [2/13] template<typename Pol >
void carl::variables (
             const Constraint < Pol > & c,
             carlVariables & vars )
11.1.4.1250 variables() [3/13] template<typename Coeff , typename Ordering , typename Policies
>
void carl::variables (
             const ContextPolynomial< Coeff, Ordering, Policies > & p,
             carlVariables & vars ) [inline]
11.1.4.1251 variables() [4/13] template<typename Pol >
void carl::variables (
            const Formula < Pol > & f,
             carlVariables & vars )
```

Add the variables of the given monomial to the variables.

Add the variables of the given polynomial to the variables.

Add the variables mentioned in underlying polynomial, excluding the root-variable "\_z".

For example, with an underlying poly p(x,y,z) we return  $\{x,y\}$ .

```
11.1.4.1256 variables() [9/13] template<typename T > carlVariables carl::variables ( const T & t ) [inline]
```

Return the variables as collected by the methods above.

```
11.1.4.1257 variables() [10/13] template<typename Coeff > void carl::variables ( const Term< Coeff > & t, carlVariables & vars)
```

Add the variables of the given term to the variables.

```
11.1.4.1258 variables() [11/13] template<typename Coeff >
void carl::variables (
             const UnivariatePolynomial< Coeff > & p,
             carlVariables & vars )
Add the variables of the given polynomial to the variables.
11.1.4.1259 variables() [12/13] template<typename Pol >
void carl::variables (
             const VariableAssignment< Pol > & f,
             carlVariables & vars ) [inline]
11.1.4.1260 variables() [13/13] template<typename Pol >
void carl::variables (
             const VariableComparison< Pol > & f,
             carlVariables & vars ) [inline]
11.1.4.1261 variant_extend() template<typename Target , typename... Args>
Target carl::variant_extend (
             const boost::variant< Args... > & variant )
11.1.4.1262 variant_hash() template<typename... T>
std::size_t carl::variant_hash (
             const boost::variant< T... > & value ) [inline]
11.1.4.1263 variant_is_type() template<typename T , typename Variant >
bool carl::variant_is_type (
             const Variant & variant ) [noexcept]
Checks whether a variant contains a value of a fiven type.
\textbf{11.1.4.1264} \quad \textbf{vars\_info()} \quad \texttt{template} < \texttt{typename Coeff , typename Ordering , typename Policies} >
VarsInfo<MultivariatePolynomial<Coeff,Ordering,Policies> > carl::vars.info (
             const MultivariatePolynomial< Coeff, Ordering, Policies > & poly,
             bool collect_coeff = false ) [inline]
11.1.4.1265 visit() template<typename Pol , typename Visitor >
void carl::visit (
             const Formula< Pol > & formula,
             Visitor func )
```

Recursively calls func on every subformula.

## **Parameters**

| formula | Formula to visit. |
|---------|-------------------|
| func    | Function to call. |

Recursively calls func on every subformula and return a new formula.

On every call of func, the passed formula is replaced by the result.

## **Parameters**

| formula | Formula to visit. |
|---------|-------------------|
| func    | Function to call. |

## Returns

New formula.

# 11.1.5 Variable Documentation

```
11.1.5.1 A_AND_B_IFF_C const signed carl::A_AND_B_IFF_C = -3
```

```
11.1.5.2 A_IFF_B const signed carl::A_IFF_B = 2
```

11.1.5.3 A\_IMPLIES\_B const signed carl::A\_IMPLIES\_B = 1

```
11.1.5.4 A_XOR_B const signed carl::A_XOR_B = -4
```

```
11.1.5.5 B_IMPLIES_A const signed carl::B_IMPLIES_A = -1
11.1.5.6 CONDITION_SIZE constexpr std::size_t carl::CONDITION_SIZE = 64 [static], [constexpr]
11.1.5.7 dependent_false_v template<class >
constexpr bool carl::dependent_false_v = false [inline], [constexpr]
11.1.5.8 dummy const dtl::enabled carl::dummy = {}
11.1.5.9 initvariable int carl::initvariable = initialize() [static]
 Call to initialize.
11.1.5.10 last_assertion_code int carl::last_assertion_code = 23
Stores an integer representation of the last assertion that was registered via REGISTER_ASSERT.
11.1.5.11 last_assertion_string std::string carl::last_assertion_string
Stores a textual representation of the last assertion that was registered via REGISTER_ASSERT.
\textbf{11.1.5.12} \quad \textbf{mMap} \quad \texttt{std::map} < \texttt{Variable::NO\_VARIABLE} \ , \\ \textbf{11.1.5.12} \quad \textbf{mMap} \quad \texttt{std::map} < \texttt{Variable::NO\_VARIABLE} \ , \\ \textbf{11.1.5.12} \quad \textbf{mMap} \quad \texttt{std::map} < \texttt{Variable::NO\_VARIABLE} \ , \\ \textbf{11.1.5.12} \quad \textbf{mMap} \quad \texttt{std::map} < \texttt{Variable::NO\_VARIABLE} \ , \\ \textbf{11.1.5.12} \quad \textbf{mMap} \quad \texttt{std::map} < \texttt{Variable::NO\_VARIABLE} \ , \\ \textbf{11.1.5.12} \quad \textbf{mMap} \quad \texttt{std::map} < \texttt{Variable::nap} < \texttt{
 Interval < double > (0) }} [static]
11.1.5.13 NOT_A_AND_B const signed carl::NOT_A_AND_B = -2
11.1.5.14 ONE_DIVIDED_BY_10_TO_THE_POWER_OF_23 const cln::cl_RA carl::ONE_DIVIDED_BY_10_TO_←
```

 $\label{eq:the_power_of_23} \texttt{THE\_POWER\_OF\_23} = \texttt{cln::cl\_RA(1)/cln::expt(cln::cl\_RA(10), 23)} \quad [\texttt{static}]$ 

11.1.5.15 ONE\_DIVIDED\_BY\_10\_TO\_THE\_POWER\_OF\_52 const cln::cl\_RA carl::ONE\_DIVIDED\_BY\_10\_TO\_ $\leftarrow$  THE\_POWER\_OF\_52 = cln::cl\_RA(1)/cln::expt(cln::cl\_RA(10), 52) [static]

11.1.5.16 PROP\_CONTAINS\_BITVECTOR constexpr Condition carl::PROP\_CONTAINS\_BITVECTOR = Condition(
26) [static], [constexpr]

11.1.5.17 PROP\_CONTAINS\_BOOLEAN constexpr Condition carl::PROP\_CONTAINS\_BOOLEAN = Condition(
22 ) [static], [constexpr]

11.1.5.18 PROP\_CONTAINS\_EQUATION constexpr Condition carl::PROP\_CONTAINS\_EQUATION = Condition(
16 ) [static], [constexpr]

11.1.5.19 PROP\_CONTAINS\_INEQUALITY constexpr Condition carl::PROP\_CONTAINS\_INEQUALITY = Condition( 17 ) [static], [constexpr]

**11.1.5.20 PROP\_CONTAINS\_INTEGER\_VALUED\_VARS** constexpr Condition carl::PROP\_CONTAINS\_← INTEGER\_VALUED\_VARS = Condition(23) [static], [constexpr]

11.1.5.21 PROP\_CONTAINS\_LINEAR\_POLYNOMIAL constexpr Condition carl::PROP\_CONTAINS\_LINEAR ← POLYNOMIAL = Condition(19) [static], [constexpr]

11.1.5.22 PROP\_CONTAINS\_MULTIVARIATE\_POLYNOMIAL constexpr Condition carl::PROP\_CONTAINS ← \_\_MULTIVARIATE\_POLYNOMIAL = Condition(21) [static], [constexpr]

11.1.5.23 PROP\_CONTAINS\_NONLINEAR\_POLYNOMIAL constexpr Condition carl::PROP\_CONTAINS\_← NONLINEAR\_POLYNOMIAL = Condition( 20 ) [static], [constexpr]

11.1.5.24 PROP\_CONTAINS\_PSEUDOBOOLEAN constexpr Condition carl::PROP\_CONTAINS\_PSEUDOBOOLEAN = Condition( 27 ) [static], [constexpr]

```
11.1.5.25 PROP_CONTAINS_REAL_VALUED_VARS constexpr Condition carl::PROP_CONTAINS_REAL_←
VALUED_VARS = Condition( 24 ) [static], [constexpr]
11.1.5.26 PROP_CONTAINS_STRICT_INEQUALITY constexpr Condition carl::PROP_CONTAINS_STRICT_←
INEQUALITY = Condition( 18 ) [static], [constexpr]
11.1.5.27 PROP_CONTAINS_UNINTERPRETED_EQUATIONS constexpr Condition carl::PROP_CONTAINS←
_UNINTERPRETED_EQUATIONS = Condition(25) [static], [constexpr]
11.1.5.28 PROP_CONTAINS_WEAK_INEQUALITY constexpr Condition carl::PROP_CONTAINS_WEAK_←
INEQUALITY = Condition( 31 ) [static], [constexpr]
11.1.5.29 PROP_IS_A_CLAUSE constexpr Condition carl::PROP_IS_A_CLAUSE = Condition(3) [static],
[constexpr]
11.1.5.30 PROP_IS_A_LITERAL constexpr Condition carl::PROP_IS_A_LITERAL = Condition( 4 ) [static],
[constexpr]
11.1.5.31 PROP_IS_AN_ATOM constexpr Condition carl::PROP_IS_AN_ATOM = Condition(5) [static],
[constexpr]
11.1.5.32 PROP_IS_IN_CNF constexpr Condition carl::PROP_IS_IN_CNF = Condition( 1 ) [static],
[constexpr]
11.1.5.33 PROP_IS_IN_NNF constexpr Condition carl::PROP_IS_IN_NNF = Condition( 0 ) [static],
[constexpr]
11.1.5.34 PROP_IS_LITERAL_CONJUNCTION constexpr Condition carl::PROP_IS_LITERAL_CONJUNCTION
= Condition(6) [static], [constexpr]
```

```
11.1.5.35 PROP_IS_PURE_CONJUNCTION constexpr Condition carl::PROP_IS_PURE_CONJUNCTION =
Condition( 2 ) [static], [constexpr]
11.1.5.36 PROP_TRUE constexpr Condition carl::PROP_TRUE = Condition() [static], [constexpr]
11.1.5.37 PROP_VARIABLE_DEGREE_GREATER_THAN_FOUR constexpr Condition carl::PROP_↔
VARIABLE_DEGREE_GREATER_THAN_FOUR = Condition( 30 ) [static], [constexpr]
11.1.5.38 PROP_VARIABLE_DEGREE_GREATER_THAN_THREE constexpr Condition carl::PROP_←
VARIABLE_DEGREE_GREATER_THAN_THREE = Condition( 29 ) [static], [constexpr]
11.1.5.39 PROP_VARIABLE_DEGREE_GREATER_THAN_TWO constexpr Condition carl::PROP_VARIABLE ←
_DEGREE_GREATER_THAN_TWO = Condition( 28 ) [static], [constexpr]
11.1.5.40 signal_installed bool carl::signal_installed = install_signal_handler() [static]
Static variable that ensures that install_signal_handler is called.
11.1.5.41 sizeOfUnsigned constexpr unsigned carl::sizeOfUnsigned = sizeof(unsigned) [constexpr]
11.1.5.42 STRONG_CONDITIONS const Condition carl::STRONG_CONDITIONS [static]
Initial value:
= PROP_IS_IN_NNF | PROP_IS_IN_CNF | PROP_IS_PURE_CONJUNCTION |
                                                             PROP_IS_A_CLAUSE | PROP_IS_A_LITERAL |
      PROP_IS_AN_ATOM | PROP_IS_LITERAL_CONJUNCTION
11.1.5.43 WEAK_CONDITIONS const Condition carl::WEAK_CONDITIONS [static]
Initial value:
 PROP_CONTAINS_EQUATION | PROP_CONTAINS_INEQUALITY | PROP_CONTAINS_STRICT_INEQUALITY
                                          | PROP_CONTAINS_LINEAR_POLYNOMIAL |
      PROP_CONTAINS_LINEAR_POLYNOMIAL | PROP_CONTAINS_NONLINEAR_POLYNOMIAL
                                          | PROP_CONTAINS_MULTIVARIATE_POLYNOMIAL |
      PROP_CONTAINS_INEQUALITY | PROP_CONTAINS_BOOLEAN
                                          | PROP_CONTAINS_REAL_VALUED_VARS |
      PROP_CONTAINS_INTEGER_VALUED_VARS
                                          | PROP_CONTAINS_UNINTERPRETED_EQUATIONS | PROP_CONTAINS_BITVECTOR
       | PROP_CONTAINS_PSEUDOBOOLEAN
                                          | PROP_VARIABLE_DEGREE_GREATER_THAN_TWO |
      PROP_VARIABLE_DEGREE_GREATER_THAN_THREE | PROP_VARIABLE_DEGREE_GREATER_THAN_FOUR
```

# 11.2 carl::benchmarks Namespace Reference

## **Functions**

```
• template<typename C , typename O , typename P >
  std::vector< MultivariatePolynomial< C, O, P >> katsura2 ()
- template<typename C , typename O , typename P >
 std::vector< MultivariatePolynomial< C, O, P >> katsura3 ()
• template<typename C , typename O , typename P >
 std::vector< MultivariatePolynomial< C, O, P >> katsura4 ()
• template<typename C , typename O , typename P >
  std::vector< MultivariatePolynomial< C, O, P >> katsura5 ()
- template<typename C , typename O , typename P >
  std::vector< MultivariatePolynomial< C, O, P >> katsura (unsigned index)
- template<typename C , typename O , typename P >
  std::vector< MultivariatePolynomial< C, O, P >> cyclic2 ()
• template<typename C , typename O , typename P >
  std::vector< MultivariatePolynomial< C, O, P >> cyclic3 ()

    template<typename C , typename O , typename P >

  std::vector< MultivariatePolynomial< C, O, P >> cyclic (unsigned index)
```

# 11.2.1 Function Documentation

```
11.2.1.6 katsura3() template<typename C , typename O , typename P >
std::vector<MultivariatePolynomial<C, O, P> > carl::benchmarks::katsura3 ( )

11.2.1.7 katsura4() template<typename C , typename O , typename P >
std::vector<MultivariatePolynomial<C, O, P> > carl::benchmarks::katsura4 ( )

11.2.1.8 katsura5() template<typename C , typename O , typename P >
std::vector<MultivariatePolynomial<C, O, P> > carl::benchmarks::katsura5 ( )
```

# 11.3 carl::checkpoints Namespace Reference

### **Data Structures**

- · class CheckpointVector
- · class CheckpointVerifier

# 11.4 carl::constraint Namespace Reference

### **Functions**

- template<typename Pol >
   BasicConstraint< Pol > init\_bound (Variable var, Relation rel, const typename Pol::NumberType &bound)
- template<typename Pol >
   BasicConstraint
   Pol > init\_constraint
   (const Pol &lhs, Relation rel)
- template<typename Pol > void normalize\_integer\_inplace (BasicConstraint< Pol > &constraint)
- template<typename Pol >
   unsigned is\_consistent\_definiteness (const BasicConstraint< Pol > &constraint, std::optional< Definiteness
   > lhs\_definiteness=std::nullopt)
- template<typename Pol >
   void normalize\_consistency\_inplace (BasicConstraint< Pol > &constraint, std::optional< Definiteness > Ihs
   \_definiteness=std::nullopt)
- template<typename Pol >
   bool simplify\_nonlinear\_univariate\_monomial\_inplace (BasicConstraint< Pol > &constraint, std::optional
   Definiteness > Ihs\_definiteness=std::nullopt)
- template<typename Pol >
   bool simplify\_integer\_inplace (BasicConstraint< Pol > &constraint)
- template<typename Pol >
   BasicConstraint
   Pol > create\_normalized\_constraint (const Pol &lhs, Relation rel)

### **Variables**

• static constexpr bool FULL\_EFFORT\_FOR\_DEFINITENESS\_CHECK = false

## 11.4.1 Function Documentation

```
11.4.1.1 create_normalized_bound() template<typename Pol >
BasicConstraint<Pol> carl::constraint::create_normalized_bound (
             Variable var,
             Relation rel,
             const typename Pol::NumberType & bound )
11.4.1.2 create_normalized_constraint() template<typename Pol >
BasicConstraint<Pol> carl::constraint::create_normalized_constraint (
             const Pol & lhs,
             Relation rel )
11.4.1.3 init_bound() template<typename Pol >
BasicConstraint<Pol> carl::constraint::init_bound (
             Variable var,
             Relation rel,
             const typename Pol::NumberType & bound )
11.4.1.4 init_constraint() template<typename Pol >
BasicConstraint<Pol> carl::constraint::init_constraint (
            const Pol & lhs,
             Relation rel )
11.4.1.5 is_consistent_definiteness() template<typename Pol >
unsigned carl::constraint::is_consistent_definiteness (
             const BasicConstraint< Pol > & constraint,
             std::optional< Definiteness > lhs_definiteness = std::nullopt ) [inline]
11.4.1.6 normalize_consistency_inplace() template<typename Pol >
void carl::constraint::normalize_consistency_inplace (
             BasicConstraint < Pol > & constraint,
             std::optional< Definiteness > lhs_definiteness = std::nullopt ) [inline]
```

## 11.4.2 Variable Documentation

```
11.4.2.1 FULL_EFFORT_FOR_DEFINITENESS_CHECK constexpr bool carl::constraint::FULL.←

EFFORT_FOR_DEFINITENESS_CHECK = false [static], [constexpr]
```

# 11.5 carl::constraints Namespace Reference

# **Functions**

template < typename PolType, bool AS, typename InIt, typename InsertIt > void toPolynomialConstraints (InIt start, InIt end, InsertIt out)
 Converts Constraint < RationalFunction < Poly> > to Constraint < Poly>

## 11.5.1 Function Documentation

Converts Constraint < Rational Function < Poly >> to Constraint < Poly >

## 11.6 carl::contractor Namespace Reference

#### **Data Structures**

class Evaluation

Represents a contraction operation of the form.

· class Contractor

#### **Functions**

```
    template<typename Polynomial >
        std::ostream & operator<< (std::ostream &os, const Evaluation< Polynomial > &e)
```

## 11.6.1 Function Documentation

## 11.7 carl::convert\_poly Namespace Reference

## **Data Structures**

- struct ConvertHelper
- struct ConvertHelper< ContextPolynomial< A, B, C >, MultivariatePolynomial< A, B, C >>
- struct ConvertHelper< MultivariatePolynomial< A, B, C >, ContextPolynomial< A, B, C >>

# 11.8 carl::convert\_ran Namespace Reference

#### **Data Structures**

struct ConvertHelper

## 11.9 carl::covering Namespace Reference

## **Namespaces**

heuristic

## **Data Structures**

class SetCover

Represents a set cover problem.

class TypedSetCover

Represents a set cover problem where a set is represented by some type.

#### **Functions**

```
    std::ostream & operator<< (std::ostream &os, const SetCover &sc)</li>
```

Print the set cover to os.

template<typename T >

```
std::ostream & operator<< (std::ostream &os, const TypedSetCover< T > &tsc)
```

Print the typed set cover to os.

#### 11.9.1 Function Documentation

Print the set cover to os.

Print the typed set cover to os.

## 11.10 carl::covering::heuristic Namespace Reference

## **Functions**

- Bitset exact (SetCover &sc)

Exact "heuristic": Computes a minimum set cover.

• Bitset remove\_duplicates (SetCover &sc)

Preprocessing heuristic: Compresses the matrix by removing duplicate columns.

• Bitset select\_essential (SetCover &sc)

Preprocessing heuristic: Selects essential sets which are the only once covering some element.

Bitset greedy (SetCover &sc)

Simple greedy heuristic: Selects the largest remaining set until all elements are covered.

Bitset greedy\_bounded (SetCover &sc, std::size\_t bound=12)

Bounded greedy heuristic: Selects the largest remaining set until at most bound constraints remain.

Bitset greedy\_weighted (SetCover &sc, const std::vector< double > &weights, std::size\_t bound=0)

Weighted greedy heuristic: Selects the largest remaining set according to the given weight function until at most bound constraints remain.

• template<typename T , typename F >

```
auto greedy_weighted (TypedSetCover< T > &tsc, F &&weight, std::size_t bound=0)
```

Weighted greedy heuristic: Selects the largest remaining set according to the given weight function until at most bound constraints remain.

• Bitset trivial (SetCover &sc)

Trivial heuristic: select all sets.

#### 11.10.1 Function Documentation

Exact "heuristic": Computes a minimum set cover.

```
11.10.1.3 greedy() Bitset carl::covering::heuristic::greedy (

SetCover & sc )
```

Simple greedy heuristic: Selects the largest remaining set until all elements are covered.

Bounded greedy heuristic: Selects the largest remaining set until at most bound constraints remain.

Weighted greedy heuristic: Selects the largest remaining set according to the given weight function until at most bound constraints remain.

Weighted greedy heuristic: Selects the largest remaining set according to the given weight function until at most bound constraints remain.

Preprocessing heuristic: Compresses the matrix by removing duplicate columns.

The order of the columns changes!

```
11.10.1.8 select_essential() Bitset carl::covering::heuristic::select_essential (

SetCover & sc )
```

Preprocessing heuristic: Selects essential sets which are the only once covering some element.

Trivial heuristic: select all sets.

## 11.11 carl::detail Namespace Reference

#### **Data Structures**

- struct stream\_joined\_impl
- struct variant\_is\_type\_visitor
- · struct variant\_extend\_visitor
- struct variant\_hash
- struct is\_from\_variant\_wrapper
- struct is\_from\_variant\_wrapper< Check, T, Variant< Args... > >
- struct tuple\_accumulate\_impl

Helper functor for carl::tuple\_accumulate that actually does the work.

### **Functions**

- template<typename Tuple, std::size\_t... I>
   std::ostream & stream\_tuple\_impl (std::ostream &os, const Tuple &t, std::index\_sequence< I... >)
   Helper function that actually outputs a std::tuple.
- template<typename T , typename F >
  - std::ostream & operator<< (std::ostream &os, const stream\_joined\_impl< T, F > &sji)
- uint next\_prime (const uint &n, const PrimeFactory < uint > &pf)
- mpz\_class next\_prime (const mpz\_class &n, const PrimeFactory < mpz\_class > &)
- template<typename Coeff, typename Integer >
   UnivariatePolynomial < Coeff > exclude\_linear\_factors (const UnivariatePolynomial < Coeff > &poly,
   FactorMap < Coeff > &linearFactors, const Integer &maxInt)
- template<typename CoeffType >
   void var\_info\_term (VarInfo< CoeffType > &info, const typename CoeffType::TermType &term, const Variable
   var, bool collect\_coeff)
- template<typename Coeff, typename Ordering, typename Policies >
   void vars\_info\_term (VarsInfo< MultivariatePolynomial< Coeff, Ordering, Policies >> &infos, const typename
   MultivariatePolynomial< Coeff, Ordering, Policies >::TermType &term, bool collect\_coeff)
- template < typename Tuple1 , typename Tuple2 , std::size\_t... | 1, std::size\_t... | 12>
   auto tuple\_cat\_impl (Tuple1 &&t1, Tuple2 &&t2, std::index\_sequence < | 1... > , std::index\_sequence < | 1... > )

```
Helper method for carl::tuple_apply that actually performs the call.
```

```
    template<typename Tuple, std::size_t... l>
    auto tuple_tail_impl (Tuple &&t, std::index_sequence< l... >)
```

Helper method for carl::tuple\_tail that actually performs the call.

template<typename F, typename Tuple, std::size\_t... I>
 auto tuple\_apply\_impl (F &&f, Tuple &&t, std::index\_sequence< I... >)

Helper method for carl::tuple\_apply that actually performs the call.

template<typename F , typename Tuple , std::size\_t... I>
 auto tuple\_foreach\_impl (F &&f, Tuple &&t, std::index\_sequence< I... >)

Helper method for carl::tuple\_foreach that actually does the work.

#### 11.11.1 Function Documentation

The format is (<item>, <item>, ...)

```
11.11.1.1 exclude_linear_factors() template<typename Coeff , typename Integer >
UnivariatePolynomial < Coeff > carl::detail::exclude_linear_factors (
             const UnivariatePolynomial< Coeff > & poly,
             FactorMap< Coeff > & linearFactors,
             const Integer & maxInt )
11.11.1.2 next_prime() [1/2] mpz_class carl::detail::next_prime (
             const mpz_class & n,
             const PrimeFactory< mpz_class > & ) [inline]
11.11.1.3 next_prime() [2/2] uint carl::detail::next_prime (
             const uint & n,
             const PrimeFactory< uint > & pf ) [inline]
11.11.1.4 operator << () template < typename T , typename F >
std::ostream& carl::detail::operator<< (</pre>
             std::ostream & os,
             const stream_joined_impl< T, F > & sji )
11.11.1.5 stream_tuple_impl() template<typename Tuple , std::size_t... I>
std::ostream& carl::detail::stream_tuple_impl (
             std::ostream & os,
             const Tuple & t,
             std::index\_sequence < I... > )
Helper function that actually outputs a std::tuple.
```

#### **Parameters**

| os | Output stream.       |
|----|----------------------|
| t  | tuple to be printed. |

#### Returns

Output stream.

Helper method for carl::tuple\_apply that actually performs the call.

Helper method for carl::tuple\_apply that actually performs the call.

Helper method for carl::tuple\_foreach that actually does the work.

Helper method for carl::tuple\_tail that actually performs the call.

# 11.12 carl::detail\_derivative Namespace Reference

#### **Functions**

constexpr std::size\_t multiply (std::size\_t n, std::size\_t k)
 Returns n \* (n-1) \* ... \* (n-k+1)

#### 11.12.1 Function Documentation

## 11.13 carl::detail\_sign\_variations Namespace Reference

#### **Functions**

template<typename Coefficient >
 UnivariatePolynomial< Coefficient > reverse (UnivariatePolynomial< Coefficient > &&p)
 Reverses the order of the coefficients of this polynomial.

template<typename Coefficient >
 UnivariatePolynomial< Coefficient > scale (UnivariatePolynomial< Coefficient > &&p, const Coefficient &factor)

Scale the variable, i.e.

template<typename Coefficient >
 UnivariatePolynomial< Coefficient > shift (const UnivariatePolynomial< Coefficient > &p, const Coefficient &a)

Shift the variable by a, i.e.

#### 11.13.1 Function Documentation

Reverses the order of the coefficients of this polynomial.

This method is meant to be called by signVariations only.

Runtime complexity O(n)

Scale the variable, i.e.

apply  $x \to factor * x$  This method is meant to be called by signVariations only.

#### **Parameters**

```
factor Factor to scale x.
```

## Runtime complexity O(n)

Shift the variable by a, i.e.

apply  $x \to x + a$  This method is meant to be called by signVariations only.

### **Parameters**

```
a Offset to shift x.
```

## **Runtime complexity** O(n^2)

## 11.14 carl::dtl Namespace Reference

#### **Enumerations**

• enum class enabled

## 11.14.1 Enumeration Type Documentation

```
11.14.1.1 enabled enum carl::dtl::enabled [strong]
```

# 11.15 carl::formula Namespace Reference

### **Namespaces**

- aux
- · symmetry

## **Typedefs**

- using Symmetry = std::vector< std::pair< Variable, Variable > >
   A symmetry σ represents a bijection on a set of variables.
- using Symmetries = std::vector< Symmetry >

Represents a list of symmetries.

### **Functions**

- template<typename Poly >
   Symmetries findSymmetries (const Formula< Poly > &f)
- template<typename Poly >
   Formula< Poly > breakSymmetries (const Symmetries &symmetries, bool onlyFirst=true)
- template<typename Poly >
   Formula< Poly > breakSymmetries (const Formula< Poly > &f, bool onlyFirst=true)

# 11.15.1 Typedef Documentation

## 11.15.1.1 Symmetries using carl::formula::Symmetries = typedef std::vector<Symmetry>

Represents a list of symmetries.

```
11.15.1.2 Symmetry using carl::formula::Symmetry = typedef std::vector<std::pair<Variable, Variable>
```

A symmetry  $\sigma$  represents a bijection on a set of variables.

For every entry in the vector we have  $\sigma(e.first) = e.second$ .

#### 11.15.2 Function Documentation

## 11.16 carl::formula::aux Namespace Reference

#### **Functions**

```
    template < typename Pol >
        Formula < Pol > connectPrecedingSubformulas (const Formula < Pol > &f)
        [Auxiliary method]
```

#### 11.16.1 Function Documentation

[Auxiliary method]

### Returns

The formula combining the first to the second last sub-formula of this formula by the same operator as the one of this formula. Example: this =  $(op \ a1 \ a2 \ ... \ an) \rightarrow return = (op \ a1 \ ... \ an-1)$  If n = 2, return = a1

# 11.17 carl::formula::symmetry Namespace Reference

#### **Data Structures**

· class ColorGenerator

Provides unique ids (colors) for all kinds of different objects in the formula: variable types, relations, formula types, numbers, special colors and indexes.

- struct Permutation
- · class GraphBuilder

#### **Enumerations**

enum class SpecialColors { If , Then , Else , VarExp }
 Special colors for structure nodes.

#### **Functions**

- template<typename Poly >
   Formula< Poly > createComparison (Variable x, Variable y, Relation rel)
- template<typename Poly >
   Formula< Poly > lexLeaderConstraint (const Symmetry &vars)

Creates symmetry breaking constraints from the passed symmetries in the spirit of ?.

• void addGenerator (void \*p, const unsigned int n, const unsigned int \*aut)

# 11.17.1 Enumeration Type Documentation

# 11.17.1.1 SpecialColors enum carl::formula::symmetry::SpecialColors [strong]

Special colors for structure nodes.

- · If: condition from ite
- · Then: first case from ite
- · Else: second case from ite
- · VarExp: pair of variable and exponent in terms

### Enumerator

| If     |  |
|--------|--|
| Then   |  |
| Else   |  |
| VarExp |  |

#### 11.17.2 Function Documentation

Creates symmetry breaking constraints from the passed symmetries in the spirit of ?.

## 11.18 carl::formula\_to\_cnf Namespace Reference

## **Typedefs**

- template<typename Poly >
   using TseitinConstraints = std::vector< Formula< Poly > >
- template<typename Poly >
   using ConstraintBounds = FastMap< Poly, std::map< typename Poly::NumberType, std::pair< Relation,
   Formula< Poly > >> >

#### **Functions**

template<typename Poly >
 std::vector< Formula< Poly > > construct\_iff (const Formula< Poly > &lhs, const std::vector< Formula< Poly >> &rhs\_and)

Constructs the equivalent of (iff lhs (and  $*rhs\_and$ ))) The result is the list (=> lhs (and  $*rhs\_and$ )) (=> rhs !lhs) (for each rhs in rhs\\_and)

template<typename Poly >
 Formula < Poly > to\_cnf\_or (const Formula < Poly > &f, bool keep\_constraints, bool simplify\_combinations, bool tseitin\_equivalence, TseitinConstraints < Poly > &tseitin)

Converts an OR to cnf.

## 11.18.1 Typedef Documentation

```
11.18.1.1 ConstraintBounds template<typename Poly > using carl::formula_to_cnf::ConstraintBounds = typedef FastMap<Poly, std::map<typename Poly::← NumberType, std::pair<Relation,Formula<Poly> >> >
```

```
11.18.1.2 TseitinConstraints template<typename Poly >
using carl::formula_to_cnf::TseitinConstraints = typedef std::vector<Formula<Poly> >
```

#### 11.18.2 Function Documentation

Constructs the equivalent of (iff lhs (and  $*rhs\_and$ ))) The result is the list (=> lhs (and  $*rhs\_and$ )) (=> rhs !lhs) (for each rhs in rhs\\_and)

Converts an OR to cnf.

## 11.19 carl::gcd\_detail Namespace Reference

#### **Functions**

- template < typename Polynomial >
   Variable select\_variable (const Polynomial &p1, const Polynomial &p2)
- template<typename Polynomial >
   Polynomial gcd\_calculate (const Polynomial &a, const Polynomial &b)

### 11.19.1 Function Documentation

## 11.20 carl::helper Namespace Reference

#### **Data Structures**

- struct Substitutor
- struct PolynomialSubstitutor
- struct BitvectorSubstitutor
- · struct UninterpretedSubstitutor

#### **Functions**

template < typename C, typename O, typename P >
 Factors < MultivariatePolynomial < C, O, P > > trivialFactorization (const MultivariatePolynomial < C, O, P >
 &p)

Returns a factors datastructure containing only the full polynomial as single factor.

template < typename C, typename O, typename P >
 void sanitizeFactors (const MultivariatePolynomial < C, O, P > & reference, Factors < MultivariatePolynomial <
 C, O, P >> & factors)

## 11.20.1 Function Documentation

Returns a factors datastructure containing only the full polynomial as single factor.

## 11.21 carl::io Namespace Reference

### **Namespaces**

- detail
- helper
- parser

#### **Data Structures**

- struct OPBFile
- class OPBImporter
- class InvalidInputStringException
- · class StringParser
- class DIMACSExporter

Write formulas to the DIMAS format.

· class DIMACSImporter

Parser for the DIMACS format.

- class MapleStream
- · class QEPCADStream
- class SMTLIBStream

Allows to print carl data structures in SMTLIB syntax.

#### **Typedefs**

- using BaseIteratorType = spirit::istream\_iterator
- using PositionIteratorType = spirit::line\_pos\_iterator< BaseIteratorType >
- using Iterator = PositionIteratorType
- using ErrorHandler = carl::io::helper::ErrorHandler
- using OPBPolynomial = std::vector< std::pair< int, carl::Variable > >
- using OPBConstraint = std::tuple < OPBPolynomial, Relation, int >

#### **Functions**

- std::optional < OPBFile > parseOPBFile (std::ifstream &in)
- std::ostream & operator<< (std::ostream &os, const MapleStream &ms)</li>
- std::ostream & operator<< (std::ostream &os, const QEPCADStream &qs)</li>
- std::ostream & operator<< (std::ostream &os, const SMTLIBStream &ss)</li>

Write the written data to some std::ostream.

template<typename Pol , typename... Args>
 detail::SMTLIBScriptContainer< Pol > outputSMTLIB (Logic I, std::initializer\_list< Formula< Pol >> formulas, Args &&... args)

Shorthand to allow writing SMTLIB scripts in one line.

template<typename... Args>
 detail::SMTLIBOutputContainer< Args... > asSMTLIB (Args &&... args)

Generic shorthand to write arbitrary data to an SMTLIBStream and return the result.

## 11.21.1 Typedef Documentation

```
11.21.1.1 BaselteratorType using carl::io::BaseIteratorType = typedef spirit::istream.iterator
11.21.1.2 ErrorHandler using carl::io::ErrorHandler = typedef carl::io::helper::ErrorHandler
11.21.1.3 | Iterator using carl::io::Iterator = typedef PositionIteratorType
11.21.1.4 OPBConstraint using carl::io::OPBConstraint = typedef std::tuple<OPBPolynomial,
Relation, int>
11.21.1.5 OPBPolynomial using carl::io::OPBPolynomial = typedef std::vector<std::pair<int,carl::Variable>
11.21.1.6 PositionIteratorType using carl::io::PositionIteratorType = typedef spirit::line.pos.←
iterator<BaseIteratorType>
11.21.2 Function Documentation
11.21.2.1 asSMTLIB() template<typename... Args>
detail::SMTLIBOutputContainer<Args...> carl::io::asSMTLIB (
            Args &&... args )
Generic shorthand to write arbitrary data to an SMTLIBStream and return the result.
11.21.2.2 operator<<() [1/3] std::ostream& carl::io::operator<< (
            std::ostream & os,
             const MapleStream & ms ) [inline]
11.21.2.3 operator<<() [2/3] std::ostream& carl::io::operator<< (
            std::ostream & os,
```

const QEPCADStream & qs ) [inline]

Write the written data to some std::ostream.

Shorthand to allow writing SMTLIB scripts in one line.

# 11.22 carl::io::detail Namespace Reference

#### **Data Structures**

- struct SMTLIBScriptContainer
  - Shorthand to allow writing SMTLIB scripts in one line.
- struct SMTLIBOutputContainer

#### **Functions**

```
    template<typename Pol >
        std::ostream & operator<< (std::ostream &os, const SMTLIBScriptContainer< Pol > &sc)
        Actually write an SMTLIBScriptContainer to an std::ostream.
```

```
    template<typename... Args>
        std::ostream & operator<< (std::ostream &os, const SMTLIBOutputContainer< Args... > &soc)
```

## 11.22.1 Function Documentation

Actually write an SMTLIBScriptContainer to an std::ostream.

## 11.23 carl::io::helper Namespace Reference

#### **Data Structures**

struct ErrorHandler

# 11.24 carl::io::parser Namespace Reference

#### **Data Structures**

- struct RationalPolicies
- struct ExpressionParser
- struct FormulaParser
- class Parser
- struct PolynomialParser
- · struct RationalFunctionParser

## **Typedefs**

- using <a href="left">Iterator</a> = std::string::const\_iterator
- using Skipper = boost::spirit::qi::space\_type
- template<typename Pol >
   using RatFun = RationalFunction<</li>
   Pol >
- template<typename Pol >
   using ExpressionType = boost::variant< typename Pol::CoeffType, carl::Variable, carl::Monomial::Arg, carl::Term< typename Pol::CoeffType >, Pol, RationalFunction< Pol >, carl::Formula< Pol >>

## 11.24.1 Typedef Documentation

```
11.24.1.1 ExpressionType template<typename Pol >
using carl::io::parser::ExpressionType = typedef boost::variant< typename Pol::CoeffType,
carl::Variable, carl::Monomial::Arg, carl::Term<typename Pol::CoeffType>, Pol, RationalFunction<Pol>,
carl::Formula<Pol> >
```

```
11.24.1.2 | Iterator using carl::io::parser::Iterator = typedef std::string::const_iterator
```

```
11.24.1.3 RatFun template<typename Pol >
using carl::io::parser::RatFun = typedef RationalFunction<Pol>
```

```
11.24.1.4 Skipper using carl::io::parser::Skipper = typedef boost::spirit::qi::space_type
```

# 11.25 carl::logging Namespace Reference

Contains a custom logging facility.

#### **Data Structures**

struct RecordInfo

Additional information about a log message.

class Logger

Main logger class.

class Filter

This class checks if some log message shall be forwarded to some sink.

· class Formatter

Formats a log messages.

· class Sink

Base class for a logging sink.

class StreamSink

Logging sink that wraps an arbitrary std::ostream.

class FileSink

Logging sink for file output.

### **Enumerations**

```
    enum class LogLevel {
        LVL_ALL , LVL_TRACE , LVL_DEBUG , LVL_INFO ,
        LVL_WARN , LVL_ERROR , LVL_FATAL , LVL_OFF ,
        LVL_DEFAULT = LVL_WARN }
```

Indicated which log messages should be forwarded to some sink.

# **Functions**

- void setInitialLogLevel ()
- void configureLogging ()
- bool visible (LogLevel level, const std::string &channel) noexcept
- void log (LogLevel level, const std::string &channel, const std::stringstream &ss, const RecordInfo &info)
- std::ostream & operator<< (std::ostream &os, LogLevel level)</li>

Streaming operator for LogLevel.

• Logger & logger ()

Returns the single global instance of a Logger.

## 11.25.1 Detailed Description

Contains a custom logging facility.

This logging facility is fairly generic and is used as a simple and header-only alternative to more advanced solutions like log4cplus or boost::log.

The basic components are Sinks, Channels, Filters, RecordInfos, Formatters and the central Logger component.

A Sink represents a logging output like a terminal or a log file. This implementation provides a FileSink and a StreamSink, but the basic Sink class can be extended as necessary.

A Channel is a string that identifies the context of the log message, usually something like the class name where the log message is emitted. Channels are organized hierarchically where the levels are separated by dots. For example, carl is considered the parent of carl.core.

A Filter is associated with a Sink and makes sure that only a subset of all log messages is forwarded to the Sink. Filter rules are pairs of a Channel and a minimum LogLevel, meaning that messages of this Channel and at least the given LogLevel are forwarded. If a Filter does not contain any rule for some Channel, the parent Channel is considered. Each Filter contains a rule for the empty Channel, initialized with LVL\_DEFAULT.

A RecordInfo stores auxiliary information of a log message like the filename, line number and function name where the log message was emitted.

A Formatter is associated with a Sink and produces the actual string that is sent to the Sink. Usually, it adds auxiliary information like the current time, LogLevel, Channel and information from a RecordInfo to the string logged by the user. The Formatter implements a reasonable default behaviour for log files, but it can be subclassed and modified as necessary.

The Logger class finally plugs all these components together. It allows to configure multiple Sink objects which are identified by strings called id and offers a central log() method.

Initial configuration may look like this:

```
carl::logging::logger().configure("logfile", "carl.log");
carl::logging::logger().filter("logfile")
    ("carl", carl::logging::LogLevel::LVL_INFO)
    ("carl.core", carl::logging::LogLevel::LVL_DEBUG);
carl::logging::logger().resetFormatter();
```

Macro facilitate the usage:

- CARLLOG\_<LVL> (channel, msg) produces a normal log message where channel should be string identifying the channel and msg is the message to be logged.
- CARLLOG\_FUNC (channel, args) produces a log message tailored for function calls. args should represent the function arguments.
- CARLLOG\_ASSERT (channel, condition, msg) checks the condition and if it fails calls CARLLOG\_FATAL (channel, msg) and asserts the condition.

Any message (msg or args) can be an arbitrary expression that one would stream to an std:ostream like stream << (msg);. No final newline is needed.

### 11.25.2 Enumeration Type Documentation

```
11.25.2.1 LogLevel enum carl::logging::LogLevel [strong]
```

Indicated which log messages should be forwarded to some sink.

All messages which have a level that is equal or greater than the specified value will be forwarded.

#### Enumerator

| LVL_ALL     | All log messages.   |
|-------------|---|
| LVL_TRACE   | Finer-grained informational events than the DEBUG.                              |
| LVL_DEBUG   | Fine-grained informational events that are most useful to debug an application. |
| LVL_INFO    | Highlight the progress of the application at coarse-grained level.              |
| LVL_WARN    | Potentially harmful situations or undesired states.                             |
| LVL_ERROR   | Error events that might still allow the application to continue running.        |
| LVL_FATAL   | Severe error events that will presumably lead the application to terminate.     |
| LVL_OFF     | No messages.  |
| LVL_DEFAULT | Default log level.  |

#### 11.25.3 Function Documentation

```
11.25.3.1 configureLogging() void carl::logging::configureLogging ( ) [inline]
```

```
11.25.3.2 log() void carl::logging::log (
    LogLevel level,
    const std::string & channel,
    const std::stringstream & ss,
    const RecordInfo & info )
```

```
11.25.3.3 logger() Logger& carl::logging::logger ( ) [inline]
```

Returns the single global instance of a Logger.

```
Calls Logger::getInstance().
```

#### Returns

Logger object.

Streaming operator for LogLevel.

#### **Parameters**

| os    | Output stream. |
|-------|----------------|
| level | LogLevel.      |

#### Returns

os.

```
11.25.3.5 setInitialLogLevel() void carl::logging::setInitialLogLevel ()
```

## 11.26 carl::model Namespace Reference

#### **Functions**

- template<typename Rational, typename Poly > void substituteSubformulas (Formula< Poly > &f, const Model< Rational, Poly > &m)
- template<typename Rational , typename Poly > void evaluateVarCompare (Formula < Poly > &f, const Model < Rational, Poly > &m)
- template<typename Rational , typename Poly > void evaluateVarAssign (Formula< Poly > &f, const Model< Rational, Poly > &m)
- template<typename Rational, typename Poly >
   Assignment< typename Poly::RootType > collectRANIR (const std::set< Variable > &vars, const Model
   Rational, Poly > &model)

#### 11.26.1 Function Documentation

# 11.27 carl::parser Namespace Reference

#### **Data Structures**

- struct isDivisible
- struct isDivisible < true >
- struct isDivisible < false >
- struct RationalPolicies

Specialization of qi::real\_policies for our rational types.

· struct IntegerParser

Parses (signed) integers.

· struct DecimalParser

Parses decimals, including floating point and scientific notation.

· struct RationalParser

Parses rationals, being two decimals separated by a slash.

#### **Typedefs**

• using Skipper = qi::space\_type

## **Functions**

- template<typename Parser , typename T >
   bool parse\_impl (const std::string &input, T &output)
- template<typename Parser, typename T, typename S >
   bool parse\_impl (const std::string &input, T &output, const S &skipper)
- template < typename T >
   bool parseInteger (const std::string &input, T &output)
- template < typename T >
   bool parseDecimal (const std::string &input, T &output)
- template < typename T >
   bool parseRational (const std::string &input, T &output)

# 11.27.1 Typedef Documentation

```
11.27.1.1 Skipper using carl::parser::Skipper = typedef qi::space_type
```

#### 11.27.2 Function Documentation

```
11.27.2.1 parse_impl() [1/2] template<typename Parser , typename T >
bool carl::parser::parse_impl (
            const std::string & input,
            T & output )
11.27.2.2 parse_impl() [2/2] template<typename Parser , typename T , typename S >
bool carl::parser::parse_impl (
            const std::string & input,
             T & output,
             const S & skipper )
11.27.2.3 parseDecimal() template<typename T >
bool carl::parser::parseDecimal (
            const std::string & input,
             T & output )
11.27.2.4 parseInteger() template<typename T >
bool carl::parser::parseInteger (
            const std::string & input,
             T & output )
11.27.2.5 parseRational() template<typename T >
bool carl::parser::parseRational (
             const std::string & input,
```

# 11.28 carl::poly\_helper Namespace Reference

Helpers due to the shortcomings of libpoly's C++ API.

T & output )

### **Functions**

- poly::Polynomial construct\_poly (const lp\_polynomial\_context\_t \*c, lp\_variable\_t v)
- poly::Polynomial construct\_poly (const lp\_polynomial\_context\_t \*c, poly::Integer i)

## 11.28.1 Detailed Description

Helpers due to the shortcomings of libpoly's C++ API.

#### 11.28.2 Function Documentation

## 11.29 carl::pool Namespace Reference

#### **Data Structures**

- · class RehashPolicy
  - Mimics stdlibs default rehash policy for hashtables.
- class LocalPool
- class LocalPoolElementWrapper
- class LocalPoolElement
- class Pool
- class PoolElementWrapper
- class PoolElement

## **Functions**

- template < class Content >
   std::size\_t hash\_value (const LocalPoolElementWrapper < Content > &wrapper)
- template < class Content >
   bool operator == (const LocalPoolElementWrapper < Content > &c1, const LocalPoolElementWrapper < Content > &c2)
- template < class Content >
   std::size\_t hash\_value (const PoolElementWrapper < Content > &wrapper)
- template < class Content >
   bool operator == (const PoolElementWrapper < Content > &c1, const PoolElementWrapper < Content > &c2)

## 11.29.1 Function Documentation

## 11.30 carl::ran Namespace Reference

## **Namespaces**

interval

## 11.31 carl::ran::interval Namespace Reference

## **Namespaces**

· detail\_field\_extensions

### **Data Structures**

class FieldExtensions

This class can be used to construct iterated field extensions from a sequence of real algebraic numbers.

- class LazardEvaluation
- · class RealRootIsolation

Compact class to isolate real roots from a univariate polynomial using bisection.

class ran\_evaluator

#### **Enumerations**

enum class AlgebraicSubstitutionStrategy { RESULTANT, GROEBNER }
 Indicates which strategy to use: resultants or Gröbner bases.

#### **Functions**

template<typename Number >
 std::optional< UnivariatePolynomial< Number > > algebraic\_substitution\_groebner (const std::vector
 MultivariatePolynomial
 Number >> &polynomials, const std::vector
 Variable > &variables)

Implements algebraic substitution by Gröbner basis computation.

template<typename Number >

std::optional < UnivariatePolynomial < Number >> algebraic\_substitution\_groebner (const UnivariatePolynomial < MultivariatePolynomial < Number >> &p, const std::vector < UnivariatePolynomial < MultivariatePolynomial < Number >>> &polynomials)

Implements algebraic substitution by Gröbner basis computation.

template<typename Number >

std::optional < UnivariatePolynomial < Number >> algebraic\_substitution\_resultant (const UnivariatePolynomial < MultivariatePolynomial < Number >>> &p, const std::vector < UnivariatePolynomial < MultivariatePolynomial < Number >>> &polynomials)

Implements algebraic substitution by resultant computation.

template<typename Number >

std::optional < UnivariatePolynomial < Number > > algebraic\_substitution\_resultant (const std::vector < MultivariatePolynomial < Number >> &polynomials, const std::vector < Variable > &variables)

Implements algebraic substitution by resultant computation.

• template<typename Number >

std::optional< UnivariatePolynomial< Number >> algebraic\_substitution (const UnivariatePolynomial< MultivariatePolynomial< Number >>> &p, const std::vector< UnivariatePolynomial< MultivariatePolynomial< Number >>>> &polynomials, AlgebraicSubstitutionStrategy strategy=AlgebraicSubstitutionStrategy::RESULTANT)

Computes the algebraic substitution of the given defining polynomials into a multivariate polynomial p.

• template<typename Number >

std::optional < UnivariatePolynomial < Number >> algebraic\_substitution (const std::vector < MultivariatePolynomial < Number >> &polynomials, const std::vector < Variable > &variables, AlgebraicSubstitutionStrategy strategy=AlgebraicSubstitutionStrategy::RESULTANT)

Computes the algebraic substitution of the given defining polynomials into a multivariate polynomial p.

template<typename Number, typename Coeff >
 std::optional< UnivariatePolynomial< Number > > substitute\_rans\_into\_polynomial (const UnivariatePolynomial
 Coeff > &p, const OrderedAssignment< IntRepRealAlgebraicNumber< Number >> &m, bool use\_
 lazard=false)

#### 11.31.1 Enumeration Type Documentation

**11.31.1.1** AlgebraicSubstitutionStrategy enum carl::ran::interval::AlgebraicSubstitutionStrategy [strong]

Indicates which strategy to use: resultants or Gröbner bases.

#### Enumerator

RESULTANT GROEBNER

#### 11.31.2 Function Documentation

Computes the algebraic substitution of the given defining polynomials into a multivariate polynomial p.

The result is a univariate polynomial in the main variable of p.

Computes the algebraic substitution of the given defining polynomials into a multivariate polynomial p.

The result is a univariate polynomial in the main variable of p.

Implements algebraic substitution by Gröbner basis computation.

Essentially we take all polynomials and compute a Gröbner basis with respect to an elimination order, having the remaining variable at the end. The result is then the polynomial in the last variable only.

Implements algebraic substitution by Gröbner basis computation.

Essentially we take all polynomials and compute a Gröbner basis with respect to an elimination order, having the remaining variable at the end. The result is then the polynomial in the last variable only.

Implements algebraic substitution by resultant computation.

We iteratively compute the resultant of the input polynomial with each of the defining polynomials. Eventually we obtain a polynomial univariate in the remaining variable, our result.

Note that we assume that the polynomials are in a triangular form where any polynomial may contain variables that are `'defined'' by the previous polynomials.

Implements algebraic substitution by resultant computation.

We iteratively compute the resultant of the input polynomial with each of the defining polynomials. Eventually we obtain a polynomial univariate in the remaining variable, our result.

Note that we assume that the polynomials are in a triangular form where any polynomial may contain variables that are `'defined'' by the previous polynomials.

## 11.32 carl::ran::interval::detail\_field\_extensions Namespace Reference

## 11.33 carl::resultant\_debug Namespace Reference

### **Functions**

template<typename Coeff >
 UnivariatePolynomial< Coeff > resultant\_z3 (const UnivariatePolynomial< Coeff > &p, const UnivariatePolynomial

 Coeff > &q)

A reimplementation of the resultant algorithm from z3.

template < typename Coeff >
 UnivariatePolynomial < Coeff > eliminate (const UnivariatePolynomial < Coeff > &p, const UnivariatePolynomial <
 Coeff > &q)

Eliminates the leading factor of p with q.

template<typename Coeff >
 UnivariatePolynomial< Coeff > resultant\_det (const UnivariatePolynomial< Coeff > &p, const UnivariatePolynomial< Coeff > &q)

An implementation of the naive resultant algorithm based on the silvester matrix.

#### 11.33.1 Function Documentation

Eliminates the leading factor of p with q.

An implementation of the naive resultant algorithm based on the silvester matrix.

A reimplementation of the resultant algorithm from z3.

Used for a comparative analysis of our own algorithm.

## 11.34 carl::roots Namespace Reference

### **Namespaces**

• eigen

## 11.35 carl::roots::eigen Namespace Reference

## **Functions**

std::vector< double > root\_approximation (const std::vector< double > &coeffs)
 Compute approximations of the real roots of the univariate polynomials with the given coefficients.

### 11.35.1 Function Documentation

Compute approximations of the real roots of the univariate polynomials with the given coefficients.

This method internally constructs a companion matrix and computes the eigenvalues.

## 11.36 carl::settings Namespace Reference

#### **Data Structures**

· struct duration

Helper type to parse duration as std::chrono values with boost::program\_options.

struct binary\_quantity

Helper type to parse quantities with binary SI-style suffixes.

· struct metric\_quantity

Helper type to parse quantities with SI-style suffixes.

struct OptionPrinter

Helper class to nicely print the options that are available.

· struct SettingsPrinter

Helper class to nicely print the settings that were parsed.

· class SettingsParser

Base class for a settings parser.

struct Settings

Base class for central settings class.

#### **Functions**

- void validate (boost::any &v, const std::vector< std::string > &values, carl::settings::duration \*, int)

  Custom validator for duration that wraps some std::chrono::duration.
- void validate (boost::any &v, const std::vector< std::string > &values, carl::settings::binary\_quantity \*, int)

  Custom validator for binary quantities.
- void validate (boost::any &v, const std::vector< std::string > &values, carl::settings::metric\_quantity \*, int) Custom validator for metric quantities.
- ullet template<typename Array >

std::pair< std::intmax\_t, std::size\_t > get\_proper\_suffix (std::intmax\_t value, const Array &a)

Helper method to obtain proper (unit) suffix entry from a value and a given set of possible suffixes.

std::ostream & operator<< (std::ostream &os, const duration &d)</li>

Streaming operator for duration. Auto-detects proper time suffix.

constexpr bool operator== (binary\_quantity lhs, binary\_quantity rhs)

Compare two binary quantities for equality.

constexpr bool operator< (binary\_quantity lhs, binary\_quantity rhs)</li>

Compare two binary quantities.

std::ostream & operator<< (std::ostream &os, const binary\_quantity &q)</li>

Streaming operator for binary quantity. Auto-detects proper suffix.

constexpr bool operator== (metric\_quantity lhs, metric\_quantity rhs)

Compare two metric quantities for equality.

constexpr bool operator< (metric\_quantity lhs, metric\_quantity rhs)</li>

Compare two metric quantities.

• std::ostream & operator<< (std::ostream &os, const metric\_quantity &q)

Streaming operator for metric quantity. Auto-detects proper suffix.

- std::ostream & operator<< (std::ostream &os, const boost::any &val)</li>
- std::ostream & operator<< (std::ostream &os, OptionPrinter op)</li>

Streaming operator for a option printer.

std::ostream & operator<< (std::ostream &os, SettingsPrinter sp)</li>

Streaming operator for a settings printer.

template<typename T >

void default\_to (po::variables\_map &values, const std::string &name, const T &value)

Inserts value into variables\_map if it is not yet set.

template<typename T >

void overwrite\_to (po::variables\_map &values, const std::string &name, const T &value)

Inserts or overwrites value into variables\_map.

#### 11.36.1 Function Documentation

Inserts value into variables\_map if it is not yet set.

This method is intended as a helper for finalizer functions.

Helper method to obtain proper (unit) suffix entry from a value and a given set of possible suffixes.

Can be called, for example, with a value of nanoseconds and the following array  $a = \{ \{"ns", 1000\}, \{"ms", 1000\}, \{"ms", 1000\}, \{"m", 60\}, \{"m", 60\}, \{"h", 1\} \}$ . This method will find the largest suffix such that the value will not be zero if represented with respect to this suffix. The return value is the value converted to this unit suffix and the index into the array to retrieve the appropriate suffix string. For the above example, get\_proper\_suffix (30000000000, a) =  $\{30, 3\}$ , that is 30s.

Compare two binary quantities.

Compare two metric quantities.

```
11.36.1.5 operator << () [1/6] std::ostream& carl::settings::operator << ( std::ostream & os, const binary-quantity & q) [inline]
```

Streaming operator for binary quantity. Auto-detects proper suffix.

```
11.36.1.6 operator << () [2/6] std::ostream & carl::settings::operator << ( std::ostream & os, const boost::any & val )
```

Streaming operator for duration. Auto-detects proper time suffix.

```
11.36.1.8 operator << () [4/6] std::ostream & carl::settings::operator << ( std::ostream & os, const metric_quantity & q) [inline]
```

Streaming operator for metric quantity. Auto-detects proper suffix.

Streaming operator for a option printer.

```
11.36.1.10 operator << () [6/6] std::ostream & carl::settings::operator << ( std::ostream & os, SettingsPrinter sp )
```

Streaming operator for a settings printer.

Compare two binary quantities for equality.

Compare two metric quantities for equality.

Inserts or overwrites value into variables\_map.

This method is intended as a helper for finalizer functions.

```
11.36.1.14 validate() [1/3] void carl::settings::validate (
          boost::any & v,
          const std::vector< std::string > & values,
          carl::settings::binary_quantity * ,
          int )
```

Custom validator for binary quantities.

Accepts the format <number><suffix> where suffix is one of the following: Ki, Mi, Gi, Ti, Pi, Ei.

```
11.36.1.15 validate() [2/3] void carl::settings::validate (
          boost::any & v,
          const std::vector< std::string > & values,
          carl::settings::duration * ,
           int )
```

Custom validator for duration that wraps some std::chrono::duration.

Accepts the format <number><suffix> where suffix is one of the following: ns,  $\mu$ s, us, ms, s, m, h.

```
11.36.1.16 validate() [3/3] void carl::settings::validate (
          boost::any & v,
          const std::vector< std::string > & values,
          carl::settings::metric_quantity * ,
          int )
```

Custom validator for metric quantities.

Accepts the format <number><suffix> where suffix is one of the following: K, M, G, T, P, E.

## 11.37 carl::statistics Namespace Reference

#### **Namespaces**

timing

#### **Data Structures**

- · class StatisticsCollector
- class Statistics
- struct StatisticsPrinter
- · class timer

#### **Enumerations**

enum class StatisticsOutputFormat { SMTLIB , XML }

### **Functions**

- template<typename T >
   auto & get (const std::string &name)
- template<StatisticsOutputFormat SOF>
   std::ostream & operator<< (std::ostream &os, StatisticsPrinter< SOF >)
- template<> std::ostream & operator<< (std::ostream &os, StatisticsPrinter< StatisticsOutputFormat::SMTLIB</li>
   )
- template<> std::ostream & operator<< (std::ostream &os, StatisticsPrinter< StatisticsOutputFormat::XML</li>
   )
- auto statistics\_as\_smtlib ()
- auto statistics\_as\_xml ()
- void statistics\_to\_xml\_file (const std::string &filename)

## 11.37.1 Enumeration Type Documentation

#### 11.37.1.1 StatisticsOutputFormat enum carl::statistics::StatisticsOutputFormat [strong]

#### **Enumerator**

SMTLIB XML

#### 11.37.2 Function Documentation

```
11.37.2.1 get() template<typename T >
auto& carl::statistics::get (
            const std::string & name )
11.37.2.2 operator <<() [1/3] template < StatisticsOutputFormat SOF>
std::ostream& carl::statistics::operator<< (</pre>
             std::ostream & os,
             StatisticsPrinter< SOF > )
11.37.2.3 operator<<() [2/3] template<>
\verb| std::ostream \& carl::statistics::operator << (
             std::ostream & os,
             StatisticsPrinter< StatisticsOutputFormat::SMTLIB > )
11.37.2.4 operator<<() [3/3] template<>
std::ostream& carl::statistics::operator<< (</pre>
             std::ostream & os,
             StatisticsPrinter< StatisticsOutputFormat::XML > )
11.37.2.5 statistics_as_smtlib() auto carl::statistics::statistics_as_smtlib ( )
11.37.2.6 statistics_as_xml() auto carl::statistics::statistics_as_xml ( )
11.37.2.7 statistics_to_xml_file() void carl::statistics::statistics_to_xml_file (
             const std::string & filename )
11.38 carl::statistics::timing Namespace Reference
Typedefs
```

• using clock = std::chrono::high\_resolution\_clock

The clock type used here.

• using duration = std::chrono::duration < std::size\_t, std::milli >

The duration type used here.

• using time\_point = clock::time\_point

The type of a time point.

### **Functions**

• auto now ()

Return the current time point.

• auto since (time\_point start)

Return the duration since the given start time point.

• auto zero ()

Return a zero duration.

## 11.38.1 Typedef Documentation

```
\textbf{11.38.1.1} \quad \textbf{clock} \quad \text{using carl::statistics::timing::clock = typedef std::chrono::high\_resolution} \leftarrow \\ \text{clock}
```

The clock type used here.

```
11.38.1.2 duration using carl::statistics::timing::duration = typedef std::chrono::duration<std↔ ::size_t,std::milli>
```

The duration type used here.

```
11.38.1.3 time_point using carl::statistics::timing::time_point = typedef clock::time_point
```

The type of a time point.

# 11.38.2 Function Documentation

```
11.38.2.1 now() auto carl::statistics::timing::now ( ) [inline]
```

Return the current time point.

Return the duration since the given start time point.

```
11.38.2.3 zero() auto carl::statistics::timing::zero ( ) [inline]
```

Return a zero duration.

## 11.39 carl::tree\_detail Namespace Reference

#### **Data Structures**

- struct Node
- · struct BaseIterator

This is the base class for all iterators.

struct PreorderIterator

Iterator class for pre-order iterations over all elements.

· struct PostorderIterator

Iterator class for post-order iterations over all elements.

· struct LeafIterator

Iterator class for iterations over all leaf elements.

struct DepthIterator

Iterator class for iterations over all elements of a certain depth.

· struct ChildrenIterator

Iterator class for iterations over all children of a given element.

struct PathIterator

Iterator class for iterations from a given element to the root.

### **Functions**

```
template<typename T >
  bool operator== (const Node < T > &lhs, const Node < T > &rhs)

    template<typename T >

  std::ostream & operator << (std::ostream &os, const Node < T > &n)

    template<typename T , typename I , bool r>

  T & operator* (Baselterator< T, I, r > \&bi)
• template<typename T , typename I , bool r>
  const T & operator* (const Baselterator< T, I, r > &bi)

    template<typename T, typename I, bool reverse>

  std::enable_if<!reverse, I >::type & operator++ (BaseIterator< T, I, reverse > &it)

    template<typename T , typename I , bool reverse>

  std::enable\_if < reverse, \ I > ::type \ \& \ operator + + \ (Baselterator < T, \ I, \ reverse > \&it)
• template<typename T , typename I , bool reverse>
  std::enable_if<!reverse, I >::type operator++ (Baselterator< T, I, reverse > &it, int)

    template<typename T, typename I, bool reverse>

  std::enable_if< reverse, I >::type operator++ (BaseIterator< T, I, reverse > &it, int)

    template<typename T, typename I, bool reverse>

  std::enable_if<!reverse, I >::type & operator-- (Baselterator< T, I, reverse > &it)
• template<typename T , typename I , bool reverse>
  std::enable_if< reverse, I >::type & operator-- (BaseIterator< T, I, reverse > &it)

    template<typename T , typename I , bool reverse>

  std::enable_if<!reverse, I >::type operator-- (Baselterator< T, I, reverse > &it, int)

    template<typename T , typename I , bool reverse>

  std::enable_if< reverse, I >::type operator-- (Baselterator< T, I, reverse > &it, int)
• template<typename T , typename I , bool r>
  bool operator== (const Baselterator< T, I, r > &i1, const Baselterator< T, I, r > &i2)

    template<typename T, typename I, bool r>

  bool operator!= (const Baselterator< T, I, r > &i1, const Baselterator< T, I, r > &i2)

    template<typename T , typename I , bool r>

  bool operator < (const Baselterator < T, I, r > &i1, const Baselterator < T, I, r > &i2)
```

### **Variables**

constexpr std::size\_t MAXINT = std::numeric\_limits<std::size\_t>::max()

## 11.39.1 Function Documentation

```
11.39.1.1 operator"!=() template<typename T , typename I , bool r>
bool carl::tree_detail::operator!= (
           const BaseIterator< T, I, r > & i1,
            const BaseIterator< T, I, r > & i2)
11.39.1.2 operator*() [1/2] template<typename T , typename I , bool r>
T& carl::tree_detail::operator* (
            BaseIterator< T, I, r > \& bi)
11.39.1.3 operator*() [2/2] template<typename T , typename I , bool r>
const T& carl::tree_detail::operator* (
            const BaseIterator< T, I, r > & bi)
11.39.1.4 operator++() [1/4] template<typename T , typename I , bool reverse>
std::enable_if<!reverse,I>::type& carl::tree_detail::operator++ (
            BaseIterator< T, I, reverse > & it )
11.39.1.5 operator++() [2/4] template<typename T , typename I , bool reverse>
std::enable_if<reverse,I>::type& carl::tree_detail::operator++ (
            BaseIterator< T, I, reverse > & it )
11.39.1.6 operator++() [3/4] template<typename T , typename I , bool reverse>
std::enable_if<!reverse,I>::type carl::tree_detail::operator++ (
            BaseIterator< T, I, reverse > & it,
            int )
```

```
11.39.1.7 operator++() [4/4] template<typename I , typename I , bool reverse>
std::enable_if<reverse,I>::type carl::tree_detail::operator++ (
            BaseIterator< T, I, reverse > & it,
            int )
11.39.1.8 operator--() [1/4] template<typename T , typename I , bool reverse>
std::enable_if<!reverse,I>::type& carl::tree_detail::operator-- (
            BaseIterator< T, I, reverse > & it )
11.39.1.9 operator--() [2/4] template<typename I , typename I , bool reverse>
std::enable_if<reverse,I>::type& carl::tree_detail::operator-- (
            BaseIterator< T, I, reverse > & it )
11.39.1.10 operator--()[3/4] template<typename T , typename I , bool reverse>
std::enable_if<!reverse,I>::type carl::tree_detail::operator-- (
             BaseIterator< T, I, reverse > & it,
             int )
11.39.1.11 operator--() [4/4] template<typename I , typename I , bool reverse>
std::enable_if<reverse,I>::type carl::tree_detail::operator-- (
             BaseIterator< T, I, reverse > & it,
             int )
11.39.1.12 operator<() template<typename T , typename I , bool r>
bool carl::tree_detail::operator< (</pre>
            const BaseIterator< T, I, r > & i1,
            const BaseIterator< T, I, r > & i2)
11.39.1.13 operator<<() template<typename T >
std::ostream& carl::tree_detail::operator<< (</pre>
            std::ostream & os,
            const Node < T > & n)
```

### 11.39.2 Variable Documentation

```
11.39.2.1 MAXINT constexpr std::size_t carl::tree_detail::MAXINT = std::numeric_limits<std↔ ::size_t>::max() [constexpr]
```

## 11.40 carl::vs Namespace Reference

# **Namespaces**

detail

## **Data Structures**

- · class Term
- struct zero

A square root expression with side conditions.

## **Typedefs**

```
    template<typename Poly >
        using ConstraintConjunction = std::vector< Constraint< Poly > >
        a vector of constraints
    template<typename Poly >
        using CaseDistinction = std::vector< ConstraintConjunction< Poly > >
        a vector of vectors of constraints
```

### **Enumerations**

• enum class TermType { NORMAL , PLUS\_EPSILON , MINUS\_INFINITY , PLUS\_INFINITY }

#### **Functions**

```
    template < typename Poly >
bool simplify_inplace (CaseDistinction < Poly > &cases)
```

Simplifies the case distinction in place.

template<typename Poly >
 std::optional< CaseDistinction< Poly > substitute (const Constraint< Poly > &cons, const Variable var, const Term< Poly > &term)

Applies a substitution to a constraint.

template<typename Poly >

static std::optional < std::variant < CaseDistinction < Poly >, VariableComparison < Poly > > substitute (const VariableComparison < Poly > &varcomp, const Variable var, const Term < Poly > &term)

Applies a substitution to a variable comparison.

template<class Poly >

```
std::ostream & operator<< (std::ostream &os, const Term< Poly > &s)
```

template<typename Poly >

```
std::ostream & operator<< (std::ostream &out, const zero< Poly > &z)
```

ullet template<typename Poly >

```
static bool gather_zeros (const Constraint< Poly > &constraint, const Variable &eliminationVar, std::vector< zero< Poly >> &results)
```

Gathers zeros with side conditions from the given constraint in the given variable.

template<typename Poly >
 static bool gather\_zeros (const VariableComparison< Poly > &varcomp, const Variable &eliminationVar, std
 ::vector< zero< Poly >> &results)

## 11.40.1 Typedef Documentation

```
11.40.1.1 CaseDistinction template<typename Poly >
using carl::vs::CaseDistinction = typedef std::vector<ConstraintConjunction<Poly> >
```

a vector of vectors of constraints

```
11.40.1.2 ConstraintConjunction template<typename Poly >
```

```
using carl::vs::ConstraintConjunction = typedef std::vector<Constraint<Poly> >
```

a vector of constraints

### 11.40.2 Enumeration Type Documentation

# 11.40.2.1 TermType enum carl::vs::TermType [strong]

#### Enumerator

| NORMAL         |  |
|----------------|--|
| PLUS_EPSILON   |  |
| MINUS_INFINITY |  |
| PLUS_INFINITY  |  |

### 11.40.3 Function Documentation

Gathers zeros with side conditions from the given constraint in the given variable.

```
11.40.3.2 gather_zeros() [2/2] template<typename Poly >
static bool carl::vs::gather_zeros (
            const VariableComparison< Poly > & varcomp,
             const Variable & eliminationVar,
             std::vector< zero< Poly >> & results ) [static]
11.40.3.3 operator <<() [1/2] template < class Poly >
std::ostream& carl::vs::operator<< (</pre>
             std::ostream & os,
             const Term< Poly > & s )
11.40.3.4 operator <<() [2/2] template < typename Poly >
std::ostream& carl::vs::operator<< (</pre>
            std::ostream & out,
             const zero < Poly > & z)
11.40.3.5 simplify_inplace() template<typename Poly >
bool carl::vs::simplify_inplace (
             CaseDistinction< Poly > & cases ) [inline]
```

Simplifies the case distinction in place.

## **Template Parameters**

#### **Parameters**

| cases | Case distiction to simplify. |
|-------|------------------------------|
|-------|------------------------------|

## Returns

true On success.

false Fail, cases is now invalid.

Applies a substitution to a constraint.

#### **Parameters**

| cons | The constraint to substitute in. |
|------|----------------------------------|
| subs | The substitution to apply.       |

### Returns

std::nullopt, if the upper limit in the number of combinations in the result of the substitution is exceeded. Note, that this hinders a combinatorial blow up. Thr substitution result, otherwise.

Applies a substitution to a variable comparison.

| varcomp | The variable comparison to substitute in. |
|---------|---|
| subs    | The substitution to apply.                |

#### Returns

std::nullopt, if the upper limit in the number of combinations in the result of the substitution is exceeded or the substitution cannot be applied. Note, that this hinders a combinatorial blow up. Thr substitution result, otherwise.

## 11.41 carl::vs::detail Namespace Reference

#### **Data Structures**

struct Substitution

### **Typedefs**

- using DoubleInterval = carl::Interval < double >
- using EvalDoubleIntervalMap = std::map< carl::Variable, DoubleInterval >

#### **Functions**

- template < class Poly > std::ostream & operator << (std::ostream &os, const Substitution < Poly > &s)
- template < class combineType >

bool combine (const std::vector< std::vector< combineType >> &\_toCombine, std::vector< std::vector< combineType >> &\_combination)

Combines vectors.

template<typename Poly > void simplify (CaseDistinction< Poly > &)

Simplifies a disjunction of conjunctions of constraints by deleting consistent constraint and inconsistent conjunctions of constraints.

template<typename Poly >

void simplify (CaseDistinction < Poly > &, carl::Variables &, const detail::EvalDoubleIntervalMap &)

Simplifies a disjunction of conjunctions of constraints by deleting consistent constraint and inconsistent conjunctions of constraints.

 $\bullet \ \ \text{template}{<} \text{typename Poly} >$ 

bool splitProducts (CaseDistinction < Poly > &, bool=false)

Splits all constraints in the given disjunction of conjunctions of constraints having a non-trivial factorization into a set of constraints which compare the factors instead.

• template<typename Poly >

bool splitProducts (const ConstraintConjunction< Poly > &, CaseDistinction< Poly > &, std::map< const Constraint< Poly >, CaseDistinction< Poly >> &, bool=false)

Splits all constraints in the given conjunction of constraints having a non-trivial factorization into a set of constraints which compare the factors instead.

template<typename Poly >

```
CaseDistinction < Poly > splitProducts (const Constraint < Poly > &, bool=false)
```

Splits the given constraint into a set of constraints which compare the factors of the factorization of the constraints considered polynomial.

 $\bullet \ \ {\sf template}{<} {\sf typename Poly}>$ 

void splitSosDecompositions (CaseDistinction < Poly > &)

• template<typename Poly >

```
CaseDistinction < Poly > getSignCombinations (const Constraint < Poly > &)
```

For a given constraint  $f_-1*...*f_-n \sim 0$  this method computes all combinations of constraints  $f_-1 \sim _-10...$ 

void getOddBitStrings (size\_t \_length, std::vector< std::bitset< MAX\_PRODUCT\_SPLIT\_NUMBER > > &\_←
 strings)

- void getEvenBitStrings (size\_t \_length, std::vector< std::bitset< MAX\_PRODUCT\_SPLIT\_NUMBER >> &←
   \_strings)
- template<typename Poly >

void print (CaseDistinction< Poly > &\_substitutionResults)

Prints the given disjunction of conjunction of constraints.

template<typename Poly >

bool substitute (const Constraint< Poly > &, const Substitution< Poly > &, CaseDistinction< Poly > &, bool \_accordingPaper, carl::Variables &, const detail::EvalDoubleIntervalMap &)

Applies a substitution to a constraint and stores the results in the given vector.

template<typename Poly >

bool substituteNormal (const Constraint< Poly > &\_cons, const Substitution< Poly > &\_subs, CaseDistinction< Poly > &\_result, bool \_accordingPaper, carl::Variables &\_conflictingVariables, const detail::EvalDoubleIntervalMap &\_solutionSpace)

Applies a substitution of a variable to a term, which is not minus infinity nor a to an square root expression plus an infinitesimal.

template<typename Poly >

bool substituteNormalSqrtEq (const Poly &\_radicand, const Poly &\_q, const Poly &\_r, CaseDistinction< Poly > &\_result, bool \_accordingPaper)

Sub-method of substituteNormalSqrt, where applying the substitution led to a term containing a square root.

template<typename Poly >

bool substituteNormalSqrtNeq (const Poly &\_radicand, const Poly &\_q, const Poly &\_r, CaseDistinction < Poly > &\_result, bool \_accordingPaper)

Sub-method of substituteNormalSqrt, where applying the substitution led to a term containing a square root.

template<typename Poly >

bool substituteNormalSqrtLess (const Poly &\_radicand, const Poly &\_q, const Poly &\_r, const Poly &\_ expected struction and substituteNormalSqrtLess (const Poly &\_radicand, const Poly &\_q, const Poly &\_r, const Poly &\_ expected structures are substituteNormalSqrtLess (const Poly &\_radicand, const Poly &\_q, const Poly &\_r, const Poly &\_expected structures are substituteNormalSqrtLess (const Poly &\_radicand, const Poly &\_q, const Poly &\_r, const Poly &\_expected structures are substituteNormalSqrtLess (const Poly &\_radicand, const Poly &\_q, const Poly &\_r, const Poly &\_expected structures are substituteNormalSqrtLess (const Poly &\_radicand, const Poly &\_q, const Poly &\_r, const Poly &\_expected structures are substituteNormalSqrtLess (const Poly &\_radicand, const Poly &\_radic

Sub-method of substituteNormalSqrt, where applying the substitution led to a term containing a square root.

• template<typename Poly >

bool substituteNormalSqrtLeq (const Poly &\_radicand, const Poly &\_q, const Poly &\_r, const Poly &\_ s, CaseDistinction < Poly > &\_result, bool \_accordingPaper)

Sub-method of substituteNormalSqrt, where applying the substitution led to a term containing a square root.

template<typename Poly >

bool substitutePlusEps (const Constraint< Poly > &\_cons, const Substitution< Poly > &\_subs, CaseDistinction< Poly > &\_result, bool \_accordingPaper, carl::Variables &\_conflictingVariables, const detail::EvalDoubleIntervalMap &\_solutionSpace)

Applies the given substitution to the given constraint, where the substitution is of the form [x -> t + epsilon] with x as the variable and c and b polynomials in the real theory excluding x.

template<typename Poly >

bool substituteEpsGradients (const Constraint< Poly > &\_cons, const Substitution< Poly > &\_subs, const carl::Relation \_relation, CaseDistinction< Poly > &, bool \_accordingPaper, carl::Variables &\_conflicting \( \times \) Variables, const detail::EvalDoubleIntervalMap &\_solutionSpace)

Sub-method of substituteEps, where one of the gradients in the point represented by the substitution must be negative if the given relation is less or positive if the given relation is greater.

template<typename Poly >

void substituteInf (const Constraint< Poly > &\_cons, const Substitution< Poly > &\_subs, CaseDistinction< Poly > &\_result, carl::Variables &\_conflictingVariables, const detail::EvalDoubleIntervalMap &\_solutionSpace)

Applies the given substitution to the given constraint, where the substitution is of the form [x -> -infinity] with x as the variable and c and b polynomials in the real theory excluding x.

template<typename Poly >

void substituteInfLessGreater (const Constraint< Poly > &\_cons, const Substitution< Poly > &\_subs, CaseDistinction< Poly > &\_result)

Applies the given substitution to the given constraint, where the substitution is of the form [x -> +/-infinity] with x as the variable and c and b polynomials in the real theory excluding x.

template<typename Poly >

void substitute TrivialCase (const Constraint< Poly > &\_cons, const Substitution< Poly > &\_subs, CaseDistinction< Poly > &\_result) Deals with the case, that the left hand side of the constraint to substitute is a trivial polynomial in the variable to substitute.

• template<typename Poly >

void substituteNotTrivialCase (const Constraint< Poly > &, const Substitution< Poly > &, CaseDistinction< Poly > &)

Deals with the case, that the left hand side of the constraint to substitute is not a trivial polynomial in the variable to substitute.

## 11.41.1 Typedef Documentation

```
11.41.1.1 DoubleInterval using carl::vs::detail::DoubleInterval = typedef carl::Interval < double >
```

```
11.41.1.2 EvalDoubleIntervalMap using carl::vs::detail::EvalDoubleIntervalMap = typedef std← ::map<carl::Variable, DoubleInterval>
```

#### 11.41.2 Function Documentation

#### Combines vectors.

#### **Parameters**

| _toCombine   | The vectors to combine.    |
|--------------|----------------------------|
| ₋combination | The resulting combination. |

### Returns

false, if the upper limit in the number of combinations resulting by this method is exceeded. Note, that this hinders a combinatorial blow up. true, otherwise.

#### **Parameters**

| ₋length  | The maximal length of the bit strings with even parity to compute.         |
|----------|--|
| ₋strings | All bit strings of length less or equal the given length with even parity. |

### **Parameters**

|   | ₋length  | The maximal length of the bit strings with odd parity to compute.         |
|---|----------|---|
| ſ | ₋strings | All bit strings of length less or equal the given length with odd parity. |

For a given constraint f\_1\*...\*f\_n  $\sim$  0 this method computes all combinations of constraints f\_1  $\sim$ \_1 0 ...

 $f_n \sim_n 0$  such that

```
f_1 ~_1 0 and ... and f_n ~_n 0 iff f_1*...*f_n ~ 0
```

holds.

### **Parameters**

| _constraint | A pointer to the constraint to split this way. |
|-------------|--|
|-------------|--|

### **Returns**

The resulting combinations.

Prints the given disjunction of conjunction of constraints.

#### **Parameters**

| _substitutionResults | The disjunction of conjunction of constraints to print. |
|----------------------|---|
|----------------------|---|

Simplifies a disjunction of conjunctions of constraints by deleting consistent constraint and inconsistent conjunctions of constraints.

If a conjunction of only consistent constraints exists, the simplified disjunction contains one empty conjunction.

#### **Parameters**

| _tosimplify   The disjunction of conjunctions to simplify | _toSimplify | The disjunction of conjunctions to simplify. |
|---|-------------|--|
|---|-------------|--|

Simplifies a disjunction of conjunctions of constraints by deleting consistent constraint and inconsistent conjunctions of constraints.

If a conjunction of only consistent constraints exists, the simplified disjunction contains one empty conjunction.

### **Parameters**

| _toSimplify      | The disjunction of conjunctions to simplify. |
|------------------|--|
| _conflictingVars |  |
| ₋solutionSpace   |  |

Splits all constraints in the given disjunction of conjunctions of constraints having a non-trivial factorization into a set of constraints which compare the factors instead.

#### **Parameters**

| _toSimplify | The disjunction of conjunctions of the constraints to split.                   |
|-------------|--|
| ₋onlyNeq    | A flag indicating that only constraints with the relation symbol != are split. |

#### Returns

false, if the upper limit in the number of combinations resulting by this method is exceeded. Note, that this hinders a combinatorial blow up. true, otherwise.

Splits the given constraint into a set of constraints which compare the factors of the factorization of the constraints considered polynomial.

#### **Parameters**

| _constraint | A pointer to the constraint to split.  |
|-------------|--|
| ₋onlyNeq    | A flag indicating that only constraints with the relation symbol != are split. |

## Returns

The resulting disjunction of conjunctions of constraints, which is semantically equivalent to the given constraint.

Splits all constraints in the given conjunction of constraints having a non-trivial factorization into a set of constraints which compare the factors instead.

| _toSimplify | The conjunction of the constraints to split.                                   |
|-------------|--|
| ₋result     | The result, being a disjunction of conjunctions of constraints.                |
| ₋onlyNeq    | A flag indicating that only constraints with the relation symbol != are split. |

#### Returns

false, if the upper limit in the number of combinations resulting by this method is exceeded. Note, that this hinders a combinatorial blow up. true, otherwise.

Applies a substitution to a constraint and stores the results in the given vector.

#### **Parameters**

| _cons   | The constraint to substitute in.                                |
|---------|---|
| ₋subs   | The substitution to apply.                                      |
| ₋result | The vector, in which to store the results of this substitution. |

### Returns

false, if the upper limit in the number of combinations in the result of the substitution is exceeded. Note, that this hinders a combinatorial blow up. true, otherwise.

Sub-method of substituteEps, where one of the gradients in the point represented by the substitution must be negative if the given relation is less or positive if the given relation is greater.

#### **Parameters**

| _cons                 | The constraint to substitute in.  |
|-----------------------|---|
| _subs                 | The substitution to apply.  |
| ₋relation             | The relation symbol, deciding whether the substitution result must be negative or positive.   |
| _result               | The vector, in which to store the results of this substitution. It is semantically a disjunction of conjunctions of constraints.  |
| _accordingPaper       | A flag that indicates whether to apply the virtual substitution rules according to the paper "Quantifier elimination for real algebra - the quadratic case and beyond." by Volker Weispfenning (true) or in an adapted way which omits a higher degree in the result by splitting the result in more cases (false). |
| _conflictingVariables | If a conflict with the given solution space occurs, the variables being part of this conflict are stored in this container.   |
| ₋solutionSpace        | The solution space in form of double intervals of the variables occurring in the given constraint.  |

Applies the given substitution to the given constraint, where the substitution is of the form [x -> -infinity] with x as the variable and c and b polynomials in the real theory excluding x.

The constraint is of the form "f(x) \rho 0" with \rho element of  $\{=,!=,<,>,<=,>=\}$  and k as the maximum degree of x in f.

| _cons                 | The constraint to substitute in.   |
|-----------------------|--|
| ₋subs                 | The substitution to apply.   |
| _result               | The vector, in which to store the results of this substitution. It is semantically a disjunction of conjunctions of constraints. |
| _conflictingVariables | If a conflict with the given solution space occurs, the variables being part of this conflict are stored in this container.      |
| ₋solutionSpace        | The solution space in form of double intervals of the variables occurring in the given constraint.                               |

Applies the given substitution to the given constraint, where the substitution is of the form [x -> +/-infinity] with x as the variable and c and b polynomials in the real theory excluding x.

The constraint is of the form " $a*x^2+bx+c$  \rho 0", where \rho is less or greater.

#### **Parameters**

| _cons   | The constraint to substitute in.   |
|---------|--|
| ₋subs   | The substitution to apply.   |
| _result | The vector, in which to store the results of this substitution. It is semantically a disjunction of conjunctions of constraints. |

Applies a substitution of a variable to a term, which is not minus infinity nor a to an square root expression plus an infinitesimal.

#### **Parameters**

| _cons                 | The constraint to substitute in.  |
|-----------------------|---|
| _subs                 | The substitution to apply.  |
| _result               | The vector, in which to store the results of this substitution. It is semantically a disjunction of conjunctions of constraints.  |
| _accordingPaper       | A flag that indicates whether to apply the virtual substitution rules according to the paper "Quantifier elimination for real algebra - the quadratic case and beyond." by Volker Weispfenning (true) or in an adapted way which omits a higher degree in the result by splitting the result in more cases (false). |
| _conflictingVariables | If a conflict with the given solution space occurs, the variables being part of this conflict are stored in this container.   |
| ₋solutionSpace        | The solution space in form of double intervals of the variables occurring in the given constraint.  |

```
11.41.2.18 substituteNormalSqrtEq() template<typename Poly >
```

Sub-method of substituteNormalSqrt, where applying the substitution led to a term containing a square root.

The relation symbol of the constraint to substitute is "=".

```
(_q+_r*sqrt(_radicand))
```

The term then looks like: -----\_s

### **Parameters**

| ₋radicand       | The radicand of the square root.  |
|-----------------|---|
| _ <b>q</b>      | The summand not containing the square root.   |
| _r              | The coefficient of the radicand.  |
| _result         | The vector, in which to store the results of this substitution. It is semantically a disjunction of conjunctions of constraints.  |
| _accordingPaper | A flag that indicates whether to apply the virtual substitution rules according to the paper "Quantifier elimination for real algebra - the quadratic case and beyond." by Volker Weispfenning (true) or in an adapted way which omits a higher degree in the result by splitting the result in more cases (false). |

# $\textbf{11.41.2.19} \quad \textbf{substituteNormalSqrtLeq()} \quad \texttt{template} < \texttt{typename Poly} >$

Sub-method of substituteNormalSqrt, where applying the substitution led to a term containing a square root.

The relation symbol of the constraint to substitute is less or equal.

```
(_q+_r*sqrt(_radicand))
```

The term then looks like: -----\_\_s

| ₋radicand       | The radicand of the square root.  |
|-----------------|---|
| _ <b>q</b>      | The summand not containing the square root.   |
| _r              | The coefficient of the radicand.  |
| _S              | The denominator of the expression containing the square root.   |
| _result         | The vector, in which to store the results of this substitution. It is semantically a disjunction of conjunctions of constraints.  |
| _accordingPaper | A flag that indicates whether to apply the virtual substitution rules according to the paper "Quantifier elimination for real algebra - the quadratic case and beyond." by Volker Weispfenning (true) or in an adapted way which omits a higher degree in the result by splitting the result in more cases (false). |

Sub-method of substituteNormalSqrt, where applying the substitution led to a term containing a square root.

The relation symbol of the constraint to substitute is less.

```
(_q+_r*sqrt(_radicand))
```

The term then looks like: -----\_\_s

#### **Parameters**

| ₋radicand       | The radicand of the square root.  |
|-----------------|---|
| _ <b>q</b>      | The summand not containing the square root.   |
| _r              | The coefficient of the radicand.  |
| _\$             | The denominator of the expression containing the square root.   |
| _result         | The vector, in which to store the results of this substitution. It is semantically a disjunction of conjunctions of constraints.  |
| _accordingPaper | A flag that indicates whether to apply the virtual substitution rules according to the paper "Quantifier elimination for real algebra - the quadratic case and beyond." by Volker Weispfenning (true) or in an adapted way which omits a higher degree in the result by splitting the result in more cases (false). |

## 11.41.2.21 substituteNormalSqrtNeq() template<typename Poly >

Sub-method of substituteNormalSqrt, where applying the substitution led to a term containing a square root.

The relation symbol of the constraint to substitute is "!=".

```
(\_q+\_r*sqrt(\_radicand))
```

The term then looks like: -----\_\_\_s

| ₋radicand | The radicand of the square root.            |
|-----------|---|
| _q        | The summand not containing the square root. |
| _r        | The coefficient of the radicand.            |

#### **Parameters**

| ₋result         | The vector, in which to store the results of this substitution. It is semantically a disjunction of conjunctions of constraints.  |
|-----------------|---|
| _accordingPaper | A flag that indicates whether to apply the virtual substitution rules according to the paper "Quantifier elimination for real algebra - the quadratic case and beyond." by Volker Weispfenning (true) or in an adapted way which omits a higher degree in the result by splitting the result in more cases (false). |

Deals with the case, that the left hand side of the constraint to substitute is not a trivial polynomial in the variable to substitute.

The constraints left hand side then should looks like: ax^2+bx+c

#### **Parameters**

| _cons   | The constraint to substitute in.   |
|---------|--|
| ₋subs   | The substitution to apply.   |
| ₋result | The vector, in which to store the results of this substitution. It is semantically a disjunction of conjunctions of constraints. |

Applies the given substitution to the given constraint, where the substitution is of the form [x -> t + epsilon] with x as the variable and c and b polynomials in the real theory excluding x.

The constraint is of the form "f(x) \rho 0" with \rho element of  $\{=,!=,<,>,<=,>=\}$  and k as the maximum degree of x in f.

| _cons   | The constraint to substitute in.   |
|---------|--|
| ₋subs   | The substitution to apply.   |
| ₋result | The vector, in which to store the results of this substitution. It is semantically a disjunction of conjunctions of constraints. |

#### **Parameters**

| _accordingPaper       | A flag that indicates whether to apply the virtual substitution rules according to the paper "Quantifier elimination for real algebra - the quadratic case and beyond." by Volker Weispfenning (true) or in an adapted way which omits a higher degree in the result by splitting the result in more cases (false). |
|-----------------------|---|
| _conflictingVariables | If a conflict with the given solution space occurs, the variables being part of this conflict are stored in this container.   |
| ₋solutionSpace        | The solution space in form of double intervals of the variables occurring in the given constraint.  |

Deals with the case, that the left hand side of the constraint to substitute is a trivial polynomial in the variable to substitute.

The constraints left hand side then should look like:  $ax^2+bx+c$ 

#### **Parameters**

| _cons   | The constraint to substitute in.   |
|---------|--|
| ₋subs   | The substitution to apply.   |
| ₋result | The vector, in which to store the results of this substitution. It is semantically a disjunction of conjunctions of constraints. |

## 12 Data Structure Documentation

## 12.1 carl::AbstractGBProcedure < Polynomial > Class Template Reference

```
#include <GBProcedure.h>
```

### **Public Member Functions**

- virtual ~AbstractGBProcedure ()=default
- virtual void addPolynomial (const Polynomial &p)=0
- virtual void reset ()=0
- virtual void calculate ()=0
- virtual std::list< std::pair< BitVector, BitVector >> reduceInput ()=0
- virtual const Ideal
   Polynomial > & getIdeal () const =0

## 12.1.1 Constructor & Destructor Documentation

```
12.1.1.1 ~AbstractGBProcedure() template<typename Polynomial > virtual carl::AbstractGBProcedure< Polynomial >::~AbstractGBProcedure () [virtual], [default]
```

#### 12.1.2 Member Function Documentation

```
12.1.2.1 addPolynomial() template<typename Polynomial > virtual void carl::AbstractGBProcedure< Polynomial >::addPolynomial ( const Polynomial & p) [pure virtual]
```

Implemented in carl::GBProcedure < Polynomial, Procedure, AddingPolynomialPolicy >.

```
12.1.2.2 calculate() template<typename Polynomial >
virtual void carl::AbstractGBProcedure< Polynomial >::calculate ( ) [pure virtual]
```

Implemented in carl::GBProcedure < Polynomial, Procedure, AddingPolynomialPolicy >.

```
12.1.2.3 getIdeal() template<typename Polynomial > virtual const Ideal<Polynomial>& carl::AbstractGBProcedure< Polynomial >::getIdeal ( ) const [pure virtual]
```

Implemented in carl::GBProcedure < Polynomial, Procedure, AddingPolynomialPolicy >.

```
12.1.2.4 reduceInput() template<typename Polynomial >
virtual std::list<std::pair<BitVector, BitVector> > carl::AbstractGBProcedure< Polynomial
>::reduceInput () [pure virtual]
```

Implemented in carl::GBProcedure < Polynomial, Procedure, AddingPolynomialPolicy >.

```
12.1.2.5 reset() template<typename Polynomial > virtual void carl::AbstractGBProcedure< Polynomial >::reset ( ) [pure virtual]
```

Implemented in carl::GBProcedure < Polynomial, Procedure, AddingPolynomialPolicy >.

# 12.2 carl::all< T > Struct Template Reference

Meta-logical conjunction.

```
#include <SFINAE.h>
```

## 12.2.1 Detailed Description

```
template<typename... T> struct carl::all< T>
```

Meta-logical conjunction.

## 12.3 carl::all< Head, Tail... > Struct Template Reference

```
#include <SFINAE.h>
```

## 12.4 carl::any< T > Struct Template Reference

Meta-logical disjunction.

```
#include <SFINAE.h>
```

### 12.4.1 Detailed Description

```
template<typename... T> struct carl::any< T >
```

Meta-logical disjunction.

## 12.5 carl::any< Head, Tail... > Struct Template Reference

```
#include <SFINAE.h>
```

# 12.6 carl::tree\_detail::Baselterator< T, Iterator, reverse > Struct Template Reference

This is the base class for all iterators.

```
#include <carlTree.h>
```

## **Public Member Functions**

- const auto & nodes () const
- const auto & node (std::size\_t id) const
- const auto & curnode () const
- Baselterator (const Baselterator &ii)=default
- Baselterator (Baselterator &&ii) noexcept=default
- template<typename lt , bool r>
- Baselterator (const Baselterator< T, It, r > &ii)
- Baselterator & operator= (const Baselterator &ii)=default
- Baselterator & operator= (Baselterator &&ii) noexcept=default
- std::size\_t depth () const
- std::size\_t id () const
- bool isRoot () const
- bool isValid () const
- T \* operator-> ()
- T const \* operator-> () const

### **Data Fields**

std::size\_t current

#### **Protected Member Functions**

Baselterator (const tree< T > \*t, std::size\_t root)

### **Protected Attributes**

const tree< T > \* mTree

### **Friends**

 template<typename TT , typename It , bool rev> struct BaseIterator

## 12.6.1 Detailed Description

```
template<typename T, typename Iterator, bool reverse>
struct carl::tree_detail::BaseIterator< T, Iterator, reverse>
```

This is the base class for all iterators.

It takes care of correct implementation of all operators and reversion.

An actual iterator T<reverse> only has to

- inherit from BaseIterator<T, reverse>,
- provide appropriate constructors,
- implement next() and previous(). If the iterator supports only forward iteration, it omits the template argument, inherits from BaseIterator<T, false> and does not implement previous().

### 12.6.2 Constructor & Destructor Documentation

```
12.6.2.2 Baselterator() [2/4] template<typename T , typename Iterator , bool reverse>
carl::tree_detail::BaseIterator< T, Iterator, reverse >::BaseIterator (
             const BaseIterator<br/>< T, Iterator, reverse > & ii ) [default]
12.6.2.3 Baselterator()[3/4] template<typename T , typename Iterator , bool reverse>
carl::tree_detail::BaseIterator< T, Iterator, reverse >::BaseIterator (
             BaseIterator< T, Iterator, reverse > && ii ) [default], [noexcept]
12.6.2.4 Baselterator() [4/4] template<typename T , typename Iterator , bool reverse>
template<typename It , bool r>
carl::tree_detail::BaseIterator< T, Iterator, reverse >::BaseIterator (
             const BaseIterator< T, It, r > & ii) [inline]
12.6.3 Member Function Documentation
12.6.3.1 curnode() template<typename T , typename Iterator , bool reverse>
const auto& carl::tree_detail::BaseIterator< T, Iterator, reverse >::curnode ( ) const [inline]
12.6.3.2 depth() template<typename T , typename Iterator , bool reverse>
std::size_t carl::tree_detail::BaseIterator< T, Iterator, reverse >::depth ( ) const [inline]
12.6.3.3 id() template<typename T , typename Iterator , bool reverse>
std::size_t carl::tree_detail::BaseIterator< T, Iterator, reverse >::id ( ) const [inline]
12.6.3.4 isRoot() template<typename T , typename Iterator , bool reverse>
bool carl::tree_detail::BaseIterator< T, Iterator, reverse >::isRoot ( ) const [inline]
\textbf{12.6.3.5} \quad \textbf{isValid()} \quad \texttt{template} < \texttt{typename T} \text{ , typename Iterator , bool reverse} >
bool carl::tree_detail::BaseIterator< T, Iterator, reverse >::isValid ( ) const [inline]
```

```
12.6.3.6 node() template<typename T , typename Iterator , bool reverse>
const auto& carl::tree_detail::BaseIterator< T, Iterator, reverse >::node (
            std::size_t id ) const [inline]
12.6.3.7 nodes() template<typename T , typename Iterator , bool reverse>
const auto& carl::tree_detail::BaseIterator< T, Iterator, reverse >::nodes () const [inline]
12.6.3.8 operator->()[1/2] template<typename T , typename Iterator , bool reverse>
T* carl::tree_detail::BaseIterator< T, Iterator, reverse >::operator-> ( ) [inline]
12.6.3.9 operator->() [2/2] template<typename T , typename Iterator , bool reverse>
T const* carl::tree_detail::BaseIterator< T, Iterator, reverse >::operator-> ( ) const [inline]
12.6.3.10 operator=() [1/2] template<typename T , typename Iterator , bool reverse>
BaseIterator& carl::tree_detail::BaseIterator< T, Iterator, reverse >::operator= (
            BaseIterator< T, Iterator, reverse > && ii ) [default], [noexcept]
12.6.3.11 operator=() [2/2] template<typename T , typename Iterator , bool reverse>
BaseIterator& carl::tree_detail::BaseIterator< T, Iterator, reverse >::operator= (
            const BaseIterator< T, Iterator, reverse > & ii ) [default]
12.6.4 Friends And Related Function Documentation
12.6.4.1 Baselterator template<typename T , typename Iterator , bool reverse>
template<typename TT , typename It , bool rev>
friend struct BaseIterator [friend]
12.6.5 Field Documentation
```

12.6.5.1 current template<typename T , typename Iterator , bool reverse> std::size.t carl::tree\_detail::BaseIterator< T, Iterator, reverse >::current

```
12.6.5.2 mTree template<typename T , typename Iterator , bool reverse> const tree<T>* carl::tree_detail::BaseIterator< T, Iterator, reverse >::mTree [protected]
```

## 12.7 carl::BaseRepresentation < Number > Struct Template Reference

```
#include <MultiplicationTable.h>
```

## **Public Types**

using Monomial = Term< Number >

### **Public Member Functions**

- BaseRepresentation ()=default
- BaseRepresentation (const std::vector< Monomial > &base, const MultivariatePolynomial< Number > &p)
- bool is\_zero () const
- · bool contains (uint i) const
- Number get (uint index) const

### **Data Fields**

K keys

STL member.

• T elements

STL member.

### 12.7.1 Member Typedef Documentation

```
12.7.1.1 Monomial template<typename Number > using carl::BaseRepresentation< Number >::Monomial = Term<Number>
```

### 12.7.2 Constructor & Destructor Documentation

```
12.7.2.1 BaseRepresentation() [1/2] template<typename Number > carl::BaseRepresentation
Number >::BaseRepresentation ( ) [default]
```

## 12.7.3 Member Function Documentation

```
12.7.3.1 contains() template<typename Number >
bool carl::BaseRepresentation< Number >::contains (
            uint i ) const [inline]
12.7.3.2 get() template<typename Number >
Number carl::BaseRepresentation< Number >::get (
            uint index ) const [inline]
12.7.3.3 is_zero() template<typename Number >
bool carl::BaseRepresentation< Number >::is_zero ( ) const [inline]
12.7.4 Field Documentation
12.7.4.1 elements T std::map< K, T >::elements [inherited]
STL member.
12.7.4.2 keys K std::map< K, T >::keys [inherited]
STL member.
```

# 12.8 carl::BasicConstraint< Pol > Class Template Reference

Represent a polynomial (in)equality against zero.

```
#include <BasicConstraint.h>
```

#### **Public Member Functions**

- BasicConstraint (bool is\_true)
- BasicConstraint (const Pol &lhs, const Relation rel)
- · BasicConstraint (Pol &&lhs, const Relation rel)
- const Pol & Ihs () const
- void set\_lhs (Pol &&lhs)
- Relation relation () const
- void set\_relation (Relation rel)
- size\_t hash () const
- bool is\_trivial\_true () const
- bool is\_trivial\_false () const
- unsigned is\_consistent () const
- BasicConstraint< Pol > negation () const

### 12.8.1 Detailed Description

```
template<typename Pol> class carl::BasicConstraint< Pol>
```

Represent a polynomial (in)equality against zero.

Such an (in)equality can be seen as an atomic formula/atom for the theory of real arithmetic.

#### 12.8.2 Constructor & Destructor Documentation

### 12.8.3 Member Function Documentation

```
12.8.3.1 hash() template<typename Pol >
size_t carl::BasicConstraint< Pol >::hash ( ) const [inline]
```

#### Returns

A hash value for this constraint.

```
12.8.3.2 is_consistent() template<typename Pol >
unsigned carl::BasicConstraint<< Pol >::is_consistent ( ) const [inline]

12.8.3.3 is_trivial_false() template<typename Pol >
bool carl::BasicConstraint<< Pol >::is_trivial_false ( ) const [inline]

12.8.3.4 is_trivial_true() template<typename Pol >
bool carl::BasicConstraint<< Pol >::is_trivial_true ( ) const [inline]
```

const Pol& carl::BasicConstraint< Pol >::lhs ( ) const [inline]

#### Returns

The considered polynomial being the left-hand side of this constraint. Hence, the right-hand side of any constraint is always 0.

```
12.8.3.6 negation() template<typename Pol >
BasicConstraint<Pol> carl::BasicConstraint< Pol>::negation () const [inline]
```

```
12.8.3.7 relation() template<typename Pol >
Relation carl::BasicConstraint< Pol >::relation ( ) const [inline]
```

### Returns

The relation symbol of this constraint.

12.8.3.5 lhs() template<typename Pol >

#### Returns

The considered polynomial being the left-hand side of this constraint. Hence, the right-hand side of any constraint is always 0.

#### Returns

The relation symbol of this constraint.

## 12.9 carl::settings::binary\_quantity Struct Reference

Helper type to parse quantities with binary SI-style suffixes.

```
#include <settings_utils.h>
```

### **Public Member Functions**

- constexpr binary\_quantity ()=default
- constexpr binary\_quantity (std::size\_t n)
- constexpr auto n () const
- · constexpr auto kibi () const
- · constexpr auto mebi () const
- · constexpr auto gibi () const
- · constexpr auto tebi () const
- · constexpr auto pebi () const
- · constexpr auto exbi () const

## 12.9.1 Detailed Description

Helper type to parse quantities with binary SI-style suffixes.

Intended usage:

- · use boost to parse values as quantity
- access values with q.mibi()

### 12.9.2 Constructor & Destructor Documentation

#include <Bitset.h>

```
12.9.2.1 binary_quantity() [1/2] constexpr carl::settings::binary_quantity::binary_quantity ( )
[constexpr], [default]
12.9.2.2 binary_quantity() [2/2] constexpr carl::settings::binary_quantity::binary_quantity (
             std::size\_t n) [inline], [explicit], [constexpr]
12.9.3 Member Function Documentation
12.9.3.1 exbi() constexpr auto carl::settings::binary_quantity::exbi ( ) const [inline], [constexpr]
12.9.3.2 gibi() constexpr auto carl::settings::binary_quantity::gibi ( ) const [inline], [constexpr]
12.9.3.3 kibi() constexpr auto carl::settings::binary_quantity::kibi ( ) const [inline], [constexpr]
12.9.3.4 mebi() constexpr auto carl::settings::binary.quantity::mebi () const [inline], [constexpr]
12.9.3.5 n() constexpr auto carl::settings::binary_quantity::n ( ) const [inline], [constexpr]
12.9.3.6 pebi() constexpr auto carl::settings::binary-quantity::pebi ( ) const [inline], [constexpr]
12.9.3.7 tebi() constexpr auto carl::settings::binary_quantity::tebi ( ) const [inline], [constexpr]
12.10 carl::Bitset Class Reference
This class is a simple wrapper around boost::dynamic_bitset.
```

#### **Data Structures**

· struct iterator

Iterate for iterate over all bits of a Bitset that are set to true.

### **Public Types**

using BaseType = boost::dynamic\_bitset<>
 Underlying storage type.

#### **Public Member Functions**

• Bitset (bool defaultValue=false)

Create an empty bitset.

Bitset (BaseType &&base, bool defaultValue)

Create a bitset from a BaseType object.

Bitset (const std::initializer\_list< std::size\_t > &bits, bool defaultValue=false)

Create a bitset from a list of bits indices that shall be set to true.

auto resize (std::size\_t num\_bits, bool value) const

Resize the Bitset to hold at least num\_bits bits. New bits are set to the given value.

• auto resize (std::size\_t num\_bits) const

Resize the Bitset to hold at least num\_bits bits. New bits are set to mDefault.

• Bitset & operator-= (const Bitset &rhs)

Sets all bits to false that are true in rhs.

• Bitset & operator&= (const Bitset &rhs)

Computes the bitwise and with rhs.

Bitset & operator = (const Bitset &rhs)

Computes the bitwise or with rhs.

• Bitset & set (std::size\_t n, bool value=true)

Sets the given bit to a value, true by default.

• Bitset & set\_interval (std::size\_t start, std::size\_t end, bool value=true)

Sets the a range of bits to a value, true by default.

Bitset & reset (std::size\_t n)

Resets a bit to false.

• bool test (std::size\_t n) const

Retrieves the value of the given bit.

· bool any () const

Checks if any bits are set to true. Asserts that mDefault is false.

• bool none () const

Checks if no bits are set to true. Asserts that mDefault is false.

· auto count () const noexcept

Counts the number of bits that are set to true. Asserts that mDefault is false.

• auto size () const

Retrieves the size of mData.

• auto num\_blocks () const

Retrieves the number of blocks used to store mData.

auto is\_subset\_of (const Bitset &rhs) const

Checks wether the bits set is a subset of the bits set in rhs.

std::size\_t find\_first () const

Retrieves the index of the first bit that is set to true.

std::size\_t find\_next (std::size\_t pos) const

Retrieves the index of the first bit set to true after the given position.

· iterator begin () const

Returns an iterator to the first bit that is set to true.

iterator end () const

Returns an past-the-end iterator.

### Static Public Attributes

• static constexpr auto npos = BaseType::npos

Sentinel element for iteration.

static constexpr auto bits\_per\_block = BaseType::bits\_per\_block

Number of bits in each storage block.

#### Friends

- struct std::hash< carl::Bitset >
- void alignSize (const Bitset &lhs, const Bitset &rhs)

Ensures that the explicitly stored bits of lhs and rhs have the same size.

bool operator== (const Bitset &lhs, const Bitset &rhs)

Compares Ihs and rhs.

bool operator< (const Bitset &lhs, const Bitset &rhs)</li>

Compares Ihs and rhs according to some order.

Bitset operator 
 ~ (const Bitset &lhs)

Returns the bitwise negation of lhs.

Bitset operator& (const Bitset &lhs, const Bitset &rhs)

Returns the bitwise and of lhs and rhs.

• Bitset operator (const Bitset &lhs, const Bitset &rhs)

Returns the bitwise or of lhs and rhs.

std::ostream & operator<< (std::ostream &os, const Bitset &b)</li>

Outputs b to os using the format <explicit bits>[<default>].

## 12.10.1 Detailed Description

This class is a simple wrapper around boost::dynamic\_bitset.

Its purpose is to allow for on-the-fly resizing of the bitset. Formally, a Bitset object represents an infinite bitset that starts with the bits stored in mData extended by mDefault. Whenever a bit is written that is not yet stored explicitly in mData or two Bitset objects with different mData sizes are involved, the size of mData is expanded transparently.

Note that some operations only make sense for a certain value of mDefault. For example, any () or none () require mDefault to be false.

## 12.10.2 Member Typedef Documentation

```
12.10.2.1 BaseType using carl::Bitset::BaseType = boost::dynamic.bitset<>
```

Underlying storage type.

## 12.10.3 Constructor & Destructor Documentation

```
12.10.3.1 Bitset() [1/3] carl::Bitset::Bitset (

bool defaultValue = false ) [inline], [explicit]
```

Create an empty bitset.

```
12.10.3.2 Bitset() [2/3] carl::Bitset::Bitset (

BaseType && base,

bool defaultValue) [inline]
```

Create a bitset from a BaseType object.

Create a bitset from a list of bits indices that shall be set to true.

## 12.10.4 Member Function Documentation

```
12.10.4.1 any() bool carl::Bitset::any ( ) const [inline]
```

Checks if any bits are set to true. Asserts that mDefault is false.

```
12.10.4.2 begin() iterator carl::Bitset::begin ( ) const [inline]
```

Returns an iterator to the first bit that is set to true.

```
12.10.4.3 count() auto carl::Bitset::count ( ) const [inline], [noexcept]
```

Counts the number of bits that are set to true. Asserts that mDefault is false.

```
12.10.4.4 end() iterator carl::Bitset::end ( ) const [inline]
```

Returns an past-the-end iterator.

```
12.10.4.5 find_first() std::size_t carl::Bitset::find_first ( ) const [inline]
```

Retrieves the index of the first bit that is set to true.

```
12.10.4.6 find_next() std::size_t carl::Bitset::find_next ( std::size_t pos ) const [inline]
```

Retrieves the index of the first bit set to true after the given position.

Checks wether the bits set is a subset of the bits set in rhs.

```
12.10.4.8 none() bool carl::Bitset::none ( ) const [inline]
```

Checks if no bits are set to true. Asserts that mDefault is false.

```
12.10.4.9 num_blocks() auto carl::Bitset::num_blocks ( ) const [inline]
```

Retrieves the number of blocks used to store mData.

Computes the bitwise and with rhs.

Sets all bits to false that are true in rhs.

```
12.10.4.12 operator" | =() Bitset& carl::Bitset::operator|= (

const Bitset & rhs ) [inline]
```

Computes the bitwise or with rhs.

```
12.10.4.13 reset() Bitset& carl::Bitset::reset ( std::size_t n ) [inline]
```

Resets a bit to false.

```
12.10.4.14 resize() [1/2] auto carl::Bitset::resize (
std::size_t num_bits) const [inline]
```

Resize the Bitset to hold at least num\_bits bits. New bits are set to mDefault.

Resize the Bitset to hold at least num\_bits bits. New bits are set to the given value.

```
12.10.4.16 set() Bitset& carl::Bitset::set (
    std::size.t n,
    bool value = true ) [inline]
```

Sets the given bit to a value, true by default.

Sets the a range of bits to a value, true by default.

```
12.10.4.18 size() auto carl::Bitset::size ( ) const [inline]
```

Retrieves the size of mData.

```
12.10.4.19 test() bool carl::Bitset::test ( std::size_t n ) const [inline]
```

Retrieves the value of the given bit.

## 12.10.5 Friends And Related Function Documentation

Ensures that the explicitly stored bits of lhs and rhs have the same size.

```
12.10.5.2 operator& Bitset operator& (

const Bitset & lhs,

const Bitset & rhs ) [friend]
```

Returns the bitwise and of lhs and rhs.

Compares lhs and rhs according to some order.

Outputs b to os using the format <explicit bits>[<default>].

Compares lhs and rhs.

```
12.10.5.6 operator" | Bitset operator | (

const Bitset & lhs,

const Bitset & rhs ) [friend]
```

Returns the bitwise or of lhs and rhs.

```
12.10.5.7 operator~ Bitset operator~ (

const Bitset & Ihs ) [friend]
```

Returns the bitwise negation of lhs.

```
12.10.5.8 std::hash< carl::Bitset > friend struct std::hash< carl::Bitset > [friend]
```

# 12.10.6 Field Documentation

```
12.10.6.1 bits_per_block constexpr auto carl::Bitset::bits_per_block = BaseType::bits_per_block [static], [constexpr]
```

Number of bits in each storage block.

```
12.10.6.2 npos constexpr auto carl::Bitset::npos = BaseType::npos [static], [constexpr]
```

Sentinel element for iteration.

# 12.11 carl::BitVector Class Reference

```
#include <BitVector.h>
```

# **Data Structures**

· class forward\_iterator

# **Public Types**

• using const\_iterator = forward\_iterator

#### **Public Member Functions**

- BitVector ()=default
- BitVector (unsigned pos)
- void clear ()
- size\_t size () const
- void reserve (size\_t capacity)
- bool empty () const
- size\_t findFirstSetBit () const
- void setBit (unsigned pos, bool val=true)
- bool getBit (unsigned pos) const
- bool subsetOf (const BitVector &superset)
- BitVector & calculateUnion (const BitVector &rhs)
- BitVector & operator = (const BitVector &rhs)
- forward\_iterator begin () const
- forward\_iterator end () const
- void print (std::ostream &os=std::cout) const

## **Protected Attributes**

std::vector< unsigned > mBits

# **Friends**

- bool operator== (const BitVector &lhs, const BitVector &rhs)
- BitVector operator (const BitVector &lhs, const BitVector &rhs)

# 12.11.1 Member Typedef Documentation

```
12.11.1.1 const_iterator using carl::BitVector::const_iterator = forward_iterator
```

#### 12.11.2 Constructor & Destructor Documentation

```
12.11.2.1 BitVector() [1/2] carl::BitVector::BitVector ( ) [default]
```

```
12.11.2.2 BitVector() [2/2] carl::BitVector::BitVector ( unsigned pos ) [inline], [explicit]
```

## 12.11.3 Member Function Documentation

```
12.11.3.1 begin() forward_iterator carl::BitVector::begin ( ) const [inline]
12.11.3.2 calculateUnion() BitVector& carl::BitVector::calculateUnion (
             const BitVector & rhs ) [inline]
12.11.3.3 clear() void carl::BitVector::clear ( ) [inline]
12.11.3.4 empty() bool carl::BitVector::empty ( ) const [inline]
12.11.3.5 end() forward_iterator carl::BitVector::end ( ) const [inline]
12.11.3.6 findFirstSetBit() size.t carl::BitVector::findFirstSetBit ( ) const [inline]
12.11.3.7 getBit() bool carl::BitVector::getBit (
            unsigned pos ) const [inline]
12.11.3.8 operator" | =() BitVector& carl::BitVector::operator|= (
            const BitVector & rhs ) [inline]
12.11.3.9 print() void carl::BitVector::print (
            std::ostream & os = std::cout ) const [inline]
```

```
size_t capacity ) [inline]
12.11.3.11 setBit() void carl::BitVector::setBit (
            unsigned pos,
            bool val = true ) [inline]
12.11.3.12 size() size_t carl::BitVector::size ( ) const [inline]
12.11.3.13 subsetOf() bool carl::BitVector::subsetOf (
             const BitVector & superset )
12.11.4 Friends And Related Function Documentation
12.11.4.1 operator== bool operator== (
            const BitVector & lhs,
            const BitVector & rhs ) [friend]
12.11.4.2 operator" | BitVector operator (
            const BitVector & lhs,
            const BitVector & rhs ) [friend]
12.11.5 Field Documentation
```

12.11.3.10 reserve() void carl::BitVector::reserve (

# #include <Substitution.h>

# **Public Member Functions**

BitvectorSubstitutor (const std::map< BVVariable, BVTerm > &repl)

**12.11.5.1 mBits** std::vector<unsigned> carl::BitVector::mBits [protected]

12.12 carl::helper::BitvectorSubstitutor< Pol > Struct Template Reference

• Formula < Pol > operator() (const Formula < Pol > &formula)

## **Data Fields**

• const std::map< BVVariable, BVTerm > & replacements

#### 12.12.1 Constructor & Destructor Documentation

```
12.12.1.1 BitvectorSubstitutor() template<typename Pol > carl::helper::BitvectorSubstitutor< Pol >::BitvectorSubstitutor ( const std::map< BVVariable, BVTerm > & repl ) [inline], [explicit]
```

#### 12.12.2 Member Function Documentation

#### 12.12.3 Field Documentation

```
12.12.3.1 replacements template<typename Pol > const std::map<BVVariable,BVTerm>& carl::helper::BitvectorSubstitutor< Pol >::replacements
```

# 12.13 carl::Buchberger < Polynomial, AddingPolicy > Class Template Reference

Gebauer and Moeller style implementation of the Buchberger algorithm.

```
#include <Buchberger.h>
```

# **Public Member Functions**

- Buchberger ()
- virtual ∼Buchberger ()=default
- Buchberger (const Buchberger &rhs)
- void calculate (const std::list< Polynomial > &scheduledForAdding)
- void setIdeal (const std::shared\_ptr< Ideal< Polynomial >> &ideal)
- void setCriticalPairs (const std::shared\_ptr< CritPairs > &criticalPairs)
- void update (size\_t index)

## **Protected Member Functions**

- bool addToGb (const Polynomial &newPol)
- void removeBuchbergerTriples (std::unordered\_map< size\_t, SPolPair > &spairs, std::vector< size\_t > &primelist)
- void reduce ()

#### **Protected Attributes**

- std::shared\_ptr< |deal< | Polynomial > > pGb
- std::vector< size\_t > mGbElementsIndices
- std::shared\_ptr< CritPairs > pCritPairs
- UpdateFnct< Buchberger< Polynomial, AddingPolicy >> mUpdateCallBack

## 12.13.1 Detailed Description

```
template<typename Polynomial, template< typename > class AddingPolicy> class carl::Buchberger< Polynomial, AddingPolicy >
```

Gebauer and Moeller style implementation of the Buchberger algorithm.

For more information about this Algorithm. More information can be found in the Bachelor Thesis On Groebner Bases in SMT-Compliant Decision Procedures.

# 12.13.2 Constructor & Destructor Documentation

```
12.13.2.1 Buchberger() [1/2] template<typename Polynomial , template< typename > class Adding←Policy> carl::Buchberger< Polynomial, AddingPolicy >::Buchberger ( ) [inline]

12.13.2.2 ~Buchberger() template<typename Polynomial , template< typename > class Adding←Policy> virtual carl::Buchberger< Polynomial, AddingPolicy >::~Buchberger ( ) [virtual], [default]

12.13.2.3 Buchberger() [2/2] template<typename Polynomial , template< typename > class Adding←Policy> carl::Buchberger< Polynomial, AddingPolicy >::Buchberger ( const Buchberger< Polynomial, AddingPolicy > & rhs ) [inline]
```

## 12.13.3 Member Function Documentation

```
12.13.3.1 addToGb() template<typename Polynomial , template< typename > class AddingPolicy>
bool carl::Buchberger< Polynomial, AddingPolicy >::addToGb (
             const Polynomial & newPol ) [inline], [protected]
12.13.3.2 calculate() template<typename Polynomial , template< typename > class AddingPolicy>
void carl::Buchberger< Polynomial, AddingPolicy >::calculate (
             const std::list< Polynomial > & scheduledForAdding )
12.13.3.3 reduce() template<typename Polynomial , template< typename > class AddingPolicy>
void carl::Buchberger< Polynomial, AddingPolicy >::reduce ( ) [protected]
\textbf{12.13.3.4} \quad \textbf{removeBuchbergerTriples()} \quad \texttt{template} < \texttt{typename Polynomial , template} < \texttt{typename} > \texttt{class}
AddingPolicy>
void carl::Buchberger< Polynomial, AddingPolicy >::removeBuchbergerTriples (
             std::unordered_map< size_t, SPolPair > & spairs,
             \verb|std::vector<| size_t| > & primelist|) | [protected]
12.13.3.5 setCriticalPairs() template<typename Polynomial , template< typename > class Adding←
Policy>
void carl::Buchberger< Polynomial, AddingPolicy >::setCriticalPairs (
             const std::shared_ptr< CritPairs > & criticalPairs ) [inline]
12.13.3.6 setideal() template<typename Polynomial , template< typename > class AddingPolicy>
void carl::Buchberger< Polynomial, AddingPolicy >::setIdeal (
             const std::shared_ptr< Ideal< Polynomial >> & ideal ) [inline]
12.13.3.7 update() template<typename Polynomial , template< typename > class AddingPolicy>
void carl::Buchberger< Polynomial, AddingPolicy >::update (
             size_t index )
```

# 12.13.4 Field Documentation

**12.13.4.1 mGbElementsIndices** template<typename Polynomial , template< typename > class Adding← Policy>

std::vector<size\_t> carl::Buchberger< Polynomial, AddingPolicy >::mGbElementsIndices [protected]

12.13.4.2 mUpdateCallBack template<typename Polynomial , template< typename > class Adding  $\leftarrow$  Policy>

UpdateFnct<Buchberger<Polynomial, AddingPolicy> > carl::Buchberger< Polynomial, AddingPolicy
>::mUpdateCallBack [protected]

12.13.4.3 pCritPairs template<typename Polynomial , template< typename > class AddingPolicy> std::shared\_ptr<CritPairs> carl::Buchberger< Polynomial, AddingPolicy >::pCritPairs [protected]

12.13.4.4 pGb template<typename Polynomial , template< typename > class AddingPolicy> std::shared\_ptr<Ideal<Polynomial> > carl::Buchberger< Polynomial, AddingPolicy >::pGb [protected]

# 12.14 carl::BuchbergerStats Class Reference

A little class for gathering statistics about the Buchberger algorithm calls.

#include <BuchbergerStats.h>

#### **Public Member Functions**

• void TSQWithConstant ()

Count that we found a TSQ which had a constant trailing term.

• void TSQWithoutConstant ()

Count that we found a TSQ which did not have a constant trailing term.

void SingleTermSFP ()

Count that we could reduce a single term polynomial by calculating the Squarefree part.

- void ReducibleIdentity ()
- void TreatSPair ()

Count that we take and reduce another S-Pair.

void NonZeroReduction ()

Count that an S-Pair reduced to some non zero polynomial.

- unsigned getNrTSQWithConstant () const
- unsigned getNrTSQWithoutConstant () const
- unsigned getSingleTermSFP () const
- unsigned getNrReducibleIdentities () const

#### **Static Public Member Functions**

static BuchbergerStats \* getInstance ()

## **Protected Member Functions**

• BuchbergerStats ()

#### **Protected Attributes**

- unsigned mNrOfTSQWithConstant
- unsigned mNrOfTSQWithoutConstant
- unsigned mNrOfSingleTermSFP
- unsigned mNrOfReducibleIdentities
- unsigned mNrOfReductions
- unsigned mNrOfNonZeroReductions

# 12.14.1 Detailed Description

A little class for gathering statistics about the Buchberger algorithm calls.

## 12.14.2 Constructor & Destructor Documentation

```
12.14.2.1 BuchbergerStats() carl::BuchbergerStats::BuchbergerStats () [inline], [protected]
```

## 12.14.3 Member Function Documentation

```
12.14.3.1 getInstance() BuchbergerStats * carl::BuchbergerStats::getInstance ( ) [static]
```

**12.14.3.2 getNrReducibleIdentities()** unsigned carl::BuchbergerStats::getNrReducibleIdentities () const [inline]

```
12.14.3.3 getNrTSQWithConstant() unsigned carl::BuchbergerStats::getNrTSQWithConstant () const [inline]
```

```
12.14.3.4 getNrTSQWithoutConstant() unsigned carl::BuchbergerStats::getNrTSQWithoutConstant () const [inline]
```

[protected]

| 12.14.3.5 | getSingleTermSFP()                           | unsigned carl::BuchbergerStats::getSingleTermSFP ( ) const  | [inline] |
|-----------|--|---|----------|
|           | NonZeroReduction() an S-Pair reduced to sor  | <pre>void carl::BuchbergerStats::NonZeroReduction ( ) [inline] me non zero polynomial.</pre>              |          |
| 12.14.3.7 | ReducibleIdentity() v                        | oid carl::BuchbergerStats::ReducibleIdentity ( ) [inline]   |          |
|           |  | d carl::BuchbergerStats::SingleTermSFP ( ) [inline] e term polynomial by calculating the Squarefree part. |          |
|           | TreatSPair() void can we take and reduce ano | rl::BuchbergerStats::TreatSPair () [inline] ther S-Pair.  |          |
|           | _  | void carl::BuchbergerStats::TSQWithConstant ( ) [inline]  nad a constant trailing term.                   |          |
|           |  | t() void carl::BuchbergerStats::TSQWithoutConstant ( ) [inl lid not have a constant trailing term.        | ine]     |
| 12.14.4 F | Field Documentation                          |   |          |
| 12.14.4.1 | mNrOfNonZeroReduct                           | <b>tions</b> unsigned carl::BuchbergerStats::mNrOfNonZeroReduction  | s        |

**12.14.4.2 mNrOfReducibleIdentities** unsigned carl::BuchbergerStats::mNrOfReducibleIdentities [protected]

**12.14.4.3 mNrOfReductions** unsigned carl::BuchbergerStats::mNrOfReductions [protected]

12.14.4.4 mNrOfSingleTermSFP unsigned carl::BuchbergerStats::mNrOfSingleTermSFP [protected]

12.14.4.5 mNrOfTSQWithConstant unsigned carl::BuchbergerStats::mNrOfTSQWithConstant [protected]

**12.14.4.6 mNrOfTSQWithoutConstant** unsigned carl::BuchbergerStats::mNrOfTSQWithoutConstant [protected]

# 12.15 carl::BVBinaryContent Struct Reference

#include <BVTermContent.h>

# **Public Member Functions**

- BVBinaryContent (BVTerm first, BVTerm second)
- bool operator== (const BVBinaryContent &rhs) const
- bool operator< (const BVBinaryContent &rhs) const

#### Data Fields

- BVTerm mFirst
- BVTerm mSecond

#### 12.15.1 Constructor & Destructor Documentation

```
12.15.1.1 BVBinaryContent() carl::BVBinaryContent::BVBinaryContent (
BVTerm first,
BVTerm second ) [inline]
```

## 12.15.2 Member Function Documentation

12.15.3.1 mFirst BVTerm carl::BVBinaryContent::mFirst

12.15.3.2 mSecond BVTerm carl::BVBinaryContent::mSecond

# 12.16 carl::BVConstraint Class Reference

#include <BVConstraint.h>

#### **Public Member Functions**

- const BVTerm & lhs () const
- const BVTerm & rhs () const
- BVCompareRelation relation () const
- std::size\_t id () const
- std::size\_t hash () const
- std::size\_t complexity () const
- void gatherBVVariables (std::set< BVVariable > &vars) const
- void gatherVariables (carlVariables &vars) const
- bool is\_constant () const
- bool isAlwaysConsistent () const
- bool isAlwaysInconsistent () const

# **Static Public Member Functions**

- static BVConstraint create (bool \_consistent=true)
- static BVConstraint create (const BVCompareRelation &\_relation, const BVTerm &\_lhs, const BVTerm &\_rhs)

## **Friends**

• class BVConstraintPool

#### 12.16.1 Member Function Documentation

```
12.16.1.1 complexity() std::size_t carl::BVConstraint::complexity ( ) const [inline]
```

Returns

An approximation of the complexity of this bit vector constraint.

```
12.16.1.2 create() [1/2] BVConstraint carl::BVConstraint::create ( bool _consistent = true ) [static]
```

```
12.16.1.4 gatherBVVariables() void carl::BVConstraint::gatherBVVariables ( std::set< BVVariable > & vars ) const [inline]
```

```
12.16.1.5 gatherVariables() void carl::BVConstraint::gatherVariables ( carlVariables & vars ) const [inline]
```

```
12.16.1.6 hash() std::size_t carl::BVConstraint::hash ( ) const [inline]
```

Returns

A hash value for this constraint.

```
12.16.1.7 id() std::size_t carl::BVConstraint::id ( ) const [inline]
```

Returns

The unique id of this constraint.

```
12.16.1.8 is_constant() bool carl::BVConstraint::is_constant ( ) const [inline]
```

```
12.16.1.9 isAlwaysConsistent() bool carl::BVConstraint::isAlwaysConsistent ( ) const [inline]
```

12.16.1.10 isAlwaysInconsistent() bool carl::BVConstraint::isAlwaysInconsistent () const [inline]

```
12.16.1.11 | lhs() const BVTerm& carl::BVConstraint::lhs ( ) const [inline]
```

Returns

The bit-vector term being the left-hand side of this constraint.

```
12.16.1.12 relation() BVCompareRelation carl::BVConstraint::relation ( ) const [inline]
```

Returns

The relation symbol of this constraint.

```
12.16.1.13 rhs() const BVTerm& carl::BVConstraint::rhs ( ) const [inline]
```

Returns

The bit-vector term being the right-hand side of this constraint.

# 12.16.2 Friends And Related Function Documentation

# 12.16.2.1 BVConstraintPool friend class BVConstraintPool [friend]

## 12.17 carl::BVConstraintPool Class Reference

#include <BVConstraintPool.h>

## **Public Member Functions**

- ConstConstraintPtr create (bool \_consistent=true)
- ConstConstraintPtr create (const BVCompareRelation &\_relation, const BVTerm &\_lhs, const BVTerm &\_rhs)
- void assignId (ConstraintPtr \_constraint, std::size\_t \_id) override

Assigns a unique id to the generated element.

- void print () const
- std::pair< typename FastPointerSet< BVConstraint >::iterator, bool > insert (ElementPtr \_element, bool \_assertFreshness=false)

Inserts the given element into the pool, if it does not yet occur in there.

• ConstElementPtr add (ElementPtr \_element)

Adds the given element to the pool, if it does not yet occur in there.

## **Static Public Member Functions**

static BVConstraintPool & getInstance ()

Returns the single instance of this class by reference.

#### 12.17.1 Member Function Documentation

Adds the given element to the pool, if it does not yet occur in there.

Note, that this method uses the allocator which is locked before calling.

# **Parameters**

| ₋element | The element to add to the pool. |
|----------|---------------------------------|

# Returns

The given element, if it did not yet occur in the pool; The equivalent element already occurring in the pool, otherwise.

Assigns a unique id to the generated element.

Note that this method serves as a callback for subclasses. The actual assignment of the id is done there.

#### Parameters

| ₋element | The element for which to add the id. |
|----------|--------------------------------------|
| _id      | A unique id.                         |

Reimplemented from carl::Pool< BVConstraint >.

```
12.17.1.3 create() [1/2] BVConstraintPool::ConstConstraintPtr carl::BVConstraintPool::create (
bool _consistent = true )
```

```
12.17.1.5 getInstance() static BVConstraintPool & carl::Singleton< BVConstraintPool >::get← Instance ( ) [inline], [static], [inherited]
```

Returns the single instance of this class by reference.

If there is no instance yet, a new one is created.

Inserts the given element into the pool, if it does not yet occur in there.

## **Parameters**

| _element         | The element to add to the pool.   |
|------------------|---|
| ₋assertFreshness | When true, an assertion fails if the element is not fresh (i.e., if it already occurs in the pool). |

#### Returns

The position of the given element in the pool and true, if it did not yet occur in the pool; The position of the equivalent element in the pool and false, otherwise.

```
12.17.1.7 print() void carl::Pool< BVConstraint >::print ( ) const [inline], [inherited]
```

# 12.18 carl::BVExtractContent Struct Reference

```
#include <BVTermContent.h>
```

# **Public Member Functions**

- BVExtractContent (BVTerm \_operand, std::size\_t \_highest, std::size\_t \_lowest)
- bool operator== (const BVExtractContent &rhs) const
- bool operator< (const BVExtractContent &rhs) const

# **Data Fields**

- BVTerm mOperand
- std::size\_t mHighest
- std::size\_t mLowest

# 12.18.1 Constructor & Destructor Documentation

# 12.18.2 Member Function Documentation

## 12.18.3 Field Documentation

```
12.18.3.1 mHighest std::size_t carl::BVExtractContent::mHighest
```

```
12.18.3.2 mLowest std::size_t carl::BVExtractContent::mLowest
```

```
12.18.3.3 mOperand BVTerm carl::BVExtractContent::mOperand
```

# 12.19 carl::BVReasons Struct Reference

```
#include <ReasonsAdaptor.h>
```

# **Public Member Functions**

- void setReason (unsigned index)
- void extendReasons (const BitVector &extendWith)
- BitVector getReasons () const
- void setReasons (const BitVector &reasons)

## **Static Public Attributes**

• static constexpr bool has\_reasons = true

# 12.19.1 Member Function Documentation

```
12.19.1.1 extendReasons() void carl::BVReasons::extendReasons ( const BitVector & extendWith ) [inline]
```

```
12.19.1.2 getReasons() BitVector carl::BVReasons::getReasons ( ) const [inline]
```

```
unsigned index )

12.19.1.4 setReasons() void carl::BVReasons::setReasons (
```

const BitVector & reasons ) [inline]

12.19.1.3 setReason() void carl::BVReasons::setReason (

# 12.19.2 Field Documentation

```
12.19.2.1 has_reasons constexpr bool carl::BVReasons::has_reasons = true [static], [constexpr]
```

#### 12.20 carl::BVTerm Class Reference

```
#include <BVTerm.h>
```

#### **Public Member Functions**

- BVTerm ()
- BVTerm (BVTermType \_type, BVValue \_value)
- BVTerm (BVTermType \_type, const BVVariable &\_variable)
- BVTerm (BVTermType \_type, const BVTerm &\_operand, std::size\_t \_index=0)
- BVTerm (BVTermType \_type, const BVTerm &\_first, const BVTerm &\_second)
- BVTerm (BVTermType \_type, const BVTerm &\_operand, std::size\_t \_first, std::size\_t \_last)
- std::size\_t hash () const
- std::size\_t width () const
- BVTermType type () const
- bool is\_constant () const
- size\_t complexity () const
- void gatherBVVariables (std::set< BVVariable > &vars) const
- bool isInvalid () const
- · const BVTerm & operand () const
- std::size\_t index () const
- · const BVTerm & first () const
- const BVTerm & second () const
- std::size\_t highest () const
- std::size\_t lowest () const
- const BVVariable & variable () const
- const BVValue & value () const
- BVTerm substitute (const std::map< BVVariable, BVTerm > &) const

#### **Friends**

- std::ostream & operator<< (std::ostream &os, const BVTerm &term)
- bool operator== (const BVTerm &lhs, const BVTerm &rhs)
- bool operator< (const BVTerm &lhs, const BVTerm &rhs)</li>

# 12.20.1 Constructor & Destructor Documentation

```
12.20.1.1 BVTerm() [1/6] carl::BVTerm::BVTerm ( )
12.20.1.2 BVTerm() [2/6] carl::BVTerm::BVTerm (
            BVTermType _type,
            BVValue _value )
12.20.1.3 BVTerm() [3/6] carl::BVTerm::BVTerm (
            BVTermType _type,
            const BVVariable & _variable )
12.20.1.4 BVTerm() [4/6] carl::BVTerm::BVTerm (
            BVTermType _type,
             const BVTerm & _operand,
             std::size_t _index = 0)
12.20.1.5 BVTerm() [5/6] carl::BVTerm:(
            BVTermType _type,
            const BVTerm & _first,
             const BVTerm & _second )
12.20.1.6 BVTerm() [6/6] carl::BVTerm::BVTerm (
            BVTermType _type,
            const BVTerm & _operand,
            std::size_t _first,
            std::size_t _last )
```

# 12.20.2 Member Function Documentation

```
12.20.2.1 complexity() std::size_t carl::BVTerm::complexity ( ) const
```

Returns

An approximation of the complexity of this bit vector term.

```
12.20.2.2 first() const BVTerm & carl::BVTerm::first ( ) const
```

```
12.20.2.3 gatherBVVariables() void carl::BVTerm::gatherBVVariables ( std::set< BVVariable > & vars ) const
```

```
12.20.2.4 hash() std::size_t carl::BVTerm::hash ( ) const
```

```
12.20.2.5 highest() std::size_t carl::BVTerm::highest ( ) const
```

12.20.2.6 index() std::size\_t carl::BVTerm::index ( ) const

12.20.2.7 is\_constant() bool carl::BVTerm::is\_constant ( ) const [inline]

12.20.2.8 isInvalid() bool carl::BVTerm::isInvalid ( ) const

12.20.2.9 lowest() std::size\_t carl::BVTerm::lowest ( ) const

12.20.2.10 operand() const BVTerm & carl::BVTerm::operand ( ) const

```
12.20.2.11 second() const BVTerm & carl::BVTerm::second ( ) const
12.20.2.12 substitute() BVTerm carl::BVTerm::substitute (
             const std::map< BVVariable, BVTerm > & _substitutions ) const
12.20.2.13 type() BVTermType carl::BVTerm::type ( ) const
12.20.2.14 value() const BVValue & carl::BVTerm::value ( ) const
12.20.2.15 variable() const BVVariable & carl::BVTerm::variable ( ) const
12.20.2.16 width() std::size_t carl::BVTerm::width ( ) const
12.20.3 Friends And Related Function Documentation
12.20.3.1 operator< bool operator< (
            const BVTerm & lhs,
             const BVTerm & rhs ) [friend]
12.20.3.2 operator<< std::ostream& operator<< (
            std::ostream & os,
            const BVTerm & term ) [friend]
12.20.3.3 operator== bool operator== (
            const BVTerm & lhs,
            const BVTerm & rhs ) [friend]
```

# 12.21 carl::BVTermContent Struct Reference

# **Public Types**

using ContentType = std::variant< BVVariable, BVValue, BVUnaryContent, BVBinaryContent, BVExtractContent</li>

#### **Public Member Functions**

- std::size\_t computeHash () const
- template<typename T >
   const T & as () const
- BVTermContent ()
- BVTermContent (BVTermType type, BVValue &&value)
- BVTermContent (BVTermType type, const BVVariable &variable)
- BVTermContent (BVTermType type, const BVTerm &\_operand, std::size\_t \_index=0)
- BVTermContent (BVTermType type, const BVTerm &\_first, const BVTerm &\_second)
- BVTermContent (BVTermType type, const BVTerm &\_operand, std::size\_t \_highest, std::size\_t \_lowest)
- std::size\_t id () const
- std::size\_t width () const
- BVTermType type () const
- · const auto & content () const
- bool isInvalid () const
- void gatherBVVariables (std::set< BVVariable > &vars) const
- std::size\_t complexity () const
- std::size\_t hash () const

# **Data Fields**

- BVTermType mType = BVTermType::CONSTANT
- ContentType mContent = BVValue()
- std::size\_t mWidth = 0
- std::size\_t mld = 0
- std::size\_t mHash = 0

# 12.21.1 Member Typedef Documentation

**12.21.1.1 ContentType** using carl::BVTermContent::ContentType = std::variant<BVVariable, BVValue, BVUnaryContent, BVBinaryContent, BVExtractContent>

# 12.21.2 Constructor & Destructor Documentation

# 12.21.2.1 BVTermContent() [1/6] carl::BVTermContent::BVTermContent ( ) [inline]

```
12.21.2.2 BVTermContent() [2/6] carl::BVTermContent::BVTermContent (
              BVTermType type,
              BVValue && value ) [inline]
\textbf{12.21.2.3} \quad \textbf{BVTermContent()} \; \texttt{[3/6]} \quad \texttt{carl::BVTermContent::BVTermContent} \; \; (
              BVTermType type,
              const BVVariable & variable ) [inline]
\textbf{12.21.2.4} \quad \textbf{BVTermContent()} \; \texttt{[4/6]} \quad \texttt{carl::BVTermContent::BVTermContent} \; \; \texttt{(}
              BVTermType type,
              const BVTerm & Loperand,
              std::size\_t \_index = 0) [inline]
12.21.2.5 BVTermContent() [5/6] carl::BVTermContent::BVTermContent (
              BVTermType type,
              const BVTerm & _first,
              const BVTerm & _second ) [inline]
12.21.2.6 BVTermContent() [6/6] carl::BVTermContent::BVTermContent (
              BVTermType type,
              const BVTerm & _operand,
              std::size_t _highest,
              std::size_t _lowest ) [inline]
12.21.3 Member Function Documentation
12.21.3.1 as() template<typename T >
const T& carl::BVTermContent::as ( ) const [inline]
12.21.3.2 complexity() std::size_t carl::BVTermContent::complexity ( ) const [inline]
12.21.3.3 computeHash() std::size_t carl::BVTermContent::computeHash ( ) const [inline]
```

```
12.21.3.4 content() const auto& carl::BVTermContent::content ( ) const [inline]
12.21.3.5 gatherBVVariables() void carl::BVTermContent::gatherBVVariables (
             std::set< BVVariable > & vars ) const [inline]
12.21.3.6 hash() std::size_t carl::BVTermContent::hash ( ) const [inline]
12.21.3.7 id() std::size_t carl::BVTermContent::id ( ) const [inline]
12.21.3.8 isInvalid() bool carl::BVTermContent::isInvalid ( ) const [inline]
12.21.3.9 type() BVTermType carl::BVTermContent::type ( ) const [inline]
12.21.3.10 width() std::size_t carl::BVTermContent::width ( ) const [inline]
12.21.4 Field Documentation
12.21.4.1 mContent ContentType carl::BVTermContent::mContent = BVValue()
12.21.4.2 mHash std::size_t carl::BVTermContent::mHash = 0
12.21.4.3 mld std::size_t carl::BVTermContent::mId = 0
```

12.21.4.4 mType BVTermType carl::BVTermContent::mType = BVTermType::CONSTANT

12.21.4.5 mWidth std::size\_t carl::BVTermContent::mWidth = 0

## 12.22 carl::BVTermPool Class Reference

```
#include <BVTermPool.h>
```

# **Public Types**

- using Term = BVTermContent
- using TermPtr = Term \*
- using ConstTermPtr = const Term \*

#### **Public Member Functions**

- BVTermPool ()
- BVTermPool (const BVTermPool &)=delete
- BVTermPool & operator= (const BVTermPool &)=delete
- ConstTermPtr create ()
- ConstTermPtr create (BVTermType \_type, BVValue &&\_value)
- ConstTermPtr create (BVTermType \_type, const BVVariable &\_variable)
- ConstTermPtr create (BVTermType \_type, const BVTerm &\_operand, std::size\_t \_index=0)
- ConstTermPtr create (BVTermType \_type, const BVTerm &\_first, const BVTerm &\_second)
- ConstTermPtr create (BVTermType \_type, const BVTerm &\_operand, std::size\_t \_first, std::size\_t \_last)
- void assignId (TermPtr \_term, std::size\_t \_id) override

Assigns a unique id to the generated element.

- · void print () const
- std::pair< typename FastPointerSet< BVTermContent >::iterator, bool > insert (ElementPtr \_element, bool \_assertFreshness=false)

Inserts the given element into the pool, if it does not yet occur in there.

ConstElementPtr add (ElementPtr \_element)

Adds the given element to the pool, if it does not yet occur in there.

# **Static Public Member Functions**

static BVTermPool & getInstance ()

Returns the single instance of this class by reference.

# 12.22.1 Member Typedef Documentation

# 12.22.1.1 ConstTermPtr using carl::BVTermPool::ConstTermPtr = const Term\*

```
12.22.1.2 Term using carl::BVTermPool::Term = BVTermContent
```

```
12.22.1.3 TermPtr using carl::BVTermPool::TermPtr = Term*
```

#### 12.22.2 Constructor & Destructor Documentation

```
12.22.2.1 BVTermPool() [1/2] carl::BVTermPool::BVTermPool ( )
```

## 12.22.3 Member Function Documentation

Adds the given element to the pool, if it does not yet occur in there.

Note, that this method uses the allocator which is locked before calling.

## **Parameters**

| ₋element | The element to add to the pool. |
|----------|---------------------------------|
|----------|---------------------------------|

## Returns

The given element, if it did not yet occur in the pool; The equivalent element already occurring in the pool, otherwise.

Assigns a unique id to the generated element.

Note that this method serves as a callback for subclasses. The actual assignment of the id is done there.

#### **Parameters**

| ₋element | The element for which to add the id. |
|----------|--------------------------------------|
| _id      | A unique id.                         |

Reimplemented from carl::Pool < BVTermContent >.

```
12.22.3.3 create() [1/6] BVTermPool::ConstTermPtr carl::BVTermPool::create ( )
12.22.3.4 create() [2/6] BVTermPool::ConstTermPtr carl::BVTermPool::create (
             BVTermType _type,
             BVValue && _value )
12.22.3.5 create() [3/6] BVTermPool::ConstTermPtr carl::BVTermPool::create (
             BVTermType _type,
             const BVTerm & _first,
             const BVTerm & _second )
12.22.3.6 create() [4/6] BVTermPool::ConstTermPtr carl::BVTermPool::create (
             BVTermType _type,
             const BVTerm & _operand,
             std::size_t _first,
             std::size_t _last )
12.22.3.7 create() [5/6] BVTermPool::ConstTermPtr carl::BVTermPool::create (
             BVTermType _type,
             const BVTerm & _operand,
             std::size_t = 0)
12.22.3.8 create() [6/6] BVTermPool::ConstTermPtr carl::BVTermPool::create (
             BVTermType _type,
             const BVVariable & _variable )
```

```
12.22.3.9 getInstance() static BVTermPool & carl::Singleton< BVTermPool >::getInstance () [inline], [static], [inherited]
```

Returns the single instance of this class by reference.

If there is no instance yet, a new one is created.

Inserts the given element into the pool, if it does not yet occur in there.

#### **Parameters**

| ₋element         | The element to add to the pool.   |
|------------------|---|
| _assertFreshness | When true, an assertion fails if the element is not fresh (i.e., if it already occurs in the pool). |

#### Returns

The position of the given element in the pool and true, if it did not yet occur in the pool; The position of the equivalent element in the pool and false, otherwise.

```
12.22.3.12 print() void carl::Pool< BVTermContent >::print () const [inline], [inherited]
```

# 12.23 carl::BVUnaryContent Struct Reference

```
#include <BVTermContent.h>
```

# **Public Member Functions**

- BVUnaryContent (BVTerm operand, std::size\_t index=0)
- bool operator== (const BVUnaryContent &rhs) const
- bool operator< (const BVUnaryContent &rhs) const

# **Data Fields**

- · BVTerm mOperand
- std::size\_t mlndex

## 12.23.1 Constructor & Destructor Documentation

```
12.23.1.1 BVUnaryContent() carl::BVUnaryContent::BVUnaryContent (
BVTerm operand,
std::size_t index = 0 ) [inline], [explicit]
```

## 12.23.2 Member Function Documentation

# 12.24 carl::BVValue Class Reference

```
#include <BVValue.h>
```

# **Public Types**

using Base = boost::dynamic\_bitset< uint >

# **Public Member Functions**

- BVValue ()=default
- BVValue (Base &&value)
- BVValue (std::size\_t \_width, uint \_value=0)
- BVValue (std::size\_t \_width, const mpz\_class &\_value)
- template<typename BlockInputIterator >

BVValue (BlockInputIterator \_first, BlockInputIterator \_last)

- template<typename Char , typename Traits , typename Alloc >
- BVValue (const std::basic\_string< Char, Traits, Alloc > &\_s, typename std::basic\_string< Char, Traits, Alloc > ::size\_type \_pos=0, typename std::basic\_string< Char, Traits, Alloc > ::size\_type \_n=std::basic\_string< Char, Traits, Alloc > ::npos)
- operator const Base & () const
- const Base & base () const
- std::size\_t width () const
- std::string toString () const
- · bool is\_zero () const
- BVValue rotateLeft (std::size\_t \_n) const
- BVValue rotateRight (std::size\_t \_n) const
- BVValue repeat (std::size\_t \_n) const
- BVValue extendUnsignedBy (std::size\_t \_n) const
- BVValue extendSignedBy (std::size\_t \_n) const

- Base::reference operator[] (std::size\_t \_index)
- bool operator[] (std::size\_t \_index) const
- BVValue concat (const BVValue &\_other) const
- BVValue divideSigned (const BVValue &\_other) const
- BVValue remSigned (const BVValue &\_other) const
- BVValue modSigned (const BVValue &\_other) const
- BVValue rightShiftArithmetic (const BVValue &\_other) const
- BVValue extract (std::size\_t \_highest, std::size\_t \_lowest) const
- BVValue shift (const BVValue &\_other, bool \_left, bool \_arithmetic=false) const
- BVValue divideUnsigned (const BVValue &\_other, bool \_returnRemainder=false) const

## 12.24.1 Member Typedef Documentation

```
12.24.1.1 Base using carl::BVValue::Base = boost::dynamic.bitset<uint>
```

#### 12.24.2 Constructor & Destructor Documentation

```
12.24.2.1 BVValue() [1/6] carl::BVValue::BVValue ( ) [default]
```

```
12.24.2.2 BVValue() [2/6] carl::BVValue::BVValue (

Base && value) [inline], [explicit]
```

```
12.24.2.6 BVValue() [6/6] template<typename Char , typename Traits , typename Alloc >
carl::BVValue::BVValue (
             const std::basic_string< Char, Traits, Alloc > & \_s,
             typename std::basic_string< Char, Traits, Alloc >::size_type _pos = 0,
             \texttt{typename std::basic\_string} < \texttt{Char, Traits, Alloc} > :: \texttt{size\_type} \_n = std::basic\_ \leftarrow
string<Char, Traits, Alloc>::npos ) [inline], [explicit]
12.24.3 Member Function Documentation
12.24.3.1 base() const Base& carl::BVValue::base ( ) const [inline]
12.24.3.2 concat() BVValue carl::BVValue::concat (
             const BVValue & _other ) const
12.24.3.3 divideSigned() BVValue carl::BVValue::divideSigned (
             const BVValue & _other ) const
12.24.3.4 divideUnsigned() BVValue carl::BVValue::divideUnsigned (
             const BVValue & _other,
             bool _returnRemainder = false ) const
12.24.3.5 extendSignedBy() BVValue carl::BVValue::extendSignedBy (
             std::size_t _n ) const [inline]
12.24.3.6 extendUnsignedBy() BVValue carl::BVValue::extendUnsignedBy (
             std::size_t _n ) const [inline]
12.24.3.7 extract() BVValue carl::BVValue::extract (
             std::size_t _highest,
             std::size_t _lowest ) const
```

```
12.24.3.8 is_zero() bool carl::BVValue::is_zero ( ) const [inline]
12.24.3.9 modSigned() BVValue carl::BVValue::modSigned (
             const BVValue & _other ) const
12.24.3.10 operator const Base &() carl::BVValue::operator const Base & ( ) const [inline],
[explicit]
12.24.3.11 operator[]() [1/2] Base::reference carl::BVValue::operator[] (
             std::size_t _index ) [inline]
12.24.3.12 operator[]() [2/2] bool carl::BVValue::operator[] (
             std::size_t _index ) const [inline]
12.24.3.13 remSigned() BVValue carl::BVValue::remSigned (
             const BVValue & _other ) const
12.24.3.14 repeat() BVValue carl::BVValue::repeat (
             std::size_t _n ) const [inline]
\textbf{12.24.3.15} \quad \textbf{rightShiftArithmetic()} \quad \textbf{BVValue carl::BVValue::rightShiftArithmetic (}
             const BVValue & _other ) const [inline]
12.24.3.16 rotateLeft() BVValue carl::BVValue::rotateLeft (
             std::size_t _n ) const [inline]
12.24.3.17 rotateRight() BVValue carl::BVValue::rotateRight (
             std::size_t _n ) const [inline]
```

### 12.25 carl::BVVariable Class Reference

Represent a BitVector-Variable.

```
#include <BVVariable.h>
```

#### **Public Member Functions**

- BVVariable ()=default
- BVVariable (Variable \_variable, const Sort &\_sort)
- Variable variable () const
- operator Variable () const
- const Sort & sort () const
- std::size\_t width () const
- std::string toString (bool \_friendlyNames) const

### Friends

• std::ostream & operator<< (std::ostream &os, const BVVariable &v)

Print the given bit vector variable on the given output stream.

## 12.25.1 Detailed Description

Represent a BitVector-Variable.

## 12.25.2 Constructor & Destructor Documentation

```
12.25.2.1 BVVariable() [1/2] carl::BVVariable::BVVariable ( ) [default]
```

### 12.25.3 Member Function Documentation

```
12.25.3.1 operator Variable() carl::BVVariable::operator Variable ( ) const [inline], [explicit]
```

```
12.25.3.2 sort() const Sort& carl::BVVariable::sort ( ) const [inline]
```

Returns

The sort (domain) of this uninterpreted variable.

```
12.25.3.3 toString() std::string carl::BVVariable::toString ( bool _friendlyNames ) const [inline]
```

Returns

The string representation of this bit vector variable.

```
12.25.3.4 variable() Variable carl::BVVariable::variable ( ) const [inline]
```

```
12.25.3.5 width() std::size_t carl::BVVariable::width ( ) const [inline]
```

## 12.25.4 Friends And Related Function Documentation

Print the given bit vector variable on the given output stream.

#### **Parameters**

| os | The output stream to print on.    |
|----|-----------------------------------|
| V  | The bit vector variable to print. |

#### Returns

The output stream after printing the given bit vector variable on it.

# 12.26 carl::Heap< C >::c\_iterator Class Reference

```
#include <Heap.h>
```

#### **Public Member Functions**

- c\_iterator (const Tree &tree)
- c\_iterator (const Tree &tree, Heap::Node startpos)
- const Entry get () const
- void next ()
- const Node & getNode () const

## **Protected Attributes**

- const Heap::Tree & mTree
- · Heap::Node pos

#### **Friends**

- bool operator== (c\_iterator lhs, c\_iterator rhs)
- bool operator!= (c\_iterator lhs, c\_iterator rhs)

### 12.26.1 Constructor & Destructor Documentation

### 12.26.2 Member Function Documentation

12.26.4.2 pos template<class C >

Heap::Node carl::Heap< C >::c\_iterator::pos [protected]

```
12.26.2.1 get() template<class C >
const Entry carl::Heap< C >::c_iterator::get ( ) const [inline]
12.26.2.2 getNode() template<class C >
const Node& carl::Heap< C >::c-iterator::getNode ( ) const [inline]
12.26.2.3 next() template<class C >
void carl::Heap< C >::c-iterator::next ( ) [inline]
12.26.3 Friends And Related Function Documentation
12.26.3.1 operator"!= template<class C >
bool operator!= (
            c_iterator lhs,
            c_iterator rhs ) [friend]
12.26.3.2 operator== template<class C >
bool operator== (
            c_iterator lhs,
            c_iterator rhs ) [friend]
12.26.4 Field Documentation
12.26.4.1 mTree template<class C >
const Heap::Tree& carl::Heap< C >::c_iterator::mTree [protected]
```

## 12.27 carl::Cache < T > Class Template Reference

#include <Cache.h>

#### **Data Structures**

struct Info

## **Public Types**

- using Ref = std::size\_t
- using Container = std::unordered\_set< TypeInfoPair< T, Info > \*, pointerHash< TypeInfoPair< T, Info > >,
  pointerEqual< TypeInfoPair< T, Info > >>

### **Public Member Functions**

- Cache (size\_t \_maxCacheSize=10000, double \_cacheReductionAmount=0.2, double \_decay=0.98)
- Cache (const Cache &)=delete
- Cache & operator= (const Cache &)=delete
- ~Cache ()
- std::pair< Ref, bool > cache (T \*\_toCache, bool(\*\_canBeUpdated)(const T &, const T &)=&returnFalse< T >, void(\*\_update)(const T &, const T &)=&doNothing< T >)

Caches the given object.

• void reg (Ref \_refStoragePos)

Registers the entry to the given reference.

void dereg (Ref \_refStoragePos)

Deregisters the entry to the given reference.

void rehash (Ref \_refStoragePos)

Removes and reinserts the entry with the given reference, after its hash value is recalculated.

· void decayActivity ()

Decays all activities by increasing the activity increment.

void strengthenActivity (Ref \_refStoragePos)

Strenghtens the activity of the entry in the cache with the given reference, by increasing its activity.

• void print (std::ostream &\_out=std::cout) const

Prints all information stored in this cache to std::cout.

• const T & get (Ref \_refStoragePos) const

### **Static Public Attributes**

• static const Ref NO\_REF

## 12.27.1 Member Typedef Documentation

```
12.27.1.1 Container template<typename T > using carl::Cache< T >::Container = std::unordered_set<TypeInfoPair<T,Info>*, pointerHash<TypeInfoPair<T,Info>*, pointerHash<TypeInfo>*, pointerHash<
```

```
12.27.1.2 Ref template<typename T > using carl::Cache< T >::Ref = std::size_t
```

>, pointerEqual<TypeInfoPair<T,Info> >>

### 12.27.2 Constructor & Destructor Documentation

```
12.27.2.3 \simCache() template<typename T > carl::Cache< T >::\simCache ( )
```

### 12.27.3 Member Function Documentation

Caches the given object.

# **Parameters**

| ₋toCache      | The object to cache.  |
|---------------|---|
| _canBeUpdated | A function, which determines whether, in the case an equal object has already been cached, the given object can update the information in this already cached object.   |
| ₋update       | A function which updates an object in the cache, which is equal to the given object, by the information in the given object. After this function has been applied, the corresponding entry in the cache will be reinserted in it after been rehashed. |

#### Returns

The reference of the entry, which can be used outside this class to access the entry.

```
12.27.3.2 decayActivity() template<typename T > void carl::Cache< T >::decayActivity ( )
```

Decays all activities by increasing the activity increment.

Deregisters the entry to the given reference.

It mainly decreases the usage counter of this entry in the cache.

#### **Parameters**

\_refStoragePos The reference of the entry to deregister.

#### **Parameters**

| _refStoragePos | from. |
|----------------|-------|
|----------------|-------|

## Returns

The object in the entry with the given reference.

Prints all information stored in this cache to std::cout.

### **Parameters**

\_out The stream to print on.

Registers the entry to the given reference.

It mainly increases the usage counter of this entry in the cache.

## **Parameters**

| ı |                |   |
|---|----------------|---|
|   | _refStoragePos | The reference of the entry to register. |

Removes and reinserts the entry with the given reference, after its hash value is recalculated.

#### **Parameters**

| ₋refSto | ragePos | The reference of the entry to apply the given function to. |
|---------|---------|--|
|---------|---------|--|

## Returns

The new reference.

Strenghtens the activity of the entry in the cache with the given reference, by increasing its activity.

## **Parameters**

| _refStoragePos | The reference of the entry in the cache to strengthen its activity. |
|----------------|---|
|----------------|---|

#### 12.27.4 Field Documentation

```
12.27.4.1 NO_REF template<typename T > const Ref carl::Cache< T >::NO_REF [static]
```

# 12.28 carl::CachedConstraintContent< Pol > Struct Template Reference

```
#include <Constraint.h>
```

### **Public Member Functions**

- CachedConstraintContent (BasicConstraint< Pol > &&c)
- · const auto & key () const

#### **Data Fields**

- BasicConstraint < Pol > m\_constraint
  - Basic constraint.
- Factors < Pol > m\_lhs\_factorization

Cache for the factorization.

• carlVariables m\_variables

A container which includes all variables occurring in the polynomial considered by this constraint.

VarsInfo
 Pol > m\_var\_info\_map

A map which stores information about properties of the variables in this constraint.

## 12.28.1 Constructor & Destructor Documentation

### 12.28.2 Member Function Documentation

```
12.28.2.1 key() template<typename Pol >
const auto& carl::CachedConstraintContent< Pol >::key ( ) const [inline]
```

### 12.28.3 Field Documentation

```
12.28.3.1 m_constraint template<typename Pol >
BasicConstraint<Pol> carl::CachedConstraintContent< Pol >::m_constraint
```

Basic constraint.

```
12.28.3.2 m_lhs_factorization template<typename Pol >
Factors<Pol> carl::CachedConstraintContent< Pol >::m_lhs_factorization [mutable]
```

Cache for the factorization.

```
12.28.3.3 m_var_info_map template<typename Pol >
VarsInfo<Pol> carl::CachedConstraintContent< Pol >::m_var_info_map [mutable]
```

A map which stores information about properties of the variables in this constraint.

```
12.28.3.4 m_variables template<typename Pol > carlVariables carl::CachedConstraintContent< Pol >::m_variables [mutable]
```

A container which includes all variables occurring in the polynomial considered by this constraint.

# 12.29 carl::CArLConverter Class Reference

#include <CArLConverter.h>

### 12.30 carl::carlVariables Class Reference

```
#include <Variables.h>
```

## **Public Types**

- using iterator = std::vector < Variable >::iterator
- using const\_iterator = std::vector< Variable >::const\_iterator

#### **Public Member Functions**

- carlVariables (variable\_type\_filter filter=variable\_type\_filter::all())
- carlVariables (std::initializer\_list< Variable > i, variable\_type\_filter filter=variable\_type\_filter::all())
- template<typename Iterator >
   carlVariables (const Iterator &b, const Iterator &e, variable\_type\_filter filter=variable\_type\_filter::all())
- · auto begin () const
- · auto end () const
- auto begin ()
- auto end ()
- · bool empty () const
- std::size\_t size () const
- void clear ()
- bool has (Variable var) const
- void add (Variable v)
- template<typename lterator >
   void add (const lterator &b, const lterator &e)
- void add (std::initializer\_list< Variable > i)
- void erase (Variable v)
- const std::vector < Variable > & as\_vector () const
- std::set< Variable > as\_set () const
- carlVariables filter (variable\_type\_filter &&f) const
- auto boolean () const
- auto integer () const
- · auto real () const
- auto arithmetic () const
- auto bitvector () const
- auto uninterpreted () const

## Friends

- bool operator== (const carlVariables &lhs, const carlVariables &rhs)
- std::ostream & operator<< (std::ostream &os, const carlVariables &vars)</li>

## 12.30.1 Member Typedef Documentation

```
12.30.1.1 const_iterator using carl::carlVariables::const_iterator = std::vector<Variable>← ::const_iterator
```

12.30.1.2 iterator using carl::carlVariables::iterator = std::vector<Variable>::iterator

## 12.30.2 Constructor & Destructor Documentation

```
12.30.2.1 carlVariables() [1/3] carl::carlVariables::carlVariables (
            variable_type_filter filter = variable_type_filter::all() ) [inline]
12.30.2.2 carlVariables() [2/3] carl::carlVariables::carlVariables (
            std::initializer\_list< Variable > i,
            variable_type_filter = variable_type_filter::all() ) [inline], [explicit]
12.30.2.3 carlVariables() [3/3] template<typename Iterator >
carl::carlVariables::carlVariables (
            const Iterator & b,
            const Iterator & e,
            variable_type_filter = variable_type_filter::all() ) [inline], [explicit]
12.30.3 Member Function Documentation
12.30.3.1 add() [1/3] template<typename Iterator >
void carl::carlVariables::add (
            const Iterator & b,
            const Iterator & e ) [inline]
12.30.3.2 add() [2/3] void carl::carlVariables::add (
            std::initializer\_list < Variable > i ) [inline]
12.30.3.3 add() [3/3] void carl::carlVariables::add (
            Variable v ) [inline]
12.30.3.4 arithmetic() auto carl::carlVariables::arithmetic ( ) const [inline]
12.30.3.5 as_set() std::set<Variable> carl::carlVariables::as_set () const [inline]
```

```
12.30.3.6 as_vector() const std::vector<Variable>& carl::carlVariables::as_vector ( ) const
[inline]
12.30.3.7 begin() [1/2] auto carl::carlVariables::begin ( ) [inline]
12.30.3.8 begin() [2/2] auto carl::carlVariables::begin ( ) const [inline]
12.30.3.9 bitvector() auto carl::carlVariables::bitvector ( ) const [inline]
12.30.3.10 boolean() auto carl::carlVariables::boolean ( ) const [inline]
12.30.3.11 clear() void carl::carlVariables::clear ( ) [inline]
12.30.3.12 empty() bool carl::carlVariables::empty ( ) const [inline]
12.30.3.13 end() [1/2] auto carl::carlVariables::end ( ) [inline]
12.30.3.14 end() [2/2] auto carl::carlVariables::end ( ) const [inline]
12.30.3.15 erase() void carl::carlVariables::erase (
             Variable v) [inline]
12.30.3.16 filter() carlVariables carl::carlVariables::filter (
             \label{lem:const} \mbox{variable\_type\_filter \&\& $f$ ) const [inline]}
```

```
12.30.3.17 has() bool carl::carlVariables::has (
            Variable var ) const [inline]
12.30.3.18 integer() auto carl::carlVariables::integer ( ) const [inline]
12.30.3.19 real() auto carl::carlVariables::real ( ) const [inline]
12.30.3.20 size() std::size_t carl::carlVariables::size ( ) const [inline]
12.30.3.21 uninterpreted() auto carl::carlVariables::uninterpreted ( ) const [inline]
12.30.4 Friends And Related Function Documentation
12.30.4.1 operator<< std::ostream& operator<< (
            std::ostream & os,
            const carlVariables & vars ) [friend]
12.30.4.2 operator== bool operator== (
            const carlVariables & lhs,
            const carlVariables & rhs ) [friend]
12.31 carl::characteristic < type > Struct Template Reference
Type trait for the characteristic of the given field (template argument).
#include <typetraits.h>
12.31.1 Detailed Description
```

See also

template<typename type> struct carl::characteristic< type >

UnivariatePolynomial - squareFreeFactorization for example.

Type trait for the characteristic of the given field (template argument).

# 12.32 carl::Chebyshev < Number > Struct Template Reference

Implements a generator for Chebyshev polynomials.

```
#include <Chebyshev.h>
```

#### **Public Member Functions**

- Chebyshev (Variable v)
- UnivariatePolynomial < Number > operator() (std::size\_t n) const

## **Data Fields**

Variable mVar

### 12.32.1 Detailed Description

```
template<typename Number>
struct carl::Chebyshev< Number>
```

Implements a generator for Chebyshev polynomials.

## 12.32.2 Constructor & Destructor Documentation

### 12.32.3 Member Function Documentation

## 12.32.4 Field Documentation

```
12.32.4.1 mVar template<typename Number > Variable carl::Chebyshev< Number >::mVar
```

## 12.33 carl::checking < Number > Struct Template Reference

```
#include <checking.h>
```

## **Static Public Member Functions**

```
• static Number pos_inf ()
```

- static Number neg\_inf ()
- static Number nan ()
- static bool is\_nan (const Number &)
- static Number empty\_lower ()
- static Number empty\_upper ()
- static bool is\_empty (const Number &\_left, const Number &\_right)

### 12.33.1 Member Function Documentation

```
12.33.1.6 neg_inf() template<typename Number >
static Number carl::checking< Number >::neg_inf ( ) [inline], [static]

12.33.1.7 pos_inf() template<typename Number >
static Number carl::checking< Number >::pos_inf ( ) [inline], [static]
```

## 12.34 carl::checkpoints::CheckpointVector Class Reference

```
#include <CheckpointVerifier.h>
```

#### **Public Member Functions**

- CheckpointVector ()
- · const std::string & description () const
- bool forced () const
- template<typename T >
   const T & data () const
- template<typename T >
   const T \* try\_data () const
- · bool valid () const
- void next ()
- template<typename... Args>
   void add (const std::string &description, bool forced, Args &&... args)
- void clear ()

## **Data Fields**

- bool mayExceed = true
- bool printDebug = true

### 12.34.1 Constructor & Destructor Documentation

```
\textbf{12.34.1.1} \quad \textbf{CheckpointVector()} \quad \texttt{carl::checkpoints::CheckpointVector::CheckpointVector ()} \quad \texttt{[inline]}
```

## 12.34.2 Member Function Documentation

```
12.34.2.2 clear() void carl::checkpoints::CheckpointVector::clear ( ) [inline]
12.34.2.3 data() template<typename T >
const T& carl::checkpoints::CheckpointVector::data ( ) const [inline]
12.34.2.4 description() const std::string@ carl::checkpoints::CheckpointVector::description ( )
const [inline]
12.34.2.5 forced() bool carl::checkpoints::CheckpointVector::forced ( ) const [inline]
12.34.2.6 next() void carl::checkpoints::CheckpointVector::next ( ) [inline]
12.34.2.7 try_data() template<typename T >
const T* carl::checkpoints::CheckpointVector::try_data ( ) const [inline]
12.34.2.8 valid() bool carl::checkpoints::CheckpointVector::valid ( ) const [inline]
12.34.3 Field Documentation
12.34.3.1 mayExceed bool carl::checkpoints::CheckpointVector::mayExceed = true
12.34.3.2 printDebug bool carl::checkpoints::CheckpointVector::printDebug = true
12.35 carl::checkpoints::CheckpointVerifier Class Reference
#include <CheckpointVerifier.h>
```

### **Public Member Functions**

- CheckpointVerifier ()
- template<typename... Args>
   void push (const std::string &channel, const std::string &description, bool forced, Args &&... args)
- template<typename... Args> bool check (const std::string &channel, const std::string &description, Args &&... args)
- template<typename... Args>
   void expect (const std::string &channel, const std::string &description, Args &&... args)
- void clear (const std::string &channel)
- bool & mayExceed (const std::string &channel)
- bool & printDebug (const std::string &channel)

#### **Static Public Member Functions**

static CheckpointVerifier & getInstance ()

Returns the single instance of this class by reference.

#### 12.35.1 Constructor & Destructor Documentation

```
12.35.1.1 CheckpointVerifier() carl::checkpoints::CheckpointVerifier::CheckpointVerifier () [inline]
```

#### 12.35.2 Member Function Documentation

```
12.35.2.2 clear() void carl::checkpoints::CheckpointVerifier::clear ( const std::string & channel ) [inline]
```

```
12.35.2.4 getInstance() static CheckpointVerifier & carl::Singleton< CheckpointVerifier >← ::getInstance ( ) [inline], [static], [inherited]
```

Returns the single instance of this class by reference.

If there is no instance yet, a new one is created.

## 12.36 carl::tree\_detail::ChildrenIterator< T, reverse > Struct Template Reference

Iterator class for iterations over all children of a given element.

Args &&... args ) [inline]

```
#include <carlTree.h>
```

bool forced,

## **Public Types**

using Base = BaseIterator < T, ChildrenIterator < T, reverse >, reverse >

## **Public Member Functions**

- ChildrenIterator (const tree< T > \*t, std::size\_t base, bool end=false)
- ChildrenIterator & next ()
- · ChildrenIterator & previous ()
- $\bullet \;\; {\sf template}{<} {\sf typename} \; {\sf It} >$

ChildrenIterator (const BaseIterator < T, It, reverse > &ii)

- ChildrenIterator (const ChildrenIterator &ii)
- · ChildrenIterator (ChildrenIterator &&ii)
- ChildrenIterator & operator= (const ChildrenIterator &it)
- ChildrenIterator & operator= (ChildrenIterator &&it) noexcept
- virtual ~ChildrenIterator () noexcept=default
- const auto & nodes () const
- const auto & node (std::size\_t id) const
- const auto & curnode () const
- std::size\_t depth () const
- std::size\_t id () const
- bool isRoot () const
- bool isValid () const
- T \* operator-> ()
- T const \* operator-> () const

### **Data Fields**

- std::size\_t parent
- · std::size\_t current

#### **Protected Attributes**

const tree< T > \* mTree

### 12.36.1 Detailed Description

```
template<typename T, bool reverse = false> struct carl::tree_detail::ChildrenIterator< T, reverse >
```

Iterator class for iterations over all children of a given element.

### 12.36.2 Member Typedef Documentation

```
12.36.2.1 Base template<typename T , bool reverse = false>
using carl::tree_detail::ChildrenIterator< T, reverse >::Base = BaseIterator<T,ChildrenIterator<T,reverse>,r
```

### 12.36.3 Constructor & Destructor Documentation

```
12.36.3.4 ChildrenIterator() [4/4] template<typename T , bool reverse = false>
carl::tree_detail::ChildrenIterator< T, reverse >::ChildrenIterator (
             ChildrenIterator< T, reverse > && ii ) [inline]
12.36.3.5 ~ ChildrenIterator() template<typename T , bool reverse = false>
virtual carl::tree_detail::ChildrenIterator< T, reverse >::~ChildrenIterator ( ) [virtual],
[default], [noexcept]
12.36.4 Member Function Documentation
12.36.4.1 curnode() const auto& carl::tree_detail::BaseIterator< T, ChildrenIterator< T, false
> , reverse >::curnode ( ) const [inline], [inherited]
12.36.4.2 depth() std::size_t carl::tree_detail::BaseIterator< T, ChildrenIterator< T, false >
, reverse >::depth ( ) const [inline], [inherited]
12.36.4.3 id() std::size_t carl::tree_detail::BaseIterator< T, ChildrenIterator< T, false > ,
reverse >::id ( ) const [inline], [inherited]
12.36.4.4 isRoot() bool carl::tree_detail::BaseIterator< T, ChildrenIterator< T, false > ,
reverse >::isRoot ( ) const [inline], [inherited]
12.36.4.5 isValid() bool carl::tree_detail::BaseIterator< T, ChildrenIterator< T, false > ,
reverse >::isValid ( ) const [inline], [inherited]
12.36.4.6 next() template<typename T , bool reverse = false>
ChildrenIterator& carl::tree_detail::ChildrenIterator< T, reverse >::next ( ) [inline]
12.36.4.7 node() const auto@ carl::tree_detail::BaseIterator< T, ChildrenIterator< T, false >
, reverse >::node (
             std::size_t id ) const [inline], [inherited]
```

```
12.36.4.8 nodes() const auto@ carl::tree_detail::BaseIterator< T, ChildrenIterator< T, false
> , reverse >::nodes ( ) const [inline], [inherited]
12.36.4.9 operator->() [1/2] T* carl::tree_detail::BaseIterator< T, ChildrenIterator< T, false
> , reverse >::operator-> ( ) [inline], [inherited]
12.36.4.10 operator->() [2/2] T const* carl::tree_detail::BaseIterator< T, ChildrenIterator< T,
\verb|false>|, reverse>::operator->|(|)| const [inline], [inherited]|
12.36.4.11 operator=() [1/2] template<typename T , bool reverse = false>
ChildrenIterator& carl::tree_detail::ChildrenIterator< T, reverse >::operator= (
             {\tt ChildrenIterator} < {\tt T, reverse} > \&\& it ) \quad [{\tt inline}], \; [{\tt noexcept}]
12.36.4.12 operator=() [2/2] template<typename T , bool reverse = false>
ChildrenIterator& carl::tree_detail::ChildrenIterator< T, reverse >::operator= (
             const ChildrenIterator< T, reverse > & it ) [inline]
12.36.4.13 previous() template<typename T , bool reverse = false>
ChildrenIterator& carl::tree_detail::ChildrenIterator< T, reverse >::previous ( ) [inline]
12.36.5 Field Documentation
12.36.5.1 current std::size_t carl::tree_detail::BaseIterator< T, ChildrenIterator< T, false >
, reverse >::current [inherited]
12.36.5.2 mTree const tree<T>* carl::tree_detail::BaseIterator< T, ChildrenIterator< T, false
> , reverse >::mTree [protected], [inherited]
12.36.5.3 parent template < typename T , bool reverse = false >
std::size_t carl::tree_detail::ChildrenIterator< T, reverse >::parent
```

## 12.37 carl::CMakeOptionPrinter Struct Reference

#include <CompileInfo.h>

### **Data Fields**

· bool advanced

#### 12.37.1 Field Documentation

12.37.1.1 advanced bool carl::CMakeOptionPrinter::advanced

## 12.38 carl::formula::symmetry::ColorGenerator < Number > Class Template Reference

Provides unique ids (colors) for all kinds of different objects in the formula: variable types, relations, formula types, numbers, special colors and indexes.

#include <SymmetryFinder.h>

## **Public Member Functions**

- unsigned next () const
- unsigned operator() (carl::VariableType v)
- unsigned operator() (carl::Relation v)
- unsigned operator() (carl::FormulaType v)
- unsigned operator() (const Number &v)
- $\bullet \ unsigned \ operator() \ (SpecialColors \ v) \\$
- unsigned operator() (std::size\_t v)

## 12.38.1 Detailed Description

template<typename Number> class carl::formula::symmetry::ColorGenerator< Number >

Provides unique ids (colors) for all kinds of different objects in the formula: variable types, relations, formula types, numbers, special colors and indexes.

#### 12.38.2 Member Function Documentation

```
12.38.2.1 next() template<typename Number >
unsigned carl::formula::symmetry::ColorGenerator< Number >::next ( ) const [inline]
12.38.2.2 operator()() [1/6] template<typename Number >
unsigned carl::formula::symmetry::ColorGenerator< Number >::operator() (
            carl::FormulaType v ) [inline]
12.38.2.3 operator()() [2/6] template<typename Number >
unsigned carl::formula::symmetry::ColorGenerator< Number >::operator() (
            carl::Relation v ) [inline]
12.38.2.4 operator()() [3/6] template<typename Number >
unsigned carl::formula::symmetry::ColorGenerator< Number >::operator() (
            carl::VariableType v ) [inline]
12.38.2.5 operator()() [4/6] template<typename Number >
unsigned carl::formula::symmetry::ColorGenerator< Number >::operator() (
            const Number & v ) [inline]
12.38.2.6 operator()() [5/6] template<typename Number >
unsigned carl::formula::symmetry::ColorGenerator< Number >::operator() (
            SpecialColors v ) [inline]
12.38.2.7 operator()() [6/6] template<typename Number >
unsigned carl::formula::symmetry::ColorGenerator< Number >::operator() (
            std::size_t v) [inline]
```

# 12.39 carl::CompactTree < Entry, FastIndex > Class Template Reference

This class packs a complete binary tree in a vector.

```
#include <CompactTree.h>
```

#### **Data Structures**

• class Node

### **Public Member Functions**

- CompactTree (std::size\_t initialCapacity=0)
- CompactTree (const CompactTree &tree, std::size\_t minCapacity=0)
- ∼CompactTree ()
- Entry & operator[] (Node n)
- const Entry & operator[] (Node n) const
- bool empty () const
- std::size\_t size () const
- std::size\_t capacity () const
- · Node lastLeaf () const
- void pushBack (const Entry &value)
- void pushBackWithCapacity (const Entry &value)
- void popBack ()
- bool hasFreeCapacity (size\_t extraCapacity) const
- void increaseCapacity ()
- void swap (CompactTree &tree)
- · void print (std::ostream &out) const
- void clear ()
- std::size\_t getMemoryUse () const
- bool isValid () const
- std::vector< Entry > getCopy () const

### 12.39.1 Detailed Description

template<class Entry, bool FastIndex> class carl::CompactTree< Entry, FastIndex >

This class packs a complete binary tree in a vector.

The idea is to have the root at index 1, and then the left child of node n will be at index 2n and the right child will be at index 2n + 1. The corresponding formulas when indexes start at 0 take more computation, so we need a 1-based array so we can't use std::vector.

Also, when sizeof(Entry) is a power of 2 it is faster to keep track of i \* sizeof(Entry) than directly keeping track of an index i. This doesn't work well when sizeof(Entry) is not a power of two. So we need both possibilities. That is why this class never exposes indexes. Instead you interact with Node objects that serve the role of an index, but the precise value it stores is encapsulated. This way you can't do something like \_array[i \* sizeof(Entry)] by accident. Client code also does not need to (indeed, can't) be aware of how indexes are calculated, stored and looked up.

If FastIndex is false, then Nodes contain an index i. If FastIndex is true, then Nodes contain the byte offset i \* sizeof(Entry). FastIndex must be false if sizeof(Entry) is not a power of two.

## 12.39.2 Constructor & Destructor Documentation

```
12.39.2.2 CompactTree() [2/2] template<class Entry , bool FastIndex>
carl::CompactTree< Entry, FastIndex >::CompactTree (
             const CompactTree< Entry, FastIndex > & tree,
             std::size_t minCapacity = 0 )
12.39.2.3 ~CompactTree() template<class Entry , bool FastIndex>
carl::CompactTree< Entry, FastIndex >::~CompactTree ( ) [inline]
12.39.3 Member Function Documentation
12.39.3.1 capacity() template < class Entry , bool FastIndex>
std::size.t carl::CompactTree< Entry, FastIndex >::capacity ( ) const [inline]
12.39.3.2 clear() template<class E , bool FI>
void carl::CompactTree< E, FI >::clear
12.39.3.3 empty() template<class Entry , bool FastIndex>
bool carl::CompactTree< Entry, FastIndex >::empty ( ) const [inline]
\textbf{12.39.3.4} \quad \textbf{getCopy()} \quad \texttt{template}{<} \texttt{class} \; \texttt{Entry} \; \text{, bool FastIndex}{>}
std::vector<Entry> carl::CompactTree< Entry, FastIndex >::getCopy ( ) const [inline]
12.39.3.5 getMemoryUse() template<class E , bool FI>
size_t carl::CompactTree< E, FI >::getMemoryUse
12.39.3.6 hasFreeCapacity() template<class E , bool FI>
bool carl::CompactTree< E, FI >::hasFreeCapacity (
             size_t extraCapacity ) const
```

```
12.39.3.7 increaseCapacity() template<class E , bool FI>
void carl::CompactTree< E, FI >::increaseCapacity
12.39.3.8 isValid() template<class E , bool FI>
bool carl::CompactTree< E, FI >::isValid
12.39.3.9 lastLeaf() template<class Entry , bool FastIndex>
Node carl::CompactTree< Entry, FastIndex >::lastLeaf ( ) const [inline]
12.39.3.10 operator[]() [1/2] template<class E , bool FI>
E & carl::CompactTree< E, FI >::operator[] (
             Node n )
12.39.3.11 operator[]() [2/2] template<class E , bool FI>
const E & carl::CompactTree< E, FI >::operator[] (
            Node n ) const
12.39.3.12 popBack() template<class E , bool FI>
void carl::CompactTree< E, FI >::popBack
12.39.3.13 print() template<class E , bool FI>
void carl::CompactTree< E, FI >::print (
             std::ostream & out ) const
\textbf{12.39.3.14} \quad \textbf{pushBack()} \quad \texttt{template} < \texttt{class Entry , bool FastIndex} >
void carl::CompactTree< E, FI >::pushBack (
            const Entry & value )
12.39.3.15 pushBackWithCapacity() template<class Entry , bool FastIndex>
void carl::CompactTree< E, FI >::pushBackWithCapacity (
             const Entry & value )
```

```
12.39.3.16 size() template<class Entry , bool FastIndex> std::size.t carl::CompactTree< Entry, FastIndex >::size ( ) const [inline]
```

# 12.40 carl::CompileInfo Struct Reference

Compile time generated structure holding information about compiler and system version.

```
#include <CompileInfo.h>
```

#### **Static Public Attributes**

- static const std::string SystemName = "Linux"
- static const std::string SystemVersion = "6.1.0-0.deb11.7-amd64"
- static const std::string BuildType = "DEBUG"
- static const std::string CXXCompiler = "/usr/bin/clang++-14"
- static const std::string CXXCompilerVersion = "14.0.0"
- static const std::string GitRevisionSHA1 = ""

## 12.40.1 Detailed Description

Compile time generated structure holding information about compiler and system version.

#### 12.40.2 Field Documentation

```
12.40.2.1 BuildType const std::string carl::CompileInfo::BuildType = "DEBUG" [static]
```

```
12.40.2.2 CXXCompiler const std::string carl::CompileInfo::CXXCompiler = "/usr/bin/clang++-14" [static]
```

```
12.40.2.3 CXXCompilerVersion const std::string carl::CompileInfo::CXXCompilerVersion = "14. ← 0.0" [static]
```

```
12.40.2.4 GitRevisionSHA1 const std::string carl::CompileInfo::GitRevisionSHA1 = "" [static]
12.40.2.5 SystemName const std::string carl::CompileInfo::SystemName = "Linux" [static]
12.40.2.6 SystemVersion const std::string carl::CompileInfo::SystemVersion = "6.1.0-0.deb11.↔
7-amd64" [static]
12.41 carl::Condition Class Reference
#include <Condition.h>
Public Member Functions

    constexpr Condition ()

    constexpr Condition (std::bitset< CONDITION_SIZE > _bitset)

    constexpr Condition (std::size_t i)

12.41.1 Constructor & Destructor Documentation
12.41.1.1 Condition() [1/3] constexpr carl::Condition::Condition ( ) [inline], [constexpr]
12.41.1.2 Condition() [2/3] constexpr carl::Condition::Condition (
             std::bitset< CONDITION_SIZE > _bitset ) [inline], [constexpr]
12.41.1.3 Condition() [3/3] constexpr carl::Condition::Condition (
             std::size_t i ) [inline], [explicit], [constexpr]
12.42 carl::constant_one < T > Struct Template Reference
#include <constants.h>
```

#### **Static Public Member Functions**

static const T & get ()

#### 12.42.1 Member Function Documentation

```
12.42.1.1 get() template<typename T >
static const T& carl::constant_one< T >::get () [inline], [static]
```

## 12.43 carl::constant\_zero < T > Struct Template Reference

```
#include <constants.h>
```

#### **Static Public Member Functions**

• static const T & get ()

### 12.43.1 Member Function Documentation

```
12.43.1.1 get() template<typename T >
static const T& carl::constant_zero< T >::get () [inline], [static]
```

# 12.44 carl::Constraint< Pol > Class Template Reference

Represent a polynomial (in)equality against zero.

```
#include <Constraint.h>
```

#### **Public Member Functions**

- Constraint (bool valid=true)
- Constraint (carl::Variable::Arg var, Relation rel, const typename Pol::NumberType &bound=constant\_zero < typename Pol::NumberType >::get())
- Constraint (const Pol &lhs, Relation rel)
- Constraint (const BasicConstraint < Pol > &constraint)
- Constraint (const Constraint &constraint)
- Constraint (Constraint &&constraint) noexcept
- Constraint & operator= (const Constraint &constraint)
- Constraint & operator= (Constraint &&constraint) noexcept
- operator const BasicConstraint<  $\operatorname{Pol}>$  & () const
- operator BasicConstraint< Pol > () const
- const BasicConstraint< Pol > & constr () const

Returns the associated BasicConstraint.

- const Pol & Ihs () const
- Relation relation () const
- size\_t hash () const

- · const auto & variables () const
- const Factors< Pol > & Ihs\_factorization () const
- template < bool gatherCoeff = false >
   const VarInfo < Pol > & var\_info (const Variable variable) const
- template < bool gatherCoeff = false >
   const VarsInfo < Pol > & var\_info () const
- unsigned is\_consistent () const

Checks, whether the constraint is consistent.

- · Constraint negation () const
- uint maxDegree (const Variable &\_variable) const
- uint max\_degree () const
- Pol coefficient (const Variable &\_var, uint \_degree) const

Calculates the coefficient of the given variable with the given degree.

- bool integer\_valued () const
- bool realValued () const
- · bool hasIntegerValuedVariable () const

Checks if this constraints contains an integer valued variable.

• bool hasRealValuedVariable () const

Checks if this constraints contains an real valued variable.

• bool isPseudoBoolean () const

Determines whether the constraint is pseudo-boolean.

#### **Friends**

```
    template<typename P >
        bool operator== (const Constraint< P > &lhs, const Constraint< P > &rhs)
    template<typename P >
        bool operator< (const Constraint< P > &lhs, const Constraint< P > &rhs)
```

template<typename P >
 std::ostream & operator<< (std::ostream &os, const Constraint< P > &c)

## 12.44.1 Detailed Description

```
template<typename Pol> class carl::Constraint< Pol>
```

Represent a polynomial (in)equality against zero.

Such an (in)equality can be seen as an atomic formula/atom for the theory of real arithmetic.

#### 12.44.2 Constructor & Destructor Documentation

```
12.44.2.2 Constraint() [2/6] template<typename Pol >
carl::Constraint< Pol >::Constraint (
           carl::Variable::Arg var,
           Relation rel,
           ::get() ) [inline], [explicit]
12.44.2.3 Constraint() [3/6] template<typename Pol >
carl::Constraint< Pol >::Constraint (
           const Pol & lhs,
           Relation rel ) [inline], [explicit]
12.44.2.4 Constraint() [4/6] template<typename Pol >
carl::Constraint< Pol >::Constraint (
           const BasicConstraint < Pol > & constraint ) [inline], [explicit]
12.44.2.5 Constraint() [5/6] template<typename Pol >
carl::Constraint< Pol >::Constraint (
           const Constraint < Pol > & constraint ) [inline]
12.44.2.6 Constraint() [6/6] template<typename Pol >
carl::Constraint< Pol >::Constraint (
           Constraint < Pol > && constraint ) [inline], [noexcept]
```

### 12.44.3 Member Function Documentation

Calculates the coefficient of the given variable with the given degree.

Note, that it only computes the coefficient once and stores the result.

### **Parameters**

| ₋var    | The variable for which to calculate the coefficient.                         |
|---------|--|
| ₋degree | The according degree of the variable for which to calculate the coefficient. |

#### Returns

The ith coefficient of the given variable, where i is the given degree.

```
12.44.3.2 constr() template<typename Pol >
const BasicConstraint<Pol>& carl::Constraint< Pol >::constr () const [inline]
```

Returns the associated BasicConstraint.

```
12.44.3.3 hash() template<typename Pol > size_t carl::Constraint< Pol >::hash ( ) const [inline]
```

#### Returns

A hash value for this constraint.

```
12.44.3.4 hasIntegerValuedVariable() template<typename Pol > bool carl::Constraint< Pol >::hasIntegerValuedVariable () const [inline]
```

Checks if this constraints contains an integer valued variable.

### Returns

true, if it does; false, otherwise.

```
12.44.3.5 hasRealValuedVariable() template<typename Pol >
bool carl::Constraint< Pol >::hasRealValuedVariable ( ) const [inline]
```

Checks if this constraints contains an real valued variable.

#### Returns

true, if it does; false, otherwise.

```
12.44.3.6 integer_valued() template<typename Pol >
bool carl::Constraint< Pol >::integer_valued ( ) const [inline]
```

#### Returns

true, if it contains only integer valued variables.

```
12.44.3.7 is_consistent() template<typename Pol > unsigned carl::Constraint< Pol >::is_consistent ( ) const [inline]
```

Checks, whether the constraint is consistent.

It differs between, containing variables, consistent, and inconsistent.

#### Returns

0, if the constraint is not consistent. 1, if the constraint is consistent. 2, if the constraint still contains variables.

```
12.44.3.8 isPseudoBoolean() template<typename Pol >
bool carl::Constraint< Pol >::isPseudoBoolean ( ) const [inline]
```

Determines whether the constraint is pseudo-boolean.

### Returns

True if this constraint is pseudo-boolean. False otherwise.

```
12.44.3.9 lhs() template<typename Pol >
const Pol& carl::Constraint< Pol >::lhs ( ) const [inline]
```

## Returns

The considered polynomial being the left-hand side of this constraint. Hence, the right-hand side of any constraint is always 0.

```
12.44.3.10 lhs_factorization() template<typename Pol > const Factors<Pol>& carl::Constraint< Pol >::lhs_factorization ( ) const [inline]
```

```
12.44.3.11 max_degree() template<typename Pol >
uint carl::Constraint< Pol >::max_degree ( ) const [inline]
```

#### Returns

The maximal degree of all variables in this constraint. (Monomial-wise)

#### **Parameters**

| ₋variable 1 | The variable for which to determine the maximal degree. |
|-------------|---|
|-------------|---|

## **Returns**

The maximal degree of the given variable in this constraint. (Monomial-wise)

```
12.44.3.13 negation() template<typename Pol >
Constraint carl::Constraint< Pol >::negation ( ) const [inline]
12.44.3.14 operator BasicConstraint < Pol >() template < typename Pol >
carl::Constraint< Pol >::operator BasicConstraint< Pol > ( ) const [inline]
12.44.3.15 operator const BasicConstraint < Pol > &() template < typename Pol >
12.44.3.16 operator=() [1/2] template<typename Pol >
Constraint& carl::Constraint< Pol >::operator= (
           const Constraint < Pol > & constraint ) [inline]
12.44.3.17 operator=() [2/2] template<typename Pol >
Constraint& carl::Constraint< Pol >::operator= (
           Constraint < Pol > && constraint ) [inline], [noexcept]
12.44.3.18 realValued() template<typename Pol >
bool carl::Constraint< Pol >::realValued ( ) const [inline]
```

## Returns

true, if it contains only real valued variables.

```
12.44.3.19 relation() template<typename Pol >
Relation carl::Constraint< Pol >::relation ( ) const [inline]
```

#### Returns

The relation symbol of this constraint.

```
12.44.3.20 var_info() [1/2] template<typename Pol >
template<bool gatherCoeff = false>
const VarsInfo<Pol>& carl::Constraint< Pol >::var_info ( ) const [inline]
```

#### **Parameters**

## **Template Parameters**

gatherCoeff

## Returns

The whole variable information object. Note, that if the given variable is not in this constraints, this method fails. Furthermore, the variable information returned do provide coefficients only, if the given flag gatherCoeff is set to true.

```
12.44.3.22 variables() template<typename Pol >
const auto& carl::Constraint< Pol >::variables ( ) const [inline]
```

## Returns

A container containing all variables occurring in the polynomial of this constraint.

## 12.44.4 Friends And Related Function Documentation

```
12.44.4.1 operator< template<typename Pol >
template<typename P >
bool operator< (</pre>
            const Constraint< P > & lhs,
            const Constraint< P > & rhs ) [friend]
12.44.4.2 operator << template < typename Pol >
template<typename P >
std::ostream\& operator << (
            std::ostream & os,
            const Constraint < P > & c ) [friend]
12.44.4.3 operator== template<typename Pol >
template<typename P >
bool operator == (
            const Constraint< P > & lhs,
            const Constraint < P > & rhs) [friend]
12.45 carl::Context Class Reference
#include <Context.h>
```

## **Public Member Functions**

- Context ()=delete
- Context (const Context &ctx)
- Context (Context &&ctx)
- Context & operator= (const Context &rhs)
- Context (const std::vector < Variable > &var\_order)
- const std::vector< Variable > & variable\_ordering () const
- bool has (const Variable &var) const
- bool operator== (const Context &rhs) const

## 12.45.1 Constructor & Destructor Documentation

```
12.45.1.1 Context() [1/4] carl::Context::Context ( ) [delete]
```

```
12.45.1.2 Context() [2/4] carl::Context::Context (
             const Context & ctx ) [inline]
```

```
12.45.1.3 Context() [3/4] carl::Context::Context (
            Context && ctx ) [inline]
12.45.1.4 Context() [4/4] carl::Context::Context (
            const std::vector< Variable > & var_order ) [inline]
12.45.2 Member Function Documentation
12.45.2.1 has() bool carl::Context::has (
            const Variable & var ) const [inline]
12.45.2.2 operator=() Context& carl::Context::operator= (
            const Context & rhs ) [inline]
12.45.2.3 operator == () bool carl::Context::operator == (
            const Context & rhs ) const [inline]
12.45.2.4 variable_ordering() const std::vector<Variable>& carl::Context::variable_ordering ( )
const [inline]
12.46 carl::ContextPolynomial < Coeff, Ordering, Policies > Class Template Reference
#include <ContextPolynomial.h>
```

## **Public Types**

- using ContextType = Context
- using NumberType = typename UnderlyingNumberType < Coeff >::type

  Number type within the coefficients.
- using RootType = typename UnivariatePolynomial < NumberType >::RootType

#### **Public Member Functions**

- ContextPolynomial (const Context &context, const MultivariatePolynomial < Coeff, Ordering, Policies > &p)
- ContextPolynomial (const Context &context, const UnivariatePolynomial < MultivariatePolynomial < Coeff, Ordering, Policies >> &p)
- ContextPolynomial (Context &&context, UnivariatePolynomial< MultivariatePolynomial< Coeff, Ordering, Policies >> &&p)
- ContextPolynomial (const Context &context, const Coeff &c)
- operator MultivariatePolynomial< Coeff, Ordering, Policies > () const
- operator const UnivariatePolynomial < MultivariatePolynomial < Coeff, Ordering, Policies >> & () const
- operator UnivariatePolynomial < MultivariatePolynomial < Coeff, Ordering, Policies >> & ()
- const UnivariatePolynomial< MultivariatePolynomial< Coeff, Ordering, Policies > > & content () const
- MultivariatePolynomial < Coeff, Ordering, Policies > as\_multivariate () const
- const Context & context () const
- auto main\_var () const
- auto degree () const
- auto total\_degree () const
- auto coefficients () const
- auto lcoeff () const
- · auto normalized () const
- auto constant\_part () const

#### 12.46.1 Member Typedef Documentation

```
12.46.1.1 ContextType template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> using carl::ContextPolynomial< Coeff, Ordering, Policies >::ContextType = Context
```

```
12.46.1.2 NumberType template<typename Coeff , typename Ordering = GrLexOrdering, typename
Policies = StdMultivariatePolynomialPolicies<>>
using carl::ContextPolynomial< Coeff, Ordering, Policies >::NumberType = typename UnderlyingNumberType<Coeff;
::type
```

Number type within the coefficients.

```
12.46.1.3 RootType template<typename Coeff , typename Ordering = GrLexOrdering, typename
Policies = StdMultivariatePolynomialPolicies<>>
using carl::ContextPolynomial< Coeff, Ordering, Policies >::RootType = typename UnivariatePolynomial<NumberType
```

## 12.46.2 Constructor & Destructor Documentation

```
12.46.2.1 ContextPolynomial() [1/4] template<typename Coeff , typename Ordering = GrLexOrdering,
typename Policies = StdMultivariatePolynomialPolicies<>>
carl::ContextPolynomial< Coeff, Ordering, Policies >::ContextPolynomial (
            const Context & context,
             const MultivariatePolynomial < Coeff, Ordering, Policies > & p ) [inline]
12.46.2.2 ContextPolynomial() [2/4] template<typename Coeff , typename Ordering = GrLexOrdering,
typename Policies = StdMultivariatePolynomialPolicies<>>
carl::ContextPolynomial < Coeff, Ordering, Policies >::ContextPolynomial (
             const Context & context,
             const UnivariatePolynomial< MultivariatePolynomial< Coeff, Ordering, Policies >>
& p ) [inline]
12.46.2.3 ContextPolynomial() [3/4] template<typename Coeff , typename Ordering = GrLexOrdering,
typename Policies = StdMultivariatePolynomialPolicies<>>
carl::ContextPolynomial< Coeff, Ordering, Policies >::ContextPolynomial (
             Context && context,
             UnivariatePolynomial < MultivariatePolynomial < Coeff, Ordering, Policies >> && p
) [inline]
12.46.2.4 ContextPolynomial() [4/4] template<typename Coeff , typename Ordering = GrLexOrdering,
typename Policies = StdMultivariatePolynomialPolicies<>>
carl::ContextPolynomial< Coeff, Ordering, Policies >::ContextPolynomial (
            const Context & context,
            const Coeff & c ) [inline]
12.46.3 Member Function Documentation
12.46.3.1 as_multivariate() template<typename Coeff , typename Ordering = GrLexOrdering, typename
Policies = StdMultivariatePolynomialPolicies<>>
MultivariatePolynomial < Coeff, Ordering, Policies > carl::ContextPolynomial < Coeff, Ordering,
Policies >::as_multivariate ( ) const [inline]
12.46.3.2 coefficients() template<typename Coeff , typename Ordering = GrLexOrdering, typename
Policies = StdMultivariatePolynomialPolicies<>>
auto carl::ContextPolynomial< Coeff, Ordering, Policies >::coefficients ( ) const [inline]
```

```
12.46.3.3 constant_part() template<typename Coeff , typename Ordering = GrLexOrdering, typename
Policies = StdMultivariatePolynomialPolicies<>>
auto carl::ContextPolynomial< Coeff, Ordering, Policies >::constant.part ( ) const [inline]
12.46.3.4 content() template<typename Coeff , typename Ordering = GrLexOrdering, typename
Policies = StdMultivariatePolynomialPolicies<>>
\verb|const UnivariatePolynomial| < \verb|Coeff, Ordering, Policies| > \& carl:: \verb|ContextPolynomial| < | Coeff, Ordering, Policies| > \& carl:: \verb|ContextPolynomial| < | Coeff, Ordering, Policies| > & carl:: \verb|ContextPolynomial| < | Coeff, Ordering, Policies| > & carl:: \verb|ContextPolynomial| < | Coeff, Ordering, Policies| > & carl:: \verb|ContextPolynomial| < | Coeff, Ordering, Policies| > & carl:: \verb|ContextPolynomial| < | Coeff, Ordering, Policies| < | Coeff, Ordering, Pol
Coeff, Ordering, Policies >::content ( ) const [inline]
12.46.3.5 context() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies
= StdMultivariatePolynomialPolicies<>>
const Context& carl::ContextPolynomial< Coeff, Ordering, Policies >::context ( ) const [inline]
12.46.3.6 degree() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies
= StdMultivariatePolynomialPolicies<>>
auto carl::ContextPolynomial< Coeff, Ordering, Policies >::degree ( ) const [inline]
12.46.3.7 | Icoeff() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies
= StdMultivariatePolynomialPolicies<>>
auto carl::ContextPolynomial< Coeff, Ordering, Policies >::lcoeff ( ) const [inline]
12.46.3.8 main_var() template<typename Coeff , typename Ordering = GrLexOrdering, typename
Policies = StdMultivariatePolynomialPolicies<>>
auto carl::ContextPolynomial< Coeff, Ordering, Policies >::main_var ( ) const [inline]
12.46.3.9 normalized() template<typename Coeff , typename Ordering = GrLexOrdering, typename
Policies = StdMultivariatePolynomialPolicies<>>
auto carl::ContextPolynomial< Coeff, Ordering, Policies >::normalized ( ) const [inline]
12.46.3.10 operator const UnivariatePolynomial < MultivariatePolynomial < Coeff, Ordering, Policies
>> &() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = Std\leftrightarrow
MultivariatePolynomialPolicies<>>
carl::ContextPolynomial< Coeff, Ordering, Policies >::operator const UnivariatePolynomial<</pre>
MultivariatePolynomial < Coeff, Ordering, Policies >> & ( ) const [inline]
```

```
12.46.3.11 operator MultivariatePolynomial Coeff, Ordering, Policies >() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> carl::ContextPolynomial Coeff, Ordering, Policies >::operator MultivariatePolynomial Coeff, Ordering, Policies > () const [inline]
```

12.46.3.12 operator UnivariatePolynomial < MultivariatePolynomial < Coeff, Ordering, Policies >> &() template < typename Coeff , typename Ordering = GrLexOrdering, typename Policies = Std ← MultivariatePolynomialPolicies <>> carl::ContextPolynomial < Coeff, Ordering, Policies >::operator UnivariatePolynomial < MultivariatePolynomial < Coeff, Ordering, Policies >> & ( ) [inline]

```
12.46.3.13 total_degree() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> auto carl::ContextPolynomial< Coeff, Ordering, Policies >::total_degree ( ) const [inline]
```

# 12.47 carl::Contraction < Operator, Polynomial > Class Template Reference

#include <Contraction.h>

## **Public Member Functions**

- Contraction ()=delete
- Contraction (const Polynomial &constraint)
- Contraction (const Polynomial &constraint, const Polynomial &\_original)
- Contraction (const Contraction &)=delete
- Contraction (Contraction &&\_contraction)
- Contraction & operator= (const Contraction &)=delete
- Contraction & operator= (Contraction &&)=delete
- ∼Contraction ()
- const Polynomial & polynomial () const
- bool operator() (const Interval < double >::evalintervalmap &intervals, Variable::Arg variable, Interval < double > &resA, Interval < double > &resB, bool useNiceCenter=false, bool usePropagation=false)

#### 12.47.1 Constructor & Destructor Documentation

```
12.47.1.1 Contraction() [1/5] template<template< typename > class Operator, typename Polynomial >
    carl::Contraction< Operator, Polynomial >::Contraction ( ) [delete]
```

```
12.47.1.2 Contraction() [2/5] template<template< typename > class Operator, typename Polynomial
carl::Contraction < Operator, Polynomial >::Contraction (
            const Polynomial & constraint ) [inline]
12.47.1.3 Contraction() [3/5] template<template< typename > class Operator, typename Polynomial
carl::Contraction< Operator, Polynomial >::Contraction (
            const Polynomial & constraint,
            const Polynomial & _original ) [inline]
12.47.1.4 Contraction() [4/5] template<template< typename > class Operator, typename Polynomial
carl::Contraction< Operator, Polynomial >::Contraction (
            const Contraction< Operator, Polynomial > \& ) [delete]
12.47.1.5 Contraction() [5/5] template<template< typename > class Operator, typename Polynomial
carl::Contraction< Operator, Polynomial >::Contraction (
            Contraction< Operator, Polynomial > && _contraction ) [inline]
12.47.1.6 ~Contraction() template<template< typename > class Operator, typename Polynomial >
carl::Contraction< Operator, Polynomial >::~Contraction ( ) [inline]
12.47.2 Member Function Documentation
12.47.2.1 operator()() template<template< typename > class Operator, typename Polynomial >
bool carl::Contraction< Operator, Polynomial >::operator() (
            const Interval< double >::evalintervalmap & intervals,
            Variable::Arg variable,
            Interval< double > & resA,
            Interval< double > & resB,
            bool useNiceCenter = false,
            bool usePropagation = false ) [inline]
```

```
12.47.2.4 polynomial() template<template< typename > class Operator, typename Polynomial > const Polynomial& carl::Contraction< Operator, Polynomial >::polynomial ( ) const [inline]
```

# 12.48 carl::contractor::Contractor< Origin, Polynomial, Number > Class Template Reference

#include <Contractor.h>

## **Public Member Functions**

- Contractor (const Origin &origin, const BasicConstraint< Polynomial > &c, Variable v)
- auto var () const
- const auto & dependees () const
- const auto & origin () const
- std::vector< Interval< Number >> evaluate (const std::map< Variable, Interval< Number >> &assignment) const
- std::vector< Interval< Number >> contract (const std::map< Variable, Interval< Number >> &assignment) const

## 12.48.1 Constructor & Destructor Documentation

## 12.48.2 Member Function Documentation

```
12.48.2.1 contract() template<typename Origin , typename Polynomial , typename Number = double>
std::vector < Interval < Number > carl::contractor::Contractor < Origin, Polynomial, Number > \leftarrow
::contract (
           const std::map< Variable, Interval< Number >> & assignment ) const [inline]
12.48.2.2 dependees() template<typename Origin , typename Polynomial , typename Number =
double>
const auto& carl::contractor::Contractor< Origin, Polynomial, Number >::dependees ( ) const
[inline]
12.48.2.3 evaluate() template<typename Origin , typename Polynomial , typename Number = double>
::evaluate (
            const std::map< Variable, Interval< Number >> & assignment ) const [inline]
12.48.2.4 origin() template<typename Origin , typename Polynomial , typename Number = double>
const auto& carl::contractor::Contractor< Origin, Polynomial, Number >::origin ( ) const
[inline]
12.48.2.5 var() template<typename Origin , typename Polynomial , typename Number = double>
auto carl::contractor::Contractor< Origin, Polynomial, Number >::var ( ) const [inline]
```

## 12.49 carl::ConvertFrom< C > Class Template Reference

#include <Converter.h>

## **Public Member Functions**

- template<typename N >
   C::Number number (const N &n)
- template<typename V >
   Variable variable (const V &v)
- template<typename V >
   Monomial::Arg varpower (const V &v, std::size\_t exp)
- template<typename M >
   Monomial::Arg monomial (const M &m)
- template<typename T >
   Term< typename C::Number > term (const T &t)
- template<typename P >
   MultivariatePolynomial< typename C::Number > mpolynomial (const P &p)

## 12.49.1 Member Function Documentation

```
12.49.1.1 monomial() template<typename C >
template < typename M >
Monomial::Arg carl::ConvertFrom< C >::monomial (
             const M & m ) [inline]
12.49.1.2 mpolynomial() template<typename C >
template<typename P >
MultivariatePolynomial<typename C::Number> carl::ConvertFrom< C >::mpolynomial (
             const P & p ) [inline]
12.49.1.3 number() template<typename C >
template<typename N >
C::Number carl::ConvertFrom< C >::number (
            const N & n ) [inline]
12.49.1.4 term() template<typename C >
template<typename T >
Term<typename C::Number> carl::ConvertFrom< C >::term (
            const T & t ) [inline]
12.49.1.5 variable() template<typename C >
template<typename V >
Variable carl::ConvertFrom< C >::variable (
            const V & v ) [inline]
12.49.1.6 varpower() template<typename C >
template<typename V >
\label{local_convert} $$\operatorname{Monomial::Arg\ carl::ConvertFrom}<\ C\ >:: varpower\ (
             const V & v,
             std::size_t exp ) [inline]
```

# 12.50 carl::convert\_poly::ConvertHelper< T, S > Struct Template Reference

#include <Conversion.h>

# 12.51 carl::convert\_ran::ConvertHelper< T, S > Struct Template Reference

#include <Conversion.h>

# 12.52 carl::convert\_poly::ConvertHelper< ContextPolynomial< A, B, C>, MultivariatePolynomial< A, B, C>> Struct Template Reference

#include <Conversion.h>

## **Static Public Member Functions**

• static ContextPolynomial < A, B, C > convert (const Context &context, const MultivariatePolynomial < A, B, C > &p)

#### 12.52.1 Member Function Documentation

# 12.53 carl::convert\_poly::ConvertHelper< MultivariatePolynomial< A, B, C >, ContextPolynomial< A, B, C > > Struct Template Reference

#include <Conversion.h>

#### **Static Public Member Functions**

• static MultivariatePolynomial < A, B, C > convert (const ContextPolynomial < A, B, C > &p)

## 12.53.1 Member Function Documentation

# 12.54 carl::convertible\_to\_variant < T, Variant > Struct Template Reference

```
#include <variant_util.h>
```

#### **Static Public Attributes**

static constexpr bool value = detail::is\_from\_variant\_wrapper<std::is\_convertible, T, Variant>::value

#### 12.54.1 Field Documentation

```
12.54.1.1 value template < typename T , typename Variant > constexpr bool carl::convertible_to_variant < T, Variant >::value = detail::is_from_variant_wrapper < std ← ::is_convertible, T, Variant>::value [static], [constexpr]
```

# 12.55 carl::ConvertTo< C > Class Template Reference

```
#include <Converter.h>
```

#### **Public Member Functions**

- template<typename N >
  test C::Number number (const N &n)
- C::Variable variable (Variable::Arg v)
- C::VariablePower varpower (Variable::Arg v, std::size\_t exp)
- C::Monomial monomial (const Monomial::Arg &m)
- template<typename N >
   C::Term term (const Term< N > &t)
- • template<typename N , typename O , typename P >  $C \\ :: MPolynomial \ mpolynomial \ (const \ Multivariate Polynomial < N, O, P > \&p)$

## 12.55.1 Member Function Documentation

const MultivariatePolynomial< N, O, P > & p ) [inline]

12.55.1.3 number() template<typename C >

template<typename N >

```
test C::Number carl::ConvertTo< C>::number (
           const N & n ) [inline]
12.55.1.4 term() template<typename C >
template<typename N >
C::Term carl::ConvertTo< C >::term (
            const Term< N > & t) [inline]
12.55.1.5 variable() template<typename C >
C::Variable carl::ConvertTo< C >::variable (
            Variable::Arg v) [inline]
12.55.1.6 varpower() template<typename C >
C::VariablePower carl::ConvertTo< C >::varpower (
            Variable::Arg v,
            std::size_t exp ) [inline]
12.56 carl::convRnd< NumberType > Struct Template Reference
#include <roundingConversion.h>
Public Member Functions

    CARL_RND operator() (CARL_RND _rnd)

12.56.1 Member Function Documentation
12.56.1.1 operator()() template<typename NumberType >
CARL_RND carl::convRnd< NumberType >::operator() (
            CARL_RND _rnd ) [inline]
```

12.57 carl::CriticalPairConfiguration < Compare > Class Template Reference

#include <CriticalPairs.h>

## **Public Types**

- using Entry = CriticalPairsEntry< Compare > \*
- using CompareResult = carl::CompareResult
- using Order = Compare

# **Static Public Member Functions**

- static CompareResult compare (Entry e1, Entry e2)
- static bool cmpLessThan (CompareResult res)
- static bool cmpEqual (CompareResult res)

## **Static Public Attributes**

- static const bool supportDeduplicationWhileOrdering = false
- static const bool fastIndex = true

## 12.57.1 Member Typedef Documentation

```
12.57.1.1 CompareResult template<class Compare > using carl::CriticalPairConfiguration< Compare >::CompareResult = carl::CompareResult
```

```
12.57.1.2 Entry template<class Compare >
using carl::CriticalPairConfiguration< Compare >::Entry = CriticalPairsEntry<Compare>*
```

```
12.57.1.3 Order template<class Compare >
using carl::CriticalPairConfiguration< Compare >::Order = Compare
```

## 12.57.2 Member Function Documentation

## 12.57.3 Field Documentation

```
12.57.3.1 fastIndex template<class Compare >
const bool carl::CriticalPairConfiguration< Compare >::fastIndex = true [static]
```

```
12.57.3.2 supportDeduplicationWhileOrdering template<class Compare >
const bool carl::CriticalPairConfiguration< Compare >::supportDeduplicationWhileOrdering =
false [static]
```

# 12.58 carl::CriticalPairs < Datastructure, Configuration > Class Template Reference

A data structure to store all the SPolynomial pairs which have to be checked.

```
#include <CriticalPairs.h>
```

## **Public Member Functions**

- CriticalPairs ()
- void push (std::list< SPolPair > pairs)

Add a list of s-pairs to the list.

• SPolPair pop ()

Gets the first SPol from the data structure and removes it from the data structure.

- void elimMultiples (const Monomial::Arg &lm, const std::unordered\_map< size\_t, SPolPair > &newpairs)
  - Eliminate multiples of the given monomial.
- bool empty () const

Checks whether there are any pairs in the data structure.

· void print () const

Print the underlying data structure.

• unsigned size () const

Checks the size of the data structure.

## 12.58.1 Detailed Description

 $template < template < class > class \ Datastructure, \ class \ Configuration > \\ class \ carl:: Critical Pairs < Datastructure, \ Configuration > \\$ 

A data structure to store all the SPolynomial pairs which have to be checked.

#### 12.58.2 Constructor & Destructor Documentation

```
12.58.2.1 CriticalPairs() template<template< class > class Datastructure, class Configuration > carl::CriticalPairs< Datastructure, Configuration >::CriticalPairs ( ) [inline]
```

#### 12.58.3 Member Function Documentation

Eliminate multiples of the given monomial.

## **Parameters**



```
12.58.3.2 empty() template<template< class > class Datastructure, class Configuration > bool carl::CriticalPairs< Datastructure, Configuration >::empty ( ) const [inline]
```

Checks whether there are any pairs in the data structure.

Returns

```
12.58.3.3 pop() template<template< class > class Datastructure, class Configuration > SPolPair carl::CriticalPairs< Datastructure, Configuration >::pop ()
```

Gets the first SPol from the data structure and removes it from the data structure.

Returns

```
12.58.3.4 print() template<template< class > class Datastructure, class Configuration > void carl::CriticalPairs< Datastructure, Configuration >::print () const [inline]
```

Print the underlying data structure.

Add a list of s-pairs to the list.

**Parameters** 

pairs

```
12.58.3.6 size() template<template< class > class Datastructure, class Configuration > unsigned carl::CriticalPairs< Datastructure, Configuration >::size () const [inline]
```

Checks the size of the data structure.

Please notice that this is not necessarily the number of pairs in the data structure, as the underlying elements may be lists themselves.

Returns

# 12.59 carl::CriticalPairsEntry< Compare > Class Template Reference

A list of SPol pairs which have to be checked by the Buchberger algorithm.

```
#include <CriticalPairsEntry.h>
```

#### **Public Member Functions**

CriticalPairsEntry (std::list< SPolPair > &&pairs)

Saves the list of pairs and sorts them according the configured ordering.

· const Monomial::Arg & getSortedFirstLCM () const

Get the LCM of the first element.

· const SPolPair & getFirst () const

Get the front of the list.

• bool update ()

Removes the first element.

• std::list< SPolPair >::const\_iterator getPairsBegin () const noexcept

The const iterator to the begin.

std::list< SPolPair >::const\_iterator getPairsEnd () const noexcept

The const iterator to the end()

• std::list< SPolPair >::iterator getPairsBegin () noexcept

The iterator to the end()

std::list< SPolPair >::iterator getPairsEnd () noexcept

The iterator to the end()

• std::list< SPolPair >::iterator erase (std::list< SPolPair >::iterator it)

Removes the element at the iterator.

void print (std::ostream &os=std::cout)

## 12.59.1 Detailed Description

```
template < class Compare > class carl::CriticalPairsEntry < Compare >
```

A list of SPol pairs which have to be checked by the Buchberger algorithm.

We keep the list sorted according the compare ordering on SPol Pairs.

#### 12.59.2 Constructor & Destructor Documentation

Saves the list of pairs and sorts them according the configured ordering.

#### **Parameters**

pairs

## 12.59.3 Member Function Documentation

Removes the element at the iterator.

**Parameters** 

it The iterator to the element to be erased.

Returns

The next element.

```
12.59.3.2 getFirst() template<class Compare > const SPolPair& carl::CriticalPairsEntry< Compare >::getFirst ( ) const [inline]
```

Get the front of the list.

Returns

```
12.59.3.3 getPairsBegin() [1/2] template<class Compare > std::list<SPolPair>::const_iterator carl::CriticalPairsEntry< Compare >::getPairsBegin ( ) const [inline], [noexcept]
```

The const iterator to the begin.

Returns

begin of list

```
12.59.3.4 getPairsBegin() [2/2] template<class Compare > std::list<SPolPair>::iterator carl::CriticalPairsEntry< Compare >::getPairsBegin ( ) [inline], [noexcept]
```

The iterator to the end()

Returns

begin of list

```
12.59.3.5 getPairsEnd() [1/2] template<class Compare >
std::list<SPolPair>::const.iterator carl::CriticalPairsEntry< Compare >::getPairsEnd ( )
const [inline], [noexcept]
The const iterator to the end()
Returns
     end of list
12.59.3.6 getPairsEnd() [2/2] template<class Compare >
std::list<SPolPair>::iterator carl::CriticalPairsEntry< Compare >::getPairsEnd ( ) [inline],
[noexcept]
The iterator to the end()
Returns
     end of list
12.59.3.7 getSortedFirstLCM() template<class Compare >
const Monomial::Arg& carl::CriticalPairsEntry< Compare >::getSortedFirstLCM ( ) const [inline]
Get the LCM of the first element.
Returns
12.59.3.8 print() template<class Compare >
void carl::CriticalPairsEntry< Compare >::print (
             std::ostream & os = std::cout ) [inline]
12.59.3.9 update() template<class Compare >
bool carl::CriticalPairsEntry< Compare >::update ( ) [inline]
Removes the first element.
Returns
     empty()
```

# 12.60 carl::parser::DecimalParser< T > Struct Template Reference

Parses decimals, including floating point and scientific notation.

```
#include <parser.h>
```

# 12.60.1 Detailed Description

```
template<typename T> struct carl::parser::DecimalParser< T >
```

Parses decimals, including floating point and scientific notation.

# 12.61 carl::DefaultBuchbergerSettings Struct Reference

Standard settings used if the Buchberger object is not instantiated with another template parameter.

```
#include <Buchberger.h>
```

#### Static Public Attributes

static const bool calculateRealRadical = true

## 12.61.1 Detailed Description

Standard settings used if the Buchberger object is not instantiated with another template parameter.

#### 12.61.2 Field Documentation

```
12.61.2.1 calculateRealRadical const bool carl::DefaultBuchbergerSettings::calculateRealRadical = true [static]
```

# 12.62 carl::dependent\_bool\_type< B,... > Struct Template Reference

```
#include <SFINAE.h>
```

# 12.63 carl::tree\_detail::DepthIterator< T, reverse > Struct Template Reference

Iterator class for iterations over all elements of a certain depth.

```
#include <carlTree.h>
```

## **Public Types**

• using Base = BaseIterator < T, DepthIterator < T, reverse >, reverse >

#### **Public Member Functions**

- DepthIterator (const tree< T > \*t)
- DepthIterator (const tree< T > \*t, std::size\_t root, std::size\_t \_depth)
- DepthIterator & next ()
- DepthIterator & previous ()
- template<typename It >
  - DepthIterator (const BaseIterator< T, It, reverse > &ii)
- DepthIterator (const DepthIterator &ii)
- DepthIterator (DepthIterator &&ii)
- DepthIterator & operator= (const DepthIterator &it)
- DepthIterator & operator= (DepthIterator &&it)
- virtual ~DepthIterator () noexcept=default
- const auto & nodes () const
- const auto & node (std::size\_t id) const
- · const auto & curnode () const
- std::size\_t depth () const
- std::size\_t id () const
- bool isRoot () const
- bool isValid () const
- T \* operator-> ()
- T const \* operator-> () const

## **Data Fields**

- std::size\_t depth
- std::size\_t current

# **Protected Attributes**

const tree< T > \* mTree

## 12.63.1 Detailed Description

```
template<typename T, bool reverse = false> struct carl::tree_detail::DepthIterator< T, reverse >
```

Iterator class for iterations over all elements of a certain depth.

## 12.63.2 Member Typedef Documentation

```
12.63.2.1 Base template<typename T , bool reverse = false>
using carl::tree_detail::DepthIterator< T, reverse >::Base = BaseIterator<T,DepthIterator<T,reverse>,reverse
12.63.3 Constructor & Destructor Documentation
12.63.3.1 DepthIterator() [1/5] template<typename T , bool reverse = false>
carl::tree_detail::DepthIterator< T, reverse >::DepthIterator (
             const tree< T > * t ) [inline]
12.63.3.2 DepthIterator() [2/5] template<typename T , bool reverse = false>
carl::tree_detail::DepthIterator< T, reverse >::DepthIterator (
            const tree< T > * t,
             std::size_t root,
             std::size_t _depth ) [inline]
12.63.3.3 DepthIterator() [3/5] template<typename T , bool reverse = false>
template<typename It >
carl::tree_detail::DepthIterator< T, reverse >::DepthIterator (
            const BaseIterator< T, It, reverse > & ii ) [inline]
12.63.3.4 DepthIterator() [4/5] template<typename T , bool reverse = false>
carl::tree_detail::DepthIterator< T, reverse >::DepthIterator (
            const DepthIterator< T, reverse > & ii ) [inline]
12.63.3.5 DepthIterator() [5/5] template<typename T , bool reverse = false>
carl::tree_detail::DepthIterator< T, reverse >::DepthIterator (
             DepthIterator< T, reverse > && ii ) [inline]
12.63.3.6 \sim DepthIterator() template<typename T , bool reverse = false>
```

virtual carl::tree\_detail::DepthIterator< T, reverse >::~DepthIterator ( ) [virtual], [default],

#### 12.63.4 Member Function Documentation

[noexcept]

```
12.63.4.1 curnode() const auto@ carl::tree_detail::BaseIterator< T, DepthIterator< T, false >
, reverse >::curnode ( ) const [inline], [inherited]
\textbf{12.63.4.2} \quad \textbf{depth()} \quad \texttt{std::size\_t carl::tree\_detail::BaseIterator} < \texttt{T, DepthIterator} < \texttt{T, false} > \textbf{,}
reverse >::depth ( ) const [inline], [inherited]
12.63.4.3 id() std::size_t carl::tree_detail::BaseIterator< T, DepthIterator< T, false > ,
reverse >::id ( ) const [inline], [inherited]
12.63.4.4 isRoot() bool carl::tree_detail::BaseIterator< T, DepthIterator< T, false > , reverse
>::isRoot ( ) const [inline], [inherited]
12.63.4.5 isValid() bool carl::tree_detail::BaseIterator< T, DepthIterator< T, false > , reverse
>::isValid ( ) const [inline], [inherited]
12.63.4.6 next() template<typename T , bool reverse = false>
DepthIterator& carl::tree_detail::DepthIterator< T, reverse >::next () [inline]
12.63.4.7 node() const auto@ carl::tree_detail::BaseIterator< T, DepthIterator< T, false > ,
reverse >::node (
             std::size_t id ) const [inline], [inherited]
12.63.4.8 nodes() const auto& carl::tree_detail::BaseIterator< T, DepthIterator< T, false > ,
reverse >::nodes ( ) const [inline], [inherited]
12.63.4.9 operator->() [1/2] T* carl::tree_detail::BaseIterator< T, DepthIterator< T, false > ,
reverse >::operator-> ( ) [inline], [inherited]
```

```
12.63.4.10 operator->() [2/2] T const* carl::tree_detail::BaseIterator< T, DepthIterator< T,
false > , reverse >::operator-> ( ) const [inline], [inherited]
12.63.4.11 operator=() [1/2] template<typename T , bool reverse = false>
DepthIterator& carl::tree_detail::DepthIterator< T, reverse >::operator= (
             const DepthIterator< T, reverse > & it ) [inline]
12.63.4.12 operator=() [2/2] template<typename T , bool reverse = false>
DepthIterator& carl::tree_detail::DepthIterator< T, reverse >::operator= (
             DepthIterator< T, reverse > && it ) [inline]
12.63.4.13 previous() template<typename T , bool reverse = false>
DepthIterator& carl::tree_detail::DepthIterator< T, reverse >::previous ( ) [inline]
12.63.5 Field Documentation
\textbf{12.63.5.1} \quad \textbf{current} \quad \texttt{std::size\_t} \quad \texttt{carl::tree\_detail::BaseIterator} < \texttt{T, DepthIterator} < \texttt{T, false} > \texttt{,}
reverse >::current [inherited]
12.63.5.2 depth template<typename T , bool reverse = false>
std::size_t carl::tree_detail::DepthIterator< T, reverse >::depth
12.63.5.3 mTree const tree<T>* carl::tree_detail::BaseIterator< T, DepthIterator< T, false >
, reverse >::mTree [protected], [inherited]
12.64 carl::io::DIMACSExporter< Pol > Class Template Reference
Write formulas to the DIMAS format.
#include <DIMACSExporter.h>
```

## **Public Member Functions**

- bool operator() (const Formula < Pol > &formula)
- void clear ()

#### **Friends**

```
    template<typename P >
        std::ostream & operator<< (std::ostream &os, const DIMACSExporter< P > &de)
```

## 12.64.1 Detailed Description

```
template<typename Pol> class carl::io::DIMACSExporter< Pol>
```

Write formulas to the DIMAS format.

#### 12.64.2 Member Function Documentation

```
12.64.2.1 clear() template<typename Pol >
void carl::io::DIMACSExporter< Pol >::clear ( ) [inline]
```

## 12.64.3 Friends And Related Function Documentation

# 12.65 carl::io::DIMACSImporter< Pol > Class Template Reference

Parser for the DIMACS format.

```
#include <DIMACSImporter.h>
```

## **Public Member Functions**

• DIMACSImporter (const std::string &filename)

Load the given file.

• bool hasNext () const

Checks if there is another formula to parse.

Formula < Pol > next ()

Parses and returns the next formula (until the next reset line).

## 12.65.1 Detailed Description

```
template<typename Pol> class carl::io::DIMACSImporter< Pol>
```

Parser for the DIMACS format.

Allows for solving multiple formulas from one file by adding lines that only contain "reset".

## 12.65.2 Constructor & Destructor Documentation

Load the given file.

## 12.65.3 Member Function Documentation

```
12.65.3.1 hasNext() template<typename Pol >
bool carl::io::DIMACSImporter< Pol >::hasNext ( ) const [inline]
```

Checks if there is another formula to parse.

```
12.65.3.2 next() template<typename Pol >
Formula<Pol> carl::io::DIMACSImporter< Pol >::next () [inline]
```

Parses and returns the next formula (until the next reset line).

# 12.66 carl::DiophantineEquations< Integer > Class Template Reference

Includes the algorithms 6.2 and 6.3 from the book Algorithms for Computer Algebra by Geddes, Czaper, Labahn.

```
#include <MultivariateHensel.h>
```

#### **Public Member Functions**

- DiophantineEquations (unsigned p, unsigned k)
- std::vector< Polynomial > solveMultivariateDiophantine (const std::vector< Polynomial > &a, const MultiPoly &c, const std::map< Variable, GFNumber< Integer >> &I, unsigned d) const

Solve in the domain  $Z_{-}(p^{\wedge}k)[x_{-}!,...,x_{-}v]$  the multivariate polynomial diophantine equation sigma\_1 \* b\_1 + ...

std::vector< Polynomial > univariateDiophantine (const std::vector< Polynomial > &a, Variable::Arg x, unsigned m) const

Solve in  $Z_{-}(p^{\wedge}k)[x]$  the univariate polynomial Diophantine equation:  $s_{-}1 \times b_{-}1 + ...$ 

## 12.66.1 Detailed Description

```
template<typename Integer> class carl::DiophantineEquations< Integer >
```

Includes the algorithms 6.2 and 6.3 from the book Algorithms for Computer Algebra by Geddes, Czaper, Labahn.

The Algorithms are used to computer the Multivariate GCD.

#### 12.66.2 Constructor & Destructor Documentation

## 12.66.3 Member Function Documentation

Solve in the domain  $Z_{-}(p^{k})[x_{-},...,x_{-}v]$  the multivariate polynomial diophantine equation sigma\_1 \* b\_1 + ...

sigma\_r \* b\_r = c (mod <I $^{\wedge}$ (d+1), p $^{\wedge}$ k>) where, in terms of the given list of polynomials a\_1,...,a\_r the polynomials b\_i, i = 1,...,r, are defined by: b\_i = a\_1 \* ... \* a\_(i-1) \* a\_(i+1) \* ... \* a\_r. The unique solution sigma\_i, i = 1,...,r, will be computed such that degree(sigma\_i,x\_i) < degree(a\_i,x\_1).

Conditions: (1) p must not divide lcoeff( $a_i \mod I$ ), i = 1,...,r; (2)  $A_i \mod I$ , i = 1,...,r, must be pairwise relatively prime in  $Z_p[x_1]$ ; (3) degree( $c_i = 1,...,r$ )  $c_i = 1,...,r$ 

The prime integer p and the positive integer k must bei specified in the constructor.

#### **Parameters**

| а | A list a of r > 1 polynomials in the domain $Z_{-}(p^{\wedge}k)[x_{-}1,,x_{-}v]$ .                          |  |
|---|---|--|
| С | A polynomial c from $Z_{-}(p^{\wedge}k)[x_{-}1,,x_{-}v]$ .  |  |
| 1 | A list of equations $[x_2 = alpha_2,,x_v = alpha_v]$ .  |  |
| d | A nonnegative integer d specifying the maximum total degree with respect to x_2,,x_v of the desired result. |  |

#### Returns

The list sigma = [sigma\_1,...,sigma\_r].

## Todo implement

Solve in  $Z_{(p^k)}[x]$  the univariate polynomial Diophantine equation:  $s_1 \times b_1 + ...$ 

 $s_r \times b_r === x^m \pmod{p^k}$  where in terms of the given list a:  $[a_1, ... a_r]$  the polynomials  $b_i$  for i=1...r are defined by:  $b_i = a_1 \times ... \times a_{i+1} \times a_{i+1} \times ... \times a_r$  The unique solution  $s_1, ... s_r$ , will be computed such that  $deg(s_i) < deg(a_i)$ .

# 12.67 carl::DivisionLookupResult< Polynomial > Struct Template Reference

The result of.

#include <DivisionLookupResult.h>

## **Public Member Functions**

- DivisionLookupResult ()
- DivisionLookupResult (const DivisionLookupResult &d)
- virtual ~DivisionLookupResult ()
- $\bullet \ \, \text{DivisionLookupResult (const Polynomial *divisor, const Term} < \text{typename Polynomial::} CoeffType} > \& \text{factor})$
- bool success ()

## **Data Fields**

- const Polynomial \*const mDivisor
- $\bullet \ \, \textbf{Term} {<} \, \textbf{typename Polynomial::} \textbf{CoeffType} > \textbf{mFactor} \\$

## 12.67.1 Detailed Description

```
template<typename Polynomial> struct carl::DivisionLookupResult< Polynomial >
```

The result of.

Notice that the DivisionLookupResult does not take ownership of the elements, i.e. during destruction, nothing happens. Furthermore, if the original divisor element is erased, the divisor becomes invalid. Instances of Division LookupResults are therefore merely suitable for passing information to be directly processed.

#### 12.67.2 Constructor & Destructor Documentation

```
12.67.2.1 DivisionLookupResult() [1/3] template<typename Polynomial > carl::DivisionLookupResult< Polynomial >::DivisionLookupResult ( ) [inline]
```

```
12.67.2.2 DivisionLookupResult() [2/3] template<typename Polynomial > carl::DivisionLookupResult< Polynomial >::DivisionLookupResult ( const DivisionLookupResult< Polynomial > & d ) [inline]
```

```
12.67.2.3 ~DivisionLookupResult() template<typename Polynomial > virtual carl::DivisionLookupResult< Polynomial >::~DivisionLookupResult ( ) [inline], [virtual]
```

```
12.67.2.4 DivisionLookupResult() [3/3] template<typename Polynomial > carl::DivisionLookupResult< Polynomial >::DivisionLookupResult ( const Polynomial * divisor, const Term< typename Polynomial::CoeffType > & factor ) [inline]
```

## 12.67.3 Member Function Documentation

```
12.67.3.1 success() template<typename Polynomial >
bool carl::DivisionLookupResult< Polynomial >::success ( ) [inline]
```

## 12.67.4 Field Documentation

```
12.67.4.1 mDivisor template<typename Polynomial > const Polynomial* const carl::DivisionLookupResult< Polynomial >::mDivisor
```

```
12.67.4.2 mFactor template<typename Polynomial >
Term<typename Polynomial::CoeffType> carl::DivisionLookupResult< Polynomial >::mFactor
```

# 12.68 carl::DivisionResult< Type > Struct Template Reference

A strongly typed pair encoding the result of a division, being a quotient and a remainder.

```
#include <Division.h>
```

## **Data Fields**

- Type quotient
- · Type remainder

## 12.68.1 Detailed Description

```
\label{template} \begin{tabular}{ll} template < typename Type > \\ struct carl:: DivisionResult < Type > \\ \end{tabular}
```

A strongly typed pair encoding the result of a division, being a quotient and a remainder.

## 12.68.2 Field Documentation

```
12.68.2.1 quotient template<typename Type > Type carl::DivisionResult< Type >::quotient
```

```
12.68.2.2 remainder template<typename Type > Type carl::DivisionResult< Type >::remainder
```

# 12.69 carl::settings::duration Struct Reference

Helper type to parse duration as std::chrono values with boost::program\_options.

```
#include <settings_utils.h>
```

#### **Public Member Functions**

- duration ()=default
- template<typename... Args>
   constexpr duration (Args &&... args)
- template<typename R, typename P >
   constexpr operator std::chrono::duration< R, P > () const

## 12.69.1 Detailed Description

Helper type to parse duration as std::chrono values with boost::program\_options.

Intended usage:

- · use boost to parse values as durations
- access values with std::chrono::seconds(d)

#### 12.69.2 Constructor & Destructor Documentation

```
12.69.2.1 duration() [1/2] carl::settings::duration::duration ( ) [default]
```

```
12.69.2.2 duration() [2/2] template<typename... Args> constexpr carl::settings::duration::duration (

Args &&... args ) [inline], [constexpr]
```

## 12.69.3 Member Function Documentation

```
12.69.3.1 operator std::chrono::duration < R, P > () template < typename R , typename P > constexpr carl::settings::duration::operator std::chrono::duration < R, P > ( ) const [inline], [explicit], [constexpr]
```

# 12.70 carl::EEA< IntegerType > Struct Template Reference

Extended euclidean algorithm for numbers.

```
#include <EEA.h>
```

## **Static Public Member Functions**

- static std::pair< IntegerType, IntegerType > calculate (const IntegerType &a, const IntegerType &b)
- static void calculate\_recursive (const IntegerType &a, const IntegerType &b, IntegerType &s, IntegerType &t)

## 12.70.1 Detailed Description

```
template<typename IntegerType> struct carl::EEA< IntegerType >
```

Extended euclidean algorithm for numbers.

#### 12.70.2 Member Function Documentation

Todo a iterative implementation might be faster

# 12.71 carl::equal\_to < T, mayBeNull > Struct Template Reference

Alternative specialization of std::equal\_to for pointer types.

```
#include <pointerOperations.h>
```

## **Public Member Functions**

• bool operator() (const T &lhs, const T &rhs) const

# Data Fields

std::equal\_to< T > eq

## 12.71.1 Detailed Description

```
template<typename T, bool mayBeNull = true> struct carl::equal_to< T, mayBeNull >
```

Alternative specialization of std::equal\_to for pointer types.

We consider two pointers equal, if they point to the same memory location or the objects they point to are equal. Note that the memory location may also be zero.

#### 12.71.2 Member Function Documentation

## 12.71.3 Field Documentation

```
12.71.3.1 eq template<typename T , bool mayBeNull = true> std::equal.to<T> carl::equal.to< T, mayBeNull >::eq
```

# 12.72 std::equal\_to< carl::Monomial::Arg > Struct Reference

```
#include <Monomial.h>
```

## **Public Member Functions**

• bool operator() (const carl::Monomial::Arg &lhs, const carl::Monomial::Arg &rhs) const

#### 12.72.1 Member Function Documentation

# 12.73 carl::equal\_to< std::shared\_ptr< T >, mayBeNull > Struct Template Reference

```
#include <pointerOperations.h>
```

#### **Public Member Functions**

• bool operator() (const std::shared\_ptr< const T > &lhs, const std::shared\_ptr< const T > &rhs) const

### 12.73.1 Member Function Documentation

# 12.74 carl::equal\_to < T \*, mayBeNull > Struct Template Reference

```
#include <pointerOperations.h>
```

# **Public Member Functions**

bool operator() (const T \*lhs, const T \*rhs) const

#### 12.74.1 Member Function Documentation

# 12.75 carl::io::helper::ErrorHandler Struct Reference

```
#include <SpiritHelper.h>
```

## **Data Structures**

struct result

#### **Public Member Functions**

template<typename T1, typename T2 >
 qi::error\_handler\_result operator() (T1 b, T1 e, T1 where, T2 const &what) const

## 12.75.1 Member Function Documentation

# 12.76 carl::contractor::Evaluation < Polynomial > Class Template Reference

Represents a contraction operation of the form.

```
#include <Contractor.h>
```

### **Public Member Functions**

- template<typename Number >
   void normalize (std::vector< Interval< Number >> &intervals) const
- Evaluation (const Polynomial &p, Variable v)
- auto var () const
- const auto & numerator () const
- · const auto & denominator () const
- auto root () const
- · const auto & dependees () const
- template<typename Number >
   std::vector< Interval< Number >> evaluate (const std::map< Variable, Interval< Number >> &assignment, const Interval< Number > &h=Interval< Number >(0, 0)) const

Evaluate this contraction over the given assignment.

## 12.76.1 Detailed Description

```
template<typename Polynomial> class carl::contractor::Evaluation< Polynomial >
```

Represents a contraction operation of the form.

mRoot'th root of (mNumerator / mDenominator)

#### 12.76.2 Constructor & Destructor Documentation

```
12.76.2.1 Evaluation() template<typename Polynomial > carl::contractor::Evaluation<br/>Polynomial >::Evaluation<br/>( const Polynomial & p,
Variable v ) [inline]
```

## 12.76.3 Member Function Documentation

Evaluate this contraction over the given assignment.

Returns a list of resulting intervals.

Allows to integrate a relation symbol as follows:

- Transform relation into an interval (e.g. < 0 to = (-oo, 0))</li>
- Transform constraint to equality (e.g. p\*x q < 0 to p\*x q = h)
- Evaluate with respect to interval h (e.g. x = (q + h) / p)

```
12.76.3.5 numerator() template<typename Polynomial >
const auto& carl::contractor::Evaluation< Polynomial >::numerator ( ) const [inline]

12.76.3.6 root() template<typename Polynomial >
auto carl::contractor::Evaluation< Polynomial >::root ( ) const [inline]

12.76.3.7 var() template<typename Polynomial >
auto carl::contractor::Evaluation< Polynomial >::var ( ) const [inline]
```

# 12.77 carl::io::parser::ExpressionParser< Pol > Struct Template Reference

#include <ExpressionParser.h>

#### **Data Structures**

- · class perform\_addition
- class perform\_division
- class perform\_multiplication
- class perform\_negate
- class perform\_power
- class perform\_subtraction
- class print\_expr\_type

# **Public Types**

- typedef Pol::CoeffType CoeffType
- using expr\_type = ExpressionType < Pol >

## **Public Member Functions**

- ExpressionParser ()
- void addVariable (Variable::Arg v)

# 12.77.1 Member Typedef Documentation

```
12.77.1.1 CoeffType template<typename Pol >
typedef Pol::CoeffType carl::io::parser::ExpressionParser< Pol >::CoeffType
```

```
12.77.1.2 expr_type template<typename Pol >
using carl::io::parser::ExpressionParser< Pol >::expr_type = ExpressionType<Pol>
```

#### 12.77.2 Constructor & Destructor Documentation

```
12.77.2.1 ExpressionParser() template<typename Pol > carl::io::parser::ExpressionParser< Pol >::ExpressionParser ( ) [inline]
```

Tokens

Rules

## 12.77.3 Member Function Documentation

# 12.78 carl::EZGCD< Coeff, Ordering, Policies > Class Template Reference

Extended Zassenhaus algorithm for multivariate GCD calculation.

```
#include <EZGCD.h>
```

# **Public Member Functions**

- EZGCD (const MultivariatePolynomial < Coeff, Ordering, Policies > &p1, const MultivariatePolynomial < Coeff, Ordering, Policies > &p2)
- Result calculate (bool approx=true)

## 12.78.1 Detailed Description

```
template<typename Coeff, typename Ordering = GrLexOrdering, typename Policies = StdMultivariate

PolynomialPolicies<>>>
class carl::EZGCD< Coeff, Ordering, Policies >
```

Extended Zassenhaus algorithm for multivariate GCD calculation.

## 12.78.2 Constructor & Destructor Documentation

### 12.78.3 Member Function Documentation

#### **Parameters**

approx

Returns

# 12.79 carl::Factorization < P > Class Template Reference

#include <PolynomialFactorizationPair.h>

## **Public Member Functions**

- std::pair< typename super::iterator, bool > insert (typename super::const\_iterator \_hint, const std::pair
   FactorizedPolynomial
   P >, carl::exponent > &\_val)
- super::iterator insert (typename super::const\_iterator \_hint, std::pair< FactorizedPolynomial< P >, carl::exponent > &&\_val)
- std::pair< typename super::iterator, bool > insert (const std::pair< FactorizedPolynomial< P >, carl::exponent > &\_val)
- std::pair< typename super::iterator, bool > insert (std::pair< FactorizedPolynomial< P >, carl::exponent > &&\_val)
- void insert (typename super::const\_iterator \_first, typename super::const\_iterator \_last)

## **Data Fields**

K keys

STL member.

• T elements

STL member.

## 12.79.1 Member Function Documentation

```
12.79.1.1 insert() [1/5] template<typename P >
std::pair<typename super::iterator, bool> carl::Factorization< P >::insert (
            const std::pair< FactorizedPolynomial< P >, carl::exponent > & _val ) [inline]
12.79.1.2 insert() [2/5] template<typename P >
std::pair<typename super::iterator, bool> carl::Factorization< P >::insert (
            std::pair< FactorizedPolynomial< P >, carl::exponent > && _val ) [inline]
12.79.1.3 insert() [3/5] template<typename P >
void carl::Factorization< P >::insert (
            typename super::const_iterator _first,
            typename super::const_iterator _last ) [inline]
12.79.1.4 insert() [4/5] template<typename P >
std::pair<typename super::iterator, bool> carl::Factorization< P >::insert (
            typename super::const_iterator _hint,
            const std::pair< FactorizedPolynomial< P >, carl::exponent > & _val ) [inline]
12.79.1.5 insert() [5/5] template<typename P >
super::iterator carl::Factorization< P >::insert (
            typename super::const_iterator _hint,
            std::pair< FactorizedPolynomial< P >, carl::exponent > && _val ) [inline]
12.79.2 Field Documentation
12.79.2.1 elements T std::map< K, T >::elements [inherited]
STL member.
12.79.2.2 keys K std::map< K, T >::keys [inherited]
STI member.
```

# 12.80 carl::FactorizationFactory < T > Class Template Reference

This class provides a cached factorization for numbers.

## 12.80.1 Detailed Description

```
template<typename T> class carl::FactorizationFactory< T >
```

This class provides a cached factorization for numbers.

# 12.81 carl::FactorizationFactory< uint > Class Reference

This class provides a cached prime factorization for std::size\_t.

```
#include <FactorizationFactory.h>
```

## **Public Member Functions**

- FactorizationFactory ()
- const std::vector< uint > & operator() (uint n)

Returns the factorization of n.

## 12.81.1 Detailed Description

This class provides a cached prime factorization for std::size\_t.

Factorizations contain all prime factors, including multiples. Additionally, we define:

- factorization(0) = {}
- factorization(1) = {1}

#### 12.81.2 Constructor & Destructor Documentation

```
12.81.2.1 FactorizationFactory() carl::FactorizationFactory< uint >::FactorizationFactory () [inline]
```

## 12.81.3 Member Function Documentation

```
12.81.3.1 operator()() const std::vector<uint>& carl::FactorizationFactory< uint >::operator() ( uint n ) [inline]
```

Returns the factorization of n.

# 12.82 carl::FactorizedPolynomial < P > Class Template Reference

#include <FactorizedPolynomial.h>

# **Public Types**

- enum ConstructorOperation: unsigned { ADD , SUB , MUL , DIV }
- using OrderedBy = typename P::OrderedBy

The ordering of the terms.

using CoeffType = typename P::CoeffType

Type of the coefficients.

using TermType = typename P::TermType

Type of the terms.

using MonomType = typename P::MonomType

Type of the monomials within the terms.

using Policy = typename P::Policy

Policies for this monomial.

using NumberType = typename UnderlyingNumberType < CoeffType >::type

Number type within the coefficients.

• using IntNumberType = typename IntegralType < NumberType >::type

Integer type associated with the number type.

- using PolyType = P
- using TermsType = typename P::TermsType
- using CACHE = Cache
   PolynomialFactorizationPair
   P >>

## **Public Member Functions**

- FactorizedPolynomial ()
- FactorizedPolynomial (const CoeffType &)
- FactorizedPolynomial (const P &\_polynomial, const std::shared\_ptr< CACHE > &, bool \_poly←
   Normalized=false)
- FactorizedPolynomial (const FactorizedPolynomial < P > &)
- FactorizedPolynomial (FactorizedPolynomial < P > &&)
- FactorizedPolynomial (const std::pair < ConstructorOperation, std::vector < FactorizedPolynomial >> &\_p)
- FactorizedPolynomial (Factorization
   P > &&\_factorization, const CoeffType &, const std::shared\_ptr
   CACHE > &)
- $\sim$ FactorizedPolynomial ()
- FactorizedPolynomial < P > & operator= (const FactorizedPolynomial < P > &)

Copies the given factorized polynomial.

- operator PolyType () const
- CACHE::Ref cacheRef () const
- std::shared\_ptr< CACHE > pCache () const
- CACHE & cache () const
- const PolynomialFactorizationPair< P > & content () const
- size\_t hash () const
- void setCoefficient (CoeffType coeff) const

Set coefficient.

- const Factorization < P > & factorization () const
- const P & polynomial () const
- const CoeffType & coefficient () const
- P polynomialWithCoefficient () const

- bool is\_constant () const
- · bool is\_one () const
- · bool is\_zero () const
- size\_t nr\_terms () const

Calculates the number of terms.

- size\_t size () const
- size\_t complexity () const
- bool is\_linear () const

Checks if the polynomial is linear.

- template<typename C = CoeffType, EnableIf< is\_subset\_of\_rationals\_type< C >> = dummy>
   CoeffType coprime\_factor () const
- template<typename C = CoeffType, EnableIf< is\_subset\_of\_rationals\_type< C >> = dummy>
   CoeffType coprime\_factor\_without\_constant () const
- FactorizedPolynomial
   P > coprime\_coefficients () const
- bool factorizedTrivially () const
- void gatherVariables (std::set< carl::Variable > &\_vars) const

Iterates through all factors and their terms to find variables occurring in this polynomial.

- std::set< Variable > gatherVariables () const
- CoeffType constant\_part () const

Retrieves the constant term of this polynomial or zero, if there is no constant term.

• size\_t total\_degree () const

Calculates the max.

CoeffType Icoeff () const

Returns the coefficient of the leading term.

• TermType Iterm () const

The leading term.

TermType trailingTerm () const

Gives the last term according to Ordering.

Variable single\_variable () const

For terms with exactly one variable, get this variable.

• bool is\_univariate () const

Checks whether only one variable occurs.

- UnivariatePolynomial CoeffType > toUnivariatePolynomial () const
- UnivariatePolynomial < FactorizedPolynomial < P > > toUnivariatePolynomial (Variable \_var) const
- bool has\_constant\_term () const

Checks if the polynomial has a constant term that is not zero.

- bool has (Variable \_var) const
- template<bool gatherCoeff>

VarInfo< FactorizedPolynomial< P >> var\_info (Variable \_var) const

• template<bool gatherCoeff>

VarsInfo< FactorizedPolynomial< P >> var\_info () const

- VarsInfo< FactorizedPolynomial< P > > var\_info () const
- Definiteness definiteness (bool \_fullEffort=true) const

Retrieves information about the definiteness of the polynomial.

• FactorizedPolynomial< P > derivative (const carl::Variable &\_var, unsigned \_nth=1) const

Derivative of the factorized polynomial wrt variable x.

FactorizedPolynomial < P > pow (unsigned \_exp) const

Raise polynomial to the power.

bool sqrt (FactorizedPolynomial < P > &\_result) const

Calculates the square of this factorized polynomial if it is a square.

template<typename C = CoeffType, EnableIf< is\_field\_type< C >> = dummy>
 FactorizedPolynomial
 P > divideBy (const CoeffType &\_divisor) const

Divides the polynomial by the given coefficient.

- DivisionResult< FactorizedPolynomial< P > > divideBy (const FactorizedPolynomial< P > &\_divisor) const

  Calculating the quotient and the remainder, such that for a given polynomial p we have p = \_divisor \* quotient + remainder
- template<typename C = CoeffType, Enablelf< is.field\_type< C >> = dummy>
   bool divideBy (const FactorizedPolynomial< P > &\_divisor, FactorizedPolynomial< P > &\_quotient) const
   Divides the polynomial by another polynomial.
- FactorizedPolynomial < P > operator- () const
- FactorizedPolynomial < P > & operator+= (const CoeffType &\_coef)
- FactorizedPolynomial < P > & operator+= (const FactorizedPolynomial < P > & fpoly)
- FactorizedPolynomial < P > & operator = (const CoeffType &\_coef)
- FactorizedPolynomial < P > & operator = (const FactorizedPolynomial < P > & fpoly)
- FactorizedPolynomial < P > & operator\*= (const CoeffType &\_coef)
- FactorizedPolynomial < P > & operator\*= (const FactorizedPolynomial < P > & fpoly)
- FactorizedPolynomial < P > & operator/= (const CoeffType &\_coef)

Calculates the quotient.

• FactorizedPolynomial < P > & operator/= (const FactorizedPolynomial < P > & fpoly)

Calculates the quotient.

- FactorizedPolynomial < P > quotient (const FactorizedPolynomial < P > &\_fdivisor) const
   Calculates the quotient.
- std::string toString (bool \_infix=true, bool \_friendlyVarNames=true) const

#### **Static Public Member Functions**

static std::shared\_ptr< CACHE > chooseCache (std::shared\_ptr< CACHE > \_pCacheA, std::shared\_ptr<</li>
 CACHE > \_pCacheB)

Choose a non-null cache from two caches.

#### **Friends**

• template<typename P1 >

Factorization< P1 > gcd (const PolynomialFactorizationPair< P1 > &\_pfPairA, const PolynomialFactorizationPair< P1 > &\_pfPairB, Factorization< P1 > &\_restA, Factorization< P1 > &\_rest2B, bool &\_pfPairARefined, bool &\_pfPairBRefined)

• template<typename P1 >

bool existsFactorization (const FactorizedPolynomial < P1 > &fpoly)

• template<typename P1 >

Coeff< P1 > distributeCoefficients (Factorization< P1 > &\_factorization)

Computes the coefficient of the factorization and sets the coefficients of all factors to 1.

template<typename P1 >

Factorization< P1 > commonDivisor (const FactorizedPolynomial< P1 > &\_fFactorizationA, const FactorizedPolynomial< P1 > &\_fFactorizationB, Factorization< P1 > &\_fFactorizationRestA, Factorization< P1 > &\_fFactorizationRestB)

Computes the common divisor with rest of two factorizations.

template<typename P1 >

 $\label{eq:polynomial} Factorized Polynomial < P1 > gcd (const Factorized Polynomial < P1 > \&\_fpolyA, const Factorized Polynomial < P1 > \&\_fpolyB, Factorized Polynomial < P1 > \&\_fpolyRestA, Factorized Polynomial < P1 > \&\_fpolyRestB)$ 

Determines the greatest common divisor of the two given factorized polynomials.

• template<typename P1 >

P1 computePolynomial (const FactorizedPolynomial < P1 > &\_fpoly)

template<typename P1 >

FactorizedPolynomial < P1 > quotient (const FactorizedPolynomial < P1 > &\_fpolyA, const FactorizedPolynomial < P1 > &\_fpolyB)

Calculates the quotient of the polynomials.

• template<typename P1 >

 $\label{eq:polynomial} Factorized Polynomial < P1 > lcm (const Factorized Polynomial < P1 > \&\_fpolyA, const Factorized Polynomial < P1 > \&\_fpolyB)$ 

Computes the least common multiple of two given polynomials.

template<typename P1 >

FactorizedPolynomial< P1 > commonDivisor (const FactorizedPolynomial< P1 > &\_fpolyA, const FactorizedPolynomial< P1 > &\_fpolyB)

• template<typename P1 >

FactorizedPolynomial < P1 > commonMultiple (const FactorizedPolynomial < P1 > &\_fpolyA, const FactorizedPolynomial < P1 > &\_fpolyB)

template<typename P1 >

 $\label{eq:polynomial} Factorized Polynomial < P1 > \gcd\left(\text{const Factorized Polynomial} < P1 > \&\_\text{fpolyA}, \text{const Factorized Polynomial} < P1 > \&\_\text{fpolyB}\right)$ 

Determines the greatest common divisor of the two given factorized polynomials.

• template<typename P1 >

std::pair < FactorizedPolynomial < P1 >, FactorizedPolynomial < P1 > > lazyDiv (const FactorizedPolynomial < P1 > &\_fpolyA, const FactorizedPolynomial < P1 > &\_fpolyB)

Divides each of the two given factorized polynomials by their common factors of their (partial) factorization.

template<typename P1 >

FactorizedPolynomial < P1 > > factor (const FactorizedPolynomial < P1 > &\_fpoly)

template<typename P1 >

 $\label{eq:polynomial} Factorized Polynomial < P1 > operator + (const Factorized Polynomial < P1 > \&\_lhs, const Factorized Polynomial < P1 > \&\_rhs)$ 

template<typename P1 >

FactorizedPolynomial < P1 > operator+ (const FactorizedPolynomial < P1 > &\_lhs, const typename FactorizedPolynomial < P1 > ::CoeffType &\_rhs)

template<typename P1 >

FactorizedPolynomial < P1 > operator- (const FactorizedPolynomial < P1 > &\_lhs, const FactorizedPolynomial < P1 > &\_rhs)

• template<typename P1 >

FactorizedPolynomial < P1 > operator- (const FactorizedPolynomial < P1 > &\_lhs, const typename FactorizedPolynomial < P1 > ::CoeffType &\_rhs)

• template<typename P1 >

FactorizedPolynomial < P1 > operator\* (const FactorizedPolynomial < P1 > &\_Ihs, const FactorizedPolynomial < P1 > &\_rhs)

ullet template<typename P1 >

FactorizedPolynomial < P1 > operator\* (const FactorizedPolynomial < P1 > &\_lhs, const typename FactorizedPolynomial < P1 > ::CoeffType &\_rhs)

## 12.82.1 Member Typedef Documentation

```
12.82.1.1 CACHE template<typename P >
using carl::FactorizedPolynomial< P >::CACHE = Cache<PolynomialFactorizationPair<P> >
```

```
12.82.1.2 CoeffType template<typename P >
using carl::FactorizedPolynomial< P >::CoeffType = typename P::CoeffType
```

Type of the coefficients.

```
12.82.1.3 IntNumberType template<typename P >
using carl::FactorizedPolynomial < P >::IntNumberType = typename IntegralType<NumberType> \cdot
::type
Integer type associated with the number type.

12.82.1.4 MonomType template < typename P >
using carl::FactorizedPolynomial < P >::MonomType = typename P::MonomType
```

12.82.1.5 NumberType template<typename P >
using carl::FactorizedPolynomial< P >::NumberType = typename UnderlyingNumberType<CoeffType>←
::type

Number type within the coefficients.

Type of the monomials within the terms.

```
12.82.1.6 OrderedBy template<typename P > using carl::FactorizedPolynomial< P >::OrderedBy = typename P::OrderedBy
```

The ordering of the terms.

```
12.82.1.7 Policy template<typename P >
using carl::FactorizedPolynomial< P >::Policy = typename P::Policy
```

Policies for this monomial.

```
12.82.1.8 PolyType template<typename P >
using carl::FactorizedPolynomial< P >::PolyType = P
```

```
12.82.1.9 TermsType template<typename P >
using carl::FactorizedPolynomial< P >::TermsType = typename P::TermsType
```

```
12.82.1.10 TermType template<typename P >
using carl::FactorizedPolynomial< P >::TermType = typename P::TermType
Type of the terms.
```

#### 12.82.2 Member Enumeration Documentation

```
12.82.2.1 ConstructorOperation template<typename P > enum carl::FactorizedPolynomial::ConstructorOperation : unsigned
```

# Enumerator

| ADD |  |
|-----|--|
| SUB |  |
| MUL |  |
| DIV |  |

#### 12.82.3 Constructor & Destructor Documentation

```
12.82.3.1 FactorizedPolynomial() [1/7] template<typename P >
carl::FactorizedPolynomial < P >::FactorizedPolynomial ( )
12.82.3.2 FactorizedPolynomial() [2/7] template<typename P >
\verb|carl::FactorizedPolynomial| < P > :: FactorizedPolynomial (
             const CoeffType & ) [explicit]
12.82.3.3 FactorizedPolynomial() [3/7] template<typename P >
carl::FactorizedPolynomial < P >::FactorizedPolynomial (
             const P & _polynomial,
             const std::shared_ptr< \mathtt{CACHE} \,>\, \& ,
             bool _polyNormalized = false ) [explicit]
12.82.3.4 FactorizedPolynomial() [4/7] template<typename P >
\verb|carl::FactorizedPolynomial| < P >::FactorizedPolynomial (
             const FactorizedPolynomial< P > \& )
12.82.3.5 FactorizedPolynomial() [5/7] template<typename P >
carl::FactorizedPolynomial < P >::FactorizedPolynomial (
             FactorizedPolynomial< P > && )
12.82.3.6 FactorizedPolynomial() [6/7] template<typename P >
carl::FactorizedPolynomial < P >::FactorizedPolynomial (
            const std::pair< ConstructorOperation, std::vector< FactorizedPolynomial< P >
>> & _p ) [explicit]
```

```
12.82.3.8 \simFactorizedPolynomial() template<typename P > carl::FactorizedPolynomial< P >::\simFactorizedPolynomial ()
```

#### 12.82.4 Member Function Documentation

```
12.82.4.1 cache() template<typename P >
CACHE& carl::FactorizedPolynomial< P >::cache ( ) const [inline]
```

#### Returns

The cache used by this factorized polynomial.

```
12.82.4.2 cacheRef() template<typename P >
CACHE::Ref carl::FactorizedPolynomial< P >::cacheRef ( ) const [inline]
```

#### Returns

The reference of the entry in the cache corresponding to this factorized polynomial.

Choose a non-null cache from two caches.

### **Parameters**

| _pCacheA | First cache.  |
|----------|---------------|
| ₋pCacheB | Second cache. |

A non-null cache.

```
12.82.4.4 coefficient() template<typename P >
const CoeffType& carl::FactorizedPolynomial< P >::coefficient ( ) const [inline]
```

#### Returns

Coefficient of the polynomial.

```
12.82.4.5 complexity() template<typename P >
size_t carl::FactorizedPolynomial< P >::complexity ( ) const [inline]
```

### Returns

An approximation of the complexity of this polynomial.

```
12.82.4.6 constant_part() template<typename P >
CoeffType carl::FactorizedPolynomial< P >::constant_part ( ) const
```

Retrieves the constant term of this polynomial or zero, if there is no constant term.

@reiturn Constant term.

```
12.82.4.7 content() template<typename P >
const PolynomialFactorizationPair<P>& carl::FactorizedPolynomial< P >::content ( ) const
[inline]
```

## Returns

The entry in the cache corresponding to this factorized polynomial.

```
12.82.4.8 coprime_coefficients() template<typename P >
FactorizedPolynomial<P> carl::FactorizedPolynomial< P >::coprime_coefficients ( ) const [inline]
```

## Returns

p \* p.coprime\_factor()

### See also

coprime\_factor()

```
12.82.4.9 coprime_factor() template<typename P >
template<typename C = CoeffType, EnableIf< is_subset_of_rationals_type< C >> = dummy>
CoeffType carl::FactorizedPolynomial< P >::coprime_factor ( ) const [inline]
```

The lcm of the denominators of the coefficients in p divided by the gcd of numerators of the coefficients in p.

```
12.82.4.10 coprime_factor_without_constant() template<typename P > template<typename C = CoeffType, EnableIf< is_subset_of_rationals_type< C >> = dummy> CoeffType carl::FactorizedPolynomial< P >::coprime_factor_without_constant () const
```

#### Returns

The lcm of the denominators of the coefficients (without the constant one) in p divided by the gcd of numerators of the coefficients in p.

Retrieves information about the definiteness of the polynomial.

## Returns

Definiteness of this.

Derivative of the factorized polynomial wrt variable x.

# **Parameters**

| ₋var | main variable                          |
|------|--|
| ₋nth | how often should derivative be applied |

```
Todo only _nth == 1 is supported we do not use factorization currently
```

Divides the polynomial by the given coefficient.

Applies if the coefficients are from a field.

#### **Parameters**

\_divisor

Returns

Calculating the quotient and the remainder, such that for a given polynomial p we have  $p = \_divisor * quotient + remainder$ .

### **Parameters**

```
_divisor | Another polynomial
```

Returns

A divisionresult, holding the quotient and the remainder.

See also

Note

Division is only defined on fields

Divides the polynomial by another polynomial.

If the divisor divides this polynomial, quotient contains the result of the division and true is returned. Otherwise, false is returned and the content of quotient remains unchanged. Applies if the coefficients are from a field. Note that the quotient must not be \*this.

## **Parameters**

```
_divisor
_quotient
```

## Returns

```
12.82.4.16 factorization() template<typename P >
const Factorization<P>& carl::FactorizedPolynomial< P >::factorization ( ) const [inline]
```

## Returns

The factorization of this polynomial.

```
12.82.4.17 factorizedTrivially() template<typename P > bool carl::FactorizedPolynomial< P >::factorizedTrivially ( ) const [inline]
```

## Returns

true, if this factorized polynomial, has only itself as factor.

```
12.82.4.18 gatherVariables() [1/2] template<typename P > std::set<Variable> carl::FactorizedPolynomial< P >::gatherVariables ( ) const [inline]
```

Iterates through all factors and their terms to find variables occurring in this polynomial.

## **Parameters**

vars Holds the variables occurring in the polynomial at return.

#### **Parameters**

```
_var The variable to check for its occurrence.
```

#### Returns

true, if the variable occurs in this term.

```
12.82.4.21 has_constant_term() template<typename P >
bool carl::FactorizedPolynomial< P >::has_constant_term ( ) const
```

Checks if the polynomial has a constant term that is not zero.

## Returns

If there is a constant term unequal to zero.

```
12.82.4.22 hash() template<typename P >
size_t carl::FactorizedPolynomial< P >::hash ( ) const [inline]
```

## Returns

The hash value of the entry in the cache corresponding to this factorized polynomial.

```
12.82.4.23 is_constant() template<typename P >
bool carl::FactorizedPolynomial< P >::is_constant ( ) const [inline]
```

# Returns

true, if the factorized polynomial is constant.

```
12.82.4.24 is_linear() template<typename P >
bool carl::FactorizedPolynomial< P >::is_linear ( ) const [inline]
```

Checks if the polynomial is linear.

## Returns

If this is linear.

```
12.82.4.25 is_one() template<typename P >
bool carl::FactorizedPolynomial< P >::is_one ( ) const [inline]
```

true, if the factorized polynomial is one.

```
12.82.4.26 is_univariate() template<typename P >
bool carl::FactorizedPolynomial< P >::is_univariate ( ) const
```

Checks whether only one variable occurs.

## Returns

Notice that it might be better to use the variable information if several pieces of information are requested.

```
12.82.4.27 is_zero() template<typename P >
bool carl::FactorizedPolynomial< P >::is_zero ( ) const [inline]
```

#### Returns

true, if the factorized polynomial is zero.

Returns the coefficient of the leading term.

Notice that this is not defined for zero polynomials.

Returns

The leading term.

Returns

```
12.82.4.30 nr.terms() template<typename P > size.t carl::FactorizedPolynomial< P >::nr.terms ( ) const [inline]
```

Calculates the number of terms.

(Note, that this requires to expand the factorization and, thus, can be expensive in the case that the factorization has not yet been expanded.)

### Returns

the number of terms

```
12.82.4.31 operator PolyType() template<typename P > carl::FactorizedPolynomial< P >::operator PolyType ( ) const [inline], [explicit]
```

#### **Parameters**

| _coef The factor to mu | ultiply this factorized polynomial with. |
|------------------------|--|
|------------------------|--|

### Returns

This factorized polynomial after multiplying it with the given factor.

#### **Parameters**

```
_fpoly The factor to multiply this factorized polynomial with.
```

#### Returns

This factorized polynomial after multiplying it with the given factor.

## **Parameters**

| _coef | The summand to add this factorized polynomial with. |
|-------|---|
|       |   |

## Returns

This factorized polynomial after adding the given summand.

#### **Parameters**

| _fpoly | The summand to add this factorized polynomial with. |
|--------|---|
|--------|---|

## Returns

This factorized polynomial after adding the given summand.

```
12.82.4.36 operator-() template<typename P >
FactorizedPolynomial<P> carl::FactorizedPolynomial< P >::operator- ( ) const
```

## **Parameters**

```
_fpoly The operand.
```

## Returns

The given factorized polynomial times -1.

## **Parameters**

| _coef | The number to subtract from this factorized polynomial. |
|-------|---|
|       |   |

This factorized polynomial after subtracting the given number.

## **Parameters**

| _fpoly | The factorized polynomial to subtract from this factorized polynomial. |
|--------|--|
|--------|--|

## Returns

This factorized polynomial after adding the given factorized polynomial.

Calculates the quotient.

Notice: the divisor has to be a factor of the polynomial.

#### **Parameters**

| _coef | The divisor to divide this factorized polynomial with. |
|-------|--|
|-------|--|

## Returns

This factorized polynomial after dividing it with the given divisor.

Calculates the quotient.

Notice: the divisor has to be a factor of the polynomial.

## **Parameters**

| _fpoly | The divisor to divide this factorized polynomial with. |
|--------|--|
|--------|--|

This factorized polynomial after dividing it with the given divisor.

Copies the given factorized polynomial.

#### **Parameters**

```
The factorized polynomial to copy.
```

## Returns

A reference to the copy of the given factorized polynomial.

```
12.82.4.42 pCache() template<typename P >
std::shared_ptr<CACHE> carl::FactorizedPolynomial< P >::pCache ( ) const [inline]
```

## Returns

The cache used by this factorized polynomial.

```
12.82.4.43 polynomial() template<typename P > const P& carl::FactorizedPolynomial< P >::polynomial ( ) const [inline]
```

```
12.82.4.44 polynomialWithCoefficient() template<typename P >
P carl::FactorizedPolynomial< P >::polynomialWithCoefficient ( ) const [inline]
```

Raise polynomial to the power.

#### **Parameters**

\_exp the exponent of the power

## Returns

p^exponent

**Todo** uses multiplication -> bad idea.

Calculates the quotient.

Notice: the divisor has to be a factor of the polynomial.

#### **Parameters**

```
_fdivisor The divisor
```

# Returns

The quotient

Set coefficient.

## **Parameters**

```
coeff Coefficient
```

```
12.82.4.48 single_variable() template<typename P >
Variable carl::FactorizedPolynomial< P >::single_variable ( ) const [inline]
```

For terms with exactly one variable, get this variable.

The only variable occuring in the term.

```
12.82.4.49 size() template<typename P >
size_t carl::FactorizedPolynomial< P >::size ( ) const [inline]
```

#### Returns

A rough estimation of the size of this factorized polynomial. If it has already been expanded, the number of terms of the expanded form are returned; otherwise the number of terms in the factors.

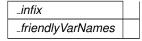
Calculates the square of this factorized polynomial if it is a square.

## **Parameters**

### Returns

true, if this factorized polynomial is a square; false, otherwise.

# Parameters



## Returns

```
12.82.4.52 total_degree() template<typename P >
size_t carl::FactorizedPolynomial< P >::total_degree ( ) const
```

Calculates the max.

degree over all monomials occurring in the polynomial. As the degree of the zero polynomial is  $-\infty$ , we assert that this polynomial is not zero. This must be checked by the caller before calling this method.

See also

?, page 48

Returns

Total degree.

```
12.82.4.53 toUnivariatePolynomial() [1/2] template<typename P >
UnivariatePolynomial<CoeffType> carl::FactorizedPolynomial< P >::toUnivariatePolynomial ( )
const [inline]
```

```
12.82.4.55 trailingTerm() template<typename P >
TermType carl::FactorizedPolynomial< P >::trailingTerm ( ) const
```

Gives the last term according to Ordering.

Notice that if there is a constant part, it is always trailing.

Returns

```
12.82.4.56 var_info() [1/3] template<typename P > template<br/>bool gatherCoeff> VarsInfo<FactorizedPolynomial<P> > carl::FactorizedPolynomial< P >::var_info () const [inline]
```

```
12.82.4.57 var_info() [2/3] template<typename P >
VarsInfo<FactorizedPolynomial<P>> carl::FactorizedPolynomial< P >::var_info ( ) const [inline]
```

#### 12.82.5 Friends And Related Function Documentation

Computes the common divisor with rest of two factorizations.

### **Parameters**

| _fFactorizationA  | The factorization of the first polynomial.  |
|---|---|
| _fFactorizationB  | The factorization of the second polynomial.   |
| _fFactorizationRestA Returns the remaining factorization of the first polynomial without the common divisor |   |
| _fFactorizationRestB  | Returns the remaining factorization of the second polynomial without the common divisor |

#### Returns

The factorization of a common divisor of the two given factorized polynomials.

# Parameters

| _fpolyA | The first factorized polynomial to compute the common divisor for. |  |
|---------|--|--|
| _fpolyB | The second factorized polynomial to compute the common divisor for |  |

A common divisor of the two given factorized polynomials.

# 

#### **Parameters**

| _fpolyA | The first factorized polynomial to compute the common multiple for.  |  |
|---------|--|--|
| _fpolyB | The second factorized polynomial to compute the common multiple for. |  |

## Returns

A common multiple of the two given factorized polynomials.

#### **Parameters**

| _fpoly | The factorized polynomial to retrieve the expanded polynomial for. |
|--------|--|
|--------|--|

## Returns

The polynomial (of the underlying polynomial type) when expanding the factorization of the given factorized polynomial.

```
12.82.5.5 distributeCoefficients template<typename P > template<typename P1 > Coeff<P1> distributeCoefficients ( Factorization < P1 > \& \_factorization ) \quad [friend]
```

Computes the coefficient of the factorization and sets the coefficients of all factors to 1.

## **Parameters**

|  | ₋factorization | The factorization. |
|--|----------------|--------------------|
|--|----------------|--------------------|

The coefficients of the whole factorization.

#### **Parameters**

#### Returns

A factorization of this factorized polynomial. (probably finer than the one factorization() returns)

Determines the greatest common divisor of the two given factorized polynomials.

The method exploits the partial factorization stored in the arguments and refines it. (c.f. Accelerating Parametric Probabilistic Verification, Section 4)

## **Parameters**

| _fpolyA   | The first factorized polynomial to compute the greatest common divisor for. |  |
|---|---|--|
| _fpolyB The second factorized polynomial to compute the greatest common divisor for |   |  |

# Returns

The greatest common divisor of the two given factorized polynomials.

Determines the greatest common divisor of the two given factorized polynomials.

The method exploits the partial factorization stored in the arguments and refines it. (c.f. Accelerating Parametric Probabilistic Verification, Section 4)

#### **Parameters**

| _fpolyA     |  |  |
|-------------|--|--|
| _fpolyB     |  |  |
| _fpolyRestA | Returns the remaining part of the first factorized polynomial without the gcd.             |  |
| _fpolyRestB | fpolyRestB Returns the remaining part of the second factorized polynomial without the good |  |

## Returns

The greatest common divisor of the two given factorized polynomials.

Divides each of the two given factorized polynomials by their common factors of their (partial) factorization.

#### **Parameters**

| _fpolyA | The first factorized polynomial.  |
|---------|-----------------------------------|
| ₋fpolyB | The second factorized polynomial. |

The pair of the resulting factorized polynomials.

Computes the least common multiple of two given polynomials.

The method refines the factorization.

#### **Parameters**

| _fpolyA | The first factorized polynomial to compute the lcm for.  |
|---------|--|
| ₋fpolyB | The second factorized polynomial to compute the lcm for. |

#### Returns

The lcm of the two given factorized polynomials.

```
12.82.5.16 operator+ [2/2] template<typename P >
template<typename P1 >
{\tt FactorizedPolynomial} < {\tt P1} > {\tt operator+} \ \ (
            const FactorizedPolynomial< P1 > & _lhs,
             const typename FactorizedPolynomial< P1 >::CoeffType & _rhs ) [friend]
12.82.5.17 operator- [1/2] template<typename P >
template<typename P1 >
FactorizedPolynomial<P1> operator- (
            const FactorizedPolynomial< P1 > & _lhs,
             const FactorizedPolynomial< P1 > & _rhs ) [friend]
12.82.5.18 operator- [2/2] template<typename P >
template<typename P1 >
FactorizedPolynomial<P1> operator- (
            const FactorizedPolynomial < P1 > & _lhs,
             const typename FactorizedPolynomial< P1 >::CoeffType & _rhs ) [friend]
12.82.5.19 quotient template<typename P >
template<typename P1 >
FactorizedPolynomial<P1> quotient (
             const FactorizedPolynomial< P1 > & _fpolyA,
             const FactorizedPolynomial< P1 > & \_fpolyB ) [friend]
```

Calculates the quotient of the polynomials.

Notice: the second polynomial has to be a factor of the first polynomial.

## **Parameters**

| _fpolyA | The dividend. |
|---------|---------------|
| _fpolyB | The divisor.  |

## Returns

The quotient

# 12.83 carl::ran::interval::FieldExtensions < Rational, Poly > Class Template Reference

This class can be used to construct iterated field extensions from a sequence of real algebraic numbers.

```
#include <FieldExtensions.h>
```

## **Public Member Functions**

- std::pair< bool, Poly > extend (Variable v, const IntRepRealAlgebraicNumber< Rational > &r)
   Extend the current number field with the field extension defined by r.
- Poly embed (const Poly &poly)

### 12.83.1 Detailed Description

```
template<typename Rational, typename Poly> class carl::ran::interval::FieldExtensions< Rational, Poly>
```

This class can be used to construct iterated field extensions from a sequence of real algebraic numbers.

In particular it makes sure that the minimal polynomials are "reduced", i.e. making sure that they are minimal polynomial w.r.t. the current extension field.

#### 12.83.2 Member Function Documentation

Extend the current number field with the field extension defined by r.

The minimal polynomial of r (with is a minimal polynomials in Q[x]) is embedded into the current number field and the minimal polynomial for r within this number field is computed. The resulting polynomial is this minimal polynomial over the current number field.

We may have one of two cases:

- We can eliminate v by substitution with some term
- · We create a new field extension and may have to reduce the lifting polynomial

In the first case, we return true and the term to substitute with. In the second case, we return false and the new minimal polynomial.

# 12.84 carl::logging::FileSink Class Reference

Logging sink for file output.

```
#include <Sink.h>
```

## **Public Member Functions**

- virtual ∼FileSink ()=default
- FileSink (const std::string &filename)

Create a FileSink that logs to the specified file.

• std::ostream & log () noexcept override

Abstract logging interface.

## 12.84.1 Detailed Description

Logging sink for file output.

## 12.84.2 Constructor & Destructor Documentation

```
12.84.2.1 ~FileSink() virtual carl::logging::FileSink::~FileSink ( ) [virtual], [default]
```

Create a FileSink that logs to the specified file.

The file is truncated upon construction.

**Parameters** 

filename

## 12.84.3 Member Function Documentation

```
12.84.3.1 log() std::ostream& carl::logging::FileSink::log ( ) [inline], [override], [virtual], [noexcept]
```

Abstract logging interface.

The intended usage is to write any log output to the output stream returned by this function.

Returns

Output stream.

Implements carl::logging::Sink.

# 12.85 carl::logging::Filter Class Reference

This class checks if some log message shall be forwarded to some sink.

```
#include <Filter.h>
```

## **Public Member Functions**

· const auto & data () const

Returns the internal filter data.

• Filter & operator() (const std::string &channel, LogLevel level)

Set the minimum log level for some channel.

• bool check (const std::string &channel, LogLevel level) const noexcept

Checks if the given log level is sufficient for the log message to be forwarded.

## **Friends**

std::ostream & operator << (std::ostream &os, const Filter &f)</li>
 Streaming operator for a Filter.

## 12.85.1 Detailed Description

This class checks if some log message shall be forwarded to some sink.

## 12.85.2 Member Function Documentation

Checks if the given log level is sufficient for the log message to be forwarded.

## **Parameters**

| channel | Channel name. |
|---------|---------------|
| level   | LogLevel.     |

## Returns

If the message shall be forwarded.

```
12.85.2.2 data() const auto& carl::logging::Filter::data ( ) const [inline]
```

Returns the internal filter data.

Set the minimum log level for some channel.

Returns \*this, hence calls to this method can be chained arbitrarily.

## **Parameters**

| channel | Channel name. |
|---------|---------------|
| level   | LogLevel.     |

## Returns

This object.

## 12.85.3 Friends And Related Function Documentation

Streaming operator for a Filter.

All the rules stored in the filter are printed in a human-readable fashion.

# **Parameters**

| os | Output stream. |
|----|----------------|
| f  | Filter.        |

# Returns

os.

# 12.86 carl::FLOAT\_T< FloatType > Class Template Reference

Templated wrapper class which allows universal usage of different IEEE 754 implementations.

```
#include <FLOAT_T.h>
```

## **Public Member Functions**

• FLOAT\_T ()

Default empty constructor, which initializes to zero.

FLOAT\_T (double \_double, CARL\_RND=CARL\_RND::N)

Constructor, which takes a double as input and optional rounding, which can be used, if the underlying fp implementation allows this.

FLOAT\_T (sint \_int, CARL\_RND=CARL\_RND::N)

Constructor, which takes an integer as input and optional rounding, which can be used, if the underlying fp implementation allows this.

- FLOAT\_T (int \_int, CARL\_RND=CARL\_RND::N)
- FLOAT\_T (unsigned \_int, CARL\_RND=CARL\_RND::N)

Constructor, which takes an unsigned integer as input and optional rounding, which can be used, if the underlying fp implementation allows this.

FLOAT\_T (const FLOAT\_T &\_float, CARL\_RND=CARL\_RND::N)

Copyconstructor which takes a FLOAT\_T<FloatType> and optional rounding as input, which can be used, if the underlying fp implementation allows this.

- FLOAT\_T (FLOAT\_T &&\_float, CARL\_RND=CARL\_RND::N) noexcept
- template<typename F = FloatType, DisableIf< std::is\_same< F, double >> = dummy>

FLOAT\_T (FloatType val, CARL\_RND=CARL\_RND::N)

Constructor, which takes an arbitrary fp type as input and optional rounding, which can be used, if the underlying fp implementation allows this.

 $\bullet \ \ template < typename \ F = Float Type, \ Enable If < carl::is\_rational\_type < F >> = dummy > type < F >$ 

FLOAT\_T (const std::string &\_string, CARL\_RND=CARL\_RND::N)

 $\bullet \ \ \text{template} < \text{typename F = FloatType, EnableIf} < \ \text{std::is\_same} < \ \text{F, double} >> \ = \ \text{dummy} >$ 

FLOAT\_T (const std::string &\_string, CARL\_RND=CARL\_RND::N)

~FLOAT\_T ()=default

Destructor.

const FloatType & value () const

Getter for the raw value contained.

• precision\_t precision () const

If precision is used, this getter returns the acutal precision (default: 53 bit).

FLOAT\_T & setPrecision (const precision\_t &)

Allows to set the desired precision.

FLOAT\_T & operator= (const FLOAT\_T &\_rhs)=default

Assignment operator.

- FLOAT\_T & operator= (const FloatType &\_rhs)
- bool operator== (const FLOAT\_T &\_rhs) const

Comparison operator for equality.

bool operator!= (const FLOAT\_T &\_rhs) const

Comparison operator for inequality.

• bool operator> (const FLOAT\_T &\_rhs) const

Comparison operator for larger than.

- bool operator> (int \_rhs) const
- bool operator> (unsigned \_rhs) const
- bool operator< (const FLOAT\_T &\_rhs) const</li>

Comparison operator for less than.

- bool operator< (int \_rhs) const
- bool operator< (unsigned \_rhs) const</li>
- bool operator<= (const FLOAT\_T &\_rhs) const</li>

Comparison operator for less or equal than.

bool operator>= (const FLOAT\_T &\_rhs) const

Comparison operator for larger or equal than.

FLOAT\_T & add\_assign (const FLOAT\_T &\_op2, CARL\_RND=CARL\_RND::N)

Function for addition of two numbers, which assigns the result to the calling number.

FLOAT\_T & add (FLOAT\_T &\_result, const FLOAT\_T &\_op2, CARL\_RND=CARL\_RND::N) const

Function which adds two numbers and puts the result in a third number passed as parameter.

FLOAT\_T & sub\_assign (const FLOAT\_T &\_op2, CARL\_RND=CARL\_RND::N)

Function for subtraction of two numbers, which assigns the result to the calling number.

FLOAT\_T & sub (FLOAT\_T &\_result, const FLOAT\_T &\_op2, CARL\_RND=CARL\_RND::N) const

Function which subtracts the righthand side from this number and puts the result in a third number passed as parameter.

FLOAT\_T & mul\_assign (const FLOAT\_T &\_op2, CARL\_RND=CARL\_RND::N)

Function for multiplication of two numbers, which assigns the result to the calling number.

FLOAT\_T & mul (FLOAT\_T &\_result, const FLOAT\_T &\_op2, CARL\_RND=CARL\_RND::N) const

Function which multiplicates two numbers and puts the result in a third number passed as parameter.

• FLOAT\_T & div\_assign (const FLOAT\_T &\_op2, CARL\_RND=CARL\_RND::N)

Function for division of two numbers, which assigns the result to the calling number.

FLOAT\_T & div (FLOAT\_T &\_result, const FLOAT\_T &\_op2, CARL\_RND=CARL\_RND::N) const

Function which divides this number by the righthand side and puts the result in a third number passed as parameter.

FLOAT\_T & sqrt\_assign (CARL\_RND=CARL\_RND::N)

Function for the square root of the number, which assigns the result to the calling number.

FLOAT\_T & sqrt (FLOAT\_T &\_result, CARL\_RND=CARL\_RND::N) const

Returns the square root of this number and puts it into a passed result parameter.

FLOAT\_T & cbrt\_assign (CARL\_RND=CARL\_RND::N)

Function for the cubic root of the number, which assigns the result to the calling number.

FLOAT\_T & cbrt (FLOAT\_T &\_result, CARL\_RND=CARL\_RND::N) const

Returns the cubic root of this number and puts it into a passed result parameter.

FLOAT\_T & root\_assign (std::size\_t, CARL\_RND=CARL\_RND::N)

Function for the nth root of the number, which assigns the result to the calling number.

FLOAT\_T & root (FLOAT\_T &, std::size\_t, CARL\_RND=CARL\_RND::N) const

Function which calculates the nth root of this number and puts it into a passed result parameter.

• FLOAT\_T & pow\_assign (std::size\_t \_exp, CARL\_RND=CARL\_RND::N)

Function for the nth power of the number, which assigns the result to the calling number.

FLOAT\_T & pow (FLOAT\_T &\_result, std::size\_t \_exp, CARL\_RND=CARL\_RND::N) const

Function which calculates the power of this number and puts it into a passed result parameter.

FLOAT\_T & abs\_assign (CARL\_RND=CARL\_RND::N)

Assigns the number the absolute value of this number.

FLOAT\_T & abs (FLOAT\_T &\_result, CARL\_RND=CARL\_RND::N) const

Function which calculates the absolute value of this number and puts it into a passed result parameter.

FLOAT\_T & exp\_assign (CARL\_RND=CARL\_RND::N)

Assigns the number the exponential of this number.

FLOAT\_T & exp (FLOAT\_T &\_result, CARL\_RND=CARL\_RND::N) const

Function which calculates the exponential of this number and puts it into a passed result parameter.

FLOAT\_T & sin\_assign (CARL\_RND=CARL\_RND::N)

Assigns the number the sine of this number.

• FLOAT\_T & sin (FLOAT\_T &\_result, CARL\_RND=CARL\_RND::N) const

Function which calculates the sine of this number and puts it into a passed result parameter.

FLOAT\_T & cos\_assign (CARL\_RND=CARL\_RND::N)

Assigns the number the cosine of this number.

FLOAT\_T & cos (FLOAT\_T &\_result, CARL\_RND=CARL\_RND::N) const

Function which calculates the cosine of this number and puts it into a passed result parameter.

FLOAT\_T & log\_assign (CARL\_RND=CARL\_RND::N)

Assigns the number the logarithm of this number.

FLOAT\_T & log (FLOAT\_T &\_result, CARL\_RND=CARL\_RND::N) const

Function which calculates the logarithm of this number and puts it into a passed result parameter.

FLOAT\_T & tan\_assign (CARL\_RND=CARL\_RND::N)

Assigns the number the tangent of this number.

FLOAT\_T & tan (FLOAT\_T &\_result, CARL\_RND=CARL\_RND::N) const

Function which calculates the tangent of this number and puts it into a passed result parameter.

FLOAT\_T & asin\_assign (CARL\_RND=CARL\_RND::N)

Assigns the number the arcus sine of this number.

FLOAT\_T & asin (FLOAT\_T &\_result, CARL\_RND=CARL\_RND::N) const

Function which calculates the arcus sine of this number and puts it into a passed result parameter.

FLOAT\_T & acos\_assign (CARL\_RND=CARL\_RND::N)

Assigns the number the arcus cosine of this number.

FLOAT\_T & acos (FLOAT\_T &\_result, CARL\_RND=CARL\_RND::N) const

Function which calculates the arcus cosine of this number and puts it into a passed result parameter.

FLOAT\_T & atan\_assign (CARL\_RND=CARL\_RND::N)

Assigns the number the arcus tangent of this number.

FLOAT\_T & atan (FLOAT\_T &\_result, CARL\_RND=CARL\_RND::N) const

Function which calculates the arcus tangent of this number and puts it into a passed result parameter.

FLOAT\_T & sinh\_assign (CARL\_RND=CARL\_RND::N)

Assigns the number the hyperbolic sine of this number.

• FLOAT\_T & sinh (FLOAT\_T &\_result, CARL\_RND=CARL\_RND::N) const

Function which calculates the hyperbolic sine of this number and puts it into a passed result parameter.

FLOAT\_T & cosh\_assign (CARL\_RND=CARL\_RND::N)

Assigns the number the hyperbolic cosine of this number.

FLOAT\_T & cosh (FLOAT\_T &\_result, CARL\_RND=CARL\_RND::N) const

Function which calculates the hyperbolic cosine of this number and puts it into a passed result parameter.

FLOAT\_T & tanh\_assign (CARL\_RND=CARL\_RND::N)

Assigns the number the hyperbolic tangent of this number.

• FLOAT\_T & tanh (FLOAT\_T &\_result, CARL\_RND=CARL\_RND::N) const

Function which calculates the hyperbolic tangent of this number and puts it into a passed result parameter.

FLOAT\_T & asinh\_assign (CARL\_RND=CARL\_RND::N)

Assigns the number the hyperbolic arcus sine of this number.

FLOAT\_T & asinh (FLOAT\_T &\_result, CARL\_RND=CARL\_RND::N) const

Function which calculates the hyperbolic arcus sine of this number and puts it into a passed result parameter.

FLOAT\_T & acosh\_assign (CARL\_RND=CARL\_RND::N)

Assigns the number the hyperbolic arcus cosine of this number.

FLOAT\_T & acosh (FLOAT\_T &\_result, CARL\_RND=CARL\_RND::N) const

Function which calculates the hyperbolic arcus cosine of this number and puts it into a passed result parameter.

FLOAT\_T & atanh\_assign (CARL\_RND=CARL\_RND::N)

Assigns the number the hyperbolic arcus tangent of this number.

• FLOAT\_T & atanh (FLOAT\_T &\_result, CARL\_RND=CARL\_RND::N) const

Function which calculates the hyperbolic arcus tangent of this number and puts it into a passed result parameter.

FLOAT\_T & floor (FLOAT\_T &\_result, CARL\_RND=CARL\_RND::N) const

Function which calculates the floor of this number and puts it into a passed result parameter.

FLOAT\_T & floor\_assign (CARL\_RND=CARL\_RND::N)

Assigns the number the floor of this number.

FLOAT\_T & ceil (FLOAT\_T &\_result, CARL\_RND=CARL\_RND::N) const

Function which calculates the ceiling of this number and puts it into a passed result parameter.

FLOAT\_T & ceil\_assign (CARL\_RND=CARL\_RND::N)

Assigns the number the ceiling of this number.

double to\_double (CARL\_RND=CARL\_RND::N) const

Function which converts the number to a double value.

operator int () const

Explicit typecast operator to integer.

• operator long () const

Explicit typecast operator to long.

• operator double () const

Explicit typecast operator to double.

- operator mpq\_class () const
- const FLOAT\_T & ei\_conj (const FLOAT\_T &x)

Function required for extension of Eigen3 with FLOAT\_T as a custom type which calculates the complex conjugate.

const FLOAT\_T & ei\_real (const FLOAT\_T &x)

Function required for extension of Eigen3 with FLOAT\_T as a custom type which calculates the real part.

FLOAT\_T ei\_imag (const FLOAT\_T &)

Function required for extension of Eigen3 with FLOAT\_T as a custom type which calculates the imaginary part.

FLOAT\_T ei\_abs (const FLOAT\_T &x)

Function required for extension of Eigen3 with FLOAT\_T as a custom type which calculates the absolute value.

FLOAT\_T ei\_abs2 (const FLOAT\_T &x)

Function required for extension of Eigen3 with FLOAT\_T as a custom type which calculates the absolute value (special Eigen3 version).

FLOAT\_T ei\_sqrt (const FLOAT\_T &x)

Function required for extension of Eigen3 with FLOAT\_T as a custom type which calculates the square root.

FLOAT\_T ei\_exp (const FLOAT\_T &x)

Function required for extension of Eigen3 with FLOAT\_T as a custom type which calculates the exponential.

FLOAT\_T ei\_log (const FLOAT\_T &x)

Function required for extension of Eigen3 with FLOAT\_T as a custom type which calculates the logarithm.

FLOAT\_T ei\_sin (const FLOAT\_T &x)

Function required for extension of Eigen3 with FLOAT\_T as a custom type which calculates the sine.

FLOAT\_T ei\_cos (const FLOAT\_T &x)

Function required for extension of Eigen3 with FLOAT\_T as a custom type which calculates the cosine.

FLOAT\_T ei\_pow (const FLOAT\_T &x, FLOAT\_T y)

Function required for extension of Eigen3 with FLOAT\_T as a custom type which calculates the power.

FLOAT\_T & operator+= (const FLOAT\_T &\_rhs)

Operator which adds the righthand side to this.

FLOAT\_T & operator+= (const FloatType &\_rhs)

Operator which adds the righthand side of the underlying type to this.

FLOAT\_T & operator-= (const FLOAT\_T &\_rhs)

Operator which subtracts the righthand side from this.

FLOAT\_T & operator== (const FloatType &\_rhs)

Operator which subtracts the righthand side of the underlying type from this.

FLOAT\_T operator- ()

Operator for unary negation of this number.

FLOAT\_T & operator\*= (const FLOAT\_T &\_rhs)

Operator which multiplicates this number by the righthand side.

FLOAT\_T & operator\*= (const FloatType &\_rhs)

Operator which multiplicates this number by the righthand side of the underlying type.

FLOAT\_T & operator/= (const FLOAT\_T &\_rhs)

Operator which divides this number by the righthand side.

FLOAT\_T & operator/= (const FloatType &\_rhs)

Operator which divides this number by the righthand side of the underlying type.

• std::string toString () const

Method which converts this number to a string.

## **Friends**

```
    std::ostream & operator<< (std::ostream &ostr, const FLOAT_T &p)</li>
```

Output stream operator for numbers of type FLOAT\_T.

FLOAT\_T operator+ (const FLOAT\_T & lhs, const FLOAT\_T & rhs)

Operator for addition of two numbers.

- FLOAT\_T operator- (const FLOAT\_T & lhs, const FLOAT\_T & rhs)
  - Operator for subtraction of two numbers.
- FLOAT\_T operator- (const FLOAT\_T &\_lhs)

Operator for unary negation of a number.

• FLOAT\_T operator\* (const FLOAT\_T &\_Ihs, const FLOAT\_T &\_rhs)

Operator for addition of two numbers.

FLOAT\_T operator/ (const FLOAT\_T &\_lhs, const FLOAT\_T &\_rhs)

Operator for addition of two numbers.

FLOAT\_T & operator++ (FLOAT\_T &\_num)

Operator which increments this number by one.

FLOAT\_T & operator-- (FLOAT\_T &\_num)

Operator which decrements this number by one.

# 12.86.1 Detailed Description

```
template<typename FloatType> class carl::FLOAT_T< FloatType >
```

Templated wrapper class which allows universal usage of different IEEE 754 implementations.

For each implementation intended to use it is necessary to implement the according specialization of this class.

## 12.86.2 Constructor & Destructor Documentation

```
12.86.2.1 FLOAT_T() [1/10] template<typename FloatType >
carl::FLOAT_T< FloatType >::FLOAT_T ( ) [inline]
```

Default empty constructor, which initializes to zero.

Constructor, which takes a double as input and optional rounding, which can be used, if the underlying fp implementation allows this.

| ₋double | Value to be initialized.     |
|---------|------------------------------|
| N       | Possible rounding direction. |

Constructor, which takes an integer as input and optional rounding, which can be used, if the underlying fp implementation allows this.

## **Parameters**

| ₋int | Value to be initialized.     |
|------|------------------------------|
| Ν    | Possible rounding direction. |

Constructor, which takes an unsigned integer as input and optional rounding, which can be used, if the underlying fp implementation allows this.

## **Parameters**

| _int | Value to be initialized.     |
|------|------------------------------|
| Ν    | Possible rounding direction. |

 $\label{lem:copyconstructor} \mbox{Copyconstructor which takes a FLOAT\_T$<FloatType>$ and optional rounding as input, which can be used, if the underlying fp implementation allows this.}$ 

12.86.2.7 FLOAT\_T() [7/10] template<typename FloatType >

#### **Parameters**

| ₋float | Value to be initialized.     |
|--------|------------------------------|
| Ν      | Possible rounding direction. |

CARL\_RND = CARL\_RND::N ) [inline], [explicit]

Constructor, which takes an arbitrary fp type as input and optional rounding, which can be used, if the underlying fp implementation allows this.

## **Parameters**

| val | val Value to be initialized. |  |
|-----|------------------------------|--|
| Ν   | Possible rounding direction. |  |

FloatType val,

Destructor.

Note that for some specializations memory management has to be included here.

## 12.86.3 Member Function Documentation

Function which calculates the absolute value of this number and puts it into a passed result parameter.

## **Parameters**

| ₋result | Result.                      |
|---------|------------------------------|
| Ν       | Possible rounding direction. |

## Returns

Reference to the result.

Assigns the number the absolute value of this number.

# Parameters

```
N Possible rounding direction.
```

# Returns

Reference to this.

Function which calculates the arcus cosine of this number and puts it into a passed result parameter.

## **Parameters**

| ₋result | Result.                      |
|---------|------------------------------|
| N       | Possible rounding direction. |

## Returns

Reference to the result.

Assigns the number the arcus cosine of this number.

## **Parameters**

```
N Possible rounding direction.
```

## Returns

Reference to this.

Function which calculates the hyperbolic arcus cosine of this number and puts it into a passed result parameter.

# **Parameters**

| ₋result | Result.                      |
|---------|------------------------------|
| Ν       | Possible rounding direction. |

# Returns

Reference to the result.

Assigns the number the hyperbolic arcus cosine of this number.

## **Parameters**

```
N Possible rounding direction.
```

## Returns

Reference to this.

Function which adds two numbers and puts the result in a third number passed as parameter.

## **Parameters**

| _result | Result of the operation.         |
|---------|----------------------------------|
| _op2    | Righthand side of the operation. |
| N       | Possible rounding direction.     |

## Returns

Reference to the result.

Function for addition of two numbers, which assigns the result to the calling number.

## **Parameters**

| _op2 | Righthand side of the operation |
|------|---------------------------------|
| Ν    | Possible rounding direction.    |

# Returns

Reference to this.

Function which calculates the arcus sine of this number and puts it into a passed result parameter.

| ₋result | Result.                      |
|---------|------------------------------|
| Ν       | Possible rounding direction. |

## Returns

Reference to the result.

Assigns the number the arcus sine of this number.

## **Parameters**

| N Possibl | e rounding direction. |
|-----------|-----------------------|
|-----------|-----------------------|

# Returns

Reference to this.

Function which calculates the hyperbolic arcus sine of this number and puts it into a passed result parameter.

# **Parameters**

| ₋result | Result.                      |
|---------|------------------------------|
| N       | Possible rounding direction. |

# Returns

Reference to the result.

Assigns the number the hyperbolic arcus sine of this number.

N Possible rounding direction.

## Returns

Reference to this.

Function which calculates the arcus tangent of this number and puts it into a passed result parameter.

#### **Parameters**

| ₋result | Result.                      |
|---------|------------------------------|
| N       | Possible rounding direction. |

## Returns

Reference to the result.

Assigns the number the arcus tangent of this number.

# **Parameters**

```
N Possible rounding direction.
```

# Returns

Reference to this.

Function which calculates the hyperbolic arcus tangent of this number and puts it into a passed result parameter.

| ₋result | Result.                      |
|---------|------------------------------|
| Ν       | Possible rounding direction. |

## Returns

Reference to the result.

Assigns the number the hyperbolic arcus tangent of this number.

## **Parameters**

| N | Possible rounding direction. |
|---|------------------------------|
|---|------------------------------|

# Returns

Reference to this.

Returns the cubic root of this number and puts it into a passed result parameter.

# **Parameters**

| ₋result | Result.                      |
|---------|------------------------------|
| Ν       | Possible rounding direction. |

# Returns

Reference to the result.

Function for the cubic root of the number, which assigns the result to the calling number.

```
N Possible rounding direction.
```

## Returns

Reference to this.

Function which calculates the ceiling of this number and puts it into a passed result parameter.

#### **Parameters**

| ₋result | Result.                      |
|---------|------------------------------|
| N       | Possible rounding direction. |

## Returns

Reference to the result.

Assigns the number the ceiling of this number.

# **Parameters**

```
N Possible rounding direction.
```

# Returns

Reference to this.

Function which calculates the cosine of this number and puts it into a passed result parameter.

| ₋result | Result.                      |
|---------|------------------------------|
| Ν       | Possible rounding direction. |

## Returns

Reference to the result.

Assigns the number the cosine of this number.

## **Parameters**

| N Possible rounding | direction. |
|---------------------|------------|
|---------------------|------------|

# Returns

Reference to this.

Function which calculates the hyperbolic cosine of this number and puts it into a passed result parameter.

# **Parameters**

| _re | sult | Result.                      |
|-----|------|------------------------------|
| N   |      | Possible rounding direction. |

# Returns

Reference to the result.

Assigns the number the hyperbolic cosine of this number.

# Returns

Reference to this.

Function which divides this number by the righthand side and puts the result in a third number passed as parameter.

## **Parameters**

| ₋result | Result of the operation.         |
|---------|----------------------------------|
| _op2    | Righthand side of the operation. |
| N       | Possible rounding direction.     |

## Returns

Reference to the result.

Function for division of two numbers, which assigns the result to the calling number.

# **Parameters**

| _op2 | Righthand side of the operation |
|------|---------------------------------|
| Ν    | Possible rounding direction.    |

# Returns

Reference to this.

Function required for extension of Eigen3 with FLOAT\_T as a custom type which calculates the absolute value.

## **Parameters**

```
x The passed number.
```

## Returns

Number which holds the absolute value of x.

Function required for extension of Eigen3 with FLOAT\_T as a custom type which calculates the absolute value (special Eigen3 version).

## **Parameters**

```
x The passed number.
```

# Returns

Number which holds the absolute value of x according to abs2 of Eigen3.

Function required for extension of Eigen3 with FLOAT\_T as a custom type which calculates the complex conjugate.

# **Parameters**

```
x The passed number.
```

## Returns

Reference to x.

Function required for extension of Eigen3 with FLOAT\_T as a custom type which calculates the cosine.

## **Parameters**

```
x The passed number.
```

## Returns

Number which holds the cosine of x.

Function required for extension of Eigen3 with FLOAT\_T as a custom type which calculates the exponential.

#### **Parameters**

```
x The passed number.
```

## Returns

Number which holds the exponential of x.

Function required for extension of Eigen3 with FLOAT\_T as a custom type which calculates the imaginary part.

## **Parameters**

```
x The passed number.
```

# Returns

Zero.

Function required for extension of Eigen3 with FLOAT\_T as a custom type which calculates the logarithm.

## **Parameters**

```
x The passed number.
```

## Returns

Number which holds the logarithm of x.

Function required for extension of Eigen3 with FLOAT\_T as a custom type which calculates the power.

## **Parameters**

| X | The passed number. |
|---|--------------------|
| У | Degree.            |

## Returns

Number which holds the power of x of degree y.

Function required for extension of Eigen3 with FLOAT\_T as a custom type which calculates the real part.

## **Parameters**

```
x The passed number.
```

# Returns

Reference to x.

Function required for extension of Eigen3 with FLOAT\_T as a custom type which calculates the sine.

## **Parameters**

```
x The passed number.
```

## Returns

Number which holds the sine of x.

Function required for extension of Eigen3 with FLOAT\_T as a custom type which calculates the square root.

#### **Parameters**

```
x The passed number.
```

## Returns

Number which holds the square root of x.

Function which calculates the exponential of this number and puts it into a passed result parameter.

# **Parameters**

| ₋result | Result.                      |  |
|---------|------------------------------|--|
| Ν       | Possible rounding direction. |  |

# Returns

Reference to the result.

Assigns the number the exponential of this number.

## **Parameters**

```
N Possible rounding direction.
```

## Returns

Reference to this.

Function which calculates the floor of this number and puts it into a passed result parameter.

## **Parameters**

| ₋result | Result.                      |
|---------|------------------------------|
| N       | Possible rounding direction. |

# Returns

Reference to the result.

Assigns the number the floor of this number.

# **Parameters**

```
N Possible rounding direction.
```

# Returns

Reference to this.

Function which calculates the logarithm of this number and puts it into a passed result parameter.

## **Parameters**

| ₋result | Result.                      |
|---------|------------------------------|
| Ν       | Possible rounding direction. |

# Returns

Reference to the result.

Assigns the number the logarithm of this number.

## **Parameters**

```
N Possible rounding direction.
```

# Returns

Reference to this.

Function which multiplicates two numbers and puts the result in a third number passed as parameter.

## **Parameters**

| ₋result | Result of the operation.         |
|---------|----------------------------------|
| _op2    | Righthand side of the operation. |
| N       | Possible rounding direction.     |

## Returns

Reference to the result.

Function for multiplication of two numbers, which assigns the result to the calling number.

## **Parameters**

| _op2 | Righthand side of the operation |
|------|---------------------------------|
| Ν    | Possible rounding direction.    |

## Returns

Reference to this.

```
12.86.3.46 operator double() template<typename FloatType > carl::FLOAT.T< FloatType >::operator double ( ) const [inline], [explicit]
```

Explicit typecast operator to double.

## Returns

Double representation of this.

```
12.86.3.47 operator int() template<typename FloatType >
carl::FLOAT_T< FloatType >::operator int ( ) const [inline], [explicit]
```

Explicit typecast operator to integer.

# Returns

Integer representation of this.

```
12.86.3.48 operator long() template<typename FloatType >
carl::FLOAT_T< FloatType >::operator long ( ) const [inline], [explicit]
```

Explicit typecast operator to long.

## Returns

Long representation of this.

```
12.86.3.49 operator mpq_class() template<typename FloatType > carl::FLOAT_T< FloatType >::operator mpq_class ( ) const [inline], [explicit]
```

Comparison operator for inequality.

## **Parameters**

\_rhs Righthand side of the comparison.

# Returns

True if \_rhs is unequal to this.

Operator which multiplicates this number by the righthand side.

## **Parameters**

₋rhs

# Returns

Reference to this.

Operator which multiplicates this number by the righthand side of the underlying type.

**Parameters** 

| _rhs  |  |
|-------|--|
| _,,,, |  |

## Returns

Reference to this.

Operator which adds the righthand side to this.

**Parameters** 

```
_rhs
```

## Returns

Reference to this.

Operator which adds the righthand side of the underlying type to this.

**Parameters** 

```
₋rhs
```

## Returns

Reference to this.

```
12.86.3.55 operator-() template<typename FloatType >
FLOAT_T carl::FLOAT_T< FloatType >::operator- ( ) [inline]
```

Operator for unary negation of this number.

Returns

Number which holds the negated original number.

Operator which subtracts the righthand side from this.

## **Parameters**

```
_rhs
```

## Returns

Reference to this.

Operator which subtracts the righthand side of the underlying type from this.

## **Parameters**

```
_rhs
```

# Returns

Reference to this.

Operator which divides this number by the righthand side.

| Do |    |   |    |     |    |
|----|----|---|----|-----|----|
| Pа | ra | m | eı | re. | rs |

\_rhs

# Returns

Reference to this.

Operator which divides this number by the righthand side of the underlying type.

## **Parameters**

\_rhs

## Returns

Reference to this.

Comparison operator for less than.

## **Parameters**

\_rhs Righthand side of the comparison.

# Returns

True if \_rhs is smaller than this.

Comparison operator for less or equal than.

## **Parameters**

```
_rhs Righthand side of the comparison.
```

## Returns

True if \_rhs is larger or equal than this.

Assignment operator.

## **Parameters**

```
_rhs Righthand side of the assignment.
```

## Returns

Reference to this.

Comparison operator for equality.

\_rhs | Righthand side of the comparison.

## Returns

True if \_rhs equals this.

Comparison operator for larger than.

# **Parameters**

```
_rhs | Righthand side of the comparison.
```

## Returns

True if \_rhs is larger than this.

Comparison operator for larger or equal than.

# **Parameters**

\_rhs Righthand side of the comparison.

## Returns

True if \_rhs is smaller or equal than this.

Function which calculates the power of this number and puts it into a passed result parameter.

## **Parameters**

| ₋result | Result.                      |  |
|---------|------------------------------|--|
| _exp    | Exponent.                    |  |
| N       | Possible rounding direction. |  |

## Returns

Reference to the result.

Function for the nth power of the number, which assigns the result to the calling number.

# **Parameters**

| _exp | Exponent.                    |
|------|------------------------------|
| N    | Possible rounding direction. |

# Returns

Reference to this.

```
12.86.3.73 precision() template<typename FloatType >
precision_t carl::FLOAT_T< FloatType >::precision ( ) const [inline]
```

If precision is used, this getter returns the acutal precision (default: 53 bit).

# Returns

Precision.

Function which calculates the nth root of this number and puts it into a passed result parameter.

#### **Parameters**

| Result. |                              |
|---------|------------------------------|
| Degree  | of the root.                 |
| N       | Possible rounding direction. |

## Returns

Reference to the result.

Todo implement root for FLOAT\_T

Function for the nth root of the number, which assigns the result to the calling number.

## **Parameters**

| Degree | of the root.                 |
|--------|------------------------------|
| N      | Possible rounding direction. |

## Returns

Reference to this.

Todo implement root\_assign for FLOAT\_T

Allows to set the desired precision.

Note: If the value is already initialized this can change the internal value.

```
Precision in bits.
```

# Returns

Reference to this.

Function which calculates the sine of this number and puts it into a passed result parameter.

## **Parameters**

| ₋result | Result.                      |
|---------|------------------------------|
| Ν       | Possible rounding direction. |

# Returns

Reference to the result.

Assigns the number the sine of this number.

## **Parameters**

```
N Possible rounding direction.
```

# Returns

Reference to this.

Function which calculates the hyperbolic sine of this number and puts it into a passed result parameter.

| ₋result | Result.                      |
|---------|------------------------------|
| N       | Possible rounding direction. |

## Returns

Reference to the result.

Assigns the number the hyperbolic sine of this number.

## **Parameters**

| N | Possible rounding direction. |
|---|------------------------------|
|---|------------------------------|

# Returns

Reference to this.

Returns the square root of this number and puts it into a passed result parameter.

# **Parameters**

| ₋resu | ılt | Result.                      |
|-------|-----|------------------------------|
| N     |     | Possible rounding direction. |

# Returns

Reference to the result.

Function for the square root of the number, which assigns the result to the calling number.

## **Parameters**

N Possible rounding direction.

# Returns

Reference to this.

Function which subtracts the righthand side from this number and puts the result in a third number passed as parameter.

## **Parameters**

| _result | Result of the operation.         |
|---------|----------------------------------|
| _op2    | Righthand side of the operation. |
| N       | Possible rounding direction.     |

# Returns

Reference to the result.

Function for subtraction of two numbers, which assigns the result to the calling number.

## **Parameters**

| _op2 | Righthand side of the operation |
|------|---------------------------------|
| Ν    | Possible rounding direction.    |

## Returns

Reference to this.

Function which calculates the tangent of this number and puts it into a passed result parameter.

#### **Parameters**

| ₋result | Result.                      |
|---------|------------------------------|
| Ν       | Possible rounding direction. |

# Returns

Reference to the result.

Assigns the number the tangent of this number.

## **Parameters**

```
N Possible rounding direction.
```

# Returns

Reference to this.

Function which calculates the hyperbolic tangent of this number and puts it into a passed result parameter.

# **Parameters**

| ₋result | Result.                      |
|---------|------------------------------|
| N       | Possible rounding direction. |

## Returns

Reference to the result.

Assigns the number the hyperbolic tangent of this number.

#### **Parameters**

```
N Possible rounding direction.
```

#### Returns

Reference to this.

Function which converts the number to a double value.

#### **Parameters**

```
N Possible rounding direction.
```

#### Returns

Double representation of this

```
12.86.3.90 toString() template<typename FloatType >
std::string carl::FLOAT_T< FloatType >::toString ( ) const [inline]
```

Method which converts this number to a string.

# Returns

String representation of this number.

```
12.86.3.91 value() template<typename FloatType >
const FloatType& carl::FLOAT.T< FloatType >::value ( ) const [inline]
```

Getter for the raw value contained.

# Returns

Raw value.

# 12.86.4 Friends And Related Function Documentation

Operator for addition of two numbers.

#### **Parameters**

| ₋lhs | Lefthand side.  |
|------|-----------------|
| ₋rhs | Righthand side. |

## Returns

Number which holds the result.

Operator for addition of two numbers.

## **Parameters**

| ₋lhs | Lefthand side.  |
|------|-----------------|
| ₋rhs | Righthand side. |

## Returns

Number which holds the result.

Operator which increments this number by one.

## **Parameters**

```
_num
```

Reference to \_num.

Operator for unary negation of a number.

## **Parameters**

```
_lhs Lefthand side.
```

## Returns

Number which holds the result.

```
12.86.4.5 operator- [2/2] template<typename FloatType > FLOAT_T operator- (

const FLOAT_T < FloatType > & .lhs,

const FLOAT_T < FloatType > & .rhs ) [friend]
```

Operator for subtraction of two numbers.

# **Parameters**

| ₋lhs | Lefthand side.  |
|------|-----------------|
| ₋rhs | Righthand side. |

# Returns

Number which holds the result.

Operator which decrements this number by one.

# **Parameters**

₋num

Reference to \_num.

Operator for addition of two numbers.

#### **Parameters**

| ₋lhs | Lefthand side.  |
|------|-----------------|
| _rhs | Righthand side. |

## Returns

Number which holds the result.

Output stream operator for numbers of type FLOAT\_T.

# **Parameters**

| ostr | Output stream. |
|------|----------------|
| р    | Number.        |

# Returns

Reference to the ostream.

# 12.87 carl::FloatConv < T1, T2 > Struct Template Reference

Struct which holds the conversion operator for any two instanciations of FLOAT\_T with different underlying floating point implementations.

```
#include <FLOAT_T.h>
```

## **Public Member Functions**

FLOAT\_T< T1 > operator() (const FLOAT\_T< T2 > &\_op2) const

Conversion operator for conversion of two instanciations of FLOAT\_T with different underlying floating point implementations.

# 12.87.1 Detailed Description

```
template<typename T1, typename T2> struct carl::FloatConv< T1, T2 >
```

Struct which holds the conversion operator for any two instanciations of FLOAT\_T with different underlying floating point implementations.

Note that this conversion introduces loss of precision, as it uses the to\_double() method and the corresponding double constructor from the target type.

#### 12.87.2 Member Function Documentation

Conversion operator for conversion of two instanciations of FLOAT\_T with different underlying floating point implementations.

#### **Parameters**

```
_op2 The source instanciation (T2)
```

#### Returns

returns an instanciation with different floating point implementation (T1)

# 12.88 carl::logging::Formatter Class Reference

Formats a log messages.

```
#include <Formatter.h>
```

# **Public Member Functions**

- virtual  $\sim$ Formatter () noexcept=default
- · virtual void configure (const Filter &f) noexcept

Extracts the maximum width of a channel to optimize the formatting.

- virtual void prefix (std::ostream &os, const std::string &channel, LogLevel level, const RecordInfo &info)

  Prints the prefix of a log message, i.e.
- virtual void suffix (std::ostream &os)

Prints the suffix of a log message, i.e.

## **Data Fields**

• bool printInformation = true

Print information like log level, file etc.

## 12.88.1 Detailed Description

Formats a log messages.

## 12.88.2 Constructor & Destructor Documentation

```
12.88.2.1 \simFormatter() virtual carl::logging::Formatter::\simFormatter ( ) [virtual], [default], [noexcept]
```

## 12.88.3 Member Function Documentation

```
12.88.3.1 configure() virtual void carl::logging::Formatter::configure ( const Filter & f ) [inline], [virtual], [noexcept]
```

Extracts the maximum width of a channel to optimize the formatting.

# **Parameters**

```
f Filter.
```

Prints the prefix of a log message, i.e.

everything that goes before the message given by the user, to the output stream.

## **Parameters**

| os      | Output stream.         |
|---------|------------------------|
| channel | Channel name.          |
| level   | LogLevel.              |
| info    | Auxiliary information. |

```
12.88.3.3 suffix() virtual void carl::logging::Formatter::suffix ( std::ostream & os ) [inline], [virtual]
```

Prints the suffix of a log message, i.e.

everything that goes after the message given by the user, to the output stream. Usually, this is only a newline.

#### **Parameters**

os Output stream.

#### 12.88.4 Field Documentation

```
12.88.4.1 printInformation bool carl::logging::Formatter::printInformation = true
```

Print information like log level, file etc.

# 12.89 carl::Formula < Pol > Class Template Reference

Represent an SMT formula, which can be an atom for some background theory or a boolean combination of (sub)formulas.

```
#include <Formula.h>
```

# **Public Types**

- using const\_iterator = typename Formulas< Pol >::const\_iterator
  - A constant iterator to a sub-formula of a formula.
- using const\_reverse\_iterator = typename Formulas< Pol >::const\_reverse\_iterator
  - A constant reverse iterator to a sub-formula of a formula.
- using PolynomialType = Pol

A typedef for the template argument.

## **Public Member Functions**

- Formula (FormulaType \_type=FALSE)
- Formula (Variable::Arg \_booleanVar)
- Formula (const Pol &\_pol, Relation \_rel)
- Formula (const Constraint < Pol > &\_constraint)
- Formula (const VariableComparison < Pol > &\_variableComparison)
- Formula (const VariableAssignment < Pol > &\_variableAssignment)
- Formula (const BVConstraint &\_constraint)
- Formula (Formula Type \_type, Formula &&\_subformula)
- Formula (Formula Type \_type, const Formula &\_subformula)
- Formula (FormulaType \_type, const Formula &\_subformulaA, const Formula &\_subformulaB)
- Formula (FormulaType \_type, const Formula &\_subformulaA, const Formula &\_subformulaB, const Formula &\_subformulaC)
- Formula (FormulaType \_type, const FormulasMulti< Pol > &\_subformulas)
- Formula (FormulaType \_type, const Formulas< Pol > &\_subasts)
- Formula (FormulaType \_type, Formulas < Pol > &&\_subasts)
- Formula (FormulaType \_type, const std::initializer\_list< Formula < Pol >> &\_subasts)
- Formula (FormulaType \_type, const FormulaSet < Pol > &\_subasts)
- Formula (FormulaType \_type, FormulaSet< Pol > &&\_subasts)
- Formula (FormulaType \_type, std::vector< Variable > &&\_vars, const Formula &.term)
- Formula (FormulaType \_type, const std::vector< Variable > &\_vars, const Formula &\_term)
- Formula (const UTerm &\_lhs, const UTerm &\_rhs, bool \_negated)
- Formula (UEquality &&\_eq)
- Formula (const UEquality &\_eq)
- Formula (const Formula &\_formula)
- Formula (Formula &&\_formula) noexcept
- ∼Formula ()
- Formula & operator= (const Formula &\_formula)
- Formula & operator= (Formula &&\_formula)
- double activity () const
- void set\_activity (double \_activity) const

Sets the activity to the given value.

- FormulaType type () const
- std::size\_t hash () const
- std::size\_t id () const
- bool is\_true () const
- bool is\_false () const
- · const Condition & properties () const
- · const Variables & variables () const
- Formula negated () const
- Formula base\_formula () const
- const Formula & remove\_negations () const
- · const Formula & subformula () const
- · const Formula & premise () const
- · const Formula & conclusion () const
- const Formula & condition () const
- const Formula & first\_case () const
- const Formula & second\_case () const
- const std::vector< carl::Variable > & quantified\_variables () const
- const Formula & quantified\_formula () const
- const Formulas < Pol > & subformulas () const
- const Constraint < Pol > & constraint () const
- const VariableComparison < Pol > & variable\_comparison () const
- const VariableAssignment < Pol > & variable\_assignment () const

- const BVConstraint & bv\_constraint () const
- · carl::Variable::Arg boolean () const
- const UEquality & u\_equality () const
- size\_t size () const
- · bool empty () const
- · const\_iterator begin () const
- const\_iterator end () const
- const\_reverse\_iterator rbegin () const
- const\_reverse\_iterator rend () const
- · const Formula & back () const
- bool property\_holds (const Condition &\_property) const

Checks if the given property holds for this formula.

- bool is\_atom () const
- bool is\_literal () const
- bool is\_boolean\_combination () const
- · bool is\_bound () const
- bool is\_nary () const
- bool is\_constraint\_conjunction () const
- bool is\_real\_constraint\_conjunction () const
- bool is\_integer\_constraint\_conjunction () const
- bool is\_only\_propositional () const
- Logic logic () const
- bool contains (const Formula &\_formula) const
- bool operator== (const Formula &\_formula) const
- bool operator!= (const Formula &\_formula) const
- bool operator< (const Formula &\_formula) const
- bool operator> (const Formula &\_formula) const
- bool operator <= (const Formula &\_formula) const
- bool operator>= (const Formula &\_formula) const
- · Formula operator! () const

## **Static Public Member Functions**

static void init (FormulaContent< Pol > &\_content)

Gets the propositions of this formula.

## Friends

- class FormulaPool
   Pol
- class FormulaContent< Pol >
- template<typename P >

std::ostream & operator << (std::ostream &os, const Formula < P > &f)

The output operator of a formula.

# 12.89.1 Detailed Description

template<typename Pol> class carl::Formula< Pol>

Represent an SMT formula, which can be an atom for some background theory or a boolean combination of (sub)formulas.

## 12.89.2 Member Typedef Documentation

```
12.89.2.1 const_iterator template<typename Pol >
using carl::Formula< Pol >::const_iterator = typename Formulas<Pol>::const_iterator
```

A constant iterator to a sub-formula of a formula.

```
12.89.2.2 const_reverse_iterator template<typename Pol >
using carl::Formula< Pol >::const_reverse_iterator = typename Formulas<Pol>::const_reverse_iterator
```

A constant reverse iterator to a sub-formula of a formula.

```
12.89.2.3 PolynomialType template<typename Pol > using carl::Formula< Pol >::PolynomialType = Pol
```

A typedef for the template argument.

# 12.89.3 Constructor & Destructor Documentation

const Pol & \_pol,

Relation \_rel ) [inline], [explicit]

```
12.89.3.4 Formula() [4/24] template<typename Pol >
carl::Formula< Pol >::Formula (
            12.89.3.5 Formula() [5/24] template<typename Pol >
carl::Formula < Pol >::Formula (
            const VariableComparison< Pol > & _variableComparison ) [inline], [explicit]
12.89.3.6 Formula() [6/24] template<typename Pol >
carl::Formula< Pol >::Formula (
            const VariableAssignment < Pol > & _variableAssignment ) [inline], [explicit]
12.89.3.7 Formula() [7/24] template<typename Pol >
carl::Formula< Pol >::Formula (
            const BVConstraint & _constraint ) [inline], [explicit]
12.89.3.8 Formula() [8/24] template<typename Pol >
carl::Formula < Pol >::Formula (
           FormulaType _type,
            Formula< Pol > && _subformula ) [inline], [explicit]
12.89.3.9 Formula() [9/24] template<typename Pol >
carl::Formula < Pol >::Formula (
            FormulaType _type,
            const Formula< Pol > & _subformula ) [inline], [explicit]
12.89.3.10 Formula() [10/24] template<typename Pol >
carl::Formula< Pol >::Formula (
           FormulaType _type,
            const Formula< Pol > & _subformulaA,
            const Formula< Pol > & _subformulaB ) [inline], [explicit]
```

```
12.89.3.11 Formula() [11/24] template<typename Pol >
carl::Formula< Pol >::Formula (
            FormulaType _type,
            const FormulaPol > & _subformulaA,
            const Formula< Pol > & _subformulaB,
            const Formula< Pol > & _subformulaC ) [inline], [explicit]
12.89.3.12 Formula() [12/24] template<typename Pol >
carl::Formula< Pol >::Formula (
            FormulaType _type,
            const FormulasMulti< Pol > & _subformulas ) [inline], [explicit]
12.89.3.13 Formula() [13/24] template<typename Pol >
carl::Formula< Pol >::Formula (
           FormulaType _type,
            const Formulas< Pol > & _subasts ) [inline], [explicit]
12.89.3.14 Formula() [14/24] template<typename Pol >
carl::Formula< Pol >::Formula (
            FormulaType _type,
            Formulas< Pol > && _subasts ) [inline], [explicit]
12.89.3.15 Formula() [15/24] template<typename Pol >
carl::Formula < Pol >::Formula (
            FormulaType _type,
            const std::initializer_list< Formula< Pol >> & _subasts ) [inline], [explicit]
12.89.3.16 Formula() [16/24] template<typename Pol >
carl::Formula< Pol >::Formula (
            FormulaType _type,
            const FormulaSet< Pol > & _subasts ) [inline], [explicit]
12.89.3.17 Formula() [17/24] template<typename Pol >
carl::Formula< Pol >::Formula (
            FormulaType _type,
            FormulaSet< Pol > && _subasts ) [inline], [explicit]
```

```
12.89.3.18 Formula() [18/24] template<typename Pol >
carl::Formula< Pol >::Formula (
            FormulaType _type,
            std::vector< Variable > && _vars,
            const Formula< Pol > & _term ) [inline], [explicit]
12.89.3.19 Formula() [19/24] template<typename Pol >
carl::Formula< Pol >::Formula (
            FormulaType _type,
            const std::vector< Variable > & _vars,
            const Formula< Pol > & _term ) [inline], [explicit]
12.89.3.20 Formula() [20/24] template<typename Pol >
carl::Formula< Pol >::Formula (
            const UTerm & _1hs,
            const UTerm & _rhs,
            bool _negated ) [inline], [explicit]
12.89.3.21 Formula() [21/24] template<typename Pol >
carl::Formula< Pol >::Formula (
            UEquality && \_eq ) [inline], [explicit]
12.89.3.22 Formula() [22/24] template<typename Pol >
carl::Formula< Pol >::Formula (
            const UEquality & _eq ) [inline], [explicit]
12.89.3.23 Formula() [23/24] template<typename Pol >
carl::Formula< Pol >::Formula (
            const Formula < Pol > & _formula ) [inline]
12.89.3.24 Formula() [24/24] template<typename Pol >
carl::Formula< Pol >::Formula (
            Formula< Pol > && _formula ) [inline], [noexcept]
12.89.3.25 \simFormula() template<typename Pol >
carl::Formula< Pol >::~Formula ( ) [inline]
```

## 12.89.4 Member Function Documentation

```
12.89.4.1 activity() template<typename Pol >
double carl::Formula< Pol >::activity ( ) const [inline]
```

#### Returns

The activity for this formula, which means, how much is this formula involved in the solving procedure.

```
12.89.4.2 back() template<typename Pol > const Formula& carl::Formula< Pol >::back ( ) const [inline]
```

#### Returns

A reference to the last sub-formula of this formula.

```
12.89.4.3 base_formula() template<typename Pol >
Formula carl::Formula< Pol >::base_formula ( ) const [inline]
```

```
12.89.4.4 begin() template<typename Pol >
const_iterator carl::Formula< Pol >::begin ( ) const [inline]
```

## Returns

A constant iterator to the beginning of the list of sub-formulas of this formula.

```
12.89.4.5 boolean() template<typename Pol > carl::Variable::Arg carl::Formula< Pol >::boolean ( ) const [inline]
```

## Returns

The name of the Boolean variable represented by this formula. Note, that this formula has to be of type BOOL, if you invoke this method.

```
12.89.4.6 bv_constraint() template<typename Pol > const BVConstraint& carl::Formula< Pol >::bv_constraint ( ) const [inline]
```

```
12.89.4.7 conclusion() template<typename Pol > const Formula& carl::Formula< Pol >::conclusion ( ) const [inline]
```

A constant reference to the conclusion, in case this formula is an implication.

```
12.89.4.8 condition() template<typename Pol > const Formula& carl::Formula< Pol >::condition ( ) const [inline]
```

#### Returns

A constant reference to the condition, in case this formula is an ite-expression of formulas.

```
12.89.4.9 constraint() template<typename Pol > const Constraint<Pol>& carl::Formula< Pol >::constraint ( ) const [inline]
```

# Returns

A constant reference to the constraint represented by this formula. Note, that this formula has to be of type CONSTRAINT, if you invoke this method.

## **Parameters**

\_formula | The pointer to the formula for which to check whether it points to a sub-formula of this formula.

## Returns

true, the given pointer to a formula points to a sub-formula of this formula; false, otherwise.

```
12.89.4.11 empty() template<typename Pol > bool carl::Formula< Pol >::empty ( ) const [inline]
```

true, if this formula has sub-formulas; false, otherwise.

```
12.89.4.12 end() template<typename Pol >
const_iterator carl::Formula< Pol >::end ( ) const [inline]
```

#### Returns

A constant iterator to the end of the list of sub-formulas of this formula.

```
12.89.4.13 first_case() template<typename Pol > const Formula& carl::Formula< Pol >::first_case ( ) const [inline]
```

#### Returns

A constant reference to the then-case, in case this formula is an ite-expression of formulas.

```
12.89.4.14 hash() template<typename Pol >
std::size_t carl::Formula< Pol >::hash () const [inline]
```

## Returns

A hash value for this formula.

```
12.89.4.15 id() template<typename Pol >
std::size_t carl::Formula< Pol >::id ( ) const [inline]
```

# Returns

The unique id for this formula.

Gets the propositions of this formula.

It updates and stores the propositions if they are not up to date, hence this method is quite efficient.

```
12.89.4.17 is_atom() template<typename Pol >
bool carl::Formula< Pol >::is_atom () const [inline]
```

true, if this formula is a Boolean atom.

```
12.89.4.18 is_boolean_combination() template<typename Pol > bool carl::Formula< Pol >::is_boolean_combination ( ) const [inline]
```

#### Returns

true, if the outermost operator of this formula is Boolean; false, otherwise.

```
12.89.4.19 is_bound() template<typename Pol >
bool carl::Formula< Pol >::is_bound ( ) const [inline]
```

```
12.89.4.20 is_constraint_conjunction() template<typename Pol > bool carl::Formula< Pol >::is_constraint_conjunction ( ) const [inline]
```

## Returns

true, if this formula is a conjunction of constraints; false, otherwise.

```
12.89.4.21 is_false() template<typename Pol >
bool carl::Formula< Pol >::is_false ( ) const [inline]
```

## Returns

true, if this formula represents FALSE.

```
12.89.4.22 is_integer_constraint_conjunction() template<typename Pol > bool carl::Formula< Pol >::is_integer_constraint_conjunction () const [inline]
```

## Returns

true, if this formula is a conjunction of integer constraints; false, otherwise.

```
12.89.4.23 is_literal() template<typename Pol >
bool carl::Formula< Pol >::is_literal ( ) const [inline]
12.89.4.24 is_nary() template<typename Pol >
bool carl::Formula< Pol >::is_nary ( ) const [inline]
Returns
     true, if the type of this formulas allows n-ary combinations of sub-formulas, for an arbitrary n.
12.89.4.25 is_only_propositional() template<typename Pol >
bool carl::Formula< Pol >::is_only_propositional ( ) const [inline]
Returns
     true, if this formula is propositional; false, otherwise.
12.89.4.26 is_real_constraint_conjunction() template<typename Pol >
bool carl::Formula< Pol >::is_real_constraint_conjunction ( ) const [inline]
Returns
     true, if this formula is a conjunction of real constraints; false, otherwise.
12.89.4.27 is_true() template<typename Pol >
bool carl::Formula< Pol >::is_true ( ) const [inline]
Returns
     true, if this formula represents TRUE.
12.89.4.28 logic() template<typename Pol >
Logic carl::Formula < Pol >::logic ( ) const [inline]
12.89.4.29 negated() template<typename Pol >
Formula carl::Formula< Pol >::negated ( ) const [inline]
12.89.4.30 operator"!() template<typename Pol >
Formula carl::Formula< Pol >::operator! ( ) const [inline]
12.89.4.31 operator"!=() template<typename Pol >
```

const Formula < Pol > & \_formula ) const [inline]

bool carl::Formula< Pol >::operator!= (

## **Parameters**

| _formula | The formula to compare with. |
|----------|------------------------------|
|----------|------------------------------|

# Returns

true, if this formula and the given formula are not equal.

#### **Parameters**

| ₋formula | The formula to compare with. |
|----------|------------------------------|
|----------|------------------------------|

## Returns

true, if the id of this formula is less than the id of the given one.

## **Parameters**

| <i>_formula</i> The formula to compare wit | h. |
|--|----|
|--|----|

# Returns

true, if the id of this formula is less or equal than the id of the given one.

```
12.89.4.35 operator=() [2/2] template<typename Pol >
Formula& carl::Formula< Pol >::operator= (
Formula< Pol > && _formula ) [inline]
```

#### **Parameters**

| ₋formula | The formula to compare with. |
|----------|------------------------------|
|----------|------------------------------|

## Returns

true, if this formula and the given formula are equal; false, otherwise.

## **Parameters**

| _formula | The formula to compare with. |
|----------|------------------------------|
|----------|------------------------------|

#### Returns

true, if the id of this formula is greater than the id of the given one.

#### **Parameters**

| ₋formula | The formula to compare with. |
|----------|------------------------------|
|----------|------------------------------|

## Returns

true, if the id of this formula is greater or equal than the id of the given one.

```
12.89.4.39 premise() template<typename Pol > const Formula& carl::Formula< Pol >::premise ( ) const [inline]
```

# Returns

A constant reference to the premise, in case this formula is an implication.

```
12.89.4.40 properties() template<typename Pol >
const Condition& carl::Formula< Pol >::properties ( ) const [inline]
```

The bit-vector representing the propositions of this formula. For further information see the Condition class.

Checks if the given property holds for this formula.

(Very cheap operation which only relies on bit checks)

#### **Parameters**

```
_property The property to check this formula for.
```

#### Returns

true, if the given property holds for this formula; false, otherwise.

```
12.89.4.42 quantified_formula() template<typename Pol > const Formula& carl::Formula< Pol >::quantified_formula ( ) const [inline]
```

# Returns

A constant reference to the bound formula, in case this formula is a quantified formula.

```
12.89.4.43 quantified_variables() template<typename Pol > const std::vector<carl::Variable>& carl::Formula< Pol >::quantified_variables ( ) const [inline]
```

## Returns

A constant reference to the quantifed variables, in case this formula is a quantified formula.

```
12.89.4.44 rbegin() template<typename Pol > const_reverse_iterator carl::Formula< Pol >::rbegin ( ) const [inline]
```

## Returns

A constant reverse iterator to the beginning of the list of sub-formulas of this formula.

```
12.89.4.45 remove_negations() template<typename Pol > const Formula& carl::Formula< Pol >::remove_negations ( ) const [inline]
```

```
12.89.4.46 rend() template<typename Pol >
const-reverse_iterator carl::Formula< Pol >::rend ( ) const [inline]
```

A constant reverse iterator to the end of the list of sub-formulas of this formula.

```
12.89.4.47 second_case() template<typename Pol > const Formula& carl::Formula
    Pol >::second_case ( ) const [inline]
```

#### Returns

A constant reference to the else-case, in case this formula is an ite-expression of formulas.

Sets the activity to the given value.

## **Parameters**

| ₋activity | The value to set the activity to. |
|-----------|-----------------------------------|
|-----------|-----------------------------------|

```
12.89.4.49 size() template<typename Pol > size.t carl::Formula< Pol >::size ( ) const [inline]
```

#### Returns

The number of sub-formulas of this formula.

```
12.89.4.50 subformula() template<typename Pol > const Formula& carl::Formula< Pol >::subformula ( ) const [inline]
```

# Returns

A constant reference to the only sub-formula, in case this formula is an negation.

```
12.89.4.51 subformulas() template<typename Pol > const Formulas<Pol>& carl::Formula
Pol >::subformulas ( ) const [inline]
```

A constant reference to the list of sub-formulas of this formula. Note, that this formula has to be a Boolean combination, if you invoke this method.

```
12.89.4.52 type() template<typename Pol >
FormulaType carl::Formula< Pol >::type ( ) const [inline]
```

## Returns

The type of this formula.

```
12.89.4.53 u_equality() template<typename Pol > const UEquality& carl::Formula< Pol >::u_equality ( ) const [inline]
```

#### Returns

A constant reference to the uninterpreted equality represented by this formula. Note, that this formula has to be of type UEQ, if you invoke this method.

```
12.89.4.54 variable_assignment() template<typename Pol >
const VariableAssignment<Pol>& carl::Formula< Pol >::variable_assignment ( ) const [inline]

12.89.4.55 variable_comparison() template<typename Pol >
const VariableComparison<Pol>& carl::Formula< Pol >::variable_comparison ( ) const [inline]
```

```
12.89.4.56 variables() template<typename Pol > const Variables& carl::Formula< Pol >::variables ( ) const [inline]
```

## 12.89.5 Friends And Related Function Documentation

```
12.89.5.1 FormulaContent< Pol > template<typename Pol > friend class FormulaContent< Pol > [friend]
```

```
12.89.5.2 FormulaPool > Pol > template < typename Pol >
friend class FormulaPool < Pol > [friend]
```

The output operator of a formula.

#### **Parameters**

| os | The stream to print on. |
|----|-------------------------|
| f  | The formula to print.   |

# 12.90 carl::FormulaContent< Pol > Class Template Reference

```
#include <FormulaContent.h>
```

# **Public Member Functions**

∼FormulaContent ()

## Destructor.

- std::size\_t hash () const
- std::size\_t id () const
- bool is\_nary () const
- bool operator== (const FormulaContent &\_content) const

# Friends

- class Formula < Pol >
- class FormulaPool< Pol >
- template<typename P > std::ostream & operator<< (std::ostream &os, const FormulaContent< P > &f)

# 12.90.1 Constructor & Destructor Documentation

```
12.90.1.1 ~FormulaContent() template<typename Pol >
carl::FormulaContent< Pol >::~FormulaContent ( ) [inline]
Destructor.
12.90.2 Member Function Documentation
12.90.2.1 hash() template<typename Pol >
std::size_t carl::FormulaContent< Pol >::hash ( ) const [inline]
12.90.2.2 id() template<typename Pol >
std::size_t carl::FormulaContent< Pol >::id ( ) const [inline]
12.90.2.3 is_nary() template<typename Pol >
bool carl::FormulaContent< Pol >::is_nary ( ) const [inline]
12.90.2.4 operator==() template<typename Pol >
bool carl::FormulaContent< Pol >::operator== (
             const FormulaContent< Pol > & _content ) const
12.90.3 Friends And Related Function Documentation
12.90.3.1 Formula < Pol > template < typename Pol >
friend class Formula< Pol > [friend]
12.90.3.2 FormulaPool < Pol > template < typename Pol >
friend class FormulaPool< Pol > [friend]
12.90.3.3 operator << template < typename Pol >
template<typename P >
std::ostream& operator<< (</pre>
```

std::ostream & os,

const FormulaContent< P > & f ) [friend]

# 12.91 carl::io::parser::FormulaParser< Pol > Struct Template Reference

```
#include <FormulaParser.h>
```

#### **Public Member Functions**

- FormulaParser ()
- void addVariable (Variable::Arg v)

#### 12.91.1 Constructor & Destructor Documentation

```
12.91.1.1 FormulaParser() template<typename Pol >
carl::io::parser::FormulaParser< Pol >::FormulaParser ( ) [inline]
```

#### 12.91.2 Member Function Documentation

# 12.92 carl::FormulaPool < Pol > Class Template Reference

```
#include <FormulaPool.h>
```

# **Public Member Functions**

- std::size\_t size () const
- void print () const
- Formula < Pol > getTseitinVar (const Formula < Pol > &\_formula)
- Formula < Pol > createTseitinVar (const Formula < Pol > &\_formula)
- template<typename ArgType >
   void forallDo (void(\*\_func)(ArgType \*, const Formula< Pol > &), ArgType \*\_arg) const
- bool formulas Inverse (const Formula < Pol > & subformula A, const Formula < Pol > & subformula B)

# **Static Public Member Functions**

static FormulaPool< Pol > & getInstance ()

Returns the single instance of this class by reference.

## **Protected Member Functions**

- FormulaPool (unsigned \_capacity=10000)
   Constructor of the formula pool.
- ∼FormulaPool ()
- const FormulaContent< Pol > \* trueFormula () const
- const FormulaContent< Pol > \* falseFormula () const

## 12.92.1 Constructor & Destructor Documentation

Constructor of the formula pool.

#### **Parameters**

```
_capacity | Expected necessary capacity of the pool.
```

```
12.92.1.2 ~FormulaPool() template<typename Pol > carl::FormulaPool< Pol >::~FormulaPool ( ) [protected]
```

# 12.92.2 Member Function Documentation

```
12.92.2.2 falseFormula() template<typename Pol > const FormulaContent<Pol>* carl::FormulaPool< Pol >::falseFormula ( ) const [inline], [protected]
```

```
12.92.2.5 getInstance() static FormulaPool< Pol > & carl::Singleton< FormulaPool< Pol > \leftrightarrow ::getInstance ( ) [inline], [static], [inherited]
```

Returns the single instance of this class by reference.

If there is no instance yet, a new one is created.

```
12.92.2.7 print() template<typename Pol >
void carl::FormulaPool
Pol >::print () const [inline]
```

```
12.92.2.8 size() template<typename Pol >
std::size_t carl::FormulaPool< Pol >::size ( ) const [inline]
```

```
12.92.2.9 trueFormula() template<typename Pol > const FormulaContent<Pol>* carl::FormulaPool< Pol >::trueFormula ( ) const [inline], [protected]
```

## 12.93 carl::BitVector::forward\_iterator Class Reference

```
#include <BitVector.h>
```

# **Public Member Functions**

- forward\_iterator (const std::vector< unsigned >::const\_iterator it, const std::vector< unsigned >↔ ::const\_iterator vectorEnd)
- bool get ()
- void next ()
- forward\_iterator operator++ (int i)
- bool isEnd ()

## **Protected Attributes**

- unsigned posInVec
- std::vector< unsigned >::const\_iterator vecIter
- const std::vector< unsigned >::const\_iterator vecEnd
- unsigned curVecElem

## **Friends**

• bool operator== (const forward\_iterator &fi1, const forward\_iterator &fi2)

## 12.93.1 Constructor & Destructor Documentation

#### 12.93.2 Member Function Documentation

```
12.93.2.1 get() bool carl::BitVector::forward_iterator::get ( ) [inline]
```

```
12.93.2.2 isEnd() bool carl::BitVector::forward_iterator::isEnd ( ) [inline]
```

```
12.93.2.3 next() void carl::BitVector::forward_iterator::next ( ) [inline]
```

```
12.93.2.4 operator++() forward_iterator carl::BitVector::forward_iterator::operator++ ( int i ) [inline]
```

## 12.93.3 Friends And Related Function Documentation

#### 12.93.4 Field Documentation

**12.93.4.1 curVecElem** unsigned carl::BitVector::forward\_iterator::curVecElem [protected]

**12.93.4.2 posinVec** unsigned carl::BitVector::forward\_iterator::posInVec [protected]

**12.93.4.3 vecEnd** const std::vector<unsigned>::const\_iterator carl::BitVector::forward.← iterator::vecEnd [protected]

# 12.94 carl::FromGiNaC< C > Class Template Reference

#include <GiNaCAdaptor.h>

# **Public Types**

· typedef C Number

# 12.94.1 Member Typedef Documentation

```
12.94.1.1 Number template<typename C > typedef C carl::FromGiNaC< C >::Number
```

# 12.95 carl::GaloisField< IntegerType > Class Template Reference

A finite field.

#include <GaloisField.h>

# **Public Types**

• using BaseIntType = unsigned

## **Public Member Functions**

• GaloisField (BaseIntType p, BaseIntType k=1)

Creating the field  $Z_{-}\{p^{\wedge}k\}$ .

• BaseIntType p () const noexcept

Returns the p from  $Z_{-}\{p^{\wedge}k\}$ .

• BaseIntType k () const noexcept

Returns the k from  $Z_{-}\{p^{\wedge}k\}$ .

- const IntegerType & size () const noexcept
- IntegerType modulo (const IntegerType &n) const
- IntegerType symmetric\_modulo (const IntegerType &n) const

## **Friends**

- bool operator== (const GaloisField &lhs, const GaloisField &rhs)
- std::ostream & operator<< (std::ostream &os, const GaloisField &rhs)</li>

# 12.95.1 Detailed Description

```
template<typename IntegerType> class carl::GaloisField< IntegerType >
```

A finite field.

# 12.95.2 Member Typedef Documentation

```
12.95.2.1 BaseIntType template<typename IntegerType >
using carl::GaloisField< IntegerType >::BaseIntType = unsigned
```

#### 12.95.3 Constructor & Destructor Documentation

Creating the field  $Z_{-}\{p^{\wedge}k\}$ .

## **Parameters**

| р | A prime number |
|---|----------------|
| k | A exponent     |

See also

GaloisFieldManager where the overhead of creating several GFs is prevented by storing them.

## 12.95.4 Member Function Documentation

```
12.95.4.1 k() template<typename IntegerType >
BaseIntType carl::GaloisField< IntegerType >::k ( ) const [inline], [noexcept]
Returns the k from Z_{-}\{p^{\wedge}k\}.
Returns
     A positive integer
12.95.4.2 modulo() template<typename IntegerType >
IntegerType carl::GaloisField< IntegerType >::modulo (
             const IntegerType & n ) const [inline]
12.95.4.3 p() template<typename IntegerType >
BaseIntType carl::GaloisField< IntegerType >::p ( ) const [inline], [noexcept]
Returns the p from Z_{-}\{p^{\wedge}k\}.
Returns
    a prime
12.95.4.4 size() template<typename IntegerType >
const IntegerType& carl::GaloisField< IntegerType >::size ( ) const [inline], [noexcept]
12.95.4.5 symmetric_modulo() template<typename IntegerType >
IntegerType carl::GaloisField< IntegerType >::symmetric_modulo (
             const IntegerType & n ) const [inline]
```

## 12.95.5 Friends And Related Function Documentation

# 12.96 carl::GaloisFieldManager < IntegerType > Class Template Reference

```
#include <GaloisField.h>
```

## **Public Types**

using BaseIntType = typename GaloisField< IntegerType >::BaseIntType

## **Public Member Functions**

const GaloisField< IntegerType > \* field (BaseIntType p, BaseIntType k=1)

## **Static Public Member Functions**

static GaloisFieldManager< IntegerType > & getInstance ()
 Returns the single instance of this class by reference.

## 12.96.1 Member Typedef Documentation

```
12.96.1.1 BaseIntType template<typename IntegerType >
using carl::GaloisFieldManager< IntegerType >::BaseIntType = typename GaloisField<Integer←
Type>::BaseIntType
```

## 12.96.2 Member Function Documentation

```
12.96.2.2 getInstance() static GaloisFieldManager< IntegerType > & carl::Singleton< GaloisFieldManager<
IntegerType > >::getInstance ( ) [inline], [static], [inherited]
```

Returns the single instance of this class by reference.

If there is no instance yet, a new one is created.

# 12.97 carl::GBProcedure< Polynomial, Procedure, AddingPolynomialPolicy > Class Template Reference

A general class for Groebner Basis calculation.

```
#include <GBProcedure.h>
```

#### **Public Member Functions**

- GBProcedure ()
- GBProcedure (const GBProcedure &old)
- virtual ∼GBProcedure ()=default
- GBProcedure & operator= (const GBProcedure &rhs)
- bool inputEmpty () const

Check whether a polynomial is scheduled to be added to the Groebner basis.

• size\_t nrOrigGenerators () const

The number of polynomials which were originally added to the GB.

void addPolynomial (const Polynomial &p)

Add a polynmomial which is added to the groebner basis during the next calculate call.

bool basisis\_constant () const

Checks whether the current representants of the GB contain a constant polynomial.

- std::list< Polynomial > listBasisPolynomials () const
- const std::vector< Polynomial > & getBasisPolynomials () const
- void printScheduledPolynomials (bool breakLines=true, bool printReasons=true, std::ostream &os=std::cout) const
- void reset ()

Remove all polynomials from the Groebner basis.

• const Ideal < Polynomial > & getIdeal () const

Get the ideal which encodes the GB.

void calculate ()

Calculate the Groebner basis of the current GB union the scheduled polynomials.

std::list< std::pair< BitVector, BitVector >> reduceInput ()

Reduce the input polynomials using the other input polynomials and the current Groebner basis.

# 12.97.1 Detailed Description

```
template < typename \ > class \ > class \ Procedure, \\ template < typename \ > class \ > class \ Procedure, \\ template < typename \ > class \ AddingPolynomialPolicy > \\ class \ carl::GBProcedure < Polynomial, Procedure, AddingPolynomialPolicy > \\ \\
```

A general class for Groebner Basis calculation.

It is parameterized not only in the type of polynomial to be used, but also in the concrete procedure to be used, and the way polynomials should be added to this procedure.

Please notice that this class is designed to support incremental calls. Therefore, it holds a queue with the polynomials which are added. Only upon calling the calculate method, these polynoimials are added to the actual groebner basis.

Moreover, we can

#### 12.97.2 Constructor & Destructor Documentation

```
12.97.2.1 GBProcedure() [1/2] template<typename Polynomial, template< typename, template<typename > class > class Procedure, template< typename > class AddingPolynomialPolicy> carl::GBProcedure< Polynomial, Procedure, AddingPolynomialPolicy >::GBProcedure () [inline]
```

```
12.97.2.3 ~GBProcedure() template<typename Polynomial, template< typename, template< typename > class > class Procedure, template< typename > class AddingPolynomialPolicy> virtual carl::GBProcedure< Polynomial, Procedure, AddingPolynomialPolicy >::~GBProcedure () [virtual], [default]
```

#### 12.97.3 Member Function Documentation

Add a polynmomial which is added to the groebner basis during the next calculate call.

### **Parameters**

p The polynomial to be added.

Implements carl::AbstractGBProcedure < Polynomial >.

```
12.97.3.2 basisis_constant() template<typename Polynomial, template< typename, template< typename > class > class Procedure, template< typename > class AddingPolynomialPolicy> bool carl::GBProcedure< Polynomial, Procedure, AddingPolynomialPolicy >::basisis_constant () const [inline]
```

Checks whether the current representants of the GB contain a constant polynomial.

Returns

12.97.3.3 calculate() template<typename Polynomial, template< typename, template< typename > class > class Procedure, template< typename > class AddingPolynomialPolicy> void carl::GBProcedure< Polynomial, Procedure, AddingPolynomialPolicy >::calculate () [inline], [virtual]

Calculate the Groebner basis of the current GB union the scheduled polynomials.

Implements carl::AbstractGBProcedure < Polynomial >.

12.97.3.4 getBasisPolynomials() template<typename Polynomial, template< typename, template<
typename > class > class Procedure, template< typename > class AddingPolynomialPolicy>
const std::vector<Polynomial>& carl::GBProcedure< Polynomial, Procedure, AddingPolynomial←
Policy >::getBasisPolynomials ( ) const [inline]

Returns

12.97.3.5 getIdeal() template<typename Polynomial , template< typename > class > class Procedure, template< typename > class AddingPolynomialPolicy> const Ideal<Polynomial>& carl::GBProcedure< Polynomial, Procedure, AddingPolynomialPolicy > ← ::getIdeal () const [inline], [virtual]

Get the ideal which encodes the GB.

Returns

Implements carl::AbstractGBProcedure < Polynomial >.

12.97.3.6 inputEmpty() template<typename Polynomial , template< typename, template< typename > class > class Procedure, template< typename > class AddingPolynomialPolicy> bool carl::GBProcedure< Polynomial, Procedure, AddingPolynomialPolicy >::inputEmpty ( ) const [inline]

Check whether a polynomial is scheduled to be added to the Groebner basis.

Returns

whether the input is empty.

12.97.3.7 listBasisPolynomials() template<typename Polynomial , template< typename, template<typename > class > class Procedure, template< typename > class AddingPolynomialPolicy> std::list<Polynomial> carl::GBProcedure< Polynomial, Procedure, AddingPolynomialPolicy > ::listBasisPolynomials ( ) const [inline]

Returns

12.97.3.8 nrOrigGenerators() template<typename Polynomial, template< typename, template<
typename > class > class Procedure, template< typename > class AddingPolynomialPolicy>
size\_t carl::GBProcedure< Polynomial, Procedure, AddingPolynomialPolicy >::nrOrigGenerators (
) const [inline]

The number of polynomials which were originally added to the GB.

#### Returns

number of polynomials added.

```
12.97.3.11 reduceInput() template<typename Polynomial , template< typename, template< typename > class > class Procedure, template< typename > class AddingPolynomialPolicy> std::list<std::pair<BitVector, BitVector> > carl::GBProcedure< Polynomial, Procedure, Adding← PolynomialPolicy >::reduceInput () [inline], [virtual]
```

Reduce the input polynomials using the other input polynomials and the current Groebner basis.

Returns

Implements carl::AbstractGBProcedure< Polynomial >.

```
12.97.3.12 reset() template<typename Polynomial , template< typename, template< typename > class > class Procedure, template< typename > class AddingPolynomialPolicy> void carl::GBProcedure< Polynomial, Procedure, AddingPolynomialPolicy >::reset () [inline], [virtual]
```

Remove all polynomials from the Groebner basis.

Implements carl::AbstractGBProcedure< Polynomial >.

# 12.98 carl::GFNumber< IntegerType > Class Template Reference

```
Galois Field numbers, i.e.
```

```
#include <GFNumber.h>
```

#### **Public Member Functions**

- GFNumber ()=default
- GFNumber (IntegerType n, const GaloisField< IntegerType > \*gf=nullptr)
- GFNumber (const GFNumber &n, const GaloisField < IntegerType > \*gf)
- const GaloisField< IntegerType > \* gf () const
- GFNumber < IntegerType > toGF (const GaloisField < IntegerType > \*newfield) const
- void normalize ()
- · bool is\_zero () const
- bool is\_one () const
- · bool is\_unit () const
- const IntegerType & representing\_integer () const
- GFNumber inverse () const
- const GFNumber operator- () const
- GFNumber & operator++ ()
- GFNumber & operator+= (const GFNumber &rhs)
- GFNumber & operator+= (const IntegerType &rhs)
- GFNumber & operator-- ()
- GFNumber & operator-= (const GFNumber &rhs)
- GFNumber & operator-= (const IntegerType &rhs)
- GFNumber & operator\*= (const GFNumber &rhs)
- GFNumber & operator\*= (const IntegerType &rhs)
- GFNumber & operator/= (const GFNumber &rhs)

#### Friends

```
    template<typename IntegerT > bool operator== (const GFNumber< IntegerT > &lhs, const GFNumber< IntegerT > &rhs)
    template<typename IntegerT > bool operator== (const GFNumber< IntegerT > &lhs, const IntegerT &rhs)
        Ihs == rhs, if rhs \in [lhs].
    template<typename IntegerT > bool operator== (const IntegerT &lhs, const GFNumber< IntegerT > &rhs)
        Ihs == rhs, if lhs \in [rhs].
    template<typename IntegerT > bool operator== (const GFNumber< IntegerT > &lhs, const GFNumber< IntegerT > &rhs)
```

```
    template<typename IntegerT >

      bool operator== (const GFNumber < IntegerT > &lhs, int rhs)
          lhs == rhs, if rhs \setminus in [lhs].

    template<typename IntegerT >

      bool operator== (int lhs, const GFNumber < IntegerT > &rhs)
          Ihs == rhs, if Ihs \setminus in [rhs].

    template<typename IntegerT >

      bool operator!= (const GFNumber < IntegerT > &lhs, const GFNumber < IntegerT > &rhs)

    template<typename IntegerT >

      bool operator!= (const GFNumber < IntegerT > &lhs, const IntegerT &rhs)

    template<typename IntegerT >

      bool operator!= (const IntegerT &lhs, const GFNumber< IntegerT > &rhs)

    template<typename IntegerT >

      bool operator!= (const GFNumber < IntegerT > &Ihs, int rhs)

    template<typename IntegerT >

      bool operator!= (int lhs, const GFNumber < IntegerT > &rhs)
    template<typename IntegerT >
      GFNumber< IntegerT > operator+ (const GFNumber< IntegerT > &lhs, const GFNumber< IntegerT >
      &rhs)

    template<typename IntegerT >

      GFNumber < IntegerT > operator+ (const GFNumber < IntegerT > &lhs, const IntegerT &rhs)
    • template<typename IntegerT >
      GFNumber < IntegerT > operator+ (const IntegerT &lhs, const GFNumber < IntegerT > &rhs)

    template<typename IntegerT >

      GFNumber < IntegerT > operator- (const GFNumber < IntegerT > &lhs, const GFNumber < IntegerT > &rhs)
    template<typename IntegerT >
      GFNumber < IntegerT > operator- (const GFNumber < IntegerT > &lhs, const IntegerT &rhs)

    template<typename IntegerT >

      GFNumber < IntegerT > operator- (const IntegerT &lhs, const GFNumber < IntegerT > &rhs)
    template<typename IntegerT >
      GFNumber < IntegerT > operator* (const GFNumber < IntegerT > &lhs, const GFNumber < IntegerT >
      &rhs)
    • template<typename IntegerT >
      GFNumber < IntegerT > operator* (const GFNumber < IntegerT > &lhs, const IntegerT &rhs)

    template<typename IntegerT >

      GFNumber < IntegerT > operator* (const IntegerT & lhs, const GFNumber < IntegerT > & rhs)
    template<typename IntegerT >
      GFNumber < IntegerT > operator/ (const GFNumber < IntegerT > &lhs, const GFNumber < IntegerT > &rhs)

    std::ostream & operator<< (std::ostream &os, const GFNumber &rhs)</li>

template<typename IntegerType>
```

# 12.98.1 Detailed Description

```
class carl::GFNumber < IntegerType >
```

Galois Field numbers, i.e.

numbers from fields with a finite characteristic.

## 12.98.2 Constructor & Destructor Documentation

```
12.98.2.1 GFNumber() [1/3] template<typename IntegerType >
carl::GFNumber< IntegerType >::GFNumber ( ) [default]
12.98.2.2 GFNumber() [2/3] template<typename IntegerType >
carl::GFNumber< IntegerType >::GFNumber (
            IntegerType n,
            const GaloisField< IntegerType > * gf = nullptr ) [inline], [explicit]
12.98.2.3 GFNumber() [3/3] template<typename IntegerType >
carl::GFNumber< IntegerType >::GFNumber (
            const GFNumber< IntegerType > & n,
            const GaloisField< IntegerType > * gf ) [inline]
12.98.3 Member Function Documentation
12.98.3.1 gf() template<typename IntegerType >
const GaloisField<IntegerType>* carl::GFNumber< IntegerType >::gf () const [inline]
12.98.3.2 inverse() template<typename IntegerT >
GFNumber< IntegerT > carl::GFNumber< IntegerT >::inverse
12.98.3.3 is_one() template<typename IntegerType >
bool carl::GFNumber< IntegerType >::is_one ( ) const [inline]
12.98.3.4 is_unit() template<typename IntegerType >
bool carl::GFNumber< IntegerType >::is_unit ( ) const [inline]
12.98.3.5 is_zero() template<typename IntegerType >
bool carl::GFNumber< IntegerType >::is_zero ( ) const [inline]
```

```
12.98.3.6 normalize() template<typename IntegerType >
void carl::GFNumber< IntegerType >::normalize ( ) [inline]
12.98.3.7 operator*=() [1/2] template<typename IntegerT >
\label{eq:GFNumber} \textit{GFNumber} < \textit{IntegerT} > \& \textit{carl::GFNumber} < \textit{IntegerT} > ::operator *= (
             const GFNumber< IntegerType > & rhs )
12.98.3.8 operator*=() [2/2] template<typename IntegerType >
GFNumber< IntegerType > & carl::GFNumber< IntegerType >::operator*= (
             const IntegerType & rhs )
12.98.3.9 operator++() template<typename IntegerT >
GFNumber< IntegerT > & carl::GFNumber< IntegerT >::operator++
12.98.3.10 operator+=() [1/2] template<typename IntegerType >
GFNumber< IntegerType > & carl::GFNumber< IntegerType >::operator+= (
             const GFNumber< IntegerType > & rhs )
12.98.3.11 operator+=() [2/2] template<typename IntegerType >
GFNumber< IntegerType > & carl::GFNumber< IntegerType >::operator+= (
             const IntegerType & rhs )
12.98.3.12 operator-() template<typename IntegerT >
const GFNumber< IntegerT > carl::GFNumber< IntegerT >::operator-
12.98.3.13 operator--() template<typename IntegerT >
GFNumber< IntegerT > & carl::GFNumber< IntegerT >::operator--
12.98.3.14 operator-=() [1/2] template<typename IntegerType >
GFNumber< IntegerType > & carl::GFNumber< IntegerType >::operator-= (
             const GFNumber< IntegerType > & rhs )
```

```
12.98.3.15 operator-=() [2/2] template<typename IntegerType >
GFNumber< IntegerType > & carl::GFNumber< IntegerType >::operator-= (
            const IntegerType & rhs )
12.98.3.16 operator/=() template<typename IntegerType >
GFNumber< IntegerT > & carl::GFNumber< IntegerT >::operator/= (
            const GFNumber< IntegerType > & rhs )
12.98.3.17 representing_integer() template<typename IntegerType >
const IntegerType& carl::GFNumber< IntegerType >::representing_integer ( ) const [inline]
12.98.3.18 toGF() template<typename IntegerType >
GFNumber<IntegerType> carl::GFNumber< IntegerType >::toGF (
             const GaloisField< IntegerType > * newfield ) const [inline]
12.98.4 Friends And Related Function Documentation
12.98.4.1 operator"!= [1/5] template<typename IntegerType >
{\tt template}{<}{\tt typename \ IntegerT} \,>\,
bool operator!= (
            const GFNumber< IntegerT > & lhs,
            const GFNumber< IntegerT > & rhs ) [friend]
12.98.4.2 operator"!= [2/5] template<typename IntegerType >
template<typename IntegerT >
bool operator!= (
            const GFNumber< IntegerT > & lhs,
             const IntegerT & rhs ) [friend]
12.98.4.3 operator"!= [3/5] template<typename IntegerType >
template<typename IntegerT >
bool operator!= (
            const GFNumber< IntegerT > & lhs,
             int rhs ) [friend]
```

```
12.98.4.4 operator"!= [4/5] template<typename IntegerType >
template<typename IntegerT >
bool operator!= (
            const IntegerT & lhs,
             const GFNumber< IntegerT > & rhs ) [friend]
12.98.4.5 operator"!= [5/5] template<typename IntegerType >
template<typename IntegerT >
bool operator!= (
            int lhs,
             const GFNumber< IntegerT > & rhs ) [friend]
12.98.4.6 operator* [1/3] template<typename IntegerType >
template<typename IntegerT >
GFNumber<IntegerT> operator* (
            const GFNumber< IntegerT > & lhs,
             const GFNumber< IntegerT > & rhs ) [friend]
12.98.4.7 operator* [2/3] template<typename IntegerType >
template<typename IntegerT >
{\tt GFNumber}{<}{\tt IntegerT}{>}\ {\tt operator*}\ (
            const GFNumber< IntegerT > & lhs,
            const IntegerT & rhs ) [friend]
12.98.4.8 operator* [3/3] template<typename IntegerType >
template<typename IntegerT >
GFNumber<IntegerT> operator* (
             const IntegerT & lhs,
             const GFNumber< IntegerT > & rhs ) [friend]
12.98.4.9 operator+[1/3] template<typename IntegerType >
template<typename IntegerT >
GFNumber<IntegerT> operator+ (
            const GFNumber< IntegerT > & lhs,
            const GFNumber< IntegerT > & rhs ) [friend]
```

```
12.98.4.10 operator+ [2/3] template<typename IntegerType >
template<typename IntegerT >
{\tt GFNumber}{<}{\tt IntegerT}{>}\ {\tt operator+}\ (
            const GFNumber< IntegerT > & lhs,
             const IntegerT & rhs ) [friend]
12.98.4.11 operator+ [3/3] template<typename IntegerType >
template<typename IntegerT >
GFNumber<IntegerT> operator+ (
             const IntegerT & lhs,
             const GFNumber< IntegerT > & rhs ) [friend]
12.98.4.12 operator- [1/3] template<typename IntegerType >
template<typename IntegerT >
GFNumber<IntegerT> operator- (
            const GFNumber< IntegerT > & lhs,
             const GFNumber< IntegerT > & rhs ) [friend]
12.98.4.13 operator-[2/3] template<typename IntegerType >
template<typename IntegerT >
GFNumber<IntegerT> operator- (
            const GFNumber< IntegerT > & lhs,
             const IntegerT & rhs ) [friend]
12.98.4.14 operator-[3/3] template<typename IntegerType >
template<typename IntegerT >
GFNumber<IntegerT> operator- (
             const IntegerT & lhs,
             const GFNumber< IntegerT > & rhs ) [friend]
12.98.4.15 operator/ template<typename IntegerType >
template<typename IntegerT >
GFNumber<IntegerT> operator/ (
            const GFNumber< IntegerT > & lhs,
             const GFNumber< IntegerT > & rhs ) [friend]
12.98.4.16 operator << template < typename IntegerType >
std::ostream& operator<< (</pre>
             std::ostream & os,
             const GFNumber< IntegerType > & rhs ) [friend]
```

```
12.98.4.17 operator== [1/6] template<typename IntegerType >
template<typename IntegerT >
bool operator== (
             const GFNumber< IntegerT > & lhs,
             const GFNumber< IntegerT > & rhs ) [friend]
12.98.4.18 operator== [2/6] template<typename IntegerType >
template<typename IntegerT >
bool operator== (
             const GFNumber< IntegerT > & lhs,
             const GFNumber< IntegerT > & rhs ) [friend]
12.98.4.19 operator== [3/6] template<typename IntegerType >
{\tt template}{<}{\tt typename \ IntegerT} \,>\,
bool operator== (
             const GFNumber< IntegerT > & lhs,
             const IntegerT & rhs ) [friend]
Ihs == rhs, if rhs \setminus in [lhs].
Returns
12.98.4.20 operator== [4/6] template<typename IntegerType >
template<typename IntegerT >
bool operator== (
             const GFNumber< IntegerT > & lhs,
             int rhs ) [friend]
Ihs == rhs, if rhs \in [Ihs].
Returns
12.98.4.21 operator== [5/6] template<typename IntegerType >
template<typename IntegerT >
bool operator== (
             const IntegerT & lhs,
             const GFNumber< IntegerT > & rhs ) [friend]
Ihs == rhs, if Ihs \inf [rhs].
```

Returns

Returns

#### 12.99 carl::GiNaCConversion Class Reference

```
#include <GiNaCAdaptor.h>
```

## **Static Public Attributes**

static std::map< carl::Variable, GiNaC::symbol > vars

#### 12.99.1 Field Documentation

```
12.99.1.1 vars std::map<carl::Variable, GiNaC::symbol> carl::GiNaCConversion::vars [static]
```

# 12.100 carl::formula::symmetry::GraphBuilder< Poly > Class Template Reference

```
#include <SymmetryFinder.h>
```

#### **Public Member Functions**

- GraphBuilder (const Formula < Poly > &f)
- Symmetries symmetries ()

#### 12.100.1 Constructor & Destructor Documentation

```
12.100.1.1 GraphBuilder() template<typename Poly > carl::formula::symmetry::GraphBuilder< Poly >::GraphBuilder ( const Formula< Poly > & f ) [inline]
```

#### 12.100.2 Member Function Documentation

```
12.100.2.1 symmetries() template<typename Poly >
Symmetries carl::formula::symmetry::GraphBuilder< Poly >::symmetries ( ) [inline]
```

# 12.101 carl::greater < T, mayBeNull > Struct Template Reference

```
#include <pointerOperations.h>
```

#### **Public Member Functions**

• bool operator() (const T &lhs, const T &rhs) const

#### **Data Fields**

std::greater
 T > \_greater

#### 12.101.1 Member Function Documentation

#### 12.101.2 Field Documentation

```
12.101.2.1 _greater template<typename T , bool mayBeNull = true>
std::greater<T> carl::greater< T, mayBeNull >::_greater
```

# 12.102 carl::greater< std::shared\_ptr< T >, mayBeNull > Struct Template Reference

```
#include <pointerOperations.h>
```

## **Public Member Functions**

• bool operator() (const std::shared\_ptr< const T > &lhs, const std::shared\_ptr< const T > &rhs) const

#### 12.102.1 Member Function Documentation

# 12.103 carl::greater < T \*, mayBeNull > Struct Template Reference

```
#include <pointerOperations.h>
```

## **Public Member Functions**

• bool operator() (const T \*Ihs, const T \*rhs) const

#### 12.103.1 Member Function Documentation

# 12.104 carl::GroebnerBase < Number > Class Template Reference

```
#include <GroebnerBase.h>
```

## **Public Types**

using Monomial = Term< Number >

#### **Public Member Functions**

- GroebnerBase ()
- template<typename InputIt > GroebnerBase (InputIt first, InputIt last)
- Polynomial reduce (const Polynomial &p) const
- const std::vector< Polynomial > & get () const
- bool isTrivialBase () const
- bool hasFiniteMon () const
- std::vector< Monomial > cor () const
- std::vector< Monomial > mon () const
- std::vector< Monomial > bor () const
- std::set< Variable > gatherVariables () const

## 12.104.1 Member Typedef Documentation

```
12.104.1.1 Monomial template<typename Number >
using carl::GroebnerBase< Number >::Monomial = Term<Number>
12.104.2 Constructor & Destructor Documentation
12.104.2.1 GroebnerBase() [1/2] template<typename Number >
carl::GroebnerBase< Number >::GroebnerBase ( ) [inline]
12.104.2.2 GroebnerBase() [2/2] template<typename Number >
template<typename InputIt >
carl::GroebnerBase< Number >::GroebnerBase (
            InputIt first,
            InputIt last ) [inline]
12.104.3 Member Function Documentation
12.104.3.1 bor() template<typename Number >
std::vector<Monomial> carl::GroebnerBase< Number >::bor ( ) const
12.104.3.2 cor() template<typename Number >
std::vector<Monomial> carl::GroebnerBase< Number >::cor ( ) const
12.104.3.3 gatherVariables() template<typename Number >
std::set<Variable> carl::GroebnerBase< Number >::gatherVariables ( ) const
12.104.3.4 get() template<typename Number >
const std::vector<Polynomial>& carl::GroebnerBase< Number >::get ( ) const [inline]
```

# 12.105 carl::has\_subtype< T > Struct Template Reference

This template is designed to provide types that are related to other types.

```
#include <typetraits.h>
```

# **Public Types**

```
    using type = T
    A type associated with the type.
```

## 12.105.1 Detailed Description

```
template<typename T> struct carl::has_subtype< T >
```

This template is designed to provide types that are related to other types.

It works very much like std::integral\_constant, except that it provides a type instead of a constant. We use it as an extension to type traits, meaning that types may have traits that are boolean or other types.

```
The class can be used as follows. Assume that you have a class A with an associated type B. template<T> struct Associated \{\}; template<> struct Associated<A>: has_subtype<B> \{\};
```

Now you can obtain the associated type with Associated < A > : : type.

## 12.105.2 Member Typedef Documentation

```
12.105.2.1 type template<typename T >
using carl::has_subtype< T >::type = T
```

A type associated with the type.

# 12.106 carl::hash< T, mayBeNull > Struct Template Reference

Alternative specialization of std::hash for pointer types.

```
#include <pointerOperations.h>
```

#### **Public Member Functions**

• bool operator() (const T &lhs, const T &rhs) const

#### **Data Fields**

std::hash
 T > \_hash

## 12.106.1 Detailed Description

```
template<typename T, bool mayBeNull = true> struct carl::hash< T, mayBeNull >
```

Alternative specialization of std::hash for pointer types.

In case the pointer is not a nullptr, we return the hash of the object it points to.

# 12.106.2 Member Function Documentation

#### 12.106.3 Field Documentation

```
12.106.3.1 _hash template<typename T , bool mayBeNull = true> std::hash<T> carl::hash< T, mayBeNull >::.hash
```

# 12.107 std::hash< carl::BasicConstraint< Pol > > Struct Template Reference

Implements std::hash for constraints.

#include <BasicConstraint.h>

#### **Public Member Functions**

• std::size\_t operator() (const carl::BasicConstraint< Pol > &constraint) const

# 12.107.1 Detailed Description

```
template<typename Pol> struct std::hash< carl::BasicConstraint< Pol>>
```

Implements std::hash for constraints.

## 12.107.2 Member Function Documentation

## **Parameters**

|            | The constant at a contract to the contract of |
|------------|---|
| constraint | The constraint to get the hash for.           |
|            | The content to got the maintain               |

## Returns

The hash of the given constraint.

## 12.108 std::hash< carl::Bitset > Struct Reference

```
#include <Bitset.h>
```

# **Public Member Functions**

• std::size\_t operator() (const carl::Bitset &bs) const

## 12.108.1 Member Function Documentation

```
12.108.1.1 operator()() std::size_t std::hash< carl::Bitset >::operator() ( const carl::Bitset & bs ) const [inline]
```

# 12.109 std::hash< carl::BoundType > Struct Reference

Specialization of std::hash for BoundType.

```
#include <BoundType.h>
```

#### **Public Member Functions**

std::size\_t operator() (carl::BoundType bt) const
 Calculates the hash of a BoundType.

## 12.109.1 Detailed Description

Specialization of std::hash for BoundType.

#### 12.109.2 Member Function Documentation

Calculates the hash of a BoundType.

# 12.110 std::hash< carl::BVBinaryContent > Struct Reference

```
#include <BVTermContent.h>
```

#### **Public Member Functions**

• std::size\_t operator() (const carl::BVBinaryContent &bc) const

#### 12.110.1 Member Function Documentation

```
12.110.1.1 operator()() std::size_t std::hash< carl::BVBinaryContent >::operator() ( const carl::BVBinaryContent & bc ) const [inline]
```

# 12.111 std::hash< carl::BVCompareRelation > Struct Reference

#include <BVCompareRelation.h>

#### **Public Member Functions**

• std::size\_t operator() (const carl::BVCompareRelation &\_rel) const

#### 12.111.1 Member Function Documentation

#### 12.112 std::hash< carl::BVConstraint > Struct Reference

Implements std::hash for bit-vector constraints.

```
#include <BVConstraint.h>
```

## **Public Member Functions**

• std::size\_t operator() (const carl::BVConstraint &c) const

## 12.112.1 Detailed Description

Implements std::hash for bit-vector constraints.

## 12.112.2 Member Function Documentation

```
12.112.2.1 operator()() std::size_t std::hash< carl::BVConstraint >::operator() ( const carl::BVConstraint & c ) const [inline]
```

# **Parameters**

| ₋constraint | The bit-vector constraint to get the hash for. |
|-------------|--|
|-------------|--|

## Returns

The hash of the given constraint.

# 12.113 std::hash< carl::BVExtractContent > Struct Reference

#include <BVTermContent.h>

#### **Public Member Functions**

• std::size\_t operator() (const carl::BVExtractContent &ec) const

#### 12.113.1 Member Function Documentation

## 12.114 std::hash< carl::BVTerm > Struct Reference

Implements std::hash for bit vector terms.

```
#include <BVTerm.h>
```

## **Public Member Functions**

std::size\_t operator() (const carl::BVTerm &t) const

## 12.114.1 Detailed Description

Implements std::hash for bit vector terms.

## 12.114.2 Member Function Documentation

## Parameters

t The bit vector term to get the hash for.

## Returns

The hash of the given bit vector term.

## 12.115 std::hash < carl::BVTermContent > Struct Reference

Implements std::hash for bit vector term contents.

#include <BVTermContent.h>

#### **Public Member Functions**

std::size\_t operator() (const carl::BVTermContent &tc) const

## 12.115.1 Detailed Description

Implements std::hash for bit vector term contents.

#### 12.115.2 Member Function Documentation

### **Parameters**

tc The bit vector term content to get the hash for.

#### Returns

The hash of the given bit vector term content.

# 12.116 std::hash< carl::BVUnaryContent > Struct Reference

#include <BVTermContent.h>

## **Public Member Functions**

• std::size\_t operator() (const carl::BVUnaryContent &uc) const

## 12.116.1 Member Function Documentation

# 12.117 std::hash< carl::BVValue > Struct Reference

Implements std::hash for bit vector values.

```
#include <BVValue.h>
```

#### **Public Member Functions**

std::size\_t operator() (const carl::BVValue &\_value) const

# 12.117.1 Detailed Description

Implements std::hash for bit vector values.

#### 12.117.2 Member Function Documentation

### **Parameters**

| _ <i>value</i> The bit vect | or value to get the hash for. |
|-----------------------------|-------------------------------|
|-----------------------------|-------------------------------|

#### Returns

The hash of the given bit vector value.

# 12.118 std::hash< carl::BVVariable > Struct Reference

Implement std::hash for bitvector variables.

```
#include <BVVariable.h>
```

#### **Public Member Functions**

• std::size\_t operator() (const carl::BVVariable &v) const

# 12.118.1 Detailed Description

Implement std::hash for bitvector variables.

# 12.118.2 Member Function Documentation

#### **Parameters**

v The bitvector variable to get the hash for.

#### Returns

The hash of the given bitvector variable.

# 12.119 std::hash< carl::Constraint< Pol > > Struct Template Reference

Implements std::hash for constraints.

```
#include <Constraint.h>
```

#### **Public Member Functions**

std::size\_t operator() (const carl::Constraint< Pol > &constraint) const

#### 12.119.1 Detailed Description

```
\label{eq:constraint} \begin{tabular}{ll} template < typename Pol > \\ struct std::hash < carl::Constraint < Pol > > \\ \end{tabular}
```

Implements std::hash for constraints.

## 12.119.2 Member Function Documentation

## **Parameters**

| constraint The const | raint to get the hash for. |
|----------------------|----------------------------|
|----------------------|----------------------------|

#### Returns

The hash of the given constraint.

# 12.120 std::hash< carl::ContextPolynomial< Coeff, Ordering, Policies > > Struct Template Reference

```
#include <ContextPolynomial.h>
```

#### **Public Member Functions**

• std::size\_t operator() (const carl::ContextPolynomial < Coeff, Ordering, Policies > &p) const

#### 12.120.1 Member Function Documentation

```
12.120.1.1 operator()() template<typename Coeff , typename Ordering , typename Policies > std::size_t std::hash< carl::ContextPolynomial< Coeff, Ordering, Policies > >::operator() ( const carl::ContextPolynomial< Coeff, Ordering, Policies > & p ) const [inline]
```

# 12.121 std::hash< carl::FactorizedPolynomial< P > > Struct Template Reference

#include <FactorizedPolynomial.h>

#### **Public Member Functions**

size\_t operator() (const carl::FactorizedPolynomial< P > &\_factPoly) const

#### 12.121.1 Member Function Documentation

# 12.122 std::hash< carl::FLOAT\_T< Number > > Struct Template Reference

```
#include <FLOAT_T.h>
```

## **Public Member Functions**

size\_t operator() (const carl::FLOAT\_T< Number > &\_in) const

# 12.122.1 Member Function Documentation

# 12.123 std::hash< carl::Formula< Pol > > Struct Template Reference

Implements std::hash for formulas.

```
#include <Formula.h>
```

#### **Public Member Functions**

std::size\_t operator() (const carl::Formula < Pol > &\_formula) const

## 12.123.1 Detailed Description

```
template<typename Pol> struct std::hash< carl::Formula< Pol>>
```

Implements std::hash for formulas.

#### 12.123.2 Member Function Documentation

# **Parameters**

| ı for. | The formula to get the hash | ₋formula |  |
|--------|-----------------------------|----------|--|
|--------|-----------------------------|----------|--|

#### Returns

The hash of the given formula.

# 12.124 std::hash< carl::FormulaContent< Pol > > Struct Template Reference

Implements std::hash for formula contents.

```
#include <Formula.h>
```

## **Public Member Functions**

 $\bullet \ \, \text{std::size\_t operator() (const carl::FormulaContent} < Pol > \&\_formulaContent) \ \, \text{const} \\$ 

#### 12.124.1 Detailed Description

```
template<typename Pol> struct std::hash< carl::FormulaContent< Pol>>
```

Implements std::hash for formula contents.

#### 12.124.2 Member Function Documentation

#### **Parameters**

\_formulaContent | The formula content to get the hash for.

#### Returns

The hash of the given formula content.

# 12.125 std::hash< carl::Interval< Number > > Struct Template Reference

Specialization of std::hash for an interval.

```
#include <Interval.h>
```

# **Public Member Functions**

std::size\_t operator() (const carl::Interval < Number > &interval) const
 Calculates the hash of an interval.

# 12.125.1 Detailed Description

```
template<typename Number>
struct std::hash< carl::Interval< Number>>
```

Specialization of std::hash for an interval.

#### 12.125.2 Member Function Documentation

Calculates the hash of an interval.

#### **Parameters**

| interval | An interval. |
|----------|--------------|
|          |              |

#### Returns

Hash of an interval.

# 12.126 std::hash< carl::IntRepRealAlgebraicNumber< Number > > Struct Template Reference

#include <Ran.h>

#### **Public Member Functions**

• std::size\_t operator() (const carl::IntRepRealAlgebraicNumber < Number > &n) const

#### 12.126.1 Member Function Documentation

## 12.127 std::hash< carl::ModelVariable > Struct Reference

```
#include <ModelVariable.h>
```

# **Public Member Functions**

std::size\_t operator() (const carl::ModelVariable &mv) const

#### 12.127.1 Member Function Documentation

# 12.128 std::hash < carl::Monomial > Struct Reference

```
The template specialization of std::hash for carl::Monomial. #include <Monomial.h>
```

#### **Public Member Functions**

std::size\_t operator() (const carl::Monomial &monomial) const

## 12.128.1 Detailed Description

The template specialization of  $\mathtt{std}:\mathtt{hash}$  for  $\mathtt{carl}:\mathtt{Monomial}.$ 

#### **Parameters**

| monomial | Monomial. |
|----------|-----------|
|----------|-----------|

## Returns

Hash of monomial.

#### 12.128.2 Member Function Documentation

# 12.129 std::hash< carl::Monomial::Arg > Struct Reference

The template specialization of std::hash for a shared pointer of a carl::Monomial.

```
#include <Monomial.h>
```

## **Public Member Functions**

• size\_t operator() (const carl::Monomial::Arg &monomial) const

## 12.129.1 Detailed Description

The template specialization of std::hash for a shared pointer of a carl::Monomial.

## **Parameters**

| monomial | The shared pointer to a monomial. |
|----------|-----------------------------------|
|----------|-----------------------------------|

# Returns

Hash of monomial.

### 12.129.2 Member Function Documentation

# 12.130 std::hash< carl::MultivariatePolynomial< C, O, P > Struct Template Reference

Specialization of std::hash for MultivariatePolynomial.

#include <MultivariatePolynomial.h>

#### **Public Member Functions**

• std::size\_t operator() (const carl::MultivariatePolynomial< C, O, P > &mpoly) const Calculates the hash of a MultivariatePolynomial.

# 12.130.1 Detailed Description

```
template<typename C, typename O, typename P> struct std::hash< carl::MultivariatePolynomial< C, O, P >>
```

Specialization of std::hash for MultivariatePolynomial.

#### 12.130.2 Member Function Documentation

Calculates the hash of a MultivariatePolynomial.

### **Parameters**

#### Returns

Hash of mpoly.

# 12.131 std::hash< carl::MultivariateRoot< Pol > > Struct Template Reference

```
#include <MultivariateRoot.h>
```

#### **Public Member Functions**

• std::size\_t operator() (const carl::MultivariateRoot< Pol > &mv) const

#### 12.131.1 Member Function Documentation

# 12.132 std::hash< carl::PolynomialFactorizationPair< P > > Struct Template Reference

#include <PolynomialFactorizationPair.h>

#### **Public Member Functions**

size\_t operator() (const carl::PolynomialFactorizationPair< P > &\_pfp) const

#### 12.132.1 Member Function Documentation

# 12.133 std::hash< carl::RationalFunction< Pol, AS >> Struct Template Reference

```
#include <RationalFunction.h>
```

#### **Public Member Functions**

• std::size\_t operator() (const carl::RationalFunction< Pol, AS > &r) const

#### 12.133.1 Member Function Documentation

```
12.133.1.1 operator()() template<typename Pol , bool AS> std::size_t std::hash< carl::RationalFunction</td>
    Pol, AS > >::operator() ( const carl::RationalFunction
    Pol, AS > & r ) const [inline]
```

# 12.134 std::hash< carl::RealAlgebraicNumberThom< Number>> Struct Template Reference

#include <ran\_thom.h>

#### **Public Member Functions**

• std::size\_t operator() (const carl::RealAlgebraicNumberThom< Number > &n) const

#### 12.134.1 Member Function Documentation

## 12.135 std::hash< carl::Relation > Struct Reference

#include <Relation.h>

#### **Public Member Functions**

std::size\_t operator() (const carl::Relation &rel) const

#### 12.135.1 Member Function Documentation

### 12.136 std::hash < carl::Sort > Struct Reference

Implements std::hash for sort.

#include <Sort.h>

#### **Public Member Functions**

std::size\_t operator() (const carl::Sort &\_sort) const

## 12.136.1 Detailed Description

Implements std::hash for sort.

## 12.136.2 Member Function Documentation

#### **Parameters**

| ₋sort | The sort to get the hash for. |
|-------|-------------------------------|
|-------|-------------------------------|

## Returns

The hash of the given sort.

## 12.137 std::hash < carl::SortValue > Struct Reference

Implements std::hash for sort value.

```
#include <SortValue.h>
```

#### **Public Member Functions**

• std::size\_t operator() (const carl::SortValue &sv) const

## 12.137.1 Detailed Description

Implements std::hash for sort value.

## 12.137.2 Member Function Documentation

## **Parameters**

sv The sort value to get the hash for.

#### Returns

The hash of the given sort value.

# 12.138 std::hash< carl::SqrtEx< Poly >> Struct Template Reference

Implements std::hash for square root expressions.

```
#include <SqrtEx.h>
```

## **Public Member Functions**

std::size\_t operator() (const carl::SqrtEx< Poly > &\_sqrtEx) const

## 12.138.1 Detailed Description

```
template<typename Poly> struct std::hash< carl::SqrtEx< Poly > >
```

Implements std::hash for square root expressions.

#### 12.138.2 Member Function Documentation

#### **Parameters**

| ₋sqrtE | r | The square root expression to get the hash for. |
|--------|---|---|
|--------|---|---|

#### Returns

The hash of the given square root expression.

## 12.139 std::hash< carl::Term< Coefficient > > Struct Template Reference

```
Specialization of std::hash for a Term.
```

```
#include <Term.h>
```

## **Public Member Functions**

 std::size\_t operator() (const carl::Term< Coefficient > &term) const Calculates the hash of a Term.

# 12.139.1 Detailed Description

```
template<typename Coefficient> struct std::hash< carl::Term< Coefficient > >
```

Specialization of std::hash for a Term.

#### 12.139.2 Member Function Documentation

Calculates the hash of a Term.

| ח∽ |    | <br>-4 | ۱. |  |
|----|----|--------|----|--|
|    | ra | ല      |    |  |
|    |    |        |    |  |

#### Returns

Hash of term.

# 12.140 std::hash< carl::TypeInfoPair< T, I >> Struct Template Reference

```
#include <Cache.h>
```

#### **Public Member Functions**

• std::size\_t operator() (const carl::TypeInfoPair< T, I > &\_tip) const

#### 12.140.1 Member Function Documentation

# 12.141 std::hash< carl::UEquality > Struct Reference

Implements std::hash for uninterpreted equalities.

```
#include <UEquality.h>
```

# **Public Member Functions**

• std::size\_t operator() (const carl::UEquality &ueq) const

#### 12.141.1 Detailed Description

Implements std::hash for uninterpreted equalities.

# 12.141.2 Member Function Documentation

#### **Parameters**

ueq The uninterpreted equality to get the hash for.

#### Returns

The hash of the given uninterpreted equality.

## 12.142 std::hash< carl::UFContent > Struct Reference

Implements std::hash for uninterpreted function's contents.

```
#include <UFManager.h>
```

#### **Public Member Functions**

• std::size\_t operator() (const carl::UFContent &ufun) const

#### 12.142.1 Detailed Description

Implements std::hash for uninterpreted function's contents.

## 12.142.2 Member Function Documentation

#### **Parameters**

*ufun* The uninterpreted function to get the hash for.

#### Returns

The hash of the given uninterpreted function.

### 12.143 std::hash< carl::UFInstance > Struct Reference

Implements std::hash for uninterpreted function instances.

```
#include <UFInstance.h>
```

## **Public Member Functions**

std::size\_t operator() (const carl::UFInstance &ufi) const

## 12.143.1 Detailed Description

Implements std::hash for uninterpreted function instances.

#### 12.143.2 Member Function Documentation

#### **Parameters**

*ufi* The uninterpreted function instance to get the hash for.

## Returns

The hash of the given uninterpreted function instance.

## 12.144 std::hash< carl::UFInstanceContent > Struct Reference

Implements std::hash for uninterpreted function instance's contents.

```
#include <UFInstanceManager.h>
```

## **Public Member Functions**

• std::size\_t operator() (const carl::UFInstanceContent &ufun) const

## 12.144.1 Detailed Description

Implements std::hash for uninterpreted function instance's contents.

### 12.144.2 Member Function Documentation

## **Parameters**

*ufun* The uninterpreted function to get the hash for.

Returns

The hash of the given uninterpreted function.

## 12.145 std::hash < carl::UFModel > Struct Reference

Implements std::hash for uninterpreted function model.

```
#include <UFModel.h>
```

#### **Public Member Functions**

• std::size\_t operator() (const carl::UFModel &ufm) const

## 12.145.1 Detailed Description

Implements std::hash for uninterpreted function model.

#### 12.145.2 Member Function Documentation

# Parameters

*ufm* The uninterpreted function model to get the hash for.

Returns

The hash of the given uninterpreted function model.

# 12.146 std::hash< carl::UninterpretedFunction > Struct Reference

Implements std::hash for uninterpreted functions.

```
#include <UninterpretedFunction.h>
```

#### **Public Member Functions**

• std::size\_t operator() (const carl::UninterpretedFunction &uf) const

## 12.146.1 Detailed Description

Implements std::hash for uninterpreted functions.

#### 12.146.2 Member Function Documentation

#### **Parameters**

*uf* The uninterpreted function to get the hash for.

#### Returns

The hash of the given uninterpreted function.

# 12.147 std::hash< carl::UnivariatePolynomial< Coefficient > > Struct Template Reference

Specialization of std::hash for univariate polynomials.

```
#include <UnivariatePolynomial.h>
```

## **Public Member Functions**

std::size\_t operator() (const carl::UnivariatePolynomial < Coefficient > &p) const
 Calculates the hash of univariate polynomial.

## 12.147.1 Detailed Description

```
template<typename Coefficient> struct std::hash< carl::UnivariatePolynomial< Coefficient > >
```

Specialization of std::hash for univariate polynomials.

## 12.147.2 Member Function Documentation

Calculates the hash of univariate polynomial.

#### **Parameters**

p UnivariatePolynomial.

#### Returns

Hash of p.

#### 12.148 std::hash< carl::UTerm > Struct Reference

Implements std::hash for uninterpreted terms.

```
#include <UTerm.h>
```

#### **Public Member Functions**

• std::size\_t operator() (const carl::UTerm &ut) const

#### 12.148.1 Detailed Description

Implements std::hash for uninterpreted terms.

### 12.148.2 Member Function Documentation

#### **Parameters**

ut The uninterpreted term to get the hash for.

#### Returns

The hash of the given uninterpreted term.

#### 12.149 std::hash< carl::UVariable > Struct Reference

Implements std::hash for uninterpreted variables.

```
#include <UVariable.h>
```

### **Public Member Functions**

std::size\_t operator() (carl::UVariable uvar) const

## 12.149.1 Detailed Description

Implements std::hash for uninterpreted variables.

#### 12.149.2 Member Function Documentation

#### **Parameters**

uvar The uninterpreted variable to get the hash for.

## Returns

The hash of the given uninterpreted variable.

## 12.150 std::hash< carl::Variable > Struct Reference

Specialization of std::hash for Variable.

```
#include <Variable.h>
```

## **Public Member Functions**

• std::size\_t operator() (const carl::Variable variable) const noexcept Calculates the hash of a Variable.

## 12.150.1 Detailed Description

Specialization of std::hash for Variable.

#### 12.150.2 Member Function Documentation

Calculates the hash of a Variable.

#### **Parameters**

#### Returns

Hash of variable

## 12.151 std::hash< carl::VariableAssignment< Pol > > Struct Template Reference

```
#include <VariableAssignment.h>
```

#### **Public Member Functions**

• std::size\_t operator() (const carl::VariableAssignment< Pol > &va) const

#### 12.151.1 Member Function Documentation

## 12.152 std::hash< carl::VariableComparison< Pol > > Struct Template Reference

```
#include <VariableComparison.h>
```

#### **Public Member Functions**

-  $std::size\_t operator() (const carl::VariableComparison < Pol > &vc) const$ 

#### 12.152.1 Member Function Documentation

## 12.153 std::hash< carl::vs::Term< Poly >> Struct Template Reference

```
#include <term.h>
```

## **Public Member Functions**

size\_t operator() (const carl::vs::Term< Poly > &term) const

#### 12.153.1 Member Function Documentation

## 12.154 std::hash< cln::cl\_l > Struct Reference

```
#include <hash.h>
```

#### **Public Member Functions**

• std::size\_t operator() (const cln::cl\_l &n) const

### 12.154.1 Member Function Documentation

```
12.154.1.1 operator()() std::size_t std::hash< cln::cl_I >::operator() ( const cln::cl_I & n ) const [inline]
```

# 12.155 std::hash< cln::cl\_RA > Struct Reference

```
#include <hash.h>
```

## **Public Member Functions**

• std::size\_t operator() (const cln::cl\_RA &n) const

## 12.155.1 Member Function Documentation

## 12.156 std::hash< mpq\_class > Struct Reference

```
#include <hash.h>
```

#### **Public Member Functions**

std::size\_t operator() (const mpq\_class &q) const

#### 12.156.1 Member Function Documentation

```
12.156.1.1 operator()() std::size_t std::hash< mpq_class >::operator() ( const mpq_class & q ) const [inline]
```

## 12.157 std::hash< mpz\_class > Struct Reference

```
#include <hash.h>
```

#### **Public Member Functions**

• std::size\_t operator() (const mpz\_class &z) const

#### 12.157.1 Member Function Documentation

```
12.157.1.1 operator()() std::size_t std::hash< mpz_class >::operator() ( const mpz_class & z ) const [inline]
```

## 12.158 carl::hash< std::shared\_ptr< T >, mayBeNull > Struct Template Reference

```
#include <pointerOperations.h>
```

#### **Public Member Functions**

std::size\_t operator() (const std::shared\_ptr< T > &t) const

## 12.158.1 Member Function Documentation

# 12.159 std::hash< std::vector< carl::BasicConstraint< Pol >>> Struct Template Reference

Implements std::hash for vectors of constraints.

```
#include <BasicConstraint.h>
```

# **Public Member Functions**

• std::size\_t operator() (const std::vector< carl::BasicConstraint< Pol >> &arg) const

#### 12.159.1 Detailed Description

```
\label{lem:lemplate} \begin{tabular}{ll} template < typename Pol > \\ struct std::hash < std::vector < carl::BasicConstraint < Pol > > \\ \end{tabular}
```

Implements std::hash for vectors of constraints.

#### 12.159.2 Member Function Documentation

#### **Parameters**

\_arg The vector of constraints to get the hash for.

## Returns

The hash of the given vector of constraints.

# 12.160 std::hash< std::vector< carl::Constraint< Pol >>> Struct Template Reference

Implements std::hash for vectors of constraints.

```
#include <Constraint.h>
```

#### **Public Member Functions**

• std::size\_t operator() (const std::vector< carl::Constraint< Pol >> &arg) const

#### 12.160.1 Detailed Description

```
template<typename Pol> struct std::hash< std::vector< carl::Constraint< Pol>>>
```

Implements std::hash for vectors of constraints.

#### 12.160.2 Member Function Documentation

#### **Parameters**

arg | The vector of constraints to get the hash for.

#### Returns

The hash of the given vector of constraints.

## 12.161 std::hash< std::vector< T > > Struct Template Reference

```
#include <hash_util.h>
```

# **Public Member Functions**

std::size\_t operator() (const std::vector< T > &v) const

#### 12.161.1 Member Function Documentation

```
12.161.1.1 operator()() template<typename T > std::size_t std::hash< std::vector< T > >::operator() ( const std::vector< T > & v ) const [inline]
```

# 12.162 carl::hash< T \*, mayBeNull > Struct Template Reference

```
#include <pointerOperations.h>
```

## **Public Member Functions**

std::size\_t operator() (const T \*t) const

#### 12.162.1 Member Function Documentation

## 12.163 carl::hash\_inserter< T > Struct Template Reference

Utility functor to hash a sequence of object using an output iterator.

```
#include <hash.h>
```

## **Public Types**

- using difference\_type = void
- using pointer = void
- using reference = void
- using value\_type = void
- using iterator\_category = std::output\_iterator\_tag

## **Public Member Functions**

- hash\_inserter & operator= (const T &t)
- hash\_inserter & operator\* ()
- hash\_inserter & operator++ ()
- const hash\_inserter operator++ (int)

#### **Data Fields**

· std::size\_t & seed

## 12.163.1 Detailed Description

```
template < typename T> struct carl::hash_inserter < T >
```

Utility functor to hash a sequence of object using an output iterator.

## 12.163.2 Member Typedef Documentation

```
12.163.2.1 difference_type template<typename T >
using carl::hash_inserter< T >::difference_type = void
\textbf{12.163.2.2} \quad \textbf{iterator\_category} \quad \texttt{template} < \texttt{typename} \ \texttt{T} \ > \\
using carl::hash_inserter< T >::iterator_category = std::output_iterator_tag
12.163.2.3 pointer template<typename T >
using carl::hash_inserter< T >::pointer = void
12.163.2.4 reference template<typename T >
using carl::hash_inserter< T >::reference = void
12.163.2.5 value_type template<typename T >
using carl::hash_inserter< T >::value_type = void
12.163.3 Member Function Documentation
12.163.3.1 operator*() template<typename T >
hash_inserter& carl::hash_inserter< T >::operator* ( ) [inline]
12.163.3.2 operator++() [1/2] template<typename T >
hash\_inserter \& carl::hash\_inserter < T >::operator ++ \ ( ) \quad [inline]
12.163.3.3 operator++() [2/2] template<typename T >
const hash_inserter carl::hash_inserter< T >::operator++ (
             int ) [inline]
```

#### 12.163.4 Field Documentation

```
12.163.4.1 seed template<typename T >
std::size_t& carl::hash_inserter< T >::seed
```

# 12.164 carl::hashEqual Struct Reference

```
#include <Monomial.h>
```

#### **Public Member Functions**

- bool operator() (const Monomial &lhs, const Monomial &rhs) const
- · bool operator() (const Monomial::Arg &lhs, const Monomial::Arg &rhs) const

## 12.164.1 Member Function Documentation

 $\verb|const Monomial::Arg \& rhs|| ) | | const [inline]|$ 

## 12.165 carl::hashLess Struct Reference

```
#include <Monomial.h>
```

## **Public Member Functions**

- bool operator() (const Monomial &lhs, const Monomial &rhs) const
- bool operator() (const Monomial::Arg &lhs, const Monomial::Arg &rhs) const

#### 12.165.1 Member Function Documentation

# 12.166 carl::Heap< C > Class Template Reference

A heap priority queue.

```
#include <Heap.h>
```

#### **Data Structures**

· class c\_iterator

## **Public Types**

- using Configuration = C
- using Entry = typename Configuration::Entry
- using const\_iterator = c\_iterator

## **Public Member Functions**

- Heap (const Configuration &configuration)
- Configuration & getConfiguration ()
- const Configuration & getConfiguration () const
- std::string get\_name () const
- void push (Entry entry)
- void push (const Entry \*begin, const Entry \*end)
- Entry pop ()
- Entry top () const
- · bool empty () const
- size\_t size () const
- c\_iterator begin () const
- c\_iterator end () const
- std::vector< Entry > getCopy () const
- void print (std::ostream &out=std::cout) const
- void decreaseTop (Entry newEntry)
- void decreasePos (Entry newEntry, c\_iterator pos)
- void popPosition (c\_iterator pos)
- size\_t getMemoryUse () const

### 12.166.1 Detailed Description

```
template < class C > class carl::Heap < C >
```

A heap priority queue.

Configuration serves the same role as for Geobucket. It must have these fields that work as for Geobucket.

A type Entry A type CompareResult A const or static method: CompareResult compare(Entry, Entry) A const or static method: bool cmpLessThan(CompareResult) A static const bool supportDeduplication A static or const method: bool cmpEqual(CompareResult) A static or const method: Entry deduplicate(Entry a, Entry b)

It also has these additional fields:

A static const bool fastIndex If this field is true, then a faster way of calculating indexes is used. This requires sizeof(Entry) to be a power of two! This can be achieved by adding padding to Entry, but this class does not do that for you.

## 12.166.2 Member Typedef Documentation

```
12.166.2.1 Configuration template<class C > using carl::Heap< C >::Configuration = C
```

```
12.166.2.2 const_iterator template<class C >
using carl::Heap< C >::const_iterator = c_iterator
```

```
12.166.2.3 Entry template<class C > using carl::Heap< C >::Entry = typename Configuration::Entry
```

## 12.166.3 Constructor & Destructor Documentation

#### 12.166.4 Member Function Documentation

```
12.166.4.1 begin() template<class C >
c_iterator carl::Heap< C >::begin ( ) const [inline]
12.166.4.2 decreasePos() template<class C >
void carl::Heap< C >::decreasePos (
            Entry newEntry,
            c_iterator pos )
12.166.4.3 decreaseTop() template<class C >
void carl::Heap< C >::decreaseTop (
            Entry newEntry )
12.166.4.4 empty() template<class C >
bool carl::Heap< C >::empty ( ) const [inline]
12.166.4.5 end() template<class C >
c_iterator carl::Heap< C >::end ( ) const [inline]
12.166.4.6 get_name() template<class C >
std::string carl::Heap< C >::get_name
12.166.4.7 getConfiguration() [1/2] template<class C >
Configuration& carl::Heap< C >::getConfiguration ( ) [inline]
12.166.4.8 getConfiguration() [2/2] template<class C >
const Configuration& carl::Heap< C >::getConfiguration ( ) const [inline]
12.166.4.9 getCopy() template<class C >
std::vector<Entry> carl::Heap< C >::getCopy ( ) const [inline]
```

```
12.166.4.10 getMemoryUse() template<class C >
size_t carl::Heap< C >::getMemoryUse
12.166.4.11 pop() template<class C >
Heap< C >::Entry carl::Heap< C >::pop
12.166.4.12 popPosition() template<class C >
void carl::Heap< C >::popPosition (
            c_iterator pos ) [inline]
12.166.4.13 print() template<class C >
void carl::Heap< C >::print (
            std::ostream & out = std::cout ) const
12.166.4.14 push() [1/2] template<class C >
void carl::Heap< C >::push (
            const Entry * begin,
            const Entry * end )
12.166.4.15 push() [2/2] template<class C >
void carl::Heap< C >::push (
            Entry entry )
12.166.4.16 size() template<class C >
size_t carl::Heap< C >::size ( ) const [inline]
12.166.4.17 top() template<class C >
Entry carl::Heap< C >::top ( ) const [inline]
12.167 carl::Ideal< Polynomial, Datastructure, CacheSize > Class Template Reference
#include <Ideal.h>
```

#### **Public Member Functions**

- Ideal ()=default
- · Ideal (const Polynomial &p1, const Polynomial &p2)
- virtual ∼ldeal ()=default
- Ideal (const Ideal &rhs)
- Ideal & operator= (const Ideal &rhs)
- size\_t addGenerator (const Polynomial &f)
- DivisionLookupResult< Polynomial > getDivisor (const Term< typename Polynomial::CoeffType > &t) const
- bool isDividable (const Term< typename Polynomial::CoeffType > &m)
- size\_t nrGenerators () const
- std::vector< Polynomial > & getGenerators ()
- const std::vector< Polynomial > & getGenerators () const
- const Polynomial & getGenerator (size\_t index) const
- std::vector< size\_t > getOrderedIndices ()
- void eliminateGenerator (size\_t index)
- void removeEliminated ()

Invalidates indices.

- void clear ()
- bool is\_constant () const
- bool is\_linear () const

Checks whether all polynomials occurring in this ideal are linear.

std::set< unsigned > gatherVariables () const

Gather all variables occurring in this ideal.

void print (bool printOrigins=true, std::ostream &os=std::cout) const

## Friends

std::ostream & operator<< (std::ostream &os, const Ideal &rhs)</li>

const Polynomial & p2 ) [inline]

#### 12.167.1 Constructor & Destructor Documentation

```
12.167.1.3 ~ | class Datastructure = Ideal ←
DatastructureVector, int CacheSize = 0>
virtual carl::Ideal< Polynomial, Datastructure, CacheSize >::~Ideal () [virtual], [default]
12.167.1.4 | Ideal()[3/3] template<class Polynomial , template< class > class Datastructure =
IdealDatastructureVector, int CacheSize = 0>
carl::Ideal < Polynomial, Datastructure, CacheSize >::Ideal (
            const Ideal< Polynomial, Datastructure, CacheSize > & rhs ) [inline]
12.167.2 Member Function Documentation
12.167.2.1 addGenerator() template<class Polynomial , template< class > class Datastructure =
IdealDatastructureVector, int CacheSize = 0>
size_t carl::Ideal< Polynomial, Datastructure, CacheSize >::addGenerator (
            const Polynomial & f ) [inline]
12.167.2.2 clear() template<class Polynomial , template< class > class Datastructure = Ideal \leftarrow
DatastructureVector, int CacheSize = 0>
void carl::Ideal< Polynomial, Datastructure, CacheSize >::clear ( ) [inline]
12.167.2.3 eliminateGenerator() template<class Polynomial , template< class > class Datastructure
= IdealDatastructureVector, int CacheSize = 0>
\verb|void carl::Ideal| < \verb|Polynomial|, \verb|Datastructure|, \verb|CacheSize| > :: eliminateGenerator| (
            size_t index ) [inline]
12.167.2.4 gatherVariables() template<class Polynomial , template< class > class Datastructure
= IdealDatastructureVector, int CacheSize = 0>
std::set<unsigned> carl::Ideal< Polynomial, Datastructure, CacheSize >::gatherVariables ( )
const [inline]
Gather all variables occurring in this ideal.
```

Returns

```
12.167.2.5 getDivisor() template<class Polynomial , template< class > class Datastructure =
IdealDatastructureVector, int CacheSize = 0>
{\tt DivisionLookupResult} < {\tt Polynomial} > {\tt carl::Ideal} < {\tt Polynomial}, \ {\tt Datastructure}, \ {\tt CacheSize} > :: {\tt get} \leftarrow {\tt CacheSize} > :: {\tt CacheSize} 
Divisor (
                           const Term< typename Polynomial::CoeffType > \& t ) const [inline]
12.167.2.6 getGenerator() template < class Polynomial , template < class > class Datastructure =
IdealDatastructureVector, int CacheSize = 0>
const Polynomial& carl::Ideal< Polynomial, Datastructure, CacheSize >::getGenerator (
                           size_t index ) const [inline]
12.167.2.7 getGenerators() [1/2] template<class Polynomial , template< class > class Datastructure
= IdealDatastructureVector, int CacheSize = 0>
std::vector<Polynomial>& carl::Ideal< Polynomial, Datastructure, CacheSize >::getGenerators (
) [inline]
12.167.2.8 getGenerators() [2/2] template<class Polynomial , template< class > class Datastructure
= IdealDatastructureVector, int CacheSize = 0>
Generators ( ) const [inline]
12.167.2.9 getOrderedIndices() template<class Polynomial , template< class > class Datastructure
= IdealDatastructureVector, int CacheSize = 0>
std::vector<size_t> carl::Ideal< Polynomial, Datastructure, CacheSize >::getOrderedIndices (
) [inline]
12.167.2.10 is_constant() template<class Polynomial , template< class > class Datastructure =
IdealDatastructureVector, int CacheSize = 0>
bool carl::Ideal< Polynomial, Datastructure, CacheSize >::is_constant ( ) const [inline]
12.167.2.11 is_linear() template<class Polynomial , template< class > class Datastructure =
IdealDatastructureVector, int CacheSize = 0>
bool carl::Ideal< Polynomial, Datastructure, CacheSize >::is_linear ( ) const [inline]
Checks whether all polynomials occurring in this ideal are linear.
```

Returns

```
12.167.2.12 isDividable() template<class Polynomial , template< class > class Datastructure =
IdealDatastructureVector, int CacheSize = 0>
\verb|bool carl::Ideal<| \verb|Polynomial|, \verb|Datastructure|, \verb|CacheSize| >:: is \verb|Dividable| | |
             const Term< typename Polynomial::CoeffType > & m ) [inline]
12.167.2.13 nrGenerators() template<class Polynomial , template< class > class Datastructure =
IdealDatastructureVector, int CacheSize = 0>
size_t carl::Ideal< Polynomial, Datastructure, CacheSize >::nrGenerators ( ) const [inline]
12.167.2.14 operator=() template<class Polynomial , template< class > class Datastructure =
IdealDatastructureVector, int CacheSize = 0>
Ideal& carl::Ideal< Polynomial, Datastructure, CacheSize >::operator= (
              const Ideal< Polynomial, Datastructure, CacheSize > & rhs ) [inline]
\textbf{12.167.2.15} \quad \textbf{print()} \quad \texttt{template} < \texttt{class Polynomial , template} < \texttt{class > class Datastructure} = \texttt{Ideal} \leftarrow
DatastructureVector, int CacheSize = 0>
void carl::Ideal< Polynomial, Datastructure, CacheSize >::print (
             bool printOrigins = true,
              std::ostream & os = std::cout ) const [inline]
12.167.2.16 removeEliminated() template<class Polynomial , template< class > class Datastructure
= IdealDatastructureVector, int CacheSize = 0>
void carl::Ideal< Polynomial, Datastructure, CacheSize >::removeEliminated ( ) [inline]
Invalidates indices.
Returns
     a vector with the new indices
12.167.3 Friends And Related Function Documentation
```

## 12.168 carl::IdealDatastructureVector< Polynomial > Class Template Reference

```
#include <IdealDSVector.h>
```

#### **Public Member Functions**

- IdealDatastructureVector (const std::vector< Polynomial > &generators, const std::unordered\_set< size\_t > &eliminated, const sortByLeadingTerm< Polynomial > &order)
- IdealDatastructureVector (const IdealDatastructureVector &id)
- virtual ∼IdealDatastructureVector ()=default
- void addGenerator (size\_t fIndex) const

Should be called whenever an generator is added.

- $\bullet \ \, \text{DivisionLookupResult} < \ \, \text{Polynomial} > \text{getDivisor} \, (\text{const Term} < \text{typename Polynomial} :: CoeffType} > \&t) \, \text{const} \,$
- · void reset ()

Should be called if the generator set is reset.

#### 12.168.1 Constructor & Destructor Documentation

```
12.168.1.2 | IdealDatastructureVector() [2/2] | template<class Polynomial > carl::IdealDatastructureVector</br>
Polynomial >::IdealDatastructureVector
const IdealDatastructureVector
Polynomial > & id ) [inline]
```

```
12.168.1.3 ~IdealDatastructureVector() template<class Polynomial > virtual carl::IdealDatastructureVector< Polynomial >::~IdealDatastructureVector ( ) [virtual], [default]
```

#### 12.168.2 Member Function Documentation

Should be called whenever an generator is added.

| Do |    |   |    |     |    |
|----|----|---|----|-----|----|
| Pа | ra | m | eı | re. | rs |

fIndex

## **Parameters**



#### Returns

A divisionresult [divisor, factor].

Todo delete divres?

```
12.168.2.3 reset() template < class Polynomial >
void carl::IdealDatastructureVector < Polynomial >::reset ( ) [inline]
```

Should be called if the generator set is reset.

# 12.169 carl::IDPool Class Reference

#include <IDPool.h>

## **Public Member Functions**

- std::size\_t size () const
- std::size\_t largestID () const
- std::size\_t get ()
- void free (std::size\_t id)
- void clear ()

### Friends

• std::ostream & operator<< (std::ostream &os, const IDPool &p)

#### 12.169.1 Member Function Documentation

```
12.169.1.1 clear() void carl::IDPool::clear ( ) [inline]
```

```
12.169.1.2 free() void carl::IDPool::free ( std::size.t id ) [inline]
```

```
12.169.1.3 get() std::size_t carl::IDPool::get ( ) [inline]
```

```
12.169.1.4 largestID() std::size_t carl::IDPool::largestID ( ) const [inline]
```

```
12.169.1.5 size() std::size_t carl::IDPool::size ( ) const [inline]
```

# 12.169.2 Friends And Related Function Documentation

# 12.170 carl::InfinityValue Struct Reference

This class represents infinity or minus infinity, depending on its flag positive.

```
#include <ModelValue.h>
```

## **Data Fields**

• bool positive = false

## 12.170.1 Detailed Description

This class represents infinity or minus infinity, depending on its flag positive.

The default is minus infinity.

#### 12.170.2 Field Documentation

```
12.170.2.1 positive bool carl::InfinityValue::positive = false
```

## 12.171 carl::Cache< T >::Info Struct Reference

```
#include <Cache.h>
```

## **Public Member Functions**

• Info (double \_activity)

#### **Data Fields**

• std::size\_t usageCount

Store the number of usages of the entry in the cache for which this information hold by external objects.

• std::vector< Ref > refStoragePositions

Stores the reference of the entry in the cache for which this information hold.

· double activity

Stores the activity of the entry in the cache for which this information hold.

#### 12.171.1 Constructor & Destructor Documentation

## 12.171.2 Field Documentation

```
12.171.2.1 activity template<typename T > double carl::Cache< T >::Info::activity
```

Stores the activity of the entry in the cache for which this information hold.

The activity states how often the entry is involved in computations in the recent past.

```
12.171.2.2 refStoragePositions template<typename T >
std::vector<Ref> carl::Cache< T >::Info::refStoragePositions
```

Stores the reference of the entry in the cache for which this information hold.

```
12.171.2.3 usageCount template<typename T >
std::size_t carl::Cache< T >::Info::usageCount
```

Store the number of usages of the entry in the cache for which this information hold by external objects.

## 12.172 carl::IntegerPairCompare < IntegerType > Struct Template Reference

```
#include <GaloisField.h>
```

#### **Public Member Functions**

bool operator() (const std::pair< IntegerType, IntegerType > &p1, const std::pair< IntegerType, IntegerType > &p2) const

### 12.172.1 Member Function Documentation

# 12.173 carl::parser::IntegerParser< T > Struct Template Reference

Parses (signed) integers.

```
#include <parser.h>
```

# 12.173.1 Detailed Description

```
template<typename T> struct carl::parser::IntegerParser< T>
```

Parses (signed) integers.

# 12.174 carl::IntegralType < RationalType > Struct Template Reference

Gives the corresponding integral type.

```
#include <typetraits.h>
```

## **Public Types**

```
• using type = sint
```

#### 12.174.1 Detailed Description

```
template<typename RationalType> struct carl::IntegralType< RationalType >
```

Gives the corresponding integral type.

Default is int.

## 12.174.2 Member Typedef Documentation

```
12.174.2.1 type template<typename RationalType >
using carl::IntegralType< RationalType >::type = sint
```

Todo Should any type have an integral type?

# 12.175 carl::IntegralType< carl::FLOAT\_T< F >> Struct Template Reference

```
#include <typetraits.h>
```

## **Public Types**

• using type = mpz\_class

# 12.175.1 Member Typedef Documentation

```
12.175.1.1 type template<typename F >
using carl::IntegralType< carl::FLOAT.T< F > >::type = mpz.class
```

# 12.176 carl::IntegralType< cln::cl\_I > Struct Reference

States that IntegralType of cln::cl\_l is cln::cl\_l .

```
#include <typetraits.h>
```

## **Public Types**

• using type = cln::cl\_l

A type associated with the type.

## 12.176.1 Detailed Description

States that IntegralType of  $cln::cl_I$  is  $cln::cl_I$ .

<>

## 12.176.2 Member Typedef Documentation

```
12.176.2.1 type using carl::has_subtype< cln::cl_I >::type = cln::cl_I [inherited]
```

A type associated with the type.

# 12.177 carl::IntegralType< cln::cl\_RA > Struct Reference

States that IntegralType of  $cln::cl_RA$  is  $cln::cl_I$ .

```
#include <typetraits.h>
```

# **Public Types**

using type = cln::cl\_l
 A type associated with the type.

# 12.177.1 Detailed Description

States that IntegralType of cln::cl\_RA is cln::cl\_I.

<>

## 12.177.2 Member Typedef Documentation

```
12.177.2.1 type using carl::has_subtype< cln::cl_I >::type = cln::cl_I [inherited]
```

A type associated with the type.

# 12.178 carl::IntegralType< double > Struct Reference

States that IntegralType of double is sint .

```
#include <typetraits.h>
```

## **Public Types**

• using type = sint

A type associated with the type.

#### 12.178.1 Detailed Description

States that IntegralType of double is sint .

<>

## 12.178.2 Member Typedef Documentation

```
12.178.2.1 type using carl::has_subtype< sint >::type = sint [inherited]
```

A type associated with the type.

# 12.179 carl::IntegralType< float > Struct Reference

States that IntegralType of float is sint .

```
#include <typetraits.h>
```

## **Public Types**

• using type = sint

A type associated with the type.

## 12.179.1 Detailed Description

States that IntegralType of float is sint .

<>

### 12.179.2 Member Typedef Documentation

```
12.179.2.1 type using carl::has.subtype< sint >::type = sint [inherited]
```

A type associated with the type.

## 12.180 carl::IntegralType< GFNumber< C > > Struct Template Reference

```
#include <typetraits.h>
```

## **Public Types**

• using type = C

## 12.180.1 Member Typedef Documentation

```
12.180.1.1 type template<typename C >
using carl::IntegralType< GFNumber< C > >::type = C
```

## 12.181 carl::IntegralType< long double > Struct Reference

States that IntegralType of long double is sint .

```
#include <typetraits.h>
```

# **Public Types**

• using type = sint

A type associated with the type.

## 12.181.1 Detailed Description

States that IntegralType of long double is sint .

<>

## 12.181.2 Member Typedef Documentation

```
12.181.2.1 type using carl::has_subtype< sint >::type = sint [inherited]
```

A type associated with the type.

# 12.182 carl::IntegralType< mpq\_class > Struct Reference

States that IntegralType of mpq\_class is mpz\_class.

```
#include <typetraits.h>
```

## **Public Types**

• using type = mpz\_class

A type associated with the type.

### 12.182.1 Detailed Description

States that IntegralType of mpq\_class is mpz\_class.

<>

## 12.182.2 Member Typedef Documentation

12.182.2.1 type using carl::has\_subtype< mpz\_class >::type = mpz\_class [inherited]

A type associated with the type.

# 12.183 carl::IntegralType< mpz\_class > Struct Reference

States that IntegralType of mpz\_class is mpz\_class .

```
#include <typetraits.h>
```

## **Public Types**

• using type = mpz\_class

A type associated with the type.

## 12.183.1 Detailed Description

States that IntegralType of mpz\_class is mpz\_class .

<>

### 12.183.2 Member Typedef Documentation

```
12.183.2.1 type using carl::has_subtype< mpz_class >::type = mpz_class [inherited]
```

A type associated with the type.

## 12.184 carl::Interval < Number > Class Template Reference

The class which contains the interval arithmetic including trigonometric functions.

```
#include <Interval.h>
```

#### **Public Types**

- using Policy = policies < Number, Interval < Number > >
- using BoostIntervalPolicies = boost::numeric::interval\_lib::policies < typename Policy::roundingP, typename Policy::checkingP >
- using BoostInterval = boost::numeric::interval < Number, BoostIntervalPolicies >
- using evalintervalmap = std::map< Variable, Interval< Number > >
- using roundingP = carl::rounding< Number >
- using checkingP = carl::checking< Number >

#### **Public Member Functions**

Interval ()

Default constructor which constructs the empty interval at point 0.

• Interval (const Number &n)

Constructor which constructs the pointinterval at n.

Interval (const Number &lower, const Number &upper)

Constructor which constructs the weak-bounded interval between lower and upper.

Interval (const BoostInterval &content, BoundType lowerBoundType=BoundType::WEAK, BoundType upperBoundType=BoundType::WEAK)

Constructor which constructs the interval according to the passed boost interval with the passed bound types.

Interval (const Number &lower, BoundType lowerBoundType, const Number &upper, BoundType upper
 — BoundType)

Constructor which constructs the interval according to the passed bounds with the passed bound types.

Interval (const Interval < Number > &o)

Copy constructor.

- template<typename Other , Disablelf< std::is\_same< Number, Other >> = dummy>
   Interval (const Interval< Other > &o)
- template<typename N = Number, DisableIf< std::is\_same< N, double >> = dummy, DisableIf< is\_rational\_type< N >> = dummy> Interval (const double &n)

Constructor which constructs a pointinterval from a passed double.

template<typename N = Number, DisableIf< std::is\_same< N, double >> = dummy, DisableIf< is\_rational\_type< N >> = dummy>
 Interval (double lower, double upper)

Constructor which constructs an interval from the passed double bounds.

template < typename N = Number, Disablelf < std::is\_same < N, double >> = dummy, Disablelf < is\_rational\_type < N >> = dummy > Interval (double lower, BoundType lowerBoundType, double upper, BoundType upperBoundType)

Constructor which constructs the interval according to the passed double bounds with the passed bound types.

template<typename N = Number, DisableIf< std::is\_same< N, int >> = dummy>
 Interval (const int &n)

Constructor which constructs a pointinterval from a passed int.

template<typename N = Number, Disablelf< std::is\_same< N, int >> = dummy>
 Interval (int lower, int upper)

Constructor which constructs an interval from the passed int bounds.

template<typename N = Number, Disablelf< std::is\_same< N, int >> = dummy>
 Interval (int lower, BoundType lowerBoundType, int upper, BoundType upperBoundType)

Constructor which constructs the interval according to the passed int bounds with the passed bound types.

template<typename N = Number, Disablelf< std::is\_same< N, unsigned int >> = dummy>
 Interval (const unsigned int &n)

Constructor which constructs a pointinterval from a passed unsigned int.

template < typename N = Number, DisableIf < std::is\_same < N, unsigned int >> = dummy > Interval (unsigned int lower, unsigned int upper)

Constructor which constructs an interval from the passed unsigned int bounds.

template < typename N = Number, Disablelf < std::is\_same < N, unsigned int >> = dummy >
 Interval (unsigned int lower, BoundType lowerBoundType, unsigned int upper, BoundType upperBoundType)

Constructor which constructs the interval according to the passed unsigned int bounds with the passed bound types.

template<typename Num = Number, typename Rational , EnableIf< std::is\_floating\_point< Num >> = dummy, DisableIf< std::is\_</li>
 same< Num, Rational >> = dummy>
 Interval (Rational n)

Constructor which constructs a pointinterval from a passed general rational number.

template<typename Num = Number, typename Rational , EnableIf< std::is\_floating\_point< Num >> = dummy, DisableIf< std::is\_←
 same< Num, Rational >> = dummy>
 Interval (Rational lower, Rational upper)

Constructor which constructs an interval from the passed general rational bounds.

• template<typename Num = Number, typename Rational , EnableIf< std::is\_floating\_point< Num >> = dummy, DisableIf< std::is\_\leftarrow same< Num, Rational >> = dummy>

Interval (Rational lower, BoundType lowerBoundType, Rational upper, BoundType upperBoundType)

Constructor which constructs the interval according to the passed general rational bounds with the passed bound types

template<typename Num = Number, typename Float , EnableIf < is\_rational\_type < Num >> = dummy, EnableIf < std::is\_floating\_←
point < Float >> = dummy, DisableIf < std::is\_same < Num, Float >> = dummy>
Interval (Float n)

Constructor which constructs a pointinterval from a passed general float number (e.g.

template<typename Num = Number, typename Float , Enablelf< is\_rational\_type< Num >> = dummy, Enablelf< std::is\_floating\_

 point< Float >> = dummy, Disablelf< std::is\_same< Num, Float >> = dummy>
 Interval (Float lower, Float upper)

Constructor which constructs an interval from the passed general float bounds (e.g.

template<typename Num = Number, typename Float, Enablelf< is\_rational\_type< Num >> = dummy, Enablelf< std::is\_floating\_←
point< Float >> = dummy, Disablelf< std::is\_same< Num, Float >> = dummy, Disablelf< std::is\_floating\_point< Num >> = dummy>
Interval (Float lower, BoundType lowerBoundType, Float upper, BoundType upperBoundType)

Constructor which constructs the interval according to the passed general float bounds (e.g.

template<typename Num = Number, typename Rational , Enablelf< is\_rational\_type< Num >> = dummy, Enablelf< is\_rational\_type<</li>
 Rational >> = dummy, Disablelf< std::is\_same< Num, Rational >> = dummy>
 Interval (Rational n)

Constructor which constructs a pointinterval from a passed general float number (e.g.

template<typename Num = Number, typename Rational , Enablelf< is\_rational\_type< Num >> = dummy, Enablelf< is\_rational\_type<</li>
 Rational >> = dummy, Disablelf< std::is\_same< Num, Rational >> = dummy>
 Interval (Rational lower, Rational upper)

Constructor which constructs an interval from the passed general float bounds (e.g.

• template<typename Num = Number, typename Rational , EnableIf< is\_rational\_type< Num >> = dummy, EnableIf< is\_rational\_type<
Rational >> = dummy, DisableIf< std::is\_same< Num, Rational >> = dummy>

Interval (Rational lower, BoundType lowerBoundType, Rational upper, BoundType upperBoundType)

- Constructor which constructs the interval according to the passed general float bounds (e.g. 
   Interval (const LowerBound< Number > &lb, const UpperBound< Number > &ub)
- Interval (const LowerBound < Number > &lb, const LowerBound < Number > &ub)
- Interval (const UpperBound < Number > &lb, const UpperBound < Number > &ub)
- ∼Interval ()=default

Destructor.

· const Number & lower () const

The getter for the lower boundary of the interval.

· const Number & upper () const

The getter for the upper boundary of the interval.

- auto lower\_bound () const
- auto upper\_bound () const
- · const BoostInterval & content () const

Returns a reference to the included boost interval.

• BoostInterval & content ()

Returns a reference to the included boost interval.

BoundType lower\_bound\_type () const

The getter for the lower bound type of the interval.

BoundType upper\_bound\_type () const

The getter for the upper bound type of the interval.

void set\_lower (const Number &n)

The setter for the lower boundary of the interval.

• void set\_upper (const Number &n)

The setter for the upper boundary of the interval.

void set\_lower\_bound (const Number &n, BoundType b)

The setter for the lower boundary of the interval.

void set\_upper\_bound (const Number &n, BoundType b)

The setter for the upper boundary of the interval.

void set\_lower\_bound\_type (BoundType b)

The setter for the lower bound type of the interval.

void set\_upper\_bound\_type (BoundType b)

The setter for the upper bound type of the interval.

Interval < Number > & operator= (const Interval < Number > &rhs)

The assignment operator.

· void set (const BoostInterval &content)

Advanced setter to modify both boundaries at once.

void set (const Number &lower, const Number &upper)

Advanced setter to modify both boundaries at once by passing a boost interval.

bool is\_infinite () const

Function which determines, if the interval is (-oo,oo).

• bool is\_unbounded () const

Function which determines, if the interval is unbounded.

• bool is\_half\_bounded () const

Function which determines, if the interval is half-bounded.

bool is\_empty () const

Function which determines, if the interval is empty.

• bool is\_point\_interval () const

Function which determines, if the interval is a pointinterval.

• bool is\_open\_interval () const

Function which determines, if the interval is open.

bool is\_closed\_interval () const

Function which determines, if the interval is closed.

bool is\_zero () const

Function which determines, if the interval is the zero interval.

bool is\_one () const

Function which determines, if the interval is the one interval.

- bool is\_positive () const
- bool is\_negative () const
- bool is\_semi\_positive () const
- bool is\_semi\_negative () const
- Sign sgn () const

Determine whether the interval lays entirely left of 0 (NEGATIVE\_SIGN), right of 0 (POSITIVE\_SIGN) or contains 0 (ZERO\_SIGN).

• Interval < Number > integral\_part () const

Computes the integral part of the given interval.

void integralPart\_assign ()

Computes and assigns the integral part of the given interval.

bool contains\_integer () const

Checks if the interval contains at least one integer value.

• Number diameter () const

Returns the diameter of the interval.

void diameter\_assign ()

Computes and assigns the diameter of the interval.

• Number diameter\_ratio (const Interval < Number > &rhs) const

Returns the ratio of the diameters of the given intervals.

void diameter\_ratio\_assign (const Interval < Number > &rhs)

Computes and assigns the ratio of the diameters of the given intervals.

• Number magnitude () const

Returns the magnitude of the interval.

void magnitude\_assign ()

Computes and assigns the magnitude of the interval.

void center\_assign ()

Computes and assigns the center point of the interval.

· bool contains (const Number &val) const

Checks if the interval contains the given value.

template < typename Num = Number, DisableIf < std::is\_same < Num, int >> = dummy > bool contains (int val) const

- bool contains (const Interval < Number > &rhs) const

Checks if the interval contains the given interval.

bool meets (const Number &n) const

Checks if the interval meets the given value, that is if the given value is contained in the **closed** interval defined by the bounds.

void bloat\_by (const Number &width)

Bloats the interval by the given value.

• void bloat\_times (const Number &factor)

Bloats the interval times the factor (multiplies the overall width).

void shrink\_by (const Number &width)

Shrinks the interval by the given value.

• void shrink\_times (const Number &factor)

Shrinks the interval by a multiple of its width.

std::pair< Interval< Number >, Interval< Number >> split () const

Splits the interval into 2 equally sized parts (strict-weak-cut).

std::list< Interval< Number > > split (unsigned n) const

Splits the interval into n equally sized parts (strict-weak-cut).

std::string toString () const

Creates a string representation of the interval.

Interval < Number > add (const Interval < Number > &rhs) const

Adds two intervals according to natural interval arithmetic.

- void add\_assign (const Interval < Number > &rhs)
- Interval < Number > sub (const Interval < Number > &rhs) const

Subtracts two intervals according to natural interval arithmetic.

- void sub\_assign (const Interval < Number > &rhs)
- Interval < Number > mul (const Interval < Number > &rhs) const

Multiplies two intervals according to natural interval arithmetic.

- void mul\_assign (const Interval < Number > &rhs)
- Interval < Number > div (const Interval < Number > &rhs) const

Divides two intervals according to natural interval arithmetic.

- void div\_assign (const Interval < Number > &rhs)
- bool div\_ext (const Interval < Number > &rhs, Interval < Number > &a, Interval < Number > &b) const
   Implements extended interval division with intervals containting zero.
- Interval < Number > inverse () const

Calculates the additive inverse of an interval with respect to natural interval arithmetic.

• Interval < Number > abs () const

Calculates the absolute value of the interval.

• void abs\_assign ()

Calculates and assigns the absolute value of the interval.

void inverse\_assign ()

Calculates and assigns the additive inverse of an interval with respect to natural interval arithmetic.

bool reciprocal (Interval < Number > &a, Interval < Number > &b) const

Calculates the multiplicative inverse of an interval with respect to natural interval arithmetic.

template<typename Num = Number, EnableIf< std::is\_floating\_point< Num >> = dummy>
 Interval< Number > root (int deg) const

Calculates the nth root of the interval with respect to natural interval arithmetic.

template<typename Num = Number, EnableIf< std::is\_floating\_point< Num >> = dummy> void root\_assign (unsigned deg)

Calculates and assigns the nth root of the interval with respect to natural interval arithmetic.

bool is\_consistent () const

A quick check for the bound values.

Number distance (const Interval < Number > &interval A)

Calculates the distance between two Intervals.

Interval < Number > convex\_hull (const Interval < Number > &interval) const

#### **Static Public Member Functions**

• static Interval < Number > unbounded\_interval ()

Method which returns the unbounded interval rooted at 0.

static Interval < Number > empty\_interval ()

Method which returns the empty interval rooted at 0.

static Interval < Number > zero\_interval ()

Method which returns the pointinterval rooted at 0.

• static void sanitize (Interval < Number > &)

## **Protected Attributes**

- · BoostInterval mContent
- BoundType mLowerBoundType = BoundType::STRICT
- BoundType mUpperBoundType = BoundType::STRICT

### **Friends**

• std::ostream & operator << (std::ostream &str, const Interval < Number > &i)

Operator which passes a string representation of this to the given ostream.

## 12.184.1 Detailed Description

```
template<typename Number> class carl::Interval< Number >
```

The class which contains the interval arithmetic including trigonometric functions.

The template parameter contains the number type used for the boundaries. It is necessary to implement the rounding and checking policies for any non-primitive type such that the desired inclusion property can be maintained.

Requirements for the NumberType:

- Operators +,-,\*,/ with the expected functionality
- Operators +=,-=,\*=,/= with the expected functionality
- Operators <,>,<=,>=,==,!= with the expected functionality
- · Operations abs, min, max, log, exp, power, sqrt
- Trigonometric functions sin, cos, tan, asin, acos, atan, sinh, cosh, tanh, asinh, acosh, atanh (these functions are needed for the specialization of the rounding modes.
- Operator <<

## 12.184.2 Member Typedef Documentation

```
12.184.2.1 BoostInterval template<typename Number >
using carl::Interval < Number >::BoostInterval = boost::numeric::interval < Number, BoostIntervalPolicies
>
```

```
12.184.2.2 BoostIntervalPolicies template<typename Number >
using carl::Interval< Number >::BoostIntervalPolicies = boost::numeric::interval_lib::policies<
typename Policy::roundingP, typename Policy::checkingP >
```

```
12.184.2.3 checkingP using carl::policies< Number, Interval< Number > >::checkingP = carl::checking<Number> [inherited]
```

```
12.184.2.4 evalintervalmap template<typename Number > using carl::Interval< Number >::evalintervalmap = std::map<Variable, Interval<Number> >
```

```
12.184.2.5 Policy template<typename Number >
using carl::Interval < Number >::Policy = policies < Number, Interval < Number > >
```

```
12.184.2.6 roundingP using carl::policies< Number, Interval< Number > >::roundingP = carl::rounding<Number>
[inherited]
```

#### 12.184.3 Constructor & Destructor Documentation

```
12.184.3.1 Interval() [1/28] template<typename Number > carl::Interval < Number >::Interval ( ) [inline]
```

Default constructor which constructs the empty interval at point 0.

Constructor which constructs the pointinterval at n.

### **Parameters**

*n* Location of the pointinterval.

Constructor which constructs the weak-bounded interval between lower and upper.

If the bounds are invalid an empty interval at point 0 is constructed.

| lower | The desired lower bound. |
|-------|--------------------------|
| upper | The desired upper bound. |

Constructor which constructs the interval according to the passed boost interval with the passed bound types.

Note that if the interval is a pointinterval with both strict bounds or the content is invalid the empty interval is constructed and if both bounds are infty the unbounded interval is constructed.

### **Parameters**

| content        | The passed boost interval.                      |
|----------------|---|
| lowerBoundType | The desired lower bound type, defaults to WEAK. |
| upperBoundType | The desired upper bound type, defaults to WEAK. |

Constructor which constructs the interval according to the passed bounds with the passed bound types.

Note that if the interval is a pointinterval with both strict bounds or the content is invalid the empty interval is constru

| lower          | The desired lower bound.      |
|----------------|-------------------------------|
| IowerBoundType | The desired lower bound type. |
| upper          | The desired upper bound.      |
| upperBoundType | The desired upper bound type. |

Copy constructor.

o The original interval.

Constructor which constructs a pointinterval from a passed double.

#### **Parameters**

n The passed double.

Constructor which constructs an interval from the passed double bounds.

| lower | The desired lower bound. |
|-------|--------------------------|
| upper | The desired upper bound. |

```
double upper,
BoundType upperBoundType ) [inline]
```

Constructor which constructs the interval according to the passed double bounds with the passed bound types.

Note that if the interval is a pointinterval with both strict bounds or the content is invalid the empty interval is constru

#### **Parameters**

| lower          | The desired double lower bound. |
|----------------|---------------------------------|
| IowerBoundType | The desired lower bound type.   |
| upper          | The desired double upper bound. |
| upperBoundType | The desired upper bound type.   |

Constructor which constructs a pointinterval from a passed int.

#### **Parameters**

```
n The passed double.
```

Constructor which constructs an interval from the passed int bounds.

| lower | The desired lower bound. |
|-------|--------------------------|
| upper | The desired upper bound. |

```
int upper,
BoundType upperBoundType ) [inline]
```

Constructor which constructs the interval according to the passed int bounds with the passed bound types.

Note that if the interval is a pointinterval with both strict bounds or the content is invalid the empty interval is constru

#### **Parameters**

| lower          | The desired lower bound.      |
|----------------|-------------------------------|
| IowerBoundType | The desired lower bound type. |
| upper          | The desired upper bound.      |
| upperBoundType | The desired upper bound type. |

Constructor which constructs a pointinterval from a passed unsigned int.

#### **Parameters**

```
n The passed double.
```

Constructor which constructs an interval from the passed unsigned int bounds.

| lower | The desired lower bound. |
|-------|--------------------------|
| upper | The desired upper bound. |

```
unsigned int upper,
BoundType upperBoundType ) [inline]
```

Constructor which constructs the interval according to the passed unsigned int bounds with the passed bound types.

Note that if the interval is a pointinterval with both strict bounds or the content is invalid the empty interval is constru

#### **Parameters**

| lower          | The desired lower bound.      |
|----------------|-------------------------------|
| IowerBoundType | The desired lower bound type. |
| upper          | The desired upper bound.      |
| upperBoundType | The desired upper bound type. |

Constructor which constructs a pointinterval from a passed general rational number.

## **Parameters**

```
n The passed double.
```

```
12.184.3.18 Interval() [18/28] template<typename Number >
template<typename Num = Number, typename Rational , EnableIf< std::is_floating_point< Num >>
= dummy, DisableIf< std::is_same< Num, Rational >> = dummy>
carl::Interval< Number >::Interval (
    Rational lower,
    Rational upper ) [inline], [explicit]
```

Constructor which constructs an interval from the passed general rational bounds.

| lower | The desired lower bound. |
|-------|--------------------------|
| upper | The desired upper bound. |

```
12.184.3.19 Interval() [19/28] template<typename Number >
template<typename Num = Number, typename Rational, EnableIf< std::is_floating_point< Num >>
= dummy, DisableIf< std::is_same< Num, Rational >> = dummy>
```

Constructor which constructs the interval according to the passed general rational bounds with the passed bound types.

Note that if the interval is a pointinterval with both strict bounds or the content is invalid the empty interval is constru

### **Parameters**

| lower          | The desired lower bound.      |
|----------------|-------------------------------|
| IowerBoundType | The desired lower bound type. |
| upper          | The desired upper bound.      |
| upperBoundType | The desired upper bound type. |

Constructor which constructs a pointinterval from a passed general float number (e.g.

### FLOAT\_T).

### **Parameters**

```
n The passed double.
```

Constructor which constructs an interval from the passed general float bounds (e.g.

### FLOAT\_T).

| lower | The desired lower bound. |
|-------|--------------------------|
| upper | The desired upper bound. |

Constructor which constructs the interval according to the passed general float bounds (e.g.

FLOAT\_T) with the passed bound types. Note that if the interval is a pointinterval with both strict bounds or the content is invalid the empty interval is constru

#### **Parameters**

| lower          | The desired lower bound.      |
|----------------|-------------------------------|
| lowerBoundType | The desired lower bound type. |
| upper          | The desired upper bound.      |
| upperBoundType | The desired upper bound type. |

Constructor which constructs a pointinterval from a passed general float number (e.g.

## FLOAT\_T).

# Parameters

```
n The passed double.
```

Constructor which constructs an interval from the passed general float bounds (e.g.

FLOAT\_T).

| lower | The desired lower bound. |
|-------|--------------------------|
| upper | The desired upper bound. |

Constructor which constructs the interval according to the passed general float bounds (e.g.

FLOAT\_T) with the passed bound types. Note that if the interval is a pointinterval with both strict bounds or the content is invalid the empty interval is constru

| lower          | The desired lower bound.      |
|----------------|-------------------------------|
| IowerBoundType | The desired lower bound type. |
| upper          | The desired upper bound.      |
| upperBoundType | The desired upper bound type. |

```
12.184.3.29 ~Interval() template<typename Number > carl::Interval < Number >::~Interval ( ) [default]
```

Destructor.

### 12.184.4 Member Function Documentation

```
12.184.4.1 abs() template<typename Number >
Interval< Number > carl::Interval< Number >::abs
```

Calculates the absolute value of the interval.

Returns

Interval.

```
12.184.4.2 abs_assign() template<typename Number >
void carl::Interval< Number >::abs_assign
```

Calculates and assigns the absolute value of the interval.

Adds two intervals according to natural interval arithmetic.

# **Parameters**

```
rhs Interval.
```

Returns

Result.

Bloats the interval by the given value.

### **Parameters**

```
width Width.
```

Bloats the interval times the factor (multiplies the overall width).

### **Parameters**

```
factor Factor.
```

```
12.184.4.7 center_assign() template<typename Number > void carl::Interval< Number >::center_assign
```

Computes and assigns the center point of the interval.

```
12.184.4.8 contains() [1/3] template<typename Number > bool carl::Interval < Number >::contains (

const Interval < Number > & rhs ) const
```

Checks if the interval contains the given interval.

## **Parameters**

```
rhs Interval to be checked.
```

## Returns

True if rhs is contained in this.

Checks if the interval contains the given value.

val Value to be checked.

### Returns

True if the value is contained in this.

```
12.184.4.11 contains_integer() template<typename Number > bool carl::Interval< Number >::contains_integer
```

Checks if the interval contains at least one integer value.

### Returns

true, if the interval contains an integer.

```
12.184.4.12 content() [1/2] template<typename Number >
BoostInterval& carl::Interval< Number >::content ( ) [inline]
```

Returns a reference to the included boost interval.

## Returns

Boost interval reference.

```
12.184.4.13 content() [2/2] template<typename Number > const BoostInterval& carl::Interval< Number >::content ( ) const [inline]
```

Returns a reference to the included boost interval.

# Returns

Boost interval reference.

```
12.184.4.15 diameter() template<typename Number > Number carl::Interval< Number >::diameter
```

Returns the diameter of the interval.

Returns

Diameter.

```
12.184.4.16 diameter_assign() template<typename Number > void carl::Interval< Number >::diameter_assign
```

Computes and assigns the diameter of the interval.

Returns the ratio of the diameters of the given intervals.

## **Parameters**

```
rhs Other interval.
```

Returns

Ratio.

Computes and assigns the ratio of the diameters of the given intervals.

## **Parameters**

rhs Other interval.

Calculates the distance between two Intervals.

### **Parameters**

## Returns

distance to intervalA

## **Parameters**

## Returns

distance to intervalA

Divides two intervals according to natural interval arithmetic.

## **Parameters**

```
rhs Interval.
```

## Returns

Result.

**Todo** Correctly determine if bounds are strict or weak.

Implements extended interval division with intervals containting zero.

### **Parameters**

| rhs | Interval. |
|-----|-----------|
| а   | Result a. |
| b   | Result b. |

## Returns

True if split occurred.

```
12.184.4.23 empty_interval() template<typename Number > static Interval<Number> carl::Interval< Number >::empty_interval ( ) [inline], [static]
```

Method which returns the empty interval rooted at 0.

## Returns

Empty interval.

```
12.184.4.24 integral_part() template<typename Number >
Interval < Number > carl::Interval < Number >::integral_part
```

Computes the integral part of the given interval.

## Returns

Interval.

```
12.184.4.25 integralPart_assign() template<typename Number > void carl::Interval< Number >::integralPart_assign
```

Computes and assigns the integral part of the given interval.

### Returns

Interval.

```
12.184.4.26 inverse() template<typename Number >
Interval< Number > carl::Interval< Number >::inverse
```

Calculates the additive inverse of an interval with respect to natural interval arithmetic.

## Returns

Interval.

```
12.184.4.27 inverse_assign() template<typename Number > void carl::Interval< Number >::inverse_assign
```

Calculates and assigns the additive inverse of an interval with respect to natural interval arithmetic.

```
12.184.4.28 is_closed_interval() template<typename Number > bool carl::Interval< Number >::is_closed_interval ( ) const [inline]
```

Function which determines, if the interval is closed.

#### Returns

True if both bounds are WEAK.

```
12.184.4.29 is_consistent() template<typename Number >
bool carl::Interval< Number >::is_consistent ( ) const [inline]
```

A quick check for the bound values.

# Returns

True if the lower bound is less or equal to the upper bound.

```
12.184.4.30 is_empty() template<typename Number > bool carl::Interval< Number >::is_empty ( ) const [inline]
```

Function which determines, if the interval is empty.

# Returns

True if the interval is empty.

```
12.184.4.31 is_half_bounded() template<typename Number > bool carl::Interval< Number >::is_half_bounded () const [inline]
```

Function which determines, if the interval is half-bounded.

### Returns

True if exactly one bound is INFTY.

```
12.184.4.32 is_infinite() template<typename Number > bool carl::Interval< Number >::is_infinite () const [inline]
```

Function which determines, if the interval is (-oo,oo).

### Returns

True if both bounds are INFTY.

```
12.184.4.33 is_negative() template<typename Number > bool carl::Interval< Number >::is_negative ( ) const [inline]
```

### Returns

true, if it this interval contains only negative values.

```
12.184.4.34 is_one() template<typename Number > bool carl::Interval< Number >::is_one ( ) const [inline]
```

Function which determines, if the interval is the one interval.

## Returns

True if it is a pointinterval rooted at 1.

```
12.184.4.35 is_open_interval() template<typename Number > bool carl::Interval< Number >::is_open_interval () const [inline]
```

Function which determines, if the interval is open.

### Returns

True if both bounds are STRICT.

```
12.184.4.36 is_point_interval() template<typename Number > bool carl::Interval< Number >::is_point_interval ( ) const [inline]
```

Function which determines, if the interval is a pointinterval.

### Returns

True if this is a pointinterval.

```
12.184.4.37 is_positive() template<typename Number > bool carl::Interval< Number >::is_positive () const [inline]
```

### Returns

true, if it this interval contains only positive values.

```
12.184.4.38 is_semi_negative() template<typename Number > bool carl::Interval< Number >::is_semi_negative () const [inline]
```

### Returns

true, if it this interval contains only negative values or 0.

```
12.184.4.39 is_semi_positive() template<typename Number > bool carl::Interval< Number >::is_semi_positive () const [inline]
```

## Returns

true, if it this interval contains only positive values or 0.

```
12.184.4.40 is_unbounded() template<typename Number > bool carl::Interval< Number >::is_unbounded ( ) const [inline]
```

Function which determines, if the interval is unbounded.

## Returns

True if at least one bound is INFTY.

```
12.184.4.41 is_zero() template<typename Number > bool carl::Interval< Number >::is_zero () const [inline]
```

Function which determines, if the interval is the zero interval.

Returns

True if it is a pointinterval rooted at 0.

```
12.184.4.42 lower() template<typename Number > const Number& carl::Interval< Number >::lower ( ) const [inline]
```

The getter for the lower boundary of the interval.

Returns

Lower interval boundary.

```
12.184.4.43 | lower_bound() template<typename Number > auto carl::Interval< Number >::lower_bound () const [inline]
```

```
12.184.4.44 | lower_bound_type() template<typename Number >
BoundType carl::Interval< Number >::lower_bound_type () const [inline]
```

The getter for the lower bound type of the interval.

Returns

Lower bound type.

```
12.184.4.45 magnitude() template<typename Number > Number carl::Interval< Number >::magnitude
```

Returns the magnitude of the interval.

Returns

Magnitude.

```
12.184.4.46 magnitude_assign() template<typename Number > void carl::Interval< Number >::magnitude_assign
```

Computes and assigns the magnitude of the interval.

Checks if the interval meets the given value, that is if the given value is contained in the **closed** interval defined by the bounds.

val Value to be checked.

# Returns

True if val is fully contained in this.

Multiplies two intervals according to natural interval arithmetic.

## **Parameters**

```
rhs Interval.
```

### Returns

Result.

The assignment operator.

### **Parameters**

```
rhs | Source interval.
```

Returns

Calculates the multiplicative inverse of an interval with respect to natural interval arithmetic.

### **Parameters**

| а | Result a. |
|---|-----------|
| b | Result b. |

## Returns

True, if split occured.

Calculates the nth root of the interval with respect to natural interval arithmetic.

### **Parameters**

```
deg Degree.
```

## Returns

Result.

```
12.184.4.53 root_assign() template<typename Number > template<typename Num , EnableIf< std::is_floating_point< Num >> > void carl::Interval< Number >::root_assign ( unsigned deg )
```

Calculates and assigns the nth root of the interval with respect to natural interval arithmetic.

```
deg Degree.
```

```
12.184.4.54 sanitize() static void carl::policies< Number, Interval< Number > >::sanitize (
Interval< Number > & ) [inline], [static], [inherited]
```

Advanced setter to modify both boundaries at once.

## **Parameters**

| lower | Lower boundary. |
|-------|-----------------|
| upper | Upper boundary. |

Advanced setter to modify both boundaries at once by passing a boost interval.

### **Parameters**

```
content Boost interval.
```

The setter for the lower boundary of the interval.

## **Parameters**

```
n Lower boundary.
```

The setter for the lower boundary of the interval.

```
n Lower boundary.
```

TODO: Fix this.

```
12.184.4.59 set_lower_bound_type() template<typename Number > void carl::Interval< Number >::set_lower_bound_type (

BoundType b ) [inline]
```

The setter for the lower bound type of the interval.

## **Parameters**

```
b Lower bound type.
```

The setter for the upper boundary of the interval.

## **Parameters**

```
n Upper boundary.
```

The setter for the upper boundary of the interval.

## **Parameters**

```
n Upper boundary.
```

TODO: Fix this.

The setter for the upper bound type of the interval.

b Upper bound type.

```
12.184.4.63 sgn() template<typename Number > Sign carl::Interval< Number >::sgn [inline]
```

Determine whether the interval lays entirely left of 0 (NEGATIVE\_SIGN), right of 0 (POSITIVE\_SIGN) or contains 0 (ZERO\_SIGN).

### Returns

NEGATIVE\_SIGN, if the interval lays entirely left of 0; POSITIVE\_SIGN, if right of 0; or ZERO\_SIGN, if contains 0.

```
12.184.4.64 shrink_by() template<typename Number > void carl::Interval< Number >::shrink_by (

const Number & width )
```

Shrinks the interval by the given value.

### **Parameters**

width Width.

Shrinks the interval by a multiple of its width.

# **Parameters**

factor Factor.

```
12.184.4.66 split() [1/2] template<typename Number > std::pair< Interval< Number >, Interval< Number > carl::Interval< Number >::split
```

Splits the interval into 2 equally sized parts (strict-weak-cut).

## Returns

pair<interval, interval>.

```
12.184.4.67 split() [2/2] template<typename Number > std::list< Interval< Number >> carl::Interval< Number >::split ( unsigned n ) const
```

Splits the interval into n equally sized parts (strict-weak-cut).

## Returns

list<interval>.

Subtracts two intervals according to natural interval arithmetic.

## **Parameters**

```
rhs Interval.
```

## Returns

Result.

```
12.184.4.70 toString() template<typename Number >
std::string carl::Interval< Number >::toString
```

Creates a string representation of the interval.

## Returns

String representation of this.

```
12.184.4.71 unbounded_interval() template<typename Number > static Interval<Number> carl::Interval< Number >::unbounded_interval ( ) [inline], [static]
```

Method which returns the unbounded interval rooted at 0.

Returns

Unbounded interval.

```
12.184.4.72 upper() template<typename Number > const Number& carl::Interval< Number >::upper ( ) const [inline]
```

The getter for the upper boundary of the interval.

Returns

Upper interval boundary.

```
12.184.4.73 upper_bound() template<typename Number > auto carl::Interval< Number >::upper_bound () const [inline]
```

```
12.184.4.74 upper_bound_type() template<typename Number >
BoundType carl::Interval< Number >::upper_bound_type () const [inline]
```

The getter for the upper bound type of the interval.

Returns

Upper bound type.

```
12.184.4.75 zero_interval() template<typename Number > static Interval<Number> carl::Interval< Number >::zero_interval ( ) [inline], [static]
```

Method which returns the pointinterval rooted at 0.

Returns

Pointinterval(0).

# 12.184.5 Friends And Related Function Documentation

```
12.184.5.1 operator << template < typename Number > std::ostream& operator << ( std::ostream & str, const Interval < Number > & i ) [friend]
```

Operator which passes a string representation of this to the given ostream.

| str | The ostream.  |
|-----|---------------|
| i   | The interval. |

#### Returns

A reference to ostream.

### 12.184.6 Field Documentation

```
12.184.6.1 mContent template<typename Number >
BoostInterval carl::Interval< Number >::mContent [protected]
```

```
12.184.6.2 mLowerBoundType template<typename Number >
BoundType carl::Interval< Number >::mLowerBoundType = BoundType::STRICT [protected]
```

```
12.184.6.3 mUpperBoundType template<typename Number >
BoundType carl::Interval< Number >::mUpperBoundType = BoundType::STRICT [protected]
```

# 12.185 carl::IntRepRealAlgebraicNumber < Number > Class Template Reference

#include <Ran.h>

## **Public Member Functions**

- void refine () const
- IntRepRealAlgebraicNumber ()
- IntRepRealAlgebraicNumber (const Number &n)
- IntRepRealAlgebraicNumber (const UnivariatePolynomial < Number > &p, const Interval < Number > &i)
- IntRepRealAlgebraicNumber (const IntRepRealAlgebraicNumber &ran)=default
- IntRepRealAlgebraicNumber (IntRepRealAlgebraicNumber &&ran)=default
- IntRepRealAlgebraicNumber & operator= (const IntRepRealAlgebraicNumber &n)=default
- IntRepRealAlgebraicNumber & operator= (IntRepRealAlgebraicNumber &&n)=default
- bool is\_numeric () const
- const auto & polynomial () const
- · const auto & interval () const
- const auto & value () const
- auto & polynomial\_int () const
- auto & interval\_int () const

## **Static Public Member Functions**

static IntRepRealAlgebraicNumber < Number > create\_safe (const UnivariatePolynomial < Number > &p, const Interval < Number > &i)

### **Friends**

- template<typename Num >
   bool compare (const IntRepRealAlgebraicNumber< Num > &, const IntRepRealAlgebraicNumber< Num >
   &, const Relation)
- template < typename Num >
  bool compare (const IntRepRealAlgebraicNumber < Num > &, const Num &, const Relation)
- template<typename Num, typename Poly >
   boost::tribool evaluate (const BasicConstraint< Poly > &, const Assignment< IntRepRealAlgebraicNumber</li>
   Num >> &, bool, bool)
- template<typename Num >
   std::optional< IntRepRealAlgebraicNumber< Num > > evaluate (MultivariatePolynomial< Num >, const
   Assignment< IntRepRealAlgebraicNumber< Num >> &, bool)
- template < typename Num > Num branching\_point (const IntRepRealAlgebraicNumber < Num > &n)
- template<typename Num >
   Num sample\_above (const IntRepRealAlgebraicNumber< Num > &n)
- template<typename Num >
   Num sample\_below (const IntRepRealAlgebraicNumber< Num > &n)
- template<typename Num >
   Num sample\_between (const IntRepRealAlgebraicNumber< Num > &lower, const IntRepRealAlgebraicNumber
   Num > &upper)
- template<typename Num >
   Num sample\_between (const IntRepRealAlgebraicNumber
   Num > &lower, const Num &upper)
- template < typename Num >
   Num sample\_between (const Num & lower, const IntRepRealAlgebraicNumber < Num > & upper)
- template < typename Num > Num floor (const IntRepRealAlgebraicNumber < Num > &n)
- template<typename Num >
   Num ceil (const IntRepRealAlgebraicNumber< Num > &n)
- template < typename Num >
   Sign sgn (const IntRepRealAlgebraicNumber < Num > &n, const UnivariatePolynomial < Num > &p)

# 12.185.1 Constructor & Destructor Documentation

```
12.185.1.1 IntRepRealAlgebraicNumber() [1/5] template<typename Number > carl::IntRepRealAlgebraicNumber< Number >::IntRepRealAlgebraicNumber ( ) [inline]
```

```
12.185.1.3 IntRepRealAlgebraicNumber() [3/5] template<typename Number >
carl::IntRepRealAlgebraicNumber < Number >::IntRepRealAlgebraicNumber (
             const UnivariatePolynomial< Number > & p,
             const Interval < Number > & i ) [inline]
12.185.1.4 IntRepRealAlgebraicNumber() [4/5] template<typename Number >
carl::IntRepRealAlgebraicNumber < Number >::IntRepRealAlgebraicNumber (
             const IntRepRealAlgebraicNumber< Number > & ran ) [default]
12.185.1.5 IntRepRealAlgebraicNumber() [5/5] template<typename Number >
carl::IntRepRealAlgebraicNumber< Number >::IntRepRealAlgebraicNumber (
             IntRepRealAlgebraicNumber < Number > && ran ) [default]
12.185.2 Member Function Documentation
12.185.2.1 create_safe() template<typename Number >
\verb|static IntRepRealAlgebraicNumber<| Number> | carl::IntRepRealAlgebraicNumber<| Number> | ::create. \\
safe (
             const UnivariatePolynomial < Number > & p,
             const Interval < Number > & i ) [inline], [static]
12.185.2.2 interval() template<typename Number >
const auto& carl::IntRepRealAlgebraicNumber < Number >::interval ( ) const [inline]
12.185.2.3 interval_int() template<typename Number >
auto& carl::IntRepRealAlgebraicNumber < Number >::interval_int ( ) const [inline]
12.185.2.4 is_numeric() template<typename Number >
bool carl::IntRepRealAlgebraicNumber < Number >::is_numeric ( ) const [inline]
12.185.2.5 operator=() [1/2] template<typename Number >
IntRepRealAlgebraicNumber& carl::IntRepRealAlgebraicNumber< Number >::operator= (
             const IntRepRealAlgebraicNumber < Number > & n ) [default]
```

```
12.185.2.6 operator=() [2/2] template<typename Number >
IntRepRealAlgebraicNumber& carl::IntRepRealAlgebraicNumber< Number >::operator= (
             {\tt IntRepRealAlgebraicNumber} < {\tt Number} > \&\& \ n \ ) \quad [{\tt default}]
12.185.2.7 polynomial() template<typename Number >
const auto& carl::IntRepRealAlgebraicNumber< Number >::polynomial ( ) const [inline]
12.185.2.8 polynomial_int() template<typename Number >
auto& carl::IntRepRealAlgebraicNumber< Number >::polynomial_int ( ) const [inline]
12.185.2.9 refine() template<typename Number >
void carl::IntRepRealAlgebraicNumber< Number >::refine ( ) const [inline]
12.185.2.10 value() template<typename Number >
const auto& carl::IntRepRealAlgebraicNumber < Number >::value ( ) const [inline]
12.185.3 Friends And Related Function Documentation
12.185.3.1 branching_point template<typename Number >
template < typename Num >
Num branching_point (
            const IntRepRealAlgebraicNumber< Num > & n ) [friend]
12.185.3.2 ceil template<typename Number >
template<typename Num >
Num ceil (
            const IntRepRealAlgebraicNumber< Num > & n) [friend]
12.185.3.3 compare [1/2] template<typename Number >
template<typename Num >
bool compare (
             const IntRepRealAlgebraicNumber< Num > & ,
             const IntRepRealAlgebraicNumber< Num > & ,
             const Relation ) [friend]
```

```
12.185.3.4 compare [2/2] template<typename Number >
template<typename Num >
bool compare (
            const IntRepRealAlgebraicNumber< Num > & ,
            const Num & ,
            const Relation ) [friend]
12.185.3.5 evaluate [1/2] template<typename Number >
template<typename Num , typename Poly >
boost::tribool\ evaluate (
            const BasicConstraint< Poly > & ,
            const Assignment< IntRepRealAlgebraicNumber< Num >> & ,
            bool ,
            bool ) [friend]
12.185.3.6 evaluate [2/2] template<typename Number >
template<typename Num >
std::optional<IntRepRealAlgebraicNumber<Num> > evaluate (
            MultivariatePolynomial< Num > ,
            const Assignment< IntRepRealAlgebraicNumber< Num >> & ,
            bool ) [friend]
12.185.3.7 floor template<typename Number >
template<typename Num >
Num floor (
            const IntRepRealAlgebraicNumber< Num > & n) [friend]
12.185.3.8 sample_above template<typename Number >
template<typename Num >
Num sample_above (
            const IntRepRealAlgebraicNumber< Num > & n ) [friend]
12.185.3.9 sample_below template<typename Number >
template<typename Num >
Num sample_below (
            const IntRepRealAlgebraicNumber< Num > & n ) [friend]
```

```
12.185.3.10 sample_between [1/3] template<typename Number >
template<typename Num >
Num sample_between (
            const IntRepRealAlgebraicNumber< Num > & lower,
             const IntRepRealAlgebraicNumber< Num > & upper ) [friend]
12.185.3.11 sample_between [2/3] template<typename Number >
template<typename Num >
Num sample_between (
             const IntRepRealAlgebraicNumber< Num > & lower,
             const Num & upper ) [friend]
12.185.3.12 sample_between [3/3] template<typename Number >
{\tt template}{<}{\tt typename~Num~>}
Num sample_between (
             const Num & lower,
             const IntRepRealAlgebraicNumber< Num > & upper ) [friend]
12.185.3.13 sgn template<typename Number >
{\tt template}{<}{\tt typename~Num~>}
Sign sgn (
             const IntRepRealAlgebraicNumber< Num > & n,
             const UnivariatePolynomial< Num > & p ) [friend]
```

# 12.186 carl::io::InvalidInputStringException Class Reference

#include <StringParser.h>

## **Public Member Functions**

- InvalidInputStringException (const std::string &msg, std::string substring, const std::string &inputString=""")
- void setInputString (const std::string &inputString)
- · virtual cstring what () const noexcept override

## 12.186.1 Constructor & Destructor Documentation

#### 12.186.2 Member Function Documentation

```
12.186.2.2 what() virtual cstring carl::io::InvalidInputStringException::what ( ) const [inline], [override], [virtual], [noexcept]
```

# 12.187 carl::is\_factorized\_type< T > Struct Template Reference

```
#include <typetraits.h>
```

# 12.188 carl::is\_factorized\_type< FactorizedPolynomial< P > > Struct Template Reference

#include <FactorizedPolynomial.h>

## 12.189 carl::is\_field\_type< T > Struct Template Reference

States if a type is a field.

```
#include <typetraits.h>
```

### 12.189.1 Detailed Description

```
template<typename T> struct carl::is_field_type< T>
```

States if a type is a field.

Default is true for rationals, false otherwise.

See also

UnivariatePolynomial - CauchyBound for example.

# 12.190 carl::is\_field\_type< GFNumber< C > > Struct Template Reference

States that a Gallois field is a field.

```
#include <typetraits.h>
```

### 12.190.1 Detailed Description

template<typename C> struct carl::is\_field\_type< GFNumber< C>>

States that a Gallois field is a field.

# 12.191 carl::is\_finite\_type< T > Struct Template Reference

States if a type represents only a finite domain.

#include <typetraits.h>

## 12.191.1 Detailed Description

template<typename T> struct carl::is\_finite\_type< T>

States if a type represents only a finite domain.

Default is true for fundamental types, false otherwise.

## 12.192 carl::is\_finite\_type< GFNumber< C >> Struct Template Reference

Type trait is\_finite\_type\_domain.

#include <typetraits.h>

## 12.192.1 Detailed Description

template<typename C> struct carl::is\_finite\_type< GFNumber< C > >

Type trait is\_finite\_type\_domain.

Default is false.

# 12.193 carl::is\_float\_type< T > Struct Template Reference

States if a type is a floating point type.

#include <typetraits.h>

#### 12.193.1 Detailed Description

```
template<typename T> struct carl::is_float_type< T>
```

States if a type is a floating point type.

Default is true if std::is\_floating\_point is true for this type.

# 12.194 carl::is\_float\_type< carl::FLOAT\_T< C > > Struct Template Reference

```
#include <typetraits.h>
```

# 12.195 carl::is\_from\_variant < T, Variant > Struct Template Reference

```
#include <variant_util.h>
```

#### **Static Public Attributes**

• static constexpr bool value = detail::is\_from\_variant\_wrapper<std::is\_same, T, Variant>::value

### 12.195.1 Field Documentation

```
12.195.1.1 value template<typename T , typename Variant > constexpr bool carl::is_from_variant< T, Variant >::value = detail::is_from_variant_wrapper<std↔ ::is_same, T, Variant>::value [static], [constexpr]
```

# 12.196 carl::detail::is\_from\_variant\_wrapper< Check, T, Variant > Struct Template Reference

# 12.197 carl::detail::is\_from\_variant\_wrapper< Check, T, Variant< Args... >> Struct Template Reference

```
#include <variant_util.h>
```

#### Static Public Attributes

• static constexpr bool value = std::disjunction<Check<T,Args>...>::value

#### 12.197.1 Field Documentation

```
12.197.1.1 value template<template< typename... > class Check, typename T , template< typename...
> class Variant, typename... Args>
constexpr bool carl::detail::is_from_variant_wrapper< Check, T, Variant< Args... > >::value =
std::disjunction<Check<T,Args>...>::value [static], [constexpr]
```

## 12.198 carl::is\_instantiation\_of Struct Reference

#include <SFINAE.h>

## **Static Public Attributes**

• static const bool value = false

## 12.198.1 Field Documentation

**12.198.1.1 value** const bool carl::is\_instantiation\_of::value = false [static]

# 12.199 carl::is\_instantiation\_of< Template, Template< Args... >> Struct Template Reference

#include <SFINAE.h>

## **Static Public Attributes**

static const bool value = true

## 12.199.1 Field Documentation

```
12.199.1.1 value template<template< typename... > class Template, typename... Args> const bool carl::is_instantiation_of< Template, Template< Args... > >::value = true [static]
```

# 12.200 carl::is\_integer\_type< T > Struct Template Reference

States if a type is an integer type.

#include <typetraits.h>

## 12.200.1 Detailed Description

```
template<typename T> struct carl::is_integer_type< T>
```

States if a type is an integer type.

Default is false.

# 12.201 carl::is\_integer\_type< cln::cl\_l > Struct Reference

States that cln::cl\_l has the trait is\_integer\_type .

```
#include <typetraits.h>
```

## 12.201.1 Detailed Description

States that cln::cl\_I has the trait is\_integer\_type .

<>

# 12.202 carl::is\_integer\_type< mpz\_class > Struct Reference

States that mpz\_class has the trait is\_integer\_type .

```
#include <typetraits.h>
```

# 12.202.1 Detailed Description

States that mpz\_class has the trait is\_integer\_type .

<>

# 12.203 carl::is\_interval\_type< Number > Struct Template Reference

States whether a given type is an Interval.

```
#include <typetraits.h>
```

# 12.203.1 Detailed Description

```
template<class Number>
struct carl::is_interval_type< Number >
```

States whether a given type is an Interval.

By default, a type is not.

# 12.204 carl::is\_interval\_type< carl::Interval< Number > > Struct Template Reference

#include <Interval.h>

# 12.205 carl::is\_interval\_type< const carl::Interval< Number > > Struct Template Reference

#include <Interval.h>

# 12.206 carl::is\_number\_type< T > Struct Template Reference

States if a type is a number type.

#include <typetraits.h>

#### **Static Public Attributes**

static const bool value = is\_subset\_of\_rationals\_type<T>::value || is\_subset\_of\_integers\_type<T>::value || is\_float\_type<T>::value

Default value of this trait.

## 12.206.1 Detailed Description

template<typename T> struct carl::is\_number\_type< T>

States if a type is a number type.

Default is true for rationals, integers and floats, false otherwise.

## 12.206.2 Field Documentation

```
12.206.2.1 value template<typename T >
constexpr bool carl::is_number_type< T >::value = is_subset_of_rationals_type<T>::value || is_float_type<T>::value [static], [constexpr]
```

Default value of this trait.

# 12.207 carl::is\_number\_type< GFNumber< C > > Struct Template Reference

#include <typetraits.h>

## 12.207.1 Detailed Description

template<typename C> struct carl::is\_number\_type< GFNumber< C>>

See also

**GFNumber** 

# 12.208 carl::is\_number\_type< Interval< T >> Struct Template Reference

#include <Interval.h>

# 12.209 carl::is\_polynomial\_type< T > Struct Template Reference

#include <typetraits.h>

# 12.210 carl::is\_polynomial\_type< carl::MultivariatePolynomial< T, O, P > > Struct Template Reference

#include <MultivariatePolynomial.h>

# 12.211 carl::is\_polynomial\_type< carl::UnivariatePolynomial< T > > Struct Template Reference

#include <UnivariatePolynomial.h>

# 12.212 carl::is\_polynomial\_type< ContextPolynomial< Coeff, Ordering, Policies > > Struct Template Reference

#include <ContextPolynomial.h>

# 12.213 carl::is\_ran\_type< T > Struct Template Reference

#include <Operations.h>

# 12.214 carl::is\_ran\_type< IntRepRealAlgebraicNumber< Number >> Struct Template Reference

#include <Ran.h>

# 12.215 carl::is\_ran\_type< RealAlgebraicNumberThom< Number >> Struct Template Reference

#include <ran\_thom.h>

#### **Static Public Attributes**

• static const bool value = true

#### 12.215.1 Field Documentation

```
12.215.1.1 value template<typename Number >
const bool carl::is_ran_type< RealAlgebraicNumberThom< Number > >::value = true [static]
```

# 12.216 carl::is\_rational\_type< T > Struct Template Reference

States if a type is a rational type.

#include <typetraits.h>

## 12.216.1 Detailed Description

```
template<typename T> struct carl::is_rational_type< T>
```

States if a type is a rational type.

We consider a type to be rational, if it can (in theory) represent any rational number. Default is false.

# 12.217 carl::is\_rational\_type< cln::cl\_RA > Struct Reference

States that cln::cl\_RA has the trait is\_rational\_type .

```
#include <typetraits.h>
```

## 12.217.1 Detailed Description

States that cln::cl\_RA has the trait is\_rational\_type .

# 12.218 carl::is\_rational\_type< FLOAT\_T< C >> Struct Template Reference

#include <typetraits.h>

# 12.219 carl::is\_rational\_type< mpq\_class > Struct Reference

States that mpq\_class has the trait is\_rational\_type.

#include <typetraits.h>

#### 12.219.1 Detailed Description

States that mpq\_class has the trait is\_rational\_type .

<>

# 12.220 carl::is\_subset\_of\_integers\_type < Type > Struct Template Reference

States if a type represents a subset of all integers.

#include <typetraits.h>

## 12.220.1 Detailed Description

template<typename Type>
struct carl::is\_subset\_of\_integers\_type< Type >

States if a type represents a subset of all integers.

Default is true for integer types, false otherwise.

# 12.221 carl::is\_subset\_of\_integers\_type< int > Struct Reference

States that int has the trait is\_subset\_of\_integers\_type .

#include <typetraits.h>

# 12.221.1 Detailed Description

States that int has the trait is\_subset\_of\_integers\_type .

# 12.222 carl::is\_subset\_of\_integers\_type< long int > Struct Reference

States that long int has the trait is\_subset\_of\_integers\_type .

```
#include <typetraits.h>
```

#### 12.222.1 Detailed Description

States that long int has the trait is\_subset\_of\_integers\_type .

<>

# 12.223 carl::is\_subset\_of\_integers\_type< long long int > Struct Reference

States that long long int has the trait is\_subset\_of\_integers\_type .

```
#include <typetraits.h>
```

#### 12.223.1 Detailed Description

States that long long int has the trait is\_subset\_of\_integers\_type .

<>

# 12.224 carl::is\_subset\_of\_integers\_type< short int > Struct Reference

States that short int has the trait is\_subset\_of\_integers\_type .

```
#include <typetraits.h>
```

#### 12.224.1 Detailed Description

States that short int has the trait is\_subset\_of\_integers\_type .

<>

## 12.225 carl::is\_subset\_of\_integers\_type< signed char > Struct Reference

States that signed char has the trait is\_subset\_of\_integers\_type .

```
#include <typetraits.h>
```

## 12.225.1 Detailed Description

States that signed char has the trait is\_subset\_of\_integers\_type .

# 12.226 carl::is\_subset\_of\_integers\_type< unsigned char > Struct Reference

States that unsigned char has the trait is\_subset\_of\_integers\_type .

```
#include <typetraits.h>
```

#### 12.226.1 Detailed Description

States that unsigned char has the trait is\_subset\_of\_integers\_type .

<>

# 12.227 carl::is\_subset\_of\_integers\_type< unsigned int > Struct Reference

States that unsigned int has the trait is\_subset\_of\_integers\_type .

```
#include <typetraits.h>
```

#### 12.227.1 Detailed Description

States that unsigned int has the trait is\_subset\_of\_integers\_type .

<>

# 12.228 carl::is\_subset\_of\_integers\_type< unsigned long int > Struct Reference

States that unsigned long int has the trait is\_subset\_of\_integers\_type .

```
#include <typetraits.h>
```

#### 12.228.1 Detailed Description

States that unsigned long int has the trait is\_subset\_of\_integers\_type .

<>

## 12.229 carl::is\_subset\_of\_integers\_type< unsigned long long int > Struct Reference

States that unsigned long long int has the trait is\_subset\_of\_integers\_type .

```
#include <typetraits.h>
```

# 12.229.1 Detailed Description

States that unsigned long long int has the trait is\_subset\_of\_integers\_type .

# 12.230 carl::is\_subset\_of\_integers\_type< unsigned short int > Struct Reference

States that unsigned short int has the trait is\_subset\_of\_integers\_type .

#include <typetraits.h>

### 12.230.1 Detailed Description

States that unsigned short int has the trait is\_subset\_of\_integers\_type .

<>

# 12.231 carl::is\_subset\_of\_rationals\_type< T > Struct Template Reference

States if a type represents a subset of all rationals and the representation is similar to a rational.

```
#include <typetraits.h>
```

#### **Static Public Attributes**

static constexpr bool value = is\_rational\_type<T>::value
 Default value of this trait.

#### 12.231.1 Detailed Description

```
template<typename T> struct carl::is_subset_of_rationals_type< T >
```

States if a type represents a subset of all rationals and the representation is similar to a rational.

Default is true for rationals, false otherwise.

## 12.231.2 Field Documentation

```
12.231.2.1 value template<typename T >
constexpr bool carl::is_subset_of_rationals_type< T >::value = is_rational_type<T>::value [static],
[constexpr]
```

Default value of this trait.

## 12.232 carl::parser::isDivisible < is\_int > Struct Template Reference

```
#include <parser.h>
```

# 12.233 carl::parser::isDivisible < false > Struct Reference

```
#include <parser.h>
```

#### **Public Member Functions**

template<typename Attr >
bool operator() (const Attr &, std::size\_t)

#### 12.233.1 Member Function Documentation

# 12.234 carl::parser::isDivisible < true > Struct Reference

```
#include <parser.h>
```

### **Public Member Functions**

template<typename Attr >
bool operator() (const Attr &n, std::size\_t exp)

## 12.234.1 Member Function Documentation

## 12.235 carl::Bitset::iterator Struct Reference

Iterate for iterate over all bits of a Bitset that are set to true.

```
#include <Bitset.h>
```

#### **Public Member Functions**

• iterator (const Bitset &b, std::size\_t bit)

Construct a new iterator from a Bitset and a bit.

operator std::size\_t () const

Retrieve the index into the Bitset.

• std::size\_t operator\* () const

Retrieve the index into the Bitset.

• iterator & operator++ ()

Step to the next bit that is set to true.

iterator operator++ (int)

Step to the next bit that is set to true.

• bool operator== (const iterator &rhs) const

Compare two iterators. Asserts that they are compatible.

bool operator!= (const iterator &rhs) const

Compare two iterators. Asserts that they are compatible.

• bool operator< (const iterator &rhs) const

Compare two iterators. Asserts that they are compatible.

## 12.235.1 Detailed Description

Iterate for iterate over all bits of a Bitset that are set to true.

If you want to iterate of all bits that are false use  $operator \sim$  ().

## 12.235.2 Constructor & Destructor Documentation

Construct a new iterator from a Bitset and a bit.

## 12.235.3 Member Function Documentation

```
12.235.3.1 operator std::size_t() carl::Bitset::iterator::operator std::size_t () const [inline]
```

Retrieve the index into the Bitset.

```
12.235.3.2 operator"!=() bool carl::Bitset::iterator::operator!= ( const iterator & rhs ) const [inline]
```

Compare two iterators. Asserts that they are compatible.

```
12.235.3.3 operator*() std::size_t carl::Bitset::iterator::operator* ( ) const [inline]
```

Retrieve the index into the Bitset.

```
12.235.3.4 operator++() [1/2] iterator& carl::Bitset::iterator::operator++ ( ) [inline]
```

Step to the next bit that is set to true.

```
12.235.3.5 operator++() [2/2] iterator carl::Bitset::iterator::operator++ (
    int ) [inline]
```

Step to the next bit that is set to true.

```
12.235.3.6 operator<() bool carl::Bitset::iterator::operator< ( const iterator & rhs ) const [inline]
```

Compare two iterators. Asserts that they are compatible.

```
12.235.3.7 operator==() bool carl::Bitset::iterator::operator== ( const iterator & rhs ) const [inline]
```

Compare two iterators. Asserts that they are compatible.

# 12.236 carl::ran::interval::LazardEvaluation< Rational, Poly > Class Template Reference

#include <LazardEvaluation.h>

## **Public Member Functions**

- LazardEvaluation (const Poly &p)
- auto substitute (Variable v, const IntRepRealAlgebraicNumber< Rational > &r, bool divideZeroFactors=true)
- · const auto & getLiftingPoly () const

#### 12.236.1 Constructor & Destructor Documentation

```
12.236.1.1 LazardEvaluation() template<typename Rational , typename Poly > carl::ran::interval::LazardEvaluation< Rational, Poly >::LazardEvaluation ( const Poly & p) [inline]
```

#### 12.236.2 Member Function Documentation

```
12.236.2.1 getLiftingPoly() template<typename Rational , typename Poly > const auto& carl::ran::interval::LazardEvaluation< Rational, Poly >::getLiftingPoly ( ) const [inline]
```

# 12.237 carl::tree\_detail::LeafIterator< T, reverse > Struct Template Reference

Iterator class for iterations over all leaf elements.

```
#include <carlTree.h>
```

# **Public Types**

using Base = BaseIterator < T, LeafIterator < T, reverse >, reverse >

#### **Public Member Functions**

- LeafIterator (const tree< T > \*t)
- LeafIterator (const tree< T > \*t, std::size\_t root)
- LeafIterator & next ()
- · LeafIterator & previous ()
- template<typename It >

LeafIterator (const BaseIterator < T, It, reverse > &ii)

- LeafIterator (const LeafIterator &ii)
- LeafIterator (LeafIterator &&ii)
- LeafIterator & operator= (const LeafIterator &it)
- LeafIterator & operator= (LeafIterator &&it)
- virtual ~LeafIterator () noexcept=default
- const auto & nodes () const
- const auto & node (std::size\_t id) const
- const auto & curnode () const
- std::size\_t depth () const
- std::size\_t id () const
- bool isRoot () const
- bool isValid () const
- T \* operator-> ()
- T const \* operator-> () const

#### **Data Fields**

• std::size\_t current

#### **Protected Attributes**

• const tree< T > \* mTree

#### 12.237.1 Detailed Description

```
template<typename T, bool reverse = false>
struct carl::tree_detail::LeafIterator< T, reverse >
```

Iterator class for iterations over all leaf elements.

## 12.237.2 Member Typedef Documentation

```
12.237.2.1 Base template<typename T , bool reverse = false>
using carl::tree_detail::LeafIterator< T, reverse >::Base = BaseIterator<T, LeafIterator<T, reverse>, reverse>
```

## 12.237.3 Constructor & Destructor Documentation

```
12.237.3.4 Leaflterator() [4/5] template<typename T , bool reverse = false>
carl::tree_detail::LeafIterator< T, reverse >::LeafIterator (
             const LeafIterator< T, reverse > & ii ) [inline]
12.237.3.5 Leaflterator() [5/5] template<typename T , bool reverse = false>
carl::tree_detail::LeafIterator< T, reverse >::LeafIterator (
             LeafIterator< T, reverse > && ii ) [inline]
12.237.3.6 \simLeaflterator() template<typename T , bool reverse = false>
virtual carl::tree_detail::LeafIterator< T, reverse >::~LeafIterator ( ) [virtual], [default],
[noexcept]
12.237.4 Member Function Documentation
12.237.4.1 curnode() const auto& carl::tree_detail::BaseIterator< T, LeafIterator< T, false >
, reverse >::curnode ( ) const [inline], [inherited]
12.237.4.2 depth() std::size_t carl::tree_detail::BaseIterator< T, LeafIterator< T, false > ,
reverse >::depth ( ) const [inline], [inherited]
12.237.4.3 id() std::size_t carl::tree_detail::BaseIterator< T, LeafIterator< T, false > ,
reverse >::id ( ) const [inline], [inherited]
\textbf{12.237.4.4} \quad \textbf{isRoot()} \quad \texttt{bool carl::tree\_detail::BaseIterator} < \texttt{T, LeafIterator} < \texttt{T, false} > \texttt{, reverse}
>::isRoot ( ) const [inline], [inherited]
12.237.4.5 isValid() bool carl::tree_detail::BaseIterator< T, LeafIterator< T, false > , reverse
>::isValid ( ) const [inline], [inherited]
```

```
12.237.4.6 next() template<typename T , bool reverse = false>
LeafIterator& carl::tree_detail::LeafIterator< T, reverse >::next () [inline]
\textbf{12.237.4.7} \quad \textbf{node()} \quad \texttt{const auto\& carl::tree\_detail::BaseIterator} < \texttt{T, LeafIterator} < \texttt{T, false} > \texttt{,}
reverse >::node (
             std::size_t id ) const [inline], [inherited]
12.237.4.8 nodes() const auto@ carl::tree_detail::BaseIterator< T, LeafIterator< T, false > ,
reverse >::nodes ( ) const [inline], [inherited]
12.237.4.9 operator->() [1/2] T* carl::tree_detail::BaseIterator< T, LeafIterator< T, false > ,
reverse >::operator-> ( ) [inline], [inherited]
12.237.4.10 operator->() [2/2] T const* carl::tree_detail::BaseIterator< T, LeafIterator< T,
false > , reverse >::operator-> ( ) const [inline], [inherited]
12.237.4.11 operator=() [1/2] template<typename T , bool reverse = false>
LeafIterator& carl::tree_detail::LeafIterator< T, reverse >::operator= (
            const LeafIterator< T, reverse > & it ) [inline]
12.237.4.12 operator=() [2/2] template<typename T , bool reverse = false>
LeafIterator& carl::tree_detail::LeafIterator< T, reverse >::operator= (
             LeafIterator< T, reverse > && it ) [inline]
12.237.4.13 previous() template<typename T , bool reverse = false>
LeafIterator& carl::tree_detail::LeafIterator< T, reverse >::previous ( ) [inline]
```

# 12.237.5 Field Documentation

```
12.237.5.1 current std::size_t carl::tree_detail::BaseIterator< T, LeafIterator< T, false > , reverse >::current [inherited]
```

```
12.237.5.2 mTree const tree<T>* carl::tree_detail::BaseIterator< T, LeafIterator< T, false > , reverse >::mTree [protected], [inherited]
```

# 12.238 carl::less< T, mayBeNull > Struct Template Reference

Alternative specialization of std::less for pointer types.

```
#include <pointerOperations.h>
```

#### **Public Member Functions**

bool operator() (const T &lhs, const T &rhs) const

#### **Data Fields**

std::less< T > \_less

## 12.238.1 Detailed Description

```
template<typename T, bool mayBeNull = true> struct carl::less< T, mayBeNull >
```

Alternative specialization of std::less for pointer types.

We consider two pointers equal, if they point to the same memory location or the objects they point to are equal. Note that the memory location may also be zero.

# 12.238.2 Member Function Documentation

## 12.238.3 Field Documentation

```
12.238.3.1 Less template<typename T , bool mayBeNull = true> std::less<T> carl::less< T, mayBeNull >::_less
```

# 12.239 std::less< carl::Monomial::Arg > Struct Reference

```
#include <Monomial.h>
```

### **Public Member Functions**

• bool operator() (const carl::Monomial::Arg &lhs, const carl::Monomial::Arg &rhs) const

#### 12.239.1 Member Function Documentation

# 12.240 std::less< carl::UnivariatePolynomial< Coefficient > > Struct Template Reference

Specialization of std::less for univariate polynomials.

```
#include <UnivariatePolynomial.h>
```

## **Public Member Functions**

- less (carl::PolynomialComparisonOrder \_order=carl::PolynomialComparisonOrder::Default) noexcept
- bool operator() (const carl::UnivariatePolynomial < Coefficient > &lhs, const carl::UnivariatePolynomial < Coefficient > &rhs) const

Compares two univariate polynomials.

bool operator() (const carl::UnivariatePolynomial < Coefficient > \*Ihs, const carl::UnivariatePolynomial < Coefficient > \*rhs) const

Compares two pointers to univariate polynomials.

bool operator() (const carl::UnivariatePolynomialPtr< Coefficient > &lhs, const carl::UnivariatePolynomialPtr<</li>
 Coefficient > &rhs) const

Compares two shared pointers to univariate polynomials.

#### **Data Fields**

· carl::PolynomialComparisonOrder order

## 12.240.1 Detailed Description

```
template<typename Coefficient> struct std::less< carl::UnivariatePolynomial< Coefficient > >
```

Specialization of std::less for univariate polynomials.

#### 12.240.2 Constructor & Destructor Documentation

#### 12.240.3 Member Function Documentation

Compares two univariate polynomials.

## **Parameters**

| lhs | First polynomial. |
|-----|-------------------|
| rhs | Second polynomial |

#### Returns

```
lhs < rhs.
```

Compares two pointers to univariate polynomials.

#### **Parameters**

| lhs | First polynomial. |
|-----|-------------------|
| rhs | Second polynomial |

#### Returns

lhs < rhs.

Compares two shared pointers to univariate polynomials.

#### **Parameters**

| lhs | First polynomial. |
|-----|-------------------|
| rhs | Second polynomial |

#### Returns

lhs < rhs.

## 12.240.4 Field Documentation

```
12.240.4.1 order template<typename Coefficient > carl::PolynomialComparisonOrder std::less< carl::UnivariatePolynomial< Coefficient > >::order
```

# 12.241 carl::less< std::shared\_ptr< T >, mayBeNull > Struct Template Reference

#include <pointerOperations.h>

## **Public Member Functions**

• bool operator() (const std::shared\_ptr< const T > &lhs, const std::shared\_ptr< const T > &rhs) const

# Data Fields

std::less< T > \_less

#### 12.241.1 Member Function Documentation

#### 12.241.2 Field Documentation

```
12.241.2.1 _less template<typename T , bool mayBeNull> std::less<T> carl::less< std::shared_ptr< T >, mayBeNull >::_less
```

# 12.242 carl::less< T \*, mayBeNull > Struct Template Reference

```
#include <pointerOperations.h>
```

## **Public Member Functions**

• bool operator() (const T \*Ihs, const T \*rhs) const

### **Data Fields**

std::less< T > \_less

## 12.242.1 Member Function Documentation

#### 12.242.2 Field Documentation

```
12.242.2.1 Less template<typename T , bool mayBeNull>std::less<T> carl::less< T *, mayBeNull>::.less
```

# 12.243 carl::pool::LocalPool< Content > Class Template Reference

```
#include <LocalPool.h>
```

#### **Public Member Functions**

- LocalPool (std::size\_t \_capacity=1000)
- ∼LocalPool ()
- template<typename Key >
   std::shared\_ptr< LocalPoolElementWrapper< Content >> add (std::shared\_ptr< LocalPool< Content >>
   pool, Key &&c)

#### **Protected Member Functions**

void free (const LocalPoolElementWrapper< Content > \*c)

#### 12.243.1 Constructor & Destructor Documentation

```
12.243.1.2 ~LocalPool() template<class Content > carl::pool::LocalPool< Content >::~LocalPool ( ) [inline]
```

## 12.243.2 Member Function Documentation

# 12.244 carl::pool::LocalPoolElement < Content > Class Template Reference

```
#include <LocalPool.h>
```

#### **Public Member Functions**

```
    template<typename Key >
        LocalPoolElement (std::shared_ptr< LocalPool</p>
        Content >> &pool, Key &&k)
```

- const Content & operator() () const
- const Content & operator\* () const
- const Content \* operator-> () const
- · auto id () const
- bool operator== (const LocalPoolElement &other) const

#### 12.244.1 Constructor & Destructor Documentation

# 12.244.2 Member Function Documentation

```
12.244.2.1 id() template<class Content >
auto carl::pool::LocalPoolElement< Content >::id ( ) const [inline]

12.244.2.2 operator()() template<class Content >
const Content& carl::pool::LocalPoolElement< Content >::operator() ( ) const [inline]

12.244.2.3 operator*() template<class Content >
const Content& carl::pool::LocalPoolElement< Content >::operator* ( ) const [inline]

12.244.2.4 operator->() template<class Content >
```

const Content\* carl::pool::LocalPoolElement< Content >::operator-> ( ) const [inline]

# 12.245 carl::pool::LocalPoolElementWrapper< Content > Class Template Reference

```
#include <LocalPool.h>
```

#### **Public Member Functions**

- template<typename ... Args>
   LocalPoolElementWrapper (std::shared\_ptr< LocalPool</p>
   Content >> pool, Args &&...args)
- ~LocalPoolElementWrapper ()
- const Content & content () const
- · auto id () const

#### 12.245.1 Constructor & Destructor Documentation

```
12.245.1.1 LocalPoolElementWrapper() template<class Content > template<typename ... Args> carl::pool::LocalPoolElementWrapper< Content >::LocalPoolElementWrapper ( std::shared_ptr< LocalPool< Content >> pool, Args &&... args ) [inline], [explicit]
```

```
12.245.1.2 ~LocalPoolElementWrapper() template<class Content > carl::pool::LocalPoolElementWrapper< Content >::~LocalPoolElementWrapper ( ) [inline]
```

## 12.245.2 Member Function Documentation

```
12.245.2.1 content() template < class Content > const Content & carl::pool::LocalPoolElementWrapper < Content >::content ( ) const [inline]
```

```
12.245.2.2 id() template<class Content >
auto carl::pool::LocalPoolElementWrapper< Content >::id ( ) const [inline]
```

# 12.246 carl::logging::Logger Class Reference

Main logger class.

```
#include <Logger.h>
```

## **Public Member Functions**

· bool has (const std::string &id) const noexcept

Check if a Sink with the given id has been installed.

void configure (const std::string &id, std::shared\_ptr< Sink > sink)

Installs the given sink.

void configure (const std::string &id, const std::string &filename)

Installs a FileSink.

void configure (const std::string &id, std::ostream &os)

Installs a StreamSink.

· Filter & filter (const std::string &id) noexcept

Retrieves the Filter for some Sink.

- const std::shared\_ptr< Formatter > & formatter (const std::string &id) noexcept

Retrieves the Formatter for some Sink.

void formatter (const std::string &id, std::shared\_ptr< Formatter > fmt) noexcept

Overwrites the Formatter for some Sink.

· void resetFormatter () noexcept

Reconfigures all Formatter objects.

bool visible (LogLevel level, const std::string &channel) const noexcept

Checks whether a log message would be visible for some sink.

void log (LogLevel level, const std::string &channel, const std::stringstream &ss, const RecordInfo &info)
 Logs a message.

#### **Static Public Member Functions**

• static Logger & getInstance ()

Returns the single instance of this class by reference.

## 12.246.1 Detailed Description

Main logger class.

## 12.246.2 Member Function Documentation

Installs a FileSink.

#### **Parameters**

| id       | Sink identifier.                 |  |
|----------|----------------------------------|--|
| filename | Filename passed to the FileSink. |  |

```
12.246.2.2 configure() [2/3] void carl::logging::Logger::configure ( const std::string & id, std::ostream & os) [inline]
```

Installs a StreamSink.

## **Parameters**

| id | Sink identifier.                        |
|----|---|
| os | Output stream passed to the StreamSink. |

```
12.246.2.3 configure() [3/3] void carl::logging::Logger::configure ( const std::string & id, std::shared.ptr< Sink > sink) [inline]
```

Installs the given sink.

If a Sink with this name is already present, it is overwritten.

## **Parameters**

| id   | Sink identifier. |
|------|------------------|
| sink | Sink.            |

```
12.246.2.4 filter() Filter& carl::logging::Logger::filter (
const std::string & id ) [inline], [noexcept]
```

Retrieves the Filter for some Sink.

## **Parameters**

id Sink identifier.

#### Returns

Filter.

Retrieves the Formatter for some Sink.

#### **Parameters**

```
id Sink identifier.
```

### Returns

Formatter.

```
12.246.2.6 formatter() [2/2] void carl::logging::Logger::formatter ( const std::string & id, std::shared_ptr< Formatter > fmt ) [inline], [noexcept]
```

Overwrites the Formatter for some Sink.

#### **Parameters**

| id  | Sink identifier. |  |
|-----|------------------|--|
| fmt | New Formatter.   |  |

```
12.246.2.7 getInstance() static Logger & carl::Singleton< Logger >::getInstance ( ) [inline], [static], [inherited]
```

Returns the single instance of this class by reference.

If there is no instance yet, a new one is created.

Check if a Sink with the given id has been installed.

## **Parameters**

```
id Sink identifier.
```

## Returns

If a Sink with this id is present.

Logs a message.

#### **Parameters**

| level   | LogLevel.              |
|---------|------------------------|
| channel | Channel name.          |
| ss      | Message to be logged.  |
| info    | Auxiliary information. |

```
12.246.2.10 resetFormatter() void carl::logging::Logger::resetFormatter ( ) [inline], [noexcept]
```

Reconfigures all Formatter objects.

This should be done once after all configuration is finished.

Checks whether a log message would be visible for some sink.

If this is not the case, we do not need to render it at all.

## **Parameters**

| level   | LogLevel.     |
|---------|---------------|
| channel | Channel name. |

# 12.247 carl::LowerBound< Number > Struct Template Reference

```
#include <Interval.h>
```

## **Data Fields**

- const Number & number
- BoundType bound\_type

## 12.247.1 Field Documentation

```
12.247.1.1 bound_type template<typename Number > BoundType carl::LowerBound< Number >::bound_type
```

```
12.247.1.2 number template<typename Number > const Number& carl::LowerBound< Number >::number
```

# 12.248 carl::io::MapleStream Class Reference

```
#include <MapleStream.h>
```

#### **Public Member Functions**

- MapleStream ()
- template<typename Pol > void assertFormula (const Formula < Pol > &formula)
- template<typename T >
   MapleStream & operator<< (T &&t)</li>
- MapleStream & operator<< (std::ostream &(\*os)(std::ostream &))</li>
- auto content () const

## 12.248.1 Constructor & Destructor Documentation

```
12.248.1.1 MapleStream() carl::io::MapleStream::MapleStream ( ) [inline]
```

#### 12.248.2 Member Function Documentation

```
12.248.2.2 content() auto carl::io::MapleStream::content ( ) const [inline]
```

```
12.248.2.3 operator << () [1/2] MapleStream& carl::io::MapleStream::operator << ( std::ostream &(*) (std::ostream &) os ) [inline]
```

```
12.248.2.4 operator << [2/2] template < typename T > MapleStream& carl::io::MapleStream::operator << (

T && t ) [inline]
```

# 12.249 carl::settings::metric\_quantity Struct Reference

Helper type to parse quantities with SI-style suffixes.

```
#include <settings_utils.h>
```

#### **Public Member Functions**

- constexpr metric\_quantity ()=default
- constexpr metric\_quantity (std::size\_t n)
- constexpr auto n () const
- · constexpr auto kilo () const
- constexpr auto mega () const
- constexpr auto giga () const
- · constexpr auto tera () const
- constexpr auto peta () const
- constexpr auto exa () const

## 12.249.1 Detailed Description

Helper type to parse quantities with SI-style suffixes.

Intended usage:

- · use boost to parse values as quantity
- access values with q.mega()

## 12.249.2 Constructor & Destructor Documentation

#### 12.249.3 Member Function Documentation

```
12.249.3.1 exa() constexpr auto carl::settings::metric_quantity::exa () const [inline], [constexpr]
12.249.3.2 giga() constexpr auto carl::settings::metric_quantity::giga ( ) const [inline],
[constexpr]
12.249.3.3 kilo() constexpr auto carl::settings::metric_quantity::kilo ( ) const [inline],
[constexpr]
12.249.3.4 mega() constexpr auto carl::settings::metric_quantity::mega ( ) const [inline],
[constexpr]
12.249.3.5 n() constexpr auto carl::settings::metric_quantity::n ( ) const [inline], [constexpr]
12.249.3.6 peta() constexpr auto carl::settings::metric_quantity::peta () const [inline],
[constexpr]
12.249.3.7 tera() constexpr auto carl::settings::metric_quantity::tera ( ) const [inline],
[constexpr]
```

# 12.250 carl::Model < Rational, Poly > Class Template Reference

Represent a collection of assignments/mappings from variables to values.

```
#include <Model.h>
```

## **Public Types**

- using key\_type = ModelVariable
- using mapped\_type = ModelValue< Rational, Poly >
- using Map = std::map< key\_type, mapped\_type >

#### **Public Member Functions**

- const auto & at (const key\_type &key) const
- auto begin () const
- · auto end () const
- auto empty () const
- · auto size () const
- void clear ()
- template<typename P >
   auto insert (const P &pair)
- template<typename P >

auto insert (typename Map::const\_iterator it, const P &pair)

template<typename... Args>
 auto emplace (const key\_type &key, Args &&...args)

template < typename... Args >
 auto emplace\_hint (typename Map::const\_iterator it, const key\_type &key, Args &&...args)

- Map::iterator erase (const ModelVariable &variable)
- Map::iterator erase (const typename Map::iterator &it)
- Map::iterator erase (const typename Map::const\_iterator &it)
- void clean ()
- auto find (const typename Map::key\_type &key) const
- auto find (const typename Map::key\_type &key)
- Model ()=default
- Model (const std::map < Variable, Rational > &assignment)
- template<typename Container >
  bool contains (const Container &c) const
- template<typename T >
   void assign (const typename Map::key\_type &key, const T &t)
- void update (const Model &model, bool disjoint=true)

Return the ModelValue for the given key, evaluated if it's a ModelSubstitution and evaluatable, otherwise return it raw.

- void print (std::ostream &os, bool simple=true) const
- void printOneline (std::ostream &os, bool simple=false) const

## 12.250.1 Detailed Description

```
template<typename Rational, typename Poly> class carl::Model< Rational, Poly >
```

Represent a collection of assignments/mappings from variables to values.

We use a ModelVariable to abstract over the different kinds of variables in CARL, and a ModelValue to abstract over the different kinds of values for these variables. Most notably, a value can be a "carl::ModelSubstitution" whose value depends on the values of other variables in the Model.

#### 12.250.2 Member Typedef Documentation

```
12.250.2.1 key_type template<typename Rational , typename Poly > using carl::Model< Rational, Poly >::key_type = ModelVariable
```

```
12.250.2.2 Map template<typename Rational , typename Poly >
using carl::Model< Rational, Poly >::Map = std::map<key_type,mapped_type>
12.250.2.3 mapped_type template<typename Rational , typename Poly >
using carl::Model< Rational, Poly >::mapped.type = ModelValue<Rational,Poly>
12.250.3 Constructor & Destructor Documentation
12.250.3.1 Model() [1/2] template<typename Rational , typename Poly >
carl::Model< Rational, Poly >::Model ( ) [default]
12.250.3.2 Model() [2/2] template<typename Rational , typename Poly >
carl::Model< Rational, Poly >::Model (
            const std::map< Variable, Rational > & assignment ) [inline]
12.250.4 Member Function Documentation
12.250.4.1 assign() template<typename Rational , typename Poly >
template<typename T >
void carl::Model< Rational, Poly >::assign (
            const typename Map::key_type & key,
            const T & t ) [inline]
12.250.4.2 at() template<typename Rational , typename Poly >
const auto& carl::Model< Rational, Poly >::at (
            const key_type & key ) const [inline]
12.250.4.3 begin() template<typename Rational , typename Poly >
```

auto carl::Model< Rational, Poly >::begin ( ) const [inline]

```
12.250.4.4 clean() template<typename Rational , typename Poly >
void carl::Model< Rational, Poly >::clean ( ) [inline]
12.250.4.5 clear() template<typename Rational , typename Poly >
void carl::Model< Rational, Poly >::clear ( ) [inline]
12.250.4.6 contains() template<typename Rational , typename Poly >
template<typename Container >
bool carl::Model< Rational, Poly >::contains (
            const Container & c ) const [inline]
12.250.4.7 emplace() template<typename Rational , typename Poly >
template<typename... Args>
auto carl::Model< Rational, Poly >::emplace (
            const key_type & key,
            Args &&... args ) [inline]
12.250.4.8 emplace_hint() template<typename Rational , typename Poly >
template<typename... Args>
auto carl::Model< Rational, Poly >::emplace_hint (
            typename Map::const_iterator it,
            const key_type & key,
            Args &&... args ) [inline]
12.250.4.9 empty() template<typename Rational , typename Poly >
auto carl::Model< Rational, Poly >::empty ( ) const [inline]
12.250.4.10 end() template<typename Rational , typename Poly >
auto carl::Model< Rational, Poly >::end ( ) const [inline]
12.250.4.11 erase() [1/3] template<typename Rational , typename Poly >
Map::iterator carl::Model< Rational, Poly >::erase (
            const ModelVariable & variable ) [inline]
```

Return the ModelValue for the given key, evaluated if it's a ModelSubstitution and evaluatable, otherwise return it raw.

#### **Parameters**

key The model must contain an assignment with the given key.

```
12.250.4.19 print() template<typename Rational , typename Poly >
void carl::Model< Rational, Poly >::print (
    std::ostream & os,
    bool simple = true ) const [inline]

12.250.4.20 printOneline() template<typename Rational , typename Poly >
void carl::Model< Rational, Poly >::printOneline (
    std::ostream & os,
    bool simple = false ) const [inline]

12.250.4.21 size() template<typename Rational , typename Poly >
auto carl::Model< Rational, Poly >::size ( ) const [inline]

12.250.4.22 update() template<typename Rational , typename Poly >
void carl::Model< Rational, Poly >::update (
    const Model< Rational, Poly > ::update (
    const Model< Rational, Poly > & model,
    bool disjoint = true ) [inline]
```

# 12.251 carl::ModelConditionalSubstitution < Rational, Poly > Class Template Reference

#include <ModelConditionalSubstitution.h>

## **Public Member Functions**

- ModelConditionalSubstitution (const std::vector< std::pair< Formula< Poly >, ModelValue< Rational, Poly >>> &values)
- ModelConditionalSubstitution (std::initializer\_list< std::pair< Formula< Poly >, ModelValue< Rational, Poly >>> values)
- virtual void multiplyBy (const Rational &n)

Multiply this model substitution by a rational.

virtual void add (const Rational &n)

Add a rational to this model substitution.

virtual ModelSubstitutionPtr< Rational, Poly > clone () const

Create a copy of this model substitution.

- virtual Formula < Poly > representingFormula (const ModelVariable &mv)
- virtual ModelValue < Rational, Poly > evaluateSubstitution (const Model < Rational, Poly > &model) const
   Evaluate this substitution with respect to the given model.
- virtual bool dependsOn (const ModelVariable &var) const

Check if this substitution needs the given model variable.

virtual void print (std::ostream &os) const

Print this substitution to the given output stream.

- const ModelValue< Rational, Poly > & evaluate (const Model< Rational, Poly > &model) const
- void resetCache () const
- template<typename Iterator >
   const ModelValue< Rational, Poly > & getModelValue (Iterator \_mvit, Model< Rational, Poly > &\_model)

#### 12.251.1 Constructor & Destructor Documentation

```
12.251.1.2 ModelConditionalSubstitution() [2/2] template<typename Rational, typename Poly > carl::ModelConditionalSubstitution< Rational, Poly >::ModelConditionalSubstitution ( std::initializer_list< std::pair< Formula< Poly >, ModelValue< Rational, Poly >>> values ) [inline]
```

#### 12.251.2 Member Function Documentation

Add a rational to this model substitution.

 $Implements\ carl:: Model Substitution < Rational,\ Poly>.$ 

```
12.251.2.2 clone() template<typename Rational , typename Poly >
virtual ModelSubstitutionPtr<Rational,Poly> carl::ModelConditionalSubstitution
Rational,
Poly >::clone ( ) const [inline], [virtual]
```

Create a copy of this model substitution.

Implements carl::ModelSubstitution< Rational, Poly >.

Check if this substitution needs the given model variable.

Reimplemented from carl::ModelSubstitution< Rational, Poly >.

```
12.251.2.4 evaluate() template<typename Rational , typename Poly >
const ModelValue<Rational, Poly>& carl::ModelSubstitution< Rational, Poly >::evaluate (
           12.251.2.5 evaluateSubstitution() template<typename Rational , typename Poly >
::evaluateSubstitution (
           Evaluate this substitution with respect to the given model.
Implements carl::ModelSubstitution< Rational, Poly >.
12.251.2.6 getModelValue() template<typename Rational , typename Poly >
template<typename Iterator >
\verb|const| ModelValue| < Rational, Poly>& carl:: ModelSubstitution| < Rational, Poly>:: getModelValue| (
           Iterator _mvit,
           Model< Rational, Poly > & _model ) [inline], [inherited]
12.251.2.7 multiplyBy() template<typename Rational , typename Poly >
virtual void carl::ModelConditionalSubstitution< Rational, Poly >::multiplyBy (
            const Rational & _number ) [inline], [virtual]
Multiply this model substitution by a rational.
Implements carl::ModelSubstitution < Rational, Poly >.
12.251.2.8 print() template<typename Rational , typename Poly >
virtual void carl::ModelConditionalSubstitution< Rational, Poly >::print (
           std::ostream & os ) const [inline], [virtual]
Print this substitution to the given output stream.
Reimplemented from carl::ModelSubstitution < Rational, Poly >.
12.251.2.9 representingFormula() template<typename Rational , typename Poly >
virtual Formula<Poly> carl::ModelConditionalSubstitution< Rational, Poly >::representing←
Formula (
           const ModelVariable & mv ) [inline], [virtual]
Implements carl::ModelSubstitution< Rational, Poly >.
```

```
12.251.2.10 resetCache() template<typename Rational , typename Poly > void carl::ModelSubstitution< Rational, Poly >::resetCache () const [inline], [inherited]
```

# 12.252 carl::ModelFormulaSubstitution < Rational, Poly > Class Template Reference

#include <ModelFormulaSubstitution.h>

#### **Public Member Functions**

- ModelFormulaSubstitution (const Formula < Poly > &f)
- virtual void multiplyBy (const Rational &)

Multiply this model substitution by a rational.

· virtual void add (const Rational &)

Add a rational to this model substitution.

virtual ModelSubstitutionPtr< Rational, Poly > clone () const

Create a copy of this model substitution.

- virtual Formula < Poly > representingFormula (const ModelVariable &mv)
- virtual ModelValue < Rational, Poly > evaluateSubstitution (const Model < Rational, Poly > &m) const Evaluate this substitution with respect to the given model.
- virtual bool dependsOn (const ModelVariable &var) const

Check if this substitution needs the given model variable.

· virtual void print (std::ostream &os) const

Print this substitution to the given output stream.

- const Formula < Poly > & getFormula () const
- const ModelValue< Rational, Poly > & evaluate (const Model< Rational, Poly > &model) const
- void resetCache () const
- template<typename Iterator >
   const ModelValue< Rational, Poly > & getModelValue (Iterator \_mvit, Model< Rational, Poly > &\_model)

#### 12.252.1 Constructor & Destructor Documentation

```
12.252.1.1 ModelFormulaSubstitution() template<typename Rational , typename Poly > carl::ModelFormulaSubstitution< Rational, Poly >::ModelFormulaSubstitution ( const Formula< Poly > & f) [inline]
```

# 12.252.2 Member Function Documentation

Add a rational to this model substitution.

Implements carl::ModelSubstitution< Rational, Poly >.

```
12.252.2.2 clone() template<typename Rational, typename Poly >
virtual ModelSubstitutionPtr<Rational,Poly> carl::ModelFormulaSubstitution
Rational, Poly
>::clone ( ) const [inline], [virtual]
```

Create a copy of this model substitution.

 $Implements\ carl:: Model Substitution < Rational,\ Poly>.$ 

Check if this substitution needs the given model variable.

Reimplemented from carl::ModelSubstitution< Rational, Poly >.

```
12.252.2.5 evaluateSubstitution() template<typename Rational, typename Poly > virtual ModelValue<Rational, Poly > carl::ModelFormulaSubstitution< Rational, Poly >::evaluate← Substitution (

const Model< Rational, Poly > & model ) const [inline], [virtual]
```

Evaluate this substitution with respect to the given model.

Implements carl::ModelSubstitution < Rational, Poly >.

```
12.252.2.6 getFormula() template<typename Rational , typename Poly > const Formula<Poly>& carl::ModelFormulaSubstitution< Rational, Poly >::getFormula ( ) const [inline]
```

```
12.252.2.8 multiplyBy() template<typename Rational , typename Poly > virtual void carl::ModelFormulaSubstitution< Rational, Poly >::multiplyBy ( const Rational & _number ) [inline], [virtual]

Multiply this model substitution by a rational.

Implements carl::ModelSubstitution< Rational, Poly >.
```

Print this substitution to the given output stream.

Reimplemented from carl::ModelSubstitution< Rational, Poly >.

```
12.252.2.11 resetCache() template<typename Rational , typename Poly > void carl::ModelSubstitution< Rational, Poly >::resetCache () const [inline], [inherited]
```

# 12.253 carl::ModelMVRootSubstitution< Rational, Poly > Class Template Reference

#include <ModelMVRootSubstitution.h>

## **Public Types**

using MVRoot = MultivariateRoot< Poly >

#### **Public Member Functions**

- ModelMVRootSubstitution (const MVRoot &r)
- virtual void multiplyBy (const Rational &)

Multiply this model substitution by a rational.

· virtual void add (const Rational &)

Add a rational to this model substitution.

• virtual ModelSubstitutionPtr< Rational, Poly > clone () const

Create a copy of this model substitution.

- virtual Formula < Poly > representingFormula (const ModelVariable &mv)
- $\bullet \ \ \mathsf{virtual} \ \ \mathsf{ModelValue} < \ \mathsf{Rational}, \ \mathsf{Poly} > \mathsf{evaluateSubstitution} \ \ (\mathsf{const} \ \ \mathsf{Model} < \ \mathsf{Rational}, \ \mathsf{Poly} > \&\mathsf{m}) \ \ \mathsf{const}$

Evaluate this substitution with respect to the given model.

virtual bool dependsOn (const ModelVariable &var) const

Check if this substitution needs the given model variable.

virtual void print (std::ostream &os) const

Print this substitution to the given output stream.

- const ModelValue < Rational, Poly > & evaluate (const Model < Rational, Poly > & model) const
- void resetCache () const
- template<typename Iterator >

 $const\ Model Value < \ Rational,\ Poly > \&\ get Model Value\ (Iterator\ \_mvit,\ Model < Rational,\ Poly > \&\_model)$ 

## 12.253.1 Member Typedef Documentation

```
12.253.1.1 MVRoot template<typename Rational , typename Poly > using carl::ModelMVRootSubstitution< Rational, Poly >::MVRoot = MultivariateRoot<Poly>
```

#### 12.253.2 Constructor & Destructor Documentation

```
12.253.2.1 ModelMVRootSubstitution() template<typename Rational , typename Poly > carl::ModelMVRootSubstitution < Rational, Poly >::ModelMVRootSubstitution ( const MVRoot & r ) [inline]
```

#### 12.253.3 Member Function Documentation

Add a rational to this model substitution.

Implements carl::ModelSubstitution< Rational, Poly >.

```
12.253.3.2 clone() template<typename Rational, typename Poly > virtual ModelSubstitutionPtr<Rational,Poly> carl::ModelMVRootSubstitution
Rational, Poly > ↔ ::clone () const [inline], [virtual]
```

Create a copy of this model substitution.

Implements carl::ModelSubstitution< Rational, Poly >.

```
12.253.3.3 dependsOn() template<typename Rational , typename Poly > virtual bool carl::ModelMVRootSubstitution< Rational, Poly >::dependsOn ( const ModelVariable & ) const [inline], [virtual]
```

Check if this substitution needs the given model variable.

Reimplemented from carl::ModelSubstitution< Rational, Poly >.

```
12.253.3.4 evaluate() template<typename Rational , typename Poly >
const ModelValue<Rational, Poly>& carl::ModelSubstitution< Rational, Poly >::evaluate (
                              const Model< Rational, Poly > & model ) const [inline], [inherited]
12.253.3.5 evaluateSubstitution() template<typename Rational , typename Poly >
\verb|virtual ModelValue| < Rational, Poly > \verb|carl::ModelMVRootSubstitution| < Rational, Poly > ::evaluate \leftrightarrow | Construction | Construction| < Construction | 
Substitution (
                              const Model< Rational, Poly > & model ) const [inline], [virtual]
Evaluate this substitution with respect to the given model.
Implements carl::ModelSubstitution < Rational, Poly >.
12.253.3.6 getModelValue() template<typename Rational , typename Poly >
template<typename Iterator >
\verb|const| ModelValue| < Rational, Poly>& carl:: ModelSubstitution| < Rational, Poly>:: getModelValue| (
                             Iterator _mvit,
                             Model< Rational, Poly > & _model ) [inline], [inherited]
12.253.3.7 multiplyBy() template<typename Rational , typename Poly >
virtual void carl::ModelMVRootSubstitution< Rational, Poly >::multiplyBy (
                              const Rational & _number ) [inline], [virtual]
Multiply this model substitution by a rational.
Implements carl::ModelSubstitution< Rational, Poly >.
12.253.3.8 print() template<typename Rational , typename Poly >
virtual void carl::ModelMVRootSubstitution< Rational, Poly >::print (
                              std::ostream & os ) const [inline], [virtual]
Print this substitution to the given output stream.
Reimplemented from carl::ModelSubstitution< Rational, Poly >.
12.253.3.9 representingFormula() template<typename Rational , typename Poly >
virtual Formula<Poly> carl::ModelMVRootSubstitution< Rational, Poly>::representingFormula (
```

Implements carl::ModelSubstitution< Rational, Poly >.

const ModelVariable & mv ) [inline], [virtual]

```
12.253.3.10 resetCache() template<typename Rational , typename Poly > void carl::ModelSubstitution< Rational, Poly >::resetCache () const [inline], [inherited]
```

# 12.254 carl::ModelPolynomialSubstitution < Rational, Poly > Class Template Reference

#include <ModelPolynomialSubstitution.h>

#### **Public Member Functions**

- ModelPolynomialSubstitution (const Poly &p)
- · const auto & getPoly () const
- virtual void multiplyBy (const Rational &n)

Multiply this model substitution by a rational.

· virtual void add (const Rational &n)

Add a rational to this model substitution.

virtual ModelSubstitutionPtr< Rational, Poly > clone () const

Create a copy of this model substitution.

- virtual Formula < Poly > representingFormula (const ModelVariable &mv)
- virtual ModelValue < Rational, Poly > evaluateSubstitution (const Model < Rational, Poly > &m) const Evaluate this substitution with respect to the given model.
- virtual bool dependsOn (const ModelVariable &var) const

Check if this substitution needs the given model variable.

virtual void print (std::ostream &os) const

Print this substitution to the given output stream.

- const ModelValue< Rational, Poly > & evaluate (const Model< Rational, Poly > & model) const
- void resetCache () const
- template<typename Iterator >
   const ModelValue< Rational, Poly > & getModelValue (Iterator \_mvit, Model< Rational, Poly > &\_model)

#### 12.254.1 Constructor & Destructor Documentation

```
12.254.1.1 ModelPolynomialSubstitution() template<typename Rational , typename Poly > carl::ModelPolynomialSubstitution
    Rational , Poly >::ModelPolynomialSubstitution ( const Poly & p) [inline]
```

## 12.254.2 Member Function Documentation

Add a rational to this model substitution.

Implements carl::ModelSubstitution< Rational, Poly >.

```
12.254.2.2 clone() template<typename Rational , typename Poly >
virtual ModelSubstitutionPtr<Rational,Poly> carl::ModelPolynomialSubstitution
Rational, Poly
>::clone () const [inline], [virtual]
```

Create a copy of this model substitution.

Implements carl::ModelSubstitution < Rational, Poly >.

```
12.254.2.3 dependsOn() template<typename Rational , typename Poly > virtual bool carl::ModelPolynomialSubstitution< Rational, Poly >::dependsOn ( const ModelVariable & ) const [inline], [virtual]
```

Check if this substitution needs the given model variable.

Reimplemented from carl::ModelSubstitution< Rational, Poly >.

```
12.254.2.5 evaluateSubstitution() template<typename Rational , typename Poly > virtual ModelValue<Rational,Poly> carl::ModelPolynomialSubstitution< Rational, Poly >::evaluate← Substitution (

const Model< Rational, Poly > & model ) const [inline], [virtual]
```

Evaluate this substitution with respect to the given model.

Implements carl::ModelSubstitution < Rational, Poly >.

```
12.254.2.7 getPoly() template<typename Rational , typename Poly > const auto& carl::ModelPolynomialSubstitution< Rational, Poly >::getPoly ( ) const [inline]
```

Multiply this model substitution by a rational.

 $Implements\ carl:: Model Substitution < Rational,\ Poly>.$ 

Print this substitution to the given output stream.

Reimplemented from carl::ModelSubstitution< Rational, Poly >.

Implements carl::ModelSubstitution< Rational, Poly >.

```
12.254.2.11 resetCache() template<typename Rational , typename Poly > void carl::ModelSubstitution< Rational, Poly >::resetCache () const [inline], [inherited]
```

# 12.255 carl::ModelSubstitution < Rational, Poly > Class Template Reference

Represent a expression for a ModelValue with variables as placeholders, where the final expression's value depends on the bindings/values of these variables.

```
#include <ModelSubstitution.h>
```

#### **Public Member Functions**

- ModelSubstitution ()=default
- virtual ~ModelSubstitution () noexcept=default
- void resetCache () const
- virtual bool dependsOn (const ModelVariable &) const

Check if this substitution needs the given model variable.

· virtual void print (std::ostream &os) const

Print this substitution to the given output stream.

virtual void multiplyBy (const Rational &\_number)=0

Multiply this model substitution by a rational.

virtual void add (const Rational &\_number)=0

Add a rational to this model substitution.

virtual ModelSubstitutionPtr< Rational, Poly > clone () const =0

Create a copy of this model substitution.

- virtual Formula < Poly > representingFormula (const ModelVariable &mv)=0
- template<typename Iterator >

 $const\ Model Value < Rational,\ Poly > \&\ get Model Value\ (Iterator\ \_mvit,\ Model < Rational,\ Poly > \&\_model)$ 

#### **Protected Member Functions**

virtual ModelValue< Rational, Poly > evaluateSubstitution (const Model< Rational, Poly > &model) const
 =0

Evaluate this substitution with respect to the given model.

#### 12.255.1 Detailed Description

```
template<typename Rational, typename Poly> class carl::ModelSubstitution< Rational, Poly>
```

Represent a expression for a ModelValue with variables as placeholders, where the final expression's value depends on the bindings/values of these variables.

The values are given in the (abstract) form of a "carl::Model".

#### 12.255.2 Constructor & Destructor Documentation

```
12.255.2.1 ModelSubstitution() template<typename Rational , typename Poly > carl::ModelSubstitution< Rational, Poly >::ModelSubstitution () [default]
```

```
12.255.2.2 ~ModelSubstitution() template<typename Rational, typename Poly > virtual carl::ModelSubstitution< Rational, Poly >::~ModelSubstitution () [virtual], [default], [noexcept]
```

## 12.255.3 Member Function Documentation

Add a rational to this model substitution.

Implemented in carl::ModelPolynomialSubstitution< Rational, Poly >, carl::ModelConditionalSubstitution< Rational, Poly >, carl::ModelMVRootSubstitution< Rational, Poly >, and carl::ModelFormulaSubstitution< Rational, Poly >.

```
12.255.3.2 clone() template<typename Rational , typename Poly >
virtual ModelSubstitutionPtr<Rational,Poly> carl::ModelSubstitution
( ) const [pure virtual]
```

Create a copy of this model substitution.

Implemented in carl::ModelPolynomialSubstitution< Rational, Poly >, carl::ModelMVRootSubstitution< Rational, Poly >, carl::ModelFormulaSubstitution< Rational, Poly >, and carl::ModelConditionalSubstitution< Rational, Poly >.

```
12.255.3.3 dependsOn() template<typename Rational , typename Poly > virtual bool carl::ModelSubstitution< Rational, Poly >::dependsOn ( const ModelVariable & ) const [inline], [virtual]
```

Check if this substitution needs the given model variable.

 $Reimplemented \ in \ carl:: Model Polynomial Substitution < Rational, \ Poly>, \ carl:: Model MVRoot Substitution < Rational, \ Poly>, \ carl:: Model Formula Substitution < Rational, \ Poly>, \ and \ carl:: Model Conditional Substitution < Rational, \ Poly>.$ 

```
12.255.3.4 evaluate() template<typename Rational , typename Poly > const ModelValue<Rational, Poly>& carl::ModelSubstitution< Rational, Poly >::evaluate ( const Model< Rational, Poly > & model ) const [inline]
```

```
12.255.3.5 evaluateSubstitution() template<typename Rational, typename Poly > virtual ModelValue<Rational, Poly> carl::ModelSubstitution< Rational, Poly >::evaluate ← Substitution (

const Model< Rational, Poly > & model ) const [protected], [pure virtual]
```

Evaluate this substitution with respect to the given model.

Implemented in carl::ModelConditionalSubstitution< Rational, Poly >, carl::ModelPolynomialSubstitution< Rational, Poly >, carl::ModelMVRootSubstitution< Rational, Poly >, and carl::ModelFormulaSubstitution< Rational, Poly >.

Multiply this model substitution by a rational.

 $Implemented \ in \ carl:: Model Polynomial Substitution < Rational, \ Poly >, \ carl:: Model Conditional Substitution < Rational, \ Poly >, \ carl:: Model MVRoot Substitution < Rational, \ Poly >, \ and \ carl:: Model Formula Substitution < Rational, \ Poly >.$ 

Print this substitution to the given output stream.

 $Reimplemented \ in \ carl:: Model Polynomial Substitution < Rational, \ Poly>, \ carl:: Model MVRoot Substitution < Rational, \ Poly>, \ carl:: Model Formula Substitution < Rational, \ Poly>, \ and \ carl:: Model Conditional Substitution < Rational, \ Poly>.$ 

```
12.255.3.9 representingFormula() template<typename Rational , typename Poly > virtual Formula<Poly> carl::ModelSubstitution< Rational, Poly >::representingFormula ( const ModelVariable & mv ) [pure virtual]
```

 $Implemented\ in\ carl:: Model Polynomial Substitution < Rational,\ Poly>,\ carl:: Model MVRoot Substitution < Rational,\ Poly>,\ carl:: Model Formula Substitution < Rational,\ Poly>,\ and\ carl:: Model Conditional Substitution < Rational,\ Poly>.$ 

```
12.255.3.10 resetCache() template<typename Rational , typename Poly > void carl::ModelSubstitution
    Rational , Poly >::resetCache ( ) const [inline]
```

# 12.256 carl::ModelValue < Rational, Poly > Class Template Reference

Represent a sum type/variant over the different kinds of values that can be assigned to the different kinds of variables that exist in CARL and to use them in a more uniform way, e.g.

```
#include <ModelValue.h>
```

#### **Public Member Functions**

• ModelValue ()=default

Default constructor.

- ModelValue (const ModelValue &mv)
- ModelValue (ModelValue &&mv)=default
- template<typename T, typename T2 = typename std::enable\_if<convertible\_to\_variant<T, Super>::value, T>::type>
   ModelValue (const T &\_t)

Initialize the Assignment from some valid type of the underlying variant.

- template<typename T, typename T2 = typename std::enable\_if<convertible\_to\_variant<T, Super>::value, T>::type>
  ModelValue (T &&.t)
- template<typename ... Args>

ModelValue (const std::variant < Args... > &variant)

- ModelValue (const MultivariateRoot< Poly > &mr)
- ModelValue & operator= (const ModelValue &mv)
- ModelValue & operator= (ModelValue &&mv)=default
- template<typename T >

ModelValue & operator= (const T &t)

Assign some value to the underlying variant.

- template<typename ... Args>
  - ModelValue & operator= (const std::variant< Args... > &variant)
- ModelValue & operator= (const MultivariateRoot< Poly > &mr)
- template<typename F > auto visit (F &&f) const
- bool isBool () const
- bool isRational () const
- bool isSqrtEx () const
- · bool isRAN () const
- bool isBVValue () const
- bool isSortValue () const
- bool isUFModel () const
- bool isPlusInfinity () const
- bool isMinusInfinity () const
- bool isSubstitution () const
- bool asBool () const
- const Rational & asRational () const
- const SqrtEx< Poly > & asSqrtEx () const
- const Poly::RootType & asRAN () const
- const carl::BVValue & asBVValue () const
- · const SortValue & asSortValue () const
- const UFModel & asUFModel () const
- UFModel & asUFModel ()
- const InfinityValue & asInfinity () const
- const ModelSubstitutionPtr< Rational, Poly > & asSubstitution () const
- ModelSubstitutionPtr< Rational, Poly > & asSubstitution ()

## **Friends**

- template<typename R, typename P >
   std::ostream & operator<< (std::ostream &os, const ModelValue< R, P > &mv)
- template<typename R , typename P > bool operator== (const ModelValue< R, P > &Ihs, const ModelValue< R, P > &rhs)
- template < typename R, typename P >
   bool operator < (const ModelValue < R, P > &Ihs, const ModelValue < R, P > &rhs)

# 12.256.1 Detailed Description

```
template<typename Rational, typename Poly> class carl::ModelValue< Rational, Poly >
```

Represent a sum type/variant over the different kinds of values that can be assigned to the different kinds of variables that exist in CARL and to use them in a more uniform way, e.g.

a plain "bool", "infinity", a "carl::RealAlgebraicNumber", a (bitvector) "carl::BVValue" etc.

## 12.256.2 Constructor & Destructor Documentation

Default constructor.

Initialize the Assignment from some valid type of the underlying variant.

## 12.256.3 Member Function Documentation

```
12.256.3.1 asBool() template<typename Rational , typename Poly > bool carl::ModelValue< Rational, Poly >::asBool () const [inline]
```

#### Returns

The stored value as a bool.

```
12.256.3.2 asBVValue() template<typename Rational , typename Poly > const carl::BVValue& carl::ModelValue< Rational, Poly >::asBVValue ( ) const [inline]
```

# Returns

The stored value as a real algebraic number.

```
12.256.3.3 asInfinity() template<typename Rational , typename Poly > const InfinityValue& carl::ModelValue< Rational, Poly >::asInfinity ( ) const [inline]
```

#### Returns

The stored value as a infinity value.

```
12.256.3.4 asRAN() template<typename Rational , typename Poly > const Poly::RootType& carl::ModelValue< Rational, Poly >::asRAN ( ) const [inline]
```

#### Returns

The stored value as a real algebraic number.

```
12.256.3.5 asRational() template<typename Rational , typename Poly > const Rational& carl::ModelValue< Rational, Poly >::asRational () const [inline]
```

The stored value as a rational.

```
12.256.3.6 asSortValue() template<typename Rational , typename Poly > const SortValue& carl::ModelValue< Rational, Poly >::asSortValue () const [inline]
```

#### Returns

The stored value as a sort value.

```
12.256.3.7 asSqrtEx() template<typename Rational , typename Poly > const SqrtEx<Poly>& carl::ModelValue< Rational, Poly >::asSqrtEx ( ) const [inline]
```

#### Returns

The stored value as a square root expression.

```
12.256.3.8 asSubstitution() [1/2] template<typename Rational , typename Poly > ModelSubstitutionPtr<Rational,Poly>& carl::ModelValue< Rational, Poly >::asSubstitution ( ) [inline]
```

```
12.256.3.9 asSubstitution() [2/2] template<typename Rational, typename Poly > const ModelSubstitutionPtr<Rational,Poly>& carl::ModelValue< Rational, Poly >::asSubstitution ( ) const [inline]
```

```
12.256.3.10 asUFModel() [1/2] template<typename Rational , typename Poly > UFModel& carl::ModelValue< Rational, Poly >::asUFModel ( ) [inline]
```

```
12.256.3.11 asUFModel() [2/2] template<typename Rational , typename Poly > const UFModel& carl::ModelValue< Rational, Poly >::asUFModel () const [inline]
```

# Returns

The stored value as a uninterpreted function model.

```
12.256.3.12 isBool() template<typename Rational , typename Poly > bool carl::ModelValue< Rational, Poly >::isBool () const [inline]
```

true, if the stored value is a bool.

```
12.256.3.13 isBVValue() template<typename Rational , typename Poly > bool carl::ModelValue< Rational, Poly >::isBVValue () const [inline]
```

#### Returns

true, if the stored value is a bitvector literal.

```
12.256.3.14 isMinusInfinity() template<typename Rational , typename Poly > bool carl::ModelValue< Rational, Poly >::isMinusInfinity ( ) const [inline]
```

#### Returns

true, if the stored value is -infinity.

```
12.256.3.15 isPlusInfinity() template<typename Rational , typename Poly > bool carl::ModelValue< Rational, Poly >::isPlusInfinity ( ) const [inline]
```

# Returns

true, if the stored value is +infinity.

```
12.256.3.16 isRAN() template<typename Rational , typename Poly > bool carl::ModelValue< Rational, Poly >::isRAN ( ) const [inline]
```

## Returns

true, if the stored value is a real algebraic number.

```
12.256.3.17 isRational() template<typename Rational , typename Poly > bool carl::ModelValue< Rational, Poly >::isRational () const [inline]
```

true, if the stored value is a rational.

```
12.256.3.18 isSortValue() template<typename Rational , typename Poly > bool carl::ModelValue< Rational, Poly >::isSortValue () const [inline]
```

## Returns

true, if the stored value is a sort value.

```
12.256.3.19 isSqrtEx() template<typename Rational , typename Poly > bool carl::ModelValue< Rational, Poly >::isSqrtEx () const [inline]
```

#### Returns

true, if the stored value is a square root expression.

```
12.256.3.20 isSubstitution() template<typename Rational , typename Poly > bool carl::ModelValue< Rational, Poly >::isSubstitution () const [inline]
```

```
12.256.3.21 isUFModel() template<typename Rational , typename Poly > bool carl::ModelValue< Rational, Poly >::isUFModel () const [inline]
```

#### Returns

true, if the stored value is a uninterpreted function model.

```
12.256.3.23 operator=() [2/5] template<typename Rational , typename Poly >
ModelValue& carl::ModelValue< Rational, Poly >::operator= (
            const MultivariateRoot< Poly > & mr ) [inline]
12.256.3.24 operator=() [3/5] template<typename Rational , typename Poly >
template<typename ... Args>
ModelValue& carl::ModelValue< Rational, Poly >::operator= (
            const std::variant< Args... > & variant ) [inline]
12.256.3.25 operator=() [4/5] template<typename Rational , typename Poly >
template<typename T >
ModelValue& carl::ModelValue< Rational, Poly >::operator= (
            const T & t ) [inline]
Assign some value to the underlying variant.
Parameters
 t Some value.
Returns
     *this.
12.256.3.26 operator=() [5/5] template<typename Rational , typename Poly >
ModelValue& carl::ModelValue< Rational, Poly >::operator= (
            ModelValue< Rational, Poly > && mv ) [default]
12.256.3.27 visit() template<typename Rational , typename Poly >
template < typename F >
auto carl::ModelValue< Rational, Poly >::visit (
            F && f ) const [inline]
12.256.4 Friends And Related Function Documentation
12.256.4.1 operator< template<typename Rational , typename Poly >
template<typename R , typename P >
bool operator< (
```

const ModelValue< R, P > & lhs,

const ModelValue< R, P > & rhs ) [friend]

const ModelValue< R, P > & rhs ) [friend]

# 12.257 carl::ModelVariable Class Reference

const ModelValue< R, P > & lhs,

Represent a sum type/variant over the different kinds of variables that exist in CARL to use them in a more uniform way, e.g.

```
#include <ModelVariable.h>
```

## **Public Member Functions**

bool operator== (

template<typename T, typename T2 = typename std::enable\_if<convertible\_to\_variant<T, Base>::value, T>::type>
 ModelVariable (const T &\_t)

Initialize the ModelVariable from some valid type of the underlying variant.

- bool is\_variable () const
- bool isBVVariable () const
- bool isUVariable () const
- bool isFunction () const
- carl::Variable as Variable () const
- const carl::BVVariable & asBVVariable () const
- const carl::UVariable & asUVariable () const
- const carl::UninterpretedFunction & asFunction () const

## **Friends**

bool operator== (const ModelVariable &lhs, const ModelVariable &rhs)

Return true if lhs is equal to rhs.

• bool operator< (const ModelVariable &lhs, const ModelVariable &rhs)

Return true if lhs is smaller than rhs.

std::ostream & operator<< (std::ostream &os, const ModelVariable &mv)</li>

# 12.257.1 Detailed Description

Represent a sum type/variant over the different kinds of variables that exist in CARL to use them in a more uniform way, e.g.

an (algebraic) "carl::Variable", an (uninterpreted) "carl::UVariable", an "carl::UninterpretedFunction" etc.

## 12.257.2 Constructor & Destructor Documentation

Initialize the ModelVariable from some valid type of the underlying variant.

## 12.257.3 Member Function Documentation

```
12.257.3.1 asBVVariable() const carl::BVVariable& carl::ModelVariable::asBVVariable () const [inline]
```

#### Returns

The stored value as a bitvector variable.

```
12.257.3.2 asFunction() const carl::UninterpretedFunction& carl::ModelVariable::asFunction ( ) const [inline]
```

## Returns

The stored value as a function.

```
12.257.3.3 asUVariable() const carl::UVariable& carl::ModelVariable::asUVariable ( ) const [inline]
```

#### Returns

The stored value as an uninterpreted variable.

```
12.257.3.4 asVariable() carl::Variable carl::ModelVariable::asVariable () const [inline]
```

#### Returns

The stored value as a variable.

```
12.257.3.5 is_variable() bool carl::ModelVariable::is_variable ( ) const [inline]
```

true, if the stored value is a variable.

```
12.257.3.6 isBVVariable() bool carl::ModelVariable::isBVVariable ( ) const [inline]
```

Returns

true, if the stored value is a bitvector variable.

```
12.257.3.7 isFunction() bool carl::ModelVariable::isFunction ( ) const [inline]
```

Returns

true, if the stored value is a function.

```
12.257.3.8 isUVariable() bool carl::ModelVariable::isUVariable ( ) const [inline]
```

Returns

true, if the stored value is an uninterpreted variable.

## 12.257.4 Friends And Related Function Documentation

```
12.257.4.1 operator< bool operator< (
const ModelVariable & lhs,
const ModelVariable & rhs ) [friend]
```

Return true if lhs is smaller than rhs.

```
12.257.4.3 operator== bool operator== (

const ModelVariable & lhs,

const ModelVariable & rhs ) [friend]
```

Return true if lhs is equal to rhs.

## 12.258 carl::Monomial Class Reference

The general-purpose monomials.

```
#include <Monomial.h>
```

# **Public Types**

- using Arg = std::shared\_ptr< const Monomial >
- using Content = std::vector< std::pair< Variable, std::size\_t >>

## **Public Member Functions**

- ∼Monomial ()
- Monomial ()=delete

Default constructor.

- Monomial (const Monomial &rhs)=delete
- Monomial (Monomial &&rhs)=delete
- exponents\_it begin ()

Returns iterator on first pair of variable and exponent.

• exponents\_clt begin () const

Returns constant iterator on first pair of variable and exponent.

• exponents\_it end ()

Returns past-the-end iterator.

· exponents\_clt end () const

Returns past-the-end iterator.

• std::size\_t hash () const

Returns the hash of this monomial.

• std::size\_t id () const

Return the id of this monomial.

· exponent tdeg () const

Gives the total degree, i.e.

- const Content & exponents () const
- bool is\_constant () const

Checks whether the monomial is a constant.

- bool integer\_valued () const
- bool is\_linear () const

Checks whether the monomial has exactly degree one.

• bool isAtMostLinear () const

Checks whether the monomial has at most degree one.

• bool is\_square () const

Checks whether the monomial is a square, i.e.

• std::size\_t num\_variables () const

Returns the number of variables that occur in the monomial.

Variable single\_variable () const

Retrieves the single variable of the monomial.

bool has\_no\_other\_variable (Variable v) const

Checks that there is no other variable than the given one.

const std::pair < Variable, std::size\_t > & operator[] (std::size\_t index) const

Retrieves the given VarExpPair.

exponent exponent\_of\_variable (Variable v) const

Retrieves the exponent of the given variable.

· bool has (Variable v) const

TODO: write code if binary search is preferred.

Monomial::Arg drop\_variable (Variable v) const

For a monomial  $m = Prod(x_i^{\wedge} \{e_i\}) * v^{\wedge} e$ , divides m by  $v^{\wedge} e$ .

· bool divide (Variable v, Monomial::Arg &res) const

Divides the monomial by a variable v.

• bool divisible (const Monomial::Arg &m) const

Checks if this monomial is divisible by the given monomial m.

bool divide (const Monomial::Arg &m, Monomial::Arg &res) const

Returns a new monomial that is this monomial divided by m.

Monomial::Arg sqrt () const

Calculates and returns the square root of this monomial, iff the monomial is a square as checked by is\_square().

bool is\_consistent () const

Checks if the monomial is consistent.

## **Static Public Member Functions**

- static CompareResult compareLexical (const Monomial::Arg &lhs, const Monomial::Arg &rhs)
- static CompareResult compareLexical (const Monomial::Arg &lhs, Variable rhs)
- static CompareResult compareGradedLexical (const Monomial::Arg &lhs, const Monomial::Arg &rhs)
- static CompareResult compareGradedLexical (const Monomial::Arg &lhs, Variable rhs)
- static Monomial::Arg lcm (const Monomial::Arg &lhs, const Monomial::Arg &rhs)

Calculates the least common multiple of two monomial pointers.

static Monomial::Arg calcLcmAndDivideBy (const Monomial::Arg &lhs, const Monomial::Arg &rhs)

Returns lcm(lhs, rhs) / rhs.

static CompareResult lexicalCompare (const Monomial &lhs, const Monomial &rhs)

This method performs a lexical comparison as defined in ?, page 47.

static std::size\_t hashContent (const Monomial::Content &c)

Calculate the hash of a monomial based on its content.

## **Friends**

· class MonomialPool

## 12.258.1 Detailed Description

The general-purpose monomials.

Notice that we aim to keep this object as small as possbible, while also limiting the use of expensive language features such as RTTI, exceptions and even polymorphism.

Although a Monomial can conceptually be seen as a map from variables to exponents, this implementation uses a vector of pairs of variables and exponents. Due to the fact that monomials usually contain only a small number of variables, the overhead introduced by std::map makes up for the asymptotically slower std::find on the std::vector that is used.

Besides, many operations like multiplication, division or substitution do not rely on finding some variable, but must iterate over all entries anyway.

# 12.258.2 Member Typedef Documentation

```
12.258.2.1 Arg using carl::Monomial::Arg = std::shared_ptr<const Monomial>
\textbf{12.258.2.2} \quad \textbf{Content} \quad \texttt{using carl::Monomial::Content = std::vector < std::pair < Variable, \ \texttt{std} \leftarrow \texttt{vector} < \texttt{
  ::size_t> >
12.258.3 Constructor & Destructor Documentation
12.258.3.1 \simMonomial() carl::Monomial::\simMonomial ()
12.258.3.2 Monomial() [1/3] carl::Monomial::Monomial ( ) [delete]
Default constructor.
\textbf{12.258.3.3} \quad \textbf{Monomial() [2/3]} \quad \texttt{carl::Monomial::Monomial (}
                                                                                     const Monomial & rhs ) [delete]
12.258.3.4 Monomial() [3/3] carl::Monomial::Monomial (
                                                                                     Monomial && rhs ) [delete]
```

# 12.258.4 Member Function Documentation

```
12.258.4.1 begin() [1/2] exponents_it carl::Monomial::begin ( ) [inline]
```

Returns iterator on first pair of variable and exponent.

Returns

Iterator on begin.

```
12.258.4.2 begin() [2/2] exponents_cIt carl::Monomial::begin ( ) const [inline]
```

Returns constant iterator on first pair of variable and exponent.

Returns

Iterator on begin.

```
12.258.4.3 calcLcmAndDivideBy() static Monomial::Arg carl::Monomial::calcLcmAndDivideBy (
             const Monomial::Arg & lhs,
             const Monomial::Arg & rhs ) [inline], [static]
Returns lcm(lhs, rhs) / rhs.
12.258.4.4 compareGradedLexical() [1/2] static CompareResult carl::Monomial::compareGraded←
Lexical (
             const Monomial::Arg & lhs,
             const Monomial::Arg & rhs ) [inline], [static]
12.258.4.5 compareGradedLexical() [2/2] static CompareResult carl::Monomial::compareGraded←
Lexical (
             const Monomial::Arg & lhs,
             Variable rhs ) [inline], [static]
12.258.4.6 compareLexical() [1/2] static CompareResult carl::Monomial::compareLexical (
             const Monomial:: Arg & 1hs,
             const Monomial::Arg & rhs ) [inline], [static]
12.258.4.7 compareLexical() [2/2] static CompareResult carl::Monomial::compareLexical (
             const Monomial::Arg & lhs,
             Variable rhs ) [inline], [static]
12.258.4.8 divide() [1/2] bool carl::Monomial::divide (
```

Returns a new monomial that is this monomial divided by m.

const Monomial::Arg & m,  ${\tt Monomial::Arg \& res) const}$ 

Returns a pair of a monomial pointer and a bool. The bool indicates if the division was possible. The monomial pointer holds the result of the division. If the division resulted in an empty monomial (i.e. the two monomials were equal), the pointer is nullptr.

## **Parameters**

| m   | Monomial.           |
|-----|---------------------|
| res | Resulting monomial. |

## **Returns**

this divided by m.

Divides the monomial by a variable v.

If the division is impossible (because v does not occur in the monomial), nullptr is returned.

#### **Parameters**

| V   | Variable           |
|-----|--------------------|
| res | Resulting monomial |

## Returns

This divided by v.

Checks if this monomial is divisible by the given monomial m.

#### **Parameters**

```
m Monomial.
```

# Returns

If this is divisible by m.

```
12.258.4.11 drop_variable() Monomial::Arg carl::Monomial::drop_variable ( Variable\ v ) const
```

For a monomial m = Prod(  $x_i^{\land} \{e_i\}$  ) \*  $v^{\land} e$ , divides m by  $v^{\land} e$ .

nullptr if result is 1, otherwise m/v^e.

**Todo** this should work on the shared\_ptr directly. Then we could directly return this shared\_ptr instead of the ugly copying.

```
12.258.4.12 end() [1/2] exponents_it carl::Monomial::end ( ) [inline]
```

Returns past-the-end iterator.

Returns

Iterator on end.

```
12.258.4.13 end() [2/2] exponents_cIt carl::Monomial::end ( ) const [inline]
```

Returns past-the-end iterator.

Returns

Iterator on end.

```
12.258.4.14 exponent_of_variable() exponent carl::Monomial::exponent_of_variable ( Variable v ) const [inline]
```

Retrieves the exponent of the given variable.

**Parameters** 

```
v Variable.
```

Returns

Exponent of v.

```
12.258.4.15 exponents() const Content& carl::Monomial::exponents ( ) const [inline]
```

```
12.258.4.16 has() bool carl::Monomial::has (

Variable v ) const [inline]
```

TODO: write code if binary search is preferred.

## **Parameters**

```
v The variable to check for its occurrence.
```

#### Returns

true, if the variable occurs in this term.

```
12.258.4.17 has_no_other_variable() bool carl::Monomial::has_no_other_variable ( Variable\ v ) const [inline]
```

Checks that there is no other variable than the given one.

#### **Parameters**

```
v Variable.
```

## Returns

If there is only v.

```
12.258.4.18 hash() std::size_t carl::Monomial::hash ( ) const [inline]
```

Returns the hash of this monomial.

# Returns

Hash.

```
12.258.4.19 hashContent() static std::size_t carl::Monomial::hashContent ( const Monomial::Content & c ) [inline], [static]
```

Calculate the hash of a monomial based on its content.

## **Parameters**

c Content of a monomial.

Hash of the monomial.

```
12.258.4.20 id() std::size_t carl::Monomial::id ( ) const [inline]
```

Return the id of this monomial.

Returns

ld.

12.258.4.21 integer\_valued() bool carl::Monomial::integer\_valued ( ) const [inline]

Returns

true, if the image of this monomial is integer-valued.

12.258.4.22 is\_consistent() bool carl::Monomial::is\_consistent ( ) const

Checks if the monomial is consistent.

Returns

If this is consistent.

12.258.4.23 is\_constant() bool carl::Monomial::is\_constant ( ) const [inline]

Checks whether the monomial is a constant.

Returns

If monomial is constant.

12.258.4.24 is\_linear() bool carl::Monomial::is\_linear ( ) const [inline]

Checks whether the monomial has exactly degree one.

Returns

If monomial is linear.

```
12.258.4.25 is_square() bool carl::Monomial::is_square ( ) const [inline]
```

Checks whether the monomial is a square, i.e.

whether all exponents are even.

#### Returns

If monomial is a square.

```
12.258.4.26 isAtMostLinear() bool carl::Monomial::isAtMostLinear ( ) const [inline]
```

Checks whether the monomial has at most degree one.

#### Returns

If monomial is linear or constant.

Calculates the least common multiple of two monomial pointers.

If both are valid objects, the lcm of both is calculated. If only one is a valid object, this one is returned. If both are invalid objects, an empty monomial is returned.

#### **Parameters**

| lhs | First monomial.  |
|-----|------------------|
| rhs | Second monomial. |

#### Returns

lcm of lhs and rhs.

This method performs a lexical comparison as defined in ?, page 47.

We define the exponent vectors to be in decreasing order, i.e. the exponents of the larger variables first.

## **Parameters**

| lhs | First monomial.  |
|-----|------------------|
| rhs | Second monomial. |

## Returns

Comparison result.

## See also

?, page 47.

```
12.258.4.29 num_variables() std::size_t carl::Monomial::num_variables ( ) const [inline]
```

Returns the number of variables that occur in the monomial.

# Returns

Number of variables.

```
12.258.4.30 operator[]() const std::pair<Variable, std::size_t>& carl::Monomial::operator[] ( std::size_t index ) const [inline]
```

Retrieves the given VarExpPair.

# **Parameters**

```
index Index.
```

# Returns

VarExpPair.

```
12.258.4.31 single_variable() Variable carl::Monomial::single_variable ( ) const [inline]
```

Retrieves the single variable of the monomial.

Asserts that there is in fact only a single variable.

## Returns

Variable.

```
12.258.4.32 sqrt() Monomial::Arg carl::Monomial::sqrt ( ) const
```

Calculates and returns the square root of this monomial, iff the monomial is a square as checked by is\_square().

Otherwise, nullptr is returned.

## Returns

The square root of this monomial, iff the monomial is a square as checked by is\_square().

```
12.258.4.33 tdeg() exponent carl::Monomial::tdeg ( ) const [inline]
```

Gives the total degree, i.e.

the sum of all exponents.

Returns

Total degree.

## 12.258.5 Friends And Related Function Documentation

```
12.258.5.1 MonomialPool friend class MonomialPool [friend]
```

# 12.259 carl::MonomialComparator< f, degreeOrdered > Struct Template Reference

A class for term orderings.

```
#include <MonomialOrdering.h>
```

# **Public Member Functions**

- bool operator() (const Monomial::Arg &m1, const Monomial::Arg &m2) const
- template<typename Coeff > bool operator() (const Term< Coeff > &t1, const Term< Coeff > &t2) const

## **Static Public Member Functions**

- static CompareResult compare (const Monomial::Arg &m1, const Monomial::Arg &m2)
- template<typename Coeff > static CompareResult compare (const Term< Coeff > &t1, const Term< Coeff > &t2)
- template < typename Coeff > static bool less (const Term < Coeff > &t1, const Term < Coeff > &t2)
- static bool less (const Monomial::Arg &m1, const Monomial::Arg &m2)
- template<typename Coeff >
   static bool equal (const Term< Coeff > &t1, const Term< Coeff > &t2)
- static bool equal (const Monomial::Arg &m1, const Monomial::Arg &m2)

## **Static Public Attributes**

• static const bool degreeOrder = degreeOrdered

# 12.259.1 Detailed Description

```
template < Monomial Ordering Function \ f, \ bool \ degree Ordered > \\ struct \ carl:: Monomial Comparator < f, \ degree Ordered > \\
```

A class for term orderings.

#### 12.259.2 Member Function Documentation

```
12.259.2.1 compare() [1/2] template<MonomialOrderingFunction f, bool degreeOrdered>
static CompareResult carl::MonomialComparator< f, degreeOrdered >::compare (
            const Monomial::Arg & m1,
            const Monomial::Arg & m2 ) [inline], [static]
12.259.2.2 compare() [2/2] template<MonomialOrderingFunction f, bool degreeOrdered>
template<typename Coeff >
static CompareResult carl::MonomialComparator< f, degreeOrdered >::compare (
            const Term< Coeff > & t1,
            const Term< Coeff > \& t2) [inline], [static]
12.259.2.3 equal() [1/2] template<MonomialOrderingFunction f, bool degreeOrdered>
static bool carl::MonomialComparator< f, degreeOrdered >::equal (
            const Monomial:: Arg & m1,
            const Monomial::Arg & m2 ) [inline], [static]
12.259.2.4 equal() [2/2] template<MonomialOrderingFunction f, bool degreeOrdered>
template<typename Coeff >
static bool carl::MonomialComparator< f, degreeOrdered >::equal (
            const Term< Coeff > & t1,
            const Term< Coeff > \& t2) [inline], [static]
12.259.2.5 less() [1/2] template<MonomialOrderingFunction f, bool degreeOrdered>
static bool carl::MonomialComparator< f, degreeOrdered >::less (
            const Monomial::Arg & m1,
            const Monomial::Arg & m2 ) [inline], [static]
```

## 12.259.3 Field Documentation

```
12.259.3.1 degreeOrder template<MonomialOrderingFunction f, bool degreeOrdered> const bool carl::MonomialComparator< f, degreeOrdered >::degreeOrder = degreeOrdered [static]
```

## 12.260 carl::MonomialPool Class Reference

```
#include <MonomialPool.h>
```

## **Public Member Functions**

Monomial::Arg create (Variable \_var, exponent \_exp)

Creates a monomial from a variable and an exponent.

• template<typename Number >

Monomial::Arg create (Variable \_var, Number &&\_exp)

Creates a monomial from a variable and an exponent.

- $\bullet \ \ Monomial:: Arg\ create\ (std::vector < std::pair < Variable,\ exponent >> \&\&\_exponents,\ exponent\ \_totalDegree)$ 
  - Creates a monomial from a list of variables and their exponents.
- Monomial::Arg create (const std::initializer\_list< std::pair< Variable, exponent >> &\_exponents)

Creates a Monomial.

Monomial::Arg create (std::vector< std::pair< Variable, exponent >> &&\_exponents)

Creates a monomial from a list of variables and their exponents.

- void free (const Monomial \*m)
- std::size\_t size () const
- std::size\_t largestID () const

## **Static Public Member Functions**

• static MonomialPool & getInstance ()

Returns the single instance of this class by reference.

## **Protected Member Functions**

- MonomialPool (std::size\_t \_capacity=1000)
  - Constructor of the pool.
- →MonomialPool ()
- Monomial::Arg add (Monomial::Content &&c, exponent totalDegree=0)
- void check\_rehash ()

## **Friends**

- class Singleton < MonomialPool >
- std::ostream & operator<< (std::ostream &os, const MonomialPool &mp)</li>

## 12.260.1 Constructor & Destructor Documentation

Constructor of the pool.

# **Parameters**

```
_capacity | Expected necessary capacity of the pool.
```

```
12.260.1.2 ~MonomialPool() carl::MonomialPool::~MonomialPool ( ) [inline], [protected]
```

# 12.260.2 Member Function Documentation

```
12.260.2.2 check_rehash() void carl::MonomialPool::check_rehash ( ) [inline], [protected]
```

```
12.260.2.3 create() [1/5] Monomial::Arg carl::MonomialPool::create (

const std::initializer_list< std::pair< Variable, exponent >> & _exponents )
```

Creates a Monomial.

## **Parameters**

| _exponents | Possibly unsorted list of variables and epxonents. |
|------------|--|
|------------|--|

Creates a monomial from a list of variables and their exponents.

Note that the input is required to be sorted.

## **Parameters**

| S | orted | list of variables and exponents. |
|---|-------|----------------------------------|
|---|-------|----------------------------------|

Creates a monomial from a list of variables and their exponents.

Note that the input is required to be sorted.

# **Parameters**

| ₋exponents   | Sorted list of variables and exponents. |
|--------------|---|
| ₋totalDegree | Total degree.                           |

Creates a monomial from a variable and an exponent.

Creates a monomial from a variable and an exponent.

```
12.260.2.9 getInstance() static MonomialPool & carl::Singleton< MonomialPool >::getInstance (
) [inline], [static], [inherited]
```

Returns the single instance of this class by reference.

If there is no instance yet, a new one is created.

```
12.260.2.10 largestID() std::size_t carl::MonomialPool::largestID ( ) const [inline]
```

```
12.260.2.11 size() std::size_t carl::MonomialPool::size ( ) const [inline]
```

# 12.260.3 Friends And Related Function Documentation

```
12.260.3.2 Singleton< MonomialPool > friend class Singleton< MonomialPool > [friend]
```

# 12.261 carl::mpl\_concatenate < T > Struct Template Reference

```
#include <mpl_utils.h>
```

## **Public Types**

typedef mpl\_concatenate\_impl< sizeof...(T), T... >::type type

## 12.261.1 Member Typedef Documentation

```
12.261.1.1 type template<typename... T>
typedef mpl_concatenate_impl<sizeof...(T), T...>::type carl::mpl_concatenate< T >::type
```

# 12.262 carl::mpl\_concatenate\_impl < S, Front, Tail > Struct Template Reference

```
#include <mpl_utils.h>
```

# **Public Types**

- typedef mpl\_concatenate\_impl< S-1, Tail... >::type TailConcatenation
- typedef boost::mpl::copy< Front, boost::mpl::back\_inserter< TailConcatenation > >::type type

## 12.262.1 Member Typedef Documentation

```
12.262.1.1 TailConcatenation template<std::size_t S, typename Front , typename... Tail> typedef mpl_concatenate_impl<S-1, Tail...>::type carl::mpl_concatenate_impl< S, Front, Tail >← ::TailConcatenation
```

```
12.262.1.2 type template<std::size_t S, typename Front , typename... Tail>
typedef boost::mpl::copy<Front, boost::mpl::back_inserter<TailConcatenation>>::type carl::mpl_concatenate_impl_s, Front, Tail>::type
```

# 12.263 carl::mpl\_concatenate\_impl< 1, Front, Tail... > Struct Template Reference

```
#include <mpl_utils.h>
```

# **Public Types**

· typedef Front type

# 12.263.1 Member Typedef Documentation

```
12.263.1.1 type template<typename Front , typename... Tail> typedef Front carl::mpl_concatenate_impl< 1, Front, Tail... >::type
```

# 12.264 carl::mpl\_unique < T > Struct Template Reference

```
#include <mpl_utils.h>
```

## **Public Types**

- typedef boost::mpl::less< boost::mpl::sizeof\_< boost::mpl::->, boost::mpl::sizeof\_< boost::mpl::-> > Less
- typedef std::is\_same< boost::mpl::\_, boost::mpl::\_ > Equal
- typedef boost::mpl::sort< T, Less >::type Sorted
- typedef boost::mpl::unique < Sorted, Equal >::type Unique
- typedef Unique type

## 12.264.1 Member Typedef Documentation

```
12.264.1.1 Equal template<typename T >
typedef std::is_same<boost::mpl::_, boost::mpl::_> carl::mpl_unique< T >::Equal

12.264.1.2 Less template<typename T >
typedef boost::mpl::less<br/>typedef boost::mpl::sizeof.<br/>boost::mpl::.> > carl::mpl_unique< T >::Less

12.264.1.3 Sorted template<typename T >
typedef boost::mpl::sort<T, Less>::type carl::mpl_unique< T >::Sorted

12.264.1.4 type template<typename T >
typedef Unique carl::mpl_unique< T >::type
12.264.1.5 Unique template<typename T >
typedef boost::mpl::unique<Sorted, Equal>::type carl::mpl_unique<T >::Unique
```

# 12.265 carl::mpl\_variant\_of < Vector > Struct Template Reference

```
#include <mpl_utils.h>
```

# **Public Types**

- typedef mpl\_unique < Vector >::type Unique
- typedef mpl\_variant\_of\_impl< boost::mpl::empty< Unique >::value, Unique >::type type

# 12.265.1 Member Typedef Documentation

```
12.265.1.1 type template<typename Vector > typedef mpl_variant_of_impl<br/>boost::mpl::empty<Unique>::value, Unique>::type carl::mpl_variant_of<br/>Vector >::type
```

```
12.265.1.2 Unique template<typename Vector >
typedef mpl_unique<Vector>::type carl::mpl_variant_of< Vector >::Unique
```

# 12.266 carl::mpl\_variant\_of\_impl< bool, Vector, Unpacked > Struct Template Reference

```
#include <mpl_utils.h>
```

# **Public Types**

- typedef boost::mpl::front< Vector >::type Front
- typedef boost::mpl::pop\_front< Vector >::type Tail
- typedef mpl\_variant\_of\_impl< boost::mpl::empty< Tail >::value, Tail, Front, Unpacked... >::type type

# 12.266.1 Member Typedef Documentation

```
12.266.1.1 Front template<bool , typename Vector , typename... Unpacked> typedef boost::mpl::front<Vector>::type carl::mpl_variant_of_impl< bool, Vector, Unpacked >← ::Front
```

```
12.266.1.2 Tail template<bool , typename Vector , typename... Unpacked>
typedef boost::mpl::pop_front<Vector>::type carl::mpl_variant_of_impl< bool, Vector, Unpacked
>::Tail
```

```
12.266.1.3 type template<bool, typename Vector, typename... Unpacked>
typedef mpl_variant_of_impl<boost::mpl::empty<Tail>::value, Tail, Front, Unpacked...>::type
carl::mpl_variant_of_impl<bool, Vector, Unpacked >::type
```

# 12.267 carl::mpl\_variant\_of\_impl< true, Vector, Unpacked... > Struct Template Reference

```
#include <mpl_utils.h>
```

# **Public Types**

typedef boost::variant< Unpacked... > type

## 12.267.1 Member Typedef Documentation

# 12.268 carl::MultiplicationTable < Number > Class Template Reference

```
#include <MultiplicationTable.h>
```

# **Data Structures**

• struct TableContent

# **Public Types**

- using IndexPairs = std::forward\_list< std::pair< uint, uint > >
- using Monomial = Term< Number >

# **Public Member Functions**

- MultiplicationTable ()
- MultiplicationTable (const GroebnerBase < Number > &gb)
- std::unordered\_map< Monomial, TableContent >::const\_iterator begin () const
- std::unordered\_map< Monomial, TableContent >::const\_iterator end () const
- std::unordered\_map< Monomial, TableContent >::const\_iterator cbegin () const
- std::unordered\_map< Monomial, TableContent >::const\_iterator cend () const
- bool contains (const Monomial &m) const
- const std::vector< Monomial > & getBase () const noexcept
- BaseRepresentation < Number > reduce (const MultivariatePolynomial < Number > &p) const
- const TableContent & getEntry (const Monomial &mon) const
- MultivariatePolynomial < Number > baseReprToPolynomial (const BaseRepresentation < Number > &baseRepr) const
- BaseRepresentation < Number > multiply (const BaseRepresentation < Number > &f, const BaseRepresentation < Number > &g) const
- Number trace (const BaseRepresentation< Number > &f) const

## **Friends**

```
    template<typename C >
        std::ostream & operator<< (std::ostream &o, const MultiplicationTable< C > &table)
```

# 12.268.1 Member Typedef Documentation

```
12.268.1.1 IndexPairs template<typename Number >
using carl::MultiplicationTable< Number >::IndexPairs = std::forward.list<std::pair<uint,
uint> >

12.268.1.2 Monomial template<typename Number >
using carl::MultiplicationTable< Number >::Monomial = Term<Number>
```

## 12.268.2 Constructor & Destructor Documentation

```
12.268.2.1 MultiplicationTable() [1/2] template<typename Number >
carl::MultiplicationTable< Number >::MultiplicationTable ( ) [inline]
```

# 12.268.3 Member Function Documentation

```
12.268.3.2 begin() template<typename Number >
std::unordered_map<Monomial, TableContent>::const_iterator carl::MultiplicationTable< Number
>::begin ( ) const [inline]
```

```
12.268.3.3 cbegin() template<typename Number >
std::unordered_map<Monomial, TableContent>::const_iterator carl::MultiplicationTable< Number
>::cbegin ( ) const [inline]
12.268.3.4 cend() template<typename Number >
std::unordered_map<Monomial, TableContent>::const_iterator carl::MultiplicationTable< Number
>::cend ( ) const [inline]
12.268.3.5 contains() template<typename Number >
bool carl::MultiplicationTable< Number >::contains (
            const Monomial & m ) const [inline]
12.268.3.6 end() template<typename Number >
std::unordered_map<Monomial, TableContent>::const_iterator carl::MultiplicationTable< Number
>::end ( ) const [inline]
12.268.3.7 getBase() template<typename Number >
const std::vector<Monomial>& carl::MultiplicationTable< Number >::getBase ( ) const [inline],
[noexcept]
12.268.3.8 getEntry() template<typename Number >
const TableContent& carl::MultiplicationTable< Number >::getEntry (
            const Monomial & mon ) const [inline]
12.268.3.9 multiply() template<typename Number >
BaseRepresentation<Number> carl::MultiplicationTable< Number >::multiply (
            const BaseRepresentation< Number > & f,
            const BaseRepresentation< Number > \& g ) const [inline]
12.268.3.10 reduce() template<typename Number >
BaseRepresentation<Number> carl::MultiplicationTable< Number >::reduce (
            const MultivariatePolynomial< Number > & p ) const [inline]
```

#### 12.268.4 Friends And Related Function Documentation

# 12.269 carl::MultivariateHensel< Coeff, Ordering, Policies > Class Template Reference

```
#include <MultivariateHensel.h>
```

# 12.270 carl::MultivariateHorner< PolynomialType, strategy > Class Template Reference

```
#include <MultivariateHorner.h>
```

## **Public Member Functions**

- MultivariateHorner ()=delete
- MultivariateHorner (const PolynomialType &inPut)
- MultivariateHorner (const PolynomialType &inPut, const std::map< Variable, Interval< double >> &map)
- MultivariateHorner (const PolynomialType &inPut, const std::map < Variable, Interval < double >> &map, int &counter)
- MultivariateHorner (const MultivariateHorner &)=default
- MultivariateHorner (MultivariateHorner &&)=default
- MultivariateHorner & operator= (const MultivariateHorner &mh)=default
- Variable getVariable () const
- void setVariable (Variable::Arg &var)
- std::shared\_ptr< MultivariateHorner > getDependent () const
- void removeDependent ()
- void removeIndepenent ()
- void setDependent (std::shared\_ptr< MultivariateHorner > dependent)
- std::shared\_ptr< MultivariateHorner > getIndependent () const
- void setIndependent (std::shared\_ptr< MultivariateHorner > independent)
- const CoeffType & getDepConstant () const
- void setDepConstant (const CoeffType &constant)
- const CoeffType & getIndepConstant () const
- void setIndepConstant (const CoeffType &constant)
- unsigned getExponent () const
- void setExponent (const unsigned &exp)

## 12.270.1 Constructor & Destructor Documentation

```
12.270.1.1 MultivariateHorner() [1/6] template<typename PolynomialType , class strategy >
carl::MultivariateHorner< PolynomialType, strategy >::MultivariateHorner ( ) [delete]
12.270.1.2 MultivariateHorner() [2/6] template<typename PolynomialType , class strategy >
carl::MultivariateHorner< PolynomialType, strategy >::MultivariateHorner (
             const PolynomialType & inPut )
12.270.1.3 MultivariateHorner() [3/6] template<typename PolynomialType , class strategy >
carl::MultivariateHorner< PolynomialType, strategy >::MultivariateHorner (
             const PolynomialType & inPut,
             const std::map< Variable, Interval< double >> & map )
\textbf{12.270.1.4} \quad \textbf{MultivariateHorner() [4/6]} \quad \texttt{template} < \texttt{typename PolynomialType , class strategy} > \\
carl::MultivariateHorner< PolynomialType, strategy >::MultivariateHorner (
             const PolynomialType & inPut,
             const std::map< Variable, Interval< double >> & map,
             int & counter )
12.270.1.5 MultivariateHorner() [5/6] template<typename PolynomialType , class strategy >
carl::MultivariateHorner< PolynomialType, strategy >::MultivariateHorner (
             const MultivariateHorner< PolynomialType, strategy > & ) [default]
12.270.1.6 MultivariateHorner() [6/6] template<typename PolynomialType , class strategy >
\verb|carl::MultivariateHorner| < Polynomial Type, strategy >:: MultivariateHorner (
             {\tt MultivariateHorner<\ PolynomialType,\ strategy>\&\&\ )\ [default]}
12.270.2 Member Function Documentation
12.270.2.1 getDepConstant() template<typename PolynomialType , class strategy >
const CoeffType& carl::MultivariateHorner< PolynomialType, strategy >::getDepConstant ( )
const [inline]
```

```
12.270.2.2 getDependent() template<typename PolynomialType , class strategy >
::getDependent ( ) const [inline]
12.270.2.3 getExponent() template<typename PolynomialType , class strategy >
unsigned carl::MultivariateHorner< PolynomialType, strategy >::getExponent ( ) const [inline]
12.270.2.4 getIndepConstant() template<typename PolynomialType , class strategy >
const CoeffType& carl::MultivariateHorner< PolynomialType, strategy >::getIndepConstant ( )
const [inline]
12.270.2.5 getIndependent() template<typename PolynomialType , class strategy >
std::shared\_ptr<MultivariateHorner> carl::MultivariateHorner< PolynomialType, strategy > \leftarrow
::getIndependent ( ) const [inline]
12.270.2.6 getVariable() template<typename PolynomialType , class strategy >
Variable carl::MultivariateHorner< PolynomialType, strategy >::getVariable ( ) const [inline]
12.270.2.7 operator=() template<typename PolynomialType , class strategy >
MultivariateHorner& carl::MultivariateHorner< PolynomialType, strategy >::operator= (
            const MultivariateHorner< PolynomialType, strategy > & mh ) [default]
12.270.2.8 removeDependent() template<typename PolynomialType , class strategy >
void carl::MultivariateHorner< PolynomialType, strategy >::removeDependent ( ) [inline]
\textbf{12.270.2.9} \quad \textbf{removeIndepenent()} \quad \texttt{template} < \texttt{typename PolynomialType , class strategy} >
void carl::MultivariateHorner< PolynomialType, strategy >::removeIndepenent ( ) [inline]
12.270.2.10 setDepConstant() template<typename PolynomialType , class strategy >
void carl::MultivariateHorner< PolynomialType, strategy >::setDepConstant (
            const CoeffType & constant ) [inline]
```

```
12.270.2.11 setDependent() template < typename Polynomial Type , class strategy >
void carl::MultivariateHorner< PolynomialType, strategy >::setDependent (
              std::shared_ptr< MultivariateHorner< PolynomialType, strategy > > dependent )
[inline]
12.270.2.12 setExponent() template<typename PolynomialType , class strategy >
\verb|void carl::MultivariateHorner| < \verb|PolynomialType|, strategy| >::setExponent (
              const unsigned & exp ) [inline]
12.270.2.13 setIndepConstant() template<typename PolynomialType , class strategy >
void carl::MultivariateHorner< PolynomialType, strategy >::setIndepConstant (
              const CoeffType & constant ) [inline]
\textbf{12.270.2.14} \quad \textbf{setIndependent()} \quad \texttt{template} < \texttt{typename PolynomialType , class strategy} >
void carl::MultivariateHorner< PolynomialType, strategy >::setIndependent (
              \verb|sta|: \verb|shared_ptr| < \verb|MultivariateHorner| < \verb|PolynomialType|, strategy| > |independent|| )
[inline]
\textbf{12.270.2.15} \quad \textbf{setVariable()} \quad \texttt{template} < \texttt{typename PolynomialType , class strategy} >
void carl::MultivariateHorner< PolynomialType, strategy >::setVariable (
              Variable::Arg & var ) [inline]
```

# 12.271 carl::MultivariatePolynomial< Coeff, Ordering, Policies > Class Template Reference

The general-purpose multivariate polynomial class.

```
#include <MultivariatePolynomial.h>
```

## **Public Types**

```
• enum class ConstructorOperation { ADD , SUB , MUL , DIV }
```

• using OrderedBy = Ordering

The ordering of the terms.

• using TermType = Term< Coeff >

Type of the terms.

• using MonomType = Monomial

Type of the monomials within the terms.

• using CoeffType = Coeff

Type of the coefficients.

• using Policy = Policies

Policies for this monomial.

using NumberType = typename UnderlyingNumberType < Coeff >::type

Number type within the coefficients.

using IntNumberType = typename IntegralType < NumberType >::type

Integer type associated with the number type.

- using PolyType = MultivariatePolynomial < Coeff, Ordering, Policies >
- using CACHE = void

The type of the cache. Multivariate polynomials do not need a cache, we set it to something.

using TermsType = std::vector< Term< Coeff >>

Type our terms vector.f.

- using RootType = typename UnivariatePolynomial < NumberType >::RootType
- template<typename C, typename T >
   using EnableIfNotSame = typename std::enable\_if<!std::is\_same< C, T >::value, T >::type

## **Public Member Functions**

- ~MultivariatePolynomial () noexcept=default
- · bool isOrdered () const

Check if the terms are ordered.

- · void reset\_ordered () const
- · void makeOrdered () const

Ensure that the terms are ordered.

const Term < Coeff > & Iterm () const

The leading term.

- Term< Coeff > & Iterm ()
- const Coeff & Icoeff () const

Returns the coefficient of the leading term.

· const Monomial::Arg & Imon () const

The leading monomial.

MultivariatePolynomial Icoeff (Variable::Arg var) const

Returns the leading coefficient with respect to the given variable.

const Term < Coeff > & trailingTerm () const

Give the last term according to Ordering.

- Term < Coeff > & trailingTerm ()
- std::size\_t total\_degree () const

Calculates the max.

• std::size\_t degree (Variable::Arg var) const

Calculates the degree of this polynomial with respect to the given variable.

• MultivariatePolynomial coeff (Variable::Arg var, std::size\_t exp) const

Calculates the coefficient of var^exp.

• bool is\_zero () const

Check if the polynomial is zero.

- bool is\_one () const
- bool is\_constant () const

Check if the polynomial is constant.

• bool is\_number () const

Check if the polynomial is a number, i.e., a constant.

- bool is\_variable () const
- bool is\_linear () const

Check if the polynomial is linear.

std::size\_t nr\_terms () const

Calculate the number of terms.

- std::size\_t size () const
- bool has\_constant\_term () const

Check if the polynomial has a constant term that is not zero.

- · bool integer\_valued () const
- const Coeff & constant\_part () const

Retrieve the constant term of this polynomial or zero, if there is no constant term.

- auto begin () const
- · auto end () const
- · auto rbegin () const
- · auto rend () const
- auto erase\_term (typename TermsType::iterator pos)
- const TermsType & terms () const
- TermsType & terms ()
- MultivariatePolynomial tail (bool makeFullyOrdered=false) const

For the polynomial p, the function calculates a polynomial p - lt(p).

MultivariatePolynomial & strip\_lterm ()

Drops the leading term.

- bool has\_single\_variable () const
- Variable single\_variable () const

For terms with exactly one variable, get this variable.

- · const CoeffType & coefficient () const
- const PolyType & polynomial () const
- bool is\_univariate () const

Checks whether only one variable occurs.

bool is\_tsos () const

Checks whether the polynomial is a trivial sum of squares.

- bool has (Variable v) const
- bool is\_reducible\_identity () const
- void subtractProduct (const Term< Coeff > &factor, const MultivariatePolynomial &p)

Subtract a term times a polynomial from this polynomial.

void addTerm (const Term < Coeff > &term)

Adds a single term without using a TermAdditionManager or changing the ordering status.

bool sqrt (MultivariatePolynomial &res) const

Calculates the square of this multivariate polynomial if it is a square.

- Coeff coprime\_factor () const
- $\bullet \ \ template < typename \ C = Coeff, \ Enable If < is\_subset\_of\_rationals\_type < C >> = dummy > type < C >$

Coeff coprime\_factor\_without\_constant () const

- MultivariatePolynomial coprime\_coefficients () const
- MultivariatePolynomial coprime\_coefficients\_sign\_preserving () const
- · MultivariatePolynomial normalize () const

For a polynomial p, returns p/lc(p)

- bool divides (const MultivariatePolynomial &b) const
- MultivariatePolynomial< typename IntegralType< Coeff >::type, Ordering, Policies > to\_integer\_domain () const
- const Term < Coeff > & operator[] (std::size\_t index) const
- MultivariatePolynomial mod (const typename IntegralType< Coeff >::type &modulo) const
- template < typename C = Coeff, Enablelf < is\_number\_type < C >> = dummy > Coeff numeric\_content () const
- template < typename C = Coeff, Disablelf < is\_number\_type < C >> = dummy > UnderlyingNumberType < C >::type numeric\_content () const

- template < typename C = Coeff, Enablelf < is\_number\_type < C >> = dummy > IntNumberType main\_denom () const
- MultivariatePolynomial operator- () const
- template < bool findConstantTerm = true, bool findLeadingTerm = true > void makeMinimallyOrdered () const

Make sure that the terms are at least minimally ordered.

• bool is\_consistent () const

Asserts that this polynomial complies with the requirements and assumptions for MultivariatePolynomial objects.

- void setReason (unsigned index)
- BitVector getReasons () const
- · void setReasons (const BitVector &) const

## **Constructors**

- MultivariatePolynomial ()
- MultivariatePolynomial (const MultivariatePolynomial < Coeff, Ordering, Policies > &p)
- MultivariatePolynomial (MultivariatePolynomial Coeff, Ordering, Policies > &&p)
- MultivariatePolynomial & operator= (const MultivariatePolynomial &p)
- MultivariatePolynomial & operator= (MultivariatePolynomial &&p) noexcept
- MultivariatePolynomial (int c)
- template<typename C = Coeff>

MultivariatePolynomial (EnableIfNotSame < C, sint > c)

• template<typename C = Coeff>

MultivariatePolynomial (EnableIfNotSame < C, uint > c)

- MultivariatePolynomial (const Coeff &c)
- MultivariatePolynomial (Variable::Arg v)
- MultivariatePolynomial (const Term < Coeff > &t)
- MultivariatePolynomial (const std::shared\_ptr< const Monomial > &m)
- MultivariatePolynomial (const UnivariatePolynomial < MultivariatePolynomial < Coeff, Ordering, Policy >> &pol)
- MultivariatePolynomial (const UnivariatePolynomial < Coeff > &p)
- template<class OtherPolicies , DisableIf< std::is\_same< Policies, OtherPolicies >> = dummy>

MultivariatePolynomial (const MultivariatePolynomial < Coeff, Ordering, OtherPolicies > &p)

- MultivariatePolynomial (TermsType &&terms, bool duplicates=true, bool ordered=false)
- MultivariatePolynomial (const TermsType &terms, bool duplicates=true, bool ordered=false)
- MultivariatePolynomial (const std::initializer\_list< Term< Coeff >> &terms)
- MultivariatePolynomial (const std::initializer\_list< Variable > &terms)
- MultivariatePolynomial (const std::pair< ConstructorOperation, std::vector< MultivariatePolynomial >> &p)
- MultivariatePolynomial (ConstructorOperation op, const std::vector< MultivariatePolynomial > &operands)

## In-place addition operators

• MultivariatePolynomial & operator+= (const MultivariatePolynomial &rhs)

Add something to this polynomial and return the changed polynomial.

MultivariatePolynomial & operator+= (const TermType &rhs)

Add something to this polynomial and return the changed polynomial.

MultivariatePolynomial & operator+= (const std::shared\_ptr< const TermType > &rhs)

Add something to this polynomial and return the changed polynomial.

- MultivariatePolynomial & operator+= (const Monomial::Arg &rhs)
- MultivariatePolynomial & operator+= (Variable rhs)

Add something to this polynomial and return the changed polynomial.

MultivariatePolynomial & operator+= (const Coeff &rhs)

Add something to this polynomial and return the changed polynomial.

## In-place subtraction operators

MultivariatePolynomial & operator= (const MultivariatePolynomial &rhs)

Subtract something from this polynomial and return the changed polynomial.

- MultivariatePolynomial & operator-= (const Term < Coeff > &rhs)
- MultivariatePolynomial & operator-= (const Monomial::Arg &rhs)
- MultivariatePolynomial & operator-= (Variable::Arg rhs)

Subtract something from this polynomial and return the changed polynomial.

MultivariatePolynomial & operator-= (const Coeff &rhs)

Subtract something from this polynomial and return the changed polynomial.

## In-place multiplication operators

- MultivariatePolynomial & operator\*= (const MultivariatePolynomial &rhs)
  - Multiply this polynomial with something and return the changed polynomial.
- MultivariatePolynomial & operator\*= (const Term< Coeff > &rhs)
- MultivariatePolynomial & operator\*= (const Monomial::Arg &rhs)
- MultivariatePolynomial & operator\*= (Variable::Arg rhs)
- MultivariatePolynomial & operator\*= (const Coeff &rhs)

## In-place division operators

- MultivariatePolynomial & operator/= (const MultivariatePolynomial &rhs)
  - Divide this polynomial by something and return the changed polynomial.
- MultivariatePolynomial & operator/= (const Term < Coeff > &rhs)

Divide this polynomial by something and return the changed polynomial.

- MultivariatePolynomial & operator/= (const Monomial::Arg &rhs)
  - Divide this polynomial by something and return the changed polynomial.
- MultivariatePolynomial & operator/= (Variable::Arg rhs)
  - Divide this polynomial by something and return the changed polynomial.
- MultivariatePolynomial & operator/= (const Coeff &rhs)

Divide this polynomial by something and return the changed polynomial.

## **Static Public Member Functions**

- static bool compareByLeadingTerm (const MultivariatePolynomial &p1, const MultivariatePolynomial &p2)
- static bool compareByNrTerms (const MultivariatePolynomial &p1, const MultivariatePolynomial &p2)

## **Static Public Attributes**

- static TermAdditionManager< MultivariatePolynomial, Ordering > mTermAdditionManager
- static const bool searchLinear = true

Linear searching means that we search linearly for a term instead of applying e.g.

static const bool has\_reasons = ReasonsAdaptor::has\_reasons

## **Friends**

- template < typename Polynomial, typename Order > class TermAdditionManager
- std::ostream & operator<< (std::ostream &os, ConstructorOperation op)</li>

## **Division operators**

template<typename C, typename O, typename P>
 MultivariatePolynomial< C, O, P > operator/ (const MultivariatePolynomial< C, O, P > &lhs, const MultivariatePolynomial< C, O, P > &rhs)

Perform a division involving a polynomial.

template
 typename C, typename O, typename P>
 MultivariatePolynomial
 C, O, P > operator/ (const MultivariatePolynomial
 C, O, P > &lhs, unsigned long rhs)

Perform a division involving a polynomial.

## 12.271.1 Detailed Description

template<typename Coeff, typename Ordering = GrLexOrdering, typename Policies = StdMultivariate

PolynomialPolicies<>>>
PolynomialPolicies = StdMultivariate

class carl::MultivariatePolynomial< Coeff, Ordering, Policies >

The general-purpose multivariate polynomial class.

It is represented as a sum of terms, being a coefficient and a monomial.

A polynomial is always *minimally ordered*. By that, we mean that the leading term and the constant term (if there is any) are at the correct positions. For some operations, the terms may be *fully ordered*. isOrdered() checks if the polynomial is *fully ordered* while makeOrdered() makes the polynomial *fully ordered*.

# 12.271.2 Member Typedef Documentation

```
12.271.2.1 CACHE template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> using carl::MultivariatePolynomial< Coeff, Ordering, Policies >::CACHE = void
```

The type of the cache. Multivariate polynomials do not need a cache, we set it to something.

```
12.271.2.2 CoeffType template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> using carl::MultivariatePolynomial< Coeff, Ordering, Policies >::CoeffType = Coeff
```

Type of the coefficients.

```
12.271.2.3 EnableIfNotSame template<typename Coeff , typename Ordering = GrLexOrdering, typename
Policies = StdMultivariatePolynomialPolicies<>>
template<typename C , typename T >
using carl::MultivariatePolynomial< Coeff, Ordering, Policies >::EnableIfNotSame = typename
std::enable_if<!std::is_same<C,T>::value,T>::type
```

```
12.271.2.4 IntNumberType template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> using carl::MultivariatePolynomial< Coeff, Ordering, Policies >::IntNumberType = typename IntegralType<NumberType>::type
```

Integer type associated with the number type.

```
12.271.2.5 MonomType template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> using carl::MultivariatePolynomial< Coeff, Ordering, Policies >::MonomType = Monomial
```

Type of the monomials within the terms.

```
12.271.2.6 NumberType template<typename Coeff , typename Ordering = GrLexOrdering, typename
Policies = StdMultivariatePolynomialPolicies<>>
using carl::MultivariatePolynomial< Coeff, Ordering, Policies >::NumberType = typename UnderlyingNumberType<(
::type
```

Number type within the coefficients.

```
12.271.2.7 OrderedBy template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> using carl::MultivariatePolynomial< Coeff, Ordering, Policies >::OrderedBy = Ordering
```

The ordering of the terms.

```
12.271.2.8 Policy template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> using carl::MultivariatePolynomial< Coeff, Ordering, Policies >::Policy = Policies
```

Policies for this monomial.

```
12.271.2.9 PolyType template<typename Coeff , typename Ordering = GrLexOrdering, typename
Policies = StdMultivariatePolynomialPolicies<>>
using carl::MultivariatePolynomial< Coeff, Ordering, Policies >::PolyType = MultivariatePolynomial<Coeff,
Ordering, Policies>
```

```
12.271.2.10 RootType template<typename Coeff , typename Ordering = GrLexOrdering, typename
Policies = StdMultivariatePolynomialPolicies<>>
using carl::MultivariatePolynomial< Coeff, Ordering, Policies >::RootType = typename UnivariatePolynomial<Num
::RootType
```

```
12.271.2.11 TermsType template<typename Coeff , typename Ordering = GrLexOrdering, typename
Policies = StdMultivariatePolynomialPolicies<>>
using carl::MultivariatePolynomial< Coeff, Ordering, Policies >::TermsType = std::vector<Term<Coeff>
```

Type our terms vector.f.

```
12.271.2.12 TermType template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> using carl::MultivariatePolynomial< Coeff, Ordering, Policies >::TermType = Term<Coeff>
```

Type of the terms.

## 12.271.3 Member Enumeration Documentation

```
12.271.3.1 ConstructorOperation template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> enum carl::MultivariatePolynomial::ConstructorOperation [strong]
```

#### **Enumerator**

| ADD |  |
|-----|--|
| SUB |  |
| MUL |  |
| DIV |  |

## 12.271.4 Constructor & Destructor Documentation

```
12.271.4.1 MultivariatePolynomial() [1/19] template<typename Coeff , typename Ordering , typename Policies > carl::MultivariatePolynomial < Coeff, Ordering, Policies >::MultivariatePolynomial
```

```
12.271.4.4 MultivariatePolynomial() [4/19] template<typename Coeff , typename Ordering = GrLex←
Ordering, typename Policies = StdMultivariatePolynomialPolicies<>>
carl::MultivariatePolynomial< Coeff, Ordering, Policies >::MultivariatePolynomial (
             int c ) [inline], [explicit]
12.271.4.5 MultivariatePolynomial() [5/19] template<typename Coeff , typename Ordering , typename
Policies >
template<typename C >
carl::MultivariatePolynomial< Coeff, Ordering, Policies >::MultivariatePolynomial (
             EnableIfNotSame< C, sint > c) [explicit]
12.271.4.6 MultivariatePolynomial() [6/19] template<typename Coeff , typename Ordering , typename
Policies >
template<typename C >
carl::MultivariatePolynomial< Coeff, Ordering, Policies >::MultivariatePolynomial (
             EnableIfNotSame< C, uint > c) [explicit]
12.271.4.7 MultivariatePolynomial() [7/19] template<typename Coeff , typename Ordering , typename
Policies >
carl::MultivariatePolynomial< Coeff, Ordering, Policies >::MultivariatePolynomial (
             const Coeff & c ) [explicit]
12.271.4.8 MultivariatePolynomial() [8/19] template<typename Coeff , typename Ordering , typename
Policies >
carl::MultivariatePolynomial< Coeff, Ordering, Policies >::MultivariatePolynomial (
             Variable::Arg v ) [explicit]
12.271.4.9 MultivariatePolynomial() [9/19] template<typename Coeff , typename Ordering , typename
Policies >
carl::MultivariatePolynomial< Coeff, Ordering, Policies >::MultivariatePolynomial (
             const Term< Coeff > & t ) [explicit]
\textbf{12.271.4.10} \quad \textbf{MultivariatePolynomial() [10/19]} \quad \texttt{template} < \texttt{typename Coeff , typename Ordering = Gr} \leftarrow \texttt{Coeff }
LexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>>>
carl::MultivariatePolynomial< Coeff, Ordering, Policies >::MultivariatePolynomial (
             const std::shared_ptr< const Monomial > & m ) [explicit]
```

```
12.271.4.11 MultivariatePolynomial() [11/19] template<typename Coeff , typename Ordering , typename
Policies >
carl::MultivariatePolynomial< Coeff, Ordering, Policies >::MultivariatePolynomial (
             const UnivariatePolynomial< MultivariatePolynomial< Coeff, Ordering, Policy >> &
pol ) [explicit]
12.271.4.12 MultivariatePolynomial() [12/19] template<typename Coeff , typename Ordering , typename
carl::MultivariatePolynomial < Coeff, Ordering, Policies >::MultivariatePolynomial (
             const UnivariatePolynomial < Coeff > & p ) [explicit]
12.271.4.13 MultivariatePolynomial() [13/19] template<typename Coeff , typename Ordering , typename
{\tt template}{<} {\tt typename \ OtherPolicies \ , \ Disable If}{<\ std} :: {\tt is\_same}{<\ Policies \ , \ OtherPolicies \ >> >} >
carl::MultivariatePolynomial< Coeff, Ordering, Policies >::MultivariatePolynomial (
             const MultivariatePolynomial< Coeff, Ordering, OtherPolicies > & p ) [explicit]
\textbf{12.271.4.14} \quad \textbf{MultivariatePolynomial() [14/19]} \quad \texttt{template} < \texttt{typename Coeff , typename Ordering = Gr} \leftarrow \texttt{Coeff }
LexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>>
carl::MultivariatePolynomial< Coeff, Ordering, Policies >::MultivariatePolynomial (
             TermsType && terms,
             bool duplicates = true,
             bool ordered = false ) [explicit]
12.271.4.15 MultivariatePolynomial() [15/19] template<typename Coeff , typename Ordering = Gr \leftarrow
LexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>>>
carl::MultivariatePolynomial< Coeff, Ordering, Policies >::MultivariatePolynomial (
             const TermsType & terms,
             bool duplicates = true,
             bool ordered = false ) [explicit]
12.271.4.16 MultivariatePolynomial() [16/19] template<typename Coeff , typename Ordering , typename
Policies >
carl::MultivariatePolynomial< Coeff, Ordering, Policies >::MultivariatePolynomial (
             const std::initializer_list< Term< Coeff >> & terms )
12.271.4.17 MultivariatePolynomial() [17/19] template<typename Coeff , typename Ordering , typename
Policies >
carl::MultivariatePolynomial< Coeff, Ordering, Policies >::MultivariatePolynomial (
             const std::initializer_list< Variable > & terms )
```

```
12.271.4.18 MultivariatePolynomial() [18/19] template<typename Coeff , typename Ordering , typename
Policies >
carl::MultivariatePolynomial< Coeff, Ordering, Policies >::MultivariatePolynomial (
             const std::pair< ConstructorOperation, std::vector< MultivariatePolynomial</pre>
Coeff, Ordering, Policies >>> \& p ) [explicit]
12.271.4.19 MultivariatePolynomial() [19/19] template<typename Coeff , typename Ordering , typename
Policies >
carl::MultivariatePolynomial< Coeff, Ordering, Policies >::MultivariatePolynomial (
             ConstructorOperation op,
             const std::vector< MultivariatePolynomial< Coeff, Ordering, Policies > > & operands
) [explicit]
\textbf{12.271.4.20} \quad \sim \textbf{MultivariatePolynomial()} \quad \texttt{template} < \texttt{typename Coeff} \text{ , typename Ordering = GrLex} \leftarrow \textbf{Coeff} \text{ .}
Ordering, typename Policies = StdMultivariatePolynomialPolicies<>>
carl::MultivariatePolynomial< Coeff, Ordering, Policies >::~MultivariatePolynomial ( ) [default],
[noexcept]
12.271.5 Member Function Documentation
12.271.5.1 addTerm() template<typename Coeff , typename Ordering , typename Policies >
void carl::MultivariatePolynomial< Coeff, Ordering, Policies >::addTerm (
             const Term< Coeff > & term )
Adds a single term without using a TermAdditionManager or changing the ordering status.
Parameters
 term Term.
12.271.5.2 begin() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies
= StdMultivariatePolynomialPolicies<>>
auto carl::MultivariatePolynomial< Coeff, Ordering, Policies >::begin ( ) const [inline]
12.271.5.3 coeff() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies
= StdMultivariatePolynomialPolicies<>>
MultivariatePolynomial carl::MultivariatePolynomial < Coeff, Ordering, Policies >::coeff (
```

Calculates the coefficient of  $var^{\wedge}exp$ .

Variable::Arg var,

std::size\_t exp ) const [inline]

## **Parameters**

| var | Variable. |
|-----|-----------|
| exp | Exponent. |

## Returns

Coefficient of var^exp.

```
12.271.5.4 coefficient() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> const CoeffType& carl::MultivariatePolynomial< Coeff, Ordering, Policies >::coefficient () const [inline]
```

## Returns

Coefficient of the polynomial (this makes only sense for polynomials storing the gcd of all coefficients separately)

```
12.271.5.7 constant_part() template<typename Coeff , typename Ordering , typename Policies > const Coeff & carl::MultivariatePolynomial< Coeff, Ordering, Policies >::constant_part
```

Retrieve the constant term of this polynomial or zero, if there is no constant term.

```
12.271.5.8 coprime_coefficients() template<typename Coeff , typename Ordering , typename Policies
MultivariatePolynomial < Coeff, Ordering, Policies > carl::MultivariatePolynomial < Coeff,
Ordering, Policies >::coprime_coefficients
Returns
     p * p.coprime_factor()
See also
     coprime_factor()
12.271.5.9 coprime_coefficients_sign_preserving() template<typename Coeff , typename Ordering ,
typename Policies >
MultivariatePolynomial < Coeff, Ordering, Policies > carl::MultivariatePolynomial < Coeff,
Ordering, Policies >::coprime_coefficients_sign_preserving
Returns
     p * |p.coprime_factor()|
See also
     coprime_coefficients()
\textbf{12.271.5.10} \quad \textbf{coprime\_factor()} \quad \texttt{template} < \texttt{typename Coeff , typename Ordering , typename Policies} > \\
Coeff carl::MultivariatePolynomial< Coeff, Ordering, Policies >::coprime_factor
```

The lcm of the denominators of the coefficients in p divided by the gcd of numerators of the coefficients in p.

```
12.271.5.11 coprime_factor_without_constant() template<typename Coeff , typename Ordering , typename Policies > template<typename C , EnableIf< is_subset_of_rationals_type< C >> > Coeff carl::MultivariatePolynomial< Coeff, Ordering, Policies >::coprime_factor_without_← constant
```

## Returns

The lcm of the denominators of the coefficients (without the constant one) in p divided by the gcd of numerators of the coefficients in p.

Calculates the degree of this polynomial with respect to the given variable.

| <b>D</b> |    |   |   |    |    |
|----------|----|---|---|----|----|
| Pа       | ra | m | ല | aı | r۹ |

```
var Variable.
```

Degree w.r.t. var.

```
12.271.5.16 getReasons() BitVector carl::NoReasons::getReasons ( ) const [inline], [inherited]
```

```
12.271.5.17 has() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> bool carl::MultivariatePolynomial< Coeff, Ordering, Policies >::has ( Variable v) const [inline]
```

## **Parameters**

v The variable to check for its occurrence.

true, if the variable occurs in this term.

```
12.271.5.18 has_constant_term() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> bool carl::MultivariatePolynomial< Coeff, Ordering, Policies >::has_constant_term ( ) const [inline]
```

Check if the polynomial has a constant term that is not zero.

```
12.271.5.19 has_single_variable() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> bool carl::MultivariatePolynomial< Coeff, Ordering, Policies >::has_single_variable () const [inline]
```

```
12.271.5.20 integer_valued() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> bool carl::MultivariatePolynomial< Coeff, Ordering, Policies >::integer_valued ( ) const [inline]
```

## Returns

true, if the image of this polynomial is integer-valued.

```
12.271.5.21 is_consistent() template<typename Coeff , typename Ordering , typename Policies > bool carl::MultivariatePolynomial< Coeff, Ordering, Policies >::is_consistent
```

Asserts that this polynomial complies with the requirements and assumptions for MultivariatePolynomial objects.

- · All terms are actually valid and not nullptr or alike
- · Only the trailing term may be constant.

```
12.271.5.22 is_constant() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> bool carl::MultivariatePolynomial< Coeff, Ordering, Policies >::is_constant ( ) const [inline]
```

Check if the polynomial is constant.

```
12.271.5.23 is_linear() template<typename Coeff , typename Ordering , typename Policies > bool carl::MultivariatePolynomial< Coeff, Ordering, Policies >::is_linear
```

Check if the polynomial is linear.

```
12.271.5.24 is_number() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> bool carl::MultivariatePolynomial< Coeff, Ordering, Policies >::is_number ( ) const [inline]
```

Check if the polynomial is a number, i.e., a constant.

```
12.271.5.25 is_one() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>>> bool carl::MultivariatePolynomial< Coeff, Ordering, Policies >::is_one ( ) const [inline]
```

#### Returns

```
12.271.5.26 is_reducible_identity() template<typename Coeff , typename Ordering , typename Policies >
bool carl::MultivariatePolynomial< Coeff, Ordering, Policies >::is_reducible_identity
```

```
12.271.5.27 is_tsos() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> bool carl::MultivariatePolynomial< Coeff, Ordering, Policies >::is_tsos () const [inline]
```

Checks whether the polynomial is a trivial sum of squares.

## Returns

true if polynomial is of the form \sum a\_im\_i^2 with a\_i > 0 for all i.

```
12.271.5.28 is_univariate() template<typename Coeff , typename Ordering , typename Policies > bool carl::MultivariatePolynomial< Coeff, Ordering, Policies >::is_univariate
```

Checks whether only one variable occurs.

# Returns

Notice that it might be better to use the variable information if several pieces of information are requested.

```
12.271.5.29 is.variable() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> bool carl::MultivariatePolynomial< Coeff, Ordering, Policies >::is_variable () const [inline]
```

true, if this polynomial consists just of one variable (with coefficient 1).

```
12.271.5.30 is_zero() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> bool carl::MultivariatePolynomial< Coeff, Ordering, Policies >::is_zero () const [inline]
```

Check if the polynomial is zero.

```
12.271.5.31 isOrdered() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> bool carl::MultivariatePolynomial< Coeff, Ordering, Policies >::isOrdered () const [inline]
```

Check if the terms are ordered.

## Returns

If terms are ordered.

```
12.271.5.32 | lcoeff() [1/2] template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> const Coeff& carl::MultivariatePolynomial< Coeff, Ordering, Policies >::lcoeff ( ) const [inline]
```

Returns the coefficient of the leading term.

Notice that this is not defined for zero polynomials.

## Returns

Leading coefficient.

Returns the leading coefficient with respect to the given variable.

| <b>Param</b> | eters |
|--------------|-------|
|--------------|-------|

| var | Variable. |
|-----|-----------|
|     |           |

Leading coefficient.

12.271.5.34 Imon() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> const Monomial::Arg& carl::MultivariatePolynomial< Coeff, Ordering, Policies >::lmon ( ) const [inline]

The leading monomial.

## Returns

monomial of leading term.

```
12.271.5.35 | lterm() [1/2] template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>>>
Term<Coeff>& carl::MultivariatePolynomial< Coeff, Ordering, Policies >::lterm () [inline]
```

12.271.5.36 lterm() [2/2] template<typename Coeff , typename Ordering = GrLexOrdering, typename
Policies = StdMultivariatePolynomialPolicies<>>
const Term<Coeff>& carl::MultivariatePolynomial< Coeff, Ordering, Policies >::lterm ( ) const
[inline]

The leading term.

## Returns

leading term.

```
12.271.5.37 main_denom() template<typename Coeff , typename O , typename P >
template<typename C , EnableIf< is_number_type< C >> >
MultivariatePolynomial< Coeff, O, P >::IntNumberType carl::MultivariatePolynomial< Coeff, O,
P >::main_denom
```

```
12.271.5.38 makeMinimallyOrdered() template<typename Coeff , typename Ordering , typename Policies > template<br/>bool findConstantTerm, bool findLeadingTerm> void carl::MultivariatePolynomial< Coeff, Ordering, Policies >::makeMinimallyOrdered
```

Make sure that the terms are at least minimally ordered.

```
12.271.5.39 makeOrdered() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> void carl::MultivariatePolynomial < Coeff, Ordering, Policies >::makeOrdered () const [inline]
```

Ensure that the terms are ordered.

```
12.271.5.41 normalize() template<typename Coeff , typename Ordering , typename Policies > MultivariatePolynomial< Coeff, Ordering, Policies > carl::MultivariatePolynomial< Coeff, Ordering, Policies >::normalize
```

For a polynomial p, returns p/lc(p)

Returns

```
12.271.5.42 nr_terms() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> std::size_t carl::MultivariatePolynomial< Coeff, Ordering, Policies >::nr_terms () const [inline]
```

Calculate the number of terms.

```
12.271.5.43 numeric_content() [1/2] template<typename Coeff , typename O , typename P >
template<typename C , EnableIf< is_number_type< C >> >
Coeff carl::MultivariatePolynomial< Coeff, O, P >::numeric_content
```

Todo gcd needed for fractions

```
12.271.5.44 numeric_content() [2/2] template<typename Coeff , typename O , typename P >
template<typename C , DisableIf< is_number_type< C >>> >
UnderlyingNumberType< C >::type carl::MultivariatePolynomial< Coeff, O, P >::numeric_content

12.271.5.45 operator*=() [1/5] template<typename Coeff , typename Ordering , typename Policies >
MultivariatePolynomial< Coeff, Ordering, Policies > & carl::MultivariatePolynomial< Coeff, Ordering, Policies >::operator*= (
```

Todo more efficient.

const Coeff & rhs )

Todo more efficient.

Multiply this polynomial with something and return the changed polynomial.

## **Parameters**

```
rhs Right hand side.
```

## Returns

Changed polynomial.

Todo more efficient.

Todo more efficient.

Add something to this polynomial and return the changed polynomial.

# **Parameters**

```
rhs Right hand side.
```

## Returns

Changed polynomial.

Todo insert at correct position if already ordered

Add something to this polynomial and return the changed polynomial.

#### **Parameters**

```
rhs Right hand side.
```

#### Returns

Changed polynomial.

Add something to this polynomial and return the changed polynomial.

#### **Parameters**

```
rhs Right hand side.
```

#### Returns

Changed polynomial.

Add something to this polynomial and return the changed polynomial.

# **Parameters**

```
rhs Right hand side.
```

#### Returns

```
12.271.5.55 operator+=() [6/6] template<typename Coeff , typename Ordering , typename Policies
```

Add something to this polynomial and return the changed polynomial.

#### **Parameters**

```
rhs Right hand side.
```

#### **Returns**

Changed polynomial.

```
12.271.5.56 operator-() template<typename Coeff , typename Ordering , typename Policies > MultivariatePolynomial< Coeff, Ordering, Policies > carl::MultivariatePolynomial< Coeff, Ordering, Policies >::operator-
```

Subtract something from this polynomial and return the changed polynomial.

## **Parameters**

```
rhs Right hand side.
```

# Returns

Changed polynomial.

**Todo** Check if this works with ordering.

Subtract something from this polynomial and return the changed polynomial.

#### **Parameters**

```
rhs Right hand side.
```

#### Returns

Changed polynomial.

Todo Check if this works with ordering.

Subtract something from this polynomial and return the changed polynomial.

# **Parameters**

```
rhs Right hand side.
```

## Returns

```
12.271.5.62 operator/=() [1/5] template<typename Coeff , typename Ordering , typename Policies
```

Divide this polynomial by something and return the changed polynomial.

#### **Parameters**

```
rhs Right hand side.
```

#### Returns

Changed polynomial.

Divide this polynomial by something and return the changed polynomial.

## **Parameters**

```
rhs Right hand side.
```

#### Returns

Changed polynomial.

Divide this polynomial by something and return the changed polynomial.

# **Parameters**

```
rhs Right hand side.
```

## Returns

Divide this polynomial by something and return the changed polynomial.

#### **Parameters**

```
rhs Right hand side.
```

#### Returns

Changed polynomial.

Divide this polynomial by something and return the changed polynomial.

# **Parameters**

```
rhs Right hand side.
```

#### Returns

```
12.271.5.69 operator[]() template<typename Coeff , typename Ordering = GrLexOrdering, typename
Policies = StdMultivariatePolynomialPolicies<>>
\verb|const Term| < \verb|Coeff| > & \verb|carl::MultivariatePolynomial| < \verb|Coeff|, Ordering|, Policies| > ::operator[] | (
             std::size_t index ) const [inline]
12.271.5.70 polynomial() template<typename Coeff , typename Ordering = GrLexOrdering, typename
Policies = StdMultivariatePolynomialPolicies<>>
const PolyType& carl::MultivariatePolynomial < Coeff, Ordering, Policies >::polynomial ( )
const [inline]
Returns
     The coprimeCoefficients of this polyomial, if this is stored internally, otherwise this polynomial.
12.271.5.71 rbegin() template<typename Coeff , typename Ordering = GrLexOrdering, typename
Policies = StdMultivariatePolynomialPolicies<>>
auto carl::MultivariatePolynomial< Coeff, Ordering, Policies >::rbegin ( ) const [inline]
12.271.5.72 rend() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies
= StdMultivariatePolynomialPolicies<>>
auto carl::MultivariatePolynomial < Coeff, Ordering, Policies >::rend ( ) const [inline]
12.271.5.73 reset_ordered() template<typename Coeff , typename Ordering = GrLexOrdering, typename
Policies = StdMultivariatePolynomialPolicies<>>
void carl::MultivariatePolynomial< Coeff, Ordering, Policies >::reset_ordered ( ) const [inline]
12.271.5.74 setReason() void carl::NoReasons::setReason (
             unsigned index ) [inherited]
12.271.5.75 setReasons() void carl::NoReasons::setReasons (
             const BitVector & ) const [inline], [inherited]
```

12.271.5.76 single\_variable() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>>>
Variable carl::MultivariatePolynomial< Coeff, Ordering, Policies >::single\_variable ( ) const [inline]

For terms with exactly one variable, get this variable.

#### Returns

The only variable occuring in the term.

```
12.271.5.77 size() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> std::size_t carl::MultivariatePolynomial< Coeff, Ordering, Policies >::size ( ) const [inline]
```

#### **Returns**

A rough estimation of the size of this polynomial being the number of its terms. (Note, that this method is required, as it is provided of other polynomials not necessarily being straightforward.)

Calculates the square of this multivariate polynomial if it is a square.

#### **Parameters**

res Used to store the result in.

## Returns

true, if this multivariate polynomial is a square; false, otherwise.

```
12.271.5.79 strip_lterm() template<typename Coeff , typename Ordering , typename Policies > MultivariatePolynomial< Coeff, Ordering, Policies > & carl::MultivariatePolynomial< Coeff, Ordering, Policies >::strip_lterm
```

Drops the leading term.

The function assumes the polynomial to be nonzero, otherwise the leading term is not defined.

# Returns

A reference to this.

Todo find new Iterm

Subtract a term times a polynomial from this polynomial.

#### **Parameters**

| factor | Term.       |
|--------|-------------|
| р      | Polynomial. |

For the polynomial p, the function calculates a polynomial p - lt(p).

The function assumes the polynomial to be nonzero, otherwise, lt(p) is not defined.

#### Returns

A new polynomial p - lt(p).

```
12.271.5.82 terms() [1/2] template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>>
TermsType& carl::MultivariatePolynomial< Coeff, Ordering, Policies >::terms () [inline]
```

```
12.271.5.83 terms() [2/2] template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> const TermsType& carl::MultivariatePolynomial< Coeff, Ordering, Policies >::terms ( ) const [inline]
```

```
12.271.5.84 to.integer_domain() template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>>>
MultivariatePolynomial<typename IntegralType<Coeff>::type, Ordering, Policies> carl::MultivariatePolynomial<
Coeff, Ordering, Policies>::to.integer_domain ( ) const
```

```
12.271.5.85 total_degree() template<typename Coeff , typename Ordering , typename Policies > std::size_t carl::MultivariatePolynomial< Coeff, Ordering, Policies >::total_degree
```

Calculates the max.

degree over all monomials occurring in the polynomial. As the degree of the zero polynomial is  $-\infty$ , we assert that this polynomial is not zero. This must be checked by the caller before calling this method.

See also

?, page 48

Returns

Total degree.

```
12.271.5.86 trailingTerm() [1/2] template<typename Coeff , typename Ordering = GrLexOrdering,
typename Policies = StdMultivariatePolynomialPolicies<>>
Term<Coeff>& carl::MultivariatePolynomial< Coeff, Ordering, Policies >::trailingTerm ( )
[inline]
```

```
12.271.5.87 trailingTerm() [2/2] template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> const Term<Coeff>& carl::MultivariatePolynomial< Coeff, Ordering, Policies >::trailingTerm () const [inline]
```

Give the last term according to Ordering.

Notice that if there is a constant part, it is always trailing.

## 12.271.6 Friends And Related Function Documentation

Perform a division involving a polynomial.

# Parameters

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

#### Returns

lhs / rhs

Perform a division involving a polynomial.

#### **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

#### Returns

lhs / rhs

```
12.271.6.4 TermAdditionManager template<typename Coeff , typename Ordering = GrLexOrdering, typename Policies = StdMultivariatePolynomialPolicies<>> template<typename Polynomial , typename Order > friend class TermAdditionManager [friend]
```

# 12.271.7 Field Documentation

```
12.271.7.1 has_reasons template<typename ReasonsAdaptor = NoReasons, typename Allocator = No↔ Allocator>
const bool carl::StdMultivariatePolynomialPolicies< ReasonsAdaptor, Allocator >::has_reasons = ReasonsAdaptor::has_reasons [static], [inherited]
```

```
12.271.7.2 mTermAdditionManager template<typename Coeff , typename Ordering , typename Policies
```

TermAdditionManager< MultivariatePolynomial< Coeff, Ordering, Policies >, Ordering > carl::MultivariatePolynomial< Coeff, Ordering, Policies >::mTermAdditionManager [static]

```
12.271.7.3 searchLinear template<typename ReasonsAdaptor = NoReasons, typename Allocator = NoAllocator>
const bool carl::StdMultivariatePolynomialPolicies< ReasonsAdaptor, Allocator >::searchLinear = true [static], [inherited]
```

Linear searching means that we search linearly for a term instead of applying e.g.

binary search. Although the worst-case complexity is worse, for polynomials with a small nr of terms, this should be better.

# 12.272 carl::MultivariateRoot< Poly > Class Template Reference

#include <MultivariateRoot.h>

# **Public Types**

- using Number = typename UnderlyingNumberType< Poly >::type
- using RAN = typename Poly::RootType

#### **Public Member Functions**

- MultivariateRoot (const Poly &poly, std::size\_t k, Variable var)
- MultivariateRoot ()
- std::size\_t k () const noexcept

Return k, the index of the root.

- const Poly & poly () const noexcept
- Poly & poly () noexcept
- · Variable var () const noexcept
- bool is\_univariate () const

#### Friends

template<typename P >
 std::optional< typename MultivariateRoot< P >::RAN > evaluate (const MultivariateRoot< P > &mr, const carl::Assignment< typename MultivariateRoot< P >::RAN > &m)

## 12.272.1 Member Typedef Documentation

```
12.272.1.1 Number template<typename Poly >
using carl::MultivariateRoot< Poly >::Number = typename UnderlyingNumberType<Poly>::type
```

```
12.272.1.2 RAN template<typename Poly > using carl::MultivariateRoot< Poly >::RAN = typename Poly::RootType
```

#### 12.272.2 Constructor & Destructor Documentation

#### **Parameters**

| poly | Must mention the root-variable "_z" and should have a at least 'rootldx'-many roots in "_z" at each subpoint where it is intended to be evaluated. |  |
|------|--|--|
| k    | The index of the root of the polynomial in "_z". The first root has index 1, the second has index 2 and so on.                                     |  |

```
12.272.2.2 MultivariateRoot() [2/2] template<typename Poly >
carl::MultivariateRoot< Poly >::MultivariateRoot ( ) [inline]
```

# 12.272.3 Member Function Documentation

```
12.272.3.1 is_univariate() template<typename Poly >
bool carl::MultivariateRoot< Poly >::is_univariate ( ) const [inline]
```

```
12.272.3.2 k() template<typename Poly >
std::size_t carl::MultivariateRoot< Poly >::k ( ) const [inline], [noexcept]
```

Return k, the index of the root.

```
12.272.3.3 poly() [1/2] template<typename Poly >
const Poly& carl::MultivariateRoot< Poly >::poly ( ) const [inline], [noexcept]
```

#### Returns

the raw underlying polynomial that still mentions the root-variable "\_z".

```
12.272.3.4 poly() [2/2] template<typename Poly >
Poly& carl::MultivariateRoot< Poly >::poly ( ) [inline], [noexcept]
```

#### Returns

the raw underlying polynomial that still mentions the root-variable "\_z".

```
12.272.3.5 var() template<typename Poly >
Variable carl::MultivariateRoot< Poly >::var ( ) const [inline], [noexcept]
```

#### Returns

The globally-unique distinguished root-variable "\_z" to allow you to build a polynomial with this variable yourself.

## 12.272.4 Friends And Related Function Documentation

# 12.273 carl::needs\_cache\_type < T > Struct Template Reference

```
#include <typetraits.h>
```

# 12.274 carl::needs\_cache\_type< FactorizedPolynomial< P >> Struct Template Reference

#include <FactorizedPolynomial.h>

# 12.275 carl::needs\_context\_type< T > Struct Template Reference

```
#include <typetraits.h>
```

# 12.276 carl::needs\_context\_type< ContextPolynomial< Coeff, Ordering, Policies > > Struct Template Reference

#include <ContextPolynomial.h>

#### 12.277 carl::NoAllocator Struct Reference

#include <PolynomialAllocator.h>

# 12.278 carl::CompactTree < Entry, FastIndex >::Node Class Reference

#include <CompactTree.h>

#### **Public Member Functions**

- Node ()
- · Node parent () const
- · Node left () const
- Node right () const
- Node sibling () const
- Node leftSibling () const
- Node next (size\_t count=1) const
- Node prev () const
- Node & operator++ ()
- bool isRoot () const
- · bool isLeft () const
- bool isRight () const
- bool operator< (Node node) const
- bool operator<= (Node node) const
- bool operator> (Node node) const
- bool operator>= (Node node) const
- bool operator== (Node node) const
- bool operator!= (Node node) const
- Node (size\_t i)
- size\_t getNormalIndex () const

## **Data Fields**

size\_t \_index

# **Static Public Attributes**

- static const bool fi = FastIndex
- static const size\_t S = sizeof(Entry)

#### **Friends**

class CompactTree< Entry, FastIndex >

### 12.278.1 Constructor & Destructor Documentation

```
12.278.1.1 Node() [1/2] template<class Entry , bool FastIndex>
carl::CompactTree< Entry, FastIndex >::Node::Node ( ) [inline]
12.278.1.2 Node() [2/2] template<class Entry , bool FastIndex>
carl::CompactTree< Entry, FastIndex >::Node::Node (
            size_t i ) [inline], [explicit]
12.278.2 Member Function Documentation
12.278.2.1 getNormalIndex() template<class Entry , bool FastIndex>
size_t carl::CompactTree< Entry, FastIndex >::Node::getNormalIndex ( ) const [inline]
12.278.2.2 isLeft() template<class Entry , bool FastIndex>
bool carl::CompactTree< Entry, FastIndex >::Node::isLeft ( ) const [inline]
12.278.2.3 isRight() template<class Entry , bool FastIndex>
bool carl::CompactTree< Entry, FastIndex >::Node::isRight ( ) const [inline]
12.278.2.4 isRoot() template<class Entry , bool FastIndex>
bool carl::CompactTree< Entry, FastIndex >::Node::isRoot ( ) const [inline]
12.278.2.5 left() template<class E , bool FI>
CompactTree< E, FI >::Node carl::CompactTree< E, FI >::Node::left
12.278.2.6 leftSibling() template<class E , bool FI>
CompactTree< E, FI >::Node carl::CompactTree< E, FI >::Node::leftSibling
```

```
12.278.2.7 next() template<class E , bool FI>
CompactTree< E, FI >::Node carl::CompactTree< E, FI >::Node::next (
            size_t count = 1 ) const
12.278.2.8 operator"!=() template<class Entry , bool FastIndex>
bool carl::CompactTree< Entry, FastIndex >::Node::operator!= (
            Node node ) const [inline]
12.278.2.9 operator++() template<class Entry , bool FastIndex>
Node& carl::CompactTree< Entry, FastIndex >::Node::operator++ ( ) [inline]
12.278.2.10 operator<() template<class Entry , bool FastIndex>
bool carl::CompactTree< Entry, FastIndex >::Node::operator< (</pre>
            Node node ) const [inline]
12.278.2.11 operator<=() template<class Entry , bool FastIndex>
bool carl::CompactTree< Entry, FastIndex >::Node::operator<= (</pre>
            Node node ) const [inline]
12.278.2.12 operator == () template < class Entry , bool FastIndex>
bool carl::CompactTree< Entry, FastIndex >::Node::operator== (
             Node node ) const [inline]
12.278.2.13 operator>() template<class Entry , bool FastIndex>
bool carl::CompactTree< Entry, FastIndex >::Node::operator> (
            Node node ) const [inline]
12.278.2.14 operator>=() template<class Entry , bool FastIndex>
bool carl::CompactTree< Entry, FastIndex >::Node::operator>= (
            Node node ) const [inline]
```

```
12.278.2.15 parent() template<class E , bool FI>
CompactTree< E, FI >::Node carl::CompactTree< E, FI >::Node::parent
12.278.2.16 prev() template<class E , bool FI>
CompactTree< E, FI >::Node carl::CompactTree< E, FI >::Node::prev
12.278.2.17 right() template<class E , bool FI>
CompactTree< E, FI >::Node carl::CompactTree< E, FI >::Node::right
12.278.2.18 sibling() template<class E , bool FI>
CompactTree< E, FI >::Node carl::CompactTree< E, FI >::Node::sibling
12.278.3 Friends And Related Function Documentation
12.278.3.1 CompactTree < Entry, FastIndex > template < class Entry , bool FastIndex >
friend class CompactTree< Entry, FastIndex > [friend]
12.278.4 Field Documentation
12.278.4.1 _index template<class Entry , bool FastIndex>
size_t carl::CompactTree< Entry, FastIndex >::Node::_index
12.278.4.2 fi template<class Entry , bool FastIndex>
const bool carl::CompactTree< Entry, FastIndex >::Node::fi = FastIndex [static]
12.278.4.3 S template<class Entry , bool FastIndex>
const size.t carl::CompactTree< Entry, FastIndex >::Node::S = sizeof(Entry) [static]
12.279 carl::tree_detail::Node< T > Struct Template Reference
```

#include <carlTree.h>

#### **Public Member Functions**

• Node (std::size\_t \_id, T &&\_data, std::size\_t \_parent, std::size\_t \_depth)

## **Data Fields**

- std::size\_t id
- T data
- std::size\_t parent
- std::size\_t previousSibling = MAXINT
- std::size\_t nextSibling = MAXINT
- std::size\_t firstChild = MAXINT
- std::size\_t lastChild = MAXINT
- std::size\_t depth = MAXINT

#### 12.279.1 Constructor & Destructor Documentation

# 12.279.2 Field Documentation

```
12.279.2.1 data template<typename T >
T carl::tree_detail::Node< T >::data [mutable]

12.279.2.2 depth template<typename T >
std::size_t carl::tree_detail::Node< T >::depth = MAXINT
```

std::size\_t carl::tree\_detail::Node< T >::firstChild = MAXINT

12.279.2.3 firstChild template<typename T >

```
12.279.2.4 id template<typename T >
std::size_t carl::tree_detail::Node< T >::id
12.279.2.5 lastChild template<typename T >
std::size_t carl::tree_detail::Node< T >::lastChild = MAXINT
12.279.2.6 nextSibling template<typename T >
std::size_t carl::tree_detail::Node< T >::nextSibling = MAXINT
12.279.2.7 parent template<typename T >
std::size_t carl::tree_detail::Node< T >::parent
12.279.2.8 previousSibling template<typename T >
std::size_t carl::tree_detail::Node< T >::previousSibling = MAXINT
12.280 carl::NoReasons Struct Reference
#include <ReasonsAdaptor.h>
Public Member Functions

    void setReason (unsigned index)

   • BitVector getReasons () const
   • void setReasons (const BitVector &) const
Static Public Attributes
   • static constexpr bool has_reasons = false
12.280.1 Member Function Documentation
```

12.280.1.1 getReasons() BitVector carl::NoReasons::getReasons ( ) const [inline]

#### 12.280.2 Field Documentation

```
12.280.2.1 has_reasons constexpr bool carl::NoReasons::has_reasons = false [static], [constexpr]
```

# 12.281 carl::not\_equal\_to < T, mayBeNull > Struct Template Reference

```
#include <pointerOperations.h>
```

#### **Public Member Functions**

• bool operator() (const T &lhs, const T &rhs) const

# **Data Fields**

std::not\_equal\_to< T > neq

# 12.281.1 Member Function Documentation

# 12.281.2 Field Documentation

```
12.281.2.1 neq template<typename T , bool mayBeNull = true> std::not_equal_to<T> carl::not_equal_to< T, mayBeNull >::neq
```

# 12.282 carl::not\_equal\_to< std::shared\_ptr< T >, mayBeNull > Struct Template Reference

#include <pointerOperations.h>

#### **Public Member Functions**

• bool operator() (const std::shared\_ptr< const T > &lhs, const std::shared\_ptr< const T > &rhs) const

#### 12.282.1 Member Function Documentation

# 12.283 carl::not\_equal\_to < T \*, mayBeNull > Struct Template Reference

#include <pointerOperations.h>

# **Public Member Functions**

• bool operator() (const T \*Ihs, const T \*rhs) const

#### 12.283.1 Member Function Documentation

# 12.284 std::numeric\_limits < carl::FLOAT\_T < Number > > Class Template Reference

```
#include <FLOAT_T.h>
```

### **Static Public Member Functions**

```
static carl::FLOAT_T (min)()
static carl::FLOAT_T (max)()
static carl::FLOAT_T < Number > lowest ()
static carl::FLOAT_T < Number > epsilon ()
static carl::FLOAT_T < Number > round_error ()
static const carl::FLOAT_T < Number > infinity ()
static const carl::FLOAT_T < Number > quiet_NaN ()
static const carl::FLOAT_T < Number > signaling_NaN ()
static const carl::FLOAT_T < Number > denorm_min ()
static float_round_style round_style ()
static int digits ()
static int digits10 ()
static int max_digits10 ()
```

#### **Static Public Attributes**

```
    static const bool is_specialized = true
```

- static const bool is\_signed = true
- static const bool is\_integer = false
- static const bool is\_exact = false
- static const int radix = 2
- static const bool has\_infinity = true
- static const bool has\_quiet\_NaN = true
- static const bool has\_signaling\_NaN = true
- static const bool is\_iec559 = true
- static const bool is\_bounded = true
- static const bool is\_modulo = false
- static const bool traps = true
- static const bool tinyness\_before = true
- static const int min\_exponent = std::numeric\_limits<Number>::min\_exponent
- static const int max\_exponent = std::numeric\_limits<Number>::max\_exponent
- static const int min\_exponent10 = std::numeric\_limits<Number>::min\_exponent10
- static const int max\_exponent10 = std::numeric\_limits<Number>::max\_exponent10

#### 12.284.1 Member Function Documentation

```
12.284.1.3 denorm_min() template<typename Number >
static const carl::FLOAT_T<Number> std::numeric_limits< carl::FLOAT_T< Number > >::denorm_min
() [inline], [static]
12.284.1.4 digits() template<typename Number >
\verb|static| int std::numeric_limits < carl::FLOAT_T < \verb|Number| > >::digits () | [inline], [static]| \\
12.284.1.5 digits10() template<typename Number >
static int std::numeric_limits< carl::FLOAT_T< Number > >::digits10 () [inline], [static]
12.284.1.6 epsilon() template<typename Number >
\verb|static carl::FLOAT.T<| \verb|Number|| > \verb|static carl::FLOAT.T<| Number| > > ::epsilon () \\
[inline], [static]
12.284.1.7 infinity() template<typename Number >
static const carl::FLOAT.T<Number> std::numeric_limits< carl::FLOAT.T< Number > >::infinity (
) [inline], [static]
12.284.1.8 lowest() template<typename Number >
static carl::FLOAT_T<Number> std::numeric.limits< carl::FLOAT_T< Number > >::lowest () [inline],
[static]
12.284.1.9 max_digits10() template<typename Number >
static int std::numeric_limits< carl::FLOAT_T< Number > >::max_digits10 () [inline], [static]
12.284.1.10 quiet_NaN() template<typename Number >
static const carl::FLOAT_T<Number> std::numeric_limits< carl::FLOAT_T< Number > >::quiet_NaN (
) [inline], [static]
12.284.1.11 round_error() template<typename Number >
\verb|static carl::FLOAT.T| < \verb|Number| > \verb|static carl::FLOAT.T| < \verb|Number| > > :: round\_error () \\
[inline], [static]
```

```
12.284.1.12 round_style() template<typename Number >
static float_round_style std::numeric_limits< carl::FLOAT_T< Number > >::round_style ( ) [inline],
[static]
12.284.1.13 signaling_NaN() template<typename Number >
\texttt{static const carl::FLOAT.T} < \texttt{Number} > \texttt{std::numeric.limits} < \texttt{carl::FLOAT.T} < \texttt{Number} > \texttt{>::signaling} \leftrightarrow \texttt{static const carl::FLOAT.T} < \texttt{Number} > \texttt{>::signaling} 
_NaN ( ) [inline], [static]
12.284.2 Field Documentation
12.284.2.1 has_infinity template<typename Number >
const bool std::numeric_limits< carl::FLOAT_T< Number > >::has_infinity = true [static]
12.284.2.2 has_quiet_NaN template<typename Number >
const bool std::numeric_limits< carl::FLOAT.T< Number > >::has_quiet_NaN = true [static]
12.284.2.3 has_signaling_NaN template<typename Number >
const bool std::numeric_limits< carl::FLOAT_T< Number > >::has_signaling_NaN = true [static]
12.284.2.4 is_bounded template<typename Number >
const bool std::numeric_limits< carl::FLOAT_T< Number > >::is_bounded = true [static]
12.284.2.5 is_exact template<typename Number >
const bool std::numeric_limits< carl::FLOAT_T< Number > >::is_exact = false [static]
12.284.2.6 is_iec559 template<typename Number >
const bool std::numeric_limits< carl::FLOAT_T< Number > >::is_iec559 = true [static]
{\bf 12.284.2.7} \quad {\bf is\_integer} \quad {\tt template}{<} {\tt typename} \ {\tt Number} \ > \\
const bool std::numeric_limits< carl::FLOAT.T< Number > >::is_integer = false [static]
```

```
12.284.2.8 is_modulo template<typename Number >
const bool std::numeric_limits< carl::FLOAT_T< Number > >::is_modulo = false [static]
12.284.2.9 is_signed template<typename Number >
const bool std::numeric_limits< carl::FLOAT_T< Number > >::is_signed = true [static]
12.284.2.10 is_specialized template<typename Number >
const bool std::numeric.limits< carl::FLOAT_T< Number > >::is_specialized = true [static]
12.284.2.11 max_exponent template<typename Number >
const int std::numeric_limits< carl::FLOAT.T< Number > >::max_exponent = std::numeric_limits<Number>←
::max_exponent [static]
12.284.2.12 max_exponent10 template<typename Number >
\verb|const| int std::numeric.limits < \verb|carl::FLOAT_T| < Number > >::max.exponent10 = std::numeric. \\ \leftarrow > >: td::numeric. \\ \leftarrow > > >: td::numeric. \\ \leftarrow > >: 
limits<Number>::max_exponent10 [static]
12.284.2.13 min_exponent template<typename Number >
::min_exponent [static]
12.284.2.14 min_exponent10 template<typename Number >
const int std::numeric.limits< carl::FLOAT_T< Number > >::min_exponent10 = std::numeric.←
limits<Number>::min_exponent10 [static]
12.284.2.15 radix template<typename Number >
const int std::numeric_limits< carl::FLOAT_T< Number > >::radix = 2 [static]
12.284.2.16 tinyness_before template<typename Number >
const bool std::numeric_limits< carl::FLOAT.T< Number > >::tinyness_before = true [static]
```

```
12.284.2.17 traps template<typename Number >
const bool std::numeric_limits< carl::FLOAT_T< Number > >::traps = true [static]
```

# 12.285 carl::io::OPBFile Struct Reference

```
#include <OPBImporter.h>
```

#### **Public Member Functions**

- OPBFile ()=default
- OPBFile (OPBPolynomial obj)
- OPBFile (OPBPolynomial obj, std::vector< OPBConstraint > cons)

#### **Data Fields**

- OPBPolynomial objective
- std::vector< OPBConstraint > constraints

#### 12.285.1 Constructor & Destructor Documentation

```
12.285.1.1 OPBFile() [1/3] carl::io::OPBFile::OPBFile ( ) [default]
```

```
12.285.1.2 OPBFile() [2/3] carl::io::OPBFile::OPBFile (
OPBPolynomial obj ) [inline], [explicit]
```

# 12.285.2 Field Documentation

```
12.285.2.1 constraints std::vector<OPBConstraint> carl::io::OPBFile::constraints
```

```
12.285.2.2 objective OPBPolynomial carl::io::OPBFile::objective
```

# 12.286 carl::io::OPBImporter< Pol > Class Template Reference

```
#include <OPBImporter.h>
```

#### **Public Member Functions**

- OPBImporter (const std::string &filename)
- std::optional< std::pair< Formula< Pol >, Pol > parse ()

#### 12.286.1 Constructor & Destructor Documentation

#### 12.286.2 Member Function Documentation

```
12.286.2.1 parse() template<typename Pol > std::optional<std::pair<Formula<Pol>,Pol> > carl::io::OPBImporter< Pol >::parse ( ) [inline]
```

# 12.287 carl::settings::OptionPrinter Struct Reference

Helper class to nicely print the options that are available.

```
#include <SettingsParser.h>
```

## Data Fields

const SettingsParser & parser
 Reference to parser.

### 12.287.1 Detailed Description

Helper class to nicely print the options that are available.

## 12.287.2 Field Documentation

```
12.287.2.1 parser const SettingsParser& carl::settings::OptionPrinter::parser
```

Reference to parser.

# 12.288 carl::overloaded< Ts > Struct Template Reference

```
#include <SFINAE.h>
```

# 12.289 carl::io::parser::Parser< Pol > Class Template Reference

```
#include <Parser.h>
```

#### **Public Member Functions**

- Parser ()
- Pol polynomial (const std::string &s)
- RatFun< Pol > rationalFunction (const std::string &s)
- Formula < Pol > formula (const std::string &s)
- void addVariable (Variable::Arg v)

## 12.289.1 Constructor & Destructor Documentation

```
12.289.1.1 Parser() template<typename Pol >
carl::io::parser::Parser< Pol >::Parser ( ) [inline]
```

#### 12.289.2 Member Function Documentation

# 12.290 carl::tree\_detail::PathIterator< T > Struct Template Reference

Iterator class for iterations from a given element to the root.

```
#include <carlTree.h>
```

# **Public Types**

using Base = Baselterator < T, Pathlterator < T >, false >

#### **Public Member Functions**

- PathIterator (const tree< T > \*t, std::size\_t root)
- PathIterator & next ()
- template<typename It >

PathIterator (const BaseIterator < T, It, false > &ii)

- PathIterator (const PathIterator &ii)
- PathIterator (PathIterator &&ii)
- PathIterator & operator= (const PathIterator &it)
- PathIterator & operator= (PathIterator &&it) noexcept
- virtual ~PathIterator () noexcept=default
- const auto & nodes () const
- const auto & node (std::size\_t id) const
- const auto & curnode () const
- std::size\_t depth () const
- std::size\_t id () const
- · bool isRoot () const
- · bool isValid () const
- T \* operator-> ()
- T const \* operator-> () const

## **Data Fields**

• std::size\_t current

# **Protected Attributes**

const tree< T > \* mTree

## 12.290.1 Detailed Description

```
template<typename T> struct carl::tree_detail::PathIterator< T>
```

Iterator class for iterations from a given element to the root.

# 12.290.2 Member Typedef Documentation

```
12.290.2.1 Base template<typename T >
using carl::tree_detail::PathIterator< T >::Base = BaseIterator<T, PathIterator<T>,false>
```

#### 12.290.3 Constructor & Destructor Documentation

```
12.290.3.4 PathIterator() [4/4] template<typename T > carl::tree_detail::PathIterator< T >::PathIterator ( PathIterator< T > && ii ) [inline]
```

```
12.290.3.5 ~PathIterator() template<typename T > virtual carl::tree_detail::PathIterator< T >::~PathIterator ( ) [virtual], [default], [noexcept]
```

#### 12.290.4 Member Function Documentation

```
12.290.4.1 curnode() const auto& carl::tree_detail::BaseIterator< T, PathIterator< T > ,
reverse >::curnode ( ) const [inline], [inherited]
\textbf{12.290.4.2} \quad \textbf{depth()} \quad \texttt{std::size\_t carl::tree\_detail::BaseIterator} < \texttt{T, PathIterator} < \texttt{T} > \texttt{, reverse}
>::depth ( ) const [inline], [inherited]
12.290.4.3 id() std::size_t carl::tree_detail::BaseIterator< T, PathIterator< T > , reverse
>::id ( ) const [inline], [inherited]
12.290.4.4 isRoot() bool carl::tree_detail::BaseIterator< T, PathIterator< T > , reverse >\leftarrow
::isRoot ( ) const [inline], [inherited]
\textbf{12.290.4.5} \quad \textbf{isValid()} \quad \texttt{bool carl::tree\_detail::BaseIterator} < \texttt{T, PathIterator} < \texttt{T} > \text{, reverse} > \leftarrow
::isValid ( ) const [inline], [inherited]
12.290.4.6 next() template<typename T >
PathIterator& carl::tree_detail::PathIterator< T >::next ( ) [inline]
\textbf{12.290.4.7} \quad \textbf{node()} \quad \texttt{const auto\& carl::tree\_detail::BaseIterator} < \texttt{T, PathIterator} < \texttt{T} > \texttt{, reverse}
>::node (
               std::size_t id ) const [inline], [inherited]
12.290.4.8 nodes() const auto@ carl::tree_detail::BaseIterator< T, PathIterator< T > , reverse
>::nodes ( ) const [inline], [inherited]
```

```
12.290.4.9 operator->() [1/2] T* carl::tree_detail::BaseIterator< T, PathIterator< T > , reverse
>::operator-> ( ) [inline], [inherited]
12.290.4.10 operator->() [2/2] T const* carl::tree_detail::BaseIterator< T, PathIterator< T > ,
reverse >::operator-> ( ) const [inline], [inherited]
12.290.4.11 operator=() [1/2] template<typename T >
PathIterator& carl::tree_detail::PathIterator< T >::operator= (
             const PathIterator< T > & it ) [inline]
12.290.4.12 operator=() [2/2] template<typename T >
PathIterator& carl::tree_detail::PathIterator< T >::operator= (
              PathIterator< T > && it ) [inline], [noexcept]
12.290.5 Field Documentation
\textbf{12.290.5.1} \quad \textbf{current} \quad \texttt{std::size\_t} \quad \texttt{carl::tree\_detail::BaseIterator} < \texttt{T}, \; \texttt{PathIterator} < \texttt{T} > \text{, reverse}
>::current [inherited]
12.290.5.2 mTree const tree<T>* carl::tree_detail::BaseIterator< T, PathIterator< T > ,
reverse >::mTree [protected], [inherited]
12.291 carl::io::parser::ExpressionParser< Pol >::perform_addition Class Reference
#include <ExpressionParser.h>
Public Member Functions

    template<typename T , typename U >

      expr_type operator() (const T &lhs, const U &rhs) const
    • expr_type operator() (const CoeffType &lhs, const CoeffType &rhs) const

    expr_type operator() (const RatFun< Pol > &lhs, const Monomial::Arg &rhs) const

    expr_type operator() (const RatFun< Pol > &lhs, const Term< CoeffType > &rhs) const

    template<typename T >
      std::enable_if<!std::is_same< Formula< Pol >, T >::value, expr_type >::type operator() (const RatFun< Pol
      > &lhs, const T &rhs) const
    • template<typename T >
      std::enable_if<!std::is_same< Formula< Pol >, T >::value, expr_type >::type operator() (const T &lhs, const
      RatFun< Pol > &rhs) const

    expr_type operator() (const RatFun< Pol > &lhs, const RatFun< Pol > &rhs) const

    template<typename T >
      expr_type operator() (const Formula < Pol > &lhs, const T &rhs) const
    template<typename T >
      std::enable_if<!std::is_same< Formula< Pol >, T >::value, expr_type >::type operator() (const T &lhs, const
```

Formula < Pol > &rhs) const

#### 12.291.1 Member Function Documentation

```
12.291.1.1 operator()() [1/9] template<typename Pol >
expr_type carl::io::parser::ExpressionParser< Pol >::perform_addition::operator() (
            const CoeffType & lhs,
             const CoeffType & rhs ) const [inline]
12.291.1.2 operator()() [2/9] template<typename Pol >
template<typename T >
expr_type carl::io::parser::ExpressionParser< Pol >::perform_addition::operator() (
            const Formula < Pol > & lhs,
            const T & rhs ) const [inline]
12.291.1.3 operator()() [3/9] template<typename Pol >
expr_type carl::io::parser::ExpressionParser< Pol >::perform_addition::operator() (
            const RatFun< Pol > & lhs,
            const Monomial::Arg & rhs ) const [inline]
12.291.1.4 operator()() [4/9] template<typename Pol >
expr_type carl::io::parser::ExpressionParser< Pol >::perform_addition::operator() (
            const RatFun< Pol > & lhs,
             const RatFun< Pol > & rhs ) const [inline]
12.291.1.5 operator()() [5/9] template<typename Pol >
template<typename T >
std::enable_if<!std::is_same<Formula<Pol>, T>::value, expr_type>::type carl::io::parser::ExpressionParser<
Pol >::perform_addition::operator() (
            const RatFun< Pol > & lhs,
            const T & rhs ) const [inline]
12.291.1.6 operator()() [6/9] template<typename Pol >
expr_type carl::io::parser::ExpressionParser< Pol >::perform_addition::operator() (
            const RatFun< Pol > & lhs,
            const Term< CoeffType > & rhs ) const [inline]
```

```
12.291.1.7 operator()() [7/9] template<typename Pol >
template<typename T >
std::enable_if<!std::is_same<Formula<Pol>, T>::value, expr_type>::type carl::io::parser::ExpressionParser<
Pol >::perform_addition::operator() (
             const T & lhs,
             const Formula< Pol > & rhs ) const [inline]
12.291.1.8 operator()() [8/9] template<typename Pol >
template < typename T >
std::enable_if<!std::is_same<Formula<Pol>, T>::value, expr_type>::type carl::io::parser::ExpressionParser<
Pol >::perform_addition::operator() (
              const T & lhs,
             const RatFun< Pol > & rhs ) const [inline]
12.291.1.9 operator()() [9/9] template<typename Pol >
template<typename T , typename U >
expr_type carl::io::parser::ExpressionParser< Pol >::perform_addition::operator() (
             const T & lhs,
              const U & rhs ) const [inline]
12.292 carl::io::parser::ExpressionParser< Pol >::perform_division Class Reference
#include <ExpressionParser.h>
Public Member Functions

    expr_type operator() (const RatFun< Pol > &lhs, const CoeffType &rhs) const

    template<typename T >

     std::enable_if<!std::is_base_of< Formula< Pol >, T >::value, expr_type >::type operator() (const RatFun<
     Pol > &lhs, const T &rhs) const

    expr_type operator() (const RatFun< Pol > &lhs, const Monomial::Arg &rhs) const

    expr_type operator() (const RatFun< Pol > &lhs, const Term< CoeffType > &rhs) const

    • expr_type operator() (const RatFun< Pol > &lhs, const RatFun< Pol > &rhs) const
    template<typename T >
     std::enable_if<!std::is_same< Formula< Pol >, T >::value, expr_type >::type operator() (const T &lhs, const
     CoeffType &coeff) const
    template<typename T >
     std::enable_if<!std::is_same< Formula< Pol >, T >::value, expr_type >::type operator() (const T &lhs, const
     RatFun < Pol > &rhs) const
    • template<typename T , typename U >
```

std::enable\_if<!std::is\_same< Formula< Pol >, T >::value, expr\_type >::type operator() (const T &lhs, const

std::enable\_if<!std::is\_same< Formula< Pol >, T >::value, expr\_type >::type operator() (const T &lhs, const

expr\_type operator() (const Formula < Pol > &lhs, const T &rhs) const

U &rhs) const

• template<typename T >

template<typename T >

Formula < Pol > &rhs) const

#### 12.292.1 Member Function Documentation

```
12.292.1.1 operator()() [1/10] template<typename Pol >
template<typename T >
expr_type carl::io::parser::ExpressionParser< Pol >::perform_division::operator() (
            const Formula< Pol > & lhs,
            const T & rhs ) const [inline]
12.292.1.2 operator()() [2/10] template<typename Pol >
expr_type carl::io::parser::ExpressionParser< Pol >::perform_division::operator() (
            const RatFun< Pol > & lhs,
            const CoeffType & rhs ) const [inline]
12.292.1.3 operator()() [3/10] template<typename Pol >
expr_type carl::io::parser::ExpressionParser< Pol >::perform_division::operator() (
            const RatFun< Pol > & lhs,
            const Monomial::Arg & rhs ) const [inline]
12.292.1.4 operator()() [4/10] template<typename Pol >
expr_type carl::io::parser::ExpressionParser< Pol >::perform_division::operator() (
            const RatFun< Pol > & lhs,
             const RatFun< Pol > & rhs ) const [inline]
12.292.1.5 operator()() [5/10] template<typename Pol >
template<typename T >
std::enable.if<!std::is.base.of<Formula<Pol>, T>::value, expr.type>::type carl::io::parser::ExpressionParser<
Pol >::perform_division::operator() (
            const RatFun< Pol > & lhs,
            const T & rhs ) const [inline]
12.292.1.6 operator()() [6/10] template<typename Pol >
expr_type carl::io::parser::ExpressionParser< Pol >::perform_division::operator() (
            const RatFun< Pol > & lhs,
            const Term< CoeffType > & rhs ) const [inline]
```

```
12.292.1.7 operator()() [7/10] template<typename Pol >
template<typename T >
std::enable_if<!std::is_same<Formula<Pol>, T>::value, expr_type>::type carl::io::parser::ExpressionParser<
Pol >::perform_division::operator() (
             const T & lhs,
             const CoeffType & coeff ) const [inline]
12.292.1.8 operator()() [8/10] template<typename Pol >
template < typename T >
std::enable_if<!std::is_same<Formula<Pol>, T>::value, expr_type>::type carl::io::parser::ExpressionParser<
Pol >::perform_division::operator() (
            const T & lhs,
             const Formula< Pol > & rhs ) const [inline]
12.292.1.9 operator()() [9/10] template<typename Pol >
template<typename T >
std::enable_if<!std::is_same<Formula<Pol>, T>::value, expr_type>::type carl::io::parser::ExpressionParser<
Pol >::perform_division::operator() (
             const T & lhs.
             const RatFun< Pol > & rhs ) const [inline]
12.292.1.10 operator()() [10/10] template<typename Pol >
template<typename T , typename U >
std::enable_if<!std::is_same<Formula<Pol>, T>::value, expr_type>::type carl::io::parser::ExpressionParser<
Pol >::perform_division::operator() (
             const T & lhs,
             const U & rhs ) const [inline]
12.293 carl::io::parser::ExpressionParser< Pol >::perform_multiplication Class
         Reference
#include <ExpressionParser.h>
Public Member Functions
   • template<typename T , typename U >
     std::enable_if<!std::is_same< Formula< Pol >, T >::value, expr_type >::type operator() (const T &lhs, const
     U &rhs) const
   • template<typename T >
     std::enable_if<!std::is_same< Formula< Pol >, T >::value, expr_type >::type operator() (const T &lhs, const
     RatFun< Pol > &rhs) const

    expr_type operator() (const RatFun< Pol > &lhs, const Monomial::Arg &rhs) const

    expr_type operator() (const RatFun< Pol > &lhs, const Term< CoeffType > &rhs) const

    expr_type operator() (const Monomial::Arg &lhs, const RatFun< Pol > &rhs) const
```

expr\_type operator() (const Term < CoeffType > &lhs, const RatFun < Pol > &rhs) const

std::enable\_if<!std::is\_same< Formula< Pol >, T >::value, expr\_type >::type operator() (const T &lhs, const

expr\_type operator() (const Formula < Pol > &lhs, const T &rhs) const

template<typename T >

template<typename T >

Formula < Pol > &rhs) const

#### 12.293.1 Member Function Documentation

```
12.293.1.1 operator()() [1/8] template<typename Pol >
template<typename T >
expr_type carl::io::parser::ExpressionParser< Pol >::perform_multiplication::operator() (
            const Formula < Pol > & lhs,
            const T & rhs ) const [inline]
12.293.1.2 operator()() [2/8] template<typename Pol >
expr_type carl::io::parser::ExpressionParser< Pol >::perform_multiplication::operator() (
            const Monomial::Arg & lhs,
             const RatFun< Pol > & rhs ) const [inline]
12.293.1.3 operator()() [3/8] template<typename Pol >
expr_type carl::io::parser::ExpressionParser< Pol >::perform_multiplication::operator() (
            const RatFun< Pol > & lhs,
             const Monomial::Arg & rhs ) const [inline]
12.293.1.4 operator()() [4/8] template<typename Pol >
expr_type carl::io::parser::ExpressionParser< Pol >::perform_multiplication::operator() (
            const RatFun< Pol > & lhs,
            const Term< CoeffType > & rhs ) const [inline]
12.293.1.5 operator()() [5/8] template<typename Pol >
template < typename T >
std::enable_if<!std::is_same<Formula<Pol>, T>::value, expr_type>::type carl::io::parser::ExpressionParser<
Pol >::perform_multiplication::operator() (
            const T & lhs,
            const Formula< Pol > & rhs ) const [inline]
12.293.1.6 operator()() [6/8] template<typename Pol >
template<typename T >
std::enable_if<!std::is_same<Formula<Pol>, T>::value, expr_type>::type carl::io::parser::ExpressionParser<
Pol >::perform_multiplication::operator() (
            const T & lhs,
            const RatFun< Pol > & rhs ) const [inline]
```

#### **Public Member Functions**

- template<typename T >
   expr\_type operator() (const T &lhs) const
   expr\_type operator() (const Formula< Pol > &lhs) const
- 12.294.1 Member Function Documentation

### 12.295 carl::io::parser::ExpressionParser< Pol >::perform\_power Class Reference

```
#include <ExpressionParser.h>
```

### **Public Member Functions**

```
    perform_power (exponent exp)
```

```
    template<typename T >
        expr_type operator() (const T &lhs) const
```

- expr\_type operator() (const RatFun< Pol > &lhs) const
- expr\_type operator() (const CoeffType &lhs) const
- expr\_type operator() (const Variable &lhs) const
- expr\_type operator() (const Monomial::Arg &lhs) const
- expr\_type operator() (const Formula < Pol > &lhs) const

#### Data Fields

exponent expVal

#### 12.295.1 Constructor & Destructor Documentation

### 12.295.2 Member Function Documentation

const Monomial::Arg & lhs ) const [inline]

#### 12.295.3 Field Documentation

```
12.295.3.1 expVal template<typename Pol >
exponent carl::io::parser::ExpressionParser< Pol >::perform_power::expVal
```

# 12.296 carl::io::parser::ExpressionParser< Pol >::perform\_subtraction Class Reference

#include <ExpressionParser.h>

### **Public Member Functions**

- template < typename T, typename U >
   expr\_type operator() (const T &lhs, const U &rhs) const
- expr\_type operator() (const CoeffType &lhs, const CoeffType &rhs) const
- expr\_type operator() (const RatFun< Pol > &lhs, const Monomial::Arg &rhs) const
- expr\_type operator() (const RatFun< Pol > &lhs, const Term< CoeffType > &rhs) const
- $\bullet \ \ \text{template}{<} \text{typename T} >$

• template<typename T >

- std::enable\_if<!std::is\_same< Formula< Pol >, T >::value, expr\_type >::type operator() (const RatFun< Pol > &lhs, const T &rhs) const
- std::enable\_if<!std::is\_same< Formula< Pol >, T >::value, expr\_type >::type operator() (const T &lhs, const RatFun< Pol > &rhs) const
- expr\_type operator() (const RatFun< Pol > &lhs, const RatFun< Pol > &rhs) const
- template<typename T >
   expr\_type operator() (const Formula< Pol > &lhs, const T &rhs) const
- template<typename T >
   std::enable\_if<!std::is\_same< Formula< Pol >, T >::value, expr\_type >::type operator() (const T &lhs, const Formula< Pol > &rhs) const

### 12.296.1 Member Function Documentation

```
12.296.1.1 operator()() [1/9] template<typename Pol >
expr_type carl::io::parser::ExpressionParser< Pol >::perform_subtraction::operator() (
            const CoeffType & lhs,
             const CoeffType & rhs ) const [inline]
12.296.1.2 operator()() [2/9] template<typename Pol >
template<typename T >
expr_type carl::io::parser::ExpressionParser< Pol >::perform_subtraction::operator() (
            const Formula < Pol > & lhs,
            const T & rhs ) const [inline]
12.296.1.3 operator()() [3/9] template<typename Pol >
expr_type carl::io::parser::ExpressionParser< Pol >::perform_subtraction::operator() (
            const RatFun< Pol > & lhs,
            const Monomial::Arg & rhs ) const [inline]
12.296.1.4 operator()() [4/9] template<typename Pol >
expr_type carl::io::parser::ExpressionParser< Pol >::perform_subtraction::operator() (
            const RatFun< Pol > & lhs,
             const RatFun< Pol > & rhs ) const [inline]
12.296.1.5 operator()() [5/9] template<typename Pol >
template < typename T >
std::enable_if<!std::is_same<Formula<Pol>, T>::value, expr_type>::type carl::io::parser::ExpressionParser<
Pol >::perform_subtraction::operator() (
            const RatFun< Pol > & lhs,
            const T & rhs ) const [inline]
12.296.1.6 operator()() [6/9] template<typename Pol >
expr_type carl::io::parser::ExpressionParser< Pol >::perform_subtraction::operator() (
            const RatFun< Pol > & lhs,
            const Term< CoeffType > & rhs ) const [inline]
```

```
12.296.1.7 operator()() [7/9] template<typename Pol >
template < typename T >
std::enable_if<!std::is_same<Formula<Pol>, T>::value, expr_type>::type carl::io::parser::ExpressionParser<
Pol >::perform_subtraction::operator() (
            const T & lhs,
            const Formula< Pol > & rhs ) const [inline]
12.296.1.8 operator()() [8/9] template<typename Pol >
template < typename T >
std::enable_if<!std::is_same<Formula<Pol>, T>::value, expr_type>::type carl::io::parser::ExpressionParser<
Pol >::perform_subtraction::operator() (
            const T & lhs,
            const RatFun< Pol > & rhs ) const [inline]
12.296.1.9 operator()() [9/9] template<typename Pol >
template<typename T , typename U >
expr_type carl::io::parser::ExpressionParser< Pol >::perform_subtraction::operator() (
            const T & lhs,
            const U & rhs ) const [inline]
```

### 12.297 carl::formula::symmetry::Permutation Struct Reference

```
#include <SymmetryFinder.h>
```

### **Data Fields**

• std::vector < std::vector < unsigned > > data

### 12.297.1 Field Documentation

```
12.297.1.1 data std::vector < std::vector < unsigned > carl::formula::symmetry::Permutation <math>\leftarrow ::data
```

### 12.298 carl::policies < Number, Interval > Struct Template Reference

Struct which holds the rounding and checking policies required for boost interval.

```
#include <Interval.h>
```

### **Public Types**

```
• using roundingP = carl::rounding< Number >
```

```
• using checkingP = carl::checking< Number >
```

#### **Static Public Member Functions**

• static void sanitize (Interval &)

### 12.298.1 Detailed Description

```
template<typename Number, typename Interval> struct carl::policies< Number, Interval>
```

Struct which holds the rounding and checking policies required for boost interval.

### 12.298.2 Member Typedef Documentation

```
12.298.2.1 checkingP template<typename Number , typename Interval > using carl::policies< Number, Interval >::checkingP = carl::checking<Number>
```

```
12.298.2.2 roundingP template<typename Number , typename Interval > using carl::policies< Number, Interval >::roundingP = carl::rounding<Number>
```

### 12.298.3 Member Function Documentation

### 12.299 carl::policies< double, Interval > Struct Template Reference

Template specialization for rounding and checking policies for native double.

```
#include <Interval.h>
```

### **Public Types**

- using roundingP = boost::numeric::interval\_lib::save\_state< boost::numeric::interval\_lib::rounded\_transc\_std</li>
   double > >
- using checkingP = boost::numeric::interval\_lib::checking\_no\_nan double, boost::numeric::interval\_lib
  ::checking\_no\_nan< double >>

### **Static Public Member Functions**

• static void sanitize (Interval &n)

### 12.299.1 Detailed Description

```
template<typename Interval> struct carl::policies< double, Interval >
```

Template specialization for rounding and checking policies for native double.

### 12.299.2 Member Typedef Documentation

```
12.299.2.1 checkingP template<typename Interval > using carl::policies< double, Interval >::checkingP = boost::numeric::interval_lib::checking-← no_nan<double, boost::numeric::interval_lib::checking_no_nan<double> >
```

```
12.299.2.2 roundingP template<typename Interval > using carl::policies< double, Interval >::roundingP = boost::numeric::interval_lib::save.← state<br/>
state<br/>
tounded_transc_std<double> >
```

### 12.299.3 Member Function Documentation

## 12.300 carl::PolynomialFactorizationPair< P > Class Template Reference

```
#include <PolynomialFactorizationPair.h>
```

### **Public Member Functions**

- PolynomialFactorizationPair ()=delete
- PolynomialFactorizationPair (Factorization< P > &&\_factorization, P \*\_polynomial=nullptr)
- PolynomialFactorizationPair (const PolynomialFactorizationPair &)=delete
- ∼PolynomialFactorizationPair ()
- PolynomialFactorizationPair & operator= (const PolynomialFactorizationPair &pfp)=default
- size\_t hash () const
- const auto & polynomial () const
- · void rehash () const

Updates the hash.

#### **Friends**

- class FactorizedPolynomial
- template<typename P1 >

P1 computePolynomial (const Factorization < P1 > &)

- template<typename P1 >
  - P1 computePolynomial (const PolynomialFactorizationPair < P1 > &)
- template<typename P1 >
   bool operator== (const PolynomialFactorizationPair< P1 > &\_polyFactA, const PolynomialFactorizationPair<
   P1 > &\_polyFactB)
- template<typename P1 >
   bool operator< (const PolynomialFactorizationPair< P1 > &\_polyFactA, const PolynomialFactorizationPair< P1 > &\_polyFactB)
- template < typename P1 >
  bool canBeUpdated (const PolynomialFactorizationPair < P1 > &\_toUpdate, const PolynomialFactorizationPair <
  P1 > &\_updateWith)
- template<typename P1 >
   void update (PolynomialFactorizationPair< P1 > &\_toUpdate, PolynomialFactorizationPair< P1 > &\_←
   updateWith)

Updates the first given polynomial factorization pair with the information stored in the second given polynomial factorization pair.

template<typename P1 >

Factorization< P1 > gcd (const PolynomialFactorizationPair< P1 > &\_pfPairA, const PolynomialFactorizationPair< P1 > &\_pfPairB, Factorization< P1 > &\_restB, typename P1::CoeffType &\_← coeff, bool &\_pfPairARefined, bool &\_pfPairBRefined)

Calculates the factorization of the gcd of the polynomial represented by the two given polynomial factorization pairs.

- template<typename P1 >
   Factors < FactorizedPolynomial < P1 > > factor (const PolynomialFactorizationPair < P1 > &\_pfPair, const typename P1::CoeffType &)
- template<typename P1 >
   std::ostream & operator<< (std::ostream &\_out, const PolynomialFactorizationPair< P1 > &\_pfPair)
   Prints the given polynomial-factorization pair on the given output stream.

### 12.300.1 Constructor & Destructor Documentation

```
12.300.1.2 PolynomialFactorizationPair() [2/3] template<typename P >
carl::PolynomialFactorizationPair < P >::PolynomialFactorizationPair (
             Factorization<br/>< P > && _factorization,
             P * \_polynomial = nullptr) [explicit]
12.300.1.3 PolynomialFactorizationPair() [3/3] template<typename P >
carl::PolynomialFactorizationPair < P >::PolynomialFactorizationPair (
             const PolynomialFactorizationPair< P > \& ) [delete]
12.300.1.4 ~PolynomialFactorizationPair() template<typename P >
\verb|carl::PolynomialFactorizationPair<|P>::\sim|PolynomialFactorizationPair||
12.300.2 Member Function Documentation
12.300.2.1 hash() template<typename P >
size_t carl::PolynomialFactorizationPair< P >::hash ( ) const [inline]
Returns
     The hash of this polynomial factorization pair.
12.300.2.2 operator=() template<typename P >
PolynomialFactorizationPair& carl::PolynomialFactorizationPair< P >::operator= (
             const PolynomialFactorizationPair< P > & pfp ) [default]
12.300.2.3 polynomial() template<typename P >
const auto& carl::PolynomialFactorizationPair< P >::polynomial ( ) const [inline]
12.300.2.4 rehash() template<typename P >
void carl::PolynomialFactorizationPair< P >::rehash ( ) const
Updates the hash.
12.300.3 Friends And Related Function Documentation
12.300.3.1 canBeUpdated template<typename P >
template<typename P1 >
bool canBeUpdated (
             const PolynomialFactorizationPair< P1 > & _toUpdate,
             const PolynomialFactorizationPair< P1 > & _updateWith ) [friend]
```

#### **Parameters**

| ₋toUpdate   | The polynomial factorization pair to be checked for the possibility to be updated. |
|-------------|--|
| _updateWith | The polynomial factorization pair used to update the first given one.              |

### Returns

true, if the first polynomial factorization pair can be updated with the second one.

### Returns

\_pfPair

A factorization of this factorized polynomial. (probably finer than the one factorization() returns)

```
12.300.3.5 FactorizedPolynomial < P > template < typename P > friend class FactorizedPolynomial < P > [friend]
```

The polynomial to calculate the factorization for.

Calculates the factorization of the gcd of the polynomial represented by the two given polynomial factorization pairs.

As a side effect the factorizations of these pairs can be refined. (c.f. Accelerating Parametric Probabilistic Verification, Algorithm 2)

#### **Parameters**

| _pfPairA        | The first polynomial factorization pair to calculate the gcd with.  |
|-----------------|---|
| _pfPairB        | The second polynomial factorization pair to calculate the gcd with.   |
| ₋restA          | The remaining factorization of the first polynomial without the gcd.  |
| ₋restB          | The remaining factorization of the second polynomial without the gcd.   |
| _coeff          |   |
| _pfPairARefined | A bool which is set to true, if the factorization of the first given polynomial factorization pair has been refined.  |
| _pfPairBRefined | A bool which is set to true, if the factorization of the second given polynomial factorization pair has been refined. |

### Returns

The factorization of the gcd of the polynomial represented by the two given polynomial factorization pairs.

#### **Parameters**

| _polyFactA | The first polynomial factorization pair to compare.  |
|------------|--|
| _polyFactB | The second polynomial factorization pair to compare. |

#### Returns

true, if the first given polynomial factorization pair is less than the second given polynomial factorization pair.

Prints the given polynomial-factorization pair on the given output stream.

#### **Parameters**

| _out    | The stream to print on.                     |
|---------|---|
| ₋pfPair | The polynomial-factorization pair to print. |

### Returns

The output stream after inserting the output.

### **Parameters**

| _polyFactA | The first polynomial factorization pair to compare.  |
|------------|--|
| _polyFactB | The second polynomial factorization pair to compare. |

### Returns

true, if the two given polynomial factorization pairs are equal.

Updates the first given polynomial factorization pair with the information stored in the second given polynomial factorization pair.

### **Parameters**

| ₋toUpdate   | The polynomial factorization pair to update with the second given one. |
|-------------|--|
| ₋updateWith | The polynomial factorization pair used to update the first given one.  |

### 12.301 carl::io::parser::PolynomialParser< Pol > Struct Template Reference

```
#include <PolynomialParser.h>
```

#### **Public Member Functions**

- · PolynomialParser ()
- void addVariable (Variable::Arg v)

### 12.301.1 Constructor & Destructor Documentation

```
12.301.1.1 PolynomialParser() template<typename Pol >
carl::io::parser::PolynomialParser< Pol >::PolynomialParser ( ) [inline]
```

#### 12.301.2 Member Function Documentation

### 12.302 carl::helper::PolynomialSubstitutor< Pol > Struct Template Reference

```
#include <Substitution.h>
```

### **Public Member Functions**

- PolynomialSubstitutor (const std::map< Variable, typename Formula< Pol >::PolynomialType > &repl)
- Formula < Pol > operator() (const Formula < Pol > &formula)

#### **Data Fields**

• const std::map< Variable, typename Formula< Pol >::PolynomialType > & replacements

#### 12.302.1 Constructor & Destructor Documentation

#### 12.302.2 Member Function Documentation

#### 12.302.3 Field Documentation

```
12.302.3.1 replacements template<typename Pol > const std::map<Variable,typename Formula<Pol>::PolynomialType>& carl::helper::PolynomialSubstitutor<
Pol >::replacements
```

### 12.303 carl::Pool < Element > Class Template Reference

```
#include <Pool.h>
```

### **Public Member Functions**

- · void print () const
- std::pair< typename FastPointerSet< Element >::iterator, bool > insert (ElementPtr \_element, bool \_assert ← Freshness=false)

Inserts the given element into the pool, if it does not yet occur in there.

ConstElementPtr add (ElementPtr \_element)

Adds the given element to the pool, if it does not yet occur in there.

### **Protected Member Functions**

- Pool (unsigned \_capacity=10000)
  - Constructor of the pool.
- ∼Pool ()
- virtual void assignId (ElementPtr, std::size\_t)

Assigns a unique id to the generated element.

### 12.303.1 Constructor & Destructor Documentation

Constructor of the pool.

#### **Parameters**

| _capacity | Expected necessary capacity of the pool. |
|-----------|--|
|-----------|--|

```
12.303.1.2 ~Pool() template<typename Element > carl::Pool< Element >::~Pool () [inline], [protected]
```

### 12.303.2 Member Function Documentation

Adds the given element to the pool, if it does not yet occur in there.

Note, that this method uses the allocator which is locked before calling.

#### **Parameters**

| the pool. | The element to add to the | ſ |
|-----------|---------------------------|---|
|-----------|---------------------------|---|

### Returns

The given element, if it did not yet occur in the pool; The equivalent element already occurring in the pool, otherwise.

Assigns a unique id to the generated element.

Note that this method serves as a callback for subclasses. The actual assignment of the id is done there.

#### **Parameters**

| ₋element | The element for which to add the id. |
|----------|--------------------------------------|
| ₋id      | A unique id.                         |

Reimplemented in carl::BVTermPool, and carl::BVConstraintPool.

Inserts the given element into the pool, if it does not yet occur in there.

### **Parameters**

| _element         | The element to add to the pool.   |
|------------------|---|
| ₋assertFreshness | When true, an assertion fails if the element is not fresh (i.e., if it already occurs in the pool). |

#### Returns

The position of the given element in the pool and true, if it did not yet occur in the pool; The position of the equivalent element in the pool and false, otherwise.

```
12.303.2.4 print() template<typename Element >
void carl::Pool< Element >::print ( ) const [inline]
```

### 12.304 carl::pool::Pool< Content > Class Template Reference

```
#include <Pool.h>
```

### **Public Member Functions**

- ∼Pool ()
- template<typename Key >
   std::shared\_ptr< PoolElementWrapper< Content > > add (Key &&c)

### **Static Public Member Functions**

static Pool < Content > & getInstance ()
 Returns the single instance of this class by reference.

### **Protected Member Functions**

- Pool (std::size\_t \_capacity=1000)
- void free (const PoolElementWrapper< Content > \*c)

### 12.304.1 Constructor & Destructor Documentation

### 12.304.2 Member Function Documentation

Returns the single instance of this class by reference.

Instance ( ) [inline], [static], [inherited]

If there is no instance yet, a new one is created.

### 12.305 carl::pool::PoolElement < Content > Class Template Reference

```
#include <Pool.h>
```

### **Public Member Functions**

- template<typename Key > PoolElement (Key &&k)
- const Content & operator() () const
- const Content & operator\* () const
- const Content \* operator-> () const
- auto id () const

### 12.305.1 Constructor & Destructor Documentation

#### 12.305.2 Member Function Documentation

```
12.305.2.1 id() template<class Content >
auto carl::pool::PoolElement< Content >::id ( ) const [inline]

12.305.2.2 operator()() template<class Content >
const Content& carl::pool::PoolElement< Content >::operator() ( ) const [inline]

12.305.2.3 operator*() template<class Content >
const Content& carl::pool::PoolElement< Content >::operator* ( ) const [inline]

12.305.2.4 operator->() template<class Content >
const Content* carl::pool::PoolElement< Content >::operator-> ( ) const [inline]
```

### 12.306 carl::pool::PoolElementWrapper< Content > Class Template Reference

```
#include <Pool.h>
```

#### **Public Member Functions**

- template<typename ... Args> PoolElementWrapper (Args &&...args)
- ∼PoolElementWrapper ()
- const Content & content () const
- · auto id () const

### 12.306.1 Constructor & Destructor Documentation

### 12.307 carl::tree\_detail::PostorderIterator< T, reverse > Struct Template Reference

Iterator class for post-order iterations over all elements.

```
#include <carlTree.h>
```

### **Public Types**

• using Base = Baselterator < T, PostorderIterator < T, reverse >, reverse >

### **Public Member Functions**

- PostorderIterator (const tree< T > \*t)
- PostorderIterator (const tree< T > \*t, std::size\_t root)
- PostorderIterator & next ()
- PostorderIterator & previous ()
- $\bullet \;\; {\sf template}{<} {\sf typename} \; {\sf It} >$

PostorderIterator (const BaseIterator< T, It, reverse > &ii)

- PostorderIterator (const PostorderIterator &ii)
- PostorderIterator (PostorderIterator &&ii)
- PostorderIterator & operator= (const PostorderIterator &it)
- PostorderIterator & operator= (PostorderIterator &&it)
- virtual ~PostorderIterator () noexcept=default
- const auto & nodes () const
- const auto & node (std::size\_t id) const
- const auto & curnode () const
- std::size\_t depth () const
- std::size\_t id () const
- bool isRoot () const
- bool isValid () const
- T \* operator-> ()
- T const \* operator-> () const

### **Data Fields**

• std::size\_t current

### **Protected Attributes**

const tree< T > \* mTree

### 12.307.1 Detailed Description

```
template<typename T, bool reverse = false>
struct carl::tree_detail::PostorderIterator< T, reverse >
```

Iterator class for post-order iterations over all elements.

### 12.307.2 Member Typedef Documentation

```
12.307.2.1 Base template<typename T , bool reverse = false>
using carl::tree_detail::PostorderIterator< T, reverse >::Base = BaseIterator<T, PostorderIterator<T,
reverse>, reverse>
```

#### 12.307.3 Constructor & Destructor Documentation

```
12.307.3.4 PostorderIterator() [4/5] template<typename T , bool reverse = false>
carl::tree_detail::PostorderIterator< T, reverse >::PostorderIterator (
            const PostorderIterator< T, reverse > & ii ) [inline]
12.307.3.5 PostorderIterator() [5/5] template<typename T , bool reverse = false>
carl::tree_detail::PostorderIterator< T, reverse >::PostorderIterator (
             PostorderIterator< T, reverse > && ii ) [inline]
12.307.3.6 \simPostorderIterator() template<typename T , bool reverse = false>
virtual carl::tree_detail::PostorderIterator< T, reverse >::~PostorderIterator ( ) [virtual],
[default], [noexcept]
12.307.4 Member Function Documentation
12.307.4.1 curnode() const auto& carl::tree_detail::BaseIterator< T, PostorderIterator< T,
false > , reverse >::curnode ( ) const [inline], [inherited]
12.307.4.2 depth() std::size_t carl::tree_detail::BaseIterator< T, PostorderIterator< T, false
> , reverse >::depth ( ) const [inline], [inherited]
12.307.4.3 id() std::size_t carl::tree_detail::BaseIterator< T, PostorderIterator< T, false > ,
reverse >::id ( ) const [inline], [inherited]
12.307.4.4 is Root() bool carl::tree_detail::BaseIterator< T, PostorderIterator< T, false > ,
reverse >::isRoot ( ) const [inline], [inherited]
12.307.4.5 isValid() bool carl::tree_detail::BaseIterator< T, PostorderIterator< T, false > ,
reverse >::isValid ( ) const [inline], [inherited]
```

```
12.307.4.6 next() template<typename T , bool reverse = false>
PostorderIterator& carl::tree_detail::PostorderIterator< T, reverse >::next ( ) [inline]
12.307.4.7 node() const auto& carl::tree_detail::BaseIterator< T, PostorderIterator< T, false
> , reverse >::node (
            std::size_t id ) const [inline], [inherited]
12.307.4.8 nodes() const auto& carl::tree_detail::BaseIterator< T, PostorderIterator< T, false
> , reverse >::nodes ( ) const [inline], [inherited]
12.307.4.9 operator->() [1/2] T* carl::tree_detail::BaseIterator< T, PostorderIterator< T,
false > , reverse >::operator-> ( ) [inline], [inherited]
12.307.4.10 operator->() [2/2] T const* carl::tree_detail::BaseIterator< T, PostorderIterator<
T, false > , reverse >::operator-> ( ) const [inline], [inherited]
12.307.4.11 operator=() [1/2] template<typename T , bool reverse = false>
PostorderIterator& carl::tree_detail::PostorderIterator< T, reverse >::operator= (
            const PostorderIterator< T, reverse > & it ) [inline]
12.307.4.12 operator=() [2/2] template<typename T , bool reverse = false>
PostorderIterator& carl::tree_detail::PostorderIterator< T, reverse >::operator= (
            PostorderIterator< T, reverse > && it ) [inline]
12.307.4.13 previous() template<typename T , bool reverse = false>
PostorderIterator& carl::tree_detail::PostorderIterator< T, reverse >::previous ( ) [inline]
```

### 12.307.5 Field Documentation

```
12.307.5.1 current std::size_t carl::tree_detail::BaseIterator< T, PostorderIterator< T, false > , reverse >::current [inherited]
```

```
12.307.5.2 mTree const tree<T>* carl::tree_detail::BaseIterator< T, PostorderIterator< T, false > , reverse >::mTree [protected], [inherited]
```

### 12.308 carl::tree\_detail::PreorderIterator< T, reverse > Struct Template Reference

Iterator class for pre-order iterations over all elements.

```
#include <carlTree.h>
```

### **Public Types**

using Base = BaseIterator < T, PreorderIterator < T, reverse >, reverse >

#### **Public Member Functions**

- PreorderIterator (const tree< T > \*t)
- PreorderIterator (const tree< T > \*t, std::size\_t root)
- PreorderIterator & next ()
- PreorderIterator & previous ()
- template<typename It , bool rev>

PreorderIterator (const BaseIterator< T, It, rev > &ii)

- PreorderIterator (const PreorderIterator &ii)
- PreorderIterator (PreorderIterator &&ii)
- PreorderIterator & operator= (const PreorderIterator &it)
- PreorderIterator & operator= (PreorderIterator &&it)
- virtual ~PreorderIterator () noexcept=default
- PreorderIterator & skipChildren ()
- · const auto & nodes () const
- const auto & node (std::size\_t id) const
- const auto & curnode () const
- std::size\_t depth () const
- std::size\_t id () const
- bool isRoot () const
- bool isValid () const
- T \* operator-> ()
- T const \* operator-> () const

### **Data Fields**

std::size\_t current

### **Protected Attributes**

const tree< T > \* mTree

### 12.308.1 Detailed Description

```
template<typename T, bool reverse = false> struct carl::tree_detail::PreorderIterator< T, reverse >
```

Iterator class for pre-order iterations over all elements.

### 12.308.2 Member Typedef Documentation

```
12.308.2.1 Base template<typename T , bool reverse = false>
using carl::tree_detail::PreorderIterator< T, reverse >::Base = BaseIterator<T, PreorderIterator<T, reverse>,
reverse>
```

#### 12.308.3 Constructor & Destructor Documentation

```
12.308.3.5 PreorderIterator() [5/5] template<typename T , bool reverse = false>
carl::tree_detail::PreorderIterator< T, reverse >::PreorderIterator (
            PreorderIterator< T, reverse > && ii ) [inline]
12.308.3.6 ~PreorderIterator() template<typename T , bool reverse = false>
virtual carl::tree_detail::PreorderIterator< T, reverse >::~PreorderIterator ( ) [virtual],
[default], [noexcept]
12.308.4 Member Function Documentation
12.308.4.1 curnode() const auto@ carl::tree_detail::BaseIterator< T, PreorderIterator< T,
false > , reverse >::curnode ( ) const [inline], [inherited]
12.308.4.2 depth() std::size_t carl::tree_detail::BaseIterator< T, PreorderIterator< T, false
> , reverse >::depth ( ) const [inline], [inherited]
12.308.4.3 id() std::size_t carl::tree_detail::BaseIterator< T, PreorderIterator< T, false > ,
reverse >::id ( ) const [inline], [inherited]
12.308.4.4 isRoot() bool carl::tree_detail::BaseIterator< T, PreorderIterator< T, false > ,
reverse >::isRoot ( ) const [inline], [inherited]
12.308.4.5 isValid() bool carl::tree_detail::BaseIterator< T, PreorderIterator< T, false > ,
reverse >::isValid ( ) const [inline], [inherited]
12.308.4.6 next() template<typename T , bool reverse = false>
PreorderIterator& carl::tree_detail::PreorderIterator< T, reverse >::next ( ) [inline]
12.308.4.7 node() const auto& carl::tree_detail::BaseIterator< T, PreorderIterator< T, false
> , reverse >::node (
            std::size_t id ) const [inline], [inherited]
```

```
12.308.4.8 nodes() const auto@ carl::tree_detail::BaseIterator< T, PreorderIterator< T, false
> , reverse >::nodes ( ) const [inline], [inherited]
12.308.4.9 operator->() [1/2] T* carl::tree_detail::BaseIterator< T, PreorderIterator< T, false
> , reverse >::operator-> ( ) [inline], [inherited]
12.308.4.10 operator->() [2/2] T const* carl::tree_detail::BaseIterator< T, PreorderIterator<
T, false > , reverse >::operator-> ( ) const [inline], [inherited]
12.308.4.11 operator=() [1/2] template<typename T , bool reverse = false>
PreorderIterator& carl::tree_detail::PreorderIterator< T, reverse >::operator= (
                                            const PreorderIterator< T, reverse > & it ) [inline]
12.308.4.12 operator=() [2/2] template<typename T , bool reverse = false>
PreorderIterator& carl::tree_detail::PreorderIterator< T, reverse >::operator= (
                                           PreorderIterator< T, reverse > && it ) [inline]
12.308.4.13 previous() template<typename T , bool reverse = false>
PreorderIterator& carl::tree_detail::PreorderIterator< T, reverse >::previous ( ) [inline]
12.308.4.14 skipChildren() template<typename T , bool reverse = false>
PreorderIterator& carl::tree_detail::PreorderIterator< T, reverse >::skipChildren ( ) [inline]
12.308.5 Field Documentation
12.308.5.1 current std::size_t carl::tree_detail::BaseIterator< T, PreorderIterator< T, false
 > , reverse >::current [inherited]
\textbf{12.308.5.2} \quad \textbf{mTree} \quad \texttt{const tree} < \texttt{T} > * \; \texttt{carl} : : \texttt{tree} \_ \texttt{detail} : : \texttt{BaseIterator} < \; \texttt{T} \text{, } \; \texttt{PreorderIterator} < \; \texttt{T} \text{, } \;
 false > , reverse >::mTree [protected], [inherited]
```

### 12.309 carl::PreventConversion< T > Class Template Reference

```
#include <typetraits.h>
```

#### **Public Member Functions**

- PreventConversion (const T &\_other)
- operator const T & () const

#### 12.309.1 Constructor & Destructor Documentation

### 12.309.2 Member Function Documentation

```
12.309.2.1 operator const T &() template<typename T >
carl::PreventConversion< T >::operator const T & ( ) const [inline]
```

### 12.310 carl::PrimeFactory< T > Class Template Reference

This class provides a convenient way to enumerate primes.

```
#include <PrimeFactory.h>
```

#### **Public Member Functions**

• std::size\_t size () const

Returns the number of already computed primes.

const T & operator[] (std::size\_t id) const

Provides const access to the computed primes. Asserts that id is smaller than size().

const T & operator[] (std::size\_t id)

Provides access to the computed primes. If id is at least size(), the missing primes are computed on-the-fly.

const T & next\_prime ()

Computed the next prime and returns it.

### 12.310.1 Detailed Description

```
\label{template} \begin{tabular}{ll} template < typename T > \\ class carl:: Prime Factory < T > \\ \end{tabular}
```

This class provides a convenient way to enumerate primes.

### 12.310.2 Member Function Documentation

```
12.310.2.1 next_prime() template<typename T >
const T & carl::PrimeFactory< T >::next_prime
```

Computed the next prime and returns it.

Provides access to the computed primes. If id is at least size(), the missing primes are computed on-the-fly.

Provides const access to the computed primes. Asserts that id is smaller than size().

```
12.310.2.4 size() template<typename T >
std::size_t carl::PrimeFactory< T >::size () const [inline]
```

Returns the number of already computed primes.

### 12.311 carl::io::parser::ExpressionParser< Pol >::print\_expr\_type Class Reference

```
#include <ExpressionParser.h>
```

### **Public Member Functions**

- void operator() (const RatFun< Pol > &expr) const
- void operator() (const Pol &expr) const
- void operator() (const Term < CoeffType > &expr) const
- void operator() (const Monomial::Arg &expr) const
- void operator() (const CoeffType &expr) const
- void operator() (const Variable &expr) const
- void operator() (const Formula < Pol > &expr) const

### 12.311.1 Member Function Documentation

```
12.311.1.1 operator()() [1/7] template<typename Pol >
void carl::io::parser::ExpressionParser< Pol >::print_expr_type::operator() (
            12.311.1.2 operator()() [2/7] template<typename Pol >
void carl::io::parser::ExpressionParser< Pol >::print_expr_type::operator() (
            const Formula< Pol > & expr ) const [inline]
12.311.1.3 operator()() [3/7] template<typename Pol >
void carl::io::parser::ExpressionParser< Pol >::print_expr_type::operator() (
            const Monomial::Arg & expr ) const [inline]
12.311.1.4 operator()() [4/7] template<typename Pol >
void carl::io::parser::ExpressionParser< Pol >::print_expr_type::operator() (
            const Pol & expr ) const [inline]
12.311.1.5 operator()() [5/7] template<typename Pol >
void carl::io::parser::ExpressionParser< Pol >::print_expr_type::operator() (
            const RatFun< Pol > & expr ) const [inline]
12.311.1.6 operator()() [6/7] template<typename Pol >
void carl::io::parser::ExpressionParser< Pol >::print_expr_type::operator() (
            const Term< CoeffType > & expr ) const [inline]
12.311.1.7 operator()() [7/7] template<typename Pol >
void carl::io::parser::ExpressionParser< Pol >::print_expr_type::operator() (
            const Variable & expr ) const [inline]
```

### 12.312 carl::io::QEPCADStream Class Reference

```
Public Member Functions
    • QEPCADStream ()
    • void initialize (const carlVariables &vars)
    • template<typename Pol >
      void initialize (std::initializer_list< Formula< Pol >> formulas)

    template<typename Pol >

      void assertFormula (const Formula < Pol > &formula)
    • template<typename T >
      QEPCADStream & operator << (T &&t)

    QEPCADStream & operator<< (std::ostream &(*os)(std::ostream &))</li>

    · auto content () const
12.312.1 Constructor & Destructor Documentation
12.312.1.1 QEPCADStream() carl::io::QEPCADStream::QEPCADStream ( ) [inline]
12.312.2 Member Function Documentation
```

```
12.312.2.1 assertFormula() template<typename Pol >
void carl::io::QEPCADStream::assertFormula (
                                                                                      const Formula < Pol > & formula ) [inline]
12.312.2.2 content() auto carl::io::QEPCADStream::content ( ) const [inline]
\textbf{12.312.2.3} \quad \textbf{initialize()} \; \texttt{[1/2]} \quad \texttt{void carl::io::QEPCADStream::initialize ()}
                                                                                        const carlVariables & vars ) [inline]
12.312.2.4 initialize() [2/2] template<typename Pol >
 void carl::io::QEPCADStream::initialize (
                                                                                        \textbf{12.312.2.5} \quad \textbf{operator} <<(\textbf{)} \; \texttt{[1/2]} \quad \texttt{QEPCADStream\& carl::io::QEPCADStream::operator} << \cdot (\textbf{)} \; \texttt{(1/2)} \; \texttt{(1/2)
```

std::ostream &(\*)(std::ostream &) os) [inline]

```
12.312.2.6 operator << () [2/2] template < typename T > QEPCADStream& carl::io::QEPCADStream::operator << ( T && t ) [inline]
```

### 12.313 carl::QuantifierContent< Pol > Struct Template Reference

Stores the variables and the formula bound by a quantifier.

```
#include <FormulaContent.h>
```

### **Public Member Functions**

- QuantifierContent (std::vector< carl::Variable > &&\_vars, Formula< Pol > &&\_formula)
   Constructs the content of a quantified formula.
- bool operator== (const QuantifierContent &\_qc) const
   Checks this content of a quantified formula and the given content of a quantified formula is equal.

### **Data Fields**

- std::vector < carl::Variable > mVariables
   The quantified variables.
- Formula < Pol > mFormula

The formula bound by this quantifier.

### 12.313.1 Detailed Description

```
template<typename Pol> struct carl::QuantifierContent< Pol>
```

Stores the variables and the formula bound by a quantifier.

### 12.313.2 Constructor & Destructor Documentation

```
12.313.2.1 QuantifierContent() template<typename Pol > carl::QuantifierContent < Pol >::QuantifierContent ( std::vector< carl::Variable > && .vars, Formula< Pol > && .formula ) [inline]
```

Constructs the content of a quantified formula.

#### **Parameters**

| ₋vars    | The quantified variables.             |
|----------|---------------------------------------|
| _formula | The formula bound by this quantifier. |

#### 12.313.3 Member Function Documentation

Checks this content of a quantified formula and the given content of a quantified formula is equal.

#### **Parameters**

 $_{-}qc$  The content of a quantified formula to check for equality.

### Returns

true, if this content of a quantified formula and the given content of a quantified formula is equal.

### 12.313.4 Field Documentation

```
12.313.4.1 mFormula template<typename Pol >
Formula<Pol> carl::QuantifierContent< Pol >::mFormula
```

The formula bound by this quantifier.

```
12.313.4.2 mVariables template<typename Pol > std::vector<carl::Variable> carl::QuantifierContent< Pol >::mVariables
```

The quantified variables.

### 12.314 carl::RadicalAwareAdding< Polynomial > Struct Template Reference

```
#include <GBUpdateProcedures.h>
```

## 12.315 carl::ran::interval::ran\_evaluator < Number > Class Template Reference

```
#include <ran_interval_extra.h>
```

### **Public Member Functions**

- ran\_evaluator (const MultivariatePolynomial < Number > &p)
- bool assign (const std::map< Variable, IntRepRealAlgebraicNumber< Number >> &m, bool refine\_←
  model=true)
- bool assign (Variable var, const IntRepRealAlgebraicNumber < Number > &ran, bool refine\_model=true)
- bool has\_value () const
- auto value ()

#### 12.315.1 Constructor & Destructor Documentation

```
12.315.1.1 ran_evaluator() template<typename Number > carl::ran::interval::ran_evaluator < Number >::ran_evaluator ( const MultivariatePolynomial< Number > & p ) [inline]
```

### 12.315.2 Member Function Documentation

### 12.316 carl::RationalFunction < Pol, AutoSimplify > Class Template Reference

```
#include <RationalFunction.h>
```

### **Public Types**

- using PolyType = Pol
- using CoeffType = typename Pol::CoeffType
- using NumberType = typename Pol::NumberType

#### **Public Member Functions**

- RationalFunction ()
- RationalFunction (int v)
- RationalFunction (const CoeffType &c)
- template < typename P = Pol, DisableIf < needs\_cache\_type < P >> = dummy > RationalFunction (Variable v)
- RationalFunction (const Pol &p)
- RationalFunction (Pol &&p)
- RationalFunction (const Pol &nom, const Pol &denom)
- RationalFunction (Pol &&nom, Pol &&denom)
- RationalFunction (std::optional < std::pair < Pol, Pol >> &&quotient, const CoeffType &num, bool simplified)
- RationalFunction (const RationalFunction &\_rf)=default
- RationalFunction (RationalFunction &&\_rf)=default
- ~RationalFunction () noexcept=default
- RationalFunction & operator= (const RationalFunction &\_rf)=default
- RationalFunction & operator= (RationalFunction &&\_rf)=default
- Pol nominator () const
- Pol denominator () const
- · const Pol & nominatorAsPolynomial () const
- · const Pol & denominatorAsPolynomial () const
- CoeffType nominatorAsNumber () const
- CoeffType denominatorAsNumber () const
- bool isSimplified () const

Checks if this rational function has been simplified since it's last modification.

- · void simplify ()
- · RationalFunction inverse () const

Returns the inverse of this rational function.

• bool is\_zero () const

Check whether the rational function is zero.

- bool is\_one () const
- bool is\_constant () const
- CoeffType constant\_part () const
- std::set < Variable > gatherVariables () const

Collect all occurring variables.

void gatherVariables (std::set< Variable > &vars) const

Add all occurring variables to the set vars.

CoeffType evaluate (const std::map< Variable, CoeffType > &substitutions) const

Evaluate the polynomial at the point described by substitutions.

- RationalFunction substitute (const std::map< Variable, CoeffType > &substitutions) const
- RationalFunction derivative (const Variable &x, unsigned nth=1) const

Derivative of the rational function with respect to variable x.

• std::string toString (bool infix=true, bool friendlyNames=true) const

### In-place addition operators

RationalFunction & operator+= (const RationalFunction &rhs)

Add something to this rational function and return the changed rational function.

RationalFunction & operator+= (const Pol &rhs)

Add something to this rational function and return the changed rational function.

RationalFunction & operator+= (const Term < CoeffType > &rhs)

Add something to this rational function and return the changed rational function.

RationalFunction & operator+= (const Monomial::Arg &rhs)

Add something to this rational function and return the changed rational function.

template<typename P = Pol, DisableIf< needs\_cache\_type< P >> = dummy>

RationalFunction & operator+= (Variable rhs)

Add something to this rational function and return the changed rational function.

RationalFunction & operator+= (const CoeffType &rhs)

Add something to this rational function and return the changed rational function.

#### In-place subtraction operators

RationalFunction & operator-= (const RationalFunction &rhs)

Subtract something from this rational function and return the changed rational function.

RationalFunction & operator-= (const Pol &rhs)

Subtract something from this rational function and return the changed rational function.

RationalFunction & operator-= (const Term < CoeffType > &rhs)

Subtract something from this rational function and return the changed rational function.

RationalFunction & operator-= (const Monomial::Arg &rhs)

Subtract something from this rational function and return the changed rational function.

template<typename P = Pol, DisableIf< needs\_cache\_type< P >> = dummy>

RationalFunction & operator-= (Variable rhs)

Subtract something from this rational function and return the changed rational function.

RationalFunction & operator-= (const CoeffType &rhs)

Subtract something from this rational function and return the changed rational function.

### In-place multiplication operators

RationalFunction & operator\*= (const RationalFunction &rhs)

Multiply something with this rational function and return the changed rational function.

RationalFunction & operator\*= (const Pol &rhs)

Multiply something with this rational function and return the changed rational function.

RationalFunction & operator\*= (const Term< CoeffType > &rhs)

Multiply something with this rational function and return the changed rational function.

RationalFunction & operator\*= (const Monomial::Arg &rhs)

Multiply something with this rational function and return the changed rational function.

template<typename P = Pol, DisableIf< needs\_cache\_type< P >> = dummy>

RationalFunction & operator\*= (Variable rhs)

Multiply something with this rational function and return the changed rational function.

RationalFunction & operator\*= (const CoeffType &rhs)

Multiply something with this rational function and return the changed rational function.

RationalFunction & operator\*= (carl::sint rhs)

Multiply something with this rational function and return the changed rational function.

### In-place division operators

RationalFunction & operator/= (const RationalFunction &rhs)

Divide this rational function by something and return the changed rational function.

RationalFunction & operator/= (const Pol &rhs)

Divide this rational function by something and return the changed rational function.

RationalFunction & operator/= (const Term< CoeffType > &rhs)

Divide this rational function by something and return the changed rational function.

RationalFunction & operator/= (const Monomial::Arg &rhs)

Divide this rational function by something and return the changed rational function.

• template<typename P = Pol, DisableIf< needs\_cache\_type< P >> = dummy>

RationalFunction & operator/= (Variable rhs)

Divide this rational function by something and return the changed rational function.

RationalFunction & operator/= (const CoeffType &rhs)

Divide this rational function by something and return the changed rational function.

RationalFunction & operator/= (unsigned long rhs)

Divide this rational function by something and return the changed rational function.

#### **Friends**

- template<typename PolA, bool ASA>
   bool operator== (const RationalFunction< PolA, ASA > &lhs, const RationalFunction< PolA, ASA > &rhs)
- template<typename PolA, bool ASA>
   bool operator< (const RationalFunction< PolA, ASA > &Ihs, const RationalFunction< PolA, ASA > &rhs)
- template<typename PolA, bool ASA>
   std::ostream & operator<< (std::ostream &os, const RationalFunction< PolA, ASA > &rhs)

#### 12.316.1 Member Typedef Documentation

```
12.316.1.1 CoeffType template<typename Pol , bool AutoSimplify = false> using carl::RationalFunction< Pol, AutoSimplify >::CoeffType = typename Pol::CoeffType
```

```
12.316.1.2 NumberType template<typename Pol , bool AutoSimplify = false> using carl::RationalFunction< Pol, AutoSimplify >::NumberType = typename Pol::NumberType
```

```
12.316.1.3 PolyType template<typename Pol , bool AutoSimplify = false> using carl::RationalFunction< Pol, AutoSimplify >::PolyType = Pol
```

# 12.316.2 Constructor & Destructor Documentation

```
12.316.2.1 RationalFunction() [1/11] template<typename Pol , bool AutoSimplify = false> carl::RationalFunction
Pol , AutoSimplify >::RationalFunction ( ) [inline]
```

```
12.316.2.2 RationalFunction() [2/11] template<typename Pol , bool AutoSimplify = false> carl::RationalFunction < Pol, AutoSimplify >::RationalFunction ( int v) [inline], [explicit]
```

```
12.316.2.4 RationalFunction() [4/11] template<typename Pol , bool AutoSimplify = false>
template<typename P = Pol, DisableIf< needs_cache_type< P >> = dummy>
\verb|carl::RationalFunction| < \verb|Pol|, AutoSimplify| > :: RationalFunction | (
            Variable v ) [inline], [explicit]
12.316.2.5 RationalFunction() [5/11] template<typename Pol , bool AutoSimplify = false>
carl::RationalFunction< Pol, AutoSimplify >::RationalFunction (
             const Pol & p ) [inline], [explicit]
12.316.2.6 RationalFunction() [6/11] template<typename Pol , bool AutoSimplify = false>
carl::RationalFunction< Pol, AutoSimplify >::RationalFunction (
             Pol && p ) [inline], [explicit]
12.316.2.7 RationalFunction() [7/11] template<typename Pol , bool AutoSimplify = false>
carl::RationalFunction< Pol, AutoSimplify >::RationalFunction (
             const Pol & nom,
            const Pol & denom ) [inline], [explicit]
12.316.2.8 RationalFunction() [8/11] template<typename Pol , bool AutoSimplify = false>
carl::RationalFunction< Pol, AutoSimplify >::RationalFunction (
             Pol && nom,
             Pol && denom ) [inline], [explicit]
12.316.2.9 RationalFunction() [9/11] template<typename Pol , bool AutoSimplify = false>
carl::RationalFunction< Pol, AutoSimplify >::RationalFunction (
             std::optional< std::pair< Pol, Pol >> && quotient,
             const CoeffType & num,
             bool simplified ) [inline], [explicit]
12.316.2.10 RationalFunction() [10/11] template<typename Pol , bool AutoSimplify = false>
carl::RationalFunction< Pol, AutoSimplify >::RationalFunction (
             const RationalFunction< Pol, AutoSimplify > & _rf ) [default]
12.316.2.11 RationalFunction() [11/11] template<typename Pol , bool AutoSimplify = false>
carl::RationalFunction< Pol, AutoSimplify >::RationalFunction (
             RationalFunction< Pol, AutoSimplify > && _rf ) [default]
```

```
12.316.2.12 ~RationalFunction() template<typename Pol , bool AutoSimplify = false> carl::RationalFunction
Pol , AutoSimplify >::~RationalFunction ( ) [default], [noexcept]
```

#### 12.316.3 Member Function Documentation

```
12.316.3.1 constant_part() template<typename Pol , bool AutoSimplify = false>
CoeffType carl::RationalFunction< Pol, AutoSimplify >::constant_part () const [inline]
```

```
12.316.3.2 denominator() template<typename Pol , bool AutoSimplify = false>
Pol carl::RationalFunction< Pol, AutoSimplify >::denominator ( ) const [inline]
```

#### Returns

The denominator

```
12.316.3.3 denominatorAsNumber() template<typename Pol , bool AutoSimplify = false>
CoeffType carl::RationalFunction< Pol, AutoSimplify >::denominatorAsNumber () const [inline]
```

#### Returns

The denominator as a polynomial.

```
12.316.3.4 denominatorAsPolynomial() template<typename Pol , bool AutoSimplify = false> const Pol& carl::RationalFunction< Pol, AutoSimplify >::denominatorAsPolynomial ( ) const [inline]
```

# Returns

The denominator as a polynomial.

Derivative of the rational function with respect to variable x.

| X   | the main variable                |  |
|-----|----------------------------------|--|
| nth | which derivative one should take |  |

#### Returns

**Todo** Currently only nth = 1 is supported

Curretnly only factorized polynomials are supported

Evaluate the polynomial at the point described by substitutions.

#### **Parameters**

#### Returns

The result of the substitution

```
12.316.3.7 gatherVariables() [1/2] template<typename Pol , bool AutoSimplify = false> std::set<Variable> carl::RationalFunction< Pol, AutoSimplify >::gatherVariables ( ) const [inline]
```

Collect all occurring variables.

#### Returns

All occcurring variables

Add all occurring variables to the set vars.

| I | Pa | ra | m | P | þ | rc |
|---|----|----|---|---|---|----|
|   |    |    |   |   |   |    |

vars

```
12.316.3.9 inverse() template<typename Pol , bool AutoSimplify = false>
RationalFunction carl::RationalFunction< Pol, AutoSimplify >::inverse ( ) const [inline]
```

Returns the inverse of this rational function.

#### Returns

Inverse of this.

```
12.316.3.10 is_constant() template<typename Pol , bool AutoSimplify = false> bool carl::RationalFunction< Pol, AutoSimplify >::is_constant ( ) const [inline]
```

```
12.316.3.11 is_one() template<typename Pol , bool AutoSimplify = false> bool carl::RationalFunction< Pol, AutoSimplify >::is_one () const [inline]
```

```
12.316.3.12 is zero() template<typename Pol , bool AutoSimplify = false> bool carl::RationalFunction< Pol, AutoSimplify >::is_zero () const [inline]
```

Check whether the rational function is zero.

#### Returns

true if it is

```
12.316.3.13 isSimplified() template<typename Pol , bool AutoSimplify = false> bool carl::RationalFunction< Pol, AutoSimplify >::isSimplified () const [inline]
```

Checks if this rational function has been simplified since it's last modification.

Note that if AutoSimplify is true, this should always return true.

#### Returns

If this is simplified.

```
12.316.3.14 nominator() template<typename Pol , bool AutoSimplify = false>
Pol carl::RationalFunction< Pol, AutoSimplify >::nominator ( ) const [inline]
```

#### Returns

The nominator

```
12.316.3.15 nominatorAsNumber() template<typename Pol , bool AutoSimplify = false>
CoeffType carl::RationalFunction< Pol, AutoSimplify >::nominatorAsNumber () const [inline]
```

#### Returns

The nominator as a polynomial.

```
12.316.3.16 nominatorAsPolynomial() template<typename Pol , bool AutoSimplify = false> const Pol& carl::RationalFunction< Pol, AutoSimplify >::nominatorAsPolynomial ( ) const [inline]
```

#### Returns

The nominator as a polynomial.

Multiply something with this rational function and return the changed rational function.

#### **Parameters**

```
rhs Right hand side.
```

# Returns

Changed rational function.

Multiply something with this rational function and return the changed rational function.

rhs Right hand side.

#### Returns

Changed rational function.

Multiply something with this rational function and return the changed rational function.

# **Parameters**

```
rhs Right hand side.
```

#### Returns

Changed rational function.

Multiply something with this rational function and return the changed rational function.

#### **Parameters**

```
rhs Right hand side.
```

# Returns

Changed rational function.

Multiply something with this rational function and return the changed rational function.

rhs Right hand side.

#### Returns

Changed rational function.

Multiply something with this rational function and return the changed rational function.

# **Parameters**

rhs Right hand side.

#### Returns

Changed rational function.

Multiply something with this rational function and return the changed rational function.

# **Parameters**

```
rhs Right hand side.
```

#### Returns

Changed rational function.

Add something to this rational function and return the changed rational function.

```
rhs Right hand side.
```

#### Returns

Changed rational function.

Add something to this rational function and return the changed rational function.

# **Parameters**

```
rhs Right hand side.
```

#### Returns

Changed rational function.

Add something to this rational function and return the changed rational function.

#### **Parameters**

```
rhs Right hand side.
```

# Returns

Changed rational function.

Add something to this rational function and return the changed rational function.

rhs Right hand side.

#### Returns

Changed rational function.

Add something to this rational function and return the changed rational function.

#### **Parameters**

rhs Right hand side.

#### Returns

Changed rational function.

Add something to this rational function and return the changed rational function.

# **Parameters**

```
rhs Right hand side.
```

#### Returns

Changed rational function.

Subtract something from this rational function and return the changed rational function.

rhs Right hand side.

#### Returns

Changed rational function.

Subtract something from this rational function and return the changed rational function.

# **Parameters**

rhs Right hand side.

#### Returns

Changed rational function.

Subtract something from this rational function and return the changed rational function.

#### **Parameters**

rhs Right hand side.

# Returns

Changed rational function.

Subtract something from this rational function and return the changed rational function.

rhs Right hand side.

#### Returns

Changed rational function.

```
12.316.3.34 operator-=() [5/6] template<typename Pol , bool AutoSimplify = false> RationalFunction& carl::RationalFunction< Pol, AutoSimplify >::operator-= ( const Term< CoeffType > & rhs ) [inline]
```

Subtract something from this rational function and return the changed rational function.

#### **Parameters**

rhs Right hand side.

#### Returns

Changed rational function.

Subtract something from this rational function and return the changed rational function.

# **Parameters**

```
rhs Right hand side.
```

#### Returns

Changed rational function.

Divide this rational function by something and return the changed rational function.

rhs Right hand side.

#### Returns

Changed rational function.

```
12.316.3.37 operator/=() [2/7] template<typename Pol , bool AutoSimplify = false> RationalFunction& carl::RationalFunction< Pol, AutoSimplify >::operator/= ( const Monomial::Arg & rhs ) [inline]
```

Divide this rational function by something and return the changed rational function.

# **Parameters**

rhs Right hand side.

#### Returns

Changed rational function.

Divide this rational function by something and return the changed rational function.

#### **Parameters**

rhs Right hand side.

# Returns

Changed rational function.

Divide this rational function by something and return the changed rational function.

rhs Right hand side.

#### Returns

Changed rational function.

```
12.316.3.40 operator/=() [5/7] template<typename Pol , bool AutoSimplify = false> RationalFunction& carl::RationalFunction< Pol, AutoSimplify >::operator/= ( const Term< CoeffType > & rhs ) [inline]
```

Divide this rational function by something and return the changed rational function.

#### **Parameters**

rhs Right hand side.

#### Returns

Changed rational function.

```
12.316.3.41 operator/=() [6/7] template<typename Pol , bool AutoSimplify = false> RationalFunction& carl::RationalFunction<<pre>Pol , AutoSimplify >::operator/= (
          unsigned long rhs )
```

Divide this rational function by something and return the changed rational function.

#### **Parameters**

rhs Right hand side.

# Returns

Changed rational function.

Divide this rational function by something and return the changed rational function.

```
rhs Right hand side.
```

#### Returns

Changed rational function.

```
12.316.3.44 operator=() [2/2] template<typename Pol , bool AutoSimplify = false>
RationalFunction& carl::RationalFunction< Pol, AutoSimplify >::operator= (
RationalFunction< Pol, AutoSimplify > && _rf ) [default]
```

```
12.316.3.45 simplify() template<typename Pol , bool AutoSimplify = false> void carl::RationalFunction< Pol, AutoSimplify >::simplify ( ) [inline]
```

#### 12.316.4 Friends And Related Function Documentation

# 12.317 carl::io::parser::RationalFunctionParser< Pol > Struct Template Reference

#include <RationalFunctionParser.h>

#### **Public Member Functions**

- RationalFunctionParser ()
- void addVariable (Variable::Arg v)

# 12.317.1 Constructor & Destructor Documentation

```
12.317.1.1 RationalFunctionParser() template<typename Pol > carl::io::parser::RationalFunctionParser< Pol >::RationalFunctionParser ( ) [inline]
```

#### 12.317.2 Member Function Documentation

# 12.318 carl::parser::RationalParser< T, Iterator > Struct Template Reference

Parses rationals, being two decimals separated by a slash.

```
#include <parser.h>
```

#### **Public Member Functions**

- · RationalParser ()
- T makeRational (const T &a, const boost::optional < T > &b) const

#### **Data Fields**

- DecimalParser< T > number
- qi::rule< Iterator, T(), Skipper > main

#### 12.318.1 Detailed Description

```
template<typename T, typename Iterator = std::string::const_iterator> struct carl::parser::RationalParser< T, Iterator>
```

Parses rationals, being two decimals separated by a slash.

#### 12.318.2 Constructor & Destructor Documentation

```
12.318.2.1 RationalParser() template<typename T , typename Iterator = std::string::const. ← iterator>
carl::parser::RationalParser< T, Iterator >::RationalParser ( ) [inline]
```

# 12.318.3 Member Function Documentation

#### 12.318.4 Field Documentation

```
12.318.4.1 main template<typename T , typename Iterator = std::string::const_iterator> qi::rule<Iterator, T(), Skipper> carl::parser::RationalParser< T, Iterator >::main
```

```
12.318.4.2 number template<typename T , typename Iterator = std::string::const_iterator>
DecimalParser<T> carl::parser::RationalParser< T, Iterator >::number
```

# 12.319 carl::io::parser::RationalPolicies < Coeff > Struct Template Reference

```
#include <Common.h>
```

# **Static Public Member Functions**

- template<typename It , typename Attr >
   static bool parse\_nan (It &, It const &, Attr &)
- template<typename It , typename Attr >
   static bool parse\_inf (It &, It const &, Attr &)

#### 12.319.1 Member Function Documentation

# 12.320 carl::parser::RationalPolicies < T > Struct Template Reference

Specialization of qi::real\_policies for our rational types.

```
#include <parser.h>
```

#### **Static Public Member Functions**

- template<typename It >
   static bool parse\_dot (It &first, const It &last)
- template < typename It , typename Attr >
   static bool parse\_frac\_n (It &first, const It &last, Attr &attr)
- template<typename It , typename Attr >
   static bool parse\_exp\_n (It &first, const It &last, Attr &attr\_)
- template<typename It , typename Attr >
   static bool parse\_nan (It &, const It &, Attr &)
- template<typename It , typename Attr >
   static bool parse\_inf (It &, const It &, Attr &)

#### **Static Public Attributes**

- static constexpr bool T\_is\_int = carl::is\_subset\_of\_integers\_type<T>::value
- static constexpr bool allow\_leading\_dot = true
- static constexpr bool allow\_trailing\_dot = true
- static constexpr bool expect\_dot = false

# 12.320.1 Detailed Description

```
template<typename T> struct carl::parser::RationalPolicies< T >
```

Specialization of qi::real\_policies for our rational types.

Specifies that neither NaN nor Inf is allowed.

#### 12.320.2 Member Function Documentation

```
12.320.2.1 parse_dot() template<typename T >
{\tt template}{<}{\tt typename}~{\tt It}~{>}
static bool carl::parser::RationalPolicies< T >::parse_dot (
            It & first,
             const It & last ) [inline], [static]
12.320.2.2 parse_exp_n() template<typename T >
template<typename It , typename Attr >
static bool carl::parser::RationalPolicies< T >::parse_exp_n (
             It & first,
             const It & last,
             Attr & attr.) [inline], [static]
12.320.2.3 parse_frac_n() template<typename T >
template<typename It , typename Attr >
static bool carl::parser::RationalPolicies< T >::parse_frac_n (
             It & first,
             const It & last,
             Attr & attr ) [inline], [static]
```

```
12.320.2.4 parse_inf() template<typename T >
template<typename It , typename Attr >
static bool carl::parser::RationalPolicies< T >::parse_inf (
            It & ,
            const It & ,
            Attr & ) [inline], [static]
12.320.2.5 parse_nan() template<typename T >
template<typename It , typename Attr >
static bool carl::parser::RationalPolicies< T >::parse_nan (
            It & ,
            const It & ,
            Attr & ) [inline], [static]
12.320.3 Field Documentation
12.320.3.1 allow_leading_dot template<typename T >
constexpr bool carl::parser::RationalPolicies< T >::allow_leading_dot = true [static], [constexpr]
12.320.3.2 allow_trailing_dot template<typename T >
constexpr bool carl::parser::RationalPolicies< T >::allow_trailing_dot = true [static], [constexpr]
12.320.3.3 expect_dot template<typename T >
constexpr bool carl::parser::RationalPolicies< T >::expect_dot = false [static], [constexpr]
12.320.3.4 T_is_int template<typename T >
constexpr bool carl::parser::RationalPolicies< T >::T_is_int = carl::is_subset_of_integers_type<T>↔
::value [static], [constexpr]
12.321
        carl::RealAlgebraicNumber < Number > Class Template Reference
```

# 12.322 carl::RealAlgebraicNumberThom< Number > Struct Template Reference

```
#include <ran_thom.h>
```

#### **Public Member Functions**

- RealAlgebraicNumberThom (const ThomEncoding< Number > &te)
- auto & thom\_encoding ()
- const auto & thom\_encoding () const
- · const auto & polynomial () const
- const auto & main\_var () const
- auto sign\_condition () const
- · const auto & point () const
- std::size\_t bitsize () const
- std::size\_t dimension () const
- bool is\_integral () const
- bool is\_zero () const
- bool contained\_in (const Interval< Number > &i) const
- Number integer\_below () const
- Sign sgn () const
- Sign sgn (const UnivariatePolynomial< Number > &p) const

#### **Friends**

- template<typename Num >
   bool operator== (const RealAlgebraicNumberThom< Num > &lhs, const RealAlgebraicNumberThom< Num > &rhs)
- template<typename Num >
   bool operator< (const RealAlgebraicNumberThom< Num > &lhs, const RealAlgebraicNumberThom< Num > &rhs)

# 12.322.1 Constructor & Destructor Documentation

```
12.322.1.1 RealAlgebraicNumberThom() template<typename Number > carl::RealAlgebraicNumberThom< Number >::RealAlgebraicNumberThom ( const ThomEncoding< Number > & te ) [inline]
```

# 12.322.2 Member Function Documentation

```
12.322.2.3 dimension() template<typename Number >
std::size_t carl::RealAlgebraicNumberThom< Number >::dimension ( ) const [inline]
12.322.2.4 integer_below() template<typename Number >
Number carl::RealAlgebraicNumberThom< Number >::integer_below ( ) const [inline]
12.322.2.5 is_integral() template<typename Number >
bool carl::RealAlgebraicNumberThom< Number >::is_integral ( ) const [inline]
12.322.2.6 is zero() template<typename Number >
bool carl::RealAlgebraicNumberThom< Number >::is.zero ( ) const [inline]
12.322.2.7 main_var() template<typename Number >
const auto& carl::RealAlgebraicNumberThom< Number >::main_var ( ) const [inline]
12.322.2.8 point() template<typename Number >
const auto& carl::RealAlgebraicNumberThom< Number >::point ( ) const [inline]
12.322.2.9 polynomial() template<typename Number >
const auto@ carl::RealAlgebraicNumberThom< Number >::polynomial ( ) const [inline]
12.322.2.10 sgn() [1/2] template<typename Number >
Sign carl::RealAlgebraicNumberThom< Number >::sgn ( ) const [inline]
12.322.2.11 sgn() [2/2] template<typename Number >
Sign carl::RealAlgebraicNumberThom< Number >::sgn (
            const UnivariatePolynomial< Number > & p ) const [inline]
```

```
12.322.2.12 sign_condition() template<typename Number >
auto carl::RealAlgebraicNumberThom< Number >::sign_condition ( ) const [inline]

12.322.2.13 thom_encoding() [1/2] template<typename Number >
auto& carl::RealAlgebraicNumberThom< Number >::thom_encoding ( ) [inline]

12.322.2.14 thom_encoding() [2/2] template<typename Number >
const auto& carl::RealAlgebraicNumberThom< Number >::thom_encoding ( ) const [inline]
```

#### 12.322.3 Friends And Related Function Documentation

# 12.323 carl::RealRadicalAwareAdding< Polynomial > Struct Template Reference

```
#include <GBUpdateProcedures.h>
```

#### **Public Member Functions**

- virtual ∼RealRadicalAwareAdding ()
- bool addToGb (const Polynomial &p, std::shared\_ptr< | Idea|< Polynomial >> gb, UpdateFnc \*update)

#### 12.323.1 Constructor & Destructor Documentation

```
12.323.1.1 ~RealRadicalAwareAdding() template<typename Polynomial > virtual carl::RealRadicalAwareAdding Polynomial >::~RealRadicalAwareAdding () [inline], [virtual]
```

#### 12.323.2 Member Function Documentation

# 12.324 carl::ran::interval::RealRootIsolation < Number > Class Template Reference

Compact class to isolate real roots from a univariate polynomial using bisection.

```
#include <RealRootIsolation.h>
```

#### **Public Member Functions**

- RealRootIsolation (const UnivariatePolynomial < Number > &polynomial, const Interval < Number > &interval)
- std::vector < IntRepRealAlgebraicNumber < Number > > get\_roots ()
   Compute and sort the roots of mPolynomial within mInterval.

# 12.324.1 Detailed Description

```
template<typename Number> class carl::ran::interval::RealRootIsolation< Number >
```

Compact class to isolate real roots from a univariate polynomial using bisection.

After some rather easy preprocessing (make polynomial square-free, eliminate zero roots, solve low-degree polynomial trivially, use root bounds to shrink the interval) we employ bisection which can optionally be initialized by approximations.

#### 12.324.2 Constructor & Destructor Documentation

#### 12.324.3 Member Function Documentation

```
12.324.3.1 get_roots() template<typename Number >
std::vector<IntRepRealAlgebraicNumber<Number> > carl::ran::interval::RealRootIsolation
Number >::get_roots () [inline]
```

Compute and sort the roots of mPolynomial within mInterval.

# 12.325 carl::RealRootsResult < RAN > Class Template Reference

```
#include <RealRoots.h>
```

# **Public Types**

using roots\_t = std::vector< RAN >

#### **Public Member Functions**

- bool is\_nullified () const
- bool is\_univariate () const
- bool is\_non\_univariate () const
- const roots\_t & roots () const

### **Static Public Member Functions**

- static RealRootsResult nullified\_response ()
- static RealRootsResult non\_univariate\_response ()
- static RealRootsResult roots\_response (roots\_t &&real\_roots)
- static RealRootsResult no\_roots\_response ()

### 12.325.1 Member Typedef Documentation

```
12.325.1.1 roots_t template<typename RAN >
using carl::RealRootsResult< RAN >::roots_t = std::vector<RAN>
```

#### 12.325.2 Member Function Documentation

```
12.325.2.1 is_non_univariate() template<typename RAN >
bool carl::RealRootsResult< RAN >::is_non_univariate ( ) const [inline]
12.325.2.2 is_nullified() template<typename RAN >
bool carl::RealRootsResult< RAN >::is_nullified ( ) const [inline]
12.325.2.3 is_univariate() template<typename RAN >
bool carl::RealRootsResult< RAN >::is_univariate ( ) const [inline]
12.325.2.4 no_roots_response() template<typename RAN >
static RealRootsResult carl::RealRootsResult< RAN >::no_roots_response ( ) [inline], [static]
12.325.2.5 non_univariate_response() template<typename RAN >
static RealRootsResult carl::RealRootsResult< RAN >::non_univariate_response ( ) [inline],
[static]
12.325.2.6 nullified_response() template<typename RAN >
static RealRootsResult carl::RealRootsResult< RAN >::nullified_response ( ) [inline], [static]
12.325.2.7 roots() template<typename RAN >
const roots_t& carl::RealRootsResult< RAN >::roots ( ) const [inline]
12.325.2.8 roots_response() template<typename RAN >
static RealRootsResult carl::RealRootsResult < RAN >::roots_response (
            roots_t && real_roots ) [inline], [static]
```

# 12.326 carl::logging::RecordInfo Struct Reference

Additional information about a log message.

```
#include <logging.h>
```

#### **Data Fields**

• std::string filename

File name.

std::string func

Function name.

• std::size\_t line

Line number.

# 12.326.1 Detailed Description

Additional information about a log message.

#### 12.326.2 Field Documentation

```
12.326.2.1 filename std::string carl::logging::RecordInfo::filename
```

File name.

```
12.326.2.2 func std::string carl::logging::RecordInfo::func
```

Function name.

```
12.326.2.3 line std::size_t carl::logging::RecordInfo::line
```

Line number.

# 12.327 carl::Reductor< InputPolynomial, PolynomialInIdeal, Datastructure, Configuration > Class Template Reference

A dedicated algorithm for calculating the remainder of a polynomial modulo a set of other polynomials.

```
#include <Reductor.h>
```

# **Public Member Functions**

- Reductor (const Ideal < PolynomialInIdeal > &ideal, const InputPolynomial &f)
- Reductor (const Ideal< PolynomialInIdeal > &ideal, const Term< Coeff > &f)
- virtual ∼Reductor ()=default
- bool reduce ()

The basic reduce routine on a priority queue.

bool reductionOccured ()

Gets the flag which indicates that a reduction has occurred ( $p \rightarrow p'$  with  $p' \neq p$ )

• InputPolynomial fullReduce ()

Uses the ideal to reduce a polynomial as far as possible.

# **Protected Types**

- using Order = typename InputPolynomial::OrderedBy
- using EntryType = typename Configuration < InputPolynomial >::EntryType
- using Coeff = typename InputPolynomial::CoeffType

#### 12.327.1 Detailed Description

template<typename InputPolynomial, typename PolynomialInIdeal, template< class > class Datastructure = carl::Heap, template< typename Polynomial > class Configuration = ReductorConfiguration> class carl::Reductor< InputPolynomial, PolynomialInIdeal, Datastructure, Configuration >

A dedicated algorithm for calculating the remainder of a polynomial modulo a set of other polynomials.

#### 12.327.2 Member Typedef Documentation

```
12.327.2.1 Coeff template<typename InputPolynomial , typename PolynomialInIdeal , template<
class > class Datastructure = carl::Heap, template< typename Polynomial > class Configuration
= ReductorConfiguration>
using carl::Reductor< InputPolynomial, PolynomialInIdeal, Datastructure, Configuration >←
::Coeff = typename InputPolynomial::CoeffType [protected]
```

```
12.327.2.2 EntryType template<typename InputPolynomial , typename PolynomialInIdeal , template< class > class Datastructure = carl::Heap, template< typename Polynomial > class Configuration = ReductorConfiguration>
using carl::Reductor< InputPolynomial, PolynomialInIdeal, Datastructure, Configuration > 
::EntryType = typename Configuration<InputPolynomial>::EntryType [protected]
```

```
12.327.2.3 Order template<typename InputPolynomial , typename PolynomialInIdeal , template< class > class Datastructure = carl::Heap, template< typename Polynomial > class Configuration = ReductorConfiguration> using carl::Reductor< InputPolynomial, PolynomialInIdeal, Datastructure, Configuration > ∴ :Order = typename InputPolynomial::OrderedBy [protected]
```

# 12.327.3 Constructor & Destructor Documentation

#### 12.327.4 Member Function Documentation

::~Reductor ( ) [virtual], [default]

= ReductorConfiguration>

```
12.327.4.1 fullReduce() template<typename InputPolynomial , typename PolynomialInIdeal , template< class > class Datastructure = carl::Heap, template< typename Polynomial > class Configuration = ReductorConfiguration>
InputPolynomial carl::Reductor< InputPolynomial, PolynomialInIdeal, Datastructure, Configuration >::fullReduce ( ) [inline]
```

Uses the ideal to reduce a polynomial as far as possible.

Returns

```
12.327.4.2 reduce() template<typename InputPolynomial , typename PolynomialInIdeal , template< class > class Datastructure = carl::Heap, template< typename Polynomial > class Configuration = ReductorConfiguration> bool carl::Reductor< InputPolynomial, PolynomialInIdeal, Datastructure, Configuration > ::reduce () [inline]
```

The basic reduce routine on a priority queue.

Returns

12.327.4.3 reductionOccured() template<typename InputPolynomial , typename PolynomialInIdeal , template< class > class Datastructure = carl::Heap, template< typename Polynomial > class Configuration = ReductorConfiguration> bool carl::Reductor< InputPolynomial, PolynomialInIdeal, Datastructure, Configuration > ∴::reductionOccured ( ) [inline]

Gets the flag which indicates that a reduction has occurred (p -> p' with p' != p)

#### Returns

the value of the flag

# 12.328 carl::ReductorConfiguration < Polynomial > Class Template Reference

Class with the settings for the reduction algorithm.

```
#include <Reductor.h>
```

# **Public Types**

- using EntryType = ReductorEntry< Polynomial >
- using Entry = EntryType \*
- using CompareResult = carl::CompareResult

# **Static Public Member Functions**

- static CompareResult compare (Entry e1, Entry e2)
- static bool cmpLessThan (CompareResult res)
- static bool cmpEqual (CompareResult res)
- static bool deduplicate (Entry e1, Entry e2)

should only be called if the compare result was EQUAL eliminate duplicate leading monomials

#### Static Public Attributes

- static const bool supportDeduplicationWhileOrdering = false
- static const bool fastIndex = true

#### 12.328.1 Detailed Description

```
template<class Polynomial> class carl::ReductorConfiguration< Polynomial >
```

Class with the settings for the reduction algorithm.

#### 12.328.2 Member Typedef Documentation

```
12.328.2.1 CompareResult template<class Polynomial >
using carl::ReductorConfiguration< Polynomial >::CompareResult = carl::CompareResult
12.328.2.2 Entry template<class Polynomial >
using carl::ReductorConfiguration< Polynomial >::Entry = EntryType*
12.328.2.3 EntryType template<class Polynomial >
using carl::ReductorConfiguration< Polynomial >::EntryType = ReductorEntry<Polynomial>
12.328.3 Member Function Documentation
12.328.3.1 cmpEqual() template<class Polynomial >
static bool carl::ReductorConfiguration< Polynomial >::cmpEqual (
             CompareResult res ) [inline], [static]
12.328.3.2 cmpLessThan() template<class Polynomial >
static bool carl::ReductorConfiguration< Polynomial >::cmpLessThan (
             CompareResult res ) [inline], [static]
12.328.3.3 compare() template<class Polynomial >
static CompareResult carl::ReductorConfiguration< Polynomial >::compare (
             Entry e1,
             Entry e2 ) [inline], [static]
12.328.3.4 deduplicate() template<class Polynomial >
\verb|static bool carl::ReductorConfiguration<| \verb|Polynomial >::deduplicate| (
             Entry e1,
             Entry e2 ) [inline], [static]
should only be called if the compare result was EQUAL eliminate duplicate leading monomials
```

| e1 | upper entry |
|----|-------------|
| e2 | lower entry |

#### Returns

true if e1->It is cancelled

#### 12.328.4 Field Documentation

```
12.328.4.1 fastIndex template < class Polynomial >
const bool carl::ReductorConfiguration < Polynomial >::fastIndex = true [static]
```

```
12.328.4.2 supportDeduplicationWhileOrdering template<class Polynomial > const bool carl::ReductorConfiguration< Polynomial >::supportDeduplicationWhileOrdering = false [static]
```

# 12.329 carl::ReductorEntry< Polynomial > Class Template Reference

An entry in the reduction polynomial.

```
#include <ReductorEntry.h>
```

### **Public Member Functions**

- ReductorEntry (const Term < Coeff > &multiple, const Polynomial &pol)
  - Constructor with a factor and a polynomial.
- ReductorEntry (const Term < Coeff > &pol)

Constructor with implicit factor = 1.

- · const Polynomial & getTail () const
- const Term < Coeff > & getLead () const
- const Term < Coeff > & getMultiple () const
- void removeLeadingTerm ()

Calculate p - lt(p).

- bool addCoefficient (const Coeff &coeffToBeAdded)
- bool empty () const
- void print (std::ostream &os=std::cout)

Output the current polynomial.

# **Protected Types**

using Coeff = typename Polynomial::CoeffType

#### **Protected Attributes**

- Polynomial mTail
- Term< Coeff > mLead
- Term< Coeff > mMultiple

#### **Friends**

 • template<class C > std::ostream & operator<< (std::ostream &os, const ReductorEntry< C > rhs)

# 12.329.1 Detailed Description

```
template<class Polynomial> class carl::ReductorEntry< Polynomial >
```

An entry in the reduction polynomial.

The class decodes a polynomial given by mLead + mMultiple \* mTail.

# 12.329.2 Member Typedef Documentation

```
12.329.2.1 Coeff template<class Polynomial >
using carl::ReductorEntry< Polynomial >::Coeff = typename Polynomial::CoeffType [protected]
```

# 12.329.3 Constructor & Destructor Documentation

Constructor with a factor and a polynomial.

# **Parameters**

| multiple |  |
|----------|--|
| pol      | Resulting polynomial = multiple * pol. |

Constructor with implicit factor = 1.

| pol |  |
|-----|--|
|     |  |

#### 12.329.4 Member Function Documentation

#### **Parameters**

coeffToBeAdded

Returns

```
12.329.4.2 empty() template<class Polynomial >
bool carl::ReductorEntry< Polynomial >::empty ( ) const [inline]
```

#### Returns

true iff the polynomial equals zero

```
12.329.4.3 getLead() template<class Polynomial > const Term<Coeff>& carl::ReductorEntry< Polynomial >::getLead ( ) const [inline]
```

Returns

```
12.329.4.4 getMultiple() template<class Polynomial > const Term<Coeff>& carl::ReductorEntry< Polynomial >::getMultiple ( ) const [inline]
```

Returns

```
12.329.4.5 getTail() template<class Polynomial > const Polynomial& carl::ReductorEntry< Polynomial >::getTail ( ) const [inline]
```

#### Returns

The tail of the polynomial, not multiplied by the correct factor!

Output the current polynomial.

#### **Parameters**

os

```
12.329.4.7 removeLeadingTerm() template<class Polynomial >
void carl::ReductorEntry< Polynomial >::removeLeadingTerm ( ) [inline]
Calculate p - It(p).
```

# 12.329.5 Friends And Related Function Documentation

# 12.329.6 Field Documentation

```
12.329.6.1 mLead template<class Polynomial >
Term<Coeff> carl::ReductorEntry< Polynomial >::mLead [protected]
```

```
12.329.6.2 mMultiple template<class Polynomial >
Term<Coeff> carl::ReductorEntry< Polynomial >::mMultiple [protected]
```

```
12.329.6.3 mTail template<class Polynomial >
Polynomial carl::ReductorEntry< Polynomial >::mTail [protected]
```

# 12.330 carl::pool::RehashPolicy Class Reference

Mimics stdlibs default rehash policy for hashtables.

```
#include <PoolHelper.h>
```

#### **Public Member Functions**

- RehashPolicy (float maxLoadFactor=0.95f, float growthFactor=2.f)
- std::size\_t numBucketsFor (std::size\_t numElements) const
- std::pair < bool, std::size\_t > needRehash (std::size\_t numBuckets, std::size\_t numElements) const

# 12.330.1 Detailed Description

Mimics stdlibs default rehash policy for hashtables.

```
See https://gcc.gnu.org/onlinedocs/libstdc++/libstdc++-html-USERS-4.1/hashtable-source.chtml
```

# 12.330.2 Constructor & Destructor Documentation

# 12.330.3 Member Function Documentation

```
12.330.3.2 numBucketsFor() std::size_t carl::pool::RehashPolicy::numBucketsFor ( std::size_t numElements ) const
```

## 12.331 carl::remove\_all< T, U > Struct Template Reference

```
#include <typetraits.h>
```

# 12.332 carl::remove\_all< T, T > Struct Template Reference

```
#include <typetraits.h>
```

## **Public Types**

• using type = T

# 12.332.1 Member Typedef Documentation

```
12.332.1.1 type template<typename T >
using carl::remove_all< T, T >::type = T
```

## 12.333 carl::io::helper::ErrorHandler::result< typename > Struct Template Reference

```
#include <SpiritHelper.h>
```

### **Public Types**

• using type = qi::error\_handler\_result

### 12.333.1 Member Typedef Documentation

```
12.333.1.1 type template<typename > using carl::io::helper::ErrorHandler::result< typename >::type = qi::error_handler_result
```

# 12.334 carl::rounding < Number > Struct Template Reference

```
#include <rounding.h>
```

#### **Public Member Functions**

- Number add\_down (Number \_lhs, Number \_rhs)
- Number add\_up (Number \_lhs, Number \_rhs)
- Number sub\_down (Number \_lhs, Number \_rhs)
- Number sub\_up (Number \_lhs, Number \_rhs)
- Number mul\_down (Number \_lhs, Number \_rhs)
- Number mul\_up (Number \_lhs, Number \_rhs)
- Number div\_down (Number \_lhs, Number \_rhs)
- Number div\_up (Number \_lhs, Number \_rhs)
- Number sqrt\_down (Number \_val)
- Number sqrt\_up (Number \_val)
- Number exp\_down (Number \_val)
- Number exp\_up (Number \_val)
- Number log\_down (Number \_val)
- Number log\_up (Number \_val)
- Number sin\_up (Number \_val)
- Number sin\_down (Number \_val)
- Number cos\_down (Number \_val)
- Number cos\_up (Number \_val)
- Number tan\_down (Number \_val)
- Number tan\_up (Number \_val)
- Number asin\_down (Number \_val)
- Number asin\_up (Number \_val)
- Number acos\_down (Number \_val)
- Number acos\_up (Number \_val)
- Number atan\_down (Number \_val)
- Number atan\_up (Number \_val)
- Number sinh\_down (Number \_val)
- Number sinh\_up (Number \_val)
- Number cosh\_down (Number \_val)
- Number cosh\_up (Number \_val)
- Number tanh\_down (Number \_val)
- Number tanh\_up (Number \_val)
- Number asinh\_down (Number \_val)
- Number asinh\_up (Number \_val)
- Number acosh\_down (Number \_val)
- Number acosh\_up (Number \_val)
- Number atanh\_down (Number \_val)
- Number atanh\_up (Number \_val)
- Number median (Number \_val1, Number \_val2)
- Number int\_down (Number \_val)
- Number int\_up (Number \_val)
- template<typename U > Number conv\_down (U \_val)
- template<typename U >
   Number conv\_up (U \_val)

### 12.334.1 Member Function Documentation

```
12.334.1.1 acos_down() template<typename Number >
Number carl::rounding< Number >::acos_down (
            Number _val ) [inline]
12.334.1.2 acos_up() template<typename Number >
Number carl::rounding< Number >::acos_up (
            Number _val ) [inline]
12.334.1.3 acosh_down() template<typename Number >
Number carl::rounding< Number >::acosh_down (
           Number _val ) [inline]
12.334.1.4 acosh_up() template<typename Number >
Number carl::rounding< Number >::acosh_up (
           Number _val ) [inline]
12.334.1.5 add_down() template<typename Number >
Number carl::rounding< Number >::add_down (
            Number _lhs,
            Number _rhs ) [inline]
12.334.1.6 add_up() template<typename Number >
Number carl::rounding< Number >::add_up (
            Number _lhs,
            Number _rhs ) [inline]
12.334.1.7 asin_down() template<typename Number >
Number carl::rounding< Number >::asin_down (
            Number _val ) [inline]
12.334.1.8 asin_up() template<typename Number >
Number carl::rounding< Number >::asin_up (
           Number _val ) [inline]
```

```
12.334.1.9 asinh_down() template<typename Number >
Number carl::rounding< Number >::asinh_down (
             Number _val ) [inline]
12.334.1.10 asinh_up() template<typename Number >
Number carl::rounding< Number >::asinh_up (
             Number _val ) [inline]
12.334.1.11 atan_down() template<typename Number >
Number carl::rounding< Number >::atan_down (
            Number _val ) [inline]
12.334.1.12 atan_up() template<typename Number >
Number carl::rounding< Number >::atan_up (
            Number _val ) [inline]
\textbf{12.334.1.13} \quad \textbf{atanh\_down()} \quad \texttt{template} < \texttt{typename Number} >
Number carl::rounding< Number >::atanh_down (
             Number _val ) [inline]
12.334.1.14 atanh_up() template<typename Number >
Number carl::rounding< Number >::atanh_up (
             Number _val ) [inline]
12.334.1.15 conv_down() template<typename Number >
template<typename U >
Number carl::rounding< Number >::conv_down (
             U _val ) [inline]
12.334.1.16 conv_up() template<typename Number >
template<typename U >
Number carl::rounding< Number >::conv_up (
            U _val ) [inline]
```

```
12.334.1.17 cos_down() template<typename Number >
Number carl::rounding< Number >::cos_down (
            Number _val ) [inline]
12.334.1.18 cos\_up() template<typename Number >
Number carl::rounding< Number >::cos\_up (
             Number _val ) [inline]
12.334.1.19 cosh_down() template<typename Number >
Number carl::rounding< Number >::cosh_down (
            Number _val ) [inline]
12.334.1.20 cosh_up() template<typename Number >
Number carl::rounding< Number >::cosh_up (
            Number _val ) [inline]
\textbf{12.334.1.21} \quad \textbf{div\_down()} \quad \texttt{template} < \texttt{typename Number} >
Number carl::rounding< Number >::div_down (
             Number _lhs,
             Number _rhs ) [inline]
12.334.1.22 div_up() template<typename Number >
Number carl::rounding< Number >::div_up (
             Number _lhs,
             Number _rhs ) [inline]
12.334.1.23 exp_down() template<typename Number >
Number carl::rounding< Number >::exp_down (
             Number _val ) [inline]
12.334.1.24 exp_up() template<typename Number >
Number carl::rounding< Number >::exp_up (
            Number _val ) [inline]
```

```
12.334.1.25 int_down() template<typename Number >
Number carl::rounding< Number >::int_down (
             Number _val ) [inline]
12.334.1.26 int_up() template<typename Number >
Number carl::rounding< Number >::int_up (
             Number _val ) [inline]
12.334.1.27 log_down() template<typename Number >
Number carl::rounding< Number >::log_down (
             Number _val ) [inline]
12.334.1.28 log_up() template<typename Number >
Number carl::rounding< Number >::log_up (
            Number _val ) [inline]
\textbf{12.334.1.29} \quad \textbf{median()} \quad \texttt{template} < \texttt{typename Number} >
Number carl::rounding< Number >::median (
             Number _val1,
             Number _val2 ) [inline]
12.334.1.30 mul_down() template<typename Number >
Number carl::rounding< Number >::mul_down (
             Number _lhs,
             Number _rhs ) [inline]
12.334.1.31 mul_up() template<typename Number >
Number carl::rounding< Number >::mul_up (
             Number _lhs,
             Number _rhs ) [inline]
12.334.1.32 sin_down() template<typename Number >
Number carl::rounding< Number >::sin_down (
             Number _val ) [inline]
```

```
12.334.1.33 sin_up() template<typename Number >
Number carl::rounding< Number >::sin_up (
            Number _val ) [inline]
\textbf{12.334.1.34} \quad \textbf{sinh\_down()} \quad \texttt{template} < \texttt{typename Number} >
Number carl::rounding< Number >::sinh_down (
            Number _val ) [inline]
12.334.1.35 sinh_up() template<typename Number >
Number carl::rounding< Number >::sinh_up (
            Number _val ) [inline]
12.334.1.36 sqrt_down() template<typename Number >
Number carl::rounding< Number >::sqrt_down (
            Number _val ) [inline]
12.334.1.37 sqrt_up() template<typename Number >
Number carl::rounding< Number >::sqrt_up (
             Number _val ) [inline]
12.334.1.38 sub_down() template<typename Number >
Number carl::rounding< Number >::sub_down (
             Number _lhs,
             Number _rhs ) [inline]
12.334.1.39 sub_up() template<typename Number >
Number carl::rounding< Number >::sub_up (
            Number _lhs,
             Number _rhs ) [inline]
12.334.1.40 tan_down() template<typename Number >
Number carl::rounding< Number >::tan_down (
            Number _val ) [inline]
```

```
12.334.1.41 tan_up() template<typename Number >
Number carl::rounding< Number >::tan_up (
             Number _val ) [inline]
12.334.1.42 tanh_down() template<typename Number >
Number carl::rounding< Number >::tanh_down (
             Number _val ) [inline]
12.334.1.43 tanh_up() template<typename Number >
Number carl::rounding< Number >::tanh_up (
             Number _val ) [inline]
12.335 carl::rounding < FLOAT_T < FloatType > > Struct Template Reference
Public Member Functions

    FLOAT_T< FloatType > add_down (FLOAT_T< FloatType > _lhs, FLOAT_T< FloatType > _rhs)

    FLOAT_T< FloatType > add_up (FLOAT_T< FloatType > _lhs, FLOAT_T< FloatType > _rhs)

    FLOAT_T< FloatType > sub_down (FLOAT_T< FloatType > _lhs, FLOAT_T< FloatType > _rhs)

    FLOAT_T< FloatType > sub_up (FLOAT_T< FloatType > _rhs)

    FLOAT_T< FloatType > mul_down (FLOAT_T< FloatType > _lhs, FLOAT_T< FloatType > _rhs)

    FLOAT_T< FloatType > mul_up (FLOAT_T< FloatType > _lhs, FLOAT_T< FloatType > _rhs)

    FLOAT_T< FloatType > div_down (FLOAT_T< FloatType > _lhs, FLOAT_T< FloatType > _rhs)

    FLOAT_T< FloatType > div_up (FLOAT_T< FloatType > .lhs, FLOAT_T< FloatType > .rhs)

    FLOAT_T< FloatType > sqrt_down (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > sqrt_up (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > exp_down (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > exp_up (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > log_down (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > log_up (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > cos_down (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > cos_up (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > tan_down (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > tan_up (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > asin_down (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > asin_up (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > acos_down (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > acos_up (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > atan_down (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > atan_up (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > sinh_down (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > sinh_up (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > cosh_down (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > cosh_up (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > tanh_down (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > tanh_up (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > asinh_down (FLOAT_T< FloatType > _val)
```

FLOAT\_T< FloatType > asinh\_up (FLOAT\_T< FloatType > \_val)

```
    FLOAT_T< FloatType > acosh_down (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > acosh_up (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > atanh_down (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > atanh_up (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > median (FLOAT_T< FloatType > _val1, FLOAT_T< FloatType > _val2)

    FLOAT_T< FloatType > int_down (FLOAT_T< FloatType > _val)

    FLOAT_T< FloatType > int_up (FLOAT_T< FloatType > _val)

    template<typename U >

     FLOAT_T< FloatType > conv_down (U _val)
    • template<typename U >
      FLOAT_T < FloatType > conv_up (U _val)
12.335.1 Member Function Documentation
12.335.1.1 acos_down() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::acos_down (
              FLOAT_T< FloatType > _val ) [inline]
12.335.1.2 acos_up() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::acos_up (
              FLOAT_T< FloatType > _val ) [inline]
12.335.1.3 acosh_down() template<typename FloatType >
{\tt FLOAT\_T} < {\tt FloatType} > {\tt carl::rounding} < {\tt FLOAT\_T} < {\tt FloatType} > {\tt ::acosh\_down} \  \, (
              FLOAT_T< FloatType > _val ) [inline]
```

```
12.335.1.5 add_down() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::add_down (
            FLOAT_T< FloatType > _lhs,
            FLOAT_T< FloatType > _rhs ) [inline]
```

 $\label{loss_float_type} \verb| carl::rounding< FLOAT_T< FloatType > > :: acosh\_up ($ 

FLOAT\_T< FloatType > \_val ) [inline]

12.335.1.4 acosh\_up() template<typename FloatType >

```
12.335.1.6 add_up() template<typename FloatType >
\label{local_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_total_tot
                              FLOAT_T< FloatType > _lhs,
                              FLOAT_T< FloatType > _rhs ) [inline]
12.335.1.7 asin_down() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::asin_down (
                              FLOAT_T< FloatType > _val ) [inline]
12.335.1.8 asin_up() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::asin_up (
                              FLOAT_T< FloatType > _val ) [inline]
12.335.1.9 asinh_down() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::asinh_down (
                              FLOAT_T< FloatType > _val ) [inline]
12.335.1.10 asinh_up() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::asinh_up (
                              FLOAT_T< FloatType > _val ) [inline]
12.335.1.11 atan_down() template<typename FloatType >
FLOAT_T< FloatType > _val ) [inline]
12.335.1.12 atan_up() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::atan_up (
                              FLOAT_T< FloatType > _val ) [inline]
12.335.1.13 atanh_down() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::atanh_down (
                              FLOAT_T< FloatType > _val ) [inline]
```

```
12.335.1.14 atanh_up() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::atanh_up (
           FLOAT_T< FloatType > _val ) [inline]
12.335.1.15 conv_down() template<typename FloatType >
template<typename U >
U _val ) [inline]
12.335.1.16 conv_up() template<typename FloatType >
template<typename U >
FLOAT.T<FloatType> carl::rounding< FLOAT.T< FloatType > >::conv_up (
           U _val ) [inline]
12.335.1.17 cos_down() template<typename FloatType >
FLOAT_T< FloatType > _val ) [inline]
12.335.1.18 cos_up() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::cos_up (
           {\tt FLOAT\_T} < {\tt FloatType} > {\tt \_val} \ ) \quad [{\tt inline}]
12.335.1.19 cosh_down() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::cosh_down (
           FLOAT_T< FloatType > _val ) [inline]
12.335.1.20 cosh_up() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::cosh_up (
           FLOAT_T< FloatType > _val ) [inline]
12.335.1.21 div_down() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::div_down (
           FLOAT_T< FloatType > _lhs,
           FLOAT_T< FloatType > _rhs ) [inline]
```

```
12.335.1.22 div_up() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::div_up (
            FLOAT_T< FloatType > _lhs,
            FLOAT_T< FloatType > _rhs ) [inline]
12.335.1.23 exp_down() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::exp_down (
            FLOAT_T< FloatType > _val ) [inline]
12.335.1.24 exp_up() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::exp_up (
            FLOAT_T< FloatType > _val ) [inline]
12.335.1.25 int_down() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::int_down (
            FLOAT_T< FloatType > _val ) [inline]
12.335.1.26 int_up() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::int_up (
            FLOAT_T< FloatType > _val ) [inline]
12.335.1.27 log_down() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::log_down (
            FLOAT_T< FloatType > _val ) [inline]
12.335.1.28 log_up() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::log.up (
            FLOAT_T< FloatType > _val ) [inline]
12.335.1.29 median() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::median (
            FLOAT_T< FloatType > _val1,
            FLOAT_T< FloatType > _val2 ) [inline]
```

```
12.335.1.30 mul_down() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::mul_down (
           FLOAT_T< FloatType > _lhs,
           FLOAT_T< FloatType > _rhs ) [inline]
12.335.1.31 mul_up() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::mul_up (
            FLOAT_T< FloatType > _lhs,
            FLOAT_T< FloatType > _rhs ) [inline]
12.335.1.32 sinh_down() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::sinh_down (
            FLOAT_T< FloatType > _val ) [inline]
12.335.1.33 sinh_up() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::sinh.up (
            FLOAT_T< FloatType > _val ) [inline]
12.335.1.34 sqrt_down() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::sqrt_down (
            FLOAT_T< FloatType > _val ) [inline]
12.335.1.35 sqrt_up() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::sqrt_up (
           FLOAT_T< FloatType > _val ) [inline]
12.335.1.36 sub_down() template<typename FloatType >
FLOAT_T< FloatType > _lhs,
            FLOAT_T< FloatType > _rhs ) [inline]
12.335.1.37 sub_up() template<typename FloatType >
FLOAT_T<FloatType> carl::rounding< FLOAT_T< FloatType > >::sub_up (
            FLOAT_T< FloatType > _lhs,
            FLOAT_T< FloatType > _rhs ) [inline]
```

## 12.336 carl::covering::SetCover Class Reference

Represents a set cover problem.

```
#include <SetCover.h>
```

## **Public Member Functions**

• void set (std::size\_t set, std::size\_t element)

States that s covers the given element.

void set (std::size\_t set, const Bitset &elements)

States that s covers the given elements.

const auto & get\_set (std::size\_t set) const

Returns the given set.

• std::size\_t element\_count () const

Returns the number of elements.

• void prune\_sets ()

Removes empty sets.

• std::size\_t set\_count () const

Returns the number of sets.

• std::size\_t active\_set\_count () const

Returns the number of active sets (that still cover uncovered elements).

• std::size\_t largest\_set () const

Returns the id of the largest set.

std::size\_t largest\_set (const std::vector< double > &weights) const

Returns the id of the largest set with respect to given weights.

· Bitset get\_uncovered () const

Returns the uncovered elements.

void select\_set (std::size\_t s)

Selects the given set and purges the covered elements from all other sets.

#### **Friends**

std::ostream & operator<< (std::ostream &os, const SetCover &sc)</li>
 Print the set cover to os.

## 12.336.1 Detailed Description

Represents a set cover problem.

Allows to state which sets cover which elements and offers some helper methods to work with this set cover for the heuristics.

## 12.336.2 Member Function Documentation

```
12.336.2.1 active_set_count() std::size_t carl::covering::SetCover::active_set_count ( ) const
```

Returns the number of active sets (that still cover uncovered elements).

```
12.336.2.2 element_count() std::size_t carl::covering::SetCover::element_count ( ) const
```

Returns the number of elements.

```
12.336.2.3 get_set() const auto& carl::covering::SetCover::get_set ( std::size_t set ) const [inline]
```

Returns the given set.

```
12.336.2.4 get_uncovered() Bitset carl::covering::SetCover::get_uncovered ( ) const
```

Returns the uncovered elements.

```
12.336.2.5 largest_set() [1/2] std::size_t carl::covering::SetCover::largest_set ( ) const
```

Returns the id of the largest set.

Returns the id of the largest set with respect to given weights.

```
12.336.2.7 prune_sets() void carl::covering::SetCover::prune_sets ( )
```

Removes empty sets.

```
12.336.2.8 select_set() void carl::covering::SetCover::select_set ( std::size_t s )
```

Selects the given set and purges the covered elements from all other sets.

States that s covers the given elements.

States that s covers the given element.

```
12.336.2.11 set_count() std::size_t carl::covering::SetCover::set_count ( ) const
```

Returns the number of sets.

### 12.336.3 Friends And Related Function Documentation

Print the set cover to os.

## 12.337 carl::settings::Settings Struct Reference

Base class for central settings class.

```
#include <Settings.h>
```

#### **Public Member Functions**

```
    template<typename T >
        T & get (const std::string &name)
```

Get settings data of type T from the identifier name. Constructs the data object if it does not exist yet.

### 12.337.1 Detailed Description

Base class for central settings class.

Wraps a map from a string identifier to some struct holding the actual settings, wrapped as std::any. Simply call .get<SettingsData>("identifier") to obtain a reference to the settings data, which is created (and thereby initialized) lazily.

#### 12.337.2 Member Function Documentation

Get settings data of type T from the identifier name. Constructs the data object if it does not exist yet.

## 12.338 carl::settings::SettingsParser Class Reference

Base class for a settings parser.

```
#include <SettingsParser.h>
```

## **Public Member Functions**

• virtual ~SettingsParser ()=default

Virtual destructor.

• void finalize ()

Finalizes the parser.

po::options\_description & add (const std::string &title)

Adds a new options\_description with a title and a reference to the settings object.

template<typename F > void add\_finalizer (F &&f)

Adds a finalizer function to be called after parsing.

void parse\_options (int argc, char \*argv[], bool allow\_unregistered=true)

Parse the options.

• OptionPrinter print\_help () const

Print a help page.

SettingsPrinter print\_options () const

Print the parsed settings.

#### **Protected Member Functions**

void warn\_for\_unrecognized (const po::parsed\_options &parsed) const

Checks for unrecognized options that were found.

void parse\_command\_line (int argc, char \*argv[], bool allow\_unregistered)

Parses the command line.

void parse\_config\_file (bool allow\_unregistered)

Parses the config file if one was configured.

• bool finalize\_settings ()

Calls the finalizer functions.

virtual void warn\_for\_unrecognized\_option (const std::string &s) const

Prints a warning if an option was unrecognized. Can be overridden.

virtual void warn\_config\_file (const std::string &file) const

Prints a warning if loading the config file failed. Can be overridden.

virtual std::string name\_of\_config\_file () const

Gives the option name for the config file name. Can be overridden.

#### **Protected Attributes**

char \* argv\_zero = nullptr

Stores the name of the current binary.

po::positional\_options\_description mPositional

Stores the positional arguments.

• po::options\_description mAllOptions

Accumulates all available options.

• po::variables\_map mValues

Stores the parsed values.

• std::vector< po::options\_description > mOptions

Stores the individual options until the parser is finalized.

 $\bullet \ \ \mathsf{std} :: \mathsf{vector} < \mathsf{std} :: \mathsf{function} < \mathsf{bool}() >> \mathsf{mFinalizer}$ 

Stores hooks for setting object finalizer functions.

#### **Friends**

- std::ostream & settings::operator<< (std::ostream &os, settings::OptionPrinter op)</li>
- std::ostream & settings::operator<< (std::ostream &os, settings::SettingsPrinter sp)

## 12.338.1 Detailed Description

Base class for a settings parser.

## 12.338.2 Constructor & Destructor Documentation

```
12.338.2.1 ~SettingsParser() virtual carl::settings::SettingsParser::~SettingsParser ( ) [virtual], [default]
```

Virtual destructor.

#### 12.338.3 Member Function Documentation

```
12.338.3.1 add() po::options_description& carl::settings::SettingsParser::add ( const std::string & title ) [inline]
```

Adds a new options\_description with a title and a reference to the settings object.

The settings object is needed to pass it to the finalizer function.

Adds a finalizer function to be called after parsing.

boost::program\_options::notify() is called before running the finalizer functions. The finalizer function should accept a boost::program\_options::variables\_map as its only argument and should return a bool indicating whether it changed the variables map. If any finalizer changed the variables map, boost::program\_options::notify() is called again afterwards.

```
12.338.3.3 finalize() void carl::settings::SettingsParser::finalize ()
```

Finalizes the parser.

```
12.338.3.4 finalize_settings() bool carl::settings::SettingsParser::finalize_settings ( ) [protected]
```

Calls the finalizer functions.

```
12.338.3.5 name_of_config_file() virtual std::string carl::settings::SettingsParser::name_of_← config_file ( ) const [inline], [protected], [virtual]
```

Gives the option name for the config file name. Can be overridden.

Parses the command line.

```
12.338.3.7 parse_config_file() void carl::settings::SettingsParser::parse_config_file ( bool allow_unregistered ) [protected]
```

Parses the config file if one was configured.

Parse the options.

If allow\_unregistered is set to true, we allow them but call warn\_for\_unrecognized\_option() for each one. Otherwise an exception is raised when an unrecognized option is encountered.

```
12.338.3.9 print_help() OptionPrinter carl::settings::SettingsParser::print_help ( ) const [inline]
```

Print a help page.

Returns a helper object so that it can be used as follows: std::cout << parser.print\_help() << std::endl;

```
12.338.3.10 print_options() SettingsPrinter carl::settings::SettingsParser::print_options () const [inline]
```

Print the parsed settings.

Returns a helper object so that it can be used as follows: std::cout << parser.print\_options() << std::endl;

Prints a warning if loading the config file failed. Can be overridden.

```
12.338.3.12 warn_for_unrecognized() void carl::settings::SettingsParser::warn_for_unrecognized ( const po::parsed_options & parsed ) const [protected]
```

Checks for unrecognized options that were found.

```
12.338.3.13 warn_for_unrecognized_option() virtual void carl::settings::SettingsParser::warn_\leftarrow for_unrecognized_option ( const std::string & s ) const [inline], [protected], [virtual]
```

Prints a warning if an option was unrecognized. Can be overridden.

### 12.338.4 Friends And Related Function Documentation

#### 12.338.5 Field Documentation

```
12.338.5.1 argv_zero char* carl::settings::SettingsParser::argv_zero = nullptr [protected]
```

Stores the name of the current binary.

**12.338.5.2 mAllOptions** po::options\_description carl::settings::SettingsParser::mAllOptions [protected]

Accumulates all available options.

**12.338.5.3 mFinalizer** std::vector<std::function<bool()>> carl::settings::SettingsParser::m $\leftarrow$  Finalizer [protected]

Stores hooks for setting object finalizer functions.

Stores the individual options until the parser is finalized.

**12.338.5.5 mPositional** po::positional\_options\_description carl::settings::SettingsParser::m↔ Positional [protected]

Stores the positional arguments.

**12.338.5.6 mValues** po::variables\_map carl::settings::SettingsParser::mValues [protected]

Stores the parsed values.

# 12.339 carl::settings::SettingsPrinter Struct Reference

Helper class to nicely print the settings that were parsed.

#include <SettingsParser.h>

### **Data Fields**

• const SettingsParser & parser Reference to parser.

## 12.339.1 Detailed Description

Helper class to nicely print the settings that were parsed.

## 12.339.2 Field Documentation

12.339.2.1 parser const SettingsParser& carl::settings::SettingsPrinter::parser

Reference to parser.

## 12.340 carl::SignCondition Class Reference

#include <SignCondition.h>

# **Public Member Functions**

- bool isPrefixOf (const SignCondition &other)
- bool isSuffixOf (const SignCondition &other) const
- SignCondition trailingPart (uint count) const

### **Static Public Member Functions**

• static ThomComparisonResult compare (const SignCondition &lhs, const SignCondition &rhs)

### **Data Fields**

• T elements

STL member.

### **Friends**

std::ostream & operator<< (std::ostream &os, const SignCondition &rhs)</li>

### 12.340.1 Member Function Documentation

## 12.340.2 Friends And Related Function Documentation

#### 12.340.3 Field Documentation

```
12.340.3.1 elements T std::list< T >::elements [inherited] STL member.
```

## 12.341 carl::SignDetermination < Number > Class Template Reference

```
#include <SignDetermination.h>
```

### **Public Member Functions**

- template<typename InputIt >
   SignDetermination (InputIt zeroSet\_first, InputIt zeroSet\_last)
- SignDetermination (const SignDetermination &other)
- uint sizeOfZeroSet () const
- · const auto & processedPolynomials () const
- · const auto & signs () const
- const auto & products () const
- · const auto & adaptedList () const
- const auto & matrix () const
- bool needsUpdate () const
- std::list< SignCondition > getSigns (const Polynomial &p)
- std::list< SignCondition > getSignsAndAdd (const Polynomial &p)
- template<typename InputIt >
   std::list< SignCondition > getSignsAndAddAll (InputIt first, InputIt last)

## 12.341.1 Constructor & Destructor Documentation

```
12.341.1.2 SignDetermination() [2/2] template<typename Number > carl::SignDetermination< Number >::SignDetermination ( const SignDetermination< Number > & other ) [inline]
```

### 12.341.2 Member Function Documentation

```
12.341.2.1 adaptedList() template<typename Number >
const auto& carl::SignDetermination< Number >::adaptedList ( ) const [inline]
12.341.2.2 getSigns() template<typename Number >
\verb|std::list<|SignCondition>| carl::SignDetermination<| Number >::getSigns | (
             const Polynomial & p ) [inline]
12.341.2.3 getSignsAndAdd() template<typename Number >
std::list<SignCondition> carl::SignDetermination< Number >::getSignsAndAdd (
             const Polynomial & p ) [inline]
12.341.2.4 getSignsAndAddAll() template<typename Number >
template<typename InputIt >
std::list<SignCondition> carl::SignDetermination< Number >::getSignsAndAddAll (
             InputIt first,
             InputIt last ) [inline]
12.341.2.5 matrix() template<typename Number >
const auto& carl::SignDetermination< Number >::matrix ( ) const [inline]
\textbf{12.341.2.6} \quad \textbf{needsUpdate()} \quad \texttt{template} < \texttt{typename Number} >
bool carl::SignDetermination< Number >::needsUpdate ( ) const [inline]
12.341.2.7 processedPolynomials() template<typename Number >
\verb|const| auto@carl::SignDetermination| < Number >::processedPolynomials () const [inline] \\
12.341.2.8 products() template<typename Number >
const auto& carl::SignDetermination< Number >::products ( ) const [inline]
12.341.2.9 signs() template<typename Number >
const auto& carl::SignDetermination< Number >::signs ( ) const [inline]
```

```
12.341.2.10 sizeOfZeroSet() template<typename Number >
uint carl::SignDetermination< Number >::sizeOfZeroSet ( ) const [inline]
```

# 12.342 carl::SimpleNewton < Polynomial > Class Template Reference

```
#include <Contraction.h>
```

### **Public Member Functions**

template<typename evalType >
 bool contract (const Interval< double >::evalintervalmap &intervals, Variable::Arg variable, const evalType
 &constraint, const evalType &derivative, Interval< double > &resA, Interval< double > &resB, bool use
 NiceCenter=false)

#### 12.342.1 Member Function Documentation

## 12.343 carl::Singleton < T > Class Template Reference

Base class that implements a singleton.

```
#include <Singleton.h>
```

#### **Public Member Functions**

- Singleton (const Singleton &)=delete
- Singleton (Singleton &&)=delete
- Singleton & operator= (const Singleton &)=delete
- Singleton & operator= (Singleton &&)=delete
- virtual ∼Singleton () noexcept=default

Virtual destructor.

## Static Public Member Functions

• static T & getInstance ()

Returns the single instance of this class by reference.

### **Protected Member Functions**

• Singleton ()=default

Protected default constructor.

## 12.343.1 Detailed Description

```
template<typename T> class carl::Singleton< T>
```

Base class that implements a singleton.

A class that shall be a singleton can inherit from this class (the template argument being the class itself, see CRTP for this). It takes care of

- · deleting the copy constructor and the assignment operator,
- providing a protected default constructor and a virtual destructor and
- providing getInstance() that returns the one single object of this type.

#### 12.343.2 Constructor & Destructor Documentation

```
12.343.2.1 Singleton() [1/3] template<typename T > carl::Singleton< T >::Singleton ( ) [protected], [default]
```

Protected default constructor.

```
12.343.2.3 Singleton() [3/3] template<typename T > carl::Singleton< T >::Singleton ( Singleton< T > && ) [delete]
```

```
12.343.2.4 \simSingleton() template<typename T > virtual carl::Singleton< T >::\simSingleton ( ) [virtual], [default], [noexcept]
```

Virtual destructor.

### 12.343.3 Member Function Documentation

```
12.343.3.1 getInstance() template<typename T >
static T& carl::Singleton< T >::getInstance ( ) [inline], [static]
```

Returns the single instance of this class by reference.

If there is no instance yet, a new one is created.

```
12.343.3.3 operator=() [2/2] template<typename T > Singleton& carl::Singleton< T >::operator= ( Singleton< T > && ) [delete]
```

# 12.344 carl::logging::Sink Class Reference

Base class for a logging sink.

```
#include <Sink.h>
```

### **Public Member Functions**

virtual std::ostream & log () noexcept=0
 Abstract logging interface.

# 12.344.1 Detailed Description

Base class for a logging sink.

It only provides an interface to access some std::ostream.

## 12.344.2 Member Function Documentation

```
12.344.2.1 log() virtual std::ostream& carl::logging::Sink::log ( ) [pure virtual], [noexcept]
```

Abstract logging interface.

The intended usage is to write any log output to the output stream returned by this function.

Returns

Output stream.

Implemented in carl::logging::FileSink, and carl::logging::StreamSink.

## 12.345 carl::io::detail::SMTLIBOutputContainer < Args > Struct Template Reference

```
#include <SMTLIBStream.h>
```

## **Public Member Functions**

• SMTLIBOutputContainer (Args &&... args)

### **Data Fields**

• std::tuple < Args... > mData

### 12.345.1 Constructor & Destructor Documentation

### 12.345.2 Field Documentation

```
12.345.2.1 mData template<typename... Args>
std::tuple<Args...> carl::io::detail::SMTLIBOutputContainer< Args >::mData
```

## 12.346 carl::io::detail::SMTLIBScriptContainer< Pol > Struct Template Reference

Shorthand to allow writing SMTLIB scripts in one line.

```
#include <SMTLIBStream.h>
```

#### **Public Member Functions**

- SMTLIBScriptContainer (Logic I, std::initializer\_list< Formula< Pol >> f, bool getModel=false)
- SMTLIBScriptContainer (Logic I, std::initializer\_list< Formula< Pol >> f, const Pol &objective, bool get
   — Model=false)

#### Data Fields

- Logic mLogic
- std::initializer\_list< Formula< Pol > > mFormulas
- bool mGetModel
- Pol mObjective

### 12.346.1 Detailed Description

```
template<typename Pol> struct carl::io::detail::SMTLIBScriptContainer< Pol>
```

Shorthand to allow writing SMTLIB scripts in one line.

#### 12.346.2 Constructor & Destructor Documentation

## 12.346.3 Field Documentation

```
12.346.3.1 mFormulas template<typename Pol > std::initializer_list<Formula<Pol> > carl::io::detail::SMTLIBScriptContainer< Pol >::m← Formulas
```

```
12.346.3.2 mGetModel template<typename Pol >
bool carl::io::detail::SMTLIBScriptContainer< Pol >::mGetModel
12.346.3.3 mLogic template<typename Pol >
Logic carl::io::detail::SMTLIBScriptContainer< Pol >::mLogic
12.346.3.4 mObjective template<typename Pol >
Pol carl::io::detail::SMTLIBScriptContainer< Pol >::mObjective
12.347 carl::io::SMTLIBStream Class Reference
Allows to print carl data structures in SMTLIB syntax.
#include <SMTLIBStream.h>
Public Member Functions

    void comment (const std::string &c)

          Writes a comment.

    void declare (Logic I)

         Declare a logic via set-logic.

    void declare (Sort s)

         Declare a sort via declare-sort.

    void declare (UninterpretedFunction uf)

          Declare a fresh function via declare-fun.

    void declare (Variable v)

         Declare a fresh variable via declare-fun.
    • void declare (BVVariable v)
         Declare a bitvector variable via declare-fun.
    • void declare (UVariable v)
         Declare an uninterpreted variable via declare-fun.

    void declare (const std::set< UninterpretedFunction > &ufs)

         Declare a set of functions.

    void declare (const carlVariables &vars)

         Declare a set of variables.

    void declare (const std::set< BVVariable > &bvvs)

         Declare a set of bitvector variables.

    void declare (const std::set< UVariable > &uvs)

          Declare a set of uninterpreted variables.
    • void initialize (Logic I, const carlVariables &vars, const std::set < UninterpretedFunction > &ufs={}, const
      std::set< BVVariable > &bvvs={}, const std::set< UVariable > &uvs={})
```

Generic initializer including the logic, a set of variables and a set of functions.

Generic initializer including the logic and variables and functions from a set of formulas.

void initialize (Logic I, std::initializer\_list< Formula< Pol >> formulas)

template<typename Pol >

```
    void setInfo (const std::string &name, const std::string &value)

     Set information via set-info.

    void setOption (const std::string &name, const std::string &value)

     Set option via set-option.
template<typename Pol >
 void assertFormula (const Formula < Pol > &formula)
     Assert a formula via assert.
template<typename Pol >
  void minimize (const Pol &objective)
     Minimize an objective via custom minimize.
· void checkSat ()
     Check satisfiability via check-sat.

    void getAssertions ()

     Print assertions via get-assertions.

    void getModel ()

     Print model via get-model.
• void echo (const std::string &str)
     Echo via echo.
• void reset ()
     Reset via reset.
• void exit ()
     Exit via exit.
• template<typename T >
  SMTLIBStream & operator << (T &&t)
     Write some data to this stream.

    SMTLIBStream & operator<< (std::ostream &(*os)(std::ostream &))</li>

      Write io operators (like std::endl) directly to the underlying stream.
• auto str () const
     Return the written data as a string.
```

## 12.347.1 Detailed Description

• auto content () const

Allows to print carl data structures in SMTLIB syntax.

Return the underlying stream buffer.

## 12.347.2 Member Function Documentation

```
12.347.2.1 assertFormula() template<typename Pol > void carl::io::SMTLIBStream::assertFormula ( const Formula < Pol > & formula ) [inline]
```

Assert a formula via assert.

```
12.347.2.2 checkSat() void carl::io::SMTLIBStream::checkSat ( ) [inline]
```

Check satisfiability via check-sat.

```
12.347.2.3 comment() void carl::io::SMTLIBStream::comment ( const std::string & c ) [inline]
```

Writes a comment.

```
12.347.2.4 content() auto carl::io::SMTLIBStream::content ( ) const [inline]
```

Return the underlying stream buffer.

```
12.347.2.5 declare() [1/10] void carl::io::SMTLIBStream::declare ( $\tt BVVariable\ v ) [inline]
```

Declare a bitvector variable via declare-fun.

Declare a set of variables.

Declare a set of bitvector variables.

Declare a set of functions.

```
12.347.2.9 declare() [5/10] void carl::io::SMTLIBStream::declare (
const std::set< UVariable > & uvs ) [inline]
```

Declare a set of uninterpreted variables.

```
12.347.2.10 declare() [6/10] void carl::io::SMTLIBStream::declare ( Logic l ) [inline]
```

Declare a logic via set-logic.

```
12.347.2.11 declare() [7/10] void carl::io::SMTLIBStream::declare ( Sort s ) [inline]
```

Declare a sort via declare-sort.

Declare a fresh function via declare-fun.

Declare an uninterpreted variable via declare-fun.

```
12.347.2.14 declare() [10/10] void carl::io::SMTLIBStream::declare ( Variable\ v ) [inline]
```

Declare a fresh variable via declare-fun.

Echo via echo.

```
12.347.2.16 exit() void carl::io::SMTLIBStream::exit () [inline]
```

Exit via exit.

```
12.347.2.17 getAssertions() void carl::io::SMTLIBStream::getAssertions ( ) [inline]
```

 $\begin{picture}(100,00) \put(0,0){\line(0,0){100}} \put(0,0){\line(0,0){$ 

```
12.347.2.18 getModel() void carl::io::SMTLIBStream::getModel ( ) [inline]
```

Print model via get-model.

```
12.347.2.19 initialize() [1/2] void carl::io::SMTLIBStream::initialize (
    Logic 1,
    const carlVariables & vars,
    const std::set< UninterpretedFunction > & ufs = {},
    const std::set< BVVariable > & bvvs = {},
    const std::set< UVariable > & uvs = {} ) [inline]
```

Generic initializer including the logic, a set of variables and a set of functions.

Generic initializer including the logic and variables and functions from a set of formulas.

Minimize an objective via custom minimize.

```
12.347.2.22 operator << () [1/2] SMTLIBStream& carl::io::SMTLIBStream::operator << ( std::ostream &(*) (std::ostream &) os ) [inline]
```

Write io operators (like std::endl) directly to the underlying stream.

Write some data to this stream.

```
12.347.2.24 reset() void carl::io::SMTLIBStream::reset ( ) [inline]
```

Reset via reset.

Set information via  $\operatorname{set-info}$ .

Set option via set-option.

```
12.347.2.27 str() auto carl::io::SMTLIBStream::str ( ) const [inline]
```

Return the written data as a string.

## 12.348 carl::Sort Class Reference

Implements a sort (for defining types of variables and functions).

```
#include <Sort.h>
```

### **Public Member Functions**

- Sort () noexcept=default
- std::size\_t arity () const
- std::size\_t id () const

## **Friends**

- class SortManager
- std::ostream & operator<< (std::ostream &\_os, const Sort &\_sort)

  Prints the given sort on the given output stream.

# 12.348.1 Detailed Description

Implements a sort (for defining types of variables and functions).

## 12.348.2 Constructor & Destructor Documentation

```
12.348.2.1 Sort() carl::Sort::Sort () [default], [noexcept]
```

#### 12.348.3 Member Function Documentation

```
12.348.3.1 arity() std::size_t carl::Sort::arity ( ) const
```

# Returns

The aritiy of this sort.

```
12.348.3.2 id() std::size_t carl::Sort::id ( ) const [inline]
```

# Returns

The id of this sort.

# 12.348.4 Friends And Related Function Documentation

Prints the given sort on the given output stream.

#### **Parameters**

| _OS   | The output stream to print on. |
|-------|--------------------------------|
| ₋sort | The sort to print.             |

# Returns

The output stream after printing the given sort on it.

12.348.4.2 SortManager friend class SortManager [friend]

# 12.349 sortByLeadingTerm < Polynomial > Class Template Reference

Sorts generators of an ideal by their leading terms.

#include <PolynomialSorts.h>

## **Public Member Functions**

- sortByLeadingTerm (const std::vector< Polynomial > &generators)
- bool operator() (std::size\_t a, std::size\_t b) const

# 12.349.1 Detailed Description

template<class Polynomial> class sortByLeadingTerm< Polynomial >

Sorts generators of an ideal by their leading terms.

# **Parameters**

generators

# 12.349.2 Constructor & Destructor Documentation

## 12.349.3 Member Function Documentation

# 12.350 sortByPolSize < Polynomial > Class Template Reference

Sorts generators of an ideal by their number of terms.

```
#include <PolynomialSorts.h>
```

## **Public Member Functions**

- sortByPolSize (const std::vector< Polynomial > &generators)
- bool operator() (std::size\_t a, std::size\_t b) const

# 12.350.1 Detailed Description

```
\label{lem:lemplate} \begin{split} & template {<} class \ Polynomial {>} \\ & class \ sortByPolSize {<} \ Polynomial \ {>} \end{split}
```

Sorts generators of an ideal by their number of terms.

**Parameters** 

generators

# 12.350.2 Constructor & Destructor Documentation

# 12.350.3 Member Function Documentation

# 12.351 carl::SortContent Struct Reference

The actual content of a sort.

```
#include <SortManager.h>
```

#### **Public Member Functions**

- SortContent ()=delete
- SortContent (std::string \_name) noexcept

Constructs a sort content.

SortContent (std::string \_name, const std::vector < Sort > &\_parameters)

Constructs a sort content.

- SortContent (std::string \_name, std::vector < Sort > &&\_parameters)
- SortContent (const SortContent &sc)
- ∼SortContent () noexcept=default

Destructs a sort content.

- SortContent & operator= (const SortContent &sc)=delete
- SortContent (SortContent &&sc) noexcept=default
- SortContent & operator= (SortContent &&sc)=default
- · SortContent getUnindexed () const

Return a copy of this SortContent without any indices.

# **Data Fields**

· std::string name

The sort's name.

std::unique\_ptr< std::vector< Sort > > parameters

The sort's argument types. It is nullptr, if the sort's arity is zero.

- std::unique\_ptr< std::vector< std::size\_t >> indices

The sort's indices. A sort can be indexed with the "\_" operator. It is nullptr, if no indices are present.

# 12.351.1 Detailed Description

The actual content of a sort.

## 12.351.2 Constructor & Destructor Documentation

```
12.351.2.1 SortContent() [1/6] carl::SortContent::SortContent ( ) [delete]
```

```
12.351.2.2 SortContent() [2/6] carl::SortContent::SortContent (
std::string _name ) [inline], [explicit], [noexcept]
```

Constructs a sort content.

#### **Parameters**

| name The name of the sort content to cons | truct. |
|---|--------|
|---|--------|

Constructs a sort content.

#### **Parameters**

| ₋name       | The name of the sort content to construct.                   |
|-------------|--|
| _parameters | The sorts of the arguments of the sort content to construct. |

```
\textbf{12.351.2.6} \quad \sim \textbf{SortContent()} \quad \texttt{carl::SortContent::} \sim \texttt{SortContent ()} \quad \texttt{[default], [noexcept]}
```

Destructs a sort content.

```
12.351.2.7 SortContent() [6/6] carl::SortContent::SortContent (
SortContent && sc ) [default], [noexcept]
```

# 12.351.3 Member Function Documentation

```
12.351.3.1 getUnindexed() SortContent carl::SortContent::getUnindexed ( ) const [inline]
```

Return a copy of this SortContent without any indices.

## 12.351.4 Field Documentation

```
\textbf{12.351.4.1} \quad \textbf{indices} \quad \texttt{std::unique\_ptr} < \texttt{std::vector} < \texttt{std::size\_t} > \\ \texttt{carl::SortContent::indices}
```

The sort's indices. A sort can be indexed with the "\_" operator. It is nullptr, if no indices are present.

```
12.351.4.2 name std::string carl::SortContent::name
```

The sort's name.

 $\textbf{12.351.4.3} \quad \textbf{parameters} \quad \texttt{std::unique\_ptr} < \texttt{std::vector} < \texttt{Sort} > \\ \texttt{carl::SortContent::parameters}$ 

The sort's argument types. It is nullptr, if the sort's arity is zero.

# 12.352 carl::SortManager Class Reference

Implements a manager for sorts, containing the actual contents of these sort and allocating their ids.

```
#include <SortManager.h>
```

# **Public Types**

using SortTemplate = std::pair< std::vector< std::string >, Sort >
 The type of a sort template, define by define-sort.

#### **Public Member Functions**

- SortManager (const SortManager &)=delete
- SortManager (SortManager &&)=delete
- SortManager & operator= (const SortManager &)=delete
- SortManager & operator= (SortManager &&)=delete
- ~SortManager () noexcept override=default
- void clear ()
- const std::string & get\_name (const Sort &sort) const
- const std::vector < Sort > \* getParameters (const Sort &sort) const
- const std::vector< std::size\_t > \* getIndices (const Sort &sort) const
- VariableType getType (const Sort &sort) const
- std::ostream & print (std::ostream &os, const Sort &sort) const

Prints the given sort on the given output stream.

- · void exportDefinitions (std::ostream &os) const
- Sort getInterpreted (VariableType type) const
- Sort replace (const Sort &sort, const std::map< std::string, Sort > &parameters)

Recursively replaces sorts within the given sort according to the mapping of sort names to sorts as declared by the given map.

bool declare (const std::string &name, std::size\_t arity)

Adds a sort declaration.

bool define (const std::string &name, const std::vector< std::string > &params, const Sort &sort)

Adds a sort template definitions.

- std::size\_t getArity (const Sort &sort) const
- Sort addInterpretedMapping (const Sort &sort, VariableType type)
- Sort addInterpretedSort (const std::string &name, VariableType type)
- Sort addInterpretedSort (const std::string &name, const std::vector < Sort > &parameters, VariableType type)
- Sort addSort (const std::string &name, VariableType type=VariableType::VT\_UNINTERPRETED)
- Sort addSort (const std::string &name, const std::vector < Sort > &parameters, VariableType type=VariableType::VT\_UNINTERF
- void makeSortIndexable (const Sort &sort, std::size\_t indices, VariableType type)
- bool isInterpreted (const Sort &sort) const
- Sort index (const Sort &sort, const std::vector< std::size\_t > &indices)
- Sort getSort (const std::string &name)

Gets the sort with arity zero (thus it is maybe interpreted) corresponding the given name.

Sort getSort (const std::string &name, const std::vector < Sort > &params)

Gets the sort with arity greater than zero corresponding the given name and having the arguments of the given sorts.

- Sort getSort (const std::string &name, const std::vector< std::size\_t > &indices)
- Sort getSort (const std::string &name, const std::vector < std::size\_t > &indices, const std::vector < Sort > &params)

#### **Static Public Member Functions**

static SortManager & getInstance ()

Returns the single instance of this class by reference.

# 12.352.1 Detailed Description

Implements a manager for sorts, containing the actual contents of these sort and allocating their ids.

# 12.352.2 Member Typedef Documentation

```
12.352.2.1 SortTemplate using carl::SortManager::SortTemplate = std::pair<std::vector<std↔ ::string>, Sort>
```

The type of a sort template, define by define-sort.

#### 12.352.3 Constructor & Destructor Documentation

```
12.352.3.1 SortManager() [1/2] carl::SortManager::SortManager (
              const SortManager & ) [delete]
12.352.3.2 SortManager() [2/2] carl::SortManager::SortManager (
              SortManager && ) [delete]
12.352.3.3 ~SortManager() carl::SortManager::~SortManager () [override], [default], [noexcept]
12.352.4 Member Function Documentation
12.352.4.1 addInterpretedMapping() Sort carl::SortManager::addInterpretedMapping (
              const Sort & sort,
              VariableType type ) [inline]
\textbf{12.352.4.2} \quad \textbf{addInterpretedSort()} \; \texttt{[1/2]} \quad \texttt{Sort} \; \texttt{carl::SortManager::addInterpretedSort} \; \; \texttt{(}
              const std::string & name,
              const std::vector< Sort > & parameters,
              VariableType type ) [inline]
```

12.352.4.3 addInterpretedSort() [2/2] Sort carl::SortManager::addInterpretedSort (

const std::string & name,
VariableType type ) [inline]

Adds a sort declaration.

#### **Parameters**

| name  | The name of the declared sort.  |
|-------|---------------------------------|
| arity | The arity of the declared sort. |

# Returns

true, if the given sort declaration has not been added before; false, otherwise.

Adds a sort template definitions.

# **Parameters**

| name   | The name of the defined sort template.      |
|--------|---|
| params | The template parameter of the defined sort. |
| sort   | The sort to instantiate into.               |

#### Returns

true, if the given sort template definition has not been added before; false, otherwise.

```
12.352.4.9 exportDefinitions() void carl::SortManager::exportDefinitions ( std::ostream & os ) const
```

Todo fix this

## **Parameters**

```
sort A sort.
```

#### Returns

The name if the given sort.

# Parameters

```
sort The sort to get the arity for.
```

# Returns

The arity of the given sort.

```
12.352.4.13 getInstance() static SortManager & carl::Singleton< SortManager >::getInstance () [inline], [static], [inherited]
```

Returns the single instance of this class by reference.

If there is no instance yet, a new one is created.

```
12.352.4.14 getInterpreted() Sort carl::SortManager::getInterpreted ( VariableType type ) const [inline]
```

```
12.352.4.16 getSort() [1/4] Sort carl::SortManager::getSort ( const std::string & name )
```

Gets the sort with arity zero (thus it is maybe interpreted) corresponding the given name.

#### **Parameters**

## Returns

The resulting sort.

Gets the sort with arity greater than zero corresponding the given name and having the arguments of the given sorts.

# **Parameters**

| name   | The name of the sort to get.                  |
|--------|---|
| params | The sort of the arguments of the sort to get. |

# Returns

The resulting sort.

```
12.352.4.19 getSort() [4/4] Sort carl::SortManager::getSort (
             const std::string & name,
             const std::vector< std::size_t > & indices,
             const std::vector< Sort > & params)
12.352.4.20 getType() VariableType carl::SortManager::getType (
             const Sort & sort ) const [inline]
12.352.4.21 index() Sort carl::SortManager::index (
             const Sort & sort,
             const std::vector< std::size_t > & indices )
12.352.4.22 isInterpreted() bool carl::SortManager::isInterpreted (
             const Sort & sort ) const [inline]
Parameters
 sort A sort.
Returns
    true, if the given sort is interpreted.
12.352.4.23 makeSortIndexable() void carl::SortManager::makeSortIndexable (
             const Sort & sort,
             std::size_t indices,
             VariableType type )
12.352.4.24 operator=() [1/2] SortManager& carl::SortManager::operator= (
             const SortManager & ) [delete]
12.352.4.25 operator=() [2/2] SortManager& carl::SortManager::operator= (
             SortManager && ) [delete]
12.352.4.26 print() std::ostream & carl::SortManager::print (
             std::ostream & os,
             const Sort & sort ) const
```

Prints the given sort on the given output stream.

#### **Parameters**

| os   | The output stream to print the given sort on. |
|------|---|
| sort | The sort to print.                            |

#### Returns

The output stream after printing the given sort on it.

Recursively replaces sorts within the given sort according to the mapping of sort names to sorts as declared by the given map.

## **Parameters**

| sort       | The sort to replace sorts by sorts in. |
|------------|--|
| parameters | The map of sort names to sorts.        |

#### Returns

The resulting sort.

# 12.353 carl::SortValue Class Reference

Implements a sort value, being a value of the uninterpreted domain specified by this sort.

```
#include <SortValue.h>
```

# **Public Member Functions**

- SortValue () noexcept=default
- const carl::Sort & sort () const noexcept
- std::size\_t id () const noexcept

## **Friends**

• class SortValueManager

# 12.353.1 Detailed Description

Implements a sort value, being a value of the uninterpreted domain specified by this sort.

#### 12.353.2 Constructor & Destructor Documentation

```
12.353.2.1 SortValue() carl::SortValue::SortValue () [default], [noexcept]
```

# 12.353.3 Member Function Documentation

```
12.353.3.1 id() std::size_t carl::SortValue::id ( ) const [inline], [noexcept]
```

#### Returns

The id of this sort value.

```
12.353.3.2 sort() const carl::Sort& carl::SortValue::sort ( ) const [inline], [noexcept]
```

#### Returns

The sort of this value.

# 12.353.4 Friends And Related Function Documentation

```
12.353.4.1 SortValueManager friend class SortValueManager [friend]
```

# 12.354 carl::SortValueManager Class Reference

Implements a manager for sort values, containing the actual contents of these sort and allocating their ids.

```
#include <SortValueManager.h>
```

# **Public Member Functions**

• SortValue newSortValue (const Sort &sort)

Creates a new value for the given sort.

• SortValue defaultSortValue (const Sort &sort) const

Returns the default value for the given sort.

## **Static Public Member Functions**

• static SortValueManager & getInstance ()

Returns the single instance of this class by reference.

# 12.354.1 Detailed Description

Implements a manager for sort values, containing the actual contents of these sort and allocating their ids.

# 12.354.2 Member Function Documentation

Returns the default value for the given sort.

#### **Parameters**

## Returns

The resulting sort value.

```
12.354.2.2 getInstance() static SortValueManager & carl::Singleton< SortValueManager >::get ← Instance ( ) [inline], [static], [inherited]
```

Returns the single instance of this class by reference.

If there is no instance yet, a new one is created.

```
12.354.2.3 newSortValue() SortValue carl::SortValueManager::newSortValue ( const Sort & sort ) [inline]
```

Creates a new value for the given sort.

# **Parameters**

#### Returns

The resulting sort value.

# 12.355 carl::SPolPair Struct Reference

# Basic spol-pair.

```
#include <SPolPair.h>
```

## **Public Member Functions**

- SPolPair (std::size\_t p1, std::size\_t p2, Monomial::Arg lcm)
- void print (std::ostream &os=std::cout) const

## **Data Fields**

- const std::size\_t mP1
- const std::size\_t mP2
- const Monomial::Arg mLcm

# 12.355.1 Detailed Description

Basic spol-pair.

Optimizations could be deducing p2 from the structure where it is saved, and not saving the lcm. Also sugar might be added.

# Parameters

| p1  | index of polynomial p1  |
|-----|-------------------------|
| p2  | index of polynomial p2  |
| lcm | the lcm(lt(p1), lt(p2)) |

# 12.355.2 Constructor & Destructor Documentation

```
12.355.2.1 SPolPair() carl::SPolPair::SPolPair (
    std::size_t p1,
    std::size_t p2,
    Monomial::Arg lcm ) [inline]
```

# 12.355.3 Member Function Documentation

```
12.355.3.1 print() void carl::SPolPair::print (
    std::ostream & os = std::cout ) const [inline]
```

# 12.355.4 Field Documentation

```
12.355.4.1 mLcm const Monomial::Arg carl::SPolPair::mLcm
```

```
12.355.4.2 mP1 const std::size_t carl::SPolPair::mP1
```

```
12.355.4.3 mP2 const std::size_t carl::SPolPair::mP2
```

# 12.356 carl::SPolPairCompare < Compare > Struct Template Reference

```
#include <SPolPair.h>
```

# **Public Member Functions**

• bool operator() (const SPolPair &s1, const SPolPair &s2)

## 12.356.1 Member Function Documentation

# 12.357 carl::SqrtEx< Poly > Class Template Reference

```
#include <SqrtEx.h>
```

# **Public Types**

• using Rational = typename UnderlyingNumberType< Poly >::type

#### **Public Member Functions**

• SqrtEx ()

Default Constructor.

SqrtEx (Poly &&\_poly)

Constructs a square root expression from a polynomial p leading to (p + 0 \* sqrt(0)) / 1.

- SqrtEx (const Poly &\_poly)
- SqrtEx (Variable::Arg \_var)
- SqrtEx (const Poly &\_constantPart, const Poly &\_factor, const Poly &\_denominator, const Poly &\_radicand)

Constructs a square root expression from given constant part, factor, denominator and radicand.

- SqrtEx (Poly &&\_constantPart, Poly &&\_factor, Poly &&\_denominator, Poly &&\_radicand)
- const Poly & constant\_part () const
- · const Poly & factor () const
- · const Poly & denominator () const
- · const Poly & radicand () const
- bool has\_sqrt () const
- bool is\_polynomial () const
- Poly as\_polynomial () const
- bool is\_constant () const
- Rational asConstant () const
- bool isRational () const
- · Rational asRational () const
- bool is\_integer () const
- bool operator== (const SqrtEx &\_toCompareWith) const
- SqrtEx & operator= (const Poly &\_poly)
- SqrtEx operator+ (const SqrtEx &rhs) const
- SqrtEx operator- (const SqrtEx &rhs) const
- SqrtEx operator\* (const SqrtEx &rhs) const
- SqrtEx operator/ (const SqrtEx &rhs) const
- std::string toString (bool \_infix=false, bool \_friendlyNames=true) const

# Friends

```
    template<typename P >
        std::ostream & operator<< (std::ostream &_out, const SqrtEx< P > &_sqrtEx)
        Prints the given square root expression on the given stream.
```

## 12.357.1 Member Typedef Documentation

```
12.357.1.1 Rational template<typename Poly > using carl::SqrtEx< Poly >::Rational = typename UnderlyingNumberType<Poly>::type
```

## 12.357.2 Constructor & Destructor Documentation

Constructs a square root expression from a polynomial p leading to (p + 0 \* sqrt(0)) / 1.

#### **Parameters**

\_poly | The polynomial to construct a square root expression for.

Constructs a square root expression from given constant part, factor, denominator and radicand.

### **Parameters**

| ₋constantPart | The constant part of the square root expression to construct. |
|---------------|---|
| ₋factor       | The factor of the square root expression to construct.        |
| ₋denominator  | The denominator of the square root expression to construct.   |
| ₋radicand     | The radicand of the square root expression to construct.      |

## 12.357.3 Member Function Documentation

```
12.357.3.1 as_polynomial() template<typename Poly > Poly carl::SqrtEx< Poly >::as_polynomial ( ) const [inline]
```

#### Returns

The square root expression as a polynomial (note that there must be no square root nor denominator

```
12.357.3.2 asConstant() template<typename Poly >
Rational carl::SqrtEx< Poly >::asConstant ( ) const [inline]
```

## Returns

This sqrtEx as an integer (note, that it must actually represent an integer then).

```
12.357.3.3 asRational() template<typename Poly >
Rational carl::SqrtEx< Poly >::asRational () const [inline]
```

# Returns

This sqrtEx as a rational (note, that it must actually represent a rational then).

```
12.357.3.4 constant_part() template<typename Poly > const Poly& carl::SqrtEx< Poly >::constant_part ( ) const [inline]
```

#### Returns

A constant reference to the constant part of this square root expression.

```
12.357.3.5 denominator() template<typename Poly >
const Poly& carl::SqrtEx< Poly >::denominator ( ) const [inline]
```

#### Returns

A constant reference to the denominator of this square root expression.

```
12.357.3.6 factor() template<typename Poly >
const Poly& carl::SqrtEx< Poly >::factor ( ) const [inline]
```

#### Returns

A constant reference to the factor of this square root expression.

```
12.357.3.7 has_sqrt() template<typename Poly > bool carl::SqrtEx< Poly >::has_sqrt ( ) const [inline]
```

#### Returns

true, if the square root expression has a non trivial radicand; false, otherwise.

```
12.357.3.8 is_constant() template<typename Poly > bool carl::SqrtEx< Poly >::is_constant ( ) const [inline]
```

# Returns

true, if there is no variable in this square root expression; false, otherwise.

```
12.357.3.9 is_integer() template<typename Poly >
bool carl::SqrtEx< Poly >::is_integer ( ) const [inline]
```

# Returns

true, if the this square root expression corresponds to an integer value; false, otherwise.

```
12.357.3.10 is_polynomial() template<typename Poly > bool carl::SqrtEx< Poly >::is_polynomial ( ) const [inline]
```

## Returns

true, if the square root expression can be expressed as a polynomial; false, otherwise.

```
12.357.3.11 isRational() template<typename Poly > bool carl::SqrtEx< Poly >::isRational () const [inline]
```

# Returns

true, if there is no variable in this square root expression; false, otherwise.

#### **Parameters**

| ₋factorA | First factor.  |
|----------|----------------|
| ₋factorB | Second factor. |

# Returns

The product of the given square root expressions.

#### **Parameters**

| _summandA | First summand.  |
|-----------|-----------------|
| _summandB | Second summand. |

# Returns

The sum of the given square root expressions.

#### **Parameters**

| ₋minuend    | Minuend.    |
|-------------|-------------|
| _subtrahend | Subtrahend. |

#### Returns

The difference of the given square root expressions.

## **Parameters**

| ₋dividend | Dividend. |
|-----------|-----------|
| _divisor  | Divisor.  |

# Returns

The result of the first given square root expression divided by the second one Note that the second argument is not allowed to contain a square root.

# **Parameters**

| _sqrtEx A square root expression, which gets the new content of this square root expression. |
|--|
|--|

# Returns

A reference to this object.

## **Parameters**

\_poly A polynomial, which gets the new content of this square root expression.

#### Returns

A reference to this object.

## **Parameters**

| ₋sqrtEx | Square root expression to compare with. |
|---------|---|
|---------|---|

## **Returns**

true, if this square root expression and the given one are equal; false, otherwise.

```
12.357.3.18 radicand() template<typename Poly > const Poly& carl::SqrtEx< Poly >::radicand ( ) const [inline]
```

## Returns

A constant reference to the radicand of this square root expression.

# Parameters

| _infix         | A string which is printed in the beginning of each row.  |
|----------------|--|
| _friendlyNames | A flag that indicates whether to print the variables with their internal representation (false) or |
|                | with their dedicated names.  |

# Returns

The string representation of this square root expression.

# 12.357.4 Friends And Related Function Documentation

Prints the given square root expression on the given stream.

#### **Parameters**

| _out    | The stream to print on.              |
|---------|--------------------------------------|
| ₋sqrtEx | The square root expression to print. |

## Returns

The stream after printing the square root expression on it.

# 12.358 carl::statistics::Statistics Class Reference

```
#include <Statistics.h>
```

## **Public Member Functions**

- Statistics ()=default
- virtual  $\sim$ Statistics ()=default
- Statistics (const Statistics &)=delete
- Statistics (Statistics &&)=delete
- Statistics & operator= (const Statistics &)=delete
- Statistics & operator= (Statistics &&)=delete
- void set\_name (const std::string &name)
- virtual bool enabled () const
- virtual void collect ()
- const auto & name () const
- · const auto & collected () const

# **Protected Member Functions**

template<typename T >
 void addKeyValuePair (const std::string &key, const T &value)

# 12.358.1 Constructor & Destructor Documentation

```
12.358.1.2 ~Statistics() virtual carl::statistics::Statistics::~Statistics ( ) [virtual],
[default]
12.358.1.3 Statistics() [2/3] carl::statistics::Statistics:(
            const Statistics & ) [delete]
12.358.1.4 Statistics() [3/3] carl::statistics::Statistics:(
            Statistics && ) [delete]
12.358.2 Member Function Documentation
12.358.2.1 addKeyValuePair() template<typename T >
void carl::statistics::Statistics::addKeyValuePair (
            const std::string & key,
            const T & value ) [inline], [protected]
12.358.2.2 collect() virtual void carl::statistics::Statistics::collect ( ) [inline], [virtual]
12.358.2.3 collected() const auto& carl::statistics::Statistics::collected ( ) const [inline]
12.358.2.4 enabled() virtual bool carl::statistics::Statistics::enabled ( ) const [inline],
[virtual]
12.358.2.5 name() const auto& carl::statistics::Statistics::name ( ) const [inline]
12.358.2.6 operator=() [1/2] Statistics& carl::statistics::Statistics::operator= (
            const Statistics & ) [delete]
```

```
12.358.2.7 operator=() [2/2] Statistics@ carl::statistics::Statistics::operator= (
             Statistics && ) [delete]
12.358.2.8 set_name() void carl::statistics::Statistics::set_name (
             const std::string & name ) [inline]
12.359 carl::statistics::StatisticsCollector Class Reference
#include <StatisticsCollector.h>
Public Member Functions
   • template<typename T >
     T & get (const std::string &name)

    void collect ()

   • const auto & statistics () const
Static Public Member Functions
   • static StatisticsCollector & getInstance ()
        Returns the single instance of this class by reference.
12.359.1 Member Function Documentation
12.359.1.1 collect() void carl::statistics::StatisticsCollector::collect ( )
12.359.1.2 get() template<typename T >
T& carl::statistics::StatisticsCollector::get (
             const std::string & name ) [inline]
12.359.1.3 getInstance() static StatisticsCollector & carl::Singleton< StatisticsCollector >←
::getInstance ( ) [inline], [static], [inherited]
```

Returns the single instance of this class by reference.

If there is no instance yet, a new one is created.

**12.359.1.4 statistics()** const auto& carl::statistics::StatisticsCollector::statistics ( ) const [inline]

# 12.360 carl::statistics::StatisticsPrinter< SOF > Struct Template Reference

#include <StatisticsPrinter.h>

# 12.361 carl::StdAdding< Polynomial > Struct Template Reference

```
#include <GBUpdateProcedures.h>
```

#### **Public Member Functions**

- virtual ∼StdAdding ()=default
- bool addToGb (const Polynomial &p, std::shared\_ptr< Ideal< Polynomial >> gb, UpdateFnc \*update)

#### 12.361.1 Constructor & Destructor Documentation

```
12.361.1.1 ~StdAdding() template<typename Polynomial > virtual carl::StdAdding< Polynomial >::~StdAdding ( ) [virtual], [default]
```

# 12.361.2 Member Function Documentation

# 12.362 carl::StdMultivariatePolynomialPolicies < ReasonsAdaptor, Allocator > Struct Template Reference

The default policy for polynomials.

```
#include <MultivariatePolynomialPolicy.h>
```

# **Public Member Functions**

- void setReason (unsigned index)
- BitVector getReasons () const
- void setReasons (const BitVector &) const

# **Static Public Attributes**

- static const bool searchLinear = true

  Linear searching means that we search linearly for a term instead of applying e.g.
- static const bool has\_reasons = ReasonsAdaptor::has\_reasons

# 12.362.1 Detailed Description

template<typename ReasonsAdaptor = NoReasons, typename Allocator = NoAllocator> struct carl::StdMultivariatePolynomialPolicies< ReasonsAdaptor, Allocator >

The default policy for polynomials.

# 12.362.2 Member Function Documentation

```
12.362.2.1 getReasons() BitVector carl::NoReasons::getReasons ( ) const [inline], [inherited]
```

```
12.362.2.2 setReason() void carl::NoReasons::setReason ( unsigned index ) [inherited]
```

# 12.362.3 Field Documentation

```
12.362.3.1 has_reasons template<typename ReasonsAdaptor = NoReasons, typename Allocator = No↔ Allocator>
const bool carl::StdMultivariatePolynomialPolicies< ReasonsAdaptor, Allocator >::has_reasons = ReasonsAdaptor::has_reasons [static]
```

```
12.362.3.2 searchLinear template<typename ReasonsAdaptor = NoReasons, typename Allocator = NoAllocator>
const bool carl::StdMultivariatePolynomialPolicies< ReasonsAdaptor, Allocator >::searchLinear = true [static]
```

Linear searching means that we search linearly for a term instead of applying e.g.

binary search. Although the worst-case complexity is worse, for polynomials with a small nr of terms, this should be better.

# 12.363 carl::strategy Struct Reference

#include <MultivariateHornerSettings.h>

## **Static Public Attributes**

- static CONSTEXPR variableSelectionHeurisics selectionType = GREEDY\_I
- static constexpr double targetDiameter = 0.1
- static CONSTEXPR bool use\_arithmeticOperationsCounter = false

# 12.363.1 Field Documentation

```
12.363.1.1 selectionType CONSTEXPR variableSelectionHeurisics carl::strategy::selectionType = GREEDY_I [static]
```

```
12.363.1.2 targetDiameter constexpr double carl::strategy::targetDiameter = 0.1 [static], [constexpr]
```

```
12.363.1.3 use_arithmeticOperationsCounter CONSTEXPR bool carl::strategy::use_arithmetic← OperationsCounter = false [static]
```

# 12.364 carl::detail::stream\_joined\_impl< T, F > Struct Template Reference

#include <streamingOperators.h>

# **Data Fields**

- std::string glue
- · const T & values
- F callable

# 12.364.1 Field Documentation

```
12.364.1.1 callable template<typename T , typename F > F carl::detail::stream.joined.impl< T, F >::callable
```

```
12.364.1.2 glue template<typename T , typename F >
std::string carl::detail::stream_joined_impl< T, F >::glue
```

```
12.364.1.3 values template<typename T , typename F > const T& carl::detail::stream_joined_impl< T, F >::values
```

# 12.365 carl::logging::StreamSink Class Reference

Logging sink that wraps an arbitrary std::ostream.

```
#include <Sink.h>
```

## **Public Member Functions**

• StreamSink (std::ostream &\_os)

Create a StreamSink from some output stream.

• std::ostream & log () noexcept override

Abstract logging interface.

# 12.365.1 Detailed Description

Logging sink that wraps an arbitrary std::ostream.

It is meant to be used for streams like std::cout or std::cerr.

# 12.365.2 Constructor & Destructor Documentation

```
12.365.2.1 StreamSink() carl::logging::StreamSink::StreamSink ( std::ostream & Los ) [inline], [explicit]
```

Create a StreamSink from some output stream.

#### **Parameters**

```
_os Output stream.
```

## 12.365.3 Member Function Documentation

**12.365.3.1** log() std::ostream& carl::logging::StreamSink::log () [inline], [override], [virtual], [noexcept]

Abstract logging interface.

The intended usage is to write any log output to the output stream returned by this function.

#### Returns

Output stream.

Implements carl::logging::Sink.

# 12.366 carl::io::StringParser Class Reference

```
#include <StringParser.h>
```

#### **Public Member Functions**

- StringParser ()
- const std::map< std::string, Variable > & variables () const
- void setVariables (std::list< std::string > variables)
- bool setImplicitMultiplicationMode (bool to)
- void setSumOfTermsForm (bool to)

In SumOfTermsForm, input strings are expected to be of the form " $c_-1 * m_-1 + ... + c_-n * m_-n$ ", where  $c_-i$  are coefficients and  $m_-i$  are monomials.

- template<typename C , typename O = typename MultivariatePolynomial<C>::OrderedBy, typename P = typename Multivariate ← Polynomial<C>::Policy>
  - RationalFunction < MultivariatePolynomial < C, O, P >> parseRationalFunction (const std::string &input $\leftarrow$  String) const
- template<typename C , typename O = typename MultivariatePolynomial<C>::OrderedBy, typename P = typename Multivariate ← Polynomial<C>::Policy>
- MultivariatePolynomial < C, O, P > parseMultivariatePolynomial (const std::string &inputString) const
- template<typename C >

Term < C > parseTerm (const std::string &inputStr) const

#### **Protected Member Functions**

template < typename C >
 C constructCoefficient (const std::string &inputString) const

# **Protected Attributes**

- · bool mSingleSymbVariables
- bool mImplicitMultiplicationMode = false
- bool mSumOfTermsForm = true
- std::map< std::string, Variable > mVars

# 12.366.1 Constructor & Destructor Documentation

```
12.366.1.1 StringParser() carl::io::StringParser::StringParser () [inline]
 12.366.2 Member Function Documentation
12.366.2.1 constructCoefficient() template<typename C >
 C carl::io::StringParser::constructCoefficient (
                                                                                     const std::string & inputString ) const [inline], [protected]
\textbf{12.366.2.2} \quad \textbf{parseMultivariatePolynomial()} \quad \texttt{template} < \texttt{typename C , typename O = typename Multivariate} \leftarrow \texttt{typename C } \\ \textbf{12.366.2.2} \quad \textbf{12.
Polynomial<C>::OrderedBy, typename P = typename MultivariatePolynomial<C>::Policy>
MultivariatePolynomial <C, O, P > carl::io::StringParser::parseMultivariatePolynomial (
                                                                                     const std::string & inputString ) const [inline]
\textbf{12.366.2.3} \quad \textbf{parseRationalFunction()} \quad \texttt{template} < \texttt{typename C , typename O = typename Multivariate} \leftarrow
Polynomial<C>::OrderedBy, typename P = typename MultivariatePolynomial<C>::Policy>
 Rational Function < \texttt{MultivariatePolynomial} < \texttt{C}, \texttt{O}, \texttt{P} > \texttt{carl} :: \texttt{io} :: \texttt{StringParser} :: \texttt{parseRational} \leftarrow \texttt{C} :: \texttt{ParseRational} + \texttt{C} :: \texttt{C}
 Function (
                                                                                     const std::string & inputString ) const [inline]
12.366.2.4 parseTerm() template<typename C >
 Term<C> carl::io::StringParser::parseTerm (
                                                                                    const std::string & inputStr ) const [inline]
 12.366.2.5 setImplicitMultiplicationMode() bool carl::io::StringParser::setImplicitMultiplication←
Mode (
                                                                                      bool to ) [inline]
```

In SumOfTermsForm, input strings are expected to be of the form " $c_-1 * m_-1 + ... + c_-n * m_-n$ ", where  $c_-i$  are coefficients and  $m_-i$  are monomials.

# **Parameters**

to value to set

Returns

```
12.366.2.7 setVariables() void carl::io::StringParser::setVariables ( std::list< std::string > variables ) [inline]
```

```
12.366.2.8 variables() const std::map<std::string, Variable>& carl::io::StringParser::variables ( ) const [inline]
```

## 12.366.3 Field Documentation

```
12.366.3.1 mlmplicitMultiplicationMode bool carl::io::StringParser::mImplicitMultiplicationMode = false [protected]
```

12.366.3.2 mSingleSymbVariables bool carl::io::StringParser::mSingleSymbVariables [protected]

**12.366.3.3 mSumOfTermsForm** bool carl::io::StringParser::mSumOfTermsForm = true [protected]

**12.366.3.4 mVars** std::map<std::string, Variable> carl::io::StringParser::mVars [protected]

# 12.367 carl::vs::detail::Substitution< Poly > Struct Template Reference

#include <substitute.h>

# **Public Member Functions**

- Substitution (const Variable &variable, const Term< Poly > &term)
- · const carl::Variable & variable () const
- const Term< Poly > & term () const

## **Data Fields**

- const Variable & m\_variable
- const Term< Poly > & m\_term

## 12.367.1 Constructor & Destructor Documentation

## 12.367.2 Member Function Documentation

```
12.367.2.1 term() template<class Poly > const Term<Poly>& carl::vs::detail::Substitution< Poly >::term () const [inline]
```

```
12.367.2.2 variable() template<class Poly > const carl::Variable& carl::vs::detail::Substitution< Poly >::variable ( ) const [inline]
```

# 12.367.3 Field Documentation

```
12.367.3.1 m_term template<class Poly > const Term<Poly>& carl::vs::detail::Substitution< Poly >::m_term
```

```
12.367.3.2 m_variable template<class Poly >
const Variable& carl::vs::detail::Substitution< Poly >::m_variable
```

# 12.368 carl::helper::Substitutor < Pol > Struct Template Reference

```
#include <Substitution.h>
```

## **Public Member Functions**

- Substitutor (const std::map< Formula< Pol >, Formula< Pol >> &repl)
- Formula < Pol > operator() (const Formula < Pol > &formula)

#### **Data Fields**

const std::map< Formula< Pol >, Formula< Pol >> & replacements

## 12.368.1 Constructor & Destructor Documentation

#### 12.368.2 Member Function Documentation

#### 12.368.3 Field Documentation

```
12.368.3.1 replacements template<typename Pol > const std::map<Formula<Pol>,Formula<Pol>>& carl::helper::Substitutor< Pol >::replacements
```

# 12.369 carl::MultiplicationTable < Number >::TableContent Struct Reference

```
#include <MultiplicationTable.h>
```

# **Data Fields**

- BaseRepresentation < Number > br
- IndexPairs pairs

## 12.369.1 Field Documentation

# **Public Member Functions**

- TarskiQueryManager ()=default
- template<typename InputIt >
   TarskiQueryManager (InputIt first, InputIt last)
- QueryResultType operator() (const Polynomial &p) const
- QueryResultType operator() (const Number &c) const
- Polynomial reduceProduct (const Polynomial &a, const Polynomial &b) const

## 12.370.1 Member Typedef Documentation

```
12.370.1.1 QueryResultType template<typename Number > using carl::TarskiQueryManager< Number >::QueryResultType = int
```

### 12.370.2 Constructor & Destructor Documentation

```
12.370.2.1 TarskiQueryManager() [1/2] template<typename Number > carl::TarskiQueryManager< Number >::TarskiQueryManager ( ) [default]
```

```
12.370.2.2 TarskiQueryManager() [2/2] template<typename Number > template<typename InputIt > carl::TarskiQueryManager< Number >::TarskiQueryManager ( InputIt first, InputIt last ) [inline]
```

### 12.370.3 Member Function Documentation

## 12.371 carl::TaylorExpansion < Integer > Class Template Reference

```
#include <TaylorExpansion.h>
```

#### **Static Public Member Functions**

• static Polynomial ideal\_adic\_coeff (Polynomial &p, Variable::Arg x\_v, FiniteInt a, std::size\_t k)

## 12.371.1 Member Function Documentation

## 12.372 carl::Term < Coefficient > Class Template Reference

Represents a single term, that is a numeric coefficient and a monomial.

```
#include <Term.h>
```

#### **Public Member Functions**

• Term ()=default

Default constructor.

• Term (const Coefficient &c)

Constructs a term of value c.

• Term (Variable v)

Constructs a term of value v.

• Term (Monomial::Arg m)

Constructs a term of value m.

Term (Monomial::Arg &&m)

Constructs a term of value m.

• Term (const Coefficient &c, Monomial::Arg m)

Constructs a term of value  $c \cdot m$ .

• Term (Coefficient &&c, Monomial::Arg &&m)

Constructs a term of value  $c \cdot m$ .

• Term (const Coefficient &c, Variable v, uint e)

Constructs a term of value  $c \cdot v^e$ .

• Coefficient & coeff ()

Get the coefficient.

- const Coefficient & coeff () const
- Monomial::Arg & monomial ()

Get the monomial.

- · const Monomial::Arg & monomial () const
- · uint tdeg () const

Gives the total degree, i.e.

• bool is\_zero () const

Checks whether the term is zero.

• bool is\_one () const

Checks whether the term equals one.

• bool is\_constant () const

Checks whether the monomial is a constant.

- bool integer\_valued () const
- bool is\_linear () const

Checks whether the monomial has exactly the degree one.

- std::size\_t num\_variables () const
- bool has (Variable v) const
- Term drop\_variable (Variable v) const

Removes the given variable from the term.

bool has\_no\_other\_variable (Variable v) const

Checks if the monomial is either a constant or the only variable occuring is the variable v.

- bool is\_single\_variable () const
- Variable single\_variable () const

For terms with exactly one variable, get this variable.

• bool is\_square () const

Checks if the term is a square.

• void clear ()

Set the term to zero with the canonical representation.

· void negate ()

Negates the term by negating the coefficient.

• Term divide (const Coefficient &c) const

- bool divide (const Coefficient &c, Term &res) const
- · bool divide (Variable v, Term &res) const
- bool divide (const Monomial::Arg &m, Term &res) const
- · bool divide (const Term &t, Term &res) const
- Term calcLcmAndDivideBy (const Monomial::Arg &m) const
- bool sqrt (Term &res) const

Calculates the square root of this term.

- template < typename C = Coefficient, EnableIf < is\_field\_type < C >> = dummy > bool divisible (const Term &t) const
- template<typename C = Coefficient, Disablelf< is\_field\_type< C >> = dummy> bool divisible (const Term &t) const
- bool is\_consistent () const

#### **Static Public Member Functions**

- static bool monomialEqual (const Term &lhs, const Term &rhs)
  - Checks if two terms have the same monomial.
- static bool monomialEqual (const std::shared\_ptr< const Term > &lhs, const std::shared\_ptr< const Term > &rhs)
- static bool monomialLess (const Term &lhs, const Term &rhs)
- static bool monomialLess (const std::shared\_ptr< const Term > &lhs, const std::shared\_ptr< const Term > &rhs)

#### **Friends**

template<typename Coeff >
 std::ostream & operator<< (std::ostream &os, const Term< Coeff > &rhs)
 Streaming operator for Term.

## **Division operators**

template < typename Coeff > const Term < Coeff > operator/ (const Term < Coeff > &lhs, uint rhs)
 Perform a division involving a term.

### 12.372.1 Detailed Description

```
template<typename Coefficient> class carl::Term< Coefficient >
```

Represents a single term, that is a numeric coefficient and a monomial.

#### 12.372.2 Constructor & Destructor Documentation

```
12.372.2.1 Term() [1/8] template<typename Coefficient > carl::Term< Coefficient >::Term ( ) [default]
```

Default constructor.

Constructs a term of value zero.

Constructs a term of value c.

#### **Parameters**

c Coefficient.

Constructs a term of value v.

### **Parameters**

```
v Variable.
```

```
12.372.2.4 Term() [4/8] template<typename Coefficient > carl::Term< Coefficient >::Term (

Monomial::Arg m ) [explicit]
```

Constructs a term of value m.

## **Parameters**

```
m Monomial pointer.
```

```
12.372.2.5 Term() [5/8] template<typename Coefficient > carl::Term< Coefficient >::Term (

Monomial::Arg && m ) [explicit]
```

Constructs a term of value m.

### **Parameters**

```
m Monomial pointer.
```

Constructs a term of value  $c \cdot m$ .

## **Parameters**

| С | Coefficient.      |  |
|---|-------------------|--|
| m | Monomial pointer. |  |

Constructs a term of value  $c \cdot m$ .

### **Parameters**

| С | Coefficient.      |  |
|---|-------------------|--|
| m | Monomial pointer. |  |

Constructs a term of value  $c \cdot v^e$ .

#### **Parameters**

| С | Coefficient. |
|---|--------------|
| V | Variable.    |
| е | Exponent.    |

### 12.372.3 Member Function Documentation

Set the term to zero with the canonical representation.

```
12.372.3.3 coeff() [1/2] template<typename Coefficient > Coefficient & carl::Term< Coefficient >::coeff ( ) [inline]

Get the coefficient.
```

Returns

Coefficient.

```
12.372.3.4 coeff() [2/2] template<typename Coefficient > const Coefficient& carl::Term< Coefficient >::coeff () const [inline]
```

```
12.372.3.5 divide() [1/5] template<typename Coefficient > Term< Coefficient > carl::Term< Coefficient >::divide ( const Coefficient & c ) const
```

#### **Parameters**

```
c a non-zero coefficient.
```

Returns

Removes the given variable from the term.

#### **Parameters**

v The variable to check for its occurrence.

#### Returns

true, if the variable occurs in this term.

Checks if the monomial is either a constant or the only variable occuring is the variable v.

| Da |    |   |    |   |    |
|----|----|---|----|---|----|
| ra | ra | m | eı | œ | rs |

v The variable which may occur.

### **Returns**

true if no variable occurs, or just v occurs.

```
12.372.3.15 integer_valued() template<typename Coefficient > bool carl::Term< Coefficient >::integer_valued () const [inline]
```

### Returns

true, if the image of this term is integer-valued.

```
12.372.3.16 is_consistent() template<typename Coefficient > bool carl::Term< Coefficient >::is_consistent
```

```
12.372.3.17 is_constant() template<typename Coefficient > bool carl::Term< Coefficient >::is_constant ( ) const [inline]
```

Checks whether the monomial is a constant.

Returns

```
12.372.3.18 is_linear() template<typename Coefficient > bool carl::Term< Coefficient >::is_linear ( ) const [inline]
```

Checks whether the monomial has exactly the degree one.

Returns

```
12.372.3.19 is_one() template<typename Coefficient > bool carl::Term< Coefficient >::is_one () const [inline]
```

Checks whether the term equals one.

Returns

```
12.372.3.20 is_single_variable() template<typename Coefficient > bool carl::Term< Coefficient >::is_single_variable () const [inline]
```

```
12.372.3.21 is_square() template<typename Coefficient > bool carl::Term< Coefficient >::is_square () const [inline]
```

Checks if the term is a square.

Returns

If this is square.

```
12.372.3.22 is_zero() template<typename Coefficient > bool carl::Term< Coefficient >::is_zero ( ) const [inline]
```

Checks whether the term is zero.

Returns

```
12.372.3.23 monomial() [1/2] template<typename Coefficient >
Monomial::Arg& carl::Term< Coefficient >::monomial ( ) [inline]
```

Get the monomial.

**Returns** 

Monomial.

```
12.372.3.24 monomial() [2/2] template<typename Coefficient > const Monomial::Arg& carl::Term< Coefficient >::monomial ( ) const [inline]
```

Checks if two terms have the same monomial.

#### **Parameters**

| lhs | First term.  |
|-----|--------------|
| rhs | Second term. |

#### Returns

If both terms have the same monomial.

```
12.372.3.29 negate() template<typename Coefficient > void carl::Term< Coefficient >::negate ( ) [inline]
```

Negates the term by negating the coefficient.

```
12.372.3.30 num_variables() template<typename Coefficient > std::size_t carl::Term< Coefficient >::num_variables () const [inline]
```

Returns

```
12.372.3.31 single_variable() template<typename Coefficient >
Variable carl::Term< Coefficient >::single_variable () const [inline]
```

For terms with exactly one variable, get this variable.

### Returns

The only variable occuring in the term.

Calculates the square root of this term.

Returns true, iff the term is a square as checked by is\_square(). In that case, res will changed to be the square root. Otherwise, res is undefined.

### **Parameters**

```
res | Square root of this term.
```

#### Returns

If square root could be calculated.

```
12.372.3.33 tdeg() template<typename Coefficient >
uint carl::Term< Coefficient >::tdeg ( ) const [inline]
```

Gives the total degree, i.e.

the sum of all exponents.

## Returns

Total degree.

## 12.372.4 Friends And Related Function Documentation

Perform a division involving a term.

### **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

### Returns

lhs / rhs

Streaming operator for Term.

## **Parameters**

| os  | Output stream. |  |
|-----|----------------|--|
| rhs | Term.          |  |

## Returns

os

## 12.373 carl::vs::Term< Poly > Class Template Reference

```
#include <term.h>
```

## **Public Member Functions**

- Term (TermType type, std::optional < SqrtEx < Poly >> sqrt\_ex)
- bool is\_normal () const

- bool is\_plus\_eps () const
- bool is\_minus\_infty () const
- bool is\_plus\_infty () const
- const SqrtEx< Poly > sqrt\_ex () const
- TermType type () const
- bool operator== (const Term &) const

#### **Static Public Member Functions**

```
    static Term normal (const SqrtEx< Poly > &sqrt_ex)
```

- static Term plus\_eps (const SqrtEx< Poly > &sqrt\_ex)
- static Term minus\_infty ()
- static Term plus\_infty ()

#### 12.373.1 Constructor & Destructor Documentation

### 12.373.2 Member Function Documentation

```
12.373.2.1 is_minus_infty() template<class Poly > bool carl::vs::Term< Poly >::is_minus_infty () const [inline]
```

```
12.373.2.2 is_normal() template<class Poly >
bool carl::vs::Term< Poly >::is_normal ( ) const [inline]
```

```
12.373.2.3 is_plus_eps() template<class Poly > bool carl::vs::Term< Poly >::is_plus_eps () const [inline]
```

```
12.373.2.4 is_plus_infty() template<class Poly > bool carl::vs::Term< Poly >::is_plus_infty ( ) const [inline]
```

```
12.373.2.5 minus_infty() template<class Poly >
static Term carl::vs::Term< Poly >::minus_infty ( ) [inline], [static]
12.373.2.6 normal() template<class Poly >
static Term carl::vs::Term< Poly >::normal (
            const SqrtEx< Poly > & sqrt_ex ) [inline], [static]
12.373.2.7 operator == () template < class Poly >
bool carl::vs::Term< Poly >::operator== (
            const Term< Poly > & ) const
12.373.2.8 plus_eps() template<class Poly >
static Term carl::vs::Term< Poly >::plus_eps (
            const SqrtEx< Poly > & sqrt_ex ) [inline], [static]
12.373.2.9 plus_infty() template<class Poly >
static Term carl::vs::Term< Poly >::plus_infty ( ) [inline], [static]
12.373.2.10 sqrt_ex() template<class Poly >
const SqrtEx<Poly> carl::vs::Term< Poly >::sqrt_ex ( ) const [inline]
12.373.2.11 type() template<class Poly >
TermType carl::vs::Term< Poly >::type ( ) const [inline]
12.374 carl::TermAdditionManager < Polynomial, Ordering > Class Template Reference
#include <TermAdditionManager.h>
Public Types

    using IDType = unsigned

    using Coeff = typename Polynomial::CoeffType

   • using TermType = Term< Coeff >
   • using TermPtr = TermType
   • using TermIDs = std::vector< IDType >
   • using Terms = std::vector < TermPtr >

    using Tuple = std::tuple < TermIDs, Terms, bool, Coeff, IDType >
```

using TAMId = typename std::list< Tuple >::iterator

### **Public Member Functions**

- TermAdditionManager ()
- TAMId getId (std::size\_t expectedSize=0)
- template<bool SizeUnknown, bool NewMonomials = true> void addTerm (TAMId id, const TermPtr &term)
- TermType getMaxTerm (TAMId id) const
- void readTerms (TAMId id, Terms &terms)
- void dropTerms (TAMId id)

## 12.374.1 Member Typedef Documentation

```
12.374.1.1 Coeff template<typename Polynomial , typename Ordering > using carl::TermAdditionManager< Polynomial, Ordering >::Coeff = typename Polynomial::Coeff← Type
```

```
12.374.1.2 IDType template<typename Polynomial , typename Ordering > using carl::TermAdditionManager< Polynomial, Ordering >::IDType = unsigned
```

```
12.374.1.3 TAMId template<typename Polynomial , typename Ordering > using carl::TermAdditionManager< Polynomial, Ordering >::TAMId = typename std::list<Tuple>← ::iterator
```

```
12.374.1.4 TermIDs template<typename Polynomial , typename Ordering > using carl::TermAdditionManager< Polynomial, Ordering >::TermIDs = std::vector<IDType>
```

```
12.374.1.5 TermPtr template<typename Polynomial , typename Ordering > using carl::TermAdditionManager< Polynomial, Ordering >::TermPtr = TermType
```

```
12.374.1.6 Terms template<typename Polynomial , typename Ordering > using carl::TermAdditionManager< Polynomial, Ordering >::Terms = std::vector<TermPtr>
```

```
12.374.1.7 TermType template<typename Polynomial , typename Ordering >
using carl::TermAdditionManager< Polynomial, Ordering >::TermType = Term<Coeff>
12.374.1.8 Tuple template<typename Polynomial , typename Ordering >
using carl::TermAdditionManager< Polynomial, Ordering >::Tuple = std::tuple<TermIDs,Terms,bool,Coeff,IDType>
12.374.2 Constructor & Destructor Documentation
12.374.2.1 TermAdditionManager() template<typename Polynomial , typename Ordering >
carl::TermAdditionManager< Polynomial, Ordering >::TermAdditionManager ( ) [inline]
12.374.3 Member Function Documentation
12.374.3.1 addTerm() template<typename Polynomial , typename Ordering >
template<bool SizeUnknown, bool NewMonomials = true>
\verb"void carl::TermAdditionManager< Polynomial, Ordering >::addTerm (
            TAMId id,
            const TermPtr & term ) [inline]
12.374.3.2 dropTerms() template<typename Polynomial , typename Ordering >
void carl::TermAdditionManager< Polynomial, Ordering >::dropTerms (
            TAMId id ) [inline]
12.374.3.3 getId() template<typename Polynomial , typename Ordering >
TAMId carl::TermAdditionManager< Polynomial, Ordering >::getId (
            std::size_t expectedSize = 0 ) [inline]
12.374.3.4 getMaxTerm() template<typename Polynomial , typename Ordering >
TermType carl::TermAdditionManager< Polynomial, Ordering >::getMaxTerm (
            TAMId id ) const [inline]
```

## 12.375 carl::ThomEncoding< Number > Class Template Reference

```
#include <ThomEncoding.h>
```

#### **Public Member Functions**

- ThomEncoding (SignCondition sc, const Polynomial &p, Variable mainVar, std::shared\_ptr< ThomEncoding</li>
   Number >> point, std::shared\_ptr< SignDetermination</li>
   Number >> sd, uint mRelevant)
- ThomEncoding (const Number &n, Variable mainVar, std::shared\_ptr< ThomEncoding< Number >> point=nullptr)
- ThomEncoding (const ThomEncoding< Number > &te, std::shared\_ptr< ThomEncoding< Number >> point)
- bool is\_number () const
- const auto & get\_number () const
- bool containedIn (const Interval < Number > &i) const
- · SignCondition signCondition () const
- SignCondition relevantSignCondition () const
- Variable::Arg main\_var () const
- const Polynomial & polynomial () const
- const ThomEncoding
   Number > & point () const
- SignDetermination < Number > sd () const
- std::list< Polynomial > relevantDerivatives () const
- ThomEncoding
   Number > lowestInChain () const
- · uint dimension () const
- std::list< Polynomial > accumulatePolynomials () const
- std::list< Variable > accumulateVariables () const
- · SignCondition accumulateSigns () const
- · SignCondition accumulateRelevantSigns () const
- Sign signOnPolynomial (const Polynomial &p) const
- bool makesPolynomialZero (const Polynomial &pol, Variable::Arg pol\_mainVar) const
- · void extendSignCondition () const
- Sign sgn (const UnivariatePolynomial < Number > &p) const
- Sign sgn (const Polynomial &p) const
- · Sign sgn () const
- bool is\_integral () const
- Number integer\_below () const
- Sign sgnReprNum () const
- bool is\_zero () const
- ThomEncoding
   Number > concat (const ThomEncoding
   Number > &other) const
- bool equals (const ThomEncoding< Number > &other) const
- ThomEncoding
   Number > operator+ (const Number &rhs) const
- void print (std::ostream &os) const

#### **Static Public Member Functions**

- static ThomEncoding < Number > analyzeTEMap (const std::map < Variable, ThomEncoding < Number >> &m)
- static ThomComparisonResult compare (const ThomEncoding< Number > &lhs, const ThomEncoding
   Number > &rhs)
- static ThomComparisonResult compareRational (const ThomEncoding< Number > &lhs, const Number &rhs)
- static ThomComparisonResult compareDifferentPoly (const ThomEncoding< Number > &lhs, const ThomEncoding< Number > &rhs)
- static ThomEncoding< Number > intermediatePoint (const ThomEncoding< Number > &lhs, const ThomEncoding< Number > &rhs)
- static Number intermediatePoint (const ThomEncoding< Number > &lhs, const Number &rhs)
- static Number intermediatePoint (const Number &lhs, const ThomEncoding < Number > &rhs)

#### 12.375.1 Constructor & Destructor Documentation

```
12.375.1.1 ThomEncoding() [1/3] template<typename Number >
carl::ThomEncoding< Number >::ThomEncoding (
            SignCondition sc,
            const Polynomial & p,
            Variable mainVar,
            std::shared_ptr< ThomEncoding< Number >> point,
            std::shared_ptr< SignDetermination< Number >> sd,
            uint mRelevant ) [inline]
12.375.1.2 ThomEncoding() [2/3] template<typename Number >
carl::ThomEncoding< Number >::ThomEncoding (
            const Number & n,
            Variable mainVar,
            std::shared.ptr< ThomEncoding< Number >> point = nullptr ) [inline]
12.375.1.3 ThomEncoding() [3/3] template<typename Number >
carl::ThomEncoding< Number >::ThomEncoding (
            const ThomEncoding< Number > & te,
            std::shared_ptr< ThomEncoding< Number >> point ) [inline]
```

## 12.375.2 Member Function Documentation

```
12.375.2.1 accumulatePolynomials() template<typename Number > std::list<Polynomial> carl::ThomEncoding< Number >::accumulatePolynomials ( ) const [inline]
```

```
12.375.2.2 accumulateRelevantSigns() template<typename Number >
SignCondition carl::ThomEncoding < Number >::accumulateRelevantSigns ( ) const [inline]
12.375.2.3 accumulateSigns() template<typename Number >
{\tt SignCondition\ carl::ThomEncoding<\ Number>::accumulateSigns\ (\ )\ const\ [inline]}
12.375.2.4 accumulateVariables() template<typename Number >
std::list<Variable> carl::ThomEncoding< Number >::accumulateVariables ( ) const [inline]
12.375.2.5 analyzeTEMap() template<typename Number >
static ThomEncoding<Number> carl::ThomEncoding< Number >::analyzeTEMap (
            const std::map< Variable, ThomEncoding< Number >> & m) [inline], [static]
12.375.2.6 compare() template<typename Number >
\verb|static ThomComparisonResult carl::ThomEncoding< \verb|Number| >::compare| (
            const ThomEncoding< Number > & lhs,
            const ThomEncoding< Number > & rhs ) [inline], [static]
12.375.2.7 compareDifferentPoly() template<typename Number >
static ThomComparisonResult carl::ThomEncoding< Number >::compareDifferentPoly (
            const ThomEncoding< Number > & lhs,
            const ThomEncoding< Number > & rhs ) [static]
12.375.2.8 compareRational() template<typename Number >
const ThomEncoding< Number > & lhs,
            const Number & rhs ) [inline], [static]
12.375.2.9 concat() template<typename Number >
ThomEncoding<Number> carl::ThomEncoding< Number >::concat (
            const ThomEncoding< Number > & other ) const [inline]
```

```
12.375.2.10 containedln() template<typename Number >
bool carl::ThomEncoding< Number >::containedIn (
            12.375.2.11 dimension() template<typename Number >
uint carl::ThomEncoding< Number >::dimension ( ) const [inline]
12.375.2.12 equals() template<typename Number >
bool carl::ThomEncoding< Number >::equals (
            const ThomEncoding< Number > & other ) const [inline]
12.375.2.13 extendSignCondition() template<typename Number >
void carl::ThomEncoding< Number >::extendSignCondition ( ) const [inline]
12.375.2.14 get_number() template<typename Number >
const auto& carl::ThomEncoding< Number >::get_number ( ) const [inline]
12.375.2.15 integer_below() template<typename Number >
Number carl::ThomEncoding< Number >::integer_below ( ) const [inline]
12.375.2.16 intermediatePoint() [1/3] template<typename Number >
static Number carl::ThomEncoding< Number >::intermediatePoint (
            const Number & 1hs,
            const ThomEncoding< Number > & rhs ) [inline], [static]
12.375.2.17 intermediatePoint() [2/3] template<typename Number >
static Number carl::ThomEncoding< Number >::intermediatePoint (
            const ThomEncoding < Number > & 1hs,
            const Number & rhs ) [inline], [static]
```

```
12.375.2.18 intermediatePoint() [3/3] template<typename Number >
static ThomEncoding<Number> carl::ThomEncoding< Number >::intermediatePoint (
             const ThomEncoding< Number > & lhs,
             const ThomEncoding< Number > & rhs ) [inline], [static]
12.375.2.19 is_integral() template<typename Number >
bool carl::ThomEncoding< Number >::is_integral ( ) const [inline]
12.375.2.20 is_number() template<typename Number >
bool carl::ThomEncoding< Number >::is_number ( ) const [inline]
12.375.2.21 is_zero() template<typename Number >
bool carl::ThomEncoding< Number >::is_zero ( ) const [inline]
12.375.2.22 lowestInChain() template<typename Number >
ThomEncoding<Number> carl::ThomEncoding< Number >::lowestInChain ( ) const [inline]
12.375.2.23 main_var() template<typename Number >
Variable::Arg carl::ThomEncoding< Number >::main_var ( ) const [inline]
12.375.2.24 makesPolynomialZero() template<typename Number >
bool carl::ThomEncoding< Number >::makesPolynomialZero (
             const Polynomial & pol,
             Variable::Arg pol_mainVar ) const [inline]
\textbf{12.375.2.25} \quad \textbf{operator+()} \quad \texttt{template} < \texttt{typename Number} \, > \,
ThomEncoding<Number> carl::ThomEncoding< Number >::operator+ (
             const Number & rhs ) const [inline]
12.375.2.26 point() template<typename Number >
const ThomEncoding<Number>& carl::ThomEncoding< Number >::point ( ) const [inline]
```

```
12.375.2.27 polynomial() template<typename Number >
const Polynomial& carl::ThomEncoding< Number >::polynomial ( ) const [inline]
12.375.2.28 print() template<typename Number >
void carl::ThomEncoding< Number >::print (
            std::ostream & os ) const [inline]
12.375.2.29 relevantDerivatives() template<typename Number >
std::list<Polynomial> carl::ThomEncoding< Number >::relevantDerivatives ( ) const [inline]
12.375.2.30 relevantSignCondition() template<typename Number >
SignCondition carl::ThomEncoding< Number >::relevantSignCondition ( ) const [inline]
12.375.2.31 sd() template<typename Number >
SignDetermination<Number> carl::ThomEncoding< Number >::sd ( ) const [inline]
12.375.2.32 sgn() [1/3] template<typename Number >
Sign carl::ThomEncoding< Number >::sgn ( ) const [inline]
12.375.2.33 sgn() [2/3] template<typename Number >
Sign carl::ThomEncoding< Number >::sgn (
            const Polynomial & p ) const [inline]
12.375.2.34 sgn() [3/3] template<typename Number >
Sign carl::ThomEncoding< Number >::sgn (
            const UnivariatePolynomial< Number > \& p ) const [inline]
12.375.2.35 sgnReprNum() template<typename Number >
Sign carl::ThomEncoding< Number >::sgnReprNum ( ) const [inline]
```

```
12.375.2.36 signCondition() template<typename Number >
SignCondition carl::ThomEncoding< Number >::signCondition ( ) const [inline]
12.375.2.37 signOnPolynomial() template<typename Number >
Sign carl::ThomEncoding< Number >::signOnPolynomial (
             const Polynomial & p ) const [inline]
12.376 carl::statistics::timer Class Reference
#include <Timing.h>
Public Member Functions

    void finish (timing::time_point start)

   · auto count () const
   • auto overall_ms () const
Static Public Member Functions
   • static timing::time_point start ()
12.376.1 Member Function Documentation
12.376.1.1 count() auto carl::statistics::timer::count ( ) const [inline]
12.376.1.2 finish() void carl::statistics::timer::finish (
             timing::time_point start ) [inline]
12.376.1.3 overall_ms() auto carl::statistics::timer::overall_ms () const [inline]
```

12.376.1.4 start() static timing::time\_point carl::statistics::timer::start () [inline], [static]

## 12.377 carl::Timer Class Reference

This classes provides an easy way to obtain the current number of milliseconds that the program has been running.

```
#include <Timer.h>
```

## **Public Member Functions**

- Timer () noexcept
- std::size\_t passed () const noexcept

Calculated the number of milliseconds since this object has been created.

· void reset () noexcept

Reset the start point to now.

## 12.377.1 Detailed Description

This classes provides an easy way to obtain the current number of milliseconds that the program has been running.

### 12.377.2 Constructor & Destructor Documentation

```
12.377.2.1 Timer() carl::Timer::Timer () [inline], [noexcept]
```

## 12.377.3 Member Function Documentation

```
12.377.3.1 passed() std::size_t carl::Timer::passed ( ) const [inline], [noexcept]
```

Calculated the number of milliseconds since this object has been created.

Returns

Milliseconds passed.

```
12.377.3.2 reset() void carl::Timer::reset ( ) [inline], [noexcept]
```

Reset the start point to now.

## 12.378 carl::ToGiNaC Class Reference

```
#include <GiNaCAdaptor.h>
```

## **Public Types**

- typedef GiNaC::numeric Number
- typedef GiNaC::symbol Variable
- typedef GiNaC::ex VariablePower
- · typedef GiNaC::ex Monomial
- typedef GiNaC::ex Term
- typedef GiNaC::ex MPolynomial
- typedef GiNaC::ex UPolynomial

### **Public Member Functions**

- Number operator() (const cln::cl\_RA &n)
- Number operator() (const mpq\_class &n)
- Variable operator() (carl::Variable::Arg v)
- VariablePower operator() (GiNaC::symbol v, const carl::exponent &exp)
- Monomial operator() (const std::vector< GiNaC::ex > &vp)
- template<typename Coeff >
   Term operator() (const GiNaC::numeric &n, const GiNaC::ex &mon)
- template<typename Coeff >
   MPolynomial operator() (const std::vector< GiNaC::ex > &terms)

## 12.378.1 Member Typedef Documentation

```
12.378.1.1 Monomial typedef GiNaC::ex carl::ToGiNaC::Monomial
```

12.378.1.2 MPolynomial typedef GiNaC::ex carl::ToGiNaC::MPolynomial

12.378.1.3 Number typedef GiNaC::numeric carl::ToGiNaC::Number

12.378.1.4 Term typedef GiNaC::ex carl::ToGiNaC::Term

12.378.1.5 UPolynomial typedef GiNaC::ex carl::ToGiNaC::UPolynomial

```
12.378.1.6 Variable typedef GiNaC::symbol carl::ToGiNaC::Variable
12.378.1.7 VariablePower typedef GiNaC::ex carl::ToGiNaC::VariablePower
12.378.2 Member Function Documentation
12.378.2.1 operator()() [1/7] Variable carl::ToGiNaC::operator() (
             carl::Variable::Arg v ) [inline]
12.378.2.2 operator()() [2/7] Number carl::ToGiNaC::operator() (
             const cln::cl_RA & n ) [inline]
12.378.2.3 operator()() [3/7] template<typename Coeff >
Term carl::ToGiNaC::operator() (
             const GiNaC::numeric & n,
             const GiNaC::ex & mon ) [inline]
12.378.2.4 operator()() [4/7] Number carl::ToGiNaC::operator() (
             \verb|const mpq_class & n | [inline]|\\
12.378.2.5 operator()() [5/7] template<typename Coeff >
MPolynomial carl::ToGiNaC::operator() (
             const std::vector< GiNaC::ex > & terms ) [inline]
12.378.2.6 operator()() [6/7] Monomial carl::ToGiNaC::operator() (
             const std::vector< GiNaC::ex > & vp ) [inline]
\textbf{12.378.2.7} \quad \textbf{operator()()} \; \texttt{[7/7]} \quad \texttt{VariablePower carl::ToGiNaC::operator()} \; \; \texttt{(}
             GiNaC::symbol v,
              const carl::exponent & exp ) [inline]
```

## 12.379 carl::tree < T > Class Template Reference

This class represents a tree.

```
#include <carlTree.h>
```

### **Public Types**

```
    using value_type = T

    using Node = tree_detail::Node < T >

template<bool reverse>
  using PreorderIterator = tree_detail::PreorderIterator < T, reverse >
• template<bool reverse>
  using PostorderIterator = tree_detail::PostorderIterator < T, reverse >
template<bool reverse>
  using LeafIterator = tree_detail::LeafIterator < T, reverse >
· template<bool reverse>
  using DepthIterator = tree_detail::DepthIterator < T, reverse >
```

- template<bool reverse> using ChildrenIterator = tree\_detail::ChildrenIterator < T, reverse >
- using PathIterator = tree\_detail::PathIterator < T >
- using iterator = PreorderIterator < false >

### **Public Member Functions**

- tree ()=default
- tree (const tree &t)=default
- tree (tree &&t) noexcept=default
- tree & operator= (const tree &t)=default
- tree & operator= (tree &&t) noexcept=default
- · void debug () const
- · iterator begin () const
- · iterator end () const
- iterator rbegin () const
- iterator rend () const
- PreorderIterator< false > begin\_preorder () const
- PreorderIterator< false > end\_preorder () const
- PreorderIterator< true > rbegin\_preorder () const
- PreorderIterator< true > rend\_preorder () const
- PostorderIterator< false > begin\_postorder () const
- PostorderIterator< false > end\_postorder () const
- PostorderIterator< true > rbegin\_postorder () const
- PostorderIterator< true > rend\_postorder () const
- LeafIterator< false > begin\_leaf () const
- LeafIterator< false > end\_leaf () const
- LeafIterator< true > rbegin\_leaf () const
- LeafIterator< true > rend\_leaf () const
- DepthIterator< false > begin\_depth (std::size\_t depth) const
- DepthIterator< false > end\_depth () const
- DepthIterator< true > rbegin\_depth (std::size\_t depth) const
- DepthIterator< true > rend\_depth () const
- template<typename Iterator > ChildrenIterator < false > begin\_children (const Iterator &it) const

```
    template<typename Iterator >

  ChildrenIterator < false > end_children (const Iterator &it) const
• template<typename Iterator >
  ChildrenIterator< true > rbegin_children (const Iterator &it) const
• template<typename Iterator >
  ChildrenIterator < true > rend_children (const Iterator &it) const
• template<typename Iterator >
  PathIterator begin_path (const Iterator &it) const

    PathIterator end_path () const

· std::size_t max_depth () const
      Retrieves the maximum depth of all elements.
• template<typename Iterator >
  std::size_t max_depth (const Iterator &it) const
• template<typename Iterator >
  bool is_leaf (const Iterator &it) const
      Check if the given element is a leaf.
template<typename Iterator >
  bool is_leftmost (const Iterator &it) const
      Check if the given element is a leftmost child.

    template<typename Iterator >

  bool is_rightmost (const Iterator &it) const
      Check if the given element is a rightmost child.
• template<typename Iterator >
  bool is_valid (const Iterator &it) const
• template<typename Iterator >
  Iterator get_parent (const Iterator &it) const
      Retrieves the parent of an element.
• template<typename Iterator >
  Iterator left_sibling (const Iterator &it) const

    iterator setRoot (const T &data)

      Sets the value of the root element.

    iterator setRoot (T &&data)

• void clear ()
      Clears the tree.

    iterator append (const T &data)

      Add the given data as last child of the root element.
• template<typename Iterator >
  Iterator append (Iterator parent, const T &data)
      Add the given data as last child of the given element.

    template<typename Iterator >

  Iterator insert (Iterator position, const T &data)
      Insert element before the given position.

    iterator append (tree &&tree)

      Append another tree as last child of the root element.
• template<typename Iterator >
  Iterator append (Iterator position, tree &&data)
      Append another tree as last child of the given element.

    template<typename Iterator >

  const Iterator & replace (const Iterator & position, const T & data)
• template<typename Iterator >
  Iterator erase (Iterator position)
      Erase the element at the given position.

    template<typename Iterator >

  void eraseChildren (const Iterator &position)
```

Erase all children of the given element.

- bool is\_consistent () const
- bool is\_consistent (std::size\_t node) const

#### **Friends**

template < typename TT, typename Iterator, bool reverse > struct tree\_detail::BaseIterator

### 12.379.1 Detailed Description

```
template<typename T> class carl::tree< T>
```

This class represents a tree.

It tries to stick to the STL style as close as possible.

### 12.379.2 Member Typedef Documentation

```
12.379.2.1 ChildrenIterator template<typename T >
template<bool reverse>
using carl::tree< T >::ChildrenIterator = tree.detail::ChildrenIterator<T,reverse>

12.379.2.2 DepthIterator template<typename T >
template<bool reverse>
using carl::tree< T >::DepthIterator = tree.detail::DepthIterator<T,reverse>

12.379.2.3 iterator template<typename T >
using carl::tree< T >::iterator = PreorderIterator<false>

12.379.2.4 Leafiterator template<typename T >
template<bool reverse>
```

using carl::tree< T >::LeafIterator = tree\_detail::LeafIterator<T,reverse>

```
12.379.2.5 Node template<typename T >
using carl::tree< T >::Node = tree_detail::Node<T>
12.379.2.6 PathIterator template<typename T >
using carl::tree< T >::PathIterator = tree_detail::PathIterator<T>
12.379.2.7 PostorderIterator template<typename T >
template<bool reverse>
using carl::tree< T >::PostorderIterator = tree_detail::PostorderIterator<T,reverse>
12.379.2.8 PreorderIterator template<typename T >
template<bool reverse>
using carl::tree< T >::PreorderIterator = tree_detail::PreorderIterator<T,reverse>
12.379.2.9 value_type template<typename T >
using carl::tree< T >::value_type = T
12.379.3 Constructor & Destructor Documentation
12.379.3.1 tree() [1/3] template<typename T >
carl::tree< T >::tree ( ) [default]
12.379.3.2 tree() [2/3] template<typename T >
carl::tree< T >::tree (
            const tree< T > & t ) [default]
12.379.3.3 tree() [3/3] template<typename T >
carl::tree< T >::tree (
            tree< T > && t ) [default], [noexcept]
12.379.4 Member Function Documentation
12.379.4.1 append() [1/4] template<typename T >
iterator carl::tree< T >::append (
            const T & data ) [inline]
```

Add the given data as last child of the root element.

### **Parameters**

## Returns

Iterator to inserted element.

Add the given data as last child of the given element.

### **Parameters**

| parent | Parent element. |
|--------|-----------------|
| data   | Data.           |

## Returns

Iterator to inserted element.

Append another tree as last child of the given element.

#### **Parameters**

| position | Element. |  |
|----------|----------|--|
| tree     | Tree.    |  |

## Returns

Iterator to root of inserted subtree.

```
12.379.4.4 append() [4/4] template<typename T > iterator carl::tree< T >::append ( tree< T > \&\& tree ) \quad [inline]
```

Append another tree as last child of the root element.

#### **Parameters**

```
tree Tree.
```

#### Returns

Iterator to root of inserted subtree.

```
12.379.4.5 begin() template<typename T >
iterator carl::tree< T >::begin ( ) const [inline]
12.379.4.6 begin_children() template<typename T >
template<typename Iterator >
ChildrenIterator<false> carl::tree< T >::begin_children (
            const Iterator & it ) const [inline]
12.379.4.7 begin_depth() template<typename T >
DepthIterator<false> carl::tree< T >::begin_depth (
            std::size_t depth ) const [inline]
12.379.4.8 begin_leaf() template<typename T >
LeafIterator<false> carl::tree< T >::begin_leaf ( ) const [inline]
12.379.4.9 begin_path() template<typename T >
template<typename Iterator >
PathIterator carl::tree< T >::begin_path (
            const Iterator & it ) const [inline]
```

12.379.4.10 begin\_postorder() template<typename T >

PostorderIterator<false> carl::tree< T >::begin\_postorder ( ) const [inline]

```
12.379.4.11 begin_preorder() template<typename T >
PreorderIterator<false> carl::tree< T >::begin.preorder ( ) const [inline]
12.379.4.12 clear() template<typename T >
void carl::tree< T >::clear ( ) [inline]
Clears the tree.
12.379.4.13 debug() template<typename T >
void carl::tree< T >::debug ( ) const [inline]
12.379.4.14 end() template<typename T >
iterator carl::tree< T >::end ( ) const [inline]
12.379.4.15 end_children() template<typename T >
template < typename Iterator >
ChildrenIterator<false> carl::tree< T >::end_children (
            const Iterator & it ) const [inline]
12.379.4.16 end_depth() template<typename T >
DepthIterator<false> carl::tree< T >::end.depth ( ) const [inline]
12.379.4.17 end_leaf() template<typename T >
LeafIterator<false> carl::tree< T >::end_leaf ( ) const [inline]
12.379.4.18 end_path() template<typename T >
PathIterator carl::tree< T >::end_path ( ) const [inline]
12.379.4.19 end_postorder() template<typename T >
PostorderIterator<false> carl::tree< T >::end.postorder ( ) const [inline]
```

```
12.379.4.20 end_preorder() template<typename T >
PreorderIterator<false> carl::tree< T >::end_preorder ( ) const [inline]
```

Erase the element at the given position.

Returns an iterator to the next position.

### **Parameters**

```
position Element.
```

### Returns

Next element.

Erase all children of the given element.

#### **Parameters**

```
position Element.
```

Retrieves the parent of an element.

#### **Parameters**

it Iterator.

#### Returns

Parent of it.

Insert element before the given position.

#### **Parameters**

| position | Position to insert before. |
|----------|----------------------------|
| data     | Element to insert.         |

### Returns

PreorderIterator to inserted element.

```
12.379.4.25 is_consistent() [1/2] template<typename T > bool carl::tree< T >::is_consistent ( ) const [inline]
```

Check if the given element is a leaf.

### **Parameters**

```
it Iterator.
```

#### Returns

If it is a leaf.

Check if the given element is a leftmost child.

#### **Parameters**

```
it Iterator.
```

#### Returns

If it is a leftmost child.

Check if the given element is a rightmost child.

## **Parameters**

```
it Iterator.
```

# Returns

If it is a rightmost child.

```
12.379.4.32 max_depth() [1/2] template<typename T >
std::size_t carl::tree< T >::max_depth ( ) const [inline]
```

Retrieves the maximum depth of all elements.

Returns

```
Maximum depth.
12.379.4.33 max_depth() [2/2] template<typename T >
template<typename Iterator >
std::size\_t carl::tree< T >::max\_depth (
            const Iterator & it ) const [inline]
12.379.4.34 operator=() [1/2] template<typename T >
tree& carl::tree< T >::operator= (
            const tree< T > & t ) [default]
12.379.4.35 operator=() [2/2] template<typename T >
tree& carl::tree< T >::operator= (
            tree< T > && t ) [default], [noexcept]
12.379.4.36 rbegin() template<typename T >
iterator carl::tree< T >::rbegin ( ) const [inline]
12.379.4.37 rbegin_children() template<typename T >
template<typename Iterator >
ChildrenIterator<true> carl::tree< T >::rbegin_children (
            const Iterator & it ) const [inline]
12.379.4.38 rbegin_depth() template<typename T >
DepthIterator<true> carl::tree< T >::rbegin_depth (
            std::size_t depth ) const [inline]
```

```
12.379.4.39 rbegin_leaf() template<typename T >
LeafIterator<true> carl::tree< T >::rbegin_leaf ( ) const [inline]
12.379.4.40 rbegin_postorder() template<typename T >
PostorderIterator<true> carl::tree< T >::rbegin_postorder ( ) const [inline]
12.379.4.41 rbegin_preorder() template<typename T >
PreorderIterator<true> carl::tree< T >::rbegin.preorder ( ) const [inline]
12.379.4.42 rend() template<typename T >
iterator carl::tree< T >::rend ( ) const [inline]
12.379.4.43 rend_children() template<typename T >
template<typename Iterator >
ChildrenIterator<true> carl::tree< T >::rend_children (
            const Iterator & it ) const [inline]
12.379.4.44 rend_depth() template<typename T >
DepthIterator<true> carl::tree< T >::rend_depth ( ) const [inline]
12.379.4.45 rend_leaf() template<typename T >
LeafIterator<true> carl::tree< T >::rend_leaf ( ) const [inline]
12.379.4.46 rend_postorder() template<typename T >
PostorderIterator<true> carl::tree< T >::rend.postorder () const [inline]
12.379.4.47 rend_preorder() template<typename T >
PreorderIterator<true> carl::tree< T >::rend.preorder ( ) const [inline]
```

Sets the value of the root element.

| Parameters |  |  |    |
|------------|--|--|----|
|            |  |  |    |
|            |  |  | rs |

# Returns

Iterator to the root.

# 12.379.5 Friends And Related Function Documentation

```
12.379.5.1 tree_detail::Baselterator template<typename T > template<typename TT , typename Iterator , bool reverse> friend struct tree_detail::BaseIterator [friend]
```

# 12.380 carl::detail::tuple\_accumulate\_impl< Tuple, T, F > Struct Template Reference

Helper functor for carl::tuple\_accumulate that actually does the work.

```
#include <tuple_util.h>
```

# 12.380.1 Detailed Description

```
template<typename Tuple, typename T, typename F> struct carl::detail::tuple_accumulate_impl< Tuple, T, F >
```

Helper functor for carl::tuple\_accumulate that actually does the work.

# 12.381 carl::tuple\_convert< Converter, Information, FOut, TOut > Class Template Reference

```
#include <tuple_util.h>
```

# **Public Member Functions**

- tuple\_convert (const Information &i)
- template<typename Tuple >
   std::tuple< FOut, TOut... > operator() (const Tuple &in)

# 12.381.1 Constructor & Destructor Documentation

#### 12.381.2 Member Function Documentation

# 12.382 carl::tuple\_convert< Converter, Information, Out > Class Template Reference

```
#include <tuple_util.h>
```

### **Public Member Functions**

- tuple\_convert (const Information &i)
- template<typename In >
   std::tuple< Out > operator() (const std::tuple< In > &in)

# 12.382.1 Constructor & Destructor Documentation

```
12.382.1.1 tuple_convert() template<typename Converter , typename Information , typename Out > carl::tuple_convert< Converter, Information, Out >::tuple_convert ( const Information & i ) [inline], [explicit]
```

# 12.382.2 Member Function Documentation

# 12.383 carl::covering::TypedSetCover < Set > Class Template Reference

Represents a set cover problem where a set is represented by some type.

```
#include <TypedSetCover.h>
```

#### **Public Member Functions**

void set (const Set &s, std::size\_t element)

States that s covers the given element.

void set (const Set &s, const Bitset &elements)

States that s covers the given elements.

- const Set & get\_set (std::size\_t sid) const
- operator const SetCover & () const

Returns the underlying set cover.

• const auto & set\_cover () const

Returns the underlying set cover.

• auto & set\_cover ()

Returns the underlying set cover.

 $\bullet \;\; template\!<\! typename\; F>$ 

```
std::vector< Set > get_cover (F &&heuristic)
```

Convenience function to run the given heuristic on this set cover.

# **Friends**

```
    template<typename T >
        std::ostream & operator<< (std::ostream &os, const TypedSetCover< T > &tsc)
        Print the typed set cover to os.
```

# 12.383.1 Detailed Description

```
template<typename Set> class carl::covering::TypedSetCover< Set >
```

Represents a set cover problem where a set is represented by some type.

It actually wraps a SetCover class and takes care of mapping the custom set type to an id type.

# 12.383.2 Member Function Documentation

Convenience function to run the given heuristic on this set cover.

```
12.383.2.3 operator const SetCover &() template<typename Set > carl::covering::TypedSetCover< Set >::operator const SetCover & ( ) const [inline], [explicit]
```

Returns the underlying set cover.

States that s covers the given elements.

States that s covers the given element.

```
12.383.2.6 set_cover() [1/2] template<typename Set >
auto& carl::covering::TypedSetCover< Set >::set_cover ( ) [inline]
```

Returns the underlying set cover.

```
12.383.2.7 set_cover() [2/2] template<typename Set >
const auto& carl::covering::TypedSetCover< Set >::set_cover ( ) const [inline]
```

Returns the underlying set cover.

# 12.383.3 Friends And Related Function Documentation

Print the typed set cover to os.

# 12.384 carl::UEquality Class Reference

Implements an uninterpreted equality, that is an equality of either two uninterpreted function instances, two uninterpreted variables, or an uninterpreted function instance and an uninterpreted variable.

```
#include <UEquality.h>
```

#### **Public Member Functions**

- UEquality ()=default
- UEquality (const UEquality &)=default
- UEquality (UEquality &&)=default
- UEquality & operator= (const UEquality &)=default
- UEquality & operator= (UEquality &&)=default
- UEquality (const UTerm &lhs, const UTerm &rhs, bool negated)

Constructs an uninterpreted equality.

UEquality (const UEquality &ueq, bool invert)

Copies the given uninterpreted equality.

- bool negated () const
- · const UTerm & Ihs () const
- · const UTerm & rhs () const
- std::size\_t complexity () const
- UEquality negation () const
- void gatherVariables (carlVariables &vars) const
- void gatherUFs (std::set< UninterpretedFunction > &ufs) const
- void gatherUVariables (std::set< UVariable > &uvars) const

# 12.384.1 Detailed Description

Implements an uninterpreted equality, that is an equality of either two uninterpreted function instances, two uninterpreted variables, or an uninterpreted function instance and an uninterpreted variable.

# 12.384.2 Constructor & Destructor Documentation

```
12.384.2.1 UEquality() [1/5] carl::UEquality::UEquality ( ) [default]
```

Constructs an uninterpreted equality.

#### **Parameters**

| negated | true, if the negation of this equality shall hold, which means that it is actually an inequality.   |
|---------|---|
| lhs     | An uninterpreted variable, which is going to be the left-hand side of this uninterpreted equality.  |
| rhs     | An uninterpreted variable, which is going to be the right-hand side of this uninterpreted equality. |

Copies the given uninterpreted equality.

## **Parameters**

| ueq    | The uninterpreted equality to copy.  |
|--------|--|
| invert | true, if the inverse of the given uninterpreted equality shall be constructed. (== -> != resp. != -> ==) |

# 12.384.3 Member Function Documentation

```
12.384.3.1 complexity() std::size_t carl::UEquality::complexity ( ) const [inline]
```

```
Returns
```

An approximation of the complexity of this uninterpreted equality.

```
12.384.3.2 gatherUFs() void carl::UEquality::gatherUFs (
             std::set< UninterpretedFunction > & ufs ) const [inline]
12.384.3.3 gatherUVariables() void carl::UEquality::gatherUVariables (
             std::set< UVariable > & uvars ) const
12.384.3.4 gatherVariables() void carl::UEquality::gatherVariables (
             carlVariables & vars ) const [inline]
12.384.3.5 lhs() const UTerm& carl::UEquality::lhs ( ) const [inline]
Returns
     The left-hand side of this equality.
12.384.3.6 negated() bool carl::UEquality::negated ( ) const [inline]
Returns
     true, if the negation of this equation shall hold, that is, it is actually an inequality.
12.384.3.7 negation() UEquality carl::UEquality::negation ( ) const [inline]
12.384.3.8 operator=() [1/2] UEquality& carl::UEquality::operator= (
             const UEquality & ) [default]
```

```
12.384.3.10 rhs() const UTerm& carl::UEquality::rhs ( ) const [inline]
```

Returns

The right-hand side of this equality.

# 12.385 carl::UFContent Class Reference

The actual content of an uninterpreted function instance.

```
#include <UFManager.h>
```

# **Public Member Functions**

- UFContent (std::string &&name, std::vector < Sort > &&domain, Sort codomain)
   Constructs the content of an uninterpreted function.
- UFContent ()=delete
- UFContent (const UFContent &)=delete
- UFContent (UFContent &&)=delete
- const std::string & name () const
- const std::vector< Sort > & domain () const
- Sort codomain () const

# **Friends**

class UFManager

# 12.385.1 Detailed Description

The actual content of an uninterpreted function instance.

# 12.385.2 Constructor & Destructor Documentation

Constructs the content of an uninterpreted function.

# **Parameters**

| name     | The name of the uninterpreted function to construct.     |
|----------|--|
| domain   | The domain of the uninterpreted function to construct.   |
| codomain | The codomain of the uninterpreted function to construct. |

```
12.385.2.2 UFContent() [2/4] carl::UFContent::UFContent ( ) [delete]
```

## 12.385.3 Member Function Documentation

```
12.385.3.1 codomain() Sort carl::UFContent::codomain ( ) const [inline]
```

# Returns

The codomain of the uninterpreted function.

```
12.385.3.2 domain() const std::vector<Sort>& carl::UFContent::domain ( ) const [inline]
```

# Returns

The domain of the uninterpreted function.

```
12.385.3.3 name() const std::string& carl::UFContent::name ( ) const [inline]
```

# Returns

The name of the uninterpreted function.

# 12.385.4 Friends And Related Function Documentation

12.385.4.1 UFManager friend class UFManager [friend]

# 12.386 carl::UFInstance Class Reference

Implements an uninterpreted function instance.

#include <UFInstance.h>

# **Public Member Functions**

- UFInstance ()=default
- std::size\_t id () const
- const UninterpretedFunction & uninterpretedFunction () const
- const std::vector< UTerm > & args () const
- std::size\_t complexity () const
- void gatherVariables (carlVariables &vars) const
- void gatherUFs (std::set< UninterpretedFunction > &ufs) const

# **Friends**

· class UFInstanceManager

# 12.386.1 Detailed Description

Implements an uninterpreted function instance.

# 12.386.2 Constructor & Destructor Documentation

12.386.2.1 UFInstance() carl::UFInstance::UFInstance () [default]

# 12.386.3 Member Function Documentation

```
12.386.3.1 args() const std::vector< UTerm > & carl::UFInstance::args () const
```

Returns

The arguments of this uninterpreted function instance.

```
12.386.3.2 complexity() std::size_t carl::UFInstance::complexity ( ) const
```

```
12.386.3.3 gatherUFs() void carl::UFInstance::gatherUFs ( std::set< UninterpretedFunction > & ufs ) const
```

```
12.386.3.4 gatherVariables() void carl::UFInstance::gatherVariables ( carlVariables & vars ) const
```

```
12.386.3.5 id() std::size_t carl::UFInstance::id ( ) const [inline]
```

Returns

The unique id of this uninterpreted function instance.

```
12.386.3.6 uninterpretedFunction() const UninterpretedFunction & carl::UFInstance::uninterpreted← Function ( ) const
```

Returns

The underlying uninterpreted function of this instance.

# 12.386.4 Friends And Related Function Documentation

12.386.4.1 UFInstanceManager friend class UFInstanceManager [friend]

# 12.387 carl::UFInstanceContent Class Reference

The actual content of an uninterpreted function instance.

```
#include <UFInstanceManager.h>
```

#### **Public Member Functions**

- UFInstanceContent ()=delete
- UFInstanceContent (const UFInstanceContent &)=delete
- UFInstanceContent (UFInstanceContent &&)=delete
- UFInstanceContent (const UninterpretedFunction &uf, std::vector< UTerm > &&args)

Constructs the content of an uninterpreted function instance.

• UFInstanceContent (const UninterpretedFunction &uf, const std::vector< UTerm > &args)

Constructs the content of an uninterpreted function instance.

- const UninterpretedFunction & uninterpretedFunction () const
- const std::vector< UTerm > & args () const
- bool operator== (const UFInstanceContent &ufic) const
- bool operator< (const UFInstanceContent &ufic) const

#### **Friends**

· class UFInstanceManager

# 12.387.1 Detailed Description

The actual content of an uninterpreted function instance.

## 12.387.2 Constructor & Destructor Documentation

```
12.387.2.1 UFInstanceContent() [1/5] carl::UFInstanceContent::UFInstanceContent ( ) [delete]

12.387.2.2 UFInstanceContent() [2/5] carl::UFInstanceContent::UFInstanceContent ( const UFInstanceContent & ) [delete]

12.387.2.3 UFInstanceContent() [3/5] carl::UFInstanceContent::UFInstanceContent ( UFInstanceContent & ) [delete]
12.387.2.4 UFInstanceContent() [4/5] carl::UFInstanceContent::UFInstanceContent (
```

Constructs the content of an uninterpreted function instance.

const UninterpretedFunction & uf,

std::vector< UTerm > && args ) [inline], [explicit]

#### **Parameters**

| uf   | The underlying function of the uninterpreted function instance to construct. |
|------|--|
| args | The arguments of the uninterpreted function instance to construct.           |

Constructs the content of an uninterpreted function instance.

#### **Parameters**

| uf   | The underlying function of the uninterpreted function instance to construct. |
|------|--|
| args | The arguments of the uninterpreted function instance to construct.           |

## 12.387.3 Member Function Documentation

```
12.387.3.1 args() const std::vector<UTerm>& carl::UFInstanceContent::args () const [inline]
```

# Returns

The arguments of the uninterpreted function instance.

# **Parameters**

*ufic* The uninterpreted function instance's content to compare with.

# Returns

true, if this uninterpreted function instance's content is less than the given one.

#### **Parameters**

*ufic* The uninterpreted function instance's content to compare with.

#### Returns

true, if this uninterpreted function instance's content is less than the given one.

#### Returns

The underlying function of the uninterpreted function instance

#### 12.387.4 Friends And Related Function Documentation

12.387.4.1 UFInstanceManager friend class UFInstanceManager [friend]

# 12.388 carl::UFInstanceManager Class Reference

Implements a manager for uninterpreted function instances, containing their actual contents and allocating their ids.

#include <UFInstanceManager.h>

# **Public Member Functions**

- const UninterpretedFunction & getUninterpretedFunction (const UFInstance &ufi) const
- const std::vector< UTerm > & getArgs (const UFInstance &ufi) const
- UFInstance newUFInstance (const UninterpretedFunction &uf, std::vector< UTerm > &&args)

Gets the uninterpreted function instance with the given name, domain, arguments and codomain.

• UFInstance newUFInstance (const UninterpretedFunction &uf, const std::vector< UTerm > &args)

Gets the uninterpreted function instance with the given name, domain, arguments and codomain.

# **Static Public Member Functions**

- static bool argsCorrect (const UFInstanceContent &ufic)
- static UFInstanceManager & getInstance ()

Returns the single instance of this class by reference.

# 12.388.1 Detailed Description

Implements a manager for uninterpreted function instances, containing their actual contents and allocating their ids.

# 12.388.2 Member Function Documentation

```
12.388.2.1 argsCorrect() bool carl::UFInstanceManager::argsCorrect ( const UFInstanceContent & ufic ) [static]
```

# Returns

true, if the arguments domains coincide with those of the domain.

#### **Parameters**

*ufi* An uninterpreted function instance.

# Returns

The arguments of the given uninterpreted function instance.

```
12.388.2.3 getInstance() static UFInstanceManager & carl::Singleton< UFInstanceManager >::get← Instance ( ) [inline], [static], [inherited]
```

Returns the single instance of this class by reference.

If there is no instance yet, a new one is created.

## **Parameters**

*ufi* An uninterpreted function instance.

#### Returns

The underlying uninterpreted function of the uninterpreted function of the given uninterpreted function instance.

Gets the uninterpreted function instance with the given name, domain, arguments and codomain.

## **Parameters**

| uf   | The underlying function of the uninterpreted function instance to get. |
|------|--|
| args | The arguments of the uninterpreted function instance to get.           |

#### Returns

The resulting uninterpreted function instance.

Gets the uninterpreted function instance with the given name, domain, arguments and codomain.

# **Parameters**

| uf   | The underlying function of the uninterpreted function instance to get. |
|------|--|
| args | The arguments of the uninterpreted function instance to get.           |

## Returns

The resulting uninterpreted function instance.

# 12.389 carl::UFManager Class Reference

Implements a manager for uninterpreted functions, containing their actual contents and allocating their ids.

```
#include <UFManager.h>
```

# **Public Member Functions**

- const auto & ufContents () const
- const auto & ufIDMap () const
- const std::string & get\_name (const UninterpretedFunction &uf) const
- const std::vector < Sort > & getDomain (const UninterpretedFunction &uf) const
- Sort getCodomain (const UninterpretedFunction &uf) const
- UninterpretedFunction newUninterpretedFunction (std::string &&name, std::vector < Sort > &&domain, Sort codomain)

Gets the uninterpreted function with the given name, domain, arguments and codomain.

#### **Static Public Member Functions**

• static UFManager & getInstance ()

Returns the single instance of this class by reference.

## 12.389.1 Detailed Description

Implements a manager for uninterpreted functions, containing their actual contents and allocating their ids.

#### 12.389.2 Member Function Documentation

```
12.389.2.1 get_name() const std::string& carl::UFManager::get_name ( const UninterpretedFunction & uf ) const [inline]
```

# **Parameters**

*uf* An uninterpreted function.

# Returns

The name of the uninterpreted function of the given uninterpreted function.

```
12.389.2.2 getCodomain() Sort carl::UFManager::getCodomain ( const UninterpretedFunction & uf ) const [inline]
```

## **Parameters**

*uf* An uninterpreted function.

#### Returns

The codomain of the uninterpreted function of the given uninterpreted function.

```
12.389.2.3 getDomain() const std::vector<Sort>& carl::UFManager::getDomain ( const UninterpretedFunction & uf ) const [inline]
```

#### **Parameters**

```
uf An uninterpreted function.
```

#### Returns

The domain of the uninterpreted function of the given uninterpreted function.

```
12.389.2.4 getInstance() static UFManager & carl::Singleton< UFManager >::getInstance () [inline], [static], [inherited]
```

Returns the single instance of this class by reference.

If there is no instance yet, a new one is created.

```
12.389.2.5 newUninterpretedFunction() UninterpretedFunction carl::UFManager::newUninterpreted←

Function (

std::string && name,

std::vector< Sort > && domain,

Sort codomain ) [inline]
```

Gets the uninterpreted function with the given name, domain, arguments and codomain.

# **Parameters**

| name     | The name of the uninterpreted function of the uninterpreted function to get.     |
|----------|--|
| domain   | The domain of the uninterpreted function of the uninterpreted function to get.   |
| codomain | The codomain of the uninterpreted function of the uninterpreted function to get. |

## Returns

The resulting uninterpreted function.

```
12.389.2.6 ufContents() const auto@ carl::UFManager::ufContents ( ) const [inline]
```

```
12.389.2.7 uflDMap() const auto& carl::UFManager::ufIDMap ( ) const [inline]
```

# 12.390 carl::UFModel Class Reference

Implements a sort value, being a value of the uninterpreted domain specified by this sort.

```
#include <UFModel.h>
```

#### **Public Member Functions**

- UFModel (const UninterpretedFunction &uf)
- bool extend (const std::vector < SortValue > &\_args, const SortValue &\_value)
- SortValue get (const std::vector< SortValue > &\_args) const
- const auto & function () const
- · const auto & values () const

# 12.390.1 Detailed Description

Implements a sort value, being a value of the uninterpreted domain specified by this sort.

#### 12.390.2 Constructor & Destructor Documentation

## 12.390.3 Member Function Documentation

12.390.3.2 function() const auto@ carl::UFModel::function ( ) const [inline]

```
12.390.3.4 values() const auto& carl::UFModel::values ( ) const [inline]
```

# 12.391 carl::UnderlyingNumberType< T > Struct Template Reference

Gives the underlying number type of a complex object.

```
#include <typetraits.h>
```

# **Public Types**

```
• using type = T
```

A type associated with the type.

# 12.391.1 Detailed Description

```
template<typename T> struct carl::UnderlyingNumberType< T>
```

Gives the underlying number type of a complex object.

Default is the type itself.

# 12.391.2 Member Typedef Documentation

```
12.391.2.1 type template<typename T >
using carl::has_subtype< T >::type = T [inherited]
```

A type associated with the type.

# 12.392 carl::UnderlyingNumberType< MultivariatePolynomial< C, O, P > Struct Template Reference

States that UnderlyingNumberType of MultivariatePolynomial < C,O,P > is UnderlyingNumberType < C >::type.

```
#include <MultivariatePolynomial.h>
```

# **Public Types**

using type = UnderlyingNumberType < C >::type
 A type associated with the type.

# 12.392.1 Detailed Description

 $\label{eq:continuous} \begin{tabular}{ll} template < typename C, typename O, typename P > \\ struct carl:: Underlying Number Type < Multivariate Polynomial < C, O, P > > \\ \end{tabular}$ 

States that UnderlyingNumberType of MultivariatePolynomial < C,O,P > is UnderlyingNumberType < C >::type.

# 12.392.2 Member Typedef Documentation

12.392.2.1 type using carl::has\_subtype< UnderlyingNumberType< C >::type >::type = UnderlyingNumberType<
C >::type [inherited]

A type associated with the type.

# 12.393 carl::UnderlyingNumberType< UnivariatePolynomial< C >> Struct Template Reference

States that UnderlyingNumberType of UnivariatePolynomial<T> is UnderlyingNumberType<C>::type.

#include <UnivariatePolynomial.h>

# **Public Types**

using type = UnderlyingNumberType < C >::type
 A type associated with the type.

# 12.393.1 Detailed Description

 $\label{lem:continuous} \mbox{template} < \mbox{typename C} > \\ \mbox{struct carl::UnderlyingNumberType} < \mbox{UnivariatePolynomial} < \mbox{C} > > \\ \mbox{}$ 

 $States\ that\ Underlying Number Type\ of\ Univariate Polynomial < T> is\ Underlying Number Type\ < C>::type.$ 

# 12.393.2 Member Typedef Documentation

12.393.2.1 type using carl::has\_subtype< UnderlyingNumberType< C >::type >::type = UnderlyingNumberType< C >::type [inherited]

A type associated with the type.

# 12.394 carl::UninterpretedFunction Class Reference

Implements an uninterpreted function.

```
#include <UninterpretedFunction.h>
```

#### **Public Member Functions**

• UninterpretedFunction () noexcept=default

Default constructor.

- std::size\_t id () const
- const std::string & name () const
- const std::vector < Sort > & domain () const
- Sort codomain () const

# **Friends**

· class UFManager

# 12.394.1 Detailed Description

Implements an uninterpreted function.

# 12.394.2 Constructor & Destructor Documentation

```
12.394.2.1 UninterpretedFunction() carl::UninterpretedFunction::UninterpretedFunction () [default], [noexcept]
```

Default constructor.

# 12.394.3 Member Function Documentation

```
\textbf{12.394.3.1} \quad \textbf{codomain()} \quad \texttt{Sort carl::UninterpretedFunction::codomain ( ) const}
```

# Returns

The codomain of this uninterpreted function.

12.394.3.2 domain() const std::vector< Sort > & carl::UninterpretedFunction::domain ( ) const

# Returns

The domain of this uninterpreted function.

12.394.3.3 id() std::size\_t carl::UninterpretedFunction::id ( ) const [inline]

# Returns

The unique id of this uninterpreted function instance.

12.394.3.4 name() const std::string & carl::UninterpretedFunction::name ( ) const

# Returns

The name of this uninterpreted function.

# 12.394.4 Friends And Related Function Documentation

12.394.4.1 UFManager friend class UFManager [friend]

# 12.395 carl::helper::UninterpretedSubstitutor< Pol > Struct Template Reference

#include <Substitution.h>

# **Public Member Functions**

- UninterpretedSubstitutor (const std::map< UVariable, UFInstance > &repl)
- Formula < Pol > operator() (const Formula < Pol > &formula)

# **Data Fields**

• const std::map< UVariable, UFInstance > & replacements

# 12.395.1 Constructor & Destructor Documentation

#### 12.395.2 Member Function Documentation

# 12.395.3 Field Documentation

```
12.395.3.1 replacements template<typename Pol > const std::map<UVariable,UFInstance>& carl::helper::UninterpretedSubstitutor< Pol >::replacements
```

# 12.396 carl::UnivariatePolynomial < Coefficient > Class Template Reference

This class represents a univariate polynomial with coefficients of an arbitrary type.

```
#include <UnivariatePolynomial.h>
```

# **Public Types**

- using NumberType = typename UnderlyingNumberType < Coefficient >::type
- The number type that is ultimately used for the coefficients.

   using IntNumberType = typename IntegralType < NumberType >::type

The integral type that belongs to the number type.

- using CACHE = void
- using CoeffType = Coefficient
- using PolyType = UnivariatePolynomial < Coefficient >
- using RootType = IntRepRealAlgebraicNumber < NumberType >

# **Public Member Functions**

UnivariatePolynomial ()=delete

Default constructor shall not exist.

UnivariatePolynomial (const UnivariatePolynomial &p)

Copy constructor.

• UnivariatePolynomial (UnivariatePolynomial &&p) noexcept

Move constructor.

UnivariatePolynomial & operator= (const UnivariatePolynomial &p)

Copy assignment operator.

• UnivariatePolynomial & operator= (UnivariatePolynomial &&p) noexcept

Move assignment operator.

UnivariatePolynomial (Variable mainVar)

Construct a zero polynomial with the given main variable.

• UnivariatePolynomial (Variable mainVar, const Coefficient &coeff, std::size\_t degree=0)

Construct  $coeff \cdot mainVar^{degree}$ .

• UnivariatePolynomial (Variable mainVar, std::initializer\_list< Coefficient > coefficients)

Construct polynomial with the given coefficients.

template<typename C = Coefficient, DisableIf< std::is\_same< C, typename UnderlyingNumberType< C >::type >> = dummy>
 UnivariatePolynomial (Variable mainVar, std::initializer\_list< typename UnderlyingNumberType< C >::type > coefficients)

Construct polynomial with the given coefficients from the underlying number type of the coefficient type.

• UnivariatePolynomial (Variable mainVar, const std::vector< Coefficient > &coefficients)

Construct polynomial with the given coefficients.

UnivariatePolynomial (Variable mainVar, std::vector < Coefficient > &&coefficients)

Construct polynomial with the given coefficients, moving the coefficients.

UnivariatePolynomial (Variable mainVar, const std::map< uint, Coefficient > &coefficients)

Construct polynomial with the given coefficients.

∼UnivariatePolynomial ()=default

Destructor.

• bool is\_zero () const

Checks if the polynomial is equal to zero.

bool is\_one () const

Checks if the polynomial is equal to one.

· UnivariatePolynomial one () const

Creates a polynomial of value one with the same main variable.

• const Coefficient & Icoeff () const

Returns the leading coefficient.

· const Coefficient & tcoeff () const

Returns the trailing coefficient.

• bool is\_constant () const

Checks whether the polynomial is constant with respect to the main variable.

- bool is\_linear\_in\_main\_var () const
- bool is\_number () const

Checks whether the polynomial is only a number.

NumberType constant\_part () const

Returns the constant part of this polynomial.

bool is\_univariate () const

Checks if the polynomial is univariate, that means if only one variable occurs.

• uint degree () const

Get the maximal exponent of the main variable.

uint total\_degree () const

Returns the total degree of the polynomial, that is the maximum degree of any monomial.

· void truncate ()

Removes the leading term from the polynomial.

const std::vector< Coefficient > & coefficients () const &

Retrieves the coefficients defining this polynomial.

std::vector < Coefficient > & coefficients () &

Returns the coefficients as non-const reference.

std::vector< Coefficient > && coefficients () &&

Returns the coefficients as rvalue. The polynomial may be in an undefined state afterwards!

Variable main\_var () const

Retrieves the main variable of this polynomial.

· bool has (Variable v) const

Checks if the given variable occurs in the polynomial.

• template<typename C = Coefficient, EnableIf< is\_subset\_of\_rationals\_type< C >> = dummy> Coefficient coprime\_factor () const

Calculates a factor that would make the coefficients of this polynomial coprime integers.

- template<typename C = Coefficient, DisableIf< is\_subset\_of\_rationals\_type< C >> = dummy> template<typename C = Coefficient, EnableIf< is\_subset\_of\_rationals\_type< C >> = dummy>
  - UnderlyingNumberType< Coefficient >::type coprime\_factor () const

UnivariatePolynomial < typename IntegralType < Coefficient >::type > coprime\_coefficients () const

Constructs a new polynomial that is scaled such that the coefficients are coprime.

- template<typename C = Coefficient, DisableIf< is\_subset\_of\_rationals\_type< C >> = dummy>
  - UnivariatePolynomial < Coefficient > coprime\_coefficients () const

• template<typename C = Coefficient, EnableIf< is\_subset\_of\_rationals\_type< C >> = dummy> UnivariatePolynomial < typename IntegralType < Coefficient >::type > coprime\_coefficients\_sign\_preserving () const

• template<typename C = Coefficient, DisableIf< is\_subset\_of\_rationals\_type< C >> = dummy> UnivariatePolynomial < Coefficient > coprime\_coefficients\_sign\_preserving () const

bool is\_normal () const

Checks whether the polynomial is unit normal.

UnivariatePolynomial normalized () const

The normal part of a polynomial is the polynomial divided by the unit part.

Coefficient unit\_part () const

The unit part of a polynomial over a field is its leading coefficient for nonzero polynomials, and one for zero polynomi-

UnivariatePolynomial negate\_variable () const

Constructs a new polynomial q such that q(x) = p(-x) where p is this polynomial.

• UnivariatePolynomial reverse\_coefficients () const

Reverse coefficients safely.

· bool divides (const UnivariatePolynomial &divisor) const

Checks if this polynomial is divisible by the given divisor, that is if the remainder is zero.

UnivariatePolynomial & mod (const Coefficient &modulus)

Replaces every coefficient c by c mod modulus.

UnivariatePolynomial mod (const Coefficient &modulus) const

Constructs a new polynomial where every coefficient c is replaced by c mod modulus.

UnivariatePolynomial pow (std::size\_t exp) const

Returns this polynomial to the given power.

- · Coefficient evaluate (const Coefficient &value) const
- · carl::Sign sgn (const Coefficient &value) const

Calculates the sign of the polynomial at some point.

```
    template<typename SubstitutionType , typename C = Coefficient, EnableIf< is_instantiation_of< MultivariatePolynomial, C >> = dummv>
```

UnivariatePolynomial < Coefficient > evaluateCoefficient (const std::map < Variable, SubstitutionType > &) const

template<typename SubstitutionType , typename C = Coefficient, DisableIf< is\_instantiation\_of< MultivariatePolynomial, C >> = dummy>

UnivariatePolynomial < Coefficient > evaluateCoefficient (const std::map < Variable, SubstitutionType > &) const

template<typename T = Coefficient, EnableIf< has\_normalize< T >> = dummy>
 UnivariatePolynomial & normalizeCoefficients ()

template<typename T = Coefficient, DisableIf< has\_normalize< T >> = dummy>
 UnivariatePolynomial & normalizeCoefficients ()

• template<typename C = Coefficient, EnableIf< is\_instantiation\_of< GFNumber, C >> = dummy> UnivariatePolynomial< typename IntegralType< Coefficient >::type > to\_integer\_domain () const

Works only from rationals, if the numbers are already integers.

- template<typename C = Coefficient, DisableIf< is\_instantiation\_of< GFNumber, C >> = dummy> UnivariatePolynomial< typename IntegralType< Coefficient >::type > to\_integer\_domain () const
- UnivariatePolynomial < GFNumber < typename IntegralType < Coefficient >::type > > toFiniteDomain (const GaloisField < typename IntegralType < Coefficient >::type > \*galoisField) const
- template<typename C = Coefficient, DisableIf< is\_number\_type< C >> = dummy>
   UnivariatePolynomial
   NumberType > toNumberCoefficients () const

Asserts that is\_univariate() is true.

• template<typename NewCoeff >

UnivariatePolynomial < NewCoeff > convert () const

template<typename NewCoeff >

UnivariatePolynomial < NewCoeff > convert (const std::function < NewCoeff(const Coefficient &) > &f) const

• NumberType numeric\_content (std::size\_t i) const

Returns the numeric content part of the i'th coefficient.

NumberType numeric\_unit () const

Returns the numeric unit part of the polynomial.

template < typename N = NumberType, EnableIf < is\_subset\_of\_rationals\_type < N >> = dummy > UnderlyingNumberType < Coefficient >::type numeric\_content () const

Obtains the numeric content part of this polynomial.

template<typename C = Coefficient, EnableIf< is\_number\_type< C >> = dummy>
 IntNumberType main\_denom () const

Compute the main denominator of all numeric coefficients of this polynomial.

- template<typename C = Coefficient, DisableIf< is\_number\_type< C >> = dummy> IntNumberType main\_denom () const
- Coefficient synthetic\_division (const Coefficient &zeroOfDivisor)
- bool zero\_is\_root () const

Checks if zero is a real root of this polynomial.

- bool less (const UnivariatePolynomial< Coefficient > &rhs, const PolynomialComparisonOrder &order=PolynomialComparisonOrder::Default) const
- · UnivariatePolynomial operator- () const
- template < typename C = Coefficient, EnableIf < is\_number\_type < C >> = dummy > bool is\_consistent () const

Asserts that this polynomial over numeric coefficients complies with the requirements and assumptions for UnivariatePolynomial objects.

 template<typename C = Coefficient, DisableIf< is\_number\_type< C >> = dummy> bool is\_consistent () const

Asserts that this polynomial over polynomial coefficients complies with the requirements and assumptions for UnivariatePolynomial objects.

- void strip\_leading\_zeroes ()
- template<typename Coeff >

UnivariatePolynomial (Variable mainVar, const Coeff &coeff, std::size\_t degree)

```
    template<typename Coeff >

  UnivariatePolynomial (Variable mainVar, std::initializer_list< Coeff > coefficients)
template<typename Coeff >
  UnivariatePolynomial (Variable mainVar, const std::vector < Coeff > &coefficients)

    template<typename Coeff >

  UnivariatePolynomial (Variable mainVar, std::vector < Coeff > &coefficients)
template<typename Coeff >
  UnivariatePolynomial (Variable mainVar, const std::map < uint, Coeff > &coefficients)

    template<typename C , DisableIf< is_number_type< C >> >

  \label{lem:univariatePolynomial} UnivariatePolynomial < Coeff > :: NumberType > toNumberCoefficients \ ()
  const

    template<typename NewCoeff >

  UnivariatePolynomial < NewCoeff > convert (const std::function < NewCoeff (const Coeff &) > &f) const

    template<typename C , EnableIf< is_subset_of_rationals_type< C >> >

  Coeff coprime_factor () const

    template<typename C , EnableIf< is_subset_of_rationals_type< C >> >

  UnivariatePolynomial < typename IntegralType < Coeff >::type > coprime_coefficients () const

    template<typename C , DisableIf< is_subset_of_rationals_type< C >> >

  UnivariatePolynomial < Coeff > coprime_coefficients () const
- template<typename C , EnableIf< is_subset_of_rationals_type< C >> >
  UnivariatePolynomial < typename IntegralType < Coeff >::type > coprime_coefficients_sign_preserving ()

    template<typename C , DisableIf< is_subset_of_rationals_type< C >> >

  UnivariatePolynomial < Coeff > coprime_coefficients_sign_preserving () const
• template<typename C , EnableIf< is_instantiation_of< GFNumber, C >> >
  UnivariatePolynomial < typename IntegralType < Coeff >::type > to_integer_domain () const

    template<typename N , EnableIf< is_subset_of_rationals_type< N >> >

  UnivariatePolynomial < Coeff >::NumberType numeric_content () const

    template<typename C , EnableIf< is_number_type< C >> >

  UnivariatePolynomial < Coefficient > & operator*= (Variable rhs)

    template<typename I , DisableIf< std::is_same< Coeff, I >> ...>

  UnivariatePolynomial < Coeff > & operator*= (const typename IntegralType < Coeff >::type &rhs)

    template<typename C , EnableIf< is_field_type< C >> >

  UnivariatePolynomial < Coeff > & operator/= (const Coeff &rhs)
```

# In-place addition operators

- UnivariatePolynomial & operator+= (const Coefficient &rhs)
  - Add something to this polynomial and return the changed polynomial.
- UnivariatePolynomial & operator+= (const UnivariatePolynomial &rhs)

Add something to this polynomial and return the changed polynomial.

## In-place subtraction operators

- UnivariatePolynomial & operator-= (const Coefficient &rhs)
  - Subtract something from this polynomial and return the changed polynomial.
- UnivariatePolynomial & operator-= (const UnivariatePolynomial &rhs)

Subtract something from this polynomial and return the changed polynomial.

# In-place multiplication operators

- template<typename C = Coefficient, EnableIf< is\_number\_type< C >> = dummy>
   UnivariatePolynomial & operator\*= (Variable rhs)
  - Multiply this polynomial with something and return the changed polynomial.
- template<typename C = Coefficient, Disablelf< is\_number\_type< C >> = dummy>
   UnivariatePolynomial & operator\*= (Variable rhs)

Multiply this polynomial with something and return the changed polynomial.

UnivariatePolynomial & operator\*= (const Coefficient &rhs)

Multiply this polynomial with something and return the changed polynomial.

• template<typename I = Coefficient, DisableIf< std::is\_same< Coefficient, I >> ...>

UnivariatePolynomial & operator\*= (const typename IntegralType< Coefficient >::type &rhs)

Multiply this polynomial with something and return the changed polynomial.

UnivariatePolynomial & operator\*= (const UnivariatePolynomial &rhs)

Multiply this polynomial with something and return the changed polynomial.

# In-place division operators

template < typename C = Coefficient, EnableIf < is\_field\_type < C >> = dummy>
 UnivariatePolynomial & operator/= (const Coefficient &rhs)

Divide this polynomial by something and return the changed polynomial.

template < typename C = Coefficient, DisableIf < is\_field\_type < C >> = dummy > UnivariatePolynomial & operator/= (const Coefficient &rhs)

Divide this polynomial by something and return the changed polynomial.

#### **Friends**

template < class T >
 class UnivariatePolynomial

Declare all instantiations of univariate polynomials as friends.

template<typename C >

bool operator < (const UnivariatePolynomial < C > &lhs, const UnivariatePolynomial < C > &rhs)

 $\bullet \ \ template {<} typename \ C >$ 

std::ostream & operator<< (std::ostream &os, const UnivariatePolynomial< C > &rhs)

Streaming operator for univariate polynomials.

# **Equality comparison operators**

• template<typename C >

bool operator== (const C &lhs, const UnivariatePolynomial < C > &rhs)

Checks if the two arguments are equal.

template<typename C >

bool operator== (const UnivariatePolynomial < C > &lhs, const C &rhs)

Checks if the two arguments are equal.

template<typename C >

 $bool\ operator == (const\ Univariate Polynomial < C > \&lhs,\ const\ Univariate Polynomial < C > \&rhs)$ 

Checks if the two arguments are equal.

template<typename C >

bool operator== (const UnivariatePolynomialPtr< C > &lhs, const UnivariatePolynomialPtr< C > &rhs) Checks if the two arguments are equal.

## Inequality comparison operators

template<typename C >

bool operator!= (const UnivariatePolynomial < C > &lhs, const UnivariatePolynomial < C > &rhs)

Checks if the two arguments are not equal.

template<typename C >

bool operator!= (const UnivariatePolynomialPtr< C > &lhs, const UnivariatePolynomialPtr< C > &rhs)

Checks if the two arguments are not equal.

# **Addition operators**

• template<typename C >

 $\label{eq:const_univariate} \begin{tabular}{ll} Univariate Polynomial < C > \&lhs, const Univariate Polynomial < C > \&lhs, co$ 

Performs an addition involving a polynomial.

• template<typename C >

UnivariatePolynomial < C > operator+ (const C &lhs, const UnivariatePolynomial < C > &rhs)

Performs an addition involving a polynomial.

template<typename C >

UnivariatePolynomial < C > operator+ (const UnivariatePolynomial < C > &lhs, const C &rhs)

Performs an addition involving a polynomial.

# Subtraction operators

• template<typename C >

UnivariatePolynomial < C > operator- (const UnivariatePolynomial < C > &lhs, const UnivariatePolynomial < C > &rhs)

Performs a subtraction involving a polynomial.

template<typename C >

UnivariatePolynomial < C > operator- (const C &lhs, const UnivariatePolynomial < C > &rhs)

Performs a subtraction involving a polynomial.

template<typename C >

UnivariatePolynomial < C > operator- (const UnivariatePolynomial < C > &lhs, const C &rhs)

Performs a subtraction involving a polynomial.

# **Multiplication operators**

template<typename C >

 $\label{eq:const_univariate} \mbox{UnivariatePolynomial} < \mbox{C} > \mbox{\&lhs, const UnivariatePolynomial} < \mbox{C} > \mbox{\&lhs, const UnivariatePolynomial} < \mbox{C} > \mbox{\&rhs})$ 

Perform a multiplication involving a polynomial.

template<typename C >

UnivariatePolynomial < C > operator\* (const UnivariatePolynomial < C > &lhs, Variable rhs)

Perform a multiplication involving a polynomial.

template<typename C >

 $\label{eq:const} \mbox{UnivariatePolynomial} < \mbox{C} > \mbox{operator} * \mbox{(Variable lhs, const UnivariatePolynomial} < \mbox{C} > \mbox{\&rhs)}$ 

Perform a multiplication involving a polynomial.

template<typename C >

UnivariatePolynomial < C > operator\* (const C &lhs, const UnivariatePolynomial < C > &rhs)

Perform a multiplication involving a polynomial.

 $\bullet \ \ \text{template}{<} \text{typename C} >$ 

 $\label{eq:const} \mbox{UnivariatePolynomial} < \mbox{C} > \mbox{operator} * (\mbox{const UnivariatePolynomial} < \mbox{C} > \& \mbox{lhs}, \mbox{const C \& rhs})$ 

Perform a multiplication involving a polynomial.

• template<typename C >

UnivariatePolynomial < C > operator\* (const IntegralTypeIfDifferent < C > &lhs, const UnivariatePolynomial < C > &rhs)

Perform a multiplication involving a polynomial.

template<typename C >

 $\label{eq:const} \begin{tabular}{ll} Univariate Polynomial < C > \&lhs, const Integral Type If Different < C > \&rhs) \end{tabular}$ 

Perform a multiplication involving a polynomial.

- template<typename C , typename O , typename P >

UnivariatePolynomial < C, O, P > operator\* (const UnivariatePolynomial < MultivariatePolynomial < C, O, P >> &lhs, const C &rhs)

Perform a multiplication involving a polynomial.

• template<typename C , typename O , typename P >

Perform a multiplication involving a polynomial.

# **Division operators**

template<typename C >
 UnivariatePolynomial < C > operator/ (const UnivariatePolynomial < C > &lhs, const C &rhs)
 Perform a division involving a polynomial.

# 12.396.1 Detailed Description

```
template<typename Coefficient> class carl::UnivariatePolynomial< Coefficient >
```

This class represents a univariate polynomial with coefficients of an arbitrary type.

A univariate polynomial is defined by a variable (the *main variable*) and the coefficients. The coefficients may be of any type. The intention is to use a numbers or polynomials as coefficients. If polynomials are used as coefficients, this can be seen as a multivariate polynomial with a distinguished main variable.

Most methods are specifically adapted for polynomial coefficients, if necessary.

# 12.396.2 Member Typedef Documentation

```
12.396.2.1 CACHE template<typename Coefficient >
    using carl::UnivariatePolynomial < Coefficient >::CACHE = void

12.396.2.2 CoeffType template < typename Coefficient >
    using carl::UnivariatePolynomial < Coefficient >::CoeffType = Coefficient

12.396.2.3 IntNumberType template < typename Coefficient >
    using carl::UnivariatePolynomial < Coefficient >::IntNumberType = typename IntegralType < NumberType > ↔
```

The integral type that belongs to the number type.

::type

```
12.396.2.4 NumberType template<typename Coefficient >
using carl::UnivariatePolynomial < Coefficient >::NumberType = typename UnderlyingNumberType <Coefficient >
::type
```

The number type that is ultimately used for the coefficients.

```
12.396.2.5 PolyType template<typename Coefficient > using carl::UnivariatePolynomial<Coefficient >::PolyType = UnivariatePolynomial<Coefficient>
```

```
12.396.2.6 RootType template<typename Coefficient > using carl::UnivariatePolynomial< Coefficient >::RootType = IntRepRealAlgebraicNumber<NumberType>
```

# 12.396.3 Constructor & Destructor Documentation

```
12.396.3.1 UnivariatePolynomial() [1/15] template<typename Coefficient > carl::UnivariatePolynomial < Coefficient >::UnivariatePolynomial ( ) [delete]
```

Default constructor shall not exist.

Use UnivariatePolynomial(Variable) instead.

```
12.396.3.2 UnivariatePolynomial() [2/15] template<typename Coeff > carl::UnivariatePolynomial < Coeff >::UnivariatePolynomial ( const UnivariatePolynomial < Coefficient > & p )
```

Copy constructor.

Move constructor.

Construct a zero polynomial with the given main variable.

# **Parameters**

| mainVar | New main variable. |
|---------|--------------------|

Construct  $coeff \cdot mainVar^{degree}$ .

#### **Parameters**

| mainVar | New main variable.   |
|---------|----------------------|
| coeff   | Leading coefficient. |
| degree  | Degree.              |

Construct polynomial with the given coefficients.

#### **Parameters**

| mainVar      | New main variable.    |
|--------------|-----------------------|
| coefficients | List of coefficients. |

Construct polynomial with the given coefficients from the underlying number type of the coefficient type.

### **Parameters**

| mainVar      | New main variable.    |
|--------------|-----------------------|
| coefficients | List of coefficients. |

Construct polynomial with the given coefficients.

| mainVar      | New main variable.      |
|--------------|-------------------------|
| coefficients | Vector of coefficients. |

Construct polynomial with the given coefficients, moving the coefficients.

## **Parameters**

| mainVar      | New main variable.      |
|--------------|-------------------------|
| coefficients | Vector of coefficients. |

Construct polynomial with the given coefficients.

### **Parameters**

| mainVar      | New main variable.                    |
|--------------|---------------------------------------|
| coefficients | Assignment of degree to coefficients. |

```
12.396.3.11 ~UnivariatePolynomial() template<typename Coefficient > carl::UnivariatePolynomial < Coefficient >::~UnivariatePolynomial ( ) [default]
```

Destructor.

```
12.396.3.13 UnivariatePolynomial() [12/15] template<typename Coefficient >
template<typename Coeff >
Variable mainVar,
                                  std::initializer_list< Coeff > coefficients )
12.396.3.14 UnivariatePolynomial() [13/15] template<typename Coefficient >
template<typename Coeff >
carl::UnivariatePolynomial < Coefficient >::UnivariatePolynomial (
                                  Variable mainVar,
                                  const std::vector< Coeff > & coefficients )
12.396.3.15 UnivariatePolynomial() [14/15] template<typename Coefficient >
template<typename Coeff >
carl::UnivariatePolynomial < Coefficient >::UnivariatePolynomial (
                                 Variable mainVar,
                                  std::vector< Coeff > && coefficients )
12.396.3.16 UnivariatePolynomial() [15/15] template<typename Coefficient >
template<typename Coeff >
carl::UnivariatePolynomial < Coefficient >::UnivariatePolynomial (
                                  Variable mainVar,
                                  const std::map< uint, Coeff > & coefficients )
12.396.4 Member Function Documentation
12.396.4.1 coefficients() [1/3] template<typename Coefficient >
std::vector<Coefficient>& carl::UnivariatePolynomial< Coefficient >::coefficients ( ) & [inline]
Returns the coefficients as non-const reference.
12.396.4.2 coefficients() [2/3] template<typename Coefficient >
\verb|std::vector<Coefficient>\&\& carl::UnivariatePolynomial<|Coefficient>::coefficients||()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&|()| &\&
[inline]
```

Returns the coefficients as rvalue. The polynomial may be in an undefined state afterwards!

```
12.396.4.3 coefficients() [3/3] template<typename Coefficient >
const std::vector<Coefficient>& carl::UnivariatePolynomial< Coefficient >::coefficients ( )
const & [inline]
```

Retrieves the coefficients defining this polynomial.

#### Returns

Coefficients.

```
12.396.4.4 constant_part() template<typename Coefficient >
NumberType carl::UnivariatePolynomial< Coefficient >::constant_part ( ) const [inline]
```

Returns the constant part of this polynomial.

#### Returns

Constant part.

Constructs a new polynomial that is scaled such that the coefficients are coprime.

It is calculated by multiplying it with the coprime factor. By definition, this results in a polynomial with integral coefficients.

### Returns

This polynomial multiplied with the coprime factor.

```
12.396.4.9 coprime_coefficients() [2/4] template<typename Coefficient >
template<typename C = Coefficient, DisableIf< is_subset_of_rationals_type< C >> = dummy>
UnivariatePolynomial < Coefficient > carl::UnivariatePolynomial < Coefficient >::coprime_coefficients
 ( ) const
12.396.4.10 coprime_coefficients() [3/4] template<typename Coefficient >
 \label{template} $$ \  \  \, $$ template < typename C , EnableIf < is_subset_of_rationals_type < C >> > $$
UnivariatePolynomial<typename IntegralType<Coeff>::type> carl::UnivariatePolynomial< Coefficient
>::coprime_coefficients ( ) const
12.396.4.11 coprime_coefficients() [4/4] template<typename Coefficient >
template<typename C , DisableIf< is_subset_of_rationals_type< C >> >
UnivariatePolynomial < Coeff> carl::UnivariatePolynomial < Coefficient >::coprime_coefficients (
 ) const
 12.396.4.12 coprime_coefficients_sign_preserving() [1/4] template<typename Coefficient >
template<typename C = Coefficient, EnableIf< is_subset_of_rationals_type< C >> = dummy>
UnivariatePolynomial<typename IntegralType<Coefficient>::type> carl::UnivariatePolynomial<
Coefficient >::coprime_coefficients_sign_preserving ( ) const
12.396.4.13 coprime_coefficients_sign_preserving() [2/4] template<typename Coefficient >
UnivariatePolynomial < Coefficient > carl::UnivariatePolynomial < Coefficient >::coprime_coefficients ←
_sign_preserving ( ) const
\textbf{12.396.4.14} \quad \textbf{coprime\_coefficients\_sign\_preserving() [3/4]} \quad \texttt{template} < \texttt{typename Coefficient} > \texttt{typename Co
 template<typename C , EnableIf< is_subset_of_rationals_type< C >> >
UnivariatePolynomial < typename Integral Type < Coeff >:: type > carl:: UnivariatePolynomial < Coefficient
>::coprime_coefficients_sign_preserving ( ) const
 12.396.4.15 coprime_coefficients_sign_preserving() [4/4] template<typename Coefficient >
 template<typename C , DisableIf< is_subset_of_rationals_type< C >> >
\label{linear_coeff} \begin{tabular}{ll} Univariate Polynomial < Coefficient >:: coprime\_coefficients\_ \leftrightarrow Invariate Polynomial < Coefficients\_ 
sign_preserving ( ) const
```

```
12.396.4.16 coprime_factor() [1/3] template<typename Coefficient > template<typename C = Coefficient, EnableIf< is_subset_of_rationals_type< C >> = dummy> Coefficient carl::UnivariatePolynomial< Coefficient >::coprime_factor ( ) const
```

Calculates a factor that would make the coefficients of this polynomial coprime integers.

We consider a set of integers coprime, if they share no common factor. Technically, the coprime factor is lcm(N)/gcd(D) where N is the set of the numerators and D is the set of the denominators of all coefficients.

## Returns

Coprime factor of this polynomial.

```
12.396.4.17 coprime_factor() [2/3] template<typename Coeff > template<typename C , DisableIf< is_subset_of_rationals_type< C >> > UnderlyingNumberType< Coeff >::type carl::UnivariatePolynomial< Coeff >::coprime_factor
```

```
12.396.4.18 coprime_factor() [3/3] template<typename Coefficient > template<typename C , EnableIf< is_subset_of_rationals_type< C >> > Coeff carl::UnivariatePolynomial< Coefficient >::coprime_factor ( ) const
```

```
12.396.4.19 degree() template<typename Coefficient > uint carl::UnivariatePolynomial< Coefficient >::degree ( ) const [inline]
```

Get the maximal exponent of the main variable.

As the degree of the zero polynomial is  $-\infty$ , we assert that this polynomial is not zero. This must be checked by the caller before calling this method.

See also

?, page 38

Returns

Degree.

Checks if this polynomial is divisible by the given divisor, that is if the remainder is zero.

| divisor | Polynomial. |
|---------|-------------|
|---------|-------------|

#### Returns

If divisor divides this polynomial.

Todo Is this correct?

```
12.396.4.24 has() template<typename Coefficient > bool carl::UnivariatePolynomial< Coefficient >::has ( Variable v ) const [inline]
```

Checks if the given variable occurs in the polynomial.

```
v Variable.
```

If v occurs in the polynomial.

```
12.396.4.25 is_consistent() [1/2] template<typename Coefficient >
template<typename C , DisableIf< is_number_type< C >> >
bool carl::UnivariatePolynomial< Coefficient >::is_consistent
```

Asserts that this polynomial over numeric coefficients complies with the requirements and assumptions for UnivariatePolynomial objects.

· The leading term is not zero.

```
12.396.4.26 is_consistent() [2/2] template<typename Coefficient > template<typename C = Coefficient, DisableIf< is_number_type< C >> = dummy> bool carl::UnivariatePolynomial< Coefficient >::is_consistent () const
```

Asserts that this polynomial over polynomial coefficients complies with the requirements and assumptions for UnivariatePolynomial objects.

- · The leading term is not zero.
- The main variable does not occur in any coefficient.

```
12.396.4.27 is_constant() template<typename Coefficient > bool carl::UnivariatePolynomial< Coefficient >::is_constant ( ) const [inline]
```

Checks whether the polynomial is constant with respect to the main variable.

## Returns

If polynomial is constant.

```
12.396.4.28 is_linear_in_main_var() template<typename Coefficient >
bool carl::UnivariatePolynomial< Coefficient >::is_linear_in_main_var ( ) const [inline]
```

```
12.396.4.29 is_normal() template<typename Coeff > bool carl::UnivariatePolynomial< Coeff >::is_normal
```

Checks whether the polynomial is unit normal.

A polynomial is unit normal, if the leading coefficient is unit normal, that is if it is either one or minus one.

See also

```
?, page 39
```

Returns

If polynomial is normal.

```
12.396.4.30 is_number() template<typename Coefficient > bool carl::UnivariatePolynomial< Coefficient >::is_number ( ) const [inline]
```

Checks whether the polynomial is only a number.

Returns

If polynomial is a number.

```
12.396.4.31 is_one() template<typename Coefficient >
bool carl::UnivariatePolynomial< Coefficient >::is_one () const [inline]
```

Checks if the polynomial is equal to one.

Returns

If polynomial is one.

```
12.396.4.32 is_univariate() template<typename Coefficient >
bool carl::UnivariatePolynomial< Coefficient >::is_univariate ( ) const [inline]
```

Checks if the polynomial is univariate, that means if only one variable occurs.

Returns

true.

```
12.396.4.33 is.zero() template<typename Coefficient > bool carl::UnivariatePolynomial< Coefficient >::is.zero () const [inline]
```

Checks if the polynomial is equal to zero.

#### Returns

If polynomial is zero.

```
12.396.4.34 | lcoeff() template<typename Coefficient > const Coefficient& carl::UnivariatePolynomial< Coefficient >::lcoeff ( ) const [inline]
```

Returns the leading coefficient.

Asserts, that the polynomial is not empty.

#### Returns

The leading coefficient.

```
12.396.4.36 main_denom() [1/2] template<typename Coeff >
template<typename C , DisableIf< is_number_type< C >> >
UnivariatePolynomial< Coeff >::IntNumberType carl::UnivariatePolynomial< Coeff >::main_denom
```

Compute the main denominator of all numeric coefficients of this polynomial.

This method only applies if the Coefficient type is a number.

### Returns

the main denominator of all coefficients of this polynomial.

```
12.396.4.37 main_denom() [2/2] template<typename Coefficient > template<typename C = Coefficient, DisableIf< is_number_type< C >> = dummy>
IntNumberType carl::UnivariatePolynomial< Coefficient >::main_denom ( ) const
```

```
12.396.4.38 main_var() template<typename Coefficient >
Variable carl::UnivariatePolynomial< Coefficient >::main_var ( ) const [inline]
```

Retrieves the main variable of this polynomial.

#### Returns

Main variable.

Replaces every coefficient c by c mod modulus.

## **Parameters**

```
modulus Modulus.
```

#### Returns

This.

Constructs a new polynomial where every coefficient c is replaced by c mod modulus.

### **Parameters**

```
modulus Modulus.
```

## Returns

New polynomial.

```
12.396.4.41 negate_variable() template<typename Coefficient >
UnivariatePolynomial carl::UnivariatePolynomial < Coefficient >::negate_variable ( ) const
[inline]
```

Constructs a new polynomial  ${\bf q}$  such that q(x)=p(-x) where  ${\bf p}$  is this polynomial.

## Returns

New polynomial with negated variable.

```
12.396.4.42 normalizeCoefficients() [1/2] template<typename Coefficient >
template<typename T = Coefficient, EnableIf< has_normalize< T >> = dummy>
UnivariatePolynomial& carl::UnivariatePolynomial< Coefficient >::normalizeCoefficients ( )
[inline]
```

```
12.396.4.43 normalizeCoefficients() [2/2] template<typename Coefficient >
template<typename T = Coefficient, DisableIf< has_normalize< T >> = dummy>
UnivariatePolynomial& carl::UnivariatePolynomial< Coefficient >::normalizeCoefficients ( )
[inline]
```

```
12.396.4.44 normalized() template<typename Coeff >
UnivariatePolynomial< Coeff > carl::UnivariatePolynomial< Coeff >::normalized
```

The normal part of a polynomial is the polynomial divided by the unit part.

See also

?, page 42.

#### Returns

This polynomial divided by the unit part.

```
12.396.4.45 numeric_content() [1/3] template<typename Coefficient > template<typename N = NumberType, EnableIf< is_subset_of_rationals_type< N >> = dummy> UnderlyingNumberType<Coefficient>::type carl::UnivariatePolynomial< Coefficient >::numeric_← content ( ) const
```

Obtains the numeric content part of this polynomial.

The numeric content part of a polynomial is defined as the gcd() of the numeric content parts of all coefficients. This is only possible if the underlying number type is either integral or fractional.

As for fractional numbers, we consider the following definition: gcd(a/b, c/d) = gcd(a/b\*I, c/d\*I) / I where I = lcm(b,d).

## Returns

numeric content part of the polynomial.

## See also

UnivariatePolynomials::numeric\_content(std::size\_t)

```
12.396.4.46 numeric_content() [2/3] template<typename Coefficient > template<typename N , EnableIf< is_subset_of_rationals_type< N >> > UnivariatePolynomial<Coeff>::NumberType carl::UnivariatePolynomial< Coefficient >::numeric_\( \to \) const
```

Returns the numeric content part of the i'th coefficient.

If the coefficients are numbers, this is simply the i'th coefficient. If the coefficients are polynomials, this is the numeric content part of the i'th coefficient.

#### **Parameters**

```
i number of the coefficient
```

## Returns

numeric content part of i'th coefficient.

```
12.396.4.48 numeric_unit() template<typename Coefficient >
NumberType carl::UnivariatePolynomial< Coefficient >::numeric_unit ( ) const [inline]
```

Returns the numeric unit part of the polynomial.

If the coefficients are numbers, this is the sign of the leading coefficient. If the coefficients are polynomials, this is the unit part of the leading coefficient.s

### Returns

unit part of the polynomial.

```
12.396.4.49 one() template<typename Coefficient >
UnivariatePolynomial carl::UnivariatePolynomial < Coefficient >::one ( ) const [inline]
```

Creates a polynomial of value one with the same main variable.

## Returns

One.

Multiply this polynomial with something and return the changed polynomial.

```
rhs Right hand side.
```

## Returns

Changed polynomial.

```
12.396.4.52 operator*=() [3/7] template<typename Coefficient >

template<typename I = Coefficient, DisableIf< std::is_same< Coefficient, I >> ...>

UnivariatePolynomial& carl::UnivariatePolynomial< Coefficient >::operator*= (

const typename IntegralType< Coefficient >::type & rhs)
```

Multiply this polynomial with something and return the changed polynomial.

## **Parameters**

```
rhs Right hand side.
```

### Returns

Changed polynomial.

Multiply this polynomial with something and return the changed polynomial.

## **Parameters**

```
rhs Right hand side.
```

# Returns

Changed polynomial.

Multiply this polynomial with something and return the changed polynomial.

#### **Parameters**

```
rhs Right hand side.
```

#### Returns

Changed polynomial.

Multiply this polynomial with something and return the changed polynomial.

## **Parameters**

```
rhs Right hand side.
```

### Returns

Changed polynomial.

```
12.396.4.56 operator*=() [7/7] template<typename Coefficient > template<typename C , DisableIf< is_number_type< C >> > UnivariatePolynomial< Coefficient > & carl::UnivariatePolynomial< Coefficient >::operator*= ( Variable rhs )
```

Add something to this polynomial and return the changed polynomial.

| rhs | Right hand side. |
|-----|------------------|

Changed polynomial.

Add something to this polynomial and return the changed polynomial.

#### **Parameters**

```
rhs Right hand side.
```

#### Returns

Changed polynomial.

```
12.396.4.59 operator-() template<typename Coeff >
UnivariatePolynomial< Coeff > carl::UnivariatePolynomial< Coeff >::operator-
```

Subtract something from this polynomial and return the changed polynomial.

## **Parameters**

```
rhs Right hand side.
```

## Returns

Changed polynomial.

Subtract something from this polynomial and return the changed polynomial.

```
rhs Right hand side.
```

## Returns

Changed polynomial.

TODO not fully sure whether this is necessary

Divide this polynomial by something and return the changed polynomial.

## **Parameters**

```
rhs Right hand side.
```

## Returns

Changed polynomial.

Divide this polynomial by something and return the changed polynomial.

## **Parameters**

```
rhs Right hand side.
```

## Returns

Changed polynomial.

```
12.396.4.65 operator=() [1/2] template<typename Coeff > UnivariatePolynomial< Coeff > & carl::UnivariatePolynomial< Coeff >::operator= ( const UnivariatePolynomial< Coefficient > & p)
```

Copy assignment operator.

```
12.396.4.66 operator=() [2/2] template<typename Coeff > UnivariatePolynomial< Coeff > & carl::UnivariatePolynomial< Coeff >::operator= ( UnivariatePolynomial< Coefficient > && p) [noexcept]
```

Move assignment operator.

Returns this polynomial to the given power.

## **Parameters**

```
exp Exponent.
```

### Returns

This to the power of exp.

```
12.396.4.68 reverse_coefficients() template<typename Coefficient >
UnivariatePolynomial carl::UnivariatePolynomial < Coefficient >::reverse_coefficients ( ) const
[inline]
```

Reverse coefficients safely.

```
12.396.4.69 sgn() template<typename Coefficient > carl::Sign carl::UnivariatePolynomial< Coefficient >::sgn ( const Coefficient & value ) const [inline]
```

Calculates the sign of the polynomial at some point.

```
Returns
```

Sign at value.

```
12.396.4.70 strip_leading_zeroes() template<typename Coefficient > void carl::UnivariatePolynomial< Coefficient >::strip_leading_zeroes ( ) [inline]
```

```
12.396.4.71 synthetic_division() template<typename Coefficient > Coeff carl::UnivariatePolynomial< Coeff >::synthetic_division ( const Coefficient & zeroOfDivisor)
```

```
12.396.4.72 tcoeff() template<typename Coefficient >
const Coefficient& carl::UnivariatePolynomial< Coefficient >::tcoeff ( ) const [inline]
```

Returns the trailing coefficient.

Asserts, that the polynomial is not empty.

Returns

The trailing coefficient.

```
12.396.4.73 to_integer_domain() [1/3] template<typename Coefficient > template<typename C = Coefficient, EnableIf< is_instantiation_of< GFNumber, C >> = dummy> UnivariatePolynomial<typename IntegralType<Coefficient>::type> carl::UnivariatePolynomial<Coefficient >::to_integer_domain ( ) const
```

Works only from rationals, if the numbers are already integers.

Returns

```
12.396.4.74 to_integer_domain() [2/3] template<typename Coefficient >
template<typename C = Coefficient, DisableIf< is_instantiation_of< GFNumber, C >> = dummy>
UnivariatePolynomial<typename IntegralType<Coefficient>::type> carl::UnivariatePolynomial<
Coefficient >::to_integer_domain ( ) const
```

Total degree.

```
12.396.4.75 to_integer_domain() [3/3] template<typename Coeff >
template<typename C , DisableIf< is_instantiation_of< GFNumber, C >> >
UnivariatePolynomial< typename IntegralType< Coeff >::type > carl::UnivariatePolynomial<
Coeff >::to_integer_domain
12.396.4.76 toFiniteDomain() template<typename Coefficient >
UnivariatePolynomial < GFNumber < typename IntegralType < Coeff >::type > > carl::UnivariatePolynomial <
Coeff >::toFiniteDomain (
             const GaloisField< typename IntegralType< Coefficient >::type > * galoisField )
const
12.396.4.77 toNumberCoefficients() [1/2] template<typename Coefficient >
template<typename C = Coefficient, DisableIf< is_number_type< C >> = dummy>
UnivariatePolynomial<NumberType> carl::UnivariatePolynomial< Coefficient >::toNumberCoefficients
() const
Asserts that is_univariate() is true.
12.396.4.78 toNumberCoefficients() [2/2] template<typename Coefficient >
template<typename C , DisableIf< is_number_type< C >> >
UnivariatePolynomial<typename UnivariatePolynomial<Coeff>::NumberType> carl::UnivariatePolynomial<
Coefficient >::toNumberCoefficients ( ) const
12.396.4.79 total_degree() template<typename Coefficient >
uint carl::UnivariatePolynomial< Coefficient >::total_degree ( ) const [inline]
Returns the total degree of the polynomial, that is the maximum degree of any monomial.
As the degree of the zero polynomial is -\infty, we assert that this polynomial is not zero. This must be checked by
the caller before calling this method.
See also
     ?, page 38
```

```
12.396.4.80 truncate() template<typename Coefficient >
void carl::UnivariatePolynomial< Coefficient >::truncate ( ) [inline]
```

Removes the leading term from the polynomial.

```
12.396.4.81 unit_part() template<typename Coeff > Coeff carl::UnivariatePolynomial< Coeff >::unit_part
```

The unit part of a polynomial over a field is its leading coefficient for nonzero polynomials, and one for zero polynomials.

The unit part of a polynomial over a ring is the sign of the polynomial for nonzero polynomials, and one for zero polynomials.

#### See also

?, page 42.

#### Returns

The unit part of the polynomial.

```
12.396.4.82 zero_is_root() template<typename Coefficient >
bool carl::UnivariatePolynomial< Coefficient >::zero_is_root ( ) const [inline]
```

Checks if zero is a real root of this polynomial.

## Returns

True if zero is a root.

## 12.396.5 Friends And Related Function Documentation

Checks if the two arguments are not equal.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs != rhs
```

Checks if the two arguments are not equal.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

### Returns

```
lhs != rhs
```

Perform a multiplication involving a polynomial.

## **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

## Returns

```
lhs * rhs
```

Perform a multiplication involving a polynomial.

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

## Returns

```
lhs * rhs
```

Perform a multiplication involving a polynomial.

## **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

#### Returns

```
lhs * rhs
```

Perform a multiplication involving a polynomial.

# **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

# Returns

```
lhs * rhs
```

Perform a multiplication involving a polynomial.

## **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

## Returns

```
lhs * rhs
```

Perform a multiplication involving a polynomial.

# Parameters

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

## Returns

```
lhs * rhs
```

Perform a multiplication involving a polynomial.

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

```
lhs * rhs
```

Perform a multiplication involving a polynomial.

## **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

## Returns

lhs \* rhs

Perform a multiplication involving a polynomial.

## **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

## Returns

```
lhs * rhs
```

Performs an addition involving a polynomial.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs + rhs
```

Performs an addition involving a polynomial.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

### Returns

```
lhs + rhs
```

Performs an addition involving a polynomial.

# **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs + rhs
```

Performs a subtraction involving a polynomial.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs - rhs
```

Performs a subtraction involving a polynomial.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

### Returns

```
lhs - rhs
```

Performs a subtraction involving a polynomial.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs - rhs
```

Perform a division involving a polynomial.

#### **Parameters**

| lhs | Left hand side.  |
|-----|------------------|
| rhs | Right hand side. |

## Returns

lhs / rhs

Streaming operator for univariate polynomials.

### **Parameters**

| os  | Output stream. |
|-----|----------------|
| rhs | Polynomial.    |

### Returns

os

Checks if the two arguments are equal.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs == rhs
```

Checks if the two arguments are equal.

## **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

## Returns

```
lhs == rhs
```

Checks if the two arguments are equal.

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

```
lhs == rhs
```

Checks if the two arguments are equal.

#### **Parameters**

| lhs | First argument.  |
|-----|------------------|
| rhs | Second argument. |

### **Returns**

```
lhs == rhs
```

```
12.396.5.25 UnivariatePolynomial template<typename Coefficient >
template<class T >
friend class UnivariatePolynomial [friend]
```

Declare all instantiations of univariate polynomials as friends.

# 12.397 carl::UpdateFnc Struct Reference

```
#include <GBUpdateProcedures.h>
```

## **Public Member Functions**

- virtual void operator() (std::size\_t index)=0
- virtual ~UpdateFnc ()=default

# 12.397.1 Constructor & Destructor Documentation

```
12.397.1.1 ~UpdateFnc() virtual carl::UpdateFnc::~UpdateFnc ( ) [virtual], [default]
```

## 12.397.2 Member Function Documentation

```
12.397.2.1 operator()() virtual void carl::UpdateFnc::operator() ( std::size_t index ) [pure virtual]
```

Implemented in carl::UpdateFnct< BuchbergerProc >, and carl::UpdateFnct< carl::Buchberger< Polynomial, AddingPolicy > >.

# 12.398 carl::UpdateFnct< BuchbergerProc > Struct Template Reference

```
#include <Buchberger.h>
```

## **Public Member Functions**

- UpdateFnct (BuchbergerProc \*proc)
- ∼UpdateFnct () override=default
- void operator() (std::size\_t index) override

## 12.398.1 Constructor & Destructor Documentation

```
12.398.1.1 UpdateFnct() template<typename BuchbergerProc > carl::UpdateFnct < BuchbergerProc >::UpdateFnct (

BuchbergerProc * proc ) [inline], [explicit]
```

```
12.398.1.2 ~UpdateFnct() template<typename BuchbergerProc > carl::UpdateFnct< BuchbergerProc >::~UpdateFnct ( ) [override], [default]
```

## 12.398.2 Member Function Documentation

Implements carl::UpdateFnc.

## 12.399 carl::UpperBound < Number > Struct Template Reference

```
#include <Interval.h>
```

#### **Data Fields**

- const Number & number
- BoundType bound\_type

#### 12.399.1 Field Documentation

```
12.399.1.1 bound_type template<typename Number >
BoundType carl::UpperBound< Number >::bound_type
```

```
12.399.1.2 number template<typename Number > const Number& carl::UpperBound< Number >::number
```

## 12.400 carl::UTerm Class Reference

Implements an uninterpreted term, that is either an uninterpreted variable or an uninterpreted function instance.

```
#include <UTerm.h>
```

### **Public Member Functions**

• UTerm ()=default

Default constructor.

- UTerm (UVariable v)
- UTerm (UFInstance ufi)
- UTerm (const Super &term)

Constructs an uninterpreted term.

- · const auto & asVariant () const
- bool isUVariable () const
- bool isUFInstance () const
- UVariable asUVariable () const
- UFInstance asUFInstance () const
- · Sort domain () const
- std::size\_t complexity () const
- · void gatherVariables (carlVariables &vars) const
- void gatherUFs (std::set< UninterpretedFunction > &ufs) const

## 12.400.1 Detailed Description

Implements an uninterpreted term, that is either an uninterpreted variable or an uninterpreted function instance.

## 12.400.2 Constructor & Destructor Documentation

```
12.400.2.1 UTerm() [1/4] carl::UTerm::UTerm ( ) [default]
```

Default constructor.

Constructs an uninterpreted term.

**Parameters** 

term

# 12.400.3 Member Function Documentation

```
12.400.3.1 asUFInstance() UFInstance carl::UTerm::asUFInstance ( ) const [inline]
```

Returns

The stored term as UFInstance.

```
12.400.3.2 asUVariable() UVariable carl::UTerm::asUVariable ( ) const [inline]
```

Returns

The stored term as UVariable.

```
12.400.3.3 asVariant() const auto& carl::UTerm::asVariant () const [inline]
12.400.3.4 complexity() std::size_t carl::UTerm::complexity ( ) const
12.400.3.5 domain() Sort carl::UTerm::domain ( ) const
Returns
    The domain of this uninterpreted term.
12.400.3.6 gatherUFs() void carl::UTerm::gatherUFs (
             std::set< UninterpretedFunction > & ufs ) const
12.400.3.7 gatherVariables() void carl::UTerm::gatherVariables (
             carlVariables & vars ) const
12.400.3.8 isUFInstance() bool carl::UTerm::isUFInstance ( ) const [inline]
Returns
     true, if the stored term is a UFInstance.
12.400.3.9 isUVariable() bool carl::UTerm::isUVariable ( ) const [inline]
Returns
     true, if the stored term is a UVariable.
```

# 12.401 carl::UVariable Class Reference

Implements an uninterpreted variable.

```
#include <UVariable.h>
```

## **Public Member Functions**

• UVariable ()=default

Default constructor.

- UVariable (const UVariable &)=default
- UVariable (UVariable &&)=default
- UVariable & operator= (const UVariable &)=default
- UVariable & operator= (UVariable &&)=default
- ∼UVariable ()=default
- UVariable (Variable var)
- UVariable (Variable var, Sort domain)

Constructs an uninterpreted variable.

- Variable variable () const
- Sort domain () const

## 12.401.1 Detailed Description

Implements an uninterpreted variable.

#### 12.401.2 Constructor & Destructor Documentation

```
\textbf{12.401.2.1} \quad \textbf{UVariable()} \; \texttt{[1/5]} \quad \texttt{carl::UVariable::UVariable ()} \quad \texttt{[default]}
```

Default constructor.

The resulting object will not be a valid variable, but a dummy object.

Constructs an uninterpreted variable.

| var    | The variable of the uninterpreted variable to construct. |
|--------|--|
| domain | The domain of the uninterpreted variable to construct.   |

#### 12.401.3 Member Function Documentation

```
12.401.3.1 domain() Sort carl::UVariable::domain ( ) const [inline]
```

#### Returns

The domain of this uninterpreted variable.

```
12.401.3.2 operator=() [1/2] UVariable& carl::UVariable::operator= ( const UVariable & ) [default]
```

```
12.401.3.4 variable() Variable carl::UVariable::variable ( ) const [inline]
```

## Returns

The according variable, hence, the actual content of this class.

# 12.402 carl::Variable Class Reference

A Variable represents an algebraic variable that can be used throughout carl.

```
#include <Variable.h>
```

# **Public Types**

• using Arg = const Variable &

Argument type for variables being function arguments.

### **Public Member Functions**

• constexpr Variable ()=default

Default constructor, constructing a variable, which is considered as not an actual variable.

• constexpr std::size\_t id () const noexcept

Retrieves the id of the variable.

• constexpr VariableType type () const noexcept

Retrieves the type of the variable.

• std::string name () const

Retrieves the name of the variable.

• std::string safe\_name () const

Retrieves a unique name of the variable of the form <type><id>.

constexpr std::size\_t rank () const noexcept

Retrieves the rank of the variable.

#### **Static Public Attributes**

static constexpr std::size\_t BITSIZE = CHAR\_BIT \* sizeof(std::size\_t)

Number of bits available for the content.

static constexpr std::size\_t RESERVED\_FOR\_TYPE = 3

Number of bits reserved for the type.

static constexpr std::size\_t RESERVED\_FOR\_RANK = 4

Number of bits reserved for the rank.

static constexpr std::size\_t RESERVED = RESERVED\_FOR\_RANK + RESERVED\_FOR\_TYPE

Overall number of bits reserved.

• static constexpr std::size\_t AVAILABLE = BITSIZE - RESERVED

Number of bits available for the id.

static const Variable NO\_VARIABLE = Variable()

Instance of an invalid variable.

#### **Friends**

# **Comparison operators**

• bool operator== (Variable Ihs, Variable rhs) noexcept

Compares two variables.

• bool operator!= (Variable lhs, Variable rhs) noexcept

Compares two variables.

• bool operator< (Variable Ihs, Variable rhs) noexcept

Compares two variables.

bool operator<= (Variable lhs, Variable rhs) noexcept</li>

Compares two variables.

• bool operator> (Variable lhs, Variable rhs) noexcept

Compares two variables.

bool operator>= (Variable lhs, Variable rhs) noexcept

Compares two variables.

# 12.402.1 Detailed Description

A Variable represents an algebraic variable that can be used throughout carl.

Variables are basically bitvectors that contain [rank | id | type], called *content*.

- The id is the identifier of this variable.
- The type is the variable type.
- The rank is zero be default, but can be used to create a custom variable ordering, as the comparison operators compare the whole content. The id and the type together form a unique identifier for a variable. If the VariablePool is used to construct variables (and we advise to do so), the id's will be consecutive starting with one for each variable type. The rank is meant to change the variable order when passing a set of variables to another context, for example a function. A single variable (identified by id and type) should not occur with two different rank values in the same context and hence such a comparison should never take place.

A variable with id zero is considered invalid. It can be used as a default argument and can be compared to Variable::NO\_VARIABLE. Such a variable can only be constructed using the default constructor and its content will always be zero.

Although not templated, we keep the whole class inlined for efficiency purposes. Note that this way, any decent compiler removes the overhead introduced, while having gained strong type-definitions and thus the ability to provide operator overloading.

Moreover, notice that for small classes like this, pass-by-value could be faster than pass-by-ref. However, this depends much on the capabilities of the compiler.

#### 12.402.2 Member Typedef Documentation

```
12.402.2.1 Arg using carl::Variable::Arg = const Variable&
```

Argument type for variables being function arguments.

# 12.402.3 Constructor & Destructor Documentation

```
12.402.3.1 Variable() constexpr carl::Variable::Variable () [constexpr], [default]
```

Default constructor, constructing a variable, which is considered as not an actual variable.

Such an invalid variable is stored in NO\_VARIABLE, so use this if you need a default value for a variable.

#### 12.402.4 Member Function Documentation

```
12.402.4.1 id() constexpr std::size_t carl::Variable::id ( ) const [inline], [constexpr], [noexcept]
```

Retrieves the id of the variable.

Returns

Variable id.

```
12.402.4.2 name() std::string carl::Variable::name ( ) const
```

Retrieves the name of the variable.

Returns

Variable name.

```
12.402.4.3 rank() constexpr std::size_t carl::Variable::rank ( ) const [inline], [constexpr], [noexcept]
```

Retrieves the rank of the variable.

Returns

Variable rank.

```
12.402.4.4 safe_name() std::string carl::Variable::safe_name ( ) const
```

Retrieves a unique name of the variable of the form <type><id>.

While <type> consists of lowercase letters, <id> is a decimal number. This unique name is meant to be used wherever a unique but notationally simple identifier is required, for example when interfacing with other systems.

Returns

Variable name.

```
12.402.4.5 type() constexpr VariableType carl::Variable::type ( ) const [inline], [constexpr], [noexcept]
```

Retrieves the type of the variable.

Returns

Variable type.

# 12.402.5 Friends And Related Function Documentation

Compares two variables.

Note that for performance reasons, we compare the whole content of the variable (including the rank).

Note that the variable order is not the order of the variable id. We consider variables greater, if they are defined earlier, i.e. if they have a smaller id. Hence, the variables order and the order of the variable ids are reversed.

#### **Parameters**

| lhs | First variable.  |
|-----|------------------|
| rhs | Second variable. |

### Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two variables.

Note that for performance reasons, we compare the whole content of the variable (including the rank).

Note that the variable order is not the order of the variable id. We consider variables greater, if they are defined earlier, i.e. if they have a smaller id. Hence, the variables order and the order of the variable ids are reversed.

### **Parameters**

| lhs | First variable.  |
|-----|------------------|
| rhs | Second variable. |

# Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two variables.

Note that for performance reasons, we compare the whole content of the variable (including the rank).

Note that the variable order is not the order of the variable id. We consider variables greater, if they are defined earlier, i.e. if they have a smaller id. Hence, the variables order and the order of the variable ids are reversed.

# **Parameters**

| lhs | First variable.  |
|-----|------------------|
| rhs | Second variable. |

#### Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two variables.

Note that for performance reasons, we compare the whole content of the variable (including the rank).

Note that the variable order is not the order of the variable id. We consider variables greater, if they are defined earlier, i.e. if they have a smaller id. Hence, the variables order and the order of the variable ids are reversed.

### **Parameters**

| lhs | First variable.  |
|-----|------------------|
| rhs | Second variable. |

#### Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two variables.

Note that for performance reasons, we compare the whole content of the variable (including the rank).

Note that the variable order is not the order of the variable id. We consider variables greater, if they are defined earlier, i.e. if they have a smaller id. Hence, the variables order and the order of the variable ids are reversed.

# **Parameters**

| lhs | First variable.  |
|-----|------------------|
| rhs | Second variable. |

# Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

Compares two variables.

Note that for performance reasons, we compare the whole content of the variable (including the rank).

Note that the variable order is not the order of the variable id. We consider variables greater, if they are defined earlier, i.e. if they have a smaller id. Hence, the variables order and the order of the variable ids are reversed.

#### **Parameters**

| lhs | First variable.  |
|-----|------------------|
| rhs | Second variable. |

#### Returns

lhs  $\sim$  rhs,  $\sim$  being the relation that is checked.

#### 12.402.6 Field Documentation

```
12.402.6.1 AVAILABLE constexpr std::size_t carl::Variable::AVAILABLE = BITSIZE - RESERVED [static], [constexpr]
```

Number of bits available for the id.

```
12.402.6.2 BITSIZE constexpr std::size_t carl::Variable::BITSIZE = CHAR_BIT * sizeof(std↔ ::size_t) [static], [constexpr]
```

Number of bits available for the content.

```
12.402.6.3 NO_VARIABLE const Variable carl::Variable::NO_VARIABLE = Variable() [static]
```

Instance of an invalid variable.

```
12.402.6.4 RESERVED constexpr std::size_t carl::Variable::RESERVED = RESERVED_FOR_RANK + RESERVED_FOR_TYPE [static], [constexpr]
```

Overall number of bits reserved.

```
12.402.6.5 RESERVED_FOR_RANK constexpr std::size_t carl::Variable::RESERVED_FOR_RANK = 4 [static], [constexpr]
```

Number of bits reserved for the rank.

```
12.402.6.6 RESERVED_FOR_TYPE constexpr std::size_t carl::Variable::RESERVED_FOR_TYPE = 3 [static], [constexpr]
```

Number of bits reserved for the type.

# 12.403 carl::variable\_type\_filter Class Reference

```
#include <Variables.h>
```

#### **Public Member Functions**

- bool apply (VariableType v) const
- · bool apply (Variable v) const

### **Static Public Member Functions**

- static variable\_type\_filter all ()
- static variable\_type\_filter excluding (std::initializer\_list< VariableType > i)
- static variable\_type\_filter only (std::initializer\_list< VariableType > i)
- static auto boolean ()
- static auto integer ()
- static auto real ()
- static auto arithmetic ()
- static auto bitvector ()
- static auto uninterpreted ()

#### 12.403.1 Member Function Documentation

```
12.403.1.1 all() static variable_type_filter carl::variable_type_filter::all () [inline], [static]
```

```
12.403.1.2 apply() [1/2] bool carl::variable_type_filter::apply ( Variable v ) const [inline]
```

```
12.403.1.3 apply() [2/2] bool carl::variable_type_filter::apply (
             VariableType v ) const [inline]
12.403.1.4 arithmetic() static auto carl::variable_type_filter::arithmetic ( ) [inline], [static]
12.403.1.5 bitvector() static auto carl::variable_type_filter::bitvector ( ) [inline], [static]
12.403.1.6 boolean() static auto carl::variable_type_filter::boolean ( ) [inline], [static]
12.403.1.7 excluding() static variable_type_filter carl::variable_type_filter::excluding (
             std::initializer_list< VariableType > i ) [inline], [static]
12.403.1.8 integer() static auto carl::variable_type_filter::integer ( ) [inline], [static]
12.403.1.9 only() static variable_type_filter carl::variable_type_filter::only (
             std::initializer_list< VariableType > i ) [inline], [static]
12.403.1.10 real() static auto carl::variable_type_filter::real ( ) [inline], [static]
12.403.1.11 uninterpreted() static auto carl::variable_type_filter::uninterpreted ( ) [inline],
[static]
12.404 carl::VariableAssignment< Poly > Class Template Reference
#include <VariableAssignment.h>
Public Types

    using Number = typename Base::Number
```

using MR = typename Base::MRusing RAN = typename Base::RAN

#### **Public Member Functions**

- VariableAssignment (Variable v, const RAN &value, bool negated=false)
- VariableAssignment (Variable v, const Number &value, bool negated=false)
- Variable var () const
- const RAN & value () const
- const auto & base\_value () const
- bool negated () const
- · VariableAssignment negation () const
- operator const VariableComparison
   Poly > & () const

#### **Friends**

template<typename Pol > void variables (const VariableAssignment< Pol > &f, carlVariables &vars)

### 12.404.1 Member Typedef Documentation

```
12.404.1.1 MR template<typename Poly > using carl::VariableAssignment< Poly >::MR = typename Base::MR
```

```
12.404.1.2 Number template<typename Poly > using carl::VariableAssignment< Poly >::Number = typename Base::Number
```

```
12.404.1.3 RAN template<typename Poly > using carl::VariableAssignment< Poly >::RAN = typename Base::RAN
```

# 12.404.2 Constructor & Destructor Documentation

```
12.404.2.2 VariableAssignment() [2/2] template<typename Poly >
carl::VariableAssignment< Poly >::VariableAssignment (
            Variable v,
            const Number & value,
            bool negated = false ) [inline]
12.404.3 Member Function Documentation
12.404.3.1 base_value() template<typename Poly >
const auto& carl::VariableAssignment< Poly >::base_value ( ) const [inline]
12.404.3.2 negated() template<typename Poly >
bool carl::VariableAssignment< Poly >::negated ( ) const [inline]
12.404.3.3 negation() template<typename Poly >
VariableAssignment carl::VariableAssignment< Poly >::negation ( ) const [inline]
12.404.3.4 operator const VariableComparison< Poly > &() template<typename Poly >
carl::VariableAssignment< Poly >::operator const VariableComparison< Poly > & ( ) const [inline]
12.404.3.5 value() template<typename Poly >
const RAN& carl::VariableAssignment< Poly >::value ( ) const [inline]
12.404.3.6 var() template<typename Poly >
Variable carl::VariableAssignment< Poly >::var ( ) const [inline]
12.404.4 Friends And Related Function Documentation
12.404.4.1 variables template<typename Poly >
template<typename Pol >
void variables (
            const VariableAssignment< Pol > & f,
            carlVariables & vars ) [friend]
```

# 12.405 carl::VariableComparison < Poly > Class Template Reference

Represent a sum type/variant of an (in)equality between a variable on the left-hand side and multivariateRoot or algebraic real on the right-hand side.

#include <VariableComparison.h>

#### **Public Types**

- using Number = typename UnderlyingNumberType< Poly >::type
- using MR = MultivariateRoot< Poly >
- using RAN = typename MultivariateRoot< Poly >::RAN

### **Public Member Functions**

- VariableComparison (Variable v, const std::variant < MR, RAN > &value, Relation rel, bool neg)
- VariableComparison (Variable v, const MR &value, Relation rel)
- · VariableComparison (Variable v, const RAN &value, Relation rel)
- Variable var () const
- Relation relation () const
- bool negated () const
- const std::variant< MR, RAN > & value () const
- bool is\_equality () const
- VariableComparison negation () const
- VariableComparison invert\_relation () const

# 12.405.1 Detailed Description

```
template<typename Poly> class carl::VariableComparison< Poly>
```

Represent a sum type/variant of an (in)equality between a variable on the left-hand side and multivariateRoot or algebraic real on the right-hand side.

This is basically a special purpose atomic SMT formula. The lhs-variable must does not appear on the rhs.

# 12.405.2 Member Typedef Documentation

```
12.405.2.1 MR template<typename Poly >
using carl::VariableComparison< Poly >::MR = MultivariateRoot<Poly>
```

```
12.405.2.2 Number template<typename Poly > using carl::VariableComparison< Poly >::Number = typename UnderlyingNumberType<Poly>::type
```

```
12.405.2.3 RAN template<typename Poly > using carl::VariableComparison< Poly >::RAN = typename MultivariateRoot<Poly>::RAN
```

# 12.405.3 Constructor & Destructor Documentation

```
12.405.3.1 VariableComparison() [1/3] template<typename Poly >
carl::VariableComparison< Poly >::VariableComparison (
             Variable v_{\bullet}
             const std::variant< MR, RAN > & value,
             Relation rel,
             bool neg ) [inline]
12.405.3.2 VariableComparison() [2/3] template<typename Poly >
carl::VariableComparison< Poly >::VariableComparison (
            Variable v,
             const MR & value,
             Relation rel ) [inline]
12.405.3.3 VariableComparison() [3/3] template<typename Poly >
\verb|carl::VariableComparison| < \verb|Poly| >::VariableComparison| (
             Variable v,
             const RAN & value,
             Relation rel ) [inline]
12.405.4 Member Function Documentation
12.405.4.1 invert_relation() template<typename Poly >
VariableComparison carl::VariableComparison< Poly >::invert_relation ( ) const [inline]
12.405.4.2 is_equality() template<typename Poly >
bool carl::VariableComparison< Poly >::is_equality ( ) const [inline]
12.405.4.3 negated() template<typename Poly >
bool carl::VariableComparison< Poly >::negated ( ) const [inline]
```

```
12.405.4.4 negation() template<typename Poly >
VariableComparison carl::VariableComparison< Poly >::negation ( ) const [inline]

12.405.4.5 relation() template<typename Poly >
Relation carl::VariableComparison< Poly >::relation ( ) const [inline]

12.405.4.6 value() template<typename Poly >
const std::variant<MR, RAN>& carl::VariableComparison< Poly >::value ( ) const [inline]

12.405.4.7 var() template<typename Poly >
Variable carl::VariableComparison

Variable carl::VariableComparison

Poly >::var ( ) const [inline]
```

### 12.406 carl::VariablePool Class Reference

This class generates new variables and stores human-readable names for them.

```
#include <VariablePool.h>
```

### **Public Member Functions**

- Variable get\_fresh\_persistent\_variable (VariableType type=VariableType::VT\_REAL) noexcept
- Variable get\_fresh\_persistent\_variable (const std::string &name, VariableType type=VariableType::VT\_REAL)
- void clear () noexcept

Clears everything already created in this pool.

Variable find\_variable\_with\_name (const std::string &name) const noexcept

Searches in the friendly names list for a variable with the given name.

• std::string get\_name (Variable v, bool variableName=true) const

Get a human-readable name for the given variable.

void set\_name (Variable v, const std::string &name)

Add a name for a given Variable.

void set\_prefix (std::string prefix="\_") noexcept

Sets the prefix used when printing anonymous variables.

#### **Static Public Member Functions**

• static VariablePool & getInstance ()

Returns the single instance of this class by reference.

### **Protected Member Functions**

• VariablePool () noexcept

Private default constructor.

- Variable get\_fresh\_variable (VariableType type=VariableType::VT\_REAL) noexcept Get a variable which was not used before.
- Variable get\_fresh\_variable (const std::string &name, VariableType type=VariableType::VT\_REAL)

  Get a variable with was not used before and set a name for it.

# **Friends**

- Variable fresh\_variable (VariableType vt) noexcept
- Variable fresh\_variable (const std::string &name, VariableType vt)

### 12.406.1 Detailed Description

This class generates new variables and stores human-readable names for them.

As we want only a single unique VariablePool and need global access to it, it is implemented as a singleton.

All methods that modify the pool, that are getInstance(), get\_fresh\_variable() and set\_name(), are thread-safe.

#### 12.406.2 Constructor & Destructor Documentation

```
12.406.2.1 VariablePool() carl::VariablePool::VariablePool ( ) [protected], [noexcept]
```

Private default constructor.

#### 12.406.3 Member Function Documentation

```
12.406.3.1 clear() void carl::VariablePool::clear ( ) [inline], [noexcept]
```

Clears everything already created in this pool.

```
12.406.3.2 find_variable_with_name() Variable carl::VariablePool::find_variable_with_name ( const std::string & name ) const [noexcept]
```

Searches in the friendly names list for a variable with the given name.

#### **Parameters**

| name | The friendly variable name to look for. |
|------|---|
|------|---|

### Returns

The first variable with that friendly name.

```
12.406.3.4 get_fresh_persistent_variable() [2/2] Variable carl::VariablePool::get_fresh_persistent ← variable (

VariableType type = VariableType::VT_REAL ) [noexcept]
```

Get a variable with was not used before and set a name for it.

This method is thread-safe.

# **Parameters**

| name | Name for the new variable. |
|------|----------------------------|
| type | Type for the new variable. |

# Returns

A new variable.

```
12.406.3.6 get_fresh_variable() [2/2] Variable carl::VariablePool::get_fresh_variable (

VariableType type = VariableType::VT_REAL ) [protected], [noexcept]
```

Get a variable which was not used before.

This method is thread-safe.

#### **Parameters**

| type | Type for the new variable. |
|------|----------------------------|
|------|----------------------------|

### Returns

A new variable.

Get a human-readable name for the given variable.

If the given Variable is Variable::NO\_VARIABLE, "NO\_VARIABLE" is returned. If friendly VarName is true, the name that was set via set Variable Name() for this Variable, if there is any, is returned. Otherwise " $x_{-}$ <id>" is returned, id being the internal id of the Variable.

#### **Parameters**

| V            | Variable.  |
|--------------|--|
| variableName | Flag, if a name set via setVariableName shall be considered. |

# Returns

Some name for the Variable.

```
12.406.3.8 getInstance() static VariablePool & carl::Singleton< VariablePool >::getInstance () [inline], [static], [inherited]
```

Returns the single instance of this class by reference.

If there is no instance yet, a new one is created.

Add a name for a given Variable.

This method is thread-safe.

# **Parameters**

| V    | Variable.                        |
|------|----------------------------------|
| name | Some string naming the variable. |

```
12.406.3.10 set_prefix() void carl::VariablePool::set_prefix ( std::string prefix = "_") [inline], [noexcept]
```

Sets the prefix used when printing anonymous variables.

The default is "\_", hence they look like "\_x\_5".

#### **Parameters**

prefix Prefix for anonymous variable names.

### 12.406.4 Friends And Related Function Documentation

```
12.406.4.2 fresh_variable [2/2] Variable fresh_variable ( VariableType vt ) [friend]
```

# 12.407 carl::detail::variant\_extend\_visitor< Target > Struct Template Reference

```
#include <variant_util.h>
```

### **Public Member Functions**

template<typename T >
 Target operator() (const T &t) const

# 12.407.1 Member Function Documentation

# 12.408 carl::detail::variant\_hash Struct Reference

```
#include <variant_util.h>
```

### **Public Member Functions**

template < class T >
 std::size\_t operator() (const T &val) const

### 12.408.1 Member Function Documentation

# 12.409 carl::detail::variant\_is\_type\_visitor< T > Struct Template Reference

```
#include <variant_util.h>
```

# **Public Member Functions**

template<typename TT >
 constexpr bool operator() (const TT &) const noexcept

### 12.409.1 Member Function Documentation

# 12.410 carl::VarInfo< CoeffType > Class Template Reference

```
#include <VarInfo.h>
```

#### **Public Member Functions**

- VarInfo ()=default
- VarInfo (std::size\_t maxDegree, std::size\_t min\_degree, std::size\_t occurence, std::map< std::size\_t, CoeffType</li>
   &&coeffs)
- bool has\_coeff () const
- std::size\_t max\_degree () const
- std::size\_t min\_degree () const
- std::size\_t num\_occurences () const
- const std::map< std::size\_t, CoeffType > & coeffs () const
- void raise\_max\_degree (std::size\_t degree)
- void lower\_min\_degree (std::size\_t degree)
- void increase\_num\_occurences ()
- template<typename Term >
   void update\_coeff (std::size\_t exponent, const Term &t)

#### 12.410.1 Constructor & Destructor Documentation

```
12.410.1.1 VarInfo() [1/2] template<typename CoeffType > carl::VarInfo< CoeffType >::VarInfo ( ) [default]
```

### 12.410.2 Member Function Documentation

```
12.410.2.1 coeffs() template<typename CoeffType >
const std::map<std::size_t, CoeffType>& carl::VarInfo< CoeffType >::coeffs ( ) const [inline]
```

```
12.410.2.2 has_coeff() template<typename CoeffType >
bool carl::VarInfo< CoeffType >::has_coeff () const [inline]
```

auto end ()

```
12.410.2.3 increase_num_occurences() template<typename CoeffType >
void carl::VarInfo< CoeffType >::increase_num_occurences ( ) [inline]
12.410.2.4 lower_min_degree() template<typename CoeffType >
void carl::VarInfo< CoeffType >::lower_min_degree (
            std::size_t degree ) [inline]
12.410.2.5 max_degree() template<typename CoeffType >
std::size_t carl::VarInfo< CoeffType >::max_degree ( ) const [inline]
12.410.2.6 min_degree() template<typename CoeffType >
std::size_t carl::VarInfo< CoeffType >::min_degree ( ) const [inline]
12.410.2.7 num_occurences() template<typename CoeffType >
std::size_t carl::VarInfo< CoeffType >::num_occurences ( ) const [inline]
12.410.2.8 raise_max_degree() template<typename CoeffType >
void carl::VarInfo< CoeffType >::raise_max_degree (
             std::size_t degree ) [inline]
12.410.2.9 update_coeff() template<typename CoeffType >
template<typename Term >
void carl::VarInfo< CoeffType >::update_coeff (
            std::size_t exponent,
             const Term & t ) [inline]
12.411 carl::VarsInfo< CoeffType > Class Template Reference
#include <VarInfo.h>
Public Member Functions

    VarInfo< CoeffType > & var (Variable var)

    const VarInfo< CoeffType > & var (Variable var) const

   • bool occurs (Variable var) const
   • auto & data ()
   • auto cbegin () const

    auto cend () const

   • auto begin ()
```

### 12.411.1 Member Function Documentation

```
12.411.1.1 begin() template<typename CoeffType >
auto carl::VarsInfo< CoeffType >::begin ( ) [inline]
12.411.1.2 cbegin() template<typename CoeffType >
auto carl::VarsInfo< CoeffType >::cbegin ( ) const [inline]
12.411.1.3 cend() template<typename CoeffType >
auto carl::VarsInfo< CoeffType >::cend ( ) const [inline]
12.411.1.4 data() template<typename CoeffType >
auto& carl::VarsInfo< CoeffType >::data ( ) [inline]
12.411.1.5 end() template<typename CoeffType >
auto carl::VarsInfo< CoeffType >::end ( ) [inline]
12.411.1.6 occurs() template<typename CoeffType >
bool carl::VarsInfo< CoeffType >::occurs (
            Variable var ) const [inline]
12.411.1.7 var() [1/2] template<typename CoeffType >
VarInfo<CoeffType>& carl::VarsInfo< CoeffType >::var (
            Variable var ) [inline]
12.411.1.8 var() [2/2] template<typename CoeffType >
const VarInfo<CoeffType>& carl::VarsInfo< CoeffType >::var (
            Variable var ) const [inline]
```

# 12.412 carl::VarSolutionFormula < Polynomial > Class Template Reference

#include <Contraction.h>

#### **Public Member Functions**

- VarSolutionFormula ()=delete
- VarSolutionFormula (const Polynomial &p, Variable::Arg x)

Constructs the solution formula for the given variable x in the equation p = 0, where p is the given polynomial.

- void addRoot (const Interval< double > &\_interv, const Interval< double > &\_varInterval, std::vector
   Interval< double >> &\_result) const
- std::vector< Interval< double >> evaluate (const Interval< double >::evalintervalmap &intervals) const Evaluates this solution formula for the given mapping of the variables occurring in the solution formula to double intervals

#### 12.412.1 Constructor & Destructor Documentation

```
12.412.1.1 VarSolutionFormula() [1/2] template<typename Polynomial > carl::VarSolutionFormula< Polynomial >::VarSolutionFormula () [delete]
```

Constructs the solution formula for the given variable x in the equation p = 0, where p is the given polynomial.

The polynomial p must have one of the following forms: 1.) ax+h, with a being a rational number and h a linear polynomial not containing x and not having a constant part 2.)  $x^i+m-y$ , with i being a positive integer, m being a monomial not containing x and y being a variable different from x

#### **Parameters**

| р | The polynomial containing the given variable to construct a solution formula for. |
|---|---|
| X | The variable to construct a solution formula for.                                 |

### 12.412.2 Member Function Documentation

```
12.412.2.1 addRoot() template<typename Polynomial > void carl::VarSolutionFormula< Polynomial >::addRoot (
```

```
const Interval< double > & .interv,
const Interval< double > & .varInterval,
std::vector< Interval< double >> & .result ) const [inline]
```

```
12.412.2.2 evaluate() template<typename Polynomial >
std::vector<Interval<double> > carl::VarSolutionFormula< Polynomial >::evaluate (
const Interval< double >::evalintervalmap & intervals ) const [inline]
```

Evaluates this solution formula for the given mapping of the variables occurring in the solution formula to double intervals.

#### **Parameters**

| intervals | The mapping of the variables occurring in the solution formula to double intervals |
|-----------|--|
| resA      | The first interval of the result.  |
| resB      | The second interval of the result.   |

#### Returns

true, if the second interval is not empty. (the first interval must then be also nonempty)

# 12.413 carl::Void< typename > Struct Template Reference

```
#include <SFINAE.h>
```

# **Public Types**

• using type = void

# 12.413.1 Member Typedef Documentation

```
12.413.1.1 type template<typename >
using carl::Void< typename >::type = void
```

# 12.414 carl::vs::zero < Poly > Struct Template Reference

A square root expression with side conditions.

```
#include <zeros.h>
```

# **Data Fields**

- SqrtEx< Poly > sqrt\_ex
- Constraints < Poly > side\_condition

### 12.414.1 Detailed Description

```
template<typename Poly> struct carl::vs::zero< Poly>
```

A square root expression with side conditions.

# 12.414.2 Field Documentation

```
12.414.2.1 side_condition template<typename Poly > Constraints<Poly> carl::vs::zero< Poly >::side_condition
```

```
12.414.2.2 sqrt_ex template<typename Poly >
SqrtEx<Poly> carl::vs::zero< Poly >::sqrt_ex
```

# 13 File Documentation

# 13.1 carl-arith/core/Relation.h File Reference

```
#include <carl-logging/carl-logging.h>
#include "Sign.h"
#include <cassert>
#include <iostream>
#include <memory>
#include <sstream>
```

# **Data Structures**

• struct std::hash< carl::Relation >

# **Namespaces**

carl

carl is the main namespace for the library.

# **Enumerations**

```
    enum class carl::Relation {
        carl::EQ = 0 , carl::NEQ = 1 , carl::LESS = 2 , carl::LEQ = 4 ,
        carl::GREATER = 3 , carl::GEQ = 5 }
```

### **Functions**

### 13.1.1 Detailed Description

• template<typename T1 , typename T2 >

**Author** 

Sebastian Junges

# 13.2 carl-arith/groebner/DivisionLookupResult.h File Reference

bool carl::evaluate (const T1 &lhs, Relation r, const T2 &rhs)

#### **Data Structures**

struct carl::DivisionLookupResult< Polynomial >
 The result of.

### **Namespaces**

· carl

carl is the main namespace for the library.

# 13.2.1 Detailed Description

Author

Sebastian Junges

# 13.3 carl-arith/groebner/gb-buchberger/Buchberger.h File Reference

```
#include "../GBUpdateProcedures.h"
#include "../Ideal.h"
#include "../Reductor.h"
#include "CriticalPairs.h"
#include <list>
#include <unordered_map>
#include "Buchberger.tpp"
```

### **Data Structures**

- struct carl::UpdateFnct< BuchbergerProc >
- struct carl::DefaultBuchbergerSettings

Standard settings used if the Buchberger object is not instantiated with another template parameter.

class carl::Buchberger< Polynomial, AddingPolicy >

Gebauer and Moeller style implementation of the Buchberger algorithm.

# **Namespaces**

· carl

carl is the main namespace for the library.

# 13.3.1 Detailed Description

**Author** 

Sebastian Junges

# 13.4 carl-arith/groebner/gb-buchberger/CriticalPairs.h File Reference

```
#include <carl-arith/core/CompareResult.h>
#include <carl-arith/poly/umvpoly/MonomialOrdering.h>
#include <carl-common/datastructures/Heap.h>
#include "CriticalPairsEntry.h"
#include <unordered_map>
#include "CriticalPairs.tpp"
```

# **Data Structures**

- class carl::CriticalPairConfiguration< Compare >
- class carl::CriticalPairs
   Datastructure, Configuration >

A data structure to store all the SPolynomial pairs which have to be checked.

# **Namespaces**

carl

carl is the main namespace for the library.

# **Typedefs**

typedef CriticalPairs< Heap, CriticalPairConfiguration< GrLexOrdering >> carl::CritPairs

# 13.4.1 Detailed Description

Author

Sebastian Junges

# 13.5 carl-arith/groebner/gb-buchberger/CriticalPairsEntry.h File Reference

```
#include <carl-arith/poly/umvpoly/Monomial.h>
#include "SPolPair.h"
#include <list>
```

### **Data Structures**

class carl::CriticalPairsEntry
 Compare >

A list of SPol pairs which have to be checked by the Buchberger algorithm.

# **Namespaces**

• carl

carl is the main namespace for the library.

# 13.5.1 Detailed Description

Author

Sebastian Junges

# 13.6 carl-arith/groebner/gb-buchberger/SPolPair.h File Reference

```
#include <carl-arith/poly/umvpoly/Monomial.h>
```

# **Data Structures**

struct carl::SPolPair

Basic spol-pair.

struct carl::SPolPairCompare < Compare >

# **Namespaces**

carl

carl is the main namespace for the library.

# 13.6.1 Detailed Description

Author

Sebastian Junges

# 13.7 carl-arith/groebner/GBProcedure.h File Reference

```
#include "Ideal.h"
#include "Reductor.h"
#include <carl-logging/carl-logging.h>
#include <carl-common/datastructures/BitVector.h>
```

#### **Data Structures**

- class carl::AbstractGBProcedure< Polynomial >
- $\bullet \ \, {\it class carl} :: {\it GBProcedure} < {\it Polynomial, Procedure, AddingPolynomialPolicy} > \\$

A general class for Groebner Basis calculation.

# **Namespaces**

· carl

carl is the main namespace for the library.

### 13.7.1 Detailed Description

**Author** 

Sebastian Junges

# 13.8 carl-arith/groebner/GBUpdateProcedures.h File Reference

```
#include "../poly/umvpoly/functions/SeparablePart.h"
```

# **Data Structures**

- struct carl::UpdateFnc
- struct carl::StdAdding
   Polynomial
- struct carl::RadicalAwareAdding
   Polynomial >
- struct carl::RealRadicalAwareAdding
   Polynomial

### **Namespaces**

• carl

carl is the main namespace for the library.

# 13.8.1 Detailed Description

Author

Sebastian Junges

# 13.9 carl-arith/groebner/Ideal.h File Reference

```
#include "ideal-ds/IdealDSVector.h"
#include "ideal-ds/PolynomialSorts.h"
#include <carl-arith/poly/umvpoly/MultivariatePolynomial.h>
#include <carl-arith/poly/umvpoly/Term.h>
#include <unordered_set>
```

### **Data Structures**

class carl::Ideal
 Polynomial, Datastructure, CacheSize >

# **Namespaces**

carl

carl is the main namespace for the library.

### 13.9.1 Detailed Description

**Author** 

Sebastian Junges

# 13.10 carl-arith/groebner/ReductorEntry.h File Reference

```
#include <carl-arith/poly/umvpoly/Term.h>
#include <cassert>
#include <memory>
```

# **Data Structures**

class carl::ReductorEntry< Polynomial >
 An entry in the reduction polynomial.

### **Namespaces**

• carl

carl is the main namespace for the library.

# **Functions**

```
    template < class C >
        std::ostream & carl::operator < < (std::ostream &os, const ReductorEntry < C > rhs)
```

# 13.10.1 Detailed Description

**Author** 

Sebastian Junges

# 13.11 carl-arith/numbers/adaption\_cln/typetraits.h File Reference

```
#include "../typetraits.h"
#include "include.h"
```

# **Data Structures**

struct carl::is\_integer\_type< cln::cl\_l >

States that cln::cl\_I has the trait is\_integer\_type .

struct carl::is\_rational\_type< cln::cl\_RA >

States that cln::cl\_RA has the trait is\_rational\_type .

struct carl::IntegralType< cln::cl\_l >

States that IntegralType of cln::cl\_l is cln::cl\_l .

struct carl::IntegralType< cln::cl\_RA >

States that IntegralType of cln::cl\_RA is cln::cl\_I.

### **Namespaces**

• carl

carl is the main namespace for the library.

### 13.11.1 Detailed Description

**Author** 

Sebastian Junges Gereon Kremer

# 13.12 carl-arith/numbers/adaption\_gmpxx/typetraits.h File Reference

```
#include "../typetraits.h"
#include "include.h"
```

# **Data Structures**

struct carl::is\_integer\_type< mpz\_class >

States that mpz\_class has the trait is\_integer\_type.

struct carl::is\_rational\_type< mpq\_class >

States that mpq\_class has the trait is\_rational\_type .

struct carl::IntegralType< mpq\_class >

States that IntegralType of mpq\_class is mpz\_class.

struct carl::IntegralType< mpz\_class >

States that IntegralType of  $mpz\_class$  is  $mpz\_class$ .

#### **Namespaces**

carl

carl is the main namespace for the library.

#### 13.12.1 Detailed Description

**Author** 

Sebastian Junges

Gereon Kremer

# 13.13 carl-arith/numbers/adaption\_native/typetraits.h File Reference

```
#include "../typetraits.h"
```

#### **Data Structures**

struct carl::is\_subset\_of\_integers\_type< signed char >

States that signed char has the trait is\_subset\_of\_integers\_type .

struct carl::is\_subset\_of\_integers\_type< short int >

States that short int has the trait is\_subset\_of\_integers\_type .

struct carl::is\_subset\_of\_integers\_type< int >

States that int has the trait is\_subset\_of\_integers\_type .

- struct carl::is\_subset\_of\_integers\_type< long int >

States that long int has the trait is\_subset\_of\_integers\_type .

struct carl::is\_subset\_of\_integers\_type< long long int >

States that long long int has the trait is\_subset\_of\_integers\_type .

struct carl::is\_subset\_of\_integers\_type< unsigned char >

States that unsigned char has the trait is\_subset\_of\_integers\_type .

struct carl::is\_subset\_of\_integers\_type< unsigned short int >

States that unsigned short int has the trait is\_subset\_of\_integers\_type .

struct carl::is\_subset\_of\_integers\_type< unsigned int >

States that unsigned int has the trait is\_subset\_of\_integers\_type .

struct carl::is\_subset\_of\_integers\_type< unsigned long int >

States that unsigned long int has the trait is\_subset\_of\_integers\_type .

struct carl::is\_subset\_of\_integers\_type< unsigned long long int >

States that unsigned long long int has the trait is\_subset\_of\_integers\_type .

struct carl::IntegralType< float >

States that Integral Type of float is sint .

struct carl::IntegralType< double >

States that IntegralType of double is sint .

struct carl::IntegralType< long double >

States that IntegralType of long double is sint .

### **Namespaces**

carl

carl is the main namespace for the library.

### 13.13.1 Detailed Description

**Author** 

```
Gereon Kremer gereon.kremer@cs.rwth-aachen.de
```

# 13.14 carl-arith/numbers/typetraits.h File Reference

```
#include <carl-common/meta/platform.h>
#include <carl-common/config.h>
#include <limits>
#include <type_traits>
#include "../interval/typetraits.h"
```

```
Data Structures

    struct carl::remove_all
    T, U >

    struct carl::remove_all
    T, T >

    struct carl::has_subtype< T >

           This template is designed to provide types that are related to other types.

    struct carl::is_field_type< T >

           States if a type is a field.

    struct carl::is_field_type< GFNumber< C >>

           States that a Gallois field is a field.

    struct carl::is_finite_type< T >

           States if a type represents only a finite domain.

    struct carl::is_finite_type< GFNumber< C >>

           Type trait is_finite_type_domain.

    struct carl::is_float_type< T >

           States if a type is a floating point type.

    struct carl::is_integer_type< T >

           States if a type is an integer type.

    struct carl::is_subset_of_integers_type < Type >

           States if a type represents a subset of all integers.

    struct carl::is_number_type< T >

           States if a type is a number type.

    struct carl::is_number_type< GFNumber< C >>

    struct carl::is_rational_type< T >

           States if a type is a rational type.

    struct carl::is_subset_of_rationals_type< T >

           States if a type represents a subset of all rationals and the representation is similar to a rational.

    struct carl::characteristic< type >

           Type trait for the characteristic of the given field (template argument).

    struct carl::IntegralType< RationalType >

           Gives the corresponding integral type.

    struct carl::IntegralType< GFNumber< C >>
```

struct carl::UnderlyingNumberType< T >

class carl::PreventConversion< T >

Gives the underlying number type of a complex object.

# **Namespaces**

• carl

carl is the main namespace for the library.

#### Macros

- #define TRAIT\_TRUE(name, type, groups)
- #define TRAIT\_FALSE(name, type, groups)
- #define TRAIT\_TYPE(name, \_type, value, groups)

# **Typedefs**

template<typename C >
 using carl::IntegralTypeIfDifferent = typename std::enable\_if<!std::is\_same< C, typename IntegralType< C
 >::type >::type

### **Functions**

template<typename T, typename T2 > bool carl::fits\_within (const T2 &t)

# 13.14.1 Detailed Description

# **Author**

```
Gereon Kremer gereon.kremer@cs.rwth-aachen.de
Sebastian Junges
```

### 13.14.2 Macro Definition Documentation

template<> struct name<type>: std::true\_type {};

# 13.15 carl-arith/numbers/adaption\_cln/hash.h File Reference

```
#include "include.h"
```

# **Data Structures**

- struct std::hash< cln::cl\_RA >
- struct std::hash< cln::cl\_l >

# 13.15.1 Detailed Description

**Author** 

Sebastian Junges

Florian Corzilius

# 13.16 carl-arith/numbers/adaption\_gmpxx/hash.h File Reference

```
#include <carl-common/util/hash.h>
#include "include.h"
#include <cstddef>
#include <functional>
```

### **Data Structures**

- struct std::hash< mpz\_class >
- struct std::hash< mpq\_class >

# 13.16.1 Detailed Description

**Author** 

Sebastian Junges

Florian Corzilius

# 13.17 carl-arith/numbers/adaption\_cln/operations.h File Reference

```
#include <carl-common/meta/platform.h>
#include "typetraits.h"
#include <cassert>
#include <limits>
```

### **Namespaces**

· carl

carl is the main namespace for the library.

#### **Functions**

- bool carl::is\_zero (const cln::cl\_l &n)
- bool carl::is\_zero (const cln::cl\_RA &n)
- bool carl::is\_one (const cln::cl\_l &n)
- bool carl::is\_one (const cln::cl\_RA &n)
- bool carl::is\_positive (const cln::cl\_l &n)
- bool carl::is\_positive (const cln::cl\_RA &n)
- bool carl::is\_negative (const cln::cl\_l &n)
- bool carl::is\_negative (const cln::cl\_RA &n)
- cln::cl\_l carl::get\_num (const cln::cl\_RA &n)

Extract the numerator from a fraction.

cln::cl\_l carl::get\_denom (const cln::cl\_RA &n)

Extract the denominator from a fraction.

• bool carl::is\_integer (const cln::cl\_l &)

Check if a number is integral.

bool carl::is\_integer (const cln::cl\_RA &n)

Check if a fraction is integral.

• std::size\_t carl::bitsize (const cln::cl\_l &n)

Get the bit size of the representation of a integer.

std::size\_t carl::bitsize (const cln::cl\_RA &n)

Get the bit size of the representation of a fraction.

• double carl::to\_double (const cln::cl\_RA &n)

Converts the given fraction to a double.

double carl::to\_double (const cln::cl\_l &n)

Converts the given integer to a double.

• template<typename Integer >

Integer carl::to\_int (const cln::cl\_l &n)

 $\bullet \ \ {\it template}{<} {\it typename Integer}>$ 

Integer carl::to\_int (const cln::cl\_RA &n)

- template<> sint carl::to\_int< sint > (const cln::cl\_l &n)
- template<> uint carl::to\_int< uint > (const cln::cl\_l &n)
- template<typename To , typename From >

To carl::from\_int (const From &n)

- template<> mpz\_class carl::from\_int (const uint &n)
- template<> mpz\_class carl::from\_int (const sint &n)
- template<> cln::cl\_l carl::to\_int< cln::cl\_l > (const cln::cl\_RA &n)

Convert a fraction to an integer.

```
    template<> sint carl::to_int< sint > (const cln::cl_RA &n)

    template<> uint carl::to_int< uint > (const cln::cl_RA &n)

    cln::cl_LF carl::to_lf (const cln::cl_RA &n)

      Convert a cln fraction to a cln long float.

    template<> cln::cl_RA carl::rationalize< cln::cl_RA > (double n)

    template<> cln::cl_RA carl::rationalize< cln::cl_RA > (float n)

    template<> cln::cl_RA carl::rationalize< cln::cl_RA > (int n)

    template<> cln::cl_RA carl::rationalize< cln::cl_RA > (uint n)

    template<> cln::cl_RA carl::rationalize< cln::cl_RA > (sint n)

    template<> cln::cl_l carl::parse< cln::cl_l > (const std::string &n)

    template<> bool carl::try_parse< cln::cl_l > (const std::string &n, cln::cl_l &res)

    template<> cln::cl_RA carl::parse< cln::cl_RA > (const std::string &n)

• template<> bool carl::try_parse< cln::cl_RA > (const std::string &n, cln::cl_RA &res)

    cln::cl_l carl::abs (const cln::cl_l &n)

      Get absolute value of an integer.

    cln::cl_RA carl::abs (const cln::cl_RA &n)

      Get absolute value of a fraction.

    cln::cl_l carl::round (const cln::cl_RA &n)

      Round a fraction to next integer.

    cln::cl_l carl::round (const cln::cl_l &n)

      Round an integer to next integer, that is do nothing.

    cln::cl_l carl::floor (const cln::cl_RA &n)

      Round down a fraction.

    cln::cl_l carl::floor (const cln::cl_l &n)

      Round down an integer.

    cln::cl_l carl::ceil (const cln::cl_RA &n)

      Round up a fraction.

    cln::cl_l carl::ceil (const cln::cl_l &n)

      Round up an integer.

    cln::cl_l carl::gcd (const cln::cl_l &a, const cln::cl_l &b)

      Calculate the greatest common divisor of two integers.

    cln::cl_l & carl::gcd_assign (cln::cl_l &a, const cln::cl_l &b)

      Calculate the greatest common divisor of two integers.

    void carl::divide (const cln::cl_l &dividend, const cln::cl_l &divisor, cln::cl_l &quotient, cln::cl_l &remainder)

    cln::cl_RA & carl::gcd_assign (cln::cl_RA &a, const cln::cl_RA &b)

      Calculate the greatest common divisor of two fractions.

    cln::cl_RA carl::gcd (const cln::cl_RA &a, const cln::cl_RA &b)

      Calculate the greatest common divisor of two fractions.

    cln::cl_l carl::lcm (const cln::cl_l &a, const cln::cl_l &b)

      Calculate the least common multiple of two integers.

    cln::cl_RA carl::lcm (const cln::cl_RA &a, const cln::cl_RA &b)

      Calculate the least common multiple of two fractions.

    template<> cln::cl_RA carl::pow (const cln::cl_RA &basis, std::size_t exp)

      Calculate the power of some fraction to some positive integer.

    cln::cl_RA carl::log (const cln::cl_RA &n)

    cln::cl_RA carl::log10 (const cln::cl_RA &n)

    cln::cl_RA carl::sin (const cln::cl_RA &n)
```

cln::cl\_RA carl::sqrt (const cln::cl\_RA &a)
 std::pair< cln::cl\_RA, cln::cl\_RA > carl::sqrt\_safe (const cln::cl\_RA &a)

bool carl::sqrt\_exact (const cln::cl\_RA &a, cln::cl\_RA &b)
 Calculate the square root of a fraction if possible.

cln::cl\_RA carl::cos (const cln::cl\_RA &n)

Calculate the square root of a fraction.

• std::pair< cln::cl\_RA, cln::cl\_RA > carl::sqrt\_fast (const cln::cl\_RA &a)

Compute square root in a fast but less precise way.

- std::pair< cln::cl\_RA, cln::cl\_RA > carl::root\_safe (const cln::cl\_RA &a, uint n)
- cln::cl\_l carl::mod (const cln::cl\_l &a, const cln::cl\_l &b)

Calculate the remainder of the integer division.

cln::cl\_RA carl::div (const cln::cl\_RA &a, const cln::cl\_RA &b)

Divide two fractions.

cln::cl\_l carl::div (const cln::cl\_l &a, const cln::cl\_l &b)

Divide two integers.

cln::cl\_RA & carl::div\_assign (cln::cl\_RA &a, const cln::cl\_RA &b)

Divide two fractions.

cln::cl\_l & carl::div\_assign (cln::cl\_l &a, const cln::cl\_l &b)

Divide two integers.

cln::cl\_RA carl::quotient (const cln::cl\_RA &a, const cln::cl\_RA &b)

Divide two fractions.

cln::cl\_l carl::quotient (const cln::cl\_l &a, const cln::cl\_l &b)

Divide two integers.

• cln::cl\_l carl::remainder (const cln::cl\_l &a, const cln::cl\_l &b)

Calculate the remainder of the integer division.

• cln::cl\_l carl::operator/ (const cln::cl\_l &a, const cln::cl\_l &b)

Divide two integers.

- cln::cl\_l carl::operator/ (const cln::cl\_l &lhs, const int &rhs)
- cln::cl\_RA carl::reciprocal (const cln::cl\_RA &a)
- std::string carl::toString (const cln::cl\_RA &\_number, bool \_infix=true)
- std::string carl::toString (const cln::cl\_l &\_number, bool \_infix=true)

### Variables

- static const cln::cl\_RA carl::ONE\_DIVIDED\_BY\_10\_TO\_THE\_POWER\_OF\_23 = cln::cl\_RA(1)/cln::expt(cln::cl← \_RA(10), 23)
- static const cln::cl\_RA carl::ONE\_DIVIDED\_BY\_10\_TO\_THE\_POWER\_OF\_52 = cln::cl\_RA(1)/cln::expt(cln::cl← \_RA(10), 52)

### 13.17.1 Detailed Description

Author

Gereon Kremer gereon.kremer@cs.rwth-aachen.de
Sebastian Junges

# Warning

This file should never be included directly but only via operations.h

# 13.18 carl-arith/numbers/adaption\_gmpxx/operations.h File Reference

```
#include <carl-common/meta/platform.h>
#include "include.h"
#include "typetraits.h"
#include <climits>
#include <cmath>
#include <cstddef>
#include <iostream>
#include <sstream>
#include <vector>
```

## **Namespaces**

carl

carl is the main namespace for the library.

#### **Functions**

- bool carl::is\_zero (const mpz\_class &n)
  - Informational functions.
- bool carl::is\_zero (const mpq\_class &n)
- bool carl::is\_one (const mpz\_class &n)
- bool carl::is\_one (const mpq\_class &n)
- bool carl::is\_positive (const mpz\_class &n)
- bool carl::is\_positive (const mpq\_class &n)
- bool carl::is\_negative (const mpz\_class &n)
- bool carl::is\_negative (const mpq\_class &n)
- mpz\_class carl::get\_num (const mpq\_class &n)
- mpz\_class carl::get\_num (const mpz\_class &n)
- mpz\_class carl::get\_denom (const mpq\_class &n)
- mpz\_class carl::get\_denom (const mpz\_class &n)
- bool carl::is\_integer (const mpq\_class &n)
- bool carl::is\_integer (const mpz\_class &)
- std::size\_t carl::bitsize (const mpz\_class &n)

Get the bit size of the representation of a integer.

• std::size\_t carl::bitsize (const mpq\_class &n)

Get the bit size of the representation of a fraction.

double carl::to\_double (const mpq\_class &n)

Conversion functions.

- double carl::to\_double (const mpz\_class &n)
- $\bullet \ \ \text{template}{<} \text{typename Integer} >$

Integer carl::to\_int (const mpz\_class &n)

- template<> sint carl::to\_int< sint > (const mpz\_class &n)
- template<> uint carl::to\_int< uint > (const mpz\_class &n)
- template<typename Integer >

Integer carl::to\_int (const mpq\_class &n)

template<> mpz\_class carl::to\_int< mpz\_class > (const mpq\_class &n)

Convert a fraction to an integer.

 template<typename To , typename From >
 To carl::from\_int (const From &n)

- template<> mpz\_class carl::from\_int (const uint &n)
- template<> mpz\_class carl::from\_int (const sint &n)
- template<> sint carl::to\_int< sint > (const mpq\_class &n)

Convert a fraction to an unsigned.

- template<> uint carl::to\_int< uint > (const mpg\_class &n)
- template<typename T >

T carl::rationalize (const PreventConversion < mpq\_class > &)

- template<> mpq\_class carl::rationalize< mpq\_class > (float n)
- template<> mpg\_class carl::rationalize< mpg\_class > (double n)
- template<> mpq\_class carl::rationalize< mpq\_class > (int n)
- template<> mpq\_class carl::rationalize< mpq\_class > (uint n)
- template <> mpq\_class carl::rationalize < mpq\_class > (sint n)
- template<> mpq\_class carl::rationalize< mpq\_class > (const PreventConversion< mpq\_class > &n)
- template<> mpz\_class carl::parse< mpz\_class > (const std::string &n)
- template<> bool carl::try\_parse< mpz\_class > (const std::string &n, mpz\_class &res)
- template<> mpq\_class carl::parse< mpq\_class > (const std::string &n)
- template<> bool carl::try\_parse< mpq\_class > (const std::string &n, mpq\_class &res)
- mpz\_class carl::abs (const mpz\_class &n)

#### Basic Operators.

- mpg\_class carl::abs (const mpg\_class &n)
- mpz\_class carl::round (const mpq\_class &n)
- mpz\_class carl::round (const mpz\_class &n)
- mpz\_class carl::floor (const mpg\_class &n)
- mpz\_class carl::floor (const mpz\_class &n)
- mpz\_class carl::ceil (const mpg\_class &n)
- mpz\_class carl::ceil (const mpz\_class &n)
- mpz\_class carl::gcd (const mpz\_class &a, const mpz\_class &b)
- mpz\_class carl::lcm (const mpz\_class &a, const mpz\_class &b)
- mpq\_class carl::gcd (const mpq\_class &a, const mpq\_class &b)
- mpz\_class & carl::gcd\_assign (mpz\_class &a, const mpz\_class &b)

Calculate the greatest common divisor of two integers.

mpq\_class & carl::gcd\_assign (mpq\_class &a, const mpq\_class &b)

Calculate the greatest common divisor of two integers.

- mpq\_class carl::lcm (const mpq\_class &a, const mpq\_class &b)
- mpq\_class carl::log (const mpq\_class &n)
- mpq\_class carl::log10 (const mpq\_class &n)
- mpq\_class carl::sin (const mpq\_class &n)
- mpq\_class carl::cos (const mpq\_class &n)
- template<> mpz\_class carl::pow (const mpz\_class &basis, std::size\_t exp)
- template<> mpq\_class carl::pow (const mpq\_class &basis, std::size\_t exp)
- bool carl::sqrt\_exact (const mpq\_class &a, mpq\_class &b)

Calculate the square root of a fraction if possible.

- mpq\_class carl::sqrt (const mpq\_class &a)
- std::pair< mpq\_class, mpq\_class > carl::sqrt\_safe (const mpq\_class &a)
- std::pair< mpq\_class, mpq\_class > carl::root\_safe (const mpq\_class &a, uint n)

Calculate the nth root of a fraction.

std::pair< mpq\_class, mpq\_class > carl::sqrt\_fast (const mpq\_class &a)

Compute square root in a fast but less precise way.

- mpz\_class carl::mod (const mpz\_class &n, const mpz\_class &m)
- mpz\_class carl::remainder (const mpz\_class &n, const mpz\_class &m)
- mpz\_class carl::quotient (const mpz\_class &n, const mpz\_class &d)
- mpz\_class carl::operator/ (const mpz\_class &n, const mpz\_class &d)
- mpq\_class carl::quotient (const mpq\_class &n, const mpq\_class &d)

- mpq\_class carl::operator/ (const mpq\_class &n, const mpq\_class &d)
- void carl::divide (const mpz\_class &dividend, const mpz\_class &divisor, mpz\_class &quotient, mpz\_class &remainder)
- mpq\_class carl::div (const mpq\_class &a, const mpq\_class &b)

Divide two fractions.

mpz\_class carl::div (const mpz\_class &a, const mpz\_class &b)

Divide two integers.

mpz\_class & carl::div\_assign (mpz\_class &a, const mpz\_class &b)

Divide two integers.

mpq\_class & carl::div\_assign (mpq\_class &a, const mpq\_class &b)

Divide two integers.

- mpq\_class carl::reciprocal (const mpq\_class &a)
- mpq\_class carl::operator\* (const mpq\_class &lhs, const mpq\_class &rhs)
- std::string carl::toString (const mpq\_class &\_number, bool \_infix=true)
- std::string carl::toString (const mpz\_class &\_number, bool \_infix=true)

### 13.18.1 Detailed Description

**Author** 

```
Gereon Kremer gereon.kremer@cs.rwth-aachen.de
Sebastian Junges
```

Warning

This file should never be included directly but only via operations.h

## 13.19 carl-arith/poly/umvpoly/functions/EZGCD.h File Reference

```
#include "../MultivariatePolynomial.h"
#include "../../numbers/PrimeFactory.h"
#include "GCD.h"
```

# **Data Structures**

class carl::EZGCD< Coeff, Ordering, Policies >

Extended Zassenhaus algorithm for multivariate GCD calculation.

# Namespaces

• carl

carl is the main namespace for the library.

# 13.19.1 Detailed Description

Author

Sebastian Junges

# 13.20 carl-arith/poly/umvpoly/Monomial.h File Reference

```
#include <carl-common/util/hash.h>
#include <carl-arith/numbers/numbers.h>
#include <carl-arith/core/CompareResult.h>
#include <carl-arith/core/Variable.h>
#include <carl-arith/core/Variables.h>
#include <carl-arith/core/VariablePool.h>
#include <algorithm>
#include <list>
#include <numeric>
#include <set>
#include <set>
#include <sstream>
#include <boost/intrusive/unordered_set.hpp>
```

#### **Data Structures**

· class carl::Monomial

The general-purpose monomials.

- · struct carl::hashLess
- · struct carl::hashEqual
- struct std::equal\_to< carl::Monomial::Arg >
- struct std::less< carl::Monomial::Arg >
- struct std::hash< carl::Monomial >

The template specialization of std::hash for carl::Monomial.

struct std::hash< carl::Monomial::Arg >

The template specialization of std::hash for a shared pointer of a carl::Monomial.

### **Namespaces**

• carl

carl is the main namespace for the library.

## **Typedefs**

using carl::exponent = std::size\_t
 Type of an exponent.

#### **Functions**

bool carl::operator== (const std::pair< Variable, std::size\_t > &p, Variable v)

Compare a pair of variable and exponent with a variable.

• std::ostream & carl::operator<< (std::ostream &os, const Monomial &rhs)

Streaming operator for Monomial.

std::ostream & carl::operator<< (std::ostream &os, const Monomial::Arg &rhs)</li>

Streaming operator for std::shared\_ptr< Monomial>.

- Monomial::Arg carl::pow (Variable v, std::size\_t exp)
- void carl::variables (const Monomial &m, carlVariables &vars)

Add the variables of the given monomial to the variables.

### **Comparison operators**

- bool carl::operator== (const Monomial &lhs, const Monomial &rhs)
  - Compares two arguments where one is a Monomial and the other is either a monomial or a variable.
- bool carl::operator== (const Monomial::Arg &lhs, const Monomial::Arg &rhs)
  - Compares two arguments where one is a Monomial and the other is either a monomial or a variable.
- bool carl::operator== (const Monomial::Arg &lhs, Variable rhs)
  - Compares two arguments where one is a Monomial and the other is either a monomial or a variable.
- bool carl::operator== (Variable lhs, const Monomial::Arg &rhs)
  - Compares two arguments where one is a Monomial and the other is either a monomial or a variable.
- bool carl::operator!= (const Monomial::Arg &lhs, const Monomial::Arg &rhs)
  - Compares two arguments where one is a Monomial and the other is either a monomial or a variable.
- bool carl::operator!= (const Monomial::Arg &lhs, Variable rhs)
  - Compares two arguments where one is a Monomial and the other is either a monomial or a variable.
- bool carl::operator!= (Variable lhs, const Monomial::Arg &rhs)
  - Compares two arguments where one is a Monomial and the other is either a monomial or a variable.
- bool carl::operator < (const Monomial::Arg &lhs, const Monomial::Arg &rhs)
  - Compares two arguments where one is a Monomial and the other is either a monomial or a variable.
- bool carl::operator< (const Monomial::Arg &lhs, Variable rhs)</li>
  - Compares two arguments where one is a Monomial and the other is either a monomial or a variable.
- bool carl::operator< (Variable lhs, const Monomial::Arg &rhs)</li>
  - Compares two arguments where one is a Monomial and the other is either a monomial or a variable.
- bool carl::operator<= (const Monomial::Arg &lhs, const Monomial::Arg &rhs)
  - Compares two arguments where one is a Monomial and the other is either a monomial or a variable.
- bool carl::operator<= (const Monomial::Arg &lhs, Variable rhs)
  - Compares two arguments where one is a Monomial and the other is either a monomial or a variable.
- bool carl::operator<= (Variable lhs, const Monomial::Arg &rhs)</li>
  - Compares two arguments where one is a Monomial and the other is either a monomial or a variable.
- bool carl::operator> (const Monomial::Arg &lhs, const Monomial::Arg &rhs)
  - Compares two arguments where one is a Monomial and the other is either a monomial or a variable.
- bool carl::operator> (const Monomial::Arg &lhs, Variable rhs)
  - Compares two arguments where one is a Monomial and the other is either a monomial or a variable.
- bool carl::operator> (Variable lhs, const Monomial::Arg &rhs)
  - Compares two arguments where one is a Monomial and the other is either a monomial or a variable.
- bool carl::operator>= (const Monomial::Arg &lhs, const Monomial::Arg &rhs)
  - Compares two arguments where one is a Monomial and the other is either a monomial or a variable.
- bool carl::operator>= (const Monomial::Arg &lhs, Variable rhs)
  - Compares two arguments where one is a Monomial and the other is either a monomial or a variable.
- bool carl::operator>= (Variable lhs, const Monomial::Arg &rhs)
  - Compares two arguments where one is a Monomial and the other is either a monomial or a variable.

## **Multiplication operators**

- Monomial::Arg carl::operator\* (const Monomial::Arg &lhs, const Monomial::Arg &rhs)

  Perform a multiplication involving a monomial.
- Monomial::Arg carl::operator\* (const Monomial::Arg &lhs, Variable rhs)
  - Perform a multiplication involving a monomial.
- Monomial::Arg carl::operator\* (Variable lhs, const Monomial::Arg &rhs)
  - Perform a multiplication involving a monomial.
- Monomial::Arg carl::operator\* (Variable lhs, Variable rhs)
  - Perform a multiplication involving a monomial.

### 13.20.1 Detailed Description

**Author** 

Sebastian Junges

Florian Corzilius

# 13.21 carl-arith/poly/umvpoly/MonomialOrdering.h File Reference

```
#include <carl-arith/core/CompareResult.h>
#include "Monomial.h"
#include "Term.h"
```

#### **Data Structures**

struct carl::MonomialComparator< f, degreeOrdered >
 A class for term orderings.

### **Namespaces**

carl

carl is the main namespace for the library.

## **Typedefs**

- using carl::MonomialOrderingFunction = CompareResult(\*)(const Monomial::Arg &, const Monomial::Arg &)
- using carl::LexOrdering = MonomialComparator< Monomial::compareLexical, false >
- using carl::GrLexOrdering = MonomialComparator< Monomial::compareGradedLexical, true >

## 13.22 carl-arith/poly/umvpoly/MultivariatePolynomial.h File Reference

```
#include <algorithm>
#include <numeric>
#include <memory>
#include <type_traits>
#include <vector>
#include "MultivariatePolynomialPolicy.h"
#include "Term.h"
#include "TermAdditionManager.h"
#include "../typetraits.h"
#include "MultivariatePolynomial_operators.h"
#include "MultivariatePolynomial_tpp"
```

#### **Data Structures**

- class carl::MultivariatePolynomial< Coeff, Ordering, Policies >
  - The general-purpose multivariate polynomial class.
- struct carl::is\_polynomial\_type< carl::MultivariatePolynomial< T, O, P >>
- struct carl::UnderlyingNumberType< MultivariatePolynomial< C, O, P > >

States that UnderlyingNumberType of MultivariatePolynomial<C,O,P> is UnderlyingNumberType<C>::type.

struct std::hash< carl::MultivariatePolynomial< C, O, P >>

Specialization of std::hash for MultivariatePolynomial.

## **Namespaces**

· carl

carl is the main namespace for the library.

#### **Functions**

```
    template < typename C , typename O , typename P >
bool carl::is_one (const MultivariatePolynomial < C, O, P > &p)
```

```
    template<typename C, typename O, typename P >
        bool carl::is_zero (const MultivariatePolynomial< C, O, P > &p)
```

- template<typename C, typename O, typename P>
   std::pair< MultivariatePolynomial< C, O, P>, MultivariatePolynomial< C, O, P>> carl::lazyDiv (const MultivariatePolynomial< C, O, P> &\_polyA, const MultivariatePolynomial< C, O, P> &\_polyB)
- template < typename C , typename O , typename P >
   std::ostream & carl::operator << (std::ostream &os, const MultivariatePolynomial < C, O, P > &rhs)
   Streaming operator for multivariate polynomials.
- template<typename Coeff, typename Ordering, typename Policies >
   void carl::variables (const MultivariatePolynomial < Coeff, Ordering, Policies > &p, carlVariables &vars)
   Add the variables of the given polynomial to the variables.

### **Division operators**

template<typename C, typename O, typename P, Enablelf< carl::is\_number\_type< C>> = dummy>
 MultivariatePolynomial< C, O, P > carl::operator/ (const MultivariatePolynomial< C, O, P > &lhs, const C &rhs)

Perform a division involving a polynomial.

#### 13.22.1 Detailed Description

**Author** 

Sebastian Junges

Florian Corzilius

# 13.23 carl-arith/poly/umvpoly/MultivariatePolynomial.tpp File Reference

```
#include "MultivariatePolynomial.h"
#include "Term.h"
#include "UnivariatePolynomial.h"
#include <carl-logging/carl-logging.h>
#include <carl-arith/numbers/numbers.h>
#include <algorithm>
#include <memory>
#include <mutex>
#include <list>
#include <type_traits>
```

## Namespaces

carl

carl is the main namespace for the library.

#### **Functions**

- template<typename C , typename O , typename P > MultivariatePolynomial < C, O, P > carl::operator+ (const UnivariatePolynomial < C > &, const Multivariate  $\leftarrow$  Polynomial < C, O, P > &)
- template<typename C , typename O , typename P > MultivariatePolynomial < C, O, P > carl::operator+ (const MultivariatePolynomial < C, O, P > &, const UnivariatePolynomial < C > &)
- template<typename C, typename O, typename P>
   MultivariatePolynomial< C, O, P > carl::operator+ (const UnivariatePolynomial< MultivariatePolynomial< C
   >> &, const MultivariatePolynomial< C, O, P > &)
- template<typename C , typename O , typename P > MultivariatePolynomial < C, O, P > carl::operator+ (const MultivariatePolynomial < C, O, P > &, const UnivariatePolynomial < MultivariatePolynomial < C >> &)
- template<typename C , typename O , typename P > const MultivariatePolynomial< C, O, P > carl::operator\* (const UnivariatePolynomial< C > &, const MultivariatePolynomial< C, O, P > &)
- template<typename C, typename O, typename P >
   const MultivariatePolynomial < C, O, P > carl::operator\* (const MultivariatePolynomial < C, O, P > &lhs,
   const UnivariatePolynomial < C > &rhs)
- template<typename C, typename O, typename P>
   MultivariatePolynomial< C, O, P > carl::operator/ (const MultivariatePolynomial< C, O, P > &lhs, unsigned long rhs)

#### 13.23.1 Detailed Description

**Author** 

Sebastian Junges

# 13.24 carl-arith/poly/umvpoly/MultivariatePolynomialPolicy.h File Reference

```
#include "MonomialOrdering.h"
#include "MultivariatePolynomialAdaptors/PolynomialAllocator.h"
#include "MultivariatePolynomialAdaptors/ReasonsAdaptor.h"
```

## **Data Structures**

struct carl::StdMultivariatePolynomialPolicies < ReasonsAdaptor, Allocator >
 The default policy for polynomials.

### Namespaces

carl

carl is the main namespace for the library.

## 13.24.1 Detailed Description

**Author** 

Sebastian Junges

# 13.25 carl-arith/poly/umvpoly/UnivariatePolynomial.h File Reference

```
#include <carl-arith/numbers/numbers.h>
#include <carl-common/meta/SFINAE.h>
#include <carl-common/util/hash.h>
#include <carl-arith/core/Sign.h>
#include <functional>
#include <list>
#include <map>
#include <memory>
#include <vector>
#include "../typetraits.h"
#include "MultivariatePolynomial.h"
#include "UnivariatePolynomial.tpp"
```

#### **Data Structures**

class carl::UnivariatePolynomial< Coefficient >

This class represents a univariate polynomial with coefficients of an arbitrary type.

- struct carl::is\_polynomial\_type< carl::UnivariatePolynomial< T >>
- $\bullet \ \, \textbf{struct carl::} \textbf{UnderlyingNumberType} < \textbf{UnivariatePolynomial} < \textbf{C} > > \\$

 $States\ that\ Underlying Number Type\ of\ Univariate Polynomial < T>\ is\ Underlying Number Type < C>:: type.$ 

struct std::hash< carl::UnivariatePolynomial< Coefficient >>

Specialization of std::hash for univariate polynomials.

struct std::less< carl::UnivariatePolynomial< Coefficient >>

Specialization of std::less for univariate polynomials.

## **Namespaces**

• carl

carl is the main namespace for the library.

## **Typedefs**

```
    template < typename Coefficient >
        using carl::UnivariatePolynomialPtr = std::shared_ptr < UnivariatePolynomial < Coefficient > >
```

```
    template < typename Coefficient >
        using carl::FactorMap = std::map < UnivariatePolynomial < Coefficient >, uint >
```

### **Enumerations**

enum class carl::PolynomialComparisonOrder { carl::CauchyBound , carl::LowDegree , carl::Memory , carl::Default = LowDegree }

#### **Functions**

```
    template<typename Coefficient >
        bool carl::is_zero (const UnivariatePolynomial< Coefficient > &p)
        Checks if the polynomial is equal to zero.
    template<typename Coefficient >
        bool carl::is_one (const UnivariatePolynomial< Coefficient > &p)
        Checks if the polynomial is equal to one.
    template<typename Coeff >
        void carl::variables (const UnivariatePolynomial< Coeff > &p, carlVariables &vars)
        Add the variables of the given polynomial to the variables.
```

### 13.25.1 Detailed Description

Author

Sebastian Junges

# 13.26 carl-extpolys/ConstraintOperations.h File Reference

```
#include <iterator>
#include <carl-formula/arithmetic/Constraint.h>
#include "RationalFunction.h"
```

## **Namespaces**

· carl

carl is the main namespace for the library.

· carl::constraints

### **Functions**

template < typename PolType, bool AS, typename InIt, typename InsertIt >
 void carl::constraints::toPolynomialConstraints (InIt start, InIt end, InsertIt out)
 Converts Constraint < RationalFunction < Poly >> to Constraint < Poly >

## 13.26.1 Detailed Description

**Author** 

Sebastian Junges