# **Statistical Programming Languages**

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```
library("dplyr")
```

Due to missing insolvencies in 1996 and missing data from 2003 onwards we choose data from 1997-2002

```
data1 = filter(data, JAHR>= 1997 & JAHR<=2002)

#Extract the industry class of companies
data1$Ind.Klasse = substring(data1$VAR26, 1, 2)</pre>
```

As we are only interested in companies with high percentage in the industry composition we choose only companies belonging to the following sectors (according to German Classification of Economic Activities Standards (WZ 1993)):

- 1. Manufacturing (Man)
- 2. Wholesale and Retail (WaR)
- 3. Construction (Con)
- 4. Real Estate (RE)



```
Man = filter (data1, Ind.Klasse %in% as.character
    (15:37)
  Man$Ind.Klasse = "Man"
  WaR = filter (data1, Ind.Klasse %in% as.character
    (50:52)
WaR$Ind.Klasse = "WaR"
  Con = filter (data1, Ind.Klasse == "45")
  Con$Ind.Klasse = "Con"
10 RE = filter (data1, Ind.Klasse %in% as.character
    (70:74))
11 RE$Ind.Klasse = "RE"
```

Remove data and data1 and bind the above datasets to get one dataset containing only companies of interest:

```
rm(data, data1)

data = rbind(Man, WaR, Con, RE)
```

Furthermore we choose only companies whose total assets (VAR26) are in the range  $10^5-10^8$ .

```
data = data[data$VAR6 >= 10^5 & data$VAR6 <= 10^8,]
```



Eliminate observations with 0 value for the following variables used as denominators in calculation of financial ratios to be used in classification:

- □ cash (VAR1)
- inventories (VAR2)
- current liabilities (VAR12)
- • total assets − intangible assets − cash − lands and buildings
   (VAR6 − VAR5 − VAR1 − VAR8)
- interest expenses (VAR19)



```
data_clean = data %>% filter(VAR6 != 0,
VAR16 != 0,
VAR1 != 0,
VAR2 != 0,
VAR12 != 0,
VAR12 + VAR13 != 0,
VAR6 - VAR5 - VAR1 -
VAR8 != 0,
VAR19 != 0)
```

Show table with number of solvent/insolvent companies:

## **Data Preparation: Results**

Year	Solvent	Insolvent
1997	1084	126
1998	1175	114
1999	1277	147
2000	1592	135
2001	1920	132
2002	2543	129

#### Add columns with financial ratios:

```
test_data = data_clean %>%
    mutate(
2
       # NetIncome/TotalAssets
      x1 = VAR22/VAR6
      # NetIncome/TotalSales
      x2 = VAR22/VAR16,
      # OperatingIncome/TotalAssets
      x3 = VAR21/VAR6,
       # OperatingIncome/TotalSales
      x4 = VAR21/VAR16,
10
       # EBIT/TotalAssets
11
      x5 = VAR20/VAR6,
12
```

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Variable	Definition
x1	Net income/total assets
x2	Net income/total sales
<b>x</b> 3	Operating income/total assets
x4	Operating income/total sales
x5	Earnings before interest and tax/total assets

Variable	Definition
x6	Earnings before interest, Tax, Depreciation and amortization/t
x7	Earnings before interest and tax/total sales
x8	Own funds/total assets
x9	Ownfunds—intangibleassets
<b>A</b> 9	totalassets – intangibleassets – cashandcashequivalents – landsandbuild
x10	Current liabilities/total assets

Variable	Definition
×11	(Current liabilities - cash and cash equivalents)/total assets
x12	Total liabilities/total assets
x13	Debt/total assets
x14	Earnings before interest and tax/interest expense
x15	Cash and cash equivalents/total assets
x16	Cash and cash equivalents/current liabilities
x17	(Cash and cash equivalents - inventories)/current liabilities
x18	Current assets/current liabilities
x19	(Current assets - current liabilities)/total assets
×20	Current liabilities/total liabilities

Variable	Definition
x21	Total assets/total sales
x22	Inventories/total sales
x23	Accounts receivable/total sales
x24	Accounts payable/total sales
x25	log(total assets)
x26	Increase (decrease) in inventories/inventories
x27	Increase (decrease) in liabilities/total Liabilities
×28	Increase (decrease) in cash flow/cash and cash equivalents

Prepare dataframe containing relative variables: ID, T2, JAHR and the financial ratios will be used for classification.

#### Result:

```
Solvent Insolvent
9591 783
```

Which is almost the same result as in Zhang, Hardle (2010)



Intended Outcome: Function that takes labels and predictions as inputs and returns the following Measures, Plots and Tables:

- Confusion Matrix
  - true positives
  - true negatives
  - false positives
  - false negatives
- □ ROC + AUC
- Accuracy
- Precision
- Sensitivity



#### Get predictions from fitted probabilities:

Get TP, TN, FP, FN via a contingency table. Set factor labels to avoid pitfalls if all predictions are the same.

```
evaluate_predictions = function(labels, predictions,
     verbose = FALSE){
    ct = table(factor(x = labels, levels = c(0, 1)),
               factor(x = predictions, levels = c(0,1)
                 ))
    if(any(dim(ct) != 2)) stop("Labels or Predictions
      contain more than 2 classes.")
    TN = ct[1, 1]
    TP = ct[2, 2]
    FP = ct[1, 2]
    FN = ct[2, 1]
10
```

#### Calculate Measures:

. . .

```
reports = list(
sensitivity = TP / (TP + FN),
specificity = TN / (FP + TN),
precision = TP / (TP + FP),
accuracy = (TP + TN) / sum(ct))

if(verbose) print(data.frame(reports), digits = 3)
return(reports)
}
```

#### Calculate Values for ROC:

```
# Calculate ROC:
sensitivities = reports[names(reports) == "
sensitivity"]
specificities = reports[names(reports) == "
specificity"]
```

#### Calculate AUC:

Approximate area by two sets of rectangles. One set systematically overestimates the area, the other systematically underestimates the area. Therefore take the average of both.

```
get_auc = function(x, y){
   abs(sum(diff(x) * (head(y, -1) + tail(y, -1)))/
        2)}
auc = get_auc(1-specificities, sensitivities)
Progress Report WT 17/18
```

Choose optimal threshold, specificity, sensitivity, predictions and confusion matrix:

```
opt_ind = which.max(sensitivities + specificities
 - 1)
opt_sensitivity = sensitivities[opt_ind]
opt_specificity = specificities[opt_ind]
opt_threshold = seq(from = 0, to = 1, by = 0.0001)
 [opt_ind]
opt_predictions = get_prediction(
  fitted_probs = fitted_probs,
  threshold = opt_threshold)
ct = table(factor(x = labels, levels = c(0, 1)),
           factor(x = opt_predictions, levels = c
             (0,1))
```

#### Plot ROC-Curve

```
plot(x = 1 - specificities,
    y = sensitivities,
    main = "ROC-Curve",
    xlab = "False Positive Rate (1 - specificity)
    ",
    ylab = "True Positive Rate (sensitivity)",
    xlim = c(0, 1),
    ylim = c(0, 1),
    asp = TRUE,
    type = "l")
```

#### Return the Values:

```
return(list(sensitivity = opt_sensitivity,
specificity = opt_specificity,
threshold = opt_threshold,
predictions = opt_predictions,
auc = auc,
contingency_table = ct))
```

Cart - 3-1

### **Build the Cart Model**

#### Create a subset to train and evaluate the model:



### Cart

Since insolvent firms are underrepresented we need to oversample them in to balance the dataset.

```
#create a subset from training dataset, which only
includes insolvent firms
training_insolvent=training[training$X.T2.==1,]
#create a subset, which only includes solvent firms
training_solvent_full=training[training$X.T2.==0,]
```



Create a matrix for performance evaluation of binary classification, which will be filled with true positive/negative rates:

```
conf_mat_true_cart=0
```

Create a matrix which will store the sum of all prediction outcomes:

```
conf_mat_sum_cart=0
```



#### Cart

For each bootstrap sample use all insolvent firms in the training set and randomly sample the same number of solvent firms from the training set.

. . .



#### Cart

```
# training the model:
    names(training_complete)[1]="status"
    modfit=train(status~.,method="rpart",data=training
      _complete)
  # Validation/Test phase
    pred.cart=predict(modfit,newdata=validierung_cart)
  # Accuracy and misclassication
    conf_mat_cart=table(pred.cart, validierung_cart$
      status)
  # fill the matrix with true positive and true
    negative rates
    conf_mat_true_cart=sum(conf_mat_true_cart,conf_mat
      _cart[1,1],conf_mat_cart[2,2],na.rm=T)
10 # store total sum of predicted outcomes
    conf_mat_sum_cart=sum(conf_mat_sum_cart+sum(conf_
11
      mat_cart,na.rm=T),na.rm=T)}
```

### Cart

### Calculate accuracy rate

```
AR_cart=conf_mat_true_cart/conf_mat_sum_cart
#AR_cart: ~68%
```



Random Forest — 4-1

## Random Forest: Training the model

```
names(training_complete)[1]="status"
mod_forest_I=randomForest(as.factor(status)~.,
data=training_complete,
importance=T,
ntree = 2000,
maxnodes= 100,
norm.votes = F)
```

Random Forest — 4-2

### Validation- and Test-Phase

#### Calculate accuracy rate

```
conf_mat_true_rf=sum(conf_mat_true_rf,conf_mat_rf
[1,1],conf_mat_rf[2,2],na.rm=T)
```



Logit — 5-1

## Logit

#### Create a subset train- and testsets:

.JAHR.>=2000)

Logit — 5-2

## Logit

#### Train the model:



## **Theory**

At starting point a a (possibly multivariate) function f(x) decays fastest if one follows the negative gradient of f evaluated at a, thus we can update a by:

$$a_{n+1} = a + \eta \cdot \nabla f(a) \tag{1}$$

where  $\eta$  describes the learning-rate.

# Implementation in R - Arguments

```
gradientDescentMinimizer = function(
  obj, n_pars, epsilon_step = 0.001,
  max_iter = 10, precision = 1e-6,
  learn = 0.5, verbose = FALSE,
  report_freq = 100){
```

## Implementation in R - Gradient

Approximate Gradient by taking finite differences:

```
get_gradient = function(x, d = n_pars,
1
                             objective = obj,
2
                             epsilon = epsilon_step){
      init = matrix(data = x, nrow = d, ncol = d,
        byrow = TRUE)
      steps = init + diag(x = epsilon, ncol = d, nrow
        = d
      f_steps = apply(steps, 1, objective)
      f_comp = apply(init, 1, objective)
      D = (f_steps - f_comp) / epsilon
      D_{trimmed} = ifelse(abs(D) \le 100, abs(D), 100) *
         sign(D)
      return(D_trimmed)}
10
```

# **Choose Starting Point**

Try different Points and chose the one that provides the lowest value:

# **Update Starting Point** a

```
while(i <= max_iter & any(abs(gradient) >=
     precision)){
     if(i %% report_freq == 0 & verbose) {
       cat("\nStep:\t\t", i,
           "\nx:\t\t", a,
           "\ngradient:\t", gradient,
           "\nlearn:\t", learn_rates[i],
           "\n----")}
     i = i + 1
     a = a - learn_rates[i] * gradient
10
     gradient = get_gradient(a)
11
```

# Example

Visualize the path of a one-dimensional Gradient-Descent:

Continuously Differentiable Objective Function:

$$f(x) = \frac{x^4}{10000} + 2 \quad (2)$$



