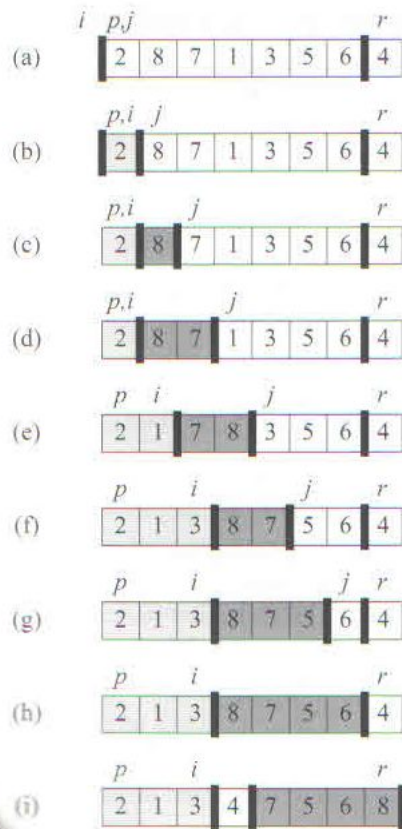


Quicksort



The following procedure implements quicksort.

QUICKSORT(A, p, r)

```

1  if  $p < r$ 
2     $q = \text{PARTITION}(A, p, r)$ 
3    QUICKSORT( $A, p, q - 1$ )
4    QUICKSORT( $A, q + 1, r$ )

```

To sort an entire array A , the initial call is QUICKSORT($A, 1, A.length$).

Partitioning the array

The key to the algorithm is the PARTITION procedure, which rearranges the subarray $A[p..r]$ in place.

PARTITION(A, p, r)

```

1   $x = A[r]$ 
2   $i = p - 1$ 
3  for  $j = p$  to  $r - 1$ 
4    if  $A[j] \leq x$ 
5       $i = i + 1$ 
6      exchange  $A[i]$  with  $A[j]$ 
7  exchange  $A[i + 1]$  with  $A[r]$ 
8  return  $i + 1$ 

```

CountingSort

COUNTING-SORT(A, B, k)

```

1  let  $C[0..k]$  be a new array
2  for  $i = 0$  to  $k$ 
3       $C[i] = 0$ 
4  for  $j = 1$  to  $A.length$ 
5       $C[A[j]] = C[A[j]] + 1$ 
6  //  $C[i]$  now contains the number of elements equal to  $i$ .
7  for  $i = 1$  to  $k$ 
8       $C[i] = C[i] + C[i - 1]$ 
9  //  $C[i]$  now contains the number of elements less than or equal to  $i$ .
10 for  $j = A.length$  downto 1
11      $B[C[A[j]]] = A[j]$ 
12      $C[A[j]] = C[A[j]] - 1$ 

```

