Statistical Computing

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March 2023



Statistical Computing: What will we do?

Chapters

- 1. R in Action
- 2. Statistical Inference
- 3. Linear Models
- 4. Model Selection and Validation
- 5. Trees
- 6. Neural Nets

Remarks

- Chapters 3 to 6: Statistical ML in Action
- Two weeks per chapter
- Exercises at end of chapter notes

Model Selection and Validation

Two Questions

- or provent overlitting (more parans - smore overfit

- "How good is our model?"
- "Which model to choose among alternatives?"

Problem and solution

- "In-sample" performance is biased
 Overfitting should not be
- rewarded
- Use data splitting to get fair results

Notation

function of it

- ► Total loss $Q(f, D) = \sum_{(y_i, \mathbf{x}_i) \in D} L(y_i, f(\mathbf{x}_i))$
- Average loss $\bar{Q}(f,D) = Q(f,D)/|D|$
- Performance measure or evaluation metric <</p> S(f,D) of interest, often $S=\bar{Q}$ or a

-> S wight be Va to consure the dimension 4/15

Outline

- Nearest-Neighbor
- Simple Validation
- Cross-Validation
- ► Test Data and Final Workflow
- Excursion: SQL and Spark

Excursion: k-Nearest-Neighbor (k-NN)

"Blade box model"

- Alternative to linear model
- ► How does it work?
- ► Classification and regression
- Standardization?

Stoler.

Example

solud coverieles look at objects with similar covariales table average response variable

covariates, measure flu distance with endidion dist.

Categorys ordinal measuring clarity is around - 2

Cantons are not 3

- during variables

Simple Validation

- In-sample, 1-NN would win any comparison!?
- ▶ Split data into training and validation sets D_{train} and D_{valid} , e.g., 80%/20%
- ▶ Use performance $S(\hat{f}, D_{\text{valid}})$ on validation set to make decisions (choose models, choose parameters like k)
- Measure amount of overfitting/optimism by

$$S(\hat{f}, D_{\mathsf{valid}}) - S(\hat{f}, D_{\mathsf{train}})$$

Example

padages

coret (R6)

MLR3

tidymoduls very strange

K-fold Cross-Validation (CV)

Simple validation is neither economic nor robust, except for large data

Algorithm

- Not the K-NN 1. Split the data into K pieces $D = \{D_1, \ldots, D_K\}$
- 2. Set aside one of the pieces (D_k) for validation
- 3. Fit model \hat{f}_k on $D \setminus D_k$
- 4. Calculate performance $\hat{\xi}_{\vec{k}} = S(\hat{f}_k, D_k)$

called "folds". Typical values for K?

- 5. Repeat Steps 2-4 for each k
- 6. Calculate CV performance $\hat{S}_{CV} = \frac{1}{K} \sum_{k=1}^{K} \hat{S}_k$

Remarks Remarks

- How to choose and fit best/final model?
- What means «best»?
- ► Stability of results? adouble
- Repeated CV?

Example

repeat CV with different seeds,

Hyperparameter Tuning

- Choosing k in k-NN is example of "hyperparameter tuning"
- ► Algorithms with more than 1 hyperparameter? 🔀 💪 💪 💪 🗸
- ► Grid Search CV good of hyp- params
- Randomized Search CV ; Ltoo big grit

Test Data and Final Workflow

Problematic consequence of model tuning?

- Overfitting on validation data or on CV!
- ▶ Performance of final model? → Test data

Workflow A simple validation

- 1. Split data into train/valid/test, e.g., by ratios 60%/20%/20%
- 2. Train different models on training data and assess performance on validation data. Choose best model, re-train on training + validation data, and call it "final model" (Simplification?) or anticharing
- 3. Assess performance of final model on test data

Workflow B coss validation

- 1. Split data into train/test, e.g., by ratios 80%/20%.
- 2. Evaluate and tune different models by K-fold CV on training data. Choose best model, re-train on full training data
 - Assess performance of final model on test data

Example of Workflow B

are con include the feet data When test data not necessary? to fit the model

Ridge Regression

- Example of penalized regression
- Model equation similar to usual linear regression

$$\mathbb{E}(Y \mid \mathbf{x}) = f(\mathbf{x}) = \beta_0 + \beta_1 x^{(1)} + \dots + \beta_p x^{(p)}$$

But with penalized least-squares objective

zed least-squares objective
$$Q(f, D_{\text{train}}) = \sum_{(y_i, \mathbf{x}_i) \in D_{\text{train}}} (y_i - f(\mathbf{x}_i))^2 + \lambda \sum_{j=1}^p \beta_j^2$$

- L2 penalty pulls coefficients slightly towards 0, fighting overfitting
- $\lambda_{\rm opt} \geq 0$ with best (cross-)validation result \rightarrow use to fit final model
- Example renalised Scally (Spendly alss (1))

 Example renalised (1)

 Scally (1)

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 for most pedrages

Using Independent Partitions is Essential

Random splits much Indep. putitions

Grouped splits

rows from different climbs
overly optimistic it have leakage Time-Series splits
or data from some client different copic
in train and test data
availed by random split by groups!

Stratified splits

in binoy response: less 1's the 0's sheap the distribution in splits:

Excursion: SQL and Spark

Data science is 80% preparing data, 20% complaining about preparing data.

Typical preprocessing steps?

Good moment to learn

- data structure
- meaning of columns
- sources of bias

How to do preprocessing?

 $\mathsf{Data} = \mathsf{files} \; \mathsf{on} \; \mathsf{disk} \; \mathsf{or} \; \mathsf{tables} \; \mathsf{in} \; \mathsf{database}$

- ightharpoonup If small ightharpoonup R/Python
- ▶ If large? \rightarrow Database Management System (DBMS) or Spark
- Communication via SQL

SQL

Structured Query Language

- Pronounced?
- Important in data science
- ► In DBMS or R/Python
- ► ISO norm ↔ dialects
- SQL queries

Learn SQL with examples

- Diamonds (from memory)
- ► Taxi (from Parquet)

DuckDB (since 2018)

- ► In-process, open-source DBMS
- Easy to install in R/Python
- No dependencies (Java etc.)
- Fast
- Out-of-core capabilities

Apache Spark

- Distributed, open-source cluster computing system for big data
- Apache project since 2013
- Heavily used in industry
- Written in Scala
- Contains SQL engine
- Can be used from R/Python

Examples

- Diamonds (from memory)
- ► Taxi (from Parquet)