



Cluster Analysis

—Partitioning Methods—

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Cluster Analysis



- ◉ What is Cluster Analysis?
- ◉ Types of Data in Cluster Analysis
- ◉ A Categorization of Major Clustering Methods
- ◉ **Partitioning Methods**
- ◉ Hierarchical Methods
- ◉ Density-Based Methods
- ◉ Grid-Based Methods
- ◉ Model-Based Clustering Methods
- ◉ Outlier Analysis
- 2 ◉ **Summary**



Partitioning Algorithms: Basic Concept



- ◉ **Partitioning method:** Construct a partition of a database D of n objects into a set of k clusters
- ◉ Given a k , find a partition of k clusters that optimizes the chosen partitioning criterion
 - ◆ Global optimal: exhaustively enumerate all partitions
 - ◆ Heuristic methods: k -means and k -medoids (K-中心点) algorithms
 - ◆ k -means (MacQueen' 67): Each cluster is represented by the center of the cluster
 - ◆ k -medoids or PAM (Partition around medoids) (Kaufman & Rousseeuw' 87): Each cluster is represented by one of the objects in the cluster

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The K-Means Clustering Method



- ◉ Given into k nonempty subsets
 - ◆ Compute seed k , the k -means algorithm is implemented in four steps:
 - ◆ Partition objects points as the centroids of the clusters of the current partition (the centroid is the center, i.e., *mean point*, of the cluster)
 - ◆ Assign each object to the cluster with the nearest seed point
 - ◆ Go back to Step 2, stop when no more new assignment

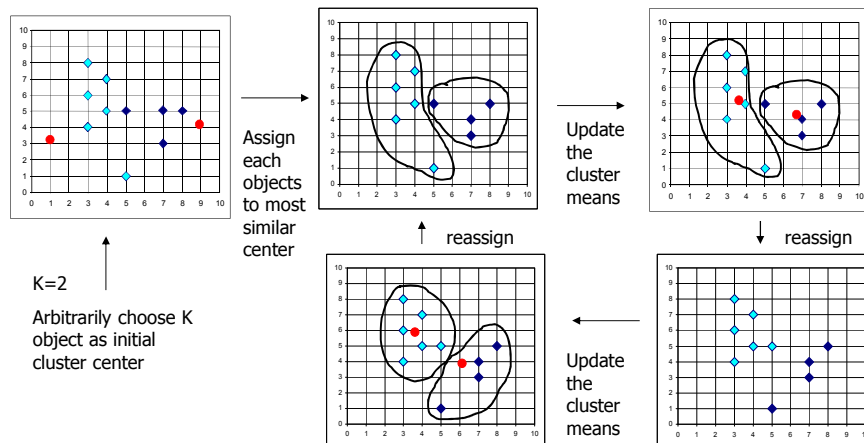
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The K-Means Clustering Method



Example



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Comments on the K-Means Method



- ◉ **Strength:** *Relatively efficient*. $O(tkn)$, where n is # objects, k is # clusters, and t is # iterations(迭代). Normally, $k, t \ll n$.
 - ◆ Comparing: PAM: $O(k(n-k)^2)$, CLARA: $O(ks^2 + k(n-k))$
- ◉ **Comment:** Often terminates at a *local optimum*. The *global optimum* may be found using techniques such as: *deterministic annealing* (模拟退火) and *genetic algorithms* (遗传算法)
- ◉ **Weakness**
 - ◆ Applicable only when *mean* is defined, then what about categorical data?
 - ◆ Need to specify k , the *number of clusters*, in advance
 - ◆ Unable to handle noisy data and *outliers*
 - ◆ Not suitable to discover clusters with *non-convex shapes*

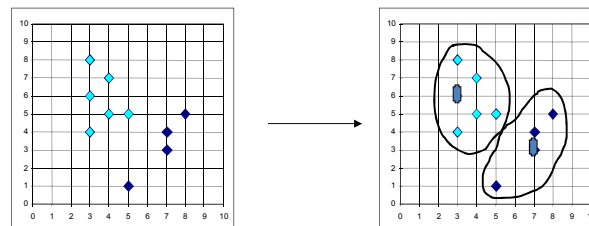
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The K-Medoids Clustering Method



- ◉ The k-means algorithm is sensitive to outliers !
 - ◆ Since an object with an extremely large value may substantially distort the distribution of the data.
- ◉ K-Medoids: Instead of taking the mean value of the object in a cluster as a reference point, medoids can be used, which is the most centrally located object in a cluster.



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The K-Medoids Clustering Method (K中心聚类)

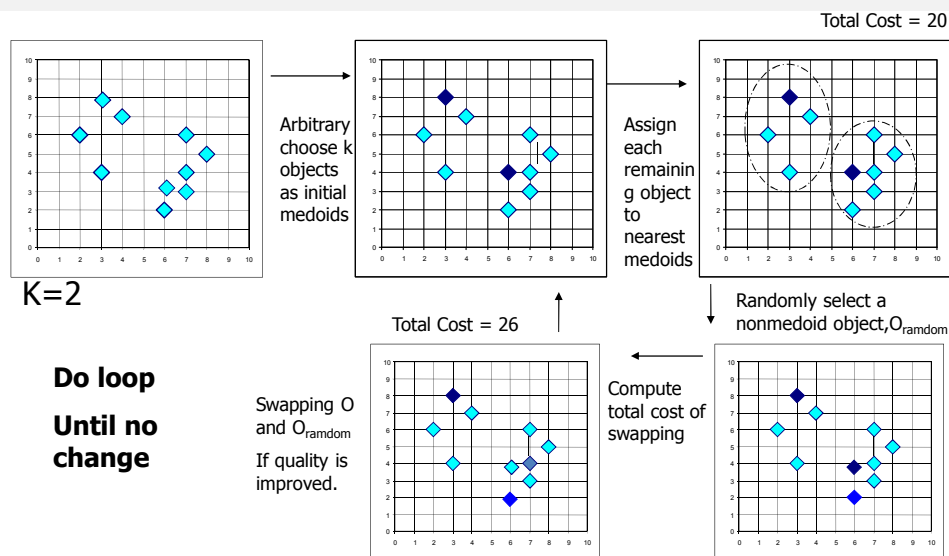


- ◉ Find *representative* objects, called medoids, in clusters
- ◉ **PAM** (Partitioning Around Medoids, 1987)
 - ◆ starts from an initial set of medoids and iteratively replaces one of the medoids by one of the non-medoids if it improves the total distance of the resulting clustering
 - ◆ **PAM** works effectively for small data sets, but does not scale well for large data sets
- ◉ **CLARA** (Kaufmann & Rousseeuw, 1990)
- ◉ **CLARANS** (Ng & Han, 1994): Randomized sampling
- ◉ Focusing + spatial data structure (Ester et al., 1995)

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Typical k-medoids algorithm (PAM)



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PAM (Partitioning Around Medoids) (1987)

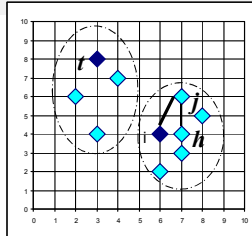


- PAM (Kaufman and Rousseeuw, 1987), built in Splus
- Use real object to represent the cluster
 1. Select k representative objects arbitrarily
 2. For each pair of non-selected object h and selected object i , calculate the total swapping cost TC_{ih}
 3. For each pair of i and h ,
 - a. If $TC_{ih} < 0$, i is replaced by h
 - b. Then assign each non-selected object to the most similar representative object
 4. repeat steps 2-3 until there is no change

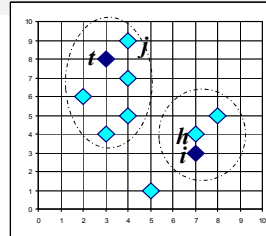
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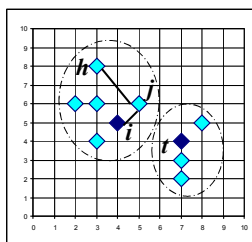
PAM Clustering: Total swapping cost $TC_{ih} = \sum_j C_{jih}$



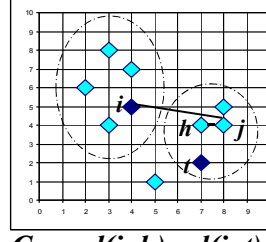
$$C_{jih} = d(j, h) - d(j, i)$$



$$C_{jih} = 0$$



$$C_{jih} = d(j, t) - d(j, i)$$



$$C_{jih} = d(j, h) - d(j, t)$$

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What is the problem with PAM?



- PAM is more robust than k-means in the presence of noise and outliers because a medoid is less influenced by outliers or other extreme values than a mean
- PAM works efficiently for small data sets but does not scale well for large data sets.
 - ◆ $O(k(n-k)^2)$ for each iteration
 - where n is # of data, k is # of clusters
- Sampling based method,
 - CLARA(Clustering LARGE Applications) and CLARANS

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CLARA (Clustering Large Applications) (1990)



- **CLARA** (Kaufmann and Rousseeuw in 1990)
 - ◆ Built in statistical analysis packages
- It draws *multiple samples* of the data set, applies *PAM* on each sample, and gives the best clustering as the output
- **Strength:** deals with larger data sets than *PAM*
- **Weakness:**
 - ◆ Efficiency depends on the sample size
 - ◆ A good clustering based on samples will not necessarily represent a good clustering of the whole data set if the sample is biased

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Thanks !

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