

# An Efficient Ride-Sharing Framework for Maximizing Shared Routes

(Extended Abstract)

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**Abstract**—Ride-sharing (RS) has great values in saving energy and alleviating traffic pressure. In this paper, we propose a new ride-sharing model, where each driver requires that the shared route percentage (SRP, the ratio of the shared route's distance to the driver's total traveled distance) exceeds her expected rate (e.g., 0.8) when sharing with a rider. We consider two variants of this problem. The first considers multiple drivers and multiple riders, and aims to compute a set of driver-rider pairs to maximize the overall SRP. We model this problem as the maximum weighted bigraph matching problem. We propose an effective exact algorithm, and an efficient approximate solution with error-bound guarantee. The second considers multiple drivers and a single rider and aims to find the top- $k$  drivers for the rider with the largest SRP. We devise pruning techniques and propose a best-first algorithm to progressively selects drivers with high probability to be in the top- $k$  results.

## I. INTRODUCTION

In this paper, we focus on the ride-sharing problem. We consider a new service called *hitch* in Uber and Didi. In the hitch service, there are a large number of part-time drivers, where each driver intends to drive from a source location to a destination and is willing to share the vehicle with a rider. If a driver shares the vehicle with a rider, the driver needs to first drive to the source of the rider from the driver's source, then drive to the destination of the rider from the rider's source (which is called the shared route between the driver and the rider), and finally drive to the destination of the driver from the rider's destination. The shared route percentage (SRP) is the ratio of the shared-route distance to the total route distance (i.e., the sum of the distances of the three parts). Since the driver must drive on the road networks, we consider the road-network distance and we assume that the driver will select the shortest route between two locations. Usually, the driver has a requirement that the SRP value must exceed an expectation value, e.g., 0.8, to guarantee a high sharing utility.

There are two variants of the ride-sharing (RS) problem.

(1) **Join-based RS.** There are a group of drivers and a group of riders and it aims to compute the driver-rider pairs that maximize the overall SRP.

(2) **Search-based RS.** There are a group of drivers and a single rider, and it aims to compute the top- $k$  drivers for the rider with the largest SRP values.

**Example 1:** Figure 1 visualizes drivers  $d_1 - d_3$  and riders  $r_1 - r_4$  on a road network. For rider  $r_1$ ,  $d_2$  is an *invalid* driver

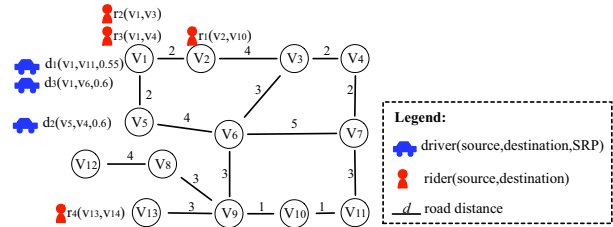


Fig. 1. Running Example.

as the SRP that  $d_2$  takes  $r_1$  (0.524) does not meet  $d_2$ 's requirement(0.6); while  $d_1$  and  $d_3$  are *valid* drivers for  $r_1$ . Pair  $\langle d_1, r_1 \rangle$  denotes that  $d_1$  picks up  $r_1$ . For Join-based RS, we want to find a set of driver-rider pairs that maximize the overall SRP, such as  $\{\langle d_1, r_1 \rangle, \langle d_2, r_3 \rangle, \langle d_3, r_2 \rangle\}$ . For Search-based RS, given rider  $r_3$ ,  $d_2$  is the top-1 driver.

In this paper, we make the following contributions. (1) We formally define the Join-based RS and Search-based RS problems and propose an efficient ride-sharing framework. (2) For Join-based RS, we devise an exact algorithm to compute the optimal driver-rider pairs. We propose an approximate algorithm to efficiently compute the driver-rider pairs with any given approximate rate. (3) We develop a best-first method for the Search-based RS problem to efficiently compute the top- $k$  drivers for a rider. (4) We conduct extensive experiments to demonstrate the high quality and efficiency of our proposed methods.

## II. PROBLEM FORMULATION

### A. Preliminaries

We use graph  $G(V, E)$  to model a road network, where each vertex  $v \in V$  denotes a geo-location (e.g., road intersection), and each edge  $(u, v) \in E$  is a road segment with a weight (e.g., road distance). A route in  $G$  is a connected path, and the route distance is the sum of the distance of each edge on the route. Given two road vertices  $u, v$ , we use  $\delta(u, v)$  to denote their shortest route distance.

A **rider**  $r_j = (r_j^s, r_j^d)$  plans to travel from source location  $r_j^s$  to destination location  $r_j^d$  by taking a shared ride with a driver  $d_i$ . A **driver**  $d_i = (d_i^s, d_i^d, \pi_i)$  plans to travel from a source location  $d_i^s$  to a destination location  $d_i^d$ , and is willing to share the ride with a rider  $r_j$  if the **shared route percentage**  $\pi(d_i, r_j)$  is no less than  $\pi_i$  ( $\pi_i \in [0, 1]$ ), where  $\pi(d_i, r_j) = \frac{\delta(r_j^s, r_j^d)}{\delta(d_i^s, r_j^s) + \delta(r_j^s, r_j^d) + \delta(r_j^d, d_i^d)}$ .

### B. Problem Formulation

**Join-based Ride Sharing.** Given a drivers set  $D = \{d_i\}$  and a riders set  $R = \{r_j\}$ , we aim to assign each rider  $r_j$  to a valid driver  $d_i$  where  $\pi(d_i, r_j) \geq \pi_i$ , in order to maximize the overall SRP.  $\mathcal{C} = \{(d_i, r_j) | \pi(d_i, r_j) \geq \pi_i\}$  denotes the set of valid driver-rider pairs,  $\mathcal{C}_j$  is the set of valid drivers for  $r_j$ .

We construct a weighted bigraph  $\mathcal{G}(\mathcal{G}_R, \mathcal{G}_D, \mathcal{G}_E)$ :  $\mathcal{G}_R = R$ ,  $\mathcal{G}_D = D$ ; if  $\pi(d_i, r_j) \geq \pi_i$ , an edge is added between  $d_i$  and  $r_j$  with weight  $\pi(d_i, r_j)$ . Then we aim to find a subgraph from  $\mathcal{G}$  of driver-rider pairs, such that one rider is assigned to at most one driver, and vice versa:

**Definition 1 (Matching Plan):** A matching plan  $P_x$  is a subgraph of  $\mathcal{G}$  if no two edges share a common bigraph vertex.

The matching plan with the largest overall weight (i.e., total SRP) is the *optimal* matching plan.

**Definition 2 (Join-based RS):** Given drivers set  $D = \{d_i\}$ , riders set  $R = \{r_j\}$ , road network  $G$ , find the optimal plan  $P^*$ :  $P^* = \arg \max_{P_x} \sum_{\langle d_i, r_j \rangle \in P_x} \pi(d_i, r_j)$

**Search-based Ride Sharing.** For any rider  $r_j$ , we aim to find the top- $k$  drivers with the largest SRP values.

**Definition 3 (Search-based RS):** For rider  $r_j$  on road network  $G$ , find a  $k$ -size valid driver set  $\mathcal{C}_j^k = \{d_{i^*}\}$ , where  
(1)  $\mathcal{C}_j^k \subseteq \mathcal{C}_j$ ,  $|\mathcal{C}_j^k| = k$ , and  
(2)  $\forall d_{i^*} \in \mathcal{C}_j^k, \forall d_i \in \mathcal{C}_j \setminus \mathcal{C}_j^k, \pi(d_{i^*}, r_j) \geq \pi(d_i, r_j)$ .

### III. ALGORITHM FRAMEWORK

#### A. Exact Method for Join-Based RS

**Invalid Pair Pruning.** We construct a candidate set  $\tilde{\mathcal{C}} = \{\langle d_i, r_j \rangle | d_i \in D_j^{\geq} \cap D_j^{\leq}, \forall r_j \in R\}$ , where  $D_j^{\geq}$  is the set of potentially valid drivers computed using  $r_j^{\geq}$ , and  $D_j^{\leq}$  is the set of potentially valid drivers computed using  $r_j^{\leq}$ . As  $|D_j^{\geq}| \ll |D|$  and  $|D_j^{\leq}| \ll |D|$ , the computational cost is greatly reduced. Set  $\tilde{\mathcal{C}}$  is *complete*, i.e.,  $\mathcal{C} \subseteq \tilde{\mathcal{C}}$ .

**The Framework for Exact Join-Based RS.**

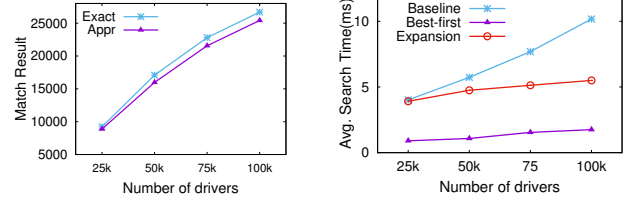
(1) **Candidate Set Generation.** For each rider  $r_j$ , we compute  $D_j^{\geq} = \{d_i | \delta(d_i^{\geq}, r_j^{\geq}) \leq (\frac{1}{\pi_0} - 1)\delta(r_j^{\geq}, r_j^{\leq})\}$  and  $D_j^{\leq} = \{d_i | \delta(r_j^{\leq}, d_i^{\leq}) \leq \delta_j^{\pi_0}\}$  [4], where  $\pi_0$  is the minimum SRP value for all drivers. Thus the candidate driver set for  $r_j$  is  $\tilde{\mathcal{C}}_j = D_j^{\geq} \cap D_j^{\leq}$ , and  $\tilde{\mathcal{C}} = \cup_{r_j \in R} \{\langle d_i, r_j \rangle | d_i \in \tilde{\mathcal{C}}_j\}$ .

(2) **Constructing the bigraph.** For each pair  $\langle d_i, r_j \rangle \in \tilde{\mathcal{C}}$ , we compute the real SRP value  $\pi(d_i, r_j)$ . If  $\pi(d_i, r_j) \geq \pi_i$ , we add an edge between  $d_i$  and  $r_j$  in the bigraph.

(3) **Computing the optimal matching plan.** The problem is essentially a maximum weighted bigraph matching problem and we use the minimal cost network flow algorithm [1] to compute the optimal matching plan  $P^*$ .

#### B. Approximate Method for Join-based RS

we propose a two-stage approximate method. First, we construct two bigraphs that bounds the accurate answer  $P^*$  within range  $[\text{LB}(P), \text{UB}(P)]$ . Then, we gradually update certain edges in the bound graphs into exact SRP values, so that  $\text{LB}(P)$  and  $\text{UB}(P)$  can converge to a predefined threshold  $\tau$ , i.e.,  $\frac{\text{UB}(P)}{\text{LB}(P)} \leq \tau$ . The final  $\text{LB}(P)$  value is the bounded approximate answer to  $P^*$ , and  $\frac{P^*}{\text{LB}(P)} \leq \tau$ .



(a) Join-based RS Effectiveness. (b) Search-based RS Efficiency. ( $\pi_0 = 0.8, \tau = 1.5$ ) ( $\pi_0 = 0.7, k = 3$ )

Fig. 2. Selected Experiment Results on Taxi Dataset.

#### C. Exact Methods for Search-based RS

Similar to Join-based RS, we first prune a large number of drivers that cannot meet the SRP requirements. Then we propose a **best-first** algorithm that progressively selects the drivers with high probability to be in the top- $k$  results and prunes the drivers that cannot be in the top- $k$  results [3].

### IV. EXPERIMENTAL STUDY

**Datasets.** We use the road network of Beijing with 338,024 vertices and 440,525 edges [2]. We use two ride-sharing datasets, Taxi and UCar. (1) Taxi contains about 200,000 trajectories of user orders generated by more than 8,000 public taxicabs in one month in Beijing. (2) UCar contains 1,267,000 trajectories of user orders generated by nearly 2,000 private drivers within one week in Beijing. We extract the pick-up and drop-off locations from Taxi and UCar and randomly assign them to a set of drivers and a set of riders.

**Evaluating Join-based RS.** We implement the Exact and the Appr solutions. We evaluate the efficiency, effectiveness, and their trends by varying parameters  $\pi_0$  and  $\tau$  (the bound ratio threshold for  $\text{UB}(P)/\text{LB}(P)$  in Appr iteration). The Appr solution achieves high performance in all test cases (Figure 2(a)).

**Evaluating Search-based RS.** We compare three strategies: (1) Baseline: searches all possible candidate drivers, computes all SRP values and selects the top  $k$  drivers (2) Expansion: expansion-based method that gradually increases the candidate drivers set for a single rider. (3) Best-first: only computes  $k$  driver-rider shared route percentages in the best scenario. Experiments show that the Best-first method is the most efficient and scalable technique for Search-based RS (Figure 2(b)).

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