# Question 1:

1.1

# Import the medical cost data from the following Kaggle link https://www.kaggle.com/datasets/mirichoi0218/insurance into R.

<b>(</b>		7 Filter								
•	age ‡	sex <sup>‡</sup>	bmi ‡	children <sup>‡</sup>	smoker <sup>‡</sup>	region <sup>‡</sup>	charges <sup>‡</sup>	isSmoker <sup>‡</sup>	healthyBMI <sup>‡</sup>	hasChildren <sup>‡</sup>
1	19	female	27.900	0	yes	southwest	16884.924	1	0	1
2	18	male	33.770	1	no	southeast	1725.552	0	0	0
3	28	male	33.000	3	no	southeast	4449.462	0	0	0
4	33	male	22.705	0	no	northwest	21984.471	0	1	1
5	32	male	28.880	0	no	northwest	3866.855	0	0	1
6	31	female	25.740	0	no	southeast	3756.622	0	0	1
7	46	female	33.440	1	no	southeast	8240.590	0	0	0
8	37	female	27.740	3	no	northwest	7281.506	0	0	0
9	37	male	29.830	2	no	northeast	6406.411	0	0	0
10	60	female	25.840	0	no	northwest	28923.137	0	0	1
11	25	male	26.220	0	no	northeast	2721.321	0	0	1
12	62	female	26.290	0	yes	southeast	27808.725	1	0	1
13	23	male	34.400	0	no	southwest	1826.843	0	0	1
14	56	female	39.820	0	no	southeast	11090.718	0	0	1
15	27	male	42.130	0	yes	southeast	39611.758	1	0	1
16	19	male	24.600	1	no	southwest	1837.237	0	1	0
17	52	female	30.780	1	no	northeast	10797.336	0	0	0

## 1.2

# Multiple linear regression with Charges being the dependent variable:

 $Charges_i = -2,136.454 + 266.544* age_i + 23,892.570* is Smoker_i - 3,145.089* \\ healthy BMI_i + 1,037.773* has Children_i + \epsilon_i$ 

# 1.3

Multiple linear regression	(charges~ age + isSm	noker +healthvBMI -	+ hasChildren)

	Dependent variable:
	charges
age	266.544***
	(12.264)
isSmoker	23,892.570***
	(425.123)
healthyBMI	-3,145.089***
	(459.968)
hasChildren	1,037.773***
	(346.847)
Constant	-2,136.454***
	(558.210)
Observations	1,338
$\mathbb{R}^2$	0.733
Adjusted R <sup>2</sup>	0.732
Residual Std. Error	6,271.992 (df = 1333)
F Statistic	912.840*** (df = 4; 1333)
Note:	*p**p***p<0.01

# What is the estimated average medical costs for a 40 year old, non-smoker individual with one child and a BMI of 19?

Estimation for average medical costs for a 40-year-old non -smoker individual with one child and a BMI of 19 is 6,417.984

### 1.5

## How does your answer to the above question change if the individual had a BMI of 27?

Estimation for average medical costs for a 40-year-old non -smoker individual with one child and a BMI of 27 is 9,563.073

#### 1.6

# Multiple linear regression with log(charges) being the dependent variable:

 $log(charges_i) = 7.299 + 0.035*age_i + 1.546*isSmoker_i - 0.118*healthyBMI_i + 0.227*hasChildren_i + \epsilon_i$ 

### 1.7

#### Multi linear regression with log(charges) being a dependent variable

	Dependent variable:
	log(charges)
age	0.035***
	(0.001)
isSmoker	1.546***
	(0.031)
healthyBMI	-0.118***
	(0.033)
hasChildren	0.227***
	(0.025)
Constant	7.299***
	(0.040)
Observations	1,338
$\mathbb{R}^2$	0.757
Adjusted R <sup>2</sup>	0.756
Residual Std. Error	0.454 (df = 1333)
F Statistic	1,036.758*** (df = 4; 1333)
Note:	*p**p***p<0.01

#### 1.8

With the new model what is the estimated average medical costs for a 40 year old, non-smoker individual with one child and a BMI of 19?

Estimation for average medical costs for a 40-year-old non -smoker individual with one child and a BMI of 19 is 6,697.871

#### 1.9

## How does your answer to the above question change if the individual had a BMI of 27?

Estimation for average medical costs for a 40-year-old non -smoker individual with one child and a BMI of 27 is 7,534.035

#### 1.10

# As an individual ages by 10 years by what percentage do their medical costs increase?

With age coefficient being 0.035, every 10 years of age results a change of 35% in log(charges).

In another word, there's 41.9% in actual charges change for every 10-year increase in age.

[1] "The percentage difference in charges for an individual that ages by 10 years:"
> print(perc\_diff)
 1
41.95096

### 1.11

Finally, estimate the following multiple regression model with the log(charges) as the dependent variable, and log(age) as one of the predictors:

 $log(chargesi) = \beta 0 + \beta 1 log(agei) + \beta 2 is Smokeri + \beta 3 healthy BMIi + \beta 4 has Childreni + \epsilon i$ 

 $log(charges_i) = 4.16 + 1.264*log(age)_i + 1.544*isSmoker_i - 0.122*healthyBMI_i + 0.168*hasChildren_i + \epsilon_i$ 

1.12

Export the regression results to MS Word using the stargazer library.

$\underline{\text{Multiple linear regression log(charges)}} \sim \log(\text{age}) + \text{isSmoker} + \text{healthyBMI} + \text{hasChildren}$						
	Dependent variable:					
	log(charges)					
log(age)	1.264***					
	(0.032)					
isSmoker	1.544***					
	(0.031)					
healthyBMI	-0.122***					
	(0.033)					
hasChildren	0.168***					
	(0.025)					
Constant	4.160***					
	(0.116)					
Observations	1,338					
$\mathbb{R}^2$	0.756					
Adjusted R <sup>2</sup>	0.755					
Residual Std. Error	0.455 (df = 1333)					
F Statistic	$1,033.279^{***} (df = 4; 1333)$					
Note:	*p**p***p<0.01					

# With the new model what is the estimated average medical costs for a 40 year old, non-smoker individual with one child and a BMI of 19?

Estimation for average medical costs for a 40-year-old non -smoker individual with one child and a BMI of 19 is 7,104.192

#### 1.14

## How does your answer to the above question change if the individual had a BMI of 27?

Estimation for average medical costs for a 40-year-old non -smoker individual with one child and a BMI of 27 is 8,029.289

#### 1.15

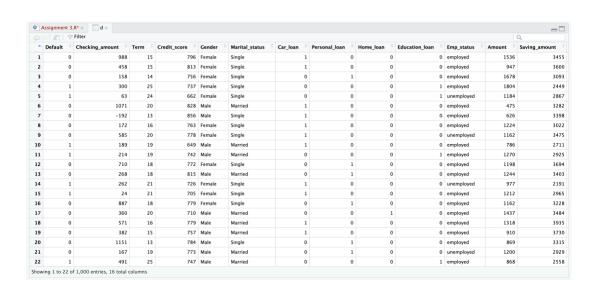
## What does the parameter β1 represent in this model?

The coefficient  $\beta$ 1=1.264 indicates that a 1% increase in age is associated with approximately a 1.264% increase in charges due to the use of logarithm for both charges and age.

### Question 2:

#### 2.1

## Import the bank loan default data set.



# Calculate summary statistics for all the numerical variables in the data set.

Checking account statistical summary:

Min: -665

1st Quartile: 164.8

Median: 351.5

Mean: 362.4

3<sup>rd</sup> Quartile: 553.5

Max: 1319.0

Term statistical summary:

Min: 9

1st Quartile: 16

Median: 18

Mean: 17.82

3<sup>rd</sup> Quartile: 20

Max: 27

Credit score statistical summary:

Min: 376

1st Quartile: 725.8

Median: 770.5

Mean: 760.5

3<sup>rd</sup> Quartile: 812

Max: 1029

# Amount statistical summary:

Min: 244

1st Quartile: 1016

Median: 1226

Mean: 1219

3<sup>rd</sup> Quartile: 1420

Max: 2362

# Saving amount statistical summary:

Min: 2082

1st Quartile: 2951

Median: 3203

Mean: 3179

3<sup>rd</sup> Quartile: 3402

Max: 4108

# Employment duration statistical summary:

Min: 0

1st Quartile: 15

Median: 41

Mean: 49.39

3<sup>rd</sup> Quartile: 85

Max: 120

# Age statistical summary:

Min: 18

1st Quartile: 29

Median: 32

Mean: 31.21

3<sup>rd</sup> Quartile: 34

Max: 42

Number of credit account statistical summary:

Min: 1

1st Quartile: 1

Median: 2

Mean: 2.546

3<sup>rd</sup> Quartile: 3

Max: 9

2.3

Tabulate all the categorical variables in the data set.

Default: 300 defaulted; 700 not defaulted

Gender: 310 female; 690 male

Marital status: 548 married; 452 single

**Car loan:** #0: 647; #1: 353 (1 if person has a car loan, 0 otherwise)

**Personal loan:** #0: 526; #1: 474 (1 if person has a personal loan, 0 otherwise)

**Home loan:** #0: 944; #1: 56 (1 if person has a home loan, 0 otherwise)

**Education loan:** #0: 888; #1: 112 (1 if person has a student loan, 0 otherwise)

**Employment status:** 304 employed and 692 unemployed

# Does there seem to be enough variation in the categorical variables to build a reliable model for loan defaults?

Yes, there seems to be enough variation in the categorical variables to build a reliable model for loan defaults.

2.5

Estimate a multiple linear regression model for loan defaults using all the variables in the data set.

**Default =** 3.465- 0.0003\*Checking Amount + 0.014\*Term – 0.001\*Credit Score + 0.008\*Gender (Male) – 0.042\*Marital Status (Single)- 0.079\*Car Loan – 0.147\*Personal Loan – 0.215\*Home Loan + 0.043\*Education Loan + 0.052\* Employment Status (Unemployed)+ 0.0001\*Amount – 0.00003\*Saving Amount -0.0002 \* Employment Duration – 0.044\*Age – 0.01\*Number of credit accounts

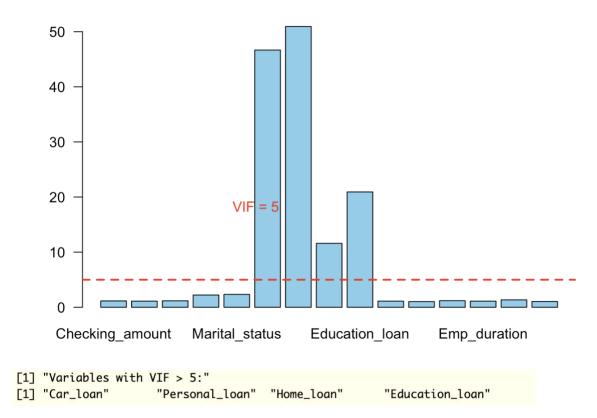
2.6

Multiple Linear Regression model for Loan Default

	Dependent variable:
	Default
Checking amount	-0.0003***
Checking_uniount	(0.0003)
Term	0.014***
Term	(0.003)
Credit_score	-0.001***
crean_secre	(0.0001)
GenderMale	0.008
	(0.027)
Marital statusSingle	0.042
	(0.026)
Car_loan	-0.079
	(0.122)
Personal loan	-0.147
	(0.122)
Home_loan	-0.215*
	(0.126)
Education loan	0.043
	(0.124)
Emp_statusunemployed	0.052***
	(0.020)
Amount	0.0001**
	(0.00003)
Saving_amount	-0.0003***
	(0.00003)
Emp_duration	-0.0002
	(0.0002)
Age	-0.044***
	(0.002)
No_of_credit_acc	-0.010*
	(0.005)
Constant	3.423***
	(0.186)
Observations	1,000
$\mathbb{R}^2$	0.660
Adjusted R <sup>2</sup>	0.655
Residual Std. Error	0.269 (df = 984)
F Statistic	127.320*** (df = 15; 984)
Note:	*p***p****p<0.01

Are there independent variables that exhibit a high degree of multicollinearity? Utilize the techniques that you learned in previous assignments (like correlation matrix, or VIF) to examine multicollinearity.

# VIF Values for Independent Variables



By using VIF, the following independent variables exhibit a high degree of multicollinearity: Car loan, Personal loan, Home loan, Education loan

#### 2.8

Remove all the variables that are insignificant and that are problematic due to collinearity and estimate your final multiple linear regression model with the remaining variables.

**Default =** 3.472 -0.0003\*Checking amount + 0.016\*Term -0.001\*Credit score +0.028\*Employment status (Unemployed) + 0.0001\*Amount -0.0003\*Saving account - 0.047\*Age

2.9

Export the regression results to MS Word using the stargazer library.

	Dependent variable:
•	Default
Checking_amount	-0.0003***
	(0.00003)
Term	0.016***
	(0.003)
Credit_score	-0.001***
	(0.0001)
Emp_statusunemployed	0.028
	(0.019)
Amount	0.0001**
	(0.00003)
Saving_amount	-0.0003***
	(0.00003)
Age	-0.047***
	(0.002)
Constant	3.472***
	(0.144)
Observations	1,000
$\mathbb{R}^2$	0.638
Adjusted R <sup>2</sup>	0.635
Residual Std. Error	0.277 (df = 992)
F Statistic	$249.642^{***}$ (df = 7; 992)
Note:	*p**p***p<0.0

Can the multiple linear regression model be used as a model of loan default probabilities? Illustrate the limitations of the linear regression model by making a few predictions that result in unexpected probability values.

The multiple linear regression model can't be used as a model of loan default probabilities because the dependent variable should've fallen into the valid range of probabilities, which is [0,1]. A probability greater than 1 or less than 0 is not valid. Below is the result for example test.

# Question 3:

#### 3.1

Estimate a multiple logistic regression model for bank loan defaults, using the same variables that you used in your final multiple linear regression model in the previous question.

 $log(\frac{P(Default=1)}{P(Default=0)}) = 38.294 - 0.005*Checking amount + 0.178*Term - 0.012*Credit score + 0.485*Employment status (Unemployed) + 0.0005*Amount - 0.0005*Saving amount - 0.626*Age$ 

3.2

	$Dependent\ variable:$
	Default
Checking_amount	-0.005***
	(0.001)
Term	0.178***
	(0.048)
Credit_score	-0.012***
	(0.002)
Emp_statusunemployed	0.485
	(0.306)
Amount	0.0005
	(0.0005)
Saving_amount	-0.005***
	(0.001)
Age	-0.626***
	(0.059)
Constant	38.294***
	(3.616)
Observations	1,000
Log Likelihood	-168.103
Akaike Inf. Crit.	352.206
Note:	*p**p***p<0.01

Remove any insignificant variables to arrive at your final logistic regression model. Estimate your final logistic regression model to answer the questions below.

 $\log\left(\frac{P(Default=1)}{P(Default=0)}\right) = 38.848 - 0.005*Checking amount + 0.175*Term - 0.011*Credit score - 0.005*Saving amount - 0.629*Age$ 

## 3.4

Export the final logistic regression model results to MS Word using the stargazer library.

Final Multiple Logistic model for Loan Default

	Dependent variable:
	Default
Checking_amount	-0.005***
	(0.001)
Term	0.175***
	(0.047)
Credit_score	-0.011***
	(0.002)
Saving_amount	-0.005***
	(0.001)
Age	-0.629***
	(0.059)
Constant	38.848***
	(3.511)
Observations	1,000
Log Likelihood	-169.985
Akaike Inf. Crit.	351.970
Note:	*p**p***p<0.01

# How does the employment status of an individual impact the probability of their loan default?

With employment status being insignificant, it doesn't affect the loan default probabilities if an individual is employed or not.

### 3.6

# What is the difference in the probability of a loan default for an individual with a 600 credit score vs. an otherwise similar individual but with an 800 credit score?

Running an example dataset for 2 similar individuals with \$500 in checking, term is 22, (credit) amount is \$2000, saving amount is \$2200 and age is 35, the prediction returns:

For an individual with a 600-credit score, their loan default probability is 81.89% (Very likely to default the loan) while a similar individual with a 800-credit score has 31.66% loan

default (<50%, not likely to default the loan). The percentage difference for probability prediction is around 50.24%

```
[1] "Probability difference:"
> print(example4_diff)
          1
50.23768
```

### Question 4:

#### 4.1

Using R, split the data set randomly into two parts: a training data set, consisting of 70% of the observations, and a testing data set, consisting of 30% of the observations.

testing_data	300 obs. of 16 variables	
① training_data	700 obs. of 16 variables	

#### 4.2

Estimate a logistic regression model with the training data set using the same variables from your final logistic regression model in the question above.

$$log\left(\frac{P(Default=1)}{P(Default=0)}\right)$$
 = 36.714 -0.004\*Checking amount + 0.157\*Term -0.012\*Credit score - 0.004\*Saving amount -0.63\*Age

### 4.3

	Dependent variable:
	Default
Checking_amount	-0.004***
	(0.001)
Term	0.157***
	(0.058)
Credit_score	-0.012***
	(0.002)
Saving_amount	-0.004***
	(0.001)
Age	-0.630***
	(0.070)
Constant	36.714***
	(3.984)
Observations	700
Log Likelihood	-121.585
Akaike Inf. Crit.	255.170
Note:	*p**p***p<0.01

Use the model you estimated to predict the probabilities of default for the individuals in the testing data set.

Preview of the probabilities when running training logistic model on testing dataset, all are within the [0,1] range:

	1	2	3	4	5	6	7	8	9	10	11	12	13	14
2	.880637e-02	8.256405e-04	9.512189e-01	3.605452e-02	8.473599e-01	1.379923e-03	8.940286e-01	1.537178e-03	2.120243e-01	1.490725e-02	3.719280e-01 3.	241203e-04	2.458328e-02 1.4	414230e-03
	15	16	17	18	19	20	21	22	23	24	25	26	27	28
1	.734761e-01	9.465866e-01	5.506784e-04	5.080209e-03	9.736357e-01	7.347651e-02	1.709776e-02	1.947222e-01	9.879691e-01	3.550718e-01	2.188391e-04 9.5	99831Ze-01	9.756326e-01 1.0	690038e-01
	29	30	31	32	33	34	35	36	37	38	39	40	41	42
9	.978145e-01	1.118274e-03	8.926646e-01	2.601659e-01	9.896496e-01	9.967809e-01	2.058117e-01	8.011409e-01	4.963191e-05	1.463572e-02	9.236863e-01 9.	453429e-01	5.940817e-02 8.	862044e-01
	43	44	45	46	47	48	49	50	51	52	53	54	55	56
5	.980782e-02	Z.164910e-03	1.73676Ze-02	1.714303e-03	9.091111e-01	1.278345e-03	1.323568e-02	1.920146e-01	8.839045e-03	1.812230e-02	9.132167e-03 2.	386374e-01	1.185323e-02 9.	797300e-01
	57	58	59	60	61	62	63	64	65	66	67	68	69	70
2	.393827e-01	6.165313e-03	7.816698e-01	2.087506e-02	7.192528e-04	2.996933e-01	9.199959e-01	1.601381e-02	2.452279e-01	9.816567e-01	9.125978e-01 9.	943505e-01	7.432784e-02 4.5	949380e-04
	71	72			75			78	79	80	81	82	83	84
6	.930184e-01	1.383530e-01	5.484040e-01	9.963305e-01	3.461864e-02	2.762494e-03	5.645399e-01	1.924228e-01	3.838959e-01	8.662519e-01	2.619195e-02 6.	249905e-04	9.985093e-01 4.:	196991e-01
	85	86	200	88	89	90		92	93	94	95	96	97	98
3	.074586e-04	2.710876e-01	1.349154e-03	1.233351e-03	1.824558e-02	9.538068e-01	1.961596e-03	7.657470e-05	4.814953e-03	1.761578e-03	1.756703e-01 4.	004654e-02	4.284871e-03 1.	717087e-02
	99	100		102	103	104		106	107	108	109	110	111	112
9											8.467795e-01 7.			
	113	114	115	116	117	118	119	120	121	122	123	124	125	126
6				0.000	31.020020 02					DIEZOZOZO OZ	2.028268e-02 1.			
	127	128	Salar State of the Control of the Co	Contract Con	131	132		134	135	136	137	138	139	140
7	.841713e-03	313133000 01	8.817654e-01	DIDDEEL OF OR	TITEOGOGC OT	TIT TOSESC OF	313121210 02	31 1301 330 02		OIDOODOLC OL	9.615248e-01 6.	0521010 02	DIDODOGLE OF ELL	896512e-03
	141	142	francisco (1980)		145	146		148	149	150	151	152	153	154
2	.547878e-03	1.261588e-02	2.420282e-01	2.091331e-04	6.050190e-01	1.014460e-02	4.475424e-02	1.510533e-02	4.768276e-03	3.693801e-02	5.605390e-01 9.	955394e-01	9.330187e-03 2.5	977473e-02
	155	156	157	158	159	160		162	163	164	165	166	167	168
1	.852936e-02	9.995526e-01	2.089265e-01	6.592358e-02	7.203815e-01	1.316913e-04	9.920840e-01	8.672370e-03	7.985511e-01	1.587542e-02	8.719060e-05 6.	505573e-02	5.114730e-04 9.	831176e-01

Assuming a cutoff probability at 70% (i.e. if the predicted probability is greater than or equal to 70% the loan will be considered as default) create a classification table for your model.

Classification table:

```
[1] "Confusion Matrix:"
> print(confusion_matrix)
  pred_class
     0   1
  0 196   3
  1 23   78
```

4.6

Using the classification table above, calculate the accuracy rate of your model as the ratio of correctly predicted outcomes over the total possible outcomes.

The accuracy rate of my model as the ratio of correctly predicted outcomes over the total possible outcomes is 91.33%

```
[1] "Accuracy percentage rate:"
> print(accuracy)
[1] 91.33333
```