

6

1

a)  $49.1875$

$$49 \div 16 = 3 \text{ R } 1$$

$$3 \div 16 = 0 \text{ R } 3$$

$$0.1875 \times 16 = 3.0$$

$$\Rightarrow 49.1875_{10} = 31.3_{16}$$

$$= 110001.0011_2$$

$$= 61.14_8$$

$$110001.0011 \times 2^0$$

$$= 0.1100010011 \times 2^6$$

$$01100010 | 01100000 | 00000000 | 00000110$$

$$6 \quad 2 \quad 6 \quad 0 \quad 0 \quad 0 \quad 0 \quad 6$$

b)  $3.07421875$

$$3 \div 16 = 0 \text{ R } 3$$

$$0.07421875 \times 16 = 1.1875$$

$$0.1875 \times 16 = 3.0$$

$$3.07421875_{10} = 3.13_{16}$$

$$= 11.00010011_2$$

$$= 3.046_8$$

$$11.00010011 \times 2^0 = 0.1100010011 \times 2^2$$

$$01100010 | 01100000 | 00000000 | 00000010$$

$$6 \quad 2 \quad 6 \quad 0 \quad 0 \quad 0 \quad 0 \quad 2$$

2

$$0.2_{10} = 0.\underline{33}_{16}$$

$$= 0.14638$$

b)  $-49.1875$

$\underbrace{10011101}_{9}$ 
 $\underbrace{10100000}_{D}$ 
 $\underbrace{10100000}_{A}$ 
 $\underbrace{00000000}_{0}$ 
 $\underbrace{00000000}_{0}$ 
 $\underbrace{00000000}_{0}$ 
 $\underbrace{00000000}_{0}$ 
 $\underbrace{0110}_{6}$

$-3.01421015$   
 01100010101100000000000000000000000010  
 100111011001111111111111111100000010  
 +1

$\underbrace{1001}_{9} \underbrace{1101}_{D} \underbrace{1101}_{A} \underbrace{0000}_O \underbrace{0000}_O \underbrace{0000}_O \underbrace{0000}_O \underbrace{10}_2$

-0.2

(3)

01100110 | 01100110 | 01100110 | 11111110  
10011001 | 10011001 | 10011001 | 11111110

+1

10011001 | 10011001 | 10011001 | 10011001 | 10011001 | 10011001 | 11111110  
9 9 9 9 9 A F E

c) 69999902

01101001 | 10011001 | 10011001 | 00000010

$$\Rightarrow 0.1101001 \times 10^2$$

$$\Rightarrow 11.01001_2 = 3.4C_{16}$$

$$3_{16} = 3 \times 16^0 = 3_{10}$$

$$0.4C_{16} = \frac{4}{16} + \frac{12}{16^2} + \frac{12}{16^3} + \frac{12}{16^4} + \dots$$

$$= \frac{1}{4} + \frac{12}{16^2} \left( 1 + \frac{1}{16} + \frac{1}{16^2} + \dots \right)$$

$$= \frac{1}{4} + \frac{3}{64} \cdot \frac{16}{15}$$

$$= \frac{3}{10} = 0.3$$

$$\Rightarrow 69999902 = 11.01001_2 = 3.4C_{16} = \boxed{3.3_{10}}$$

69999903

4

01101001 | 10011001 | 1001 1001 | 00000011

$$\rightarrow 0.1101001 \times 2^3$$

$$\rightarrow 110.1001_2 = 6.9_{16}$$

$$6_{16} = 6 \times 16^0 = 6_{10}$$

$$0.9_{16} = \frac{9}{16} + \frac{9}{16^2} + \frac{9}{16^3} + \frac{9}{16^4} + \dots$$

$$= \frac{9}{16} \left( 1 + \frac{1}{16} + \frac{1}{16^2} + \frac{1}{16^3} + \dots \right)$$

$$= \frac{9}{16} \cdot \frac{16}{15}$$

$$= 3/5 = 0.6$$

$$\rightarrow 69999903 = 110.1001_2 = 6.9_{16} = 6.6_{10}$$

966667FF

10010110 | 01100110 | 01100111 | 11111111

10010110 | 01100110 | 01100110 | 11111110

01101001 | 10011001 | 10011001 | 00000001

$$\rightarrow 0.1101001 \times 2^1$$

$$\rightarrow 1.101001_2 \rightarrow 1.A6_{16}$$

$$1_{16} = 1 \times 16^0 = 1_{10}$$

$$0.A6_{16} = \frac{10}{16} + \frac{6}{16^2} \left( 1 + \frac{1}{16} + \frac{1}{16^2} + \dots \right) = \frac{10}{16} + \frac{6}{16^2} \cdot \frac{16}{15} = 0.65$$

$$\rightarrow 966667FF$$

$$= -1.65_{10}$$